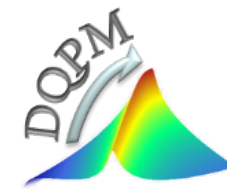
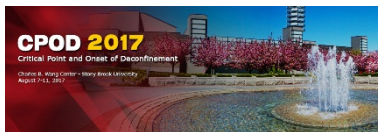


Traces of the deconfinend phase transition

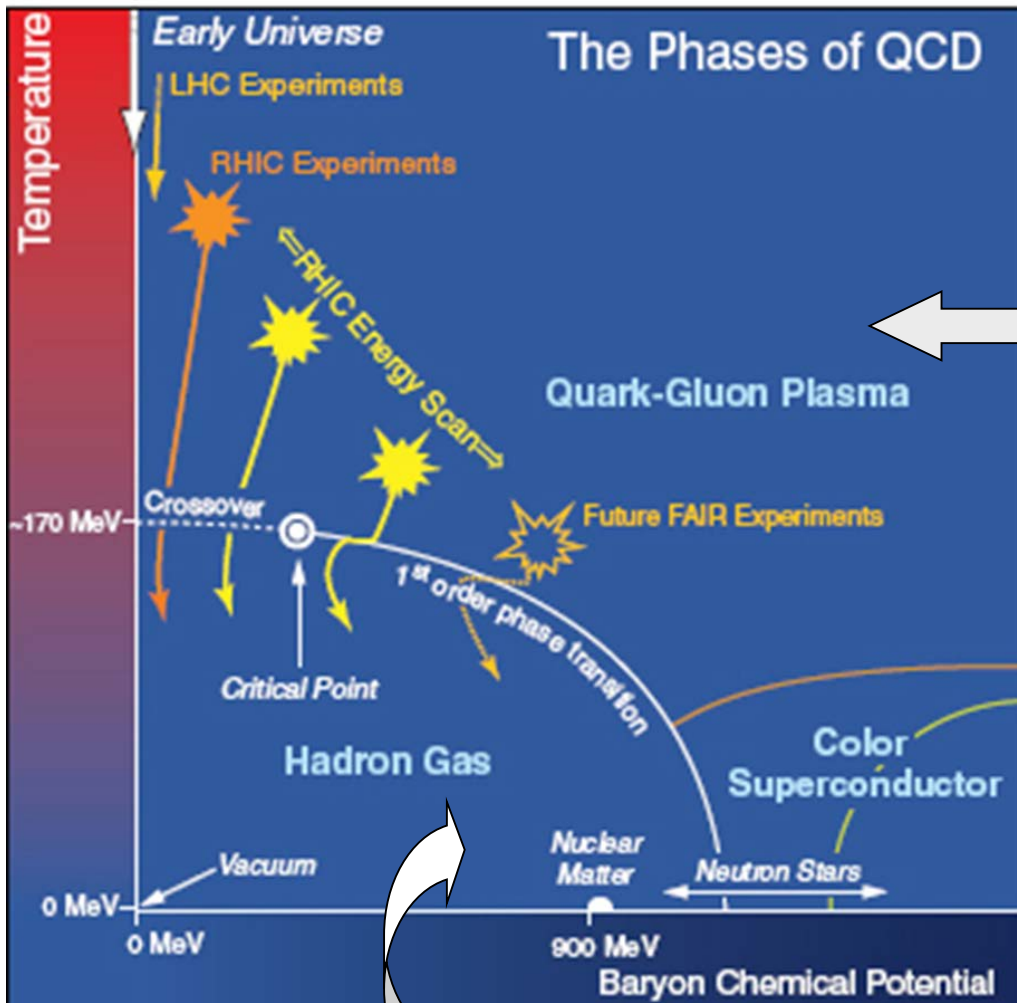
Elena Bratkovskaya
(GSI, Darmstadt & ITP, Uni. Frankfurt)

In collaboration with **Hamza Berrehrah**, Wolfgang Cassing,
Thorsten Steinert, Jörg Aichelin, Pol-Bernard Gossiaux,
Pierre Moreau, Taesoo Song

"CPOD2017": Critical Point and Onset of Deconfinement"
Stony Brook University, Stony Brook, NY
August 7-11, 2017



The ,holy grail‘ of heavy-ion physics:



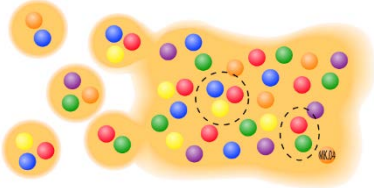
The phase diagram of QCD

- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**



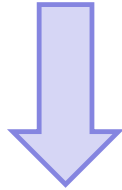
- Search for the **critical point**
- Search for signatures of **chiral symmetry restoration**

- Study of the **in-medium** properties of hadrons at high baryon density and temperature

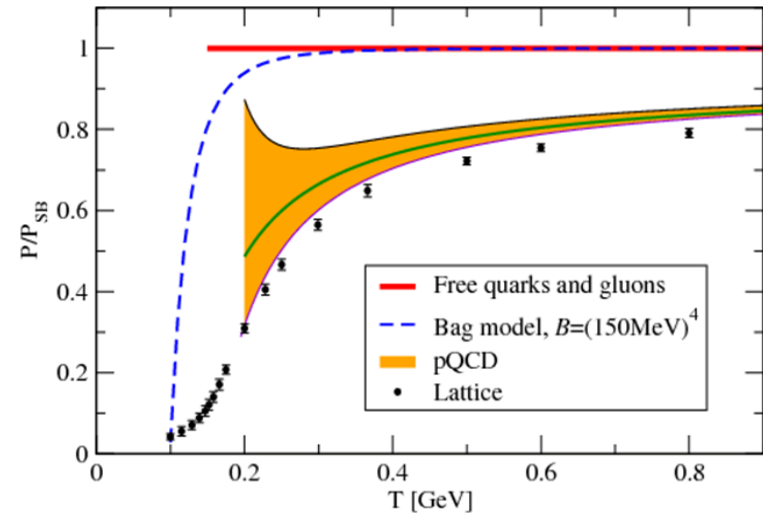


Degrees-of-freedom of QGP

❖ IQCD gives QGP EoS at finite μ_B



! need to be interpreted in terms of degrees-of-freedom



Non-perturbative QCD ← pQCD

pQCD:

- weakly interacting system
- massless quarks and gluons

Thermal QCD

= QCD at high parton densities:

- strongly interacting system
- massive quarks and gluons



❖ **Effective degrees-of-freedom**

QGP thermodynamics: from IQCD to QP/DQP

❖ Effective degrees-of-freedom → quasi-particles

➤ Grand canonical potential Ω in propagator (D,S) representation (2PI):

$$\beta\Omega[D, S] = \underbrace{\frac{1}{2}\text{Tr}[\ln D^{-1} - \Pi D]}_{\text{bosons}} - \underbrace{\text{Tr}[\ln S^{-1} + \Sigma S]}_{\text{fermions}} + \Phi[D, S]$$

Self-energies:

$$\frac{\delta\Phi}{\delta D} = \frac{1}{2}\Pi$$

$$\frac{\delta\Phi}{\delta S} = -\Sigma$$

Cf. J.P. Blaizot et al, PRD 63 (2001) 065003

1. Weakly interacting on-shell Quasi-Particles (QP):

$$\text{QP: } p_{\text{QP}}(T) = p^{\text{id gas}}(T, m^2(T)) + B(m^2(T)) \quad \frac{\partial p_{\text{QP}}(T, m^2)}{\partial m^2} = 0$$

➤ Different QP versions:

- Effective thermal masses (*Peshier et al., Greco et al, Bluhm et al,...*)
- Polyakov loop models (*Pisarski*)
- ...

Bag constant: $B(m^2(T))$

calculated self-consistently to render QGP thermodynamics consistently

Gorenstein & Yang, PRD **52**, 5206 (1995)

➤ Effective coupling, IR enhancement, massive transverse gluons

$$\alpha(T) = \frac{4\pi/11}{\ln\left(\lambda \frac{T+T_s}{T_c}\right)^2} \quad m^2(T) = \frac{1}{2} 4\pi\alpha(T)T^2$$

QGP thermodynamics: from IQCD to QP/DQP

❖ Effective degrees-of-freedom → quasi-particles

2. Strongly interacting Quasi-Particles (DQP):

➤ QPM → DQPM

- small entropy near T_c : large quasiparticle mass, large coupling from IQCD
→ large quasiparticle width γ

➤ Grand canonical potential Ω in propagator representation (2PI)
→ thermal properties of the system:

$$\Omega/V = -P \quad d\Omega = -SdT - PdV - Nd\mu \quad S = -\frac{\partial\Omega}{\partial T} \quad N = -\frac{\partial\Omega}{\partial\mu} \quad P = -\frac{\partial\Omega}{\partial V}$$

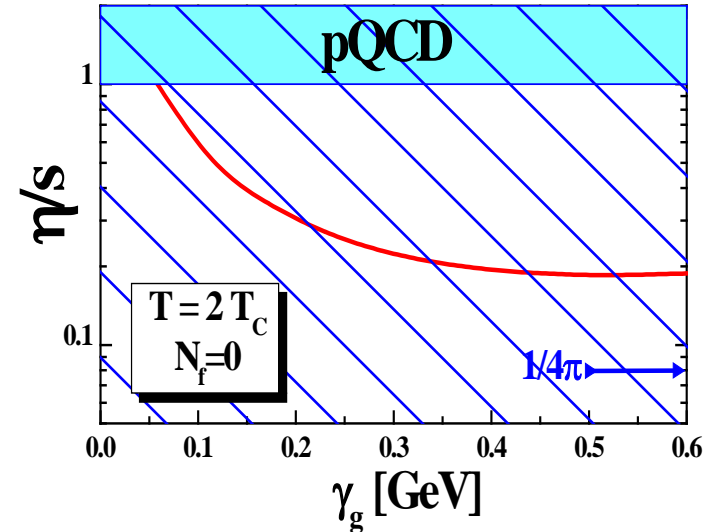


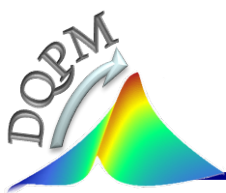
1. Determine entropy S , pressure P for DQP

2. Fit S , P from DQP with S , P from IQCD

→ Properties of quasi-particles

Peshier, Cassing, PRL 94 (2005) 172301





Dynamical QuasiParticle Model (DQPM) - Basic ideas:

DQPM describes **QCD** properties in terms of **'resumed' single-particle Green's functions** (propagators) – in the sense of a two-particle irreducible (2PI) approach:

gluon propagator: $\Delta^{-1} = P^2 - \Pi$ & quark propagator $S_q^{-1} = P^2 - \Sigma_q$
 gluon self-energy: $\Pi = M_g^2 - i2\gamma_g\omega$ & quark self-energy: $\Sigma_q = M_q^2 - i2\gamma_q\omega$

(scalar approximation)

- the resummed properties are specified by **complex (retarded) self-energies**:
 - the **real part of self-energies** (Σ_q, Π) describes a **dynamically generated mass** (M_q, M_g);
 - the **imaginary part** describes the **interaction width** of partons (γ_q, γ_g)

- **Spectral functions** : $A_q \sim \text{Im} S_q^{ret}$, $A_g \sim \text{Im} \Delta^{ret}$

□ **Entropy density of interacting bosons and fermions in the quasiparticle limit (2PI)**

(G. Baym 1998):

QGP

$$\begin{aligned}
 s^{dqp} = & -d_g \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} \frac{\partial n_B}{\partial T} (\text{Im} \ln(-\Delta^{-1}) + \text{Im} \Pi \text{Re} \Delta) && \text{gluons} \\
 & - d_q \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} \frac{\partial n_F((\omega - \mu_q)/T)}{\partial T} (\text{Im} \ln(-S_q^{-1}) + \text{Im} \Sigma_q \text{Re} S_q) && \text{quarks} \\
 & - d_{\bar{q}} \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} \frac{\partial n_F((\omega + \mu_q)/T)}{\partial T} (\text{Im} \ln(-S_{\bar{q}}^{-1}) + \text{Im} \Sigma_{\bar{q}} \text{Re} S_{\bar{q}}) && \text{antiquarks}
 \end{aligned}$$

DQPM (T)

DQPM(T): properties of quasiparticles

Properties of interacting quasi-particles:
massive quarks and gluons (g, q, q_{bar})
 with **Lorentzian spectral functions** :

$$A(\omega, p) = \frac{\gamma}{E} \left(\frac{1}{(\omega - E)^2 + \gamma^2} - \frac{1}{(\omega + E)^2 + \gamma^2} \right)$$

$$E^2 = p^2 + M^2 - \gamma^2$$

■ **Modeling of the quark/gluon masses and widths** → **HTL limit at high T**

masses: $m_g^2 = \frac{g^2}{6} \left(N_c + \frac{1}{2} N_f \right) T^2, \quad m_q^2 = g^2 \frac{N_c^2 - 1}{8N_c} T^2$

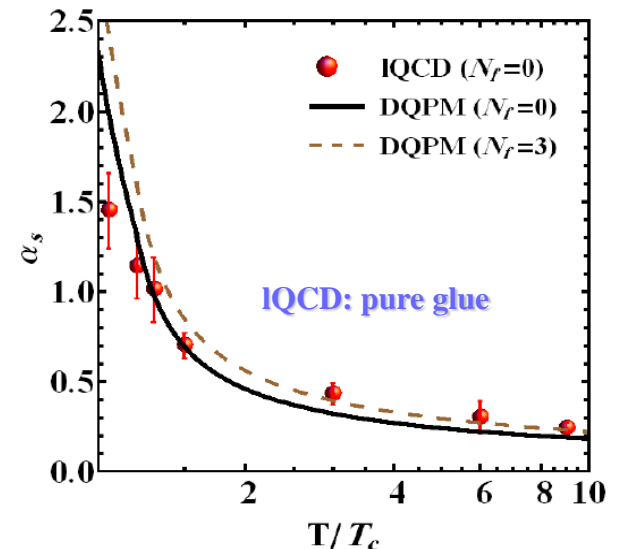
widths: $\gamma_g = \frac{1}{3} N_c \frac{g^2 T}{8\pi} \ln \left(\frac{2c}{g^2} + 1 \right), \quad \gamma_q = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{8\pi} \ln \left(\frac{2c}{g^2} + 1 \right)$

■ **running coupling (pure glue):** →

$$\alpha_s(T) = \frac{g^2(T)}{4\pi} = \frac{12\pi}{(11N_c - 2N_f) \ln[\lambda^2(T/T_c - T_s/T_c)^2]}$$

□ **fit to lattice (IQCD) results (e.g. entropy density)**

with 3 parameters: $T_s/T_c=0.46$; $c=28.8$; $\lambda=2.42$ (for pure glue $N_f=0$)



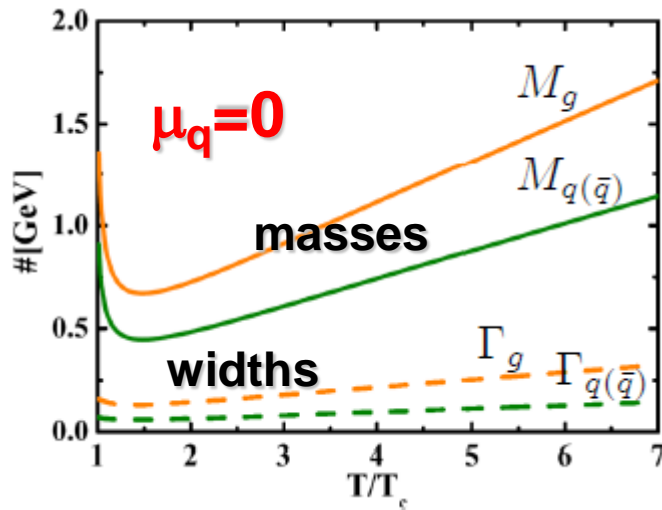
DQPM at finite T and $\mu_q=0$

➤ fit to lattice (IQCD) results

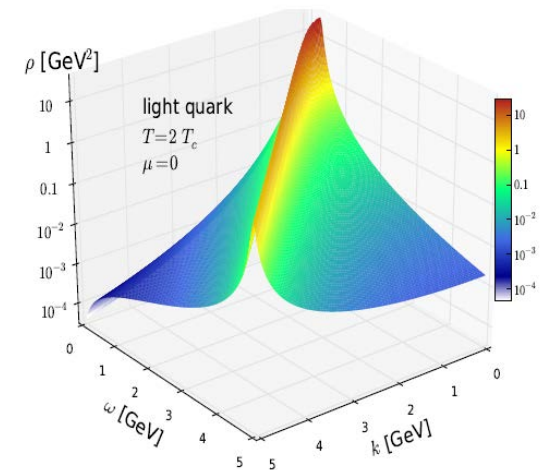
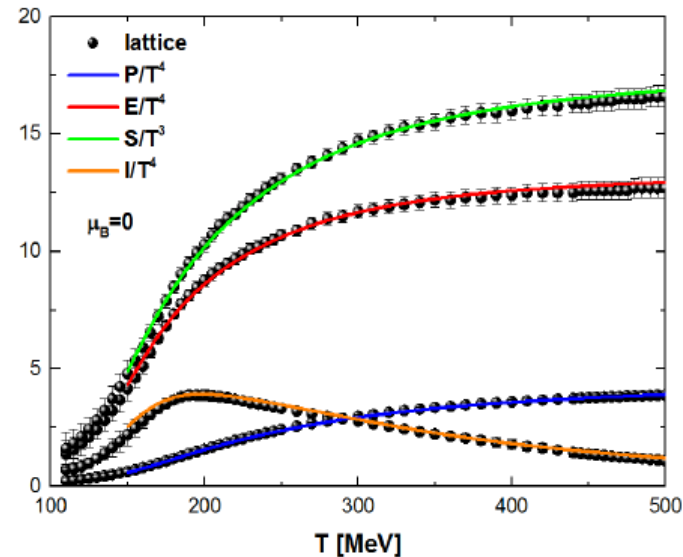
* BMW IQCD data S. Borsanyi et al., JHEP 1009 (2010) 073

➔ Quasiparticle properties:

- large width and mass for gluons and quarks



$T_C=158 \text{ MeV}$
 $\epsilon_C=0.5 \text{ GeV/fm}^3$

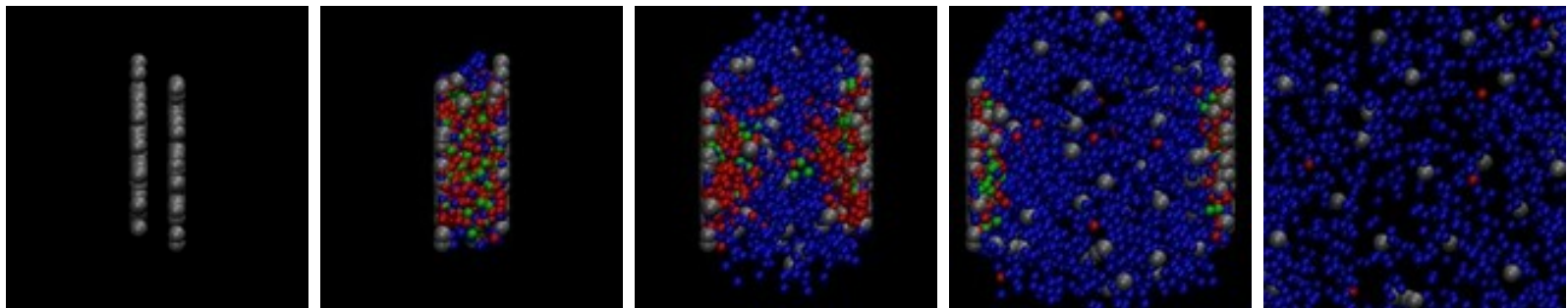


DQPM

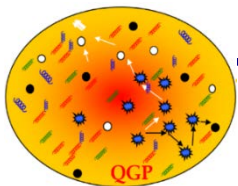
- matches well lattice QCD
- provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)
- gives transition rates for the formation of hadrons

➔ microscopic dynamical transport approach **PHSD**

Traces of the QGP in observables in high energy heavy-ion collisions



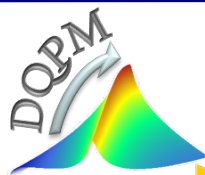
Basic idea: off-shell PHSD approach



QGP in equilibrium

Dynamical QuasiParticle Model (DQPM):

Quasiparticle properties:
 ,resummed' self-energies, propagators
 → Calculation of cross sections



fitted to

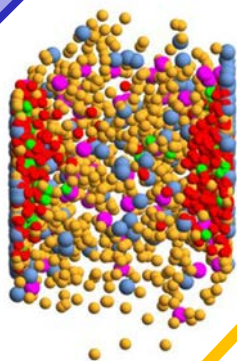
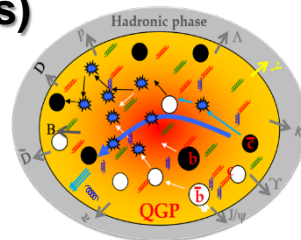
IQCD

controlled by IQCD!

Calculation of **transport coefficients in equilibrium** $\eta, \zeta, \sigma_0, \dots$

DQPM: consider the **effects of the nonperturbative nature** of the strongly interacting quark-gluon plasma (**sQGP**) constituents (vs. pQCD models)

QGP out-of-equilibrium ↔ HIC



Parton-Hadron-String-Dynamics (PHSD)

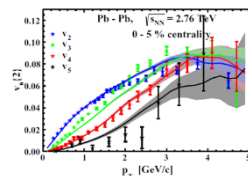
controlled by

experimental data + IQCD



Partonic interactions → DQPM
 hadronic interactions → hadron physics

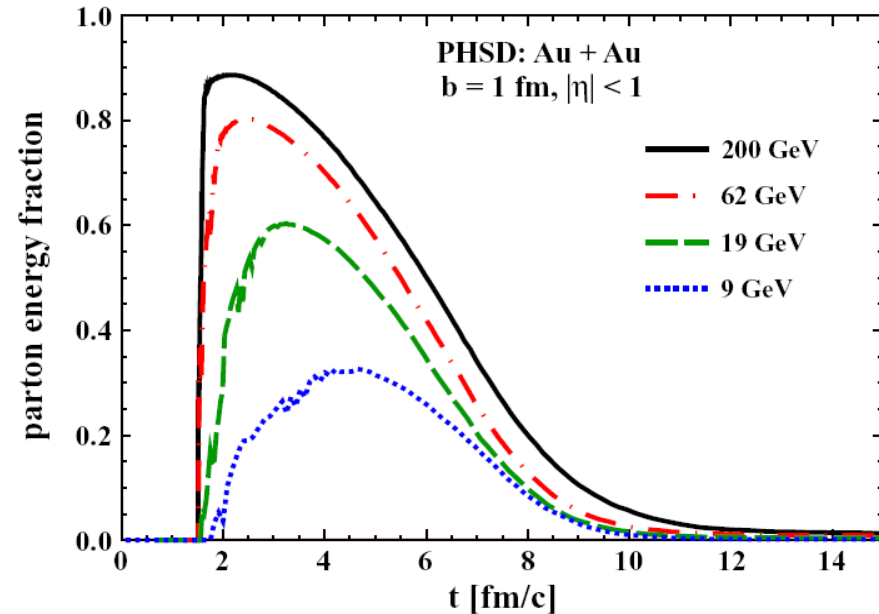
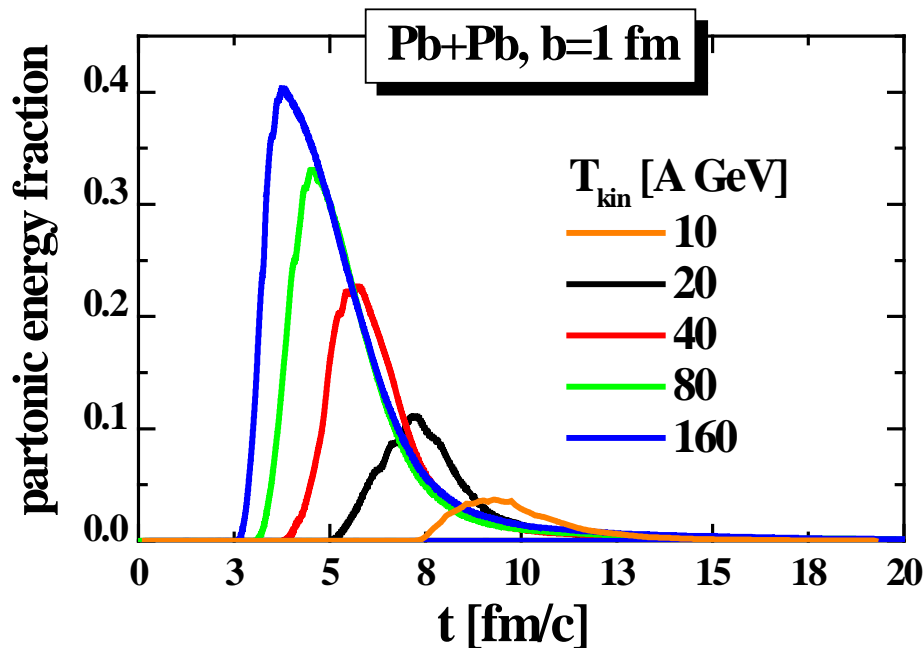
* **In-medium** hadronic interactions → many-body physics: G-matrix



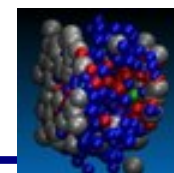


Partonic energy fraction in central A+A

Time evolution of the partonic energy fraction vs energy

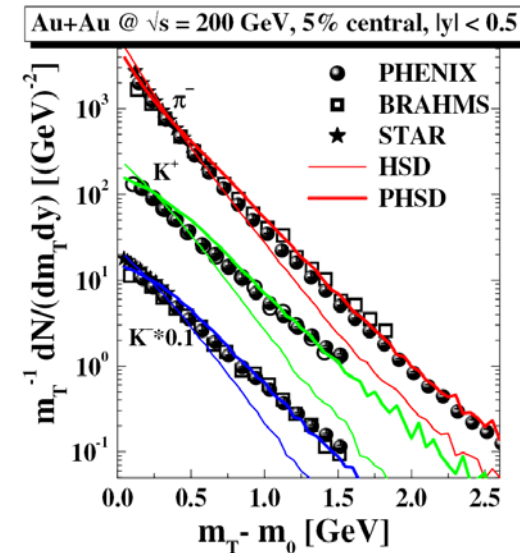
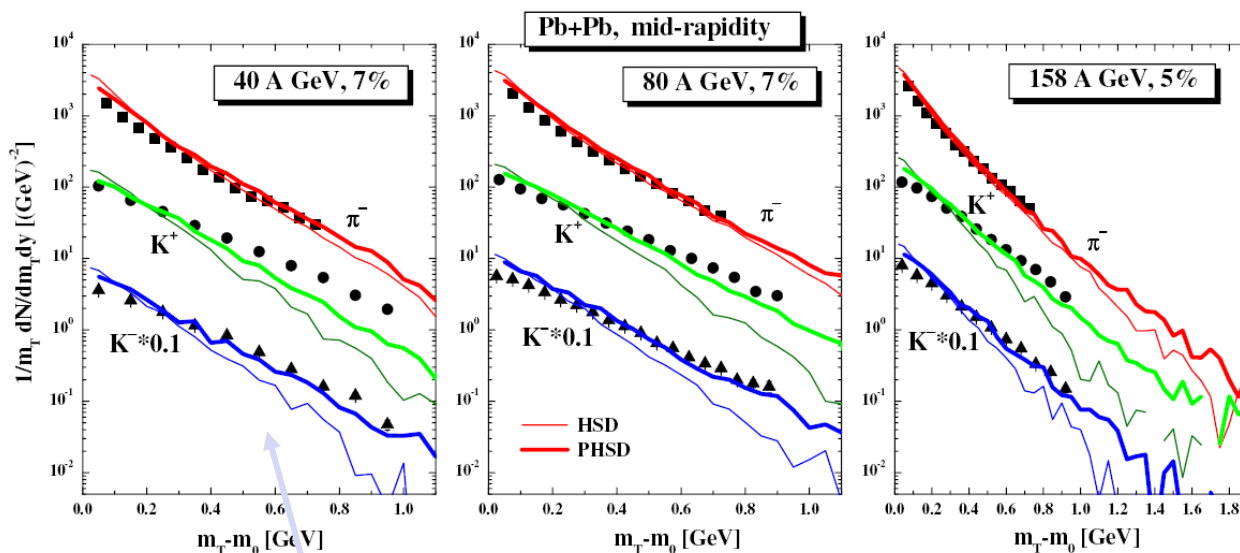


- Strong increase of partonic phase with energy from AGS to RHIC
- SPS: Pb+Pb, 160 A GeV: only about 40% of the converted energy goes to partons; the rest is contained in the large hadronic corona and leading partons
- RHIC: Au+Au, 21.3 A TeV: up to 90% - QGP



Central Pb + Pb at SPS energies

Central Au+Au at RHIC

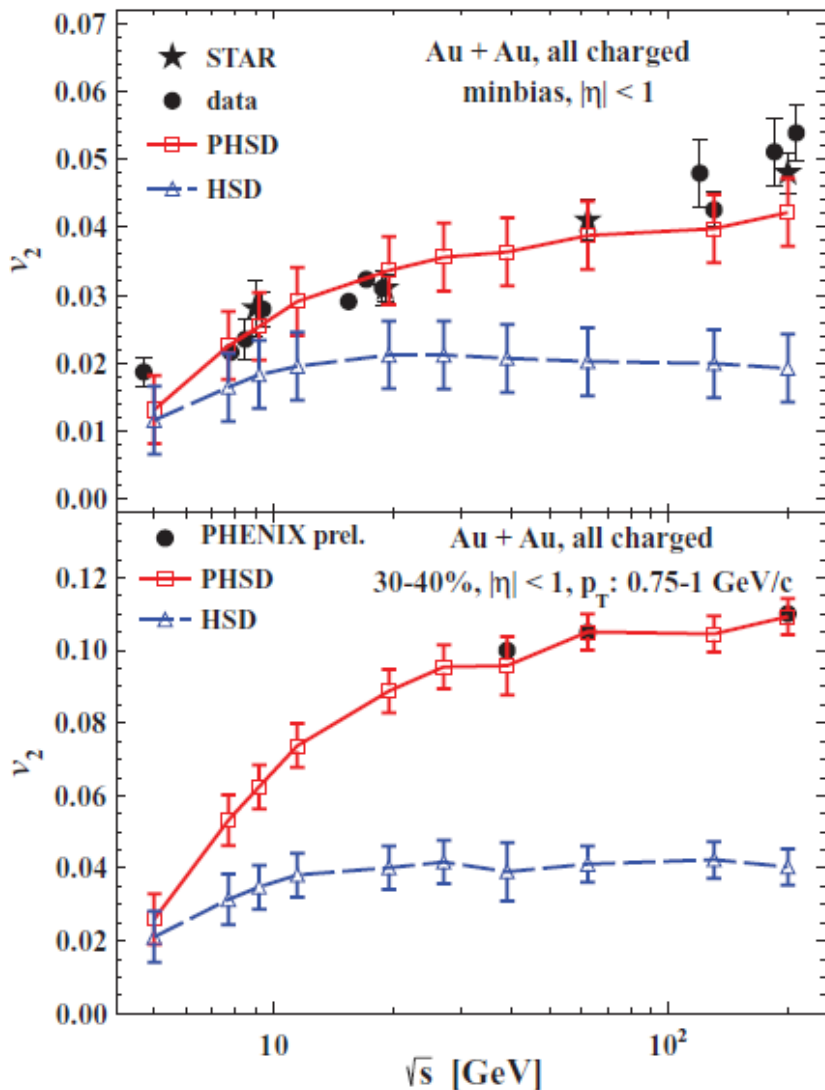
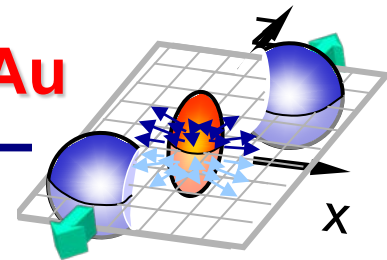


☐ PHSD gives **harder m_T spectra** and works better than HSD (wo QGP) at high energies – RHIC, SPS (and top FAIR, NICA)

☐ however, at **low SPS** (and low FAIR, NICA) energies the **effect of the partonic phase decreases** due to the decrease of the partonic fraction

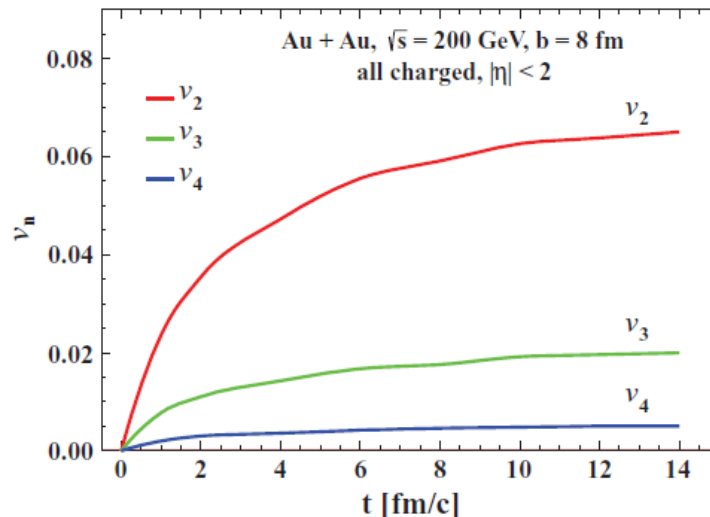


Elliptic flow v_2 vs. collision energy for Au+Au



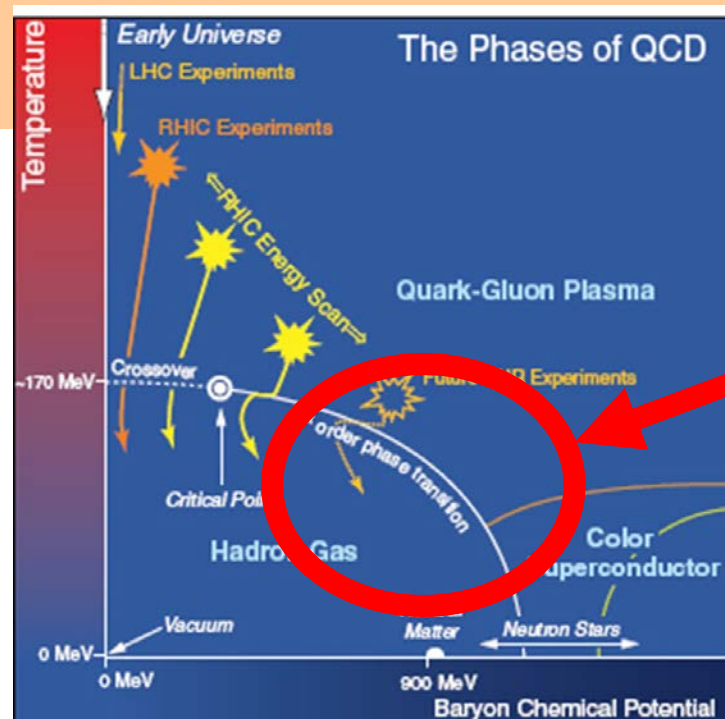
$$\frac{dN}{d\varphi} \propto \left(1 + 2 \sum_{n=1}^{+\infty} v_n \cos[n(\varphi - \psi_n)] \right)$$

$$v_n = \langle \cos n(\varphi - \psi_n) \rangle, \quad n = 1, 2, 3, \dots$$



- v_2 in PHSD is larger than in HSD due to the repulsive scalar mean-field potential $U_s(\rho)$ for partons
- v_2 grows with bombarding energy due to the increase of the parton fraction

Extended DQPM (T, μ_q)



finite μ_q

DQPM at finite (T, μ_q) : scaling hypothesis

- Scaling hypothesis for the effective temperature T^* for $N_f = N_c = 3$

$$\mu_u = \mu_d = \mu_s = \mu_q$$

$$T^{*2} = T^2 + \frac{\mu_q^2}{\pi^2}$$

- Coupling constant:

$$g(T/T_c(\mu=0)) \longrightarrow g(T^*/T_c(\mu))$$

- Critical temperature $T_c(\mu_q)$: obtained by requiring a constant energy density ε for the system at $T=T_c(\mu_q)$ where ε at $T_c(\mu_q=0)=158$ GeV is fixed by IQCD at $\mu_q=0$



$$\frac{T_c(\mu_q)}{T_c(\mu_q=0)} = \sqrt{1 - \alpha \mu_q^2} \approx 1 - \alpha/2 \mu_q^2 + \dots$$

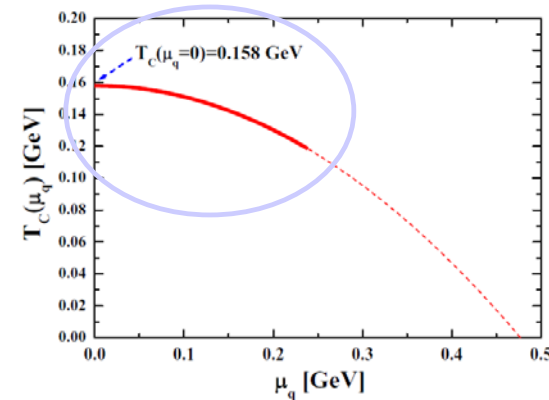
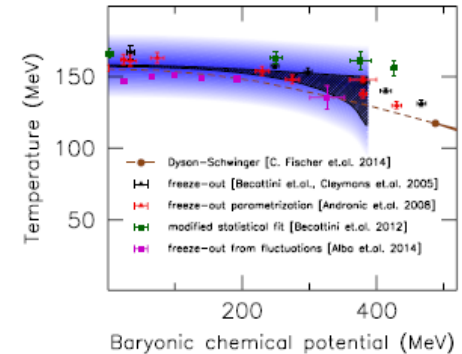
! Consistent with lattice QCD:

IQCD: C. Bonati et al., PRC90 (2014) 114025

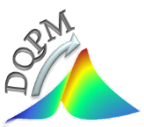
$$\frac{T_c(\mu_B)}{T_c} = 1 - \kappa \left(\frac{\mu_B}{T_c} \right)^2 + \dots$$

$$\text{IQCD } \kappa = 0.013(2) \longleftrightarrow \kappa_{DQPM} \approx 0.0122$$

Talk by Jana Gunther



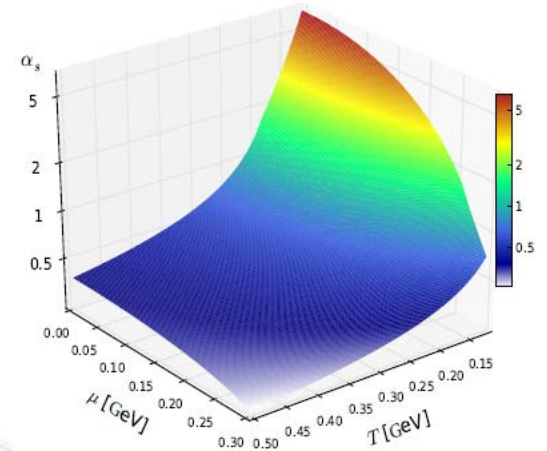
$$\alpha \approx 8.79 \text{ GeV}^{-2}$$



DQPM at finite (T, μ_q) : quasiparticle masses and widths

□ Coupling constant:

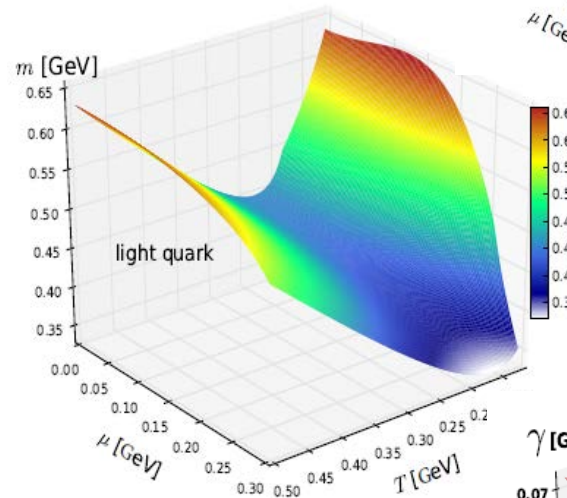
$$g^2(T^*/T_c(\mu_q)) = \frac{48\pi^2}{(11N_c - 2N_f) \ln \left(\lambda^2 \left(\frac{T^*}{T_c(\mu_q)} - \frac{T_s}{T_c(\mu_q)} \right)^2 \right)}$$



□ Quark and gluon masses:

$$M_g^2(T^*, \mu_q) = \frac{g^2(T^*/T_c(\mu_q))}{6} (N_c + \frac{1}{2}N_f) T^{*2},$$

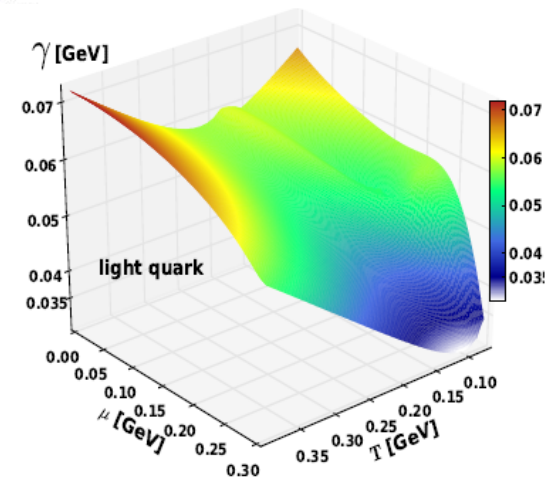
$$M_q^2(T^*, \mu_q) = \frac{N_c^2 - 1}{8N_c} g^2(T^*/T_c(\mu_q)) T^{*2},$$



□ Quark and gluon widths:

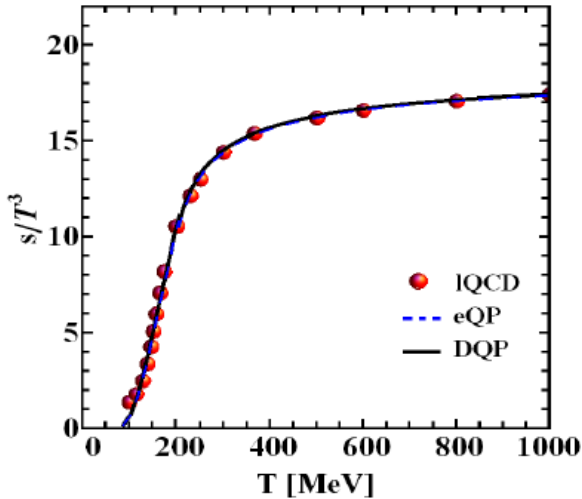
$$\gamma_g(T, \mu_q) = \frac{1}{3} N_c \frac{g^2(T^*/T_c(\mu_q))}{8\pi} T \ln \left(\frac{2c}{g^2(T^*/T_c(\mu_q))} + 1 \right),$$

$$\gamma_q(T, \mu_q) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2(T^*/T_c(\mu_q))}{8\pi} T \ln \left(\frac{2c}{g^2(T^*/T_c(\mu_q))} + 1 \right).$$

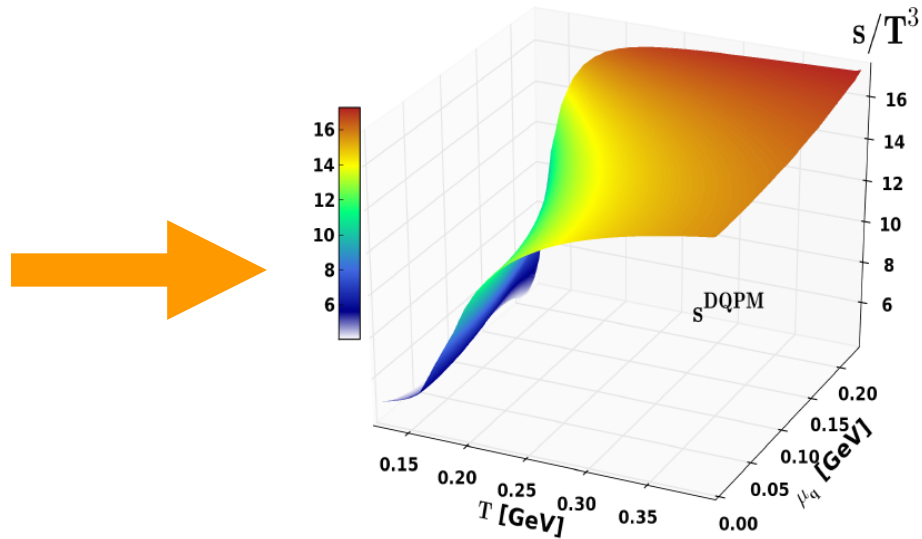


DQPM: thermodynamics at finite (T, μ_q)

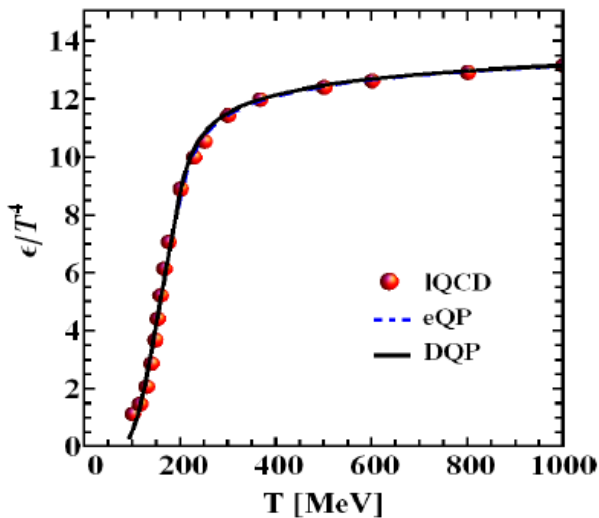
Entropy density at finite T



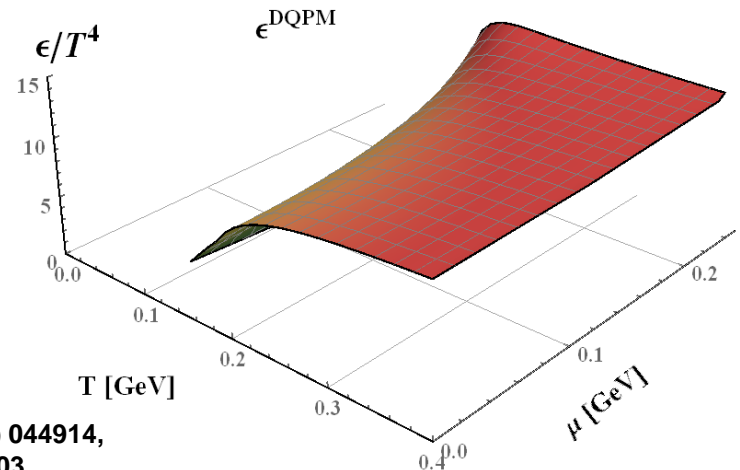
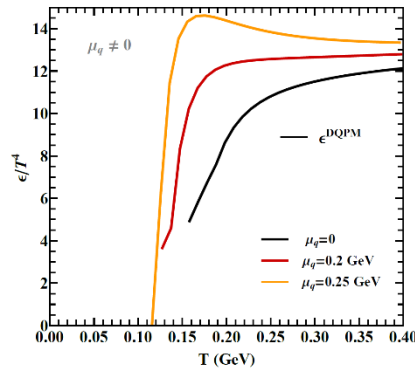
Entropy density at finite (T, μ_q)



Energy density at finite T



Energy density at finite (T, μ_q)



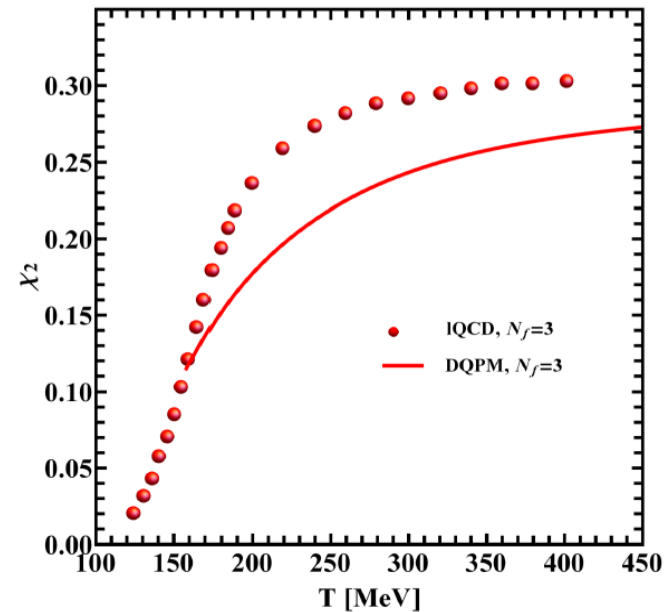
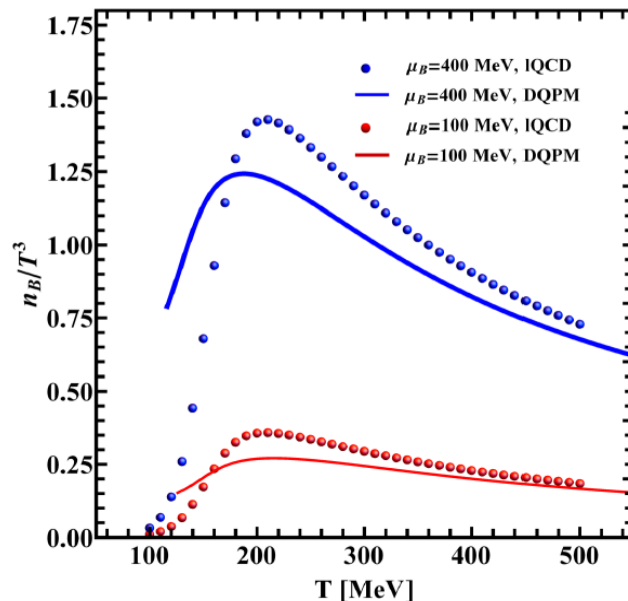
DQPM(T, μ_q): n_B , χ_q

□ Baryon number density n_B , susceptibilities χ_q at finite (T, μ)

$$\chi_q(T) = \left. \frac{\partial n_q}{\partial \mu_q} \right|_{\mu_q=0}; \quad \chi_q(T, \mu_q) = \frac{1}{9} \frac{\partial n_B}{\partial \mu_B}$$

$$\chi_2(T) = \frac{1}{9} \frac{1}{T^2} \left. \frac{\partial n_q(T, \mu_q)}{\partial \mu_q} \right|_{\mu_q=0} = \frac{1}{9} \frac{\chi_q(T)}{T^2}$$

for 3 flavours with $\mu_u = \mu_d = \mu_s = \mu_q$



- Comparison to IQCD : n_B , χ_q from DQPM is lower then IQCD data
- Quarks / gluons from DQPM are too heavy?

DQPM* (T, μ_q , p)

DQPM* at finite (T, μ_q, p): quasiparticle masses and widths

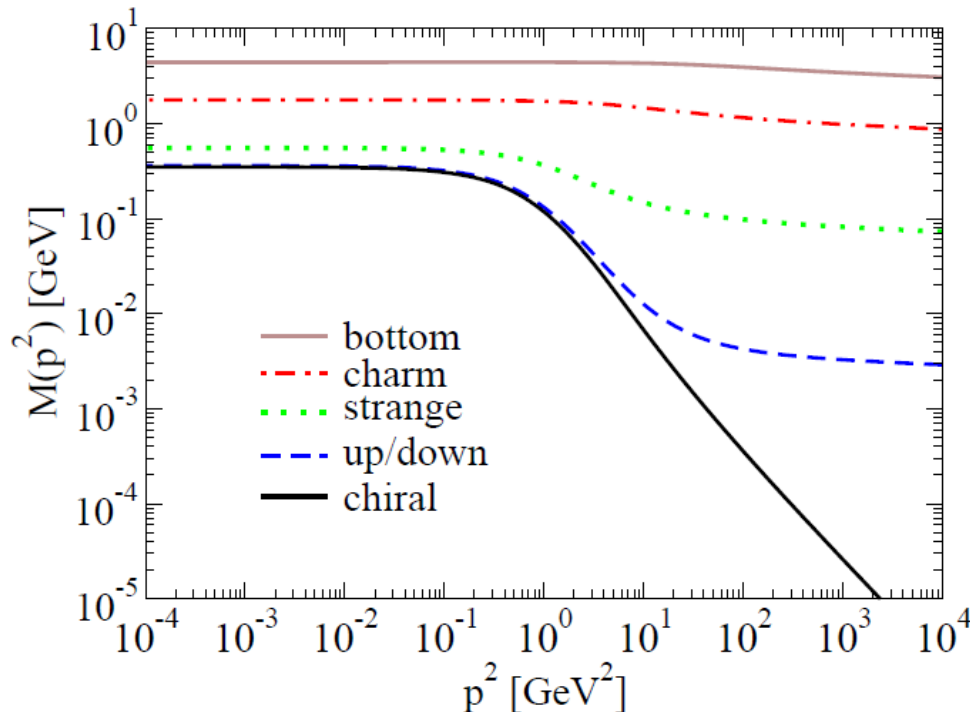
- Momentum dependent Lorentzian spectral function :

H. Berrehrah et al, PRC 93 (2016) 044914, arXiv:1512.06909;
Int.J.Mod.Phys. E25 (2016) 1642003, arXiv:1605.02371

$$\rho_i(\omega, \mathbf{p}) = \frac{\gamma_i(\mathbf{p})}{\tilde{E}_i(\mathbf{p})} \left(\frac{1}{(\omega - \tilde{E}_i(\mathbf{p}))^2 + \gamma_i^2(\mathbf{p})} - \frac{1}{(\omega + \tilde{E}_i(\mathbf{p}))^2 + \gamma_i^2(\mathbf{p})} \right)$$

$$\tilde{E}_i^2(\mathbf{p}) = p^2 + M_i^2(\mathbf{p}) - \gamma_i^2(\mathbf{p}) \text{ for } i \in [g, q, \bar{q}].$$

- p dependence of $m_{q, g}$ inspired from Dyson-Schwinger results



Ch.S. Fischer J. Phys. G: Nucl.
Part. Phys. 32 (2006) R253–R291

DQPM* at finite (T, μ_q, p): quasiparticle masses and widths

H. Berrehrah et al, PRC 93 (2016) 044914, arXiv:1512.06909;
Int.J.Mod.Phys. E25 (2016) 1642003, arXiv:1605.02371

Quark and gluon masses:

$$M_g(T, \mu_q, p) = \left(\frac{3}{2}\right) \left[\frac{g^2(T^*/T_c(\mu_q))}{6} \left[(N_c + \frac{N_f}{2})T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right] \right]^{1/2} \times \underline{h(\Lambda_g, p)} + m_{\chi_g},$$

$$M_{q,\bar{q}}(T, \mu_q, p) = \left[\frac{N_c^2 - 1}{8N_c} g^2(T^*/T_c(\mu_q)) \left[T^2 + \frac{\mu_q^2}{\pi^2} \right] \right]^{1/2} \times \underline{h(\Lambda_q, p)} + m_{\chi_q},$$

$$h(\Lambda, p) = \left[\frac{1}{1 + \Lambda(T_c(\mu_q)/T^*)p^2} \right]^{1/2}$$

Quark and gluon widths:

$$\gamma_g(T, \mu_q, p) = N_c \frac{g^2(T^*/T_c(\mu_q))}{8\pi} T \ln \left(\frac{2c}{g^2(T^*/T_c(\mu_q))} + 1.1 \right)^{3/4} \times \underline{h(\Lambda_g, p)},$$

$$\gamma_{q,\bar{q}}(T, \mu_q, p) = \frac{N_c^2 - 1}{2N_c} \frac{g^2(T^*/T_c(\mu_q))}{8\pi} T \ln \left(\frac{2c}{g^2(T^*/T_c(\mu_q))} + 1.1 \right)^{3/4} \times \underline{h(\Lambda_q, p)}$$

$$\Lambda_g(T_c(\mu_q)/T^*) = 5 (T_c(\mu_q)/T^*)^2 \text{ GeV}^{-2}$$

$$\Lambda_q(T_c(\mu_q)/T^*) = 12 (T_c(\mu_q)/T^*)^2 \text{ GeV}^{-2}$$

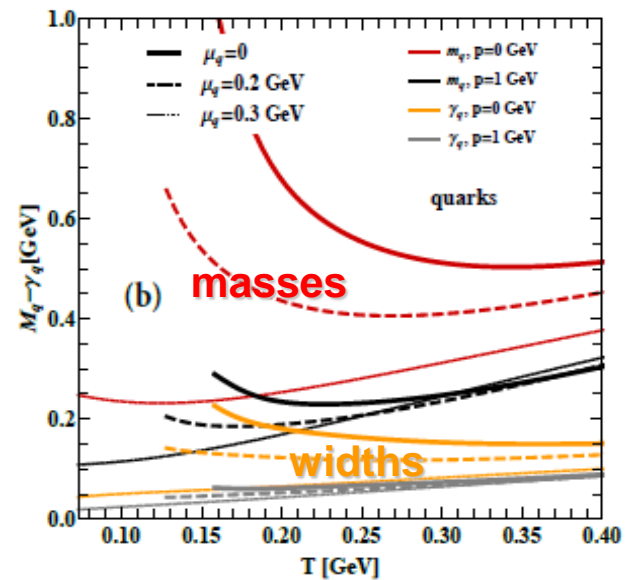
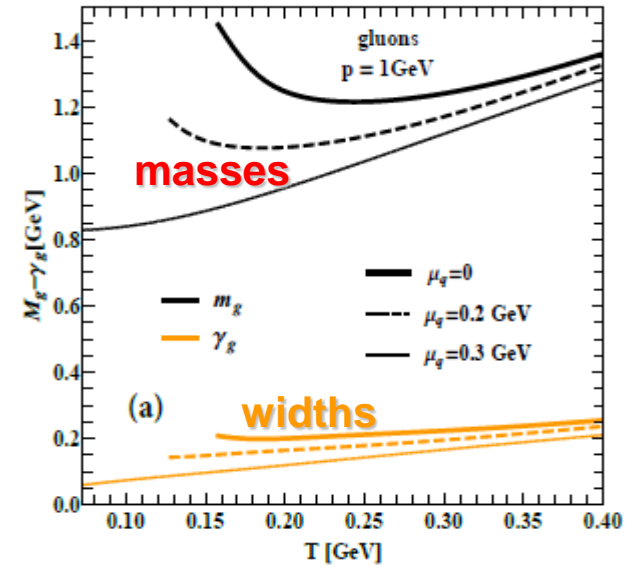
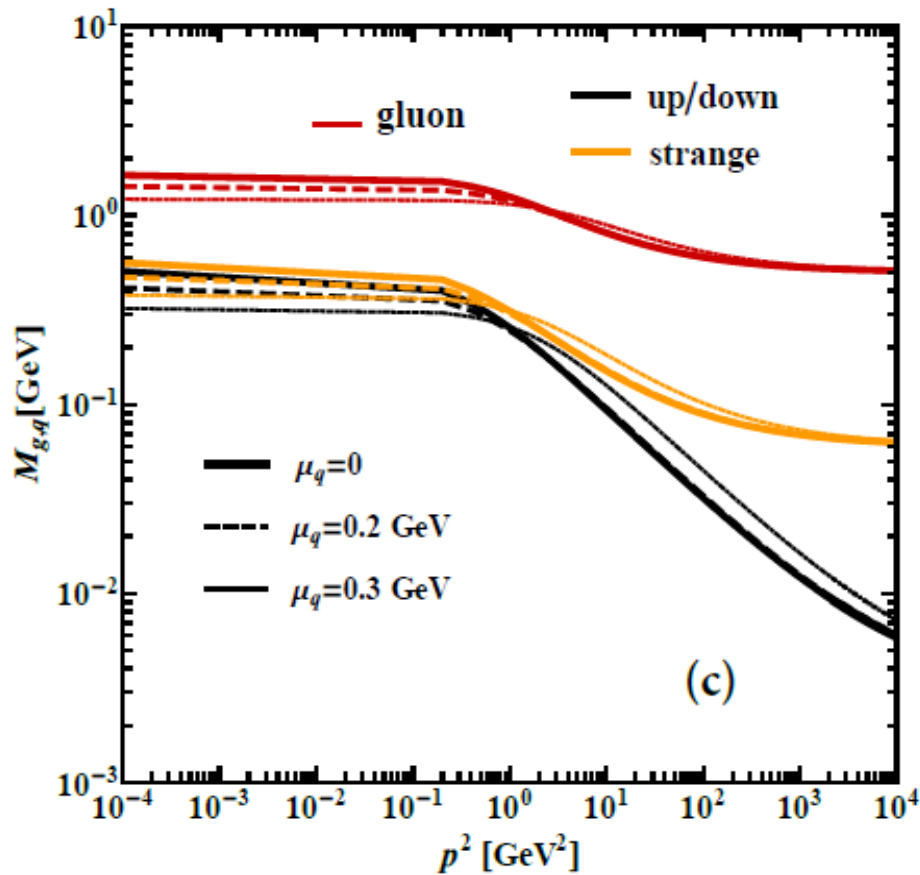
The final quark masses for the limits $p \rightarrow 0$ and $T = 0$ or for $p \rightarrow \infty$
 $m_{\chi_q} = 0.003 \text{ GeV}$ for u, d quarks and $m_{\chi_q} = 0.06 \text{ GeV}$ for s quarks

The gluon condensate: $m_{\chi_g} = 0.5 \text{ GeV}$

Effective temperature T^* for $N_f = N_c = 3$ (as in extended DQPM)

$$T^{*2} = T^2 + \frac{\mu_q^2}{\pi^2}$$

DQPM* at finite (T, μ_q, p) : quasiparticle masses and widths

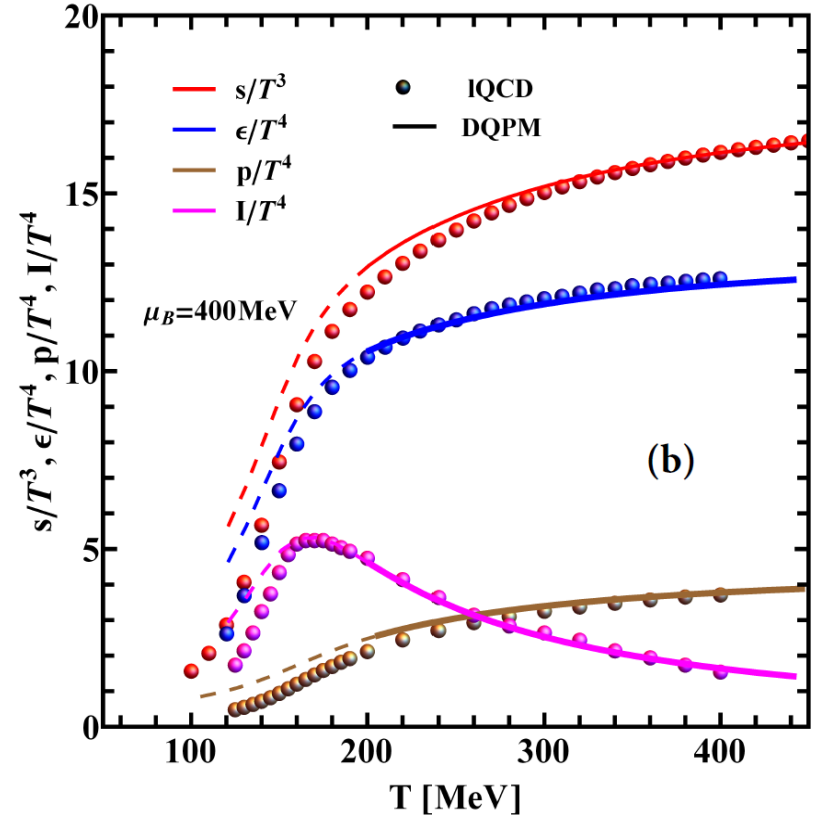
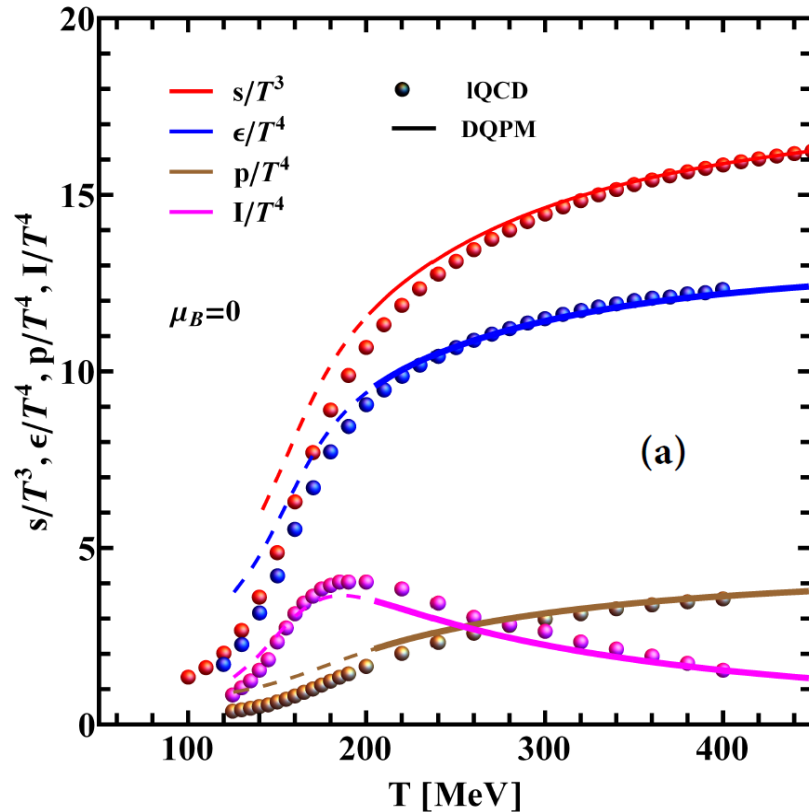


- With increasing p momenta: $M_{q,g}$ and $\gamma_{q,g}$ decrease at T, μ_q
- $\mu_q = 0 \rightarrow$ finite μ_q : decrease of $M_{q,g}$ and $\gamma_{q,g}$

QGP Thermodynamics from DQPM* (T, μ_q, ρ)

□ EoS from DQPM* at finite (T, μ_B)

Nf=3; IQCD, Sz. Borsanyi et al., JHEP08(2012)053



- High T ($T > 1.2 T_c(\mu)$): very **good agreement with the lattice data**
- Low T ($T < 1.2 T_c(\mu)$): some deviations \rightarrow additional hadronic d.o.f in the crossover region ?

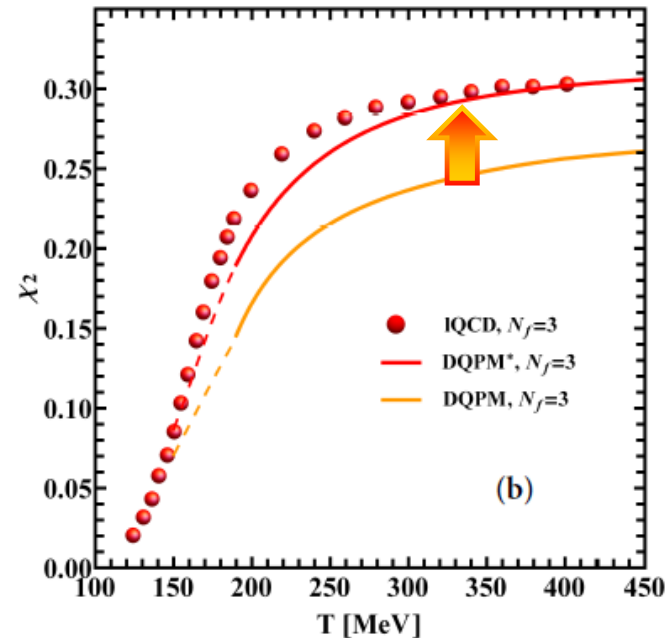
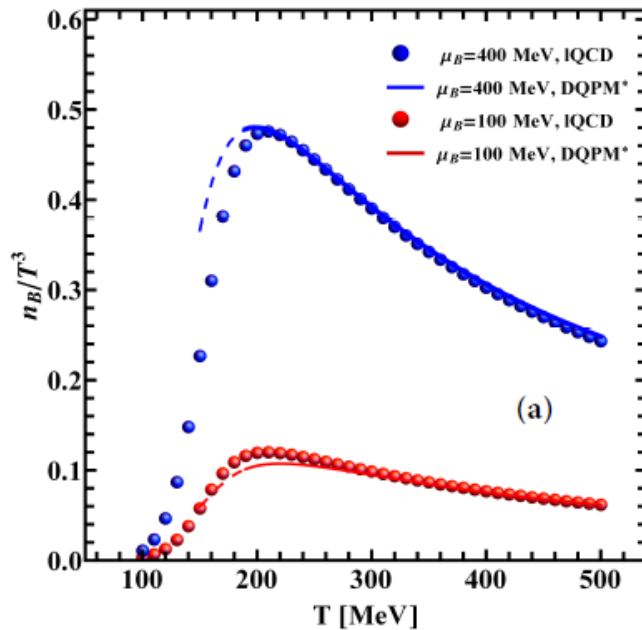
QGP Thermodynamics from DQPM* (T, μ_q, p)

□ n_B, χ_q at finite (T, μ_B)

$$\chi_q(T) = \left. \frac{\partial n_q}{\partial \mu_q} \right|_{\mu_q=0}; \quad \chi_q(T, \mu_q) = \frac{1}{9} \frac{\partial n_B}{\partial \mu_B}$$

$$\chi_2(T) = \frac{1}{9} \frac{1}{T^2} \left. \frac{\partial n_q(T, \mu_q)}{\partial \mu_q} \right|_{\mu_q=0} = \frac{1}{9} \frac{\chi_q(T)}{T^2}$$

for 3 flavours with $\mu_u = \mu_d = \mu_s = \mu_q$



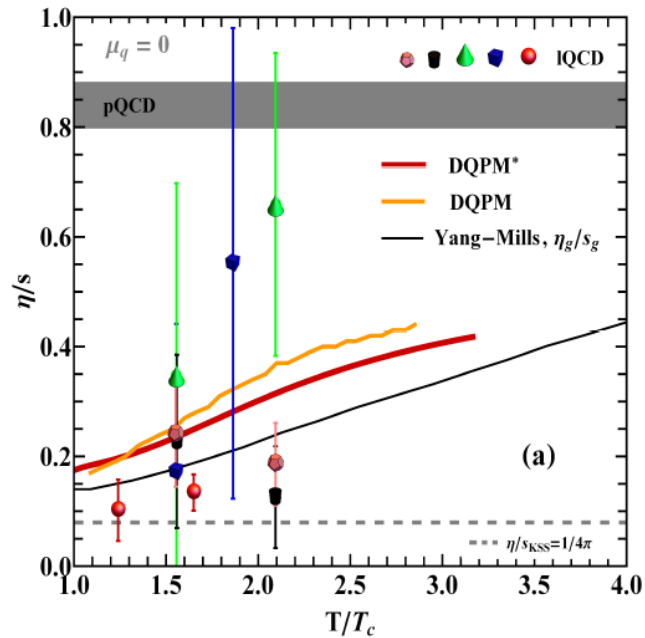
- DQPM* describes n_B , quark susceptibility and entropy/pressure...
- p dependence of masses allows DQPM* to meet IQCD

DQPM $^*(T, \mu_q, \rho)$:
transport properties at finite (T, μ_q)

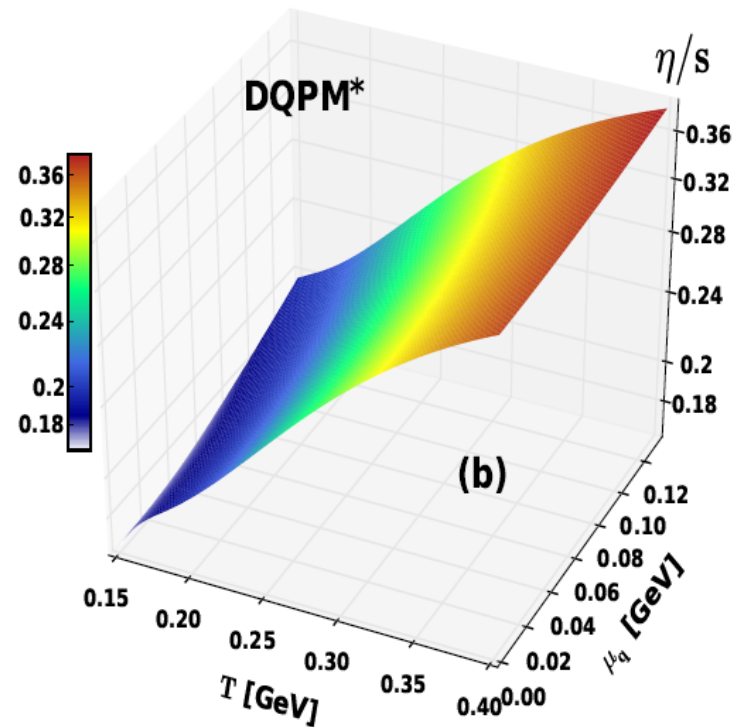
(based on relaxation time approximation - RTA)

I. DQPM*: transport properties at finite (T, μ_q) : η/s

Shear viscosity η/s at finite T



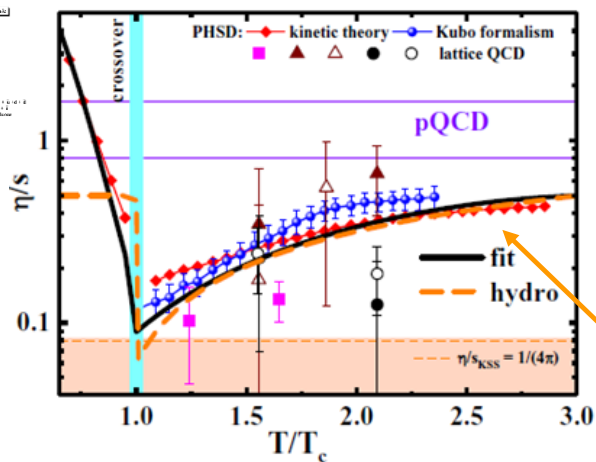
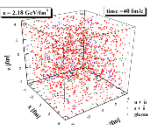
Shear viscosity η/s at finite (T, μ_q)



η/s : $\mu_q=0 \rightarrow$ finite μ_q :
smooth increase as a function of (T, μ_q)

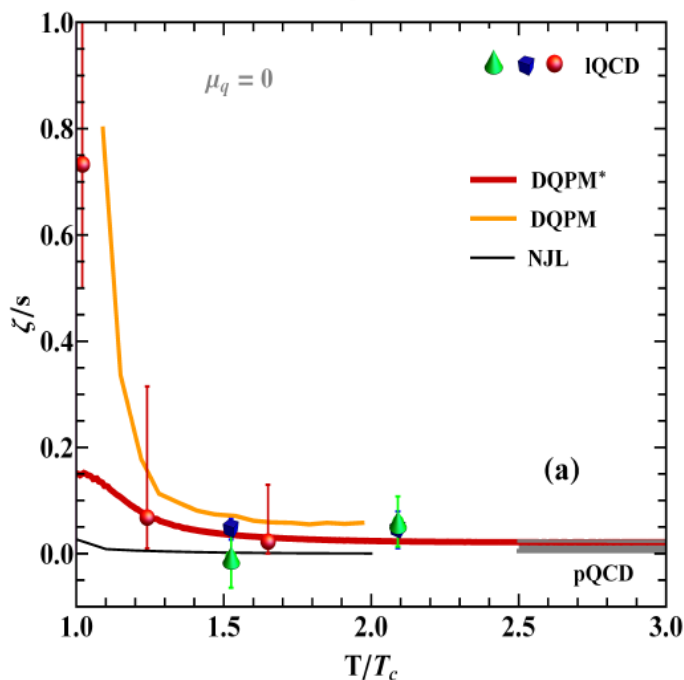
H. Berrehrah et al, PRC 93 (2016) 044914, arXiv:1512.06909;
Int.J.Mod.Phys. E25 (2016) 1642003, arXiv:1605.02371

PHSD in a box: V. Ozvenchuk et al., PRC 87 (2013) 064903

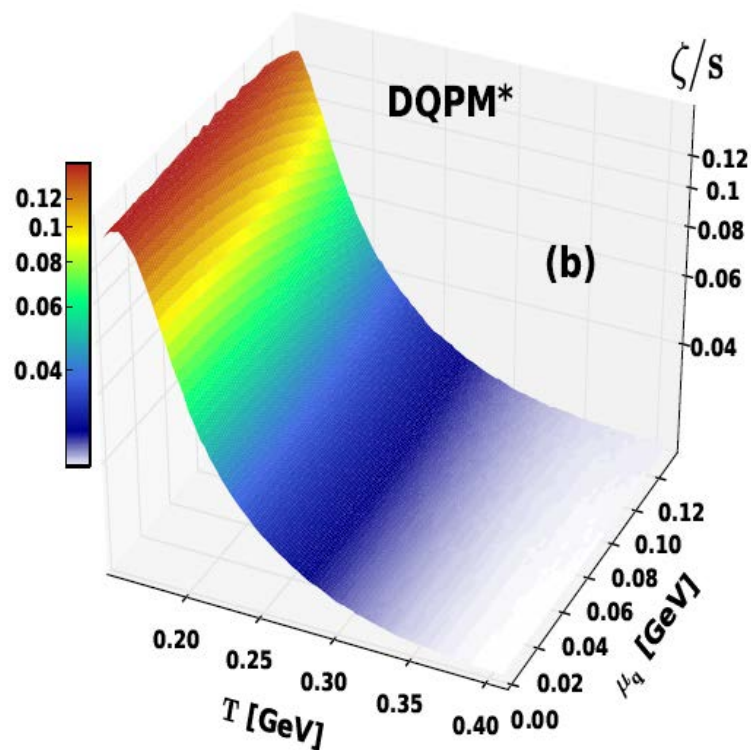


II. DQPM*: transport properties at finite (T, μ_q) : ζ/s

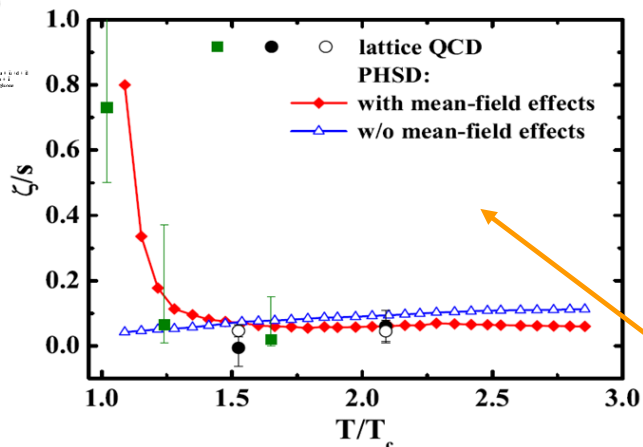
Bulk viscosity ζ/s at finite T



Bulk viscosity ζ/s at finite (T, μ_q)



ζ/s : $\mu_q=0 \rightarrow$ finite μ_q :
smooth variation as a function of (T, μ_q)

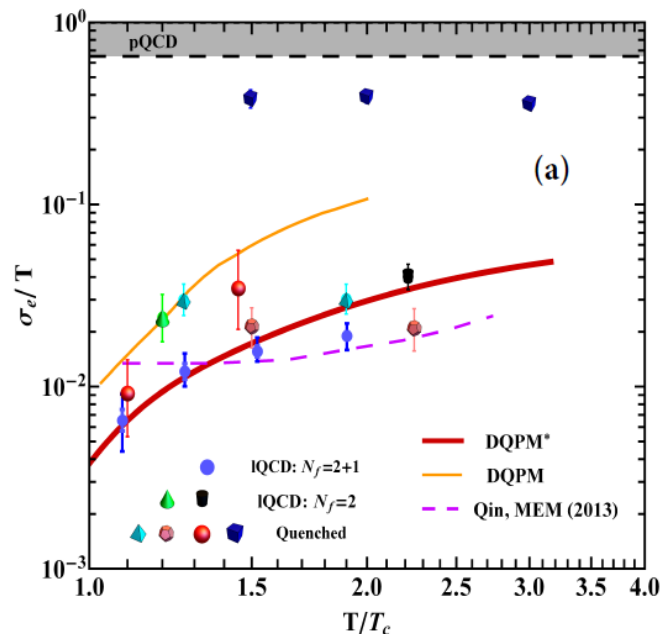


H. Berrehrah et al, PRC 93 (2016) 044914, arXiv:1512.06909;
Int.J.Mod.Phys. E25 (2016) 1642003, arXiv:1605.02371

PHSD in a box: V. Ozvenchuk et al., PRC 87 (2013) 064903

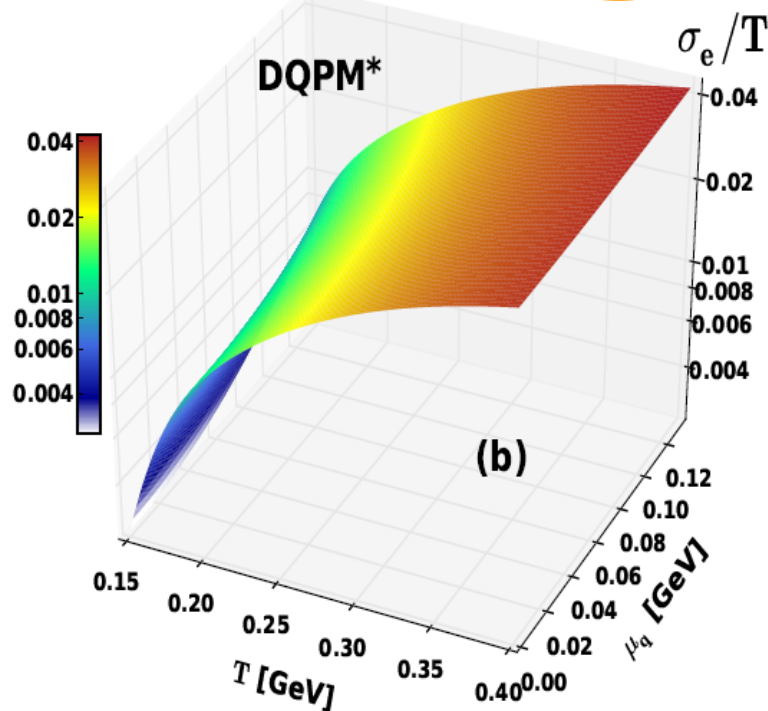
III. DQPM*: transport properties at finite (T, μ_q) : σ_e/T

Electric conductivity σ_e/T at finite T



Electric conductivity σ_e/T at finite (T, μ_q)

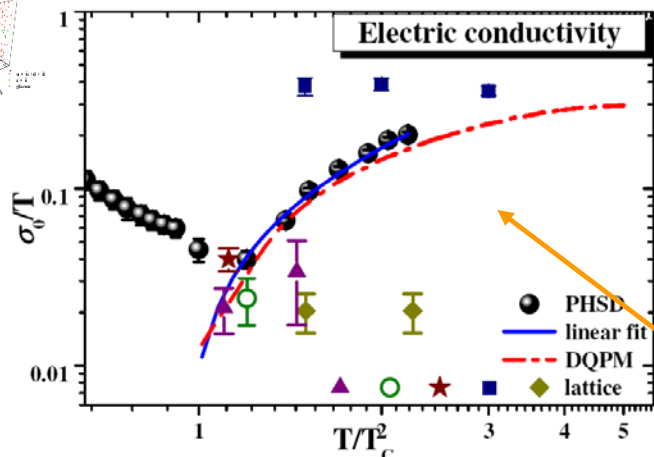
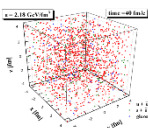
$$\sigma_e(T, \mu_q) = \sum_{f, \bar{f}}^{u, d, s} \frac{e_f^2 n_f^{\text{off}}(T, \mu_q)}{\bar{\omega}_f(T, \mu_q) \bar{\gamma}_f(T, \mu_q)}$$



σ_e/T : $\mu_q=0 \rightarrow$ finite μ_q :
smooth variation as a function of (T, μ_q)

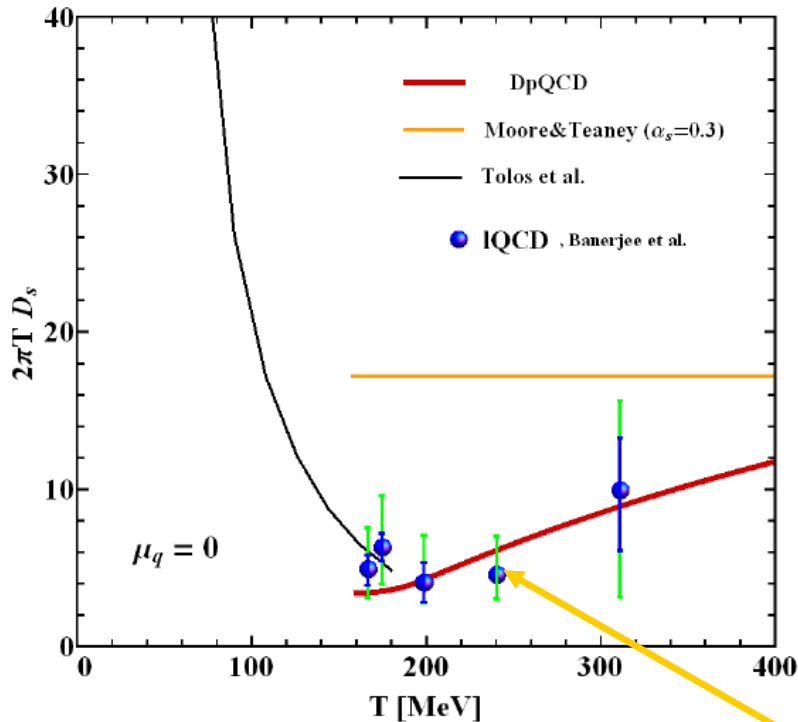
H. Berrehrah et al, PRC 93 (2016) 044914, arXiv:1512.06909;
Int.J.Mod.Phys. E25 (2016) 1642003, arXiv:1605.02371

PHSD in a box: V. Ozvenchuk et al., PRC 87 (2013) 064903

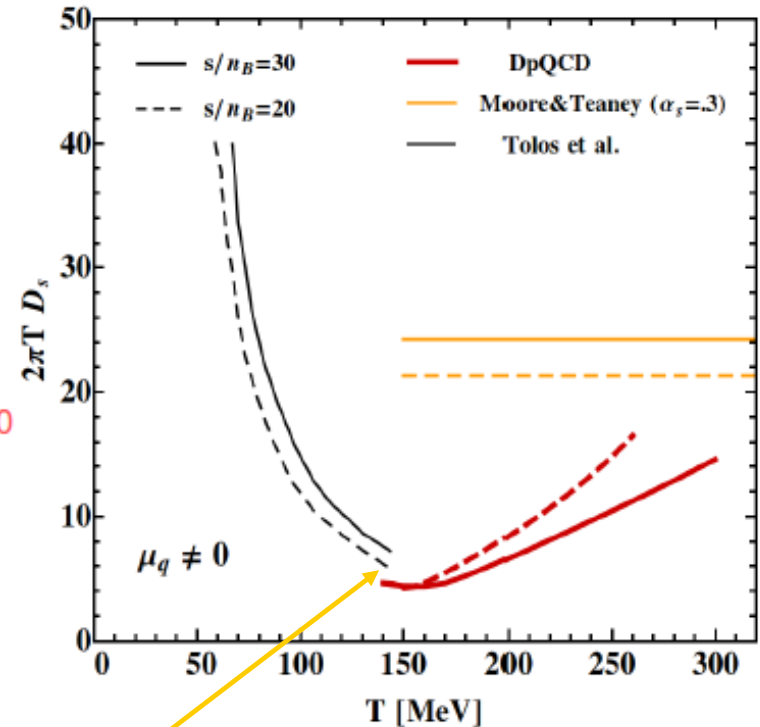


Charm spatial diffusion coefficient D_s in the hot medium

- D_s for heavy quarks as a function of T for $\mu_q=0$ and finite μ_q



\Rightarrow
 $\mu_q \neq 0$



□ $T < T_c$: hadronic D_s

L. Tolos, J. M. Torres-Rincon,
 Phys. Rev. D 88, 074019 (2013)

\rightarrow Continuous transition at T_c !

Summary: DQPM, DQPM* at finite (T, μ_q)

□ Extension of the **DQPM** to finite μ_q using **scaling hypothesis** for the effective temperature T^*

□ $\mu_q=0 \rightarrow$ finite μ_q :

▪ variations in the QGP transport coefficients

▪ **smooth dependence** on (T, μ_q)

▪ $\eta/s, \zeta/s, \sigma_e/T, D_s$ show **minima** around T_C at $\mu_q=0$ and finite μ_q

□ **additional p dependence of masses allows DQPM* to meet IQCD:**
DQPM* describes n_B , quark **susceptibility** and entropy/pressure...

□ **Outlook**

Implementation into PHSD: from $T, \mu_q=0 \rightarrow$ finite T, μ_q



Thank you!

