

Calculation of Independent and Cumulative Fission Product Yields
and Fission Spectrum with the Statistical Decay Theory

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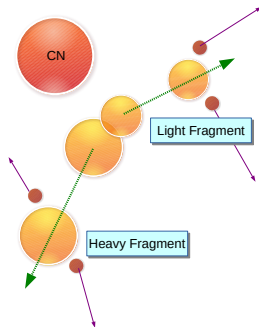
²International Atomic Energy Agency

CSEWG

Brookhaven National Laboratory, 11/5 – 7, 2018

HF³D: Hauser-Feshbach Fission Fragment Decay

Fully Deterministic Approach to Fission Yield and Prompt Neutrons



HF³D Model Inputs

- primary fission fragments $Y(Z, A, TKE)$
- R_T (energy sharing) and f (spin dist.) parameters

We integrate Hauser-Feshbach outputs over

- initial population distribution $P_0(J, \Pi, E_x)$ for
- spin, parity, and fragment excitation energy

Prompt fission neutron spectrum

- convert CMS neutron spectrum into LAB
- **consistent χ calculation with FPY**

FF Initial Configuration for $n_{\text{th}} + {}^{235}\text{U}$

Spin and parity distribution

$R(J, \pi)$ from level density J distribution,
with scaled $\sigma(U)$

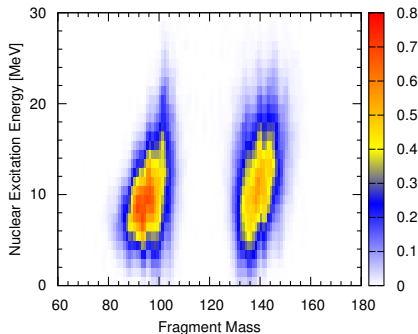
$$R(J, \pi) = \frac{J + 1/2}{2(f\sigma)^2} \exp \left\{ -\frac{(J + 1/2)^2}{2(f\sigma)^2} \right\}$$

Excitation energy distribution

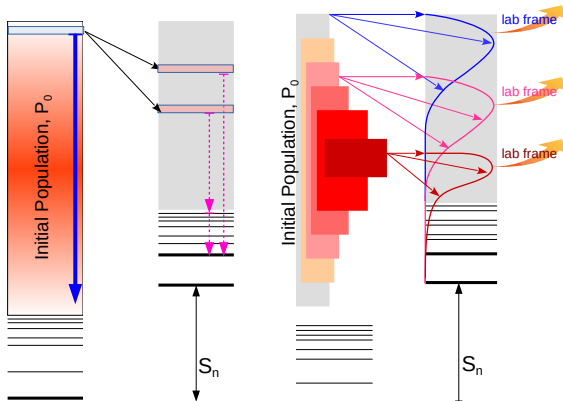
Anisothermal parameter R_T

$$R_T = \frac{T_l}{T_h} = \sqrt{\frac{U_l a_h(U_h)}{U_h a_l(U_l)}}$$

$R(J, \pi)$ and R_T determine $\bar{\nu}$ and $\nu(A)$



Deterministic Statistical Decay of CN in HF³D



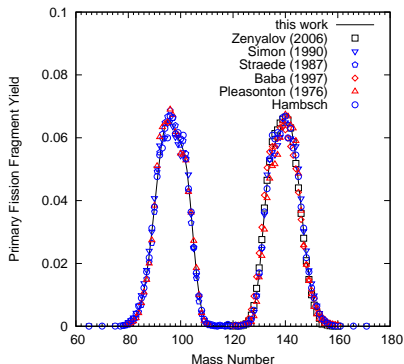
FPY case

χ case

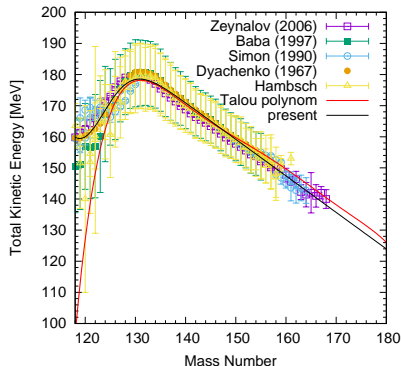
- fission fragment excitation energy discretized, $E_x(i)$
- calculate kinetic energy E_k of the fragment at each $E_x(i)$
- convert neutron energy from CMS into LAB using Feather's technique

Model Parameter Inputs

primary fission fragment, $Y(A)$

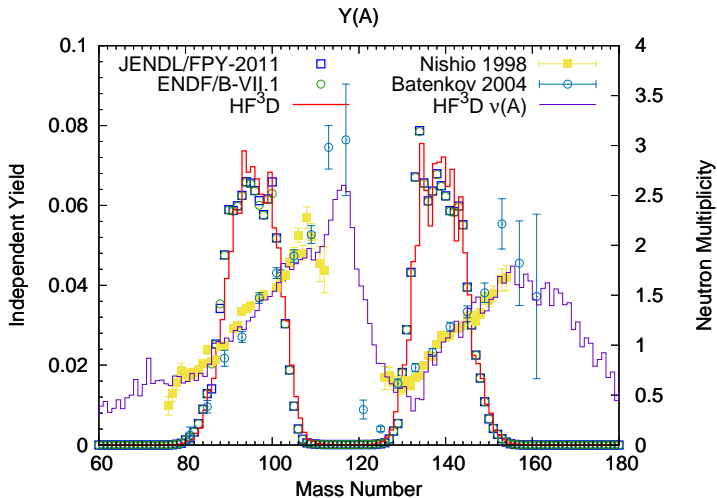


TKE(A)



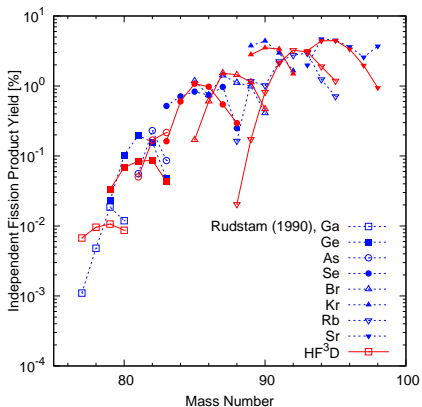
- Z-distribution by Wahl's Z_p model
- $Y(Z, A)$ and $TKE(Z, A)$ are energy-dependent up to 1st-chance fission

Independent Mass Yield for $n_{th} + {}^{235}\text{U}$

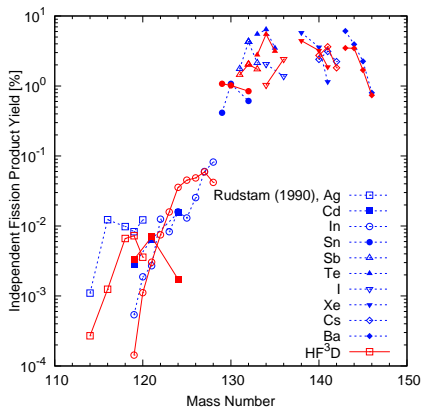


Some Selected Independent FPYs for $n_{th} + {}^{235}\text{U}$

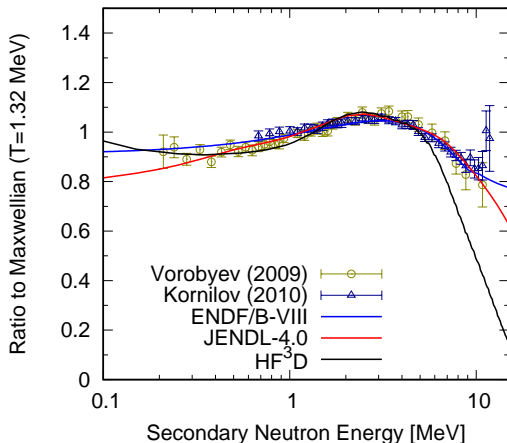
Light FPs



Heavy FPs

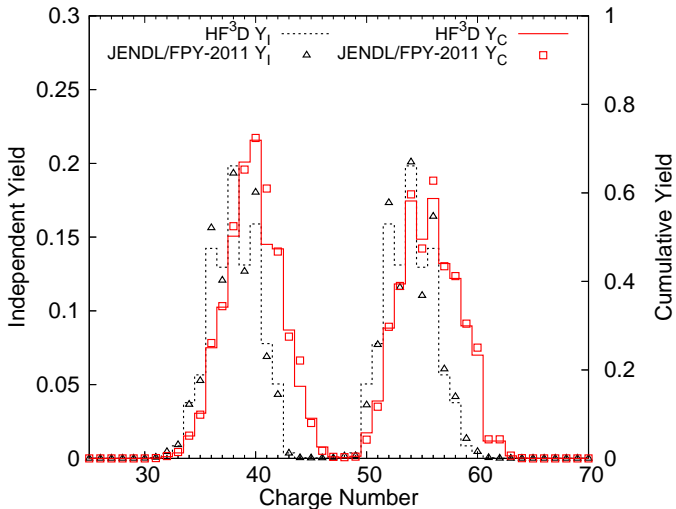


Prompt Fission Neutron Spectrum for $n_{th} + {}^{235}\text{U}$



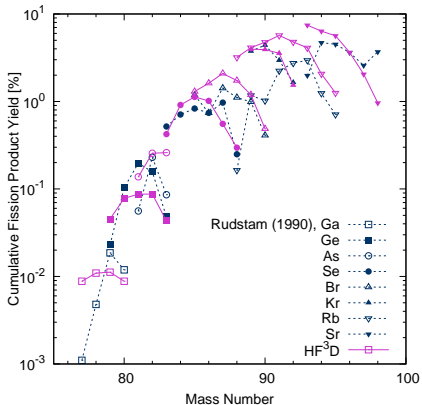
- Shape below 1 MeV different from Madland-Nix model
- HF³D result drops quickly above 5 MeV
 - already seen in our past Monte Carlo works
Becker, PRC **87**, 014617 (2013)
Kawano, NPA **913**, 51 (2013)

Independent/Cumulative FPY Charge Distributions

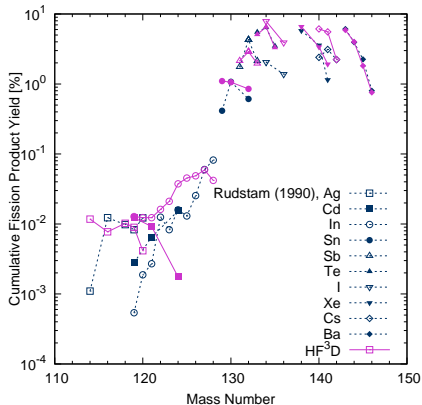


Some Selected Cumulative FPYs

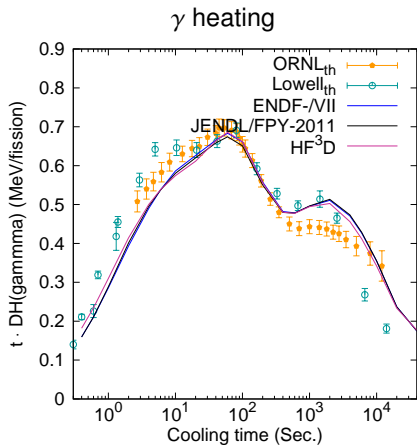
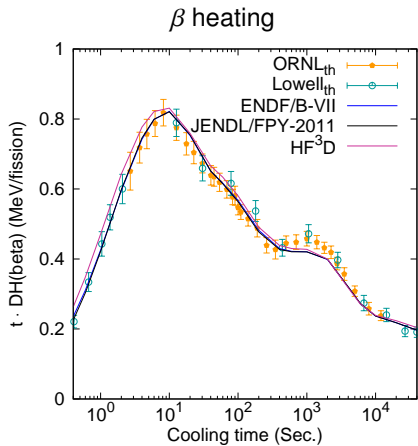
Light FPs



Heavy FPs

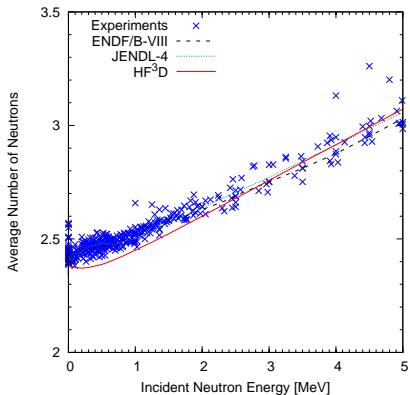


Calculated Decay Heat

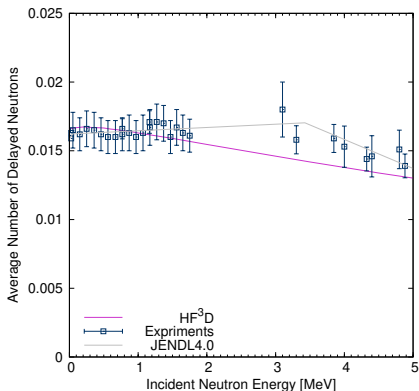


Prompt and Delayed Neutron Multiplicities

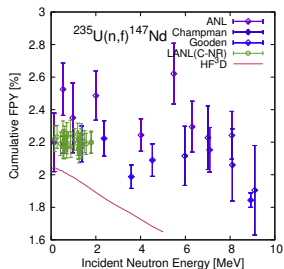
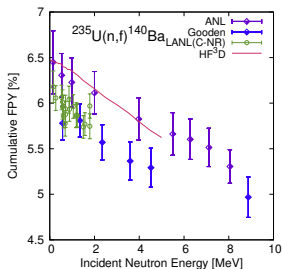
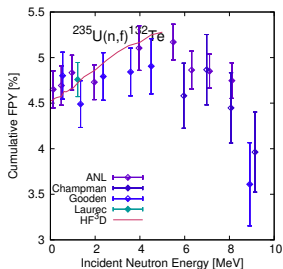
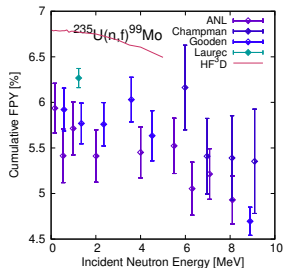
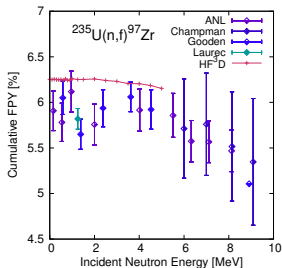
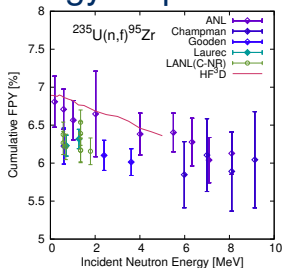
prompt neutron



β -delayed neutron

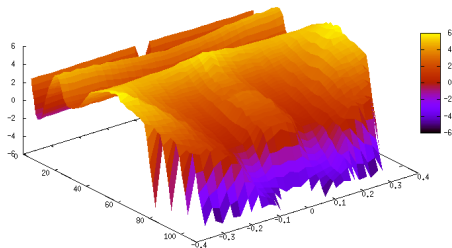


Energy-Dependent Cumulative FPYs

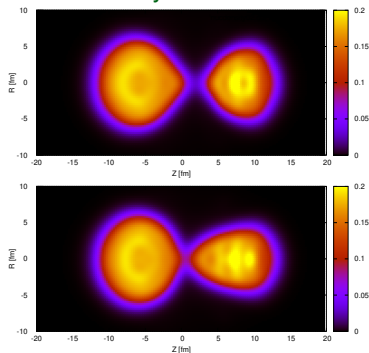


Micro/Macro Approach to Primary FF Yield

potential energy surface of ^{236}U



density distribution



These data will be produced by the FIRE collaboration, and will be employed as the energy-dependent primary fission fragment distribution

Toward New FPY Data Library, Experimental Data

Construction of Experimental Database

- Review some personal FPY databases (England, Mills, Katakura)
- Include recent FPY data, which were not given in these databases
- Prepare **a common experimental FPY database**
- Also compile other data, such as TKE, mass yield, etc, for parameter tuning

International Cooperation

- Workshop on Fission Product Yield Experimental Data
 - Los Alamos, NM, Aug. 20 – 23 (2018)
 - LANL (chair), IAEA (co-chair), BNL, JAEA, and KAERI
- IAEA Consultants' Meeting on Fission Product Yield Experimental Database
 - tentative date/place May 2018 in Tokyo
- IAEA Fission Product Yield CRP

Toward New FPY Data Library, Model and Evaluation

Application of the Hauser-Feshbach theory to the fission fragment decay process

- The HF³D model produces independent fission product yields as well as prompt fission neutron spectrum in a consistent manner
- Capable to produce energy-dependent FPYs
- Current model is limited to $n+^{235}\text{U}$ up to the second chance fission

S. Okumura et al. *J. Nucl. Sci. Tech.* **55**, 1009 (2018)

Extension and Optimization

- Prepare model parameter inputs for other fissioning systems (partly done by the CGMF team at LANL)
- Include multi-chance fission
- Theoretical prediction for primary fission fragment yields
- Large scale parameter optimization to produce the final evaluation