Fluctuations and anisotropy in heavy-ion collisions: A new paradigm

by

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Based on:

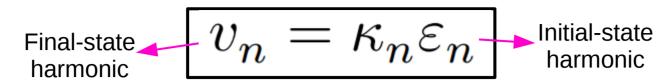
- Giacalone, Guerrero-Rodriguez, Luzum, Marquet, Ollitrault 1902.07168

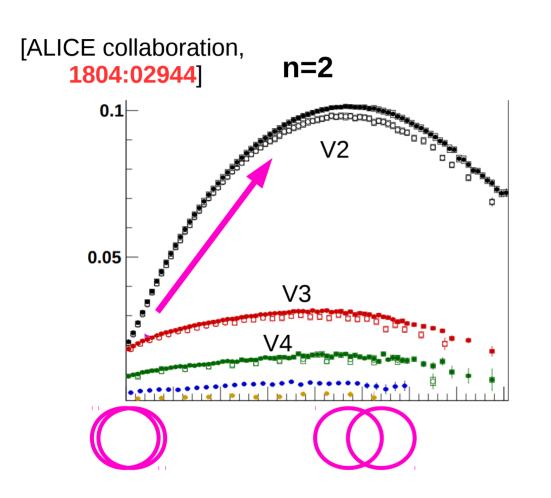


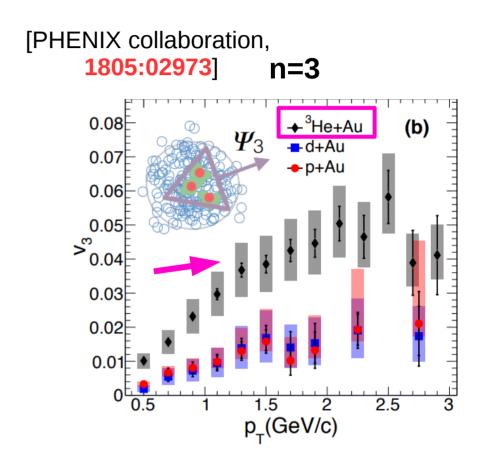




Message from data: Anisotropy from anisotropy.







This talk: AA + 'fluid paradigm'

K_n → Just a number. Rather independent of centrality up to ~20-30%. [Noronha-Hostler, Yan, Gardim, Ollitrault, arXiv 1511:03869]

How do we calculate the initial anisotropy?

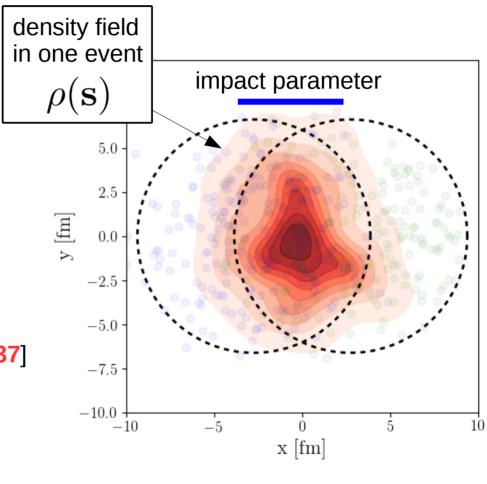
[Teaney, Yan **1010.1876**]

$$\varepsilon_n \equiv \frac{\int_{\mathbf{s}} \mathbf{s}^n \rho(\mathbf{s})}{\int_{\mathbf{s}} |\mathbf{s}|^n \rho(\mathbf{s})}$$

Origin of anisotropy:

n=2 elliptic flow → **geometry** + **fluctuations** [PHOBOS Collaboration **nucl-ex/0610037**]

n=3 triangular flow → **fluctuations only** [Alver, Roland **1003.0194**]

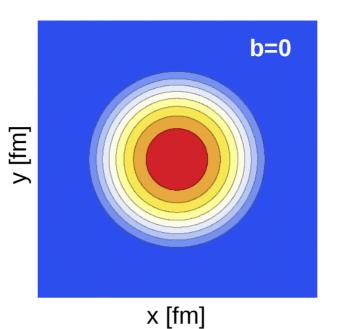


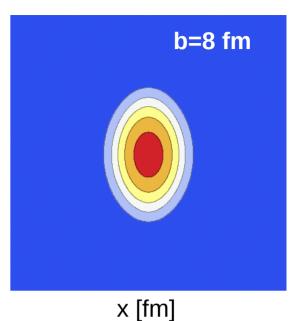
The theoretical input is a model for $\rho(s)$ and its fluctuations.

What do we need?

 $lack \langle
ho(\mathbf{s})
angle$

The average density.





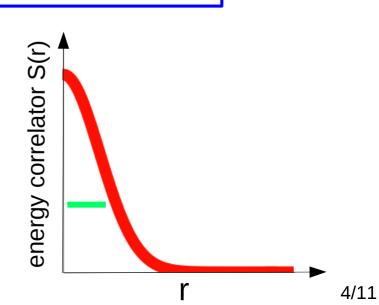
The fluctuations around the average.

$$S(\mathbf{s}_1, \mathbf{s}_2) = \langle \rho(\mathbf{s}_1) \rho(\mathbf{s}_2) \rangle - \langle \rho(\mathbf{s}_1) \rangle \langle \rho(\mathbf{s}_2) \rangle$$

Density of variance.

Quantifies the correlation of fluctuations.

$$\mathbf{r} = \mathbf{s}_1 - \mathbf{s}_2$$



Input from high-energy QCD (or CGC). Nuclei characterized by a scale:

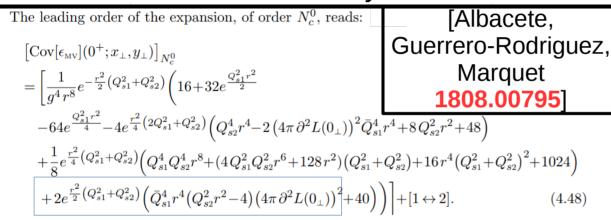
$$Q_s^2(\mathbf{s}) \propto T(\mathbf{s})$$
 - Nuclear thickness

Proportional to the density of 'color charges', that source the energy density. Average energy density after the collision known for a long time:

$$\langle \rho(\mathbf{s}) \rangle \propto Q_A^2(\mathbf{s}) Q_B^2(\mathbf{s})$$

 $\langle
ho({f s})
angle \propto Q_A^2({f s}) Q_B^2({f s})$ [Lappi hep-ph/0606207] [Lappi, Venugopalan nucl-th/0609021]

Fluctuation calculated recently:



The next term, of order N_c^{-2} , reads:

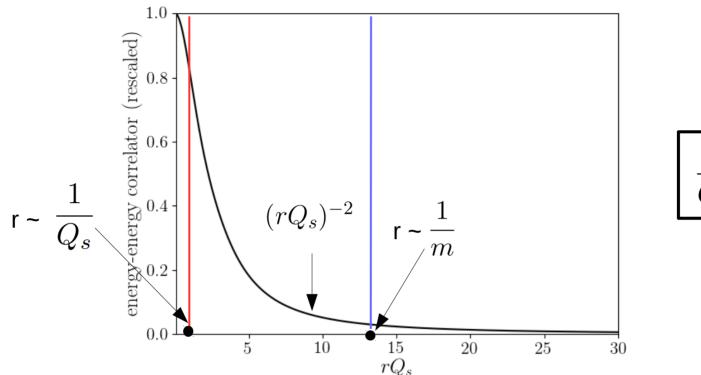
$$\begin{split} &\left[\operatorname{Cov}[\epsilon_{\scriptscriptstyle{\mathrm{MV}}}](0^{+};x_{\perp},y_{\perp})\right]_{N_{c}^{-2}} \\ &= \left[\frac{1}{N_{c}^{2}g^{4}r^{8}}e^{-\frac{r^{2}}{2}\left(Q_{s1}^{2}+Q_{s2}^{2}\right)}\left(2\left(Q_{s1}^{2}r^{2}+Q_{s2}^{2}r^{2}+8\right)^{2}\right. \\ &\left. +4Q_{s1}^{2}r^{2}(8+Q_{s1}^{2}r^{2})e^{\frac{Q_{s2}^{2}r^{2}}{2}}-8(8+Q_{s1}^{2}r^{2})(4+Q_{s1}^{2}r^{2})e^{\frac{Q_{s2}^{2}r^{2}}{4}}\right. \\ &\left. +4e^{\frac{r^{2}}{4}\left(2Q_{s1}^{2}+Q_{s2}^{2}\right)}\left(Q_{s2}^{4}r^{4}-2(4\pi\,\partial^{2}L(0_{\perp}))^{2}\bar{Q}_{s1}^{4}r^{4}+8Q_{s2}^{2}r^{2}+16Q_{s1}^{2}r^{2}\right)\right. \\ &\left. -\frac{1}{8}e^{\frac{r^{2}}{4}\left(Q_{s1}^{2}+Q_{s2}^{2}\right)}\left(Q_{s1}^{4}Q_{s2}^{4}r^{8}+(4Q_{s1}^{2}Q_{s2}^{2}r^{6}+128r^{2})\left(Q_{s1}^{2}+Q_{s2}^{2}\right)+16\,r^{4}\left(Q_{s1}^{2}+Q_{s2}^{2}\right)^{2}-1024\right)\right. \\ &\left. -2e^{\frac{r^{2}}{2}\left(Q_{s1}^{2}+Q_{s2}^{2}\right)}\left(\bar{Q}_{s1}^{4}r^{4}\left(Q_{s2}^{2}r^{2}-4\right)(4\pi\,\partial^{2}L(0_{\perp}))^{2}+32Q_{s1}^{2}r^{2}-4Q_{s1}^{2}Q_{s2}^{2}r^{4}\right)\right)\right]+\left[1\leftrightarrow2\right]. \end{split}$$

These expressions give:

$$S(\mathbf{s}_1, \mathbf{s}_2)$$
II
 $\langle
ho(\mathbf{s}_1)
ho(\mathbf{s}_2)
angle - \langle
ho(\mathbf{s}_1)
angle \langle
ho(\mathbf{s}_2)
angle$

in collisions of large nuclei.

what are the relevant features?



$$\frac{1}{Q_s} \ll \frac{1}{m}$$

- It is very sharp compared to the system size. Short-range correlations: $S(\mathbf{s}_1,\mathbf{s}_2) \approx \xi(\mathbf{s})\delta(\mathbf{r})$, $\mathbf{s} = \frac{\mathbf{s}_1 + \mathbf{s}_2}{2}$

- Its integral is divergent and dominated by r^-2 tail. An infrared cutoff naturally emerges, around the size of the nucleon. Scales are separated: we can isolate the leading contribution.

$$\xi(\mathbf{s}) \equiv \int_{\mathbf{r}} S\left(\mathbf{s} + \frac{\mathbf{r}}{2}, \mathbf{s} - \frac{\mathbf{r}}{2}\right) \propto Q_A^2(\mathbf{s}) Q_B^2(\mathbf{s}) \left[Q_A^2(\mathbf{s}) \ln\left(1 + \frac{Q_B^2(\mathbf{s})}{m^2}\right) + Q_B^2(\mathbf{s}) \ln\left(1 + \frac{Q_A^2(\mathbf{s})}{m^2}\right) \right]$$

How do we use it in practice? We follow [Blaizot, Broniowski, Ollitrault, 1405.3572].

$$\rho(\mathbf{s}) = \langle \rho(\mathbf{s}) \rangle + \delta \rho(\mathbf{s}), \quad \langle \rho(\mathbf{s}) \rangle \gg \delta \rho(\mathbf{s})$$

(on long wavelengths)

Perturbative expansion of the anisotropy: $\varepsilon_n \equiv \frac{\int_{\mathbf{s}} \mathbf{s}^n \rho(\mathbf{s})}{\int_{\mathbf{s}} |\mathbf{s}|^n \rho(\mathbf{s})}$

To first nontrivial order:

$$\langle \varepsilon_2 \varepsilon_2^* \rangle = \varepsilon_2 \{2\}^2 = \sigma^2 + \bar{\varepsilon}_2^2 \qquad \text{and} \qquad \varepsilon_3 \{2\}^2 = \frac{\int_{\mathbf{s}} |\mathbf{s}|^6 \, \xi(\mathbf{s})}{\left(\int_{\mathbf{s}} |\mathbf{s}|^2 \langle \rho(\mathbf{s}) \rangle\right)^2}$$

$$\sigma^2 = \frac{\int_{\mathbf{s}} |\mathbf{s}|^4 \, \xi(\mathbf{s})}{\left(\int_{\mathbf{s}} |\mathbf{s}|^2 \langle \rho(\mathbf{s}) \rangle\right)^2} \quad , \quad \bar{\varepsilon}_2 = \frac{\int_{\mathbf{s}} \mathbf{s}^2 \langle \rho(\mathbf{s}) \rangle}{\int_{\mathbf{s}} |\mathbf{s}|^2 \langle \rho(\mathbf{s}) \rangle}$$

From the CGC we have:

$$\langle \rho(\mathbf{s}) \rangle = \frac{4}{3a^2} Q_A^2(\mathbf{s}) Q_B^2(\mathbf{s})$$
 Prefactors from: [Albacete, Guerrero-Rodriguez, Marquet 1808.00795]

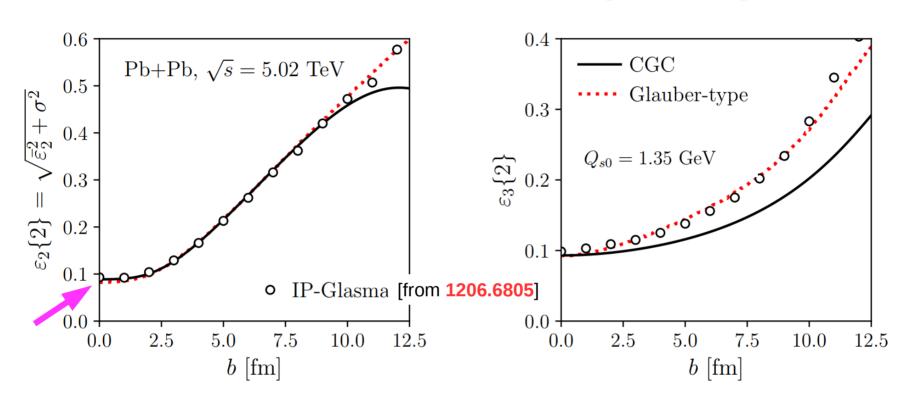
$$\xi(\mathbf{s}) = \frac{16\pi}{9g^4} Q_A^2(\mathbf{s}) Q_B^2(\mathbf{s}) \left(Q_A^2(\mathbf{s}) \ln\left(1 + \frac{Q_B^2(\mathbf{s})}{m^2}\right) + Q_B^2(\mathbf{s}) \ln\left(1 + \frac{Q_A^2(\mathbf{s})}{m^2}\right) \right)$$

Saturation scale proportional to the integrated nuclear density:

$$Q_s^2({\bf s}) = Q_{s0}^2 T({\bf s})/T({\bf 0})$$

RESULTS

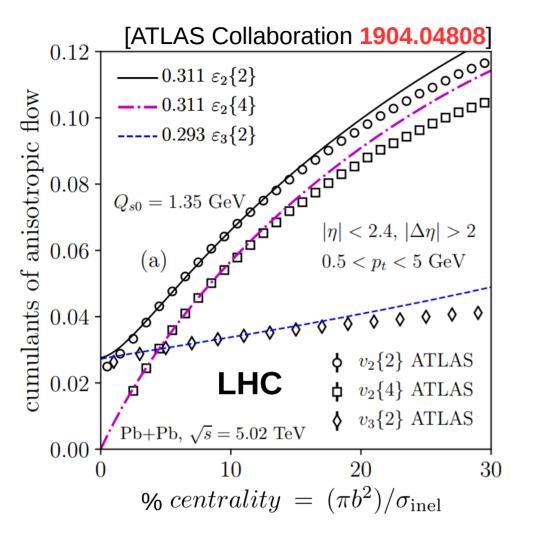
Giacalone, Guerrero-Rodriguez, Luzum, Marquet, Ollitrault [1902:07168]

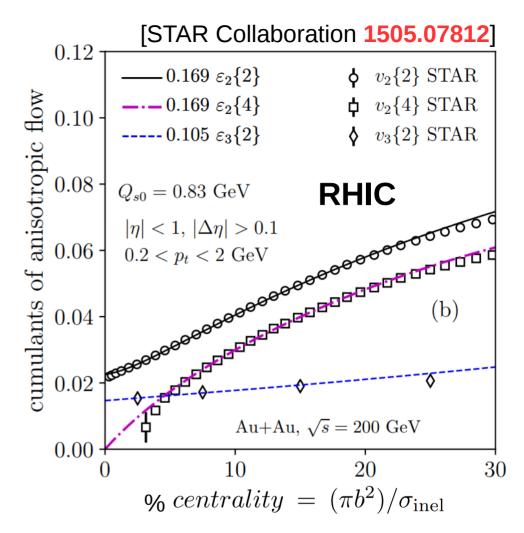


We reproduce the Glauber results. Not a lucky coincidence!

$$\varepsilon_2\{2\}^2 \approx \varepsilon_3\{2\}^2 \approx \frac{\log(Q^2/m^2)}{R^2Q^2} \longrightarrow \varepsilon_2\{2\} \approx 0.1 \text{ for } Q = 1 \text{ GeV}$$

$$R = 5 \text{ fm}$$



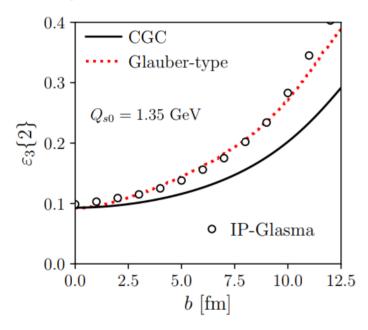


- We use $v_2\{4\}=\kappa_2\varepsilon_2\{4\}\approx\kappa_2\bar{\varepsilon}_2$ [Voloshin, Poskanzer, Tang, Wang, 0708.0800] v2{4} fixes the response coefficient k2.
- The splitting between v2{2} and v2{4} is due to fluctuations:

 $Q_s[\mathrm{LHC}] > Q_s[\mathrm{RHIC}] \Longrightarrow \text{ smaller splitting at LHC}.$

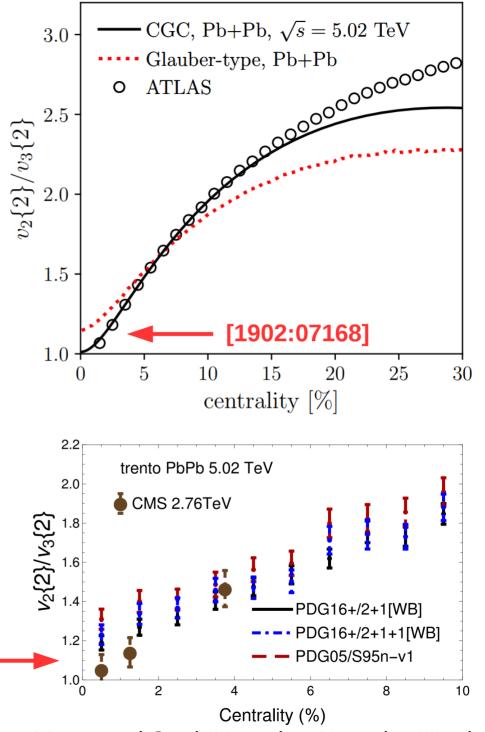
TRIANGULAR FLOW

In the CGC, triangular flow grows more mildly than in a Glauber calculation.



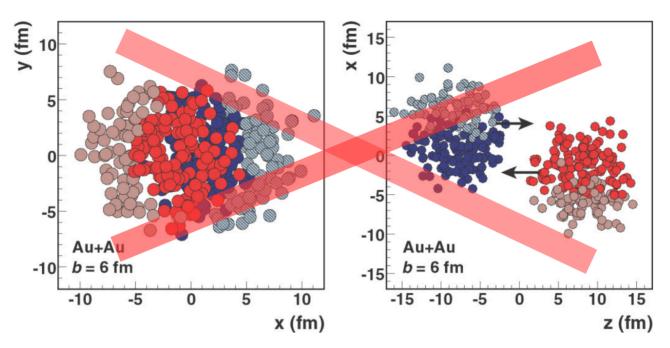
This fixes a longstanding problem of hydro-to-data comparisons:
The ratio v₂{2}/v₃{2} grows quickly with centrality.

e.g. [Shen, Qiu, Heinz, 1502.04636]



[Alba, Mantovani Sarti, Noronha, Noronha-Hostler, Parotto, Portillo Vasquez, Ratti **1711.05207**] _{10/11}

CONCLUSION: A NEW PARADIGM FOR FLUCTUATIONS.



[Miller, Reygers, Sanders, Steinberg nucl-ex/0701025]

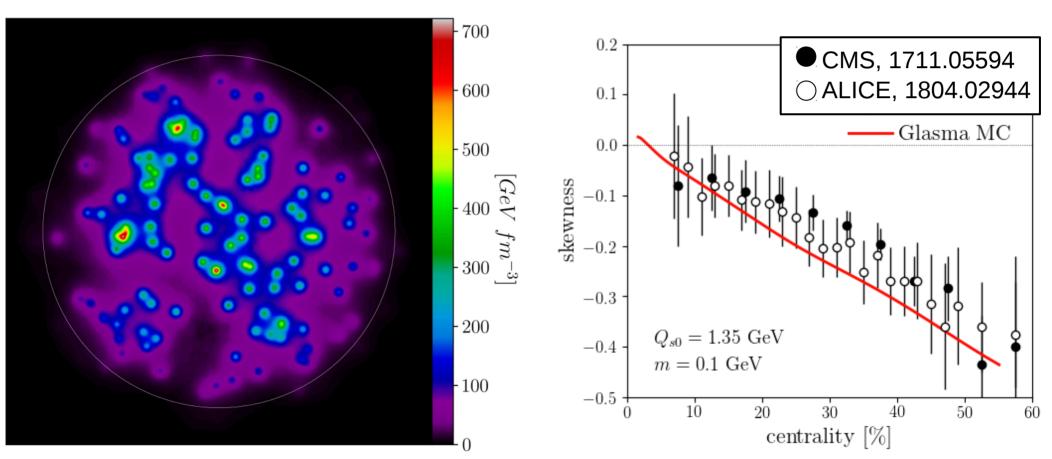
We free the description from the Glauber Monte Carlo Ansatz:

- No random sampling of nucleons.
- No ad hoc prescriptions about the deposition of energy.
- Nonperturbative physics only through the mass parameter.

BACKUP

Beyond small-and-local fluctuation approximation?

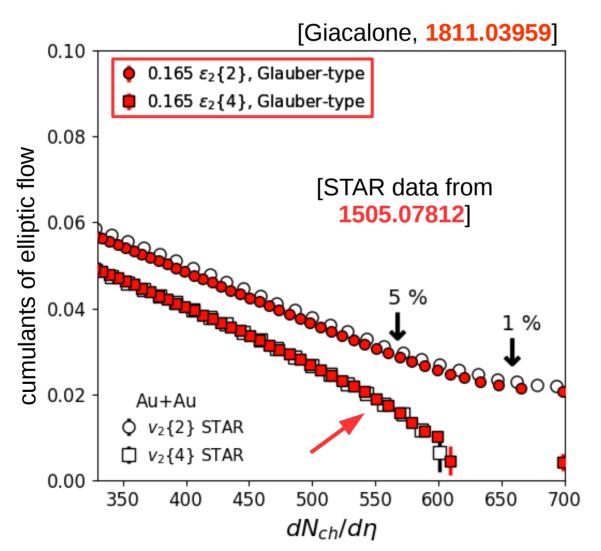
Event-by-event energy density profiles. Non-Gaussianity generated by positive sign of energy at a transverse point.

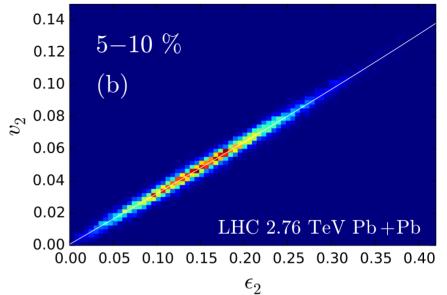


[Gelis, Giacalone, Guerrero-Rodriguez, Marquet, Ollitrault, to appear]

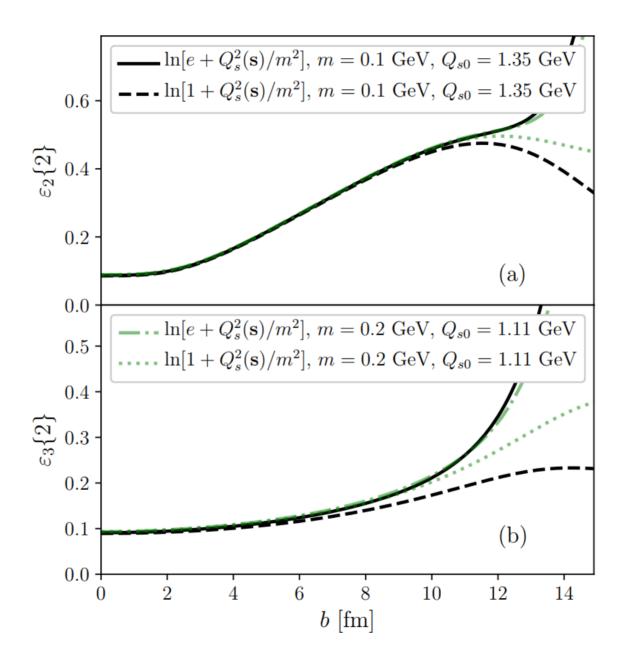
Stay tuned (or ask for details).

Calculations suggest a linear relation.





How robust is the formalism?



Breaks down at about b=12 fm.

All MC-Glauber-based models have the same eccentricities.

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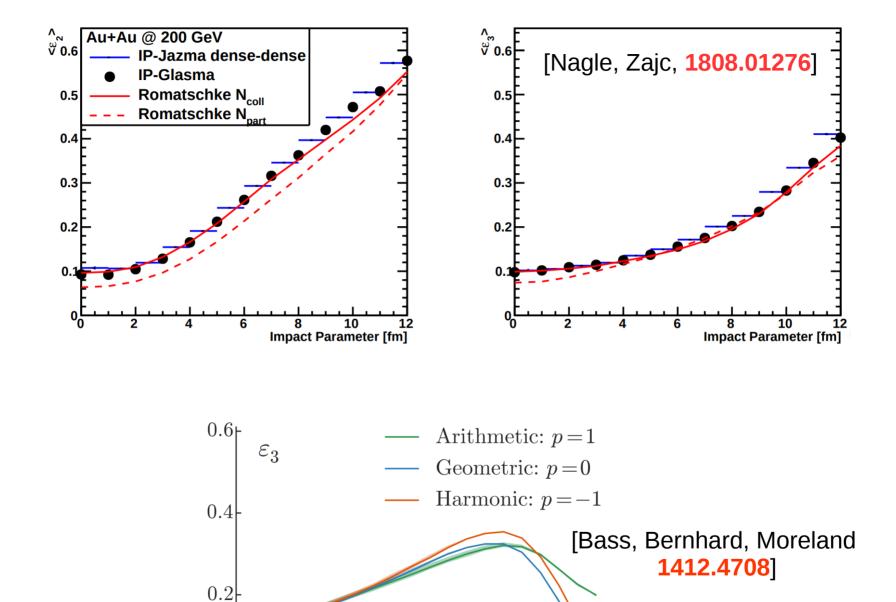
25

50

Centrality %

75

100



ELLIPTIC FLOW FLUCTUATIONS

Fluctuations of elliptic flow produce the **splitting between v2{2} and v2{4}.** Experimental data indicate that fluctuations are larger at RHIC energy.

Energy dependence of the saturation scale from fits of DIS data:

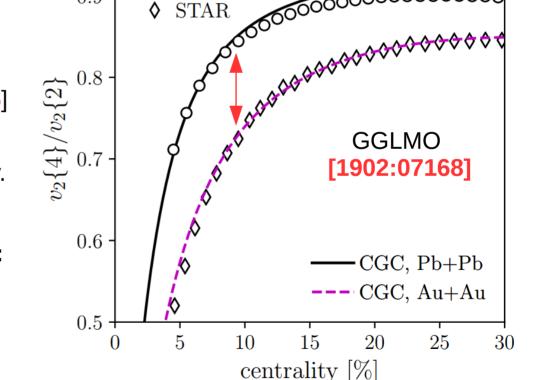
$$\frac{Q_s^2(x_1)}{Q_s^2(x_2)} = \left(\frac{\sqrt{s_1}}{\sqrt{s_2}}\right)^{0.28}$$

See e.g. [Albacete, Marquet, **1401.4866**]

Increase of ~1.6 from RHIC to LHC energy.

Compatible with the evolution of Q₅₀ found in our fit of anisotropic flow data:

$$Q_{s0}$$
 (LHC) ~ 1.3 GeV Q_{s0} (RHIC) ~ 0.8 GeV



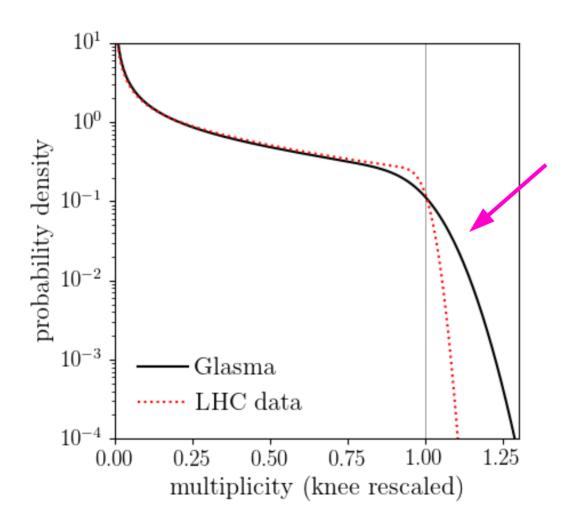
ATLAS

0.9

Very transparent physical explanation!

NB: the Glauber-type calculation does not make any specific predictions for this ratio.

The fluctuations of the primordial energy density are too large compared to the fluctuations of the final-state multiplicity observed at LHC.



Need full pre-equilibrium dynamics. Nontrivial task.