

# Investigation of the linear and mode-coupled flow harmonics in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV

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U.S. DEPARTMENT OF  
**ENERGY**

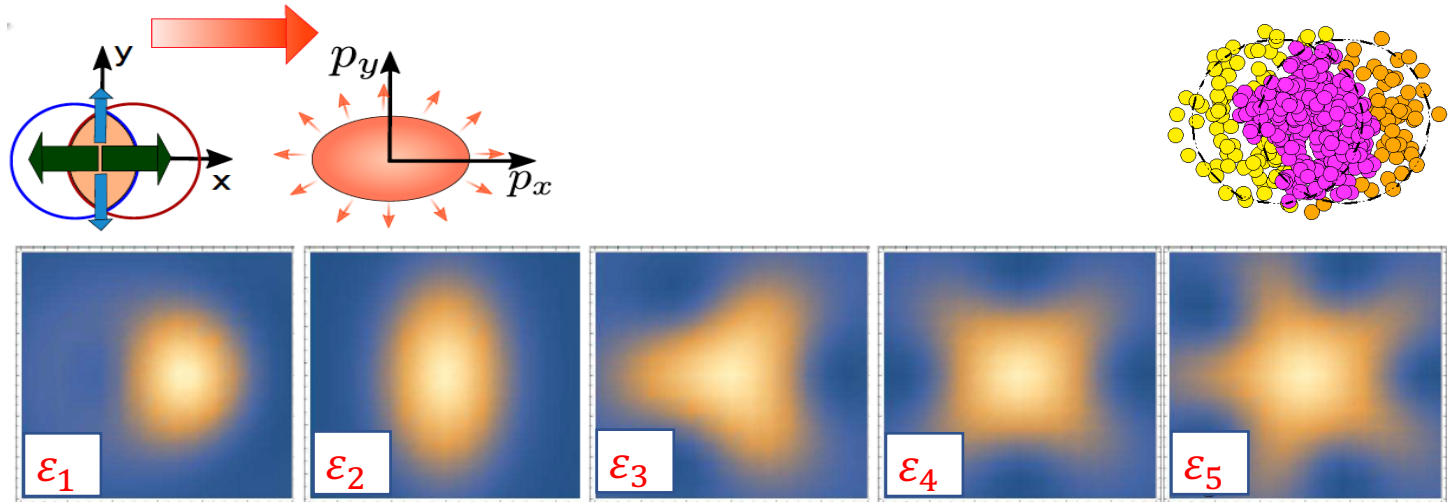
Office of  
Science

This work is supported by the grant from doe office of science

# Introduction

## Anisotropic flow

Asymmetry in initial geometry  $\rightarrow$  Final-state momentum anisotropy

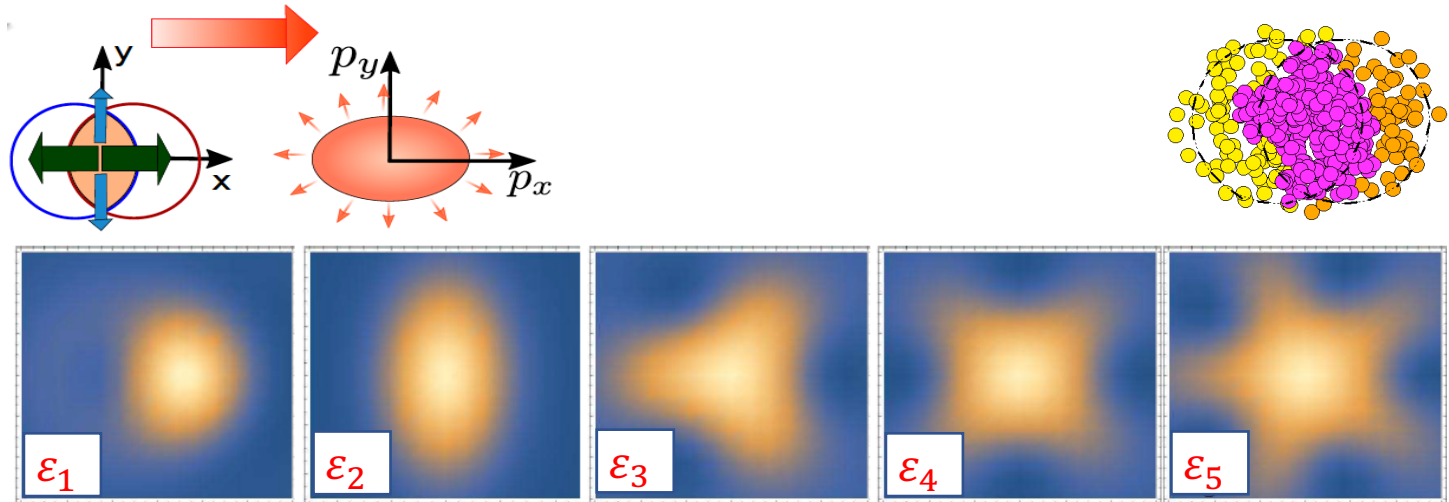


What are the respective roles of  $\epsilon_n$  and its fluctuations, flow correlations and  $\eta/s(T)$  on the  $v_n$ ?

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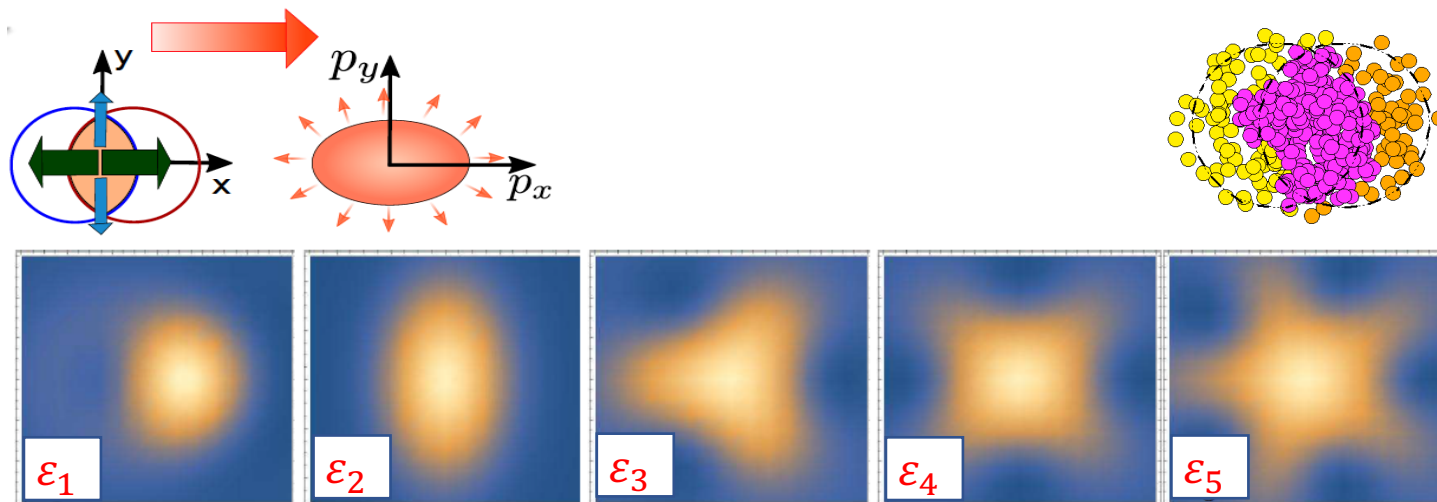
Higher-order flow harmonics ( $v_{n>3}$ ) have multiple contributions:

- ✓ Linear response  $\propto \epsilon_{n>3}$
- ✓ Mode-coupled response  $\propto \epsilon_2$  and/or  $\epsilon_3$  and the Event Plane (EP) correlations

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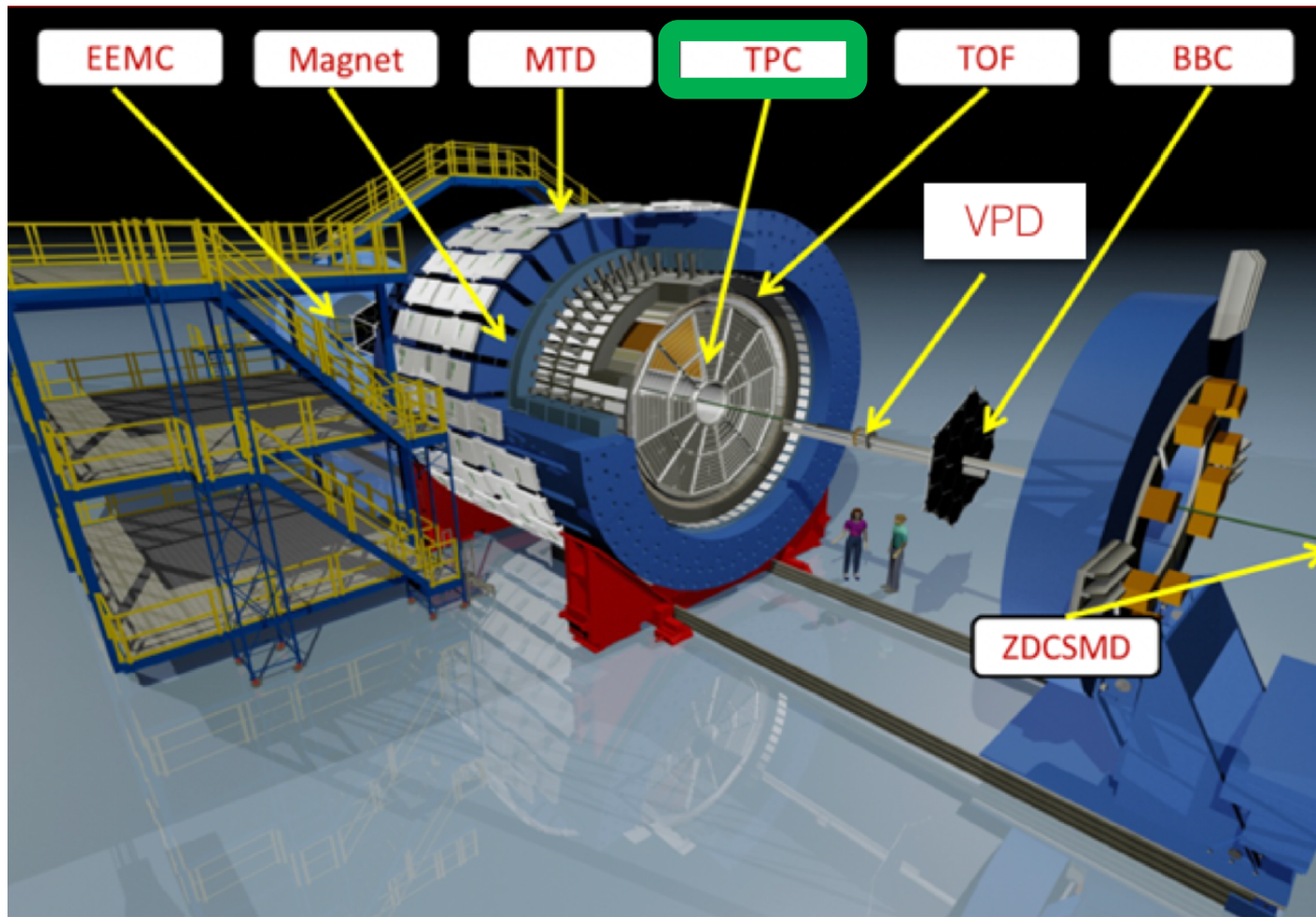
- ✓ Linear response  $\propto \epsilon_{n>3}$
- ✓ Mode-coupled response  $\propto \epsilon_2$  and/or  $\epsilon_3$  and the Event Plane (EP) correlations

The focus of this work:

- ✓ Separate and study the linear and mode-coupled contributions
- ✓ Study the nature of the eccentricity coupling and the EP correlations

# Introduction

## The Solenoidal Tracker At RHIC



### ➤ Time Projection Chamber

Tracking of charged particles with:

- ✓ Full azimuthal coverage
- ✓  $|\eta| < 1$  coverage

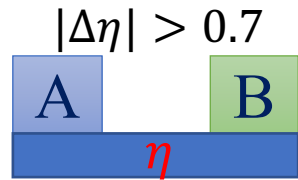
# Analysis Method

The two- and three-particle correlations:

$$C_{k,2n} = \langle \langle \cos((2+n)\varphi_1^A - 2\varphi_2^B - n\varphi_3^B) \rangle \rangle$$

$$n = 2, 3 \quad k = n + 2$$

$$v_n^{Inclusive} = \langle \langle \cos(n\varphi_1^A - n\varphi_2^B) \rangle \rangle^{1/2}$$



The four-particle correlations:

$$\begin{aligned} \langle v_2^4 \rangle &= \langle \langle \cos(2\varphi_1 + 2\varphi_2 - 2\varphi_3 - 2\varphi_4) \rangle \rangle - 2 \langle \langle \cos(2\varphi_1 - 2\varphi_2) \rangle \rangle^2 + 2 \langle \langle \cos(2\varphi_1^A - 2\varphi_2^B) \rangle \rangle^2 \\ \langle v_2^2 v_3^2 \rangle &= \langle \langle \cos(3\varphi_1 + 2\varphi_2 - 3\varphi_3 - 2\varphi_4) \rangle \rangle - \langle \langle \cos(2\varphi_1 - 2\varphi_2) \rangle \rangle \langle \langle \cos(4\varphi_1 - 3\varphi_2) \rangle \rangle \\ &\quad + \langle \langle \cos(2\varphi_1^A - 2\varphi_2^B) \rangle \rangle \langle \langle \cos(3\varphi_1^A - 3\varphi_2^B) \rangle \rangle \end{aligned}$$

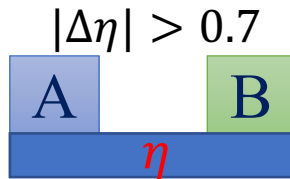
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Assume the orthogonality between  
linear and non-linear contributions

$$V_k = V_k^{Linear} + V_k^{Non-Linear}$$

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PLB 773 68 (2017)

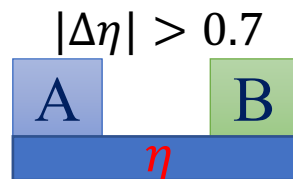
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➤  $v_k^{Non-Linear}$  carry information about:

✓ Viscous effects, EP angular correlations and Eccentricity coupling

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$$\begin{aligned} v_k^{Non-Linear} &= \frac{C_{k,2,n}}{\sqrt{\langle v_2^2 v_n^2 \rangle}}, \\ &= \frac{\langle v_k v_2 v_n \cos(k\Psi_k - n\Psi_n - 2\Psi_2) \rangle}{\langle v_2^2 v_n^2 \rangle}, \\ &\sim \langle v_k \cos(k\Psi_k - n\Psi_n - 2\Psi_2) \rangle, \end{aligned}$$

$$v_k^{Linear} = \sqrt{(v_k^{Inclusive})^2 - (v_k^{Non-Linear})^2}$$



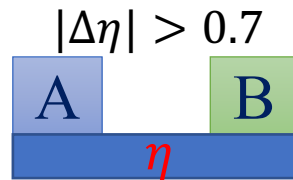
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$$v_k^{Linear} = \sqrt{(v_k^{Inclusive})^2 - (v_k^{Non-Linear})^2}$$

✓ **EP angular correlations**

$$\rho_{k,2n} = \frac{v_k^{Non-Linear}}{v_k^{Inclusive}} = \langle \cos(k\Psi_k - 2\Psi_2 - n\Psi_n) \rangle$$

✓ **Eccentricity coupling**

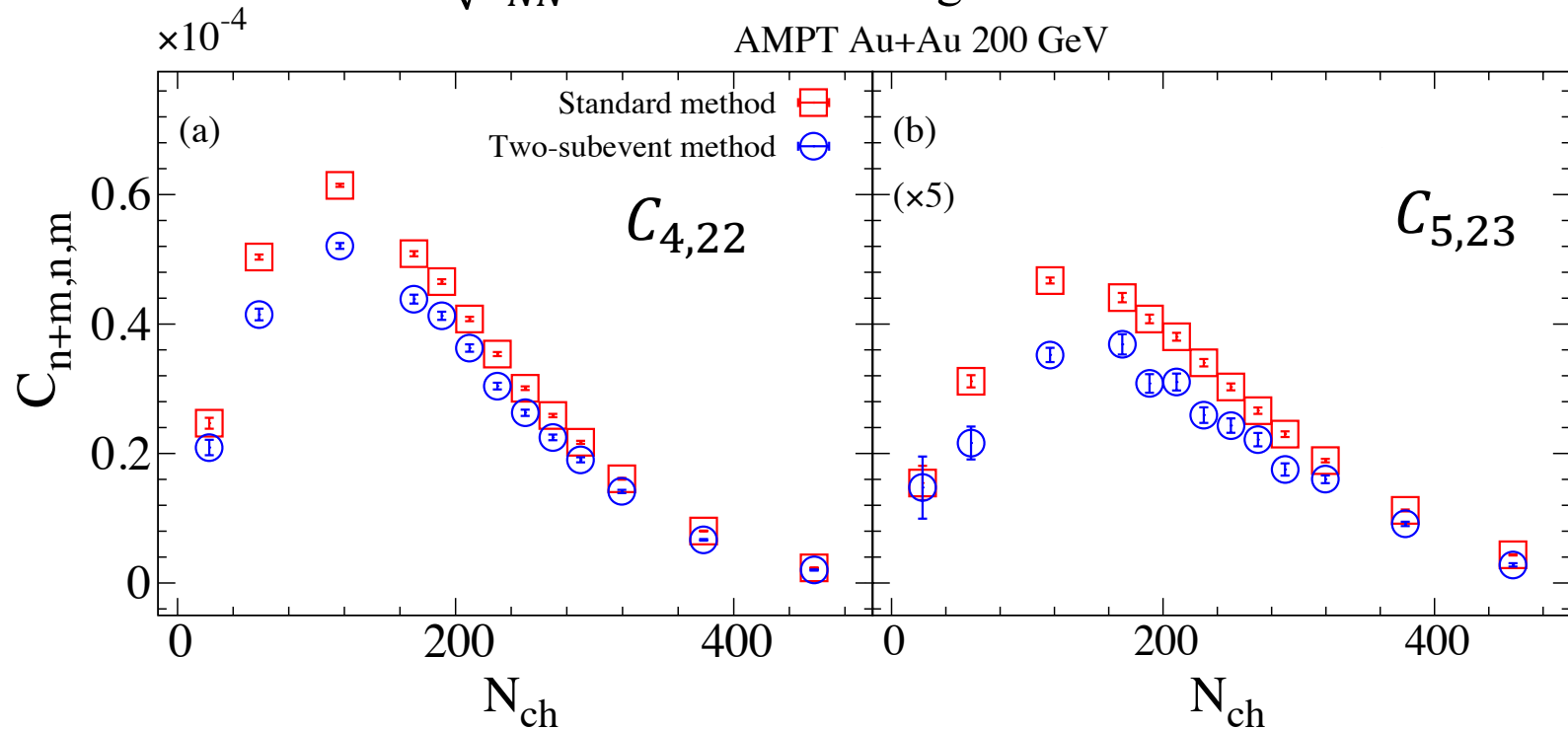
$$\chi_{k,2n} = \frac{v_k^{Non-Linear}}{\sqrt{\langle v_2^2 v_n^2 \rangle}}$$

Weak viscous effect expected

P.Liu, R.Lacey  
PRC 98, 021902 (2018)

# The short-range non-flow contributions in the three-particle correlations

Three-particle correlations,  $C_{4,22}$  and  $C_{5,23}$  for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV using the AMPT model



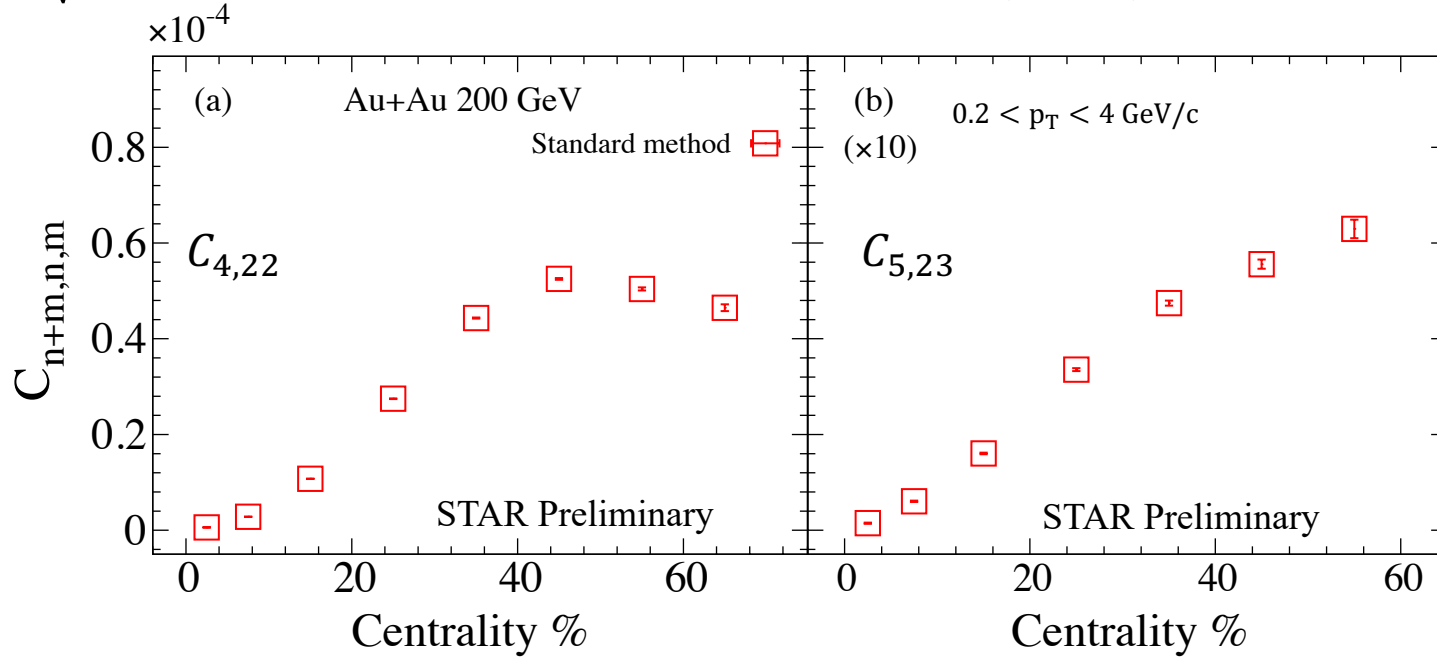
- Two-subevents reduce the short-range non-flow effects in the three-particle correlation measurements

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# Results

Three-particle correlations,  $C_{4,22}$  and  $C_{5,23}$  for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV compared with different hydrodynamic simulations.

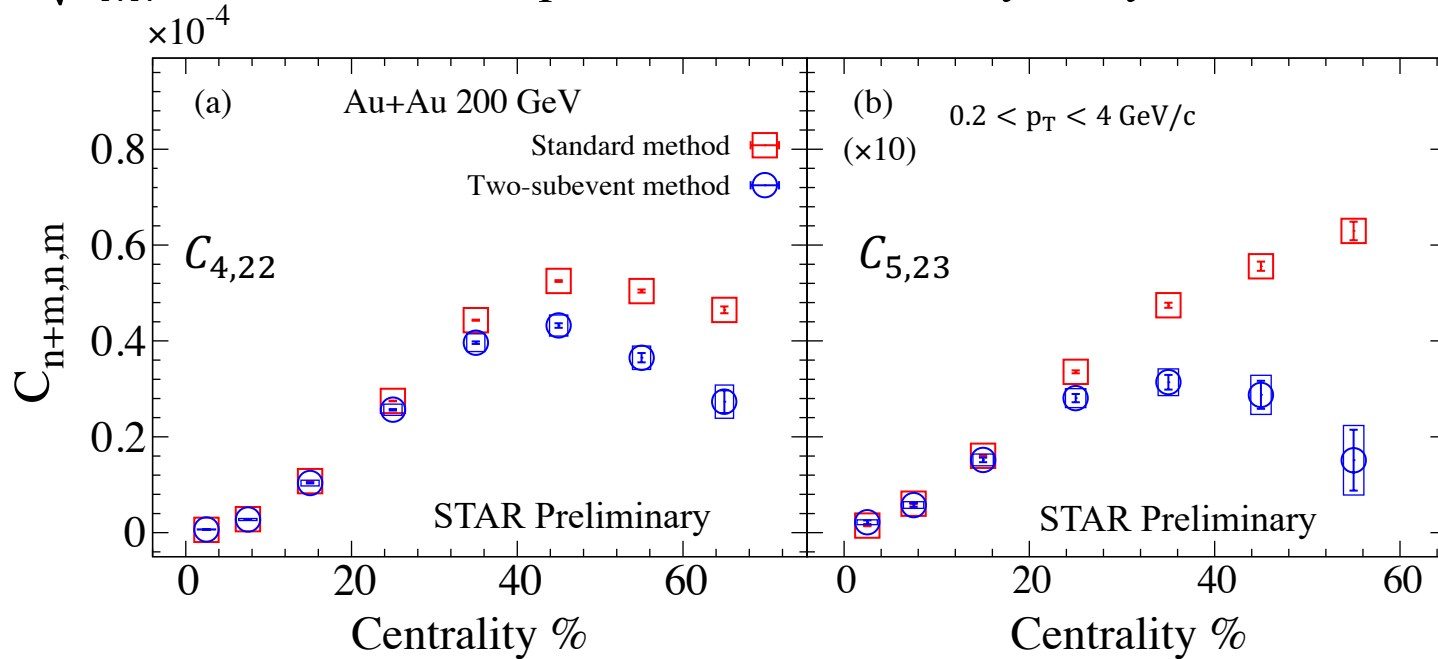


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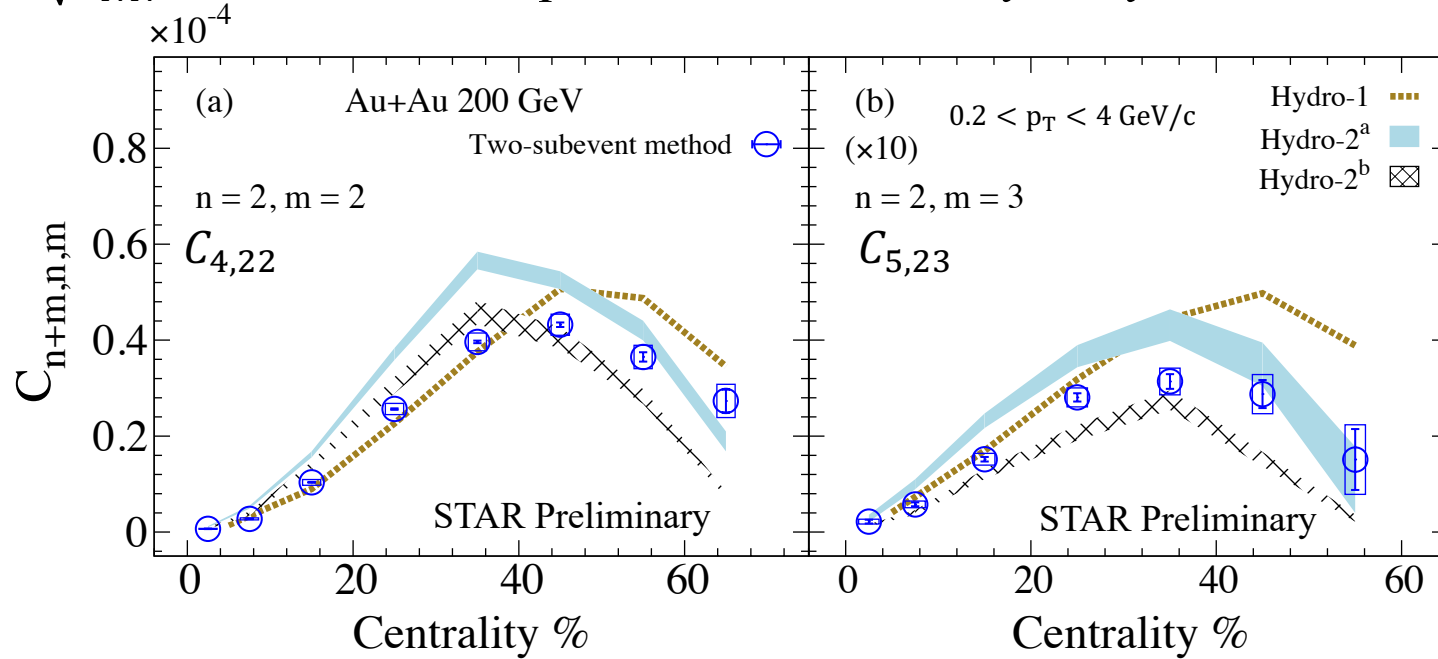
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	Hydro-1	Hydro-2 <sup>a/b</sup>
$\eta/s$	0.05	0.12
Initial conditions	TRENTO Initial conditions	IP-Glasma Initial conditions
Contributions	Hydro + Direct decays	(a) Hydro + Hadronic cascade (b) Hydro only

- (1) P. Alba, et al. PRC 98 , 034909 (2018)
- (2) B.Schenke, C.Shen, and P.TribeDY PRC 99, 044908 (2019)

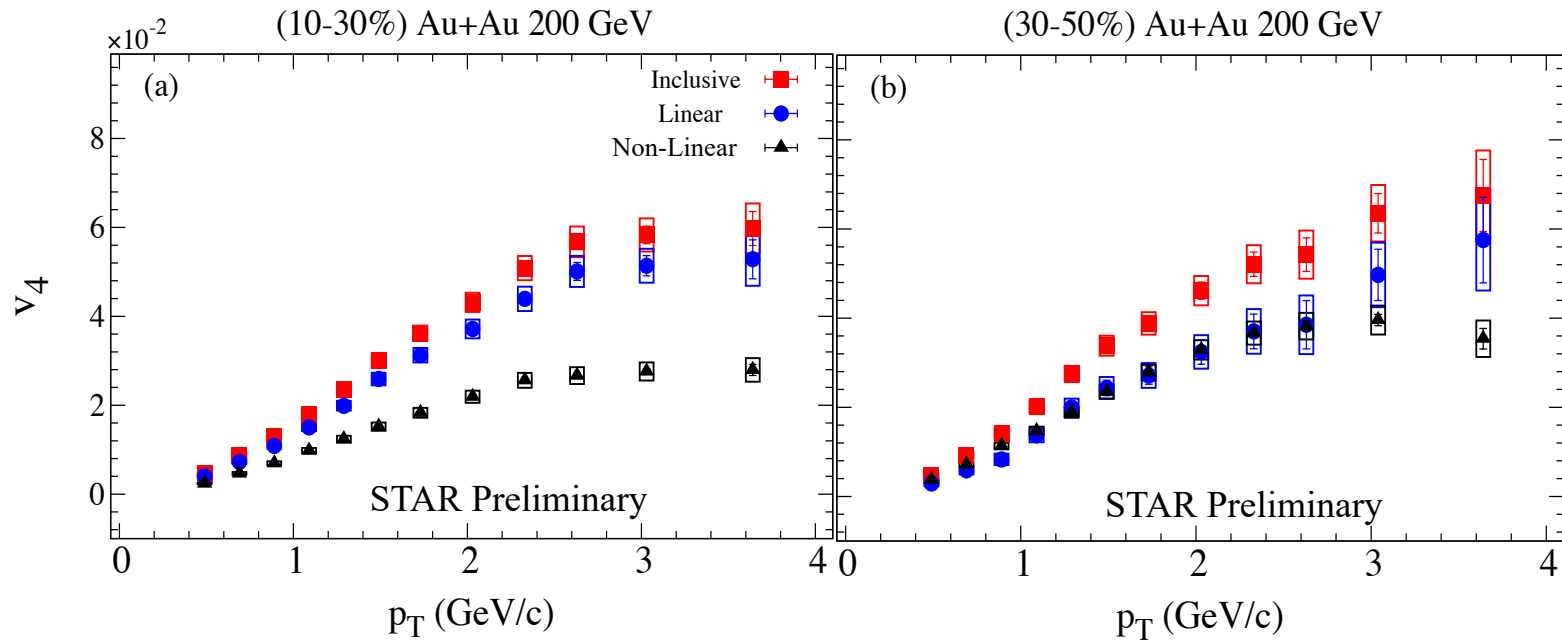
- However both models fit the  $v_n$  they need additional constraints in order to describe the 3-particle correlations

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The  $p_T$ -differential dependence of the inclusive, linear and non-linear  $v_4$  for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV are shown



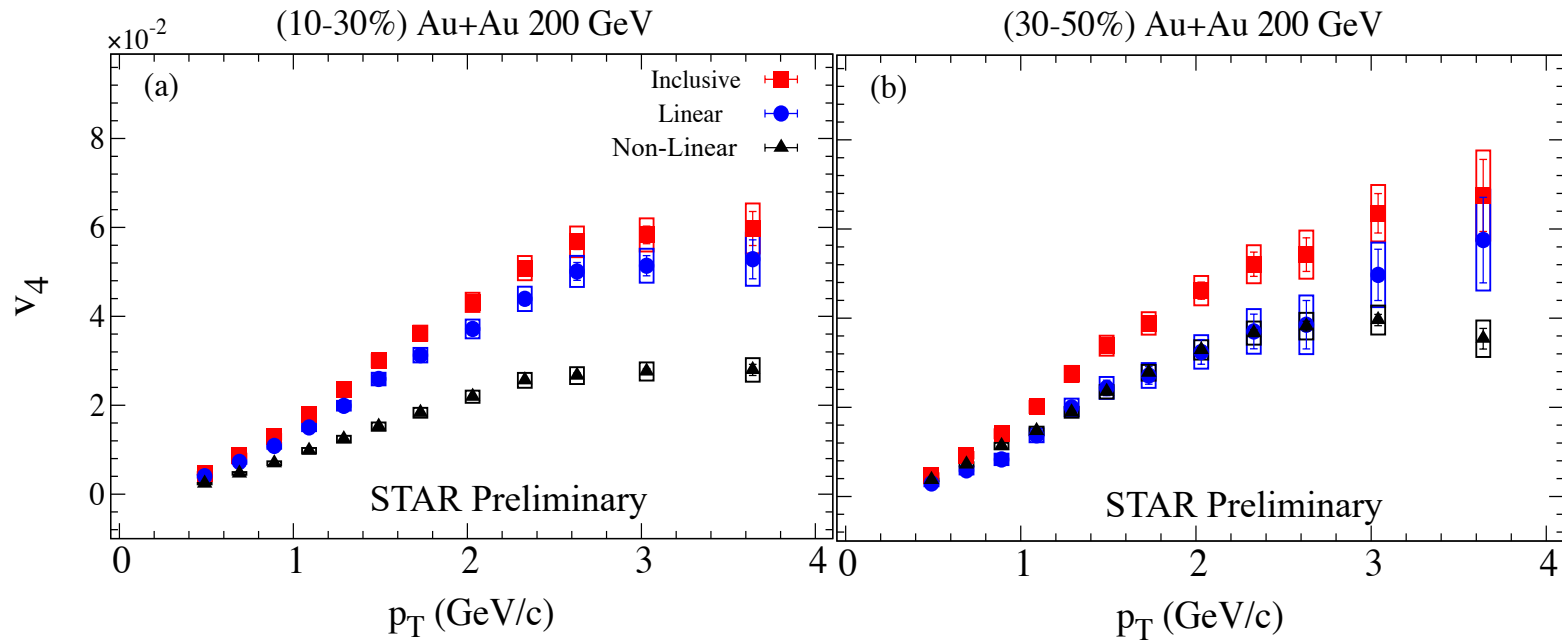
➤ The inclusive, linear and non linear  $v_4$  shows a characteristics  $p_T$  dependence

$$v_4^{Non-Linear} = \frac{C_{4,22}}{\sqrt{\langle v_2^4 \rangle}}$$

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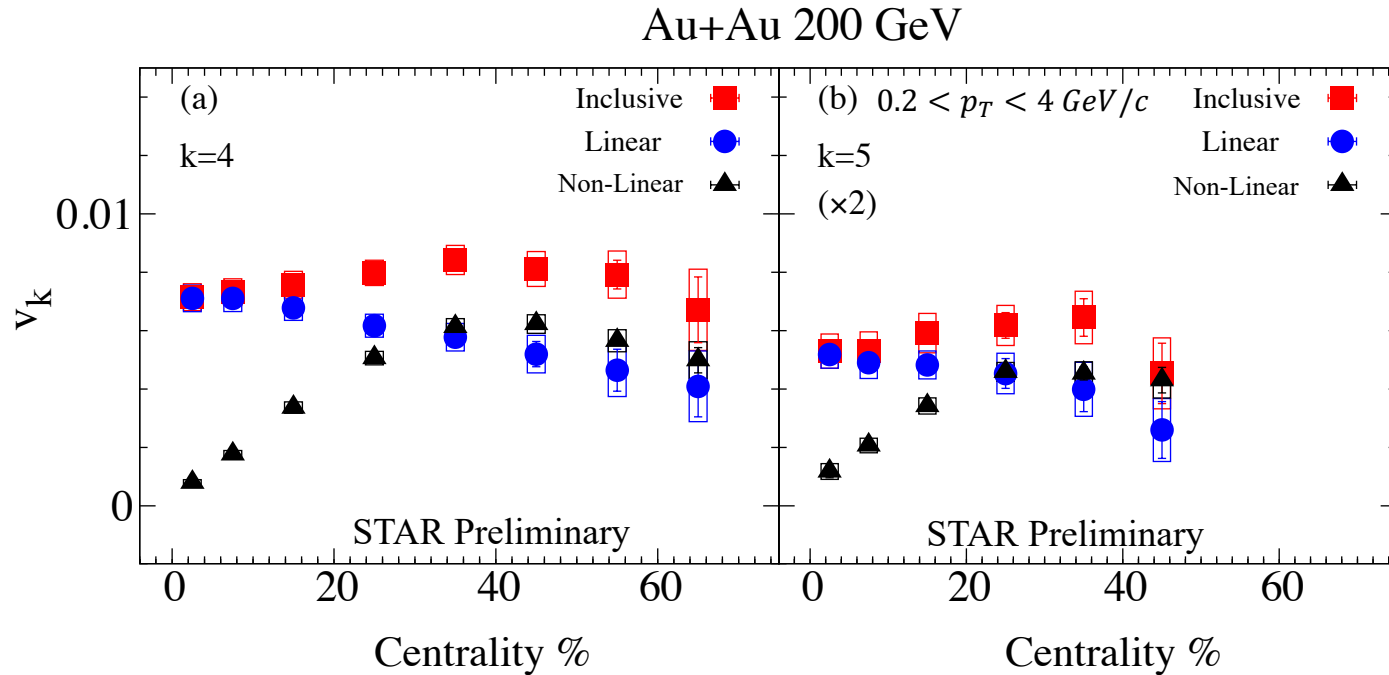
➤ The linear  $v_4$  term dominates in central collisions

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$$v_4^{Linear} = \sqrt{(v_4^{Inclusive})^2 - (v_4^{Non-Linear})^2}$$

# Results

Centrality dependence of the inclusive, linear and non-linear  $v_n$  ( $n=4,5$ ) for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV



➤ The linear  $v_n$  ( $n=4,5$ ) terms dominate in central collisions

$$v_{m+2}^{Non-Linear} = \frac{C_{m+2,2m}}{\sqrt{\langle v_2^2 v_m^2 \rangle}}$$

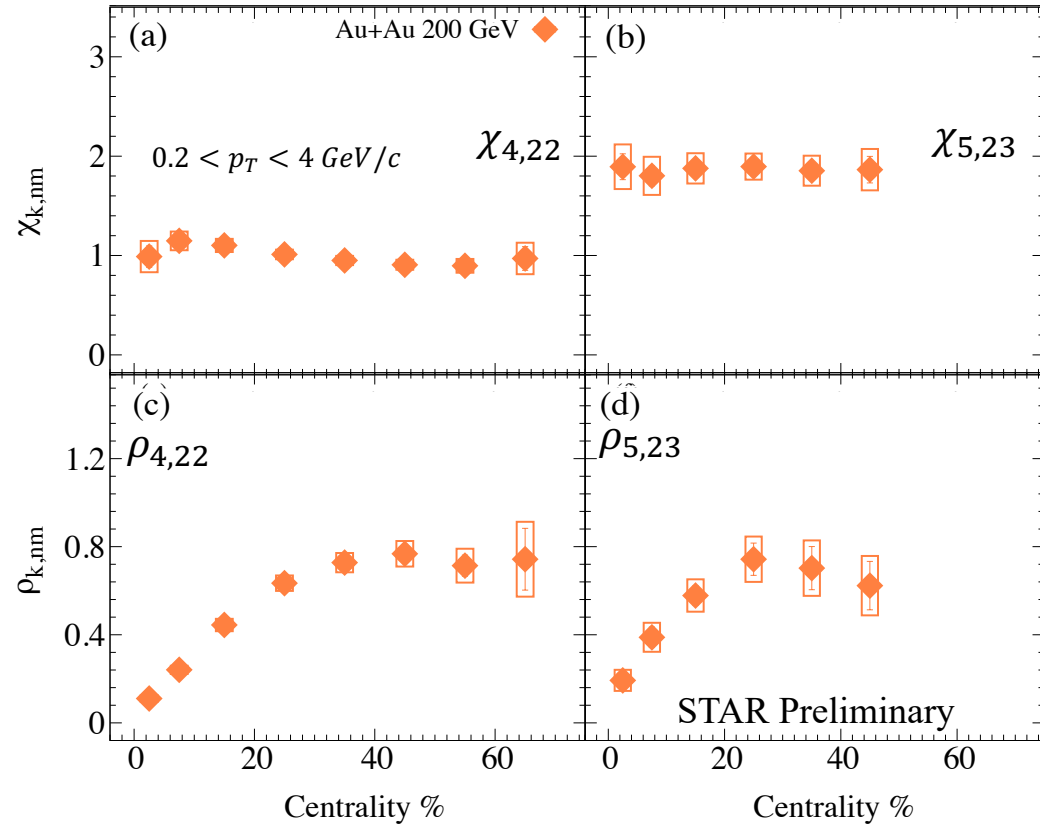
$$v_{m+2}^{Linear} = \sqrt{(v_{m+2}^{Inclusive})^2 - (v_{m+2}^{Non-Linear})^2}$$



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Centrality dependence of the non-linear mode-coupling coefficients,  $\chi_{4,22}$  and  $\chi_{5,23}$  and the EP angular correlations  $\rho_{4,22}$  and  $\rho_{5,23}$  for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV

- $\chi_{k,nm}$  shows a weak centrality dependence (weak viscous effect)
- $\rho_{k,nm}$  shows a strong centrality dependence



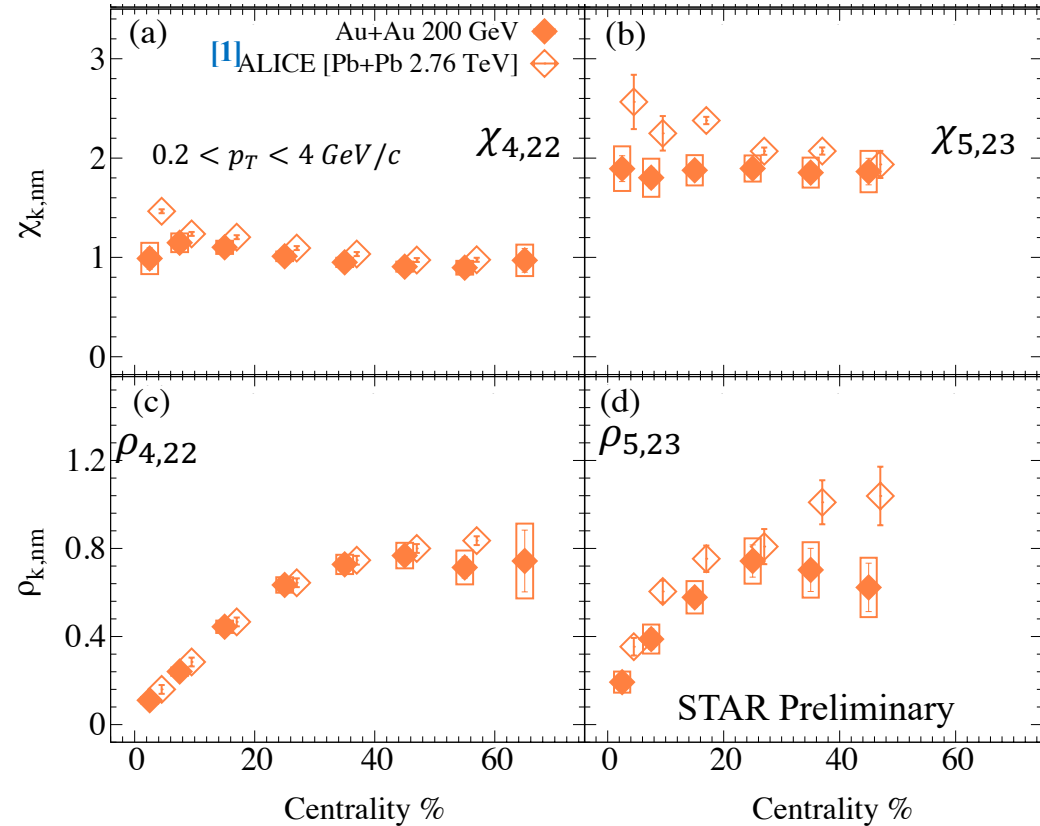
$$\chi_{m+2,2m} = v_{m+2}^{Non-Linear} / \sqrt{\langle v_2^2 v_m^2 \rangle} \quad m = 2,3$$

$$\rho_{m+2,2m} = v_{m+2}^{Non-Linear} / v_{m+2}^{Inclusive}$$

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- $\chi_{k,nm}$  shows a **weak centrality dependence** (weak viscous effect)
- $\rho_{k,nm}$  shows a **strong centrality dependence**
- $\rho_{k,nm}$  and  $\chi_{k,nm}$  show a **weak beam energy dependence**



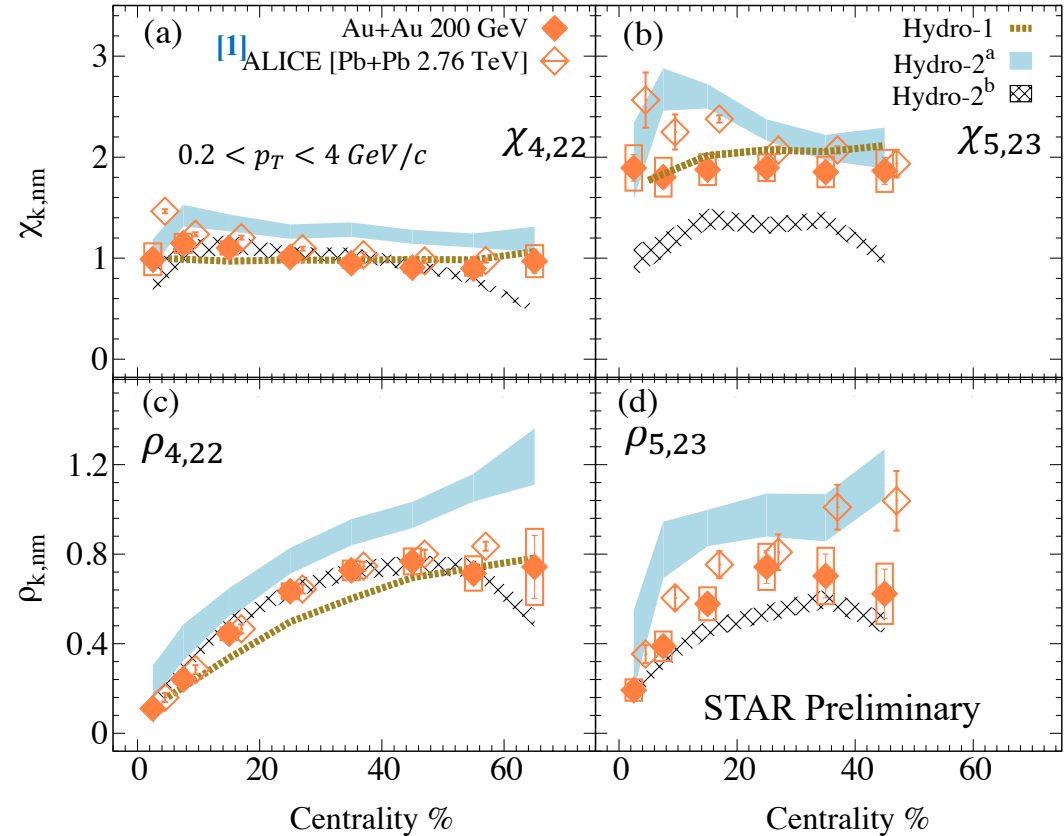
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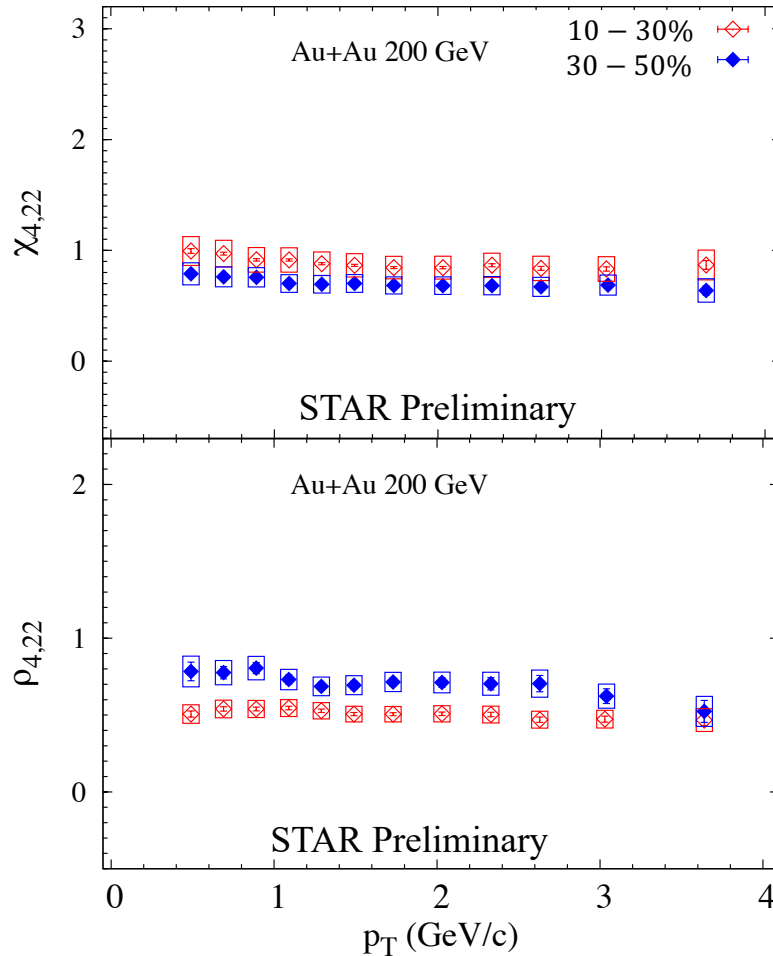


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➤  $\chi_{4,22}$  shows a weak  $p_T$  dependence

➤  $\rho_{4,22}$  shows a weak  $p_T$  dependence

✓ Dynamical final-state effects are significantly less than the initial-state effect?

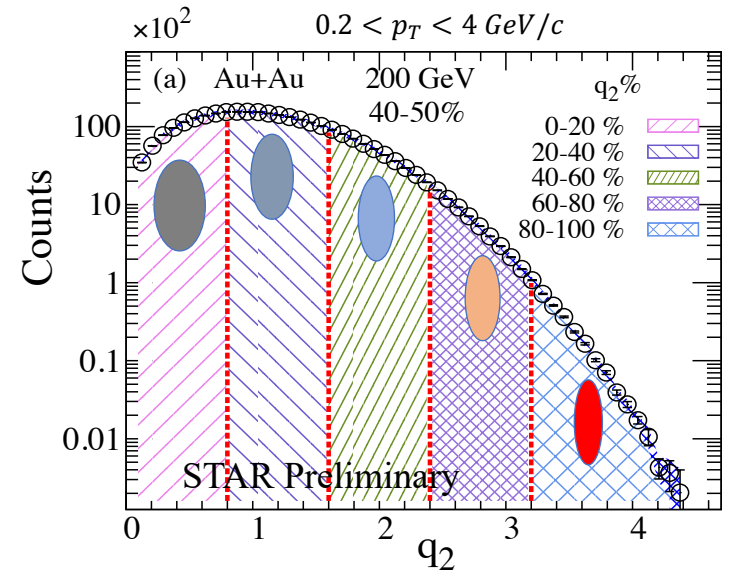
$$\chi_{m+2,2m} = v_{m+2}^{\text{Non-Linear}} / \sqrt{\langle v_2^2 v_m^2 \rangle} \quad m = 2$$

$$\rho_{m+2,2m} = v_{m+2}^{\text{Non-Linear}} / v_{m+2}^{\text{Inclusive}}$$

# The influence of event shape selection

- Events are further subdivided into groups with different  $q_2$  magnitude:

$$Q_{n,x} = \sum_{i=1}^M \cos(n \varphi_i) \quad Q_{n,y} = \sum_{i=1}^M \sin(n \varphi_i)$$
$$|Q_n| = \sqrt{Q_{n,x}^2 + Q_{n,y}^2} \quad q_n = \frac{|Q_n|}{\sqrt{M}}$$

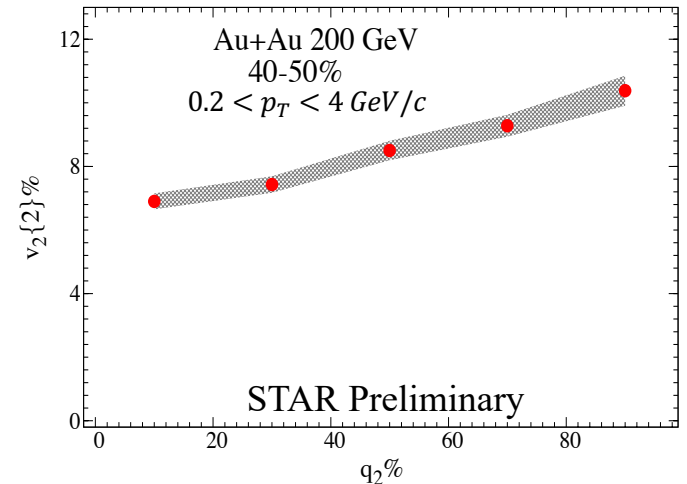
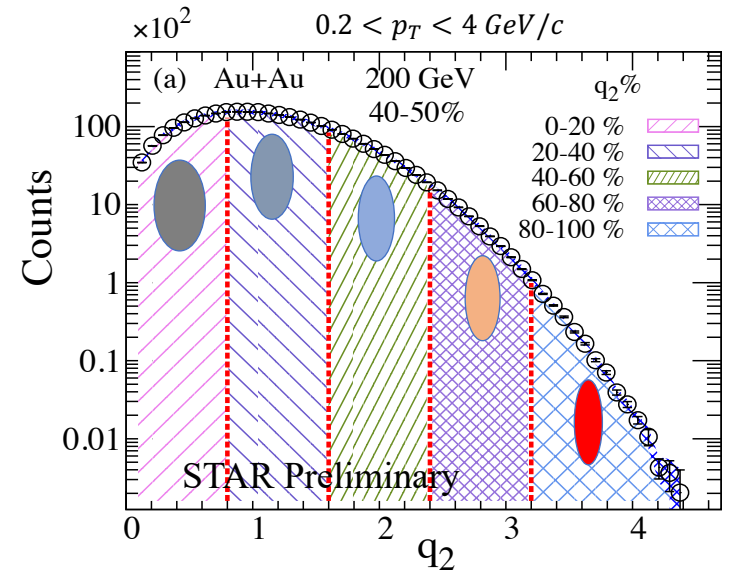


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- $v_2\{2\}$  increases linearly with  $q_2$   
 $q_2$  is good event-shape selector

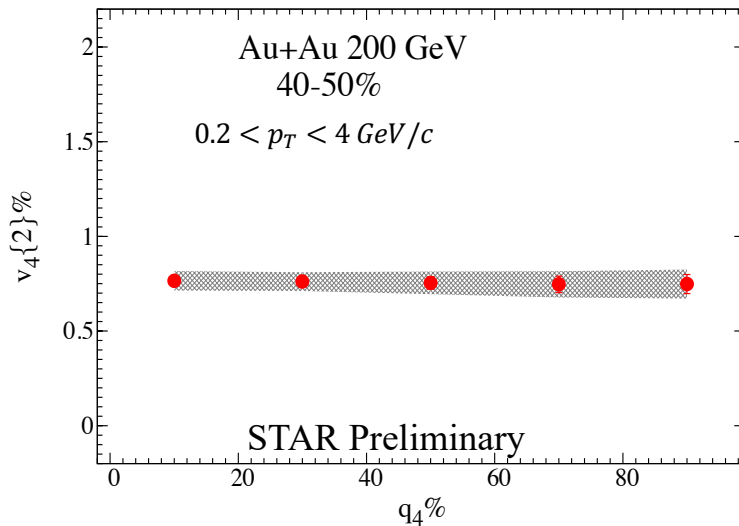
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 PRC 93, 034916 (2016)

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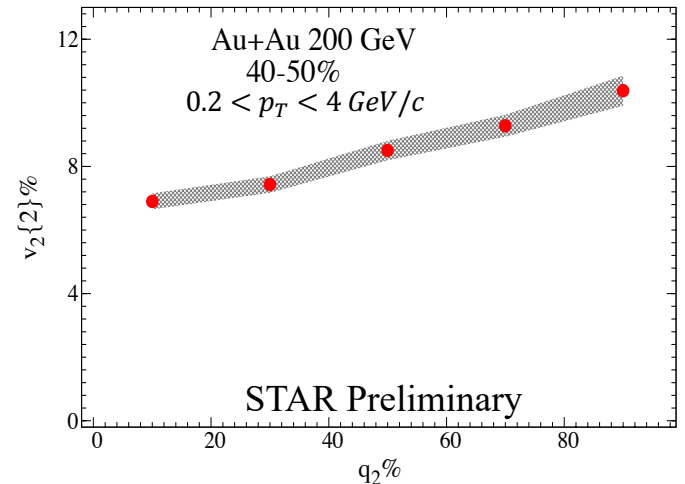
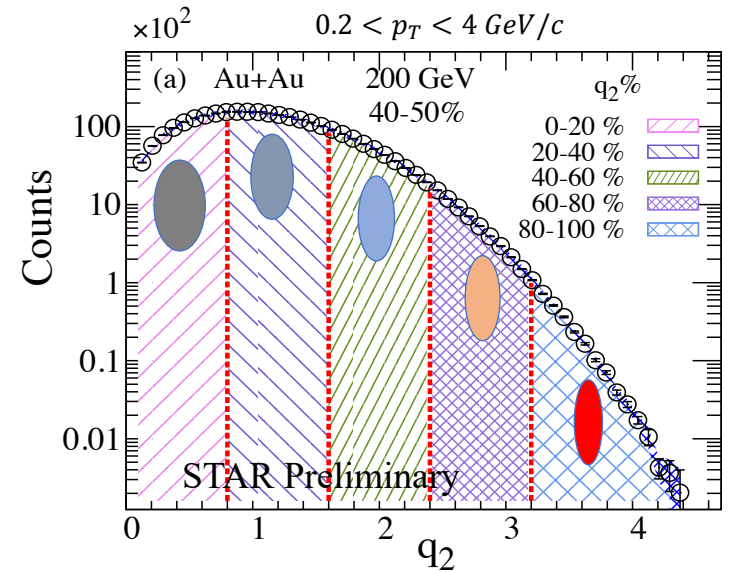
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- $v_4\{2\}$  shows no sensitivity to  $q_4$

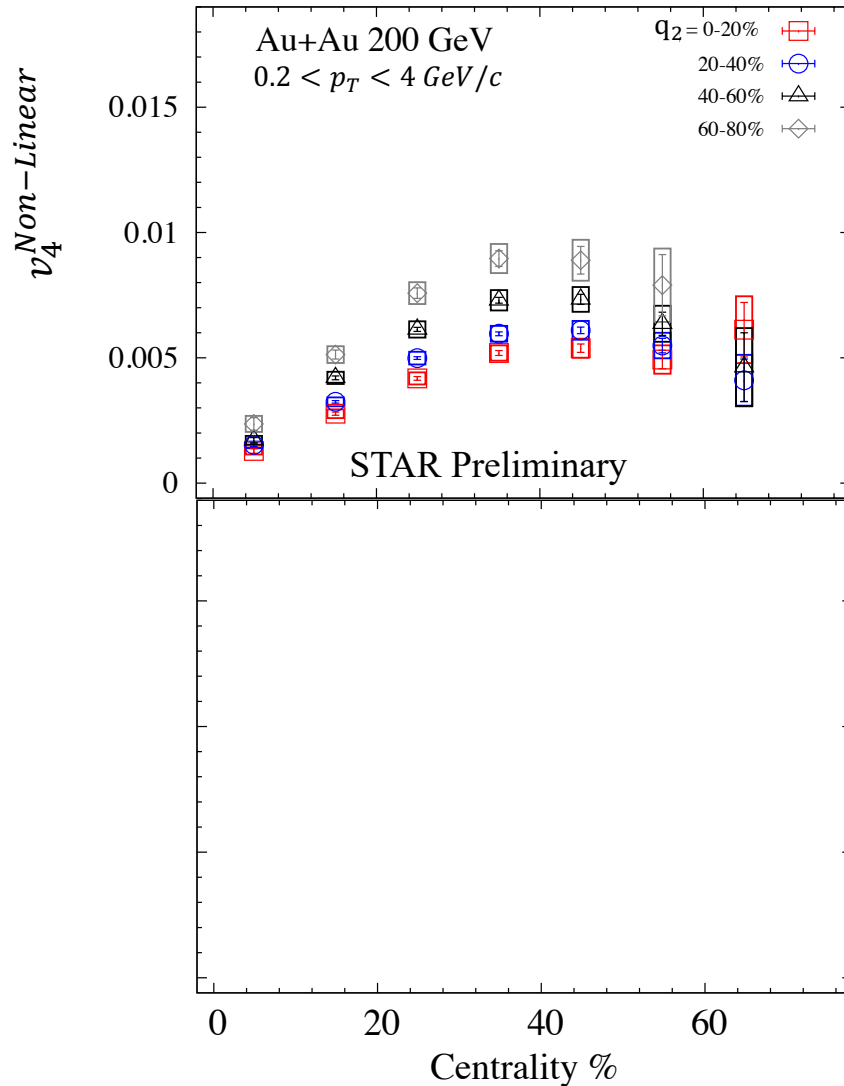


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PRC 93, 034916 (2016)

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Centrality dependence of the linear and non-linear  $v_4$  for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV with different event shape selections ( $q_2$  %)



➤ The non-linear  $v_4$  increases with  $q_2$  selections

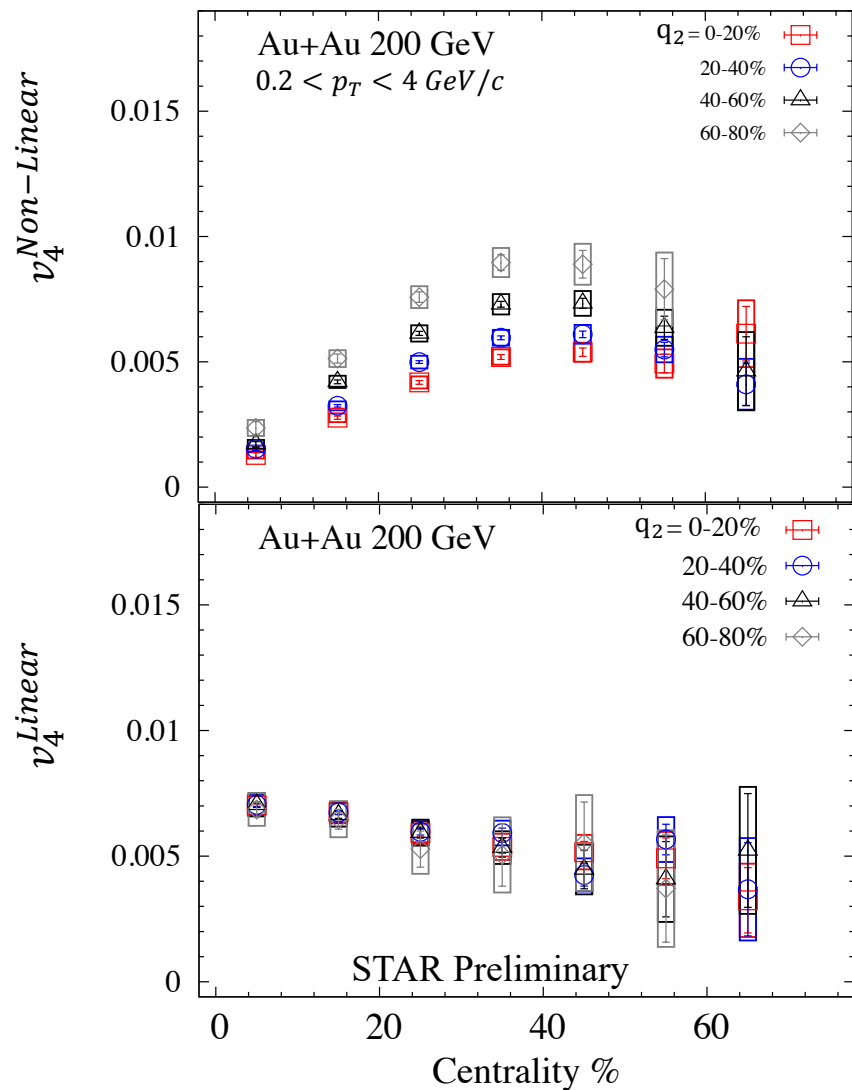
$$v_4^{Non-Linear} = \frac{C_{4,22}}{\sqrt{\langle v_2^4 \rangle}}$$

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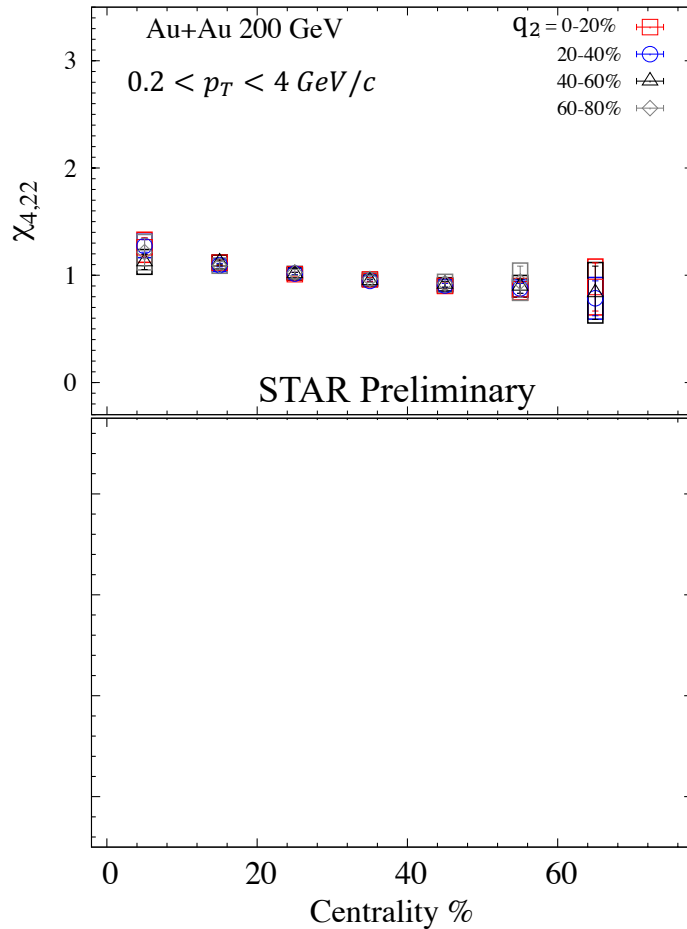
➤ The linear  $v_4$  shows a weak sensitivity to  $q_2$  selections

$$v_4^{Non-Linear} = \frac{C_{4,22}}{\sqrt{\langle v_2^4 \rangle}}$$

$$v_4^{Linear} = \sqrt{(v_4^{Inclusive})^2 - (v_4^{Non-Linear})^2}$$

# Results

Centrality dependence of the  $\rho_{4,22}$  and  $\chi_{4,22}$  for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV with different event shape selections ( $q_2$ )



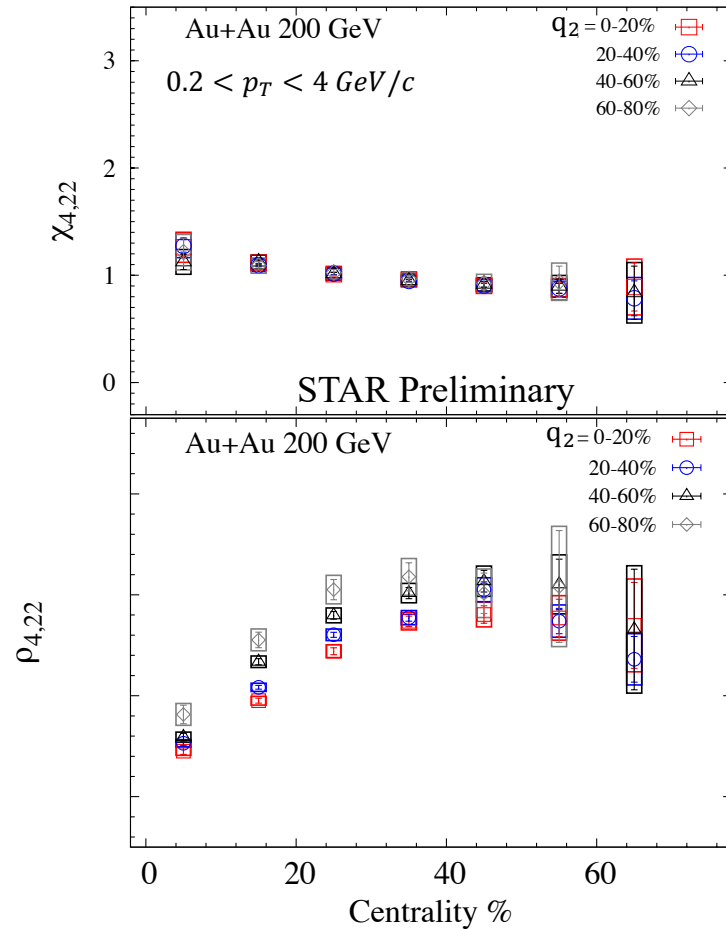
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$$\chi_{m+2,2m} = v_{m+2}^{\text{Non-Linear}} / \sqrt{\langle v_2^2 v_m^2 \rangle} \quad m = 2$$

$$\rho_{m+2,2m} = v_{m+2}^{\text{Non-Linear}} / v_{m+2}^{\text{Inclusive}}$$

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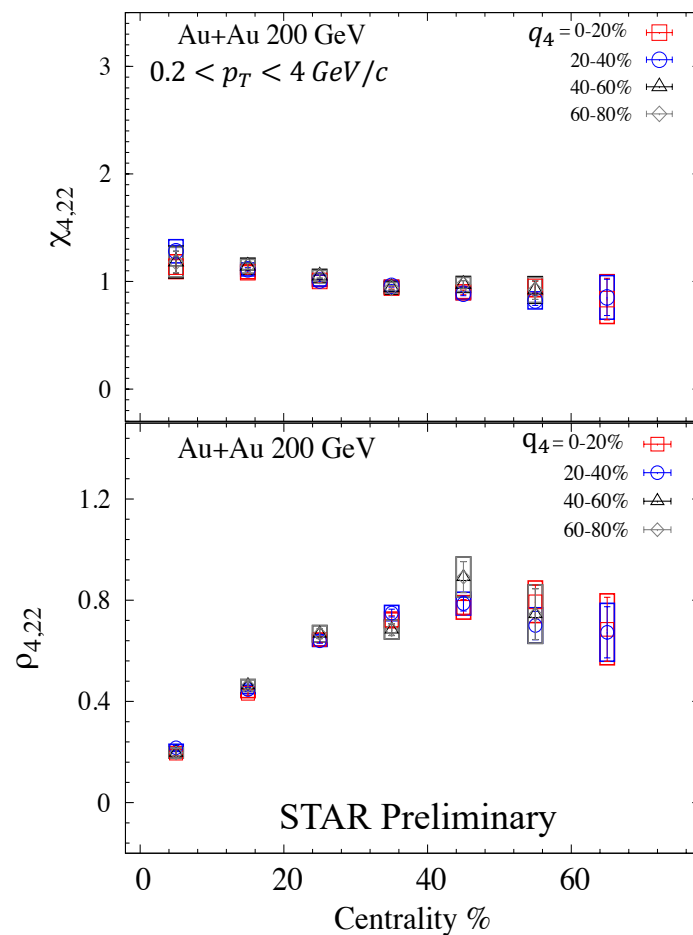
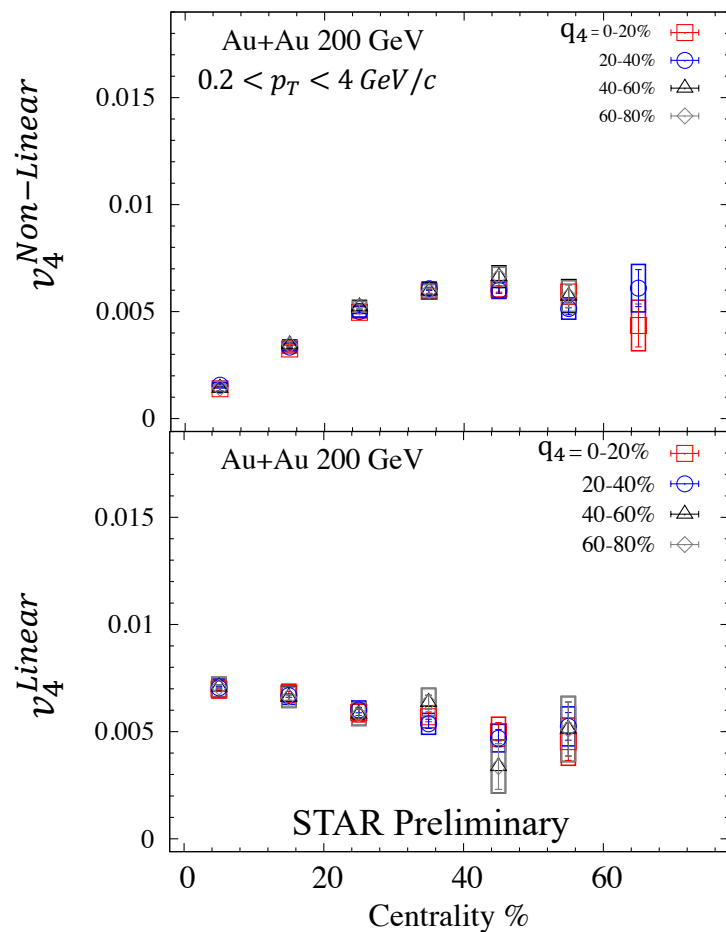
➤ The  $\rho_{4,22}$  increases with  $q_2$  selections

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# Results

Centrality dependence of the linear and non-linear  $v_4$  and the associated  $\rho_{4,22}$  and  $\chi_{4,22}$  for Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV with different event shape selection ( $q_4$ )



- The (non)linear  $v_4$  and the associated  $\rho_{4,22}$  and  $\chi_{4,22}$  show weak sensitivity to  $q_4$  selections

# Conclusion

The linear and mode-coupled contributions to the higher-order anisotropic flow coefficients  $v_4$  and  $v_5$ , have been studied using two- and multi-particle correlations in Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV

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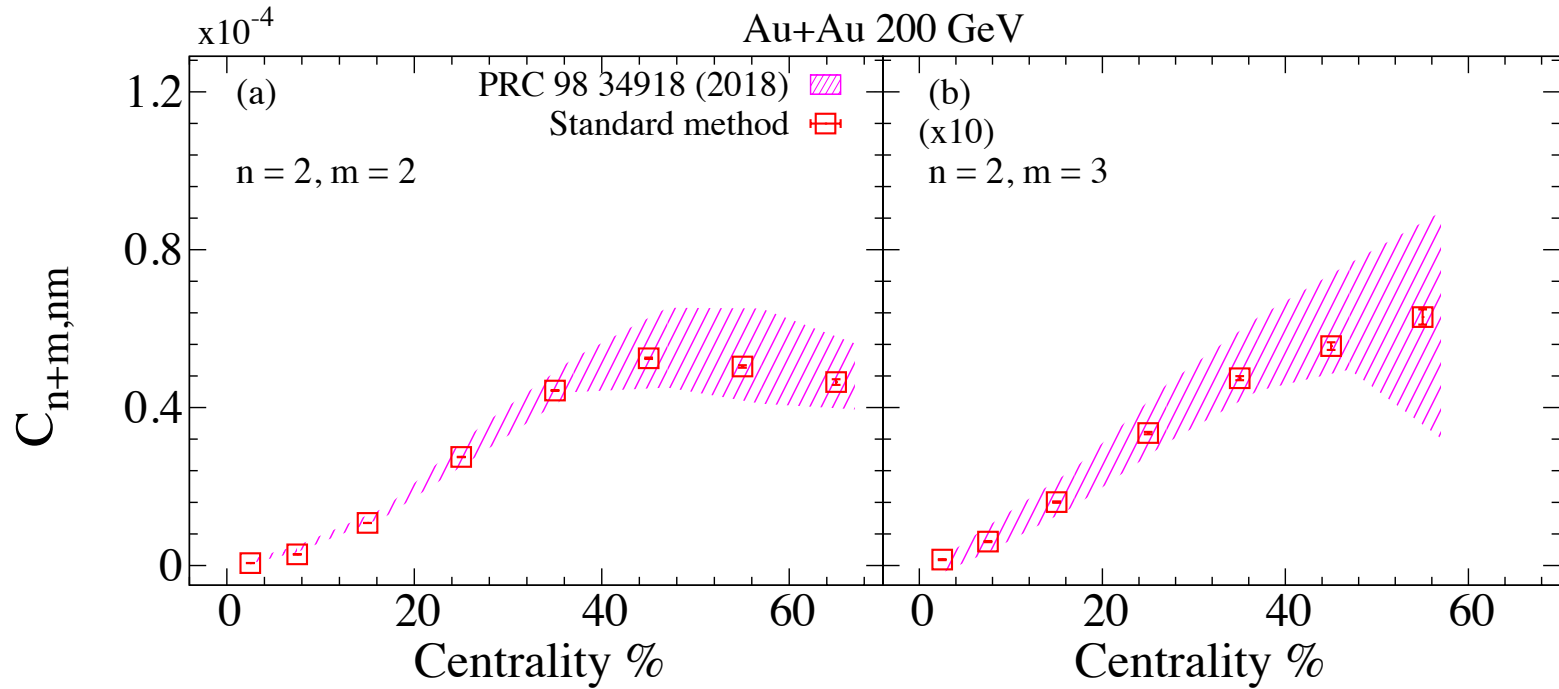
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The integrated and differential measurements, which are compared to viscous hydrodynamic model calculations, will add important constraints for the initial- and final-state models



Thank You

# Backup



Good agreement with the STAR published measurements