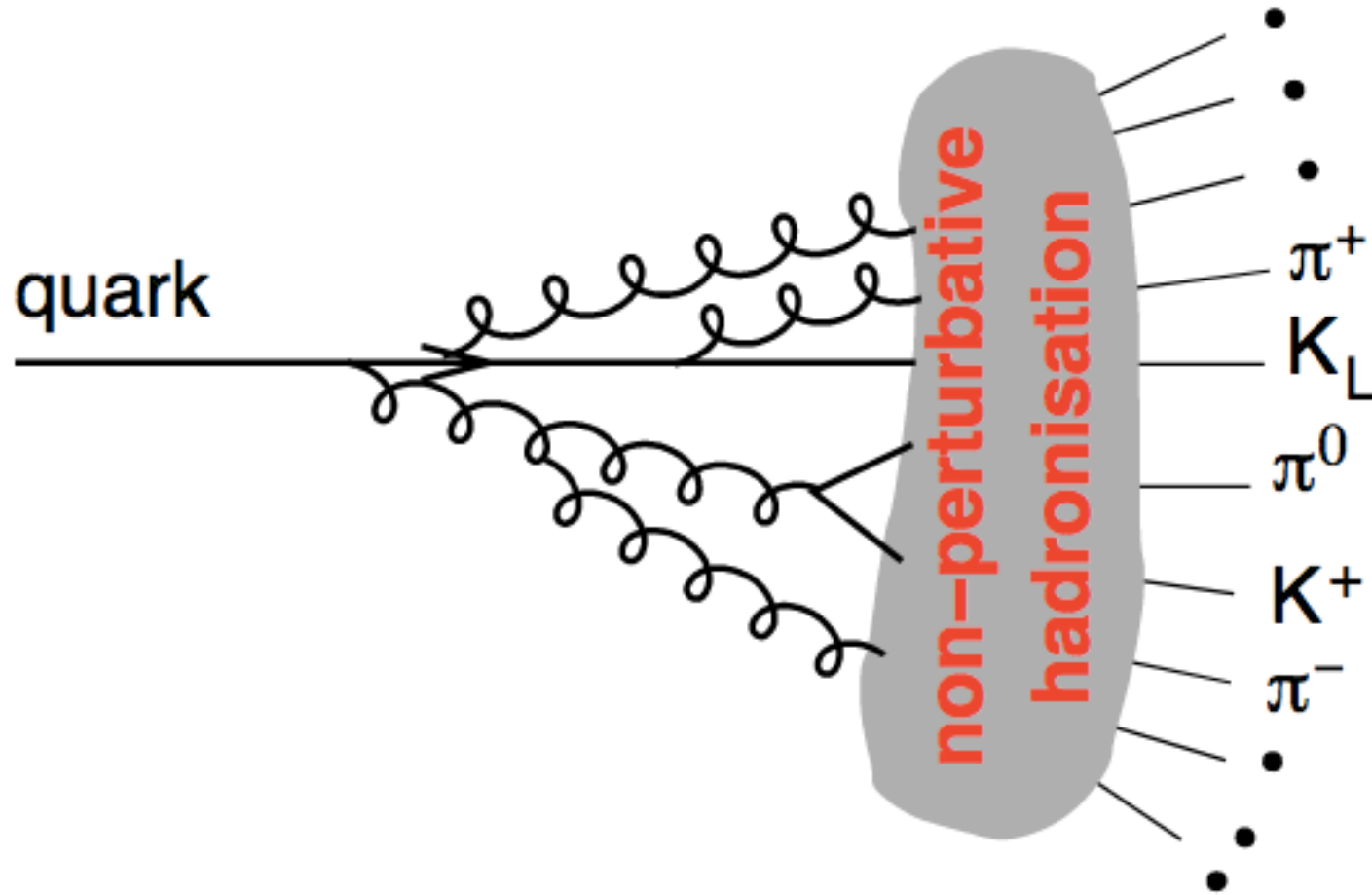


# JETS and substructure, a review

Leticia Cunqueiro  
ORNL

2<sup>nd</sup> JETSCAPE winter school, 10<sup>th</sup> January 2019  
College Station, Texas

# The jet shower



Large radiation probability,  
soft and collinear divergences

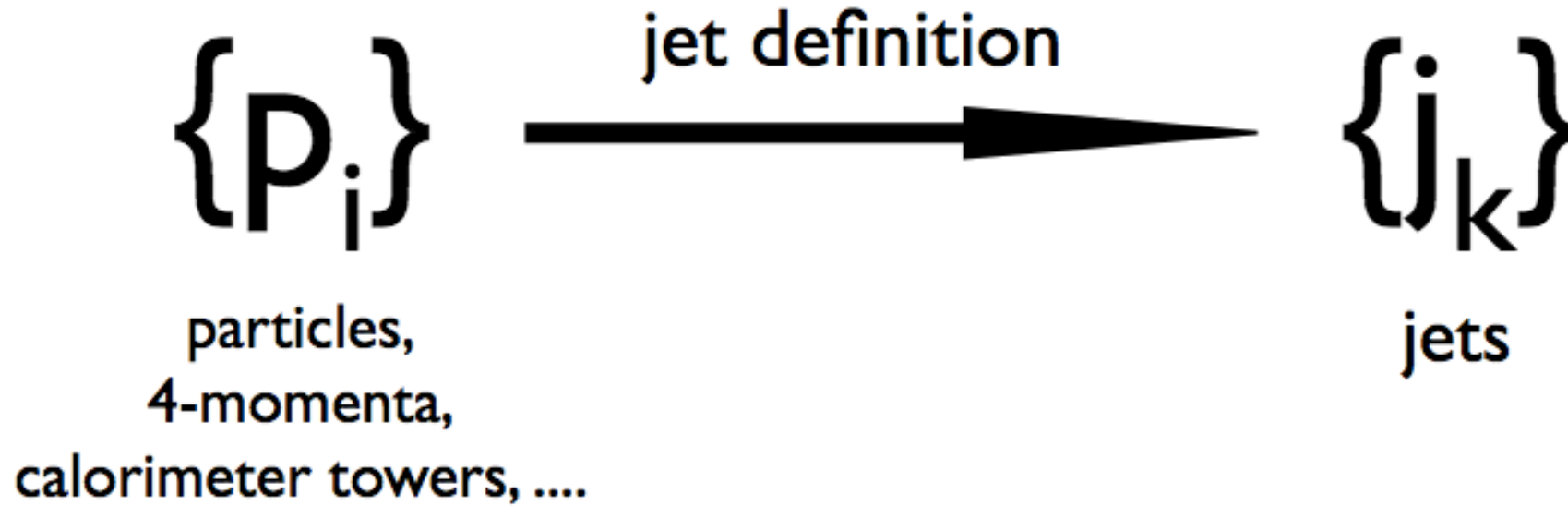
Gluon emission

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

Non-perturbative  
physics

$$\alpha_s \sim 1$$

# The projection



**Jets are energetic, collimated bunches of particles**

**A jet definition, is a projection of the **hadronic** level to **partons** (quarks and gluons)**

Key requirement of the projection: infrared and collinear safety, to preserve calculability

Projections are not unique

# Jet Definition: an example of a sequential recombination algorithm

**Two parameters,  $R$  and  $p_{t,min}$**

(These are the two parameters in essentially every widely used hadron-collider jet algorithm)

$$d_{ij} = \min(p_{ti}^2, p_{tj}^2) \frac{\Delta R_{ij}^2}{R^2}, \quad \Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

## Sequential recombination algorithm

1. Find smallest of  $d_{ij}$ ,  $d_{iB}$
2. If  $ij$ , recombine them
3. If  $iB$ , call  $i$  a jet and remove from list of particles
4. repeat from step 1 until no particles left

Only use jets with  $p_t > p_{t,min}$

**Inclusive  $k_t$  algorithm**

S.D. Ellis & Soper, 1993

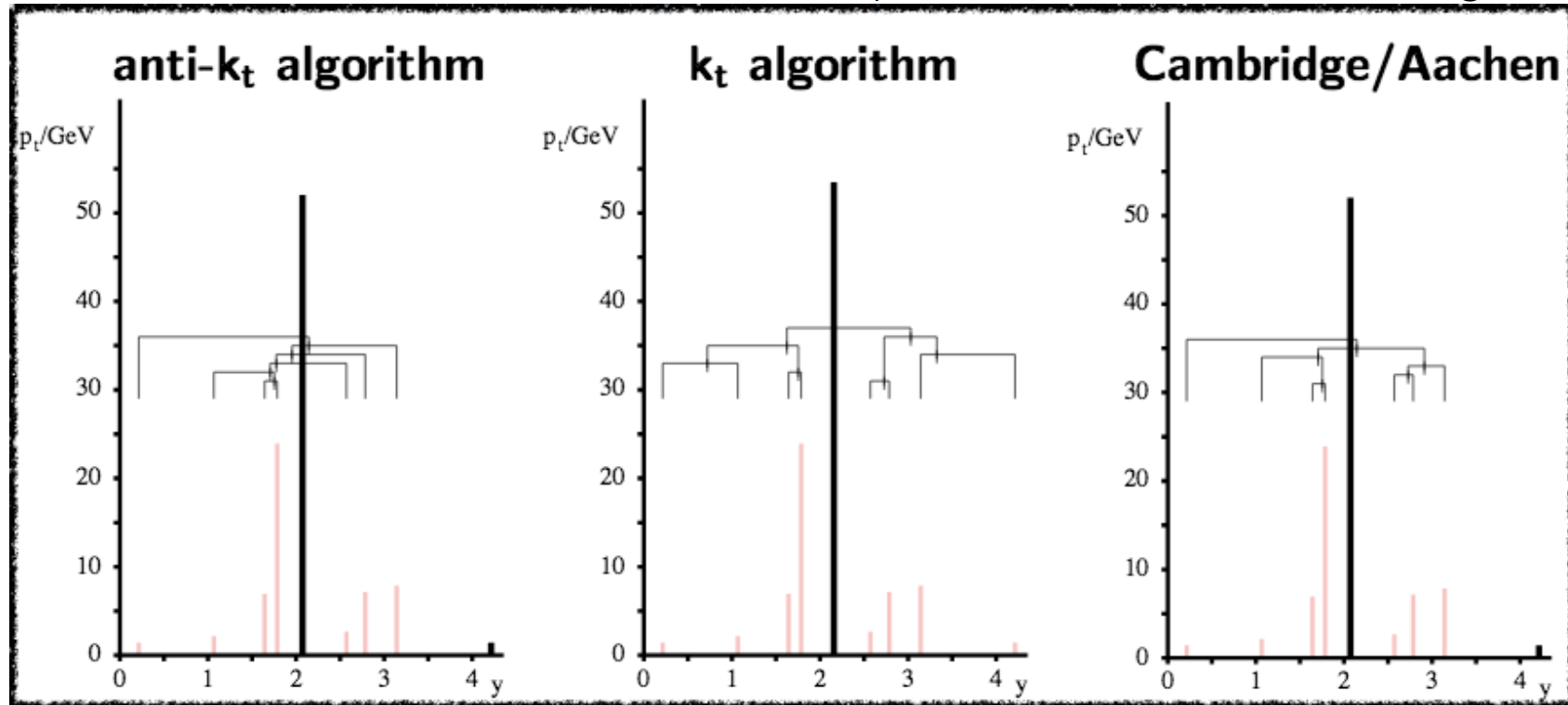
Catani, Dokshitzer, Seymour & Webber, 1993

# The sequential recombination family of algorithms

Perfect cones

Ordered in  $k_T$

Ordered in angle



$$d_{ij} = \min(p_{ti}^{2p}, p_{tj}^{2p}) \frac{\Delta y^2 + \Delta \phi^2}{R^2} \quad d_{iB} = p_{ti}^{2p}$$

$p = 1$   $k_t$  algorithm

S. Catani, Y. Dokshitzer, M. Seymour and B. Webber, Nucl. Phys. B406 (1993) 187  
S.D. Ellis and D.E. Soper, Phys. Rev. D48 (1993) 3160

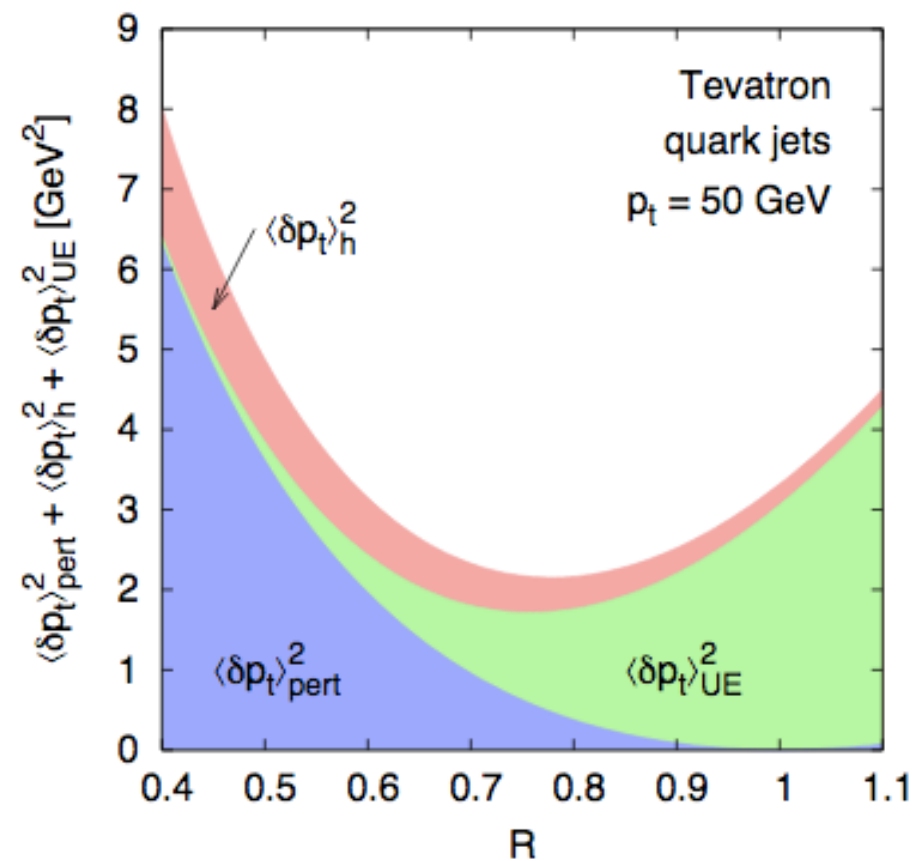
$p = 0$  Cambridge/Aachen algorithm

Y. Dokshitzer, G. Leder, S. Moretti and B. Webber, JHEP 08 (1997) 001  
M. Wobisch and T. Wengler, hep-ph/9907280

$p = -1$  anti- $k_t$  algorithm

MC, G. Salam and G. Soyez, arXiv:0802.1189

# The perturbative and non-perturbative components of the jet

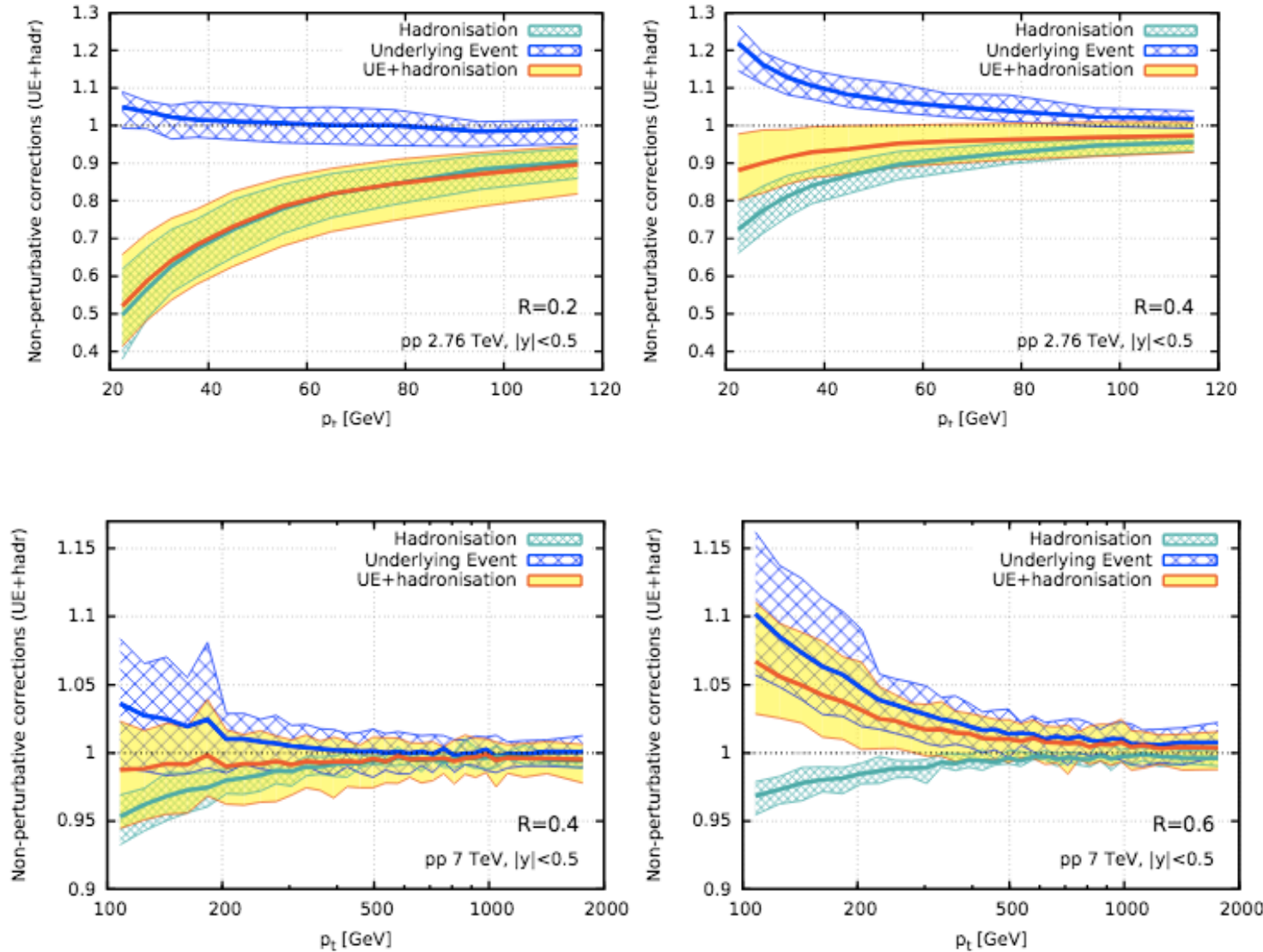


	Dependence of jet $\langle \delta p_t \rangle$ on			
	'partonic' $p_t$	colour factor	$R$	$\sqrt{s}$
perturbative radiation	$\sim \alpha_s(p_t) p_t$	$C_i$	$\ln R + \mathcal{O}(1)$	–
hadronization	–	$C_i$	$-1/R + \mathcal{O}(R)$	–
underlying event	–	–	$R^2 + \mathcal{O}(R^4)$	$s^\omega$

Dasgupta, Magnea, Salam **JHEP 0802 (2008) 055**

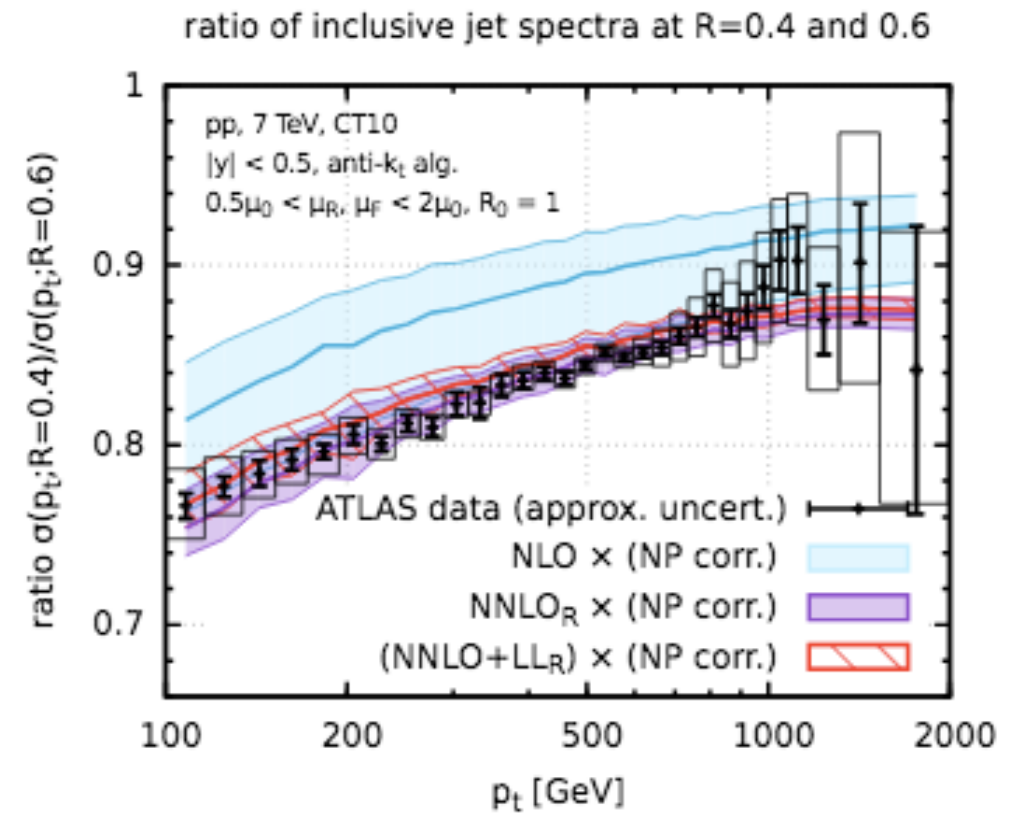
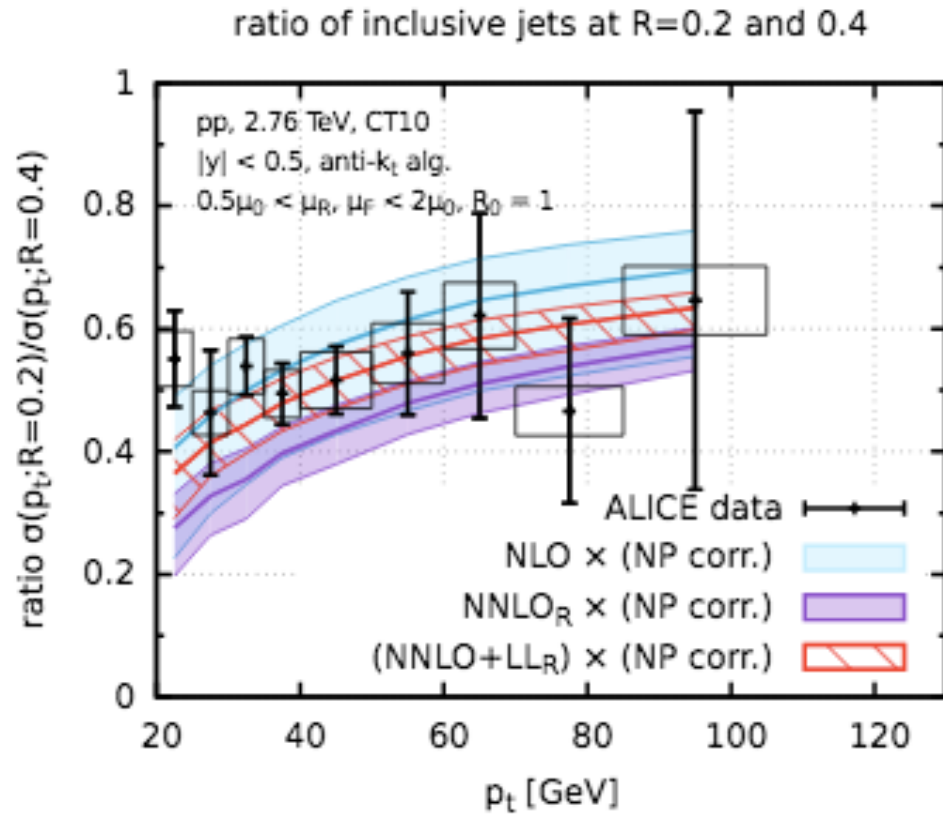
Optimal value of R depends in what component we want to study

# The perturbative and non-perturbative components of the jet



The region of low jet momentum is dominated by non-perturbative corrections

# Ratio of cross sections for different R



Dasgupta, Dreyer, Salam, Soyez, **JHEP 1606 (2016) 057**

The ratio of xsections measured with different R is sensitive to the transverse energy profile



# How to look inside a jet?

- Define jet shape variables: a function of the jet constituents.

Examples: jet mass, angularity, pTD (generalized angularities), FF...

- Recluster the jet constituents with a hierarchical algorithm.

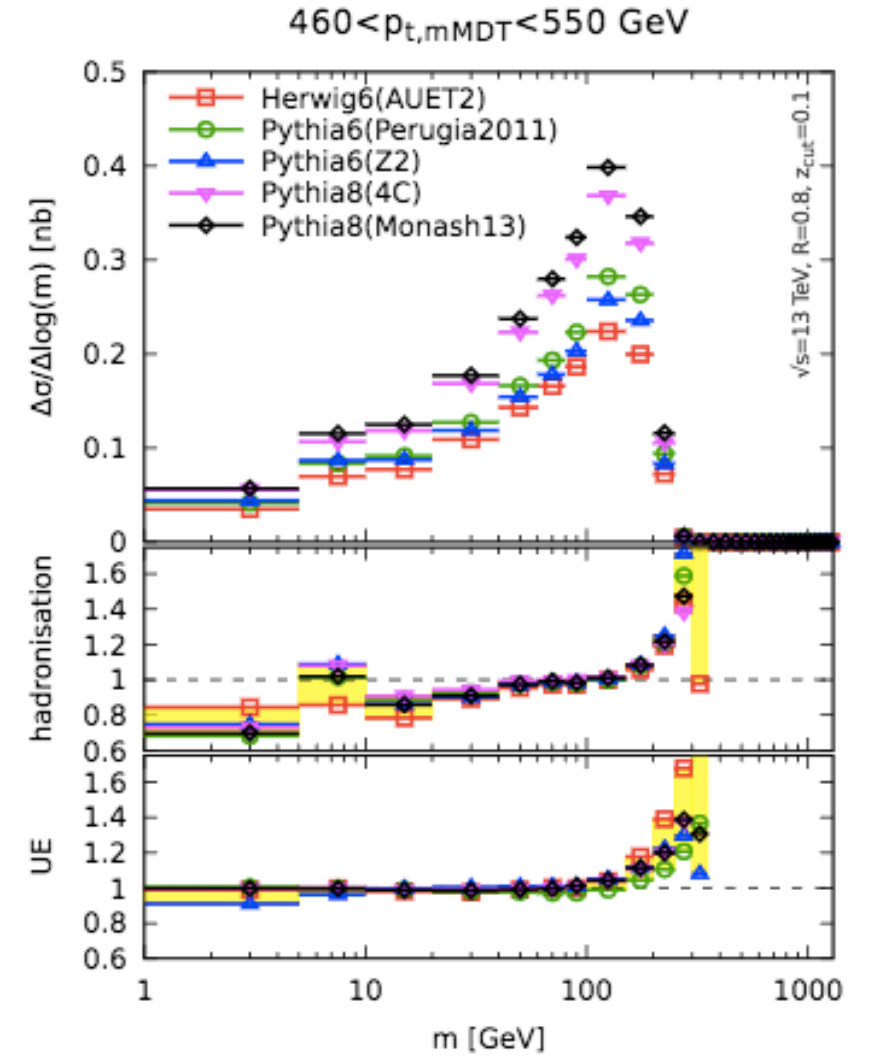
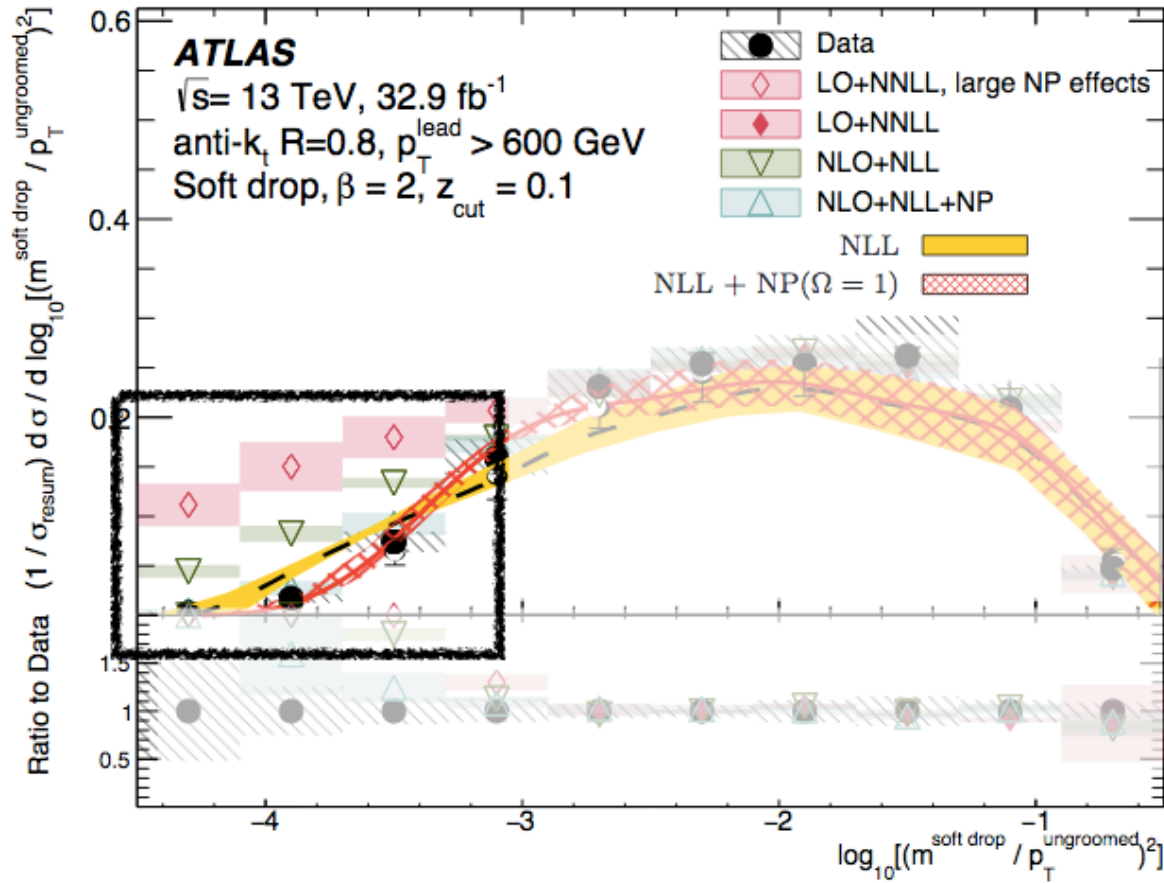
Unwind the clustering history of the jet to access the jet tree

Examples: n-subjettiness, zg, nSD,...groomed shapes in general...

Jet substructure plays a main role in LHC analysis, for instance in q/g discrimination or tagging of boosted objects.

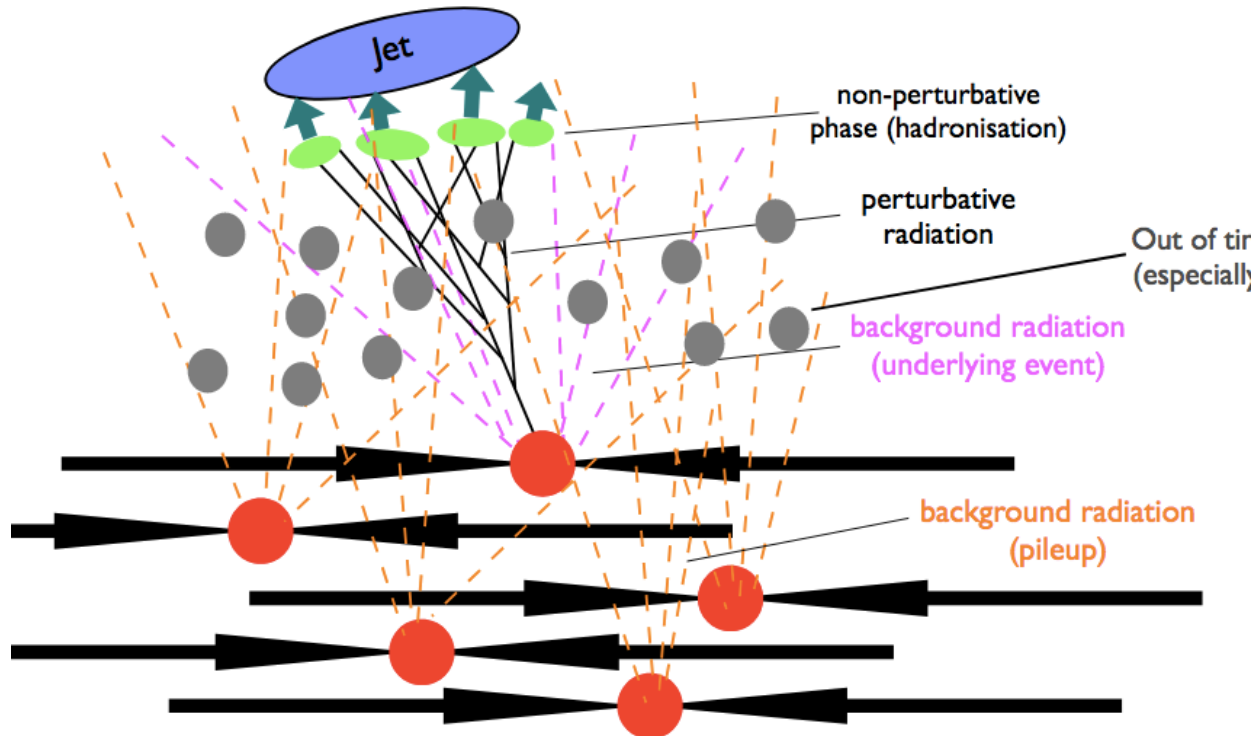
In heavy ion collisions, we use it to probe the microscopic structure of QCD matter in AA

# Jet shapes: differential constrain



Large region in mass where NP effects (yellow bands, right plot) are negligible  
 -> great constrain to perturbative aspects of parton showers

# Pileup subtraction



$$\Delta p_t = \rho A \pm (\sigma \sqrt{A})$$

Particles that are uncorrelated to the hard scattering will contaminate the jet.

The jet momentum can be adjusted, the jet area is the **background susceptibility**

The area-based equation below can be extended to shapes, to perform a zero-biased background subtraction, simultaneous in jet  $p_t$  and shape

Salam, Cacciari et al

Other methods modify the event by removing particles according to some prescription. Not bias-free.

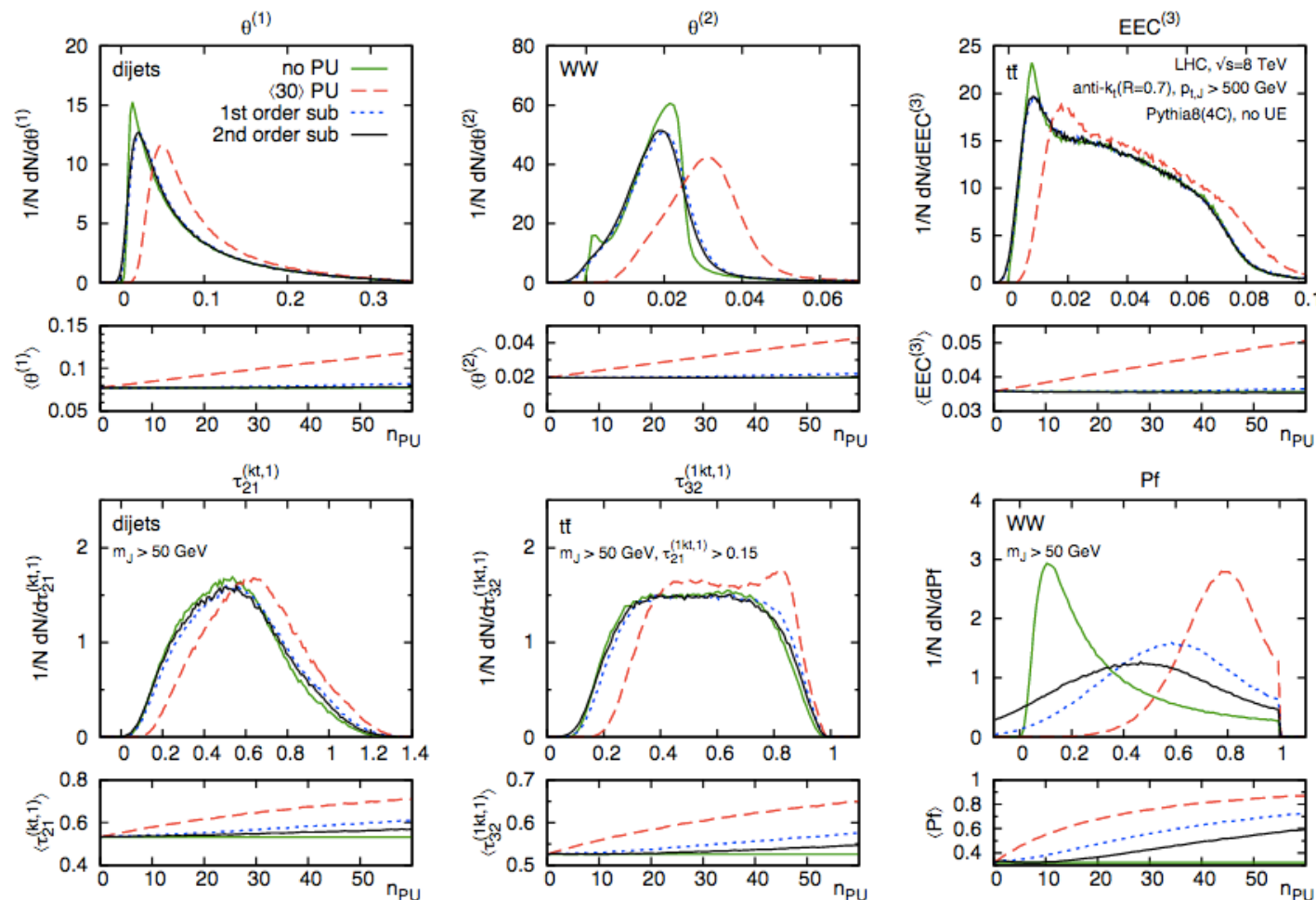
Constituent Subtraction (Berta, Spouta, Miller, Leitner, 1403.3108)

SoftKiller(MC, Salam, Soyez, 1407.0408)

PUPPI (Bertolini, Harris, Low, Tran, unpubl.)

...

# Pileup subtraction



The event pileup is characterised by  $\rho$  and  $\rho_m$ . Ghost particles are added uniformly in the acceptance, each mimicking a pileup-like component in a region of area  $A_g$ . The sensitivity of the shape to bkg is determined by calculating its derivatives with respect to the transverse momentum and mass of the ghosts. The value of the shape is then extrapolated by a Taylor series to zero pileup.

Soyez, Salam et al  
Phys.Rev.Lett. 110 (2013) no.16, 162001

# Jet grooming

## Trimming

- Take jet with radius  $R$
- Reclusters components into smaller subjets with radius  $R_{\text{sub}} < R$
- Keep subjets that satisfy  $p_{t, \text{sub}} > z_{\text{cut}} p_{t, \text{jet}}$

## Pruning

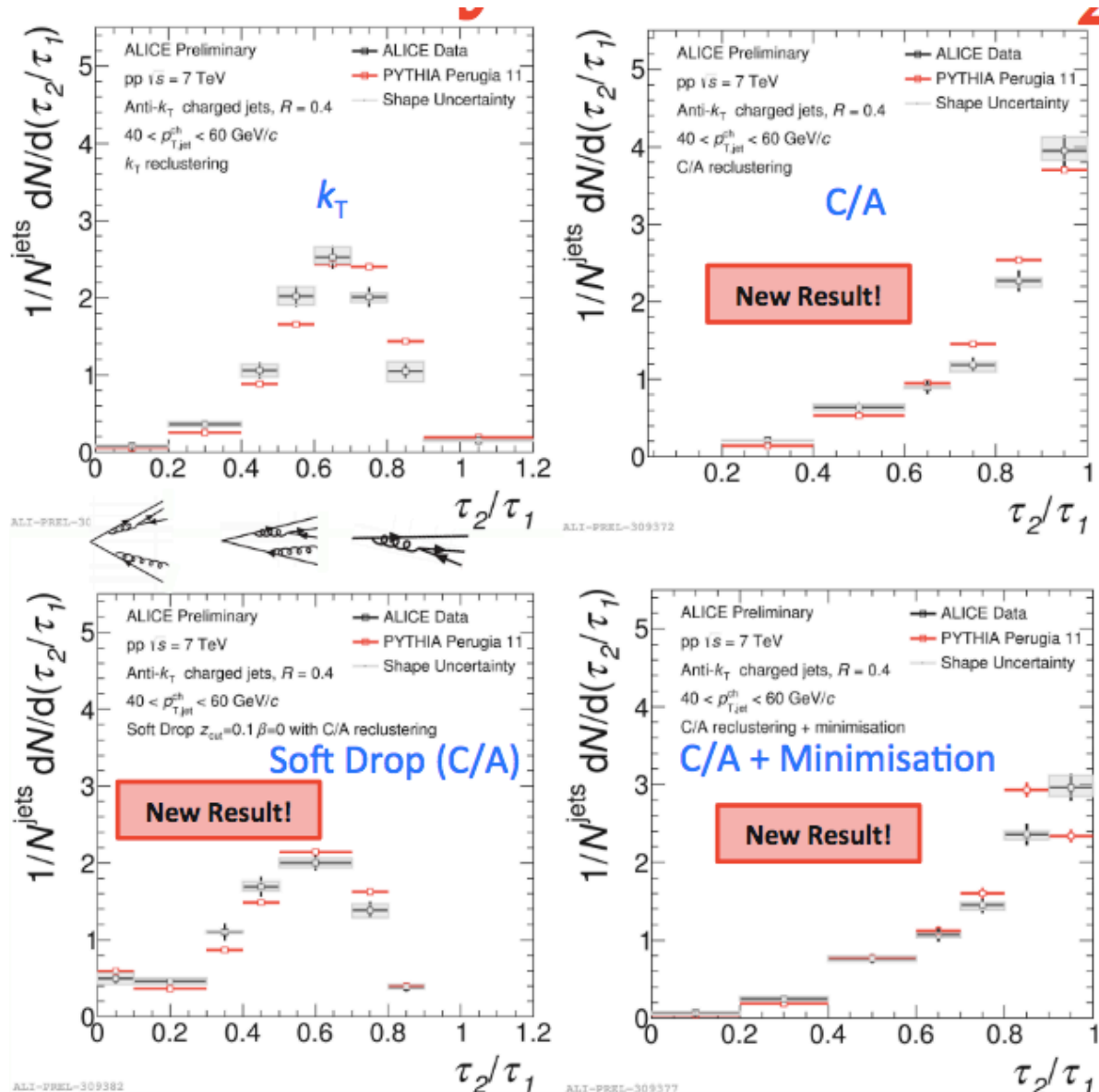
- Define pruning radius  $R_{\text{prun}} = R_{\text{cut}} * 2 m / p_t$
- For every step of clustering  $j_1 + j_2 \rightarrow j_{12}$ , check:
  - Wide-angle:  $\Delta R_{12} > R_{\text{prun}}$
  - Soft:  $\min(p_{t1}, p_{t2}) < z_{\text{cut}} p_{t, \text{jet}}$
- If either condition fails, eliminates softer subjet
- If both pass, continue clustering

## SoftDrop (or mMDT)

- Decluster jet  $j_{12} \rightarrow j_1 + j_2$
- Check condition  $\min(p_{t1}, p_{t2}) / p_{t, \text{jet}} > z_{\text{cut}} (\Delta R_{12} / R)^\beta$ 
  - $z_{\text{cut}}, \beta$ : tunable values
- If condition fails, the softer subjet is removed
- If passes, stops recursion
- For  $\beta=0$ , it is mMDT

**AIM: Limit contamination of QCD background in a controlled way while retaining the bulk of perturbative radiation ->interesting idea to export to HI!**

# Example of substructure in pp: N-Subjettiness



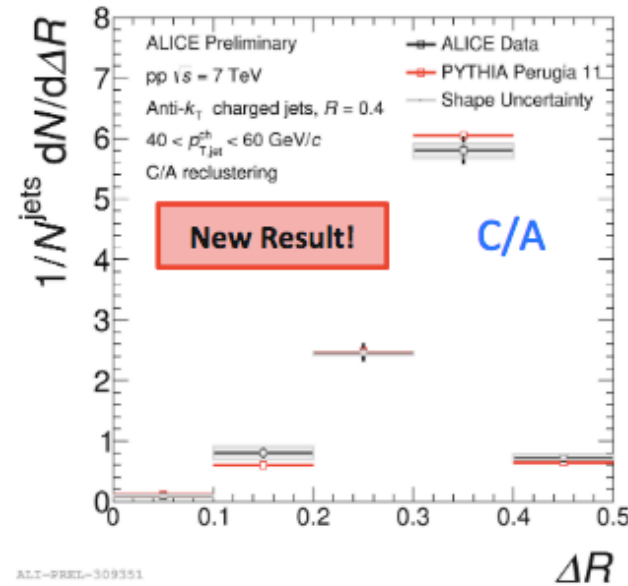
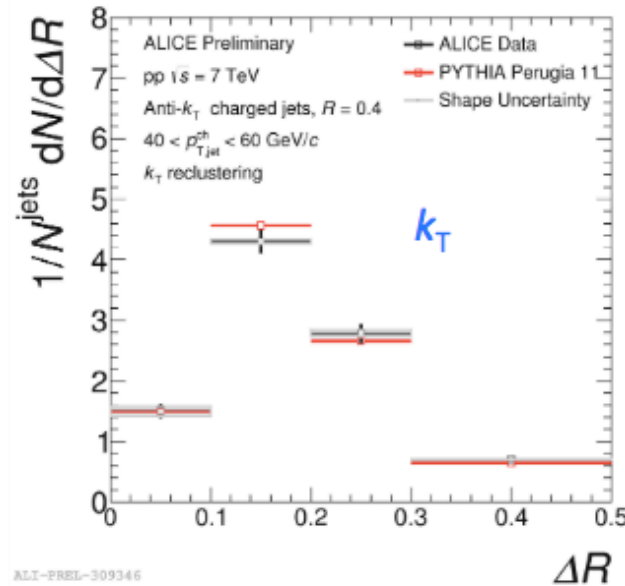
$$\tau_N = \frac{\sum_{i=1} p_{T,i} \text{Min}(\Delta R_{i,1}, \Delta R_{i,2}, \dots, \Delta R_{i,N})}{R_0 \sum_{i=1} p_{T,i}}$$

$\tau_2/\tau_1 \rightarrow 0$  means that the jet is 2-prong  
 $\tau_2/\tau_1 \rightarrow 1$  the jet has more prongs than just 2

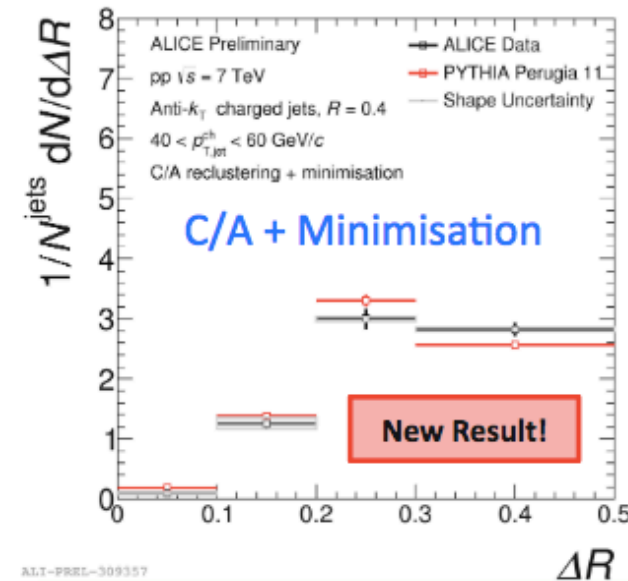
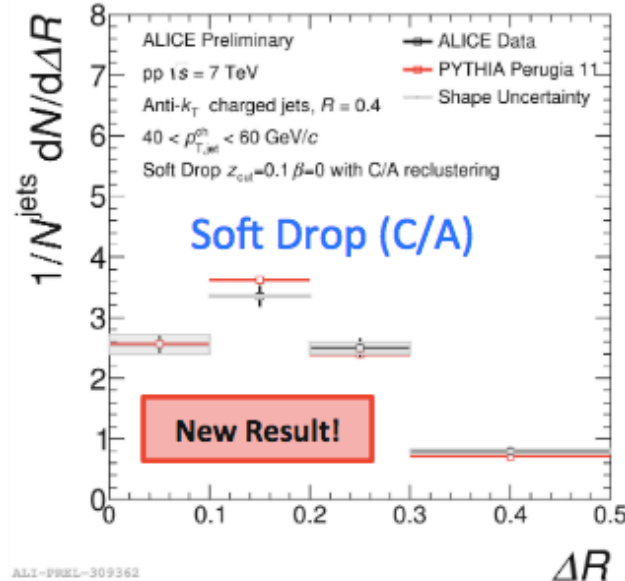
$\tau_2/\tau_1$  measures how well the radiation is aligned relative to returned axes.

Changing the reclustering algorithm allows to probe different splittings in the jet

# Example substructure in pp: aperture angle

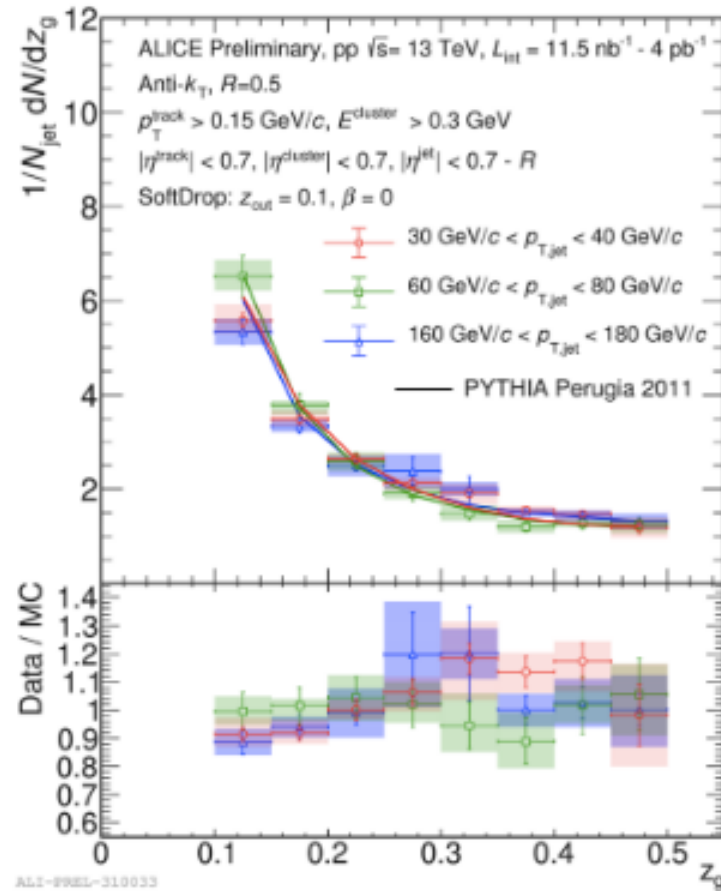


Angular separation of different splittings in the jet

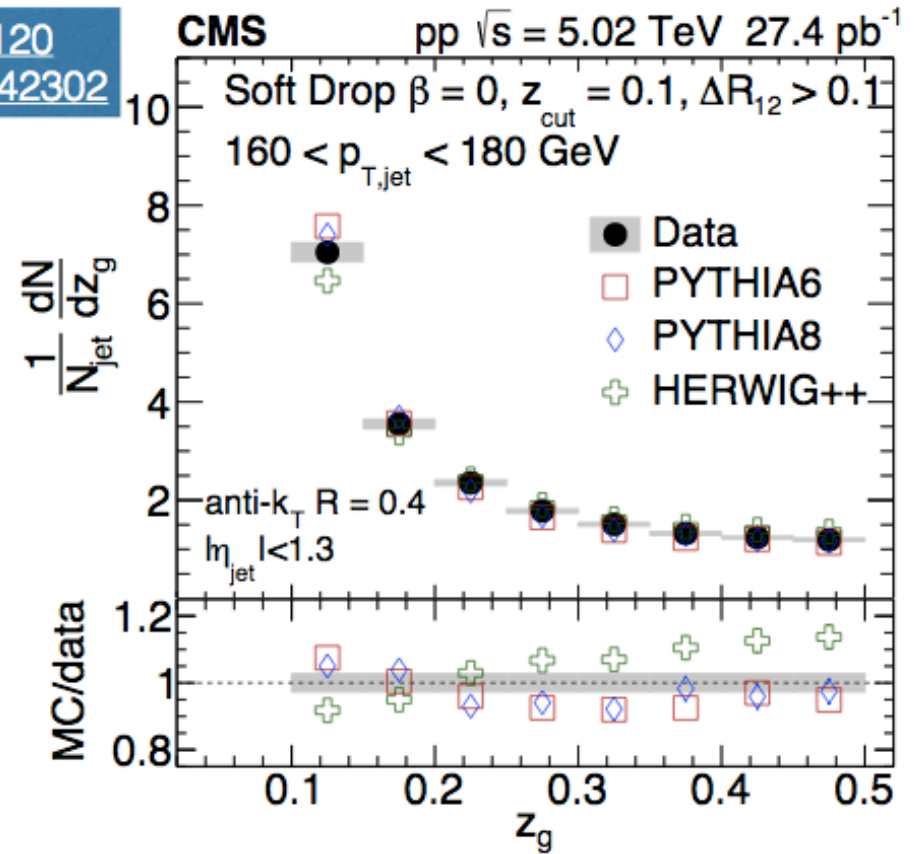




# Example of groomed substructure pp: momentum imbalance



PRL 120  
 (2018) 142302

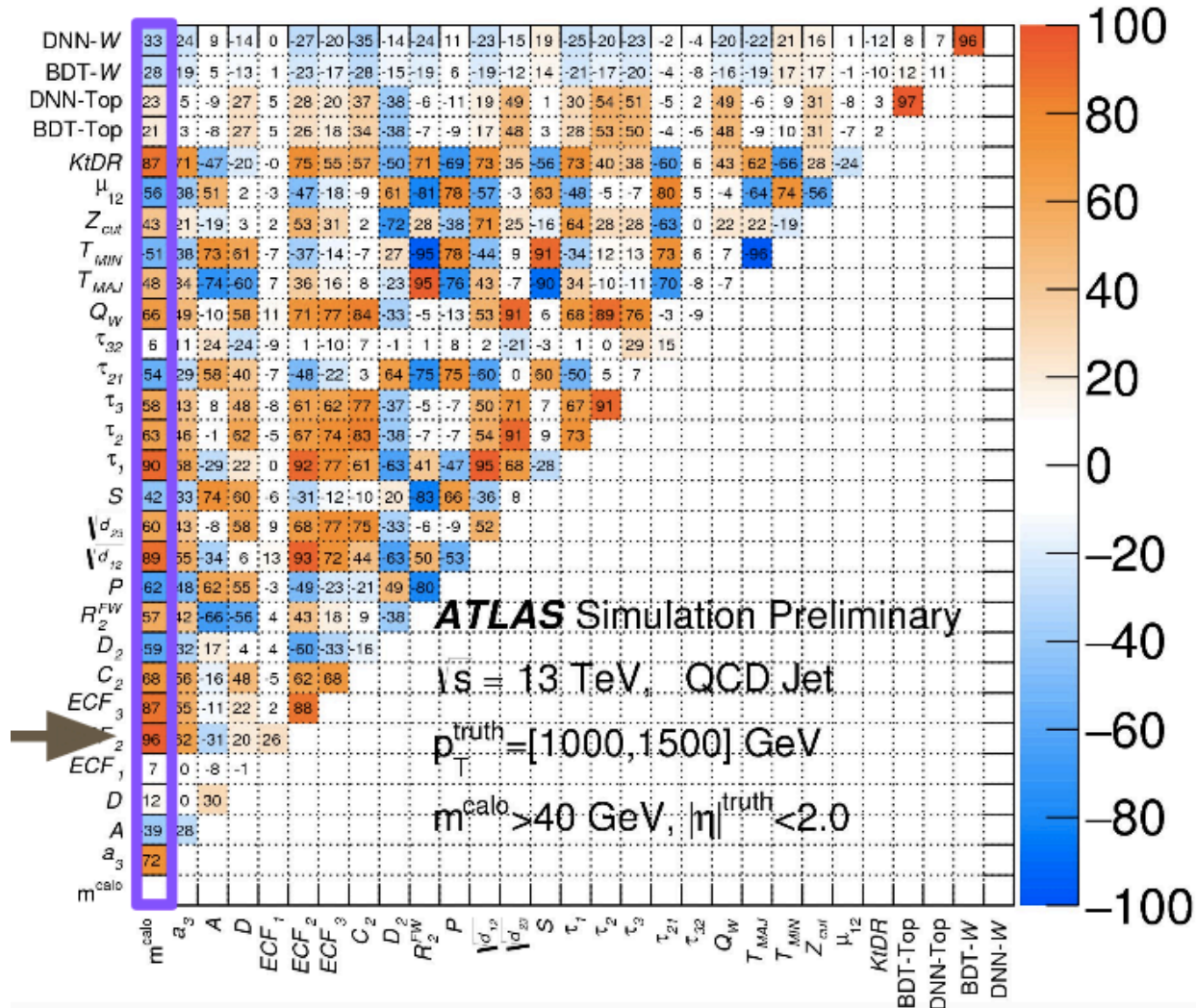


$z_g$  is the momentum imbalance of the first pair of subjects that pass the mass drop condition

No jet  $p_T$  dependence, as expected if  $z_g$  in vacuum is a valid proxy for the Altarelli-Parisi splitting kernel, universal  $1/z$  behaviour



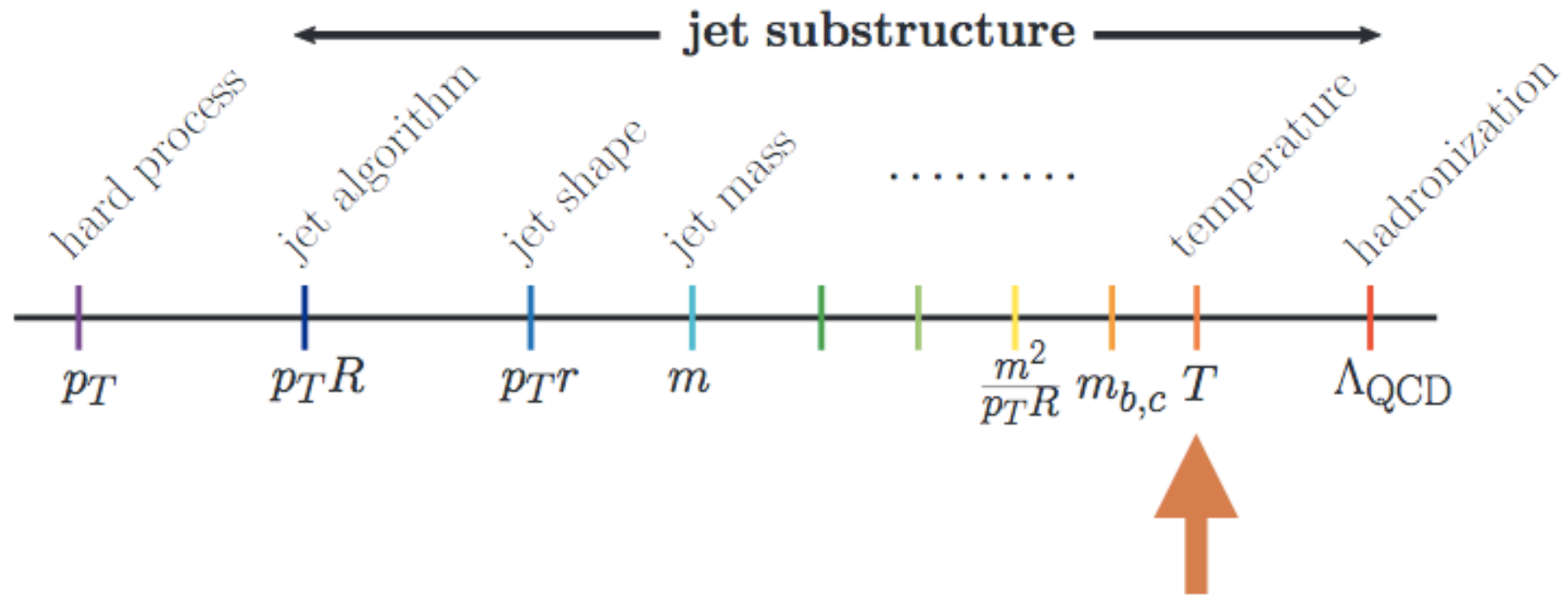
# Jet substructure observables



Difficult to find a jet shape that is not correlated/anticorrelated with the jet mass

In order to extract maximal information (ie about jet quenching), the more uncorrelated the set of observables, the better

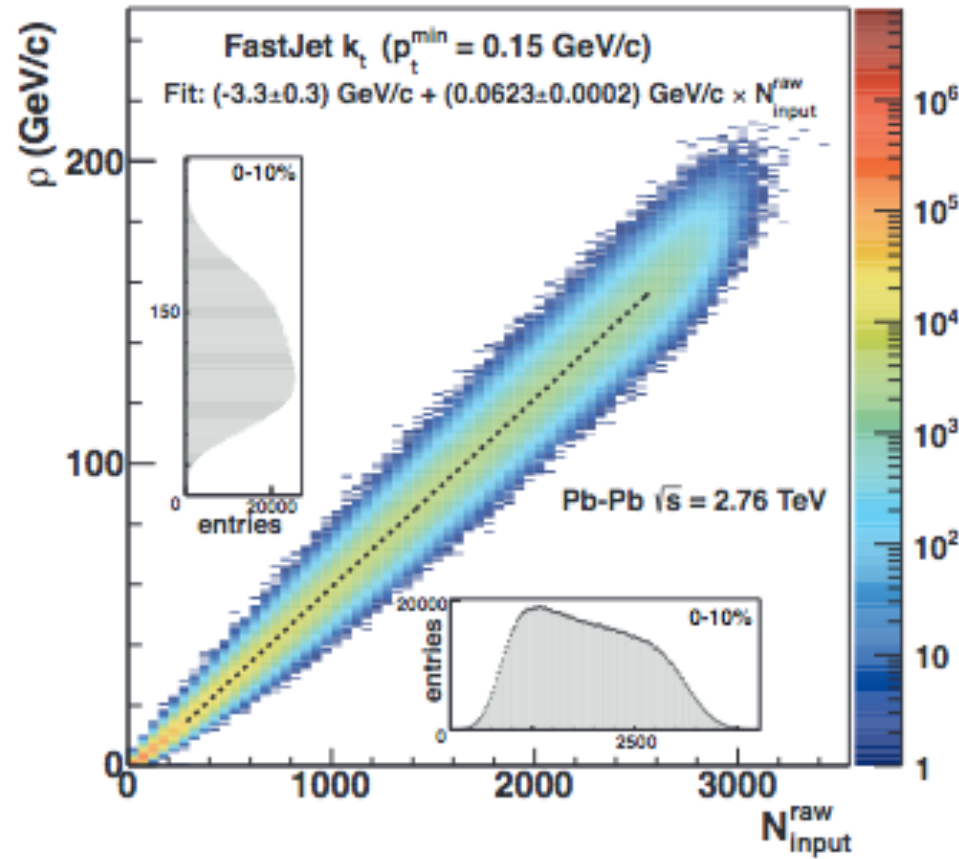
# Jets in Heavy Ion Collisions



## Several fundamental questions to answer

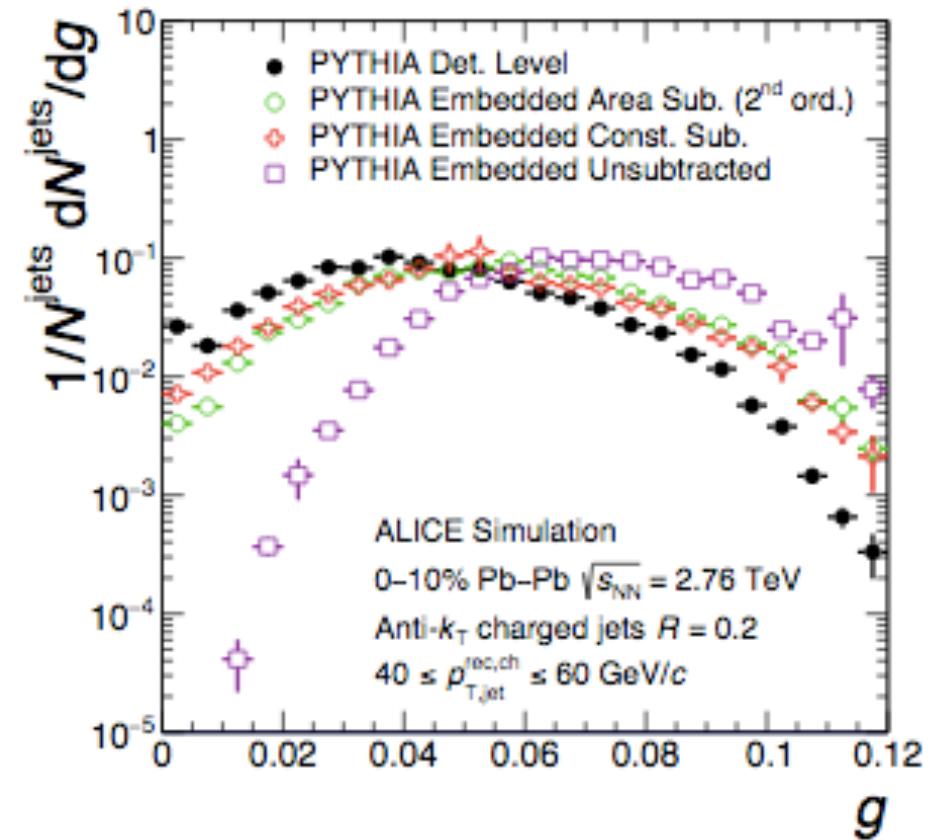
- Can we probe the partonic degrees of freedom within the strongly-coupled QGP? Do we have access to the Moliere regime? Can we detect scatterings off quasi-particles via large angle deflection of jets/constituents?
- Is color coherence at work and what are the critical angles?
- Is flavour hierarchy respected in medium?
- Related to the 3 previous points: how does energy loss depend on the jet substructure?
- Can we experimentally isolate specific aspects of the in-medium shower that are under better theoretical control?

# Large pedestal background to subtract



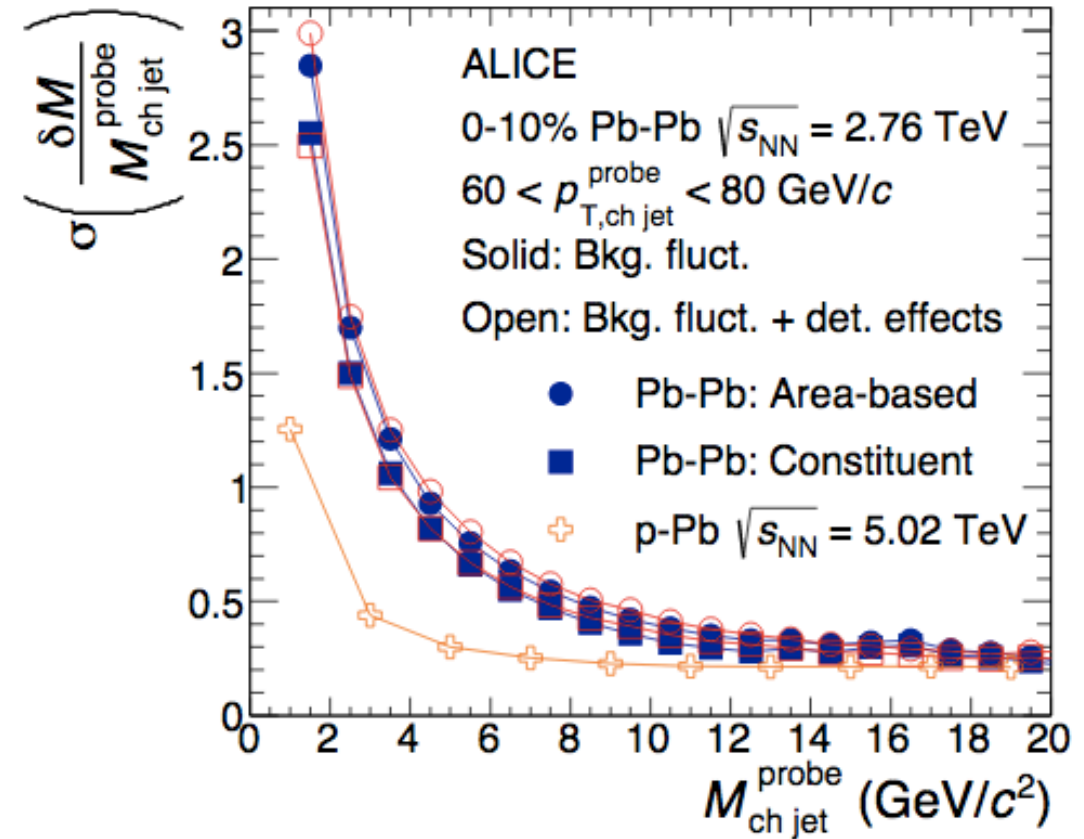
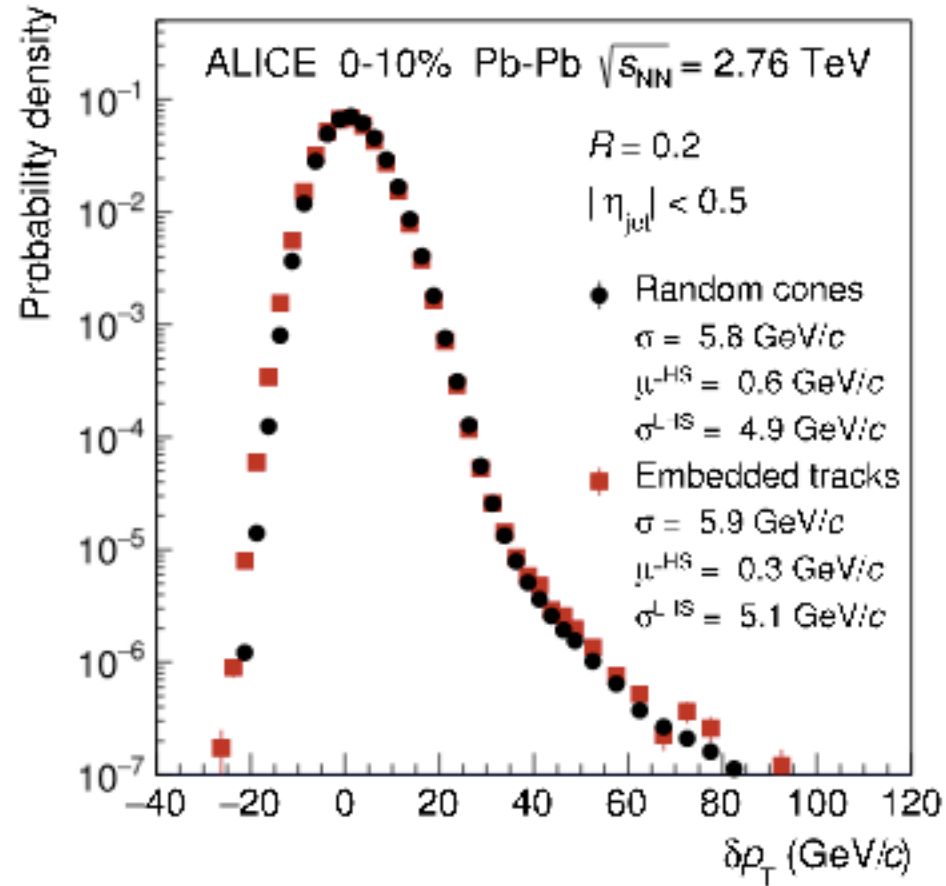
Large uncorrelated background per unit area

Pythia events embedded into PbPb data

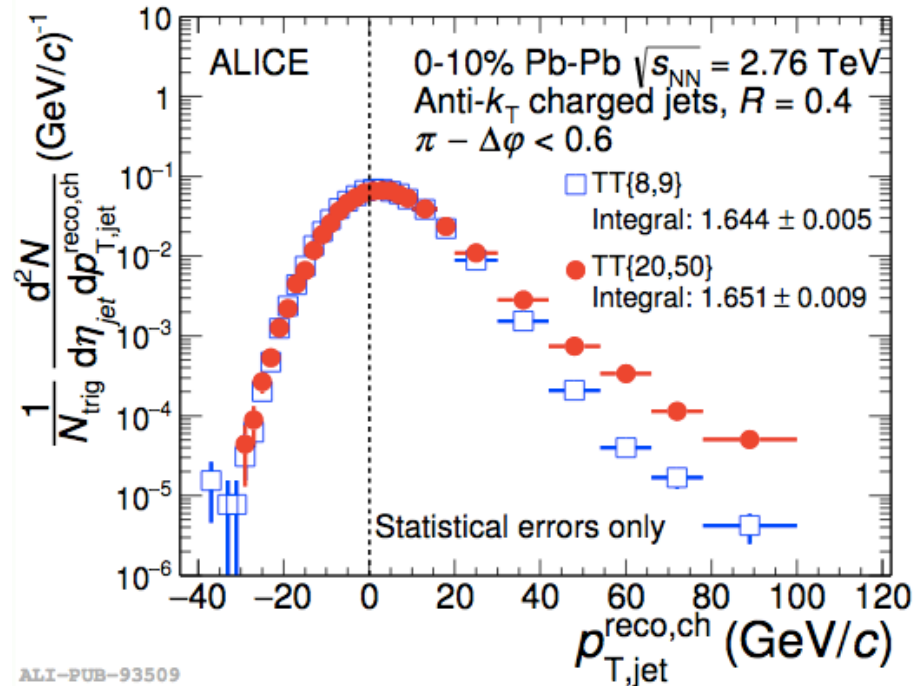


same techniques as in HEP

# Jet energy and shape irresolution to unfold



# Large combinatorial background to suppress

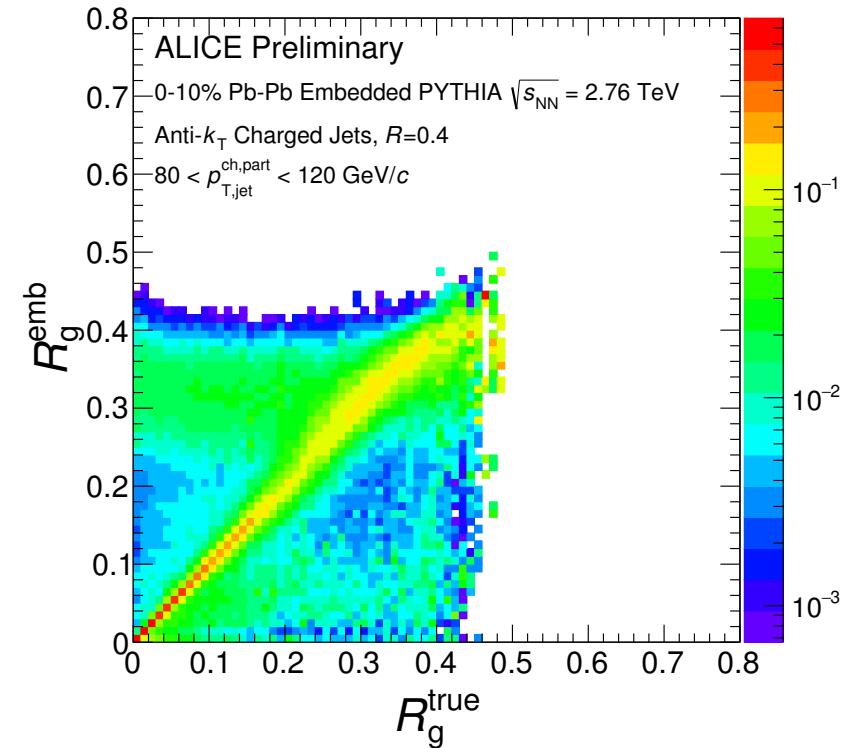


ALICE, JHEP09(2015)170

Large fake jet contribution limits inclusive jet measurements at low jet  $p_T$ /large  $R$

Data-driven techniques based on semi-inclusive coincidence measurements can be applied to subtract combinatorial background  
Jet event mixing, ML are other approaches under exploration

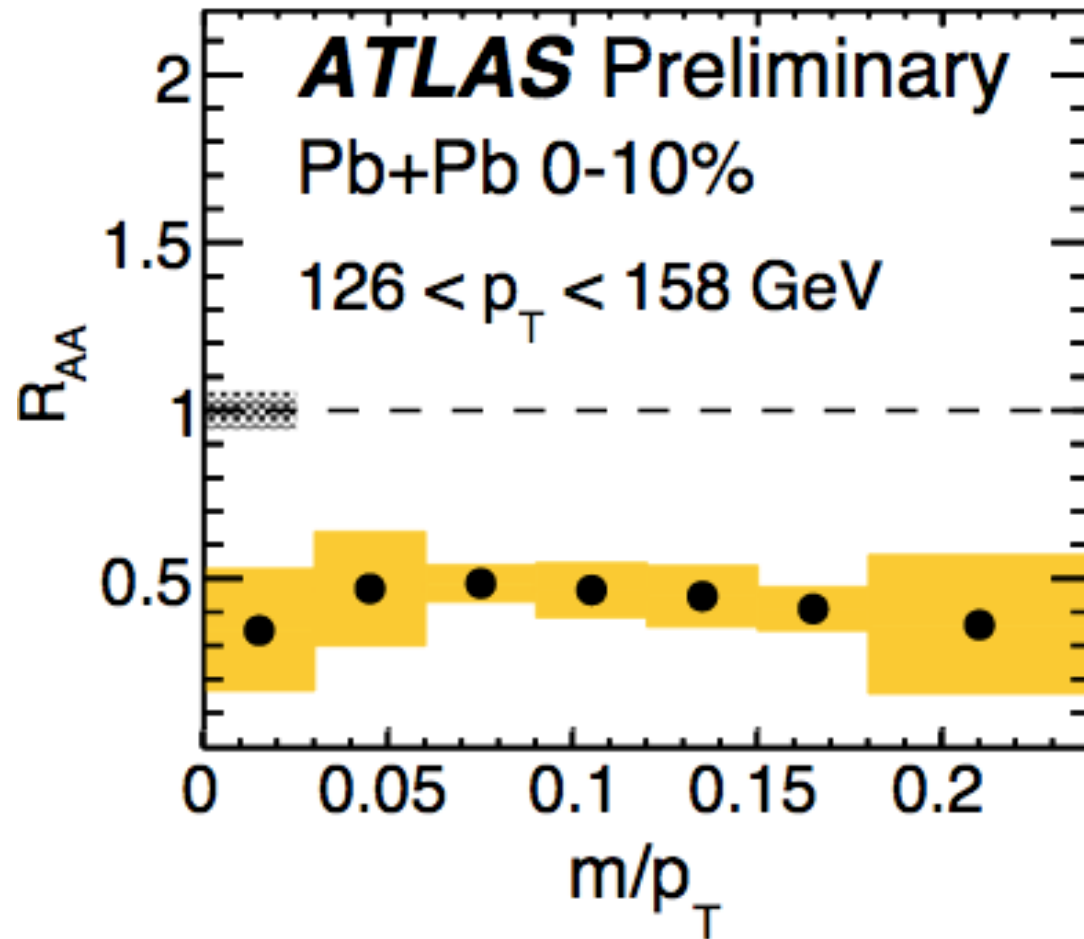
Background and detector response of the splitting aperture angle



The uncorrelated background generates fake subleading prongs at large angles (where area is maximal)

# Does the energy loss depend on the jet shape?

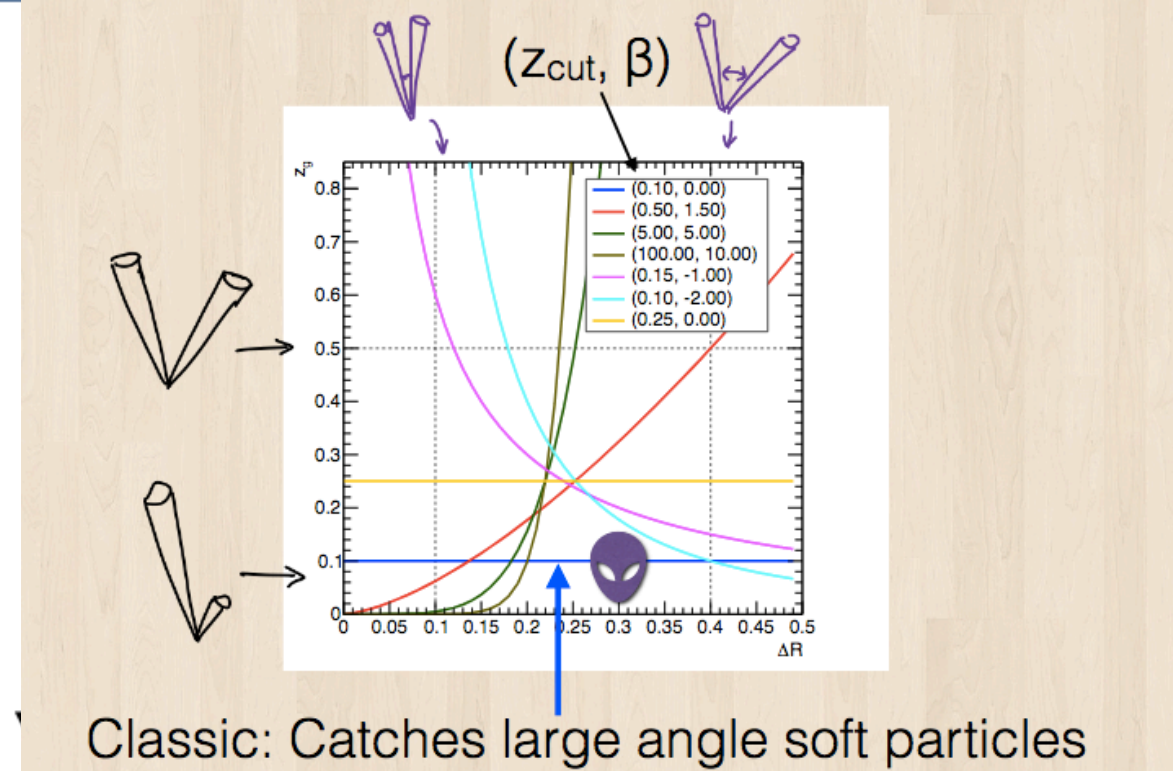
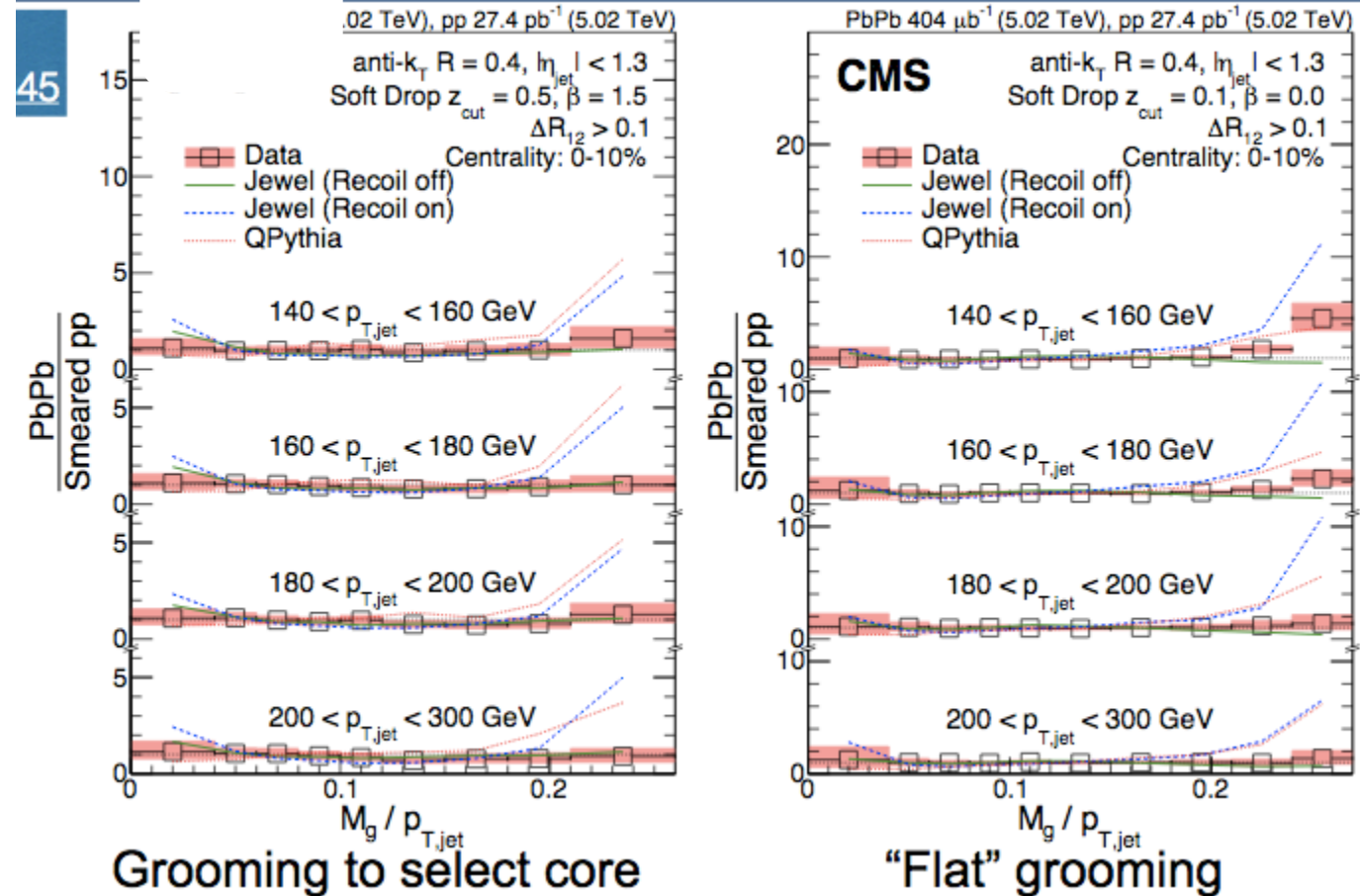
ATLAS: mass from calorimeter towers



No apparent dependence observed



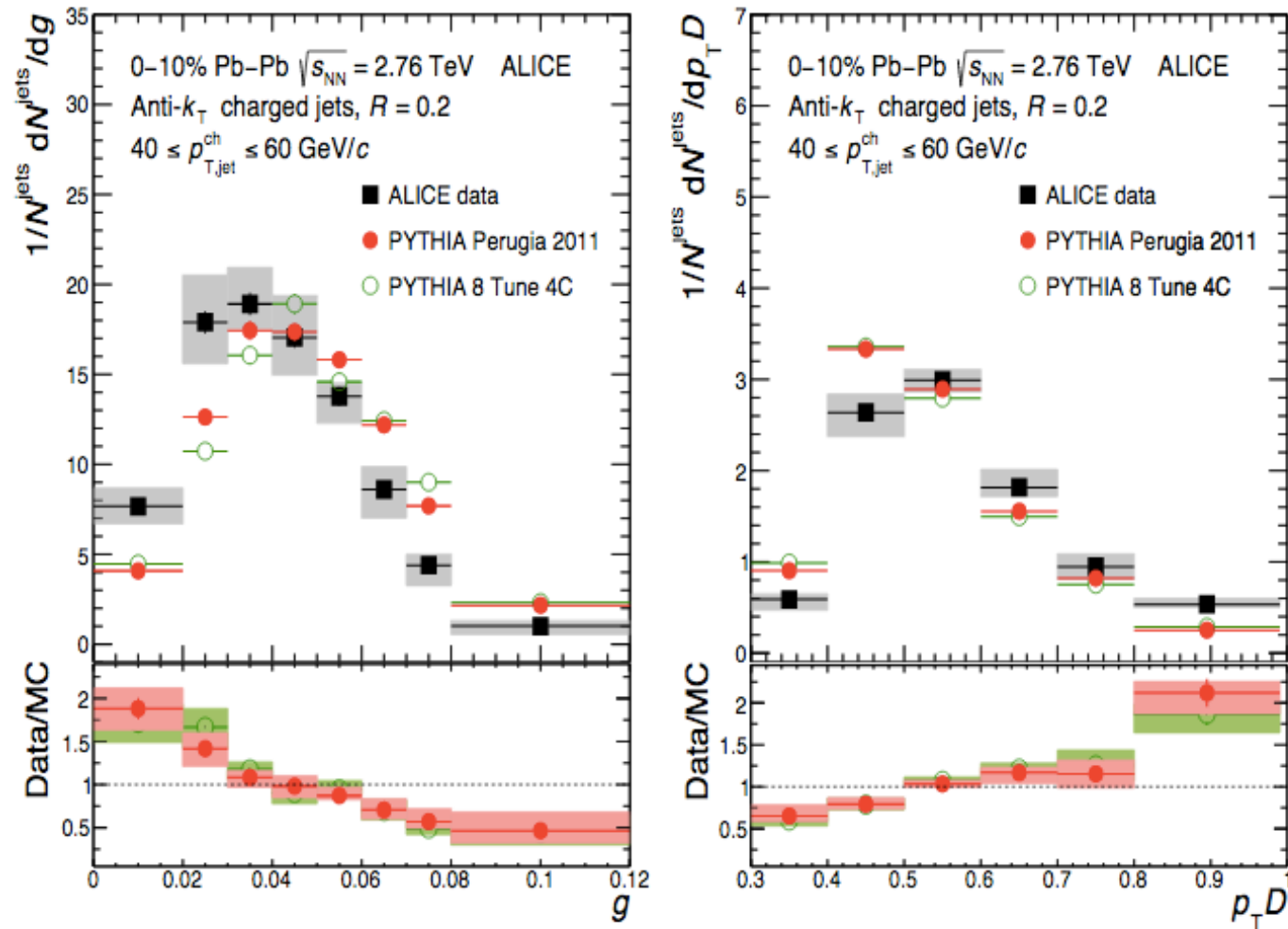
# Does the energy loss depend on the jet shape?



Interesting exploration of the phase space of emissions  
 Some effects at the tails

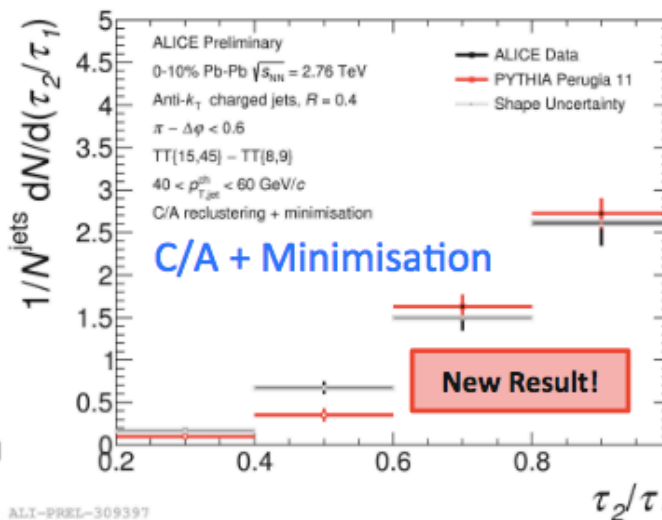
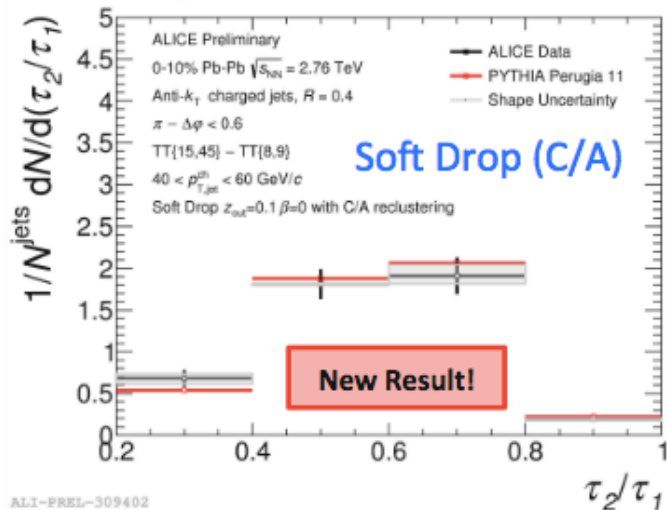
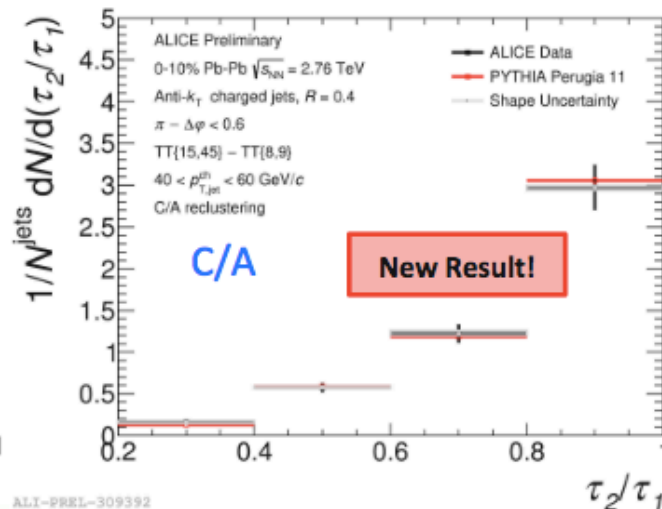
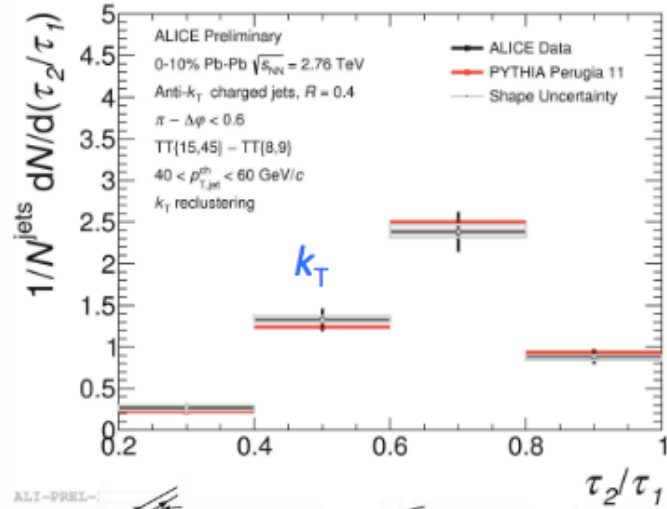


# Does the energy loss depend on the jet shape?



The jet cores seem to get narrower and harder in medium relative to vacuum, in agreement with a quark-like fragmentation

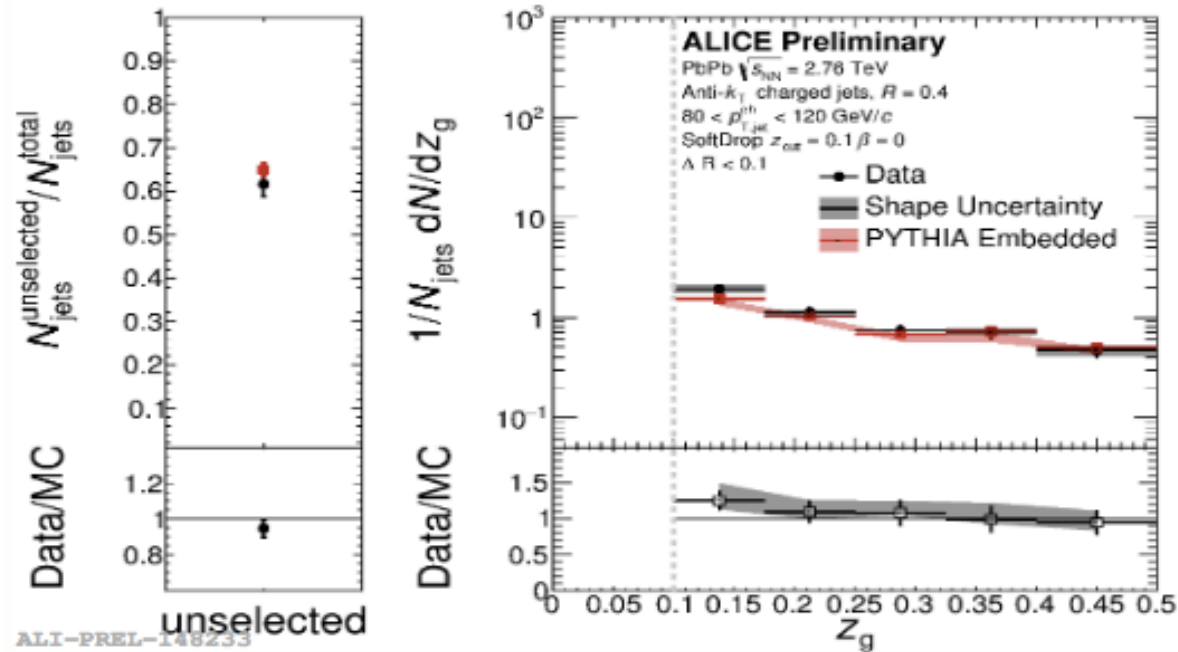
# Does the energy loss depend on the jet shape?



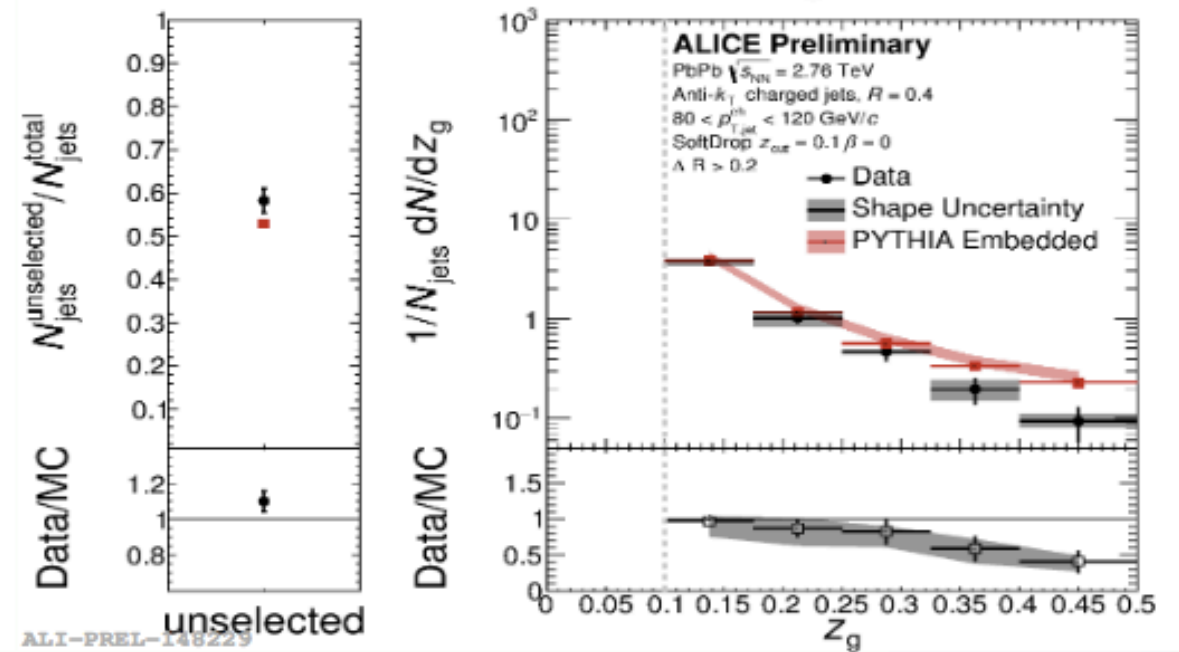
The way radiation is aligned relative to the chosen splittings ( a very different set of splittings was considered) does not change in medium relative to vacuum

# Momentum imbalance

$\Delta R < 0.1$  cut  $\swarrow \searrow$  Collimated splittings



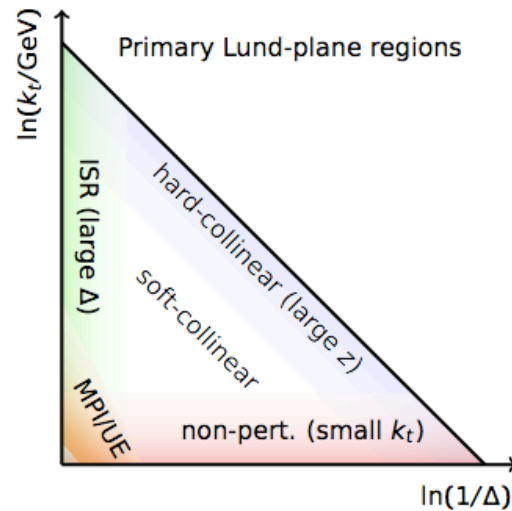
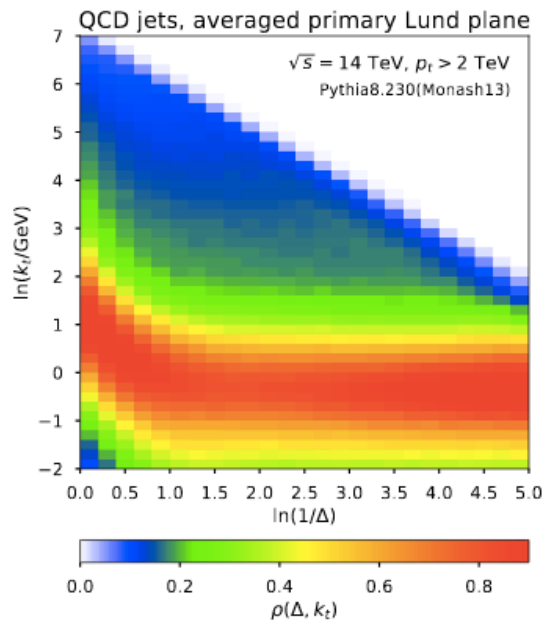
$\Delta R > 0.2$  cut  $\swarrow \searrow$  Large Angle splittings



Suppression of symmetric splittings at large angles  
 Enhancement of collinear splittings  
 Interesting implications concerning formation time

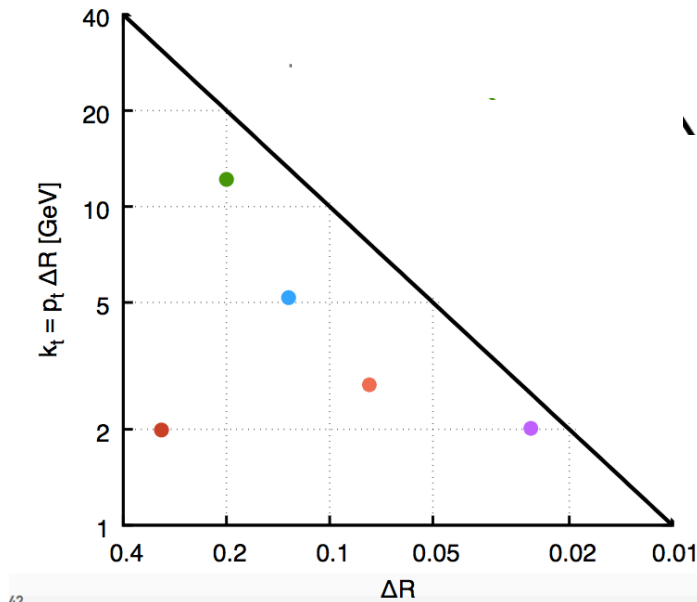
# The Lund plane

- A general 2D map of splittings, most of other substructure observables are derived from it
- Relevant scales like the splitting scale  $k_T$ , formation time, constant mass, can be marked as simple line cuts on the plane
- Powerful tool to isolate different physics ingredients in the jet quenching calculations (ideal tool for JETSCAPE)



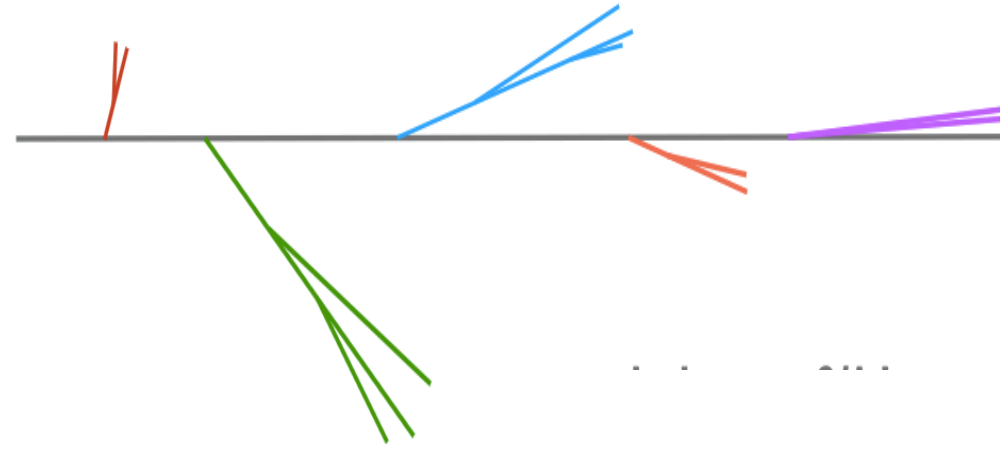
Dreyer, Salam, Soyez,  
<https://arxiv.org/pdf/1807.04758.pdf>

# The Lund plane in vacuum



*plot from G.Salam, QM18*

$$d^2 P = 2 \frac{\alpha_s(k_{\perp}) C_R}{\pi} d\ln(z\theta) d\ln\left(\frac{1}{\theta}\right)$$



## Iterative declustering:

Unwind the CA clustering (angular ordering in vacuum)

At each step, register the  $k_T$ ,  $\Delta R$  coordinates

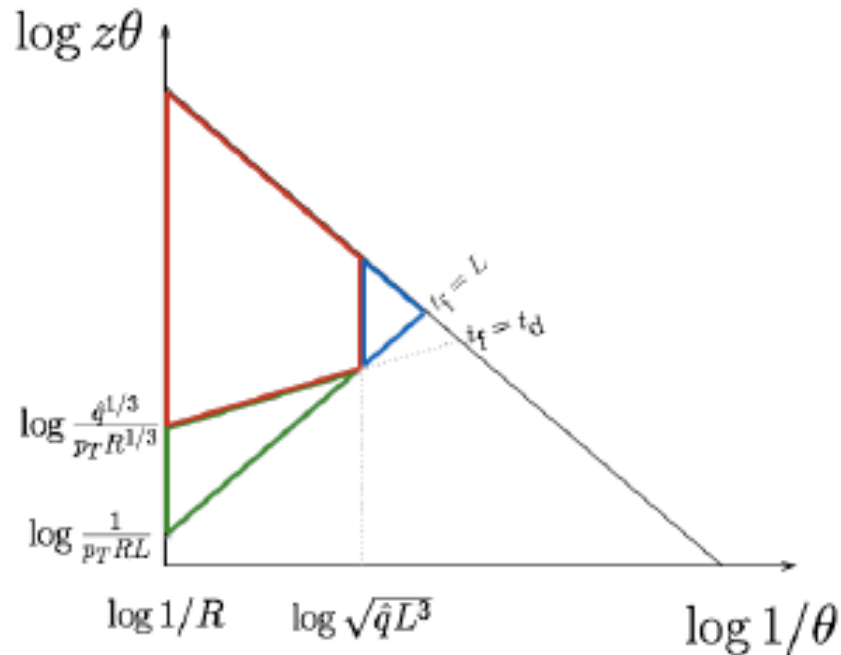
Follow the hardest branch at each step

In vacuum, flat 2D density except for variation of the coupling with  $k_T$

# The Lund plane in medium

Angular ordering not expected in medium, so using CA to recluster is an operational choice

New scales appear due to the medium and divide the phase space: formation time, decoherence time, decoherence angle...:



$t_f < t_d < L$  vacuum splittings inside the medium

In medium splittings with  $t_d > L$ : not resolved by the medium

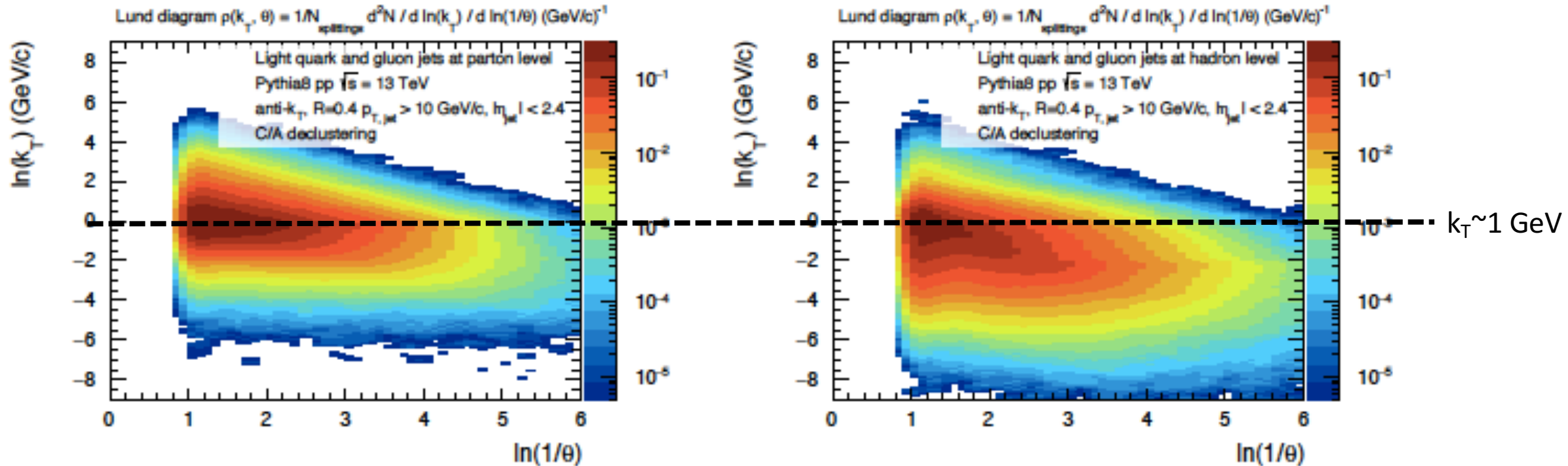
$t_d \lesssim t_f$  splitting kinematics dominated by medium effects Lund plane not filled with the pQCD uniform probability

*K.Tywoniuk et al, Novel tools and observables for jet physics in heavy ion collisions,*  
<https://arxiv.org/pdf/1808.03689.pdf>

# Map different contributions: hadronization

Parton level

Hadron level

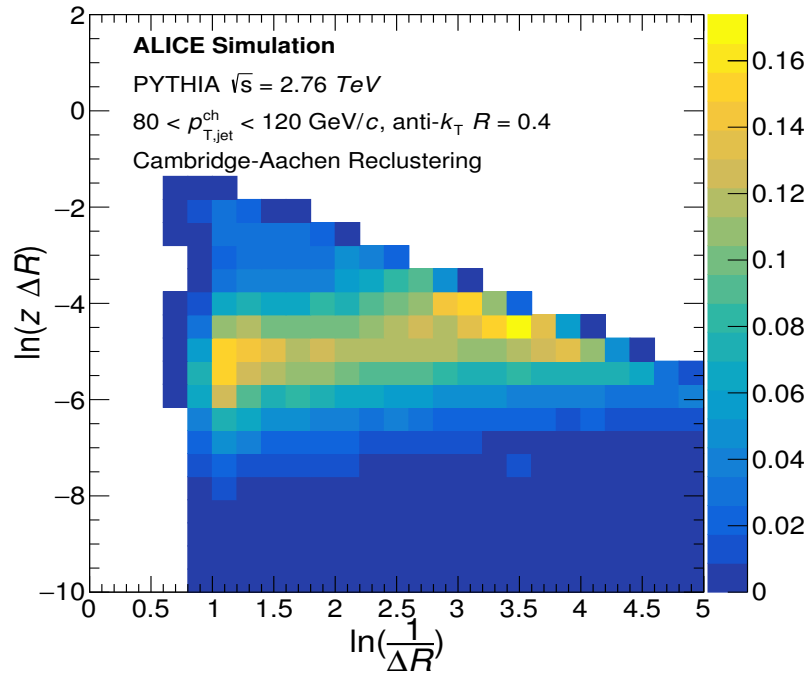


L.Cunqueiro, M.Ploskon, <https://arxiv.org/pdf/1812.00102.pdf>

Non-perturbative effects can be removed/isolated by cutting at  $\ln(k_T) > / < 0$

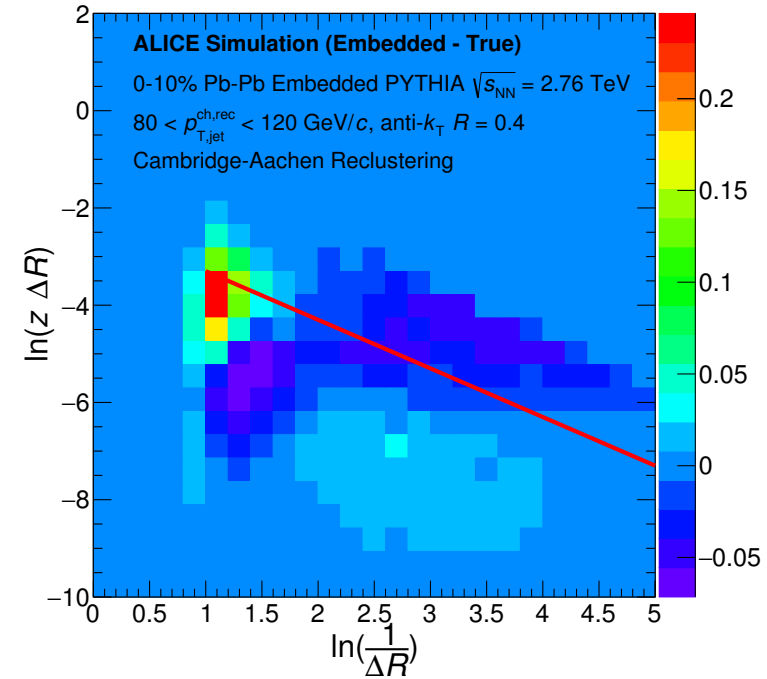
# Map different contributions: uncorrelated background

PYTHIA jets



ALI-SIMUL-161454

PYTHIA jets embedded into  
0-10% central Pb-Pb events



ALI-SIMUL-154411

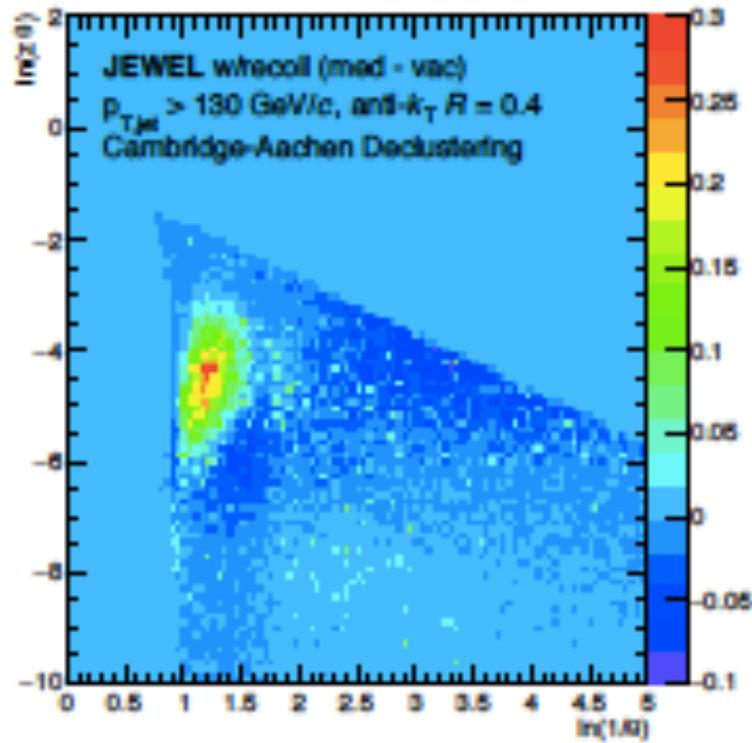
Fake splittings appear at large angles  $\theta \sim R$  and lowish  $z$

They contribute to the groomed signal (above red line representing  
SD condition  $z_{cut} > 0.1$ ,  $\beta = 0$ )



# Map different contributions: correlated background

## JEWEL MC: Medium - Vacuum



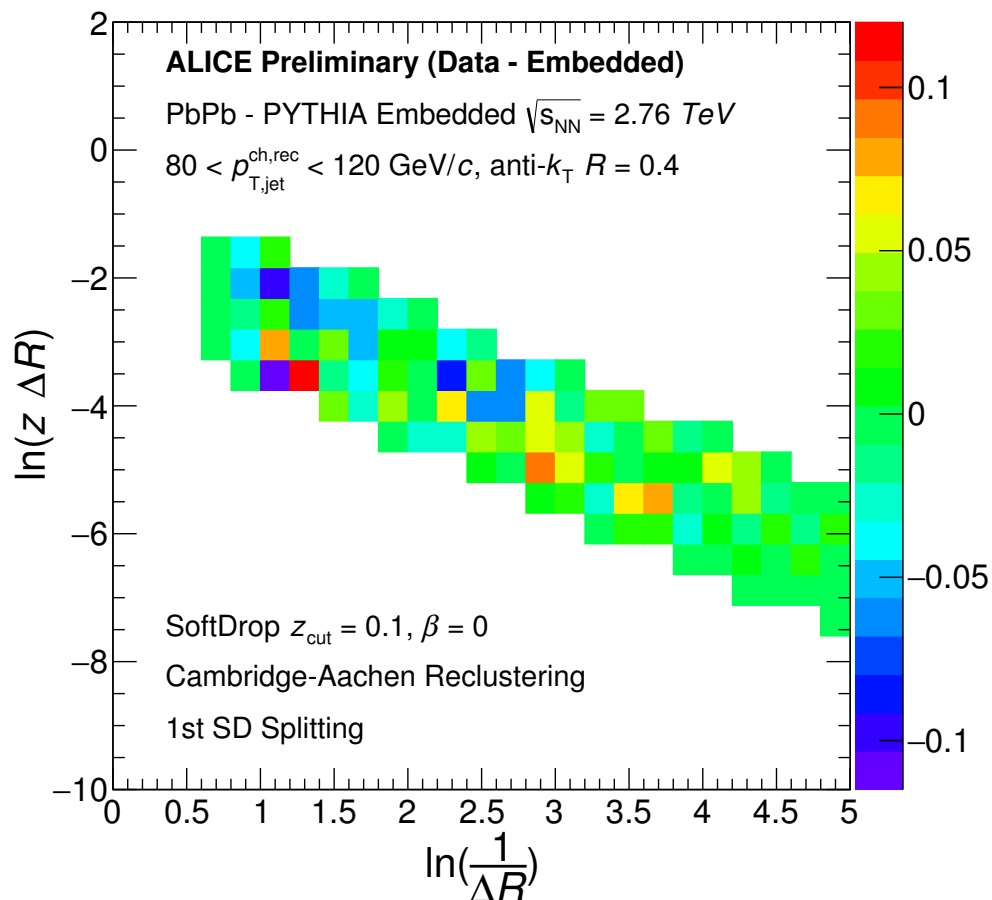
The correlated background or medium response is the background that gets “excited by the jet” and ends up in the jet cone.

As correlated bkg, it cannot be suppressed using standard techniques like event mixing or coincidence measurements.

*K.Tywoniuk et al, Novel tools and observables  
for jet physics in heavy ion collisions,  
<https://arxiv.org/pdf/1808.03689.pdf>*

# Lund plane in Pb-Pb , it can be measured

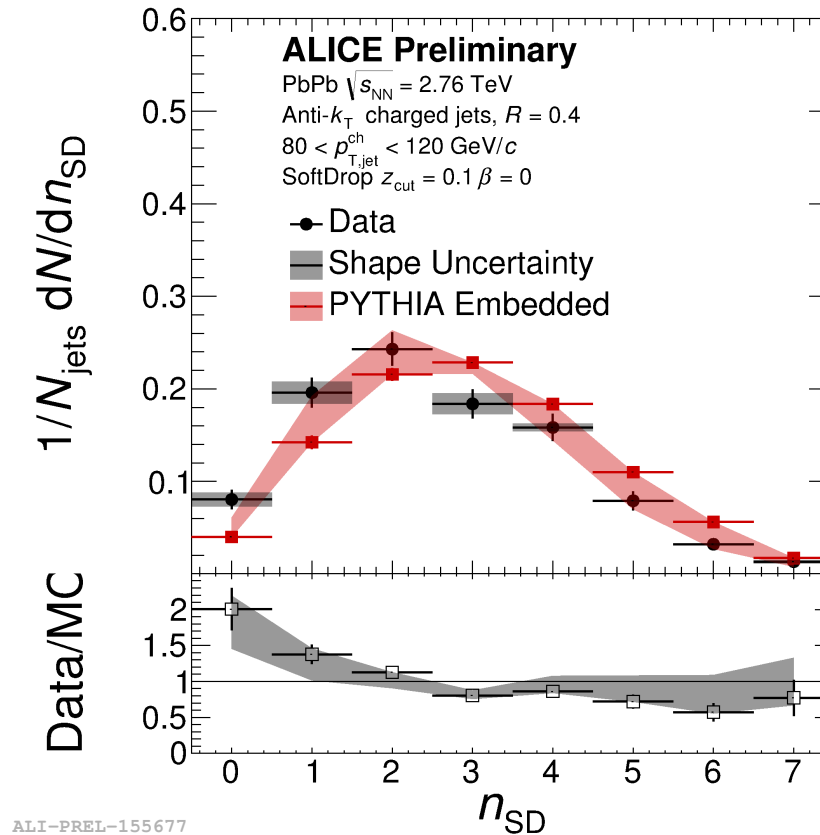
Probability density difference: Data - PYTHIA embedded into Pb-Pb events



Useful observable are 1D projections  
in bins of scale  $k_T$

Quite differential, requires plenty of  
statistics

# Lund plane: number of entries (splittings)



The density map of splittings is deformed in Pb-Pb relative to vacuum, but this deformation is not accompanied by an increase in the number of hard splittings selected by SD.

# Some thoughts on data to MC comparison in Heavy Ions in the context of JETSCAPE

## 1. The way jet observables are presented by the collaborations:

- Ideal: Fully corrected to particle level, can be directly compared to MC
- Not fully corrected observables. Sometimes unfolding is not possible, responses can be severely off-diagonal leading to unstable unfolding. Then, MC has to be smeared according to the responses the experiments provide.

**Example case:** ALICE measured the  $z_g$  vs  $\Delta R$  in a given jet  $p_T$  bin at uncorrected level, and provides a 6D response ( $z_g^{\text{part}}, \Delta R^{\text{part}}, p_T^{\text{part}}, z_g^{\text{emb}}, \Delta R^{\text{emb}}, p_T^{\text{emb}}$ )

# Some thoughts on data to MC comparison in Heavy Ions in the context of JETSCAPE

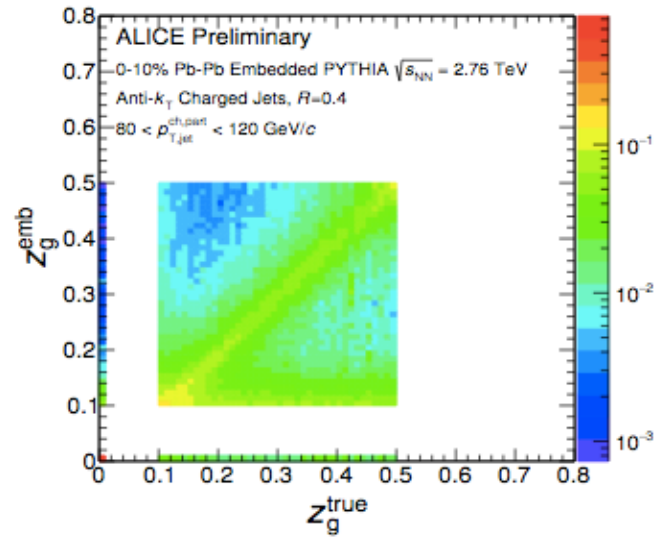
## 2. Strategies for MC to data comparison:

- **Selective choice of observables** when extracting fundamental properties like  $q_{\text{hat}}$  : choose those that **are less affected by model-dependent** components like hadronization.
- **Isolation of physics ingredients**: the modular nature of JETSCAPE allows to test what physics ingredients contribute to what regions of the jet phase space and to test them experimentally.

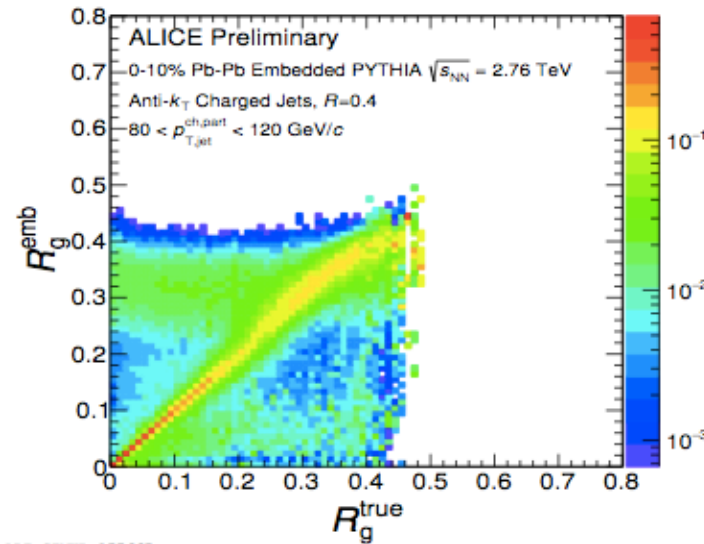
A possible example: fill the Lund map switching on/off the different physics components of the JETSCAPE framework. Is there a region of the 2D phase space map that gets modified by a single physics ingredient? -> Then opportunity to test the model and propose an experimental observable.

- THANKS!

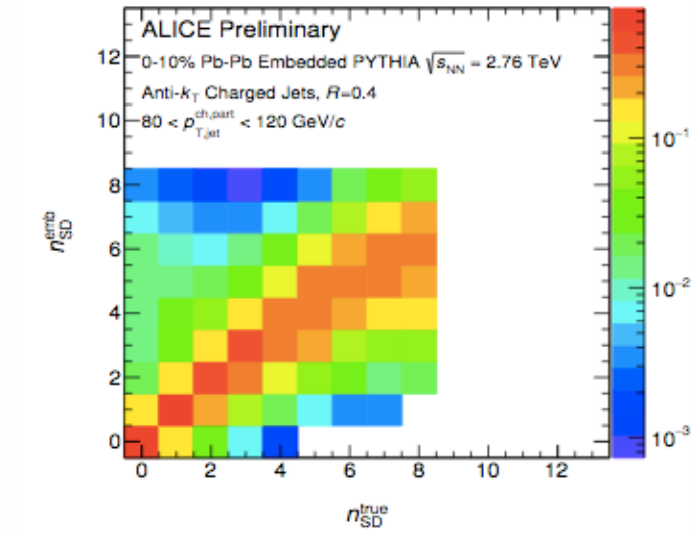
# Fake splittings



- ❖ Uncorrelated background **adds splittings at low  $z_g$ .**



- ❖ Fake splittings **appear at large  $R_g$**  due to the background.



- ❖  $n_{SD}$  appears relatively robust to the presence of background.

# Fundamental question in the physics of heavy ion collisions:

How do collective phenomena and macroscopic properties of matter arise from the elementary interactions of a non-abelian quantum field theory?

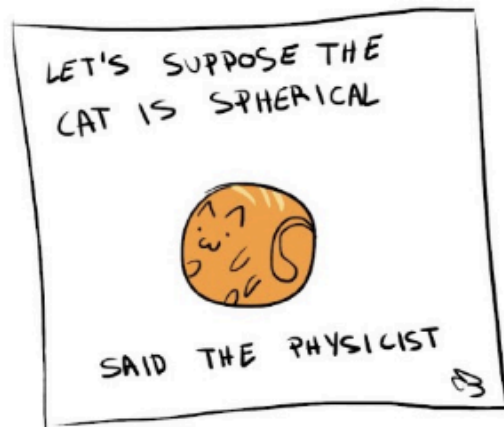
Opportunities	Tools	Status
Constraining equilibrium properties of QCD matter (eos, $\eta/s$ , $\xi$ , $\tau_\pi$ ...)	Flow and fluctuation measurements in AA	advanced
Measuring medium properties with hard auto-generated probes ( $\hat{q}$ , $\hat{e}$ , $T$ ), ...	Quarkonia, $R_{AA}$ 's, photons	in progress
Accessing microscopic structure of QCD matter in AA	Jet substructure, heavy flavor transport	in reach
Controlling initial conditions	pA (light AA) runs, npdf global fits, small-x	in reach
Testing hydrodynamization and thermalization	Combined jet and flow analyses	strategy t.b.d.
Understanding “heavy-ion like behavior” in small systems (pp, pA)	Flow, hadrochemistry, jets	recent surprises

***Slide stolen from Urs Wiedemann, Workshop on the physics of HL-LHC***



## (semi)-ANALYTIC

- Gives insight into what physics is relevant where (energy loss, decoherence, etc.)
- Can inspire what to measure
- Cannot capture all dimensions of full experimental analysis

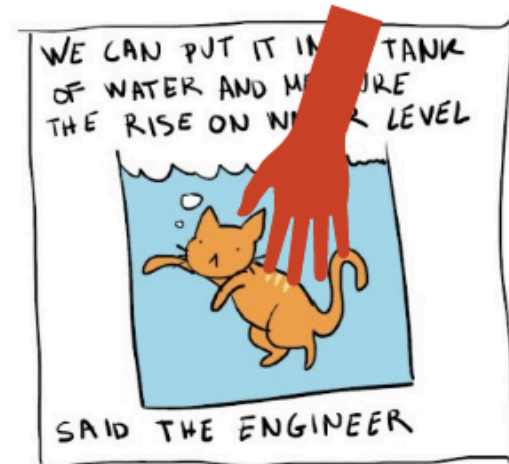


HOW TO CALCULATE THE  
VOLUME OF A CAT ?

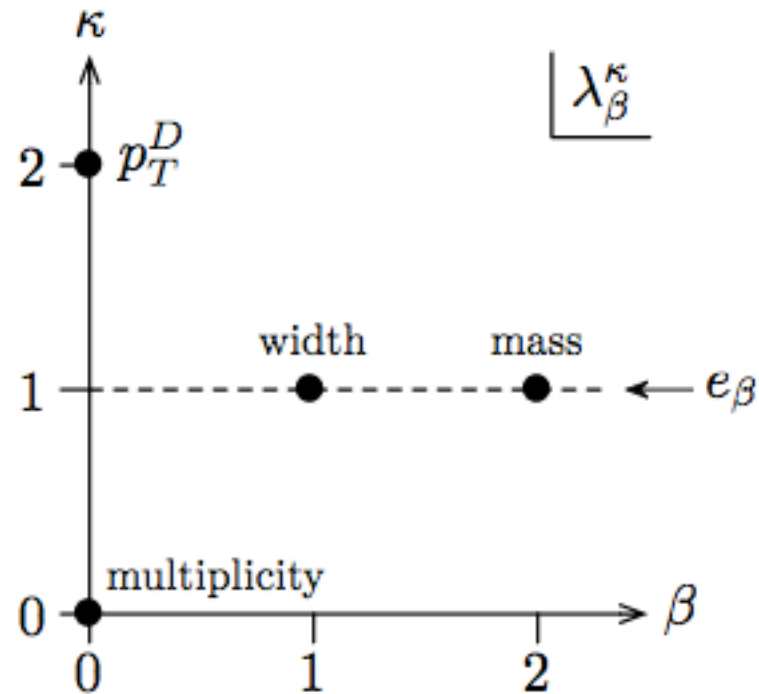
*[this morning's newsletter]*

## Monte Carlo Event Generator

- Gives ultimate realism (accuracy depends on what's inside)
- Can in principle include full medium embedding & subtraction (but that's often work in progress)
- Risks looking like a black box



# Jet shapes: generalized angularities



$$\lambda_\beta^\kappa = \sum_{i \in \text{jet}} z_i^\kappa \left( \frac{R_i}{R_0} \right)^\beta$$

*Diagram from Thaler et al*

**Exploring systematically the phase space of jet shapes**

# Plethora of techniques

