



# Exclusive vector mesons at HERA

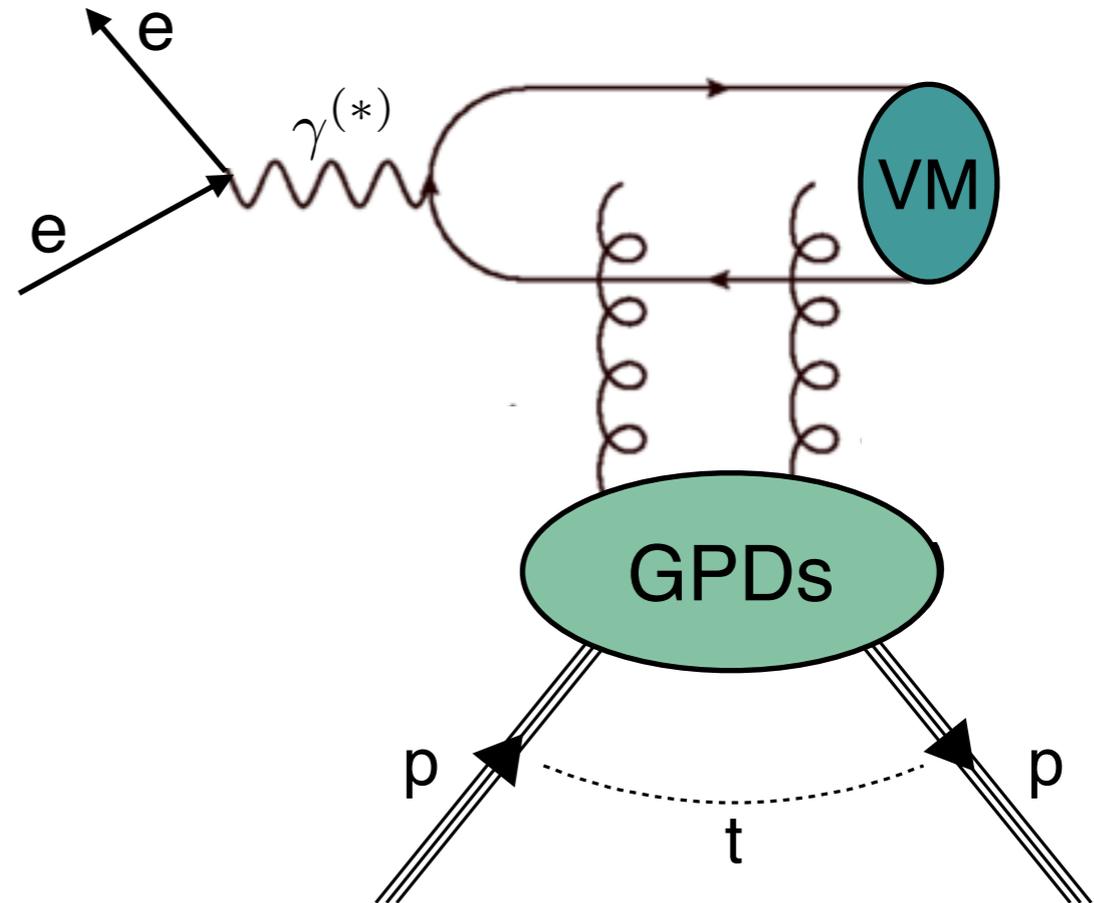
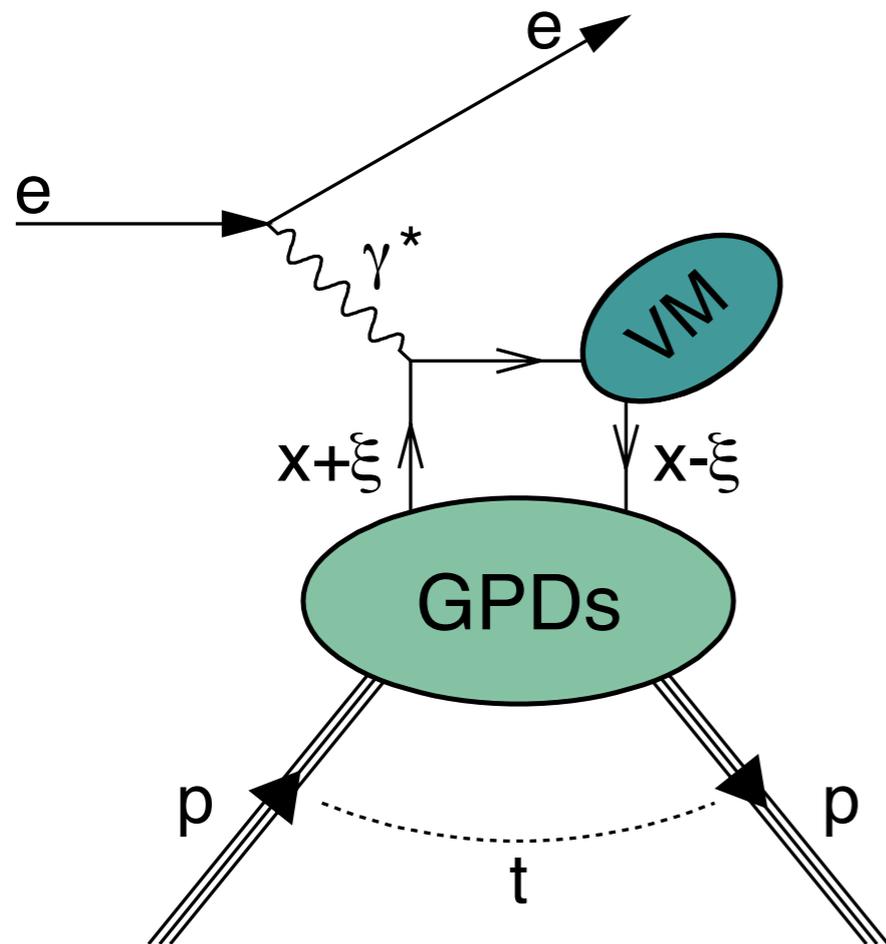
Charlotte Van Hulse  
University of the Basque Country – UPV/EHU

Next-generation GPD studies with exclusive meson production at EIC

Jun 4–6, 2018

CFNS, Stony Brook

# Exclusive vector-meson production at HERA



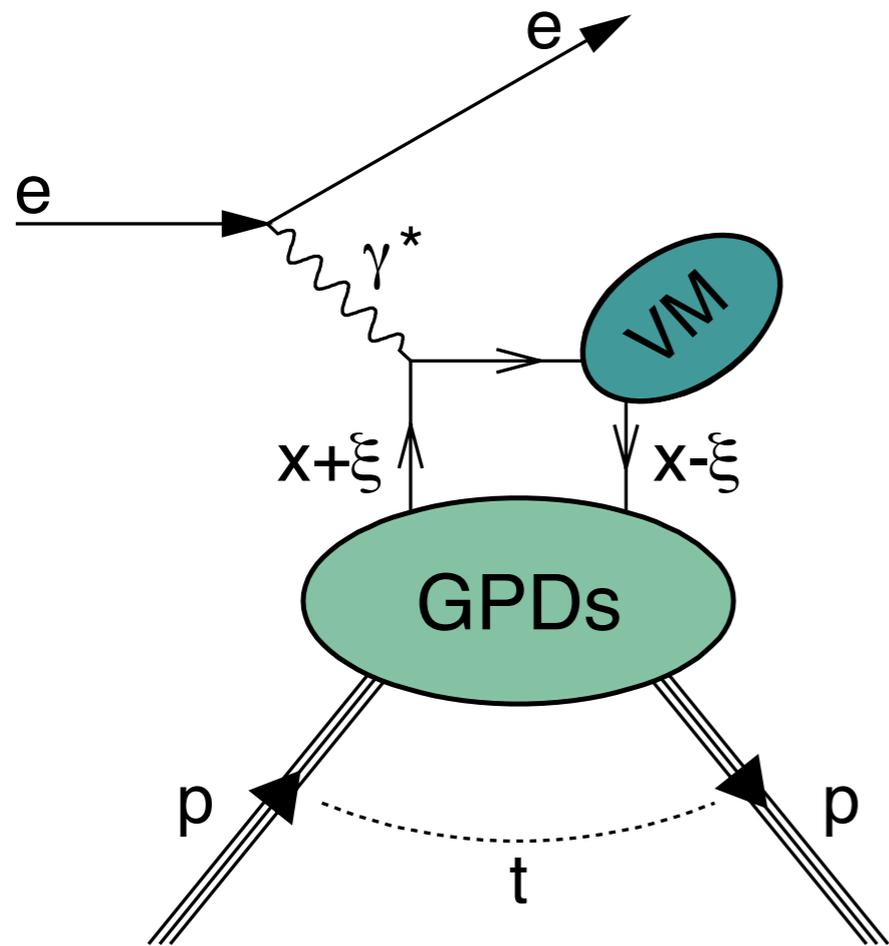
## HERMES:

- exclusive electroproduction of  $\rho$  and  $\omega$
- quark GPDs
- target:
  - unpolarized protons and deuterons
  - transversely polarized protons
- longitudinally polarized lepton beam

## H1 and ZEUS:

- exclusive electroproduction of  $\rho$ ,  $\omega$ ,  $\phi$ ,  $J/\psi$ ,  $\psi(2s)$ ,  $\Upsilon$
- exclusive photoproduction of  $J/\psi$ ,  $\psi(2s)$ ,  $\Upsilon$
- gluon GPDs
- unpolarized proton beam

# Exclusive vector-meson production at HERA

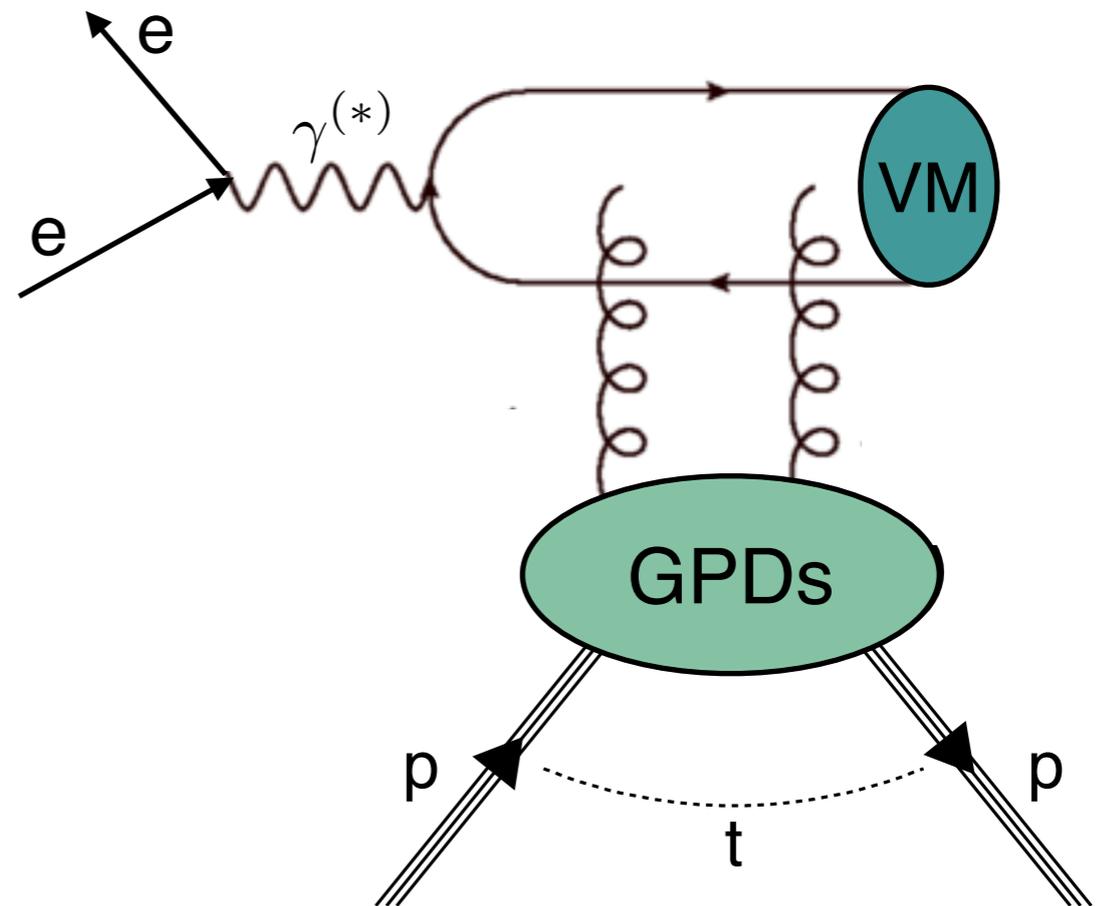


HERMES:

$$10^{-2} \leq x_B \leq 0.5$$

$$1 \text{ GeV}^2 < Q^2 < 10 \text{ GeV}^2$$

$$3.0 \text{ GeV} \leq W \leq 6.3 \text{ GeV}$$



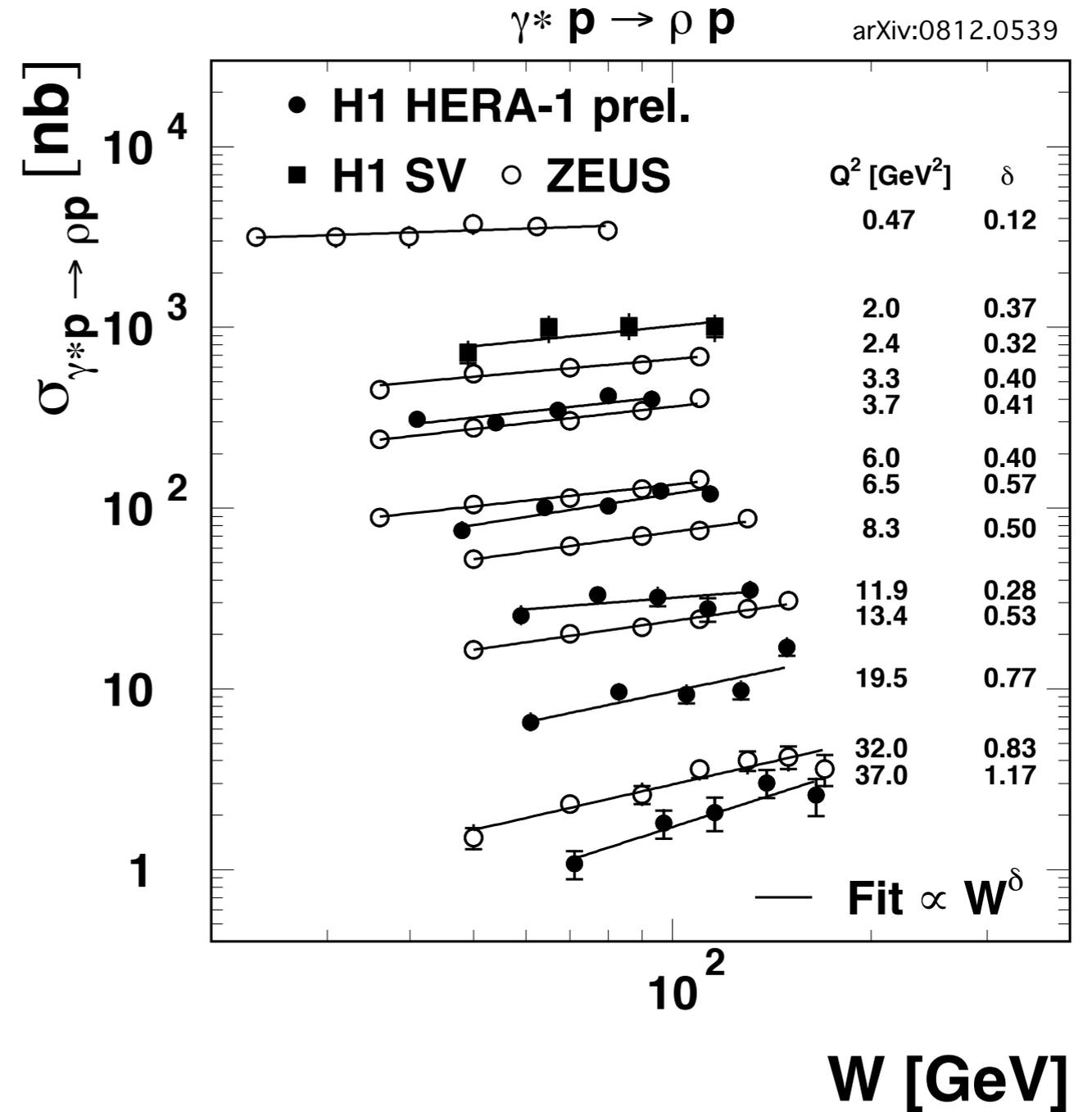
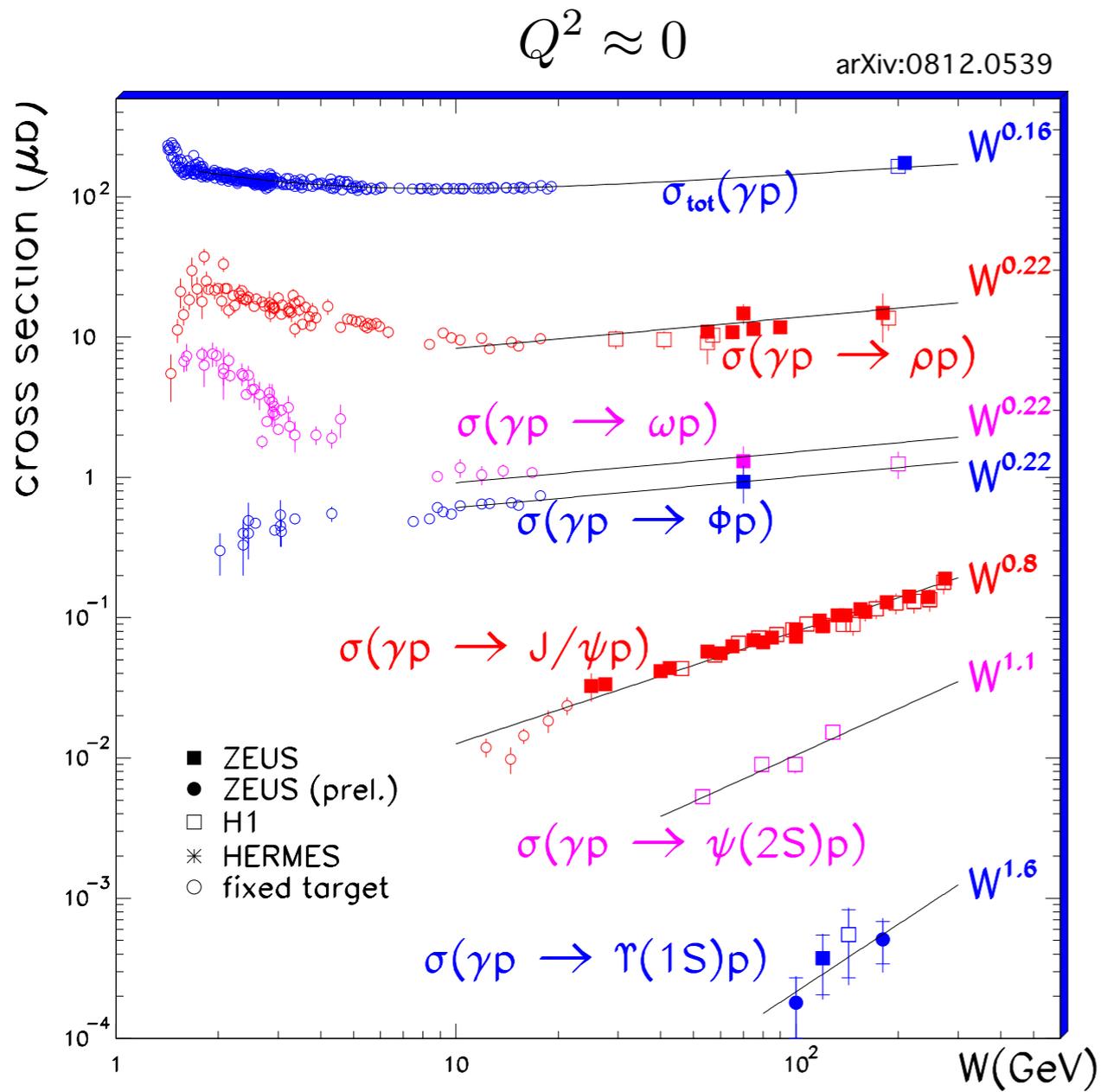
H1 and ZEUS:

$$10^{-4} \leq x_B \leq 10^{-2}$$

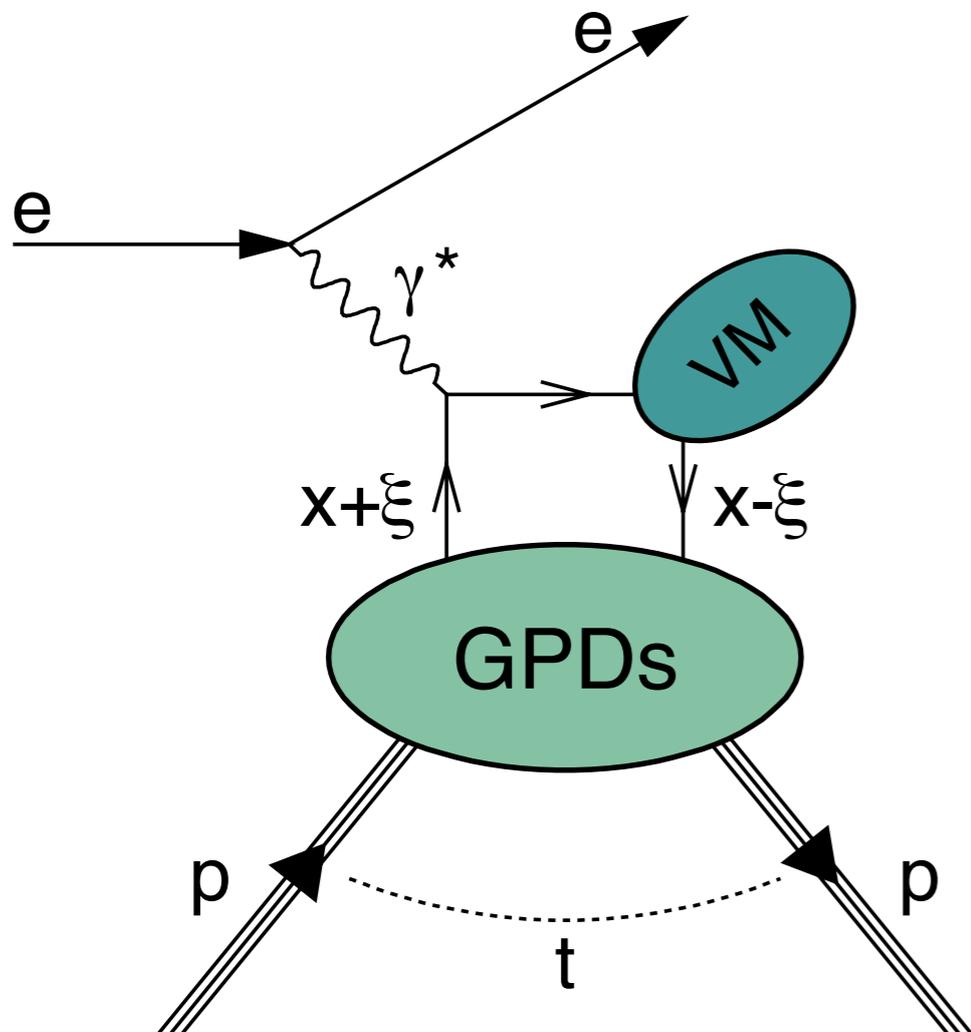
$$2 \text{ GeV}^2 \leq Q^2 \leq 100 \text{ GeV}^2 \text{ (DIS)}$$

$$30 \text{ GeV} \leq W \leq 300 \text{ GeV}$$

# W dependence



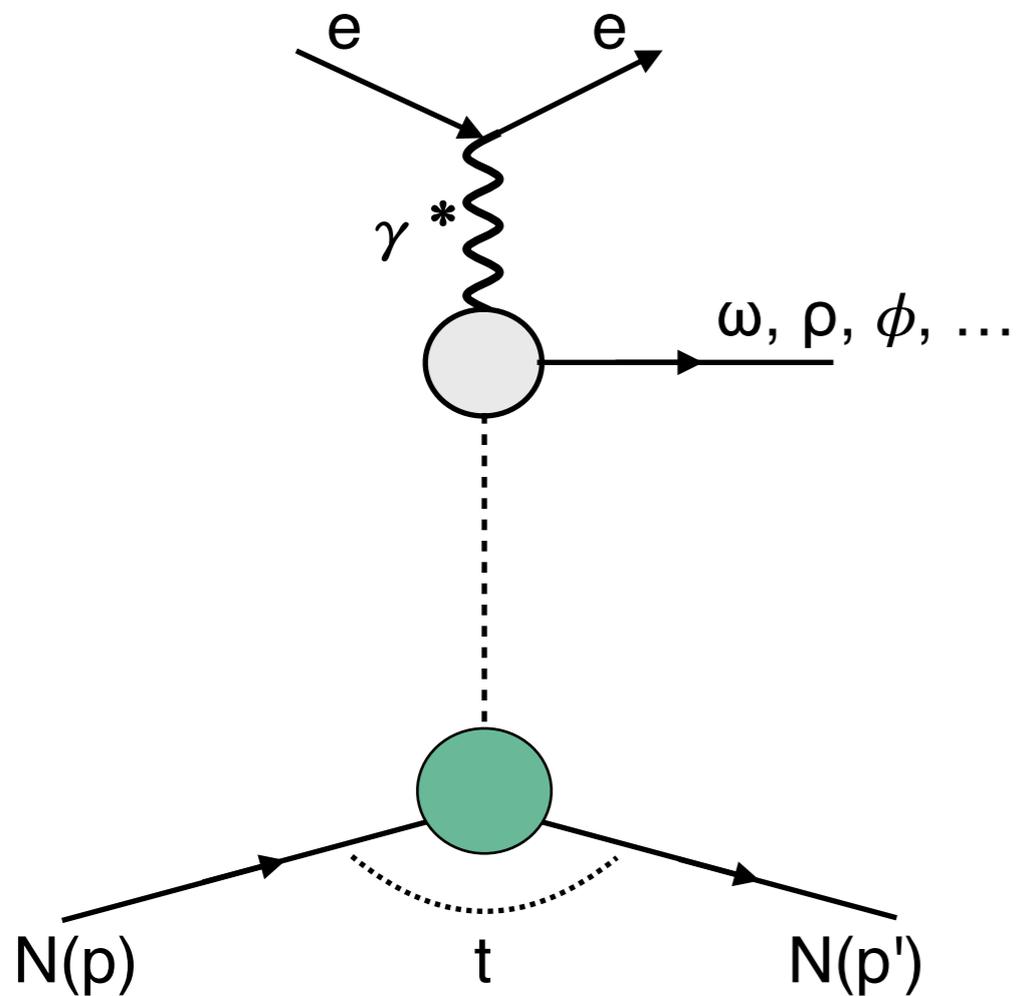
# Exclusive vector-meson production



Target polarization state

- unpolarized target:  
nucleon-helicity-non-flip GPDs  $H$ ,  $\tilde{H}$  and  $\bar{E}_T = 2H_T + \tilde{E}_T$ .
- transversely polarized target:  
nucleon-helicity-flip GPDs  $E$ ,  $\tilde{E}$  and  $H_T$ .

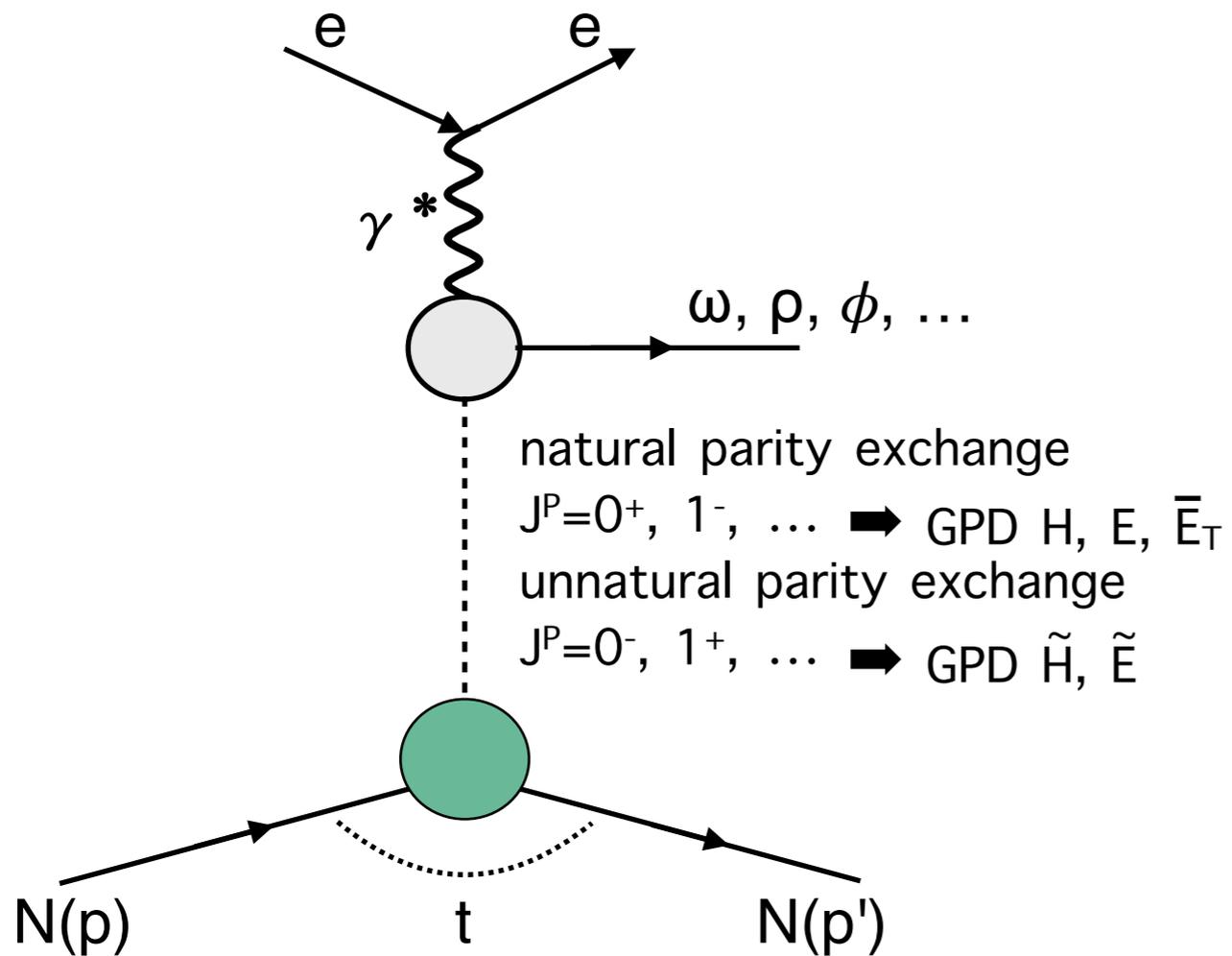
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# Exclusive vector-meson production



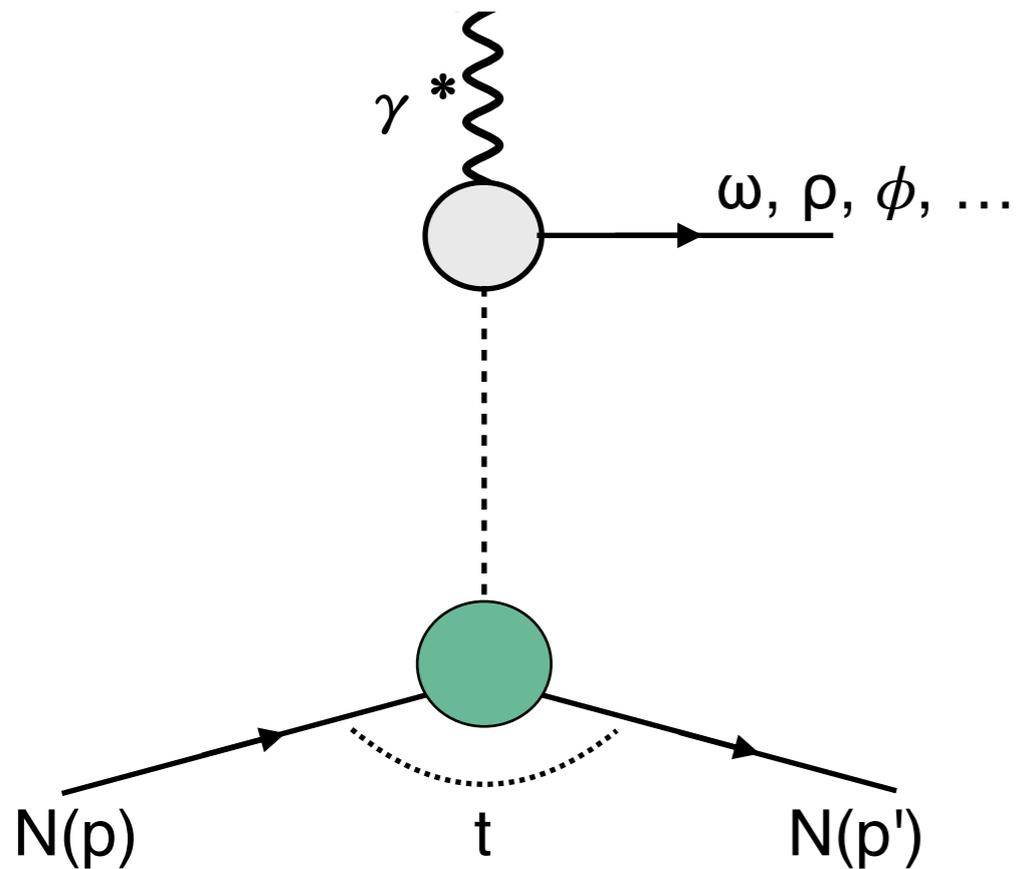
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# Helicity amplitude ratios and SDMEs

$$\gamma^*(\lambda_\gamma) + N(\lambda_N) \rightarrow V(\lambda_V) + N(\lambda'_N)$$

- Helicity amplitude  $F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N}$

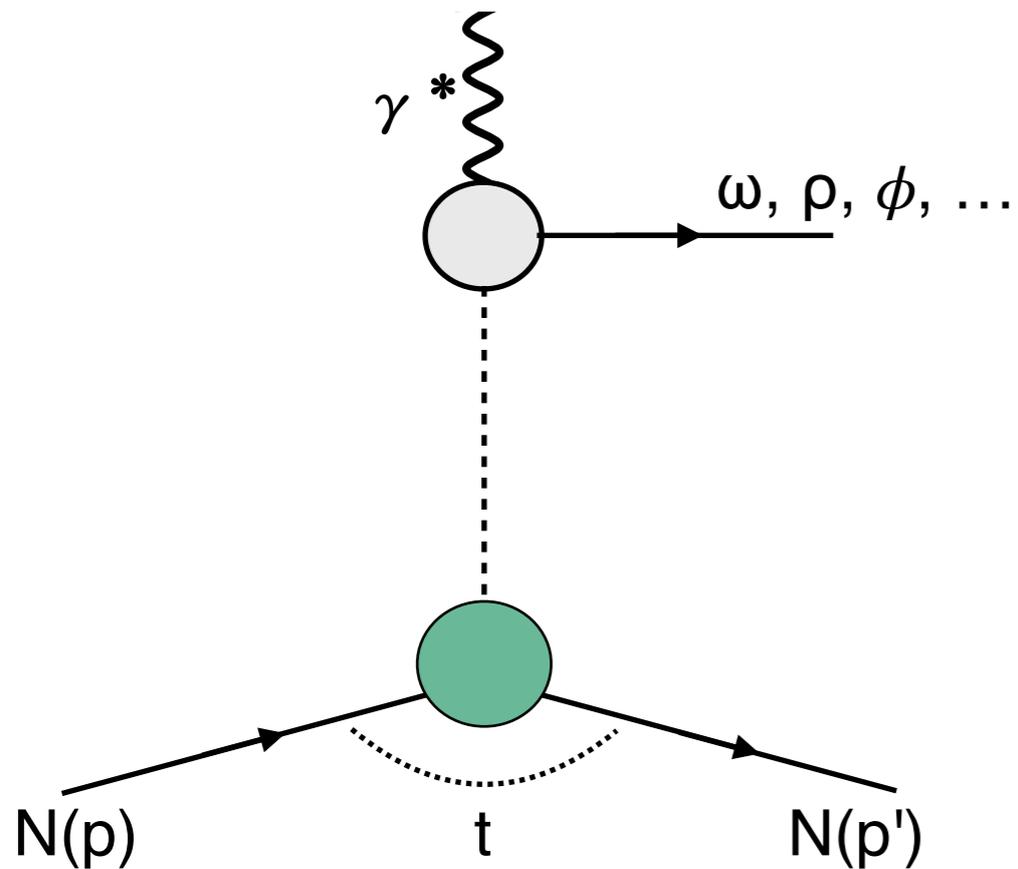


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$$F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} = T_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} + U_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N}$$

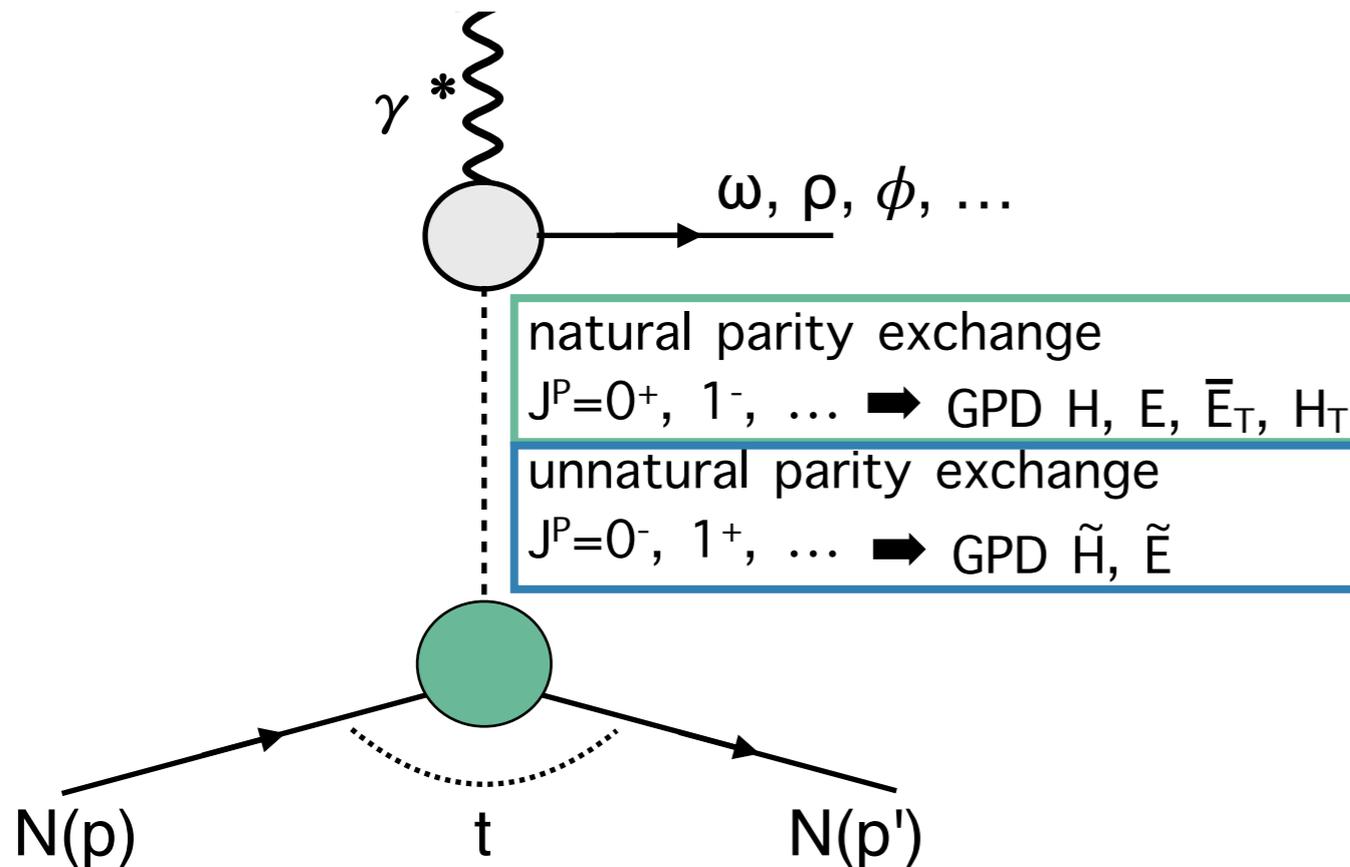


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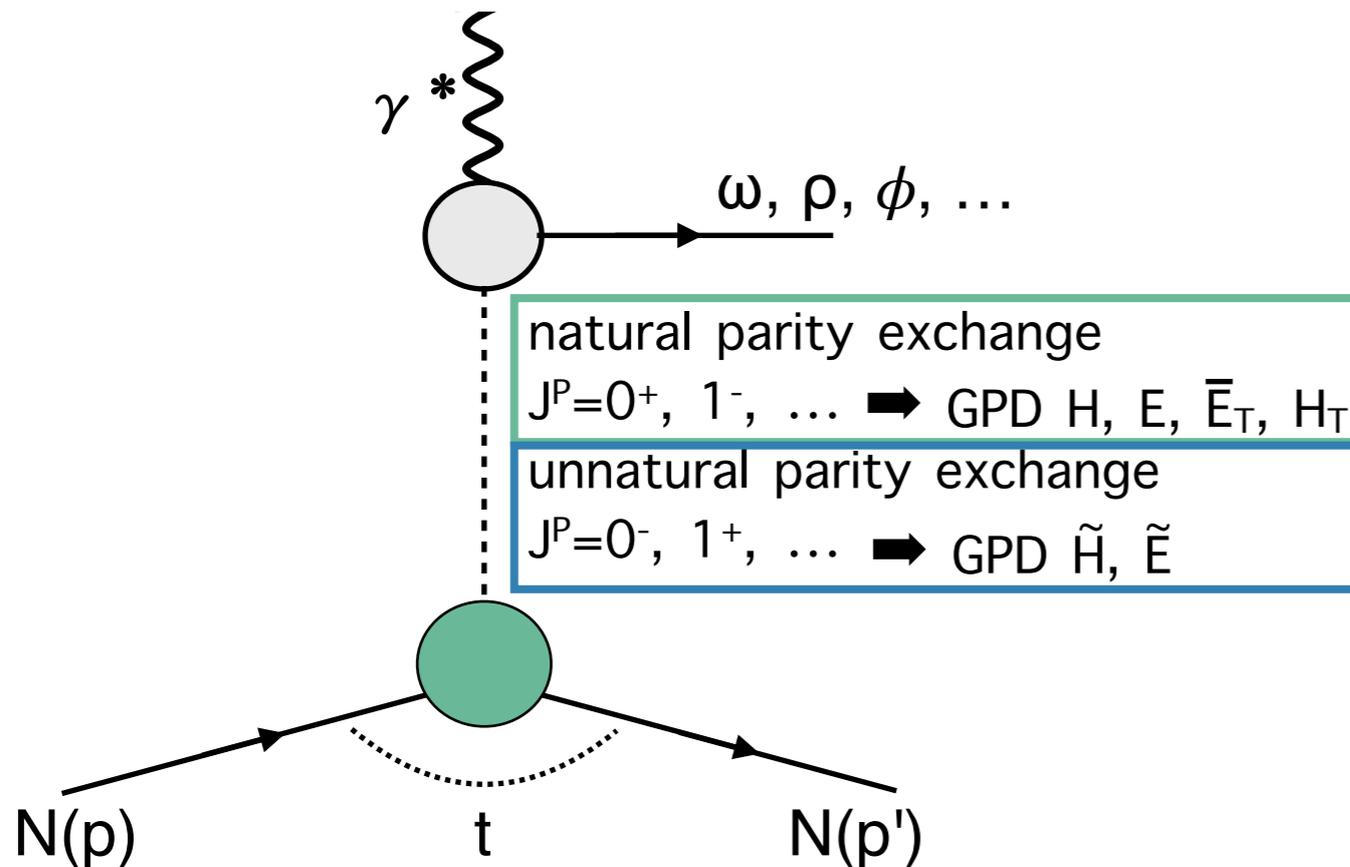
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- Helicity amplitude ratios

$$t_{\lambda_V \lambda_\gamma}^{(n)} = T_{\lambda_V \lambda_\gamma}^{(n)} / T_{0 \frac{1}{2} 0 \frac{1}{2}}$$

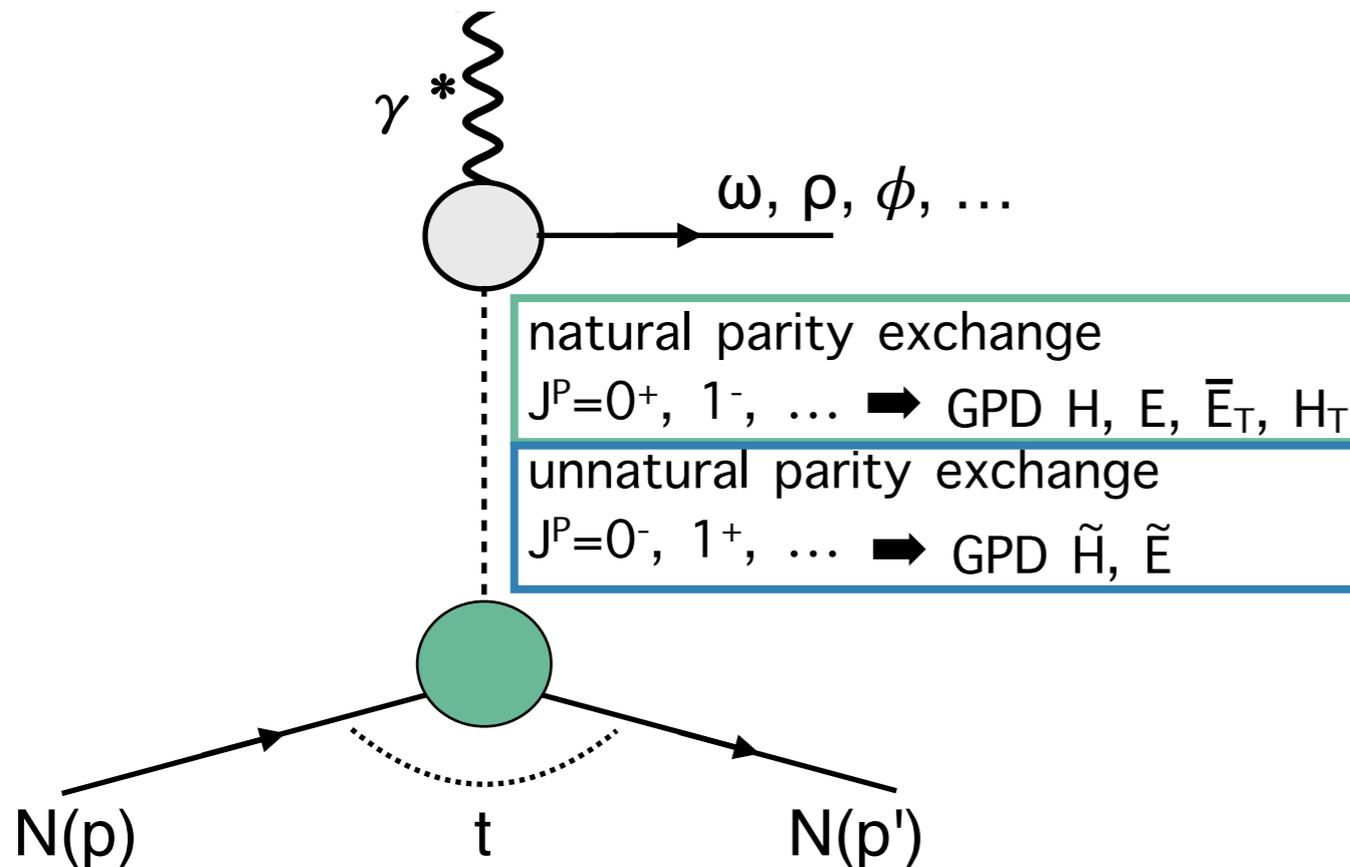
$$u_{\lambda_V \lambda_\gamma}^{(n)} = U_{\lambda_V \lambda_\gamma}^{(n)} / T_{0 \frac{1}{2} 0 \frac{1}{2}}$$

$$n = 1 \quad \lambda_N = \lambda'_N$$

$$n = 2 \quad \lambda_N \neq \lambda'_N$$

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$$\gamma^*(\lambda_\gamma) + N(\lambda_N) \rightarrow V(\lambda_V) + N(\lambda'_N)$$



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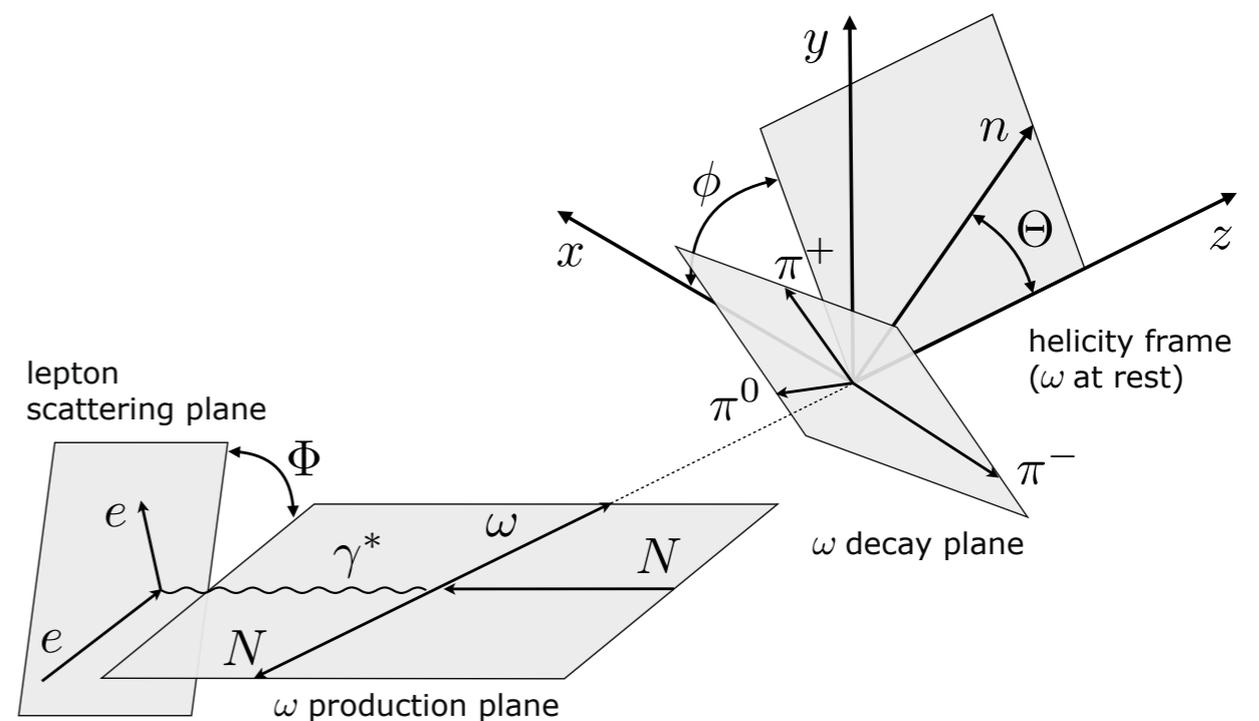
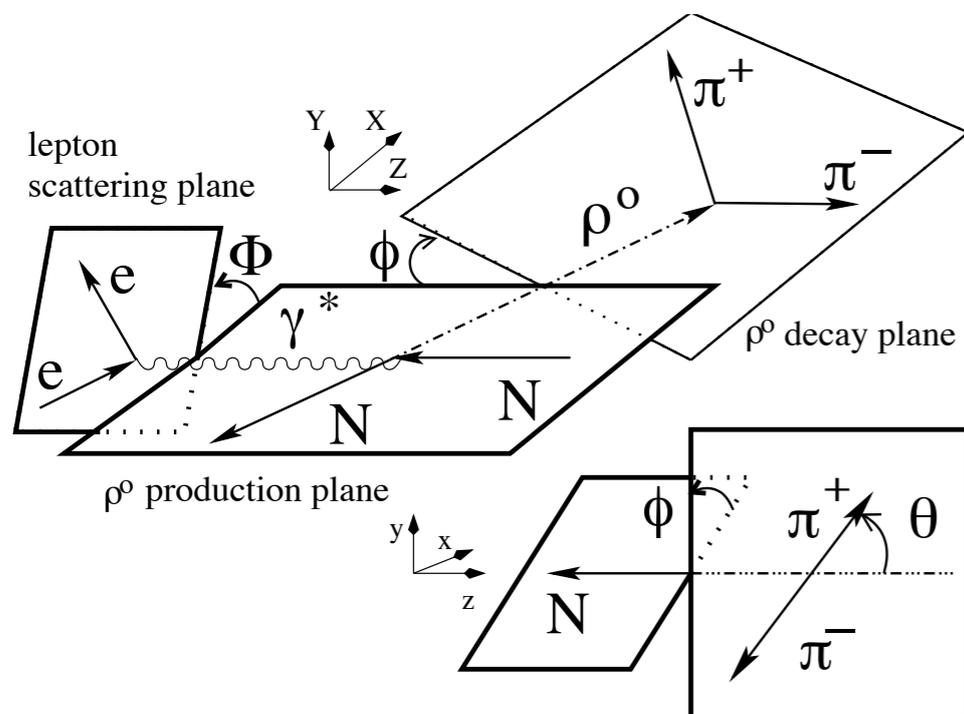
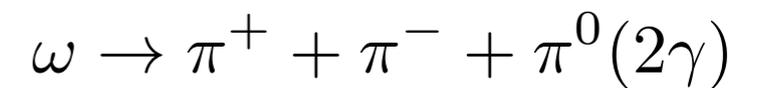
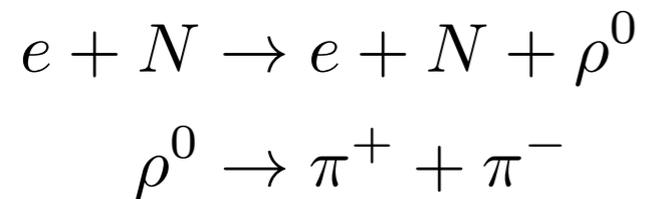
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- SDMEs

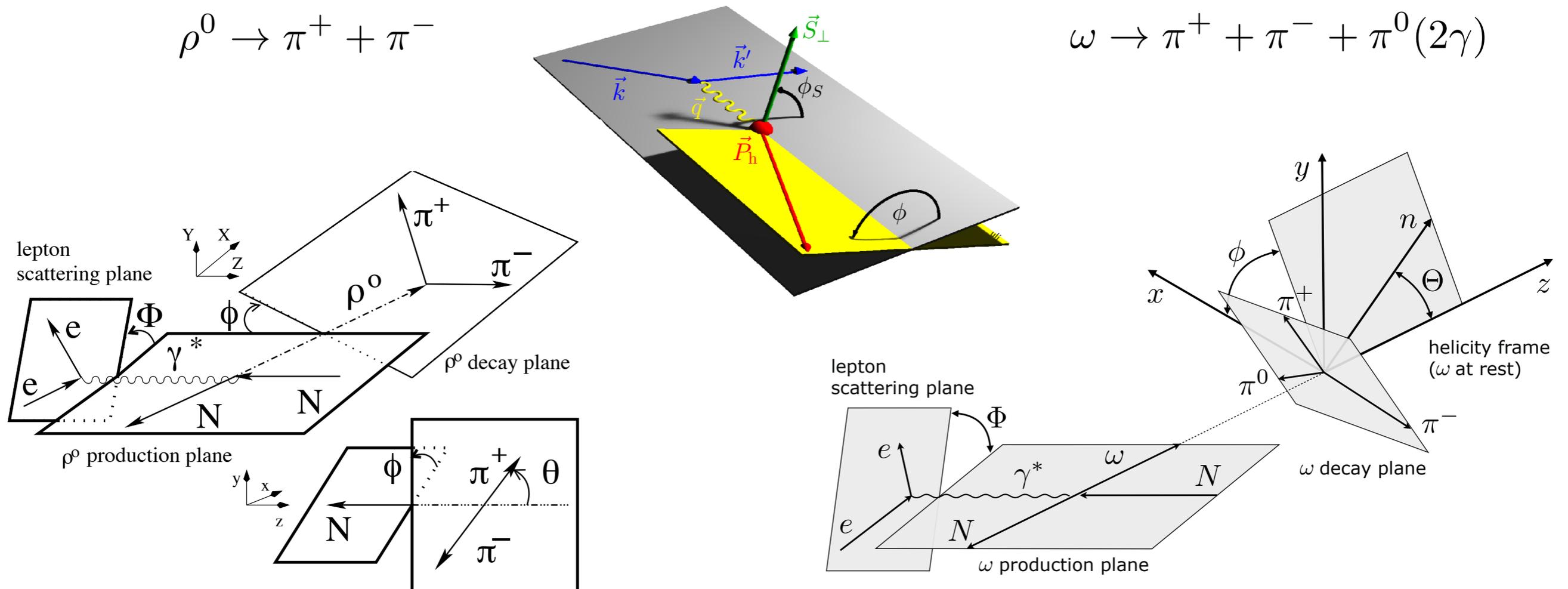
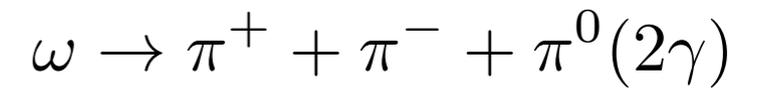
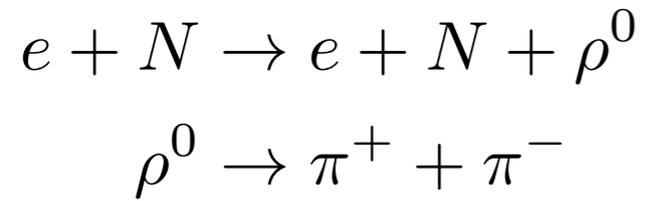
$$\propto F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} \sum_{\lambda_\gamma \lambda'_\gamma}^\alpha F_{\lambda'_V \lambda'_N \lambda'_\gamma \lambda_N}^*$$

# Angular distributions



Fit angular distribution of decay particles  $\mathcal{W}(\Phi, \phi, \Theta)$  and extract either Spin Density Matrix Elements (SDMEs) or helicity amplitude ratios

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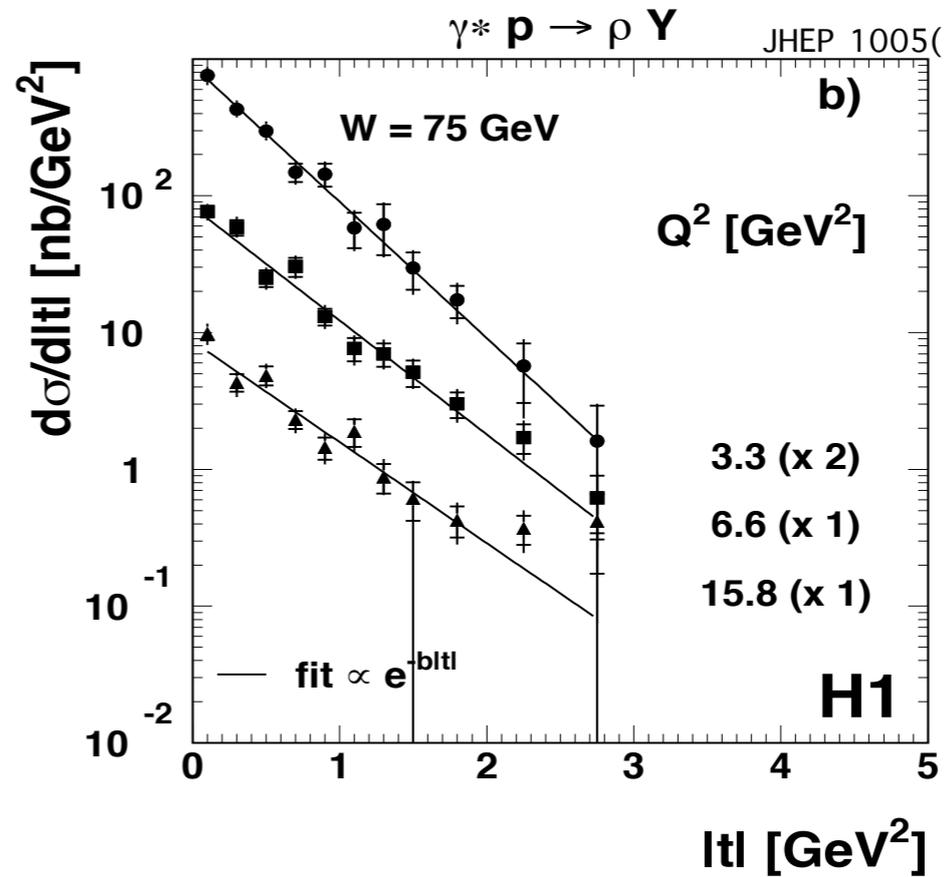
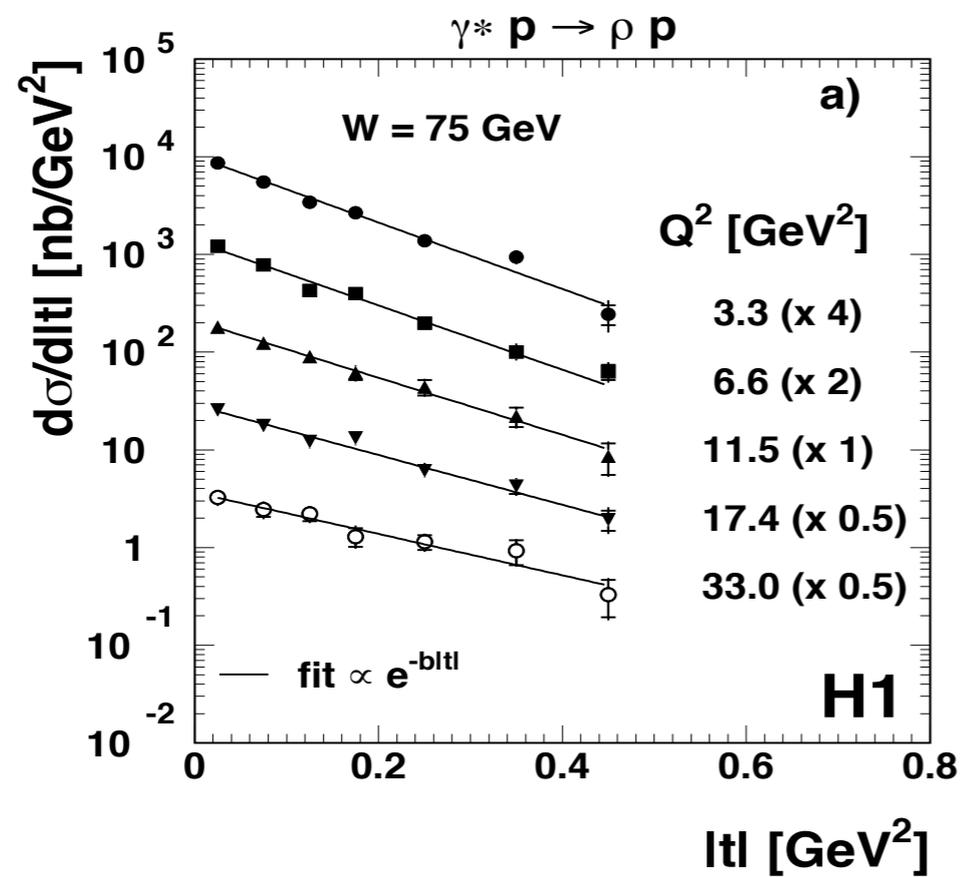


Fit angular distribution of decay particles  $\mathcal{W}(\Phi, \phi, \Theta, \phi_S)$  and extract either Spin Density Matrix Elements (SDMEs) or helicity amplitude ratios

# Exclusive $\rho^0$

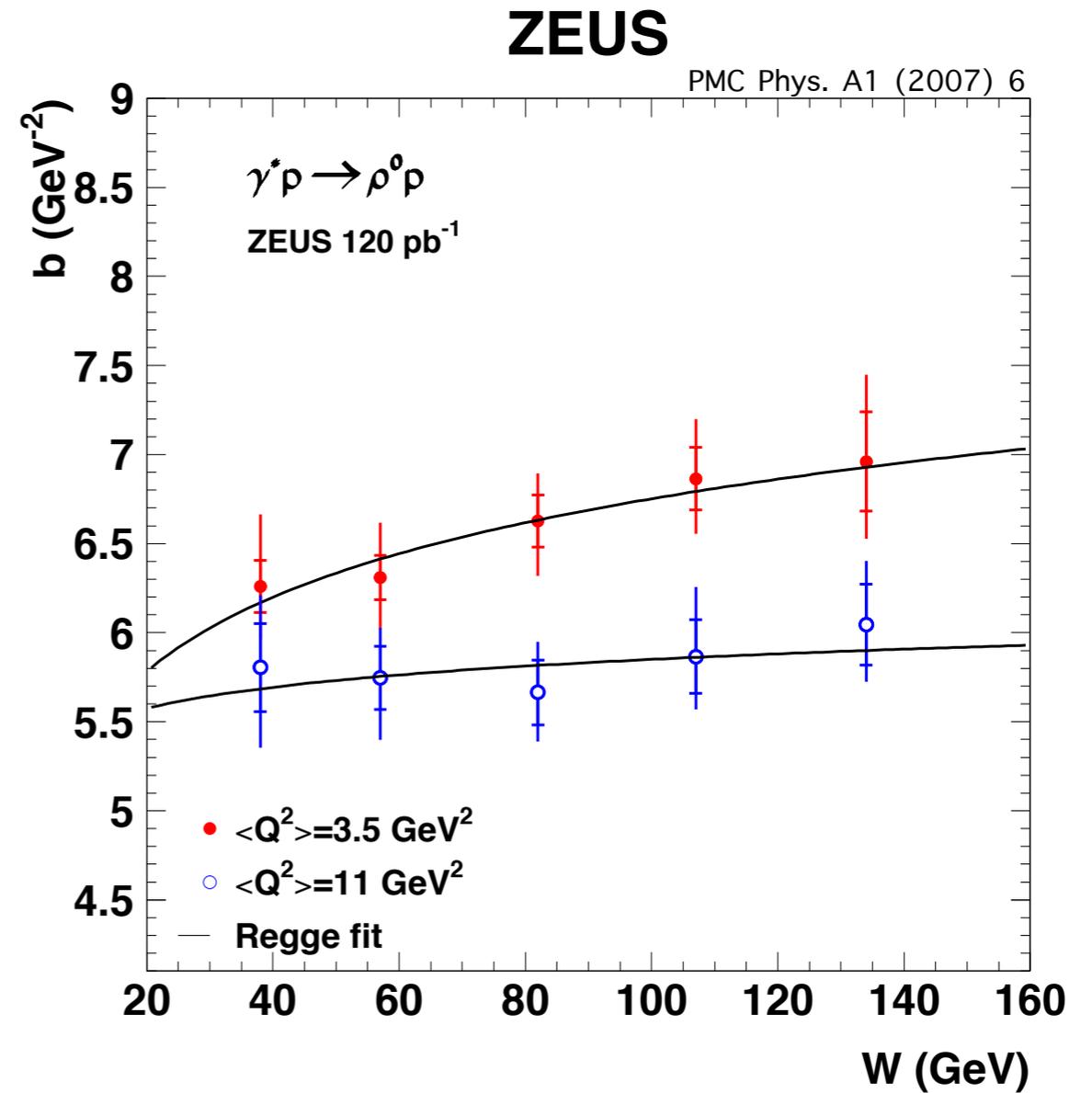
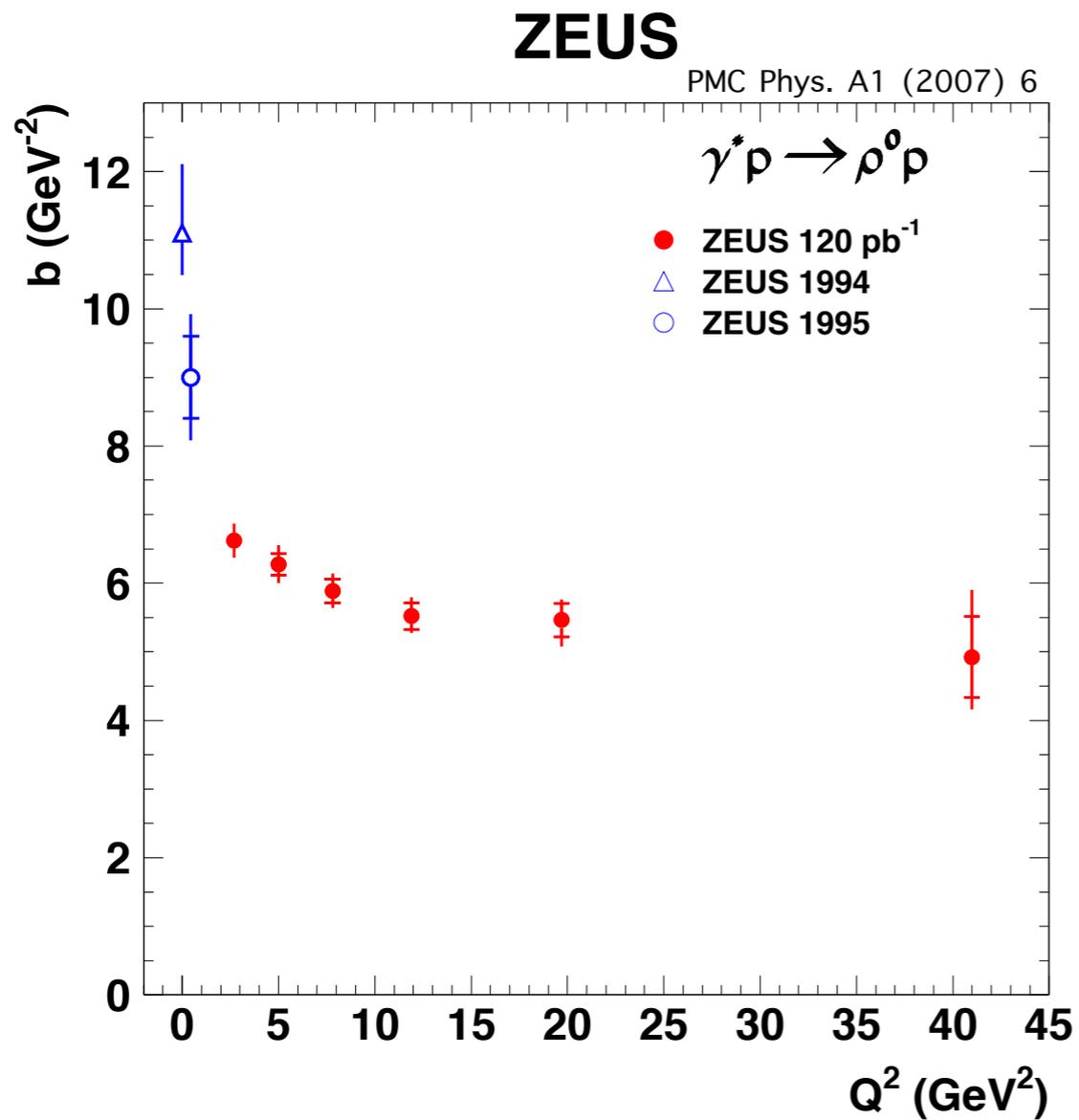
- unpolarized H and D targets
- transversely polarized H target

# t dependence



$$b = b_Y + b_{q\bar{q}} + b_{\mathbb{P}} (+b_V)$$

# b slope



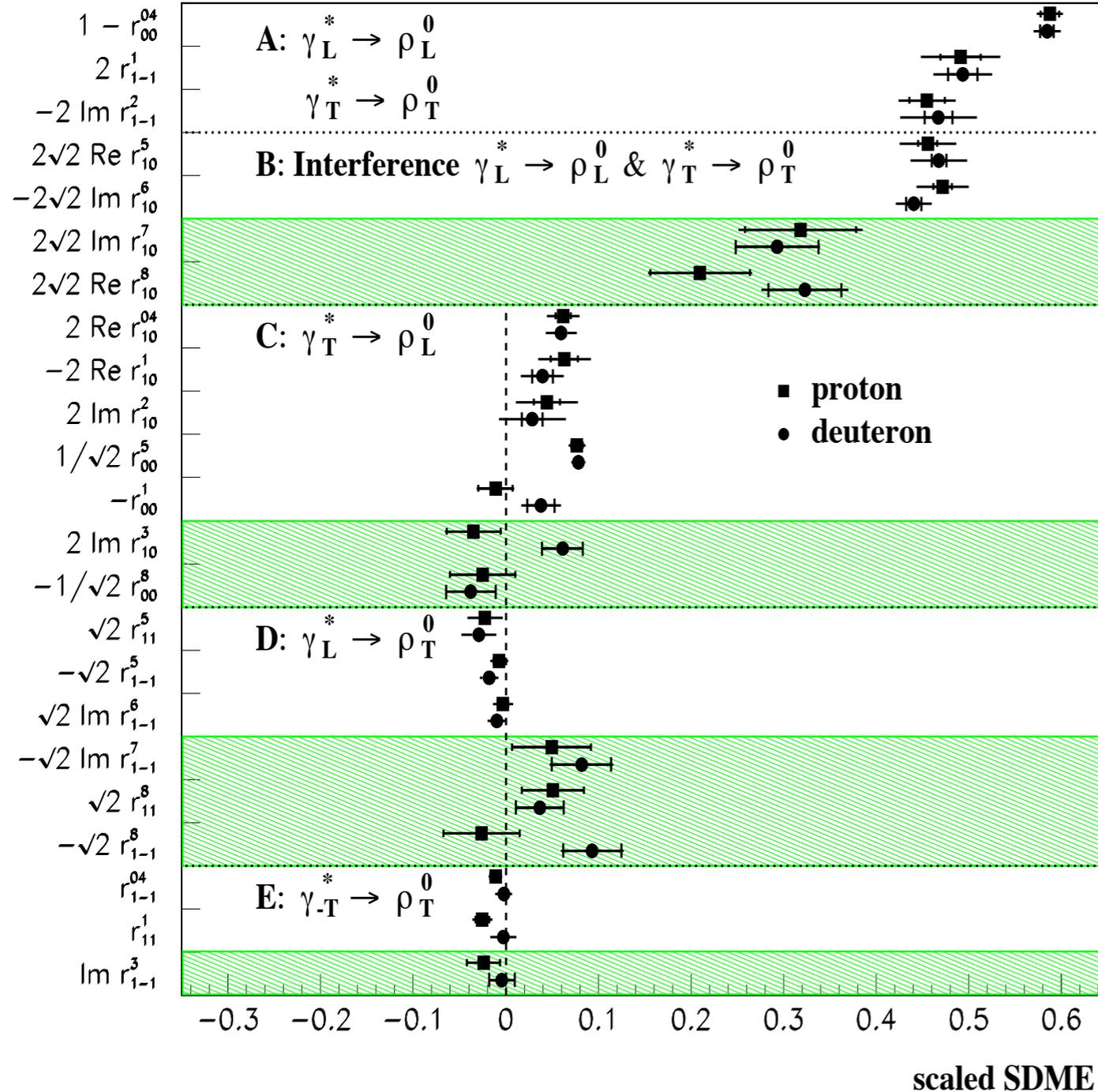
$$b = b_Y + b_{q\bar{q}} + b_{\mathbb{P}} (+b_V)$$

# Results $\rho$ SDMEs

longitudinally polarized beam  
unpolarized p and d target

HERMES

Eur. Phys. J. C62 (2009) 659-695



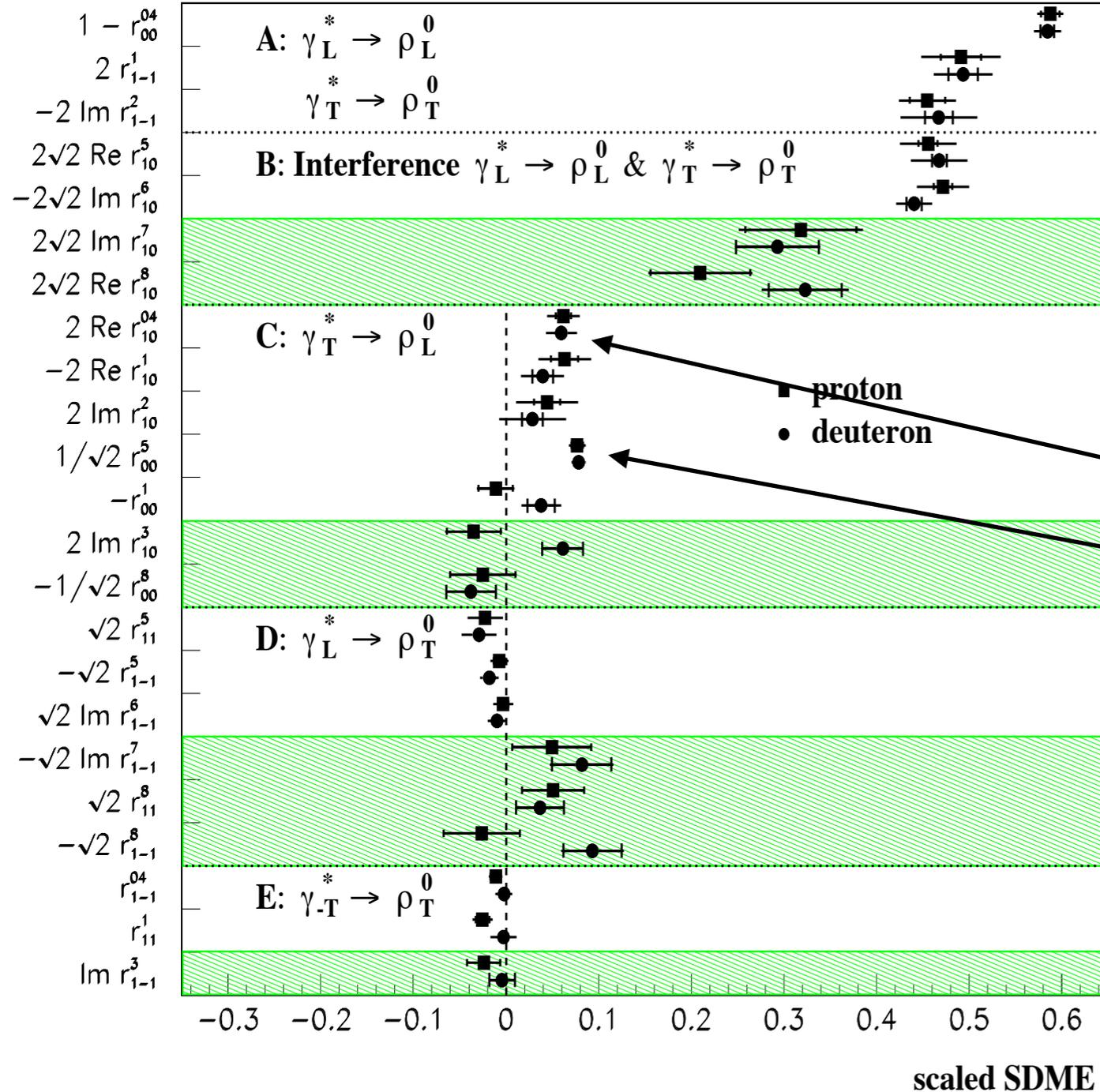
- 5 classes of SDMEs
- unpolarized and polarized SDMEs
- proton & deuteron similar

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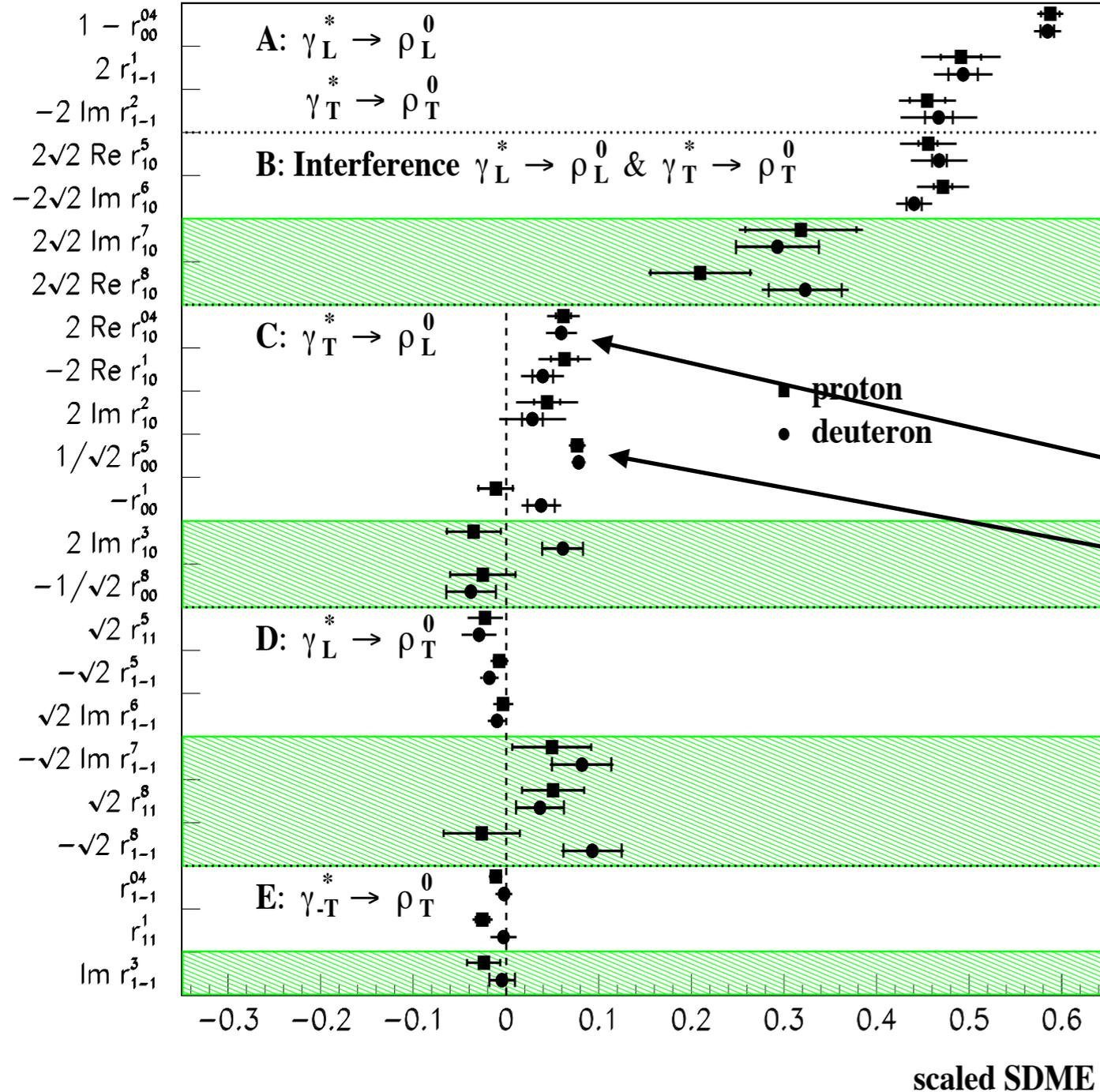
- 5 classes of SDMEs
- unpolarized and polarized SDMEs
- proton & deuteron similar
- s-channel helicity conservation ( $\lambda_{\gamma^*} = \lambda_{\omega}$ ):
  - fulfilled for class A & B
  - class C - strong violation:
    - $\Re r_{10}^{04} \neq 0$  by  $4(4)\sigma$  for p(d)
    - $r_{00}^5 \neq 0$  by  $9(10)\sigma$  for p(d)

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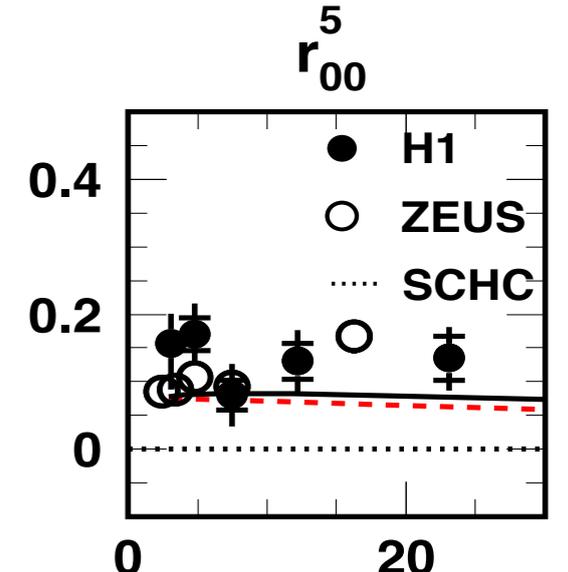
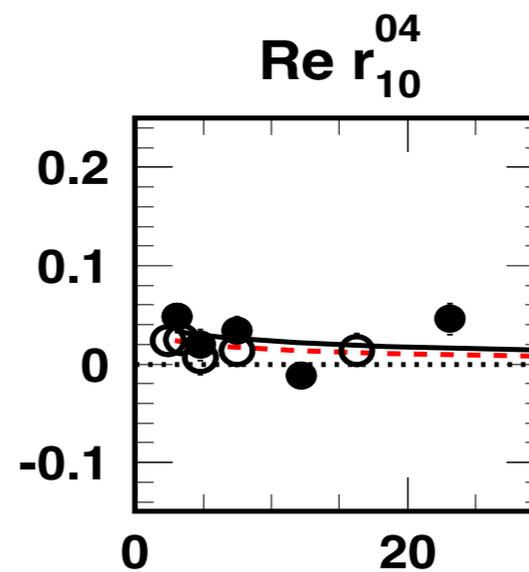
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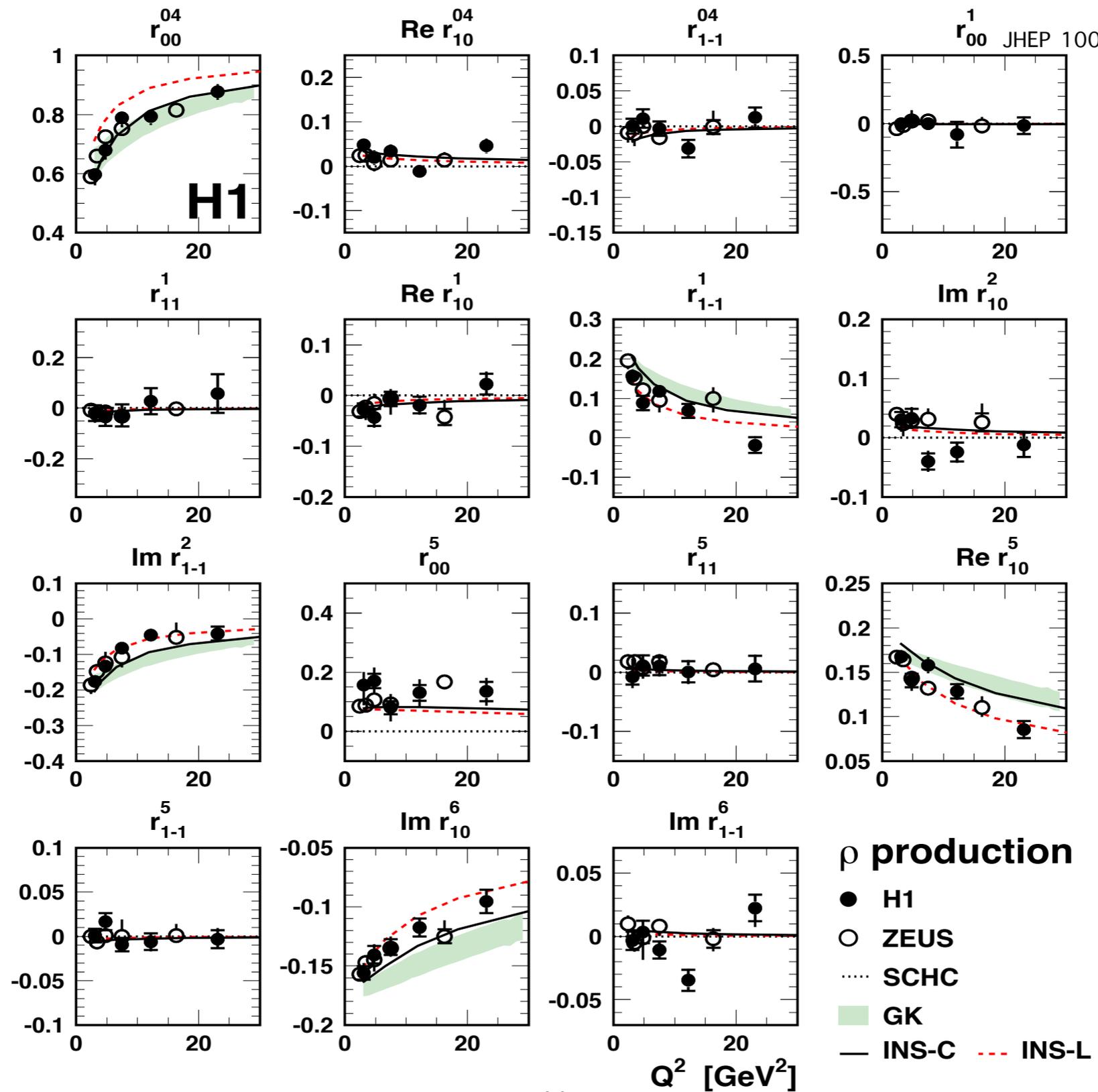


JHEP 1005(2010)032

$Q^2$  [GeV<sup>2</sup>]

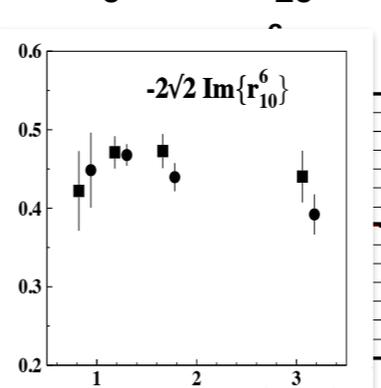
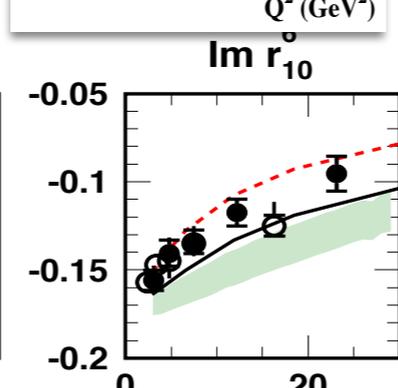
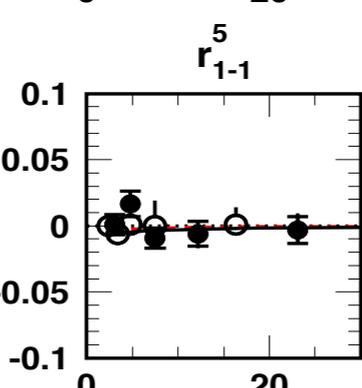
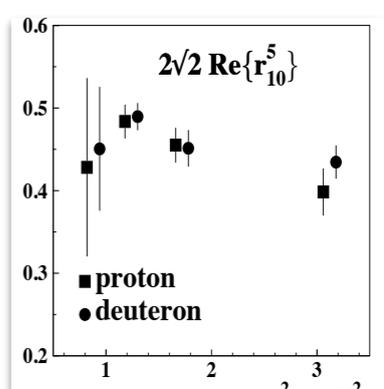
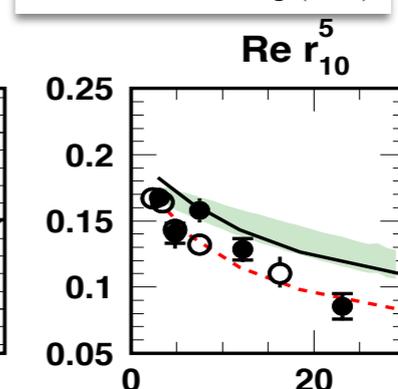
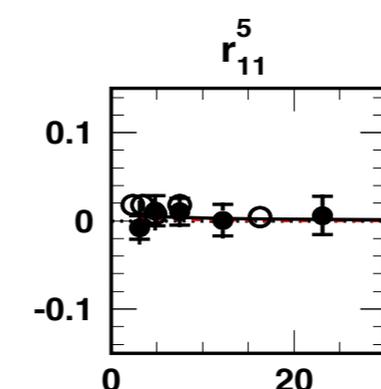
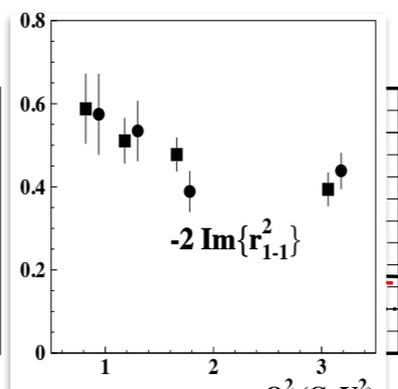
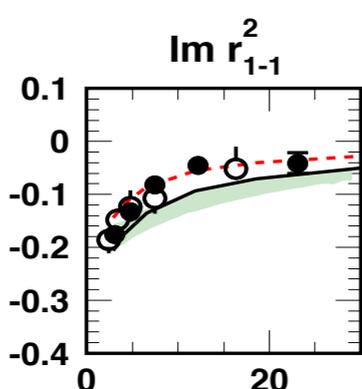
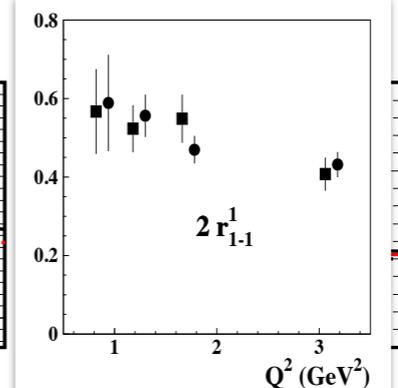
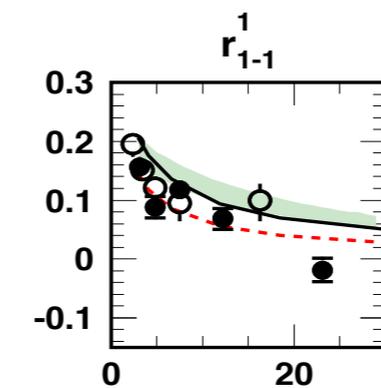
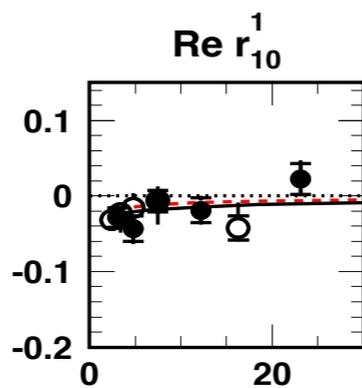
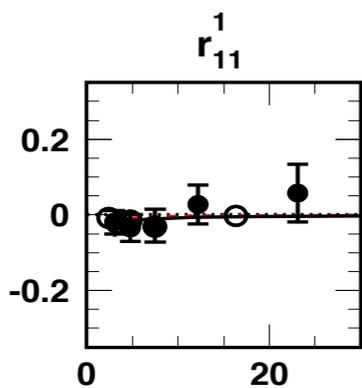
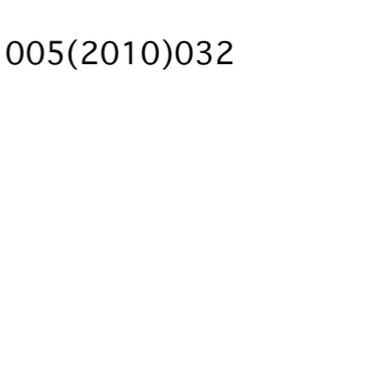
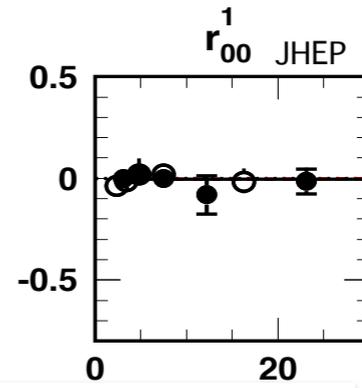
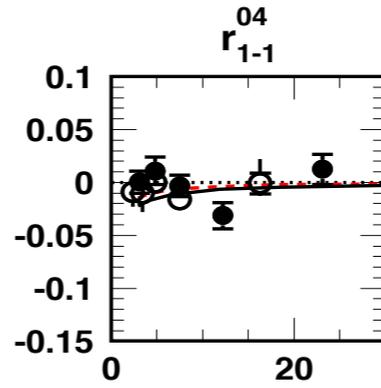
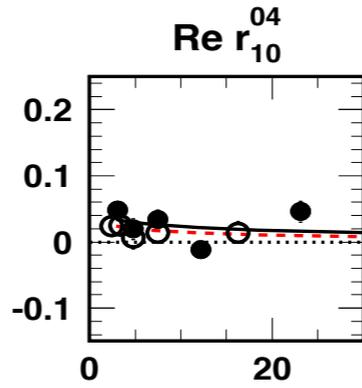
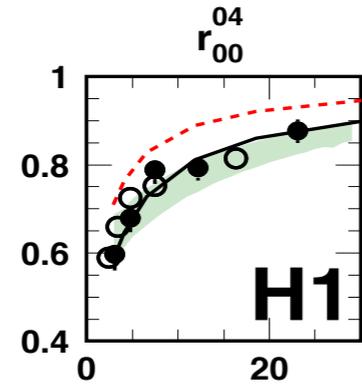
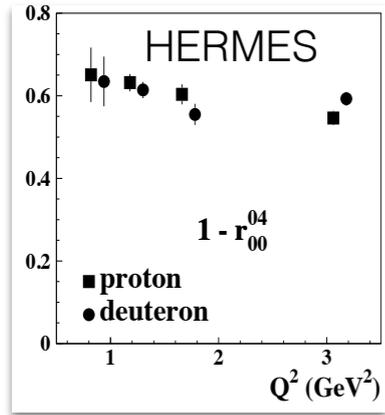
# $Q^2$ dependence

$r_{00}^1$  JHEP 1005(2010)032



# $Q^2$ dependence

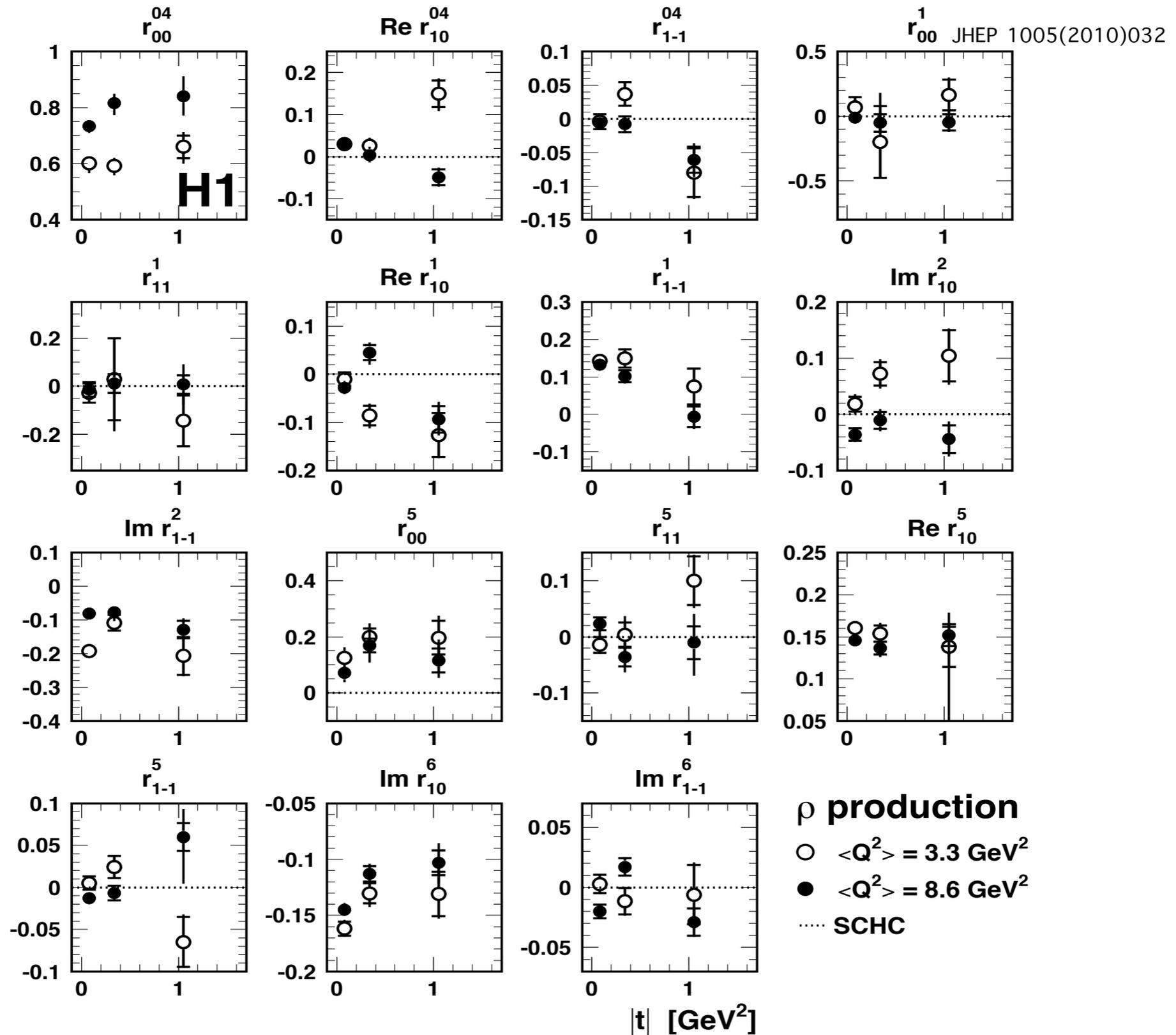
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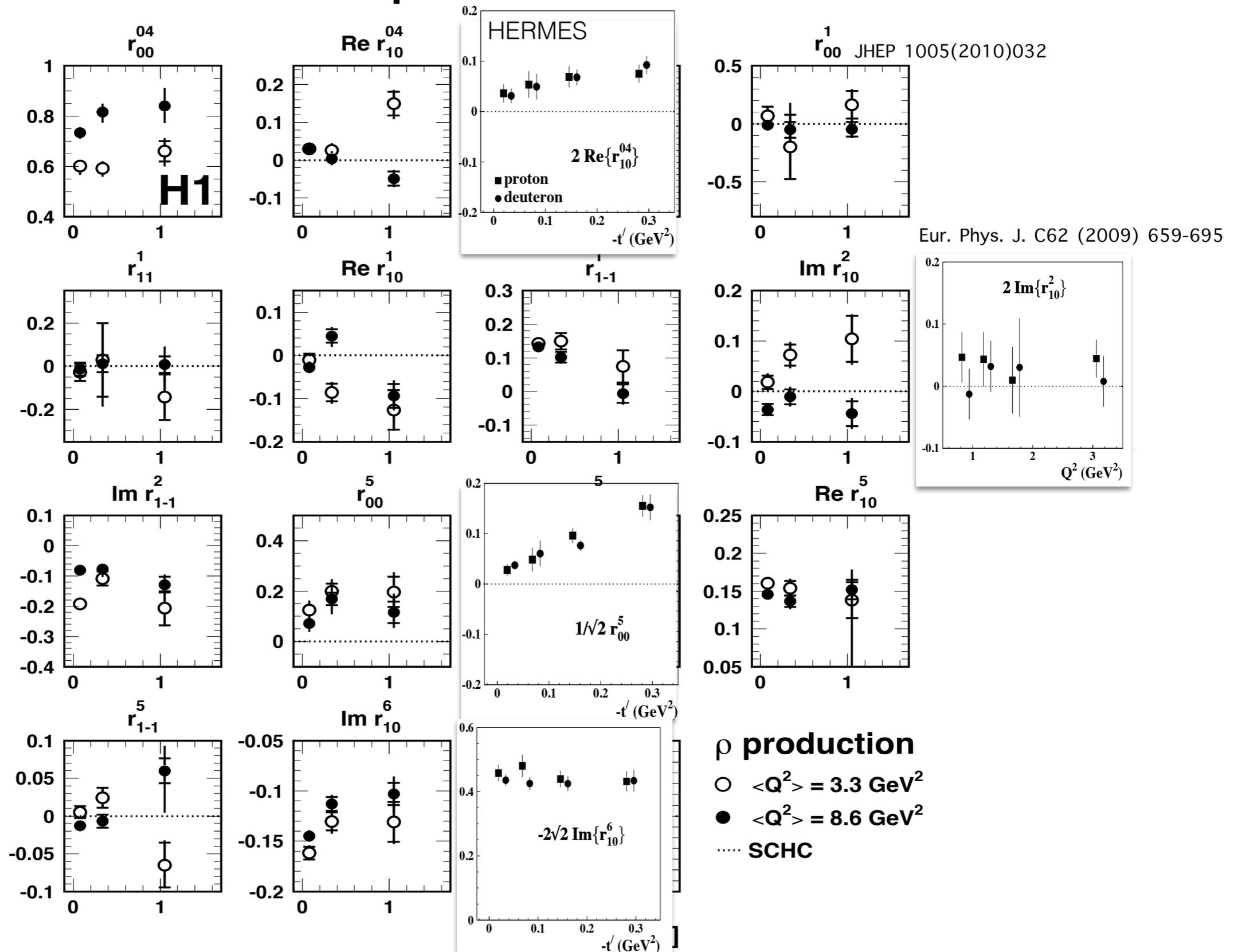
$\rho$  production

- H1
- ZEUS
- ⋯ SCHC
- GK
- INS-C
- - - INS-L

# t dependence



# t dependence



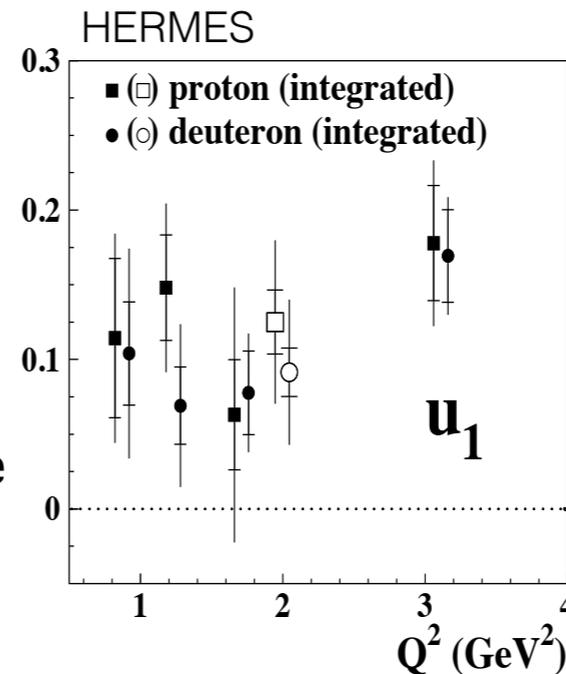
# Test of unnatural parity exchange

## SDMEs – HERMES

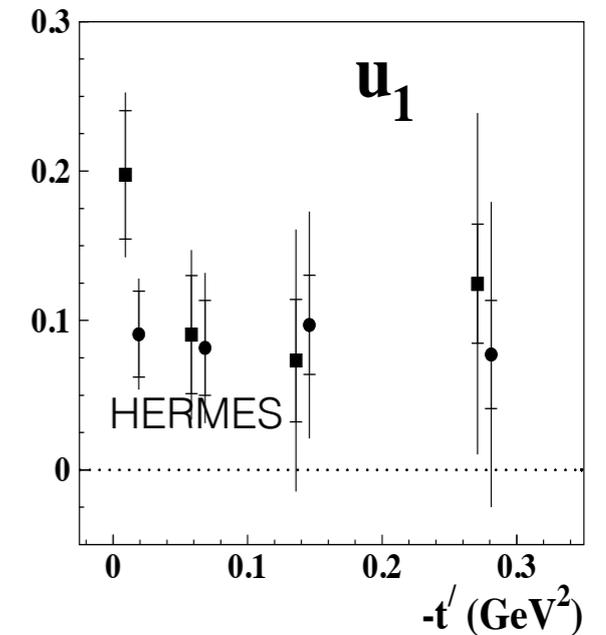
$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$$

$$\propto 2\epsilon|U_{10}|^2 + |U_{11} + U_{-11}|^2$$

- $\neq 0$  by  $2\sigma$  for proton data
- UPE for deuteron expected to be smaller because of absence of UPE for coherent scattering



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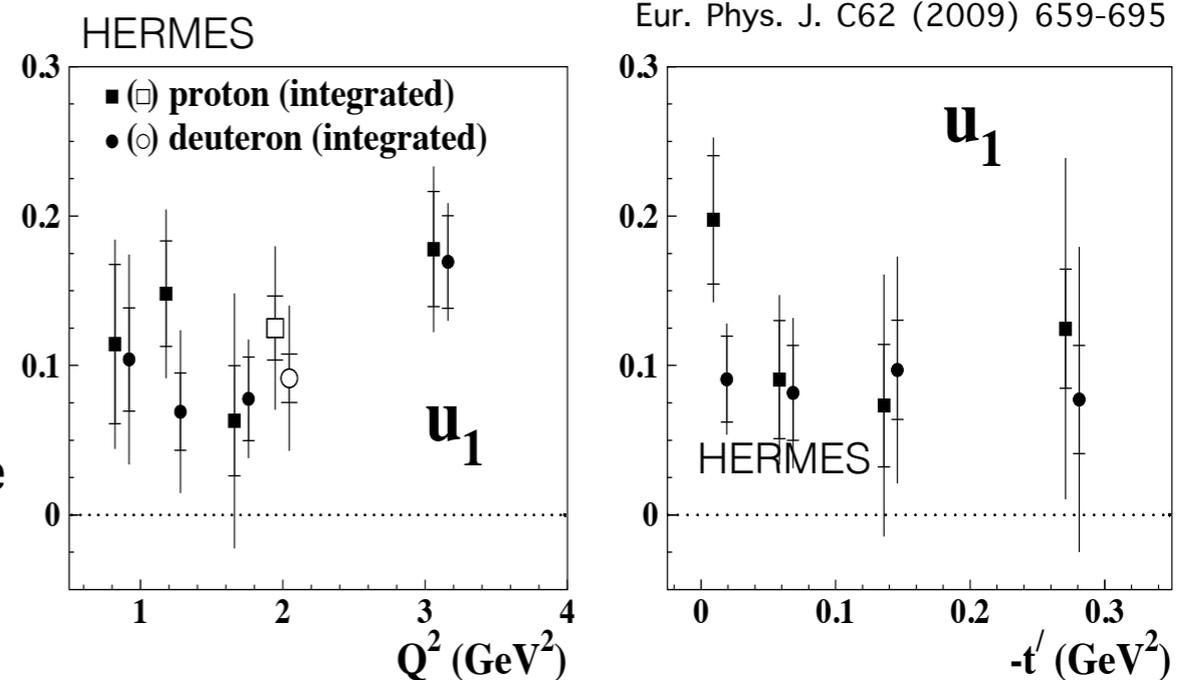
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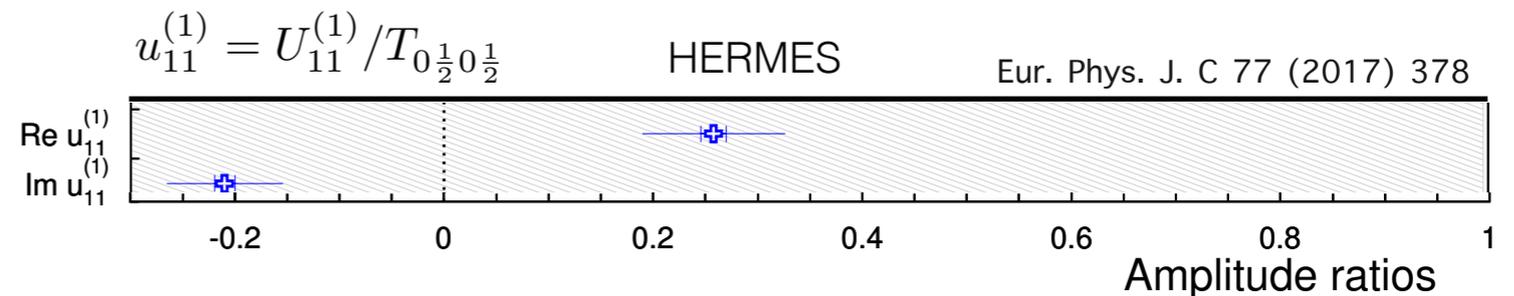
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## helicity amplitude ratio – HERMES

- unnatural parity nucleon-helicity non-flip  
 $\neq 0$  by  $4\sigma$



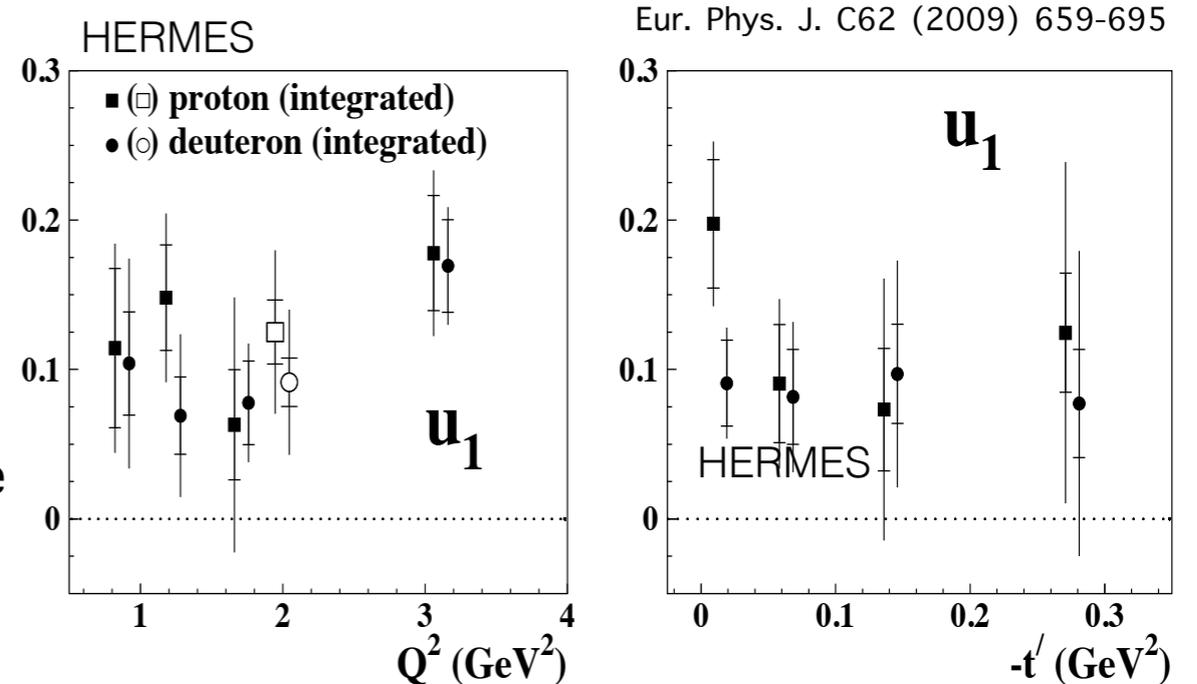
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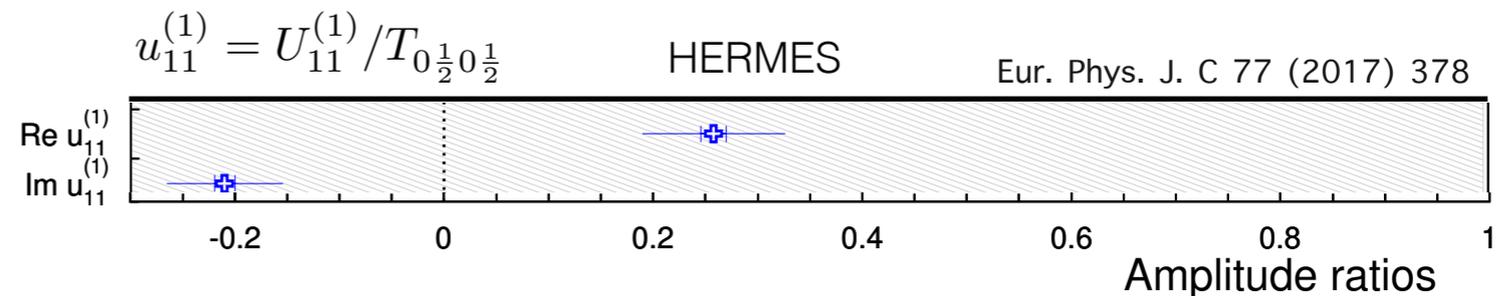
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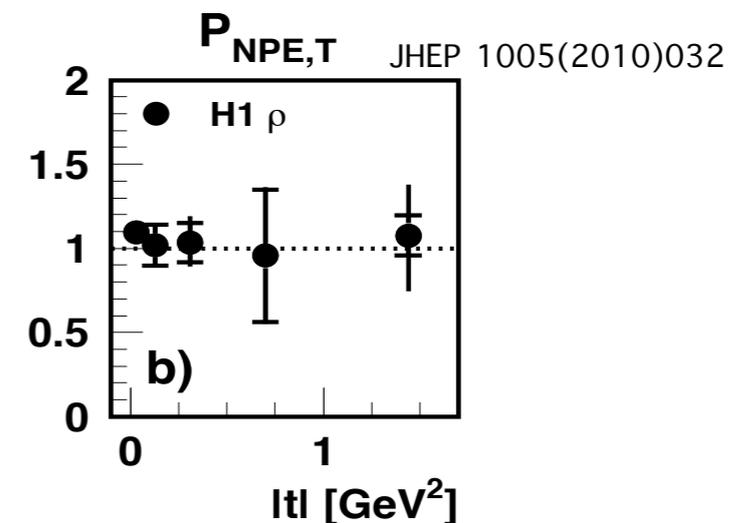
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 $\neq 0$  by  $4\sigma$



## asymmetry – H1

$$P_{NPE,T} = \frac{\sigma_T^N - \sigma_T^U}{\sigma_T^N + \sigma_T^U}$$



# Longitudinal-to-transverse cross-section ratios

$$R = \frac{1 - r_{00}^{04}}{\epsilon} = \frac{d\sigma(\gamma_L^* \rightarrow V_L) + \frac{1}{\epsilon} d\sigma(\gamma_T^* \rightarrow V_L)}{d\sigma(\gamma_T^* \rightarrow V_T) + \epsilon d\sigma(\gamma_L^* \rightarrow V_T)}$$

# Longitudinal-to-transverse cross-section ratios

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$$R^{\gamma^*} = \frac{d\sigma(\gamma_L^*)}{d\sigma(\gamma_T^*)}$$

$$R^{\gamma^*} = R - \frac{\eta(1 + \epsilon R)}{\epsilon(1 + \eta)} \quad \text{with} \quad \eta = \eta(T_{01}, T_{10}, U_{01}, U_{10})$$

$\eta = 0$  for SCHC

# Longitudinal-to-transverse cross-section ratios

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$$R^{\gamma^*} = \frac{d\sigma(\gamma_L^*)}{d\sigma(\gamma_T^*)}$$

$$R^{\gamma^*} = R - \frac{\eta(1 + \epsilon R)}{\epsilon(1 + \eta)} \quad \text{with} \quad \eta = \eta(T_{01}, T_{10}, U_{01}, U_{10})$$

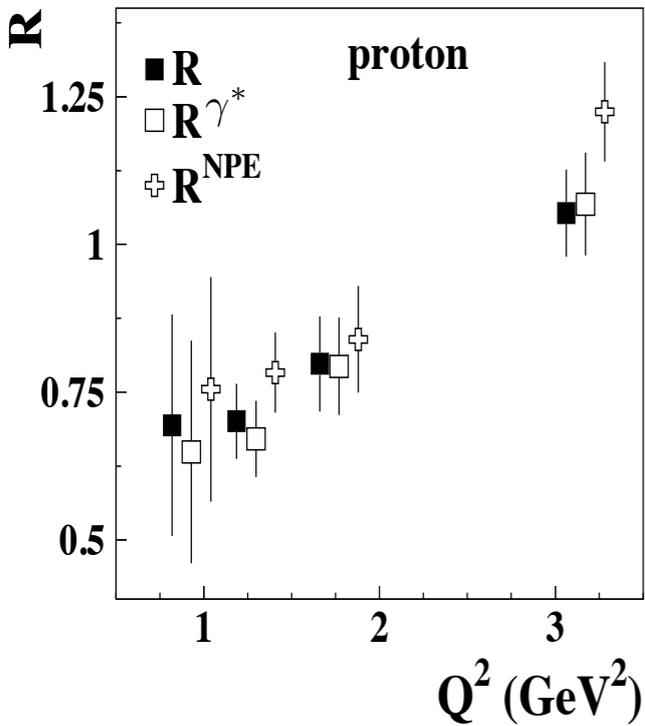
$\eta = 0$  for SCHC

$$R^{NPE} \approx R \left[ 1 + \frac{u_1}{2} (1 + \epsilon R) \right] \quad \text{with} \quad u_1 = u_1(U_{10}, U_{11}, U_{-11})$$

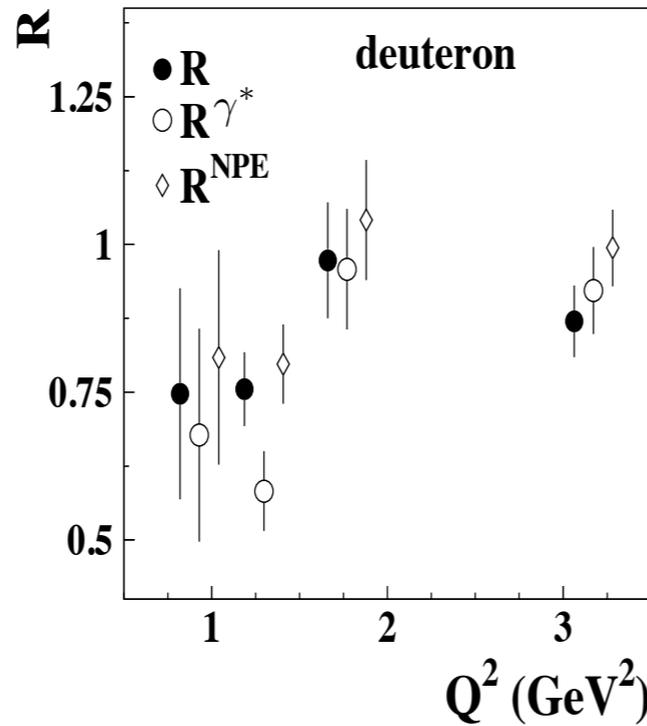
subtraction of all UPE amplitudes

# Longitudinal-to-transverse cross-section ratios

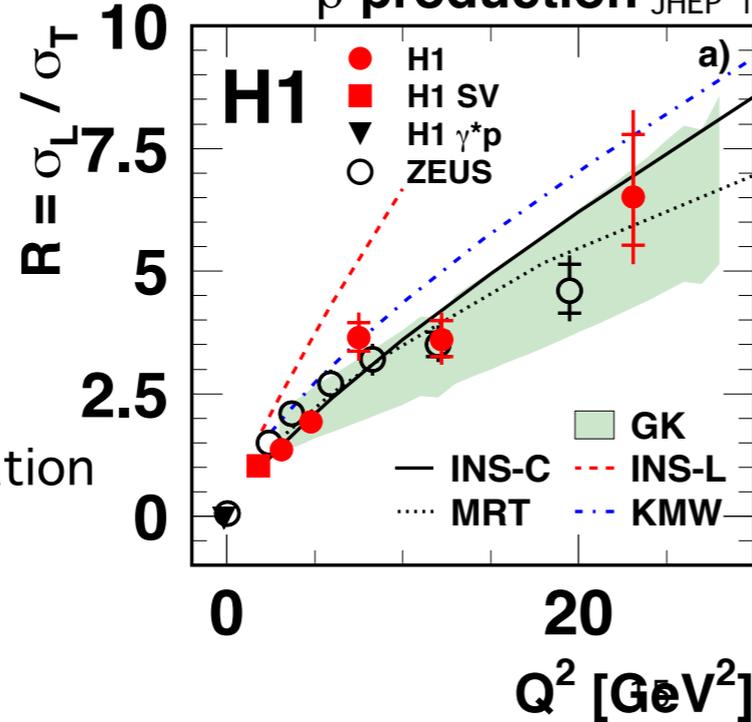
HERMES



Eur. Phys. J. C62 (2009) 659-695



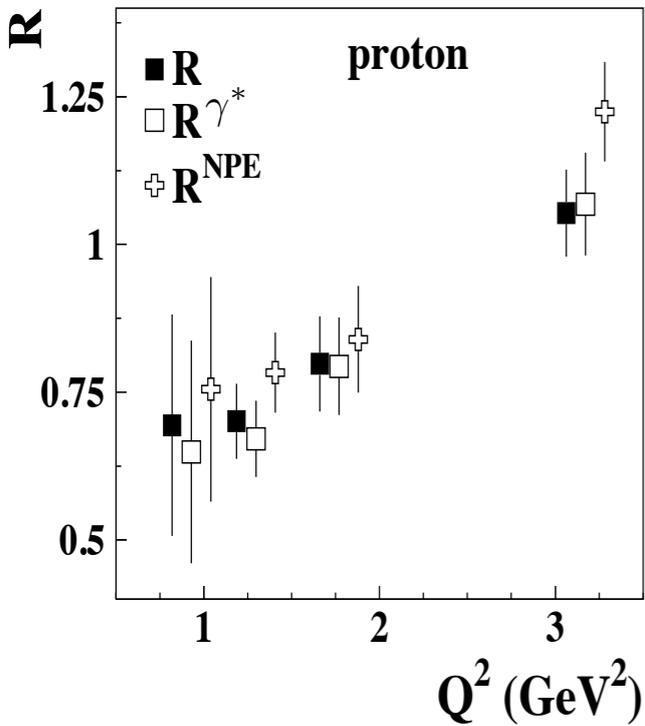
$\rho$  production JHEP 1005(2010)032



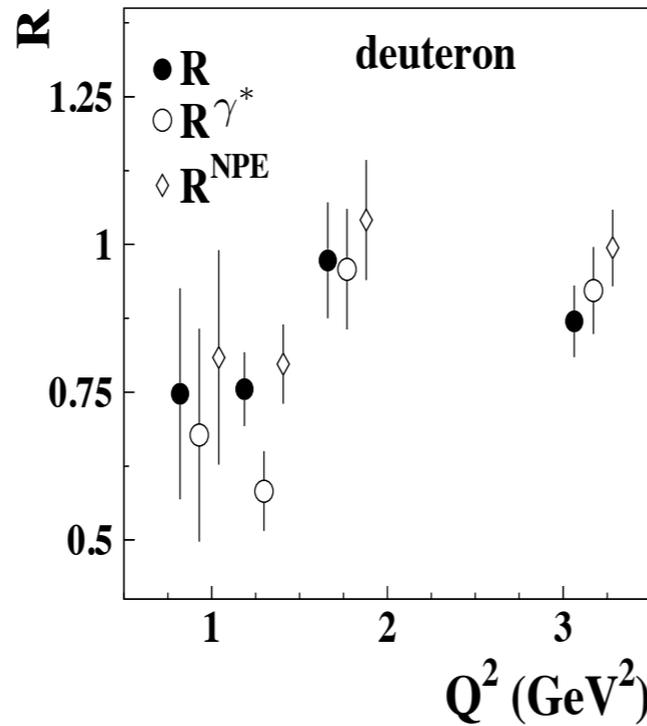
● corrected for SCHC violation  
seen in  $r_{00}^5$  and  $r_{00}^{04}$

# Longitudinal-to-transverse cross-section ratios

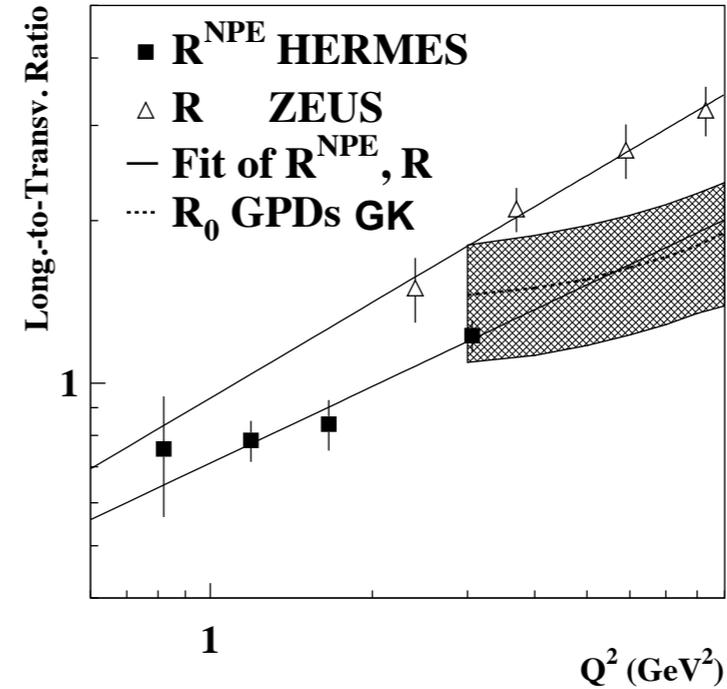
HERMES



Eur. Phys. J. C62 (2009) 659-695



Eur. Phys. J. C62 (2009) 659-695



$$R(Q^2) = c_0 \left( \frac{Q^2}{M_V^2} \right)^{c_1}$$

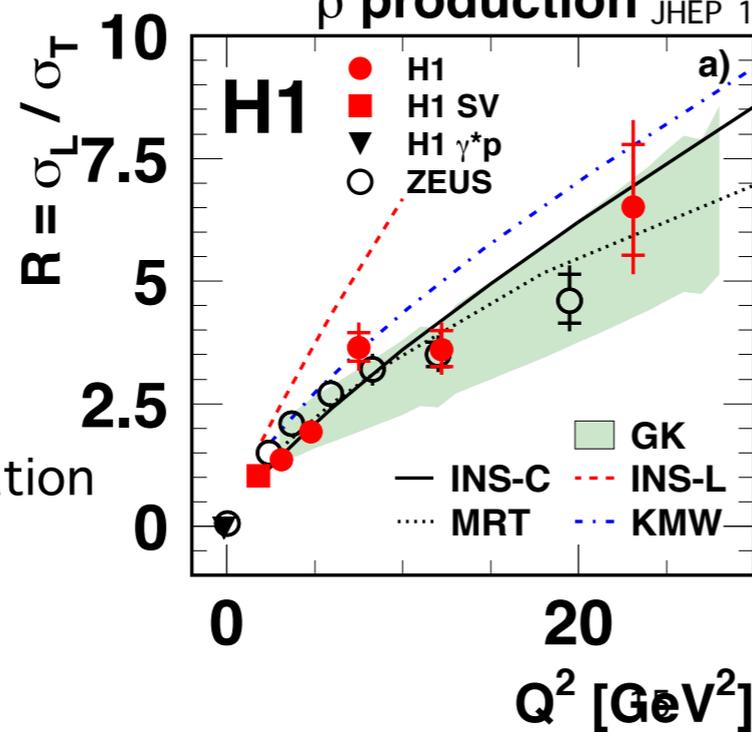
$$c_0^{\text{HERMES}} = 0.56 \pm 0.08$$

$$c_1^{\text{HERMES}} = 0.47 \pm 0.12$$

$$c_0^{\text{ZEUS}} = 0.69 \pm 0.22$$

$$c_1^{\text{ZEUS}} = 0.59 \pm 0.15$$

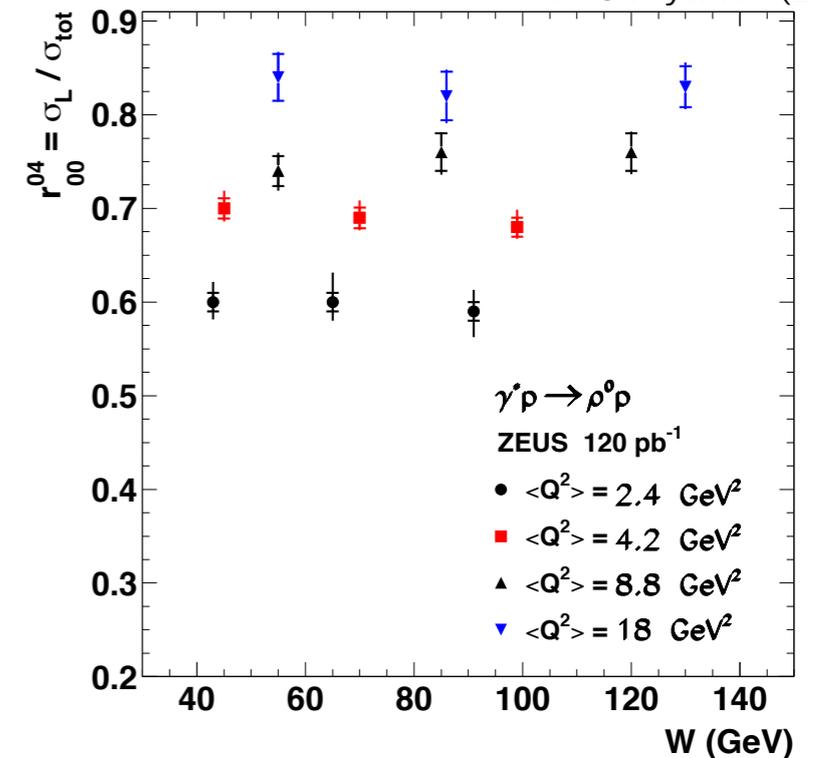
$\rho$  production JHEP 1005(2010)032



● corrected for SCHC violation  
seen in  $r_{00}^5$  and  $r_{00}^{04}$

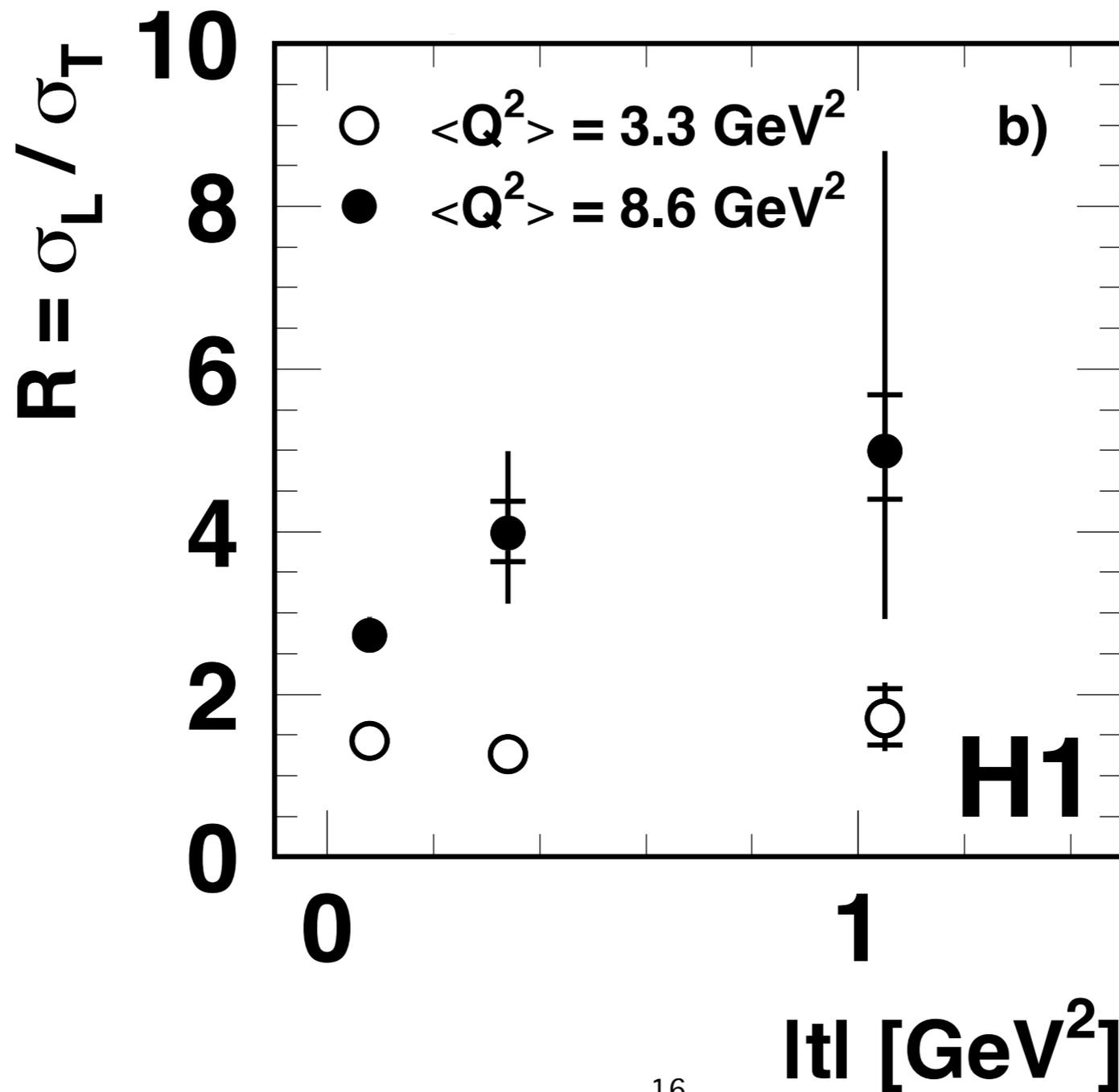
ZEUS

PMC Phys. A1 (2007) 6



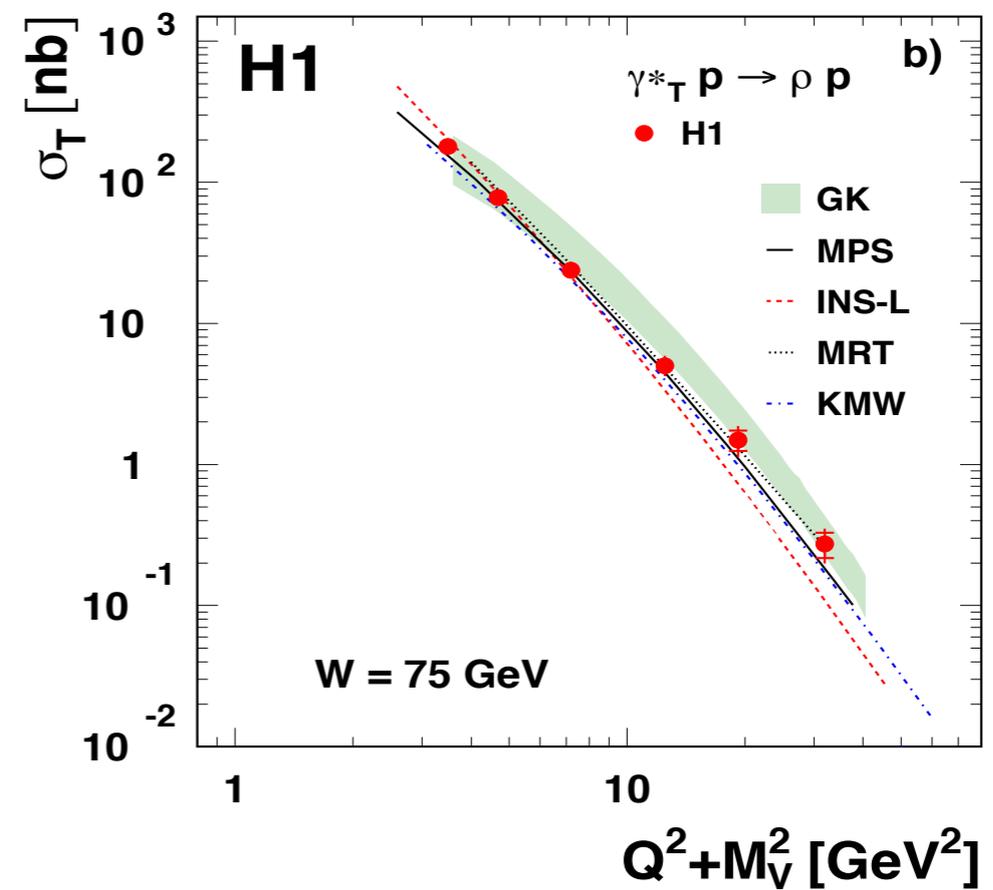
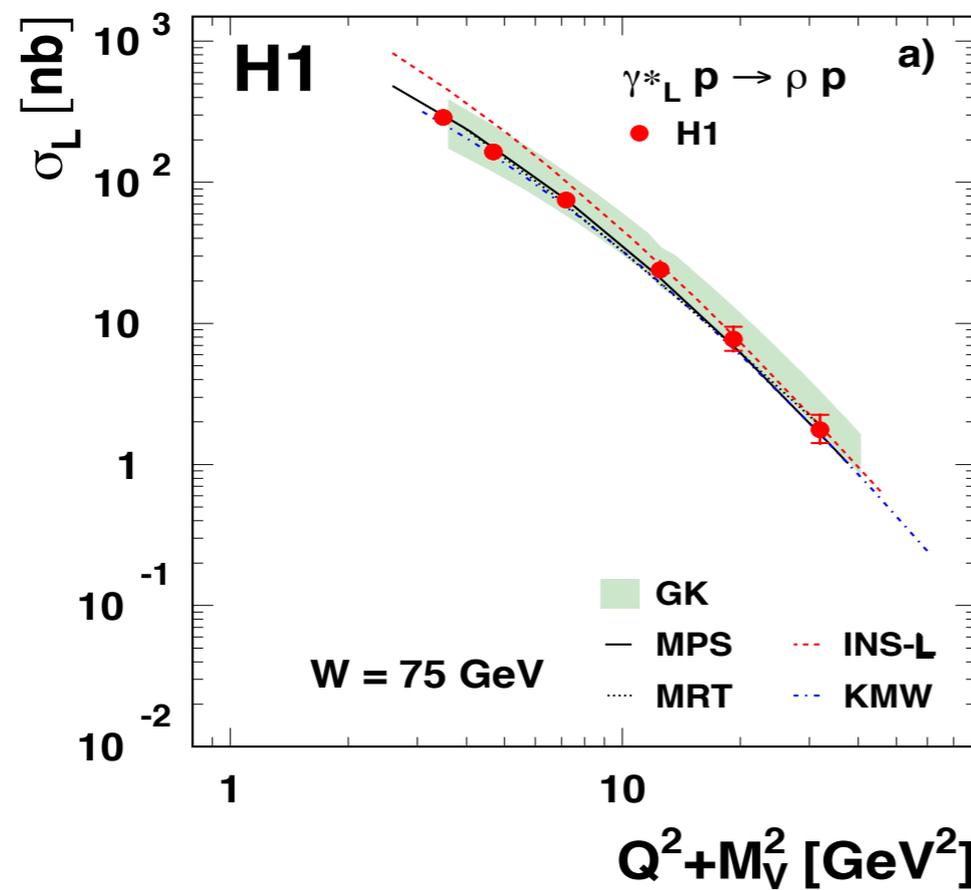
# Longitudinal-to-transverse cross-section ratios

$$R(t) \propto e^{-(b_L - b_T)|t|}$$



# Longitudinal and transverse cross sections

JHEP 1005(2010)032

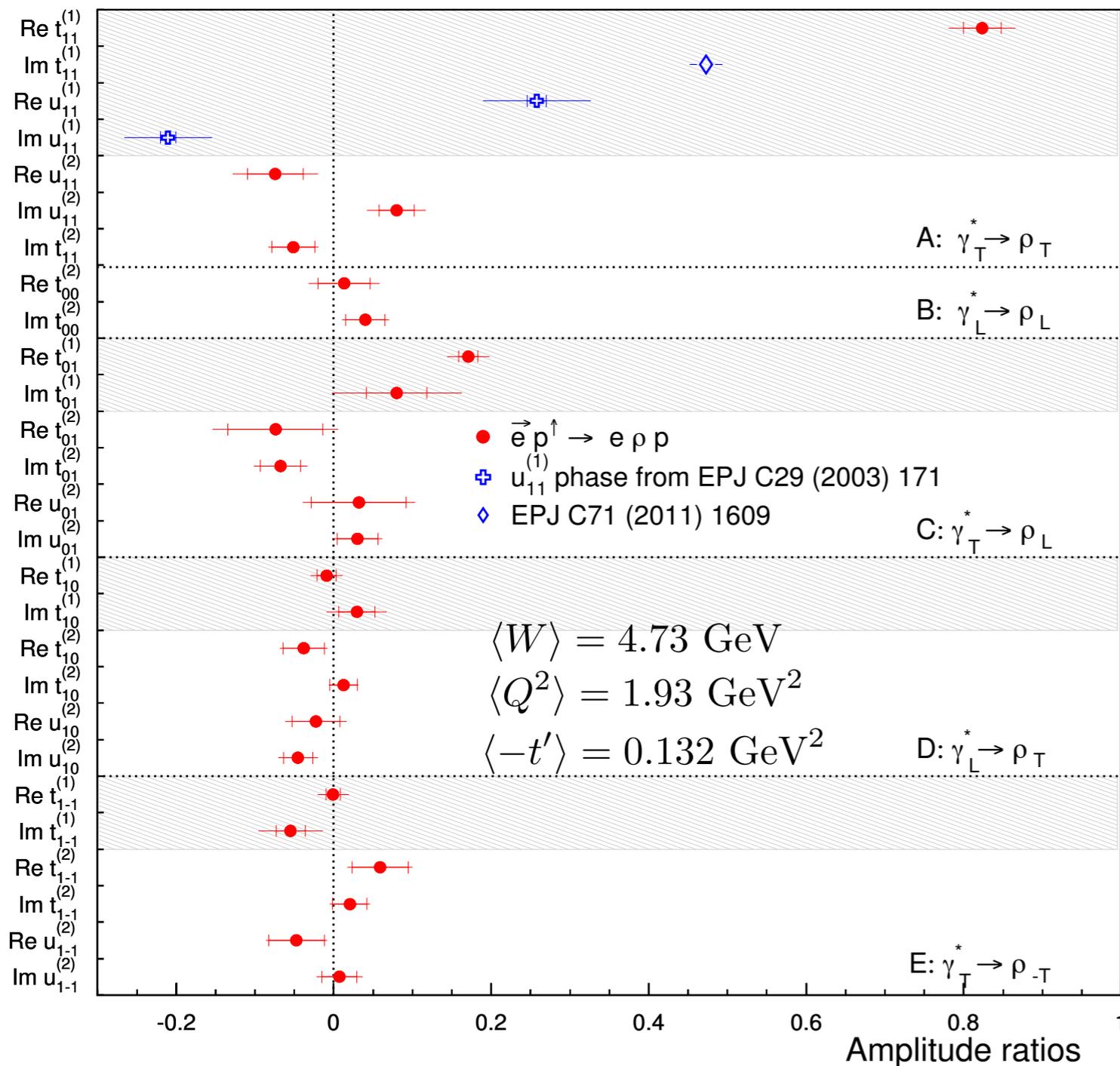


fit  $1/(Q^2 + M_V^2)^n$

$n$	
$\sigma_L(\rho)$	$\sigma_T(\rho)$
$2.17 \pm 0.09^{+0.07}_{-0.07}$	$2.86 \pm 0.07^{+0.11}_{-0.12}$

# Transversely polarized target: $\rho^0$ helicity amplitude ratios

Eur. Phys. J. C 77 (2017) 378



accessible via unpolarized target

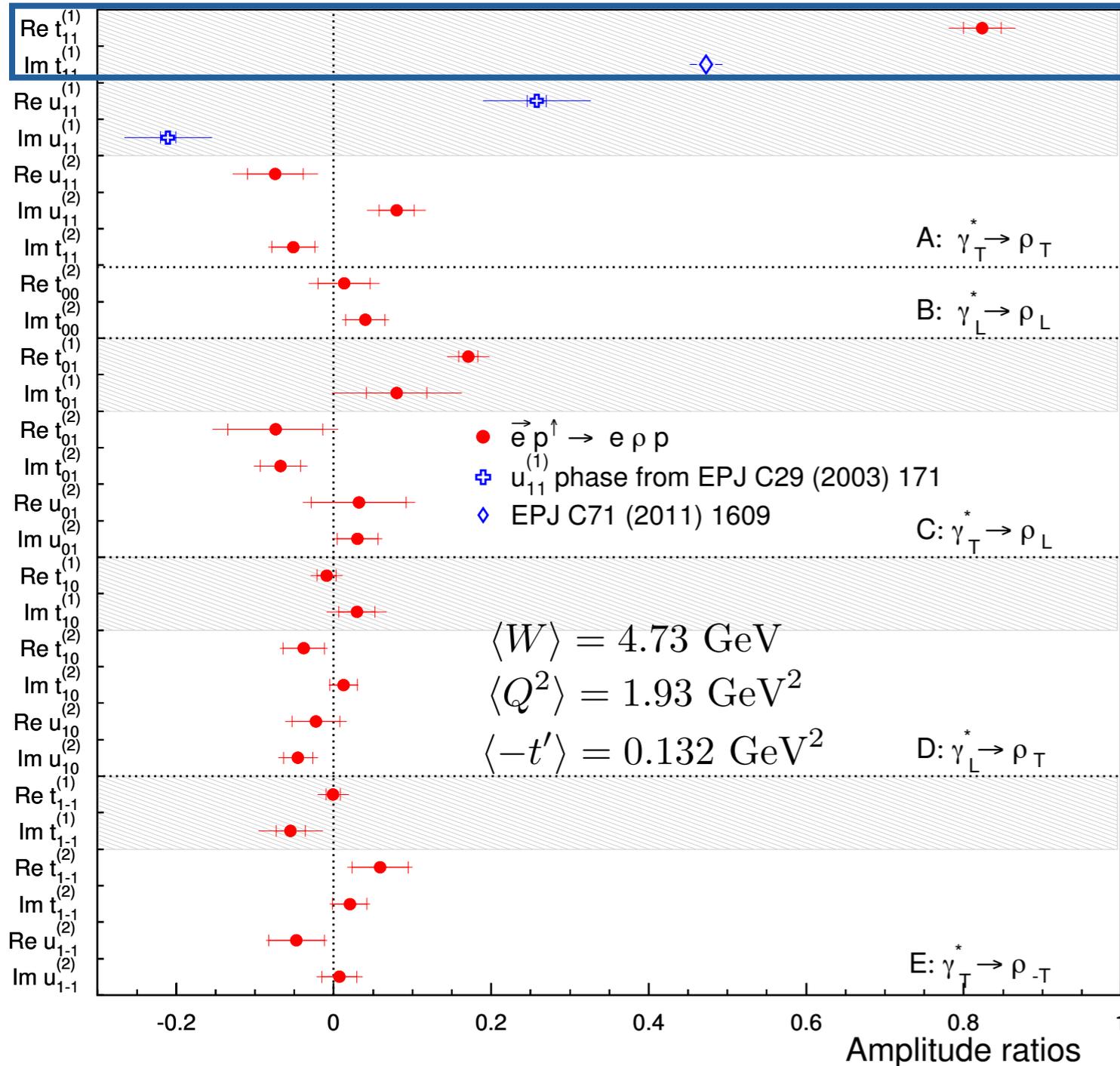
accessible via transversely polarized target

- 5 classes of helicity amplitude ratios

8% uncertainty target polarization  
2% uncertainty beam polarization

# Transversely polarized target: $\rho^0$ helicity amplitude ratios

Eur. Phys. J. C 77 (2017) 378



accessible via unpolarized target

accessible via transversely polarized target

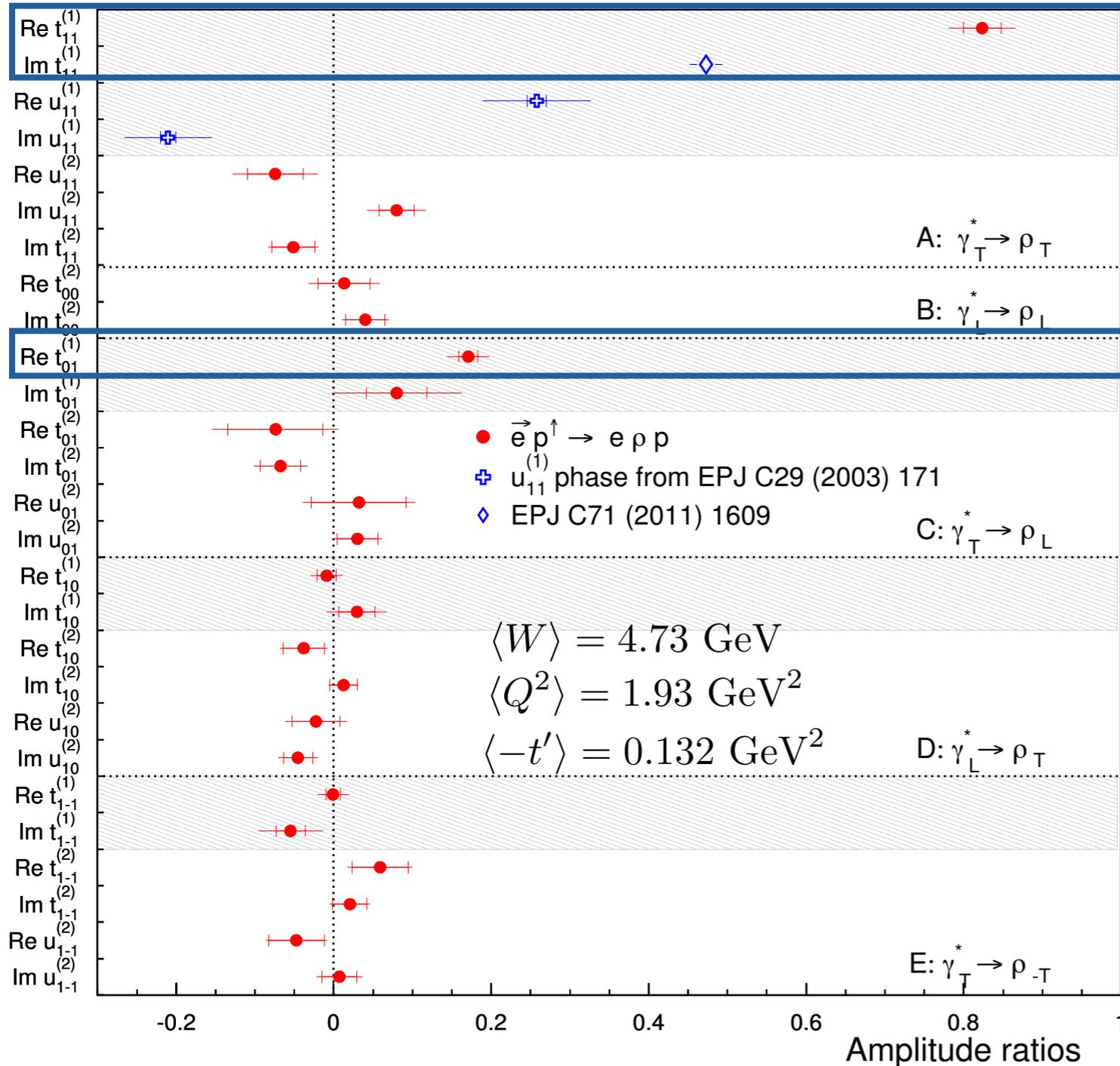
- 5 classes of helicity amplitude ratios

- dominant amplitude: natural parity nucleon-helicity non-flip  $t_{11}^{(1)}$  ( $\neq 0$  by  $>5\sigma$ )

8% uncertainty target polarization  
2% uncertainty beam polarization

# Transversely polarized target: $\rho^0$ helicity amplitude ratios

Eur. Phys. J. C 77 (2017) 378



accessible via unpolarized target

accessible via transversely polarized target

- 5 classes of helicity amplitude ratios

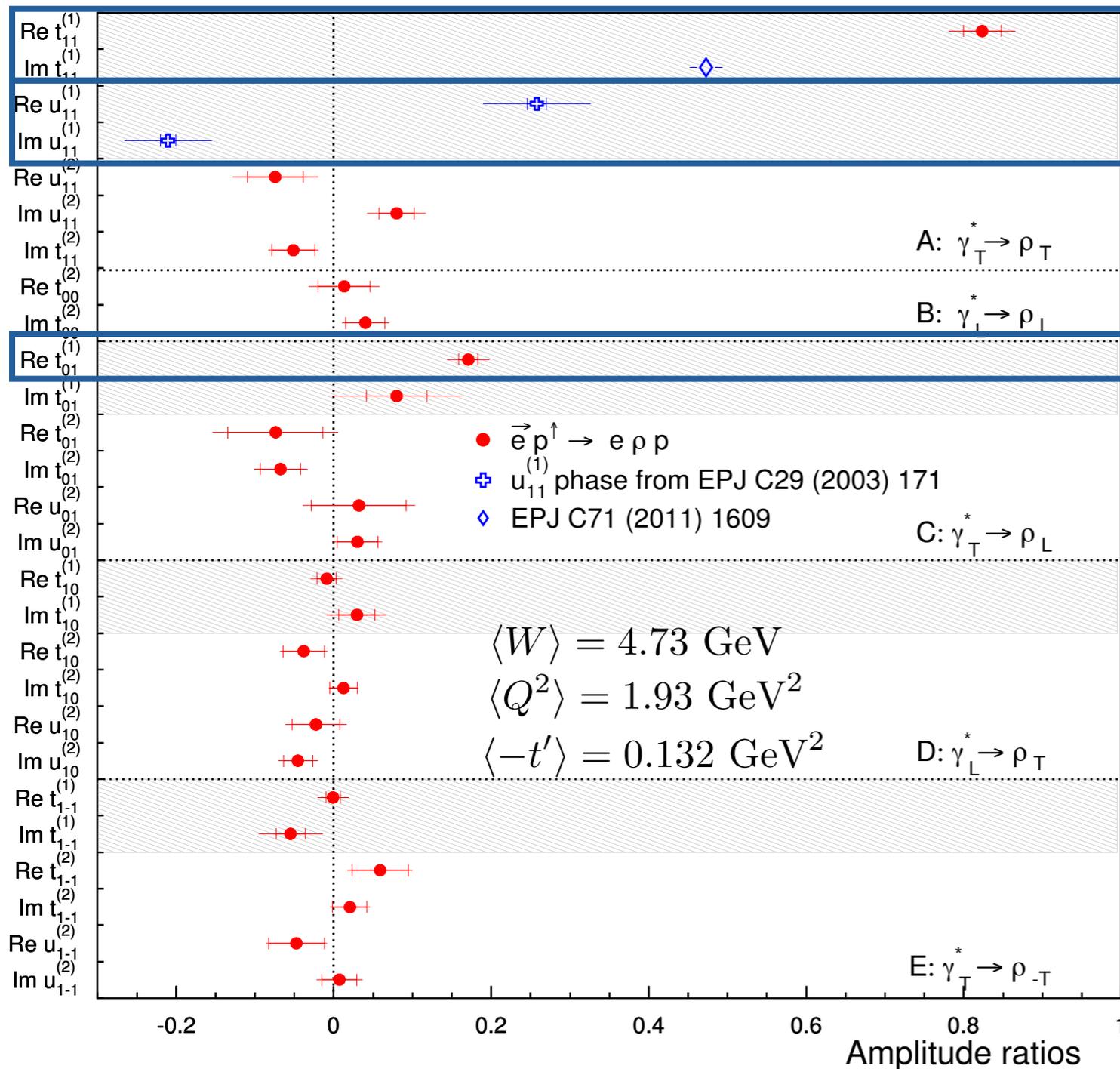
- dominant amplitude: natural parity nucleon-helicity non-flip  $t_{11}^{(1)}$  ( $\neq 0$  by  $>5\sigma$ )

- Significant nucleon-helicity non-flip  $\Re t_{01}^{(1)}$  ( $\neq 0$  by  $5\sigma$ )

8% uncertainty target polarization  
2% uncertainty beam polarization

# Transversely polarized target: $\rho^0$ helicity amplitude ratios

Eur. Phys. J. C 77 (2017) 378



accessible via unpolarized target

accessible via transversely polarized target

- 5 classes of helicity amplitude ratios

- dominant amplitude: natural parity nucleon-helicity non-flip  $t_{11}^{(1)}$  ( $\neq 0$  by  $>5\sigma$ )

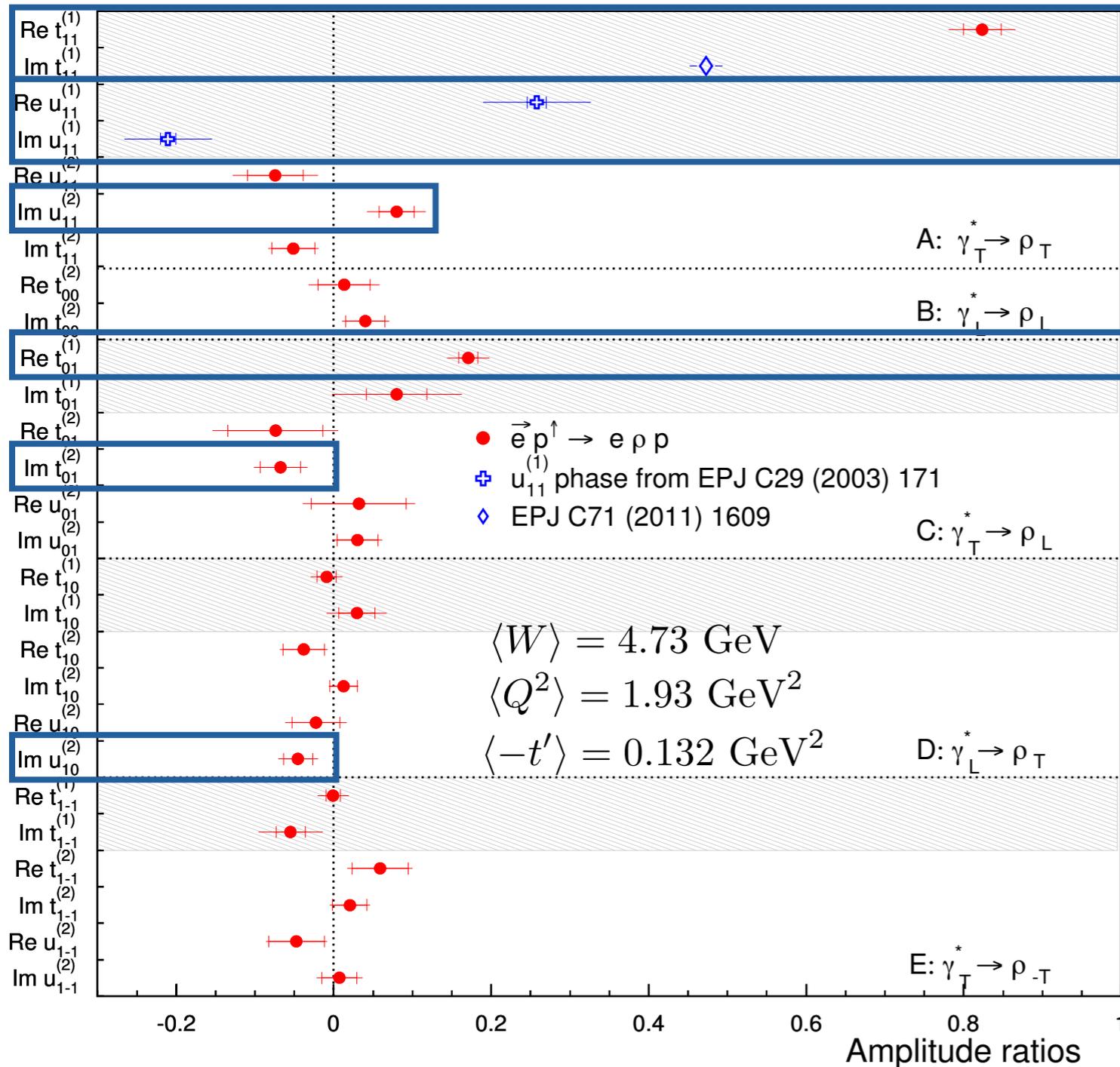
- Significant nucleon-helicity non-flip  $\Re t_{01}^{(1)}$  ( $\neq 0$  by  $5\sigma$ )

- unnatural parity nucleon-helicity non-flip  $u_{11}^{(1)} \neq 0$  by  $4\sigma$

8% uncertainty target polarization  
2% uncertainty beam polarization

# Transversely polarized target: $\rho^0$ helicity amplitude ratios

Eur. Phys. J. C 77 (2017) 378



accessible via unpolarized target

accessible via transversely polarized target

- 5 classes of helicity amplitude ratios

- dominant amplitude: natural parity nucleon-helicity non-flip  $t_{11}^{(1)}$  ( $\neq 0$  by  $>5\sigma$ )

- Significant nucleon-helicity non-flip  $\Re t_{01}^{(1)}$  ( $\neq 0$  by  $5\sigma$ )

- unnatural parity nucleon-helicity non-flip  $u_{11}^{(1)} \neq 0$  by  $4\sigma$

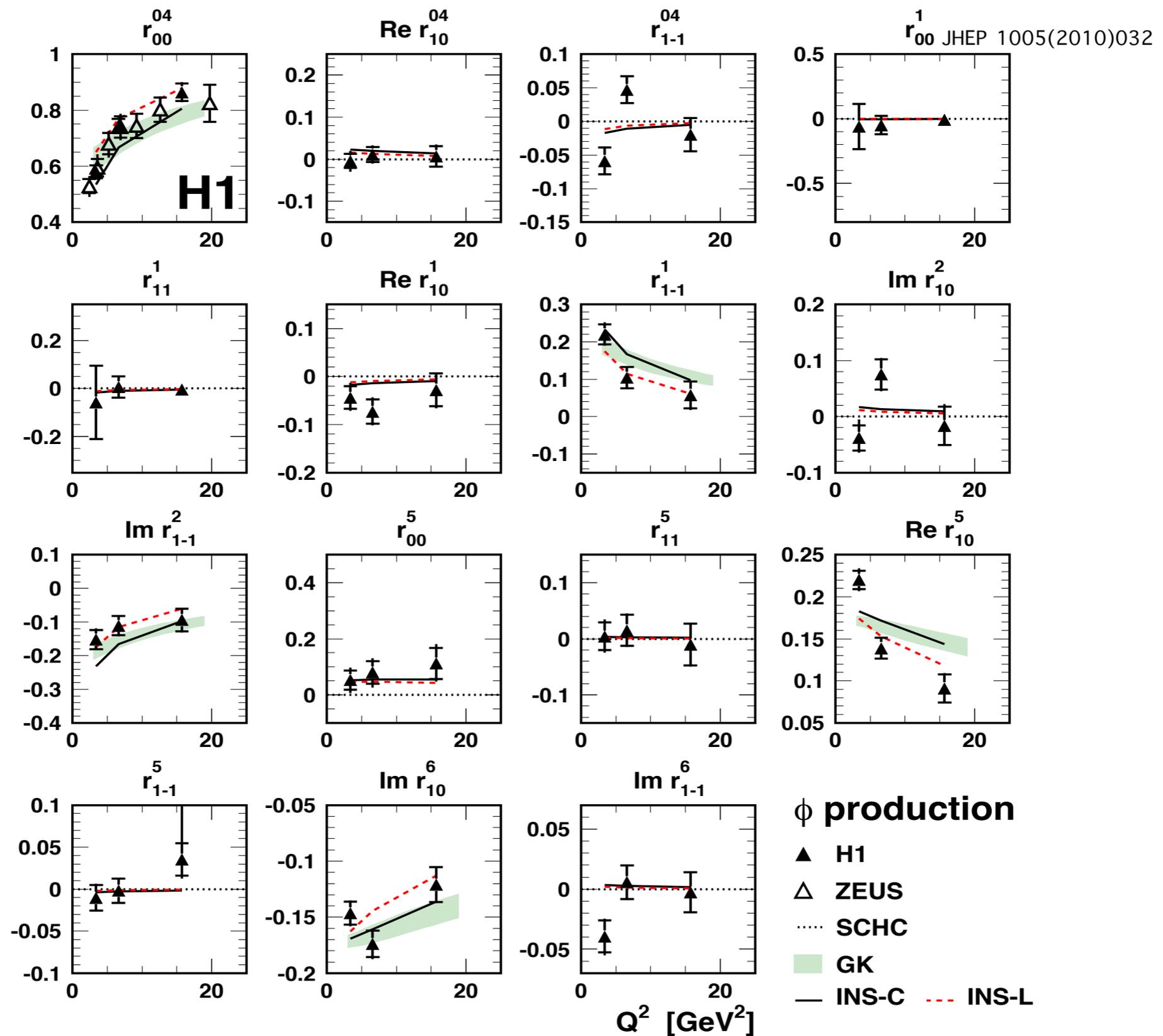
- nucleon-helicity flip  $\Im t_{01}^{(2)}, \Im u_{11}^{(2)}, \Im u_{10}^{(2)} \neq 0$  by  $2\sigma$

8% uncertainty target polarization  
2% uncertainty beam polarization

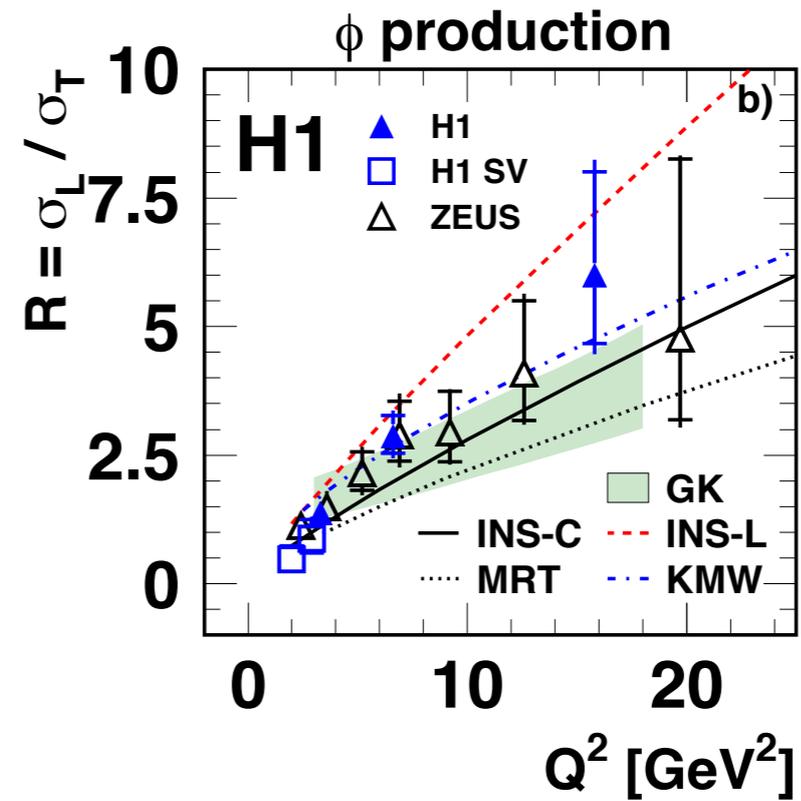
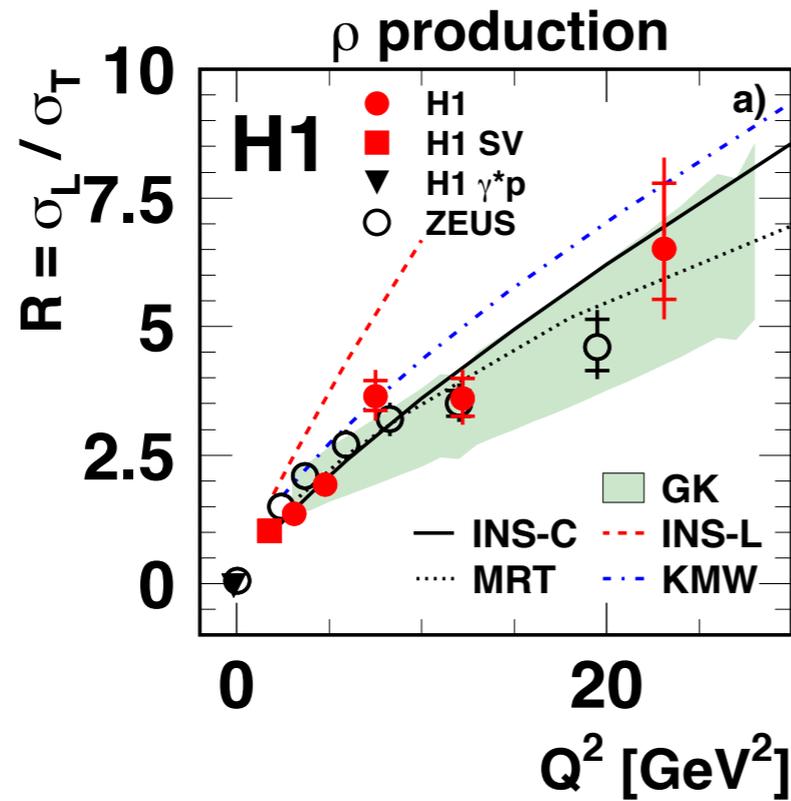
Exclusive  $\phi$

- unpolarized H target

# $Q^2$ dependence

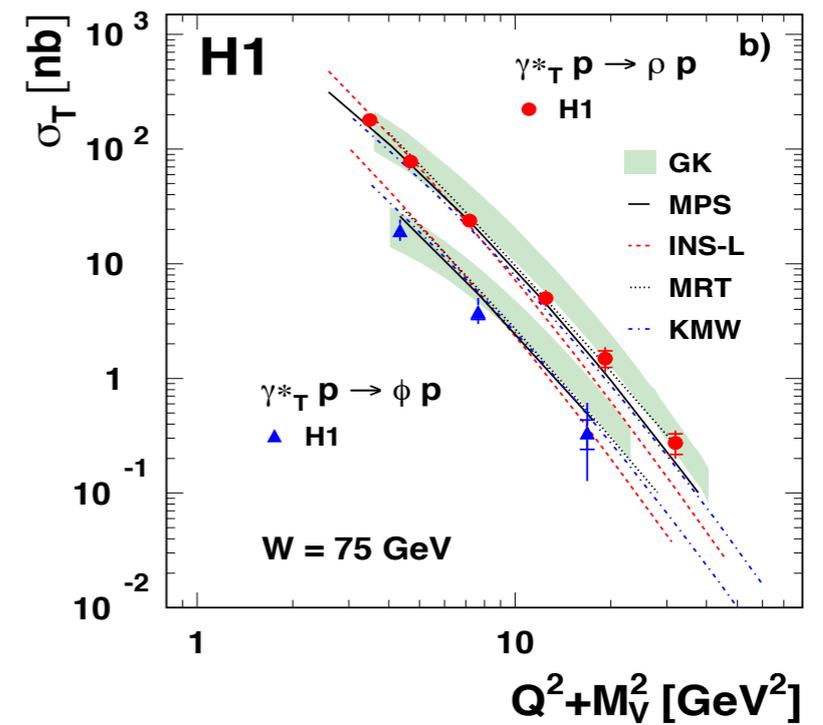
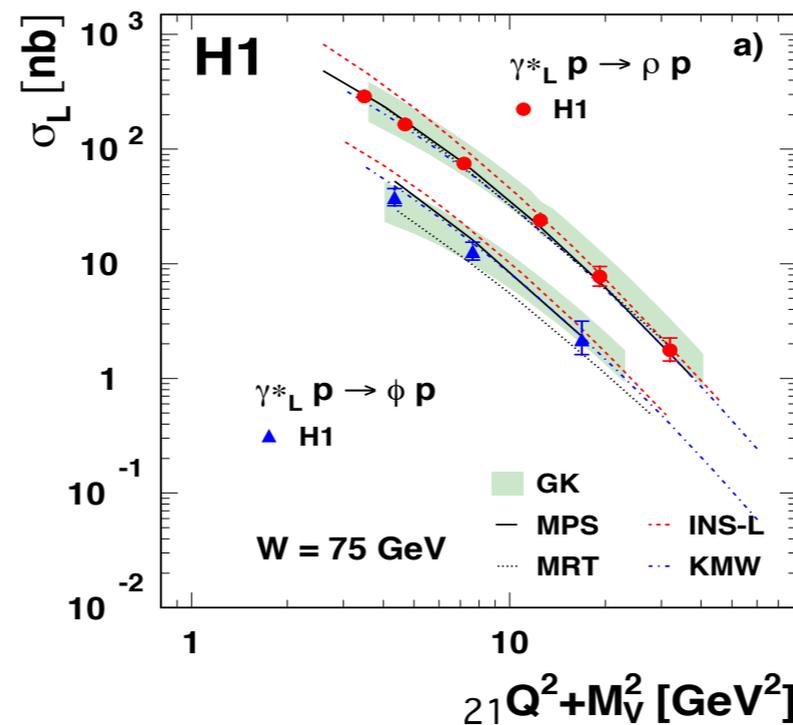


# Longitudinal and transverse cross sections



fit  $1/(Q^2 + M_V^2)^n$

$n$	
$\sigma_L(\rho)$	$\sigma_T(\rho)$
$2.17 \pm 0.09^{+0.07}_{-0.07}$	$2.86 \pm 0.07^{+0.11}_{-0.12}$
$\sigma_L(\phi)$	$\sigma_T(\phi)$
$2.06 \pm 0.49^{+0.09}_{-0.09}$	$2.97 \pm 0.52^{+0.14}_{-0.16}$

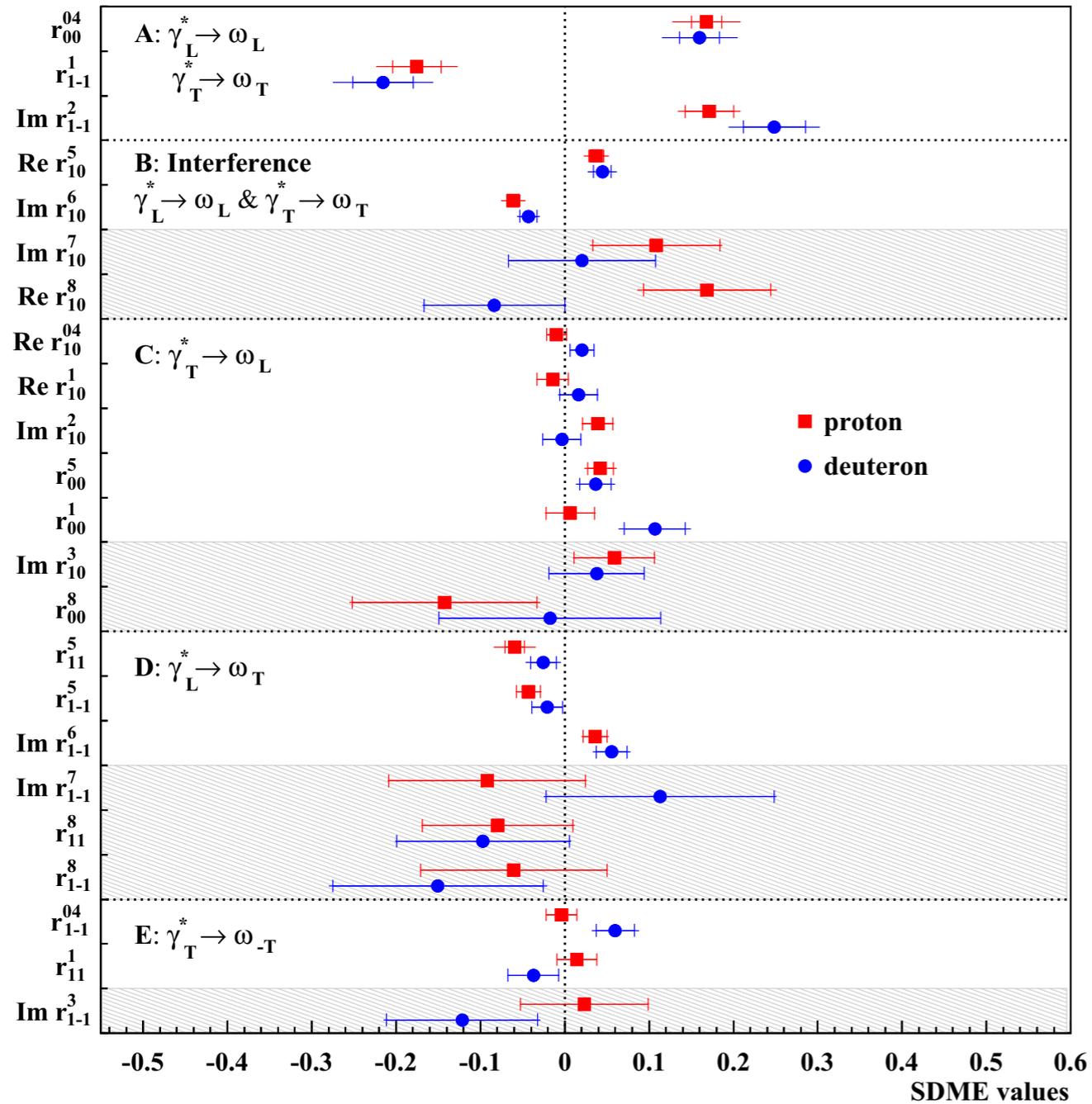


# Exclusive $\omega$

- unpolarized H and D targets
- transversely polarized H target

# Results $\omega$ SDMEs

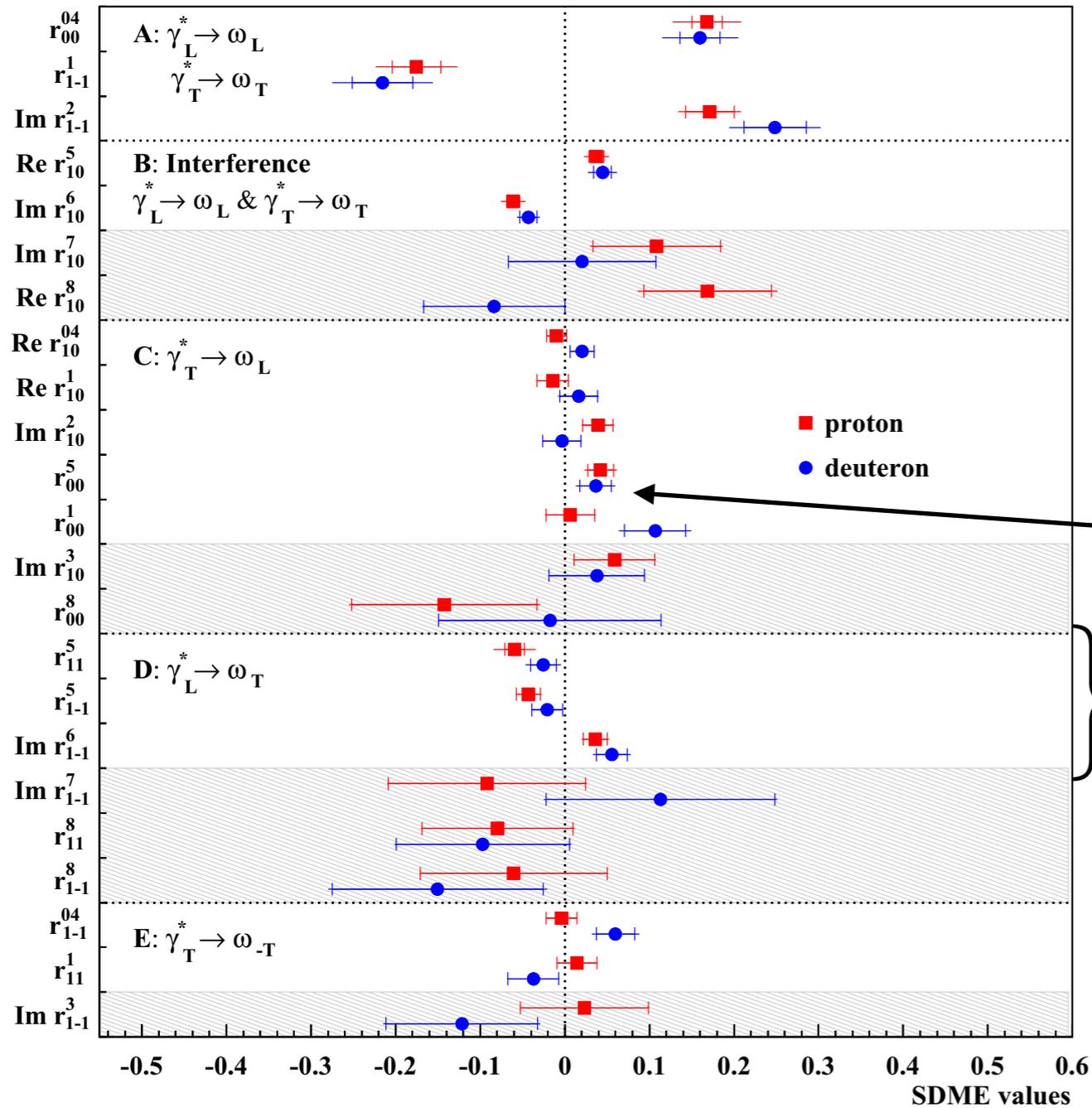
Eur. Phys. J. C 74 (2014) 3110



- 5 classes of SDMEs
- unpolarized and polarized SDMEs
- proton & deuteron similar

# Results $\omega$ SDMEs

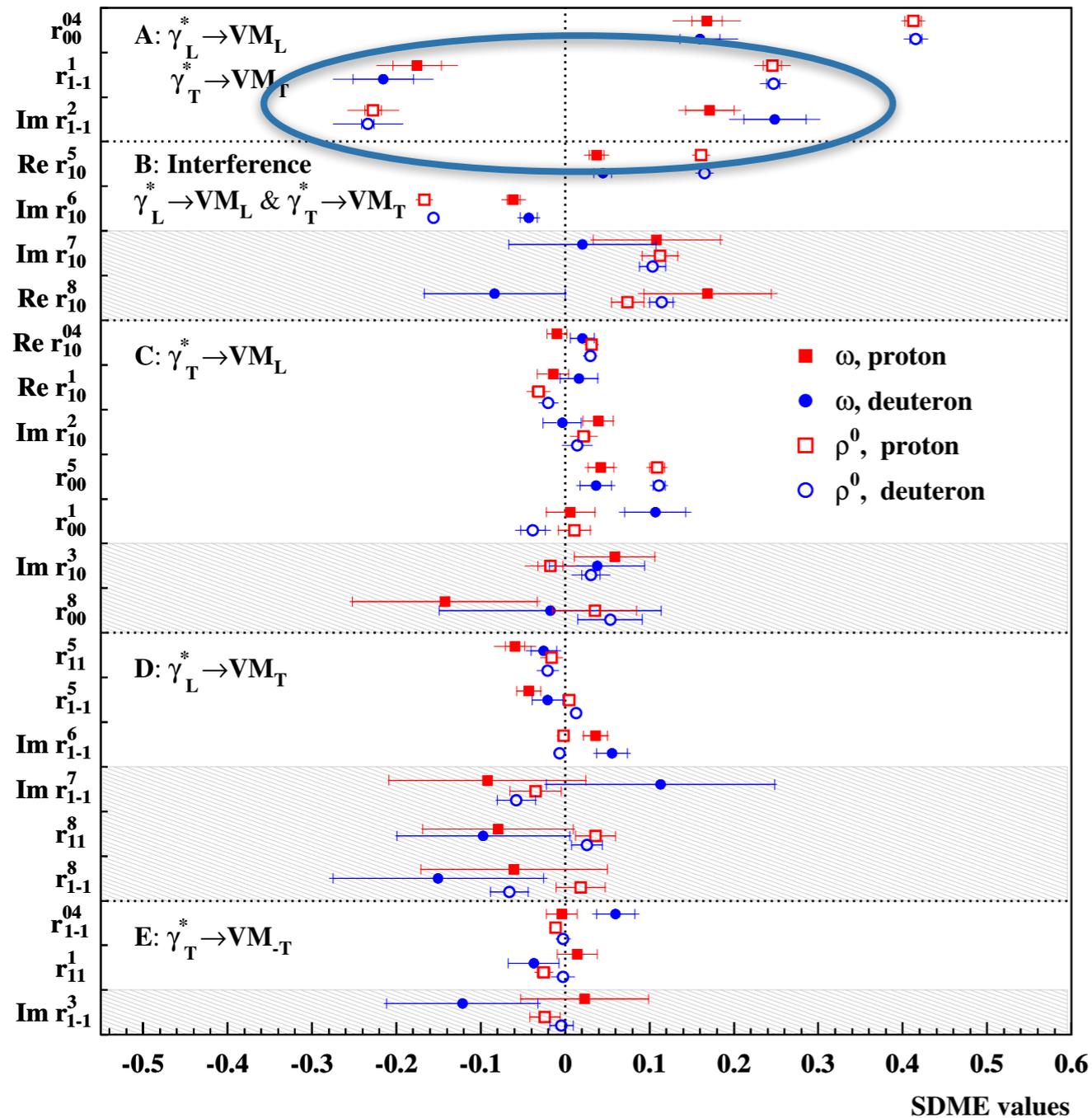
Eur. Phys. J. C 74 (2014) 3110



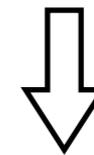
- 5 classes of SDMEs
- unpolarized and polarized SDMEs
- proton & deuteron similar
- s-channel helicity conservation ( $\lambda_{\gamma^*} = \lambda_{\omega}$ ):
  - fulfilled for class A & B
  - class C - slight violation:
- class D - slight violation:
  - $r_{00}^5 \neq 0$  by  $3(2)\sigma$  for p(d)
  - $r_{11}^5 + r_{1-1}^5 - \Im r_{1-1}^6 \neq 0$  by  $3(2.5)\sigma$  for p(d)

# Results $\omega$ and $\rho^0$ SDMEs

Eur. Phys. J. C 74 (2014) 3110



- $\omega$ :  $r_{1-1}^1 < 0$  and  $\Im r_{1-1}^2 > 0$
- $\rho$ :  $r_{1-1}^1 > 0$  and  $\Im r_{1-1}^2 < 0$



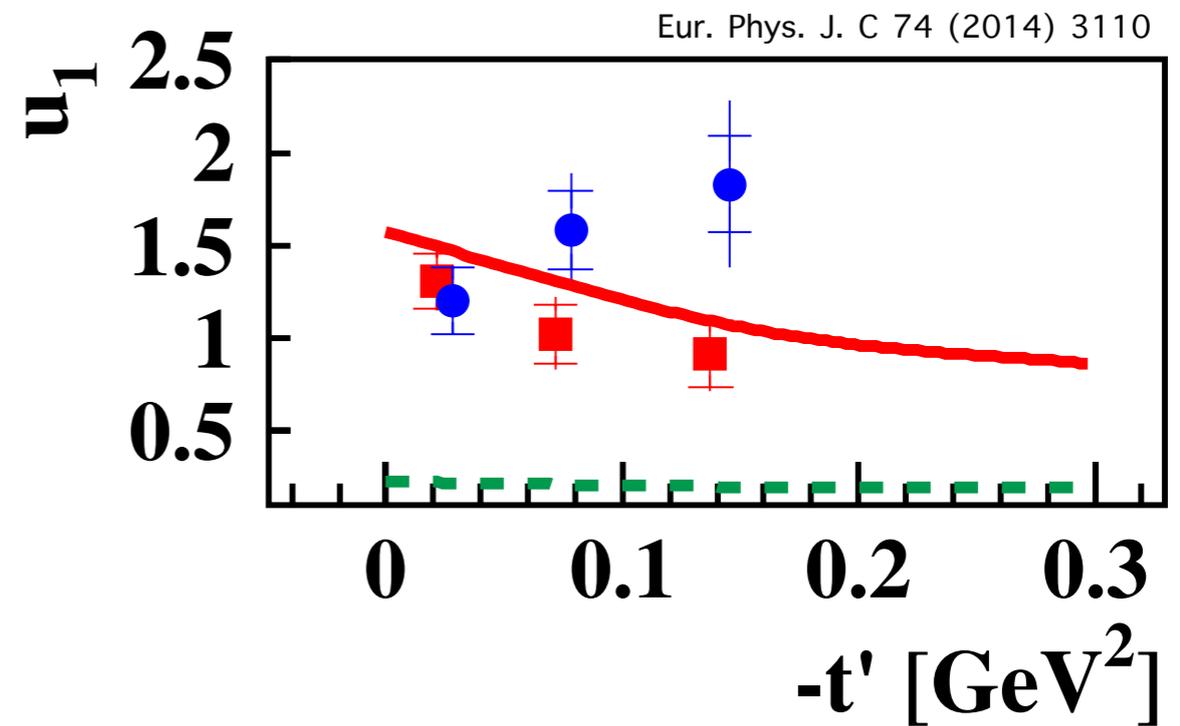
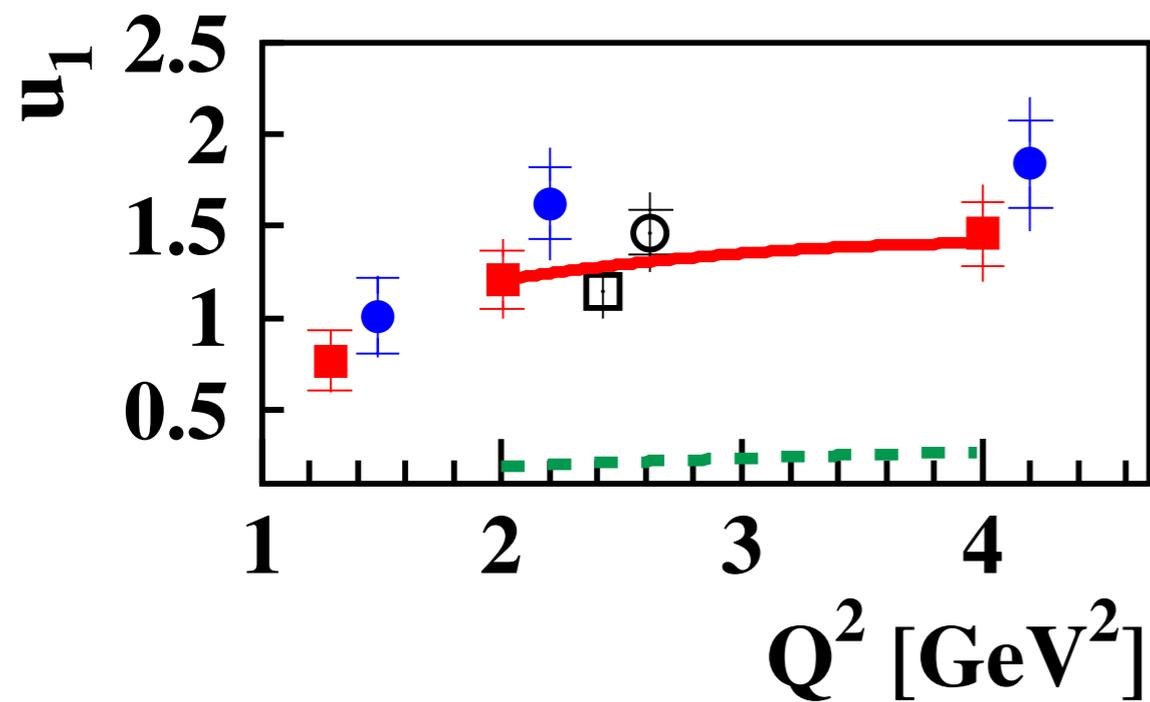
- $\omega$ : large unnatural parity exchange
- $\rho$ : large natural parity exchange

exclusive  $\rho^0$ : Eur. Phys. J. C 62 (2009) 659

# Test of unnatural parity exchange

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$$

$$\propto 2\epsilon|U_{10}|^2 + |U_{11} + U_{-11}|^2 \quad (\text{U=unnatural-parity amplitude})$$



- large unnatural parity exchange seen

# GK model

model for protons - S. Goloskokov and P. Kroll,  
Eur. Phys. J. C 50 (2007) 829; 53 (2008) 367, Eur. Phys. J. A 50 (2014) 146

$$F_{\lambda_V \frac{1}{2} \lambda_\gamma = \lambda_V \frac{1}{2}} \propto \sum_{q,g} \mathcal{I} \left[ \mathcal{A} \times \left( H^a, \frac{\xi^2}{1-\xi^2} E^a \right) + \mathcal{A}' \times \left( \tilde{H}^a, \frac{\xi^2}{1-\xi^2} \tilde{E}^a \right) \right]$$
$$F_{\lambda_V - \frac{1}{2} \lambda_\gamma = \lambda_V \frac{1}{2}} \propto \sum_{q,g} \mathcal{I} \left[ \mathcal{A} \times E^a + \mathcal{A}' \times \xi \tilde{E}^a \right]$$

# GK model

model for protons - S. Goloskokov and P. Kroll,

Eur. Phys. J. C 50 (2007) 829; 53 (2008) 367, Eur. Phys. J. A 50 (2014) 146

$$F_{\lambda_V \frac{1}{2} \lambda_\gamma = \lambda_V \frac{1}{2}} \propto \sum_{q,g} \mathcal{I} \left[ \mathcal{A} \times \left( H^a, \frac{\xi^2}{1-\xi^2} E^a \right) + \mathcal{A}' \times \left( \tilde{H}^a, \frac{\xi^2}{1-\xi^2} \tilde{E}^a \right) \right]$$

$$F_{\lambda_V -\frac{1}{2} \lambda_\gamma = \lambda_V \frac{1}{2}} \propto \sum_{q,g} \mathcal{I} \left[ \mathcal{A} \times E^a + \mathcal{A}' \times \xi \tilde{E}^a \right]$$

natural parity  
unnatural parity

# GK model

model for protons - S. Goloskokov and P. Kroll,  
 Eur. Phys. J. C 50 (2007) 829; 53 (2008) 367, Eur. Phys. J. A 50 (2014) 146

$$F_{\lambda_V \frac{1}{2} \lambda_\gamma = \lambda_V \frac{1}{2}} \propto \sum_{q,g} \mathcal{I} \left[ \mathcal{A} \times \left( H^a, \frac{\xi^2}{1-\xi^2} E^a \right) + \mathcal{A}' \times \left( \tilde{H}^a, \frac{\xi^2}{1-\xi^2} \tilde{E}^a \right) \right]$$

$$F_{\lambda_V \frac{1}{2} \lambda_\gamma = \lambda_V \frac{1}{2}} \propto \sum_{q,g} \mathcal{I} \left[ \mathcal{A} \times E^a + \mathcal{A}' \times \xi \tilde{E}^a \right]$$

natural parity

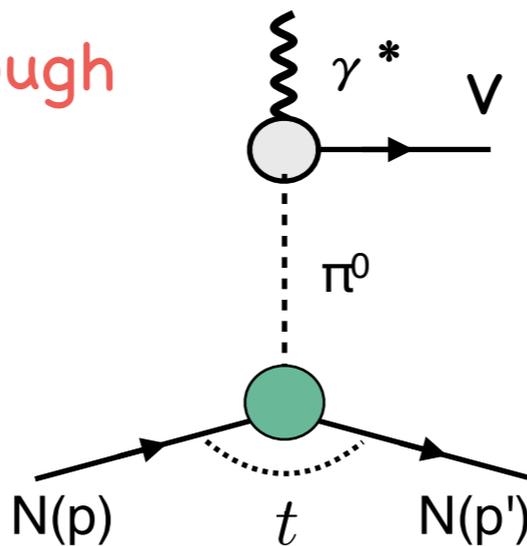
unnatural parity

Factorization only proven for  $\gamma_L^* \rightarrow V_L$ .

Assumed for other transitions.

IR singularities regularised by modified perturbative approach.

Pion pole  $\left( \propto \frac{1}{t - m_\pi^2} \right)$  through  
 one-particle exchange



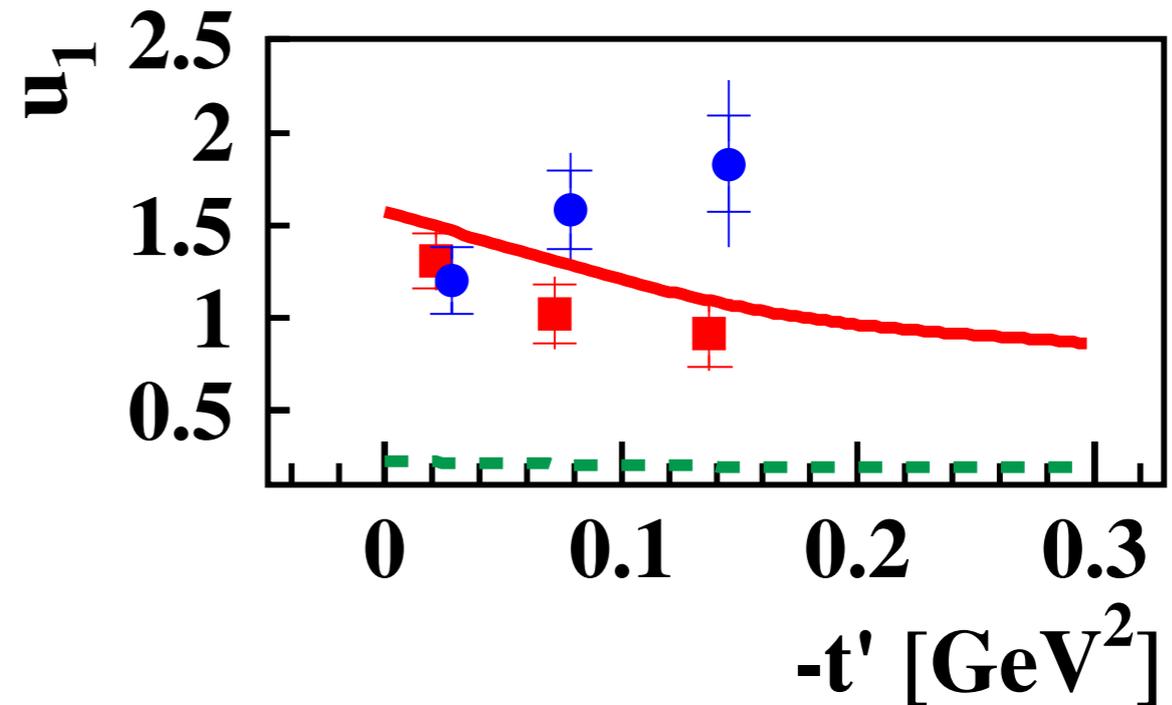
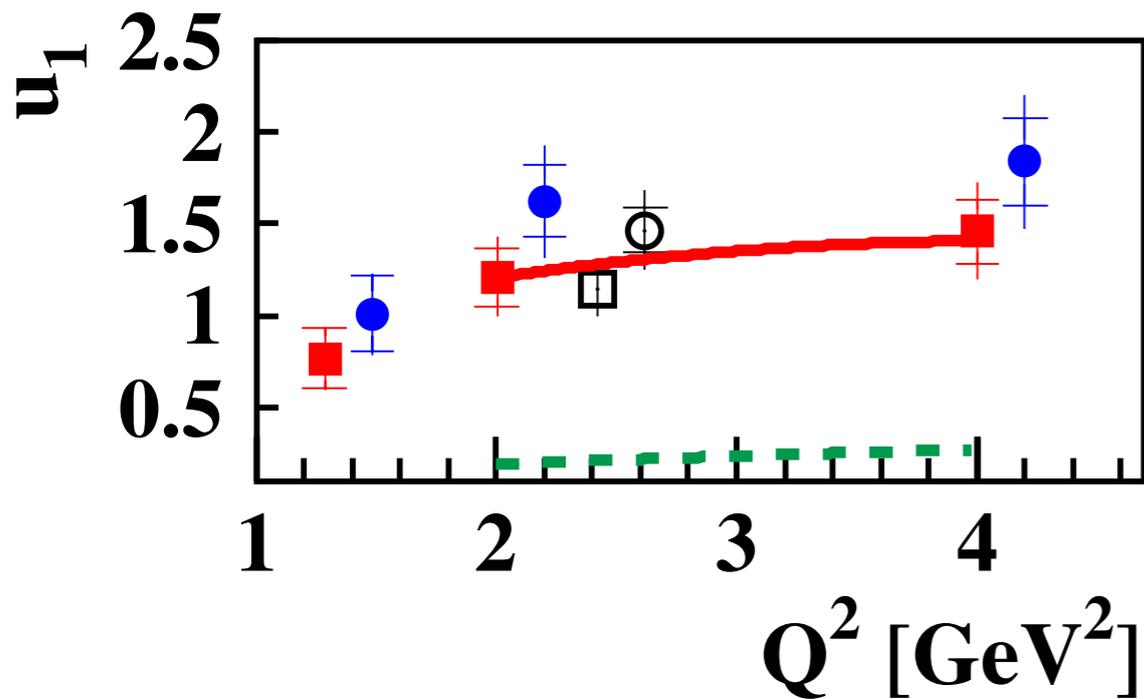
$$g_{\gamma^* \pi V}(Q^2, t) \simeq g_{\pi V}(Q^2)$$

at small  $t$

# $\pi\omega$ transition form factor extracted from $\omega$ SDMEs

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$$

GK, Eur. Phys. J. A 50 (2014) 146  
HERMES, Eur. Phys. J. C 74 (2014) 3110

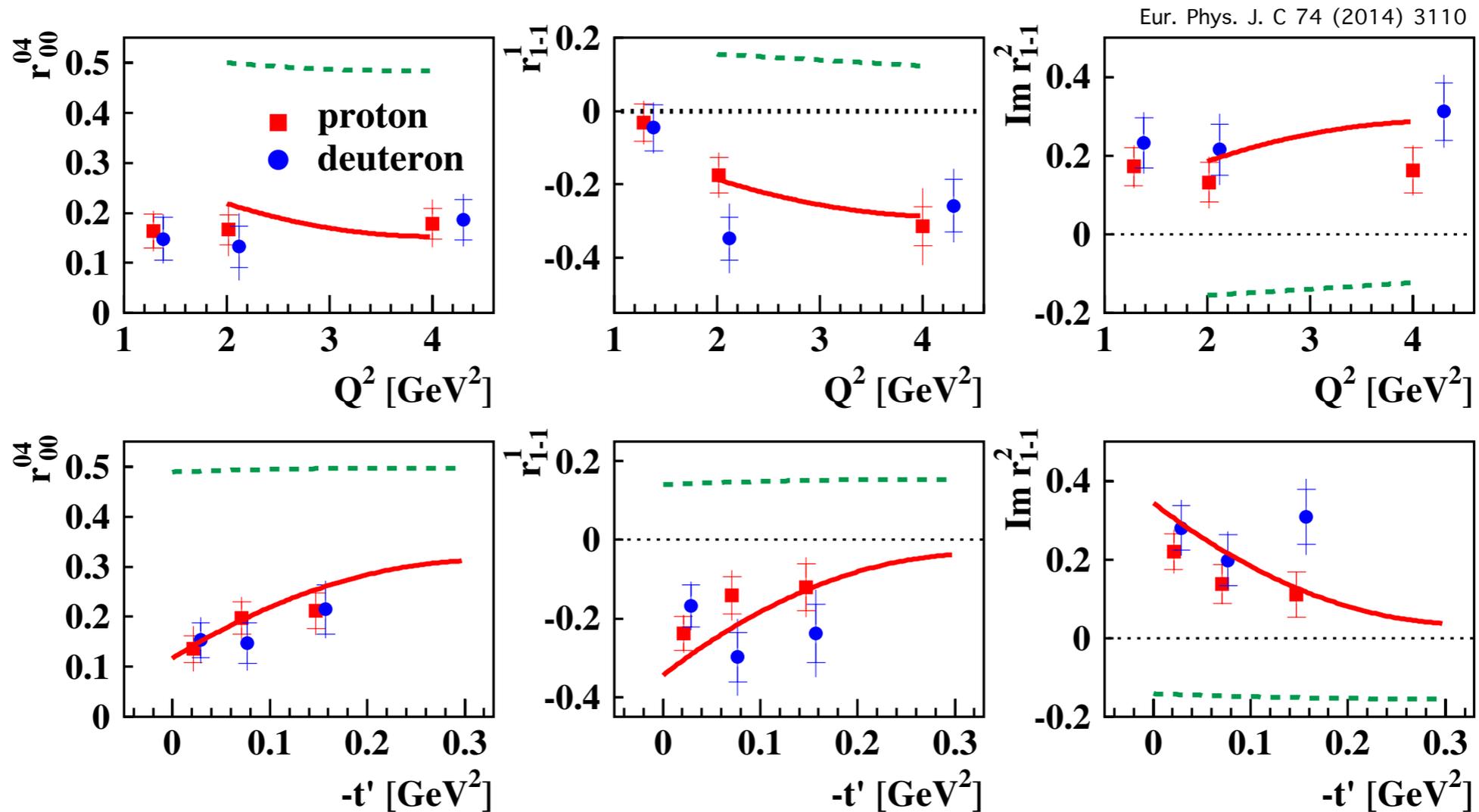


without pion-pole contribution  
with pion-pole contribution

Only magnitude of transition form factor, not sign

# Kinematic dependencies

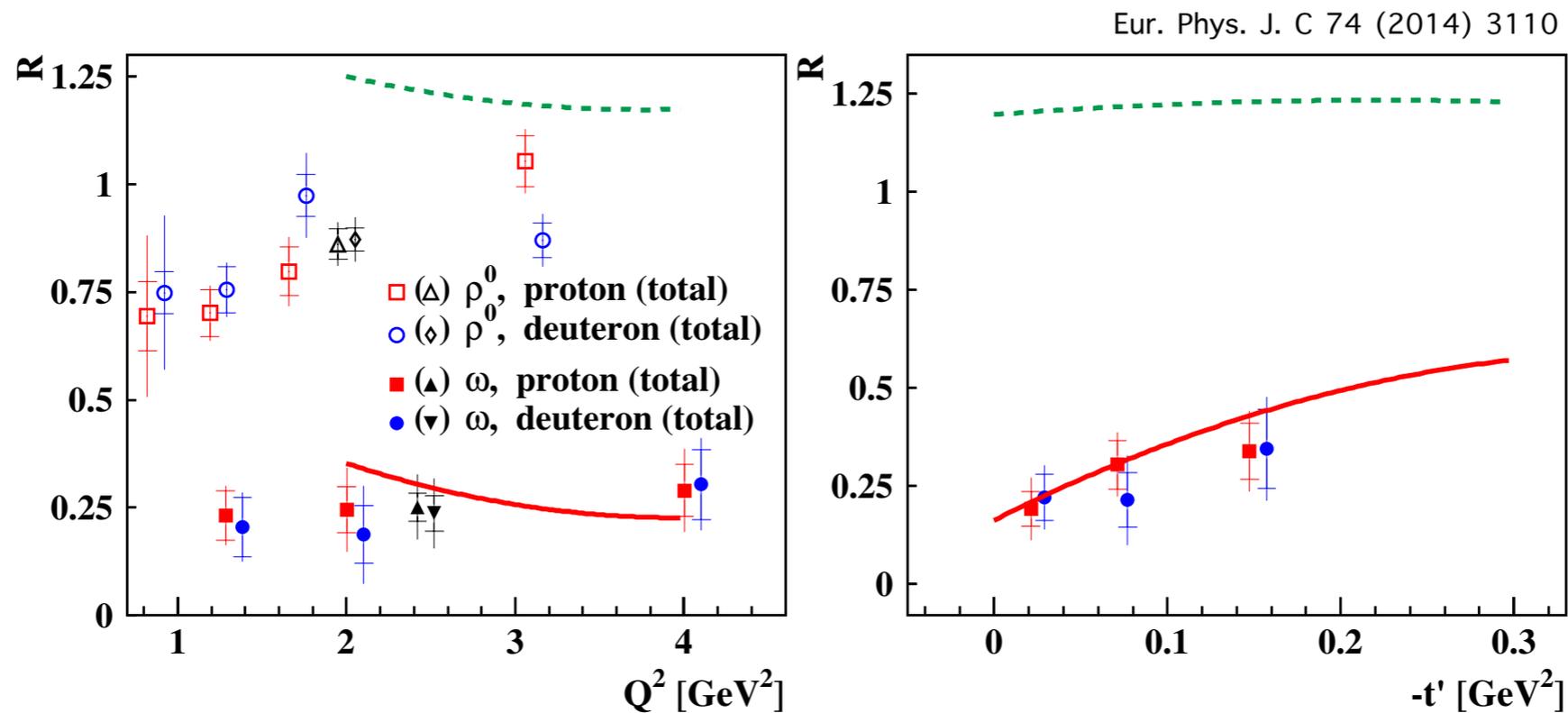
class A:  $\gamma_L^* \rightarrow \omega_L$  and  $\gamma_T^* \rightarrow \omega_T$



- no pronounced kinematic dependence observed
- again, need for pion-pole contribution observed

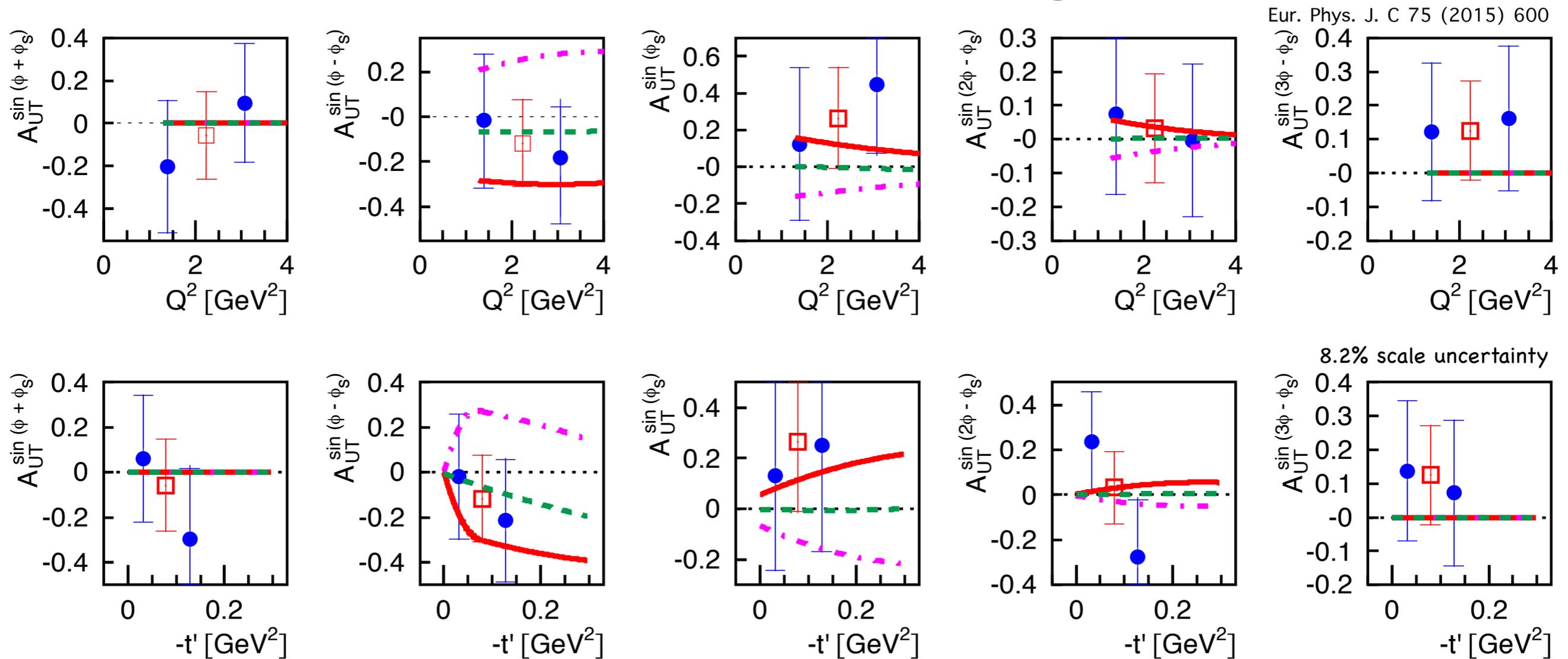
# Longitudinal-to-transverse cross-section ratio

$$R = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1 - r_{00}^{04}} = \frac{d\sigma(\gamma_L^* \rightarrow V_L) + \frac{1}{\epsilon} d\sigma(\gamma_T^* \rightarrow V_L)}{d\sigma(\gamma_T^* \rightarrow V_T) + \epsilon d\sigma(\gamma_L^* \rightarrow V_T)}$$

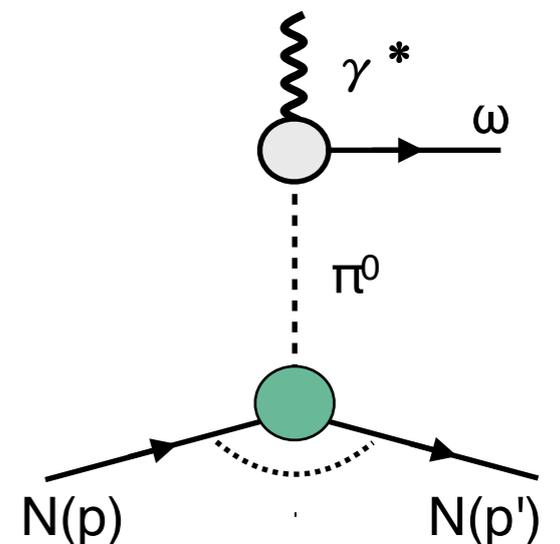


- $R(\omega)$  4 times smaller than  $R(\rho)$
- no pronounced kinematic dependence observed

# Transversely polarized target: $\omega$ $A_{UT}$



- Model S. Goloskokov and P. Kroll, Eur. Phys. J A 50 146 (2014)
  - without pion-pole contribution
  - with pion-pole contribution:  $\pi\omega$  transition FF  $> 0$
  - with pion-pole contribution:  $\pi\omega$  transition FF  $< 0$
- Positive  $\pi\omega$  transition FF favoured



Exclusive  $J/\psi$

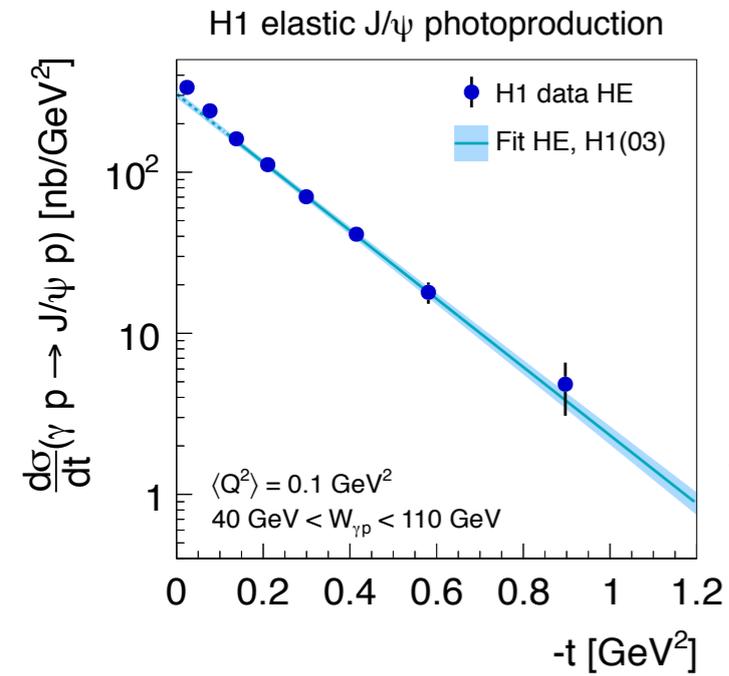
# t slope

**ZEUS** Nucl. Phys. B 695 (2004) 3-37

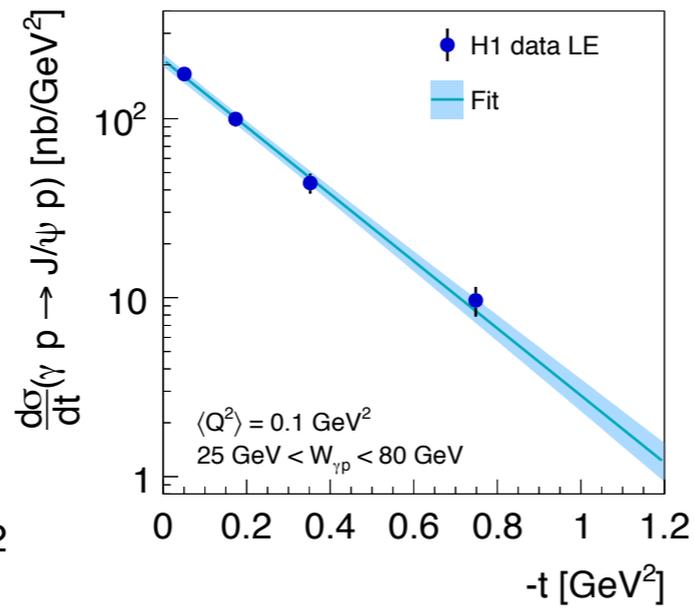
elastic

Eur. Phys. J. C73 (2013) 2466

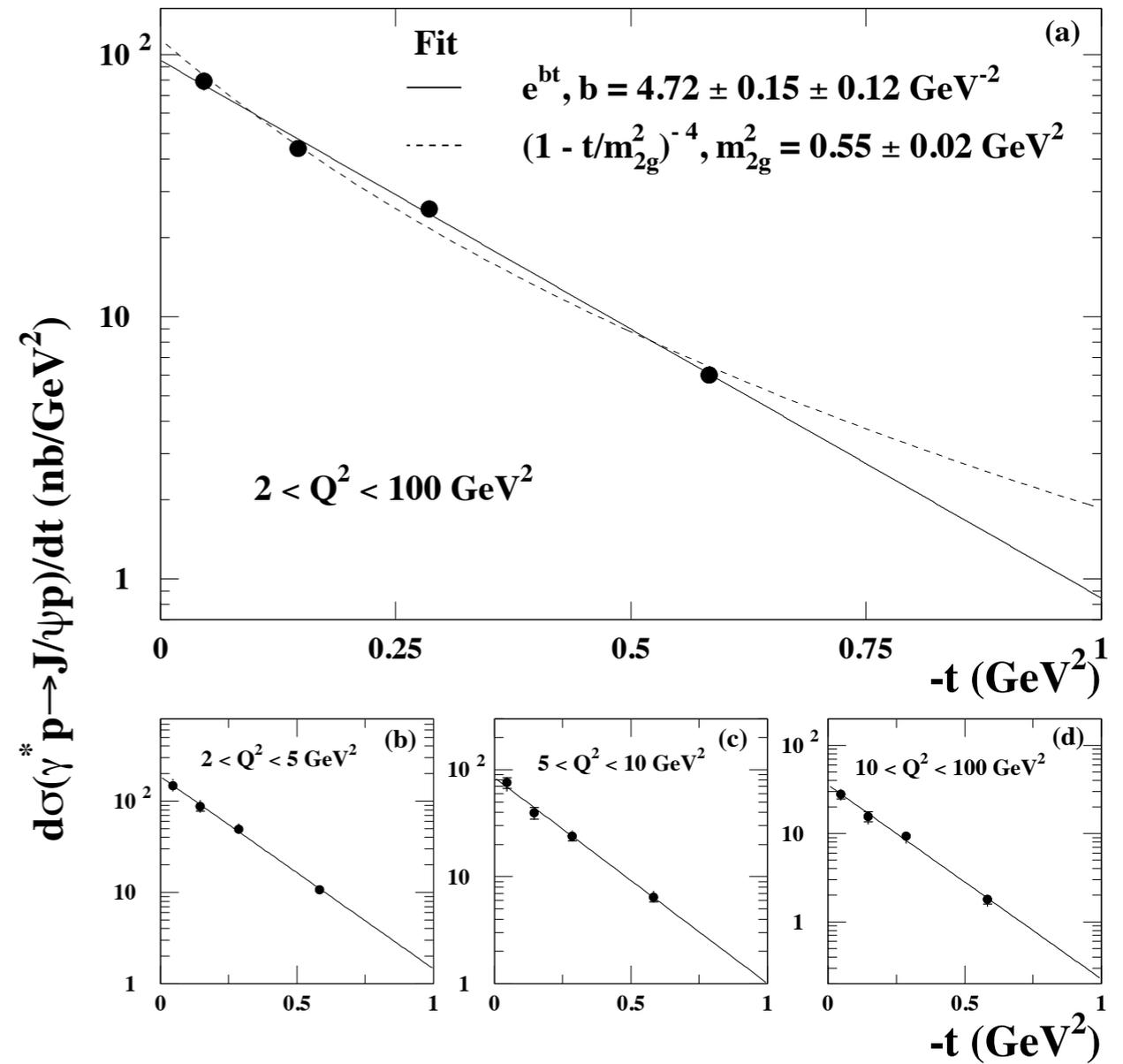
H1 elastic J/ψ photoproduction



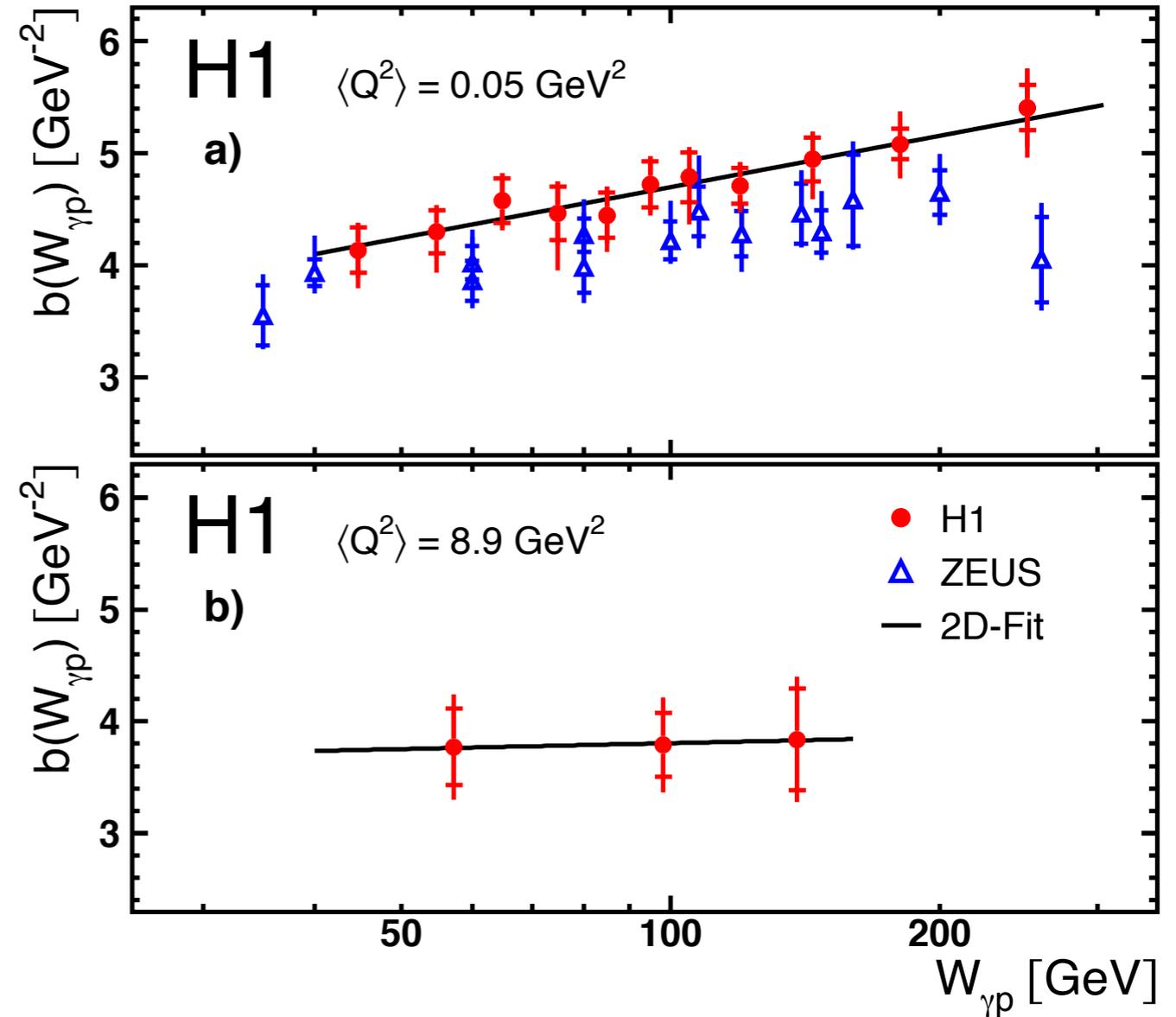
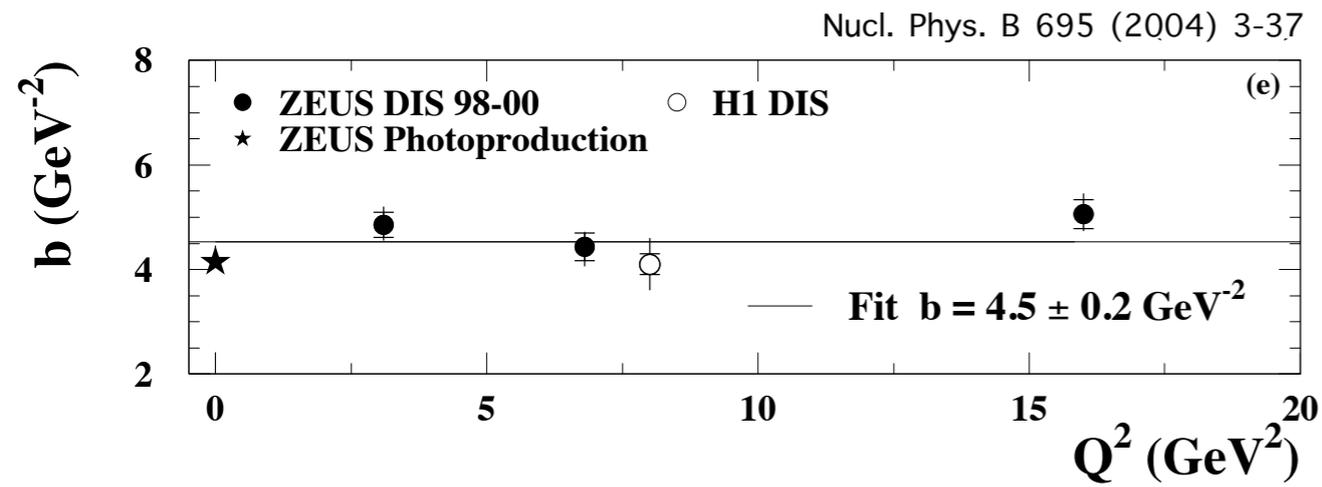
$$b = 4.88 \pm 0.15 \text{ GeV}^{-2}$$



$$b = 4.30 \pm 0.20 \text{ GeV}^{-2}$$

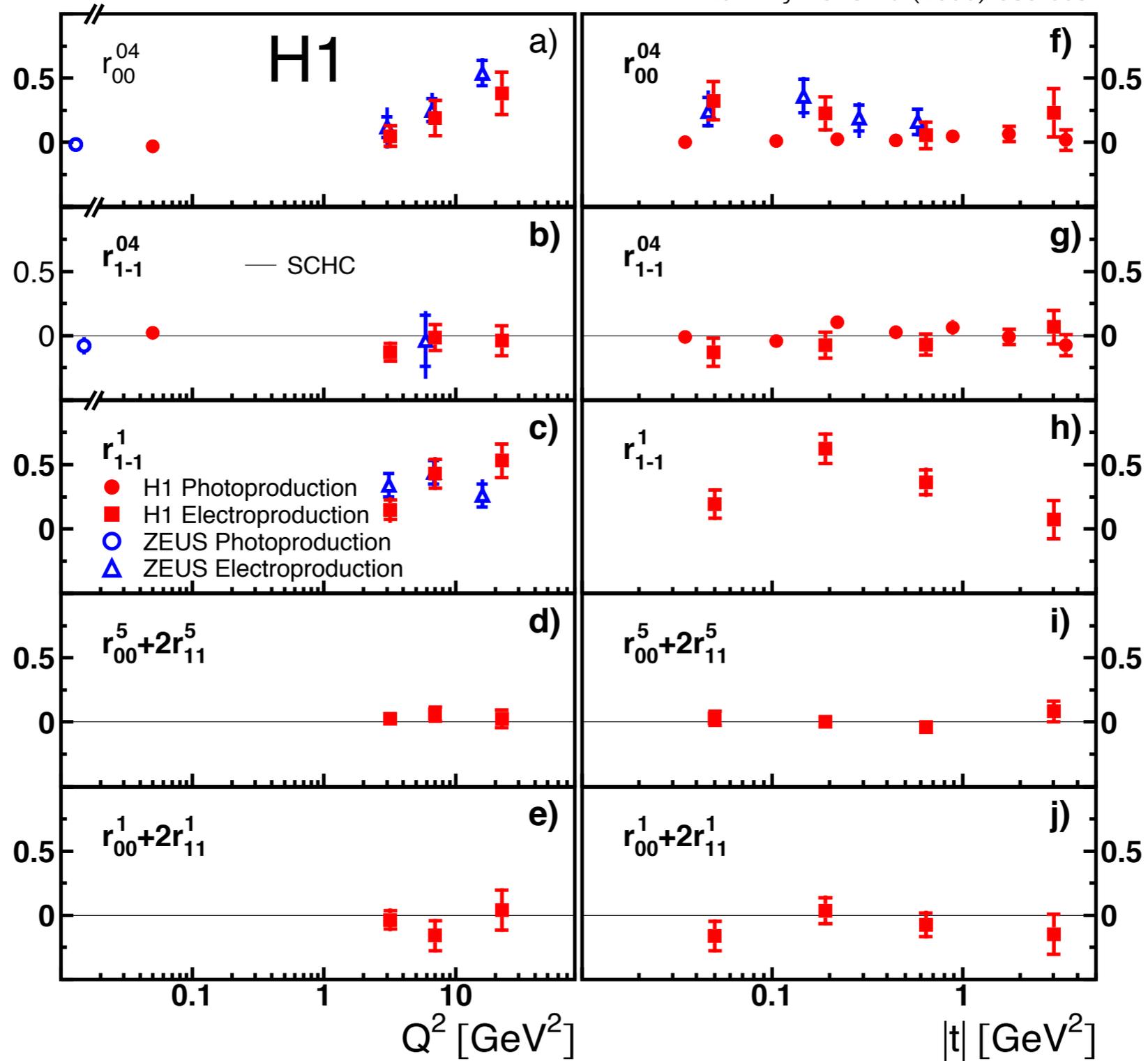


# t slope $Q^2$ and $W$ dependence



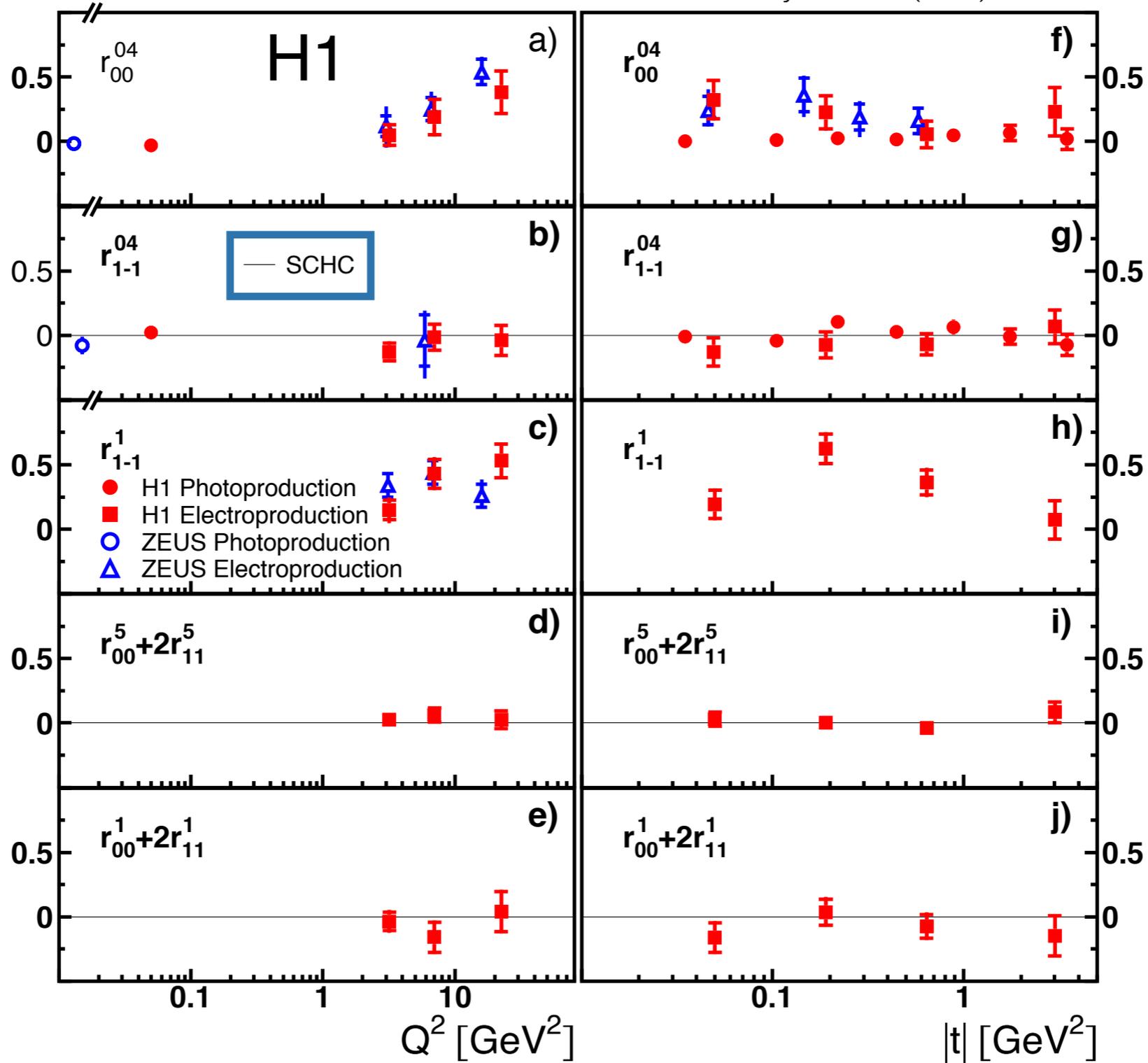
# SDMEs

Eur. Phys. J. C 46 (2006) 585-603



# SDMEs

Eur. Phys. J. C 46 (2006) 585-603



SCHC and NPE:

$$r_{1-1}^1 = \frac{1}{2} (1 - r_{00}^{04})$$

$$r_{1-1}^1 - \frac{1}{2} (1 - r_{00}^{04})$$

$$-0.10 \pm 0.09^{+0.08}_{-0.06}$$

$$0.06 \pm 0.10^{+0.08}_{-0.06}$$

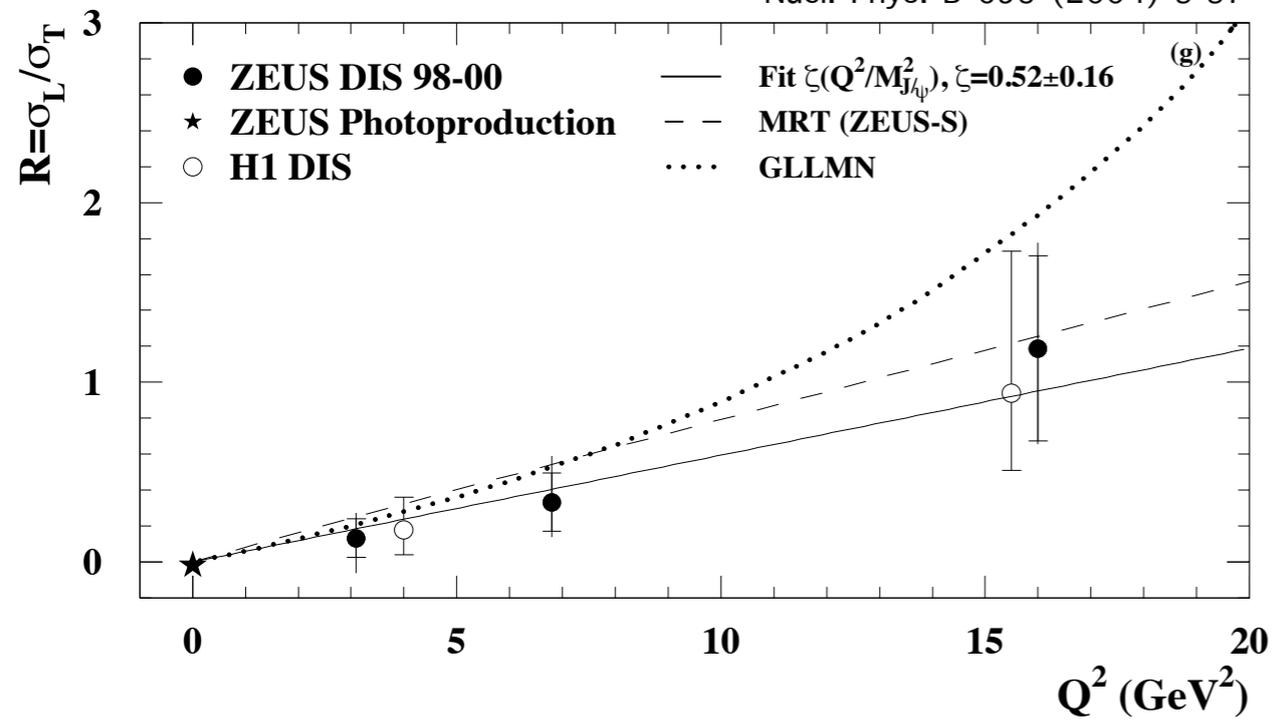
$$0.03 \pm 0.11^{+0.07}_{-0.02}$$

Nucl. Phys. B 695 (2004) 3-37

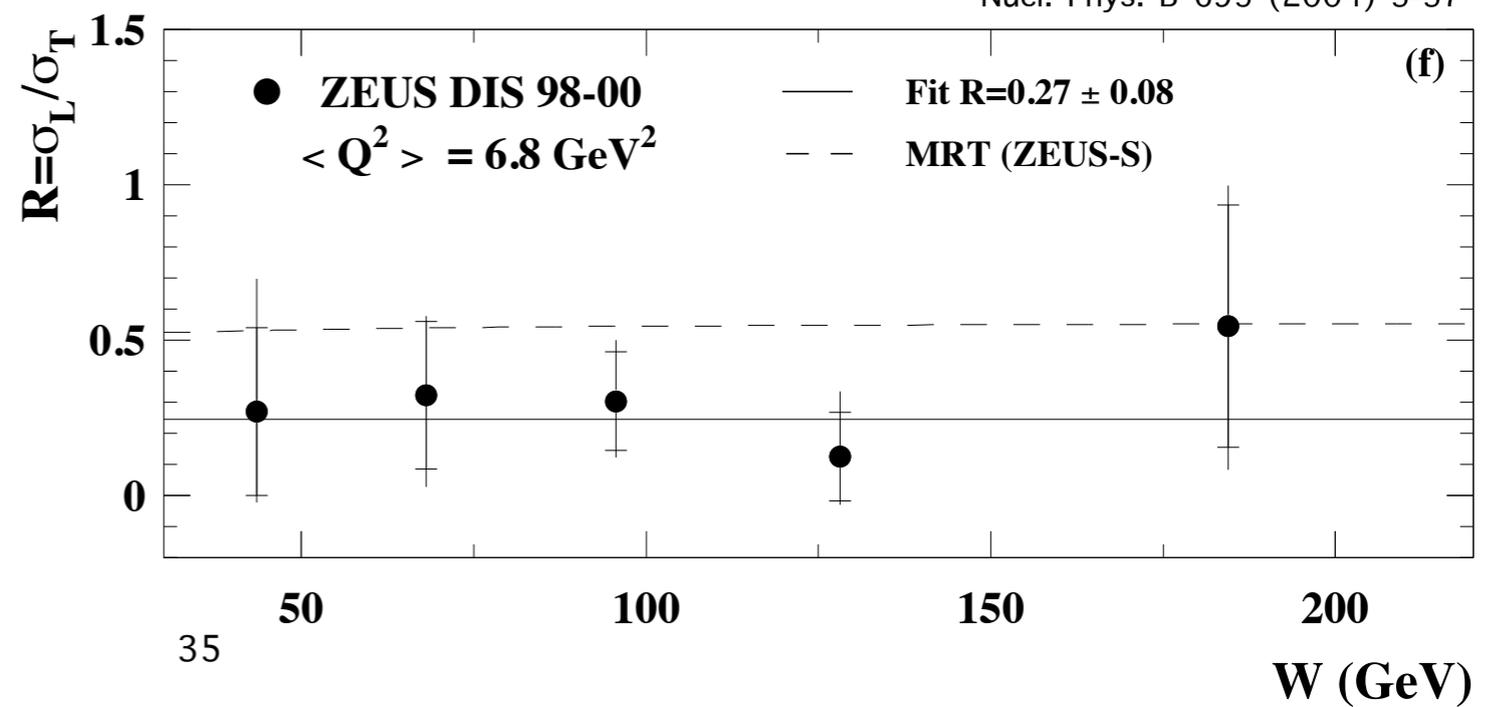
$$R = \sigma_L / \sigma_T$$

$$R = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1 - r_{00}^{04}} \Big|_{\text{SCHC}}$$

Nucl. Phys. B 695 (2004) 3-37



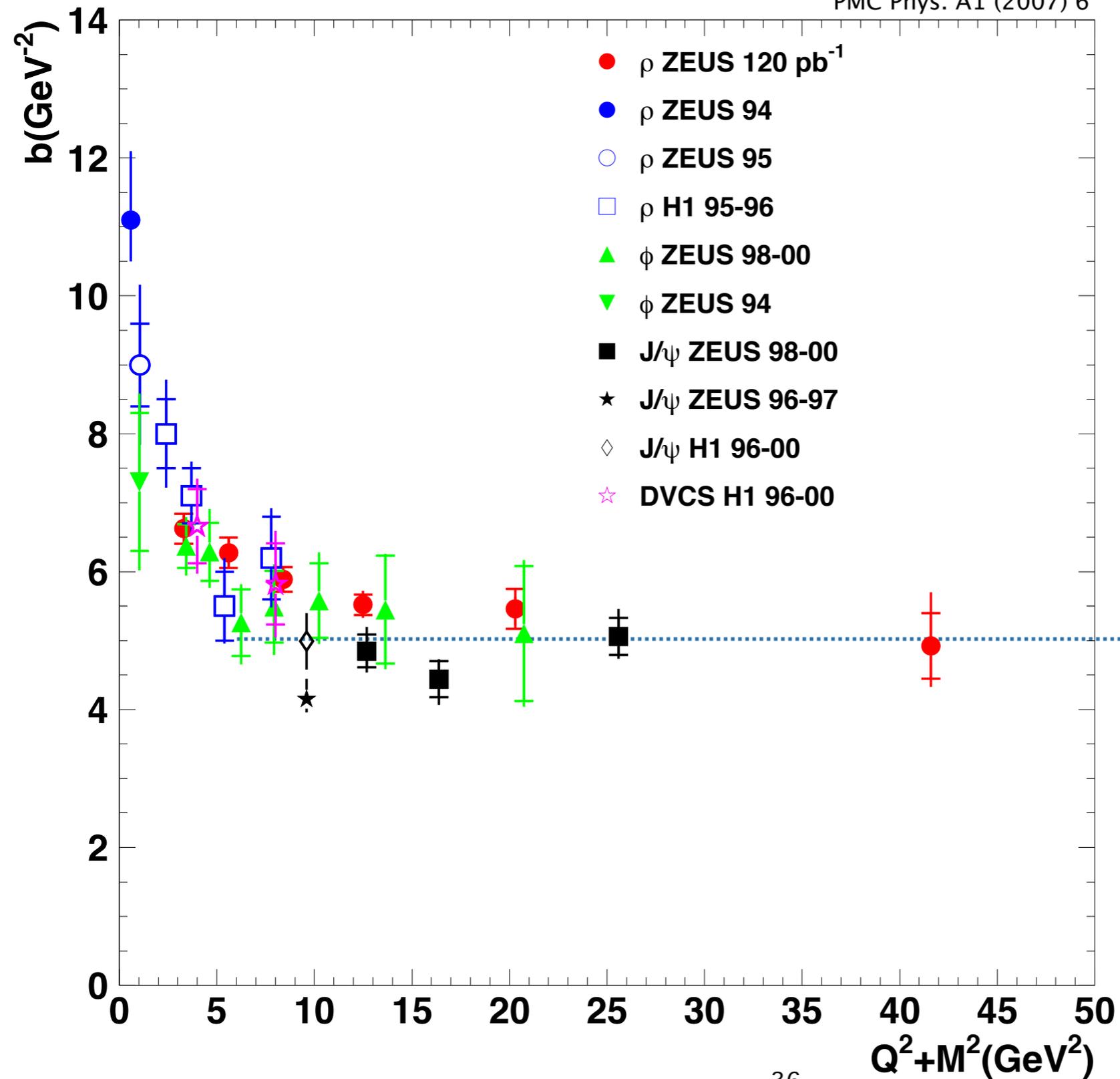
Nucl. Phys. B 695 (2004) 3-37



# $Q^2+M^2$ dependence of $b$

## ZEUS

PMC Phys. A1 (2007) 6



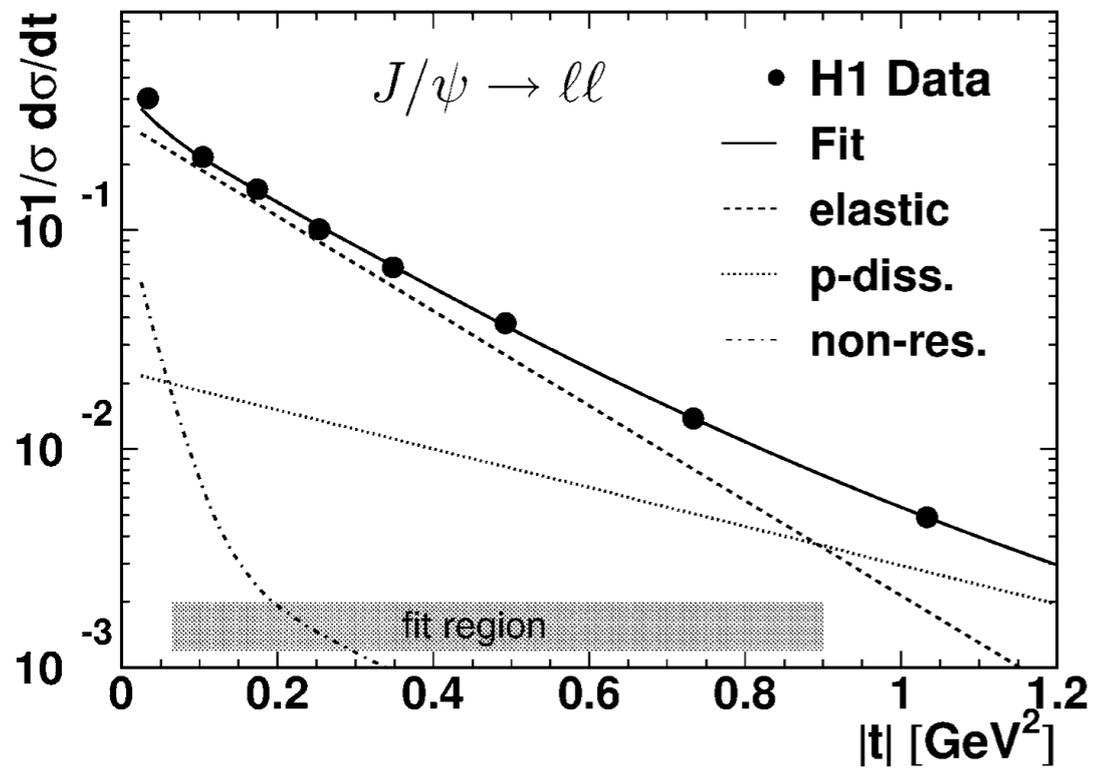
$$b = b_Y + b_{q\bar{q}} + b_{\mathbb{P}}(+b_V)$$

5 GeV<sup>2</sup> :  $\langle r \rangle_g \sim 0.6$  fm

Exclusive  $\psi(2S)$

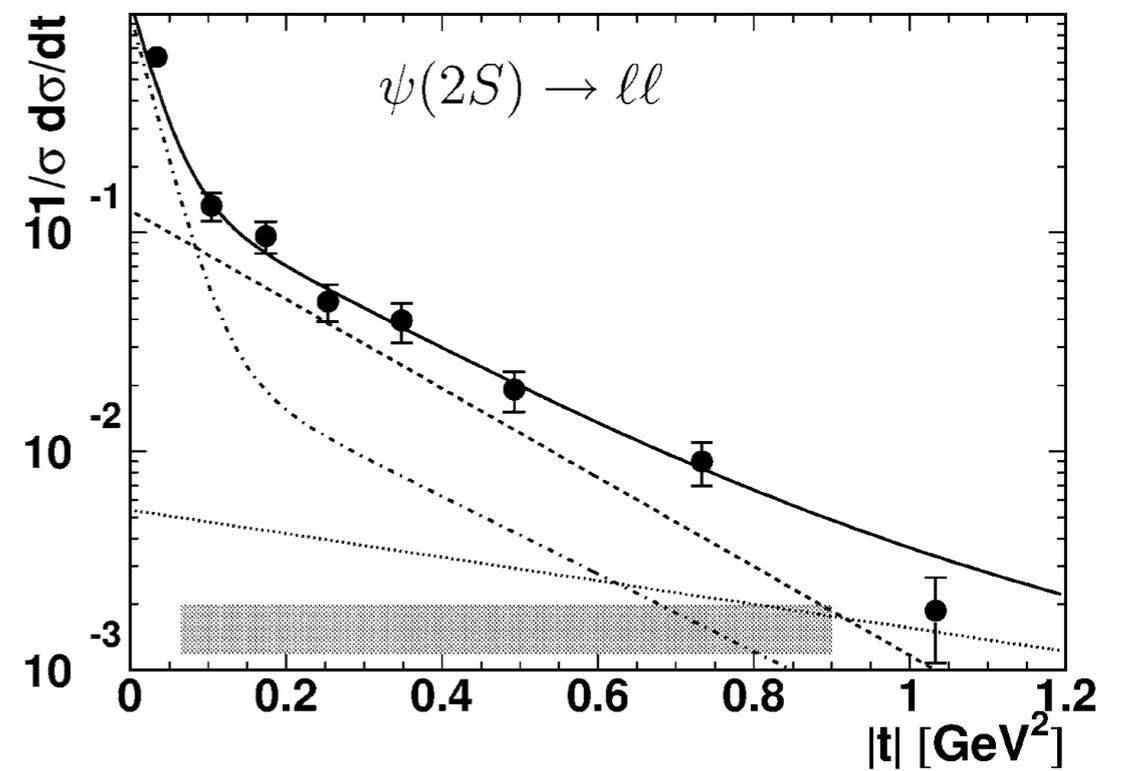
# t slope

$Q^2 \approx 0$



$$b^{J/\psi} = 4.99 \pm 0.13 \pm 0.39 \text{ GeV}^{-2}$$

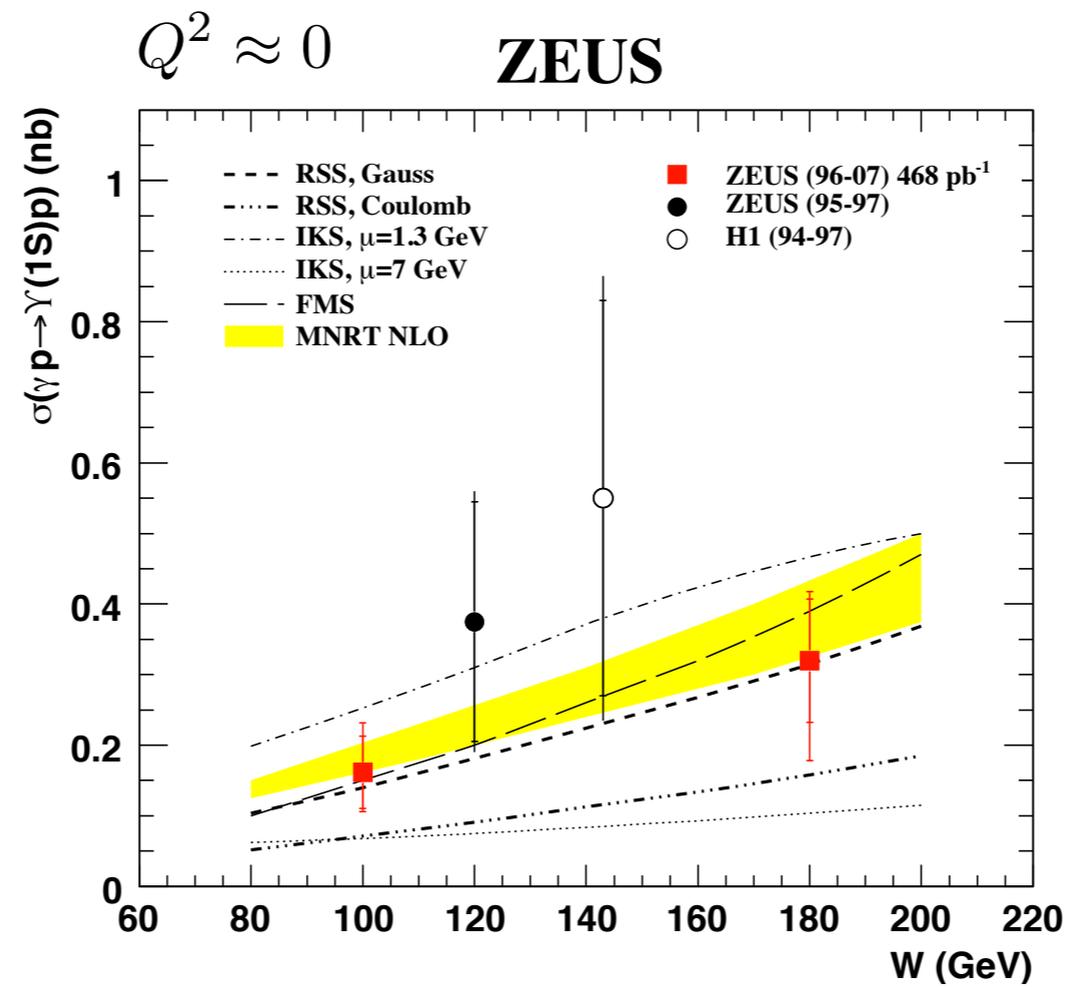
Phys. Lett. B 541 (2002) 251–264



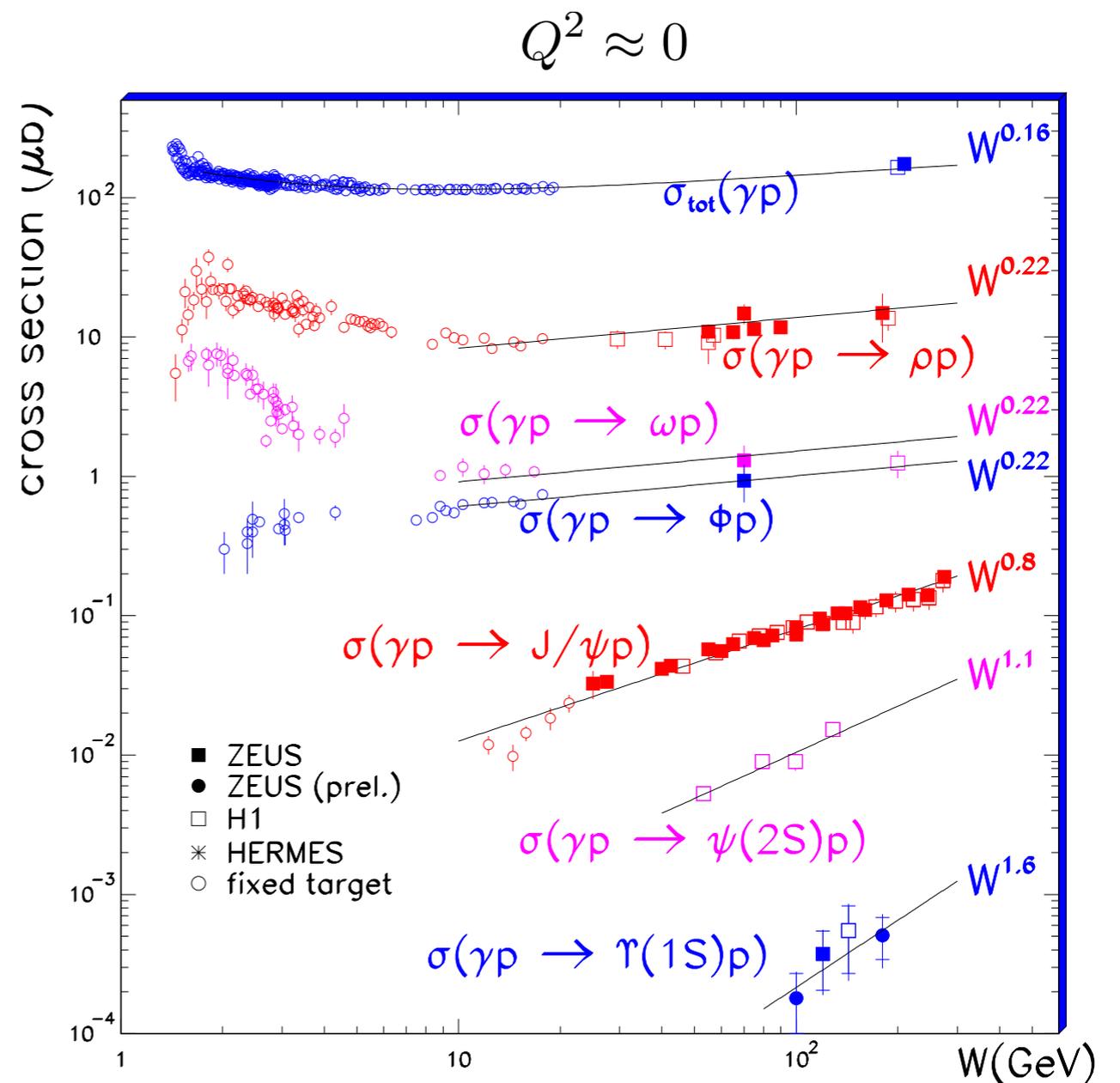
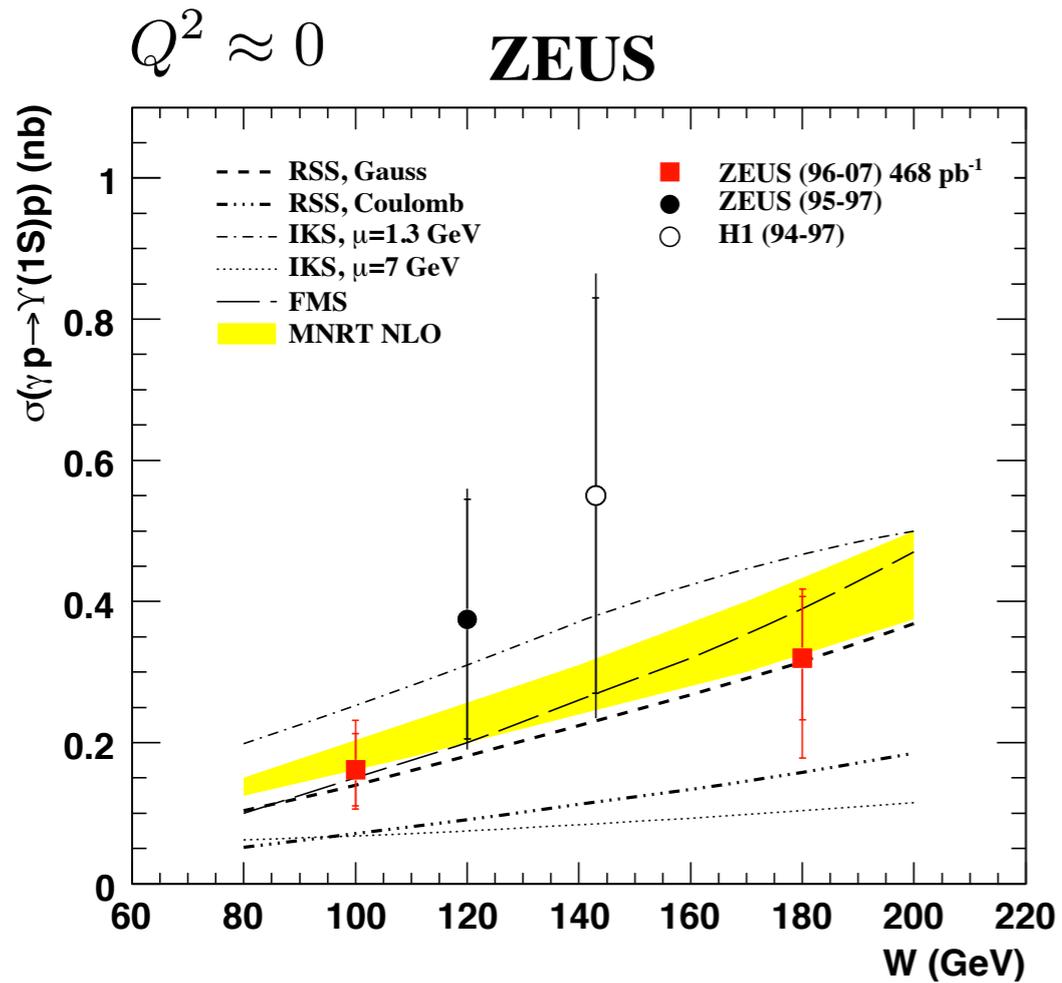
$$b^{\psi(2S)} = 4.31 \pm 0.57 \pm 0.46 \text{ GeV}^{-2}$$

Exclusive  $\gamma$

# W dependence



# W dependence



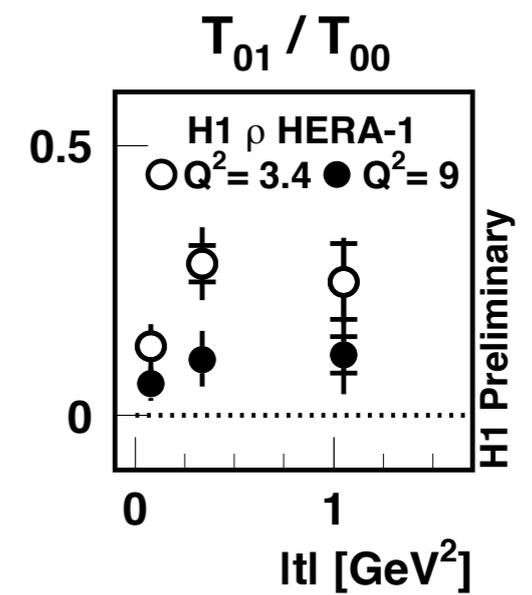
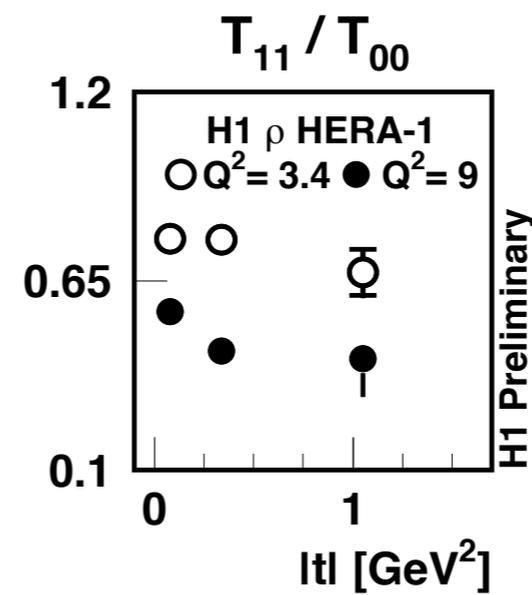
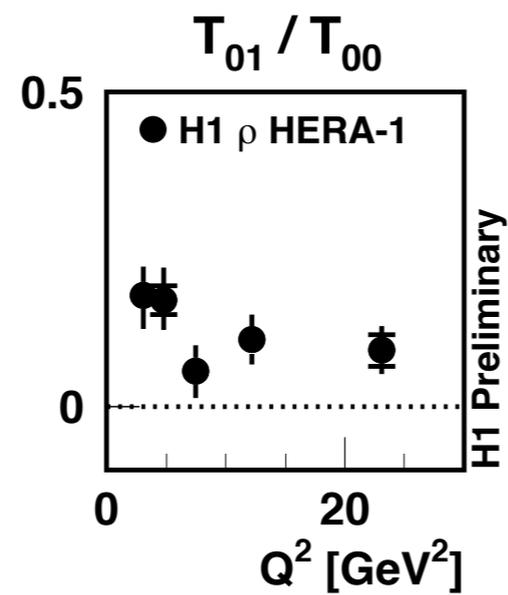
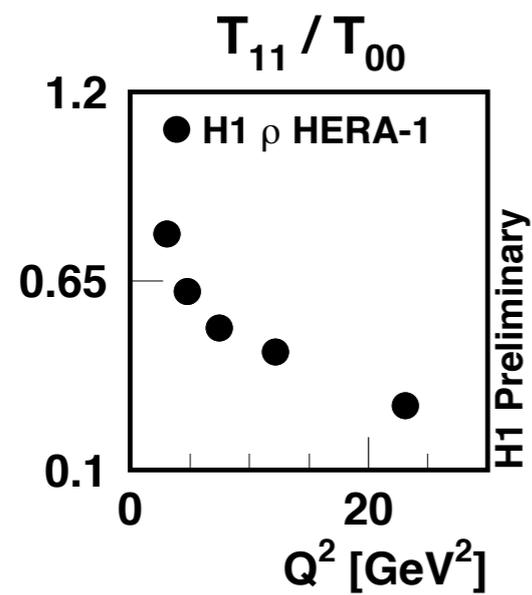
# Summary

- Exclusive measurements in electroproduction and photoproduction of  $\rho$ ,  $\phi$ ,  $\omega$ ,  $J/\psi$ ,  $\psi(2S)$ , and  $\Upsilon$
- $W$  dependence: soft and hard interactions
- 71 SDMEs; 17 helicity amplitude ratios:  
unpolarized and transversely polarized target, beam polarization
- Disentanglement of longitudinal and transverse cross section
- $t$  dependence: size of interacting systems, color distribution in hadron
- Natural and unnatural parity exchange
- $Q^2 + M_V^2$  comparison of vector mesons

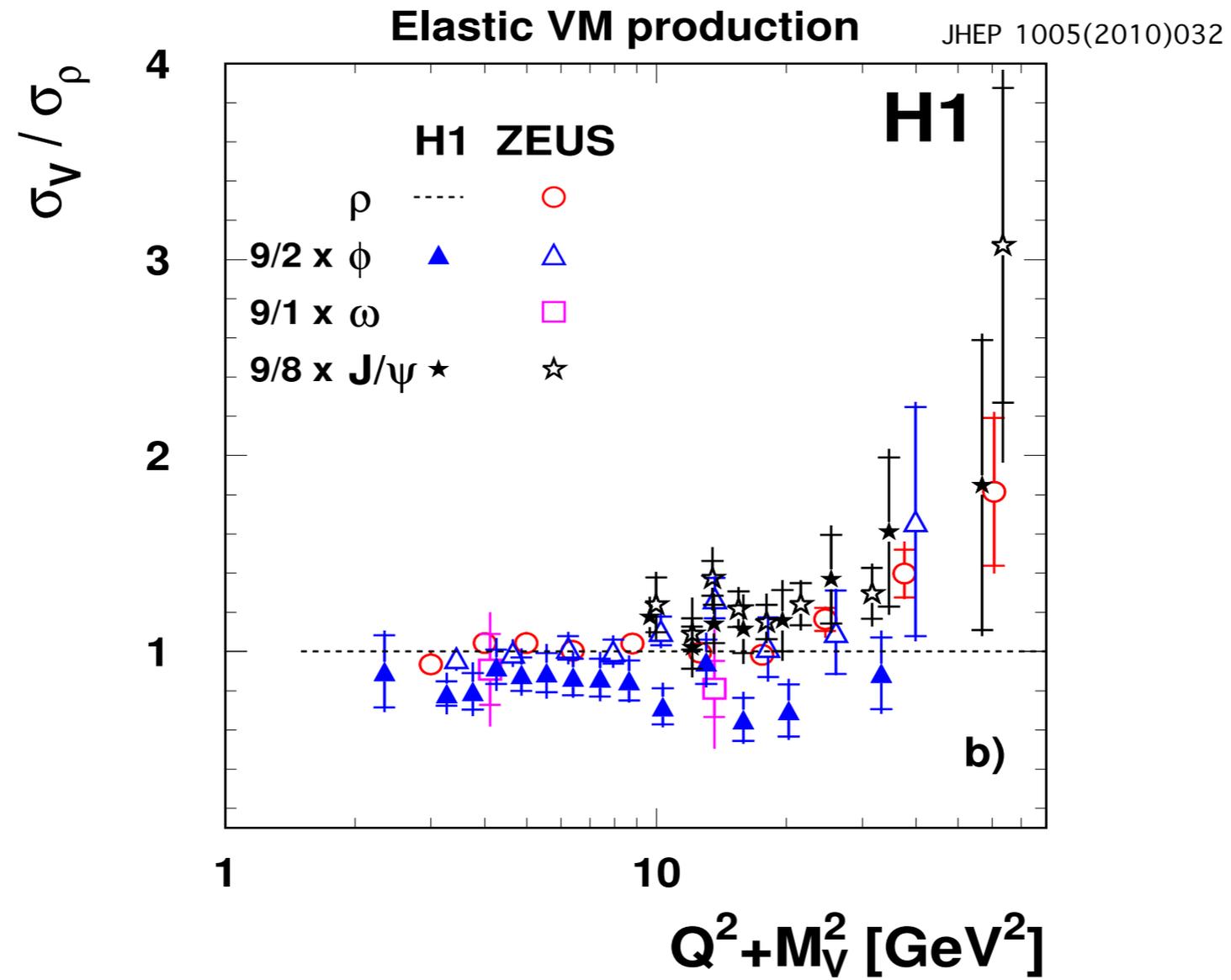
Back up

# Helicity amplitude ratios

JHEP 1005(2010)032



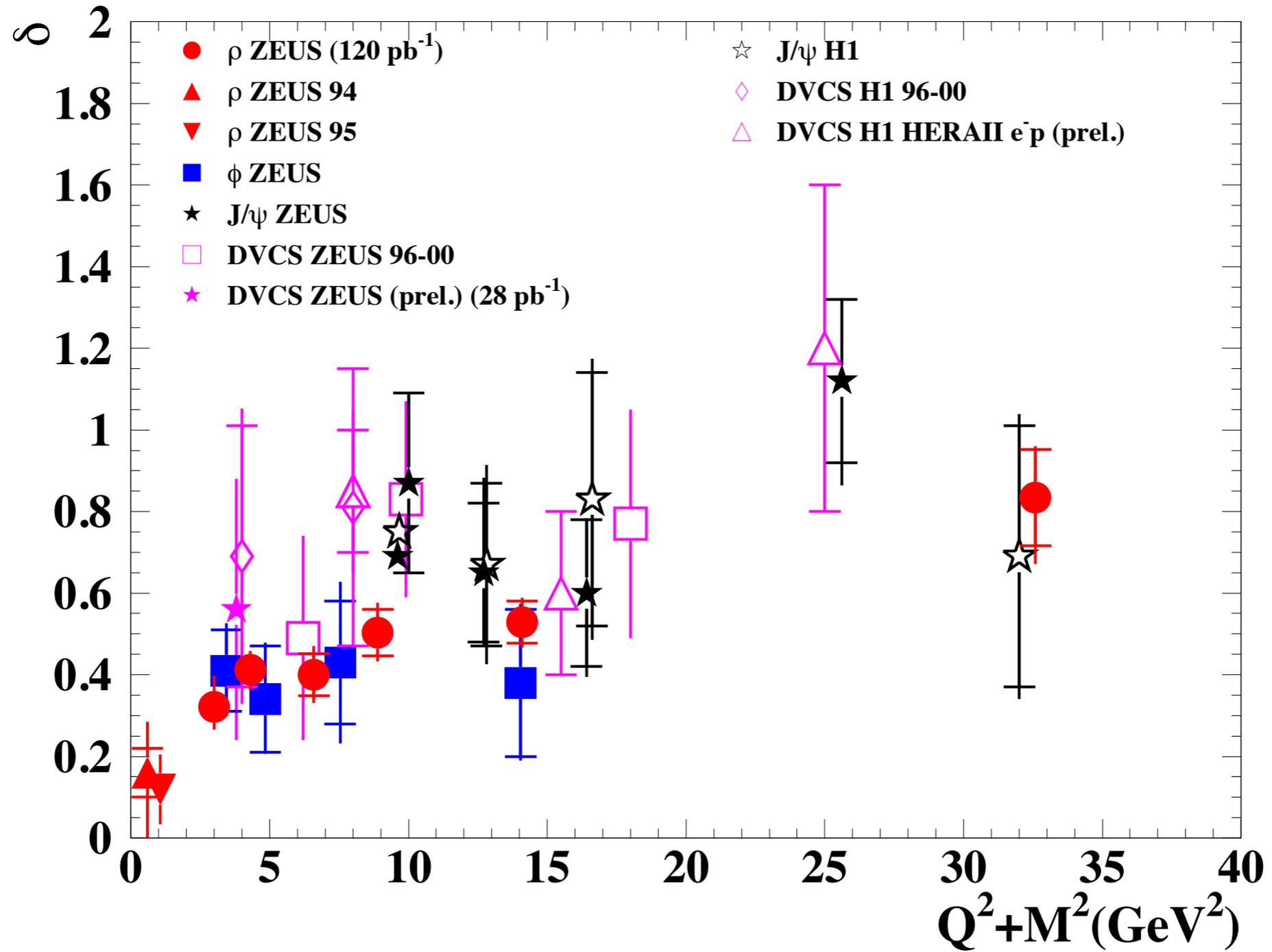
# Cross section ratios



$$\sigma \propto W_{\gamma p}^{\delta}$$

$\delta$

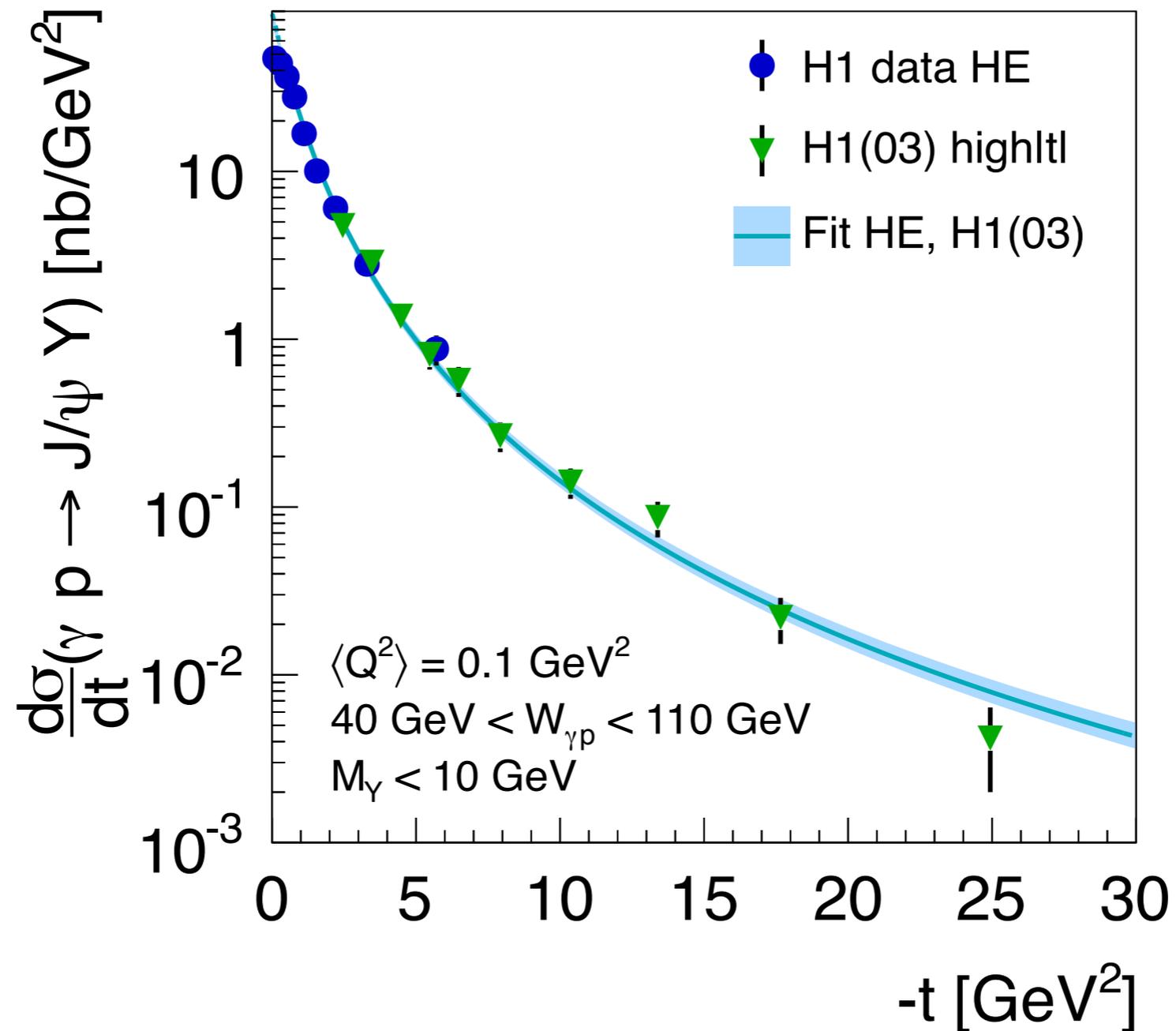
arXiv:0711.0737



# t slope low and high |t|

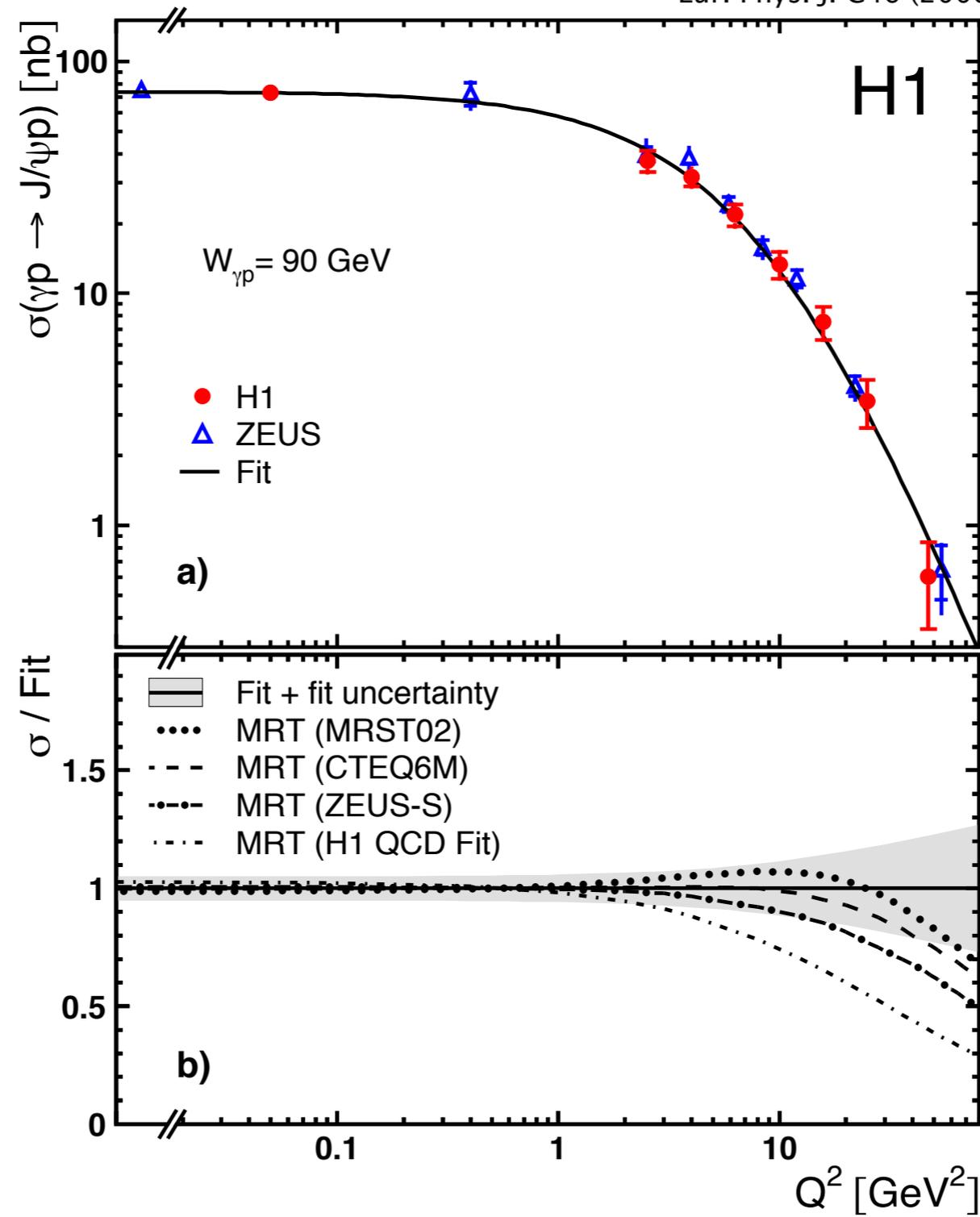
H1 p-diss. J/ψ photoproduction

Eur. Phys. J. C73 (2013) 2466

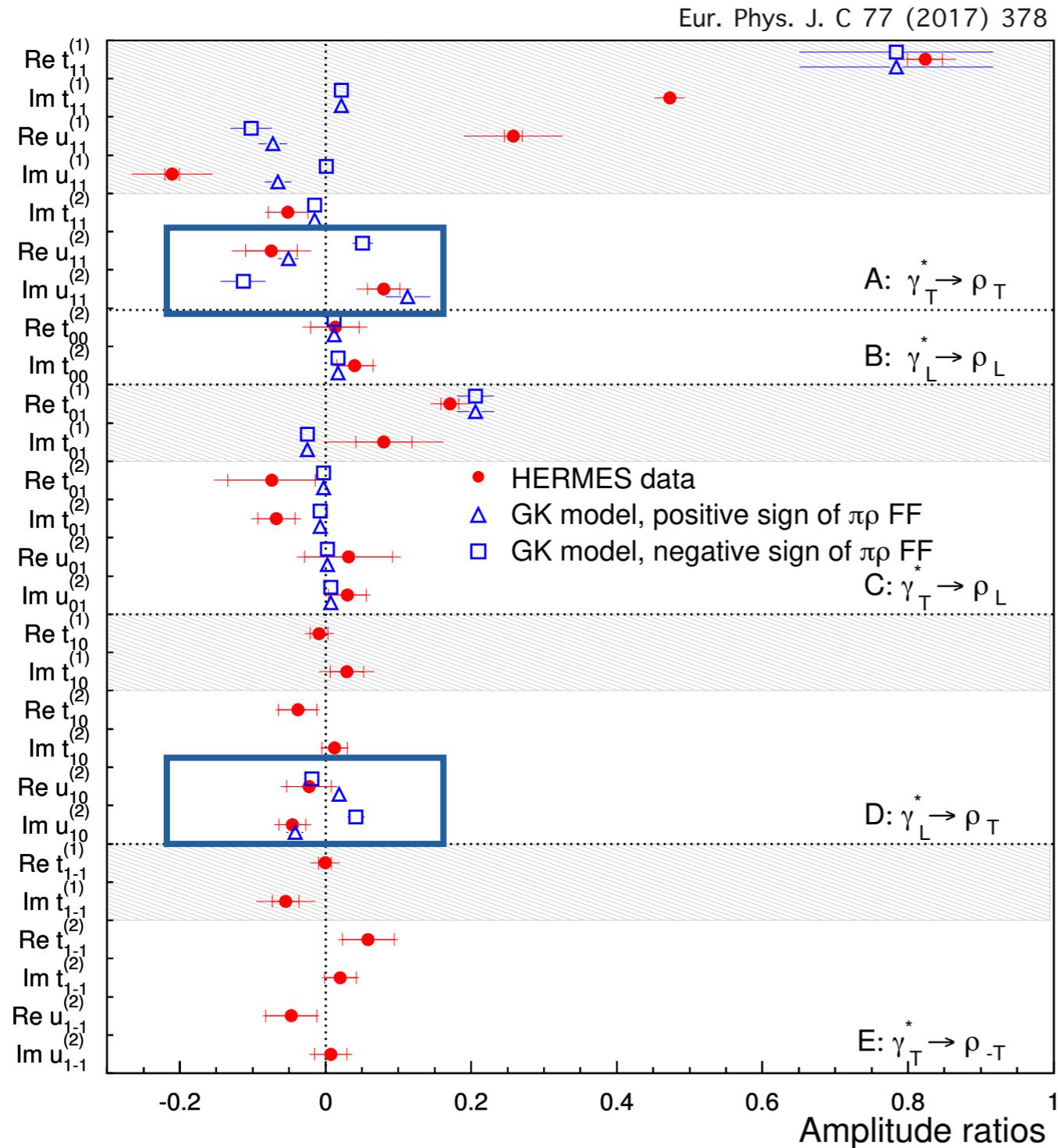


# $Q^2$ dependence

Eur. Phys. J. C46 (2006)585-603



# Comparison $\rho^0$ helicity amplitude ratios with GK model



- GPD H.
- GPD H.
- GPD  $\tilde{H}$  + pion pole.
- GPD E.
- Only pion pole. Positive form factor.
- GPD E.
- GPD  $\bar{E}_T$ .
- GPD  $H_T$ .
- Only pion pole. Positive form factor.

