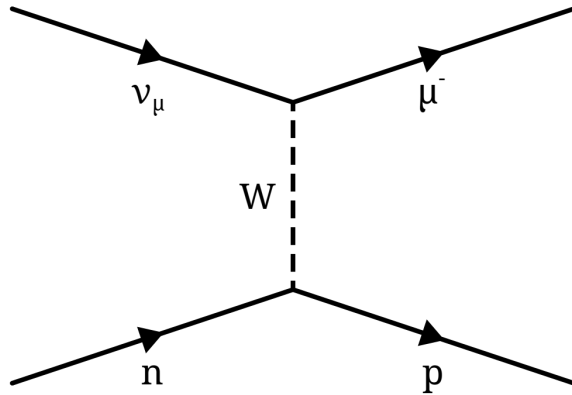
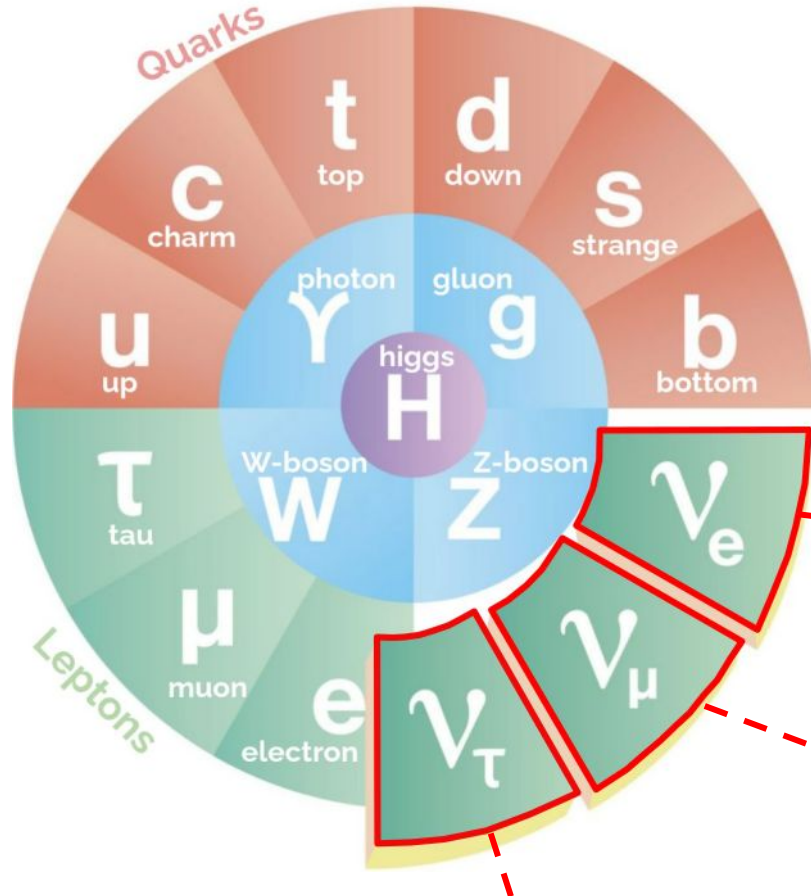


# Neutrino angle reconstruction in MicroBooNE for precision atmospheric neutrino oscillations



# Neutrinos 101



- Mysterious particles
- No charge
- Almost massless
- Incredibly hard to observe!



# Neutrino states

Flavor states



What we interact with and can  
produce/detect

# Neutrino states

Flavor states



What we interact with and can  
produce/detect

Mass states



What propagates through space  
and has defined mass

# Neutrino states

Flavor states



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

=

$\begin{pmatrix} \text{mixing} \\ \text{matrix} \end{pmatrix}$

Mass states

$$\begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



# Neutrino states

Flavor states

Mass states



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

=

(mixing  
matrix)

$$\begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$\theta$  = mixing angle

$$c_{ij} = \cos\theta_{ij}$$

$$s_{ij} = \sin\theta_{ij}$$

# Experimental overview

L: distance (baseline)

$E_\nu$ : neutrino energy

Two-neutrino approximation

$$P(\nu_\mu \rightarrow \nu_e) \approx \sin^2(\overset{\text{mixing angle}}{\uparrow} 2\theta) \sin^2\left(\overset{\text{mass difference}}{\uparrow} \frac{\Delta m^2 L}{4E_\nu}\right)$$

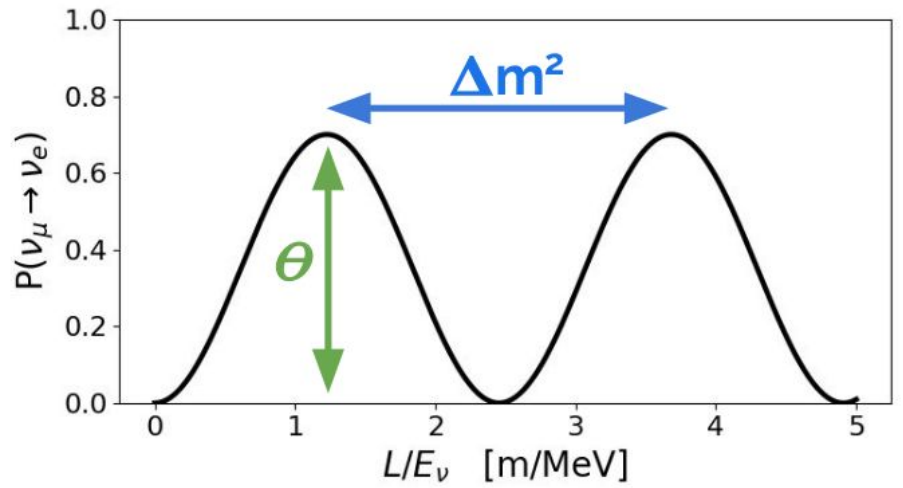
# Experimental overview

$$P(\nu_\mu \rightarrow \nu_e) \approx \underbrace{\sin^2(2\theta)}_{\text{amplitude}} \underbrace{\sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)}_{\text{frequency}}$$

mixing angle mass difference

frequency

Neutrino “oscillation”



# Experimental overview

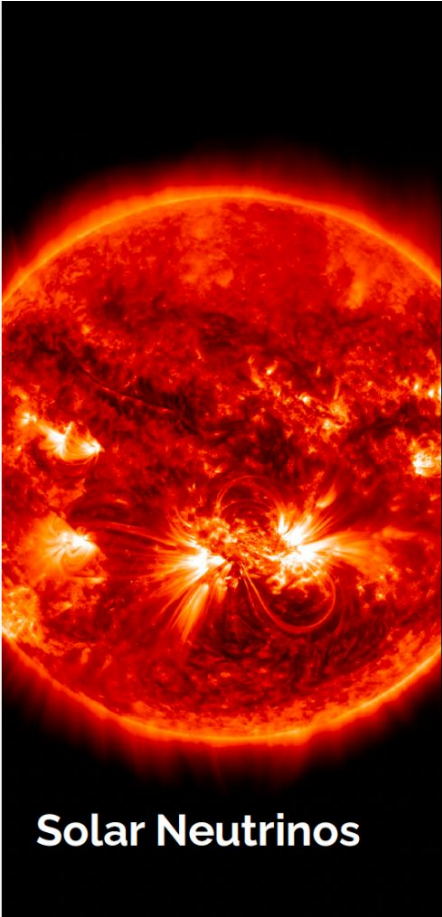
$$P(\nu_\mu \rightarrow \nu_e) \approx \underbrace{\sin^2(2\theta)}_{\text{amplitude}} \underbrace{\sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)}_{\text{frequency}}$$

mixing angle mass difference

frequency

Optimizing baseline L for a given neutrino source of energy  $E_\nu$   
Mass difference  $\Delta m^2$  and mixing angles  $\theta$  known to few %-level

# Leverage neutrino sources across wide energy spectrum



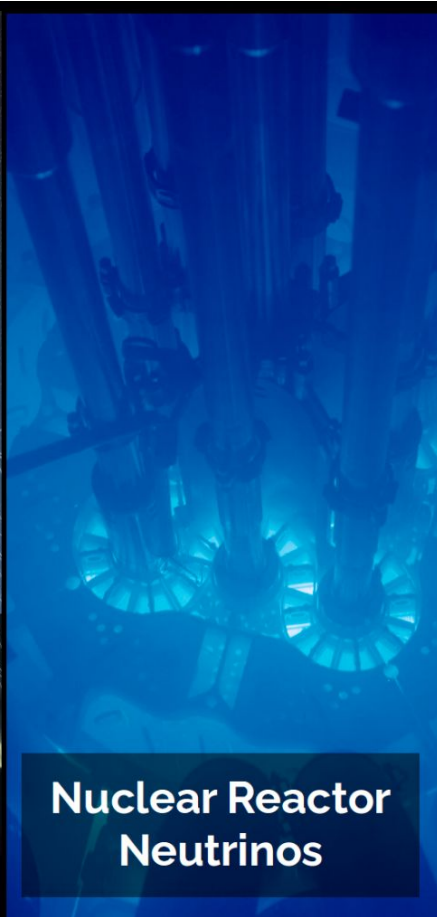
**Solar Neutrinos**

~MeV



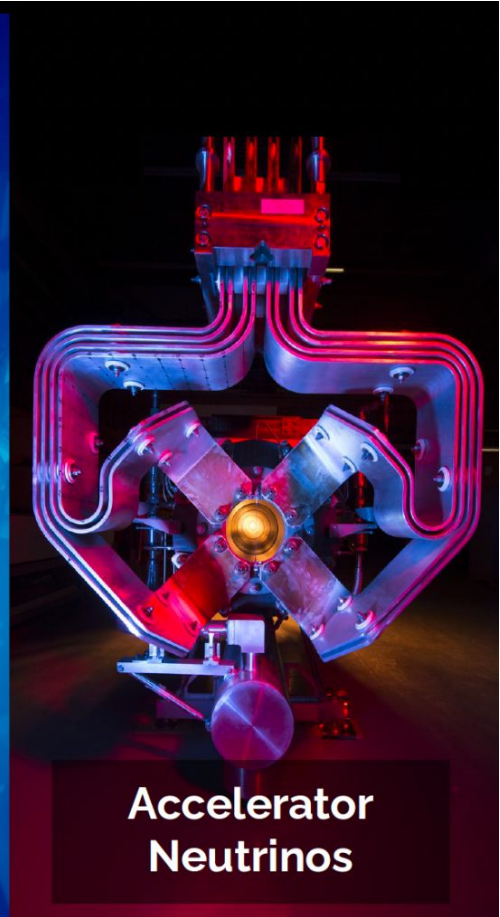
**Atmospheric  
Neutrinos**

~GeV



**Nuclear Reactor  
Neutrinos**

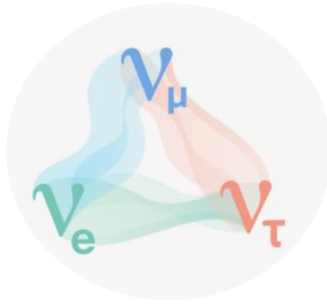
~MeV



**Accelerator  
Neutrinos**

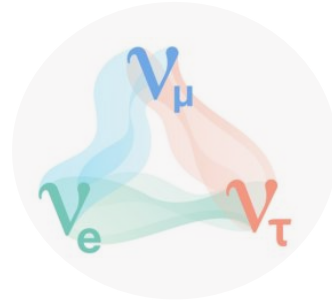
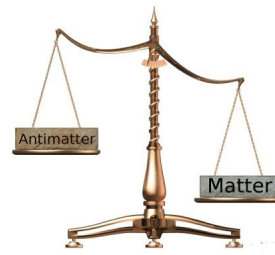
~GeV

# Open questions



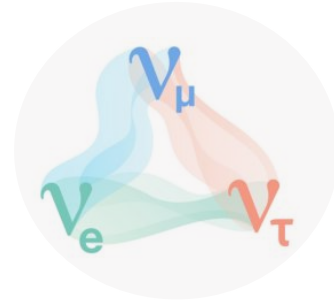
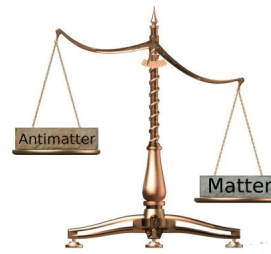
# Open questions

Charge  
parity  
violation

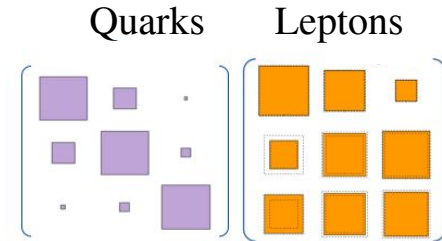


# Open questions

Charge  
parity  
violation

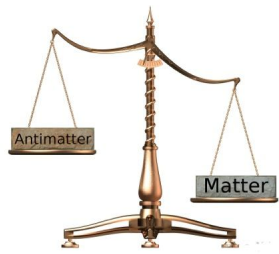


Mixing  
matrix

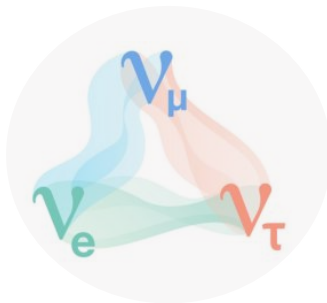
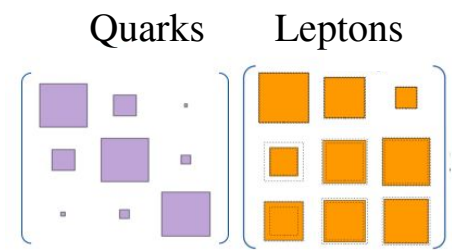


# Open questions

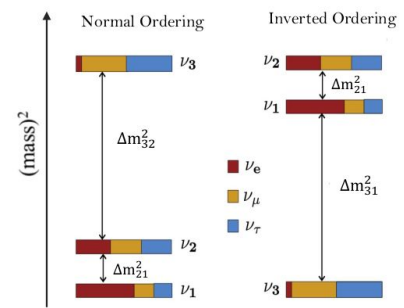
Charge  
parity  
violation



Mixing  
matrix

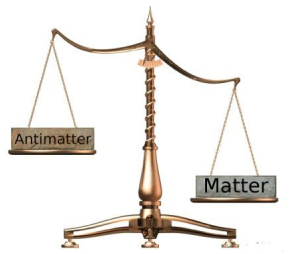


Mass  
ordering

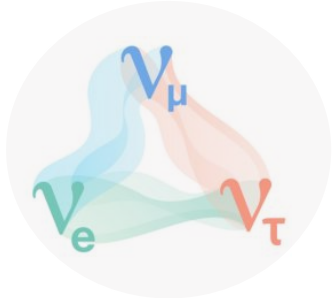


# Open questions

Charge  
parity  
violation



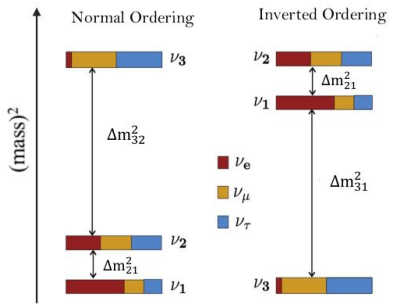
Mixing  
matrix



Mass  
mechanism

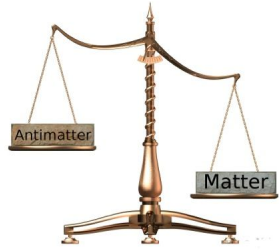


Mass  
ordering

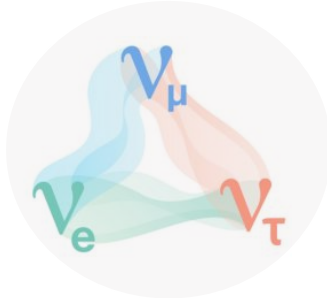
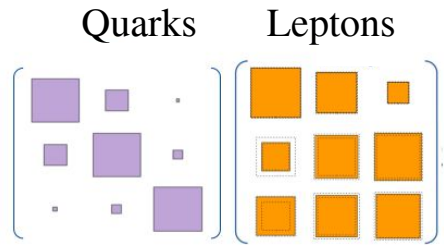


# Open questions

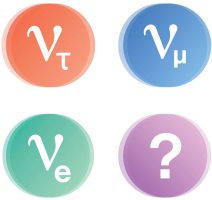
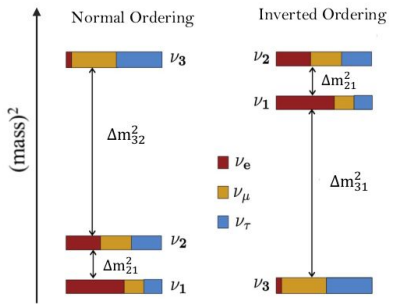
Charge parity violation



Mixing matrix



Mass ordering



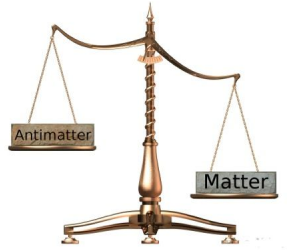
Sterile neutrinos



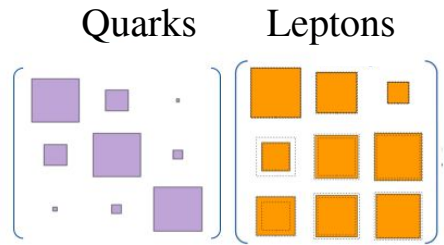
Mass mechanism

# Open questions

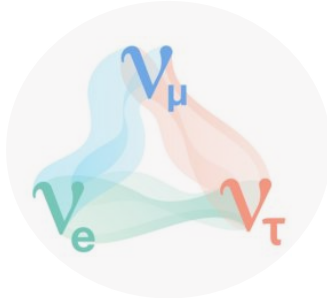
Charge parity violation



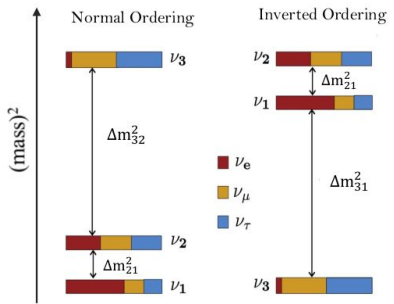
Mixing matrix



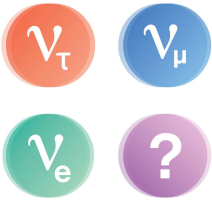
Majorana vs Dirac



Mass ordering



Sterile neutrinos



Mass mechanism



# Open questions

Charge  
parity  
violation

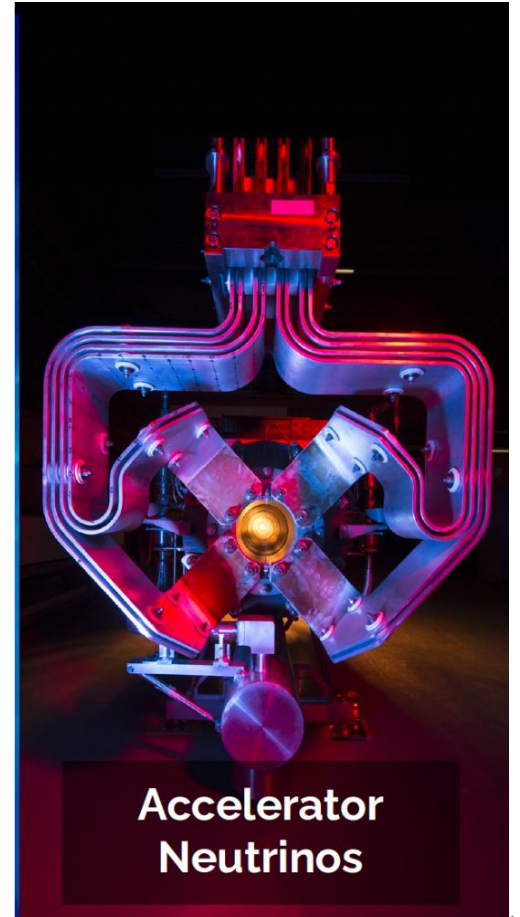
Mixing  
matrix

Investigated with high-precision  
neutrino oscillation experiments

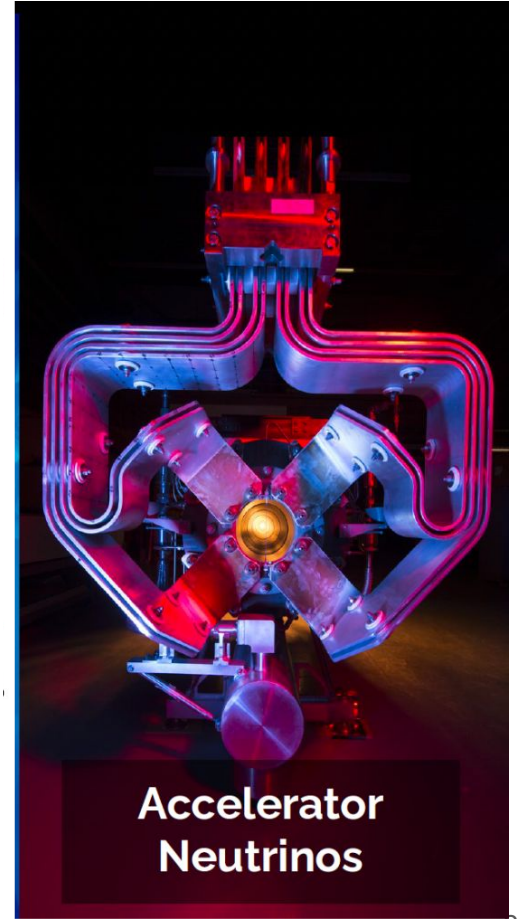
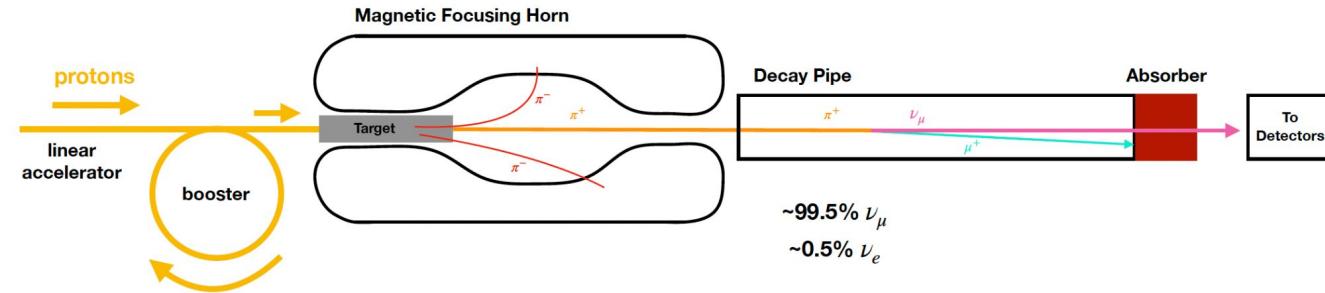
Sterile  
neutrinos

Mass  
ordering

Commonly used



# Commonly used

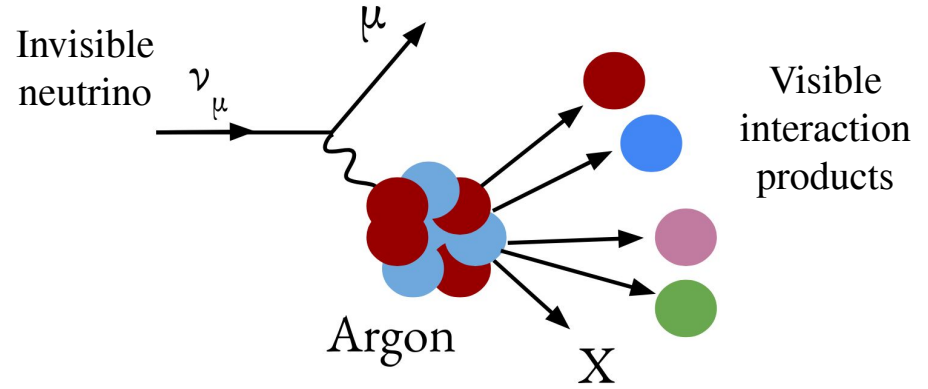


# Neutrino oscillation experiments



$E_{\text{rec}}$  = Reconstructed  $\nu$  energy

# Near detector



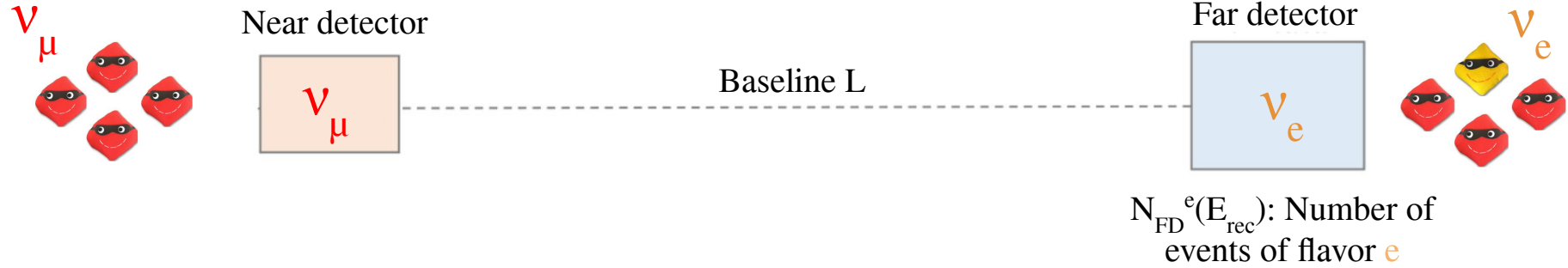
Neutrino flux  
prediction

Near detector selection  
efficiency

$$N_{ND}^\mu(E_{rec}) \sim \Phi_{ND}(E_\nu) \sigma(E_\nu) \epsilon_{ND}(E_\nu)$$

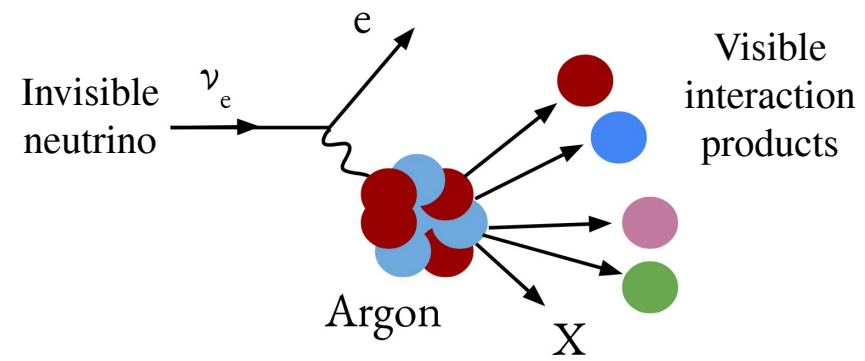
Neutrino cross  
section model

# Neutrino oscillation experiments



$E_{\text{rec}}$  = Reconstructed  $\nu$  energy

# Far detector



Neutrino flux prediction

Far detector selection efficiency

$$N_{FD}^e(E_{rec}) \sim \Phi_{FD}(L, E_\nu) \sigma(E_\nu) \epsilon_{FD}(E_\nu) P(\nu_\mu \rightarrow \nu_e)$$

Neutrino cross section model

# Far detector

$$N_{FD}^e(E_{rec}) \sim \Phi_{FD}(L, E_\nu) \sigma(E_\nu) \epsilon_{FD}(E_\nu) \boxed{P(\nu_\mu \rightarrow \nu_e)}$$

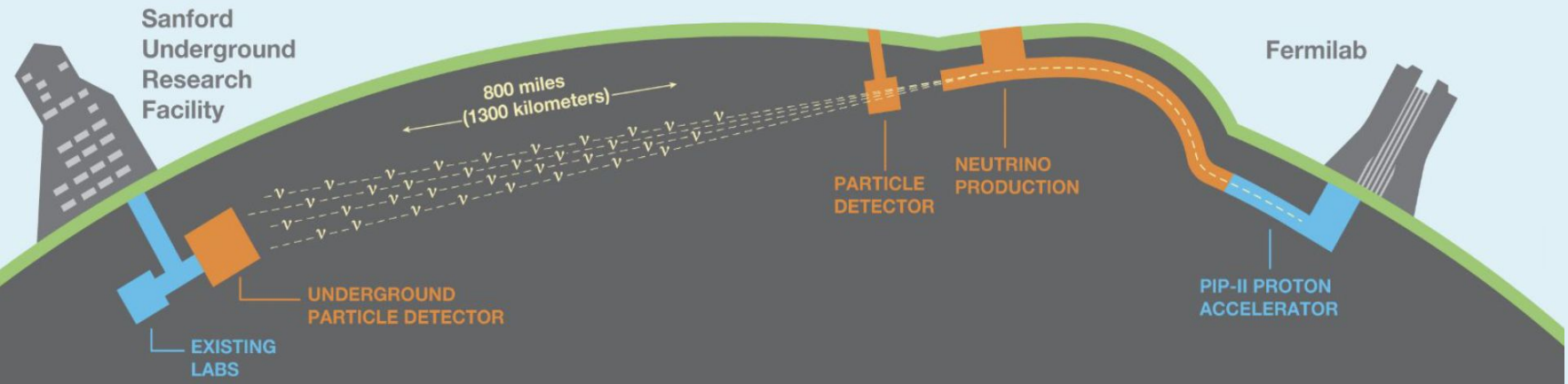
Oscillation probability

$$P(\nu_\mu \rightarrow \nu_e) \approx \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E_\nu}\right)$$

mixing angle

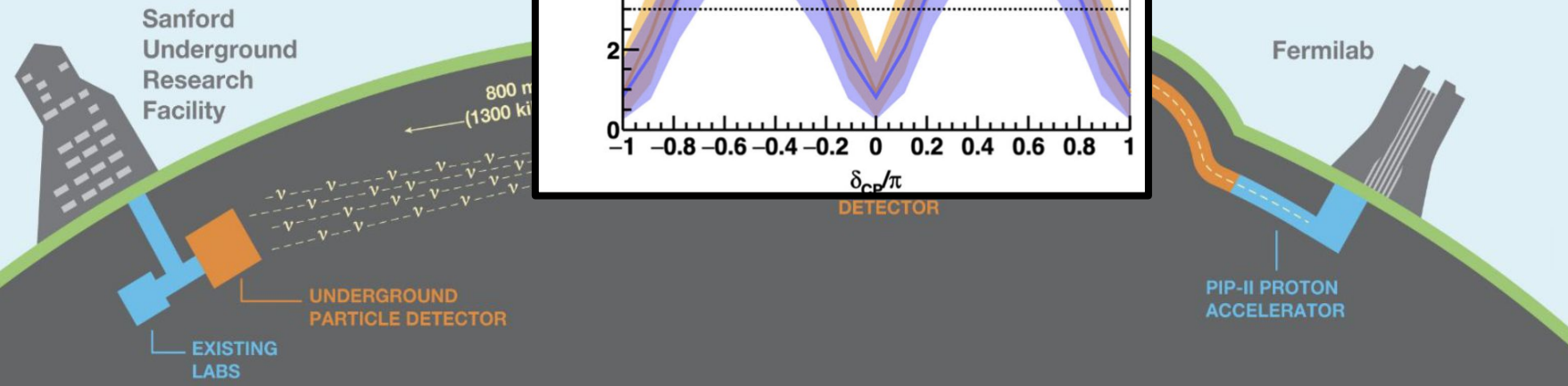
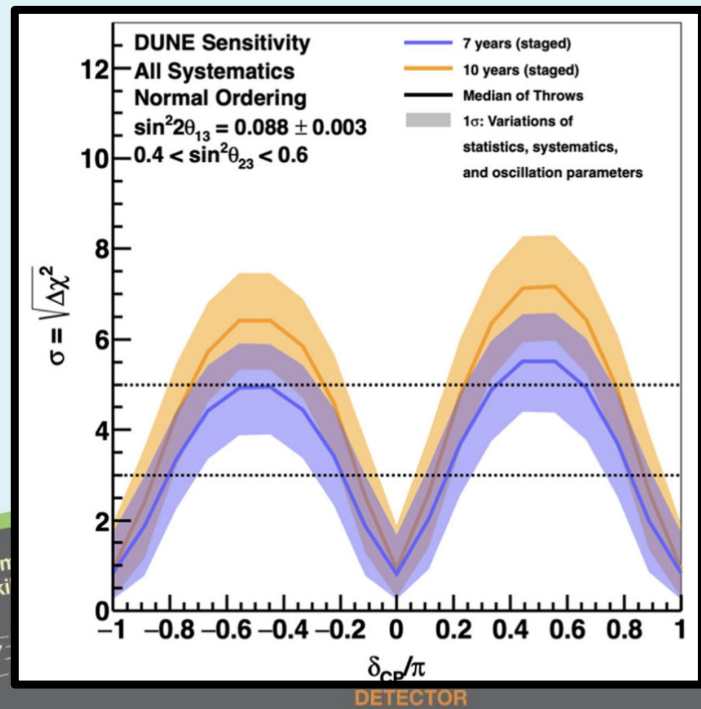
mass difference

Forthcoming neutrino oscillation experiments aim to perform **high-precision measurements** in the neutrino sector

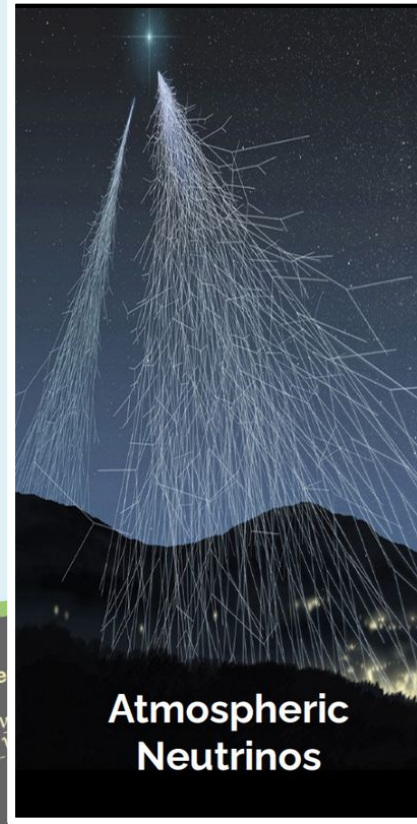


# Flagship analysis!

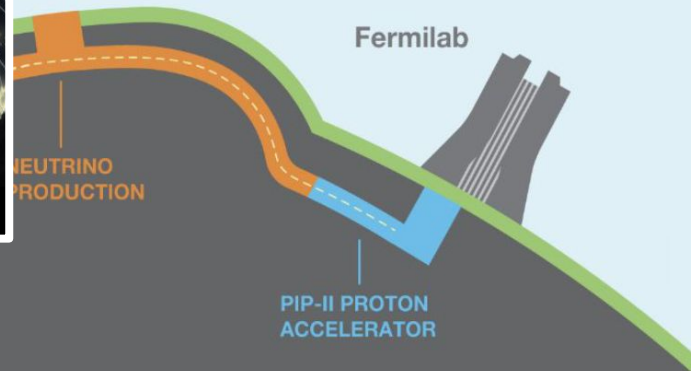
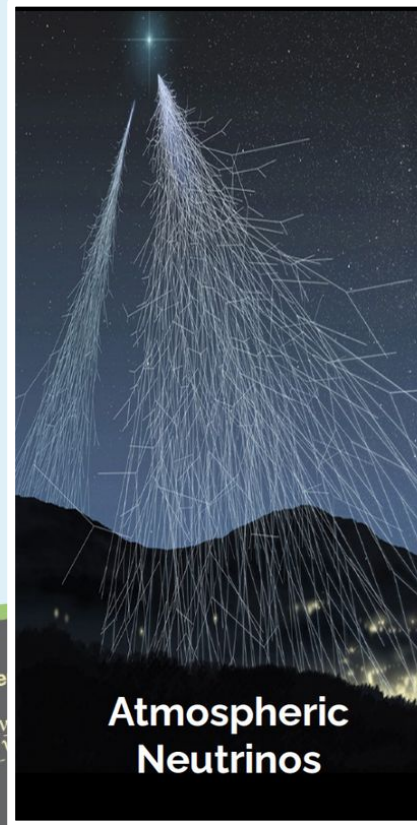
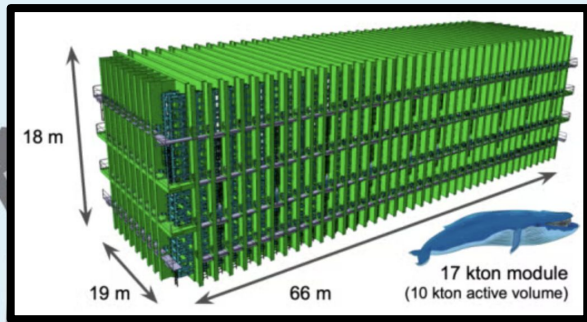
Charge-parity (CP) phase extraction might shed light on matter-antimatter asymmetry in universe



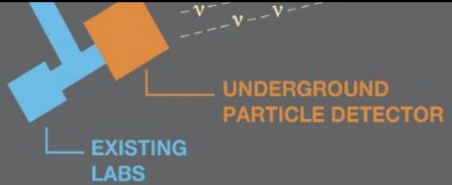
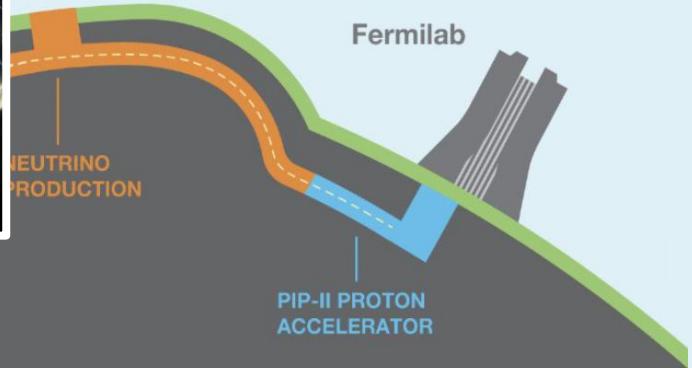
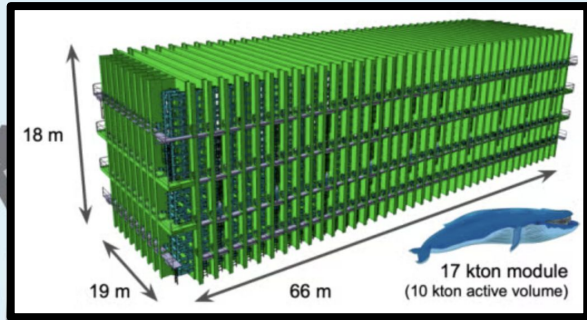
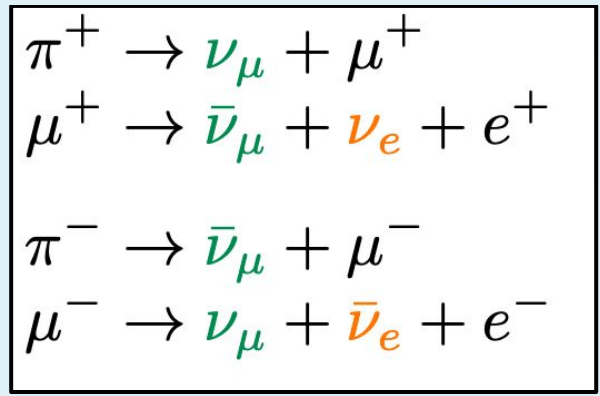
However ... **first analyses** will use atmospheric neutrino oscillations



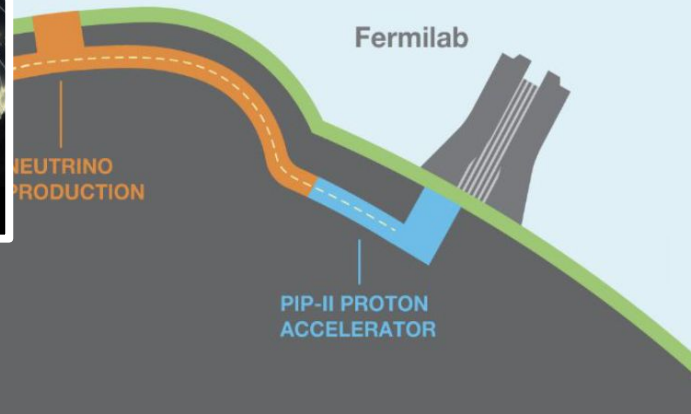
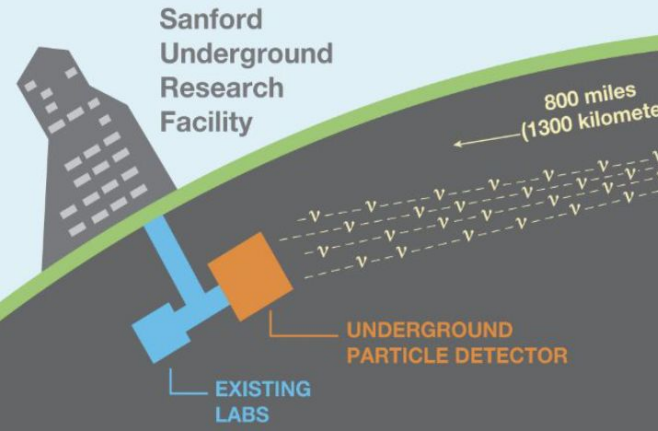
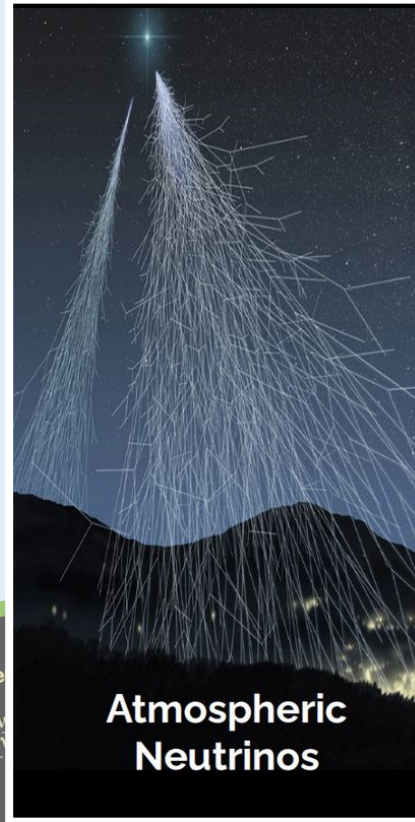
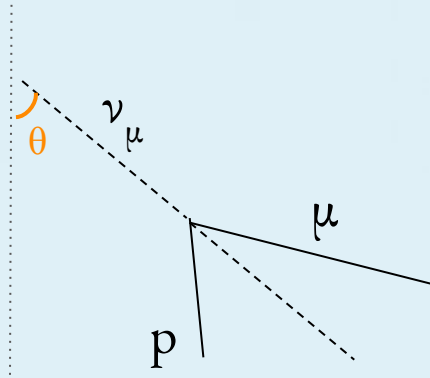
However ... **first analyses** will use atmospheric neutrino oscillations



However ... **first analyses** will use atmospheric neutrino oscillations

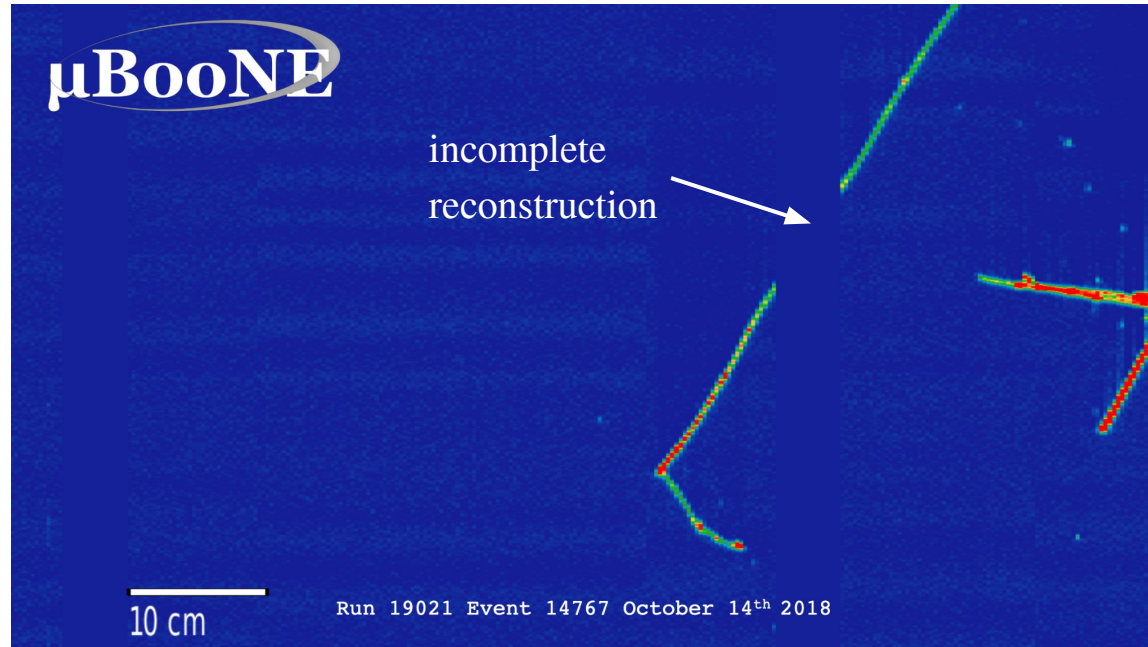


Neutrino direction ( $\theta$ ) needs to be reconstructed with high precision from interaction products



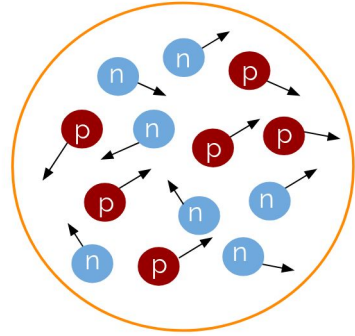
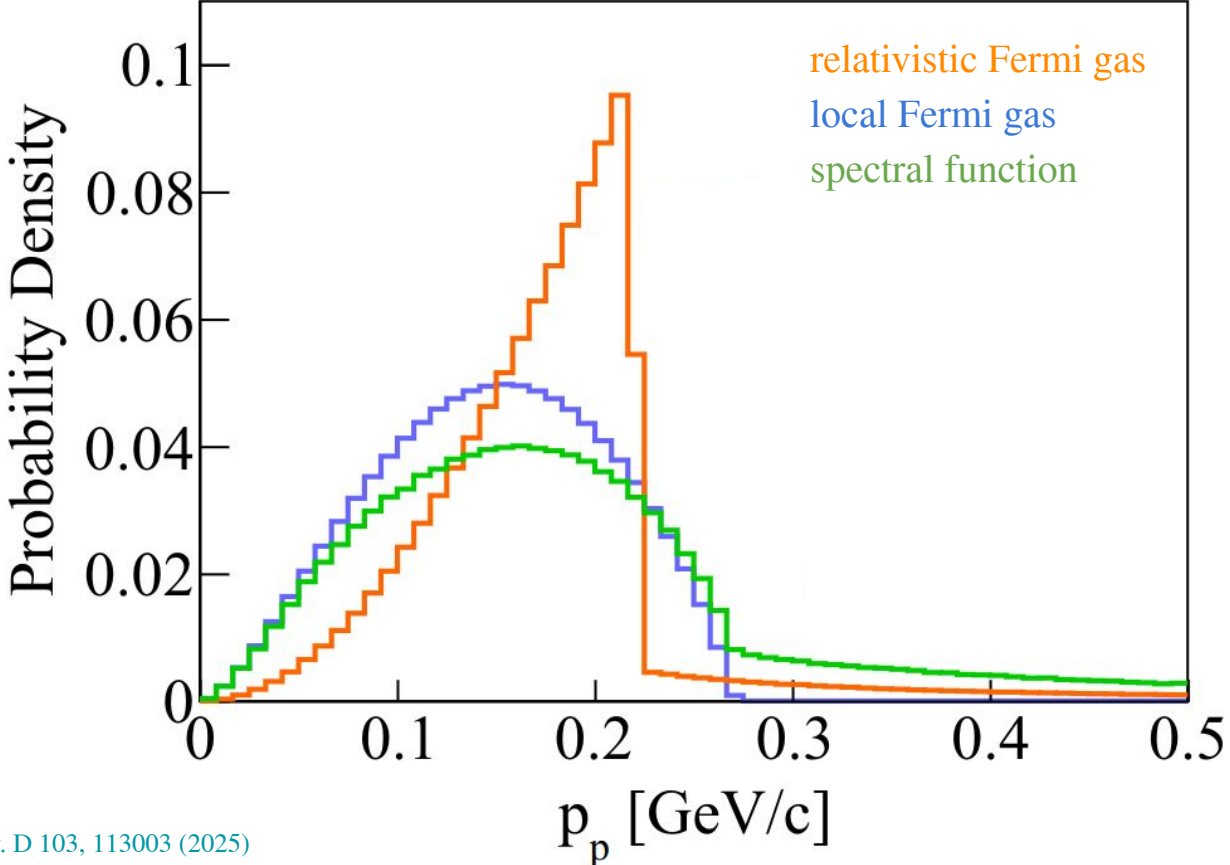
# Reconstruction limitations

Incomplete reconstruction or non-responsive detector regions



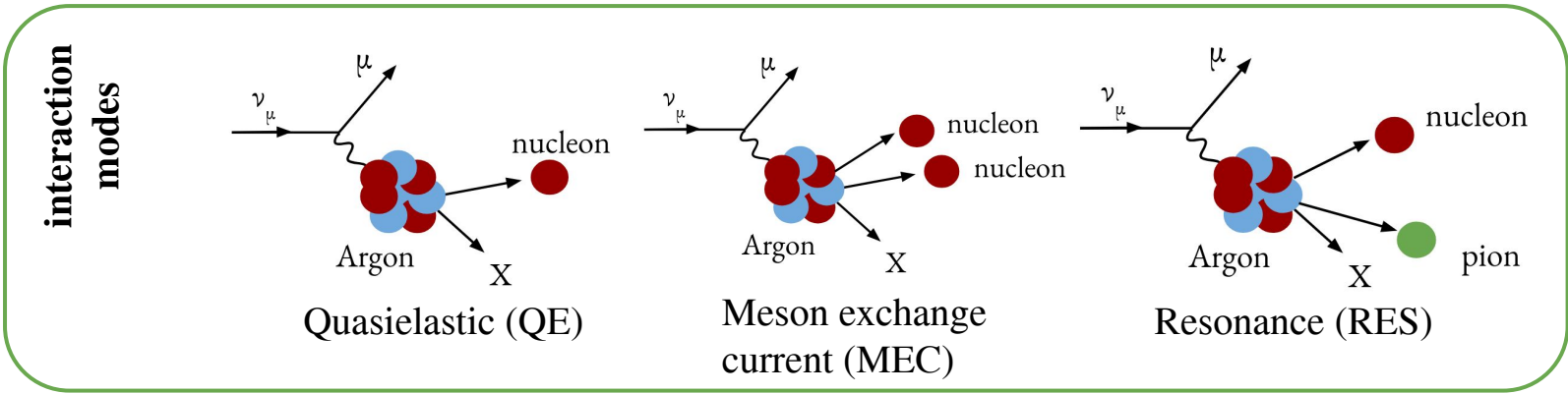
# Modeling limitations

Struck nucleon momentum



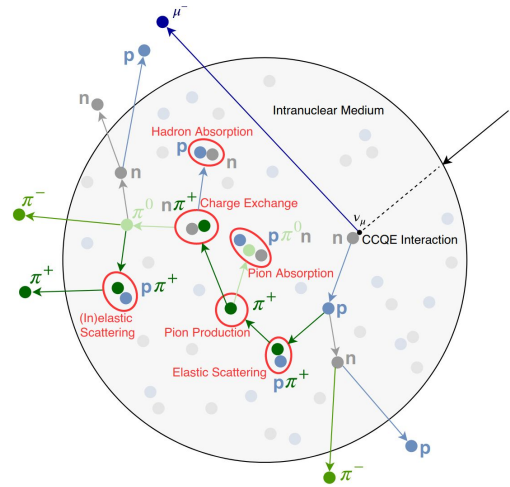
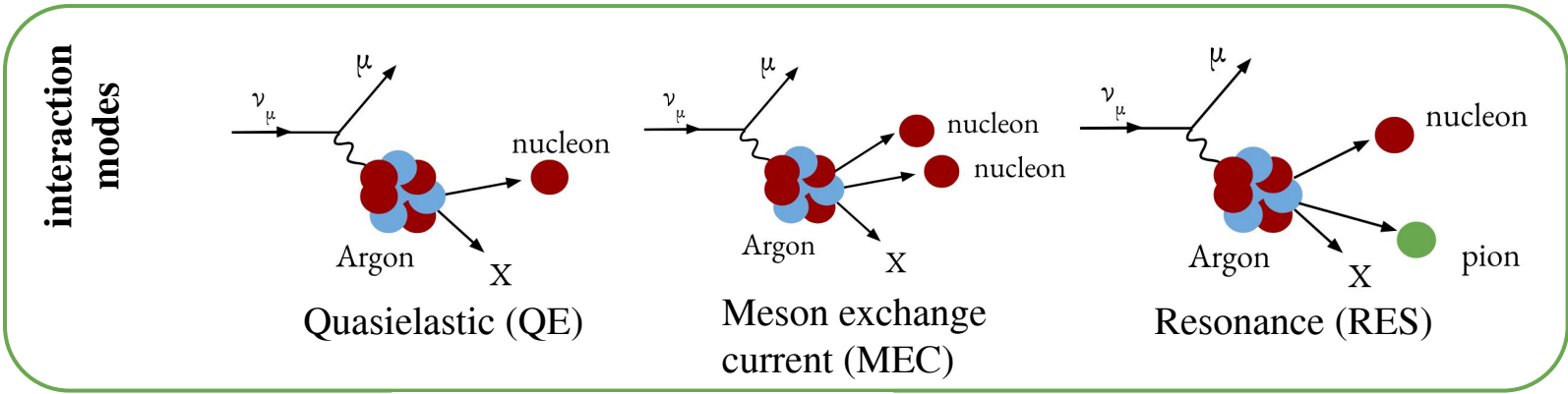
# Modeling limitations

## Hadron reinteractions



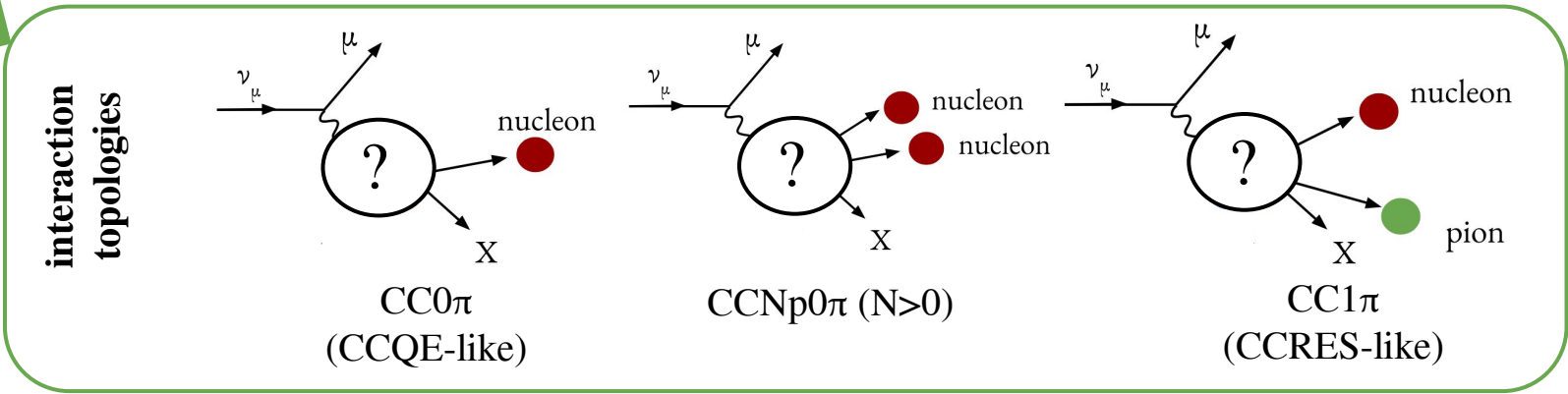
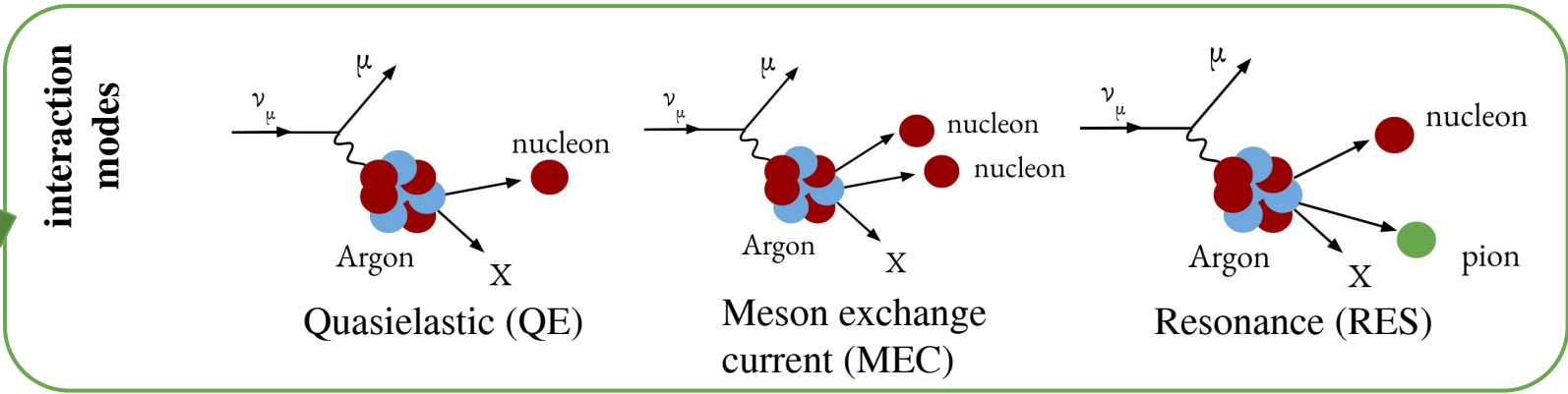
# Modeling limitations

## Hadron reinteractions



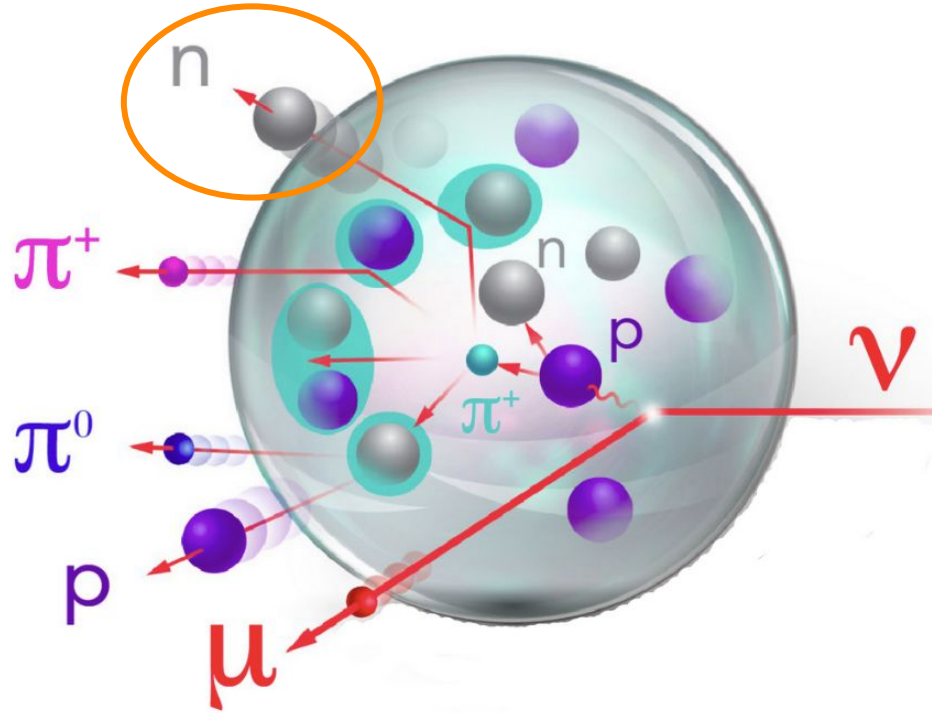
# Modeling limitations

## Hadron reinteractions



# Modeling limitations

Undetectable particles eg neutrons



Cannot easily study these effects if our neutrinos are coming from every possible direction ....



Let's be smart



# Let's be smart

- Use another detector where the neutrino origin is known



# Let's be smart

- Use another detector where the neutrino origin is known
- Treat neutrinos as “atmospheric neutrinos” of unknown origin



# Let's be smart

- Use another detector where the neutrino origin is known
- Treat neutrinos as “atmospheric neutrinos” of unknown origin
- Reconstruct the neutrino angle using the observed particles



# Let's be smart

- Use another detector where the neutrino origin is known
- Treat neutrinos as “atmospheric neutrinos” of unknown origin
- Reconstruct the neutrino angle using the observed particles
- Quantify neutrino angular reconstruction precision



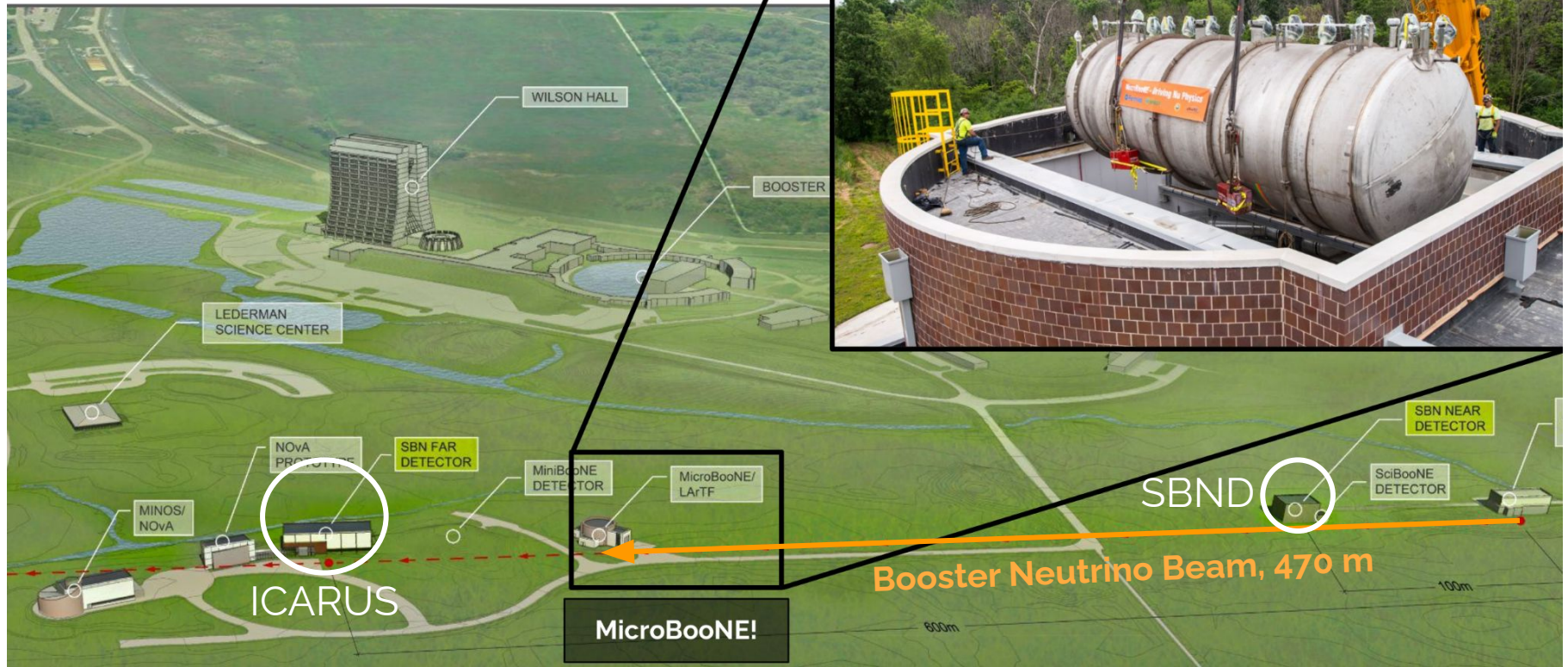
# Let's be smart

- Use another detector where the neutrino origin is known
- Treat neutrinos as “atmospheric neutrinos” of unknown origin
- Reconstruct the neutrino angle using the observed particles
- Quantify neutrino angular reconstruction precision

And that brings us to **μBooNE** !

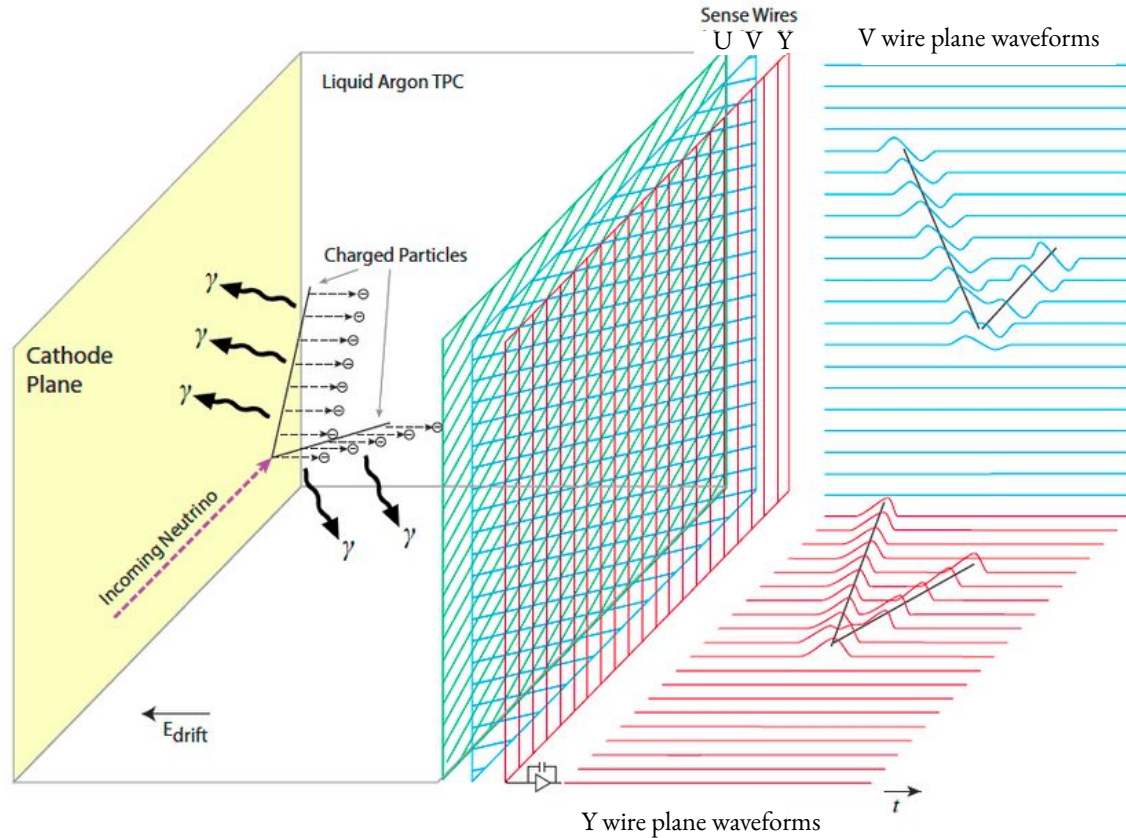


# MicroBooNE@FNAL



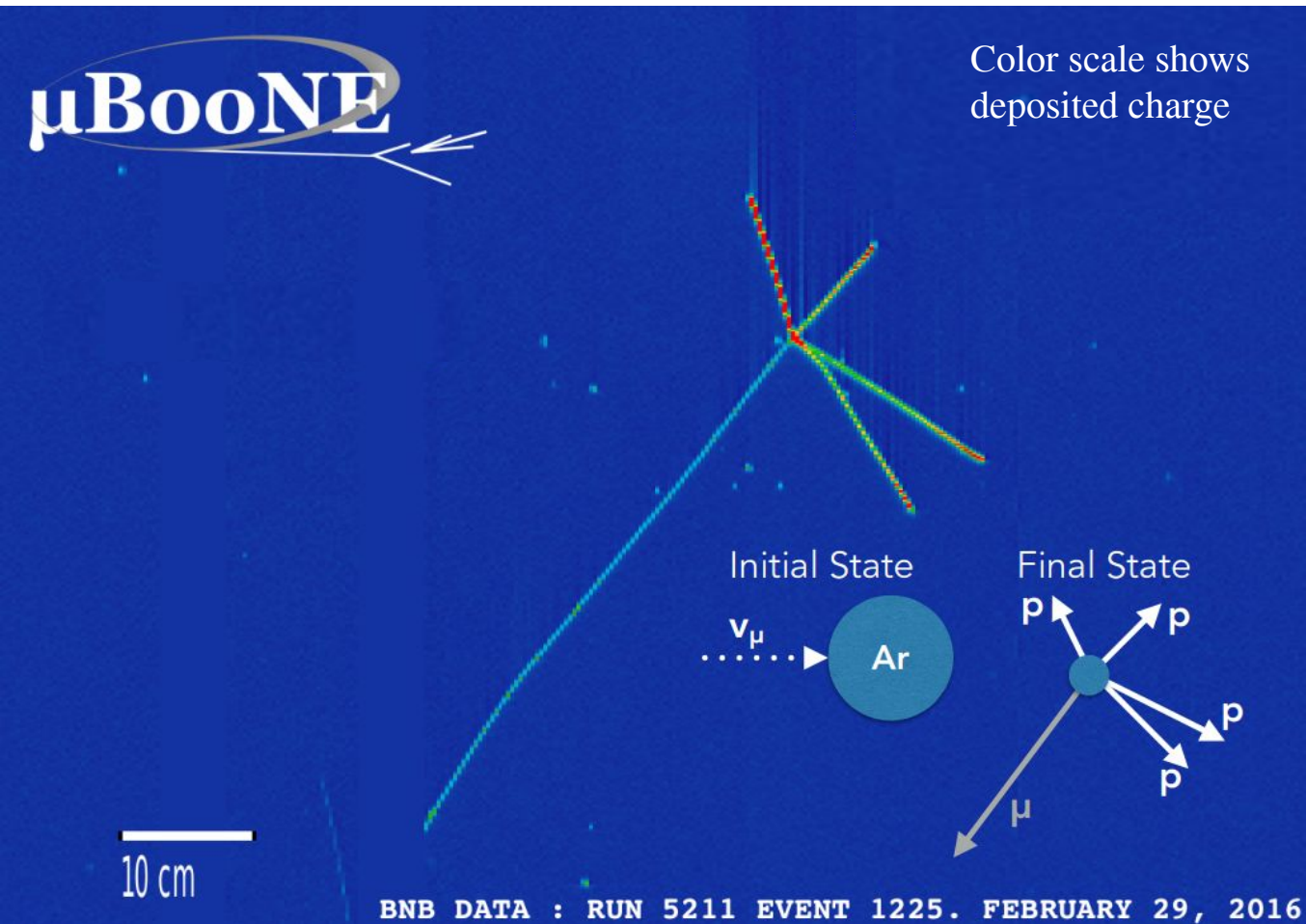
85 tonne Liquid Argon Time Projection Chamber (LArTPC)

# MicroBooNE detector



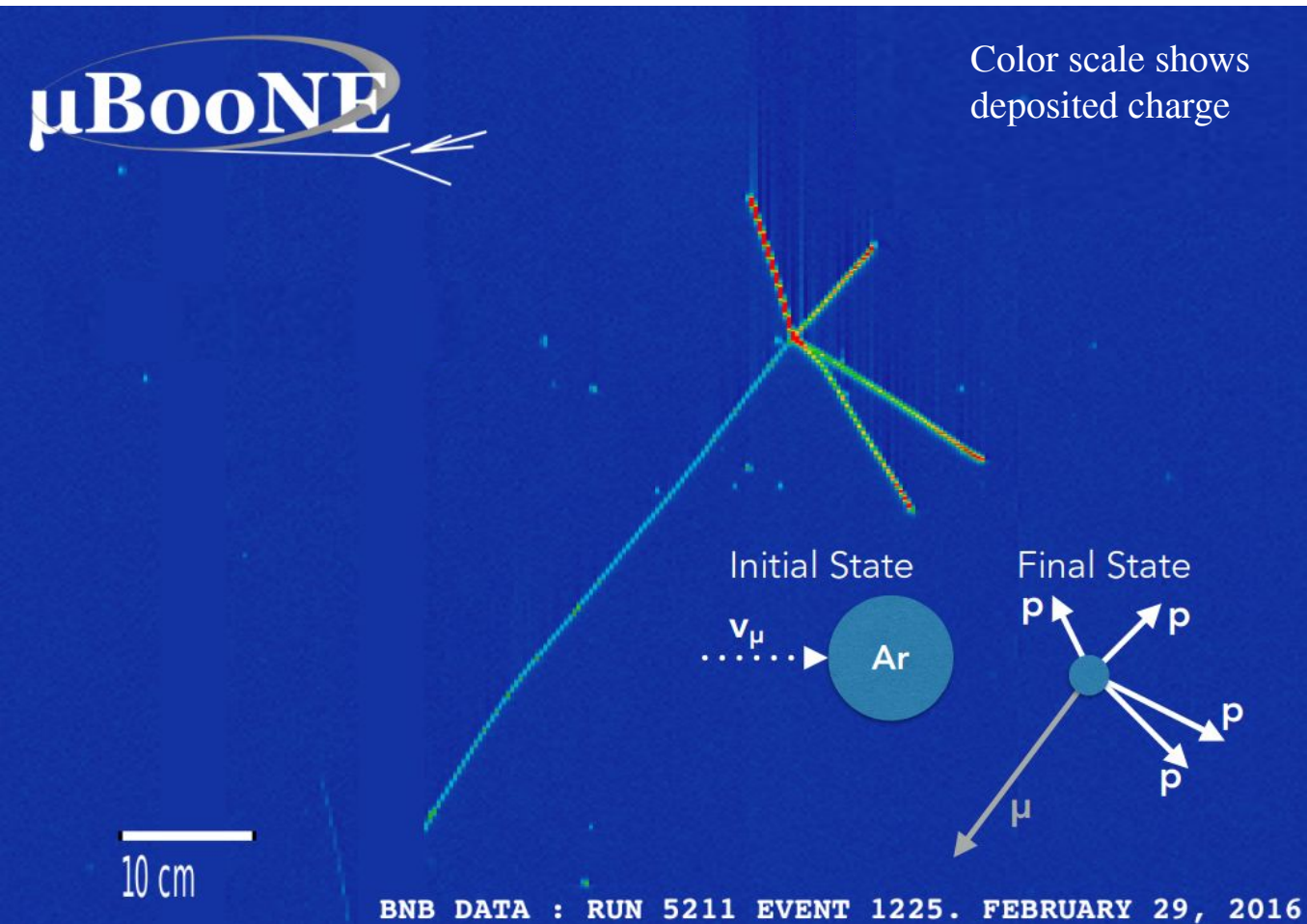
- 3 wire planes
- 8192 gold coated wires
- 3 mm wire spacing
- 32 PMTs

# MicroBooNE data events



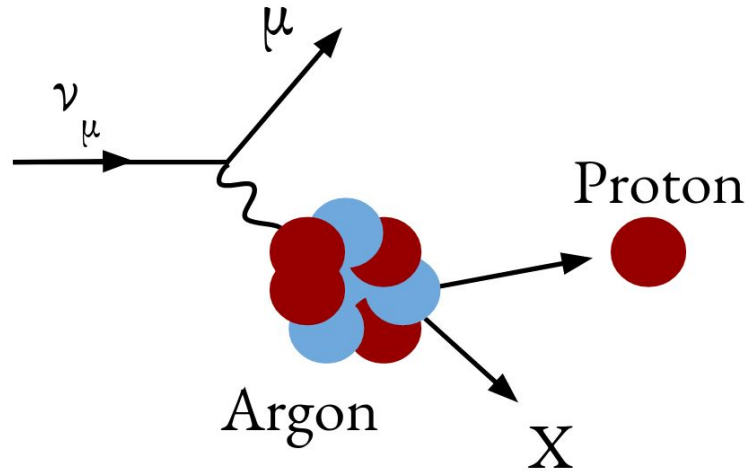
- Excellent spatial resolution
- Low detection thresholds
- Precise calorimetric information
- Powerful particle identification

# MicroBooNE data events



- One of largest available neutrino-argon data sets with ~500k recorded neutrino interactions
- More than 20 released and 30 active MicroBooNE cross section analyses
- Multiple event types investigated

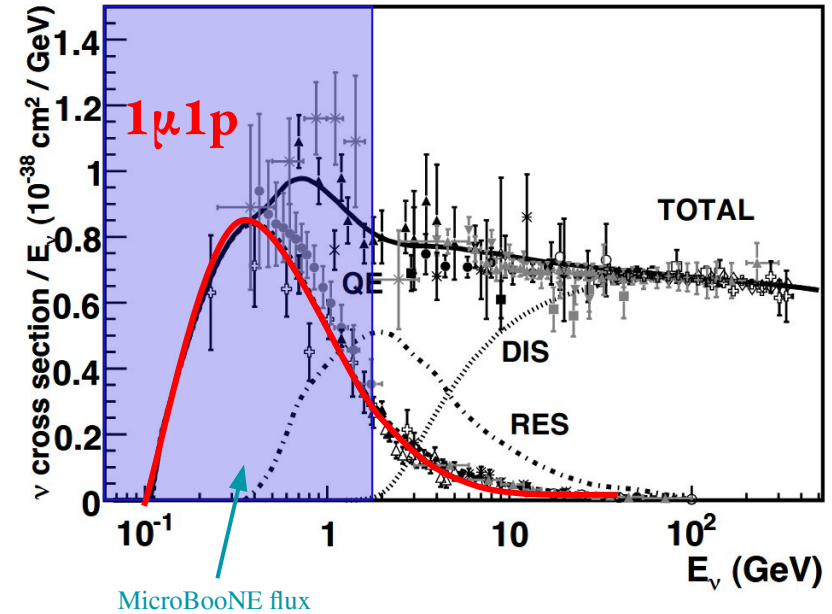
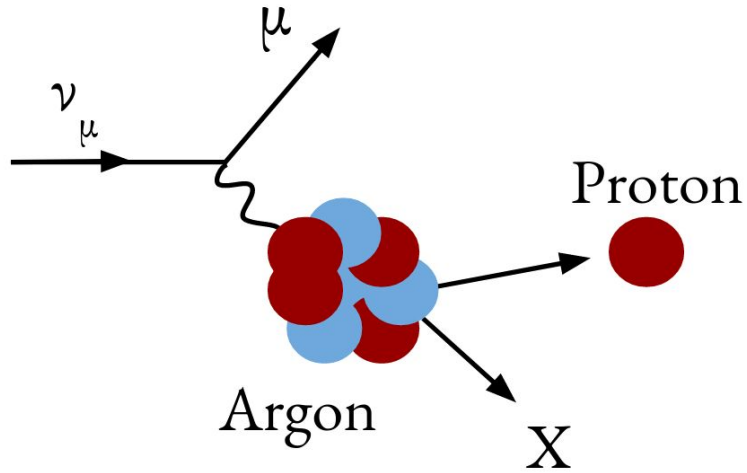
# Single-proton knockout events



- First-ever neutrino angle reconstruction data-driven study on argon
- Quantified angular reconstruction performance in specific phase-space regions

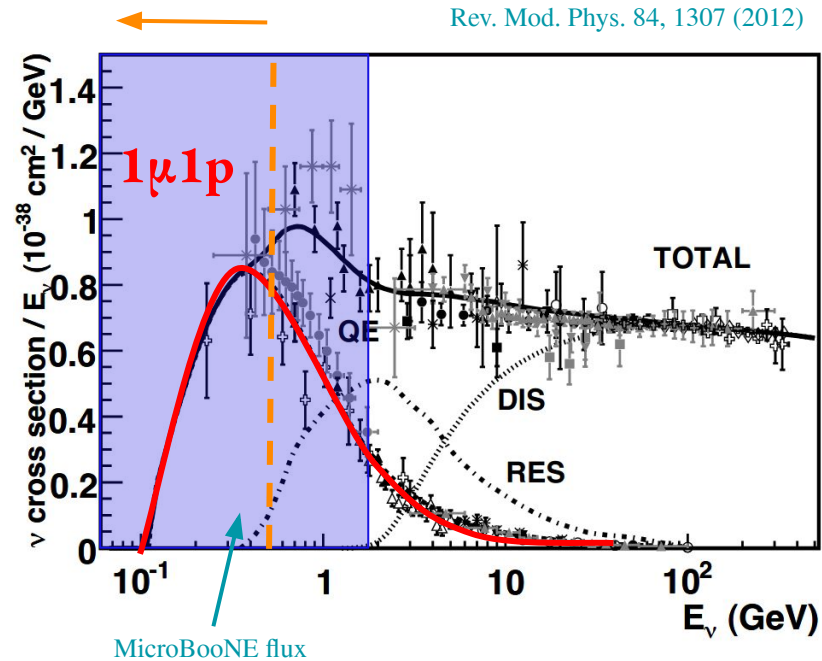
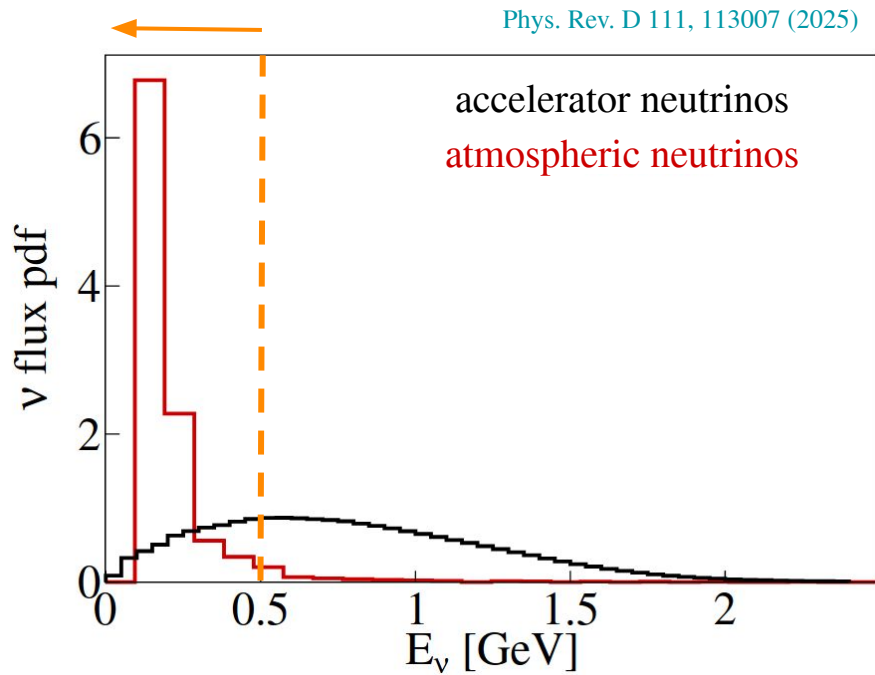
# Why single-proton events?

Rev. Mod. Phys. 84, 1307 (2012)



Simple and dominant at relevant energies

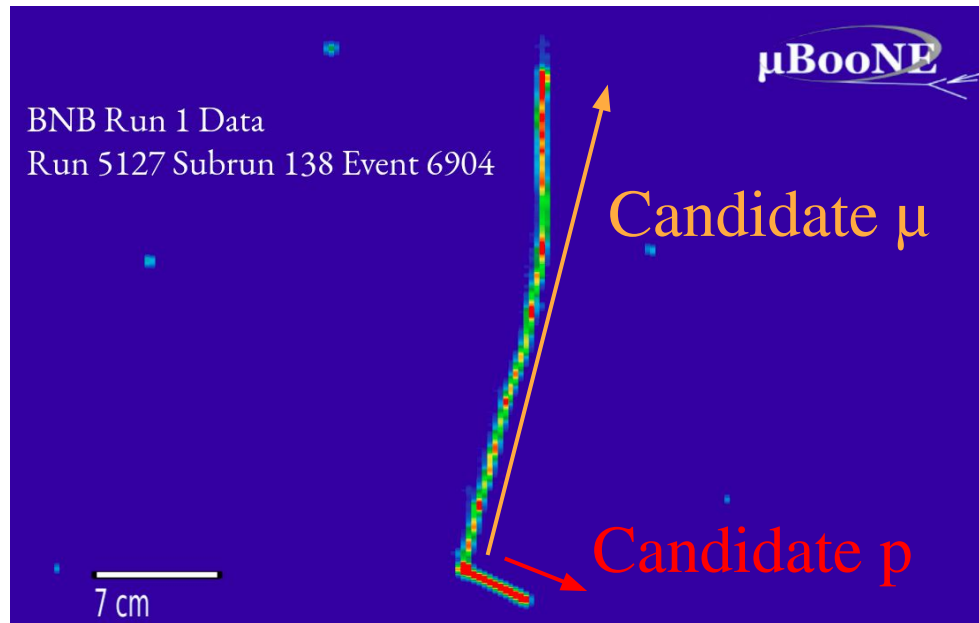
# Bonus!



Overlap with low energies relevant for atmospheric neutrinos

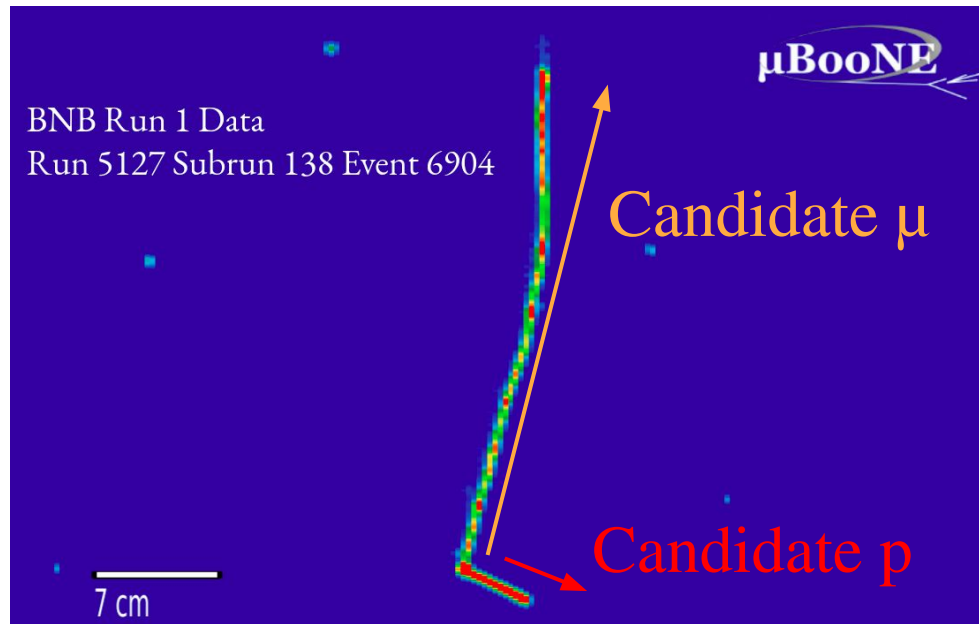
# Signal definition

- 1 muon  
 $100 < \mathbf{P}_\mu < 1200 \text{ MeV}/c$
- 1 proton  
 $300 < \mathbf{P}_p < 1000 \text{ MeV}/c$
- No  $\pi^\pm$  with  $P_\pi > 70 \text{ MeV}/c$
- No  $\pi^0$ /heavier mesons
- Any number of neutrons



# Signal definition

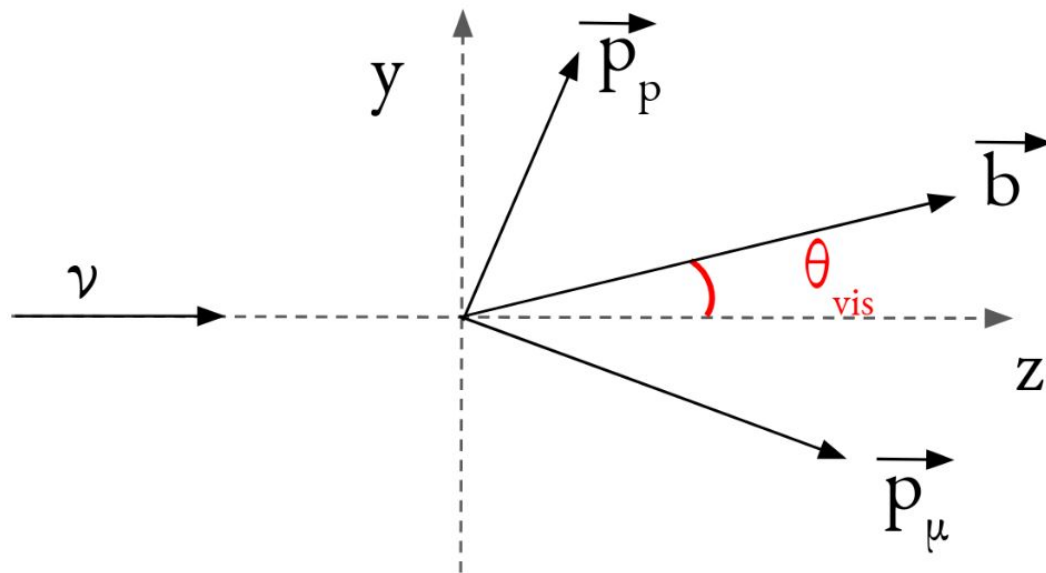
- Using Booster Neutrino Beam (BNB) flux and full MicroBooNE data set
- Fully contained tracks
- 17130  $CC1p0\pi$  candidate data events
- Purity  $\sim 70\%$
- Efficiency  $\sim 10\%$



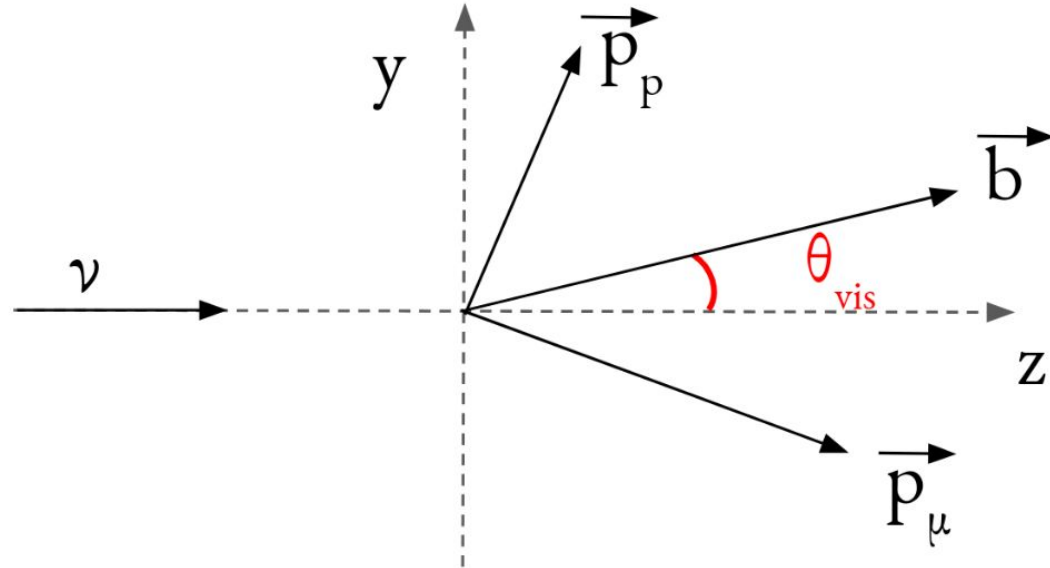
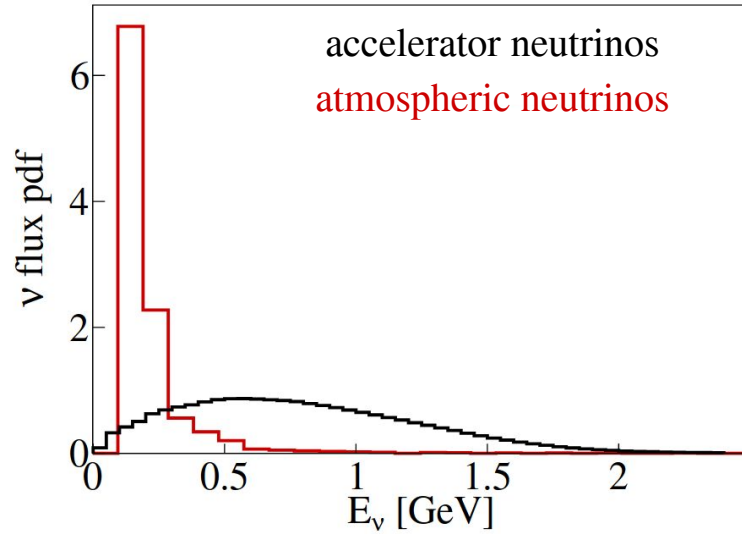
# Main observable

$$\theta_{\text{vis}} = \text{acos}\left(\frac{\vec{b} \cdot \hat{z}}{|\vec{b}|}\right)$$

$$\text{with } \vec{b} = \vec{p}_\mu + \vec{p}_p$$



# Main observable

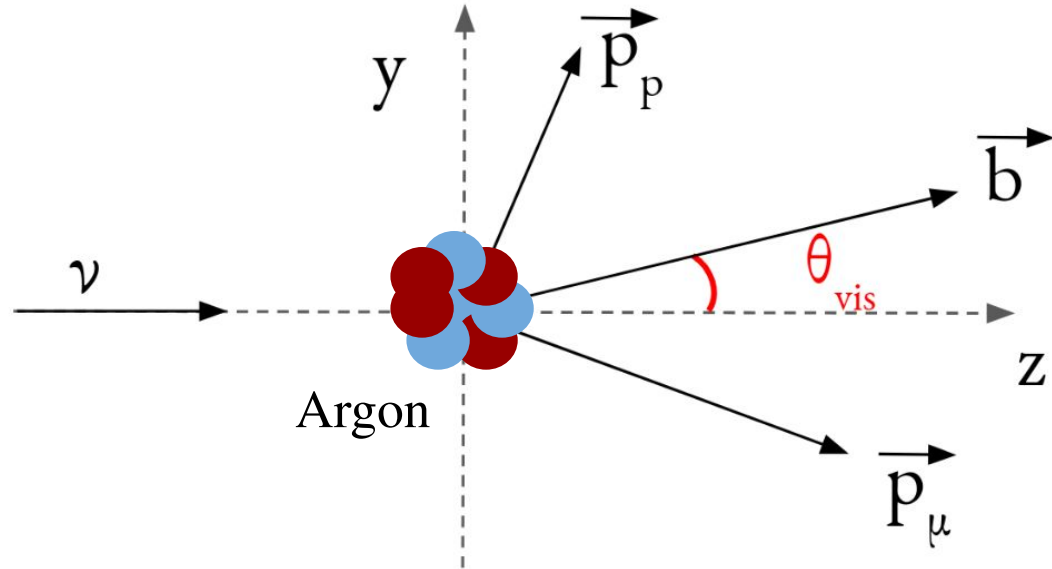


- BNB neutrinos have known origin, unlike DUNE atmospheric neutrinos
- BNB peaks at  $\sim 600$  MeV and has minimal contributions beyond 2 GeV

# Main observable

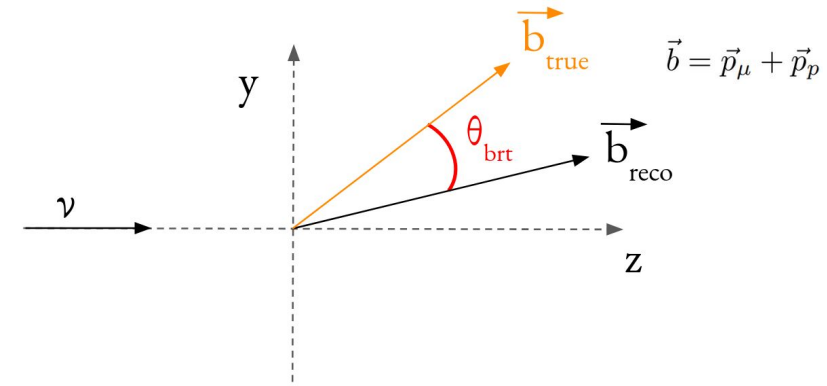
$$\theta_{\text{vis}} = \text{acos}\left(\frac{\vec{b} \cdot \hat{z}}{|\vec{b}|}\right)$$

$$\text{with } \vec{b} = \vec{p}_{\mu} + \vec{p}_p$$

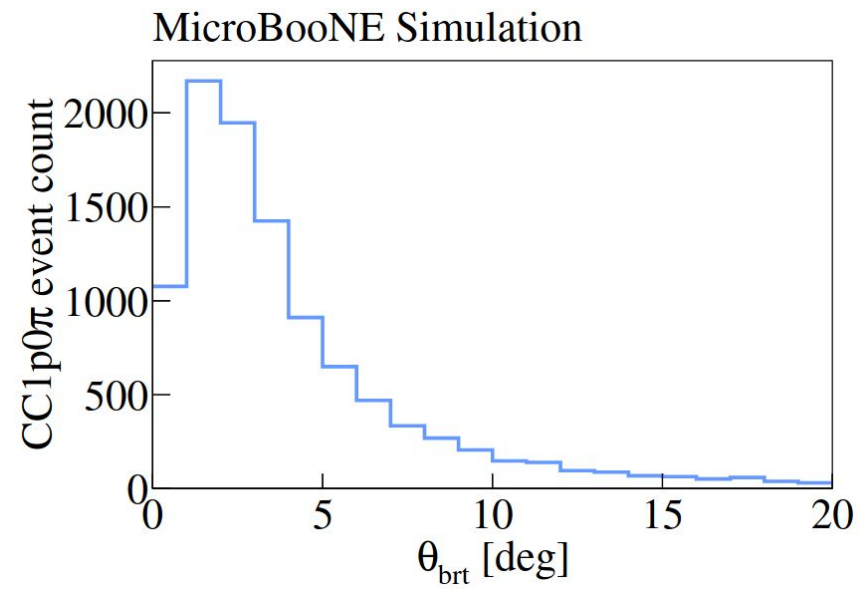
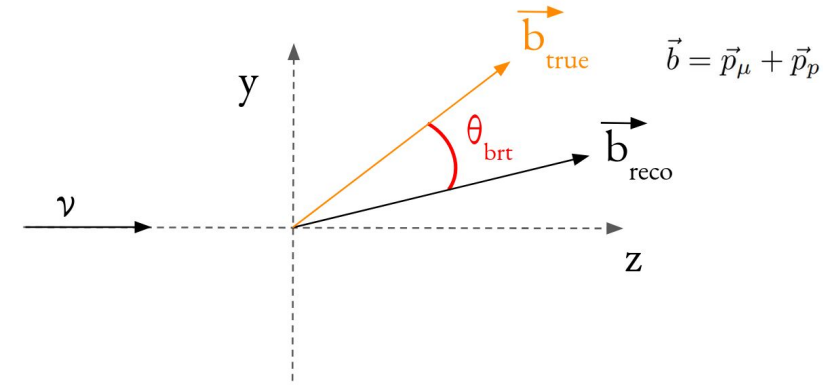


- Reconstructed angle  $\theta_{\text{vis}}$  is **not** expected to be precisely  $0^\circ$  due to detector smearing and nuclear effects that complicate our understanding of neutrino-nucleus interactions

# Reconstruction performance

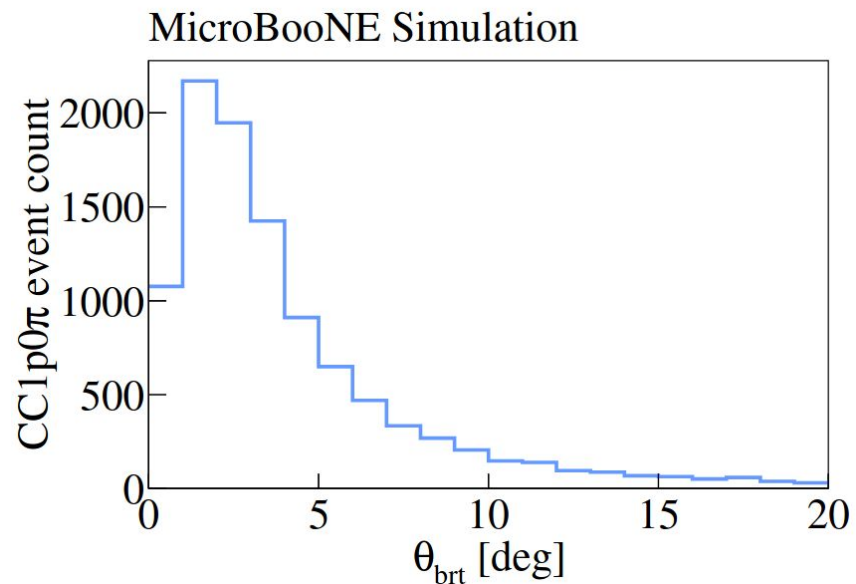
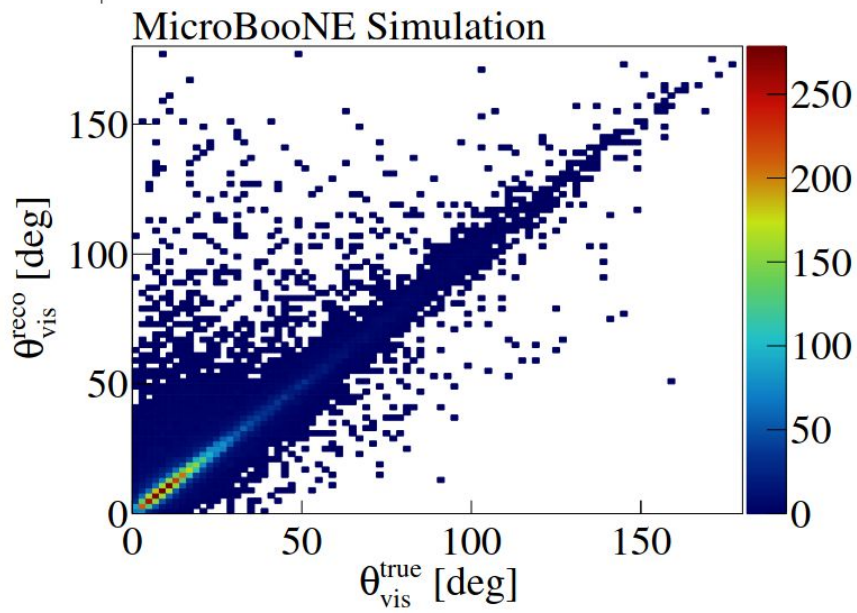
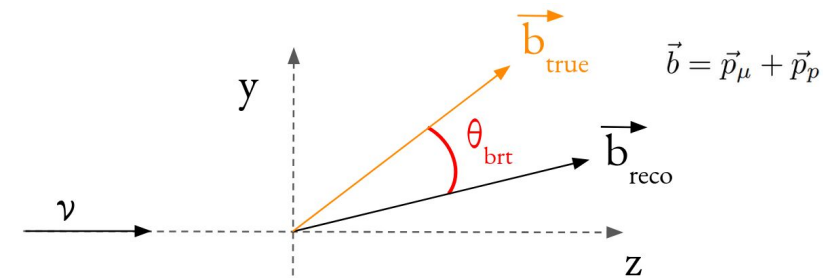


# Reconstruction performance



- Most events are reconstructed to better than  $5^\circ$

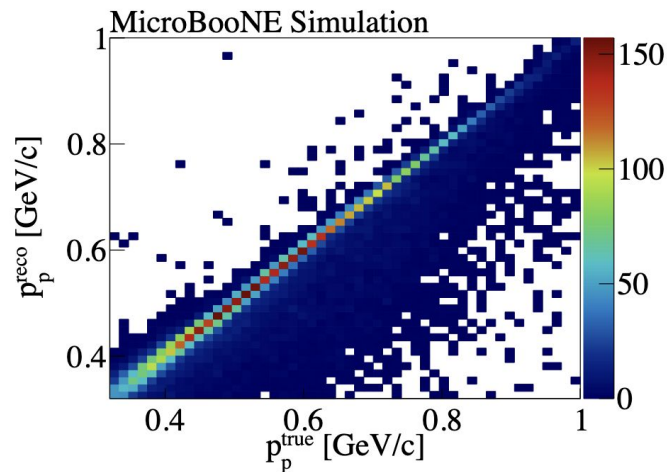
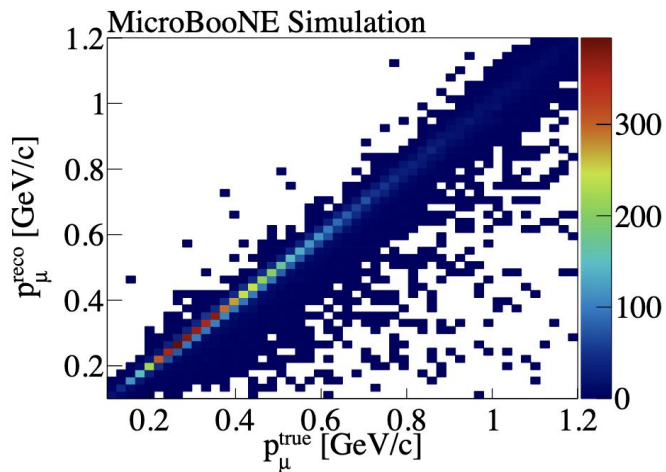
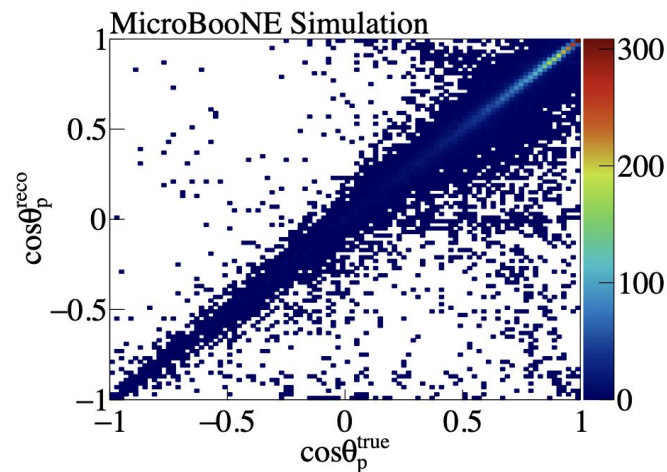
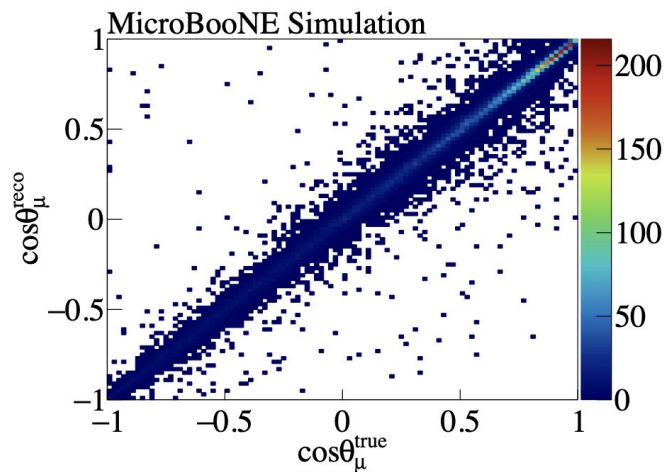
# Reconstruction performance



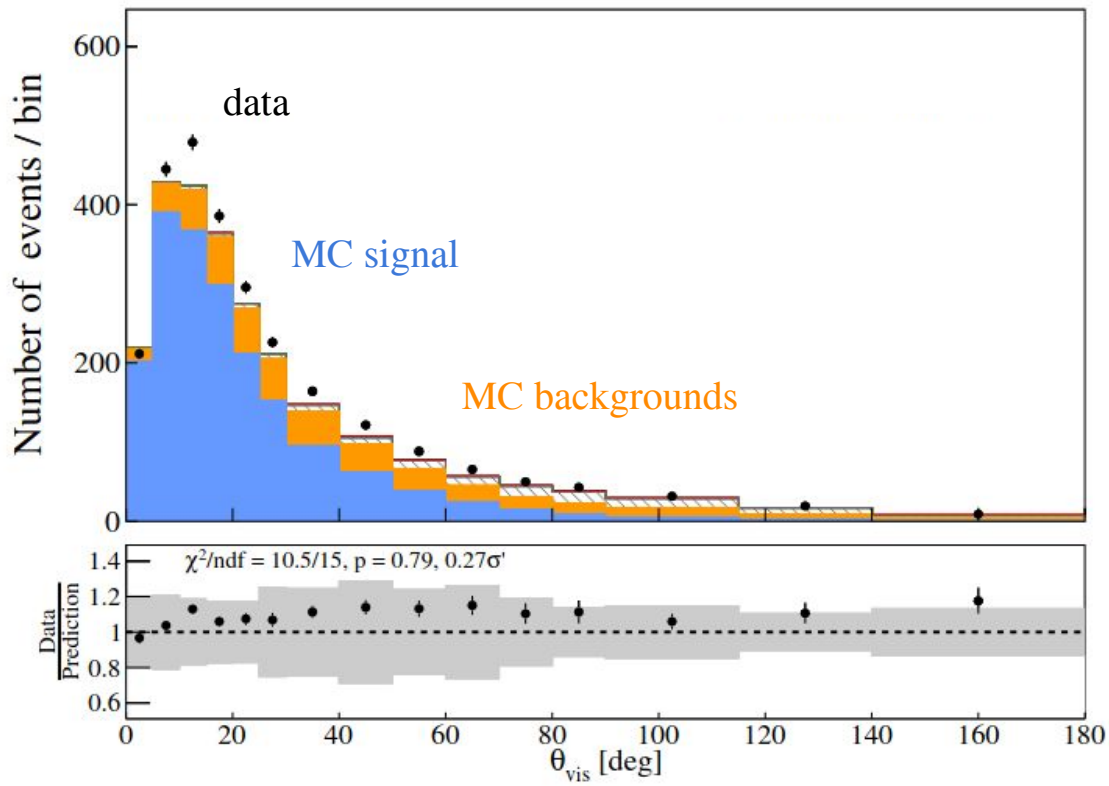
- Most events are reconstructed to better than 5°
- Very diagonal behavior

# Driving force

Excellent muon/proton  
angle & momentum  
reconstruction in  
LArTPCs



# $\theta_{\text{vis}}$ evolution



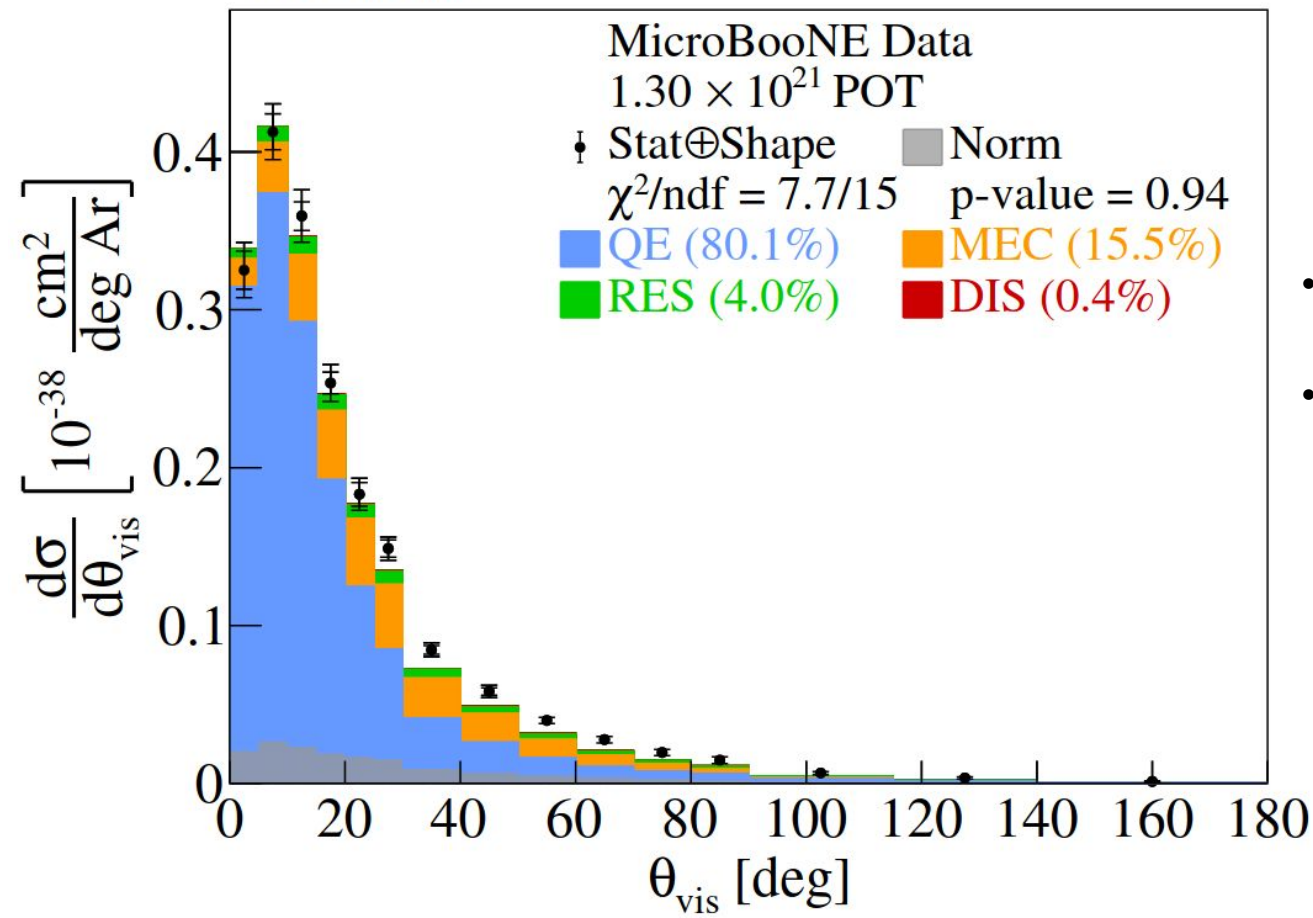
Broad distribution due to detector smearing and nuclear effects

# Cross section measurements

Detector smearing effects removed

Nuclear effects still present

# Cross section measurements



- Long tail observed
- But still no clear indication of which nuclear effect is dominant

# Regions of study

Reconstructed visible energy

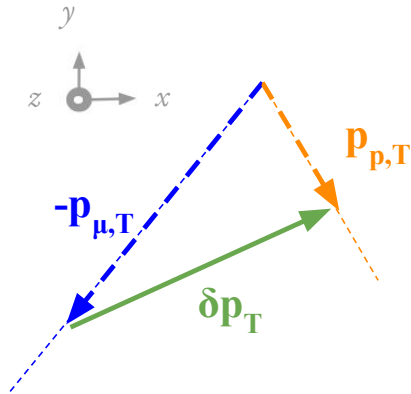
$B = 30.9$  MeV argon removal energy

$$E_{\text{reco}} = E_{\mu} + K_p + B$$

# Regions of study

$$\delta \vec{p}_T = \vec{p}_{\mu,T} + \vec{p}_{p,T}$$

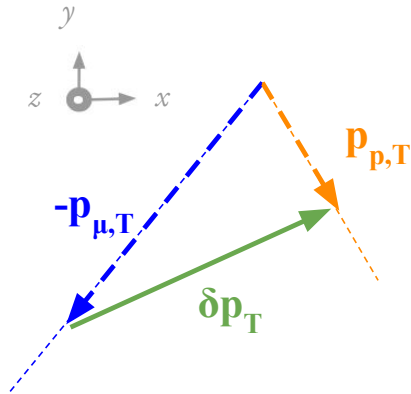
Total struck nucleon momentum



# Regions of study

$$\delta \vec{p}_T = \vec{p}_{\mu,T} + \vec{p}_{p,T}$$
$$p_L = p_{\mu,L} + p_{p,L} - E_{\text{reco}}$$

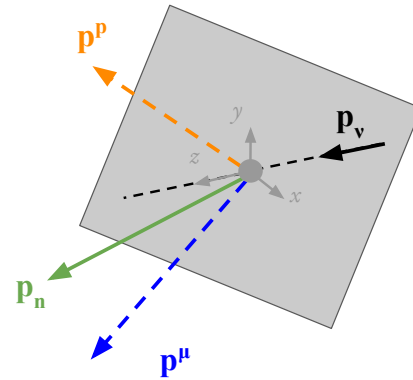
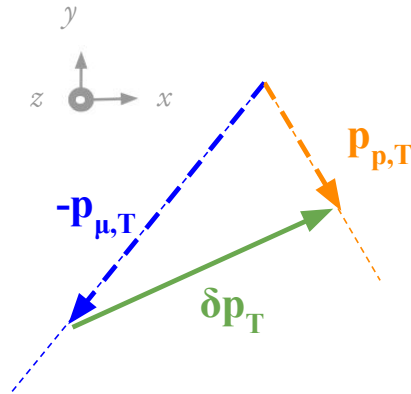
Total struck nucleon momentum



# Regions of study

Total struck nucleon momentum

$$\delta\vec{p}_T = \vec{p}_{\mu,T} + \vec{p}_{p,T}$$
$$p_L = p_{\mu,L} + p_{p,L} - E_{\text{reco}}$$
$$p_n = |\vec{p}_n| = \sqrt{p_L^2 + \delta p_T^2}$$



# Regions of study

Missing momentum

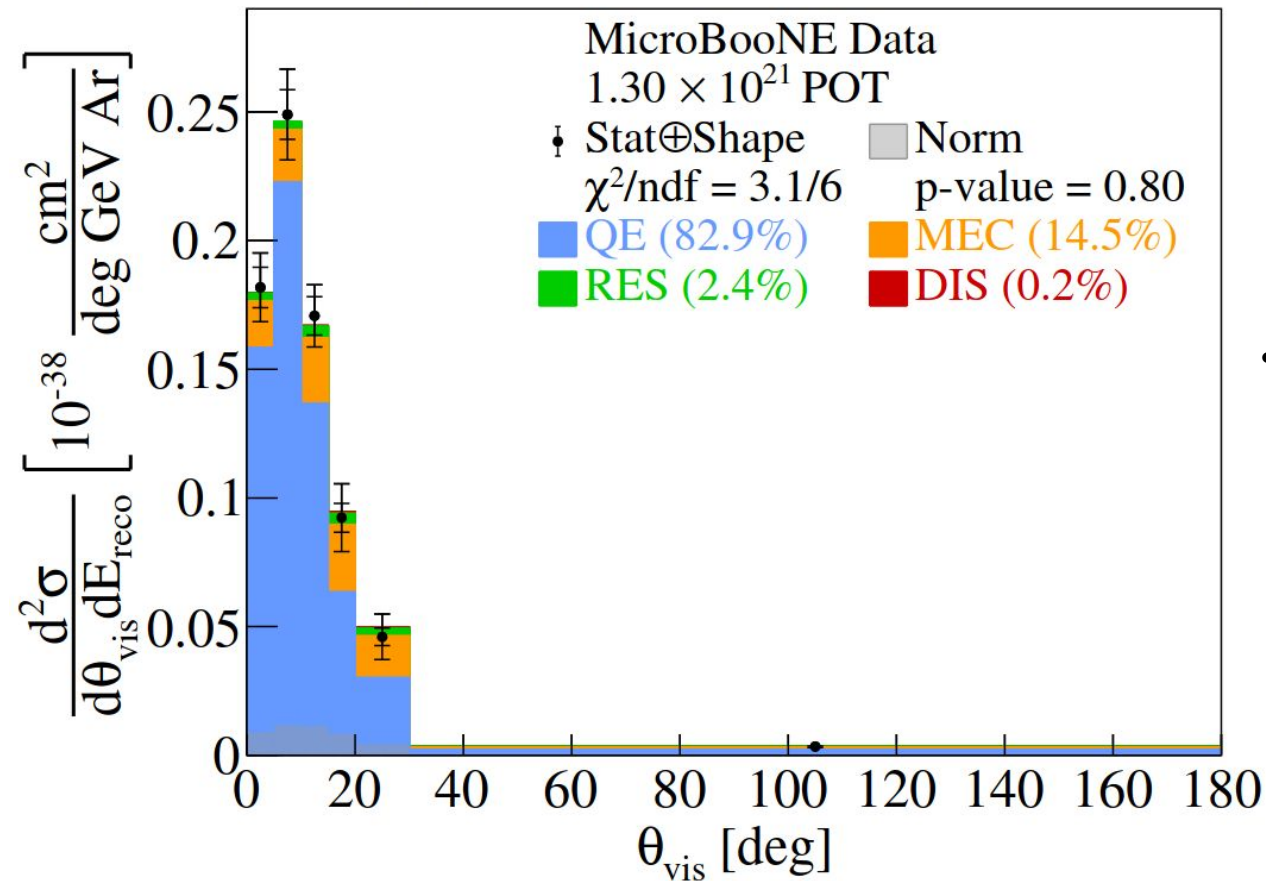
(new and agnostic to neutrino direction!)

$$\vec{b} = \vec{p}_\mu + \vec{p}_p$$
$$p_{\text{miss}} = E_{\text{reco}} - b$$

$$E_{\text{reco}} = E_{\mu} + K_p + B$$

# Cross section measurements

$0.8 < E_{\text{reco}} < 2 \text{ GeV}$

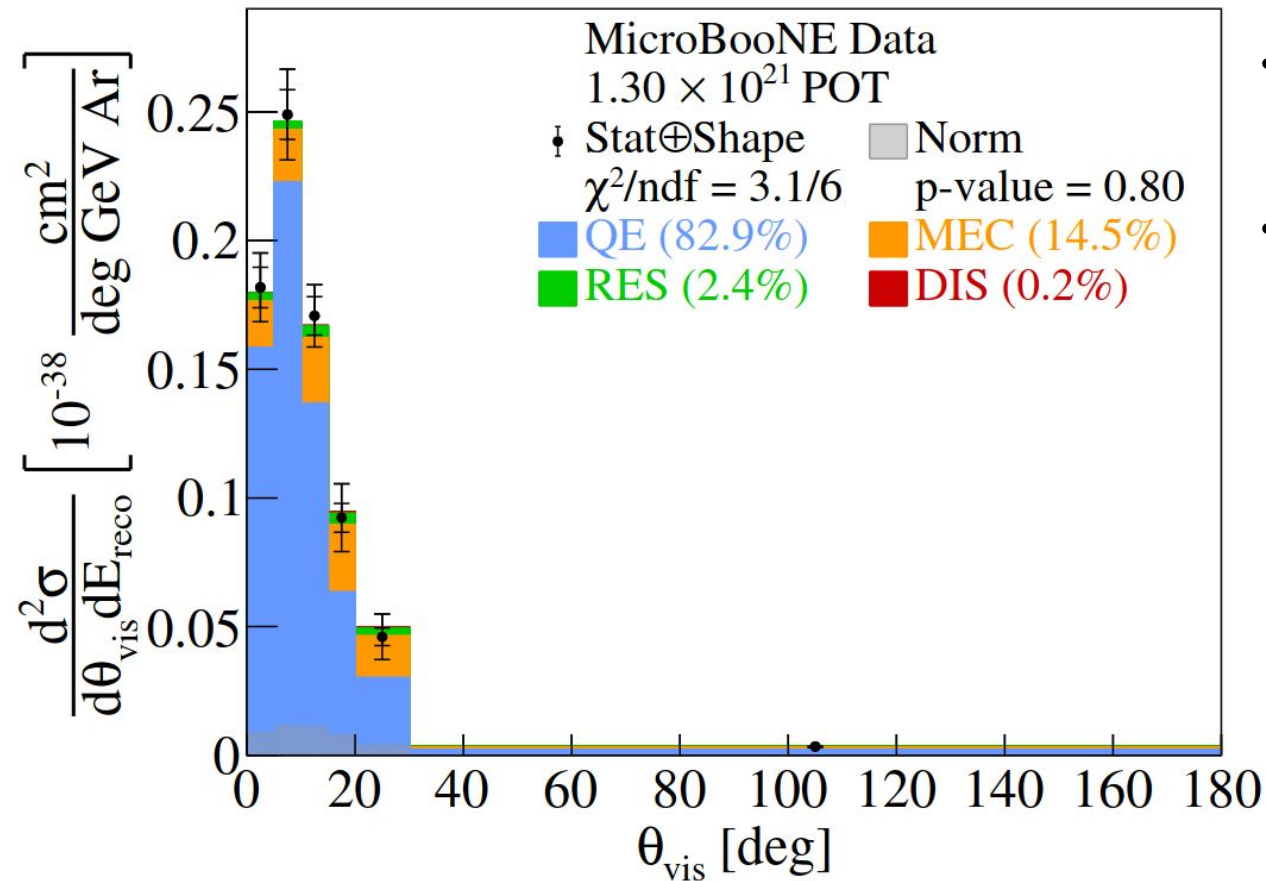


- Depleted tail  $\rightarrow$  less reinteractions or undetected particles

$$E_{\text{reco}} = E_{\mu} + K_p + B$$

# Cross section measurements

$0.8 < E_{\text{reco}} < 2 \text{ GeV}$

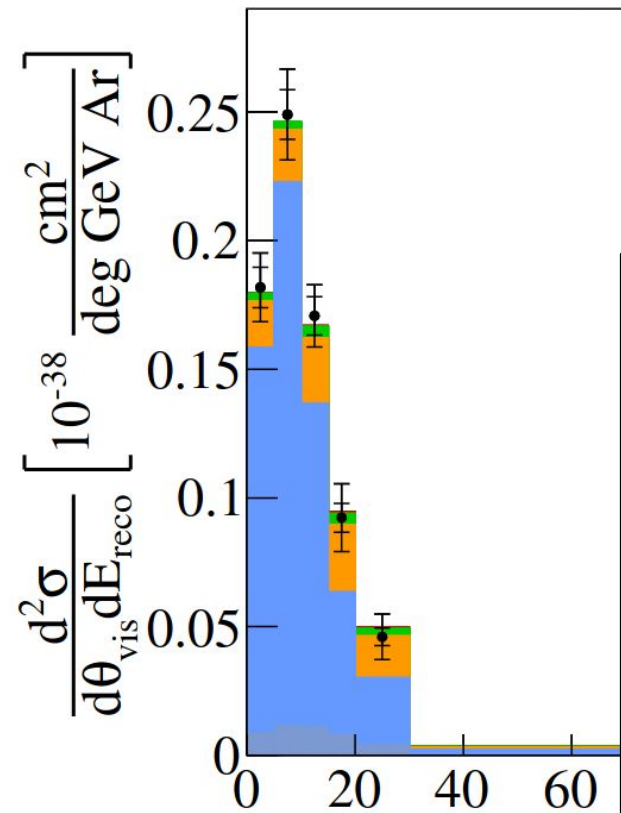


- Depleted tail  $\rightarrow$  less reinteractions or undetected particles
- Struck nucleon motion dominance

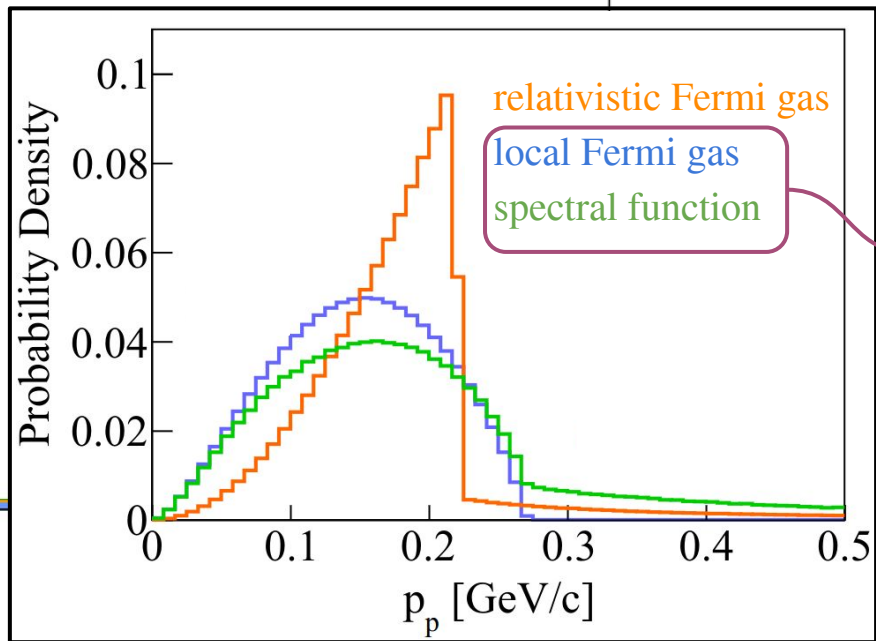
$$E_{\text{reco}} = E_{\mu} + K_p + B$$

# Cross section measurements

$0.8 < E_{\text{reco}} < 2 \text{ GeV}$



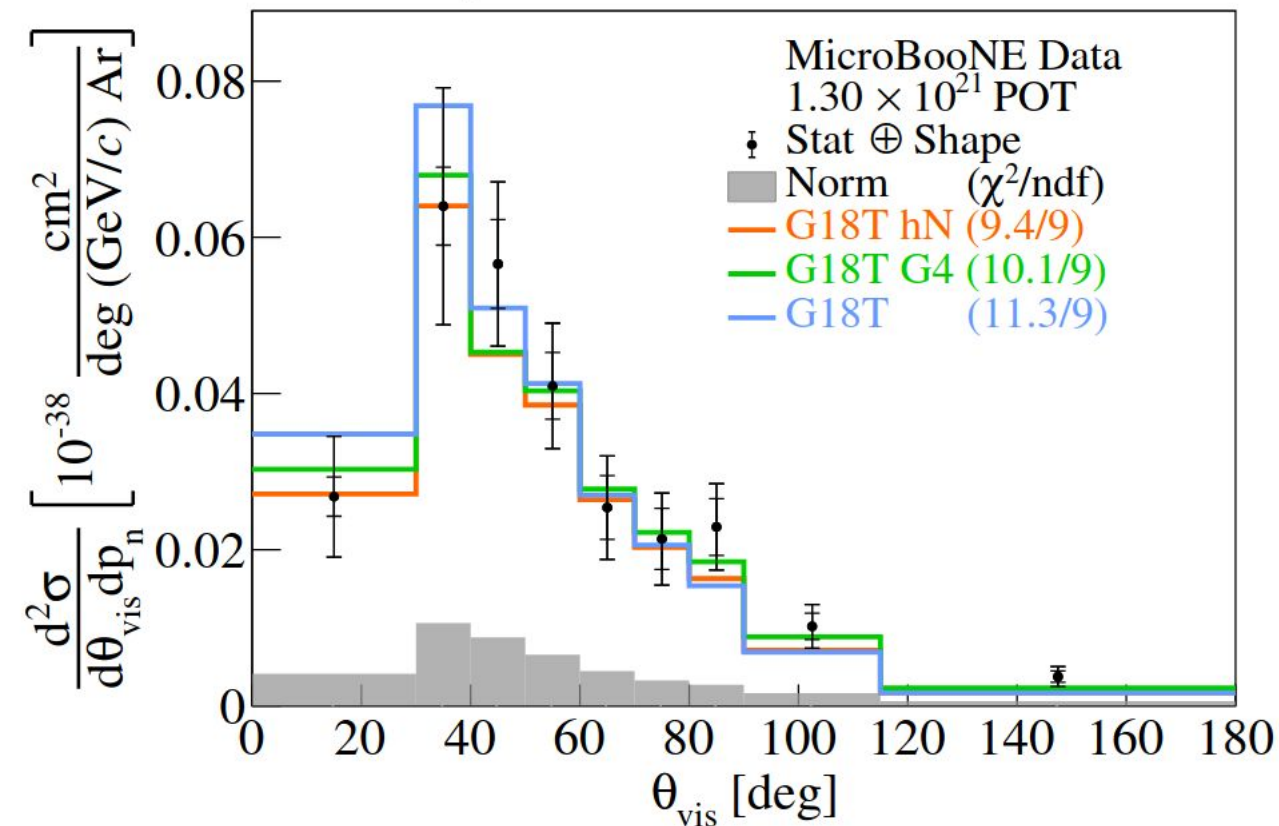
- Depleted tail  $\rightarrow$  less reinteractions or undetected particles
- Struck nucleon motion dominance



commonly used simulation options

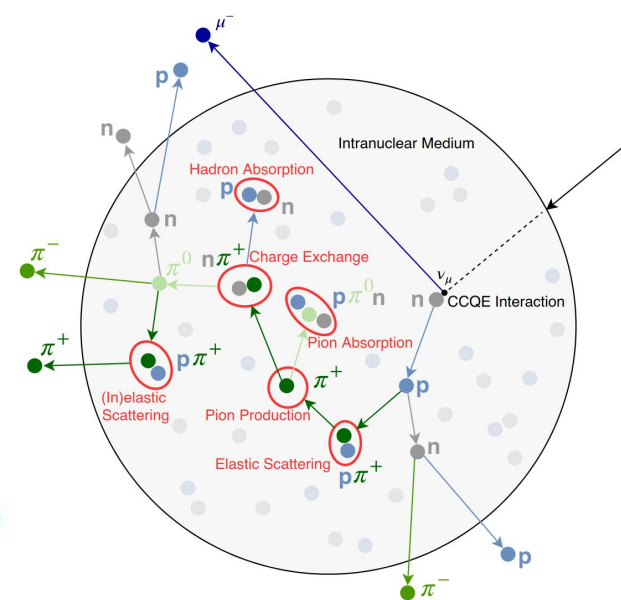
# Hadron reinteractions

$$0.4 < p_n < 1 \text{ GeV}/c$$



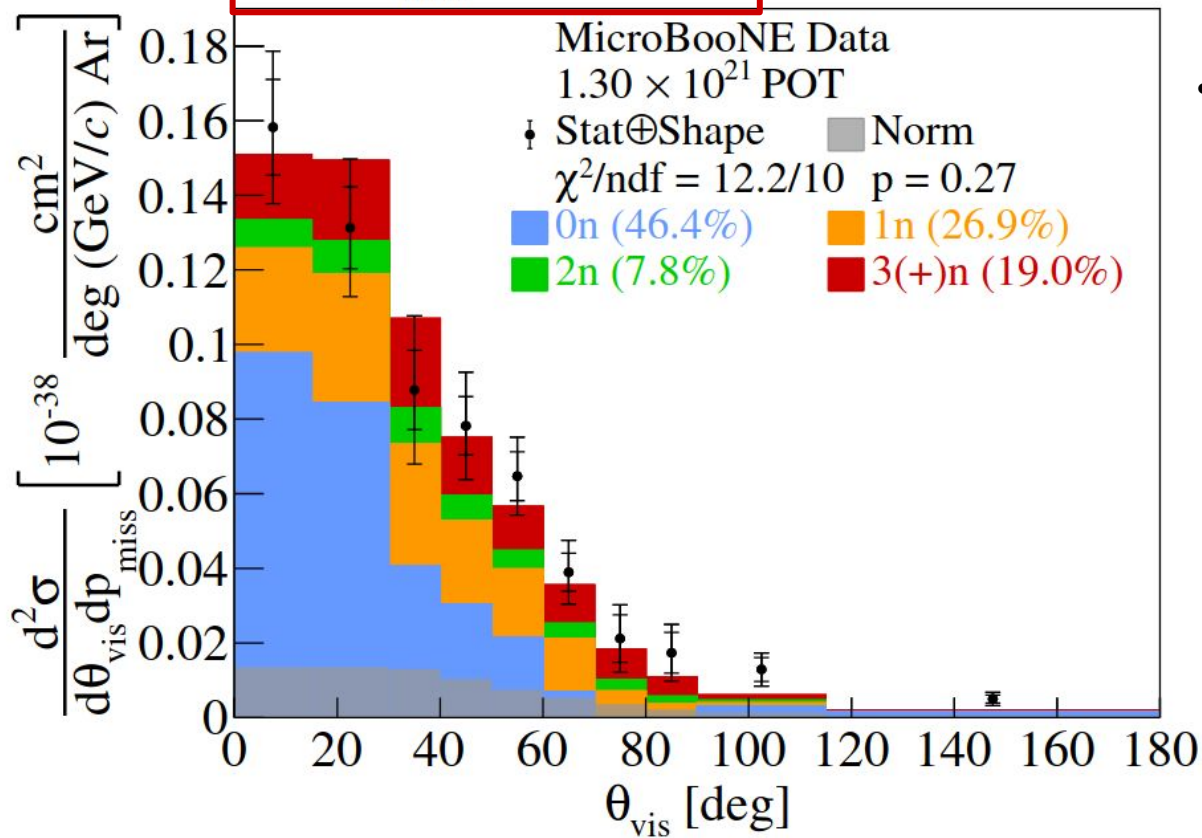
$$p_n = |\vec{p}_n| = \sqrt{p_L^2 + \delta p_T^2}$$

- Long tail  $\rightarrow$  more reinteractions
- Reinteraction models investigated



# Neutrons

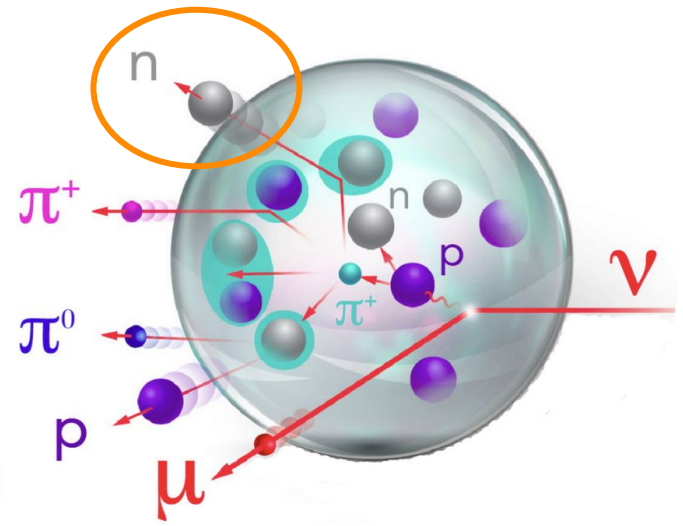
$$0.2 < |\vec{p}_{\text{miss}}| < 0.5 \text{ GeV}/c$$



$$\vec{b} = \vec{p}_\mu + \vec{p}_p$$

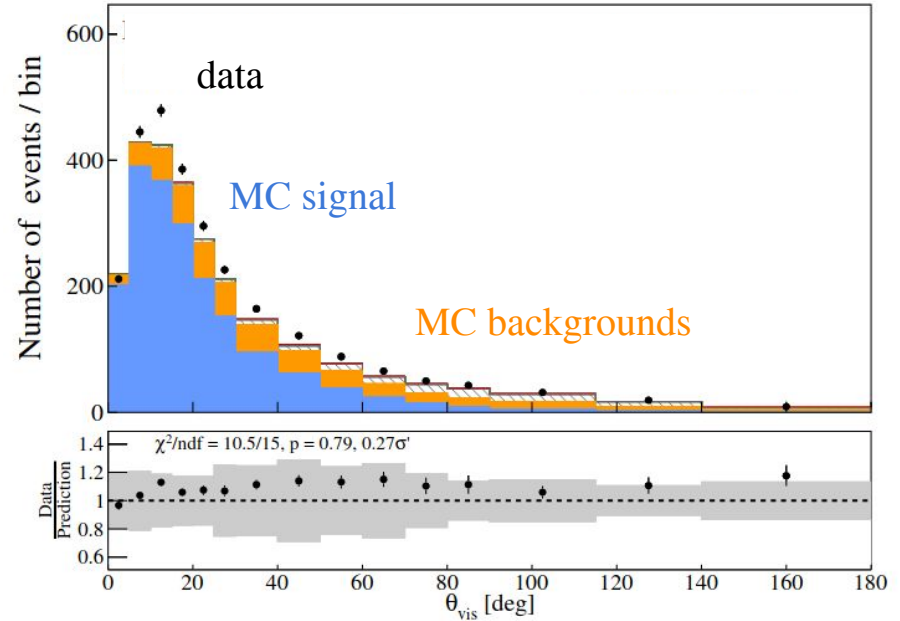
$$p_{\text{miss}} = E_{\text{reco}} - b$$

- Long tail → more undetected particles



# Summary

- First-ever neutrino angle reconstruction data-driven study with the MicroBooNE LArTPC
- Quantified angular reconstruction performance in specific phase-space regions
- Path forward towards atmospheric oscillation analyses

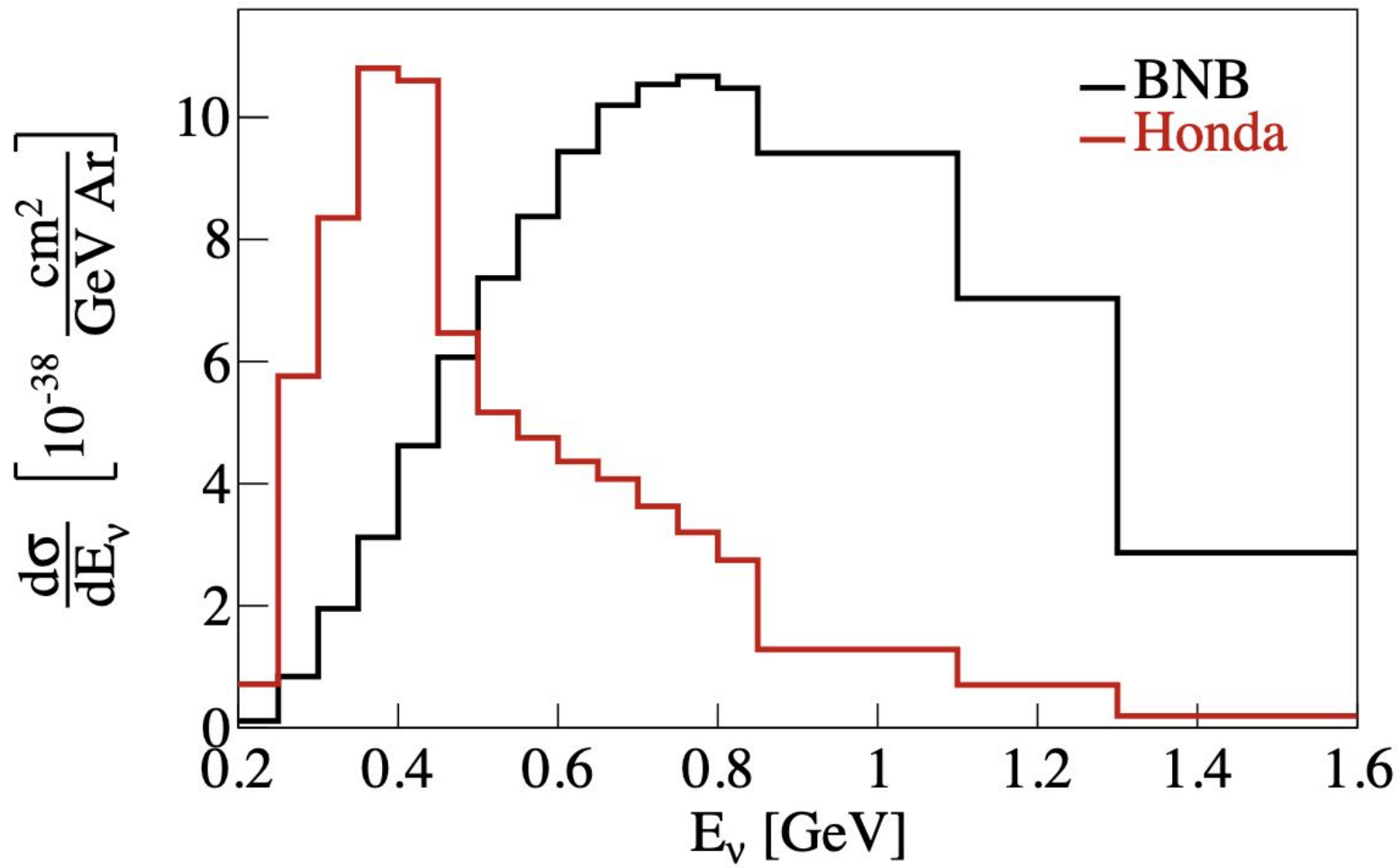


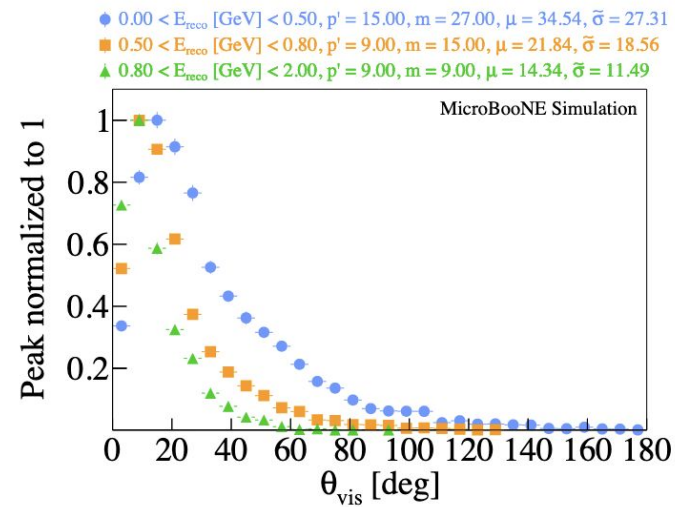
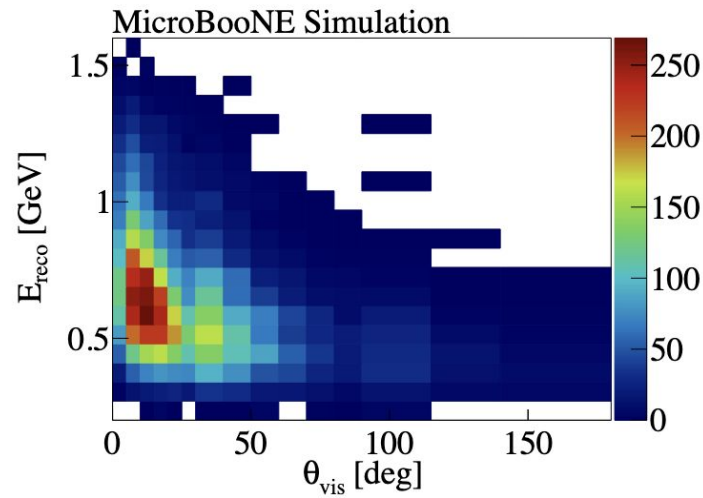


Thank you!

# Backup Slides

# Flux-averaged cross section

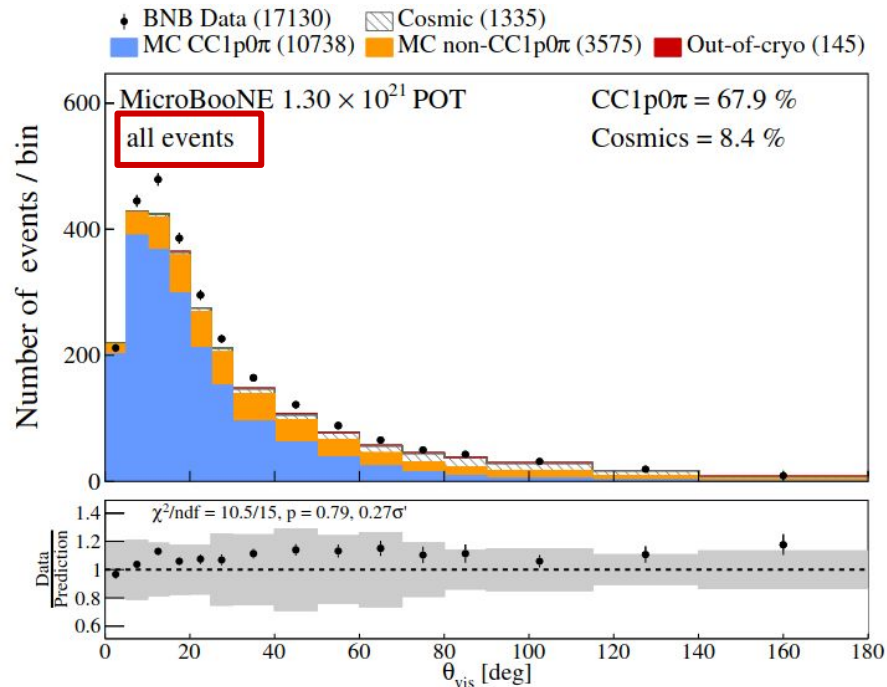




# $\theta_{\text{vis}}$ evolution

$\mu$  = mean,  $\sigma$  = standard deviation, m = median

Region	$\mu$ [deg]	$\tilde{\sigma}$ [deg]	m [deg]
All events	23.2	21.1	16.5
$E_{\text{reco}} < 0.5 \text{ GeV}$	34.5	27.3	26.5
$0.5 < E_{\text{reco}} < 0.8 \text{ GeV}$	21.8	18.6	16.5
$0.8 < E_{\text{reco}} < 2 \text{ GeV}$	14.3	11.5	10.5
$p_n < 0.2 \text{ GeV}/c$	10.0	5.8	9.5
$0.2 < p_n < 0.4 \text{ GeV}/c$	21.8	11.4	19.5
$0.4 < p_n < 1 \text{ GeV}/c$	49.3	26.3	44.5
$ p_{\text{miss}}  < 0.1 \text{ GeV}/c$	20.7	19.4	15.5
$0.1 <  p_{\text{miss}}  < 0.2 \text{ GeV}/c$	23.6	21.3	16.5
$0.2 <  p_{\text{miss}}  < 0.5 \text{ GeV}/c$	29.8	23.6	23.5

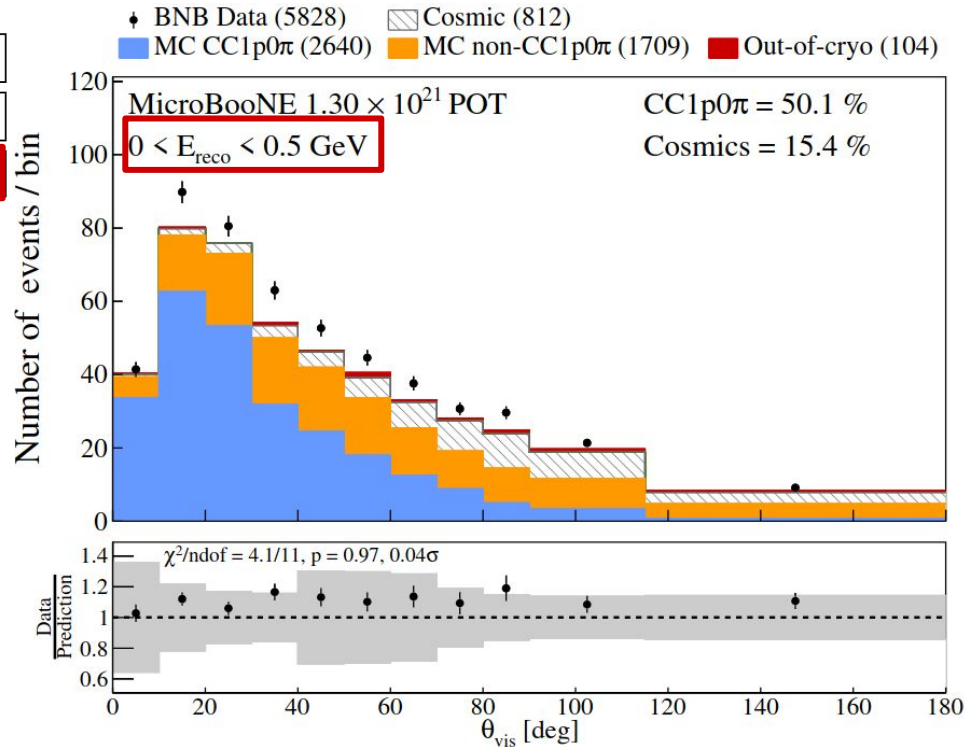


# $\theta_{\text{vis}}$ evolution

$\mu$  = mean,  $\sigma$  = standard deviation, m = median

Region	$\mu$ [deg]	$\tilde{\sigma}$ [deg]	m [deg]
All events	23.2	21.1	16.5
$E_{\text{reco}} < 0.5 \text{ GeV}$	34.5	27.3	26.5

Broad tail



# $\theta_{\text{vis}}$ evolution

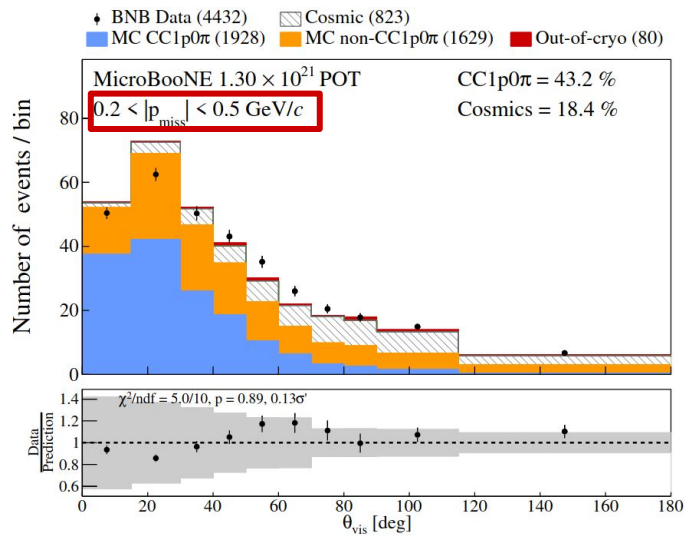
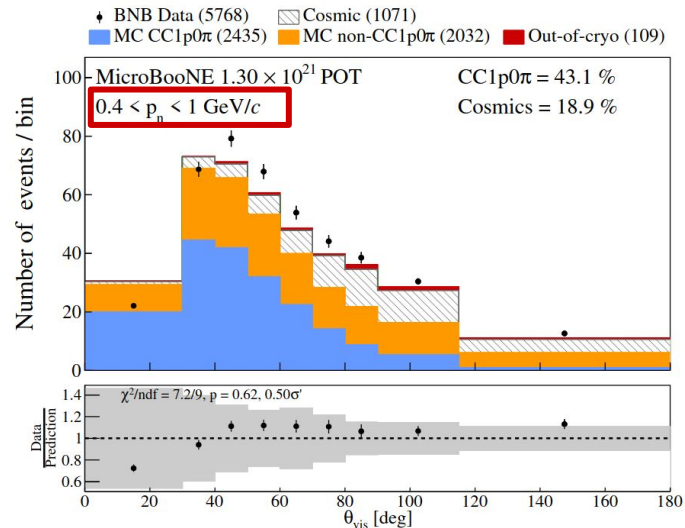
$\mu$  = mean,  $\sigma$  = standard deviation,  $m$  = median

Region	$\mu$ [deg]	$\tilde{\sigma}$ [deg]	$m$ [deg]
All events	23.2	21.1	16.5

$0.4 < p_n < 1 \text{ GeV}/c$	49.3	26.3	44.5
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$0.2 <  p_{\text{miss}}  < 0.5 \text{ GeV}/c$	29.8	23.6	23.5
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Broad tail



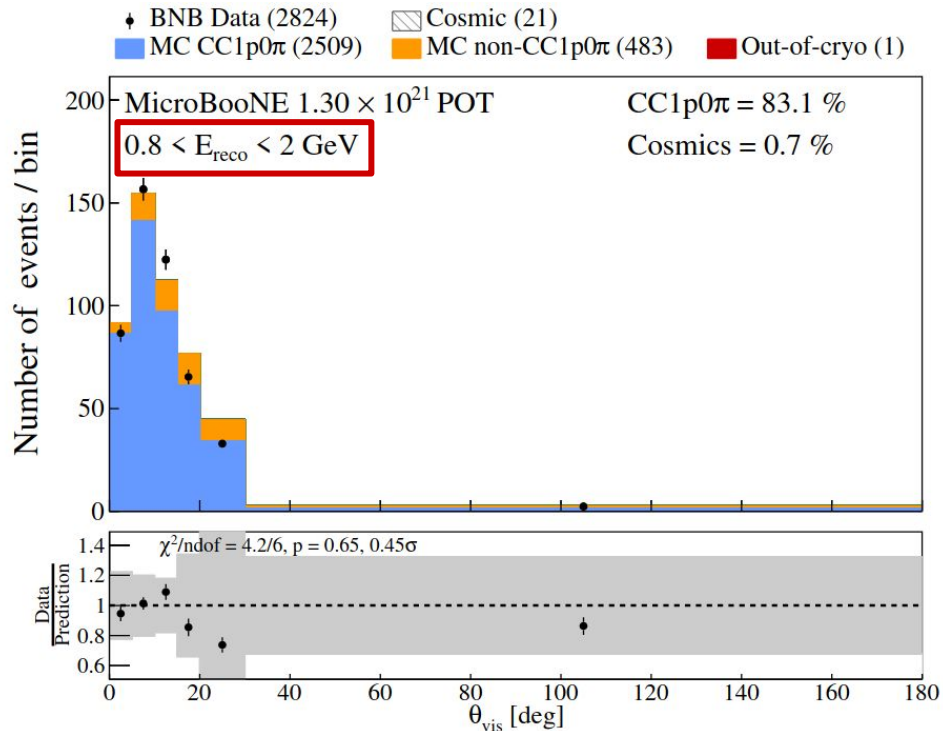
# $\theta_{\text{vis}}$ evolution

$\mu$  = mean,  $\sigma$  = standard deviation, m = median

Region	$\mu$ [deg]	$\tilde{\sigma}$ [deg]	m [deg]
All events	23.2	21.1	16.5

$0.8 < E_{\text{reco}} < 2 \text{ GeV}$	14.3	11.5	10.5
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Less broad distribution



# $\theta_{\text{vis}}$ evolution

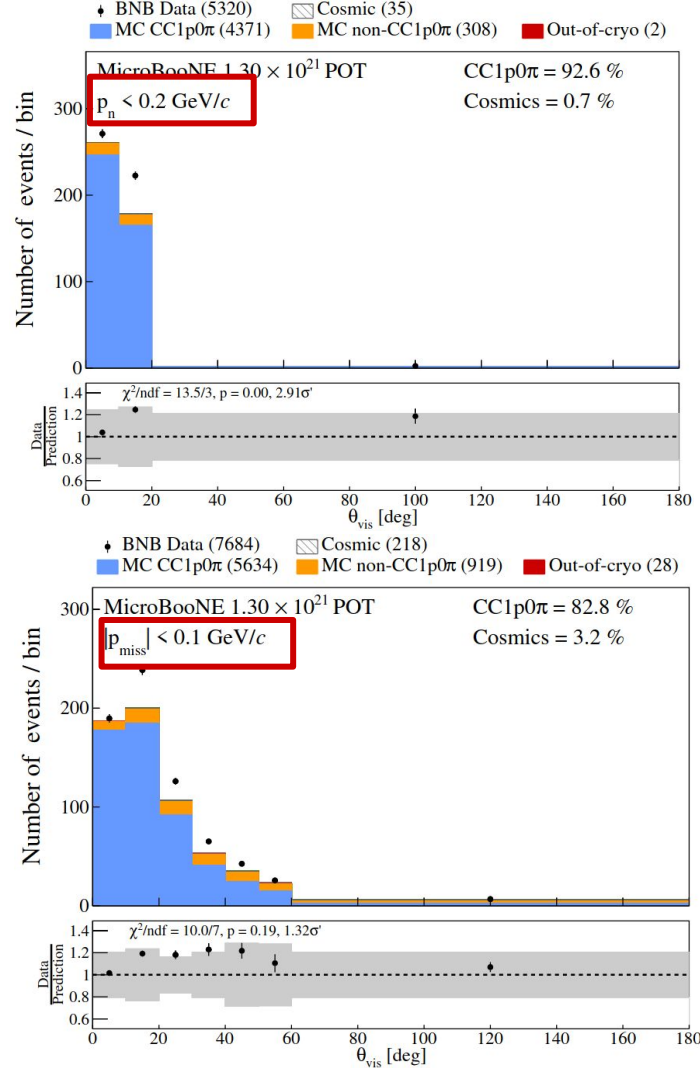
$\mu$  = mean,  $\sigma$  = standard deviation,  $m$  = median

Region	$\mu$ [deg]	$\tilde{\sigma}$ [deg]	$m$ [deg]
All events	23.2	21.1	16.5

$p_n < 0.2 \text{ GeV}/c$	10.0	5.8	9.5
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$ p_{\text{miss}}  < 0.1 \text{ GeV}/c$	20.7	19.4	15.5
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Less broad distribution



# Comparison to DUNE model

MicroBooNE uses a different default model (G18T) compared to DUNE's (AR23\_20i\_00\_000 or AR23)

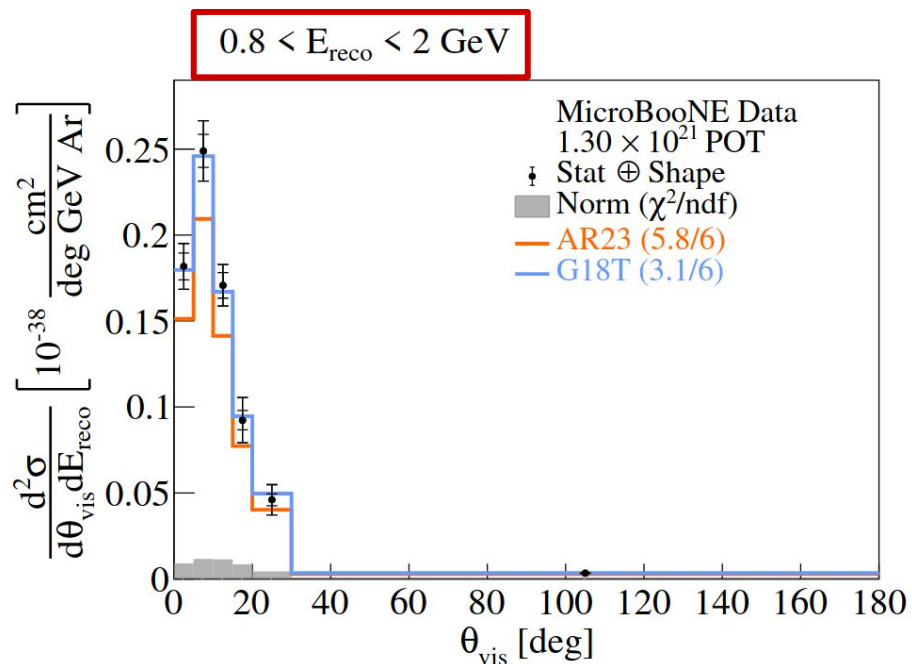
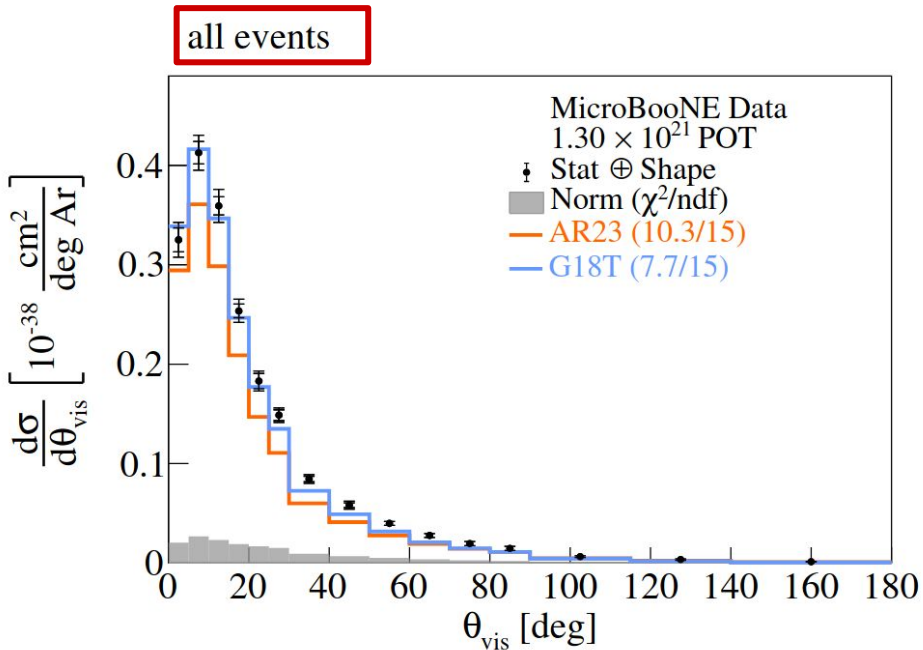
<b>Main difference</b>	<b>G18T</b>	<b>AR23</b>
QE/MEC tune	Tuned to T2K data	No tune

Most other models, eg resonance production, deep inelastic scattering, final state interactions, are ~the same

# Comparison to DUNE model

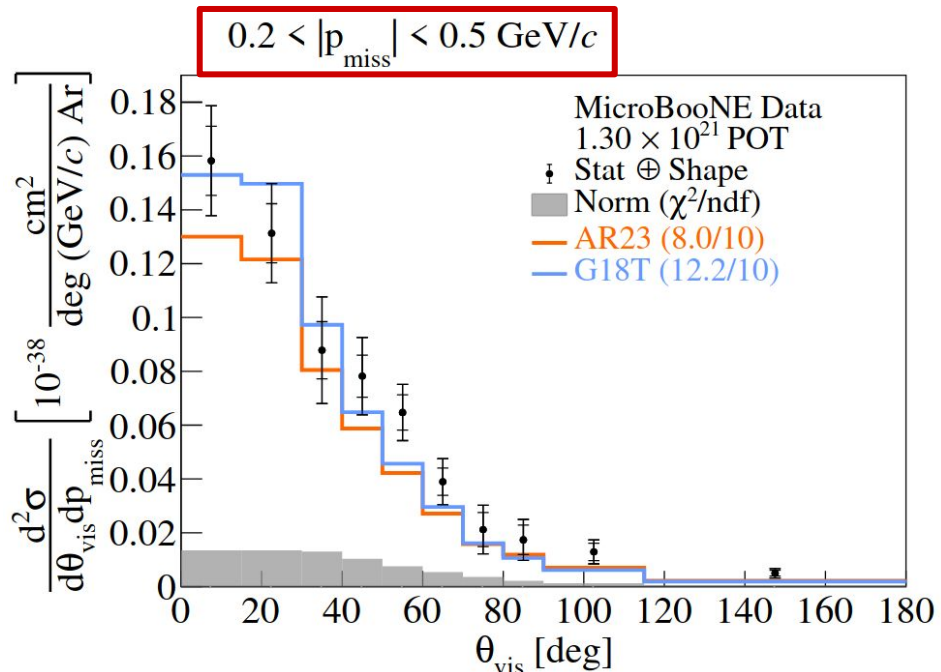
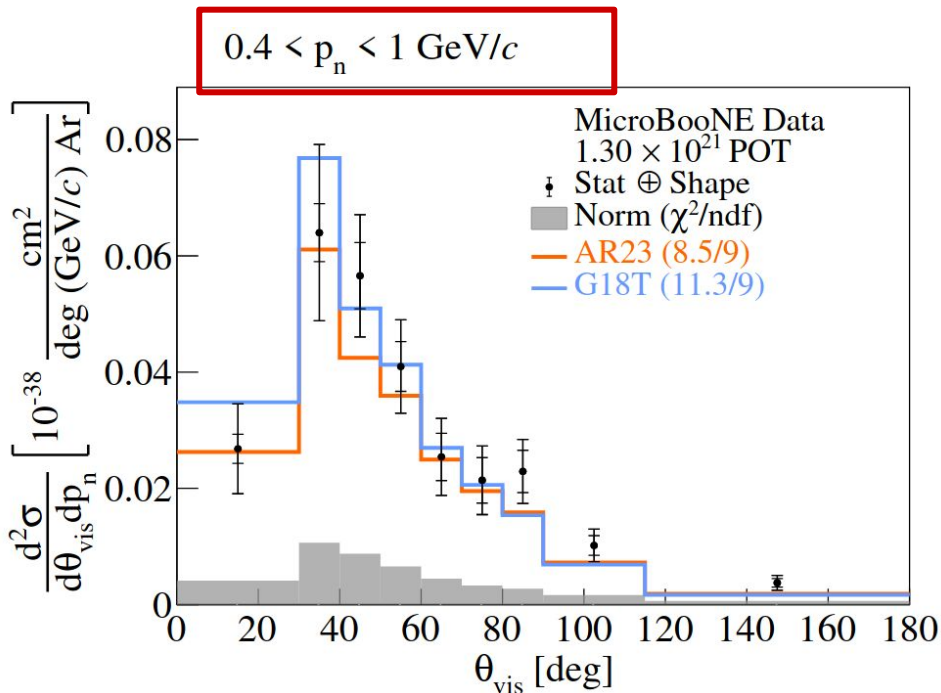
AR23 yields a systematically lower prediction across

However, no QE tune is included in the AR23 prediction ( $\sim 20\%$  effect)



# Comparison to DUNE model

AR23 yields a slightly lower prediction but within uncertainties

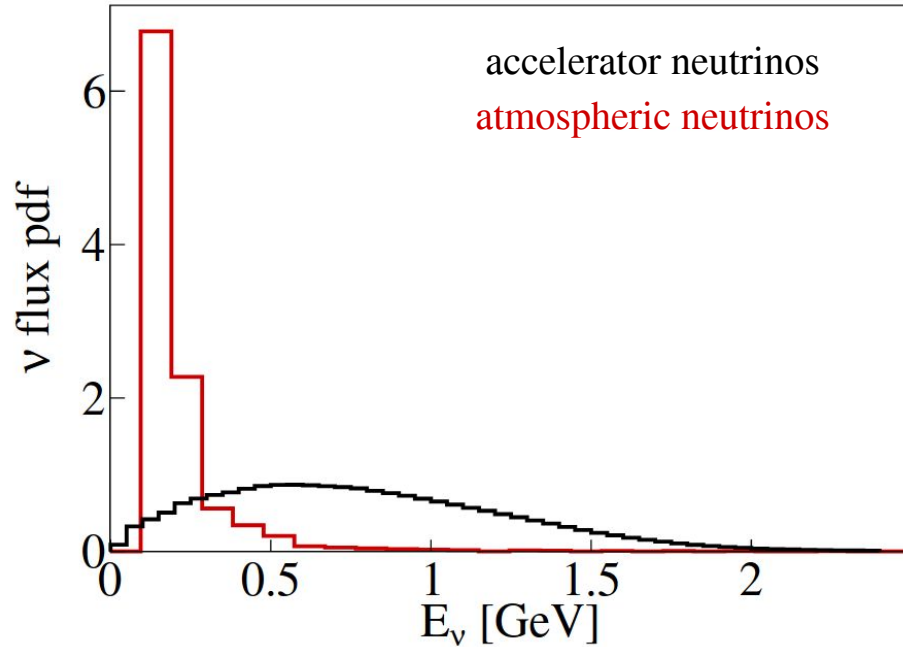


# DUNE projection

What should we expect?

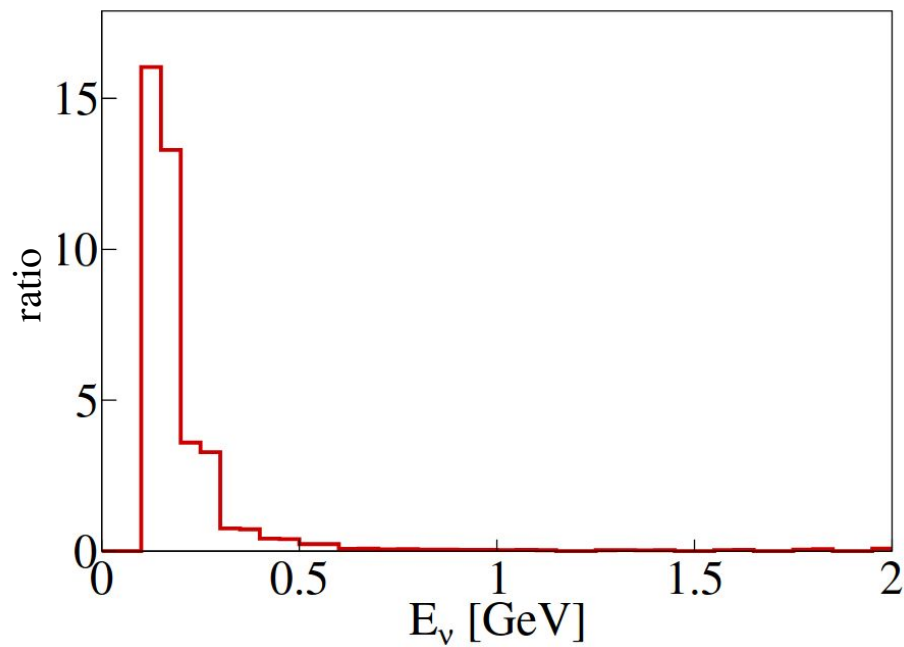
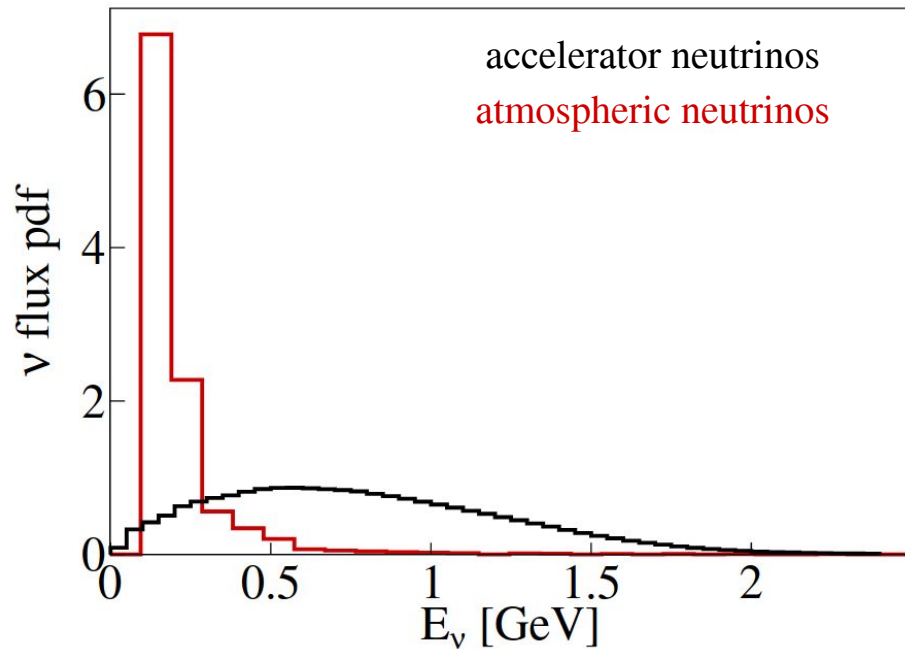
# DUNE projection

Using flux probability distribution functions (pdf) ratio to obtain a reweighting function



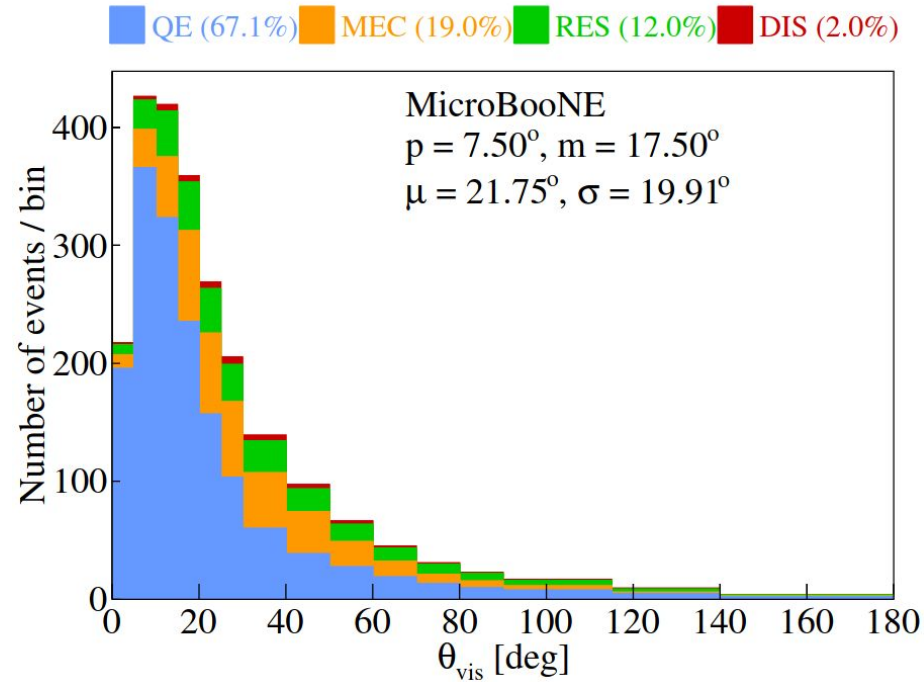
# DUNE projection

Using flux probability distribution functions (pdf) ratio to obtain a reweighting function



# DUNE projection

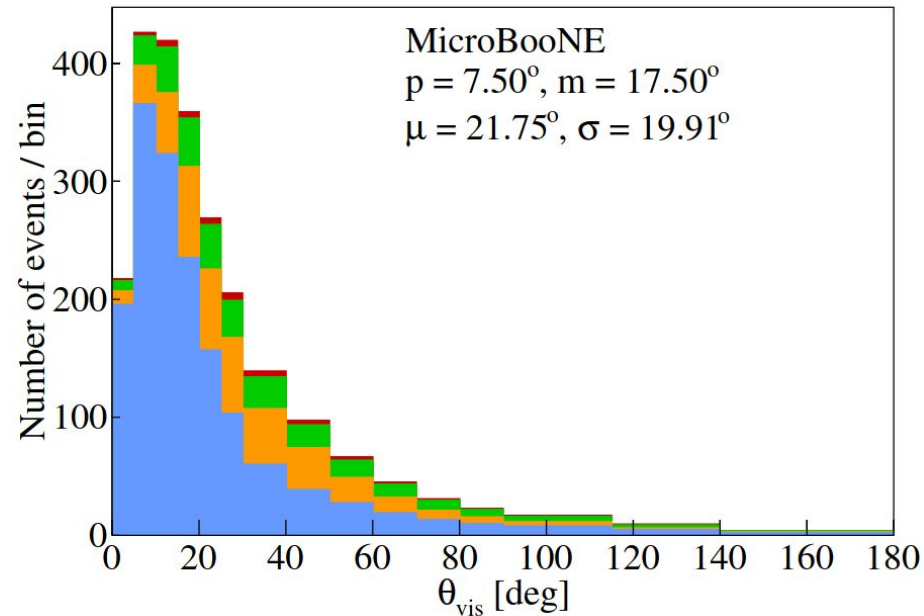
Using the reweighting function on the previous slide to reweight events on an event-by-event basis as a function of the neutrino energy, we make a projection for DUNE



# DUNE projection

Using the reweighting function on the previous slide to reweight events on an event-by-event basis as a function of the neutrino energy, we make a projection for DUNE

QE (67.1%) MEC (19.0%) RES (12.0%) DIS (2.0%)



QE (85.0%) MEC (10.5%) RES (3.9%) DIS (0.6%)

