

Neutrinoless Double-Beta Decay in Effective Field Theory

Jordy de Vries

“ $0\nu\beta\beta$ in chiral EFT: LNV at dimension 7”, 1708.09390, JHEP

“A new leading contribution to $0\nu\beta\beta$ ”, 1802.10097, PRL

“A $0\nu\beta\beta$ master formula from effective field theory” 1806.02780, JHEP

“A renormalized approach to $0\nu\beta\beta$ ”, arXiv:1904.xxxxx

**With: V. Cirigliano, W. Dekens, M. Graesser, E. Mereghetti,
S. Pastore, M. Piarulli, U. van Kolck, R. Wiringa**

Neutrinoless double beta decay in EFT

- **Part I:** What is neutrinoless double beta decay and why bother?

- **Part II:** An effective field theory approach: SM-EFT + chiral EFT
 1. Light Majorana mass (the Weinberg operator)
 2. Non-perturbative renormalization
 3. Higher-dimensional lepton number violation

The puzzle of the neutrino mass

- The Standard Model does not allow for a neutrino mass
- But of course neutrino oscillations $P_{i \rightarrow j} \sim \sin^2 \left(\frac{\Delta m_{ij} L}{2E} \right)$
- Easiest solution: add the gauge singlet ν_R and use Higgs mechanism

$$L_\nu = -y_\nu \bar{L} \tilde{\phi} \nu_R + h.c. \rightarrow -\frac{y_\nu v}{\sqrt{2}} \bar{\nu}_L \nu_R \quad y_\nu \sim 10^{-12} \rightarrow m_\nu \sim 0.1 \text{ eV}$$

- Nothing wrong with this!

The puzzle of the neutrino mass

- The Standard Model does not allow for a neutrino mass
- But of course neutrino oscillations $P_{i \rightarrow j} \sim \sin^2 \left(\frac{\Delta m_{ij}^2 L}{2E} \right)$
- Easiest solution: add the gauge singlet ν_R and use Higgs mechanism

$$L_\nu = -y_\nu \bar{L} \tilde{\phi} \nu_R + h.c. \rightarrow -\frac{y_\nu v}{\sqrt{2}} \bar{\nu}_L \nu_R \quad y_\nu \sim 10^{-12} \rightarrow m_\nu \sim 0.1 \text{ eV}$$

- Nothing wrong with this! **But nothing forbids a new mass term !**

$$L_\nu = -M_R \nu_R^T C \nu_R \quad M_R \quad \text{New mass scale not linked to EW scale}$$

- Diagonalize the neutrino mass matrix. If $M_R \gg y_\nu v$

$$M_{diag} \approx \begin{pmatrix} (y_\nu v)^2 / M_R & 0 \\ 0 & M_R \end{pmatrix}$$

$$\nu = \nu_L + \nu_L^c$$

$$N = \nu_R + \nu_R^c$$

Double beta decay with and without ν 's

- Normal double beta decay ($2\nu\beta\beta$) has been observed

$$(A, Z) \rightarrow (A, Z + 2) + 2 e^- + 2 \bar{\nu}_e$$

$$T_{1/2}^{2\nu} \left({}^{76}\text{Ge} \rightarrow {}^{76}\text{Se} \right) = \left(1.84_{-0.10}^{+0.14} \right) \times 10^{21} \text{ yr} \quad \text{Gerda collaboration '15}$$

- Neutrinoless double beta decay ($0\nu\beta\beta$) looks similar

$$(A, Z) \rightarrow (A, Z + 2) + 2 e^- \quad \text{Furry '39} \quad \Delta L = 2$$

- Violates Lepton Number by two units and **never been observed (yet) ...**

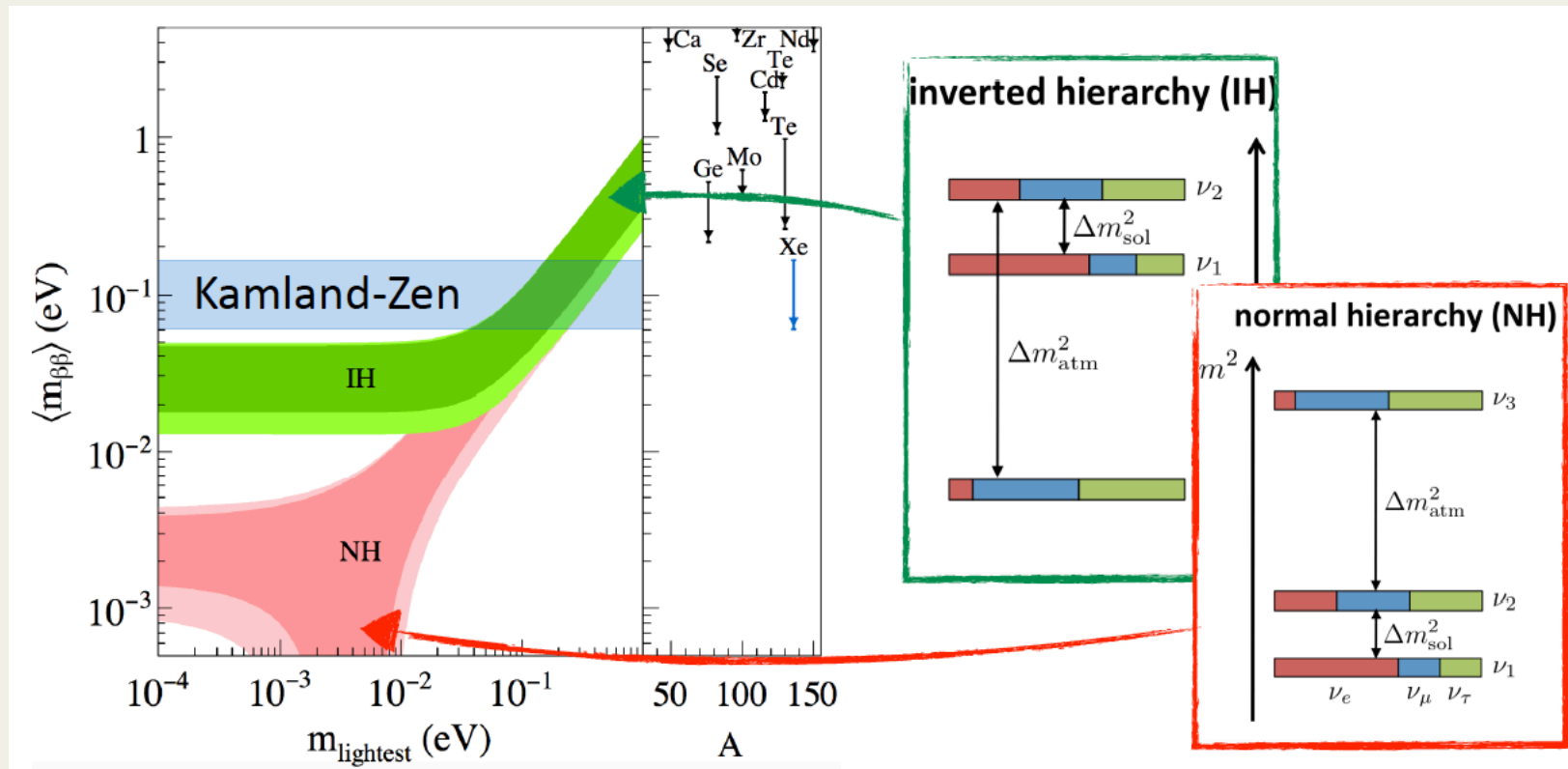
	Life time	Collaboration	year
${}^{76}\text{Ge}$	$8.0 \times 10^{25} \text{ yr}$	GERDA	2018
${}^{130}\text{Te}$	$1.3 \times 10^{25} \text{ yr}$	CUORE	2017
${}^{136}\text{Xe}$	$1.1 \times 10^{26} \text{ yr}$	KamLAND-Zen	2016

**Improvements
upcoming**

Standard interpretation

- $0\nu\beta\beta$ induced by a light-neutrino exchange $m_{\beta\beta} = \sum U_{ei}^2 m_i$
- Function of neutrino masses + mixing angles + Majorana phases

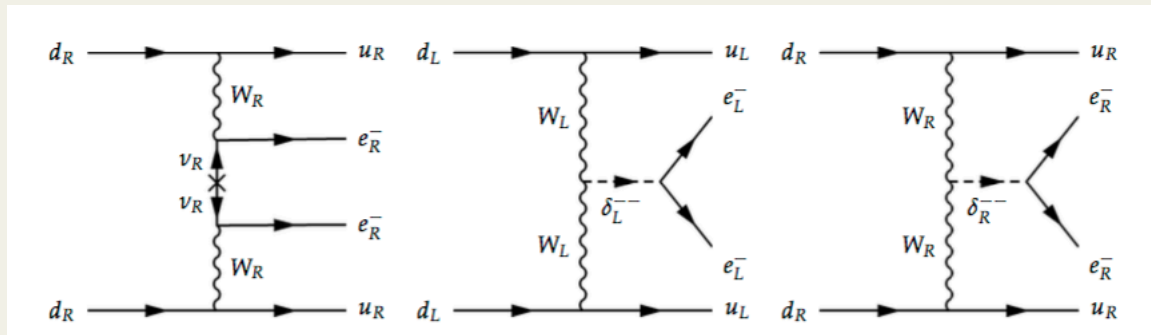
$$m_{\beta\beta} = m_{\nu 1} c_{12}^2 c_{13}^2 + m_{\nu 2} s_{12}^2 c_{13}^2 e^{2i\lambda_1} + m_{\nu 3} s_{13}^2 e^{2i(\lambda_2 - \delta_{13})}$$



- Interpretation of experimental results requires theory

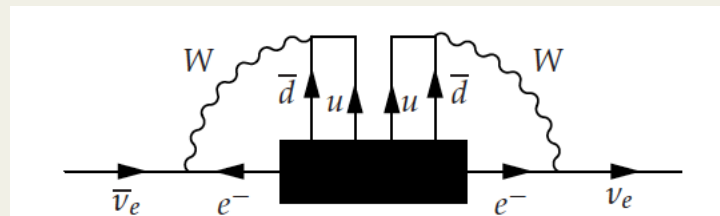
Non-Standard interpretation

- $0\nu\beta\beta$ does not have to be induced by light-neutrino exchange
- Many models induce lepton-number violation in different ways
- Example: in LR symmetric models (but also RPV SUSY, LQs, ...)



Thesis Duerr '10


- No direct link to neutrino mass. Note **Schechter-Valle** theorem '82



The anatomy of the decay

- Decay can be roughly factorized into $\frac{1}{T_{1/2}^{0\nu}} \sim m_{\beta\beta}^2 \cdot g_A^4 \cdot |M|^2 \cdot G$

Energy



$> TeV$	$m_{\beta\beta}^2$	Lepton-number-violating (LNV) source (<i>not necessarily neutrino mass</i>)
$\sim GeV$	g_A^4	Hadronic ME: quarks \rightarrow hadrons (domain of ChPT and lattice-QCD)
$\sim 100 MeV$	$ M ^2 = \left \langle 0^+ V_\nu 0^+ \rangle \right ^2$	Depends on ‘neutrino-potential’ (ChEFT) and many-body calculations
$\sim 10 MeV$	G	Phase space factor, depends on Q value $\sim Q^5$ (of order 2-5 MeV for experimental targets)

This talk: neutrinoless double beta decay

- **Part I:** What is neutrinoless double beta decay and why bother?
- **Part II: An effective field theory approach: SM-EFT + chiral EFT**
 1. Light Majorana mass (the Weinberg operator)
 2. Non-perturbative renormalization
 3. Higher-dimensional lepton number violation

Effective lepton number violation

- Lepton number = **accidental** symmetry in Standard Model (at zero T)
- But no longer once we allow for operators of $\text{dim} > 4$

- Consider the SM as an EFT
$$L_{\text{new}} = L_{\text{SM}} + \frac{1}{\Lambda} L_5 + \frac{1}{\Lambda^2} L_6 + \dots$$

- Contain SM fields only and obey SM gauge and Lorentz symmetry
- At energy E, operators of dimension (4+n) contribute as $(E / \Lambda)^n$

- **Gauge symmetry is restrictive: only 1 dim-5 operator** Weinberg '79

$$L_5 = \frac{c_5}{\Lambda} (L^T C \tilde{H})(\tilde{H}^T L) \quad L^T = (v_L \ e_L) \quad \Delta L = 2$$

- Majorana neutrino mass term after EWSB

$$m_\nu \sim eV \quad \rightarrow \quad \Lambda \sim c_5 \cdot 10^{14} \text{ GeV}$$

Higher-order in the SM-EFT

- $\Delta L = 2$ operators only appear at odd dimensions 5, 7,

Kobach '16

Dimension-five

$$\mathcal{L}_5 = \frac{c_5}{\Lambda} (L^T C \tilde{H}) (\tilde{H}^T L)$$

- One operator
- Induces Majorana mass

Dimension-seven

Lehman '14

1 : $\psi^2 H^4 + \text{h.c.}$		2 : $\psi^2 H^2 D^2 + \text{h.c.}$	
\mathcal{O}_{LH}	$\epsilon_{ij} \epsilon_{mn} (L^i C L^m) H^j H^n (H^\dagger H)$	$\mathcal{O}_{LHD}^{(1)}$	$\epsilon_{ij} \epsilon_{mn} L^i C (D^\mu L^j) H^m (D_\mu H^n)$
		$\mathcal{O}_{LHD}^{(2)}$	$\epsilon_{im} \epsilon_{jn} L^i C (D^\mu L^j) H^m (D_\mu H^n)$
3 : $\psi^2 H^3 D + \text{h.c.}$		4 : $\psi^2 H^2 X + \text{h.c.}$	
\mathcal{O}_{LHDe}	$\epsilon_{ij} \epsilon_{mn} (L^i C \gamma_\mu e) H^j H^m D^\mu H^n$	\mathcal{O}_{LHB}	$\epsilon_{ij} \epsilon_{mn} (L^i C \sigma_{\mu\nu} L^m) H^j H^n B^{\mu\nu}$
		\mathcal{O}_{LHW}	$\epsilon_{ij} (\tau^I e)_{mn} (L^i C \sigma_{\mu\nu} L^m) H^j H^n W^{I\mu\nu}$
5 : $\psi^4 D + \text{h.c.}$		6 : $\psi^4 H + \text{h.c.}$	
$\mathcal{O}_{LL\bar{d}uD}^{(1)}$	$\epsilon_{ij} (\bar{d} \gamma_\mu u) (L^i C D^\mu L^j)$	$\mathcal{O}_{LLLL\bar{e}H}$	$\epsilon_{ij} \epsilon_{mn} (\bar{e} L^i) (L^j C L^m) H^n$
$\mathcal{O}_{LL\bar{d}uD}^{(2)}$	$\epsilon_{ij} (\bar{d} \gamma_\mu u) (L^i C \sigma^{\mu\nu} D_\nu L^j)$	$\mathcal{O}_{LLQ\bar{d}H}^{(1)}$	$\epsilon_{ij} \epsilon_{mn} (\bar{d} L^i) (Q^j C L^m) H^n$
$\mathcal{O}_{LQ\bar{d}d}^{(1)}$	$(Q C \gamma_\mu d) (\bar{L} D^\mu d)$	$\mathcal{O}_{LLQ\bar{d}H}^{(2)}$	$\epsilon_{im} \epsilon_{jn} (\bar{d} L^i) (Q^j C L^m) H^n$
$\mathcal{O}_{LQ\bar{d}d}^{(2)}$	$(\bar{L} \gamma_\mu Q) (d C D^\mu d)$	$\mathcal{O}_{LL\bar{Q}uH}$	$\epsilon_{ij} (\bar{Q}_m u) (L^m C L^i) H^j$
$\mathcal{O}_{dd\bar{e}D}$	$(\bar{e} \gamma_\mu d) (d C D^\mu d)$	$\mathcal{O}_{LQ\bar{Q}dH}$	$\epsilon_{ij} (\bar{L}_m d) (Q^m C Q^i) \bar{H}^j$
		\mathcal{O}_{LddH}	$(d C d) (\bar{L} d) H$
		$\mathcal{O}_{Ldd\bar{e}H}$	$(\bar{L} d) (u C d) \bar{H}$
		$\mathcal{O}_{Leu\bar{e}H}$	$\epsilon_{ij} (L^i C \gamma_\mu e) (\bar{d} \gamma^\mu u) H^j$
		$\mathcal{O}_{eQ\bar{d}H}$	$\epsilon_{ij} (\bar{e} Q^i) (d C d) \bar{H}^j$

- 12 $\Delta L=2$ operators

Dimension-nine

Graesser '16

JdV et al '18

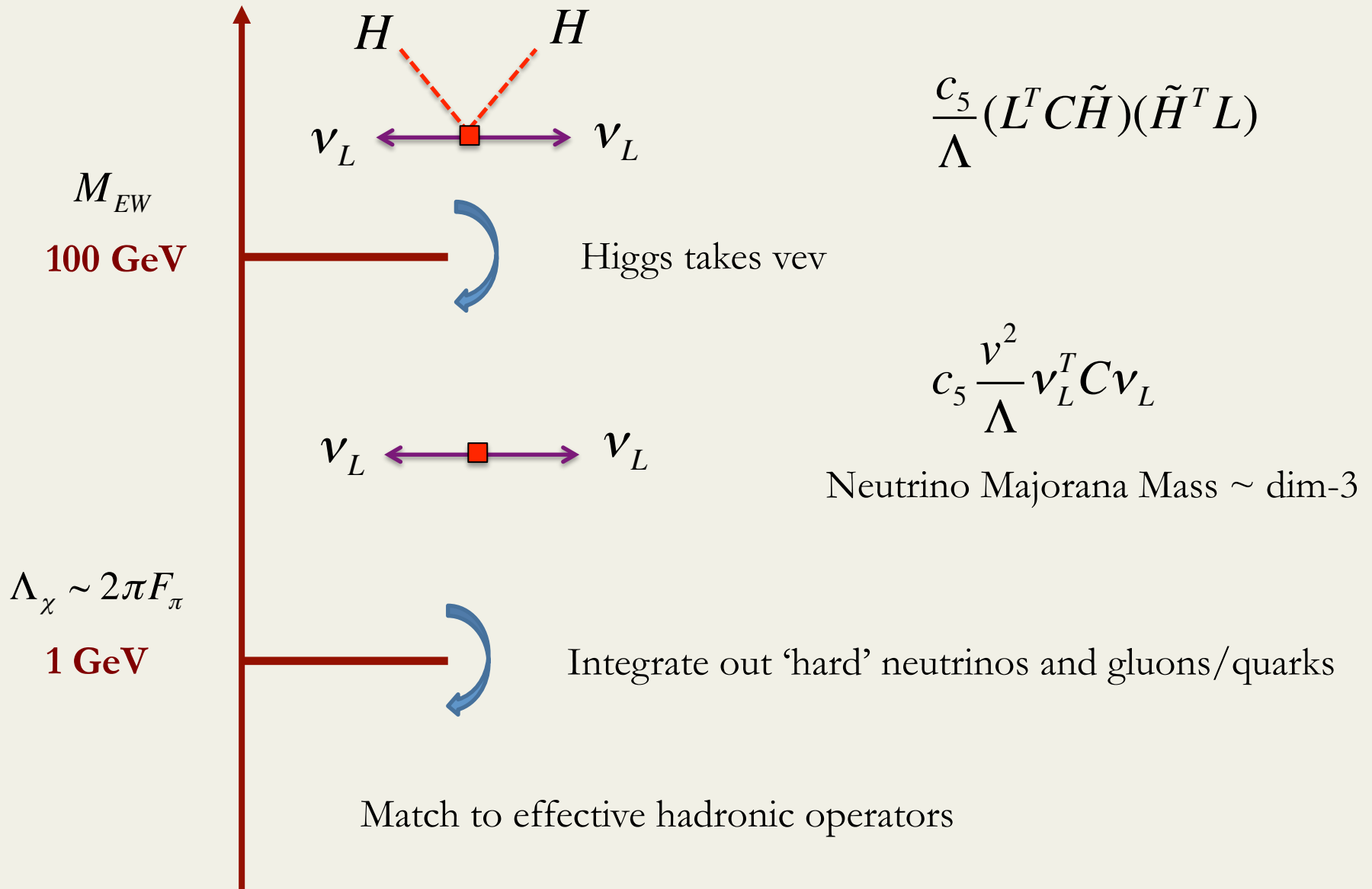
Full basis not known

19 4-quark 2-lepton operators after EWSB

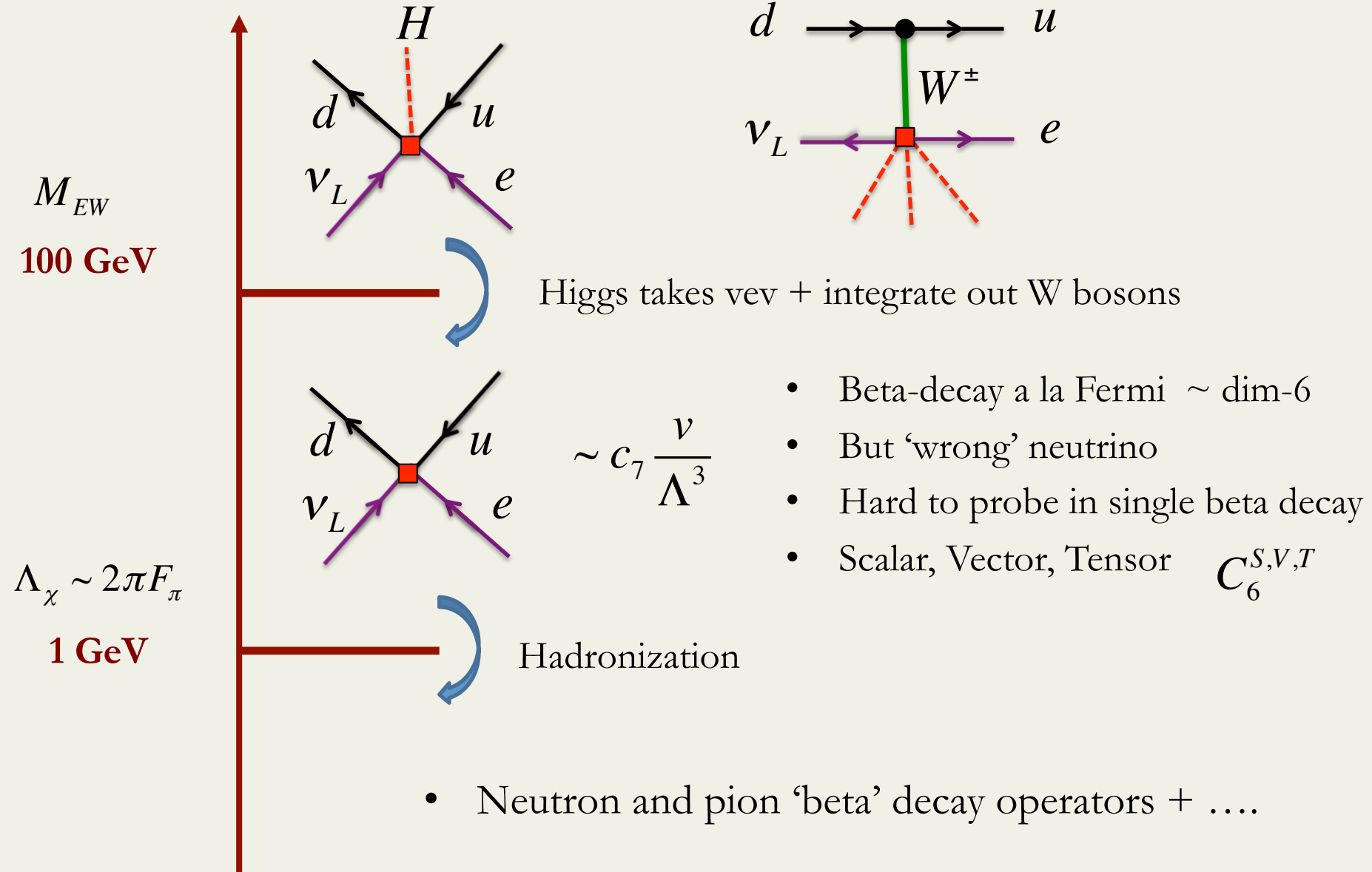
- Seems crazy to go to dim-7 if expansion parameter is $\left(\frac{v}{\Lambda}\right)^2 \sim 10^{-24}$

- Various models (left-right symmetry, RPV SUSY) $c_5 \ll 1$ Prezeau et al '03
- Example: in LR symmetry $c_5 \sim y_e^2 \sim 10^{-10}$ $c_7 \sim y_e \sim 10^{-5}$ $c_9 \sim y_e^0 \sim 1$
- Then if scale is low $\sim \Lambda \sim (10-100) \text{ TeV}$ $\text{dim}5 \sim \text{dim}7 \sim \text{dim}9$

Crossing the electroweak scale

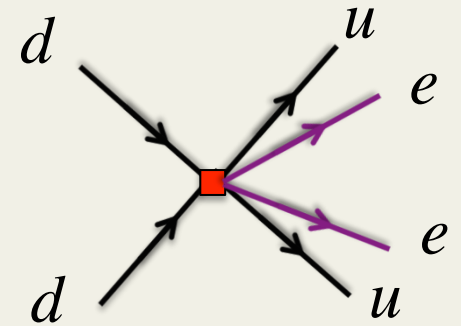
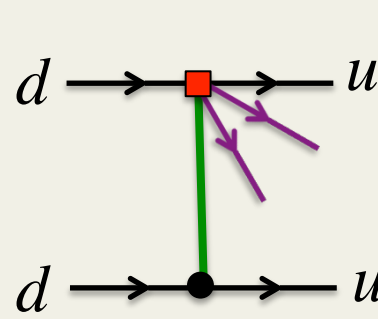
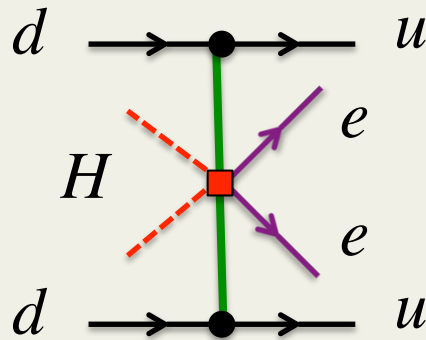


Dimension-7 operators

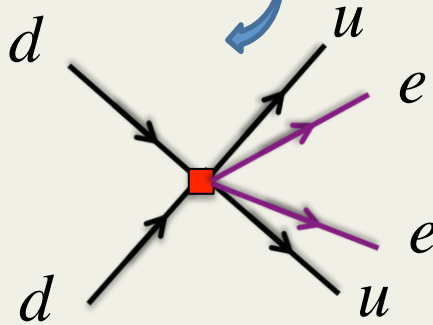


Dimension-9 operators

M_{EW}
100 GeV



$\Lambda_\chi \sim 2\pi F_\pi$
1 GeV



$$\sim c_7 \frac{1}{v^2 \Lambda^3}$$

$$\sim c_9 \frac{1}{\Lambda^5}$$

- $0\nu\beta\beta$ operators \sim 'dim 9'
- Scalar and Vector operator

Hadronization

- Hadron-electron-electron couplings

Neutrinoless double beta decay in EFT

- **Part I:** What is neutrinoless double beta decay and why bother?
- **Part II:** An effective field theory approach: SM-EFT + chiral EFT
 1. **Light Majorana mass (the Weinberg operator)**
 2. Non-perturbative renormalization
 3. Higher-dimensional lepton number violation

Chiral effective field theory

~ GeV

$$L = L_{QCD} + L_{Fermi}$$

~100 MeV

LO strong:

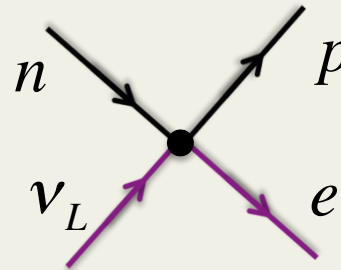
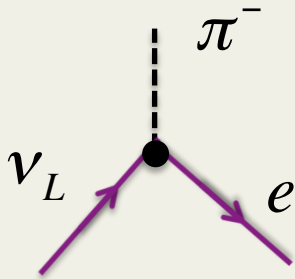
$$L_{\chi} = L_{kin} - m_N \bar{N}N - \frac{1}{2} m_{\pi}^2 \pi^2 + \frac{g_A}{f_{\pi}} D_{\mu} \vec{\pi} \cdot \bar{N} \gamma^{\mu} \gamma^5 \vec{\tau} N$$

Weak interactions

Fermi (F)

Gamow-Teller (GT)

$$L_{\chi, Fermi} = G_F f_{\pi} \left(\partial_{\mu} \pi^{-} \bar{e}_L \gamma^{\mu} \nu_L \right) + G_F \bar{p} \left(\gamma^{\mu} - g_A \gamma^{\mu} \gamma^5 \right) n \bar{e}_L \gamma^{\mu} \nu_L + \dots$$



Chiral effective field theory

$\sim \text{GeV}$

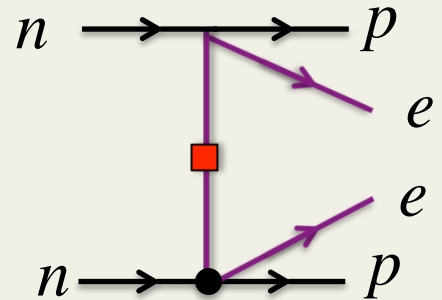
$$L = L_{QCD} + L_{Fermi} - m_{\beta\beta} \mathbf{v}_L^T C \mathbf{v}_L$$

$\sim 100 \text{ MeV}$

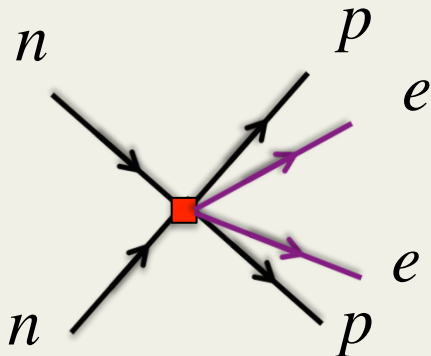
Neutrinos are still degrees of freedom in the low-energy EFT

LO interaction : $\mathbf{v}_L \longleftrightarrow \mathbf{v}_L \sim m_{\beta\beta}$

Leads to long-range $nn \rightarrow pp + ee \sim \frac{m_{\beta\beta}}{q^2}$
 $q \sim k_F \sim m_\pi$



'Hard' neutrino exchange ($E, |\vec{p}| > \Lambda_\chi$) \rightarrow short-range operators

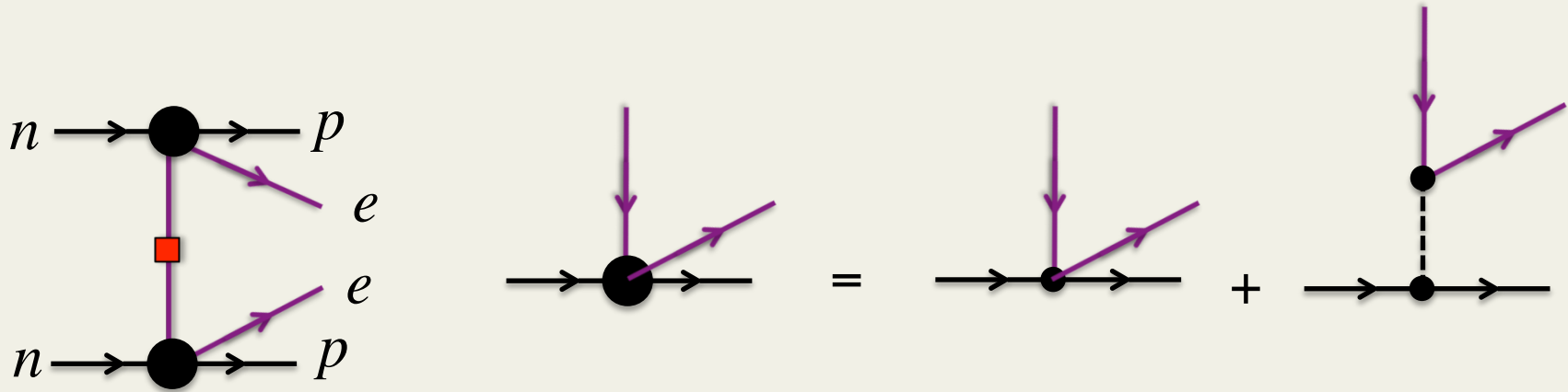


Expected at N²LO
 (Weinberg counting or naïve
 dimensional analysis)

$$\sim \frac{m_{\beta\beta}}{\Lambda_\chi^2}$$

Majorana mass contribution

- Apply chiral EFT to construct a ‘neutrino potential’
- **Standard mechanism: leading order**



$$V_v = (2G_F^2 m_{\beta\beta}) \tau_1^+ \tau_2^+ \frac{1}{\vec{q}^2} \left[1 - g_A^2 \left(\vec{\sigma}_1 \cdot \vec{\sigma}_2 - \vec{\sigma}_1 \cdot \vec{q} \vec{\sigma}_2 \cdot \vec{q} \frac{2m_\pi^2 + \vec{q}^2}{(m_\pi^2 + \vec{q}^2)^2} \right) \right] \otimes \bar{e}_L e_L^c$$

- LO long-range Coulomb-like potential $\sim 1/q^2$
- Close to ‘standard’ approach but no **Form Factors** or **Closure terms**
- All other contributions are higher order \rightarrow **pretty simple at LO**

Quick look at higher orders

Cirigliano et al '17

- The EFT approach allows for systematic corrections

1. Factorizable ‘one-body’ corrections (form factors)

$$g_A \longrightarrow g_A(q^2)$$

Quick look at higher orders

Cirigliano et al '17

- The EFT approach allows for systematic corrections

- Factorizable 'one-body' corrections

$$g_A \longrightarrow g_A(q^2)$$

- New non-factorizable pieces
+ associated **counter terms**

Some diagrams are UV divergent.....

$$V_v^{N2LO} = \tau_1^+ \tau_2^+ \left(V_{loops,finite} + V_{UV} \log \frac{m_\pi^2}{\mu_{UV}^2} + V_{CT} \right) \otimes \bar{e}_L e_L^c$$

- Counter terms appear at N²LO

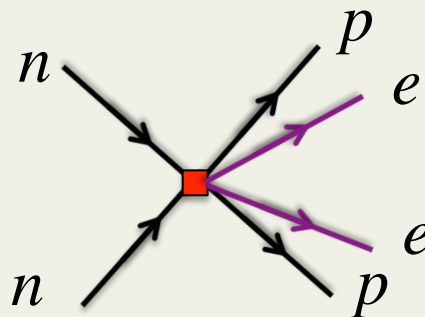
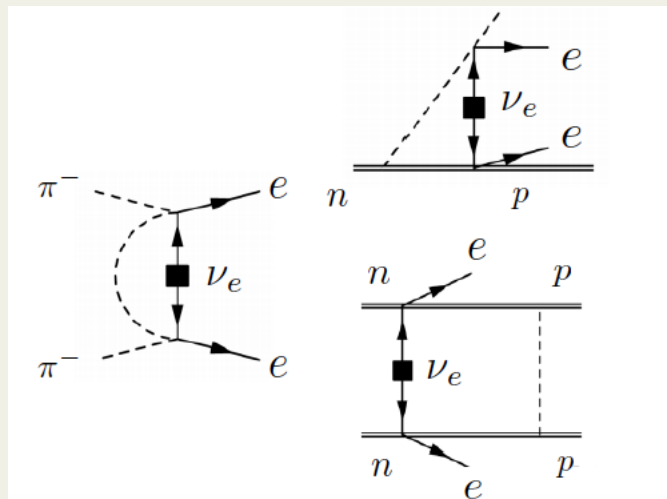
$$L_{CT} = C_v (\bar{p}n)(\bar{p}n) \otimes \bar{e}_L e_L^c$$

- Right size to absorb UV divergencies

since loops bring factor

$$\sim \frac{g_A^2 m_\pi^2}{(4\pi f_\pi^2)} \sim \frac{m_\pi^2}{\Lambda_\chi^2}$$

- As expected: short-range at N²LO



Quick look at higher orders

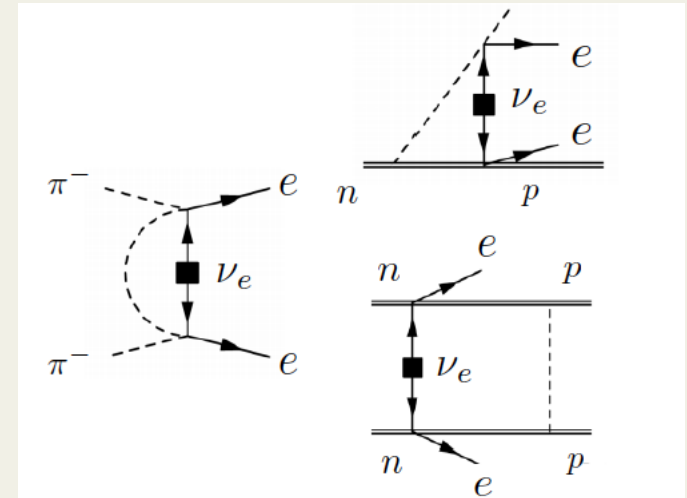
Cirigliano et al '17

- The EFT approach allows for systematic corrections

- Factorizable 'one-body' corrections

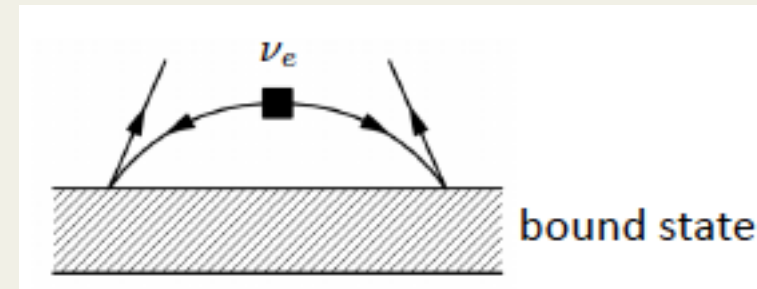
$$g_A \longrightarrow g_A(q^2)$$

- New non-factorizable pieces
+ associated **counter terms**



- Closure corrections from ultrasoft neutrino exchange
- Depends on **nuclear excited states**

$$\text{Appear at N}^2\text{LO} \sim \frac{(E_n - E_0)}{(4\pi k_F)} \sim \frac{q^2}{\Lambda_\chi^2}$$



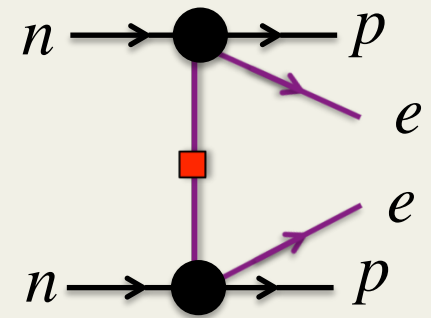
- Correspond to so-called 'closure corrections'

Review by Doi et al '83

The neutrino amplitude

- At LO the ‘standard’ mechanism is long-range

$$V_\nu = (2G_F^2 m_{\beta\beta}) \tau_1^+ \tau_2^+ \frac{1}{\vec{q}^2} \left[1 - g_A^2 \left(\vec{\sigma}_1 \cdot \vec{\sigma}_2 - \vec{\sigma}_1 \cdot \vec{q} \vec{\sigma}_2 \cdot \vec{q} \frac{2m_\pi^2 + \vec{q}^2}{(m_\pi^2 + \vec{q}^2)^2} \right) \right] \otimes \bar{e}_L e_L^c$$



- All other corrections at least N²LO ! Confirmed by many-body calculations
- Different methods have roughly a factor 2 to 3 ‘many-body spread’**

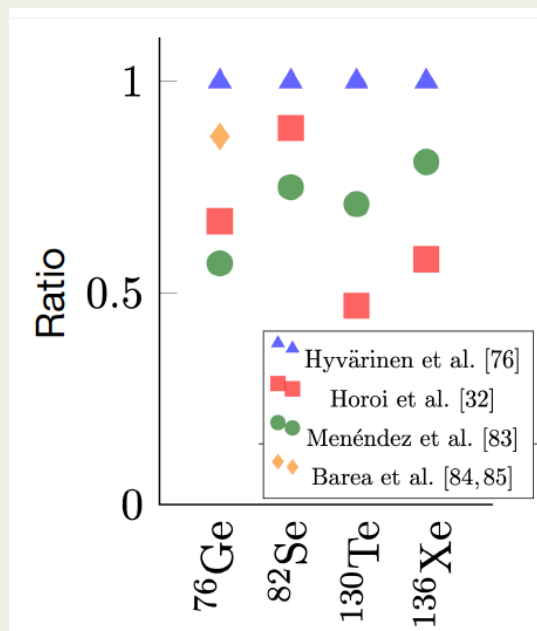
Nuclear structure problem ?

QPRA (Hyvarinen/Suhonen '15)

Shell model (Horoï/Neacsu '17 & Menendez '18)

IBM (Barea et al '15 '18)

Or could there be other problem?



Back to the basics

- Size of short-range piece was estimated by perturbation theory (NDA)
- Let's test this by studying the most simple process: $nn \rightarrow pp + ee$

“A new leading contribution to $0\nu\beta\beta$ ”, 1802.10097, PRL 120

Back to the basics

- Size of short-range piece was estimated by perturbation theory (NDA)
- Let's test this by studying the most simple process: $nn \rightarrow pp + ee$

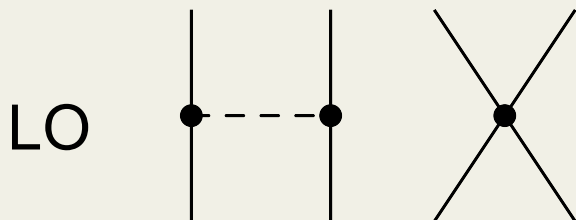
“A new leading contribution to $0\nu\beta\beta$ ”, 1802.10097, PRL 120

- First describe NN scattering by solving LS equation

$$T = V + VG_0T$$

- The potential calculated in **perturbation theory from chiral Lagrangian**
- Leading-order potential is simple (corrections discussed later)

$$L_\chi = L_{kin} - m_N \bar{N}N + \frac{g_A}{f_\pi} D_\mu \vec{\pi} \cdot \bar{N} \gamma^\mu \gamma^5 \vec{\tau} N + C_0 \bar{N}N \bar{N}N$$



$$V_{strong}^{1S_0}(LO) = C_0 - \frac{g_A^2}{4f_\pi^2} \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} + \dots$$

Nucleon-nucleon scattering

- Need to ‘regulate’ the potential (physics should be regulator independent!)

$$V_{strong}^{1S_0} = C_0 - \frac{g_A^2}{4f_\pi^2} \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} \quad V \rightarrow e^{-\frac{p^6}{\Lambda^6}} V e^{-\frac{p'^6}{\Lambda^6}} \quad C_0(\Lambda)$$

$$T(p', p, E) = V(p', p) + \int dl V(p', l) \frac{l^2}{E - l^2/m_N + i\varepsilon} T(l, p)$$

- The counter term is fitted to low-energy data (**scattering lengths**)
- Predictions are made for nucleon-nucleon **phases shifts** (all energies)

Nucleon-nucleon scattering

- Need to ‘regulate’ the potential (physics should be regulator independent!)

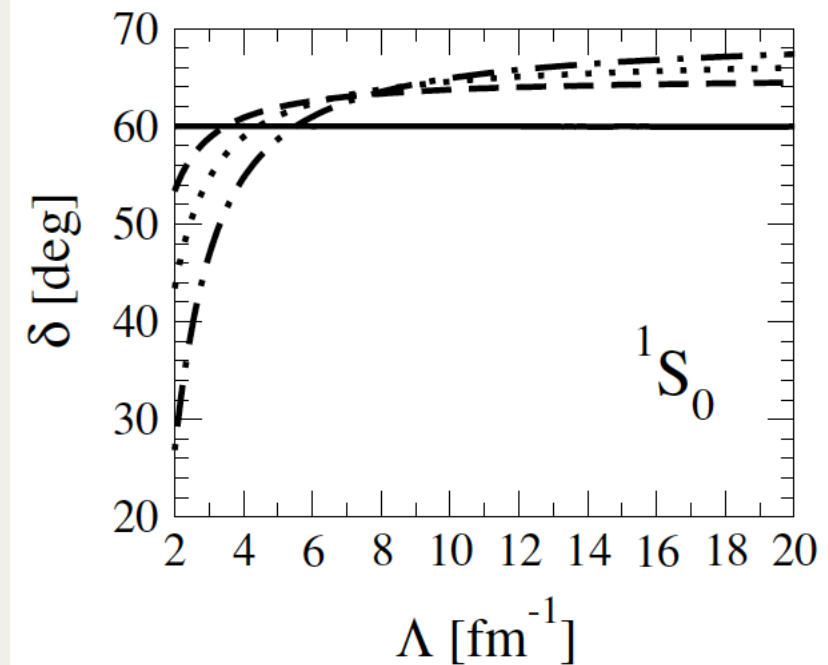
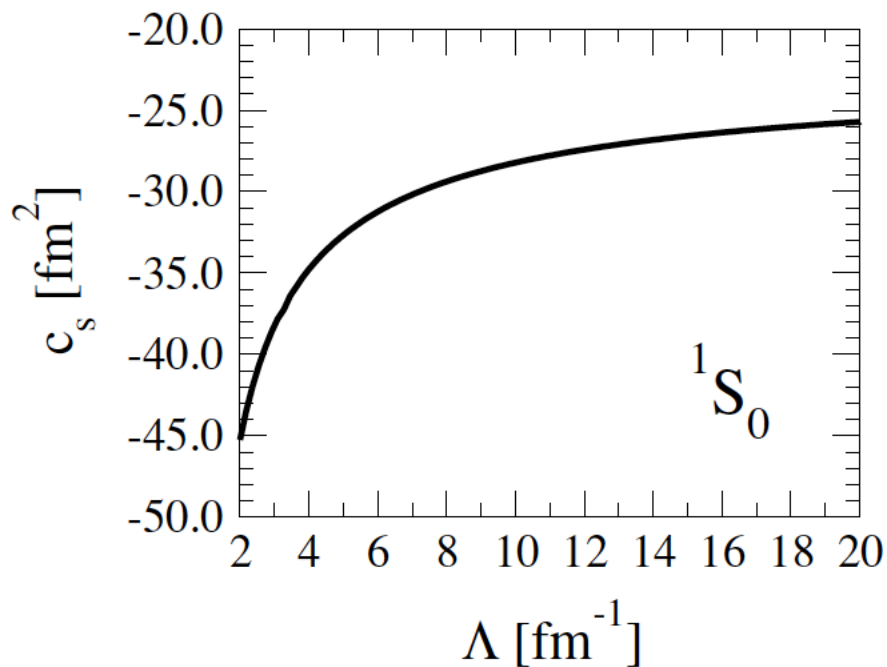
$$V_{strong}^{1S_0} = C_0 - \frac{g_A^2}{4f_\pi^2} \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} \quad V \rightarrow e^{-\frac{p^6}{\Lambda^6}} V e^{-\frac{p'^6}{\Lambda^6}} \quad C_0(\Lambda)$$

$$T(p', p, E) = V(p', p) + \int dl V(p', l) \frac{l^2}{E - l^2/m_N + i\varepsilon} T(l, p)$$

- The counter term is fitted to low-energy data (**scattering lengths**)
- Predictions are made for nucleon-nucleon **phases shifts** (all energies)
- Λ is a momentum cut-off. It should be $\Lambda \geq M_{high}$ so that we do not miss soft physics. **In practice $\Lambda \cong M_{high}$ is often useful.**
- **But one should check first that $\Lambda \gg M_{high}$ can be taken in principle !!**
- Note: 3 different regulators used in actual calculations (dim-reg, coordinate space cut-off, momentum space cut-off)

Nucleon-nucleon scattering

- Counter term shows a logarithmic dependence on cut-off
- **But phase shifts are cut-off independent (for $\Lambda > 600$ MeV)**



— Fit to 10 MeV data

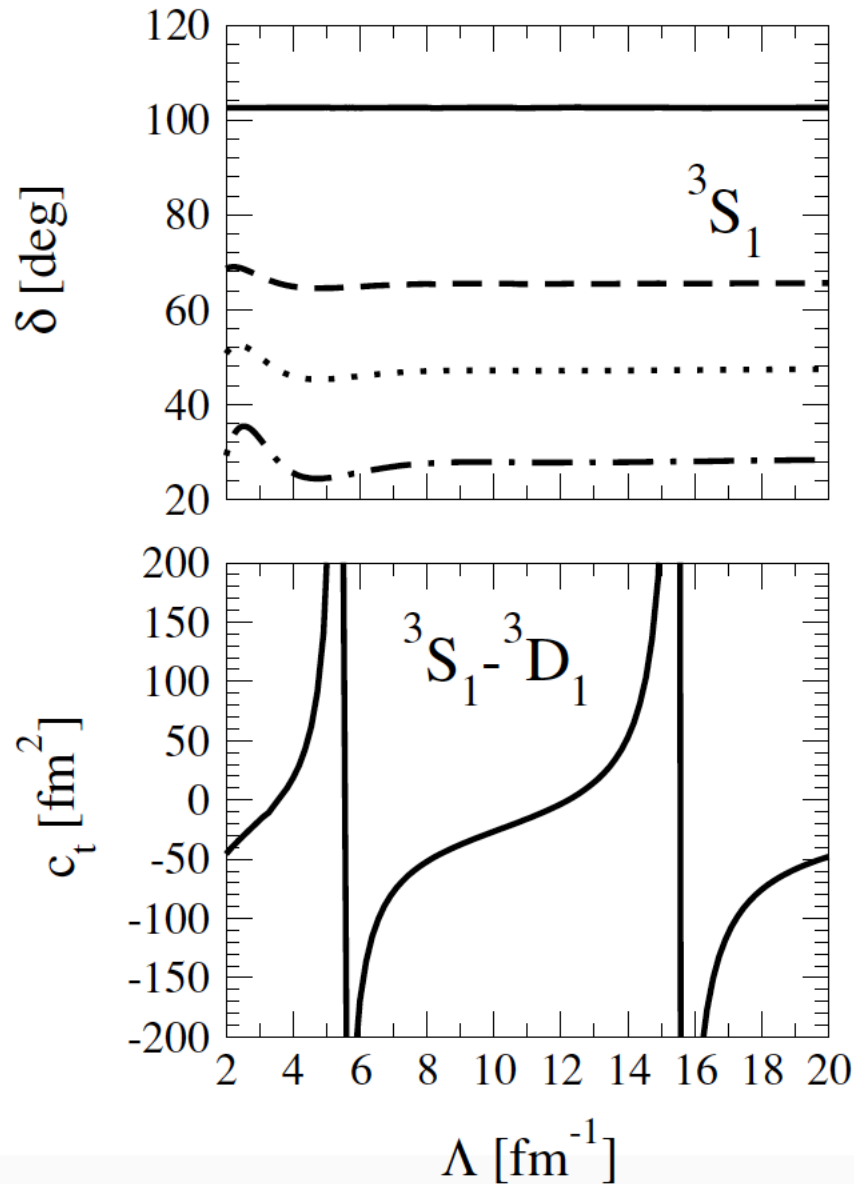
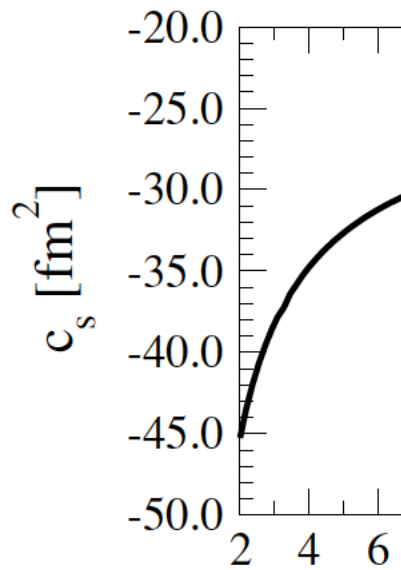
--- 50 MeV

... 100 MeV

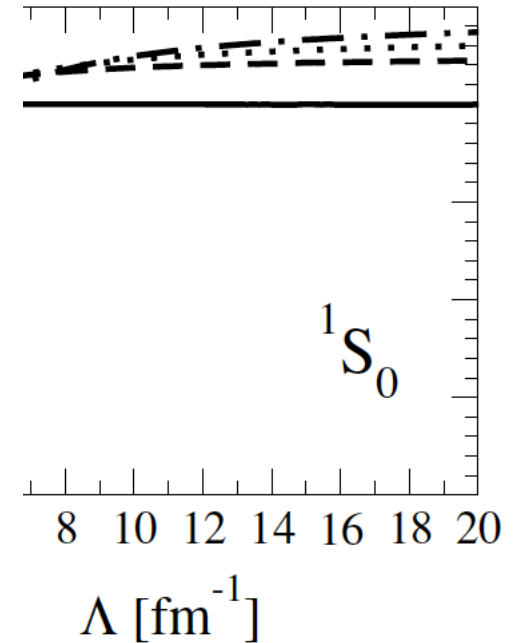
- . - . 190 MeV

Nucleon-nucleon scattering

- Counter term
- But phase



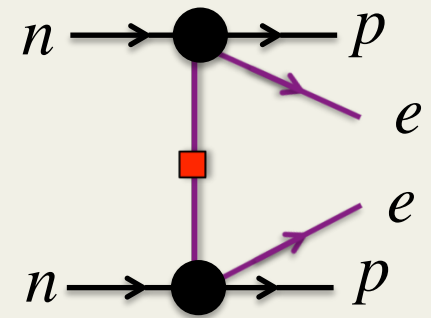
cut-off
($\Lambda > 600 \text{ MeV}$)



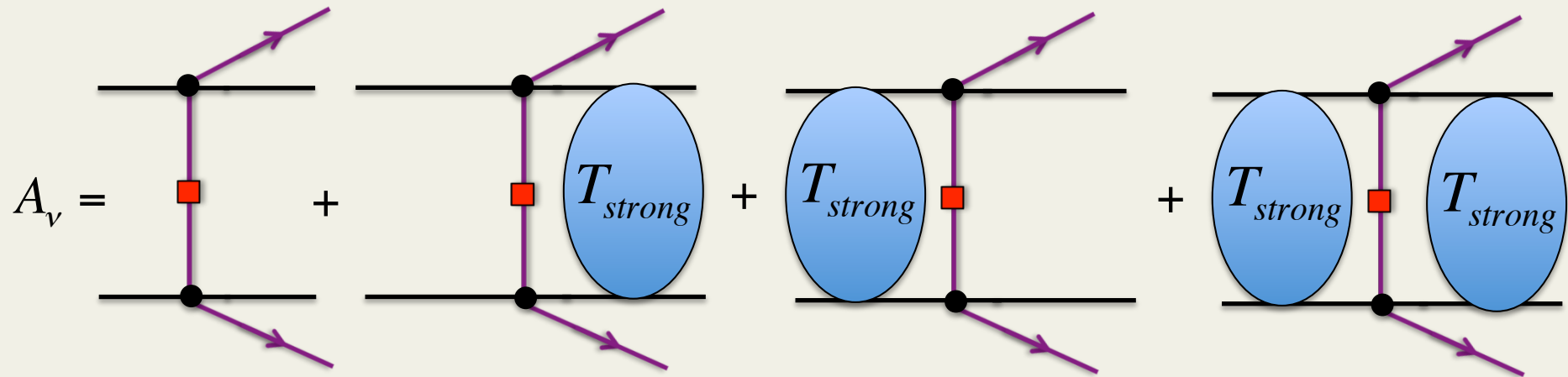
50 MeV
100 MeV
190 MeV

The neutrino amplitude

- Now insert the neutrino potential

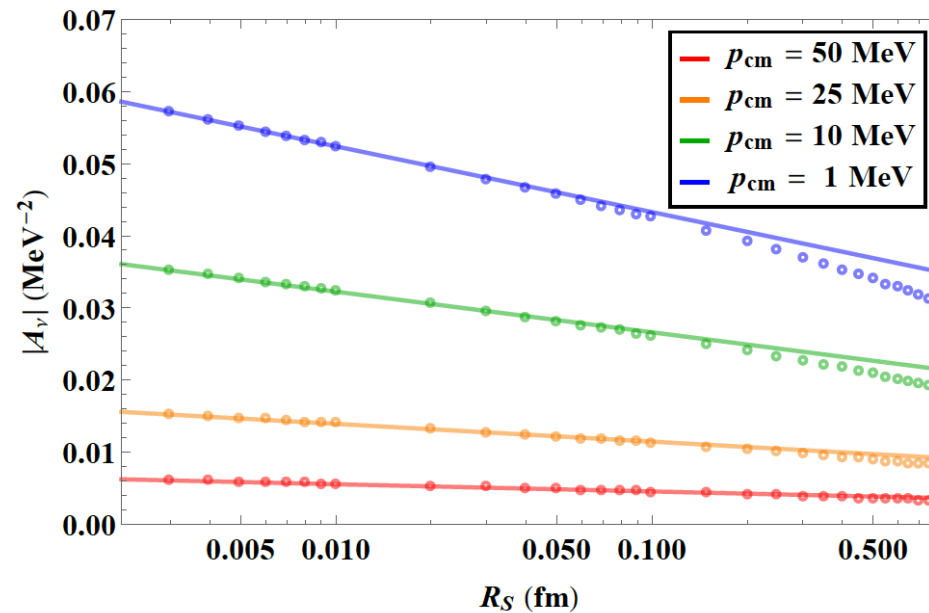
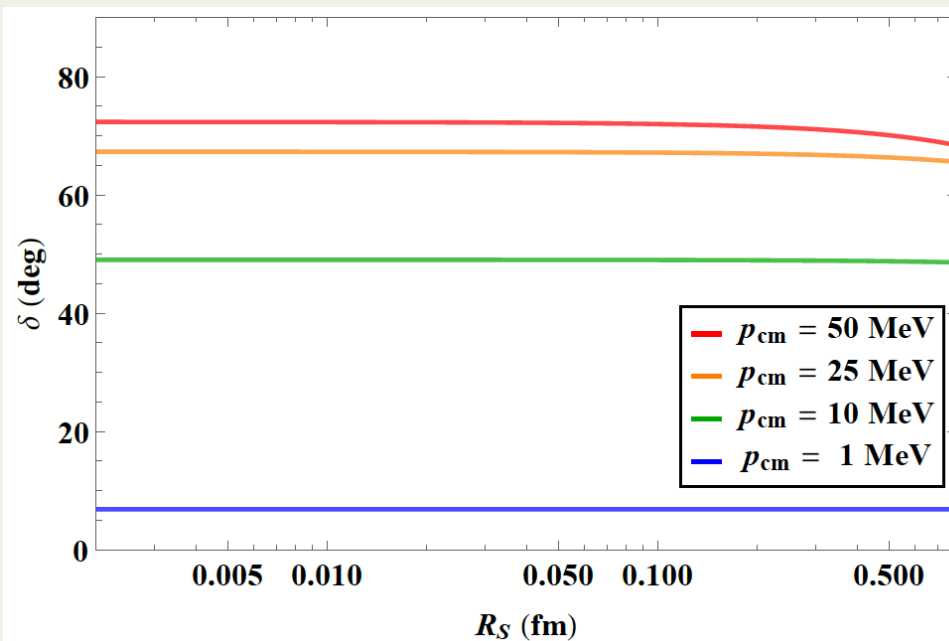


$$A_v = V_v + V_v G_0 T_{LO} + T_{LO} G_0 V_v + T_{LO} G_0 V_v G_0 T_{LO}$$

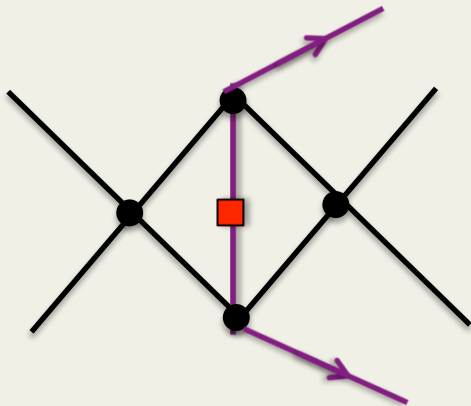


- Can be measured in principle \rightarrow should be independent of regulator !!

The neutrino amplitude



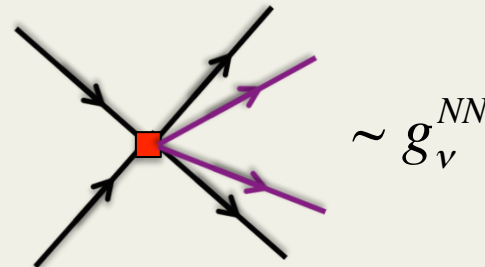
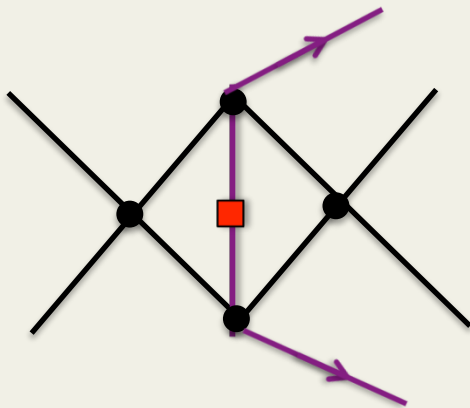
- But it is not... The amplitude depends logarithmically on the regulator.



$$\sim (1 + 2g_A^2) \left(\frac{m_N C_0}{4\pi} \right)^2 \left(\frac{1}{\varepsilon} + \log \frac{\mu^2}{p^2} \right)$$

Non-perturbative renormalization

- Now a divergence is nothing scary in an EFT calculation
- It just signals dependence on hard scales \rightarrow need a counter term
- The surprising thing perhaps is that it violates NDA (but happens in other cases too)

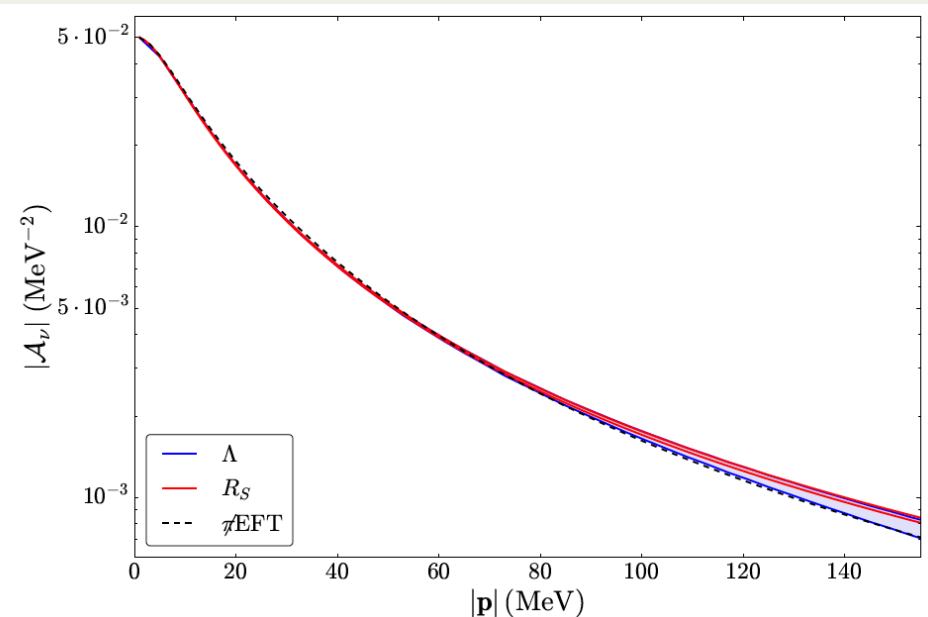
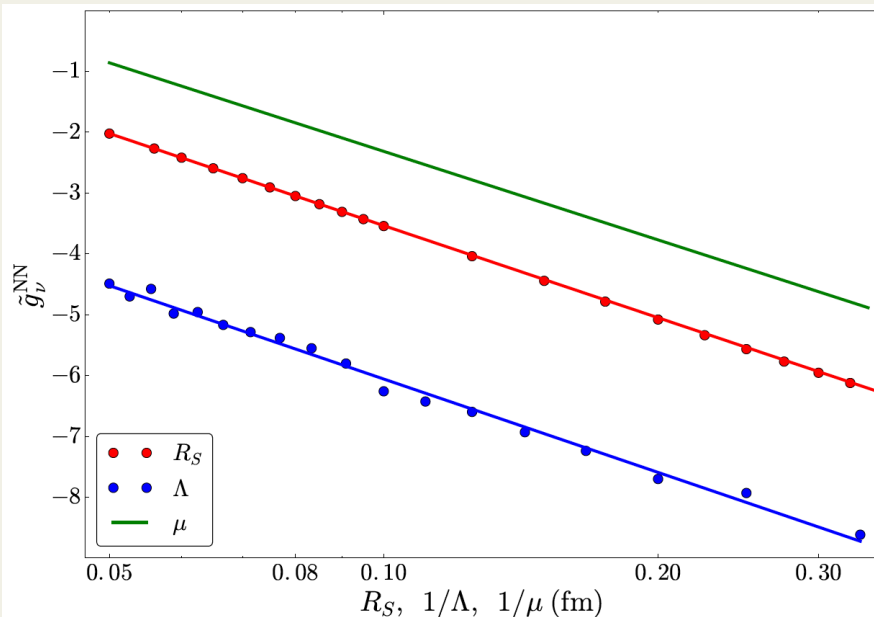
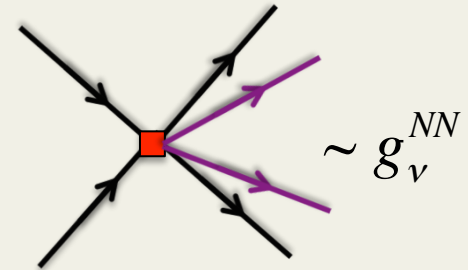


- Contact term comes with new LEC \sim QCD dynamics at $< (\Lambda_\chi)^{-1}$
- **Neutrino mass $m_{\beta\beta}$ not directly connected to decay rate**
- This is not expected to be a small correction ! **It is leading order !**
- **A counter term gets the job done though !**

Non-perturbative renormalization

Fit the counter term to a ‘measurement’ at some kinematic point

$$\frac{1}{G_F^2 m_{\beta\beta}} A_\nu(p = 1 \text{ MeV}) = 0.05 \text{ MeV}^{-2}$$



Determining the counter term

- Can we determine the LEC of the counter term in absence of data ?

We have identified **two potential strategies to get** g_v^{NN}

1. Lattice QCD calculations of $nn \rightarrow pp + ee$ (obvious but hard).

Interesting progress on $\pi\pi\pi \rightarrow ee$

Nicholson et al '18, Feng et al '18

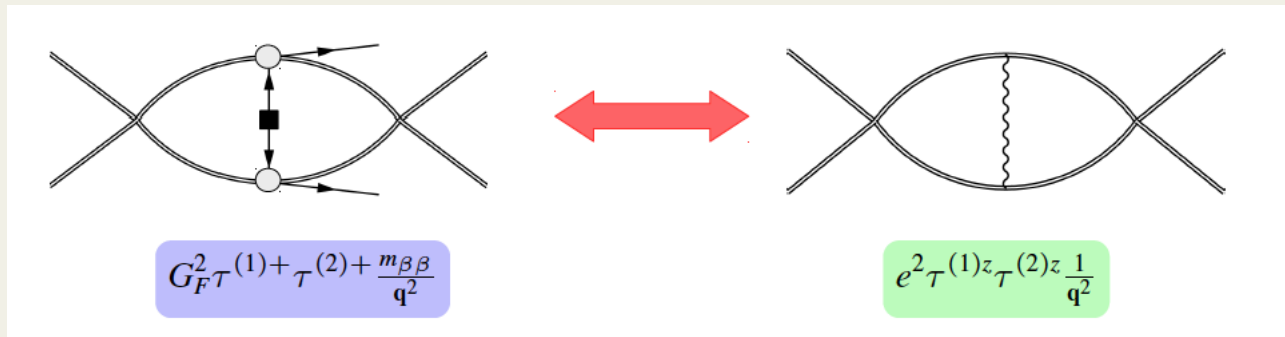
CAN THIS BE DONE ??

2. Chiral symmetry to connect to measured isospin-violating processes

- **Convincingly (IMO) demonstrates need for LO counterterm**
- **So far cannot give the full determination of** g_v^{NN}

Using chiral symmetry

- The shape of the neutrino potential is very similar to photon exchange



- LO scattering of nn, pp, and np is the same
- EM and isospin-breaking changes the picture
- Dominant contributions from photon exchange + pion-mass splitting

$$V_{\text{CIB}}^{1S_0} = \frac{e^2}{4} \left(\tau_3^{(1)} \tau_3^{(2)} - \frac{1}{3} \boldsymbol{\tau}^{(1)} \cdot \boldsymbol{\tau}^{(2)} \right) \frac{1}{q^2} \left\{ 1 + \frac{g_A^2}{F_\pi^2} \frac{m_{\pi^\pm}^2 - m_{\pi^0}^2}{e^2} \left(\frac{q^2}{q^2 + m_\pi^2} \right)^2 \right\}.$$

- In Weinberg counting short-range operators at N²LO**

Charge-independence breaking

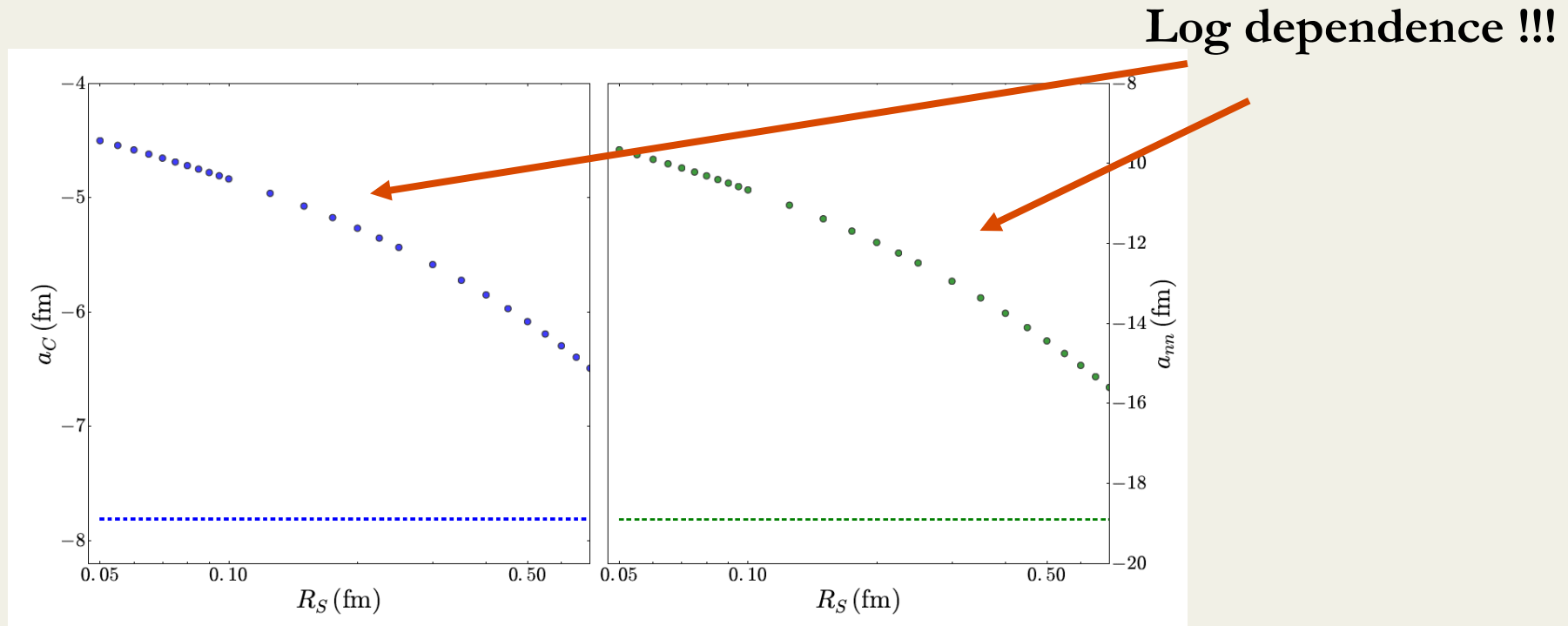
- So the idea is: we calculate the scattering lengths

$$a_{nn}$$

$$a_{np}$$

$$a_{pp}$$

- Weinberg counting: once LO strong counter term is fitted to a_{np} then a_{nn} and a_{pp} are predicted. They should be cut-off independent



Charge-independence breaking

- So the idea is: we calculate the scattering lengths

$$a_{nn} \qquad a_{np} \qquad a_{pp}$$

- Weinberg counting: once LO strong counter term is fitted to a_{np} then a_{nn} and a_{pp} are predicted. They should be cut-off independent

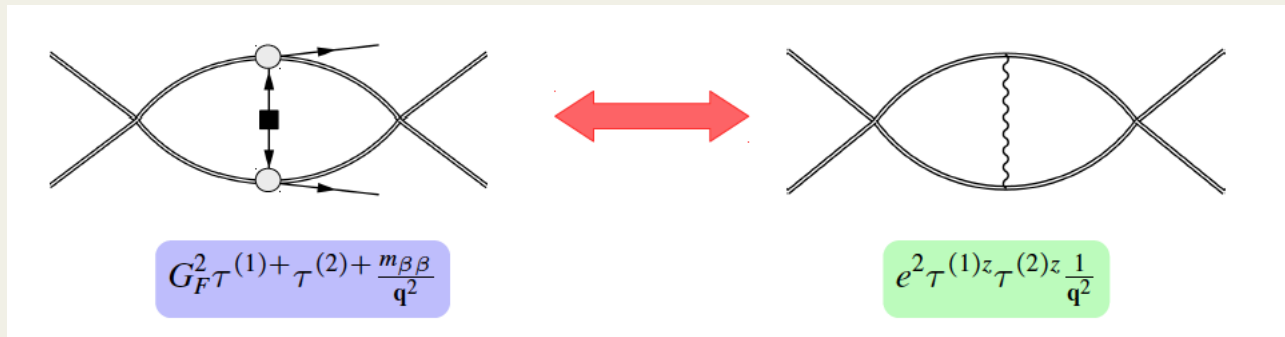
- We need to add a short-range CIB operator to describe data
- In fact: **high-quality potentials** include that term (also chiral ones)

$$C_{CIB} \sim fm^2 \sim O\left(\frac{1}{f_\pi^2}\right) \gg O\left(\frac{1}{\Lambda_\chi^2}\right)$$

- Weinberg counting failure confirmed by data
- **Conclusion: Coulomb-like potentials in 1S_0 -waves need counter terms**

A bit deeper

- The connection can be deepened



- Construct contact operators from EM I=2 operators

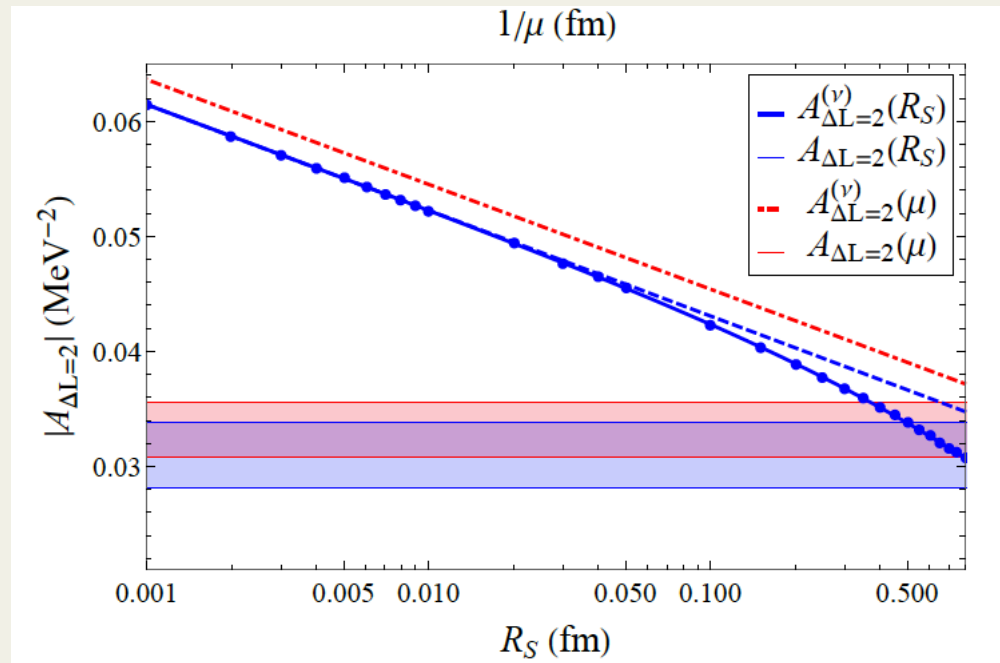
$$C_1 \left(\bar{N} Q_L N \bar{N} Q_L N - \frac{\text{Tr}[Q_L^2]}{6} \bar{N} \vec{\tau} N \cdot \bar{N} \vec{\tau} N + L \leftrightarrow R \right) \quad Q_{L,R} = u^\dagger Q_{L,R} u$$

$$C_2 \left(\bar{N} Q_L N \bar{N} Q_R N - \frac{\text{Tr}[Q_L Q_R]}{6} \bar{N} \vec{\tau} N \cdot \bar{N} \vec{\tau} N + L \leftrightarrow R \right)$$

- Fit to the CIB data gives us $C_1 + C_2$ for each value of regulator**
- for neutrinoless double beta we need $g_v^{NN} = C_2$
- For now we assume $C_1 = C_2$ but this gives an **undetermined error**

Partial success

- Recalculate amplitude with modified neutrino potential including CT



Cirigliano et al, PRL '18

- Total amplitude is regulator independent: **data-driven !**
- For regulators $R_S \sim (0.3-0.8)$ fm ($\Lambda \sim 0.4 - 1$ GeV) about 20-30% corrections (**but based on $C_1=C_2$!!**)
- The effect is amplified in $\Delta I=2$ transitions

Ab initio calculations of light nuclei

- We study neutrinoless double beta decay in light nuclei Pastore et al, PRC '17
 ${}^6\text{He} \rightarrow {}^6\text{Be} + e + e$ ${}^{12}\text{Be} \rightarrow {}^{12}\text{C} + e + e$
- Wave functions from QMC calculations with chiral potential Piarulli et al, PRC '14
- The CIB counter term extracted from potential $\rightarrow g_v^{NN} = C_{CIB}$
- **Study impact of short-range versus long-range neutrino potential**

Dimensionless NME	Long range	Short range
${}^6\text{He} \rightarrow {}^6\text{Be} + e + e$	7.8	1.2
${}^{12}\text{Be} \rightarrow {}^{12}\text{C} + e + e$	0.7	0.55

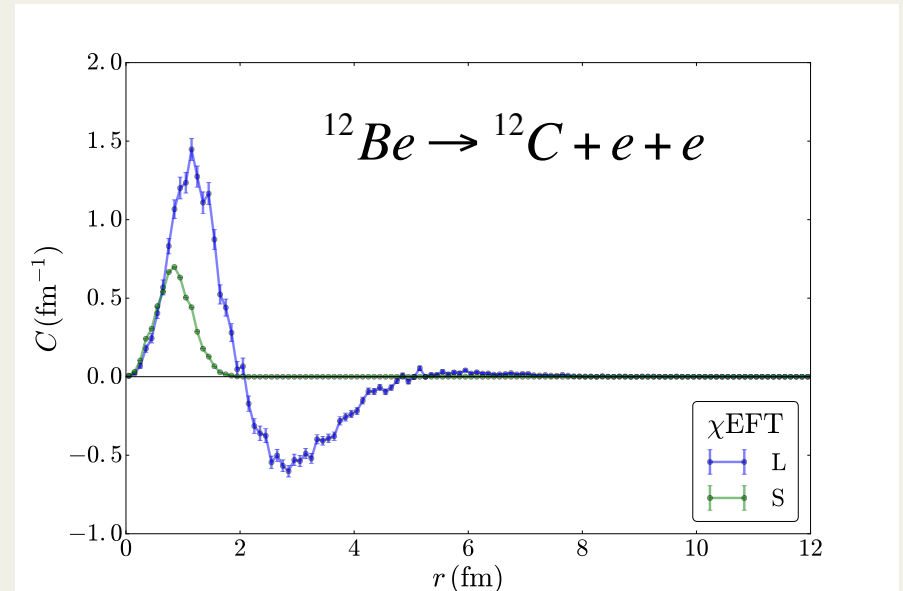
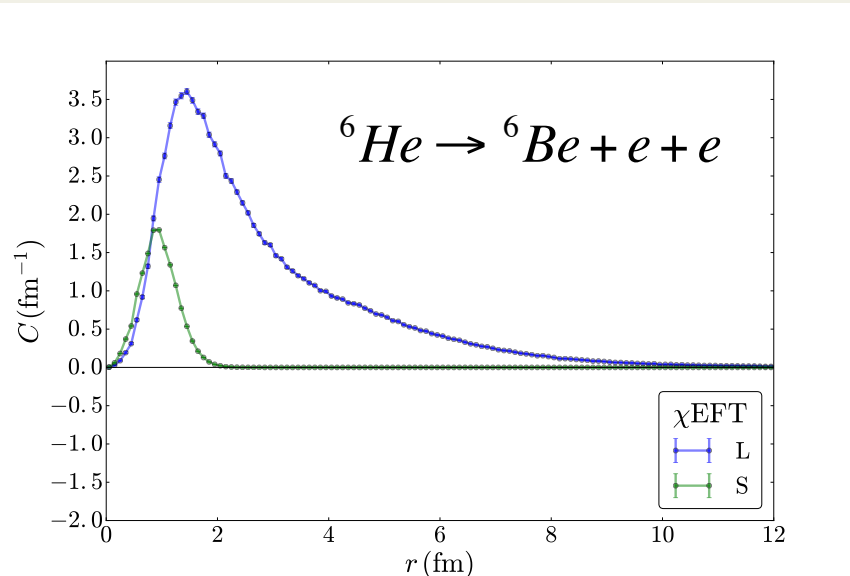
- **Confirms that new CT is bigger than N²LO**
- In both cases significant but relatively much bigger for ${}^{12}\text{Be}$
- We checked that other corrections are really N²LO (few percent level)

Ab initio calculations of light nuclei

$$A_v = \int dr C(r)$$

$$C(r) = C_{Long}(r) + C_{Short}(r)$$

Cirigliano et al, in prep



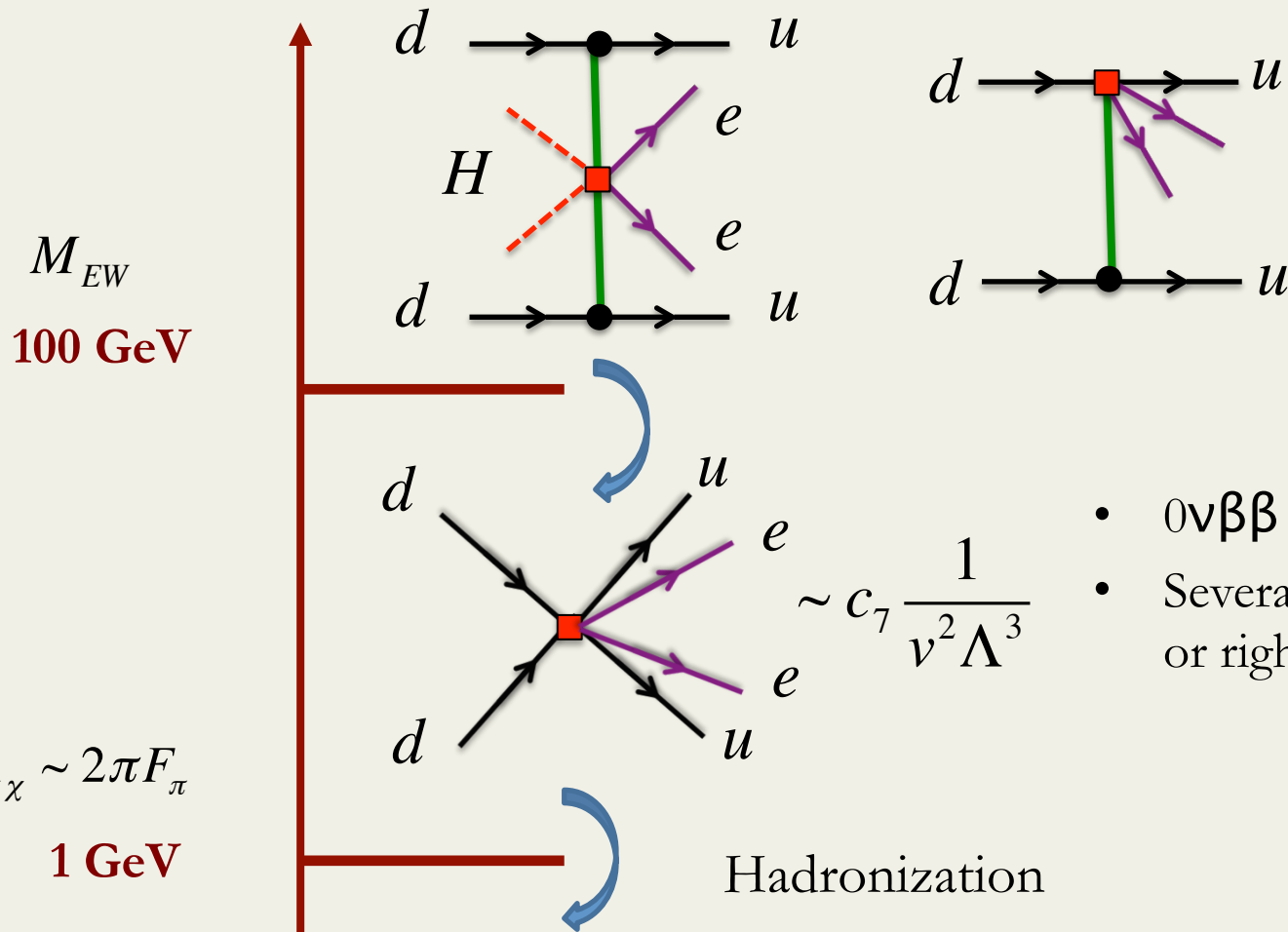
- $\Delta I=2$ transitions: orthogonal initial and final-state wave functions
- Feature of all isotopes of experimental interest
- Node causes cancellation in the long-range matrix elements
- **All together: Strong evidence for significance of g_v^{NN}**

Neutrinoless double beta decay in EFT

- **Part I:** What is neutrinoless double beta decay and why bother?

- **Part II:** An effective field theory approach: SM-EFT + chiral EFT
 1. Light Majorana mass (the Weinberg operator)
 2. Non-perturbative renormalization
 3. **Higher-dimensional lepton number violation**

Crossing the electroweak scale



- $0\nu\beta\beta$ operators \sim 'dim 9'
- Several operators with left- and/or right-handed quarks

- Difficult as similar operators not in 'standard' beta decay

Chiral effective field theory

$\sim \text{GeV}$ $L = L_{QCD} + L_{Fermi} - m_{\beta\beta} \nu_L^T C \nu_L + C_{\Gamma} \bar{e} \Gamma \bar{\nu}^T O_{2q}^{\Gamma} + C_{\Gamma'} \bar{e} \Gamma' e^c O_{4q}^{\Gamma'}$

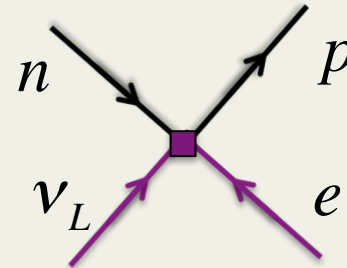
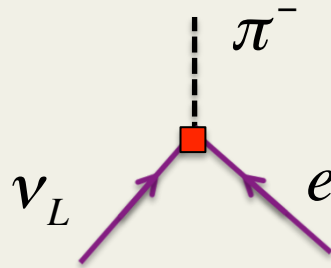
$\sim 100 \text{ MeV}$ Neutrinos are still degrees of freedom in the low-energy EFT

$\Delta L=2$ Majorana mass

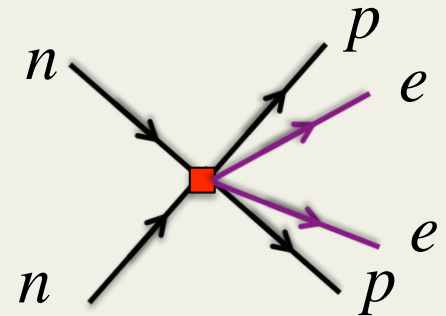
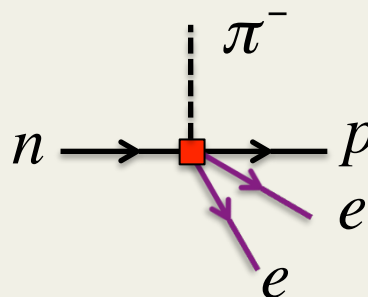
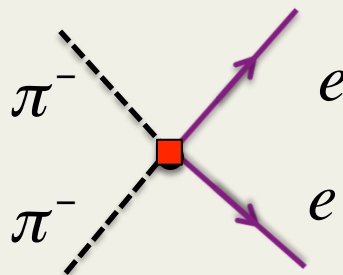
$$\nu_L \longleftrightarrow \nu_L \sim m_{\beta\beta}$$

Prezeau et al '03
JdV et al '17 '18

$\Delta L=2$ beta decay

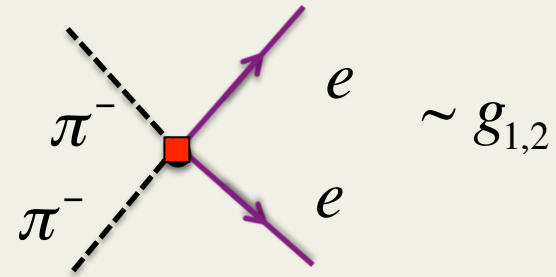


$\Delta L=2$
'neutrinoless'



Higher-dimensional LNV sources

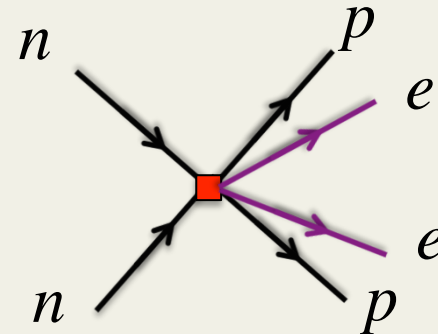
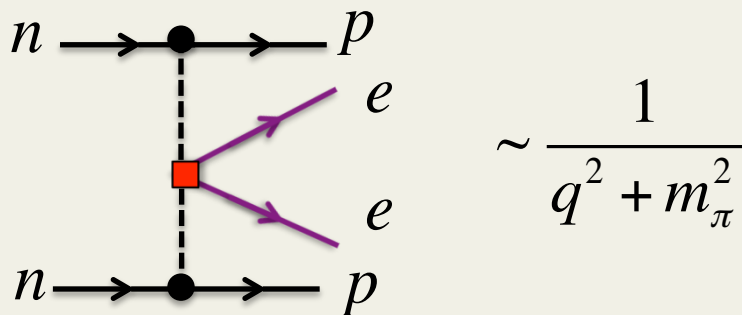
- Certain dim-7 and dim-9 LNV operators lead to
- Quite some nice lattice progress Nicholson et al '18



$$L_{\Delta L=2}^{(9)} = \left\{ C_1^{(9)} \bar{u}_L \gamma^\mu d_L \bar{u}_L \gamma^\mu d_L + C_4^{(9)} \bar{u}_L \gamma^\mu d_L \bar{u}_R \gamma^\mu d_R \right\} \frac{\bar{e}_L e_L^c}{v^5}$$

$$g_1 = -(1.9 \pm 0.2) \text{ GeV}^2 \quad g_2 = -(8 \pm 0.6) \text{ GeV}^2$$

- In Weinberg Counting the LO neutrino potential becomes



- Same UV behaviour as light-neutrino exchange \rightarrow Need a LO counter term
- But in many cases the LECs were poorly known anyway

Higher-dimensional LNV sources

• Ce

• Qu

$L_{\Delta L}^{(9)}$

• In

n

n -

• Sar

$n \rightarrow p e \nu, \pi \rightarrow e \nu$			$\pi \pi \rightarrow e e$		
g_A	1.271 ± 0.002	[58]	$g_1^{\pi\pi}$	0.36 ± 0.02	[44]
g_S	0.97 ± 0.13	[59]	$g_2^{\pi\pi}$	$2.0 \pm 0.2 \text{ GeV}^2$	[44]
g_M	4.7	[58]	$g_3^{\pi\pi}$	$-(0.62 \pm 0.06) \text{ GeV}^2$	[44]
g_T	0.99 ± 0.06	[59]	$g_4^{\pi\pi}$	$-(1.9 \pm 0.2) \text{ GeV}^2$	[44]
$ g'_T $	$\mathcal{O}(1)$		$g_5^{\pi\pi}$	$-(8.0 \pm 0.6) \text{ GeV}^2$	[44]
B	2.7 GeV		$ g_T^{\pi\pi} $	$\mathcal{O}(1)$	
$n \rightarrow p \pi e e$			$nn \rightarrow pp e e$		
$ g_1^{\pi N} $	$\mathcal{O}(1)$		$ g_1^{NN} $	$\mathcal{O}(1)$	
$ g_{6,7,8,9}^{\pi N} $	$\mathcal{O}(1)$		$ g_{6,7}^{NN} $	$\mathcal{O}(1)$	
$ g_{VL}^{\pi N} $	$\mathcal{O}(1)$		$ g_{VL}^{NN} $	$\mathcal{O}(1)$	
$ g_T^{\pi N} $	$\mathcal{O}(1)$		$ g_T^{NN} $	$\mathcal{O}(1)$	
			$ g_\nu^{NN} $	$\mathcal{O}(1/F_\pi^2)$	
			$ g_{VL,VR}^{E,m_e} $	$\mathcal{O}(1)$	
			$ g_{2,3,4,5}^{NN} $	$\mathcal{O}((4\pi)^2)$	

2

$\sim g_{1,2}$

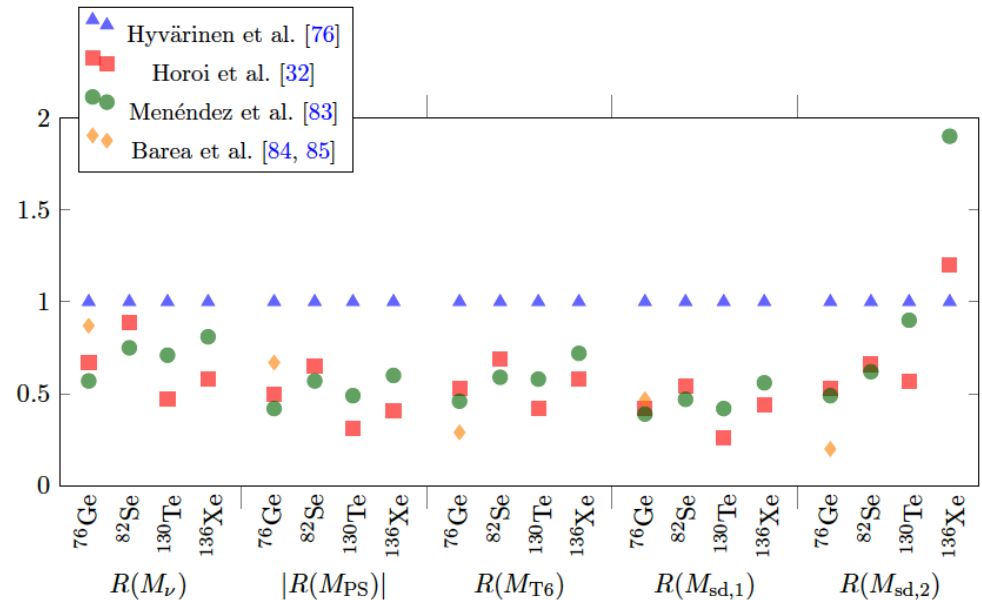
inter term

• But in many cases the LECs were poorly known anyway

Many-body uncertainties for SM-EFT

- At LO we require 9 combinations of NMEs (much less than normally calculated)
- All required NMEs can be lifted from existing literature
- **Uncertainties similar to standard scenario**
- Use chiral symmetry arguments for consistency checks

NMEs	⁷⁶ Ge				Hyvarinen/Suhonen '15 Menendez et al '17 '18 Barea et al '15 '18 Horoi/Neacsu '17																																											
	[74]	[31]	[81]	[82,83]																																												
M_F	-1.74	-0.67	-0.59	-0.68																																												
M_{GT}^{AA}	5.48	3.50	3.15	5.06																																												
M_{GT}^{AP}	-2.02	-0.25	-0.94	<table><tr><th>NMEs</th><th colspan="4">⁷⁶Ge</th></tr><tr><td>-</td><td></td><td></td><td></td><td></td></tr><tr><td>$M_{F, sd}$</td><td>-3.46</td><td>-1.55</td><td>-1.46</td><td>-1.1</td></tr><tr><td>$M_{GT, sd}^{AA}$</td><td>11.1</td><td>4.03</td><td>4.87</td><td>3.62</td></tr><tr><td>$M_{GT, sd}^{AP}$</td><td>-5.35</td><td>-2.37</td><td>-2.26</td><td>-1.37</td></tr><tr><td>$M_{GT, sd}^{PP}$</td><td>1.99</td><td>0.85</td><td>0.82</td><td>0.42</td></tr><tr><td>$M_{T, sd}^{AP}$</td><td>-0.85</td><td>0.01</td><td>-0.05</td><td>-0.97</td></tr><tr><td>$M_{T, sd}^{PP}$</td><td>0.32</td><td>0.00</td><td>0.02</td><td>0.38</td></tr></table>	NMEs	⁷⁶ Ge				-					$M_{F, sd}$	-3.46	-1.55	-1.46	-1.1	$M_{GT, sd}^{AA}$	11.1	4.03	4.87	3.62	$M_{GT, sd}^{AP}$	-5.35	-2.37	-2.26	-1.37	$M_{GT, sd}^{PP}$	1.99	0.85	0.82	0.42	$M_{T, sd}^{AP}$	-0.85	0.01	-0.05	-0.97	$M_{T, sd}^{PP}$	0.32	0.00	0.02	0.38				
NMEs	⁷⁶ Ge																																															
-																																																
$M_{F, sd}$	-3.46	-1.55	-1.46		-1.1																																											
$M_{GT, sd}^{AA}$	11.1	4.03	4.87		3.62																																											
$M_{GT, sd}^{AP}$	-5.35	-2.37	-2.26		-1.37																																											
$M_{GT, sd}^{PP}$	1.99	0.85	0.82		0.42																																											
$M_{T, sd}^{AP}$	-0.85	0.01	-0.05	-0.97																																												
$M_{T, sd}^{PP}$	0.32	0.00	0.02	0.38																																												
M_{GT}^{PP}	0.66	0.33	0.30																																													
M_{GT}^{MM}	0.51	0.25	0.22																																													
M_T^{AA}	—	—	—																																													
M_T^{AP}	-0.35	0.01	-0.01																																													
M_T^{PP}	0.10	0.00	0.00																																													
M_T^{MM}	-0.04	0.00	0.00																																													



Redundancies

$$H_{GTN} = \frac{2R}{\pi m_e m_p} \int h_A^2(q^2) j_0(qr) q^2 dq, \quad (20d)$$

$$H_{GT'} = \frac{2R^2}{\pi m_p} \int \frac{q^2 h_A^2(q^2)}{q(q + \bar{E})} j_0(qr) q^2 dq, \quad (20e)$$

$$H_{GT''} = \frac{2R^3}{\pi m_p} \int \frac{q^2 h_A^2(q^2)}{q + \bar{E}} j_0(qr) q^2 dq, \quad (20f)$$

$$H_{GT\pi\nu} = \frac{2R}{\pi} \int \frac{h_{GT\pi\nu}^2(q^2)}{q(q + \bar{E})} j_0(qr) q^2 dq, \quad (20g)$$

$$H_{GT1\pi} = -\frac{2R}{\pi} \int h_A^2(q^2) \frac{q^2/m_\pi^4}{1 + q^2/m_\pi^2} j_0(qr) q^2 dq, \quad (20h)$$

$$H_{GT2\pi} = -\frac{4R}{\pi} \int h_A^2(q^2) \frac{q^2/m_\pi^4}{(1 + q^2/m_\pi^2)^2} j_0(qr) q^2 dq, \quad (20i)$$

$$H_F = \frac{2R}{\pi} \int \frac{h_V^2(q^2)}{q(q + \bar{E})} j_0(qr) q^2 dq, \quad (20j)$$

$$H_{F\omega} = \frac{2R}{\pi} \int \frac{h_V^2(q^2)}{(q + \bar{E})^2} j_0(qr) q^2 dq, \quad (20k)$$

$$H_{Fq} = \frac{2R}{\pi} r \int \frac{h_V^2(q^2)}{q + \bar{E}} j_1(qr) q^2 dq, \quad (20l)$$

$$H_{FN} = \frac{2R}{\pi m_e m_p} \int h_V^2(q^2) j_0(qr) q^2 dq, \quad (20m)$$

$$H_{F'} = \frac{2R^2}{\pi m_p} \int \frac{q^2 h_V^2(q^2)}{q(q + \bar{E})} j_0(qr) q^2 dq, \quad (20n)$$

$$H_T = -\frac{2R}{\pi} \int \frac{h_T^2(q^2)}{q(q + \bar{E})} j_2(qr) q^2 dq, \quad (20o)$$

$$H_{Tq} = \frac{2R}{3\pi} \sqrt{\frac{2}{3}} r C^{(2)}(\hat{r}) \int \frac{h_A^2(q^2)}{q + \bar{E}} j_1(qr) q^2 dq, \quad (20p)$$

$$H_{T'} = -\frac{2R^2}{\pi m_p} \int \frac{q^2 h_A^2(q^2)}{q(q + \bar{E})} j_2(qr) q^2 dq, \quad (20q)$$

$$H_{T''} = -\frac{2R^3}{\pi m_p} \int \frac{q^2 h_A^2(q^2)}{q + \bar{E}} j_2(qr) q^2 dq, \quad (20r)$$

$$H_{T\pi\nu} = -\frac{2R}{\pi} \int \frac{h_{T\pi\nu}^2(q^2)}{q(q + \bar{E})} j_2(qr) q^2 dq, \quad (20s)$$

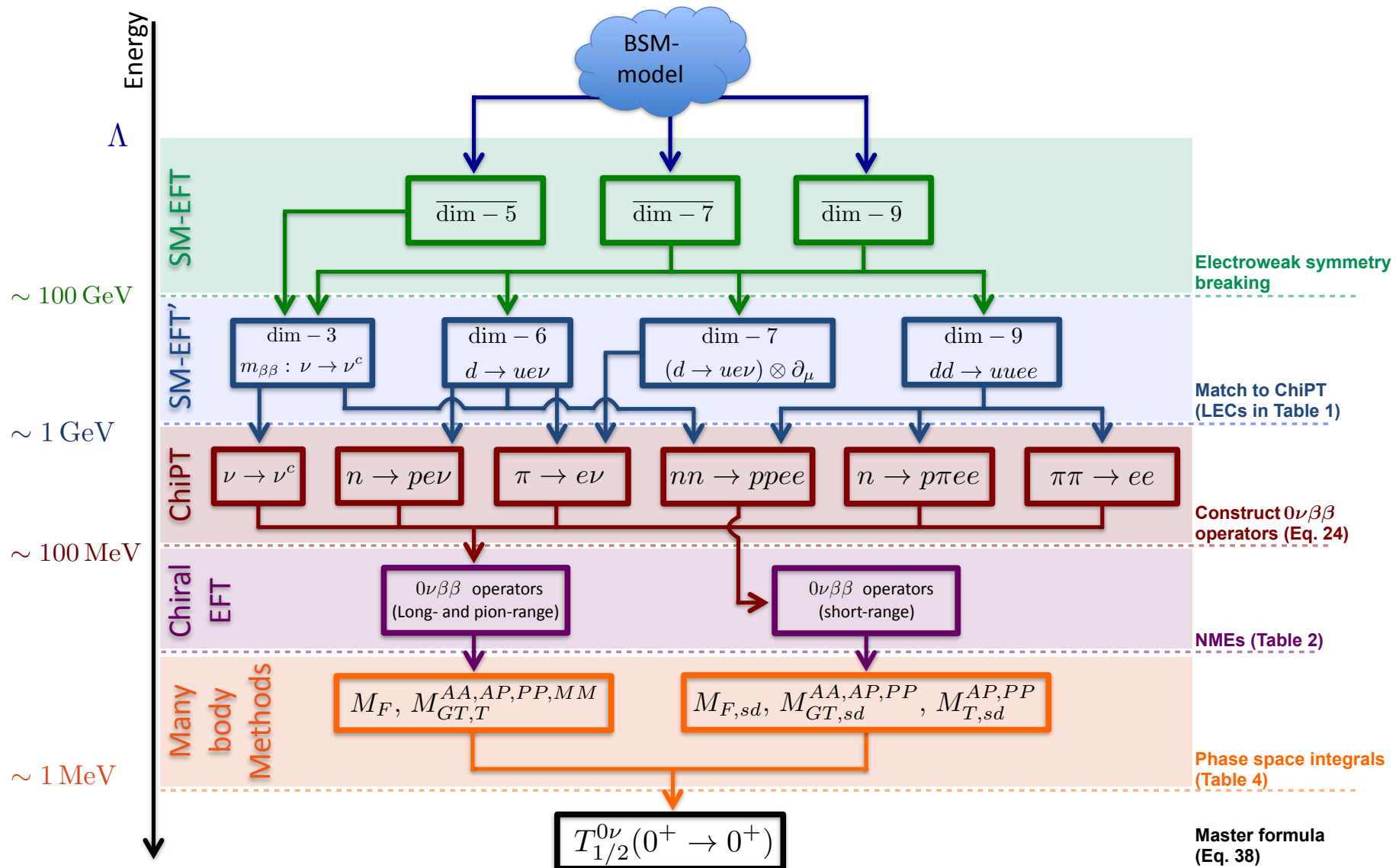
$$H_{T1\pi} = \frac{2R}{\pi} \int h_A^2(q^2) \frac{q^2/m_\pi^4}{1 + q^2/m_\pi^2} j_2(qr) q^2 dq, \quad (20t)$$

- The dozens of NMEs calculated only differ by **partial** N2LO corrections
- Many are redundant at LO !
- EFT predicts LO relations between NMEs

$$\begin{aligned} M_{GT, sd}^{PP} &= -\frac{1}{2} M_{GT, sd}^{AP} - M_{GT}^{PP}, & M_{T, sd}^{PP} &= -\frac{1}{2} M_{T, sd}^{AP} - M_T^{PP}, \\ M_{GT, sd}^{AP} &= -\frac{2}{3} M_{GT, sd}^{AA} - M_{GT}^{AP}, & M_{GT}^{MM} &= \frac{g_M^2 m_\pi^2}{6 g_A^2 m_N^2} M_{GT, sd}^{AA}, \end{aligned}$$

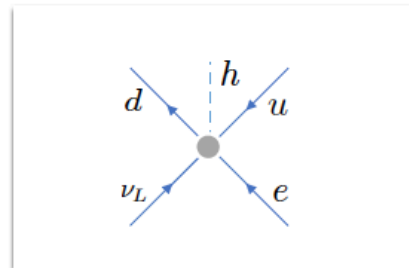
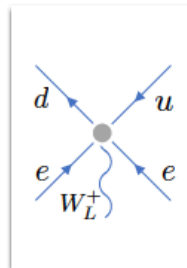
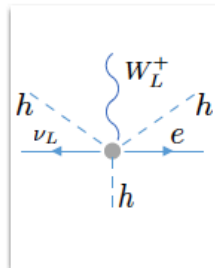
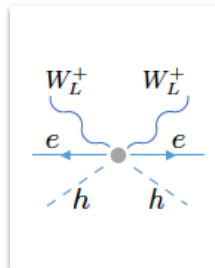
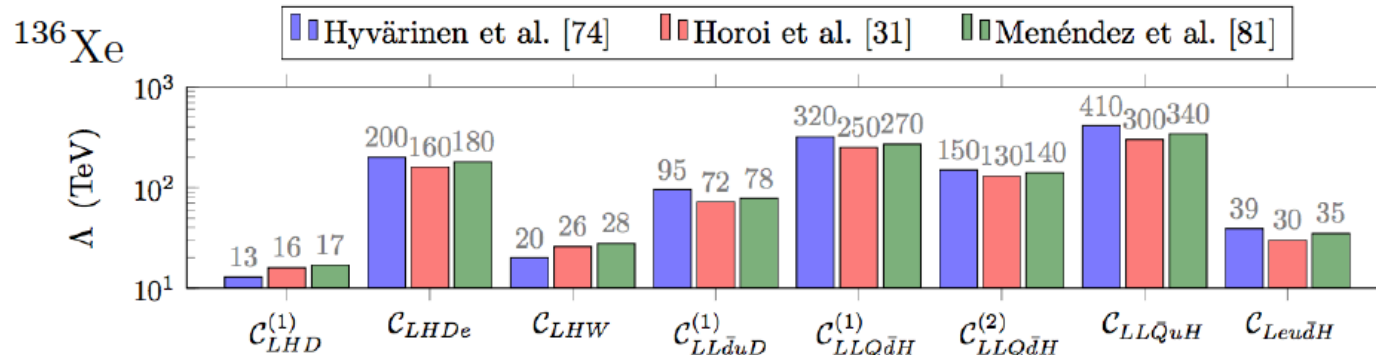
- **Hold up to 10% corrections for different many-body methods !**
- Used to find sign/factor 2 mistakes in literature

'The neutrinoless double-beta metro map'



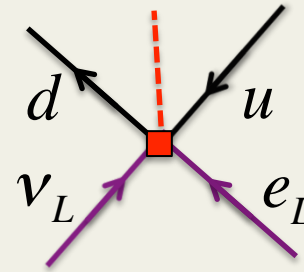
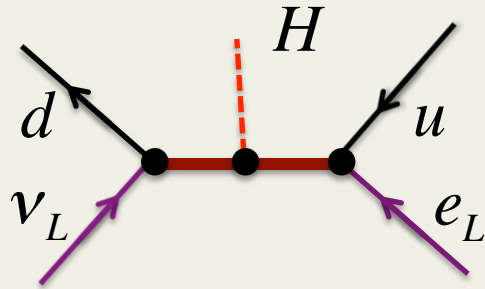
Limits on LNV sources

- We have now connected TeV LNV sources to low-energy data
- KAMLAND experiment** $T_{1/2}^{0\nu} \left({}^{136}\text{Xe} \rightarrow {}^{136}\text{Ba} \right) > 1.07 \times 10^{26} \text{ yr}$
- Limit LNV sources: dim5 $m_{\beta\beta} < 0.084 \text{ eV}$
- And also dim7 (or dim9) : assume $C_i \sim (v / \Lambda)^3$



Phenomenology

- Particular dimension-7 operator e.g. appearing in LeptoQuark models

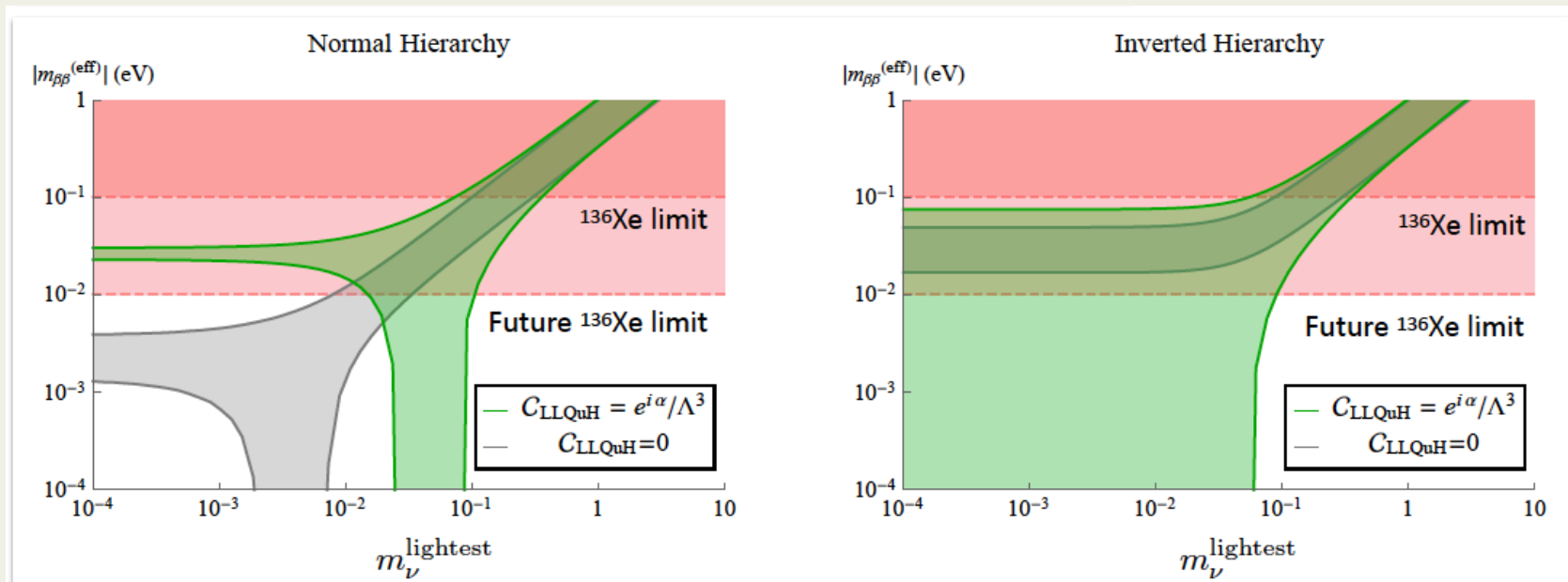


$$C_7 \sim (v / \Lambda)^3$$

$$\Lambda > 400 \text{ TeV}$$

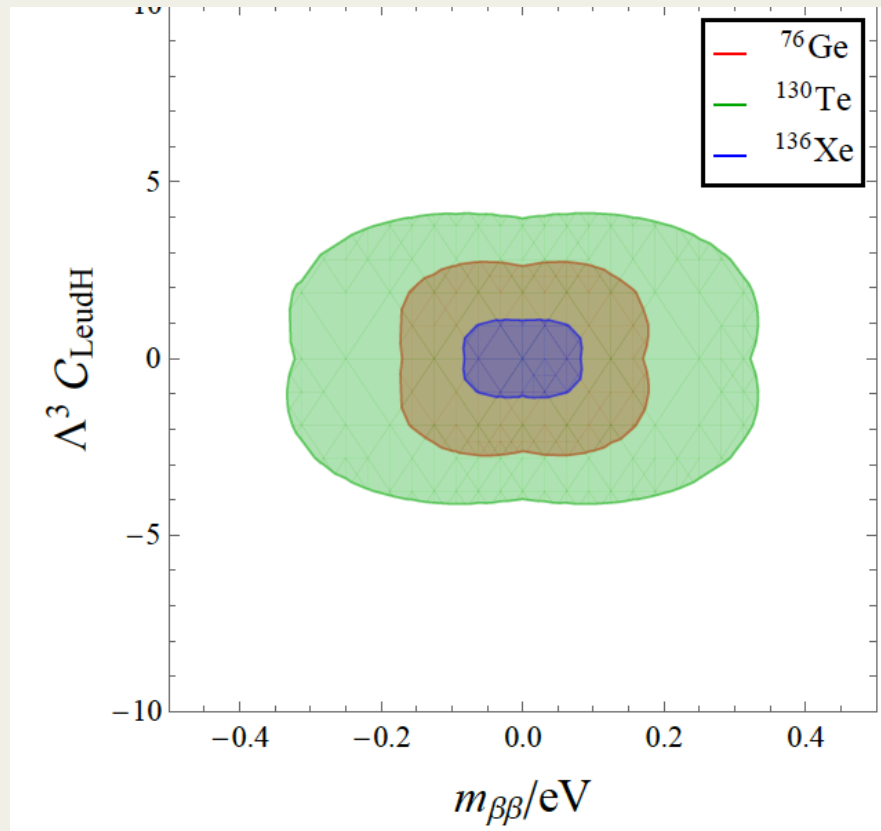
$$\Lambda_{LHC} > 5 \text{ TeV}$$

- Operator has **same ‘leptonic’** structure as ‘standard Majorana mechanism’
- Interference with Majorana mass: **interpretation needs care**



Disentangling LNV sources

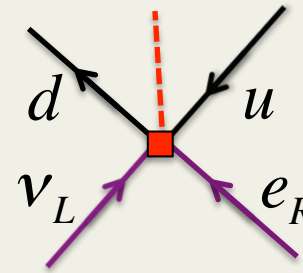
- A single measurement can be from any LNV operator
- Need several measurements to unravel the source
- However, total rates in different isotopes not very helpful....
- Similar Q values and all $0^+ \rightarrow 0^+$



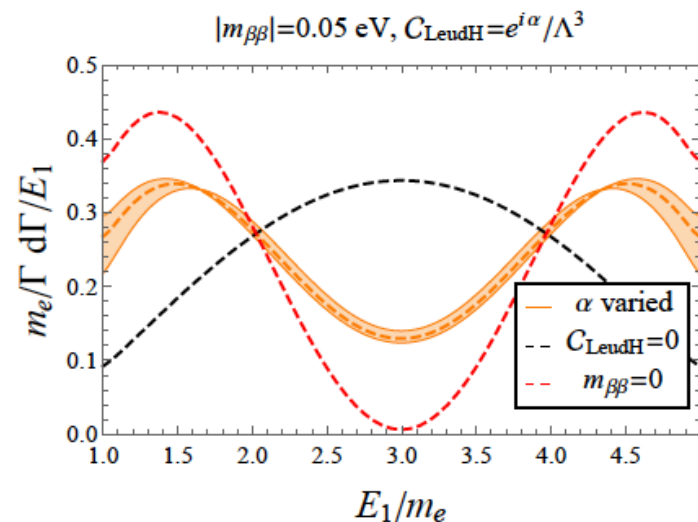
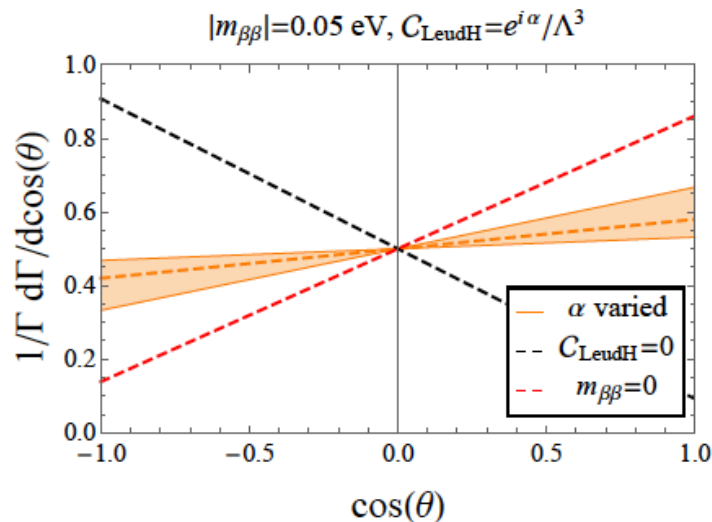
Disentangling LNV sources

- A single measurement can be from any LNV operator
- Need several measurements to unravel the source
- Instead: **angular & energy** distributions of the outgoing electrons

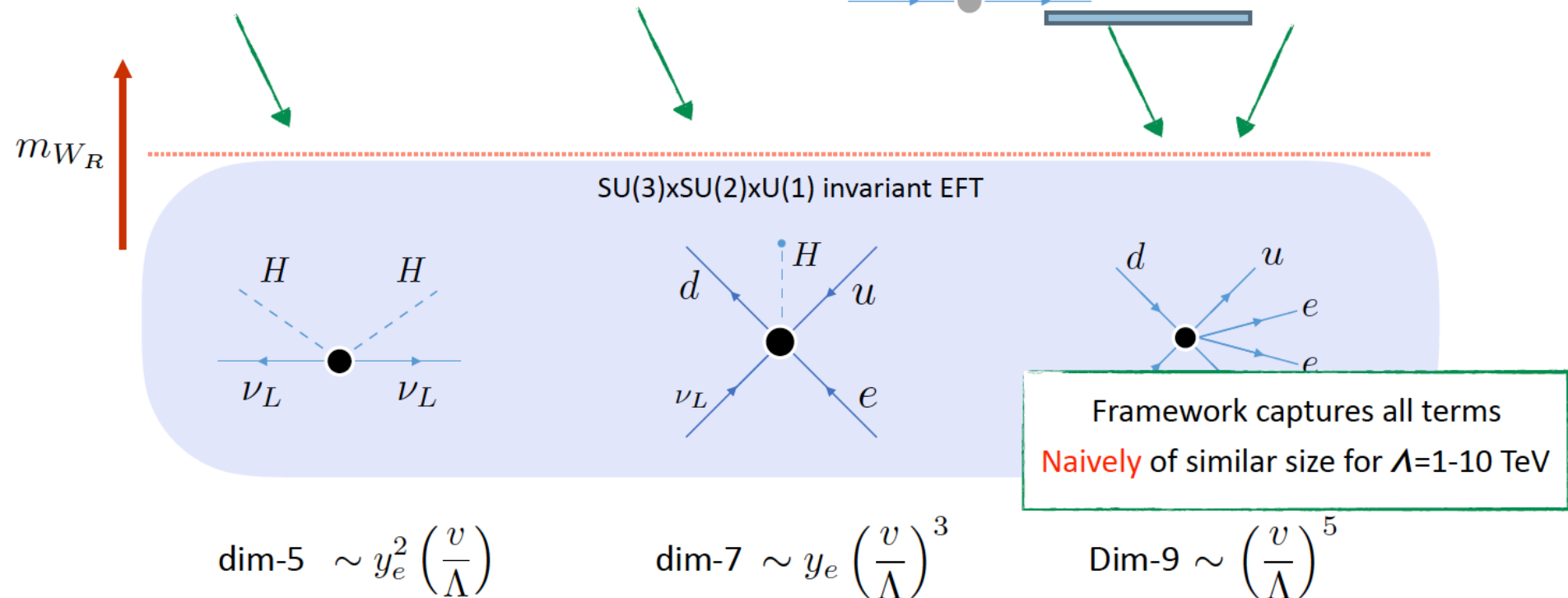
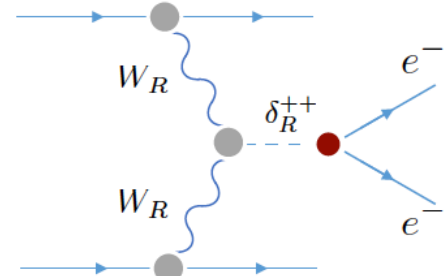
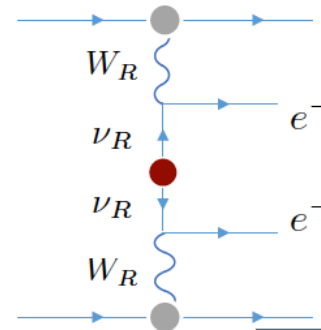
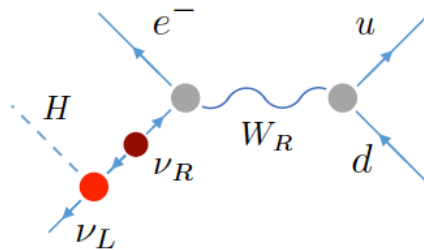
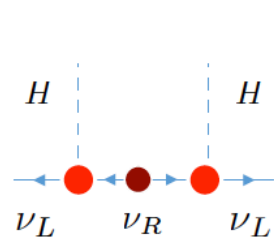
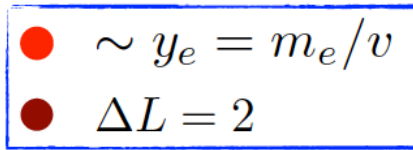
$$\nu_L \longleftrightarrow \nu_L$$



$$C_7 \sim (v / \Lambda)^3 e^{i\alpha}$$



An example: LR model



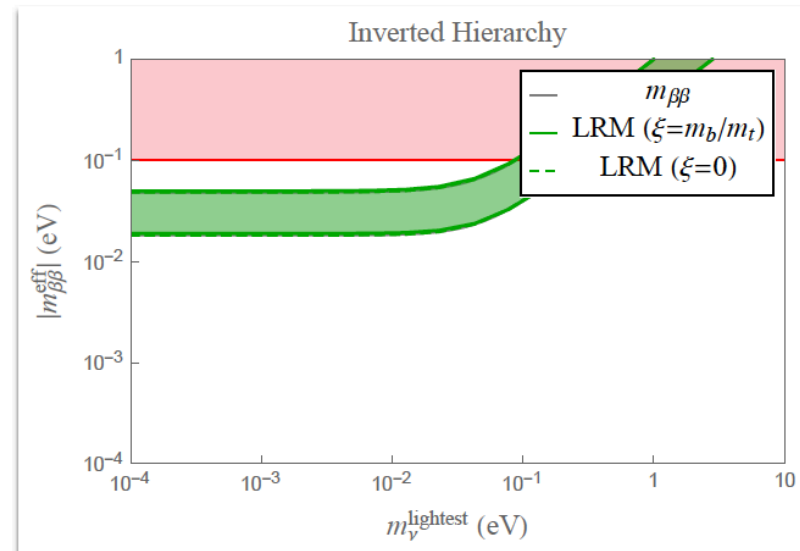
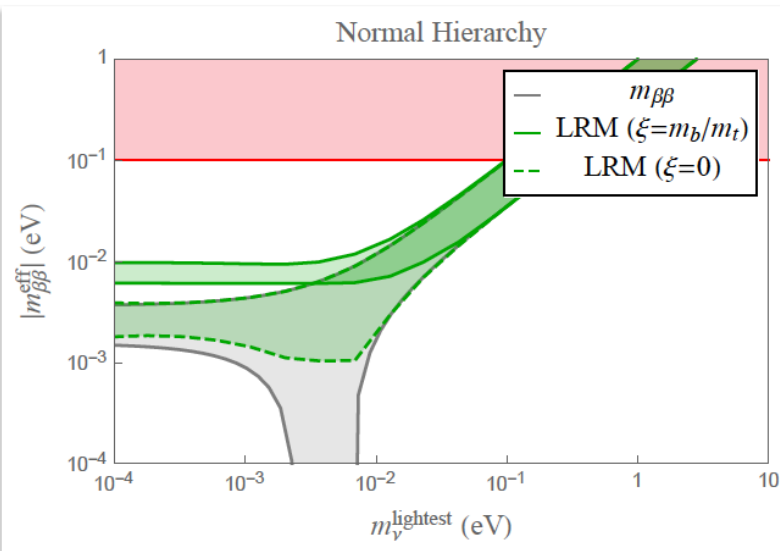
Matching to specific models

- In principle difficult phenomenology.
- **But just match to SM-EFT operators and then turn the crank**
- Obtain the neutrinoless double beta decay rate in an EFT expansion in:

$$T \sim \left(\frac{v}{\Lambda} \right)^\alpha \left(\frac{\Lambda_\chi}{v} \right)^\beta \left(\frac{m_\pi}{\Lambda_\chi} \right)^\gamma$$

$$m_{W_R} = 4.5 \text{ TeV}, \quad m_{\nu_R} = 10 \text{ TeV}, \quad m_{\delta_R^{++}} = 4 \text{ TeV}$$

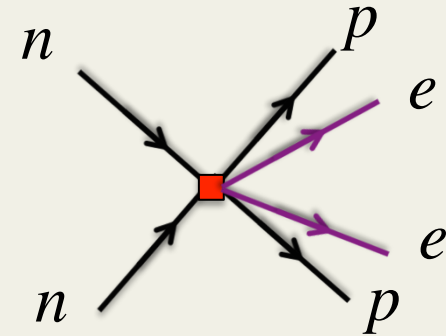
- Assume right-handed neutrino mixing follows the PMNS matrix



Conclusion/Summary

Neutrinoless Double Beta Decay

- ✓ Powerful search for BSM physics (probe high scales)
- ✓ Well motivated in order to probe nature of neutrino masses
- ✓ **However, complicated low-energy observable**



Standard Model EFT and chiral EFT frameworks

- ✓ Keep track of **symmetries** (gauge/lepton#/chiral) from TeV to nuclear scales
- ✓ Chiral EFT to organize neutrino potential in systematic fashion
- **Main result: a LO contact $nn \rightarrow pp + ee$ operator must be added**

Phenomenology

- ✓ Current experiments set very strong limits (>500 TeV in some cases)
- ✓ Differential measurements can disentangle certain sources
- ✓ **Master formula to include all contributions up to dim-9**
- ✓ **Future: add light extra neutrino states + link to LHC + LG**

