

$$\chi = \frac{1}{2} \ln \left(\frac{1+v}{1-v} \right)$$