



Radiative Corrections and Universal Extra Dimensions

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Fig.1 A multi-loop correction to a tree

The Why, the What and the How

○ the Why

- Universal Extra Dimensions (UED) is an attractive new physics model
- **KK-Parity** leads to stable dark matter candidate

○ the What

Radiative corrections: ¹⁾

- Split the heavily degenerate **mass spectrum**/open up decay channels (leading Log not sufficient)
- Induce **KK-Number violating couplings** (old and new)

○ the How

- Sum over the an **infinite tower** of states for mass corrections
- The induced couplings do not require resummation but a cutoff

¹⁾ H. Cheng, K. Matchev, M. Schmaltz hep-ph/1702.00401

Universal Extra Dimensions (UED)

Universal Extra Dimensions:

- Assume five-dimensional spacetime manifold
- To explain four-dimensional world impose boundary conditions (Kaluza Klein Compactification/**Orbifolding**)

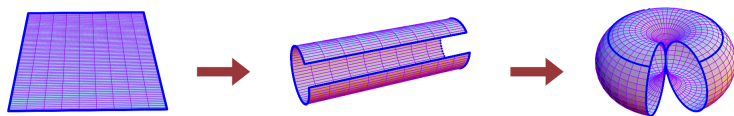
$$\Psi(x^\mu, y) = \Psi(x^\mu, y + 2\pi R)$$

(Current Limit: $M = \frac{1}{R} \geq 1400\text{GeV}$ with $\Lambda R \sim 10^{1,2,3}$ @LO)

$$\Psi(x^\mu, y) = \Psi(x^\mu, -y)$$

- Fields $\Psi(x^\mu, y)$ propagating can be decomposed into Fourier modes
- ψ_0 are the standard model modes, ψ_n a tower of additional (heavy) excitations of mass $M = \frac{n}{R}$

$$\Psi(x^\mu, y) = \frac{1}{\sqrt{\pi R}} \psi_0(x) + \sqrt{\frac{2}{\pi R}} \sum_{n=1}^{\infty} \psi_n(x) \cos \frac{ny}{R}$$

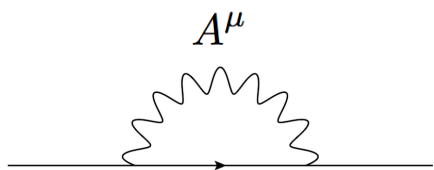
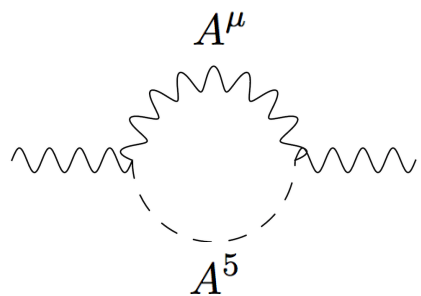
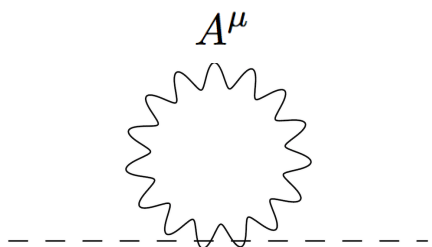


- 1) N. Deutschmann, T.Flacke, J. Kim hep-ph/1702.00401
- 2) K. Matchev, A.Datta et al hep-ph/1702.00413
- 3) ATLAS hep-ex/1501.03555

Instead of calculating 5D self-energies – try something different...

Mass Corrections (I)

...Using 4D EFT and **Poisson summation identity**:



$$\sum_{n=-\infty}^{\infty} \text{---} \left(\text{---} \Sigma_n \text{---} \right) \text{---}$$

Sum over KK-modes

$$= \sum_{k=-\infty}^{\infty} \mathcal{F} \left(\text{---} \left(\text{---} \Sigma_k \text{---} \right) \text{---} \right)$$

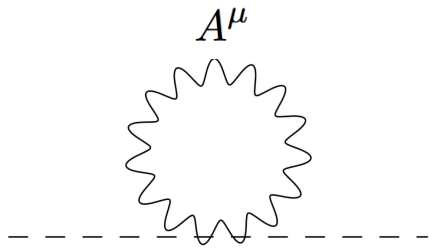
Sum over winding numbers
(formally infinite)

$$\mathcal{F}\{f\}(k) = \int dx f(x) e^{-2\pi i k x}$$

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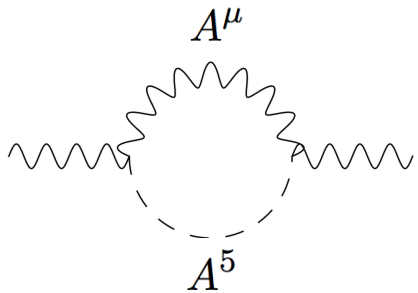
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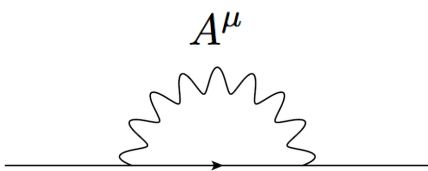
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Regularize by dropping the zero winding number, e.g.:

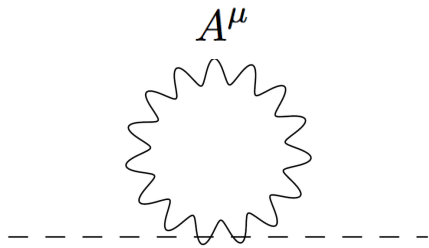
$$\sum_{n=0}^{\infty} A_o[n^2 M] = \frac{M^2}{2} \sum_{k=-\infty}^{\infty} \left[-\frac{\delta^2(k)}{4\pi^2} \left(\frac{1}{\epsilon} + 1 - \log \frac{M^2}{\mu^2} \right) - \frac{1}{2\pi^2 |k|^3} \right]$$



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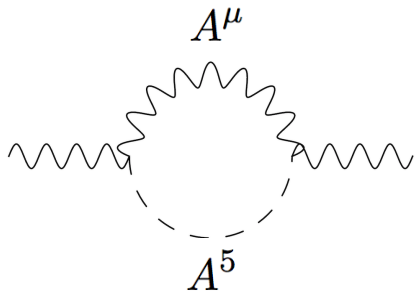
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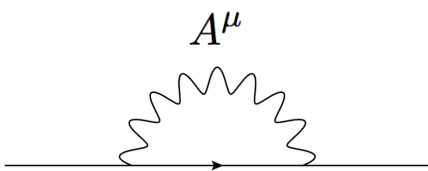
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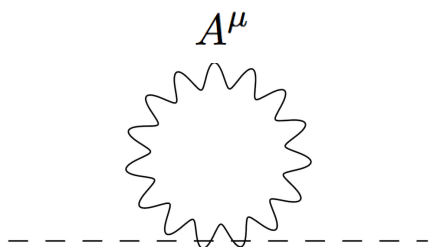
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which is contributing to the Bulk corrections.

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Mass Corrections (I)

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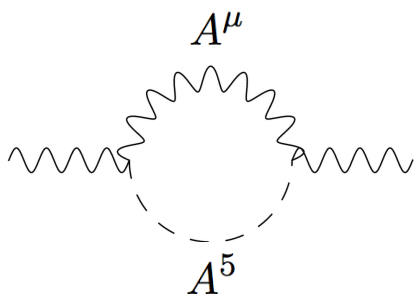
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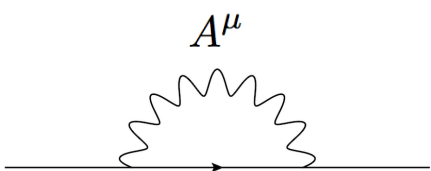
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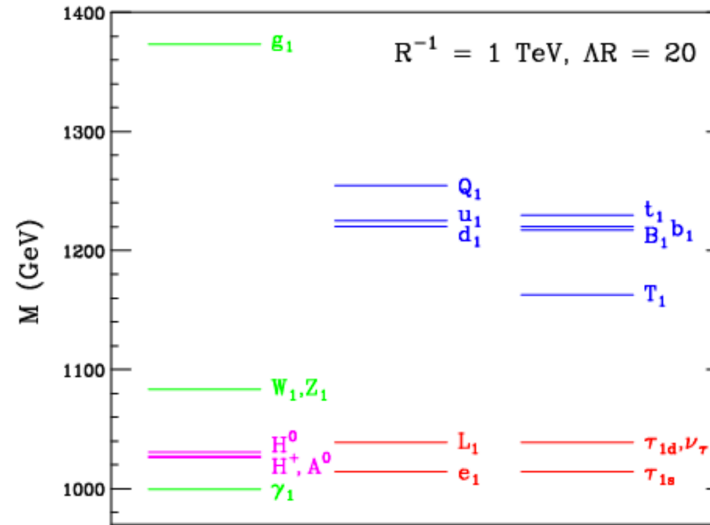
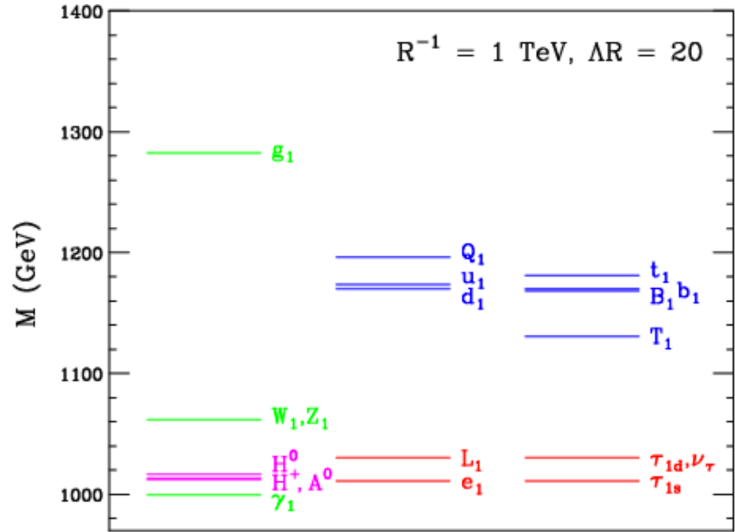
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which is contributing to the Bulk corrections.

The Brane corrections still require a \overline{MS}/EFT counterterm $\sim \frac{1}{\epsilon} + \log \frac{\Lambda^2}{\mu^2}$ ← Cutoff scale

Fig.2 n=1 mass spectrum leading log (left)
vs full one loop (right)

Mass Corrections (II)



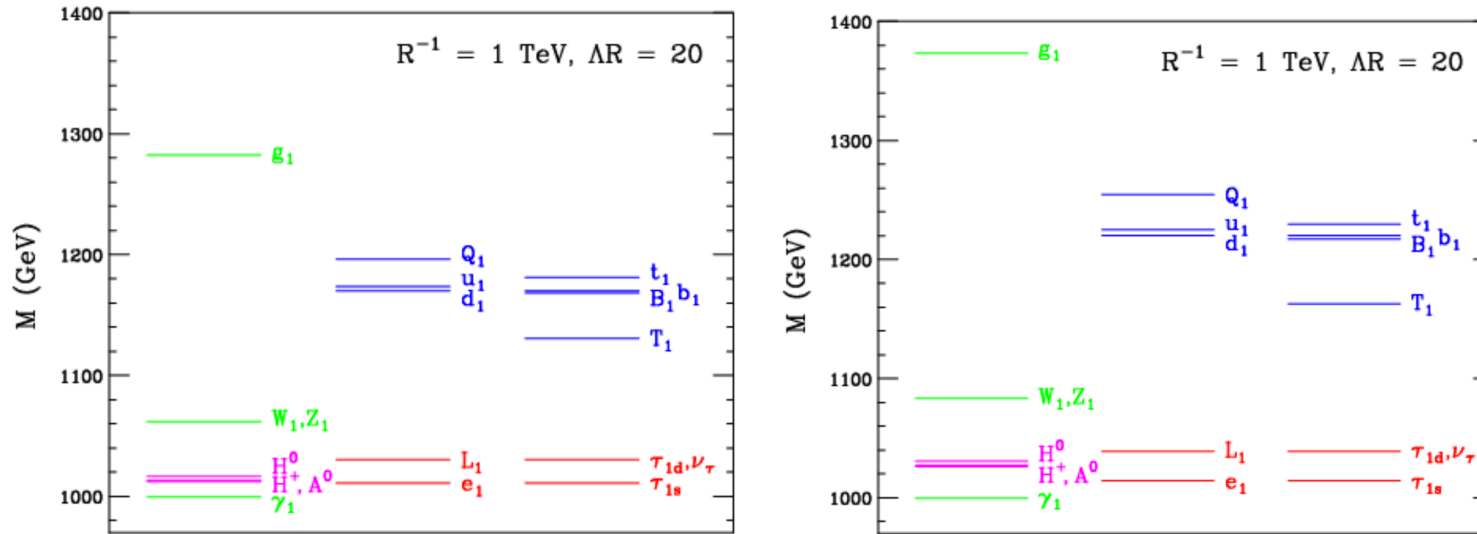
$$\delta M_{S_n}^2 = \text{Re}[\Sigma_n^S(p^2)] \Big|_{p^2=M_n^2}$$

$$\delta M_{V_n}^2 = -\text{Re}[\Sigma_n^T(p^2)] \Big|_{p^2=M_n^2}$$

$$\delta M_{F_n} = \frac{M_n}{2} \text{Re} \left[\begin{array}{c} \Sigma_n^L(M_n^2) + \Sigma_n^R(M_n^2) \\ + 2\Sigma_n^S(M_n^2) \end{array} \right]$$

Mass Corrections (II)

Fig.2 n=1 mass spectrum leading log (left) vs full one loop (right)



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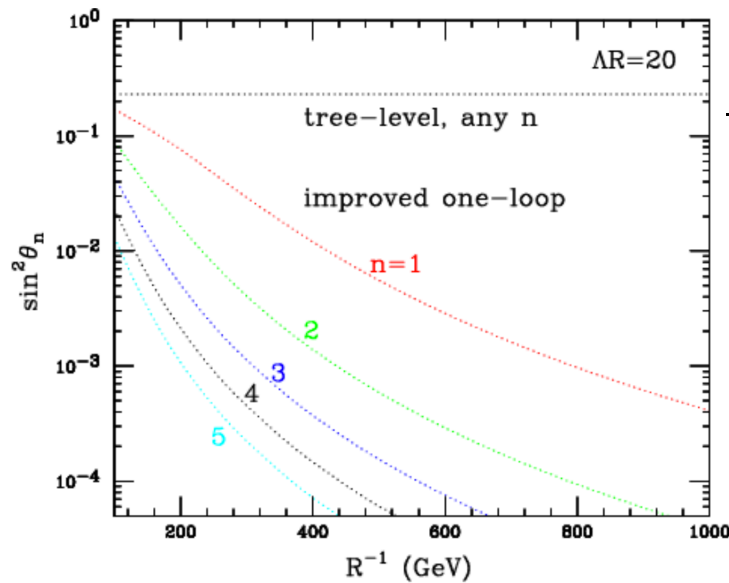


Fig.3 Weinberg mixing angle for higher modes

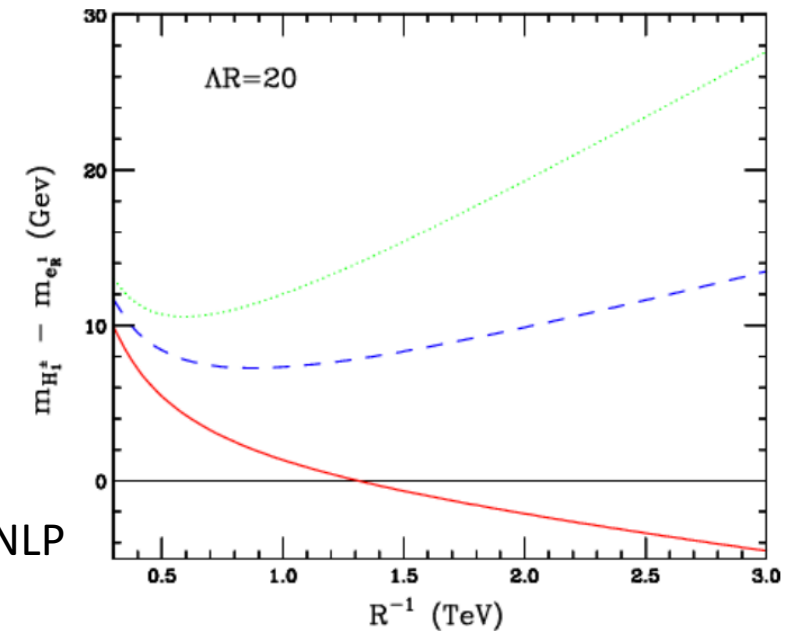
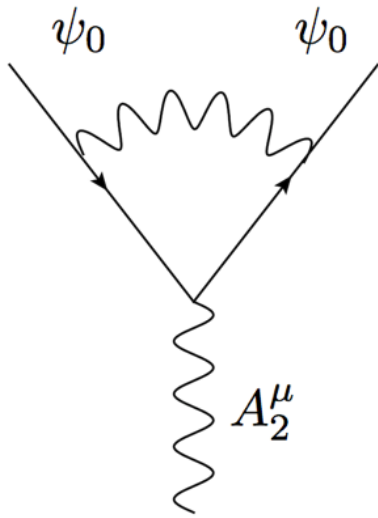


Fig.4 Higgs vs Lepton NLP

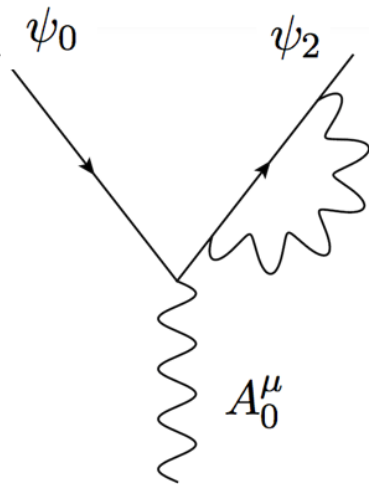
Vertex Corrections (I)

Old Couplings improved



$\log \Lambda^2 R^2$ -dependence \sim finite stuff!

$$\mathcal{L}_F \supset -igC_{200} \bar{\psi}_0 \gamma^\mu T^a \psi_0 A_{2\mu}^a$$



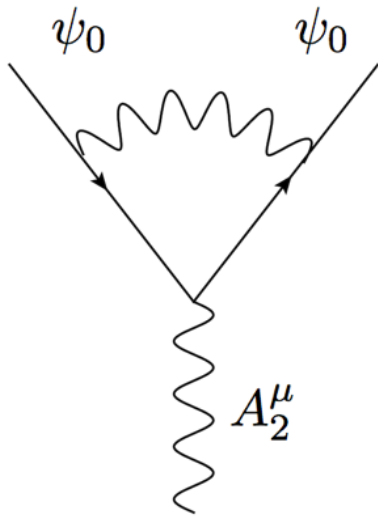
$$\mathcal{L}_{FD} \supset \underbrace{-igC_{020} \bar{\psi}_2 \gamma^\mu T^a \psi_0 A_{0\mu}^a}_{\text{Vector}} - \underbrace{igD_{020} \bar{\psi}_2 \sigma^{\mu\nu} T^a \psi_0 F_{0\mu\nu}^a}_{\text{Dipole}} + \text{h.c.}$$

Vector

Dipole

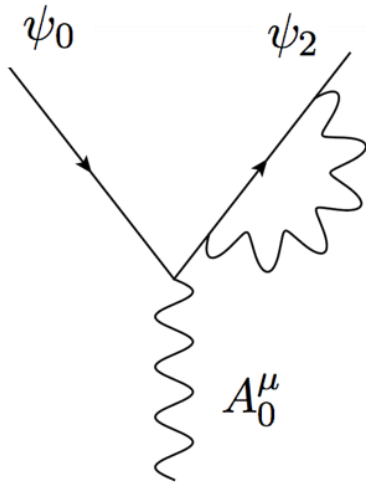
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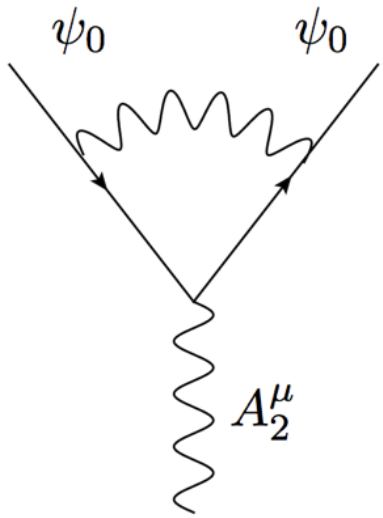
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Previously thought to be zero

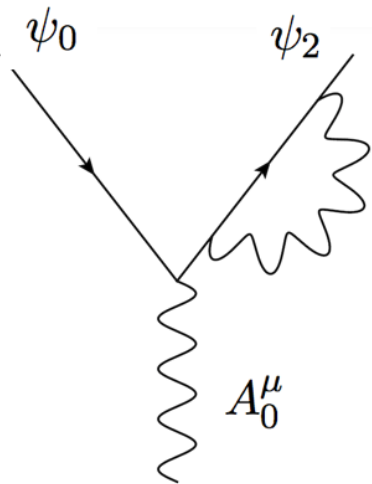
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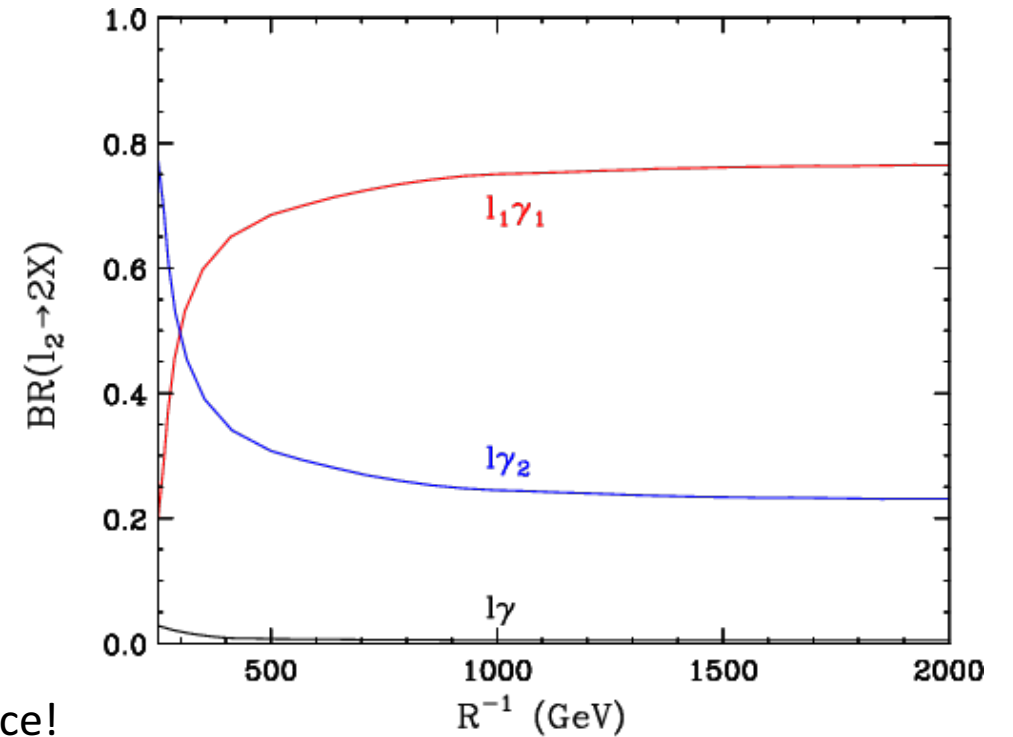
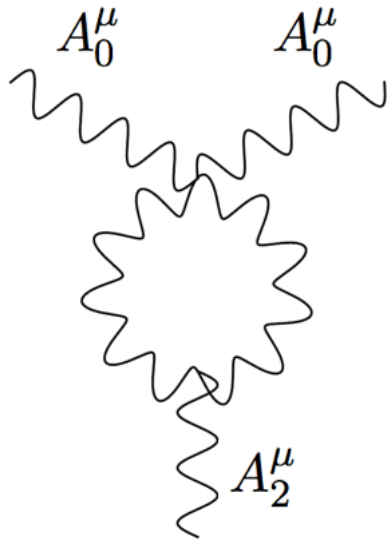


Fig.5 Lepton/NLKP decay width

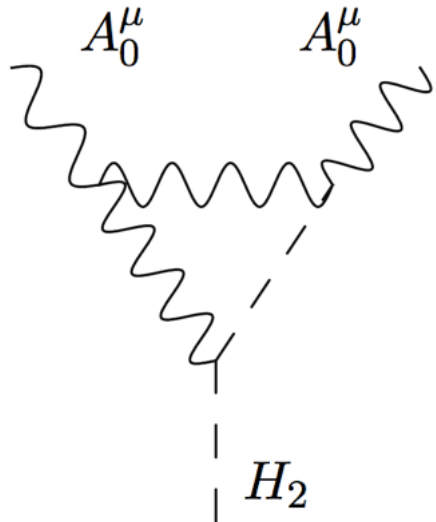
Vertex Corrections (II)

New couplings induced



$$\mathcal{L}_{3V} \supset \frac{\sqrt{2}C_{ijk}f^{abc}}{64\pi^2} [(\partial_\mu V_\nu^{a,i} - \partial_\nu V_\mu^{a,i})V^{\mu,b,j}V^{\nu,c,k}]$$

→ C_{ijk} is not cyclically symmetric! Non-Log terms violate **5D gauge invariance**

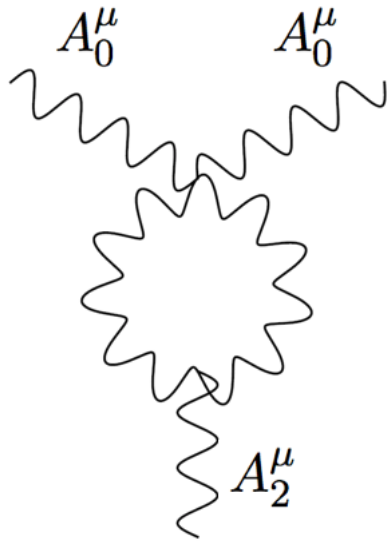


$$\mathcal{L}_{HVV} \supset \frac{iv\sqrt{2}C_{ij}}{64\pi^2 M^2} H_2 F_{\mu\nu}^i F^{i,\mu\nu}$$

→ No coupling to SM gluons for **CP-even** Higgs
→ **CP-odd** Higgs does

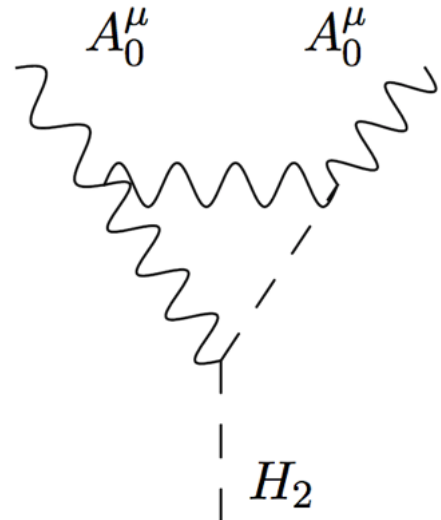
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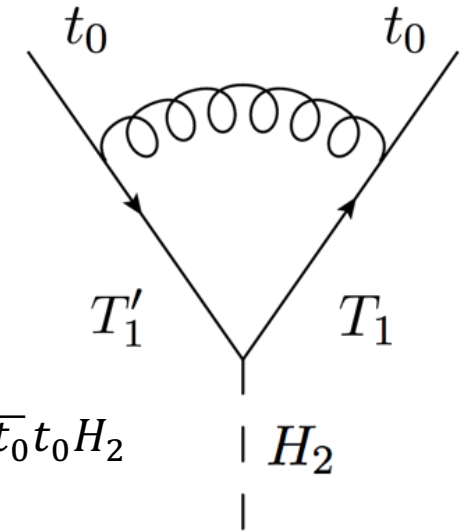
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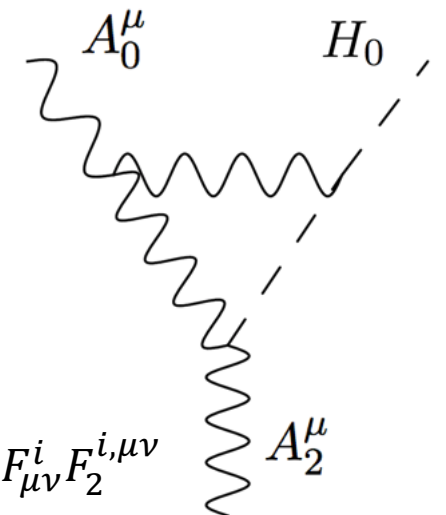
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$$\mathcal{L}_{HVV} \supset \frac{\sqrt{2}C_{ttH}}{64\pi^2} \bar{t}_0 t_0 H_2$$

$C_{ttH} \sim \mathcal{O}(\alpha_s)!$



$$\mathcal{L}_{VHV} \supset \frac{iv\sqrt{2}G_{ij}}{64\pi^2 M^2} H_0 F_{\mu\nu}^i F_2^{i,\mu\nu}$$

Decay Widths and Branching Ratios

A selection:

$$\frac{1}{R} = 1 \text{ TeV} \quad \Lambda R = 20$$

	$g_0 g_0$	$q_0 q_0$	$\bar{t}_0 t_0$	$Q_1 Q_1$
Gluon ₂	56%	34%	6%	4%

Tree-level decays

	$t_0 g_0$	$t_0 \gamma_0$	$t_1 \gamma_1$	$b_0 W_0^+$
Top ₂	78%	8%	12%	2%

	$\gamma_0 \gamma_0$	$\gamma_0 Z_0$	$Z_0 Z_0$	$W_0^+ W_0^-$	$\bar{t}_0 t_0$
Higgs ₂	2%	<1%	13%	24%	61%



(*Fine print: The branching ratios only contain a selection of decay channels so far!)

...and now what?

What we have:

- A fully **one-loop corrected mass spectrum** telling us which decay channels are open!
- A comprehensive collection of **n=2 KK-number violating Wilson coefficients** implemented in `CalcHep`

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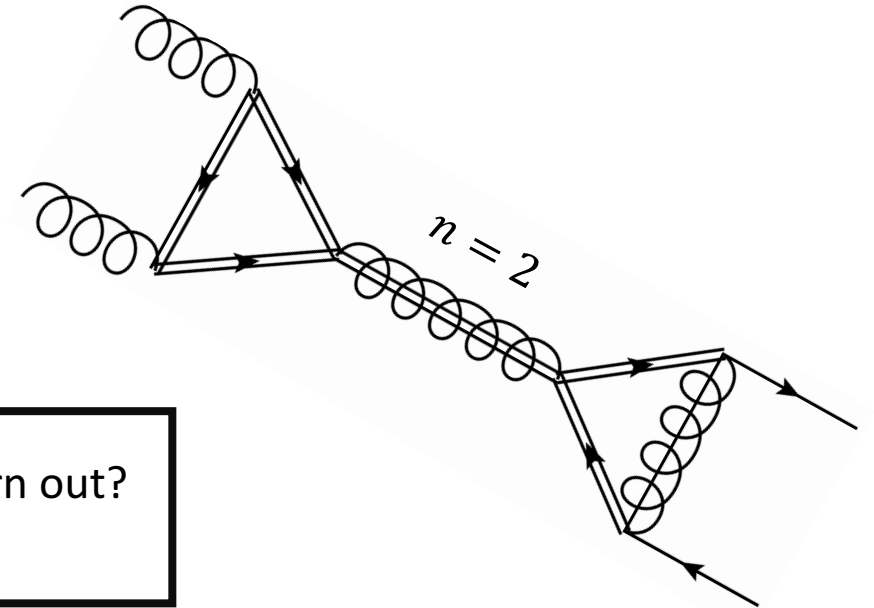
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Follow-up/Work in Progress:

- How about Collider signatures/limits?
- Implications for/from relic abundance?

How are Λ and R going to turn out?
Stay tuned!



Thanks!