

SEARCHING FOR PHYSICS BEYOND THE STANDARD MODEL IN NEUTRINO OSCILLATIONS



She/her

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BNL NUSTEAM/NUPUMAS LECTURE
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INTRODUCTION

- Originally from Montpelier, VT
- BS in physics from Georgia Tech
- PhD from University of Chicago: “CP Violation in Neutral Kaon Decays”
- Studying neutrinos at BNL since 2011
- Adjunct professor at Stony Brook University
- Experiments: DUNE, ICARUS, SBND
- Hobbies include running, climbing/bouldering, guitar



SUMMARY

- We have quite specific expectations of how neutrino oscillations behave in the 3-neutrino paradigm based on existing measurements of neutrino oscillation parameters
- The existence of neutrino mass already means there must be new physics – we just don't know yet exactly what it looks like
- Several models of new physics predict specific distortions of neutrino oscillation spectra, allowing us to search for those specific effects and place limits on the parameters of those models
- Some new physics may affect the observed spectra in ways that are semi-degenerate with the 3-neutrino oscillation parameters or with other new physics models – experiments with different energies and baselines can disentangle these effects
- We can search for new physics more generically , eg: by studying whether the PMNS matrix is unitary
- Searches for new physics in neutrino oscillation are intrinsically tied to study of 3-neutrino oscillation



INTRO TO NEUTRINO OSCILLATION

AGAIN!

In many cases we look for BSM physics by looking for deviations in observed oscillation effects from what is expected in the standard 3-neutrino paradigm. So, we have to understand 3-flavor oscillation to understand how BSM may affect those oscillations.

NEUTRINO MIXING PARAMETERS

Neutrinos have mass $\leftrightarrow$ neutrinos oscillate (already BSM physics!)

Flavor eigenstates

Mass eigenstates

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \underbrace{\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix}}_{U_{\text{PMNS}}} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

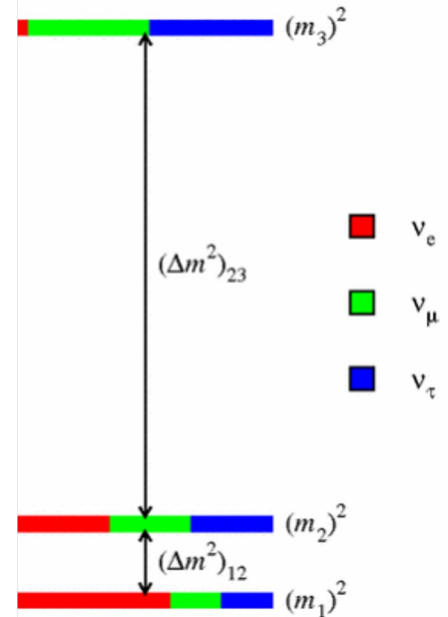


NEUTRINO MIXING PARAMETERS

$$U_{\text{PMNS}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{23} & \sin\theta_{23} \\ 0 & -\sin\theta_{23} & \cos\theta_{23} \end{pmatrix} \times \begin{pmatrix} \cos\theta_{13} & 0 & e^{-i\delta_{CP}} \sin\theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta_{CP}} \sin\theta_{13} & 0 & \cos\theta_{13} \end{pmatrix} \times \begin{pmatrix} \cos\theta_{12} & \sin\theta_{12} & 0 \\ -\sin\theta_{12} & \cos\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- $\theta_{23} \approx 45^\circ$
- Octant unknown (new symmetry?)
- $\theta_{13} \approx 10^\circ$
- δ_{CP} unknown (CP violation?)
- $\theta_{12} \approx 35^\circ$

Normal ordering

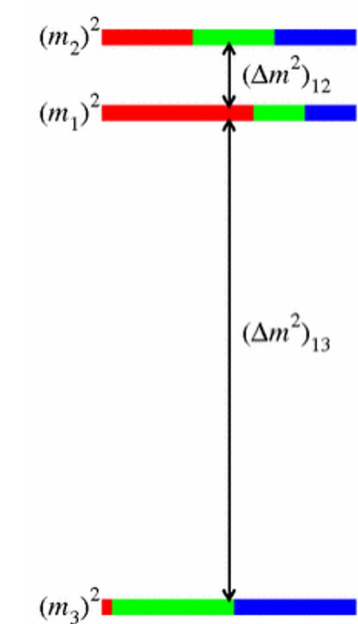


NEUTRINO MIXING PARAMETERS

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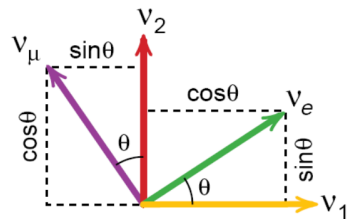
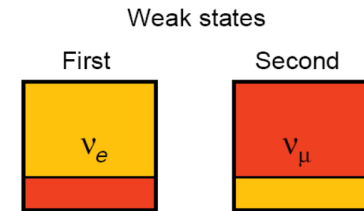
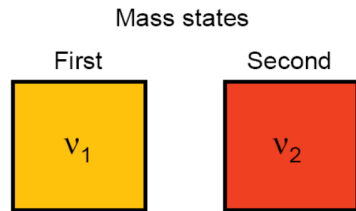
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Inverted ordering



NEUTRINO OSCILLATION PROBABILITY: BONUS HOMEWORK

- In the two-flavor approximation, derive the ν_μ to ν_e oscillation probability



$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

Step 1: Write $|\nu_\mu\rangle$ and $|\nu_e\rangle$ in terms of ν_1 and ν_2
 Step 2: Apply the Schrodinger equation to get the time evolved $|\nu_\mu(t)\rangle$ state in terms of ν_1 and ν_2
 Step 3: Use natural units, assume a common momentum for both mass states, and assume $E \gg m$ to write ΔE in terms of m_1 , m_2 , and E
 Step 4: Square the inner product of the $|\nu_e\rangle$ and $|\nu_\mu(t)\rangle$ states to get the probability of oscillation from ν_μ to ν_e

Slides 15-16 in this lecture will walk you through the calculation more fully:

https://indico.cern.ch/event/305391/contributions/701285/attachments/580248/798873/ZZ_NeutrinoPhysics_L2.pdf

NEUTRINO OSCILLATION PROBABILITY

- Two neutrino case: $P_{\alpha \rightarrow \beta, \alpha \neq \beta} = \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$
- Oscillation amplitude depends on θ (mixing angle)
- Oscillation frequency depends on Δm^2 (mass difference), baseline (L), and energy (E).

NEUTRINO OSCILLATION PROBABILITY

- Three-flavor mixing in matter:

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) \simeq & \boxed{\sin^2 \theta_{23}} \boxed{\sin^2 2\theta_{13}} \frac{\sin^2(\Delta_{31} - aL)}{(\Delta_{31} - aL)^2} \Delta_{31}^2 \\
 & + \sin 2\theta_{23} \sin 2\theta_{13} \sin 2\theta_{12} \frac{\sin(\Delta_{31} - aL)}{(\Delta_{31} - aL)} \Delta_{31} \frac{\sin(aL)}{(aL)} \Delta_{21} \cos(\Delta_{31} + \delta_{\text{CP}}) \\
 & + \cos^2 \theta_{23} \boxed{\sin^2 2\theta_{12}} \frac{\sin^2(aL)}{(aL)^2} \Delta_{21}^2,
 \end{aligned}$$

$a = G_F N_e / \sqrt{2}$

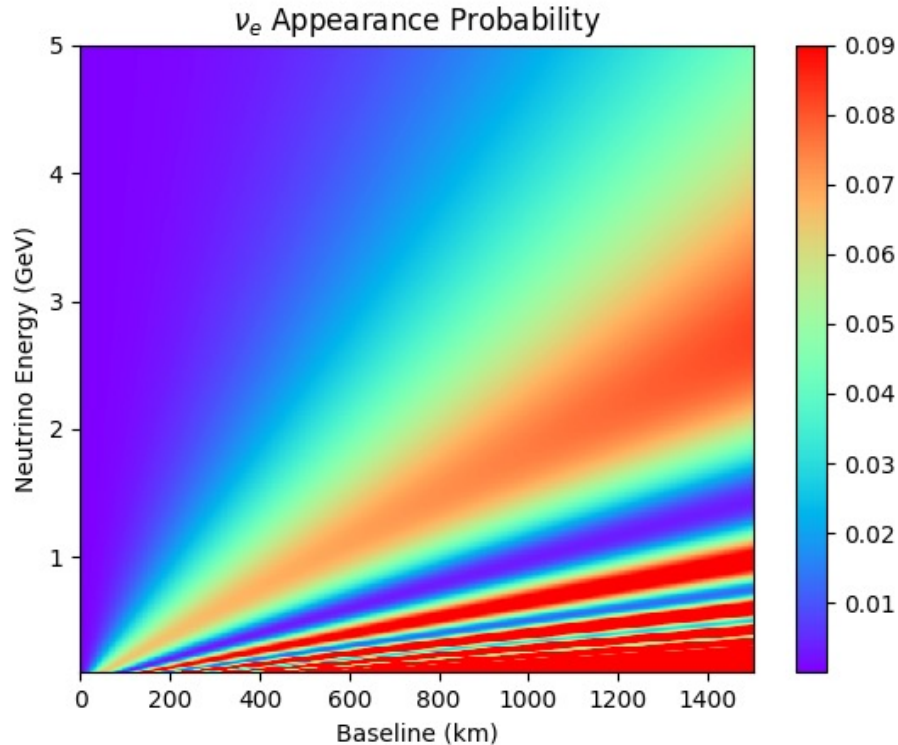
Matter effect from
coherent forward
scattering on electrons,
couples to baseline

↓
CP violation

$$\Delta_{ij} = \Delta m_{ij}^2 L / 4E_\nu$$

Same basic dependence
as two-flavor case

NEUTRINO OSCILLATION PROBABILITY



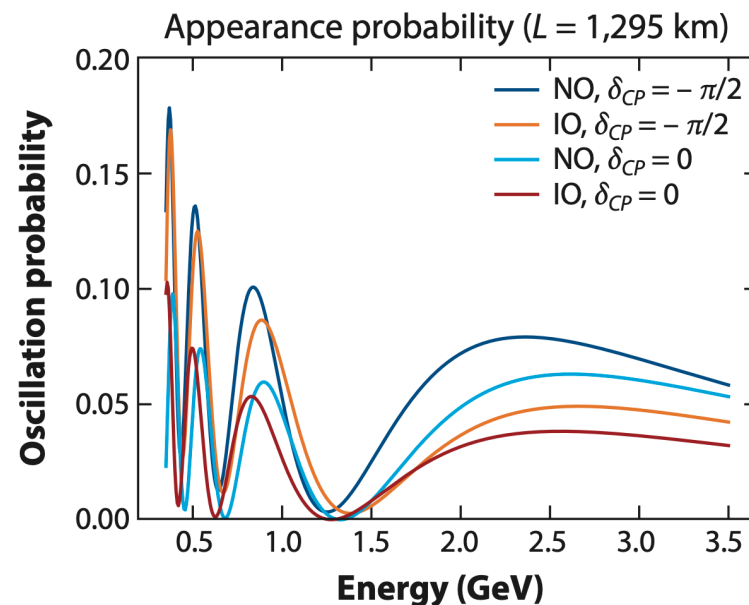
Optimize choice of baseline and energy for desired measurement (1st/2nd oscillation maxima)

Questions:

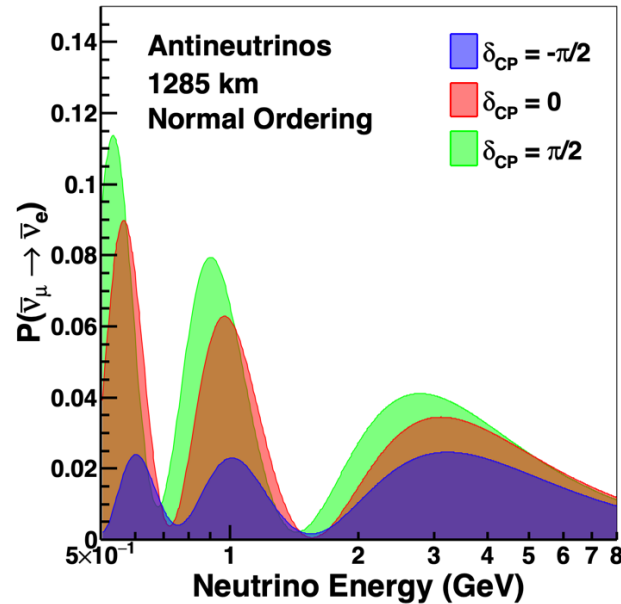
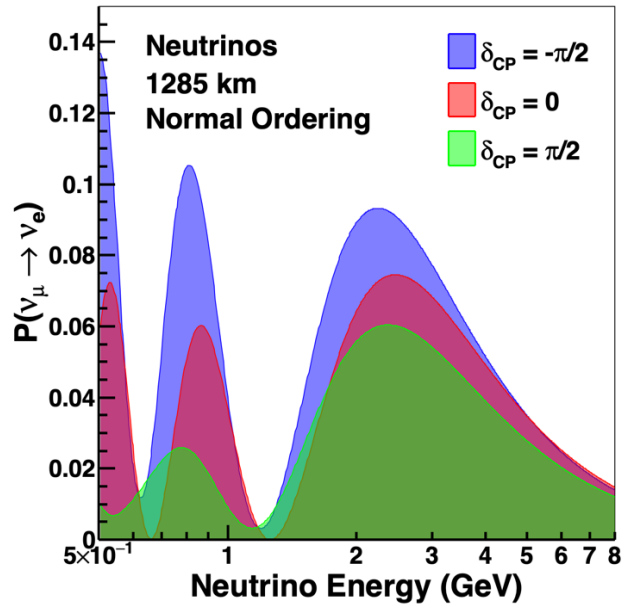
- I want to place a detector at a baseline of 600 km and observe the first oscillation maximum. What neutrino energy should I target in designing the beam?
- I have a neutrino beam energy of 750 MeV and I'd like to observe the 2nd oscillation maximum. Where should I place my detector?

MATTER EFFECT

- Matter effect occurs because there are electrons in matter, but no muons or taus:
 - Electron neutrinos can undergo coherent forward scattering in both charged-current and neutral-current interactions without a flavor change
 - Muon and tau neutrinos cannot undergo charged-current coherent forward scattering with the electrons in matter, so only the neutral-current interaction is available to them
- Effective Hamiltonian is modified in matter in a way that enhances the ν_e appearance probability for neutrinos and suppresses it for antineutrinos in normal ordering; the opposite is true for inverted ordering
- The matter effect increases with energy. Since longer-baseline experiments typically use higher energy neutrino beams (to select the desired L/E), the matter effect is in practice larger for longer baselines

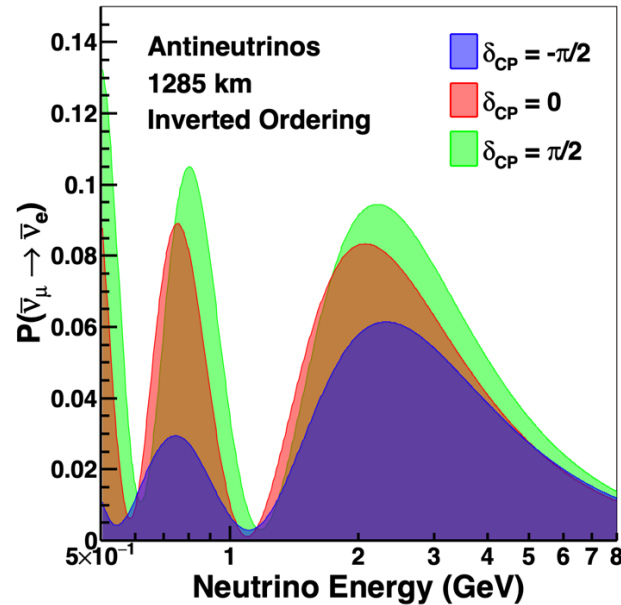
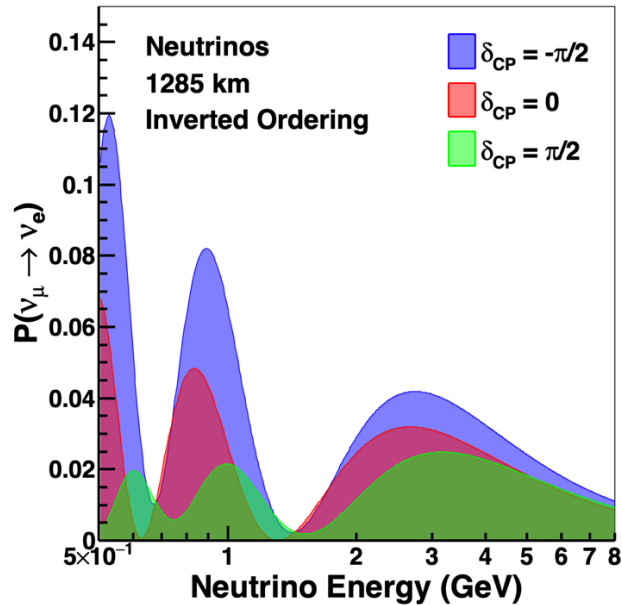


APPEARANCE PROBABILITY



- Value of δ_{CP} affects both rate and shape of appearance probability, with asymmetric impact on neutrinos and antineutrinos
- Matter effect enhances appearance probability for neutrinos and reduces it for antineutrinos if ordering is normal

APPEARANCE PROBABILITY



- Value of δ_{CP} affects both rate and shape of appearance probability, with asymmetric impact on neutrinos and antineutrinos
- Matter effect reduces appearance probability for neutrinos and enhances it for antineutrinos if ordering is inverted

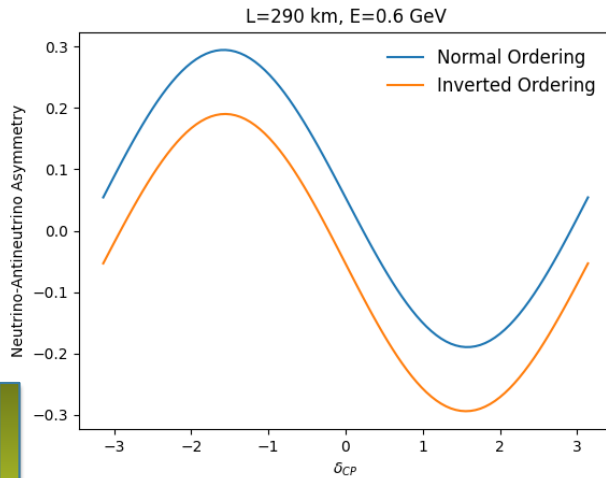
Both matter effect and δ_{CP} induce matter-antimatter asymmetry!

QUESTIONS

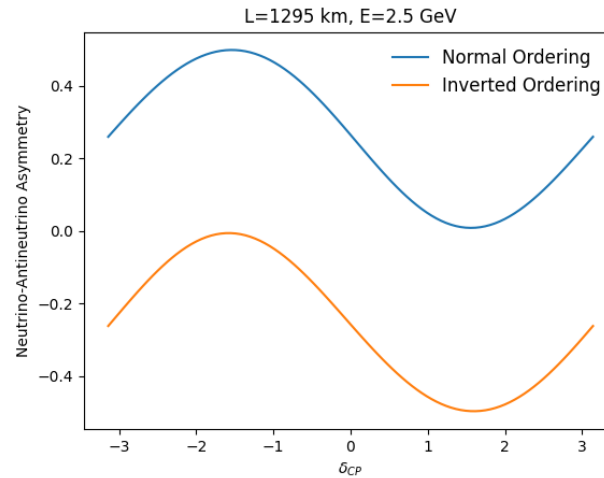
- What combination of neutrino/antineutrino, normal/inverted ordering, and δ_{CP} values gives the largest appearance probability?
- What combination of neutrino/antineutrino, normal/inverted ordering, and δ_{CP} values gives the smallest appearance probability?
- Can you find a combination of neutrino/antineutrino, normal/inverted ordering that have similar appearance probabilities for different values of δ_{CP} ?

RESOLVING DEGENERACY

Baseline of 290 km
(very little matter effect)



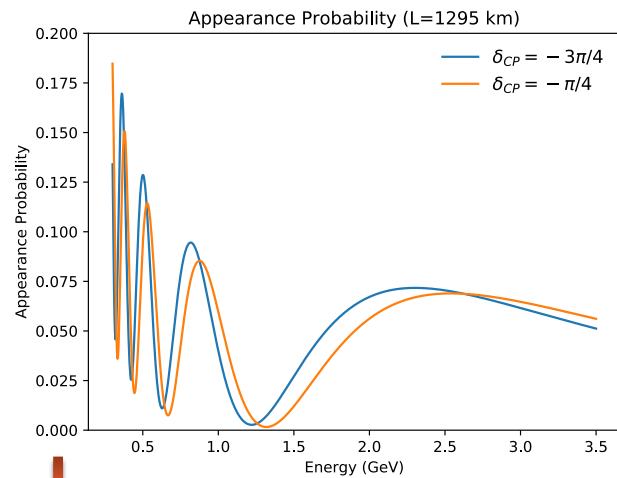
Baseline of 1295 km
(large matter effect)



Degeneracy between δ_{CP} and matter effects is lifted for baselines greater than ~ 1000 km because matter effect produces larger asymmetry

Matter-antimatter asymmetry

RESOLVING DEGENERACY



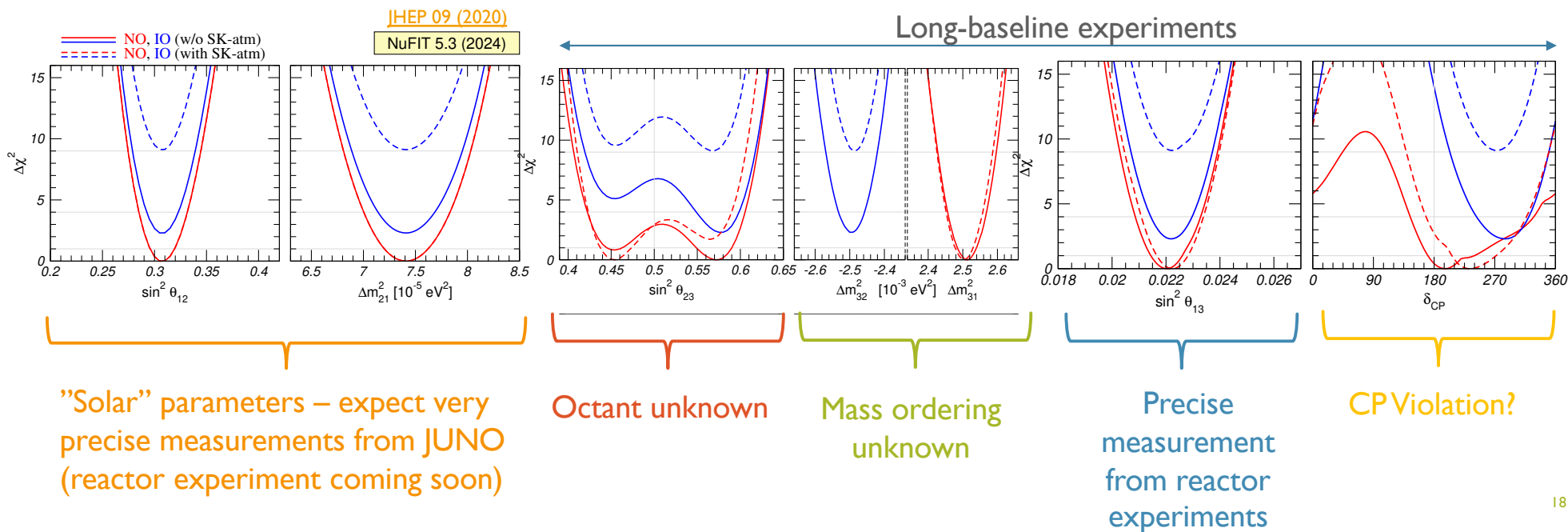
Baseline of 1295 km
(large matter effect)

Energy dependence of oscillation can resolve δ_{CP} degeneracy

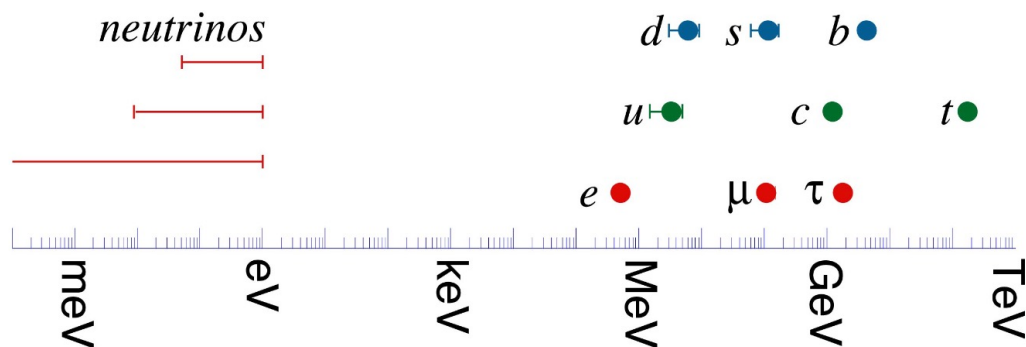
Appearance probability

CURRENT STATUS OF MEASUREMENTS

- Example of global fit for oscillation parameters:



NEUTRINOS MASS $\rightarrow$ BSM PHYSICS



- Neutrino masses (still unmeasured) are very light compared to all other known particles – suggests that perhaps their mass is generated in a different way from other particles or that they couple extremely weakly to the Higgs
- To generate neutrino mass with the Higgs mechanism would require additional (right-handed) neutrinos that are not yet observed
- Whether through a new mass-generation mechanism, new particles, or both, the currently known neutrino masses imply there must be new physics



NEW PHYSICS SCENARIOS



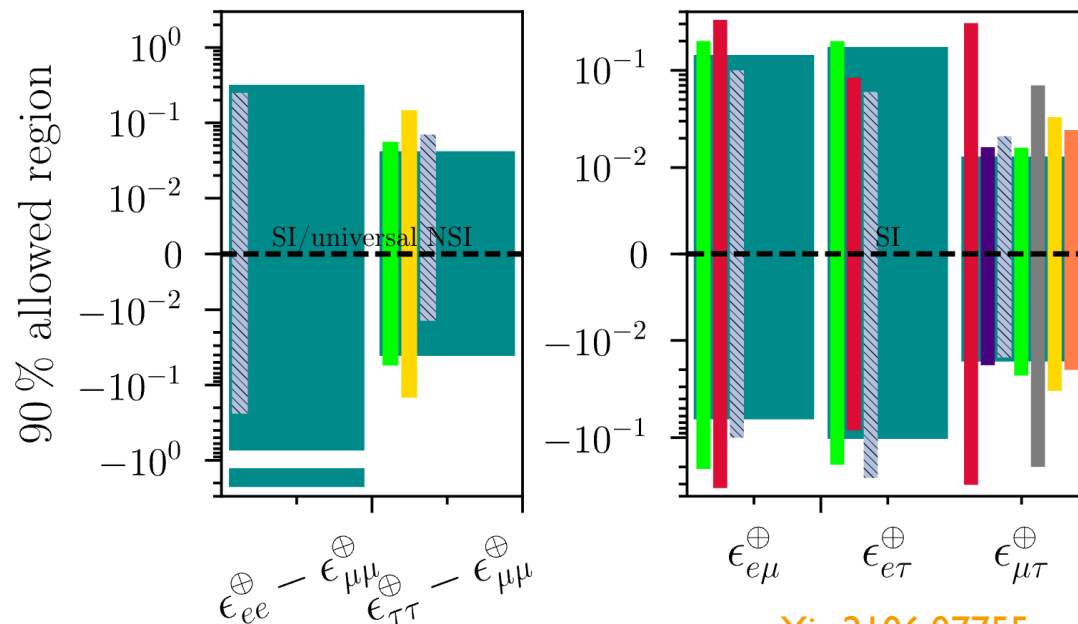
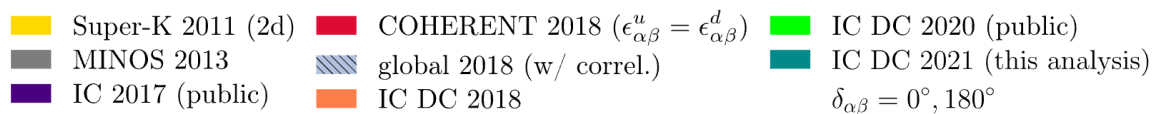
NON-STANDARD INTERACTIONS (NSI)

- New neutrino interactions
- While the new interactions could affect neutrino production, interaction, or propagation, typically we focus on propagation effects, leading to perturbations of the matter effect, eg: vector NSI

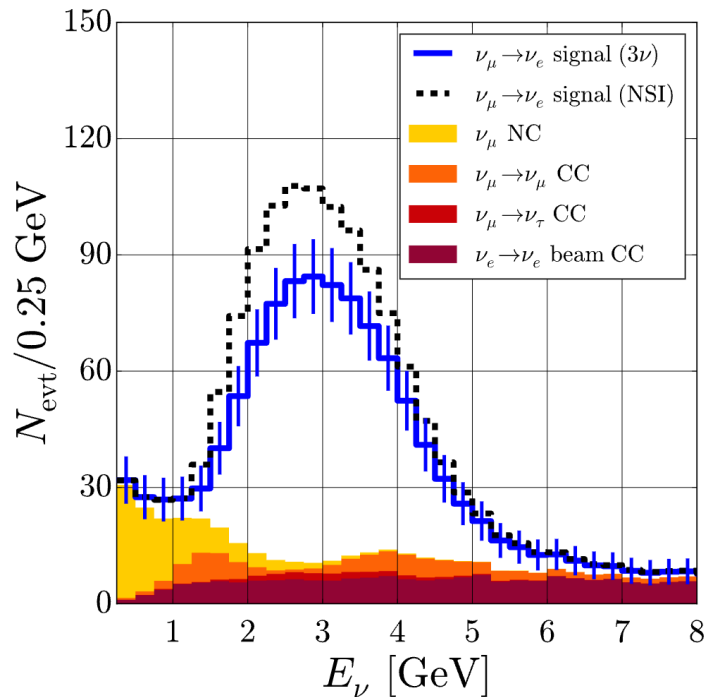
$$H = \frac{1}{2E} \left[\underbrace{U_{\text{PMNS}} \begin{pmatrix} 0 & & \\ & \Delta m_{21}^2 & \\ & & \Delta m_{31}^2 \end{pmatrix} U_{\text{PMNS}}^\dagger}_{\text{Standard oscillations}} + a \underbrace{\begin{pmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}}_{\text{Non-standard oscillations}} \right]$$

NSI SEARCHES

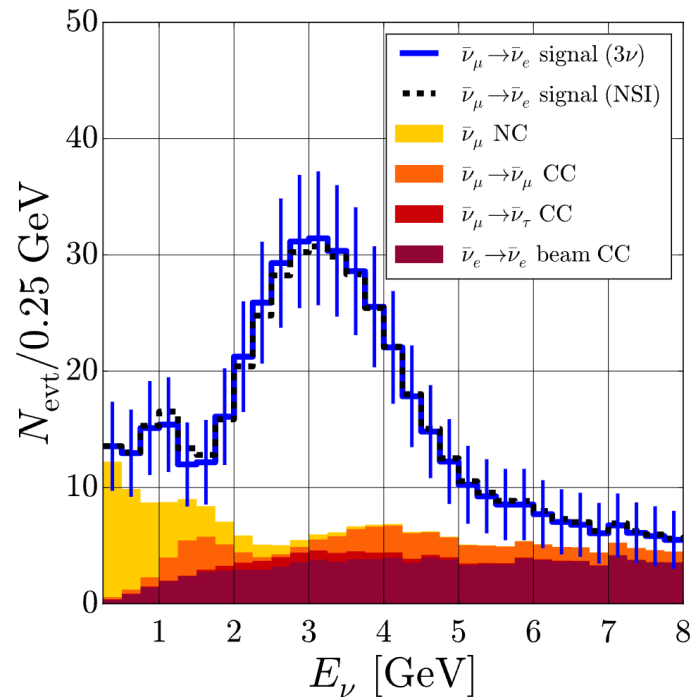
- Compare observed oscillation spectra to those expected for standard 3-flavor mixing and for values of various NSI parameters
- So far experiments have set limits, ie: “if NSI were present with parameter value x , we would have seen it – since we did not see it, we know that parameter must be smaller than x ”



NSI AT DUNE



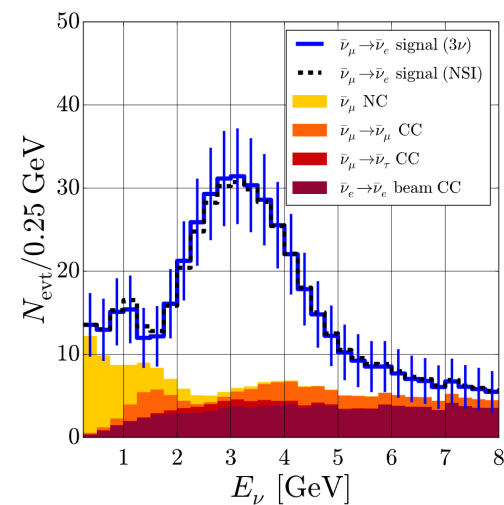
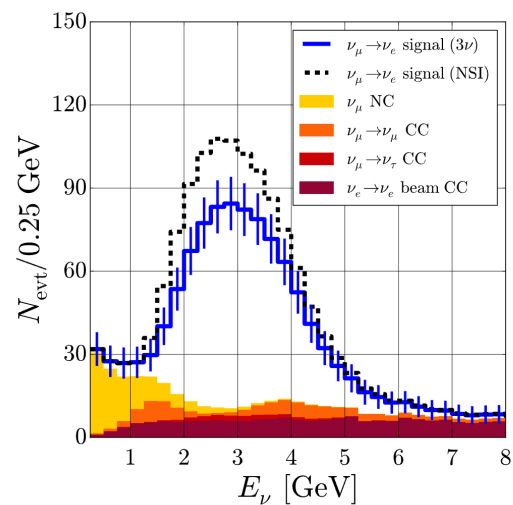
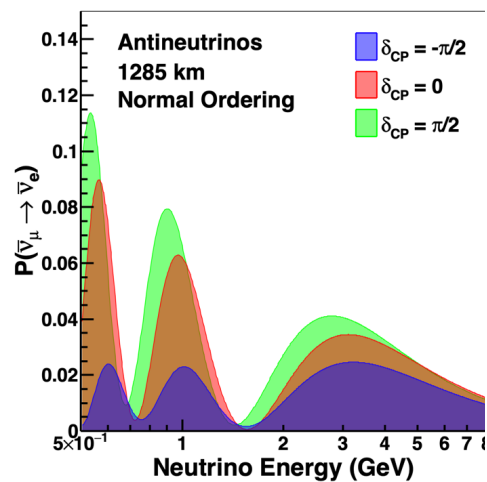
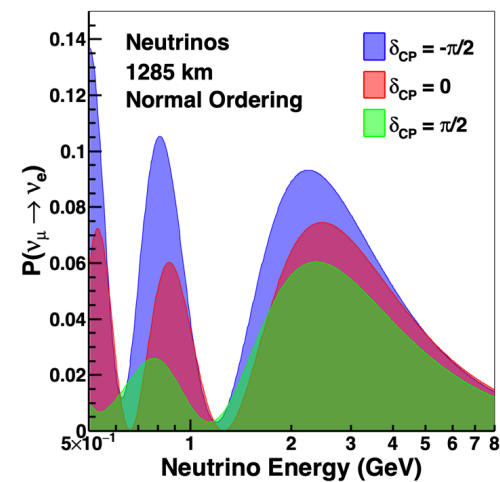
[arXiv:1511.05562](https://arxiv.org/abs/1511.05562)



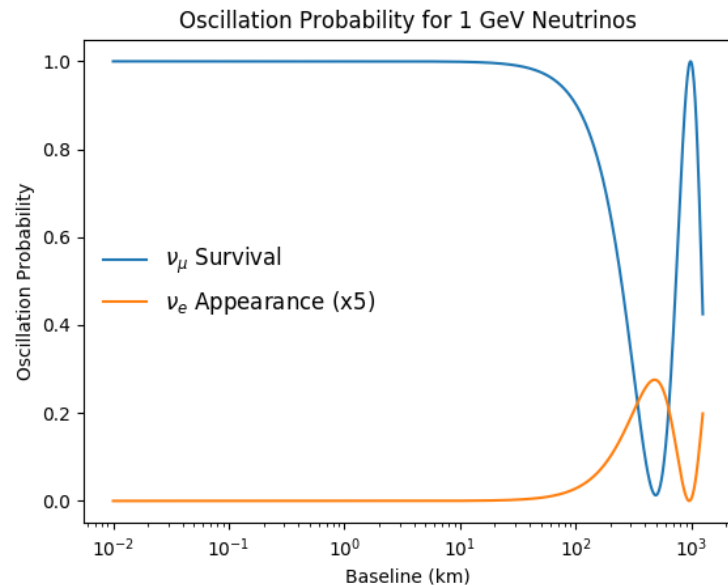
Neutrino and antineutrino appearance samples for a particular set of NSI parameters, compared to standard 3-neutrino mixing

Question: how does this compare to the impact of δ_{CP} from slide 13?

CPV VS NSI



STERILE NEUTRINOS



SBL
Experiments

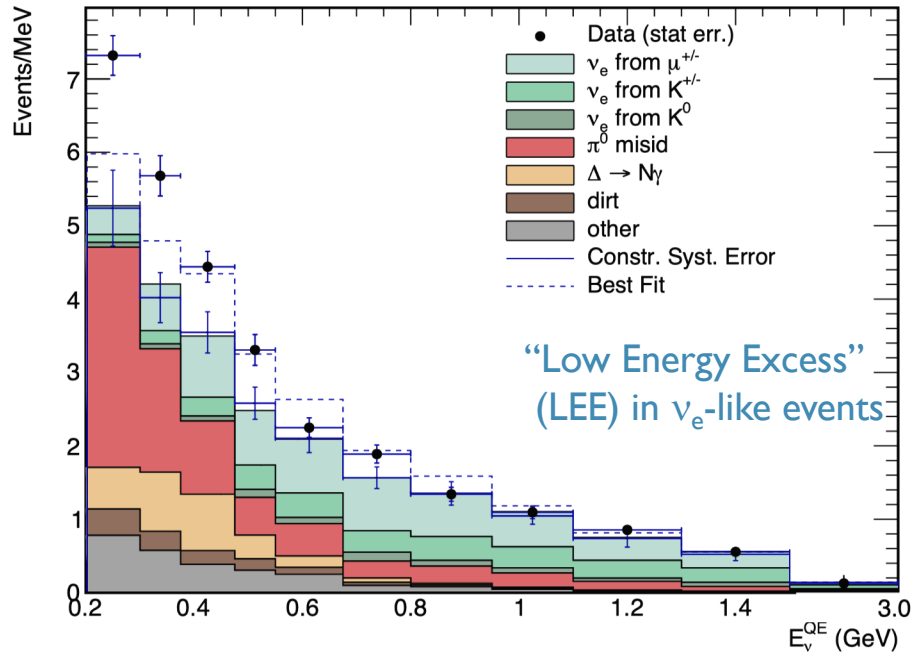


LBL
Experiments

- Based on the already-measured oscillation parameters, we do not expect to see muon neutrino oscillation at small values of L/E
 - i.e.: ν_μ survival probability should be ~ 1 and ν_e appearance probability should be ~ 0 for order 1 GeV neutrinos with baselines < 10 km
- Any ν_μ disappearance or ν_e appearance at these L/E values would require a larger mass splitting, which would require at least 1 additional neutrino mass state**

STERILE NEUTRINOS

MiniBooNE (BNB)
PRD 103,052002 (2021)



- Several experiments have observations suggesting possible ν_e appearance at $L/E \sim 1$
 - LSND, MiniBooNE
 - Potential explanation is an additional “sterile” neutrino with a mass splitting of $\sim 1 \text{ eV}^2$
- However, MicroBooNE does not observe LEE and there is no evidence for ν_μ disappearance at $L/E \sim 1$

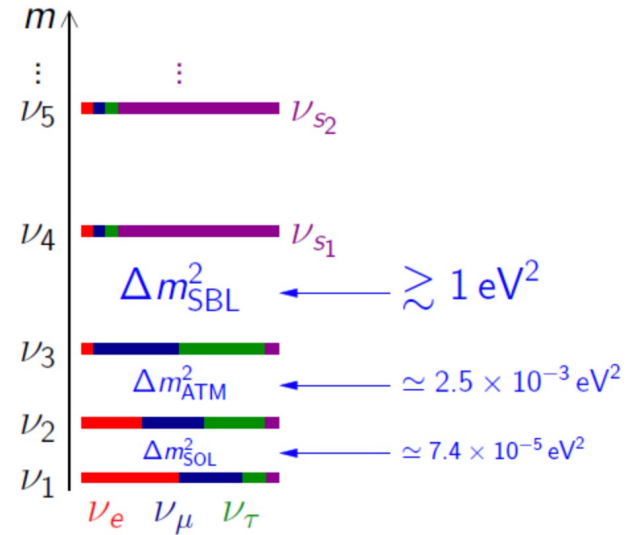
The significance of the excess observed by LSND is 3.8σ and by MiniBooNE is 4.8σ , for a combined significance of 6.1σ

STERILE NEUTRINOS

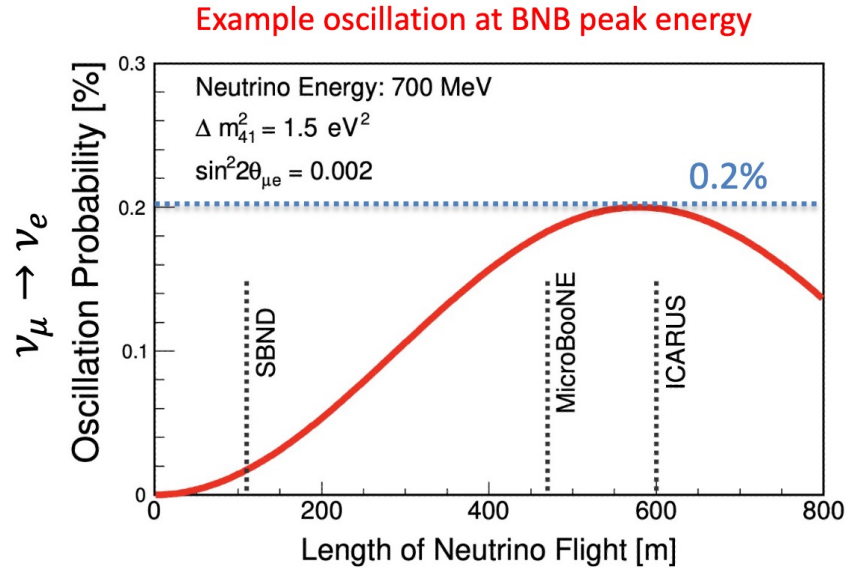
- 3 neutrino model $\rightarrow$ 3 + x neutrino model, where there are x additional, “sterile” neutrinos
- Sterile neutrinos mix with standard neutrinos (allows for additional oscillation), but do not have weak charge, (consistent with # of neutrinos from LEP/astrophysics)
- “3+1” model is simplest scenario; while this model is nearly excluded by data, we often quote sterile neutrino parameters in a simplified “2 flavor” version of this model

- $\sin^2 2\theta_{\mu e} = 4|U_{\mu 4}|^2|U_{e 4}|^2$ (ν_e appearance)
- $\sin^2 2\theta_{\mu\mu} = 4|U_{\mu 4}|^2(1-|U_{\mu 4}|^2)$ (ν_μ disappearance)
- $\sin^2 2\theta_{ee} = 4|U_{e 4}|^2(1-|U_{e 4}|^2)$ (ν_e disappearance)

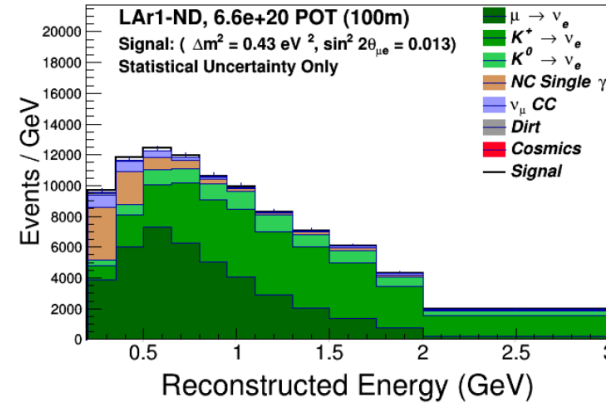
2 independent
matrix elements



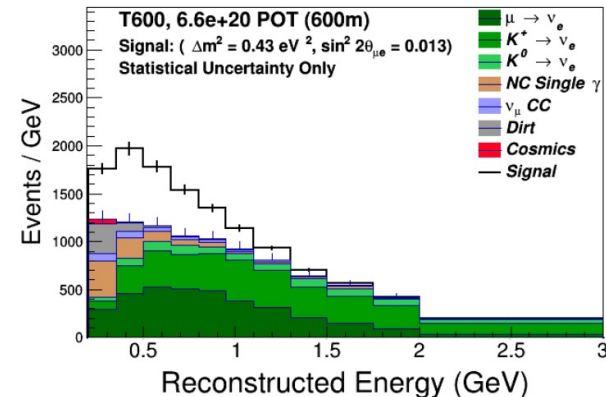
STERILE NEUTRINOS AT OSCILLATION EXPERIMENTS: SHORT BASELINE



Also sensitive to ν_μ disappearance at same baseline



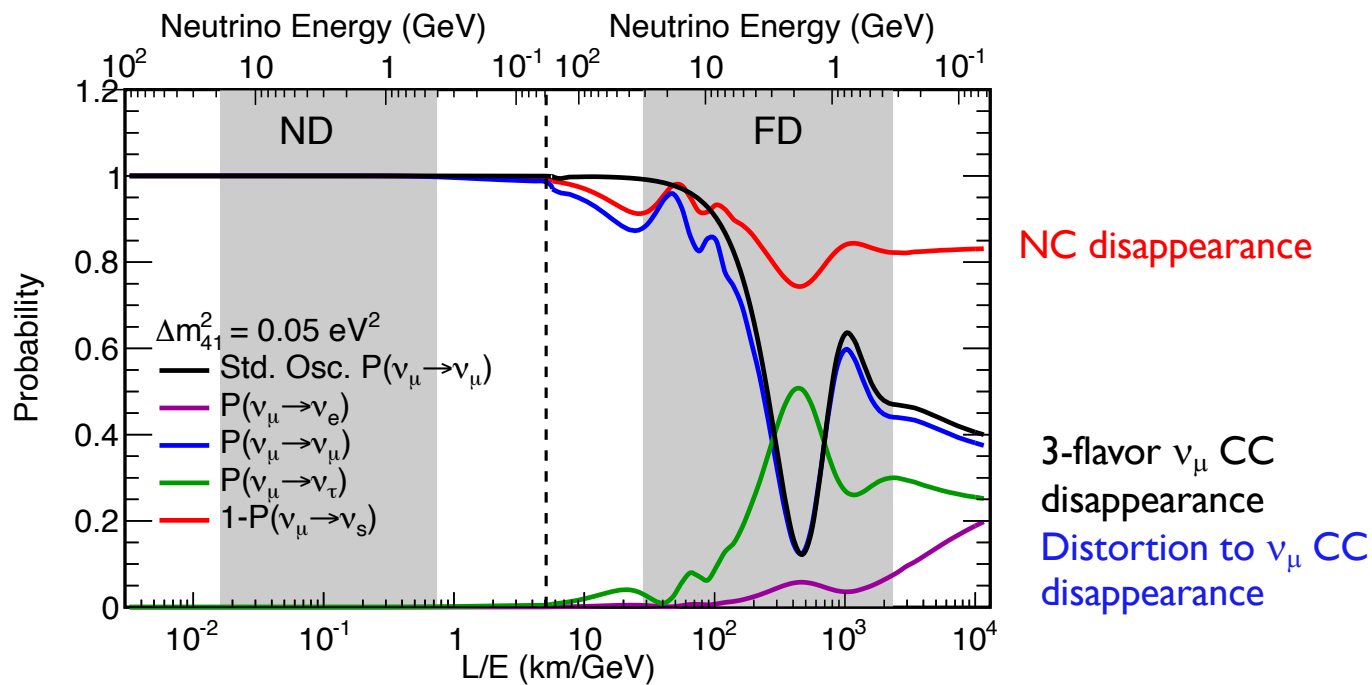
For these oscillation parameters, very little ν_e appearance at SBND



For these oscillation parameters, large ν_e appearance at ICARUS

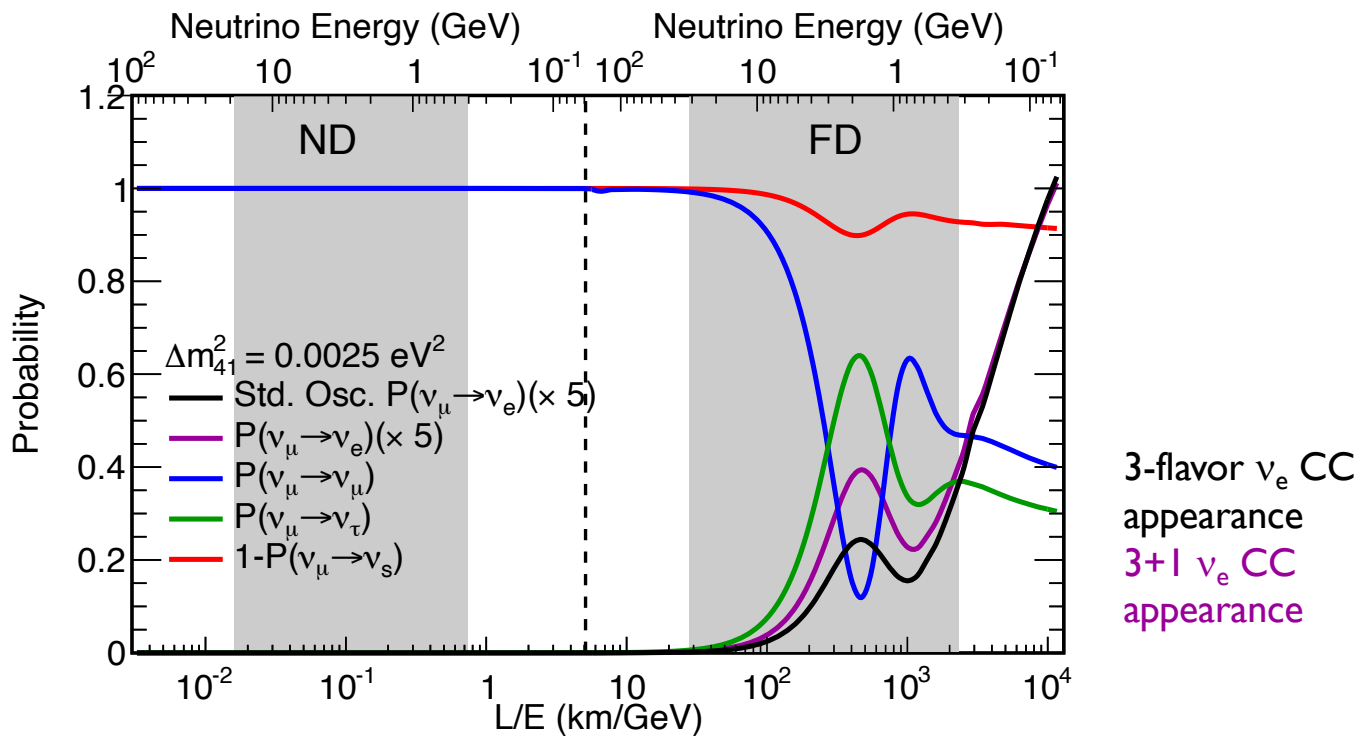
STERILE NEUTRINOS AT OSCILLATION EXPERIMENTS: LONG BASELINE

Sensitive to ν_μ disappearance at far detector in **NC** & **CC** channels



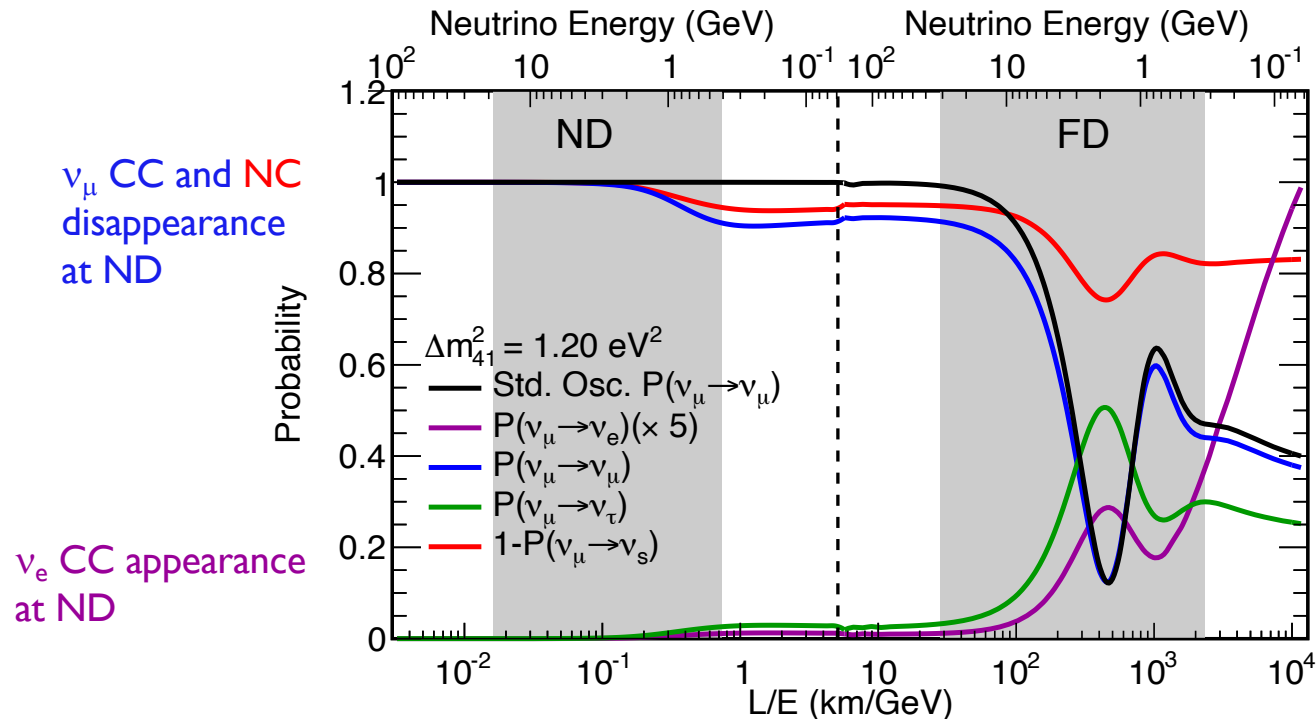
STERILE NEUTRINOS AT OSCILLATION EXPERIMENTS: LONG BASELINE

Sensitive to ν_e appearance at far detector (degenerate w/ PMNS)



STERILE NEUTRINOS AT OSCILLATION EXPERIMENTS: LONG BASELINE

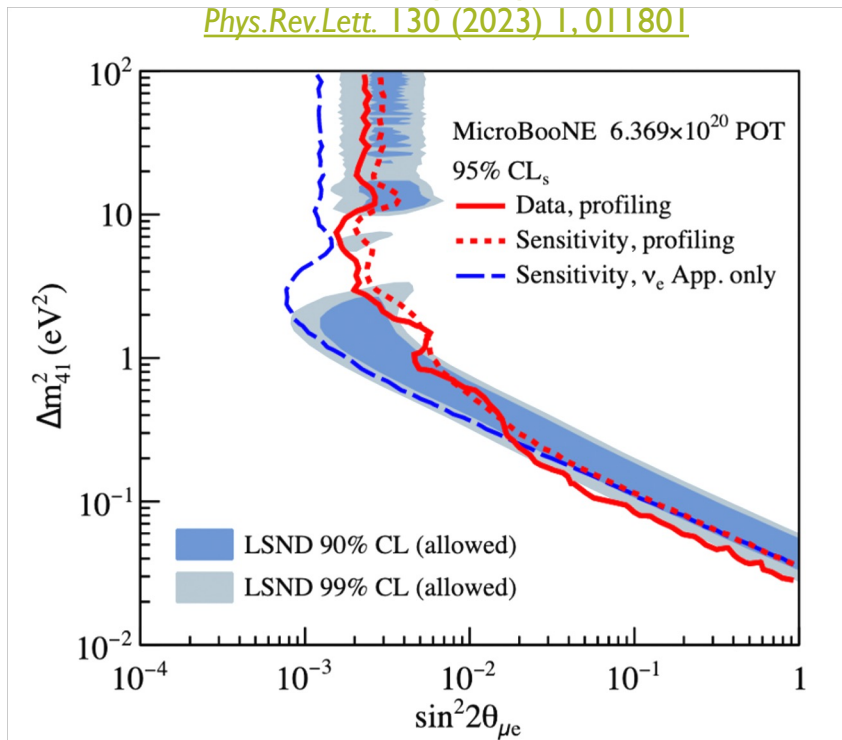
Sensitive to ν_μ disappearance and ν_e appearance at near detector



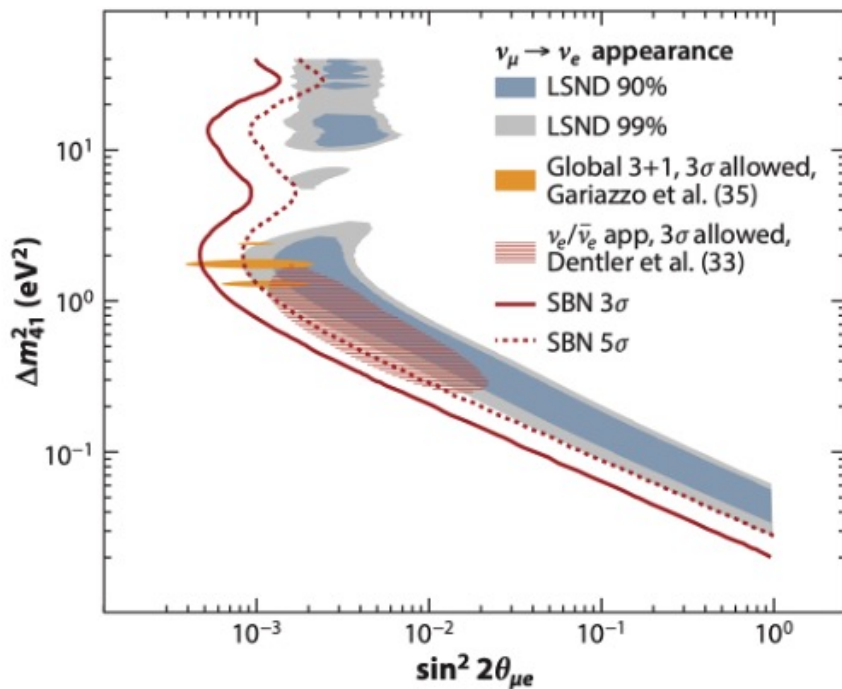
(SOME) STERILE NEUTRINO LIMITS & SENSITIVITY PROJECTIONS

MicroBooNE (BNB)

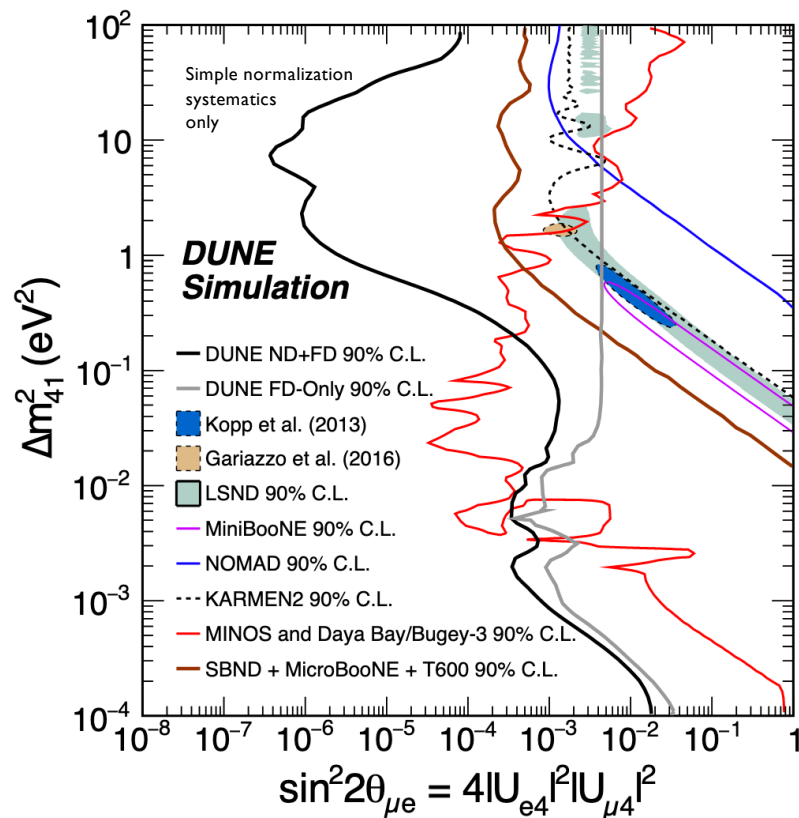
Phys.Rev.Lett. **130** (2023) 1, 011801



SBN sensitivity projection



(SOME) STERILE NEUTRINO LIMITS & SENSITIVITY PROJECTIONS



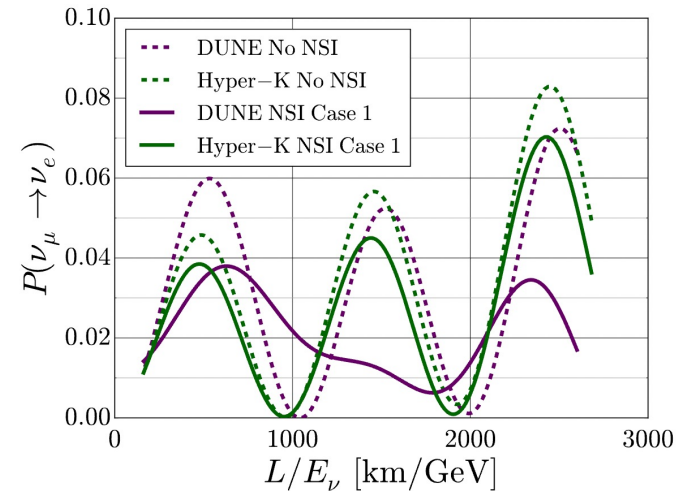
Questions:

- Why are these sensitivity/exclusion contours so wiggly?
- Compare the DUNE ND+FD and FD-only curves on this plot and the DUNE oscillation probabilities from a few slides back. Where do you think the DUNE sensitivity in the 1-10 eV² range is coming from?
- Do you think the “simple normalization systematics only” comment is important? Why?

EXPERIMENT COMPLEMENTARITY: UNDERSTANDING BSM EFFECTS

- Fun problem to have: differentiating types of new physics observed at next-gen experiments!
- NSI vs Sterile neutrino – if we see results inconsistent with 3-flavor neutrino oscillation, could we tell whether it was more likely to come from non-standard interactions or sterile neutrinos?
 - Sterile neutrino introduces new oscillation
 - Effects from NSI are similar to matter effect – more dramatic effect at higher energy/longer baseline
- Data at a different baselines (DUNE & Hyper-K) would observe very different oscillation probabilities for NSI

Appearance probabilities at DUNE and T2HK w/ NSI

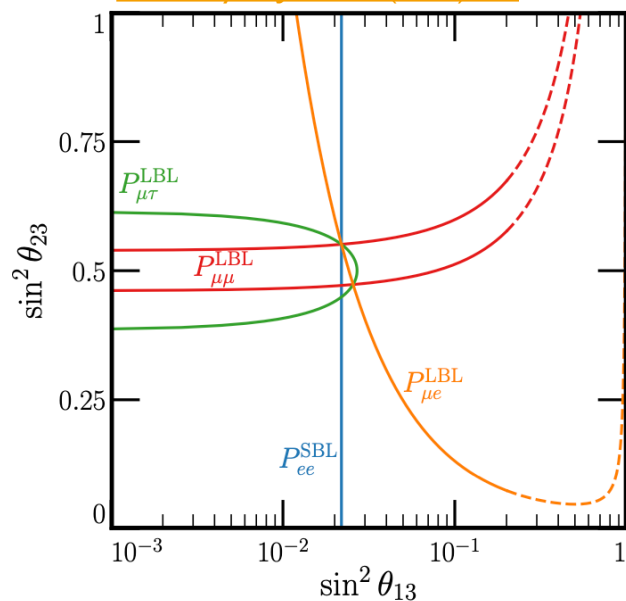


[de Gouvêa and Kelly, Nucl.Phys.B 908 \(2016\) 318-335](#)

Question: If we saw deviations from 3-flavor oscillation that behave similarly at DUNE and HyperK, what might we conclude about the new physics?

TESTING PMNS UNITARITY

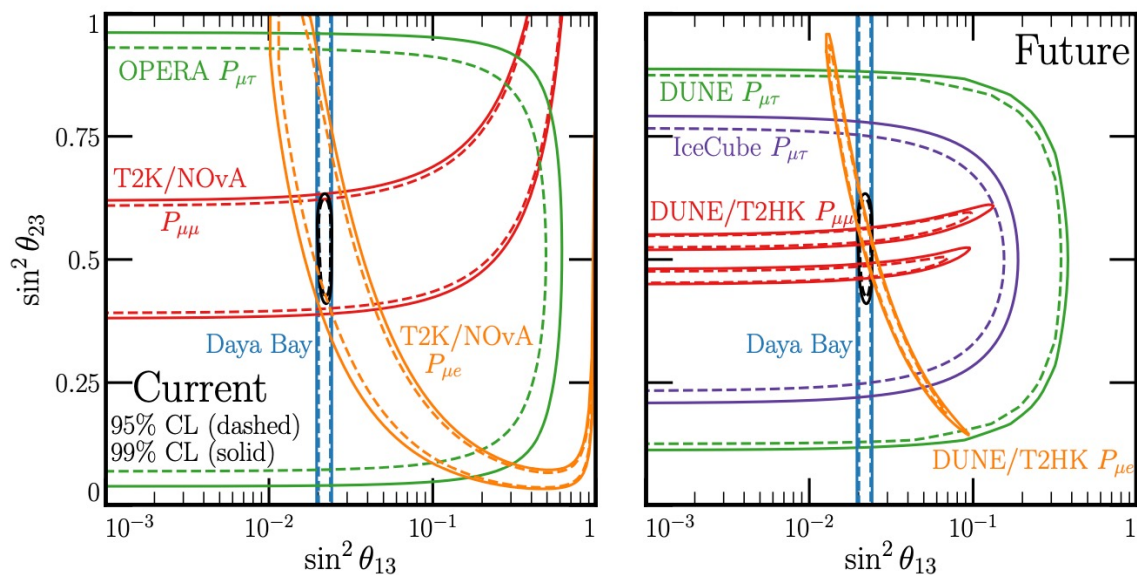
Ellis, Kelly, Li, *JHEP* 12 (2020) 068



- Hypothetical **infinite precision** measurements in $\theta_{23} - \theta_{13}$ space: combining values obtained from long-baseline oscillation measurements (ν_μ disappearance, ν_e appearance, and ν_τ appearance) with the reactor measurement of θ_{13} to test normalization of 3rd column of mixing matrix

TESTING PMNS UNITARITY

Ellis, Kelly, Li, *JHEP* 12 (2020) 068



- **Current and projected** measurements in $\theta_{23} - \theta_{13}$ space: combining values obtained from long-baseline oscillation measurements (ν_μ disappearance, ν_e appearance, and ν_τ appearance) with the reactor measurement of θ_{13} to test normalization of 3rd column of mixing matrix
- **Future experiments** dramatically tighten long-baseline contours such that if unitarity were violated, they would not overlap with the high significance we see in current data

SUMMARY

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- The existence of neutrino mass already means there must be new physics – we just don't know yet exactly what it looks like
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- Some new physics may affect the observed spectra in ways that are semi-degenerate with the 3-neutrino oscillation parameters or with other new physics models – experiments with different energies and baselines can disentangle these effects
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- Searches for new physics in neutrino oscillation are intrinsically tied to study of 3-neutrino oscillation