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# GENIE: Neutrino Interaction Modeling and Tuning

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Pittsburgh) —

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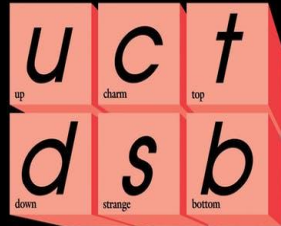
# Outline

- Introductions to Neutrinos, Neutrino Interactions/Oscillations
- Why simulation?
- What is GENIE?
  - How does GENIE work
  - How does GENIE simulate neutrino interactions
- Models used in GENIE
  - Nuclear model, cross section model, final interaction model
- Comparing and Tuning against experimental data
- Summary

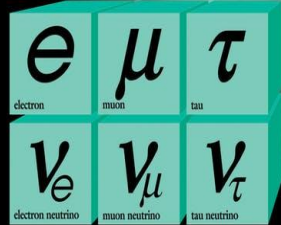


# Introduction to Neutrinos

## Quarks



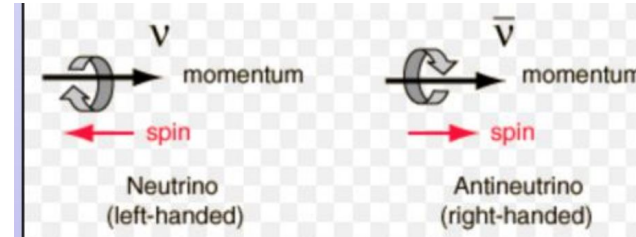
## Forces



## Leptons

Standard Model Assumes that:

- Neutrinos are massless and chargeless particles
- No strong/electromagnetic interactions



- Observation on contemporary experiments (neutrino oscillation) shows the neutrinos are **massive**
  - standard model needs to be extended
  - One of the frontiers of the standard model investigations

# Introduction to Neutrinos: Oscillations

- Neutrino flavor states  $\nu_\alpha$  and mass eigenstates  $\nu_i$  are related by Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix

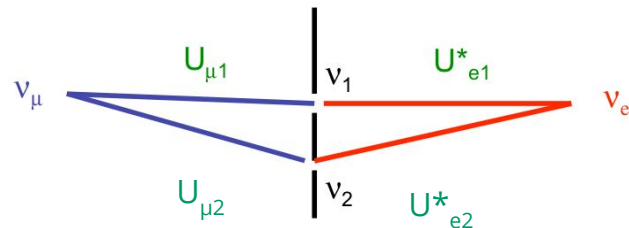
$$|\nu_\alpha\rangle = \sum_i U_{\alpha i} |\nu_i\rangle \quad i = 1, 2, 3 \quad \alpha = e, \mu, \tau$$

Two flavor model:

$$\begin{pmatrix} \nu_\alpha \\ \nu_\beta \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \cdot \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

:  $\theta$  is the mixing angle.

**Oscillation:** Given an initial flavor  $\nu_\alpha$ , observation some time later will yield a combination of  $\nu_\alpha$  and  $\nu_\beta$



**Oscillation probability:**

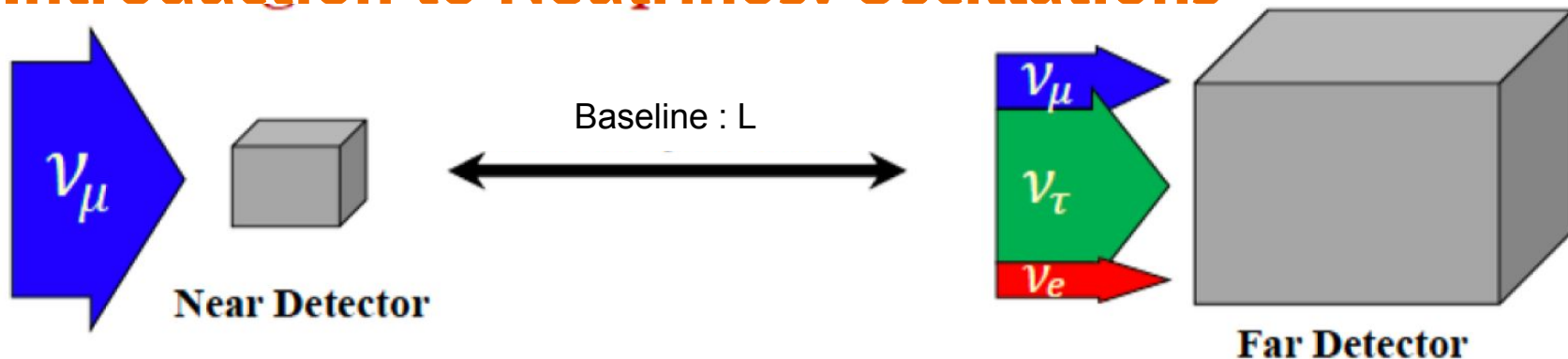
$$P(\nu_\alpha \rightarrow \nu_\beta, t) = \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2}{4E} L \right)$$

**L:** Travel distance/Baseline

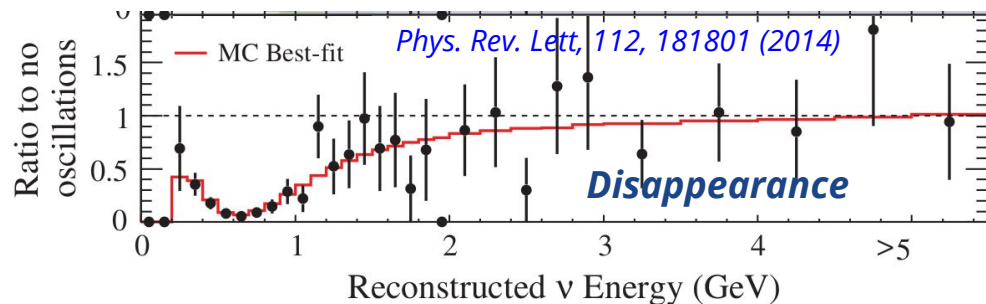
**E:** Neutrino Energy

**$\Delta m^2$ :** Mass split/difference between two different mass eigenstates

# Introduction to Neutrinos: Oscillations



- **Signature of neutrino oscillation** is a distortion of the neutrino spectrum  $E(\nu_\mu)$ 
  - Difference between measured Neutrino spectrum at Far detector and no-oscillation hypothesis
- Two types of oscillation searches
  - **"Appearance"** : Look for appearance of  $\nu_e$  Or  $\nu_\tau$  in a pure  $\nu_\mu$  beam vs L and E
  - **"Disappearance"** : Look for a change in  $\nu_\mu$  flux



**Example:** The ratio of the observed spectrum (points) to the no-oscillation hypothesis, and the best oscillation fit (solid) of T2K in Japan.

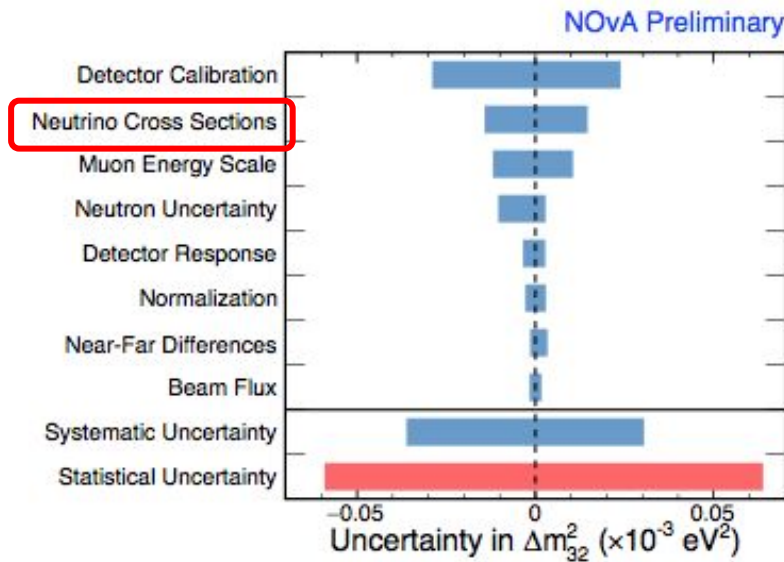
# Introduction to Neutrinos: Oscillations

- Neutrino Energy Spectrum: **Event Rate**  $N(E_\nu)$

- $E_\nu$  is not observable
- Measured through neutrino target interaction from the final states

- $N(E_\nu) = \Phi(E) \times \sigma(E) \times \varepsilon(E)$

- “ $\Phi$ ”: the neutrino flux
- “ $\sigma$ ”: **cross section**
  - a measure of the probability of an interaction occurring
  - Relates neutrino energy to final state observables
  - Source of big uncertainty in oscillation measurement
- $\varepsilon$ : Efficiency



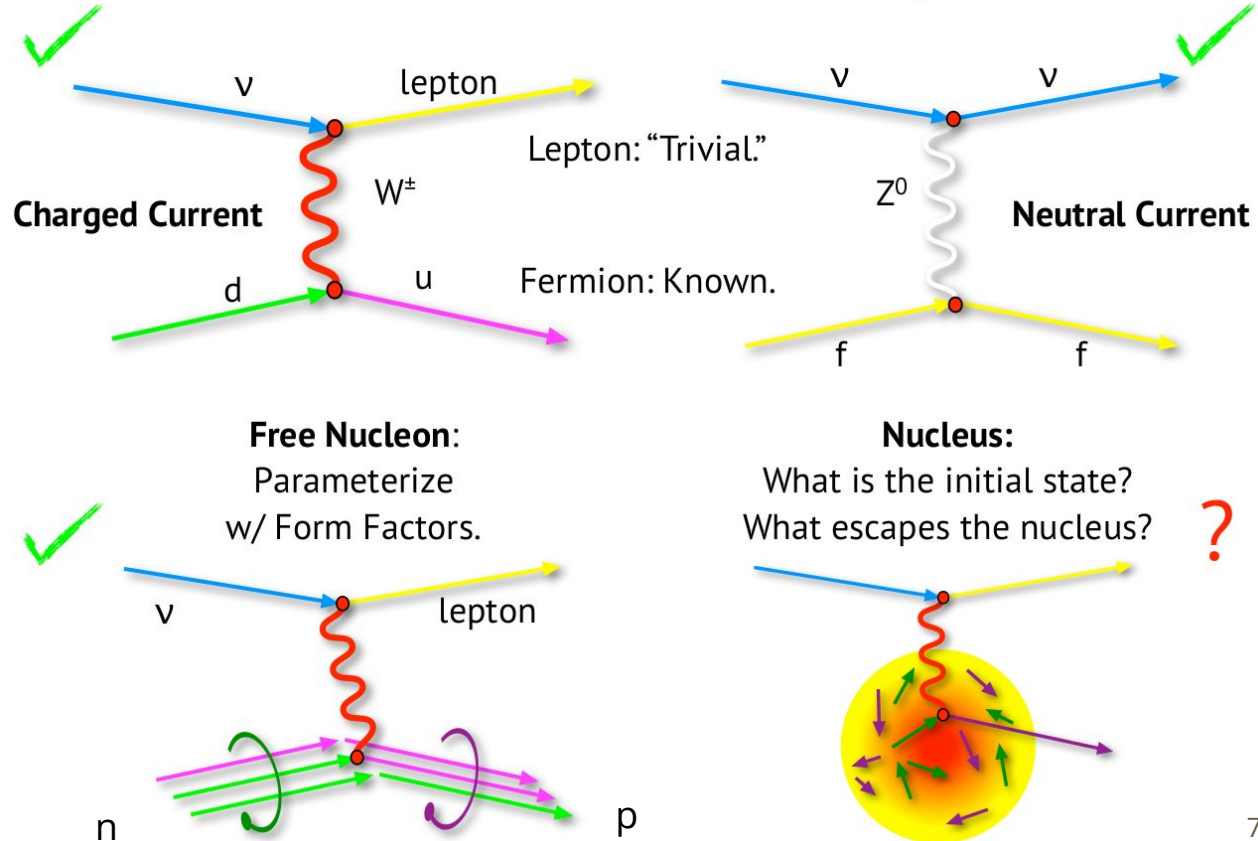
*Alex Himmel's wine&cheese talk, NovA*

- Big uncertainty from neutrino cross section measurement in the oscillation measurement.

# Introduction to Neutrinos: Interactions

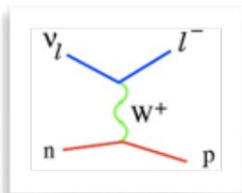
- The charged lepton in the final state identifies neutrino flavor
- Charge of leptons determines  $\nu$  or  $\bar{\nu}$
- Can not determine the flavor in the Neutral Current interactions

## Neutrino Interactions - Weak Force Only!

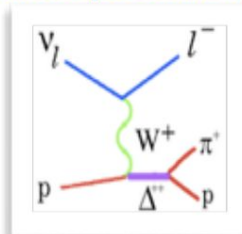


# How does GENIE work? -Cross Section Model

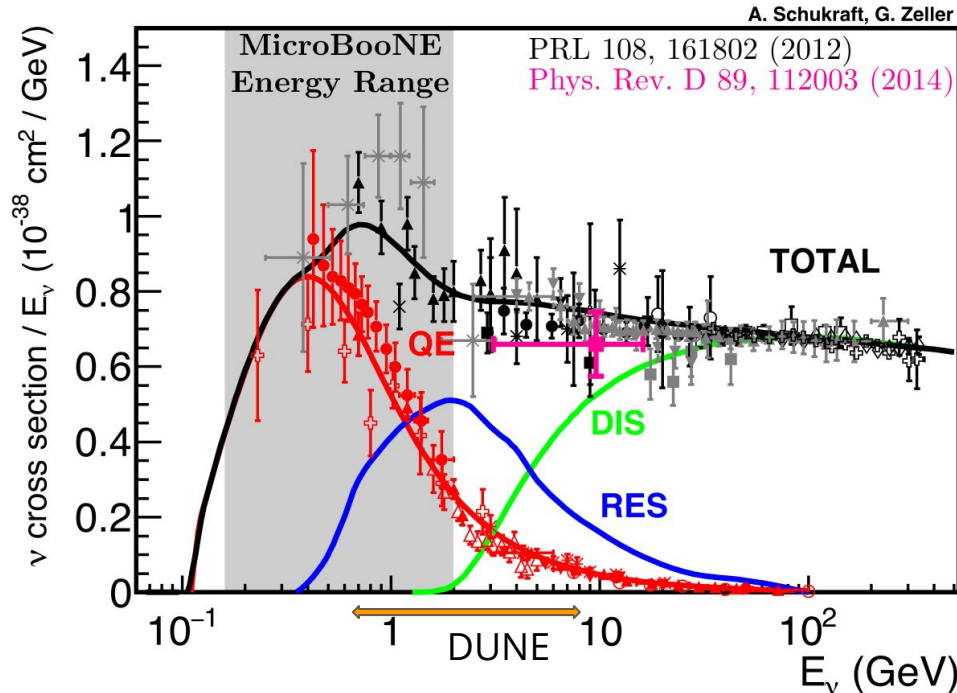
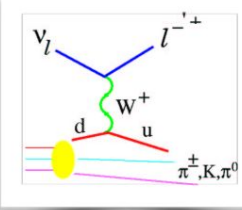
## Quasi-elastic scattering (QE)



## Resonance production (RES)



## Deep Inelastic scattering (DIS)

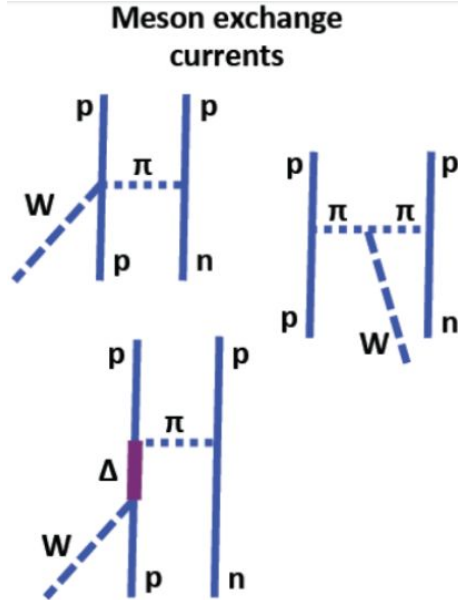


- Figure above shows the cross section distribution scale to neutrino nucleon scattering
- In case of target  $A > 1$  scattering one must consider COH(coherent pion production) and MEC(Meson Exchange Current).

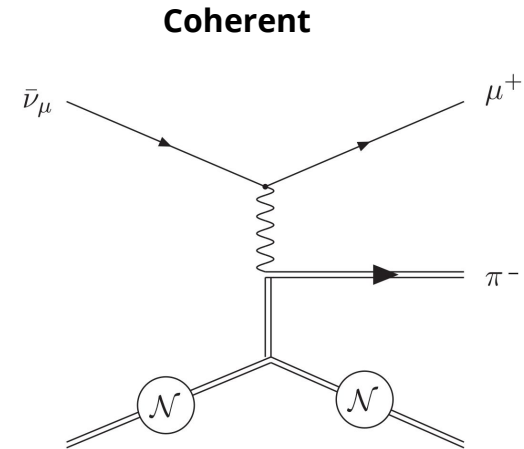


# Introduction to Neutrinos: Other Channels

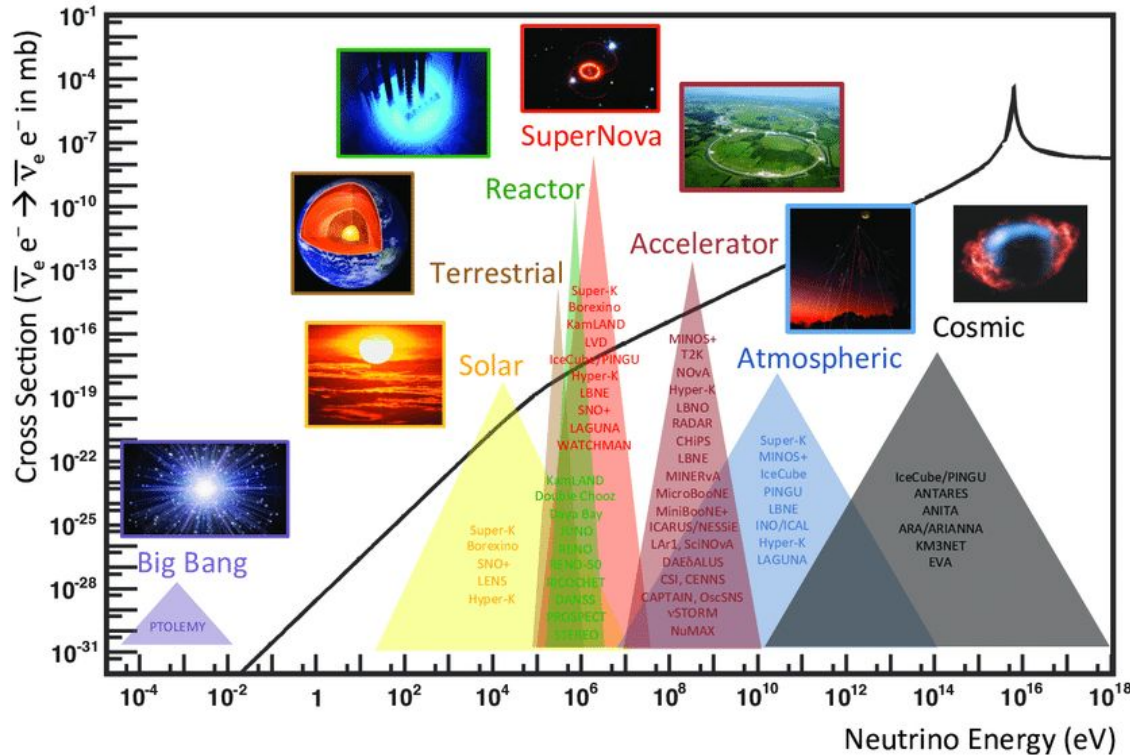
- **Meson Exchange Current (MEC)**
  - **Important background in QE measurements**
  - Many theoretical efforts
  - Need confirmation and further study!



- Due to small cross sections of **coherent** process, not many measurements until now.



# Neutrino Sources & Experiments



**Reactor neutrino experiment:** Daya Bay, Double Chooz, KamLAND, RENO, JUNO

**Solar neutrino experiment:** Borexino, Super-K, SNO

**Atmospheric neutrino experiment:** Super-K, IceCube

**Accelerator neutrino experiment:** NOMAD, Minos, MINERvA, T2K, MiniBooNE, NovA, MicroBooNE



Theory+  
Experiments??  
Why  
Simulation?

# Why Simulation?



- Theoretical models describes the cross sections in  $E_v$ ,  $Q^2$ ,  $W$ , etc
- Detector efficiencies known in particle energies, angles, etc
- A Theory-Experiment Interface → **Simulation**
  - Connect truth and observables
    - Event topologies and kinematics
    - Cross section, nuclear effect
    - Optimal coverage of physical processes
- Good Generators should also be with
  - Systematic uncertainty analysis
  - Tune the physics models against experimental result

Several MC Generators in use: **GENIE**, GiBUU, NuWRO, NEUT ...



# What is GENIE?



- **The software:**
  - **Simulates** a large variety of neutrino interactions
  - **Handles** all neutrinos and targets, and all processes relevant from MeV to PeV energy scales
  - Additionally run in **electron and hadron scattering** models
  - Many tools for studying systematics, comparison to data.
- The event generator used in almost all neutrino experiments.
  - **Interfaces** to HEP software frameworks (LArSoft ...) very well
  - Geometry
  - Reweighting - Propagating uncertainties/Systematic errors
- Needs have greatly increased as experiments become more advanced
  - New channels (**coherent p...**)
  - Improved theoretical models

# Overview of GENIE product

- **Generator** (open source)
  - State-of-the-art software framework
  - **Neutrino interaction + non-neutrino interaction physics module**
    - Nucleon decay, Neutron-antineutron oscillation. Boosted dark matter,
    - Electron/hadron Nucleus scattering
- **Comparisons** (private)
  - State-of-the-art framework and comparison plexus management
  - Vast collection of curated **data archives and implementation of data/MC comparison**
- **Tuning** (private)
  - Implements GENIE tuning strategy
- **Reweight** (open source)
  - **Propagating uncertainties** from parameters (e.g.  $M_A$ ) to any observables (e.g. cross section)

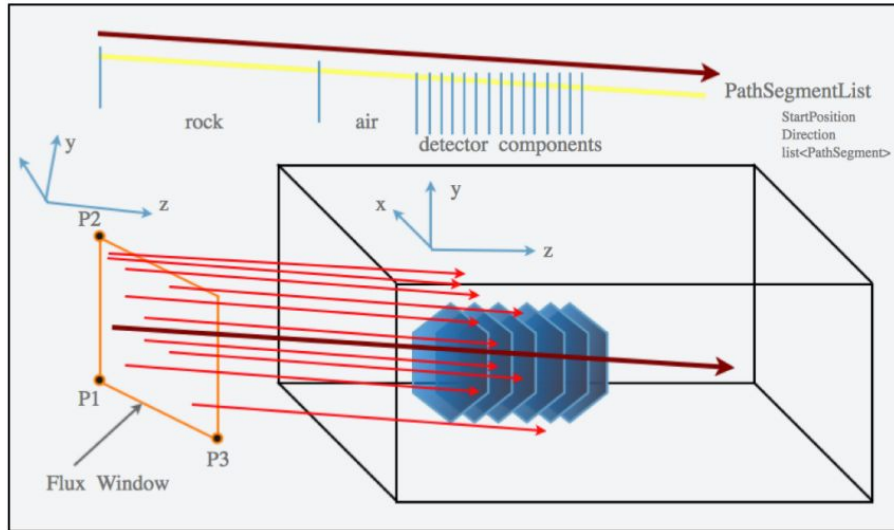
# How does GENIE work? - Flux & Geometry

- Many choices (including making your own):
  - User-specified histograms (no spatial variation, only energy and flavor)
    - Specify both the angles and energy of neutrinos
  - Simple, generic ntuple format ('**GSimpleNtpFlux**')
    - Neutrino flavor
    - Energy, momentum of neutrinos
    - Distance from source of the flux to flux window
    - Vertex position on flux window
- Wrap any of the above in a “flavor blender” adapter ('GFlavorMixerI') - this is how you handle far detector in oscillation experiment.



# How does GENIE work? - Flux & Geometry

- Experiments need to generate interaction vertices in the correct locations
- Detectors have many elements(nuclei) and complicated geometries



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  <D value="1.40" unit="g/cm3"/>  
  <fraction n="1.0000" ref="Argon"/>  
</material>  
  
</materials>
```

**Example of Geometry File I  
made for SBND**

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    y="2000"  
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  <box name="TPC"  
    lunit="cm"  
    x="500"  
    y="400"  
    z="400"/>  
</solids>  
  
<structure>  
  <volume name="volTPC">  
    <materialref ref="LAr"/>  
    <solidref ref="TPC"/>  
  </volume>  
  
  <volume name="volWorld" >  
    <materialref ref="LAr"/>  
    <solidref ref="World"/>  
    <physvol>  
      <volumeref ref="volTPC"/>  
      <position name="posTPC" unit="cm" x="0.0" y="0.0" z="0.0"/>  
    </physvol>  
  </volume>
```

# How does GENIE work?

- Currently implemented GENIE physics models rely heavily on a **factorization** assumption.

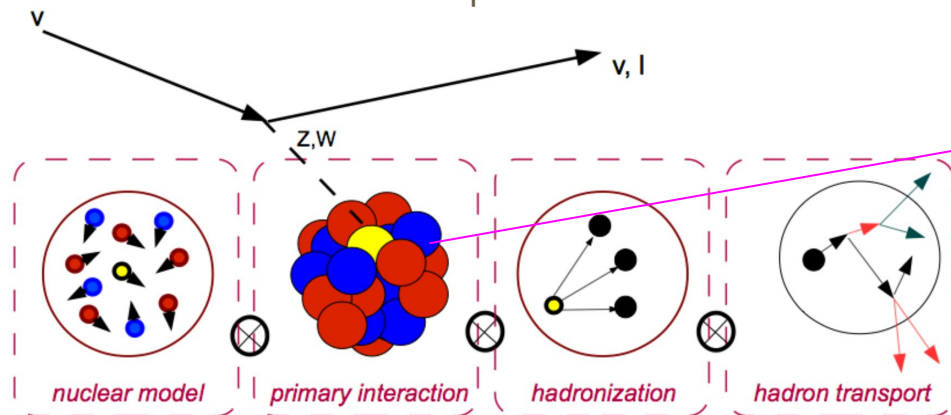
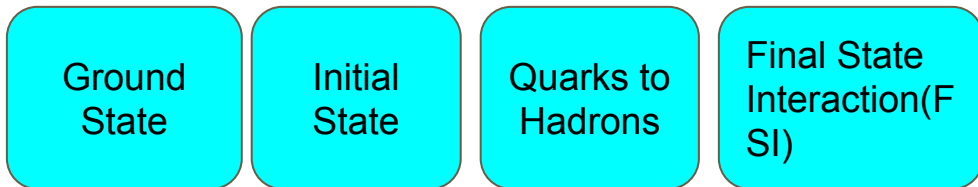
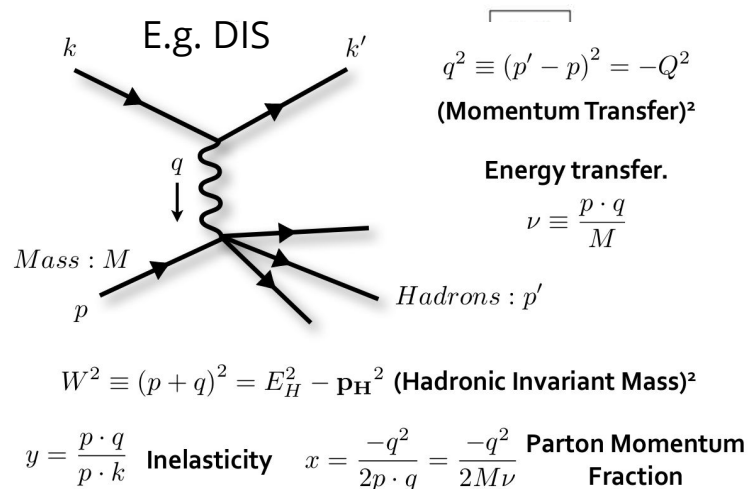


Figure by C. Andreopoulos



**Primary interactions:** using differential cross sections to get event kinematics:  $x$ ,  $y$ ,  $Q^2$ ,  $W$ ,  $t$  etc

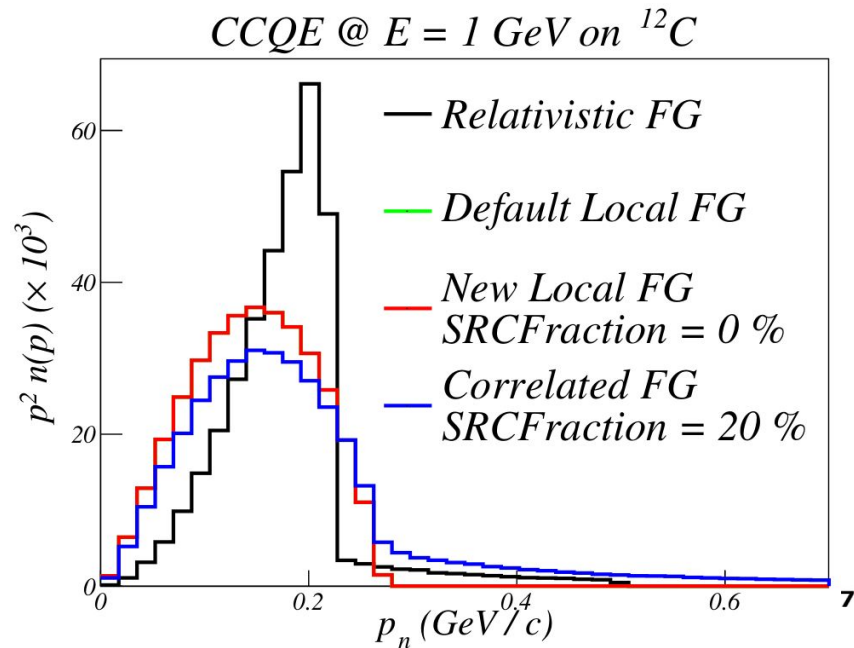




# How does GENIE work? - Nuclear Model

Model/generator	GENIE	NuWro	NEUT
Nuclear model	<b>RFG</b> , LFG, Effective spectral function	RFG, LFG, spectral function	RFG, LFG, spectral function

- Nuclear models come from proper descriptions of electron scattering (Data)
- **RFG(Relativistic Fermi Gas)** Model: is historical standard but not accurate
- New Models based on RFG model
  - **Local Fermi Gas Model (LFG)**
  - LFG with **Short Range Correlations(SRC)** implemented:  $\Delta R < 0.5 \text{ fm}$
- More modern models include **Correlated Local Fermi Gas Model** and **Benhar-Fantoni spectral functions** are almost there



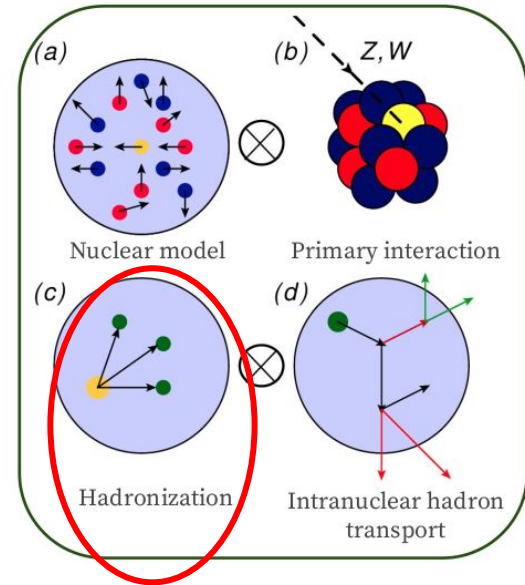
# How does GENIE work? - Cross Section Models(2017)

Model/generator	GENIE (Version2)	NuWro	NEUT
QE	Lwlyn-Smith Nieves, Eff MA	Lwlyn-Smith RPA	Lwlyn-Smith Eff RPA
MEC	Valencia Empirical	Valencia Marteau	Valencia
Delta model (Resonance)	Rein-Sehgal (updated) Berger-Sehgal	Home-grown, great	Rein-Sehgal (update) Berger-Sehgal
Coherent	Rein-Sehgal(corrected) Berger-Sehgal	Rein-Sehgal Berger-Sehgal	Rein-Sehgal Berger-Sehgal

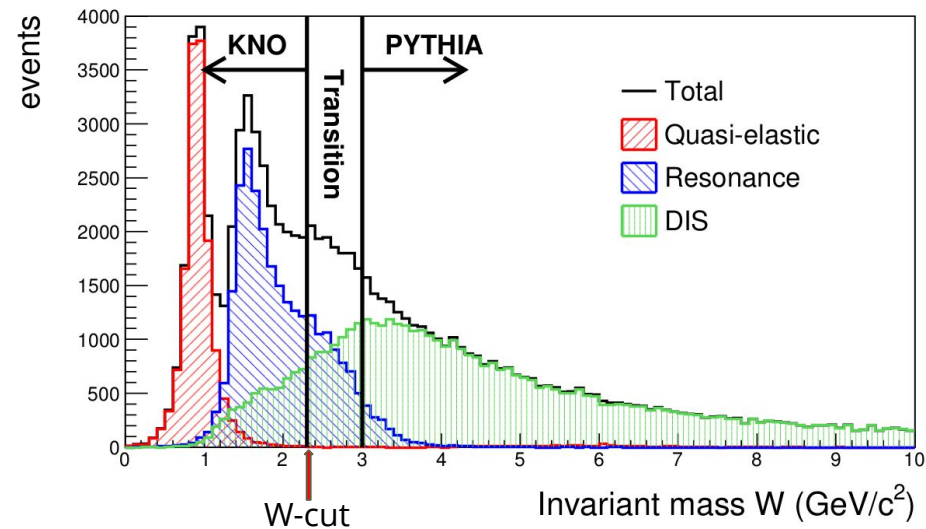
- All generators have largely the same models
- GENIE is advancing, taking more theoretical models and more channels simulated

# Hadronization Modelling

- **Hadronization:** provides the hadrons coming out of **DIS** interaction
- Hadronization Modeling Impacts (also applies to other processes)
  - **Neutrino energy reconstruction**
    - Detectors are sensitive to different particles
    - Simulation must account for missing particles
  - Efficiency calculations for **event identification**
    - Hadronization determines neutral content that is hard to measure.
      - For example, hadronic showers (from NC or high -  $y$   $\nu_\mu$  CC events with large EM component could be misclassified as  $\nu_e$  CC events, shower mismodeling can impact the estimation of backgrounds in neutrino oscillation.



# How does GENIE work? - Hadronization Model



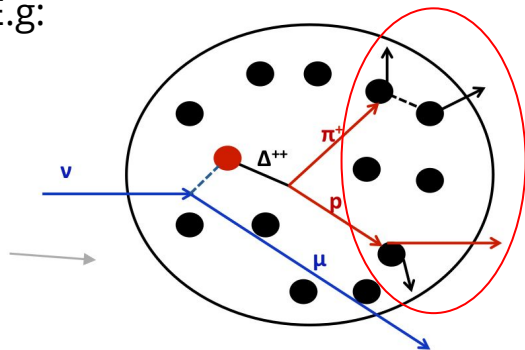
W distribution of  $\nu_\mu$ -water target interaction in GENIE, atmospheric neutrino flux

- Hadronization model in GENIE:  
**AGKY** model

- $3.0 \text{ GeV}/c^2 < W$ , **PYTHIA** only region.
- $W < 2.3 \text{ GeV}/c^2$ , **KNO** Model.
  - PYTHIA hadronization models deteriorate at low energy region
- $2.3 \text{ GeV}/c^2 < W < 3.0 \text{ GeV}/c^2$  **Transition region**
  - Resonant + Non Resonant background(DIS)
  - Scale non resonance background(DIS) with different hadron multiplicities with a scaling factor ( $R(m)$  to match the data,  $m$  is the hadron multiplicity)

# How does GENIE work? - FSI Models

E.g:



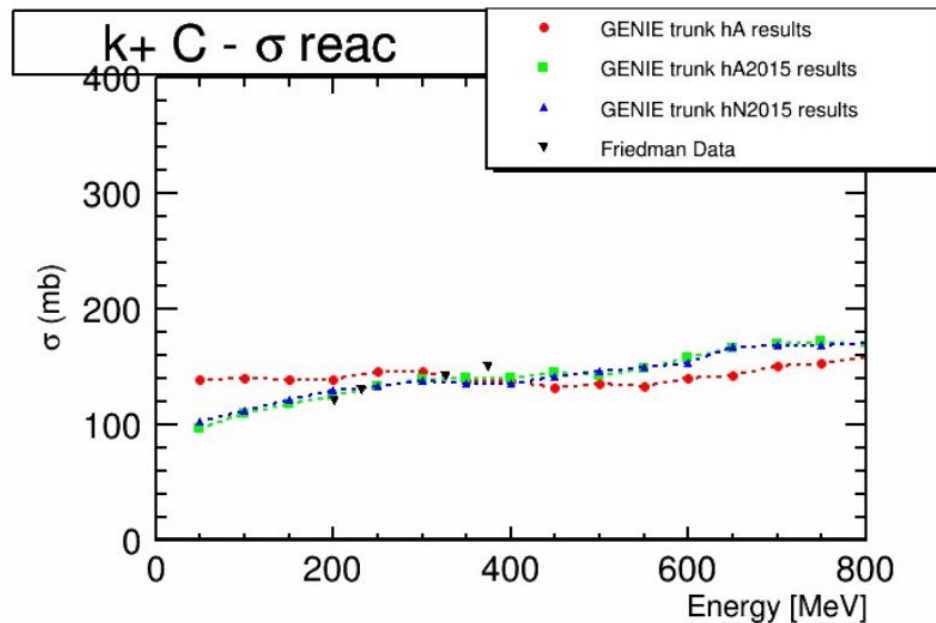
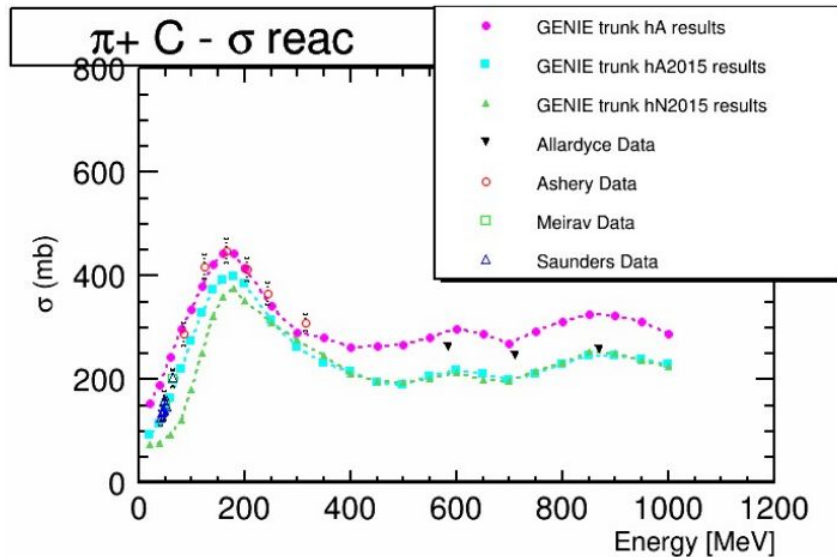
- Final state interactions describe particles interact with nucleons before exiting the nucleus
- Intranuclear Cascade model(INC) is commonly used in Generators, it is called “hN” in GENIE
  - Simulate rescattering of pions, nucleon in nucleus
- Pions,  $K^+$ , p and n included in GENIE final state interaction model

Model/generator	GENIE	NuWro	NEUT
FSI	<b>Schematic</b> Cascade (med corr)	Cascade(med corr)	Cascade(med corr)

- Schematic Model(hA): simulate the cascade model in a data -driven way (total cross section, and inclusive cross section); → Reweightable
- Medium Correlations: Low energy nucleons (describe the correlation between the nucleons as the final state being produced)

# How does GENIE work? - FSI Model

- $\pi^+$  has significant peak for  $\Delta$  excitation, none for  $K^+$ 
  - Very few kaon data
- Both hA2015 and hN2015 underpredict pion peak cross section



# GENIE Version 3



- Many new models introduced in GENIE version 2
  - Some groups developed modified tunes with these new models, but often in inconsistent ways
- GENIE v3
  - Put most compatible physics models into model sets, e.g. QE+MEC
  - Provide Comprehensive Model Configurations(CMC) for different “Model Sets” for users
    - Can be called by a parameter `--tune G**_**`
  - Presents new tunes
    - Only deuterium data for now, more later
    - Expanded resonance region (larger Wcut)
    - Provide full error analysis for each

# GENIE Version 3

- G00\_00 series: Historical default configuration.

G00_00a	G00_00b
No MEC	with (empirical) MEC

- From G00\_00 to G18\_01 series: adiabatic evolution of old default.

	G00_00	G18_01
Hadron Transport Model	HAIntranuke/HNIntranuke	HAIntranuke2018/HNIntranuke2018 Added diffractive and Lambda production

- From G18\_01 to G18\_02 series:

	G18_01	G18_02
RES	Rein-Sehgal	Berger-Sehgal
COH	Rein-Sehgal	Berger-Sehgal

- From G18\_01 to G18\_10 series: theory driven configuration.

	G18_01	G18_10
Nuclear Model	FGM BodekRitchie	Local Fermi Gas (LFG)
QEL	LwlynSmitch	Nieves
MEC	Empirical	Nieves
RES	Rein-Sehgal	Berger-Sehgal



# Additional new models now in v3.0.0

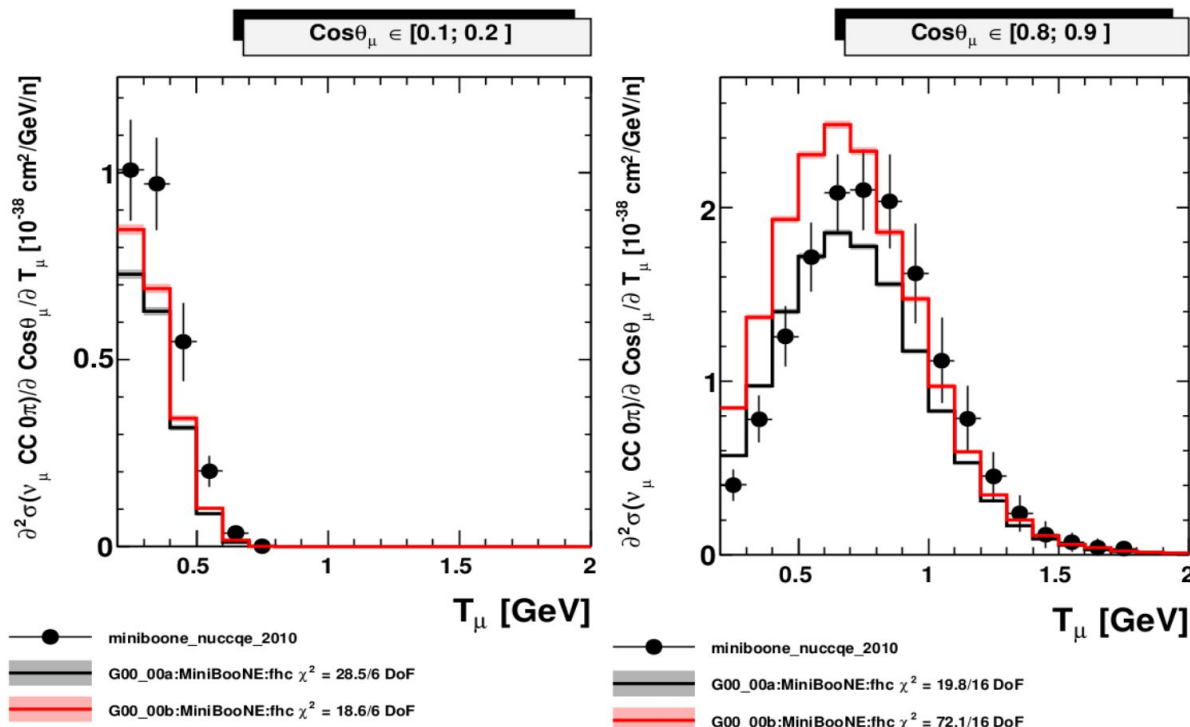
- Single  $K^+$  production
- Diffractive pion production with neutrinos
- Quasielastic hyperon production(Pais)
- Alvarez-Ruso Coherent Model (Low energy only)
- Smith-Moniz QE model

# Database and Validation

- “Comparison” Comparing GENIE predictions against public datasets
  - Modern Neutrino **Cross Section Measurements**
    - Nuclear targets
    - MiniBooNE, T2K, MINERvA
  - Historical Neutrino Cross Section Measurement
  - Measurements of neutrino-induced **hadronic system characteristics**
    - E.g. Forward/backward hadronic multiplicity distributions
  - Measurements of hadron-nucleon and hadron-nucleus event characteristics
    - FSI tuning
    - For pion, kaons, nucleons and several nuclear targets
    - Spanning hadron kinetic energies from few tens MeV to few GeV
  - Semi-inclusive **electron scattering data**
    - Electron-nucleus QE data
    - Electron-nucleus Resonance Data

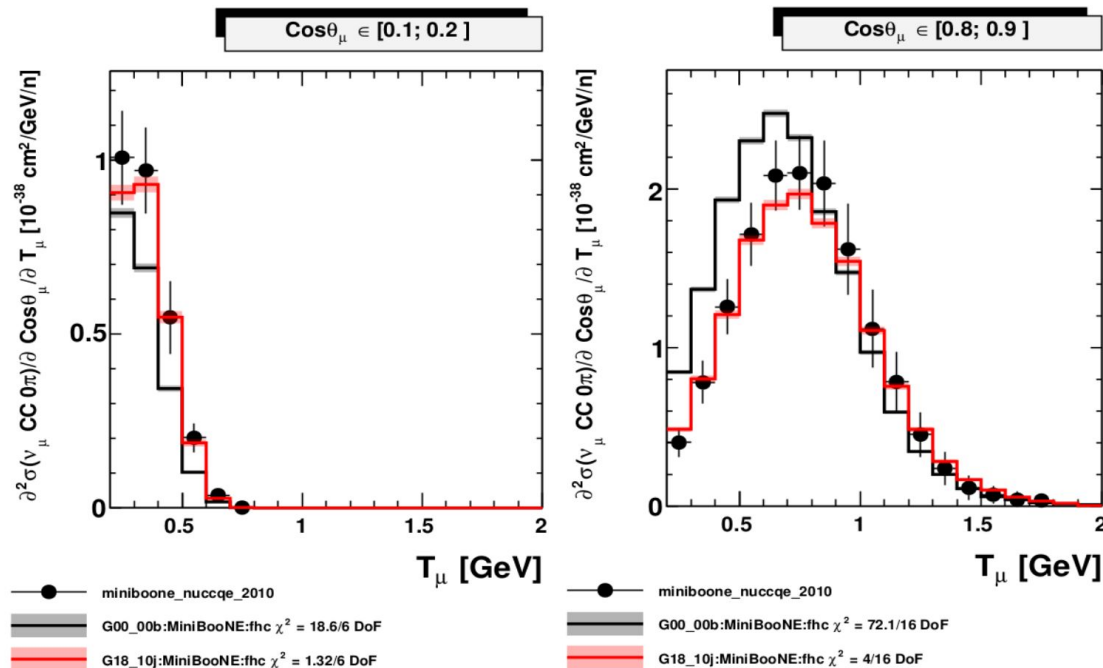
# MiniBooNE CC0 $\pi$ (2010) need for MEC ( $E_\nu \sim 1\text{GeV}$ )

- MiniBooNE published both true CCQE and CC0 $\pi$ , we use latter
- **G00\_00b (LS, with MEC)** vs **G00\_00a (LS, no MEC)**
- MEC process increases cross section of CC0 $\pi$  at all angles



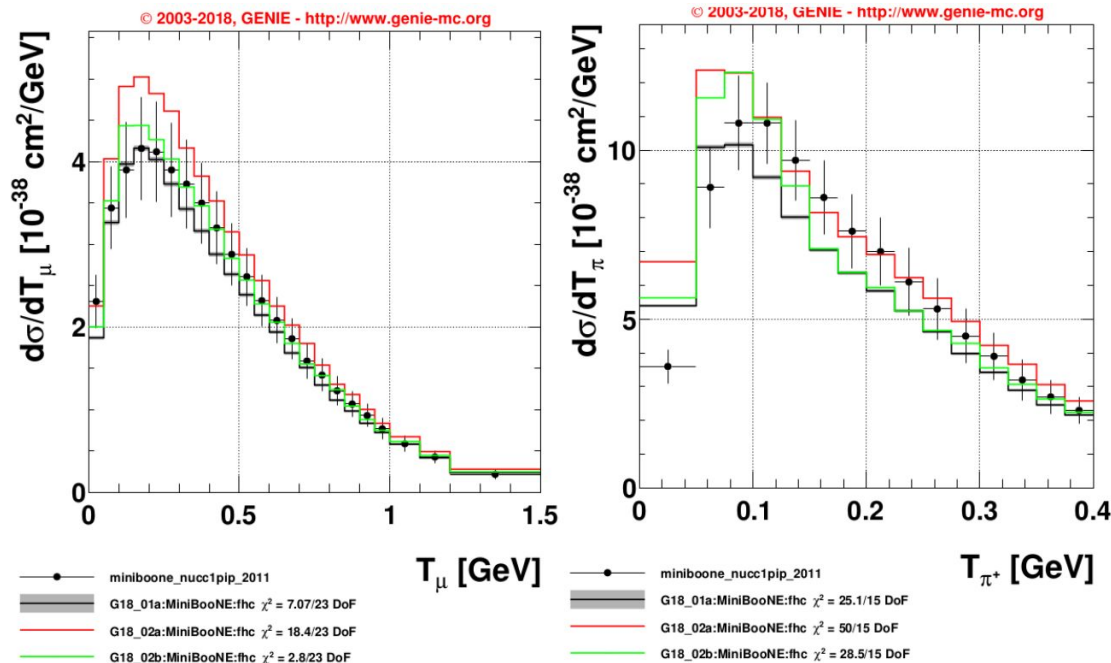
# Modern Calculation has better agreement

- G18\_10j** has **full valencia CCQE** with RPA/Coulomb, MEC with local Fermi Gas (LFG) nuclear model. Much better theoretical model compared to **L-S model** with empirical MEC (**MiniBooNE CC0 $\pi$  Data**)



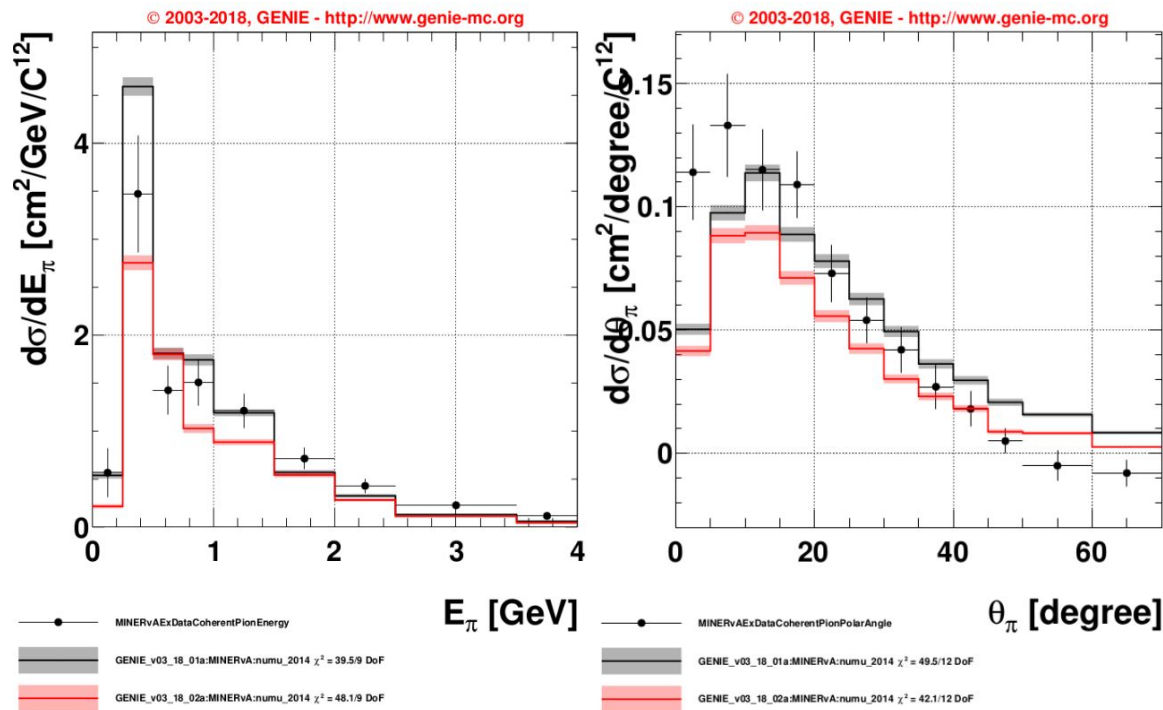
# MiniBooNE $\nu_\mu$ CC $1\pi^+$ $\langle E_\nu \rangle \sim 1\text{GeV}$

- G18\_01a(Rein-Sehgal, hA) vs 02a(Berger-Sehgal with new Form Factors, hA) vs 02b(Berger-Sehgal with new Form Factors, hN)
- G18\_02b most advanced theory, gets details best



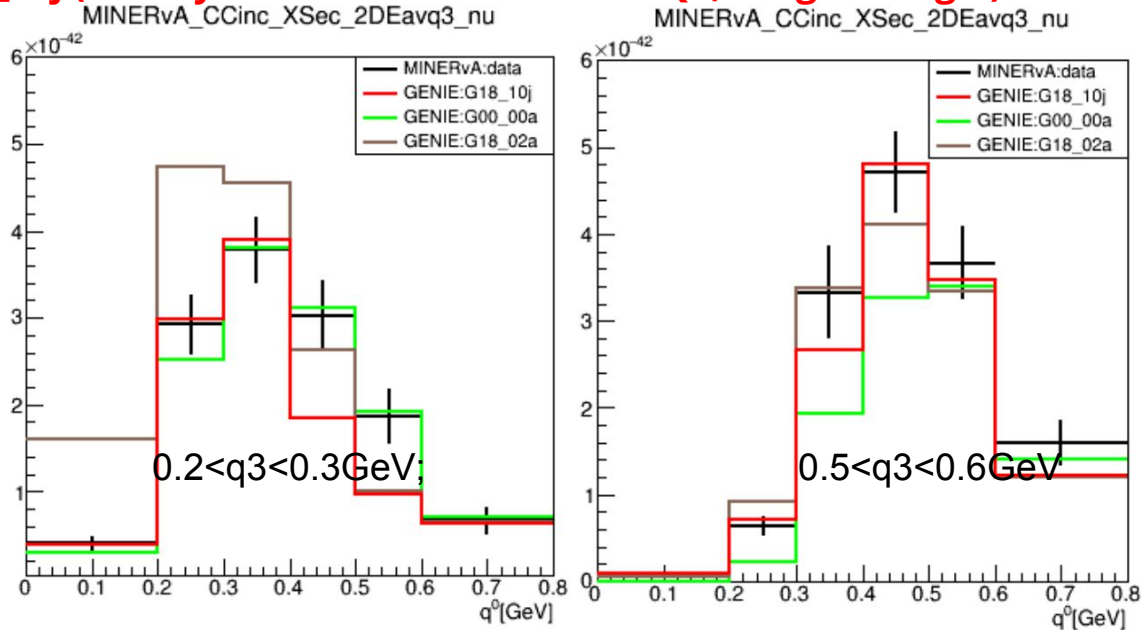
# MINERvA Coherent 2015 ( $\langle E_\nu \rangle = 4.0$ GeV)

- Compares **Berger-Sehgal (G18\_02a)** with updated Rein-Sehgal(G18\_01a)
- Better agreement with the **Berger-Sehgal** model



# MINERvA CC Inclusive (2016) [NUISANCE]

- **CCinclusive cross section in different  $q_3$  bins**
- **G18\_10j (Theory-driven model: Valencia QE, Berger-Sehgal)** has best agreement



# Tuning

- Why Tuning?
  - Constrain parameters (some parameters from old experimental data)
  - Provide specific GENIE tuning version for experiments with new parameters
    - **Deuterium** Tuning, working on others
- What kind of Minimizer used?
  - Old problems in high energy physics
  - CPU demanding
  - Multiple parameter fitting
  - Solution found in the **Professor** suite



Trying to get it working with Fermilab  
Computing grid



# Tuning against data

- GENIE Comparisons and Tuning products have built-in interfaces to professor
- Professor is a tool developed for a general purpose MC tuning at the LHC
  - Andy Buckley, Holger Schulz and collaborators.
  - <https://professor.hepforge.org>
- GENIE / Professor integration was supported by an IPPP Associateship award.

*"Fundamentally, the idea of Professor is to reduce the exponentially expensive process of brute-force tuning to a scaling closer to a power law in the number of parameters, while allowing for massive parallelisation and systematically improving the scan results by use of a deterministic parameterisation of the generator's response to changes in the steering parameters. "[Professor web page]]*

# Global Fit

- Use only  $\nu$  &  $\bar{\nu}$  deuterium data including Wikinson et al.
- Goal is to maintain CCQE fit and emphasize CCRES exclusive data

Parameter	Default value	Best tune value	
$M_A^{RES}$ [GeV/c <sup>2</sup> ]	1.12	$1.065 \pm 0.025$	
$M_A^{QE}$ [GeV/c <sup>2</sup> ]	0.99	$0.961 \pm 0.031$	
R-vp-m2	0.1	$0.008 \pm 0.00$	} Multiplicity parameters, e.g, R-vp-m2 is for $\nu p$ , 1 pions
R-vp-m3	1	$0.788 \pm 0.20$	
R-vn-m2	0.3	$0.128 \pm 0.021$	
R-vn-m3	1	$2.115 \pm 0.57$	
RES-XSecScale	1	$0.878 \pm 0.031$	} Relative normalization, RES vs. NONRES
DIS-XSecScale	1.032	$1.019 \pm 0.055$	
$W_{cut}$ [GeV]	1.7	$1.928 \pm 0.091$	Boundary – RES vs. DIS

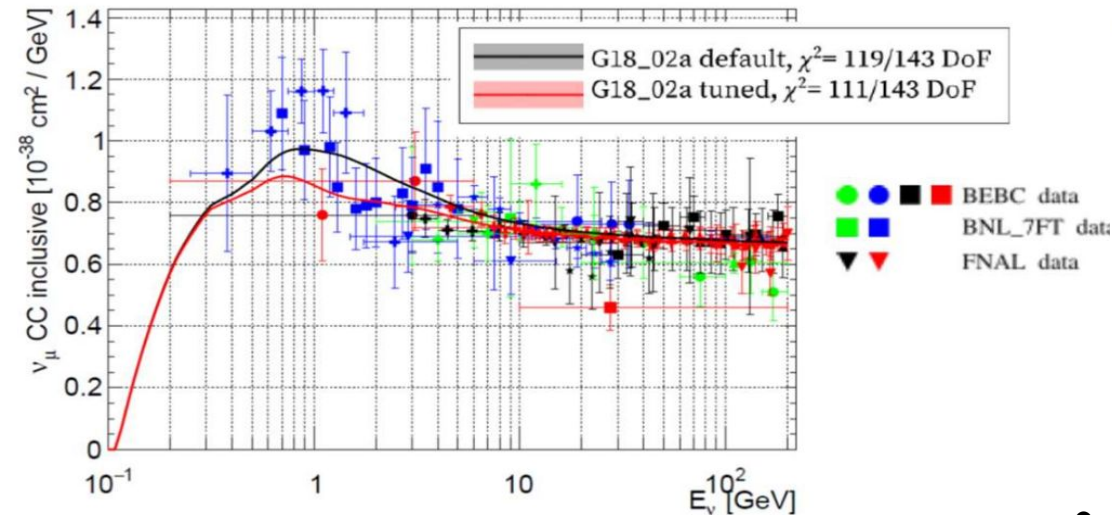
## Priors applied

$M_A^{QE} = 0.89 \pm 0.044$  GeV/c<sup>2</sup>, fit to just BEBC data [Eur. Phys. J. C (2008) 54]

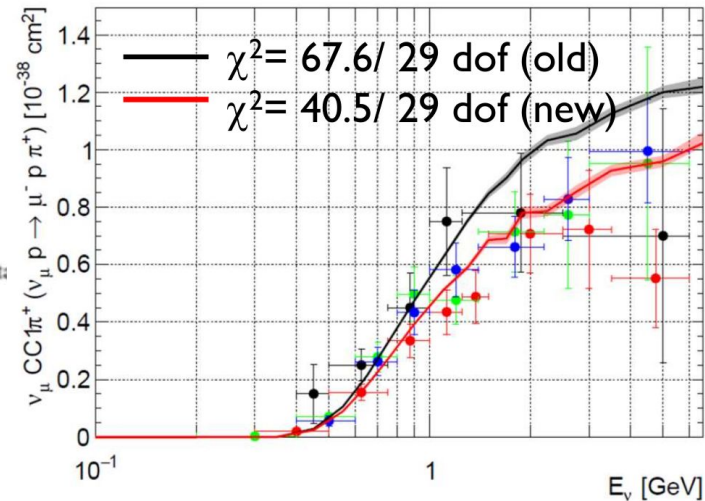
$M_A^{RES} = 1.12 \pm 0.03$  GeV/c<sup>2</sup>, [ArXiv:0606184]

DIS-XSecScale =  $1 \pm 0.05 \rightarrow$  Motivated by DIS high energy cross section values

# Compare previous with new fits



- CC inclusive cross sections before and after tuning.
- Smaller Chi2, better agreement with the parameters tuned against data
- GENIE version 3 also provide the model sets with the parameters tuned against data



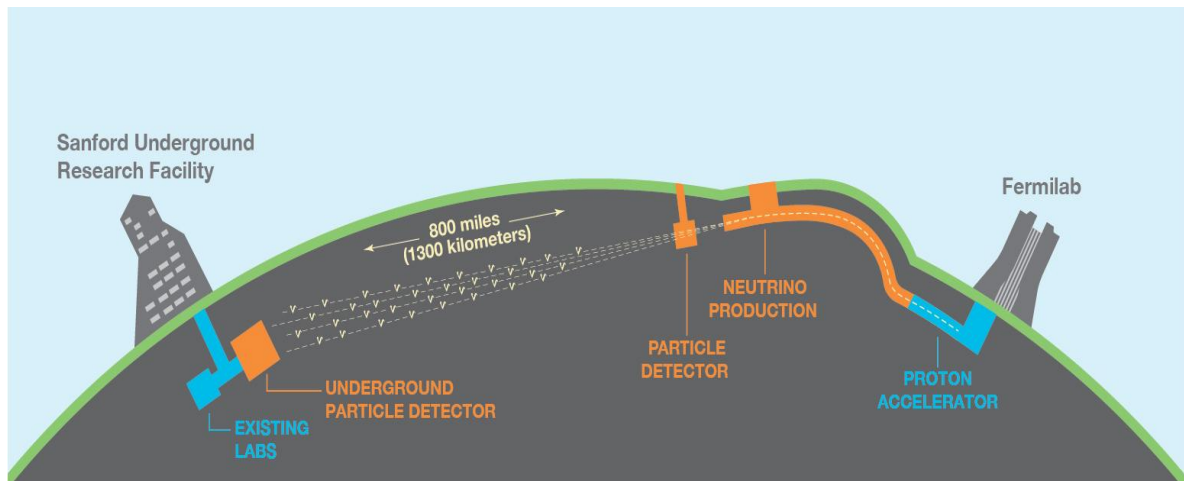
- $\nu_\mu$  CC1 $\pi$  Cross section decrease  $\sim 30\%$  by tuning.

# Data on heavier nuclei

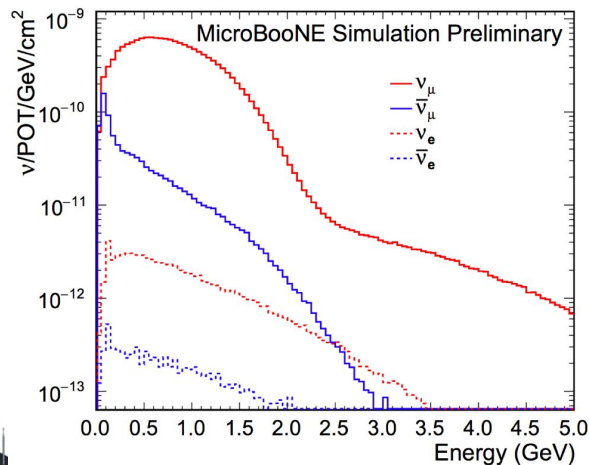
- Short Baseline Neutrino Program(SBN) and DUNE uses argon as a target
- How do we know our tune works for argon?
- We need data on argon!
  - New challenges/opportunities to study nuclear effects
  - Needs increasing for the simulator

Short Baseline Neutrino Program(SBN)

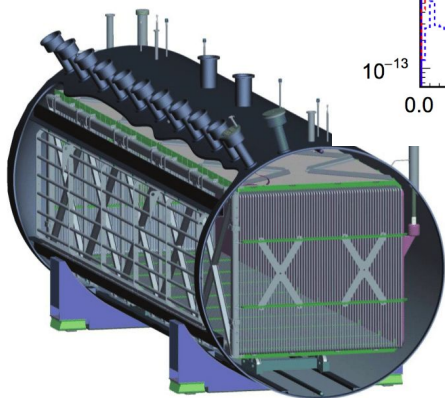
Deep Underground Neutrino Experiment (DUNE)



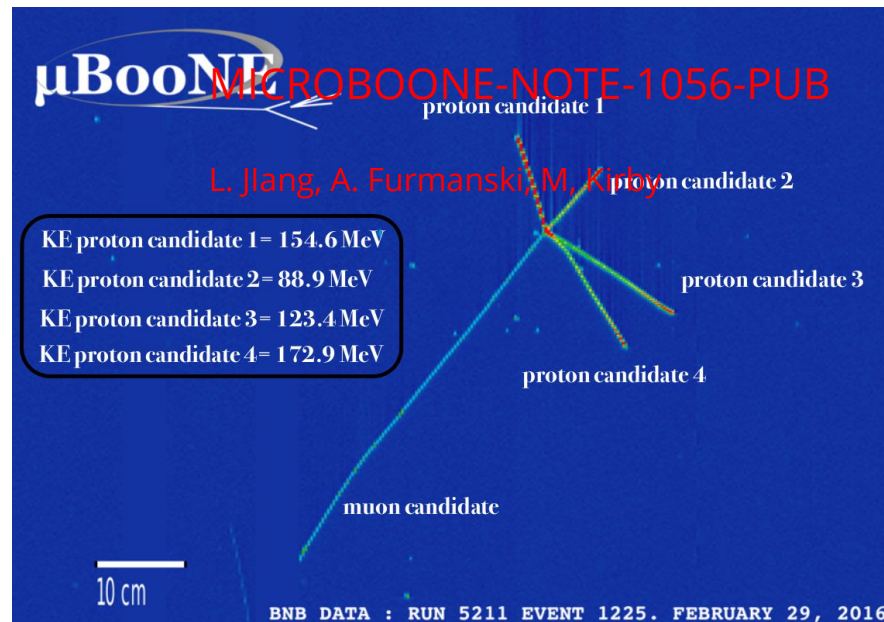
# Charged Current One Muon N proton Analysis in MicroBooNE (Liquid Argon TPC)



**Booster Neutrino Beam**



**MicroBooNE Detector**

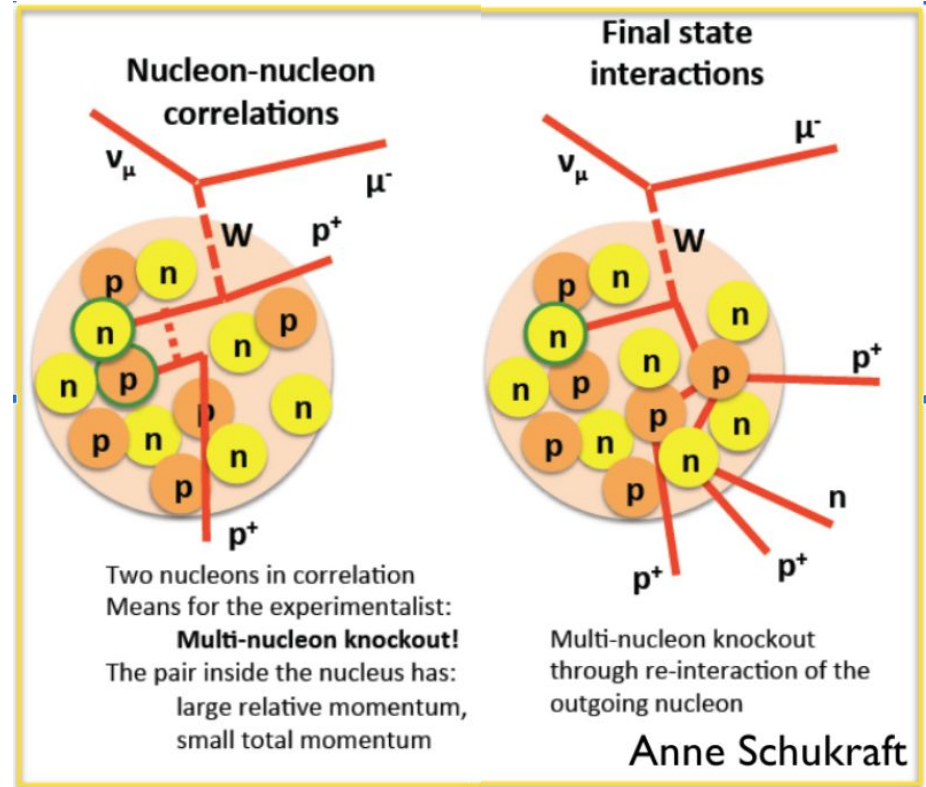


- Multiple proton events from MicroBooNE
- Proton momentum threshold measured down to 300 MeV (Kinetic Energy ~45 MeV)

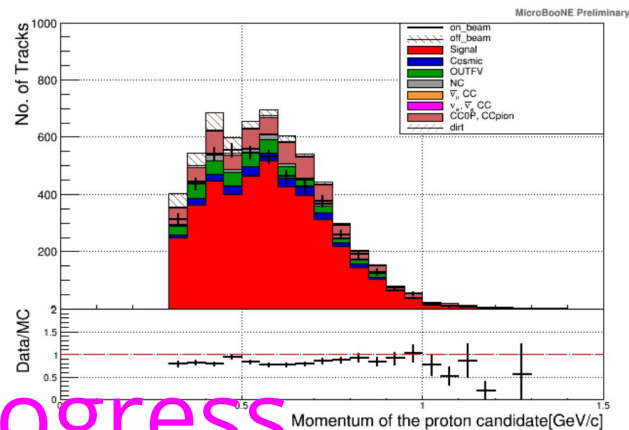
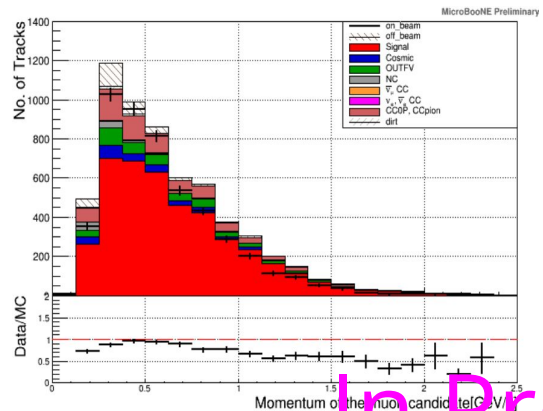
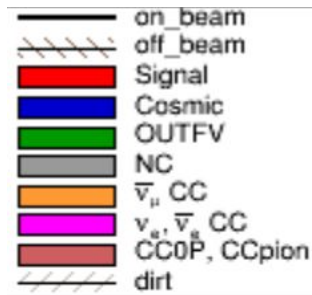


# Challenges in $\nu$ -Ar Interaction

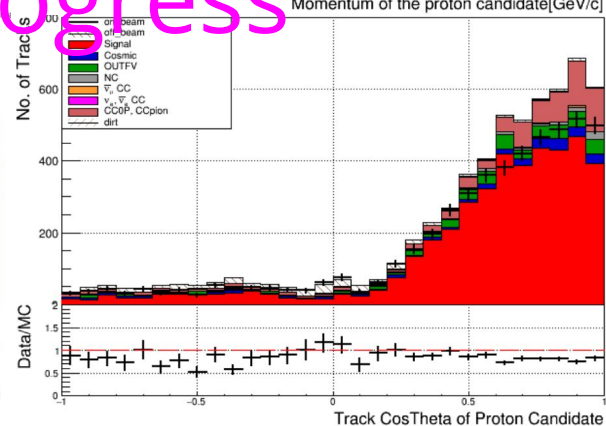
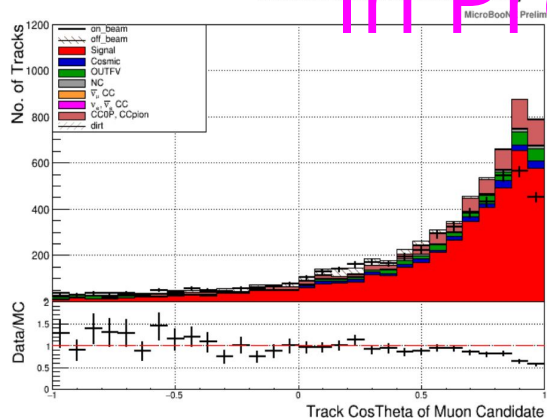
- Heavy Nucleus means complicated nuclear effects
  - Charged Current  $1\mu 0\pi$  (CC1 $\mu$ 0 $\pi$ ) data tells us about **nuclear physics** with the heavy nucleus (Ar):
    - Final and initial state interactions
    - Nucleon correlations
- Neutrons carry part of the energy without being detected in LArTPC
- Charged particles with low momentum can not be reconstructed
  - Lower proton momentum threshold in LArTPC (300 MeV/c)



# Charged Current One Muon N proton Analysis in MicroBooNE (Liquid Argon TPC)



- Better cosmic background suppression
- Both backward and forward going particle reconstruction
- First results targeted for publication



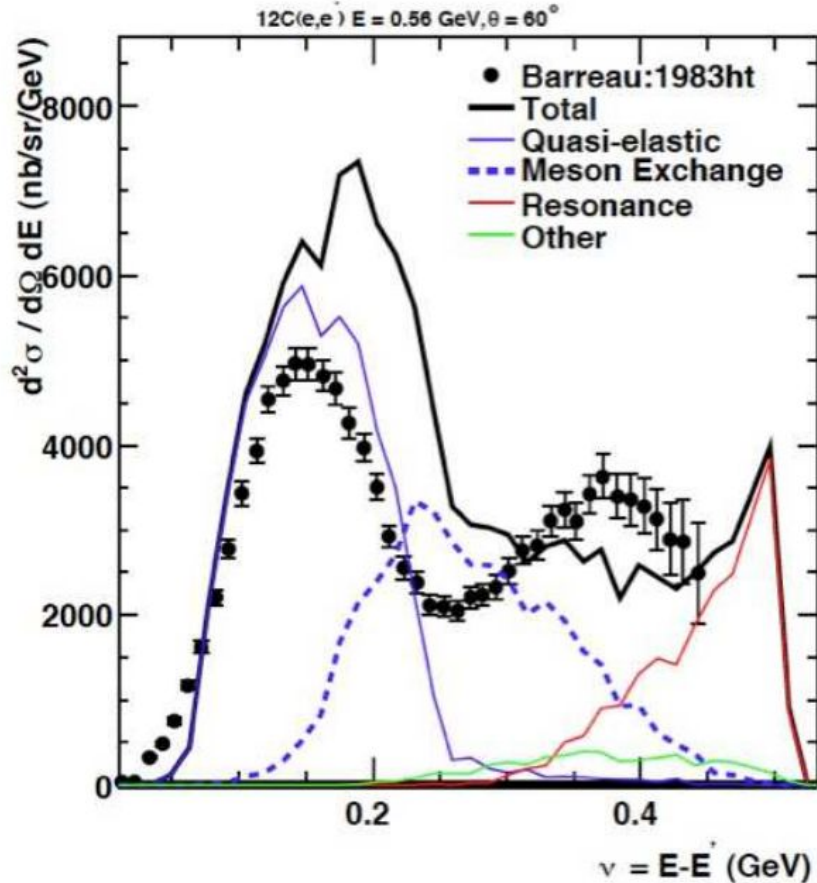
In Progress

# Summary

- With the development of detector and analysis methods, **more attentions** are paid on neutrino interaction simulation.
- GENIE provides **a framework** handles all neutrinos and targets, and almost all processes relevant from MeV to PeV energy scales. Softwares for comparison and tuning also provided.
- Both Short Baseline Neutrino Program (SBN) and DUNE use LArTPC as the detector, **new challenges**
  - Nuclear effect understanding, models improved
  - More efforts on cross section modeling and new channel needed



# MEC(Meson Exchange Current)



- **Empirical Model** is motivated by the lightbody model.
- In the lightbody model, QE and Delta peaks are give by Gaussian distributions, then MEC part is modeled as a Cauchy distribution between those 2 distributions
- **Valencia Model:**

Fermions are particles that obey Fermi-Dirac statistics, like electrons, protons, and neutrons, and, in general, particles with half-integer spin. An ideal Fermi gas or free Fermi gas is a physical model assuming a collection of non-interacting fermions in a constant potential well. It is the quantum mechanical version of an ideal gas, for the case of fermionic particles.

# Fermi Gas Model

- Free electron gas: protons and neutrons moving quasi-freely within the nuclear volume
- 2 different potentials wells for protons and neutrons.
- Spherical square well potentials with the same radius

## Statistics of the Fermi distribution

Given a volume  $V$  the number of states  $dn$  goes like:

$$dn = \frac{4\pi p^2 dp V}{(2\pi\hbar)^3}$$

$$n = \int_0^{p_F} \frac{4\pi p^2 dp V}{(2\pi\hbar)^3} = \frac{V p_F^3}{6\pi^2 \hbar^3}$$

$$N = 2n = \frac{V p_{F,n}^3}{3\pi^2 \hbar^3} \quad Z = \frac{V p_{F,p}^3}{3\pi^2 \hbar^3}$$

↓

If  $T=0$  the nucleus is in the ground state and  $p_F$  (**Fermi Momentum**) is the maximum possible momentum of the ground state.

$N$ = number of neutrons

$Z$ = number of protons

$$V = \frac{4}{3}\pi R^3 = \frac{4}{3}\pi R_0^3 A \quad R_0 = 1.21 \text{ fm}$$

$$Z = N = A/2 \quad \frac{A}{2} = \frac{4}{3} \frac{\pi R_0^3 A p_F^3}{3\pi^2 \hbar^3} \Rightarrow p_F = p_{F,n} = p_{F,p} = \frac{\hbar}{R_0} \left( \frac{9\pi}{8} \right)^{\frac{1}{3}} \approx 250 \text{ MeV}/c$$

The nucleon moves in the nucleus with a large momentum

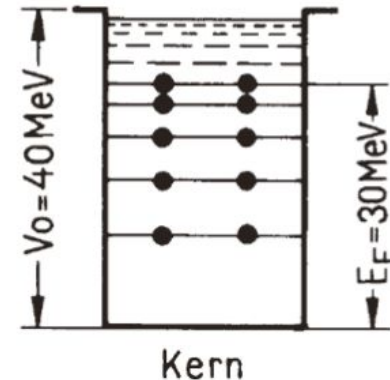
Fermi Energy

$$E_F = \frac{p_F^2}{2m_N} \approx 33 \text{ MeV}$$

Binding Energy:  $BE/A = 7-8 \text{ MeV}$

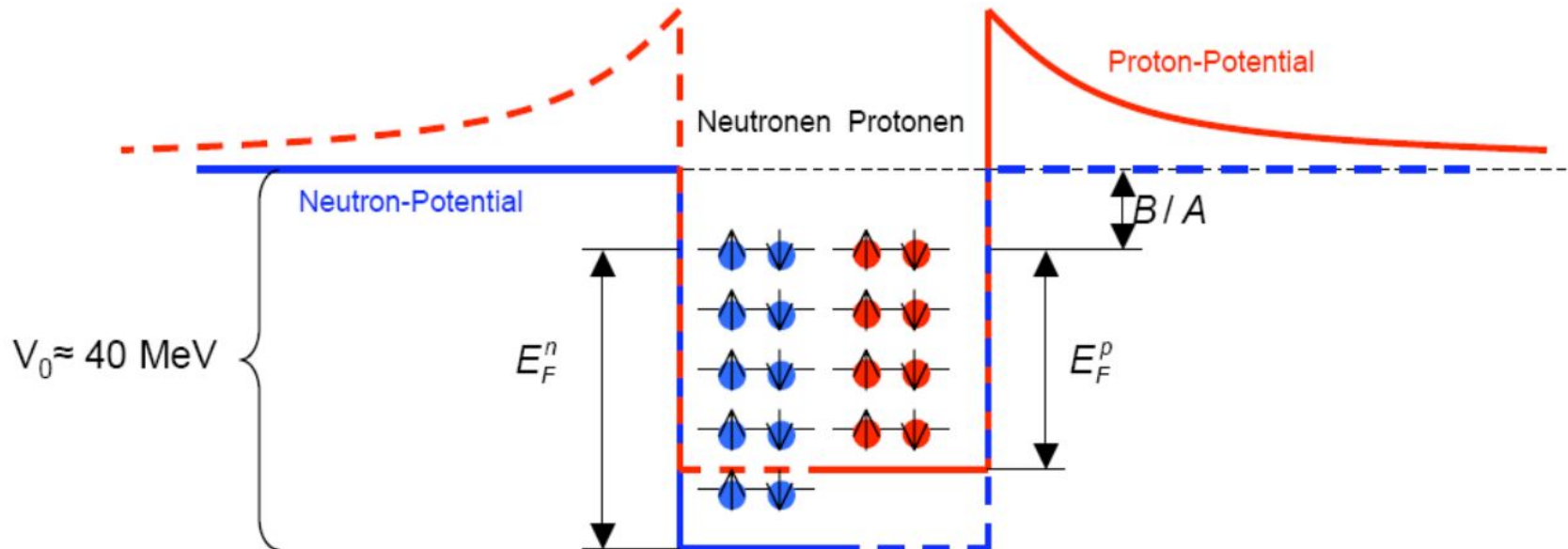
$V_0 = E_F + B/A \sim 40 \text{ MeV}$

→ Nucleons are rather weakly bound in the nucleus



# Potential well in the Fermi-gas model

The **neutron** potential well is deeper than the **proton** well because of the missing Coulomb repulsion. The Fermi Energy is the same, otherwise the  $p \rightarrow n$  decay would happen spontaneously. This implies that there are more neutron states available and hence  $N > Z$  the heavier the nuclei become.

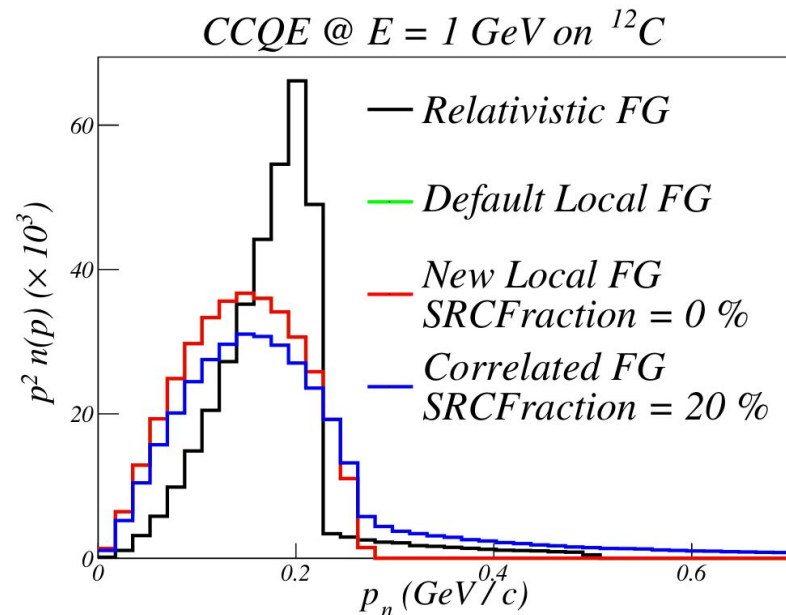
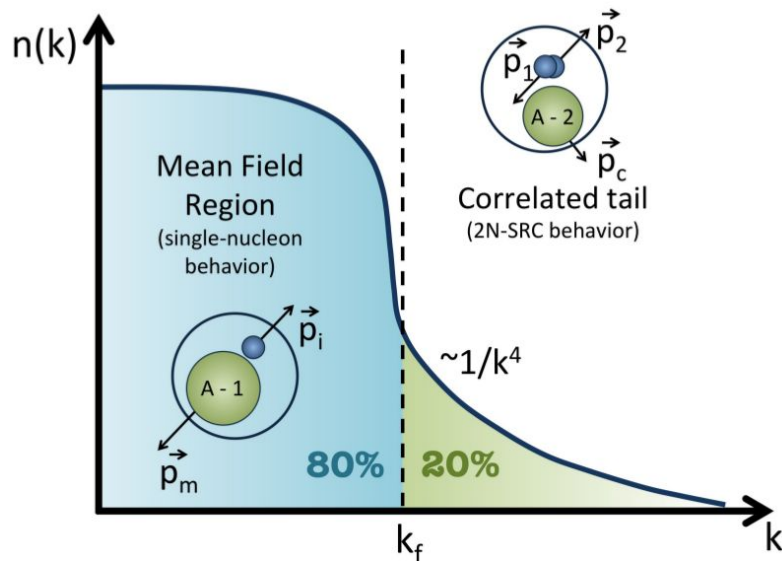


The relativistic Fermi gas model is also used for the description of large white dwarfs which are close to the Chandrasekhar limit.

# How does GENIE work? - Nuclear Model

Model/generator	GENIE	NuWro	NEUT
Nuclear model	<b>RFG</b> , LFG, Effective spectral function	RFG, LFG, spectral function	RFG, LFG, spectral function

**RFG(Relative Fermi Gas)** Model: is the default model in GENIE v2 with Bodek-Ritchie high momentum tails



KNO: Hadronization models at low  $W$  where pythia is not applicable. Describe details of the GENIE NIM paper.



# How does GENIE work? - Simulation Chain

- Vertex selection
  - Simple nuclear density model
- Initial state nuclear model
  - Removal energy and momentum
    - RFG with Bodek-Ritchie tails.
    - New: Local Fermi Gas
    - New: Effective Spectral Function
    - Almost there: "Benhar" spectral function
    - Just started: Correlated Fermi Gas (MIT)

GROUND STATE

- Hard scattering process
  - Differential cross section formula to get event kinematics (x, y, Q<sup>2</sup>, W, t, etc.)
- Lepton kinematics
- Hadronic system

INITIAL STATE

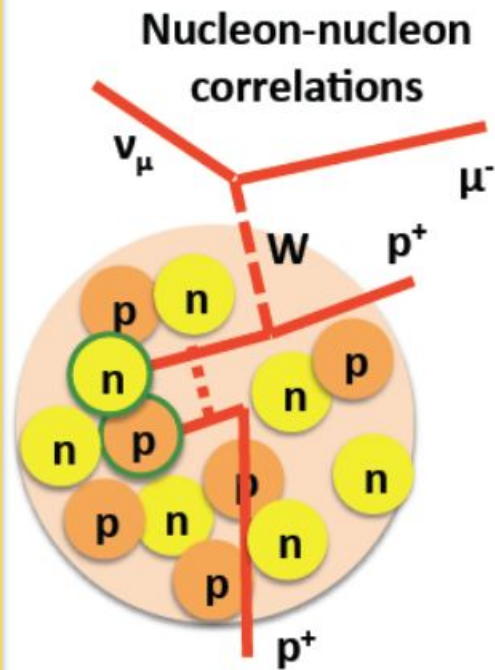
- Propagation/transport (default is an "effective cascade")
  - Fast and re-weightable

FINAL STATE

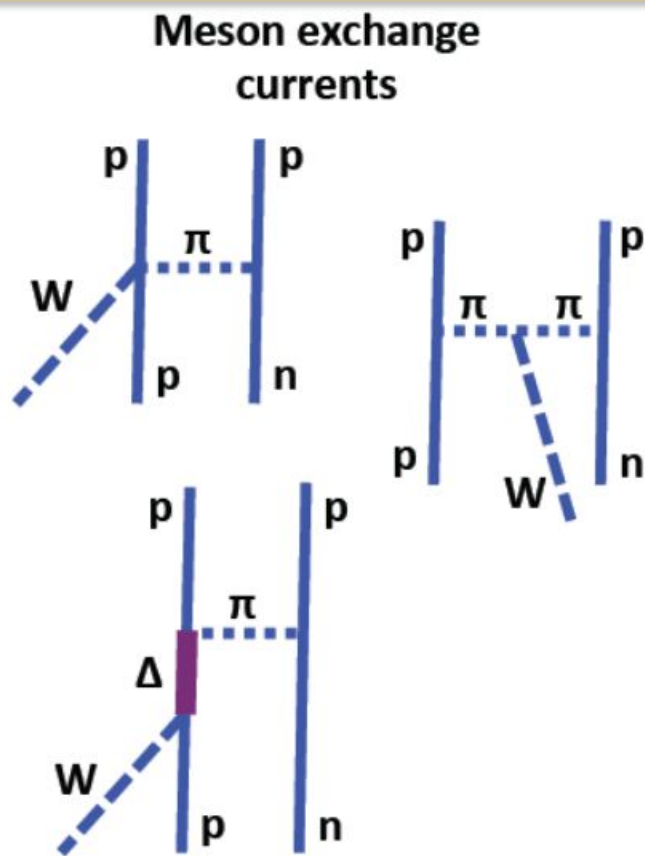
# How does GENIE work? Simulation Chain

- Decays before and after propagation
- Remnant decay
  - Just started caring about this, really...
  - Current model is very simple
    - Working on adopting other codes (Geant4, INCL++, possibly GiBUU) to handle clustering, de-excitation, evaporation
    - May be a bridge to more sophisticated transport codes

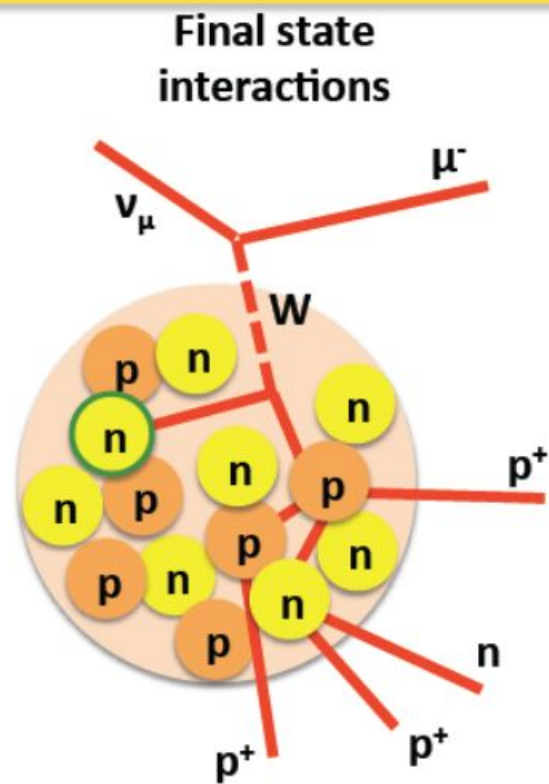
REMNANT STATE



Two nucleons in correlation  
Means for the experimentalist:  
**Multi-nucleon knockout!**  
The pair inside the nucleus has:  
large relative momentum,  
small total momentum



The observed state looks  
like QE but it was not!



Multi-nucleon knockout  
through re-interaction of the  
outgoing nucleon

Anne Schukraft

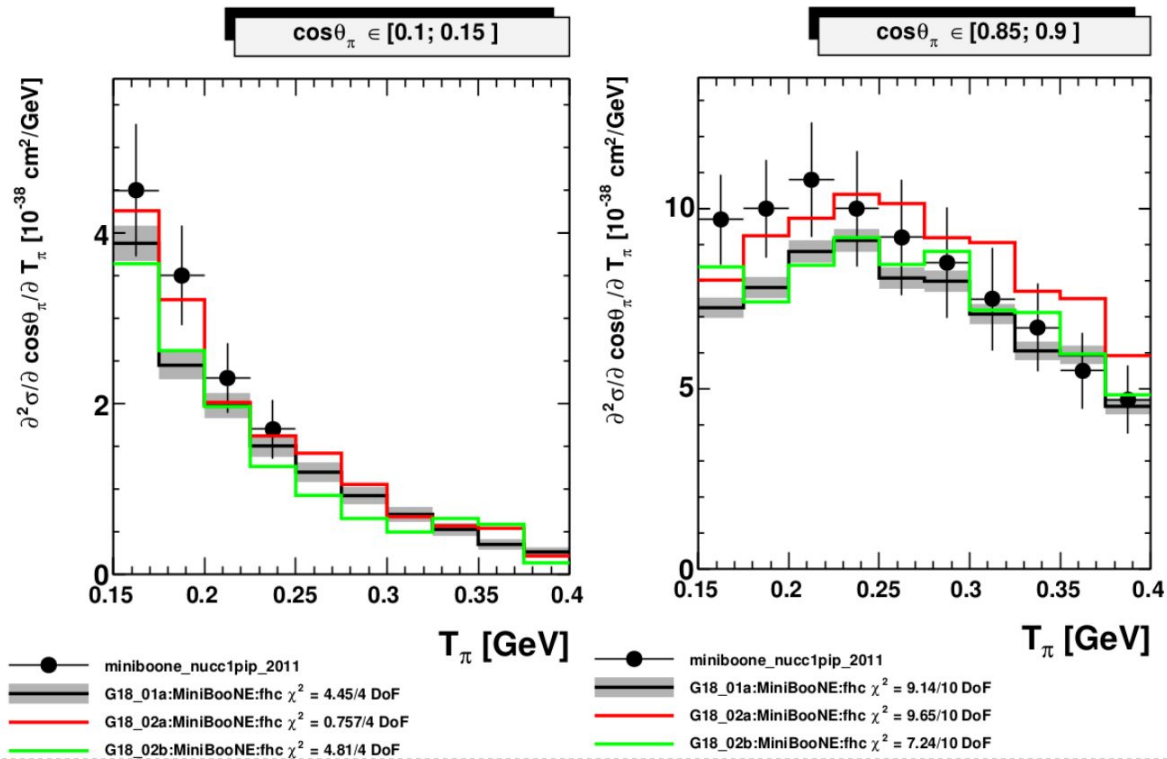
# How does GENIE work? - KNO Model

- Averaged charged hadron multiplicity data are fit to a function of invariant mass squared,  $W^2$

$$\langle n_{\text{ch}} \rangle = a_{\text{ch}} + b_{\text{ch}} * \log W^2$$

- The total averaged hadron multiplicity is deduced to be  
 $\langle n_{\text{tot}} \rangle = 1.5 * \langle n_{\text{ch}} \rangle$
- Used KNO scaling law to simulate the actual hadron multiplicity
- KNO scaling law relates the dispersion of hadron multiplicity at different invariant masses with a universal scaling function  $f(n/\langle n \rangle)$   
 $\langle n \rangle * P(n) = f(n/\langle n \rangle)$   
Where  $\langle n \rangle$  is the averaged hadron multiplicity and  $P(n)$  is the probability of generating hadrons
- The scaling function is parameterized by the Levy function
- 

$$L(z, c) = \frac{2e^{-c} c^{cz+1}}{\Gamma(cz+1)}$$



# What is GENIE?

- Dedicated webpage: [www.genie-mc.org](http://www.genie-mc.org)

## GENIE Collaboration

Luis Alvarez-Ruso [9], Costas Andreopoulos [5,7], Adi Ashkenazi [4], Christopher Barry [5], Francis Bench [5], Steve Dennis [5], Steve Dytman [6], Hugh Gallagher [8], Steven Gardiner [3], Walter Giele [3], Robert Hatcher [3], Or Hen [4], Libo Jiang [6], Rhiannon Jones [5], Igor Kakorin [2], Konstantin Kuzmin [2], Anselmo Meregaglia [1], Donna Naples [6], Vadim Naumov [2], Afroditi Papadopoulou [4], Gabriel Perdue [3], Marco Roda [5], Vladyslav Syrotenko [8], Jeremy Wolcott [8], Julia Tena Vidal [5], Julia Yarba [3]

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33175 Gradignan, France

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Dubna, Moscow region, 141980, Russia

3. Fermi National Accelerator Laboratory

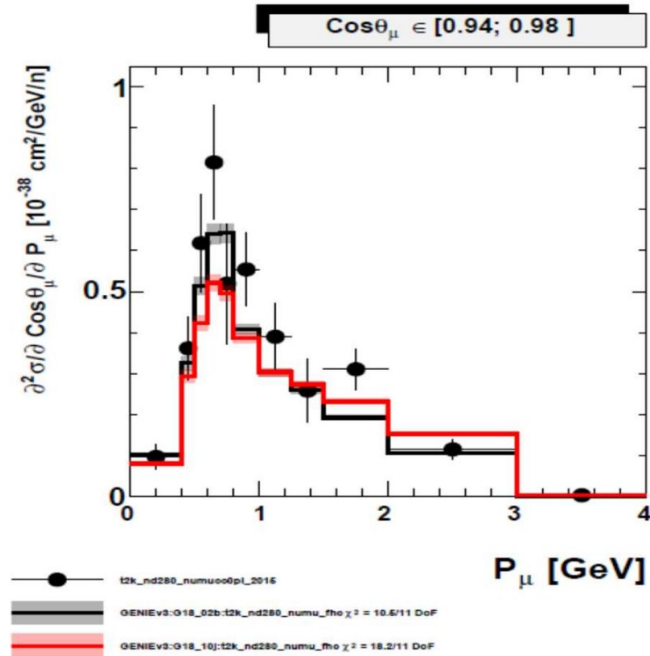
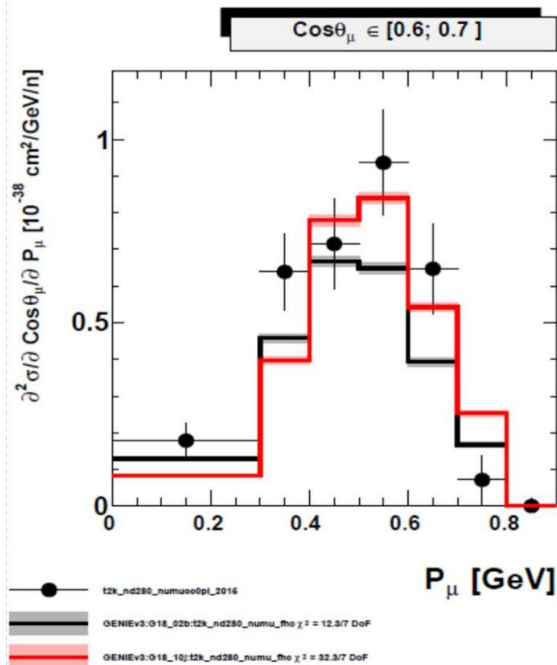
## Core GENIE mission - from GENIE by-law

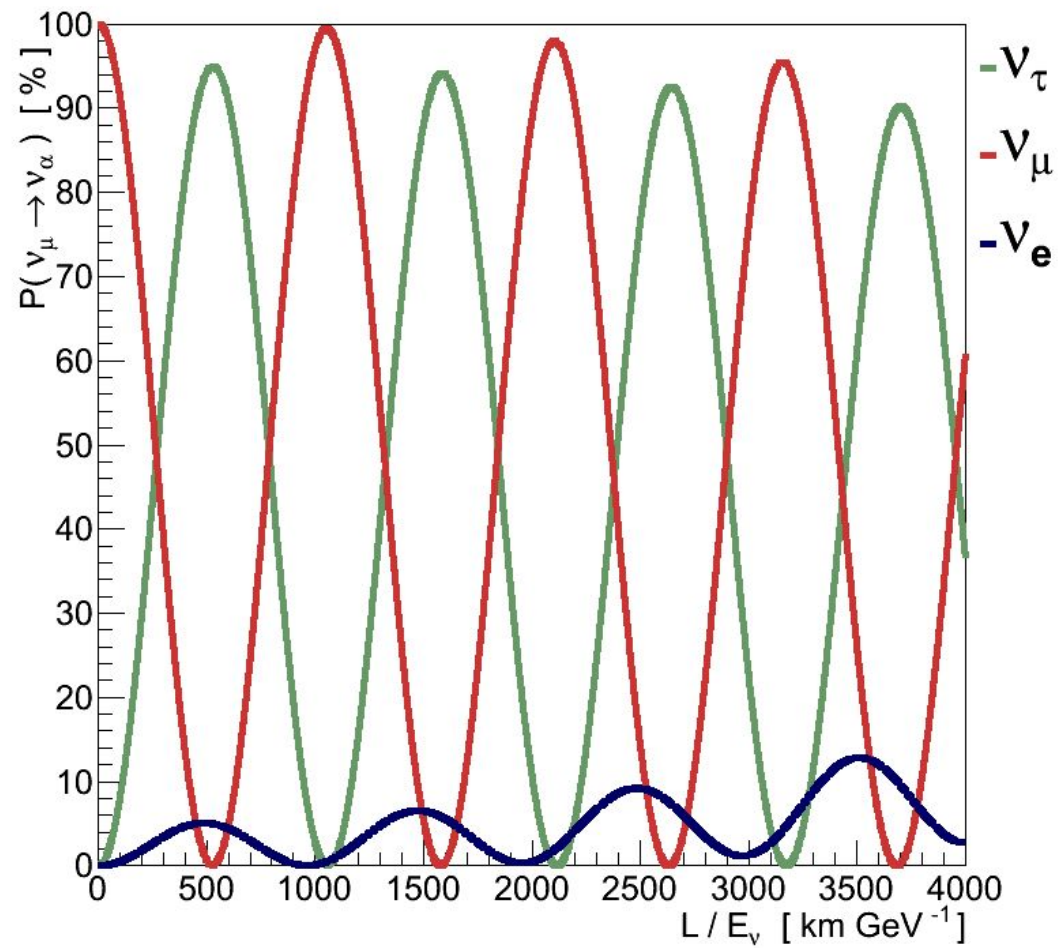
**Framework** “... provide a state-of-the-art neutrino MC generator for the world experimental neutrino community ...”

**Universality** “... simulate all processes for all neutrino species and nuclear targets, from MeV to PeV energy scales ...”

**Global fit** “... perform global fits to neutrino, charged-lepton and hadron scattering data and provide global neutrino interaction model tunes ...”

# T2K CC0 $\pi$ (2015)







# Standard Model of Elementary Particles + Gravity

three generations of matter (fermions)			interactions / force carriers (bosons)		
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
QUARKS	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> higgs
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>γ</b> photon	<b>G</b> graviton
	<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>Z</b> Z boson	
LEPTONS	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>W</b> W boson	

SCALAR BOSONS

HYPOTHETICAL  
TENSOR BOSONS

GAUGE BOSONS  
VECTOR BOSONS

# Introduction to Neutrinos : Oscillations

Three flavor neutrino model

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3}e^{i\delta} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$$U = \begin{pmatrix} \cos\theta_{12} & \sin\theta_{12} & 0 \\ -\sin\theta_{12} & \cos\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \times \begin{pmatrix} \cos\theta_{13} & 0 & e^{-i\delta_{CP}} \sin\theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta_{CP}} \sin\theta_{13} & 0 & \cos\theta_{13} \end{pmatrix} \times \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{23} & \sin\theta_{23} \\ 0 & -\sin\theta_{23} & \cos\theta_{23} \end{pmatrix}$$

If  $\delta \neq 0, \pi$ , then have **CP violation**  $\Rightarrow P(\nu_\mu \rightarrow \nu_e) \neq P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$

# Introduction to Neutrinos : Oscillations

Three flavor neutrino model

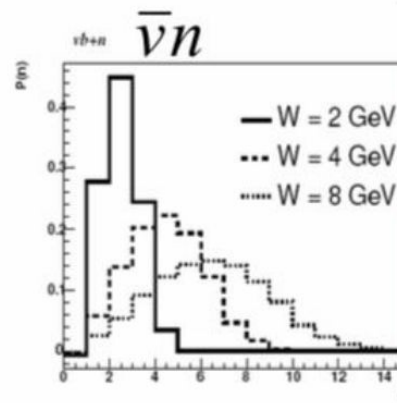
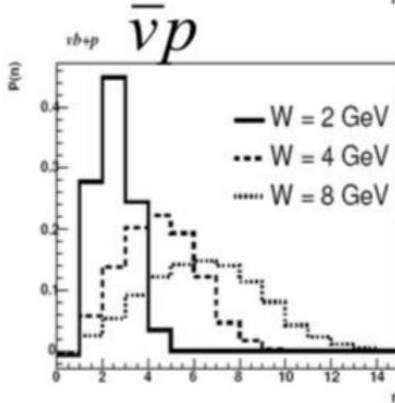
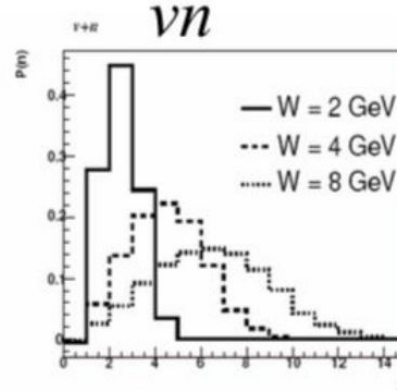
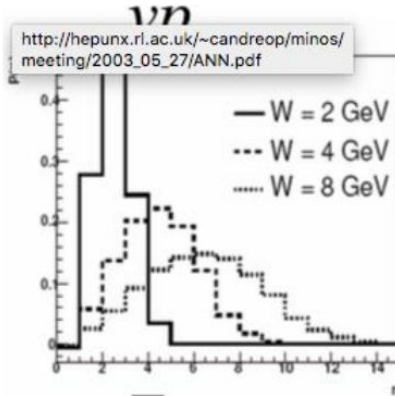
$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) \simeq & \boxed{\sin^2 \theta_{23}} \boxed{\sin^2 2\theta_{13}} \frac{\sin^2(\Delta_{31} - \boxed{aL})}{(\Delta_{31} - \boxed{aL})^2} \Delta_{31}^2 \\
 & + \boxed{\sin 2\theta_{23}} \boxed{\sin 2\theta_{13}} \sin 2\theta_{12} \frac{\sin(\Delta_{31} - \boxed{aL})}{(\Delta_{31} - \boxed{aL})} \Delta_{31} \frac{\sin \boxed{aL}}{\boxed{aL}} \Delta_{21} \cos(\Delta_{31} - \delta_{\text{CP}}) \\
 & + \boxed{\cos^2 \theta_{23}} \sin^2 2\theta_{12} \frac{\sin^2 \boxed{aL}}{\boxed{aL}^2} \Delta_{21}^2,
 \end{aligned}$$

- parameters to determine
  - CP violation phase  $\delta$
  - Mass hierarchy
  - 3 Mixing angles

$$a = G_F N_e / \sqrt{2}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

# Multiplicity probability distributions



- We obtain them directly from the hadronization model ( $W < 2.3 \text{ GeV}$ )
- $P(m, W)$  probability distribution

$$\langle n \rangle = a + b \ln W$$

$$\langle n \rangle \cdot P(n) = 2e^{-c} \frac{c^{\frac{n}{\langle n \rangle} + 1}}{\Gamma\left(c \frac{n}{\langle n \rangle} + 1\right)}$$

# GENIE Reweighting Scheme

- Propagating neutrino interaction uncertainties
- For a physical quantity  $P$ , introduce a systematics parameter  $x_p$ . Tweaking this systematic parameter modifies the corresponding physics parameter  $P$  as follows:

$$P \rightarrow P' = P(1 + x_p * (\delta P / P))$$

$\delta P$  is the standard deviation of  $P$ .

Tweaking the systematic parameter by  $\pm 1$  modifies

the corresponding physics quantity  $P$  by  $\pm P$

# Pythia

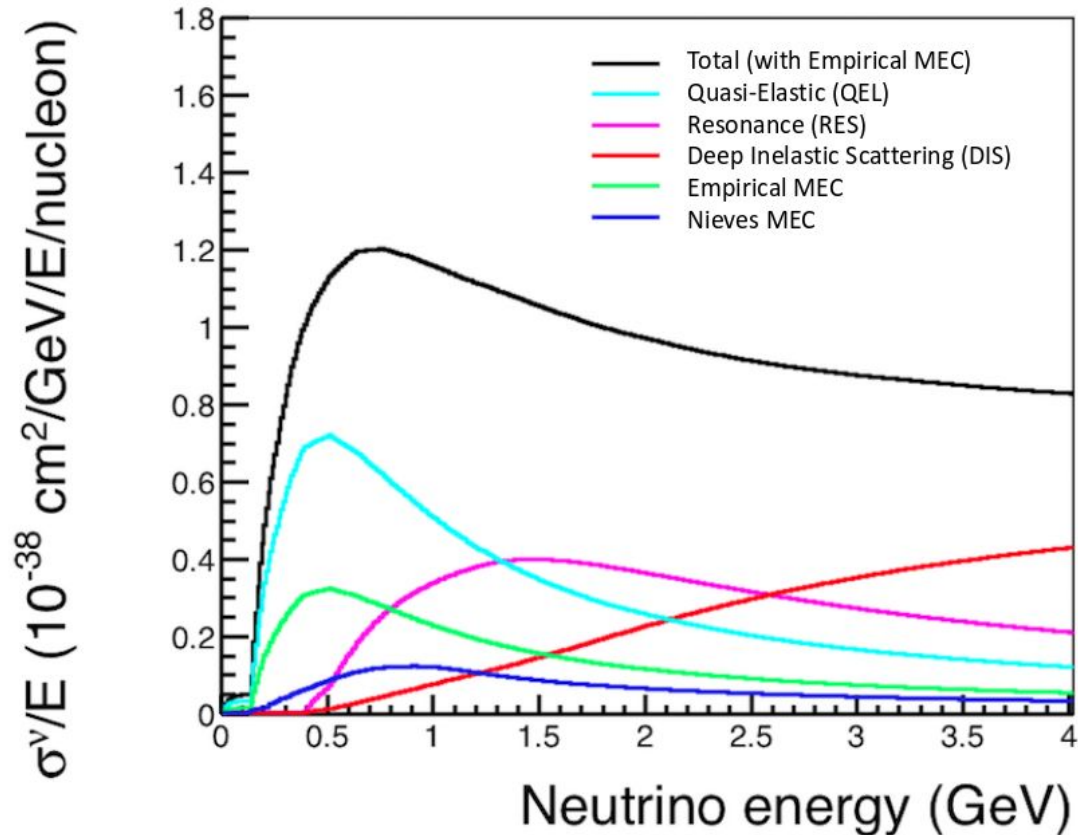
- The high invariant mass hadronization is performed by the PYTHIA model [85]. The PYTHIA program is a standard tool for the generation of high-energy collisions, comprising a coherent set of physics models for the evolution from a few-body hard process to a complex multi-hadronic final state. **It contains a library of hard processes and models for initial- and final-state parton showers, multiple parton-parton interactions, beam remnants, string fragmentation and particle decays.** The hadronization model in PYTHIA is based on the Lund string fragmentation framework.
- Fragmentation in PYTHIA is described by the Lund string fragmentation model, which is a model based on the dynamics of one-dimensional relativistic strings that are stretched between colored partons
- **Tuned on BEBC data.**

transverse momentum,  $p_{\perp}^2 (= p_x^2 + p_y^2)$ , for the produced hadron. The fraction of  $E + p_z$  taken by the produced hadron is given by the variable  $z$ , defined by the hadron energy  $E$  and energy transfer  $\nu$  ( $z = E/\nu$ ). An associated fragmentation function  $f(z)$  gives the probability that a given  $z$  is chosen. The simplified Lund symmetric fragmentation function is given by,

$$f(z) \propto z^{-1} (1-z)^a \cdot \exp\left(\frac{-bm_{\perp}^2}{z}\right). \quad (1)$$

Here,  $m_{\perp}^2$  is the transverse mass of the hadron ( $m_{\perp}^2 \equiv m^2 + p_{\perp}^2$ ). The Gaussian term describes quantum tunneling in the transverse direction, and tunable “Lund  $a$ ” and “Lund  $b$ ” parameters decide the longitudinal distribution of energy. Thus, these two parameters mainly decide how to distribute available energy to the produced hadrons. Fig. 1 shows the Lund symmetric

# Total Cross Section



# Simulation in Neutrino Oscillation Physics

- **Interface between neutrino flux and experimental observables**

- Calculate predictions
- Constrain flux ( $\nu$ -electron scattering)



- **Compare data with event generator models**

- Cross sections
- Experimental distributions:  $P$ ,  $\theta$
- Understanding models is key



- **Compare dataset against dataset**

- Data quality is increasing, analysis are improving
  - Inconsistency/bias can be introduced
- Highlight tensions → can not use a single model to do everything (e.g. MINERvA and MinibooNE QE-like).

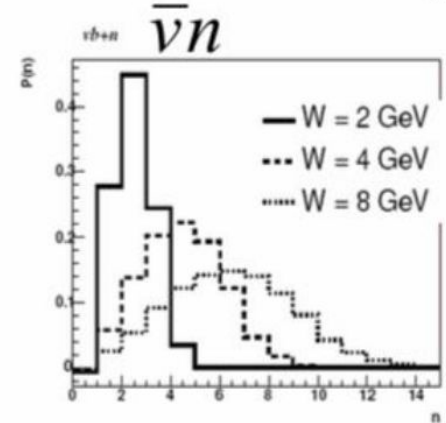
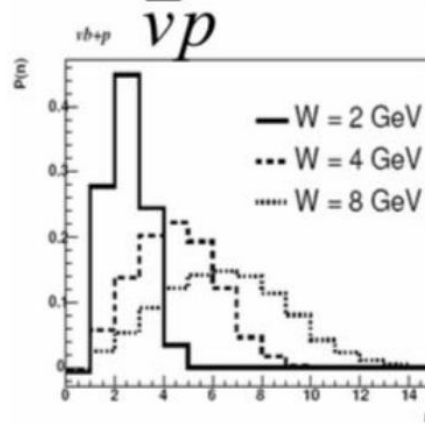
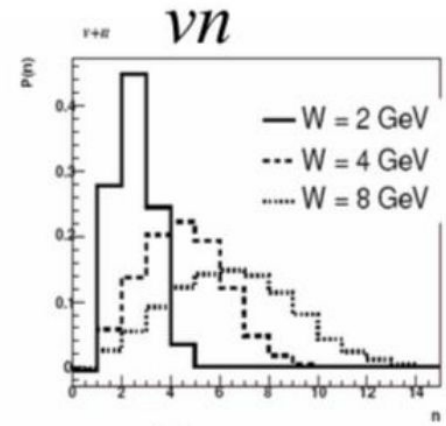
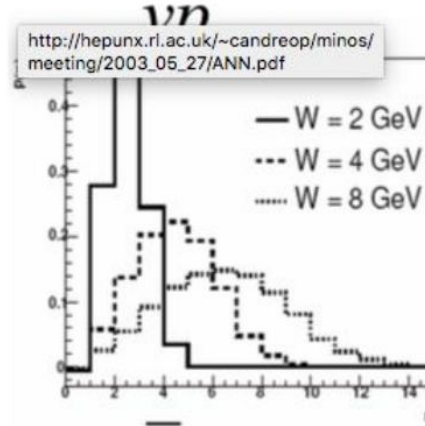


# How does GENIE work? - KNO Model

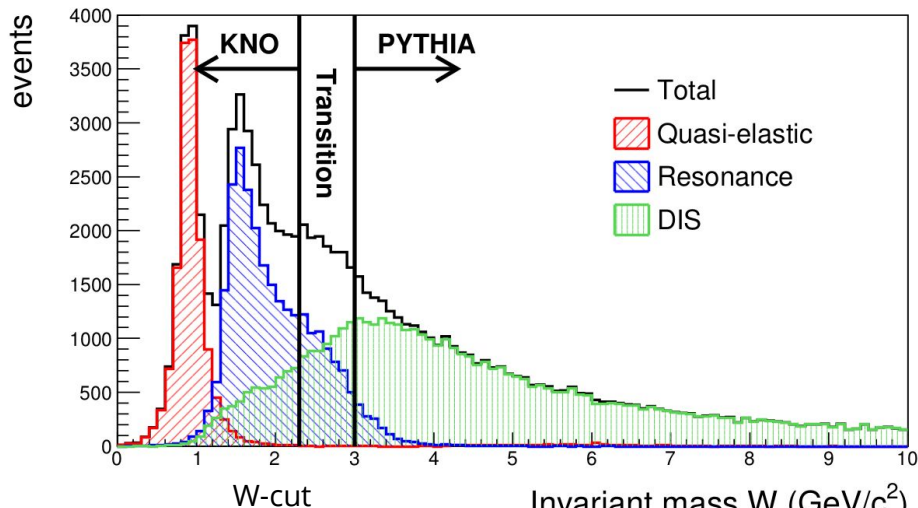
- Averaged charged hadron multiplicity data are fit to a function of invariant mass squared,  $W^2$   
 $\langle n_{\text{ch}} \rangle = a_{\text{ch}} + b_{\text{ch}} \cdot \log W^2$
- Total hadron multiplicity  $\langle n \rangle = 1.5 \cdot \langle n_{\text{ch}} \rangle$
- probability distribution  $P(n, W) \cdot \langle n \rangle$  parameterized by the Levy function

$$\langle n \rangle = a + b \ln W$$

$$\langle n \rangle \cdot P(n) = 2e^{-c} \frac{c^{\frac{n}{\langle n \rangle} + 1}}{\Gamma\left(c \frac{n}{\langle n \rangle} + 1\right)}$$



# How does GENIE work? - Modeling the Transition Region



$$\frac{d^2\sigma^{inel}}{dQ^2 dW} = \frac{d^2\sigma^{RES}}{dQ^2 dW} + \frac{d^2\sigma^{DIS}}{dQ^2 dW}$$

**Non-Resonant Background**  
Contribution to this particular  
multiplicity channel

$W < W_{cut}$ : RES+scaled DIS with some multiplicity factors

- $f_m = R_m \cdot P_m$
- $m$ =multiplicity of the hadronic system
  - 2 for  $1\pi$
  - 3 for  $2\pi$
- $R_m$  Tunable parameter
- $P_m$  Is the probability that the DIS final state has multiplicity  $m$ , obtained directly from the hadronization model.

$W > W_{cut}$ : Pure DIS model (not scaled)

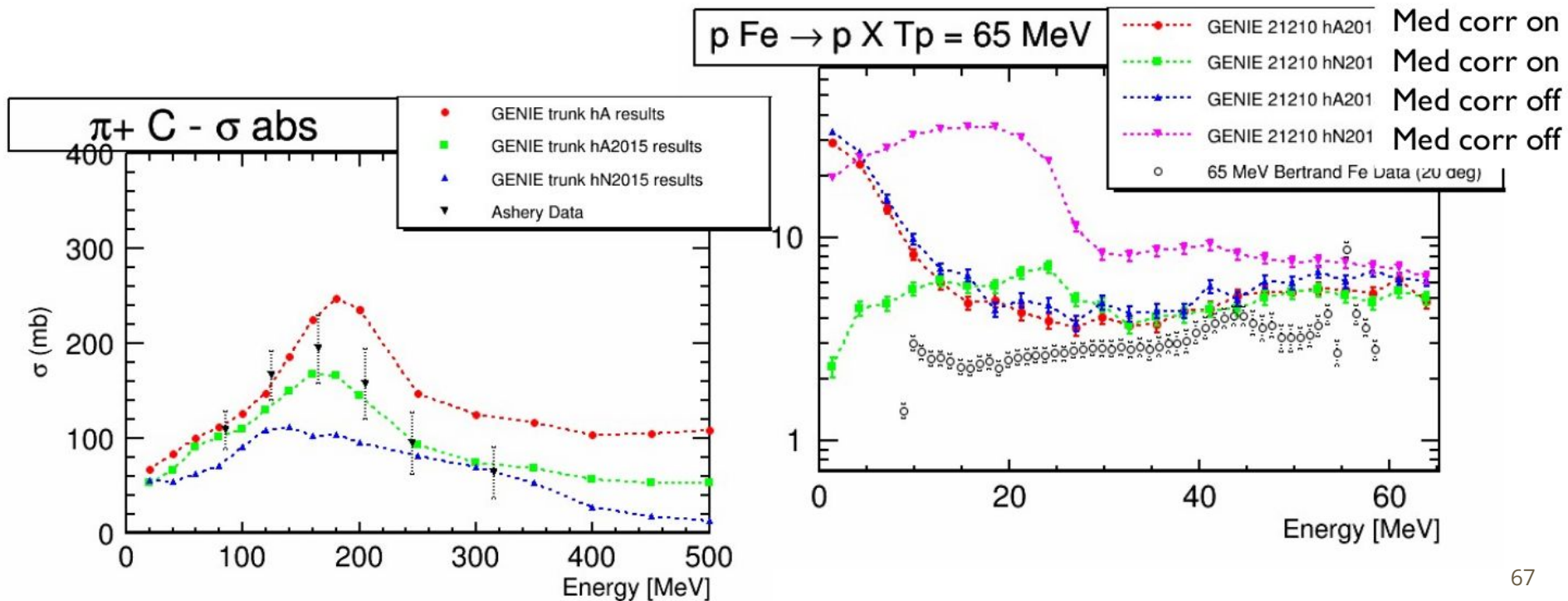
$$\frac{d^2\sigma^{RES}}{dQ^2 dW} = \sum_k \left( \frac{d^2\tilde{\sigma}^{RES}}{dQ^2 dW} \right) \cdot \Theta(W_{cut} - W)$$

$$\frac{d^2\sigma^{DIS}}{dQ^2 dW} = \left( \frac{d^2\tilde{\sigma}^{DIS}}{dQ^2 dW} \right) \cdot \Theta(W - W_{cut})$$

$$+ \left( \frac{d^2\tilde{\sigma}^{DIS}}{dQ^2 dW} \right) \cdot \Theta(W_{cut} - W) \left( \sum_m f_m \right)$$

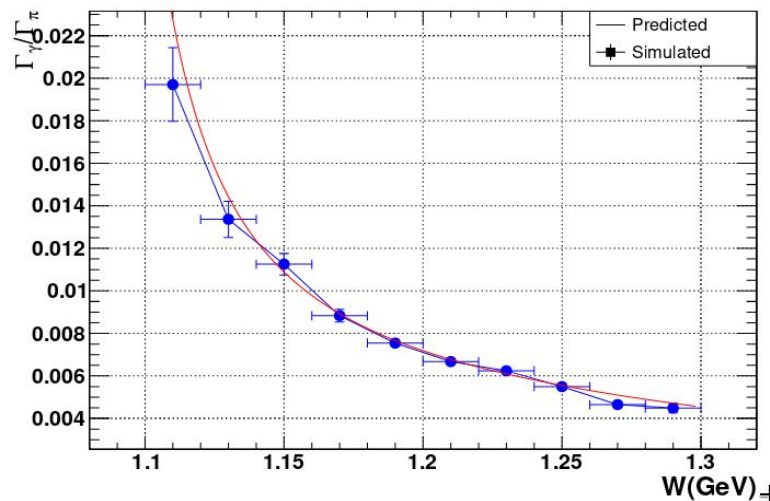
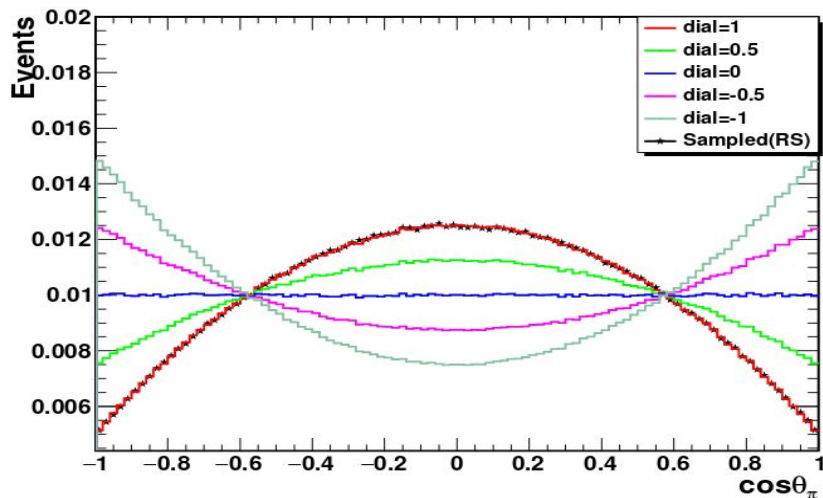
# How does GENIE work? - FSI model

- hA 2018 is latest version of schematic model
- Recent emphasis on medium corr. hN2018 is new intranuclear cascade (INC) model with same nuclear medium corrections( $\pi N$ ) as NuWro
- Medium corrections suppress multiple scattering, decrease cross section. Strong A dependence!



# Improvements of Delta Decay

- Sampled  $\pi$  angular distributions from Delta decay non-isotropically with function.
  - Parameters in the function come from fitting to ANL and BNL(same as NuWRO)
- Branching Ratio between  $\Delta \rightarrow N + \gamma$  and  $\Delta \rightarrow N + \pi$  changed from a constant into a function of  $W$



# How to get GENIE

- If you are an experimentalist at Fermilab, you can set it up through UPS:
  - <https://cdcv.s.fnal.gov/redmine/projects/genie/wiki>
- You can easily get the source code from github and build it on Linux
  - <https://github.com/GENIE-MC/Generator.git>
- You can build on a Mac/windows also, but we do not have a pre-packed script
  - Additional products need to setup to build GENIE, e.g. ROOT, LHAPDF, Pythia...
- New Physics And User Manual in preparation (private temporarily)