

# Charmless Hadronic B decays from Belle

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## □ Introduction

## □ Study of

➤  $B^\pm \rightarrow K^+ K^- \pi^\pm$

PRD **96**, 031101 (2017)

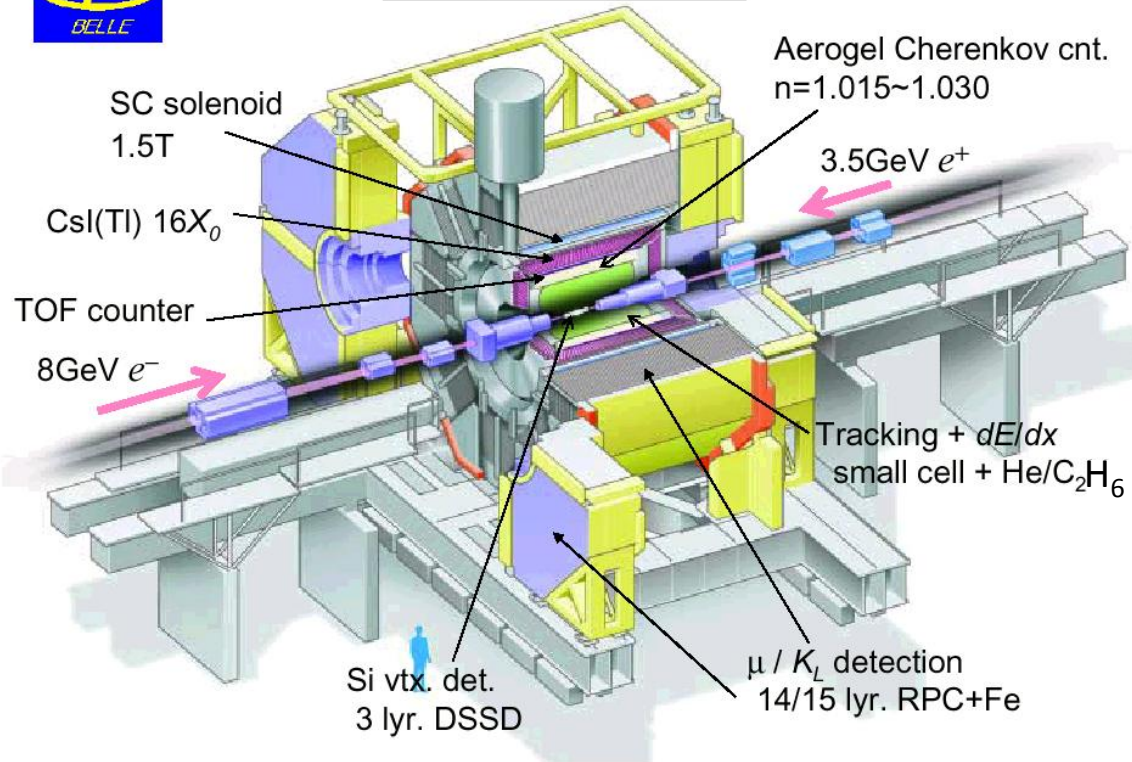
➤  $B^0 \rightarrow \pi^0 \pi^0$

PRD **96**, 032007 (2017)

## □ Summary



## Belle Detector



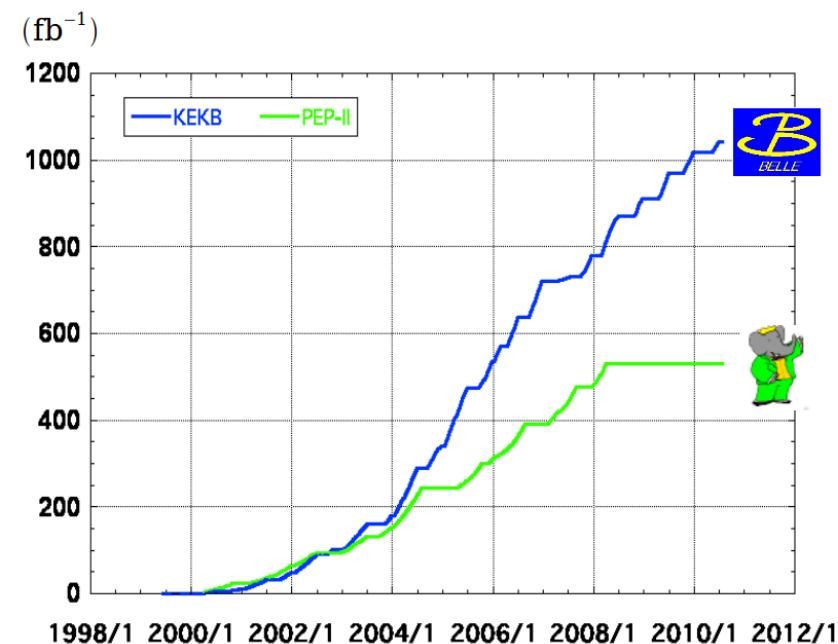
☐ Recorded 772 million  $B\bar{B}$  pairs

☐ All analyses presented here are based on the full Belle data sample

☐ Operated at the KEKB collider in Tsukuba, Japan (1999 – 2010)

☐ Asymmetric beam energy at the  $\Upsilon(4S)$  resonance (8 GeV  $e^-$  on 3.5 GeV  $e^+$ )

## Integrated luminosity of B factories



**> 1 ab<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(5S)$ : 121  $\text{fb}^{-1}$   
 $\Upsilon(4S)$ : 711  $\text{fb}^{-1}$   
 $\Upsilon(3S)$ : 3  $\text{fb}^{-1}$   
 $\Upsilon(2S)$ : 25  $\text{fb}^{-1}$   
 $\Upsilon(1S)$ : 6  $\text{fb}^{-1}$   
**Off reson./scan:**  
 $\sim 100 \text{ fb}^{-1}$

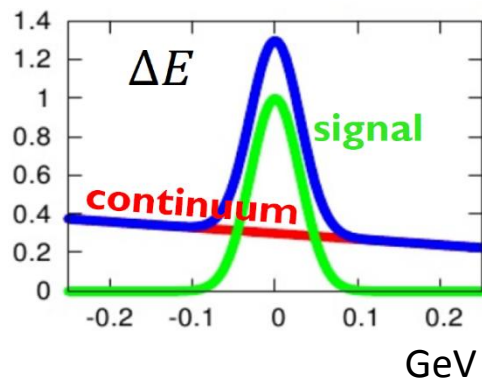
**$\sim 550 \text{ fb}^{-1}$**   
**On resonance:**  
 $\Upsilon(4S)$ : 433  $\text{fb}^{-1}$   
 $\Upsilon(3S)$ : 30  $\text{fb}^{-1}$   
 $\Upsilon(2S)$ : 14  $\text{fb}^{-1}$   
**Off resonance:**  
 $\sim 54 \text{ fb}^{-1}$

# Analysis Technique

□ To identify  $B$  decays, two kinematic variables are used:  $\Delta E$  and  $M_{bc}$

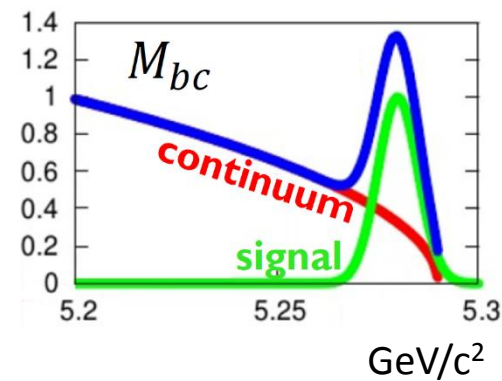
Energy difference

$$\Delta E = \sum_i E_i - E_{beam}$$



Beam-constrained mass

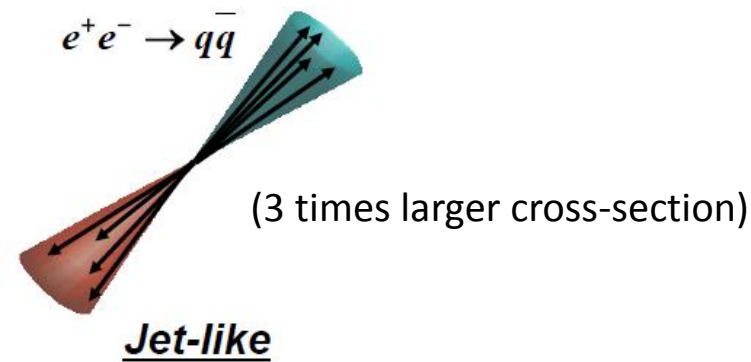
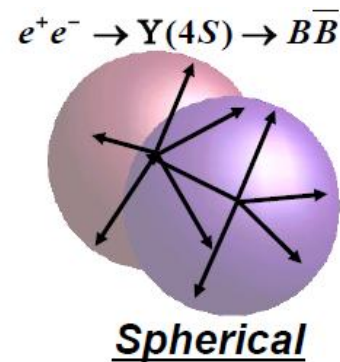
$$M_{bc} = \sqrt{E_{beam}^2 - |\sum_i \vec{p}_i|^2}$$



$p_i$  and  $E_i$  are the momentum and energy of  $i^{\text{th}}$  daughter of the reconstructed  $B$  meson in the CM frame

# Analysis Technique (contd.)

- Continuum events are the primary source of background:  $e^+e^- \rightarrow q\bar{q}$  ( $q = u, d, s$  and  $c$ )  $\rightarrow$  fragmentation  $\rightarrow$  hadrons as two back-to-back jets
- To suppress this background, variables describing the event shape topology are combined in a multivariate analyzer, such as a neural network (NN) or a Fisher discriminant



- Use an unbinned extended maximum likelihood (ML) fit based on different discriminating variables
- The fit usually includes signal, continuum, charm and charmless B background components

# $B^\pm \rightarrow K^+ K^- \pi^\pm$

☐ Mainly proceeds via  $b \rightarrow u$  tree and  $b \rightarrow d$  penguin diagrams

☐ No intermediate state observed yet

☐ Previous measurements:

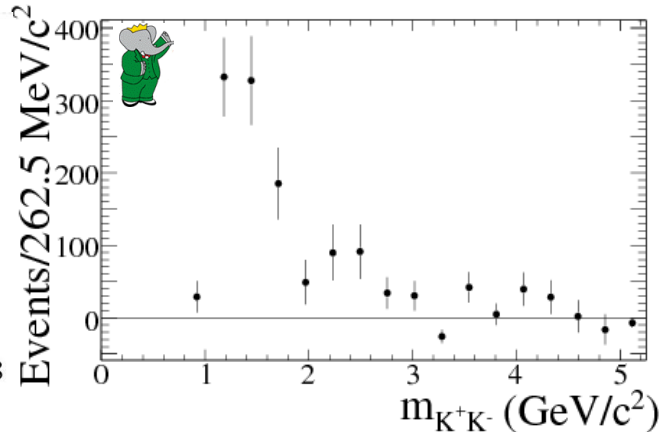
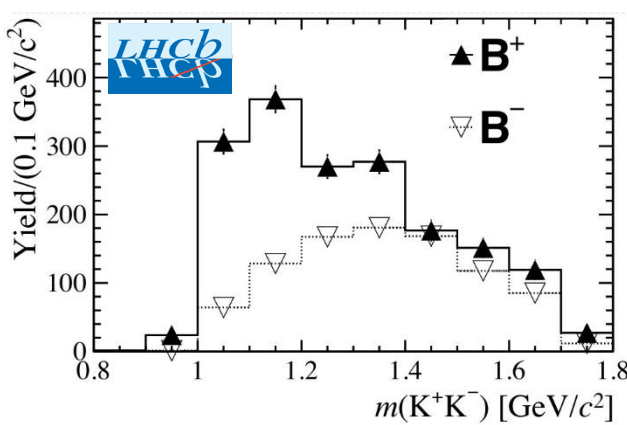
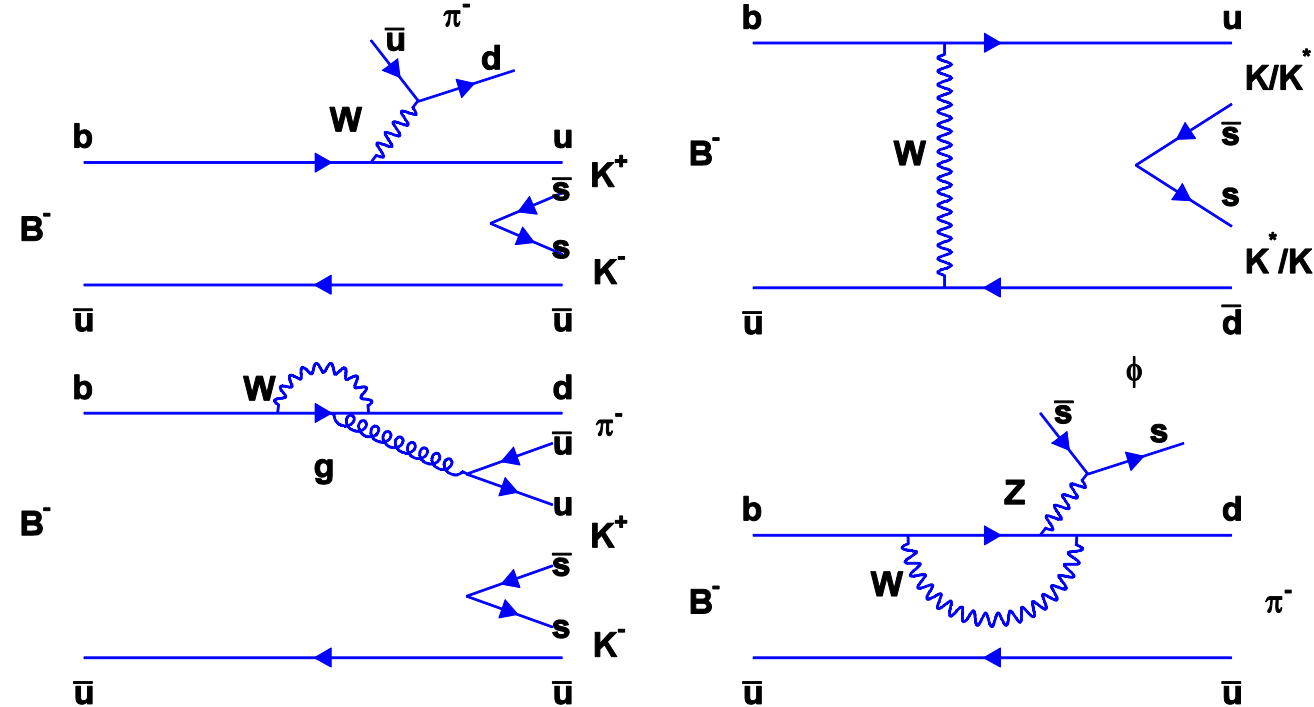
$$BF(B^\pm \rightarrow K^+ K^- \pi^\pm) = (5.0 \pm 0.5 \pm 0.5) \times 10^{-6}$$

PRL 99, 221801 (2007)



$$A_{CP} = -0.123 \pm 0.017 \pm 0.012 \pm 0.007$$

PRD 90, 112004 (2014)



☐ A structure is seen by BaBar and LHCb in  $K^+ K^-$  low invariant mass spectrum of  $B^+ \rightarrow K^+ K^- \pi^+$  and a large local CP asymmetry in the same mass region

☐ Final state interactions may contribute to CP violation

PRD 89, 094013 (2014)

# $B^\pm \rightarrow K^+ K^- \pi^\pm$ : Backgrounds

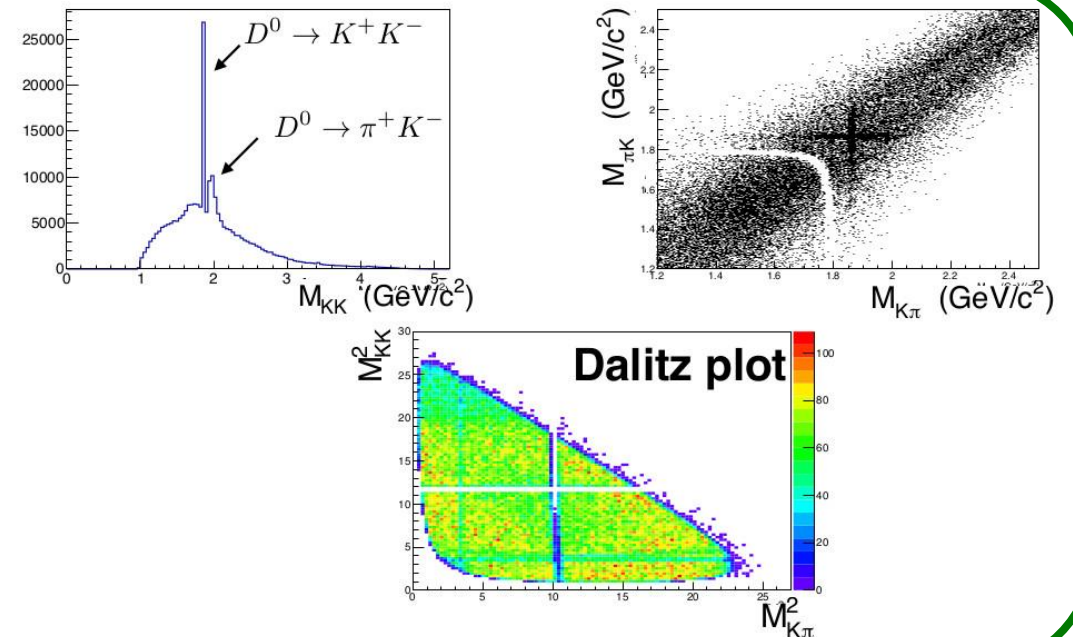
- ❑ Continuum background
- ❑ Continuum background suppression: Implement a NN based on 5 event-shape variables
- ❑ A tight requirement on NN removes 99% of the continuum events while retaining 48% of the signal

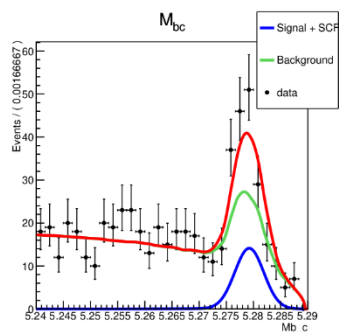
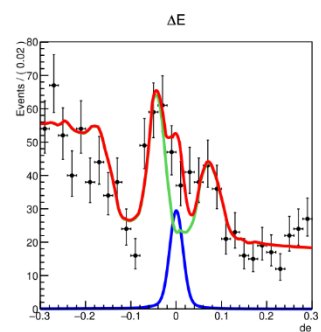
- ❑ Generic B background
- ❑ Arises due to B decays via the dominant  $b \rightarrow c$  transition
- ❑ Charm veto to reject  $b \rightarrow c$  backgrounds after investigating the  $K^+ K^-$  and  $K^+ \pi^-$

- ❑ Rare B background
- ❑ Arises due to B decays in which one of the B decays via  $b \rightarrow u, d, s$

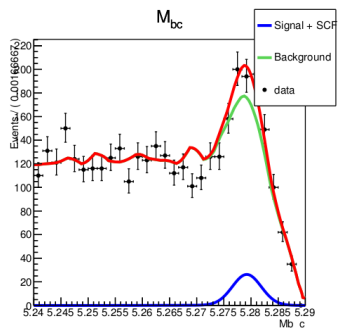
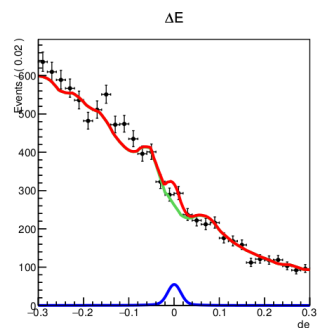
NN selection requirement is optimized by maximizing a figure of merit

$$\text{F. O. M} = \frac{N_S}{\sqrt{N_S + N_B}}$$



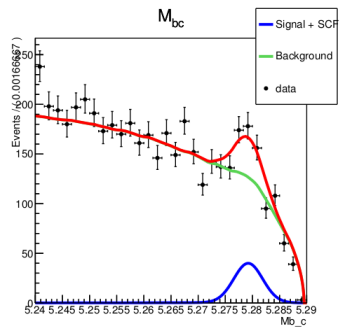
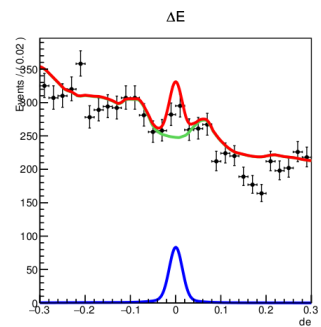


Bin0

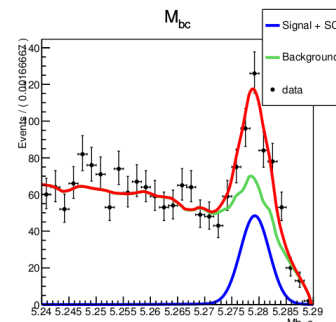
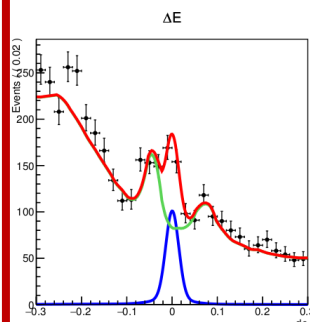


Bin1

Bin2



Bin4



Bin3

Signal enhanced projection plots



Fit components:  
Signal, continuum background, generic B background and rare B background

Signal and  $A_{CP}$  are fitted in  $M_{KK}$  bins

The overall results are obtained by integrating over the whole  $M_{KK}$  region

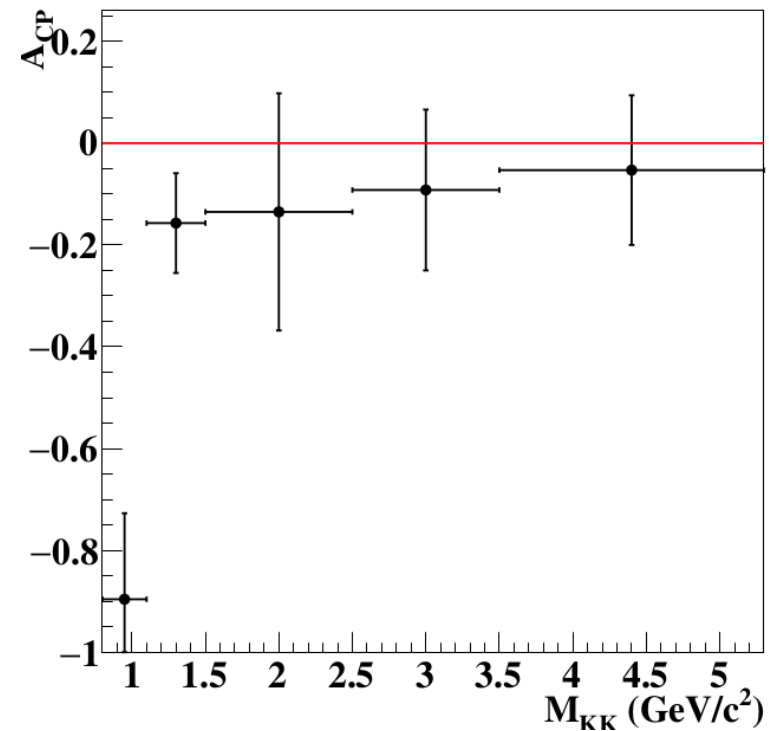
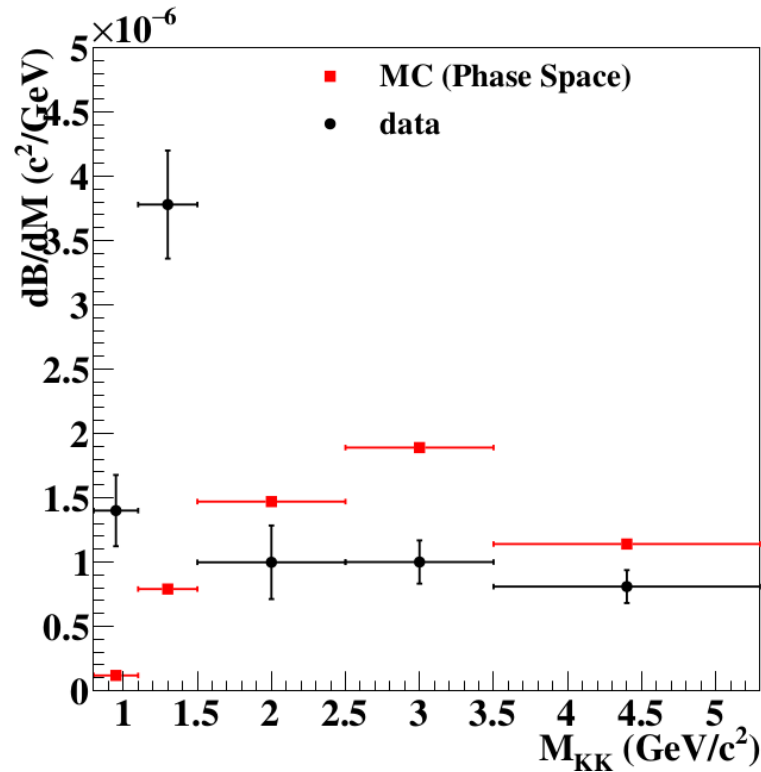
We obtain

Signal yield =  $715 \pm 48$



$$B^{\pm} \rightarrow K^{+} K^{-} \pi^{\pm}$$

- An excess and a large CP asymmetry are seen in  $M_{K^{+}K^{-}} < 1.5 \text{ GeV}/c^2$ , confirming the observations by BaBar and LHCb
- We find a strong evidence of a large CP asymmetry of  $-0.90 \pm 0.17 \pm 0.03$  with  $4.8\sigma$  significance for  $M_{K^{+}K^{-}} < 1.1 \text{ GeV}/c^2$



$$B^{\pm} \rightarrow K^{+}K^{-}\pi^{\pm}$$

$M_{K^{+}K^{-}}$ (GeV/c <sup>2</sup> )	$N_{\text{sig}}$	Efficiency (%)	dBF/dM (x10 <sup>-7</sup> )	$A_{\text{CP}}$
0.8-1.1	59.8±11.4±2.6	19.7	14.0±2.7±0.8	-0.90±0.17±0.04
1.1-1.5	212.4±21.3±6.7	19.3	37.8±3.8±1.9	-0.16±0.10±0.01
1.5-2.5	113.5±26.7±18.6	15.6	10.0±2.3±1.7	-0.15±0.23±0.03
2.5-3.5	110.1±17.6±4.9	15.1	10.0±1.6±0.6	-0.09±0.16±0.01
3.5-5.3	172.6±25.7±7.4	16.3	8.1±1.2±0.5	-0.05±0.15±0.01

□ Overall BF and  $A_{\text{CP}}$

$$\text{BF}(B^{+} \rightarrow K^{+}K^{-}\pi^{+}) = (5.38 \pm 0.40 \pm 0.35) \times 10^{-6}$$

$$A_{\text{CP}} = -0.182 \pm 0.071 \pm 0.016$$

# $B^0 \rightarrow \pi^0 \pi^0$

- Proceeds via  $b \rightarrow u$  tree and  $b \rightarrow d$  penguin diagrams
- Time dependent measurements of  $B \rightarrow \pi\pi$  are sensitive to the UT angle  $\phi_2/\alpha$
- Among the  $B \rightarrow \pi\pi$  decays,  $BF$  and  $A_{CP}$  for  $B^0 \rightarrow \pi^0\pi^0$  are the least well determined
- Previous measurements:

$$BF = \left( 2.3 \begin{array}{cc} +0.4 & +0.2 \\ -0.5 & -0.3 \end{array} \right) \times 10^{-6} \quad \text{BELLE} \quad (275 \times 10^6 \text{ B}\bar{\text{B}})$$

PRL **94**, 181803 (2005)

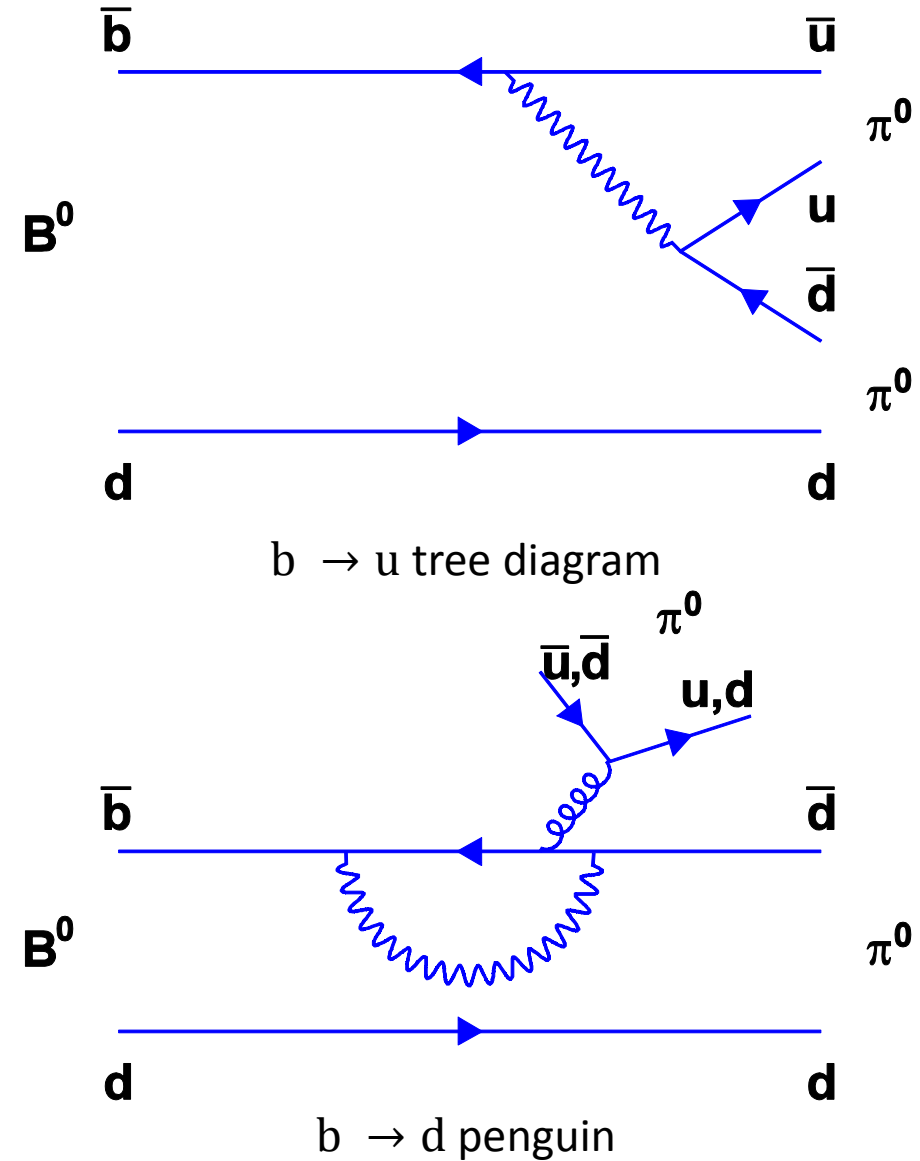
$$BF = (1.83 \pm 0.21 \pm 0.13) \times 10^{-6} \quad \text{BABAR} \quad (467 \times 10^6 \text{ B}\bar{\text{B}})$$

PRD **87**, 052009 (2013)

- Theory: quantum chromodynamics based factorization predicts  $BF$  below  $1 \times 10^{-6}$

PRD **73**, 114014 (2006)

PRD **83**, 034023 (2011)



$$B^0 \rightarrow \pi^0 \pi^0$$

□ 3D fit to  $\Delta E$ ,  $M_{bc}$  and  $T_c$  (continuum suppression variable) with four components:

- Signal
- Continuum background
- $B^+ \rightarrow \rho^+ \pi^0$
- Other rare charmless

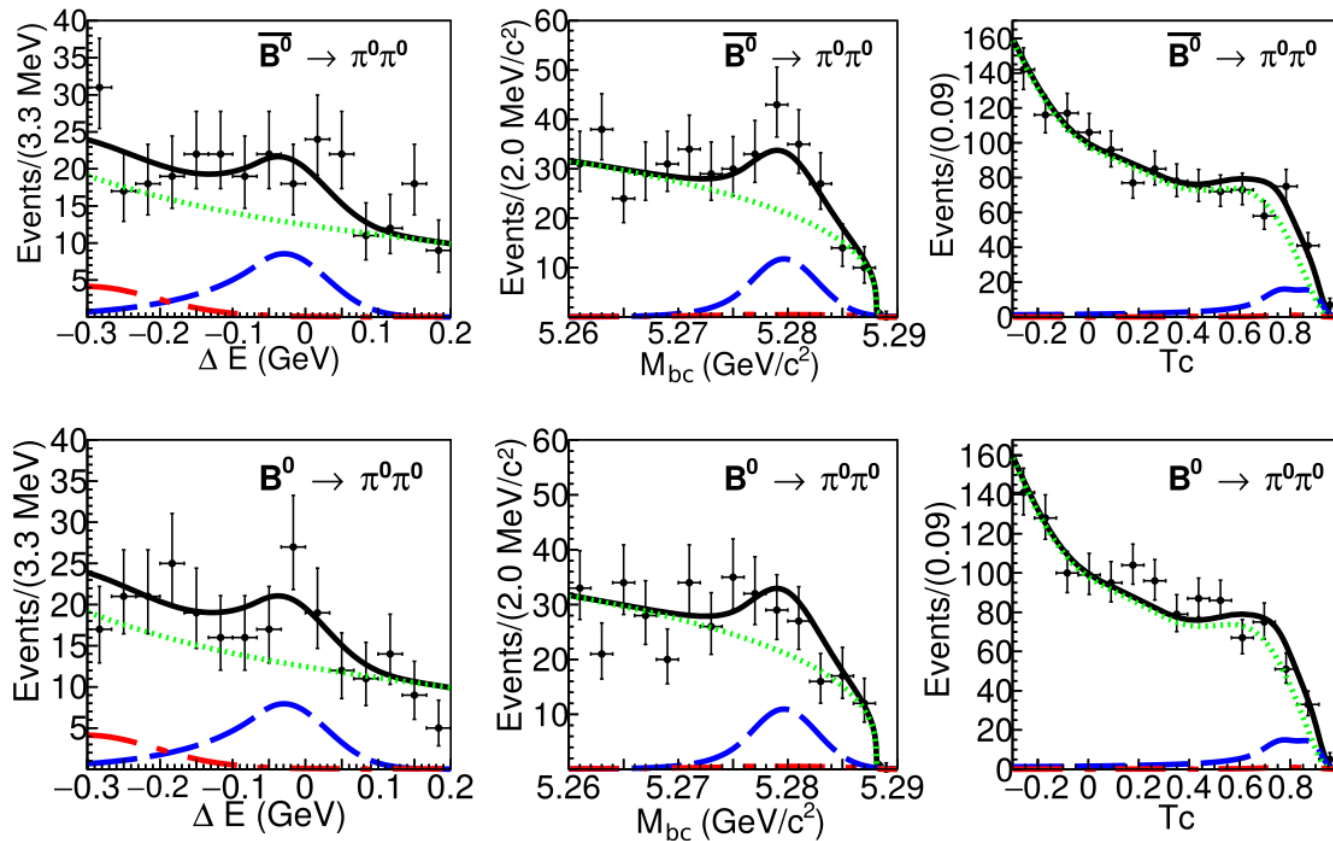
- $b$  –flavor charge  $q$ :  
[+1(−1) tagging a  $B^0(\bar{B}^0)$ ]
- $r$ : purity

□ Simultaneous fit to 14 bins in the flavor tagging variable ( $q \cdot r$ ) for SVD1 (2)

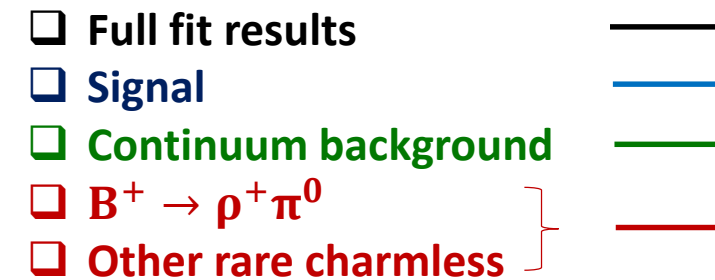
□  $T_c$ : Fisher discriminant of likelihood (Fox-Wolfram moments), cosine of the polar angle of the B candidate with respect to the z axis and cosine of the angle between the thrust axis of the B candidate and rest of the event in the CM frame

$$B^0 \rightarrow \pi^0 \pi^0$$

Signal enhanced projection plots



- Data are points with error bars



Signal yield =  $217 \pm 32$

$$\text{BF}(B^0 \rightarrow \pi^0 \pi^0) = (1.31 \pm 0.19 \pm 0.18) \times 10^{-6}$$

$$A_{\text{CP}} = +0.14 \pm 0.36 \pm 0.12$$

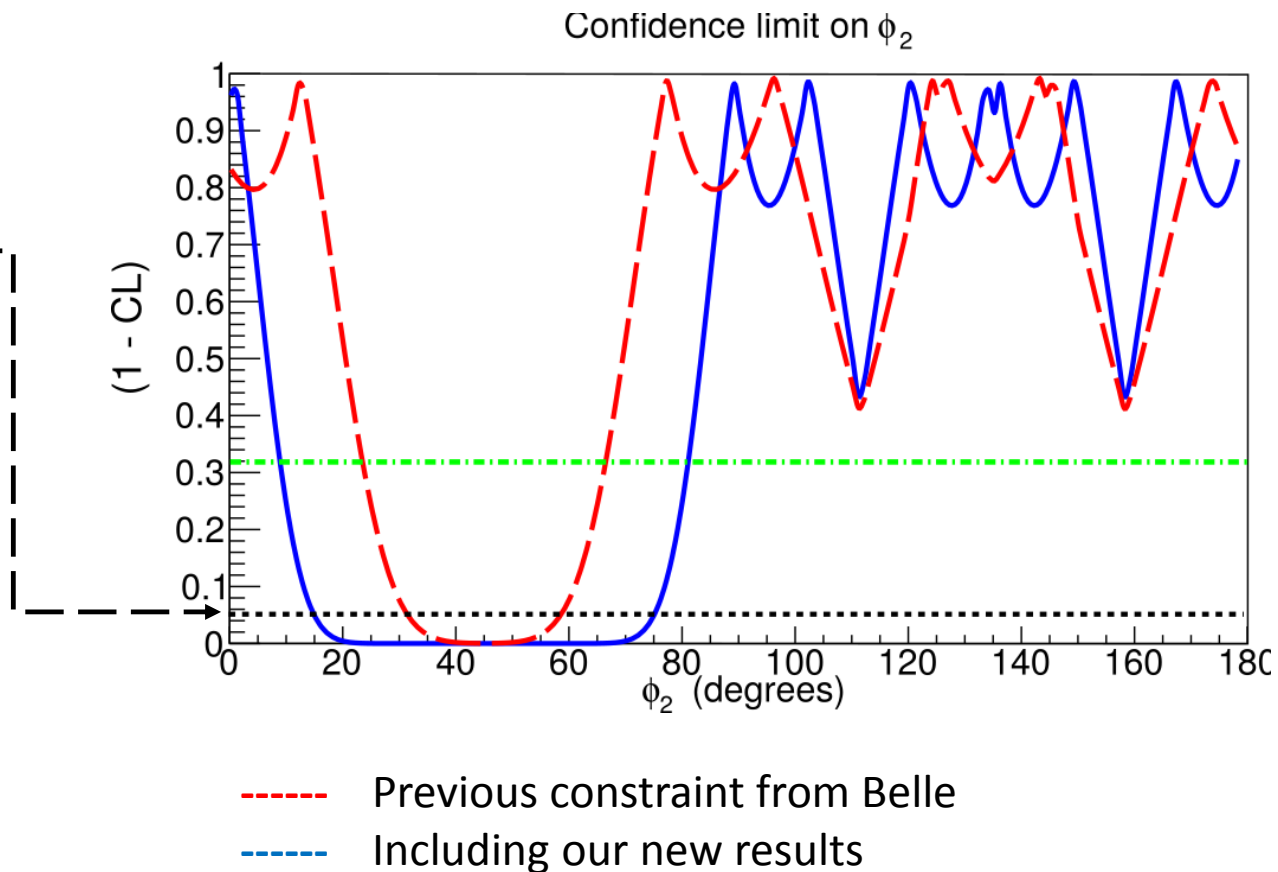
$$B^0 \rightarrow \pi^0 \pi^0$$

PRD **87**, 031103 (2012)

- BF and  $A_{CP}$  results for  $B^0 \rightarrow \pi^0 \pi^0$  are combined with previous Belle results on  $B^0 \rightarrow \pi^+ \pi^-$  and  $B^+ \rightarrow \pi^+ \pi^0$  to constrain  $\phi_2$  employing isospin relations

PRL **65**, 3381 (1990)PRD **88**, 092003 (2013)

- We exclude the CP violating parameter  $\phi_2$  from the range  $15.5^\circ < \phi_2 < 75^\circ$  at 95% confidence level

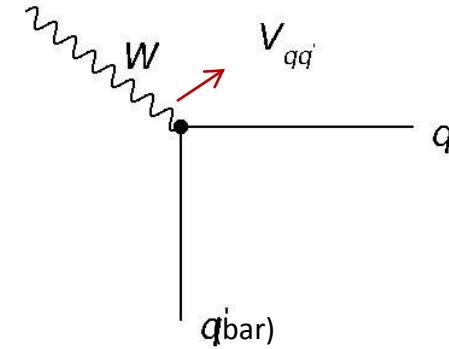
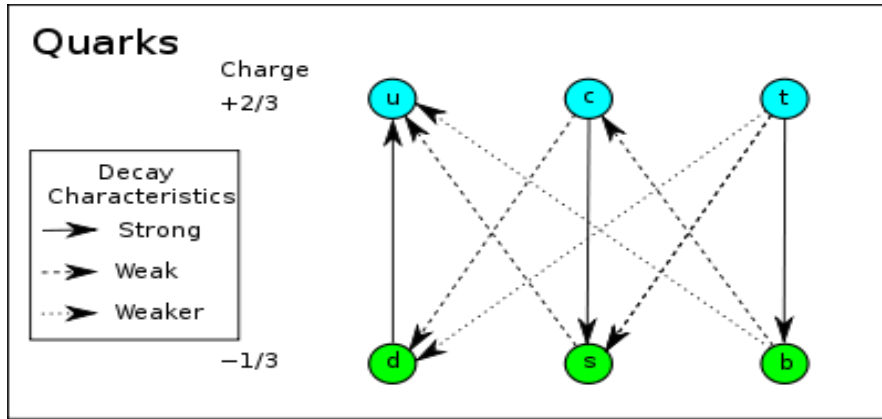


# Summary

- ❑ Measured BF ( $B^+ \rightarrow K^+ K^- \pi^+$ ) is  $(5.38 \pm 0.40 \pm 0.35) \times 10^{-6}$
- ❑  $A_{CP} = -0.182 \pm 0.071 \pm 0.016$
- ❑ An excess and a large CP asymmetry are seen in  $M_{K^+ K^-} < 1.5 \text{ GeV}/c^2$ , confirming the observations by BaBar and LHCb
- ❑ We find a strong evidence of a large CP asymmetry of  $-0.90 \pm 0.17 \pm 0.03$  with  $4.8\sigma$  significance for  $M_{K^+ K^-} < 1.1 \text{ GeV}/c^2$
  
- ❑ Measured BF ( $B^0 \rightarrow \pi^0 \pi^0$ ) is  $(1.31 \pm 0.19 \pm 0.18) \times 10^{-6}$  ( $6.4\sigma$ )
- ❑  $A_{CP} = +0.14 \pm 0.36 \pm 0.12$
- ❑ We exclude the CP violating parameter  $\phi_2$  from the range  $15.5^\circ < \phi_2 < 75^\circ$  at 95% confidence



# Introduction to CKM matrix



- ❖ CKM matrix describes the probability of a transition from one quark  $i$  to another quark  $j$ . These transitions are proportional to  $|V_{ij}|^2$
- ❖  $3 \times 3$  Unitarity matrix  $\Rightarrow$  4 independent parameters (1 irreducible phase)

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

## Wolfenstein parameterization

$$V_{CKM} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} \quad \text{Unitarity } V^\dagger V = 1$$

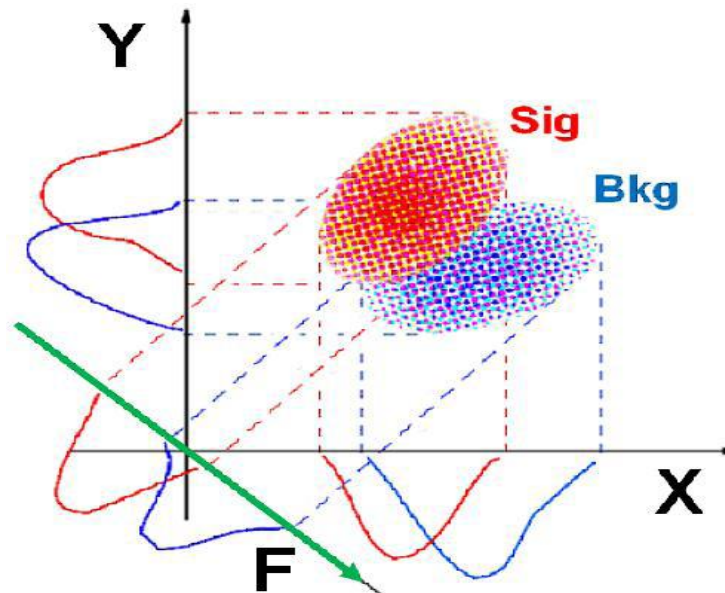
$$\lambda = 0.22, A = 0.81, \rho = 0.14 \text{ and } \eta = 0.35$$



# Fisher Discriminant

The variable: 
$$F = \sum_{i=1}^N \alpha_i x_i$$

1. The discriminant  $F$  is a linear combination of the input variables  $x_i$  (such as FW moments)
2. Multi variables can be combined into a single variable
3. Project multi dimensional data onto one dimension (axis)
4. Find the axis (best set of  $\alpha_i$ ) to separate signal and background maximally



## Fox Wolfram moments

$$H_l = \sum_{ij} |p_i| |p_j| P_l(\cos \theta_{ij})$$

The diagram illustrates the components of the Fox-Wolfram moment equation. Red arrows point from text boxes below to the corresponding parts of the equation:

- i,j= particles** points to the summation index  $ij$ .
- Momentum of particle i and j** points to the momentum vectors  $p_i$  and  $p_j$ .
- Legendre polynomial** points to  $P_l(\cos \theta_{ij})$ .
- Angle between particle i and j** points to the angle  $\theta_{ij}$ .