

# Some thoughts about the theory of meson production

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Workshop on Next-generation GPD studies with  
exclusive meson production at EIC  
Stony Brook, 5 June 2018

**HELMHOLTZ** RESEARCH FOR  
GRAND CHALLENGES





## Disclaimer

- ▶ this is not a regular talk (in particular, no new results)
- ▶ will present some thoughts about different theoretical issues
  - old and open problems
  - new developments in recent years
- ▶ my apologies if I have overlooked important references

## Imaging partons in the nucleon or in nuclei

- ▶ basic idea: elastic scattering on quarks/gluons in target with a high-resolution probe (photon  $\rightarrow$  meson transition)

transverse momentum transfer to target

$\xrightarrow{FT}$  transverse spatial distribution of partons

- ▶ two theoretical formalisms:

- GPDs and hard-scattering factorisation
- small- $x$  factorisation ( $k_T$  fact., dipole picture, CGC)

somewhat different physics emphasis, but both suitable for imaging at intermediate  $x$  both should be valid

## Imaging partons in the nucleon or in nuclei

- ▶ for high-resolution images need either large  $Q^2$  or small meson, or both
- ▶ conveniently seen in dipole formulation:  
typical dipole size  $r$  from wave fct overlap  $\int dz \Psi_\gamma(Q, r, z) \Psi_M(r, z)$

$$\Psi_\gamma(Q, r, z) \sim K_{0,1}(\epsilon r)$$

$$\epsilon^2 = z(1-z)Q^2 + m_q^2$$

$m_q$  = quark mass,  $Q$  = photon virtuality,  $z$  = mom. fraction of  $q$  in  $\gamma$

- Macdonald fcts  $K_{0,1}(z) \sim e^{-z}$  for  $z \gg 1$
- for light quarks: small size of probe spoiled for  $z$  close to end-points
- ▶ quarkonium
  - $J/\Psi$ :  $m_c \sim 1.3 \text{ GeV}$  large, but not very large
  - non-relativistic ansatz for meson wave function, more theory guidance than for light mesons, but not very precise
  - $\Upsilon$ : very high scales, lower rates  
different region of  $x_V = (Q^2 + M_V^2)/(2pq)$

↪ talk by S Joosten tomorrow

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- for light quarks: small size of probe spoiled for  $z$  close to end-points
- ▶ opportunity for EIC:  $J/\Psi$  production at large  $Q^2$ 
  - efficiently decreases typical dipole size ( $z \sim 1/2$ )  
less sensitivity to meson wave fct, finer resolution
  - compared with  $Q = 0$  have more observables ( $J/\Psi$  polarisation)  
 $\rightsquigarrow$  validate theory description
  - missing: higher-order corrections in  $\alpha_s$   
in GPD framework:  $z$  dependence of  $J/\Psi$  wave fct

## Imaging partons in the nucleon or in nuclei

from EIC White Paper:

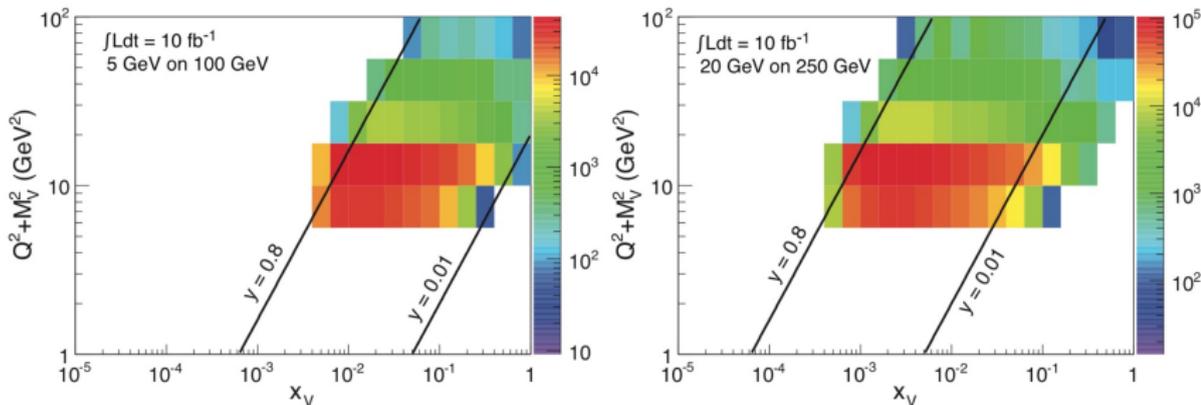
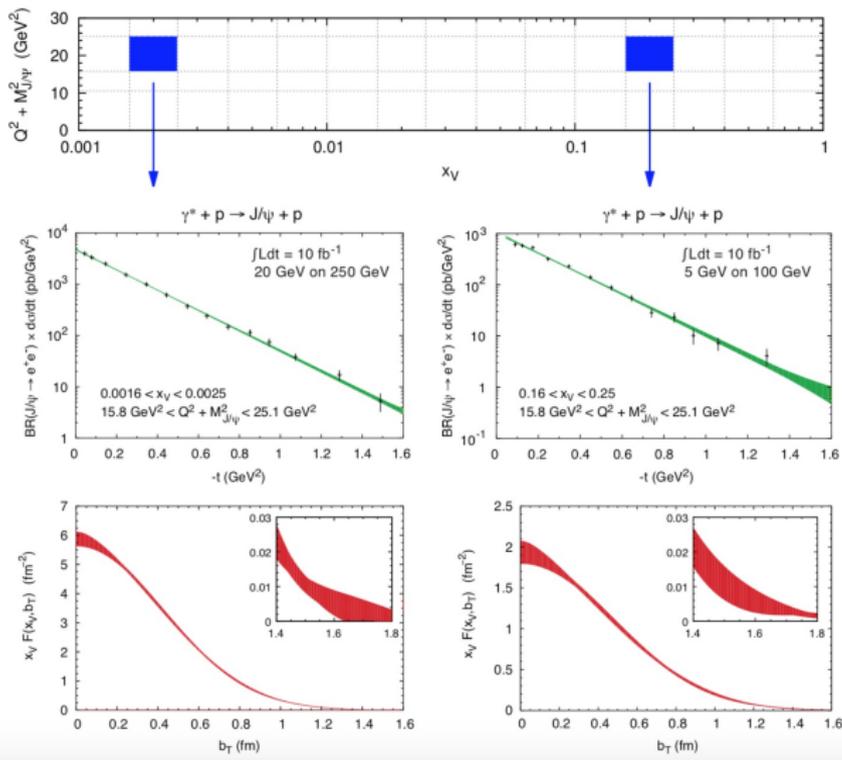


Figure 2.25: Expected number of events for exclusive  $J/\Psi$  production in bins of  $x_V$  and  $Q^2$ .

$$x_V = \frac{Q^2 + M_V^2}{W^2 + Q^2 + M_V^2}$$

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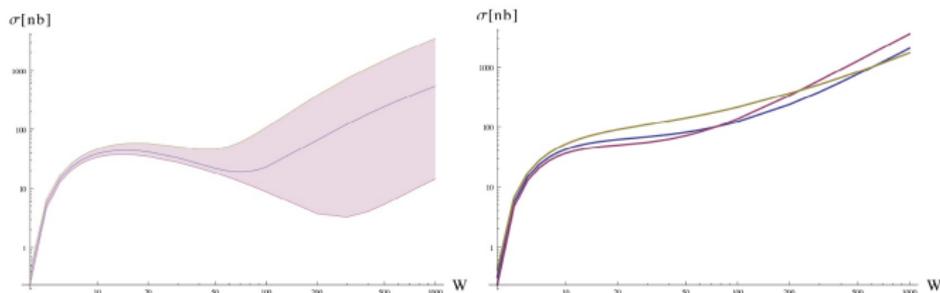
## Higher order corrections: GPD factorisation

- ▶ long known: NLO for production of  $\pi (K)$ , of  $\rho (\phi, \omega)$  and for  $J/\Psi, \Upsilon$  photoproduction  
Belitsky, Müller 2001, Ivanov et al 2004
- ▶ detailed numerical studies Müller et al 2013  
at small  $x$  find size of corrections strongly dependent on GPDs
- ▶ vector meson results of Ivanov et al had mistake, now corrected  
tends to decrease size of corrections Jones et al 2015, Ivanov et al 2016
- ▶ calculation for  $\eta$  channel Duplančić et al 2016
- ▶ in general: NLO corrections can be large, both at low and high  $x$   
also holds for e.m. pion form factor Melič et al 1999
- ▶ at small  $x$ : possibility to resum small- $x$  logarithms  
Ivanov et al 2016

## Higher order corrections

- ▶ at small  $x$ : possibility to resum small- $x$  logarithms

from Ivanov et al, arXiv:1601.07338

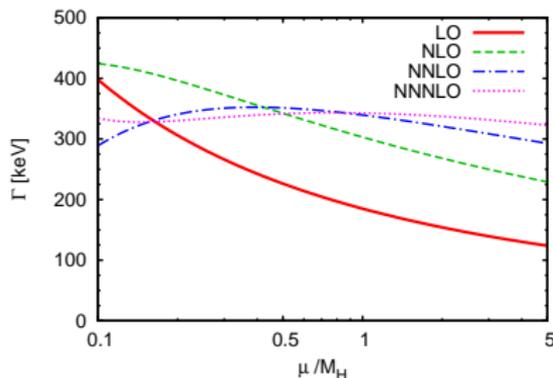


**Figure 6.** NLO(left panel) and resummed (right panel) photoproduction cross section (only gluonic GPDs included in both cases) as a function of  $W = \sqrt{s_{\gamma p}}$  for  $\mu_F^2 = M_{J/\psi}^2 \times \{0.5, 1, 2\}$  (pink, blue and yellow lines respectively)

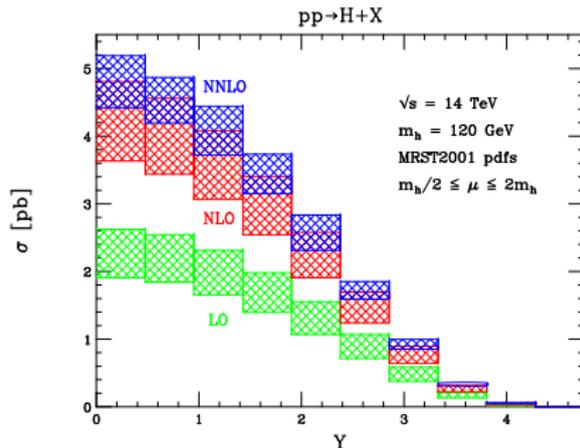
- ▶ in CGC formalism: NLO impact factors for  $\gamma^* \rightarrow V$  Bousserie et al 2016

## Higher order corrections

- more general perspective: NLO corrections are **not always small**  
situation in DIS or  $e^+e^- \rightarrow \text{hadrons}$  is not typical



decay width for  $H \rightarrow \text{light hadrons}$   
Baikov, Chetyrkin 2006



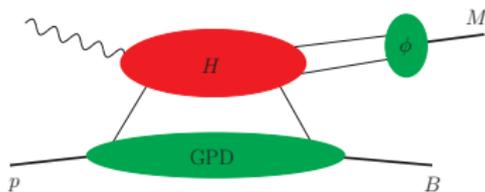
Higgs rapidity spectrum  
Anastasiou et al 2005

- my take: **use NLO** results where available  
don't panic if 100% corrections between LO and NLO

## Factorisation and end-point contributions: some reminders

### Collinear factorisation theorem

Collins, Frankfurt, Strikman '96



- ▶ **collinear subgraphs**, in factorisation formula represented by GPD and by meson distribution amplitude (DA)
- ▶ **hard subgraph**, starting at order  $\alpha_s$
- ▶ at leading power only  $\gamma_L^*$  and  $M_L$

$$\mathcal{A}(\gamma_L^* p \rightarrow M_L B) \sim \frac{f_M}{Q}$$

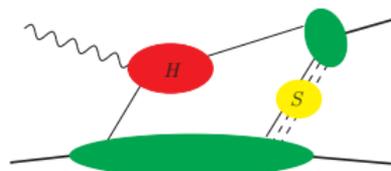
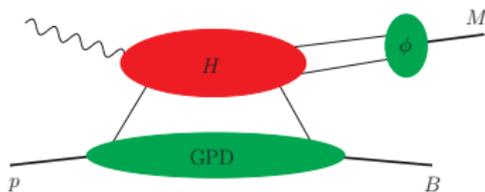
$$\frac{d\sigma_L}{dP_{M\perp}^2} \sim \frac{d\sigma}{dt} \sim \frac{f_M^2}{Q^6}$$

only two observables:  $\sigma_L$  and  $A_{UT}^{\sin(\phi-\phi_S)}$

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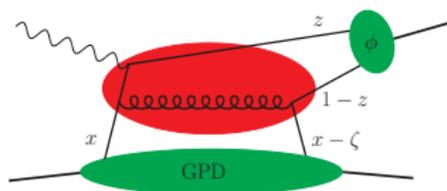
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only two observables:  $\sigma_L$  and  $A_{UT}^{\sin(\phi-\phi_S)}$

- ▶ soft exchanges between coll. subgraphs cancel in sum over graphs at leading-power accuracy

## The problem of end-point contributions



- ▶ in collinear approx. have denominators of gluon  $\times$  quark propagators

$$\frac{1}{Q^2 \frac{\zeta-x}{\zeta} (1-z) - i\epsilon} \frac{1}{Q^2 (1-z)}$$

- ▶ for  $\gamma_L^*$ :  $(1-z)^2$  in denominator cancelled by  $\phi(z) \propto z(1-z)$  and by factor  $(1-z)$  from fermion trace

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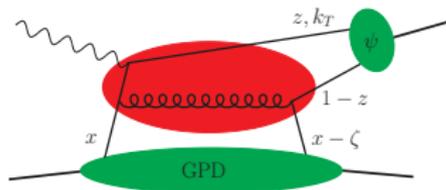


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- ▶ for  $\gamma_T^*$ : no  $(1-z)$  from fermion trace
  - in collin. “factorisation formula” have  $\int_0^1 dz/(1-z)$  divergence
  - endpoint region  $z \approx 1$  **not** power suppressed compared with  $z \sim \frac{1}{2}$

## A phenomenological way out



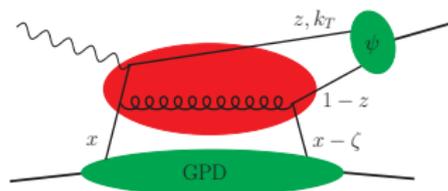
several papers for small  $x_B$   
 Guichon, Guidal, Vanderhaeghen '99  
 Goloskokov, Kroll '05-now

- ▶ in hard scattering do not make collinear approx. but include  $k_T$ 
  - on meson side replace  $\phi(z) \rightarrow$  light-cone wave function  $\psi(z, k_T^2)$
  - may or may not retain  $k_T$  on proton side
- ▶ propagators become finite for  $z \rightarrow 1$ :

$$\frac{1}{Q^2 \frac{\zeta-x}{\zeta} (1-z) + \vec{k}_T^2 - i\epsilon} \frac{1}{Q^2 (1-z) + \vec{k}_T^2}$$

- makes calculation possible for  $\gamma_T^*$
- gives important corrections to leading-twist result for  $\gamma_L^*$  unless  $Q^2 \sim$  tens of  $\text{GeV}^2$

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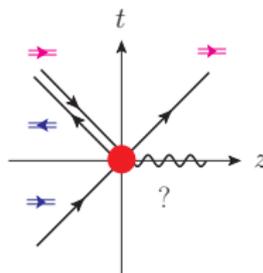
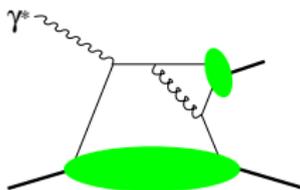
- ▶ not a systematic treatment of power-suppressed contributions
- ▶ contributions from  $z \approx 1$  finite but not suppressed  
 $\rightsquigarrow$  problem of further soft gluon exchanges remains
- ▶ but: quite successful phenomenology at small  $x_B$  and fixed-target energies

## Another reminder: Helicity selection rules

- ▶ selection of helicities in **hard-scattering part**
- ▶ ingredients: conservation of angular mom. and of chirality
  - scattering collinear  $\rightarrow$  ang. mom.  $J^z =$  sum of helicities
  - chirality conserved by quark-gluon and quark-photon coupling

chirality	+1	-1
$q$ helicity	+1/2	-1/2
$\bar{q}$ helicity	-1/2	+1/2

light meson production (not  $J/\Psi$  or  $\Upsilon$ )



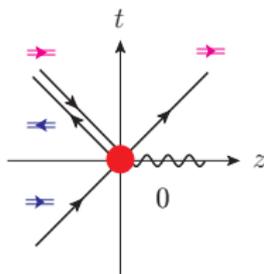
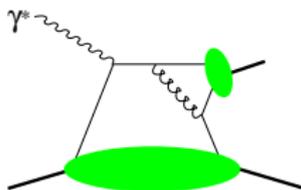
(analogous argument for graphs with gluon GPD)

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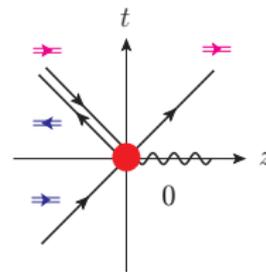
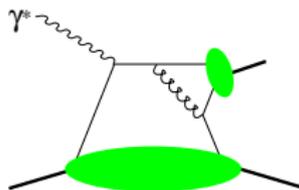
- ▶ dominant transition:  $\mathcal{A}(\gamma_L^* \rightarrow \text{meson}_L) \sim 1/Q$

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- ▶  $\mathcal{A}(\gamma_L^* \rightarrow V_T)$  not possible at leading power

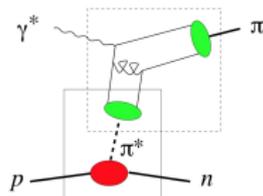
MD, Gousset, Pire 1998; Colins, MD 1999

## Transverse photons

- ▶  $\mathcal{A}(\gamma_T^* \rightarrow V_T) \sim 1/Q^2$ , but sizeable at  $Q^2 \sim \text{few GeV}^2$  ( $\rho$  and  $\phi$  data)  
can describe phenomenologically by keeping  $k_T$  finite in hard scattering
- ▶  $\mathcal{A}(\gamma_T^* \rightarrow \text{meson}_L) \sim 1/Q^2$   
several studies using chiral-odd twist-three meson wave function ( $\pi$  or  $\rho$ )  
 $\rightsquigarrow$  access to **chiral-odd GPDs**  
Ahmad, Liuti, Goldstein 2009-15; Goloskokov, Kroll 2010-11  
**but:** sensitive to endpoints  $z \sim 0$  or 1, divergent in collinear factorisation
- ▶ note: no endpoint problem in high-energy factorisation  
obtain finite impact factors for  $\gamma_T^* \rightarrow \rho_{T,L}$   
Anikin et al 2010-11; Boussarie et al 2016

## End-point contributions in $\pi$ production

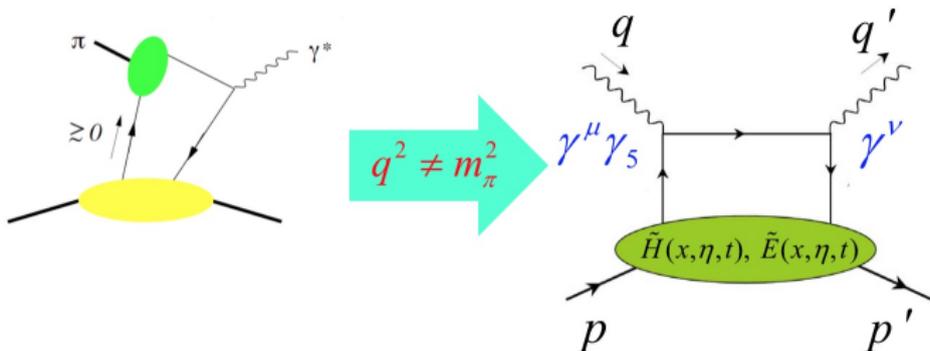
- ▶ end-point contribution in pion form factor long known closely related with pion electroproduction
- ▶ model end-point contribution using light-cone sum rules



Braun, Khodjamirian, Maul 1999

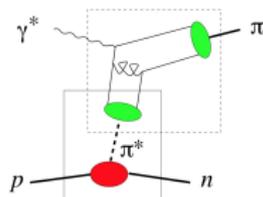
- ▶ analogous work in progress for  $\pi p \rightarrow \gamma^* n$ , planned for  $\gamma^* p \rightarrow \pi n$

K Tanaka, talk at POETIC 8, Regensburg, March 2018



distinct from nonfactorisable  $\pi$  exchange contribution (with  $\tilde{E}$ )

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