

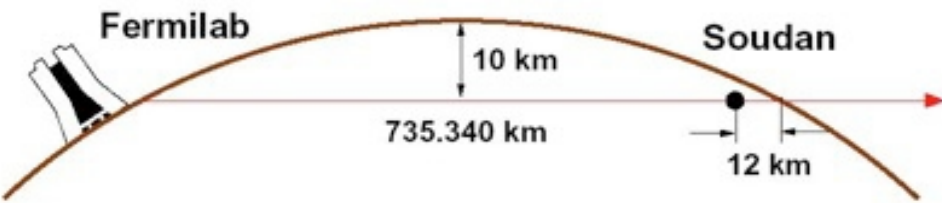
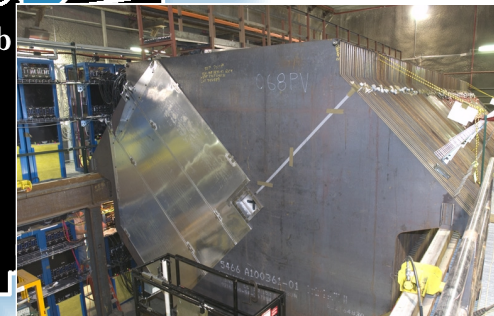
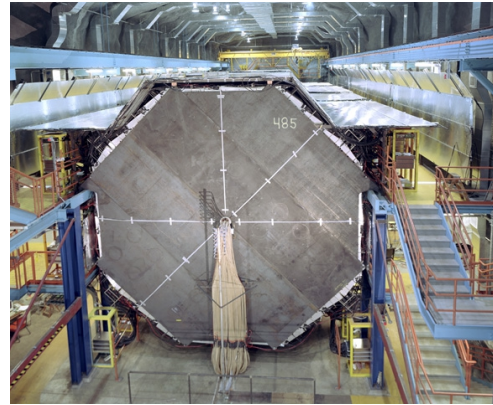
Measuring Neutrino Oscillations with the MINOS Experiment



Alexander Radovic
University College London

MINOS

- MINOS or Main Injector Neutrino Oscillation Search
- Uses Neutrinos from the NuMI beam line
- Has a peak L/E of $\sim 250 \text{ km/GeV}$
- Leading measure of $|\Delta m_{\text{atm}}^2|$



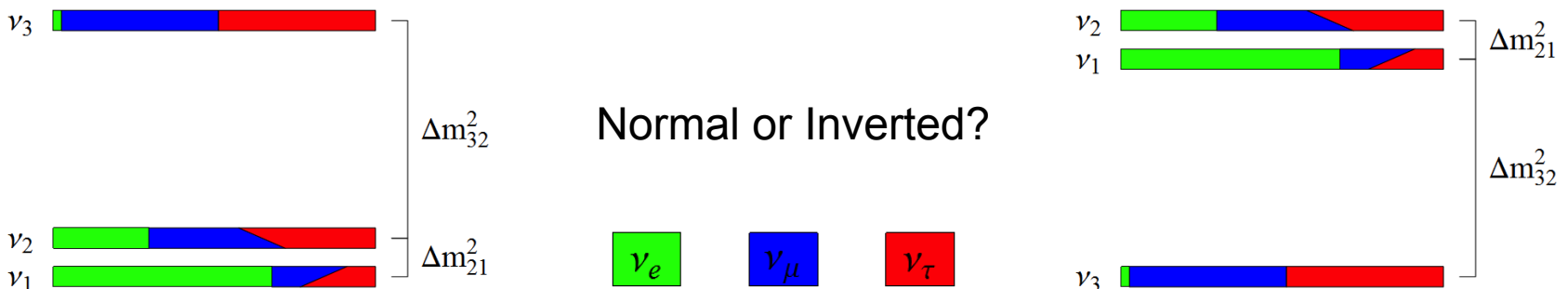
MINOS Physics Goals

NEW

- The measurement of **3ν** oscillations via the study of the NuMI and atmospheric neutrinos

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U^* \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \quad P(\nu_\alpha \rightarrow \nu_\beta) = \left| \sum_j U_{\beta j}^* e^{-i \frac{m_j^2 L}{2E}} U_{\alpha j} \right|^2$$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

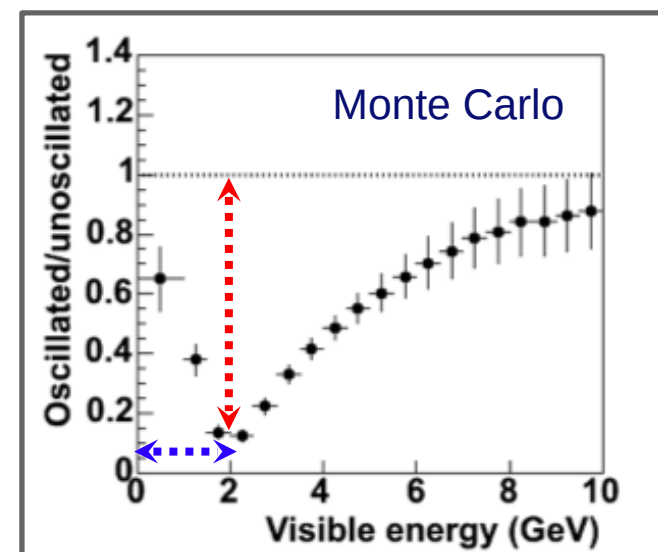
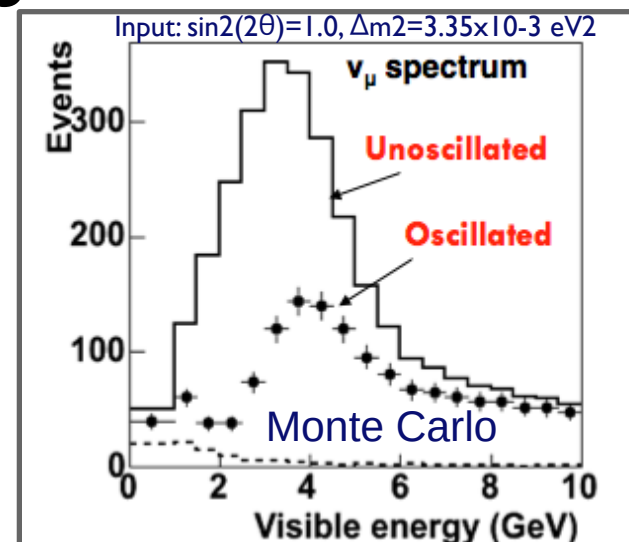


NuMI Neutrino Disappearance

- Precise measurement of muon neutrino disappearance
- Direct measurement of muon antineutrino disappearance
- Far detector prediction from near detector is compared to far detector measurement
- Neutrino oscillations deplete rate and distort the energy spectrum

$$P(\nu_\mu \rightarrow \nu_\mu) \approx$$

$$1 - \sin^2(2\theta_{23}) \sin^2\left(\frac{1.27\Delta m_{atm}^2 L}{E}\right)$$



NuMI Neutrino Appearance

- Muons can also oscillate into electron neutrinos, giving us power to measure:
 - θ_{13}
 - δ_{cp}
 - θ_{23} octant
 - Mass hierarchy

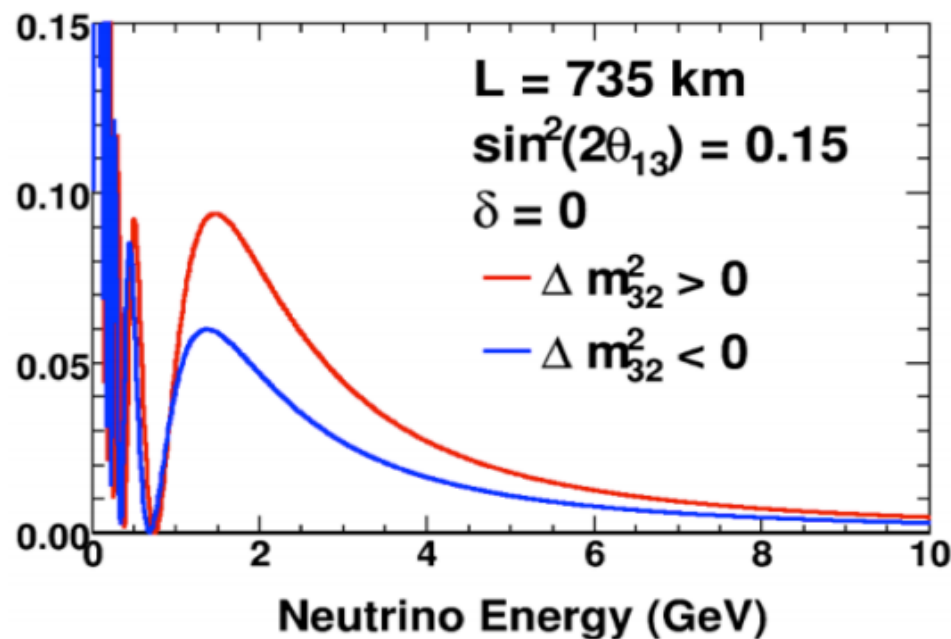
$$P(\nu_\mu \rightarrow \nu_e) \approx \left| \sqrt{P_{atm}} e^{-i\left(\frac{\Delta m_{32}^2 L}{4E} + \delta_{cp}\right)} + \sqrt{P_{sol}} \right|^2$$

$$P_{atm} = \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$

Solar term contributes
<1% at MINOS L/E

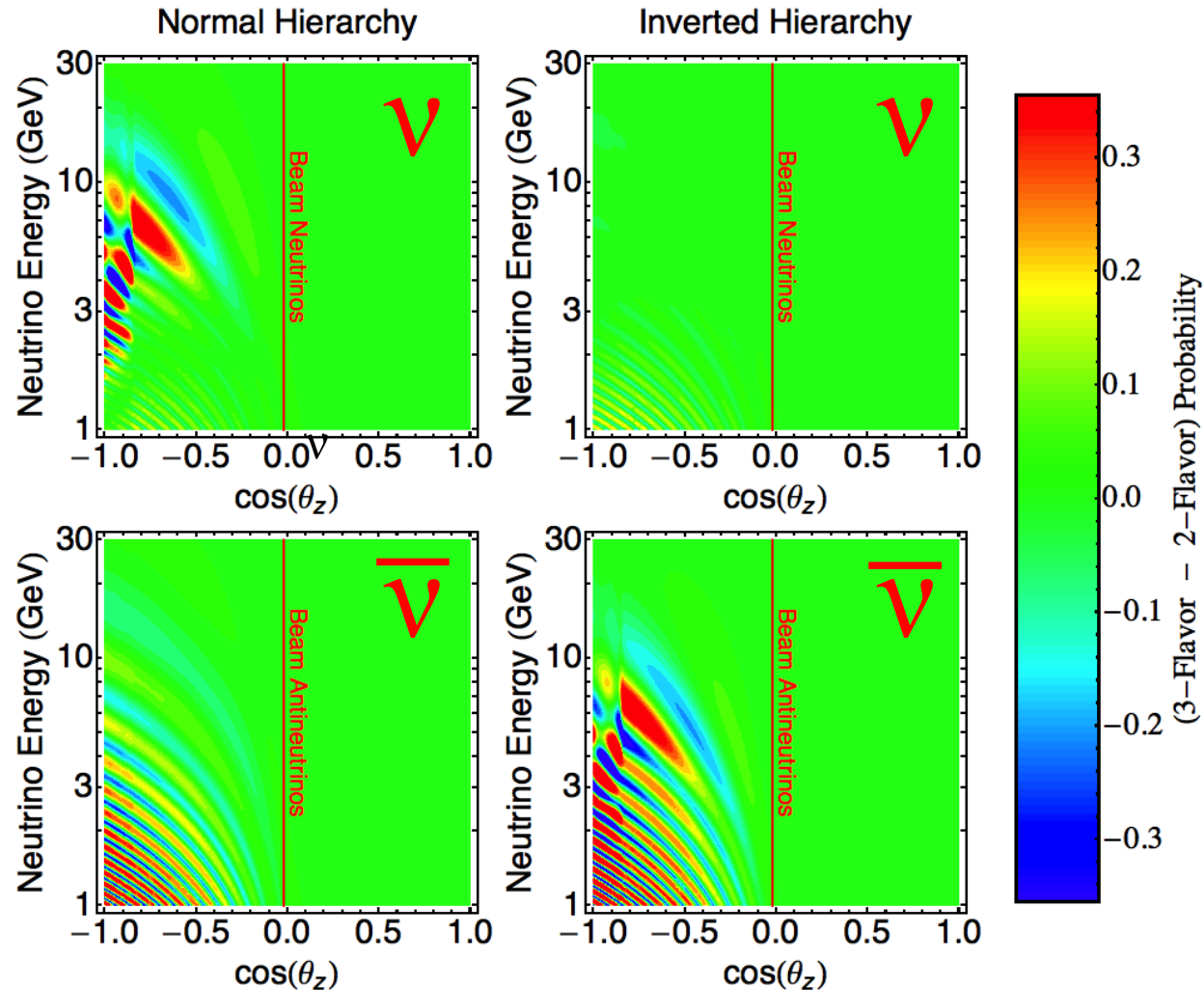
NuMI Neutrino Appearance

- Muons can also oscillate into electron neutrinos, giving us power to measure:
 - θ_{13}
 - δ_{cp}
 - θ_{23} octant
 - Mass hierarchy
- Electron neutrinos experience an extra CC interaction as they pass through matter, modifying oscillation probabilities



Atmospheric Neutrino Disappearance

- Very long baselines through matter compared to NuMI disappearance analysis
- Some sensitivity to θ_{23} octant, mass hierarchy and δ_{cp}

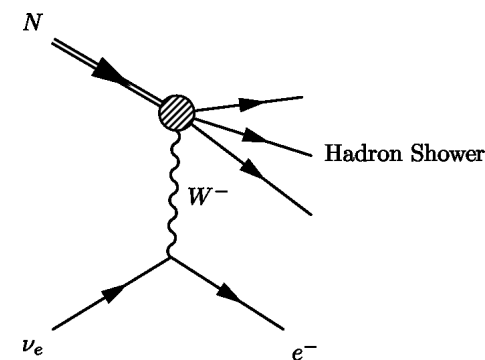
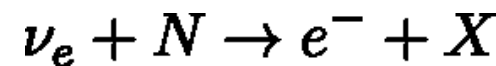
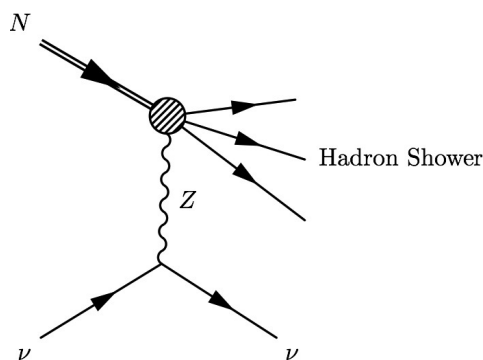
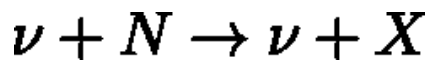
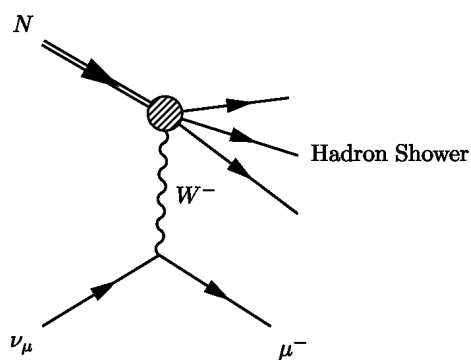
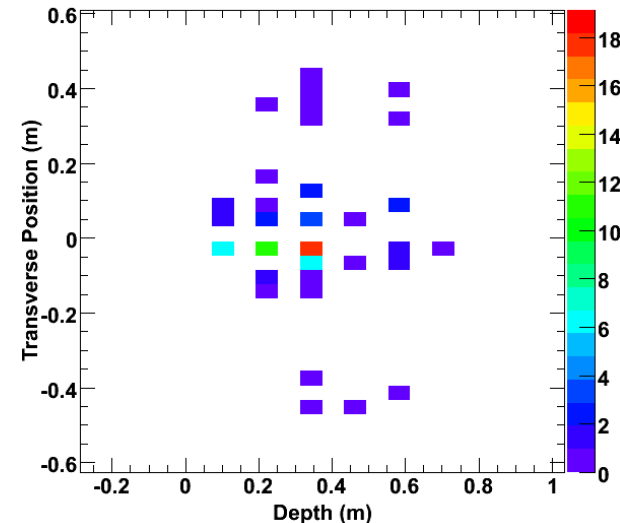
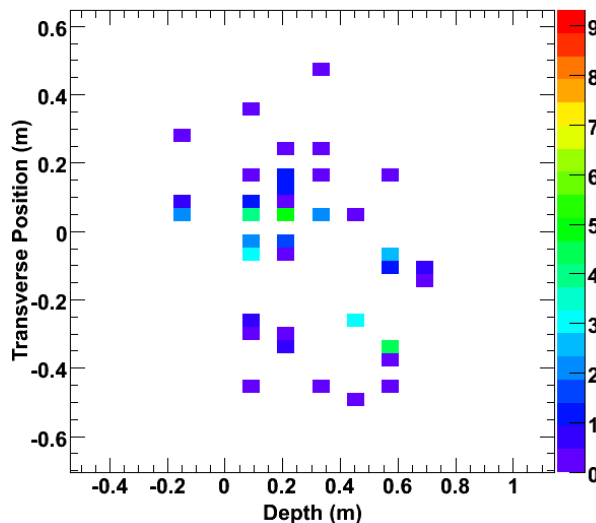
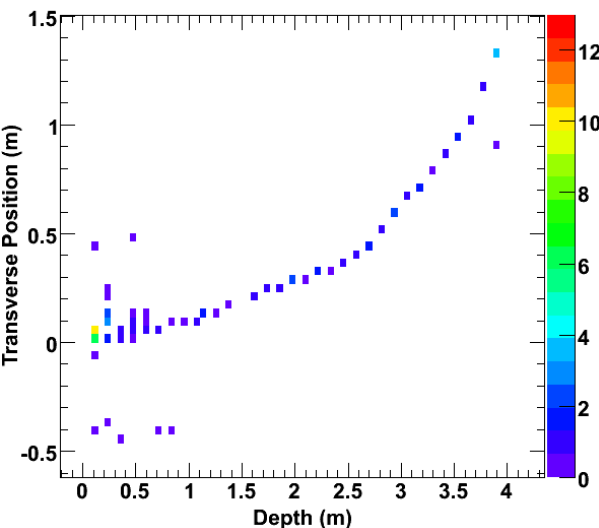


MC Event Topologies

ν_μ Charged Current (CC)

Neutral Current (NC)

ν_e CC



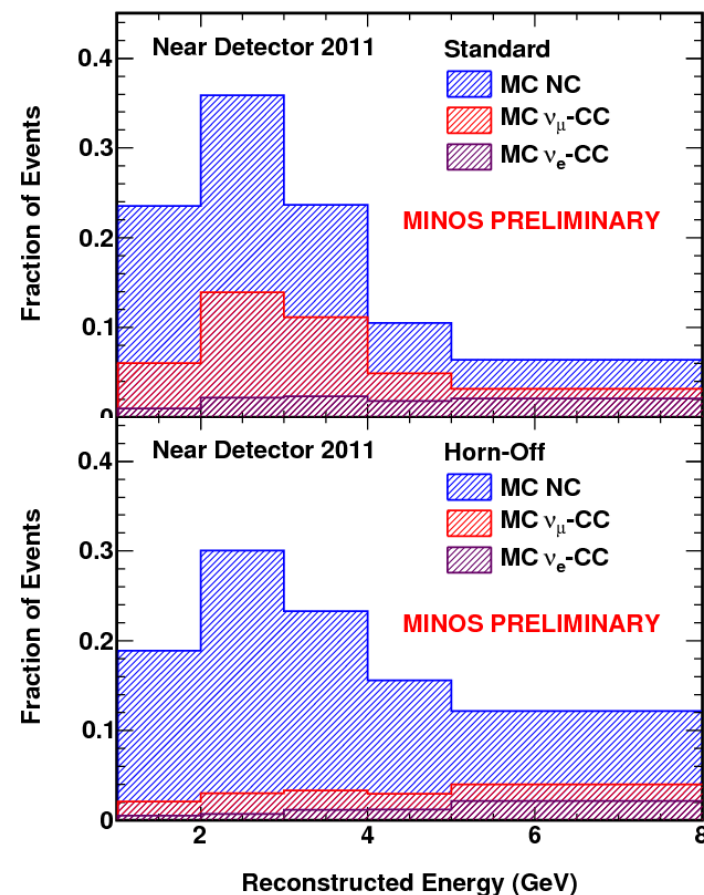
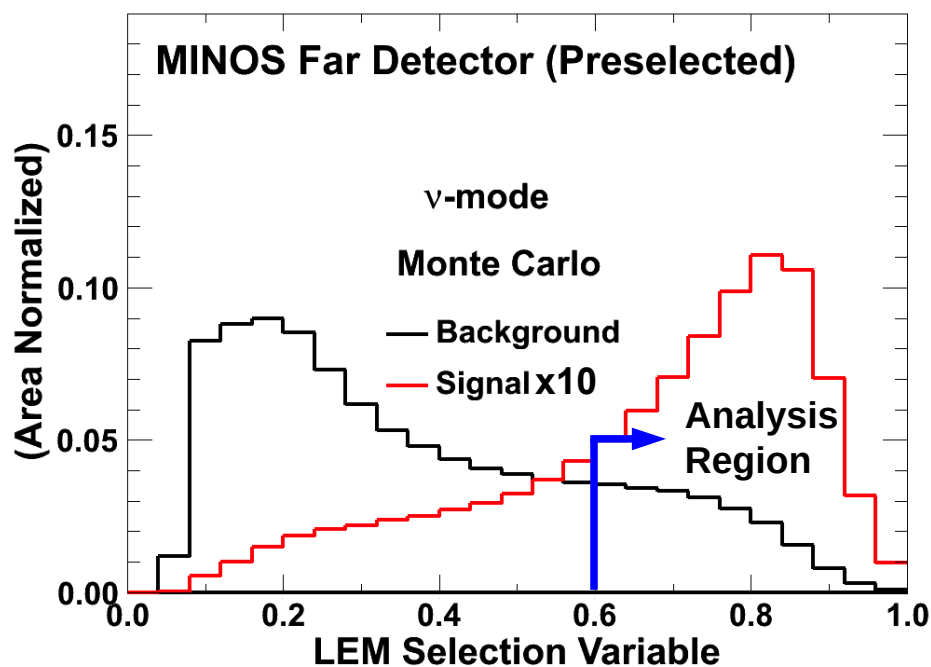
Electron Neutrino Appearance

Electron Neutrino Appearance

- MINOS detector granularity makes ν_e CC identification challenging

identification challenging

- Background estimation based on Near Detector data
- Compare candidate events to a library of MC using “Library Event Matching” (LEM)



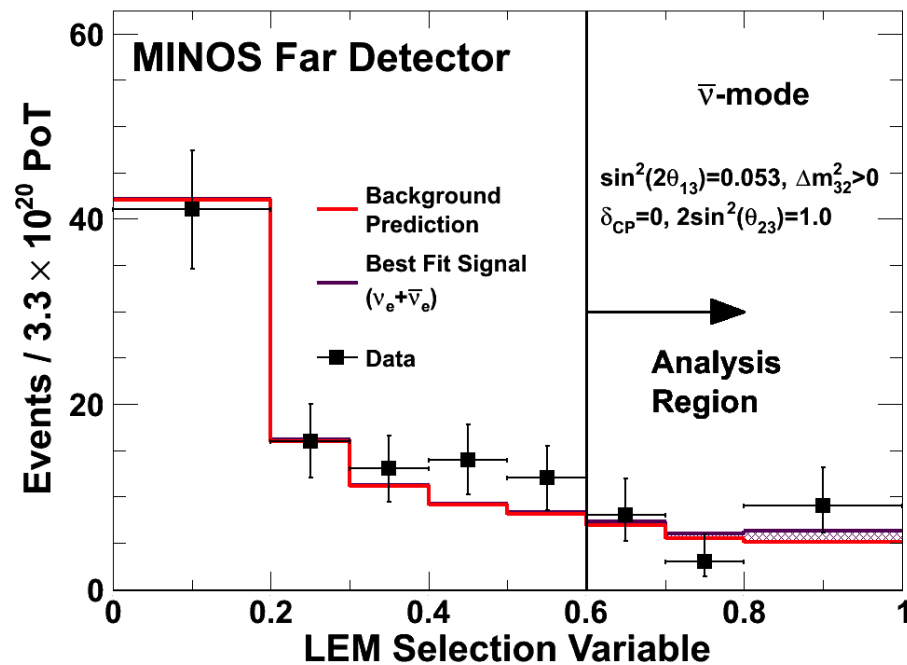
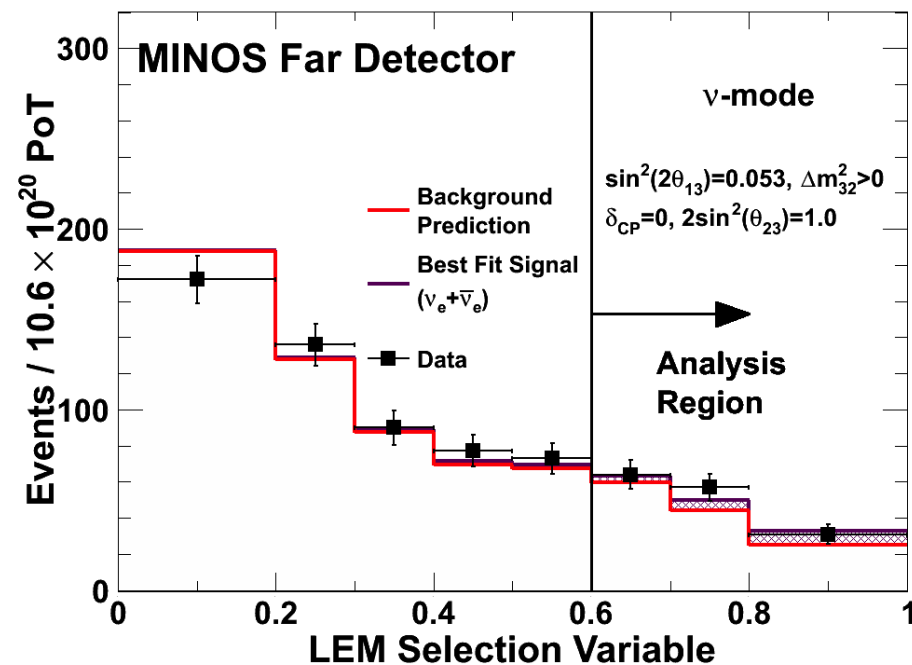
Electron Neutrino Appearance

With the *neutrino-enhanced* beam in Signal Enhanced Region:

- If $\theta_{13} = 0$: 128.6 BG Events
- If $\sin^2(2\theta_{13}) = 0.1$: +32.5 Events
- Total Prediction: 161 Events
- Observed: 152 Events

With the *antineutrino-enhanced* beam in Signal Enhanced Region:

- If $\theta_{13} = 0$: 17.5 BG Events
- If $\sin^2(2\theta_{13}) = 0.1$: +3.7 Events
- Total Prediction: 21.2 Events
- Observed: 20 Events



Combined Electron Neutrino Appearance

Cannot distinguish between ν_e and anti- ν_e events, so we perform a combined analysis:

At $\delta_{CP} = 0$ and $\theta_{23} < \pi/4$,

- Assuming normal hierarchy:

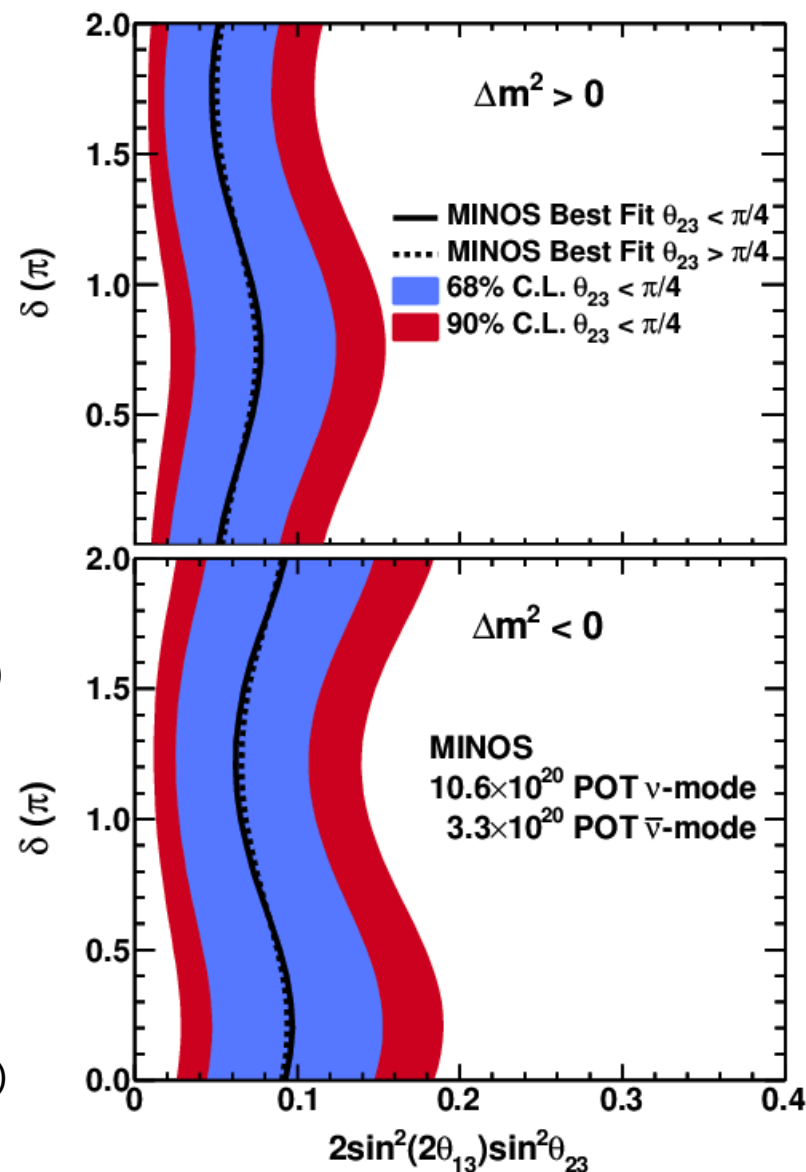
$$2 \sin^2(2\theta_{13}) \sin^2(\theta_{23}) = 0.051^{+0.038}_{-0.030}$$

$$0.01 < 2 \sin^2(2\theta_{13}) \sin^2(\theta_{23}) < 0.12 \text{ (90\% C.L.)}$$

- Assuming inverted hierarchy:

$$2 \sin^2(2\theta_{13}) \sin^2(\theta_{23}) = 0.093^{+0.054}_{-0.049}$$

$$0.03 < 2 \sin^2(2\theta_{13}) \sin^2(\theta_{23}) < 0.18 \text{ (90\% C.L.)}$$



Muon Neutrino Disappearance

Neutrino Disappearance

- Five distinct data sets are used to study muon neutrino disappearance:
 - 10.7×10^{20} POT in “neutrino-enhanced” NuMI beam
 - Muon neutrino charged current interactions
 - Anti muon neutrino charged current interactions
 - 3.4×10^{20} POT in “antineutrino-enhanced” NuMI beam
 - Anti-muon neutrino charged current interactions
 - 37.9 kton-years of atmospheric neutrinos
 - Muon neutrino charged current interactions
 - Anti muon neutrino charged current interactions

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Neutrino Disappearance

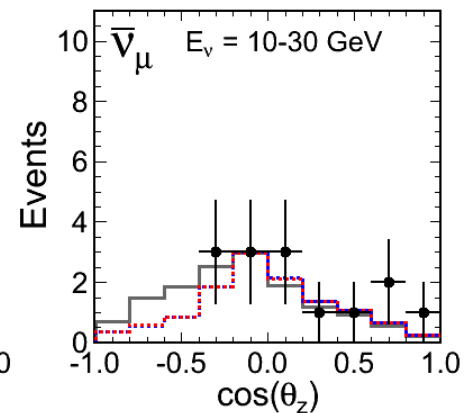
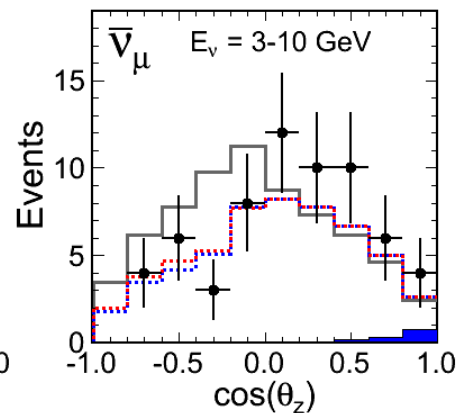
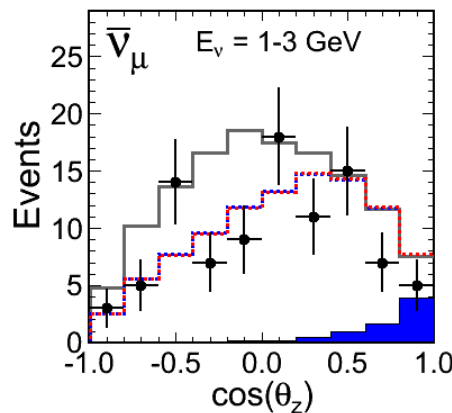
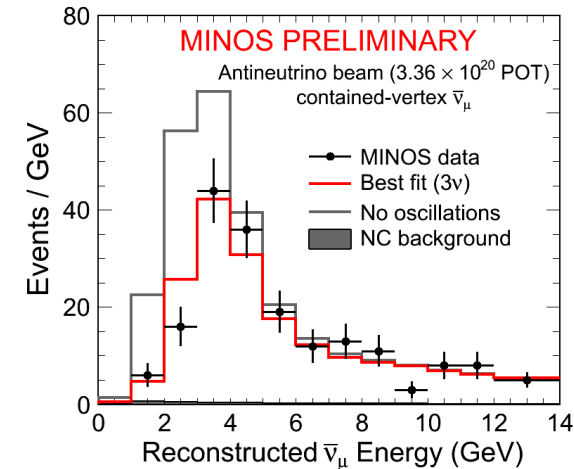
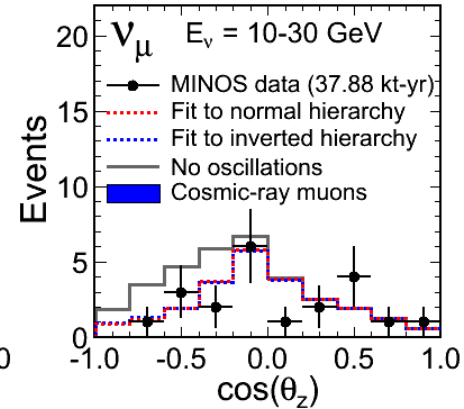
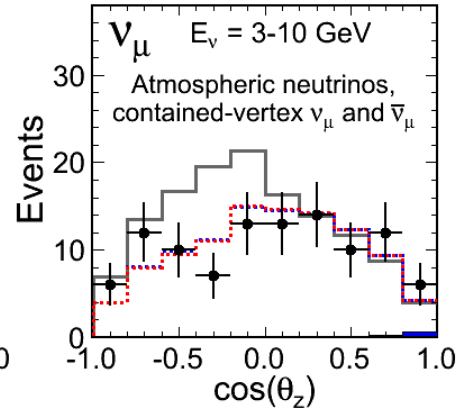
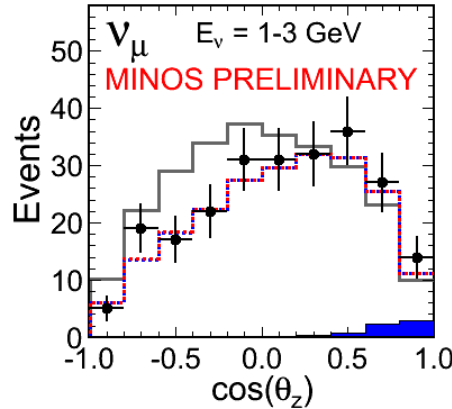
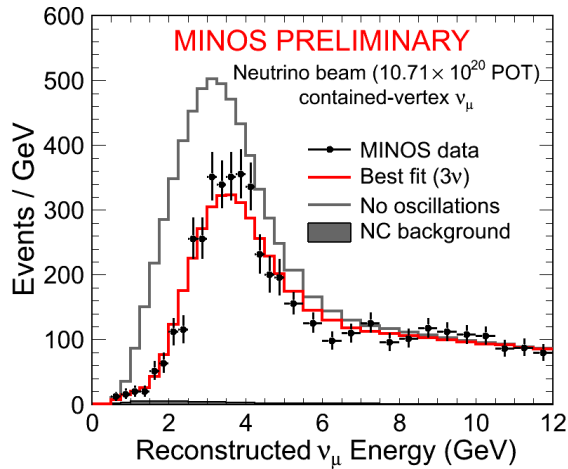
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Neutrino Disappearance

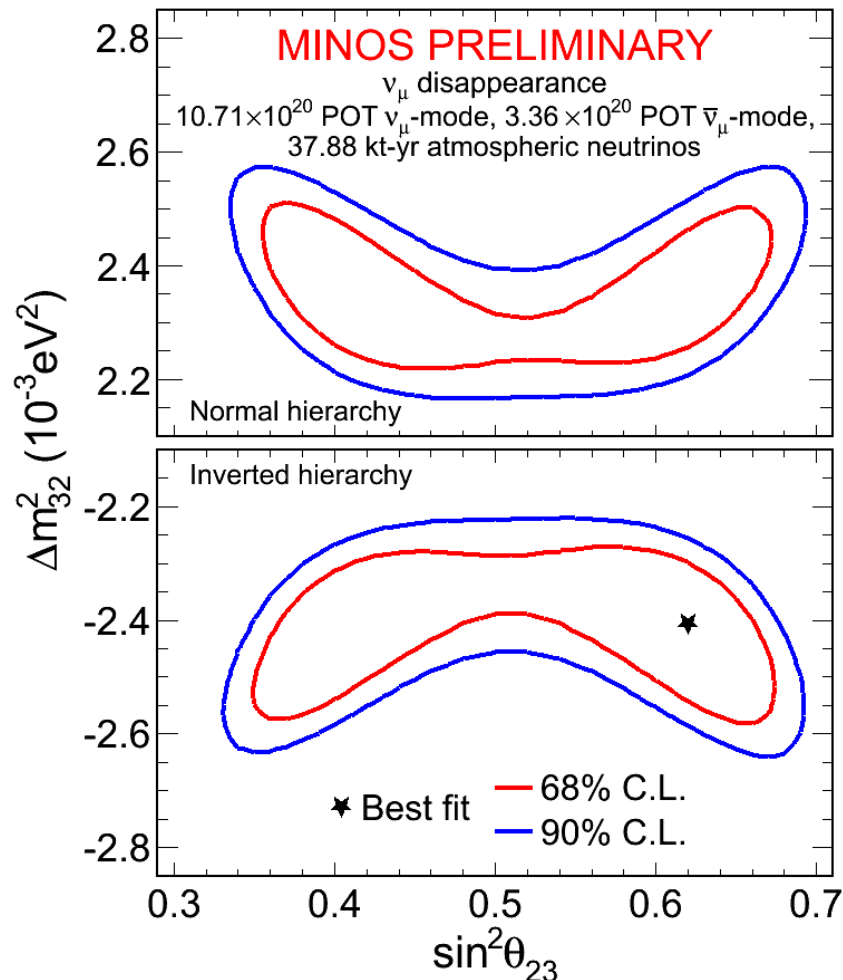
NEW



Combined Beam and Atmospheric Neutrino Disappearance Best Fit

NEW

- Assumes identical neutrino and antineutrino mixing parameters
- Gaussian constraint based on world knowledge of θ_{13}
- δ_{cp} allowed to freely float in $[0, 2\pi]$ range
- Other mixing parameters set at world's best knowledge
- 15 systematics included as nuisance parameters

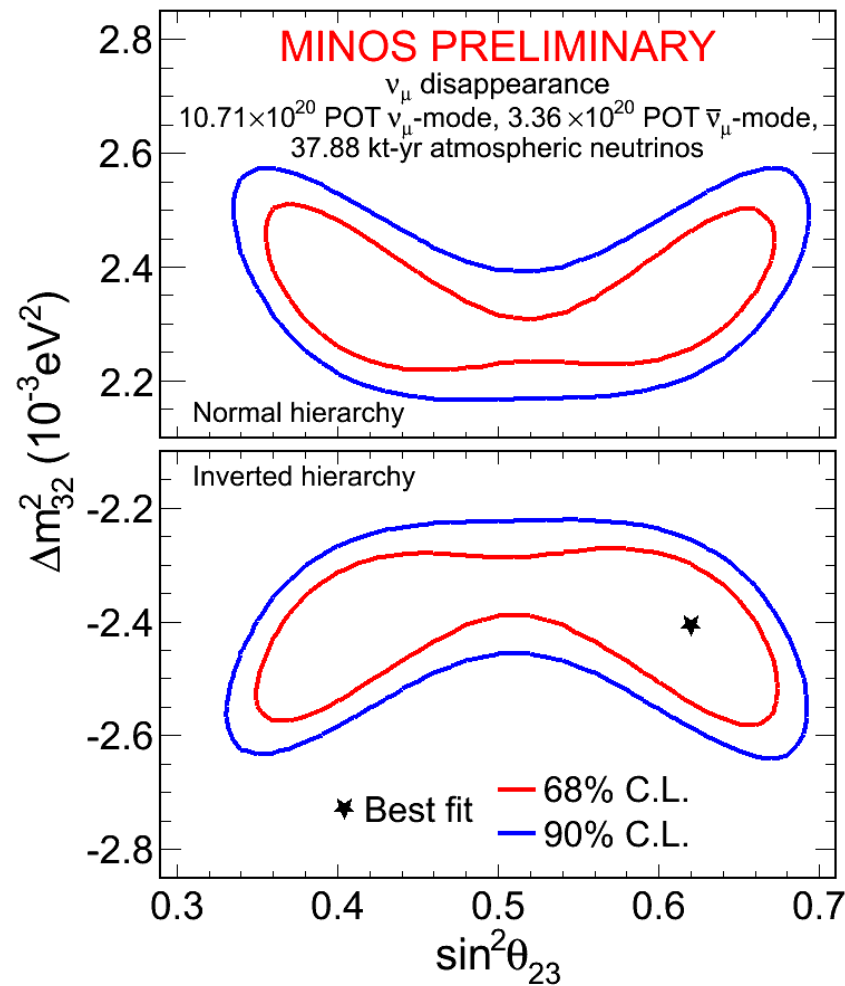


Combined Muon Disappearance and Electron Neutrino Appearance

Combined Neutrino Appearance and Disappearance Best Fit

NEW

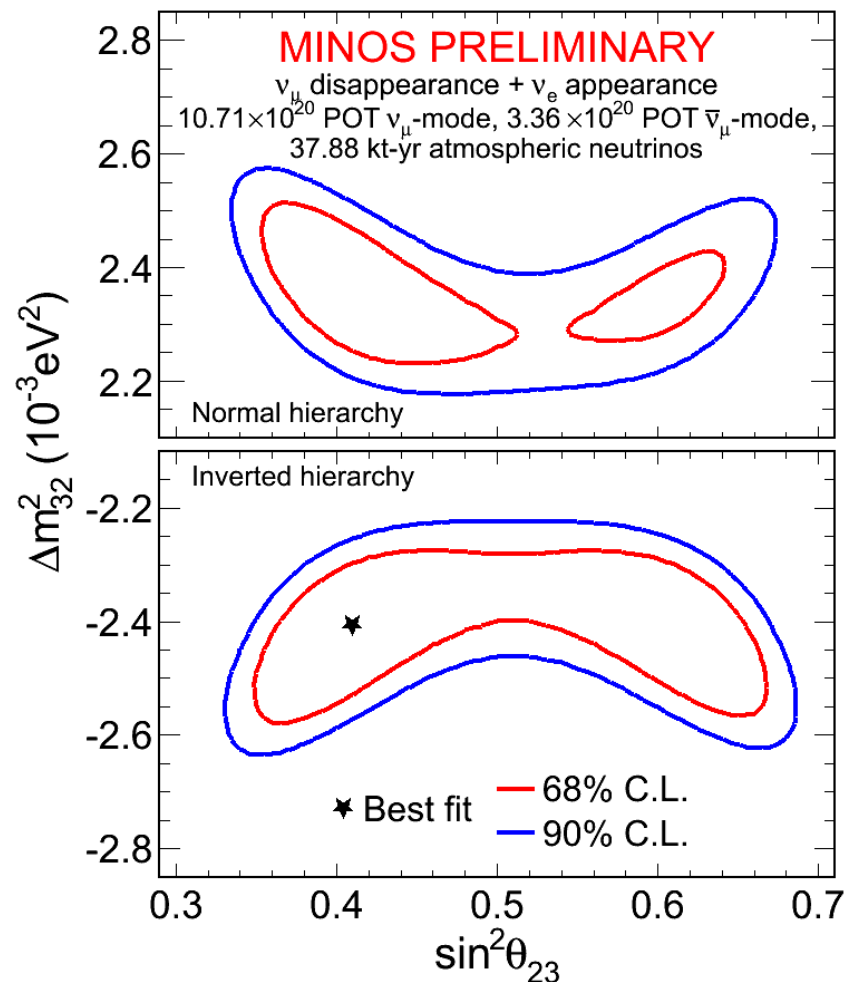
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- Appearance systematics included, assumes no correlation with disappearance



Combined Neutrino Appearance and Disappearance Best Fit

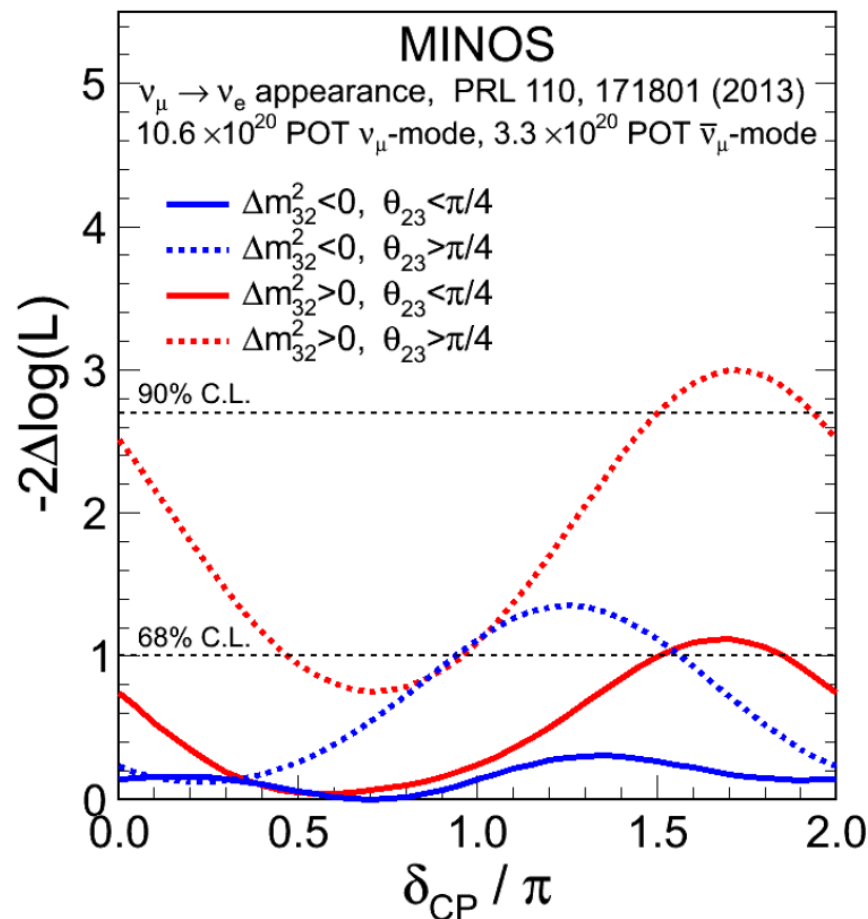
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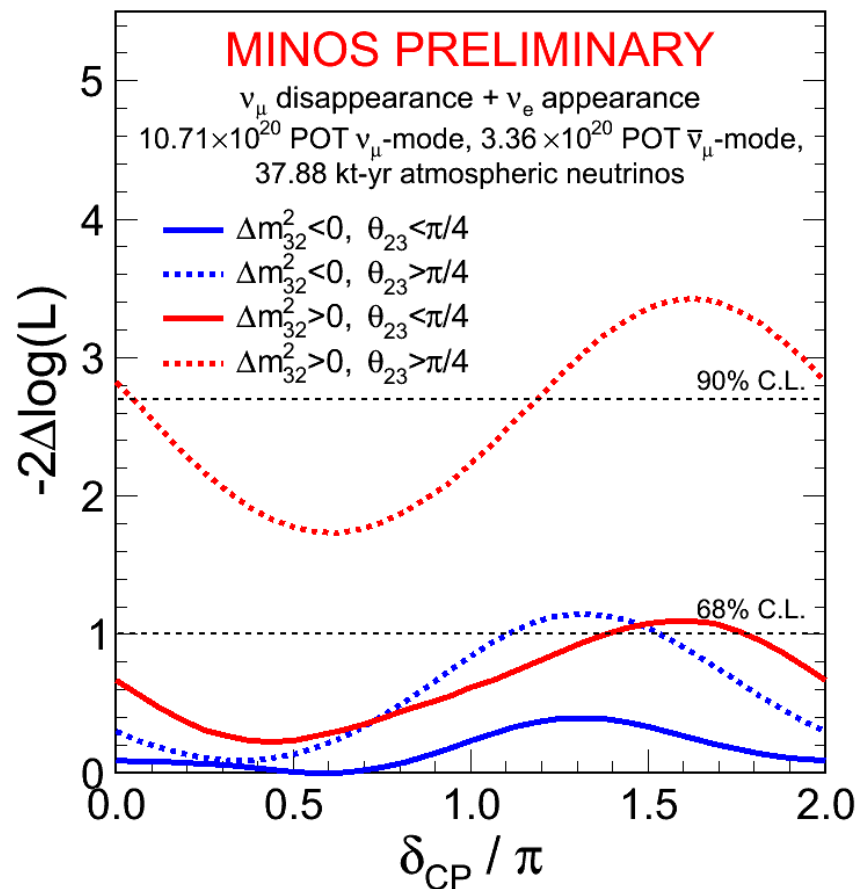
- We can also marginalize over δ_{cp}
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Combined Neutrino Appearance and Disappearance Best Fit

NEW

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Combined Neutrino Appearance and Disappearance Best Fit

NEW

Hierarchy, Octant	Best fit oscillation parameters				$-2\Delta \log(L)$
	$\Delta m_{32}^2 / 10^{-3} \text{eV}^2$	$\sin^2 \theta_{23}$	$\sin^2 \theta_{13}$	δ_{CP}/π	
Normal, Lower	+2.37	0.41	0.0242	0.44	0.23
Normal, Higher	+2.35	0.61	0.0238	0.62	1.74
Inverted, Lower	-2.41	0.41	0.0243	0.62	–
Inverted, Higher	-2.41	0.61	0.0241	0.37	0.09

	Parameter	Best fit	Confidence limits
Normal hierarchy	$ \Delta m_{32}^2 /10^{-3} \text{eV}^2$	2.37	2.28 – 2.46 (68% C.L.)
	$\sin^2 \theta_{23}$	0.41	0.35 – 0.65 (90% C.L.)
Inverted hierarchy	$ \Delta m_{32}^2 /10^{-3} \text{eV}^2$	2.41	2.32 – 2.53 (68% C.L.)
	$\sin^2 \theta_{23}$	0.41	0.34 – 0.67 (90% C.L.)

Preference for inverted hierarchy: $-2\Delta \log L = 0.23$
 Preference for lower octant: $-2\Delta \log L = 0.09$
 Exclusion of maximal mixing: $-2\Delta \log L = 1.54 (\Rightarrow 79\% \text{ C.L.})$

Summary

MINOS has completed a combined analysis of:

- 10.7×10^{20} POT to measure muon neutrino disappearance
- 3.4×10^{20} POT to measure muon antineutrino disappearance
- 37.9 kton-years of atmospheric data

MINOS has completed a combined analysis of:

- 10.6×10^{20} POT to measure electron neutrino appearance
- 3.3×10^{20} POT to measure electron antineutrino appearance
- And now a full combination of our neutrino appearance and disappearance fits, allowing us to make our strongest comments yet on the octant degeneracy, δ_{cp} , and the mass hierarchy

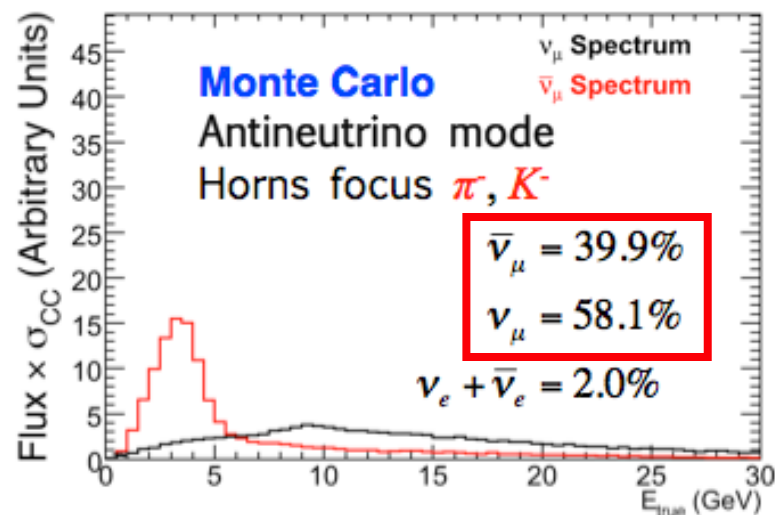
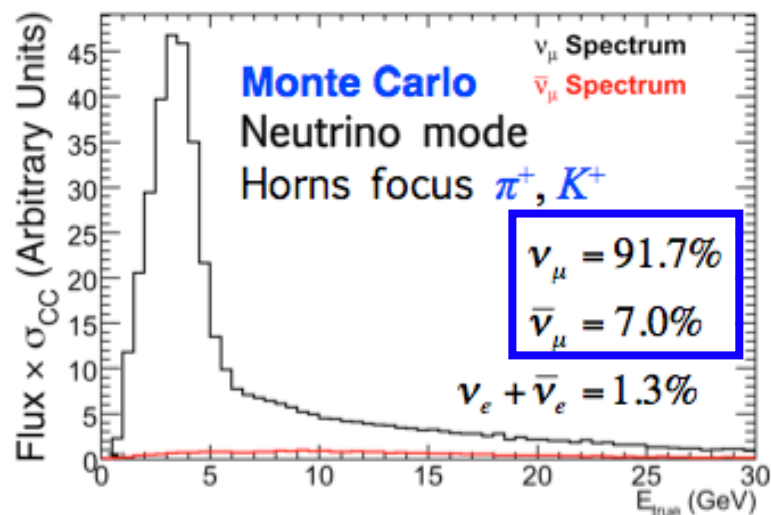
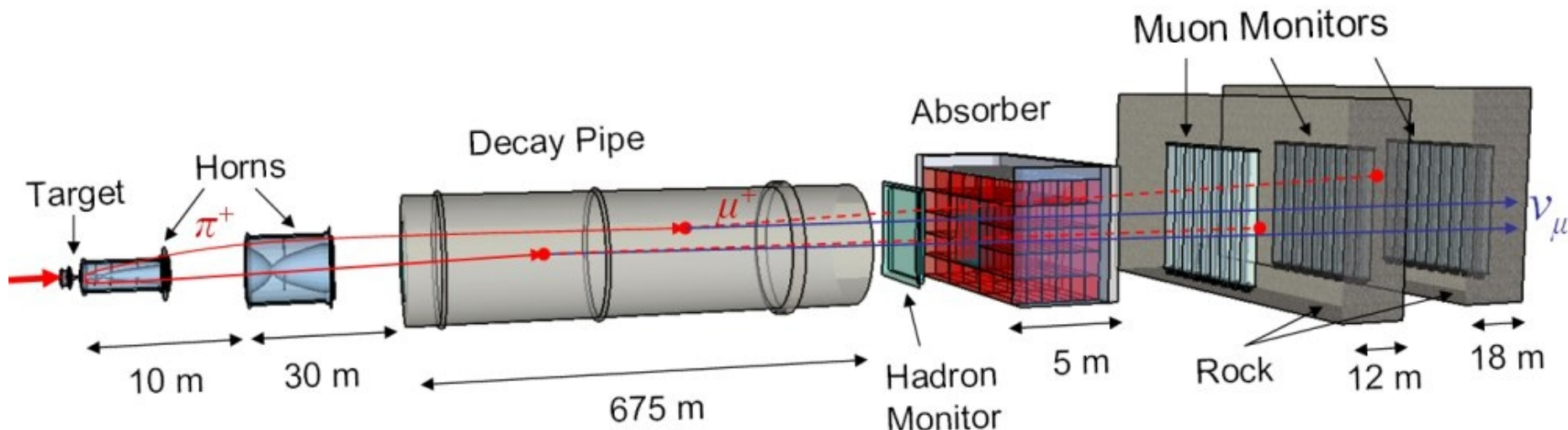
Q&A



Q&A

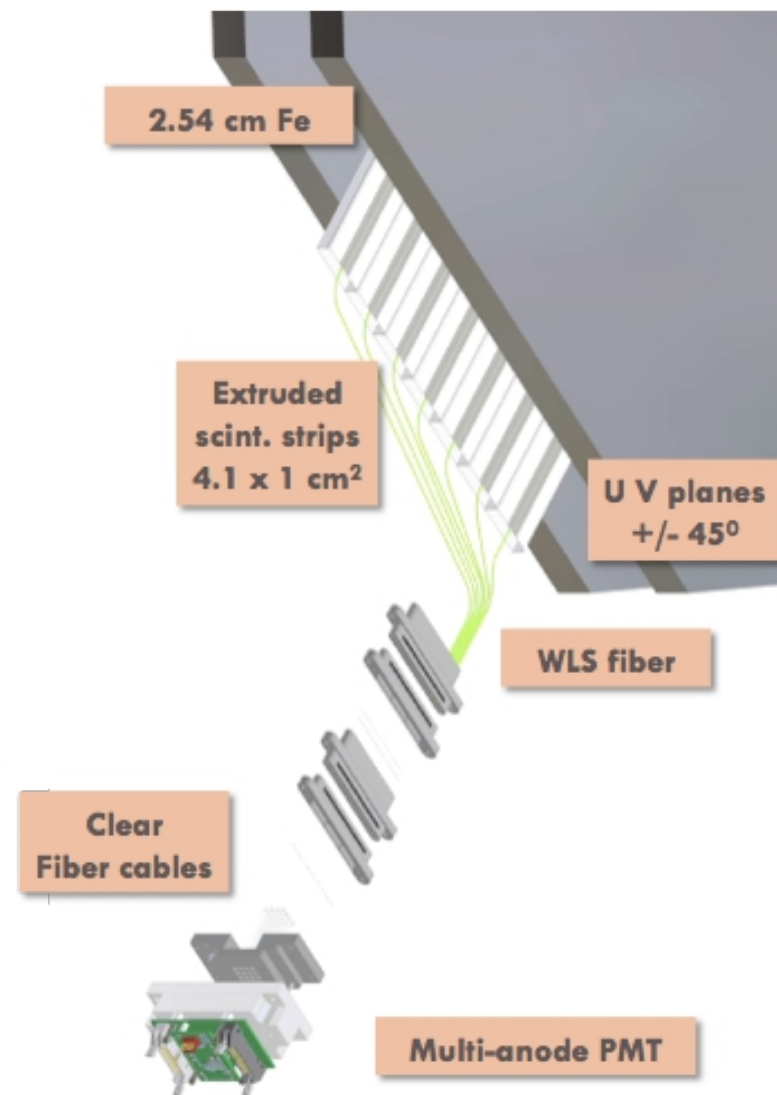
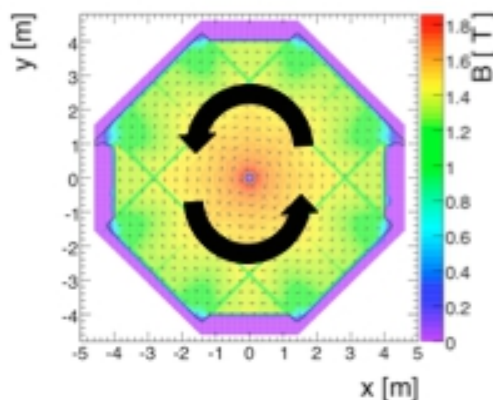
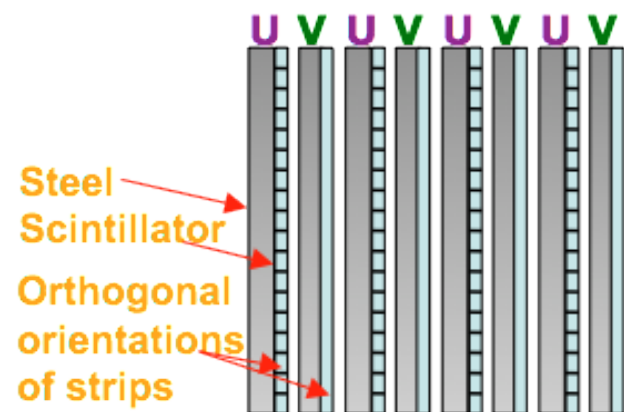


NuMI Neutrino Beam



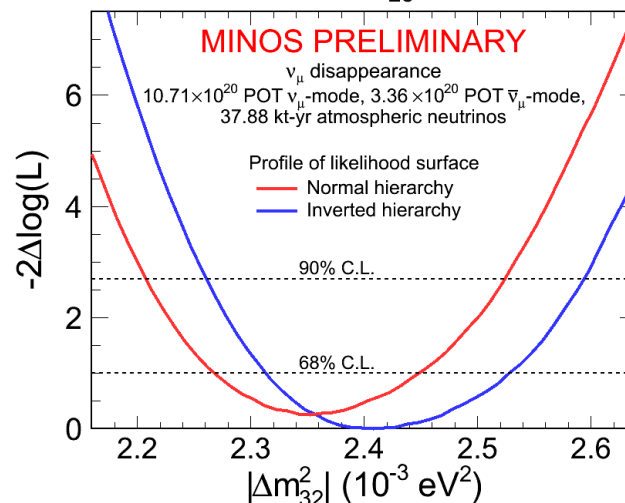
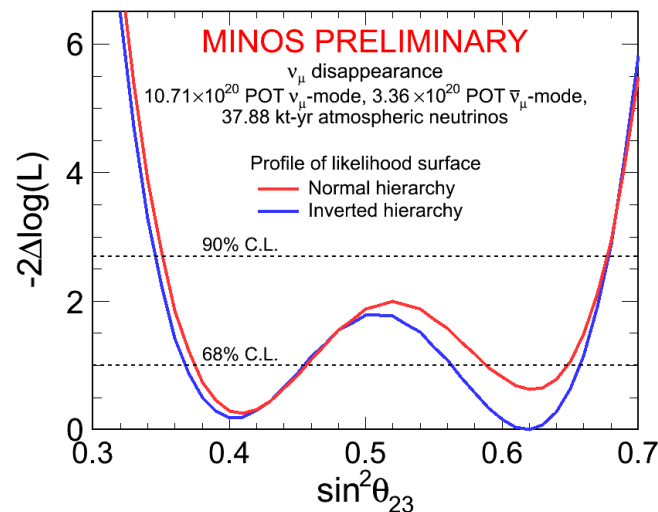
MINOS Detector

- Steel/Scintillator Tracking Calorimeter
 - 2.54 cm-thick steel plates
 - 1 cm-thick, 4.1 cm-wide extruded polystyrene scintillator strips
- Magnetized at $\langle B \rangle \sim 1.3\text{T}$
 - Able to distinguish between μ^- and μ^+



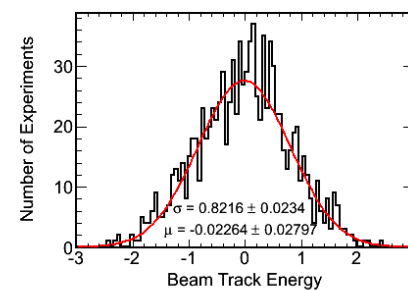
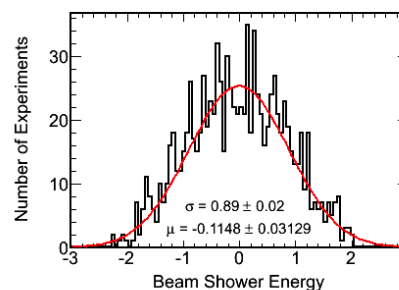
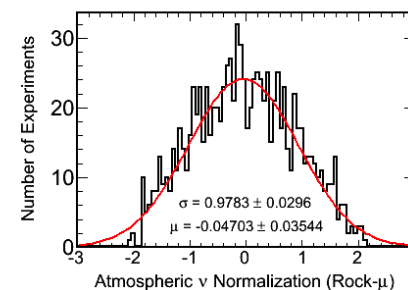
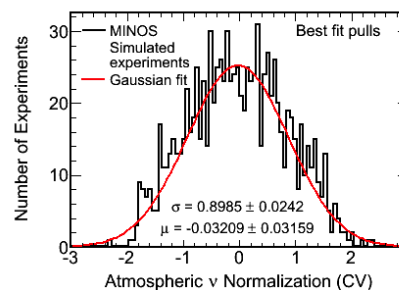
Combined Beam and Atmospheric Neutrino Disappearance Best Fit

- 2 parameter fit assumes identical neutrino and antineutrino mixing parameters
- Gaussian constraint based on world knowledge of θ_{13}
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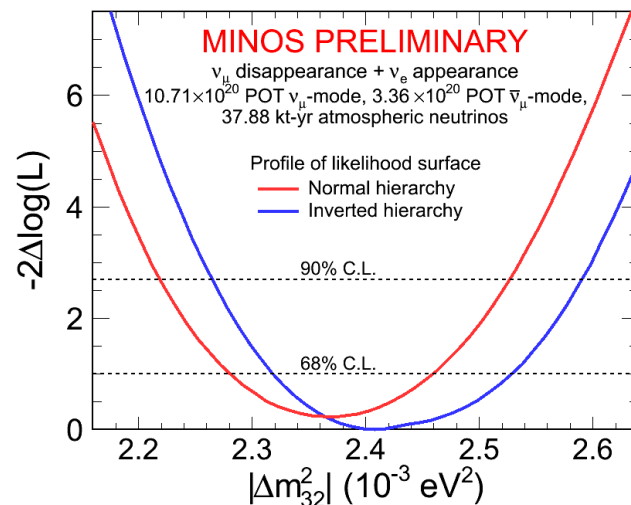
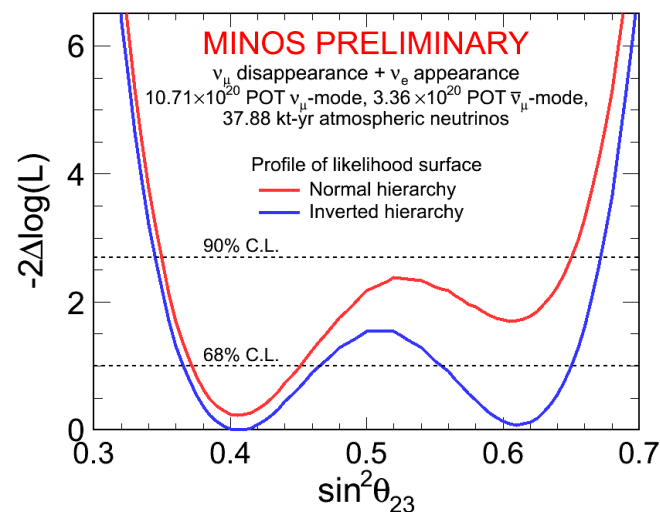
Combined Beam and Atmospheric Neutrino Disappearance Best Fit

- 15 largest systematics included as nuisance parameters
- Best fit systematics all have a mean value near zero and width close to unity
- Well described by gaussian distributions
- No apparent bias or pathology



Combined Neutrino Appearance and Disappearance Best Fit

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Combined Neutrino Appearance and Disappearance Best Fit Inputs

- θ_{23} , $|\Delta m_{32}^2|$ and δ_{cp} allowed to freely float
- Gaussian constraint based on world knowledge of θ_{13} , $\sin^2\theta_{13} = 0.0242 \pm 0.0025$. Based on a weighted average of published results from the Daya Bay, RENO and Double-Chooz reactor neutrino experiments
- The solar parameters are set to fixed values of $\Delta m_{21}^2 = 7.54 \times 10^{-5} \text{ eV}^2$ and $\sin^2(\theta_{12}) = 0.307$, from the Fogli global analysis*

*"Global analysis of neutrino masses, mixings and phases: entering the era of leptonic CP violation searches", Fogli, G. L. et al, Phys. Rev. D, 86,1,2012

Combined Electron Neutrino Appearance

Cannot distinguish between ν_e and anti- ν_e events, so we perform a combined analysis: $\delta(\pi)$

At $\delta_{CP} = 0$ and $\theta_{23} < \pi/4$,

- Assuming normal hierarchy:

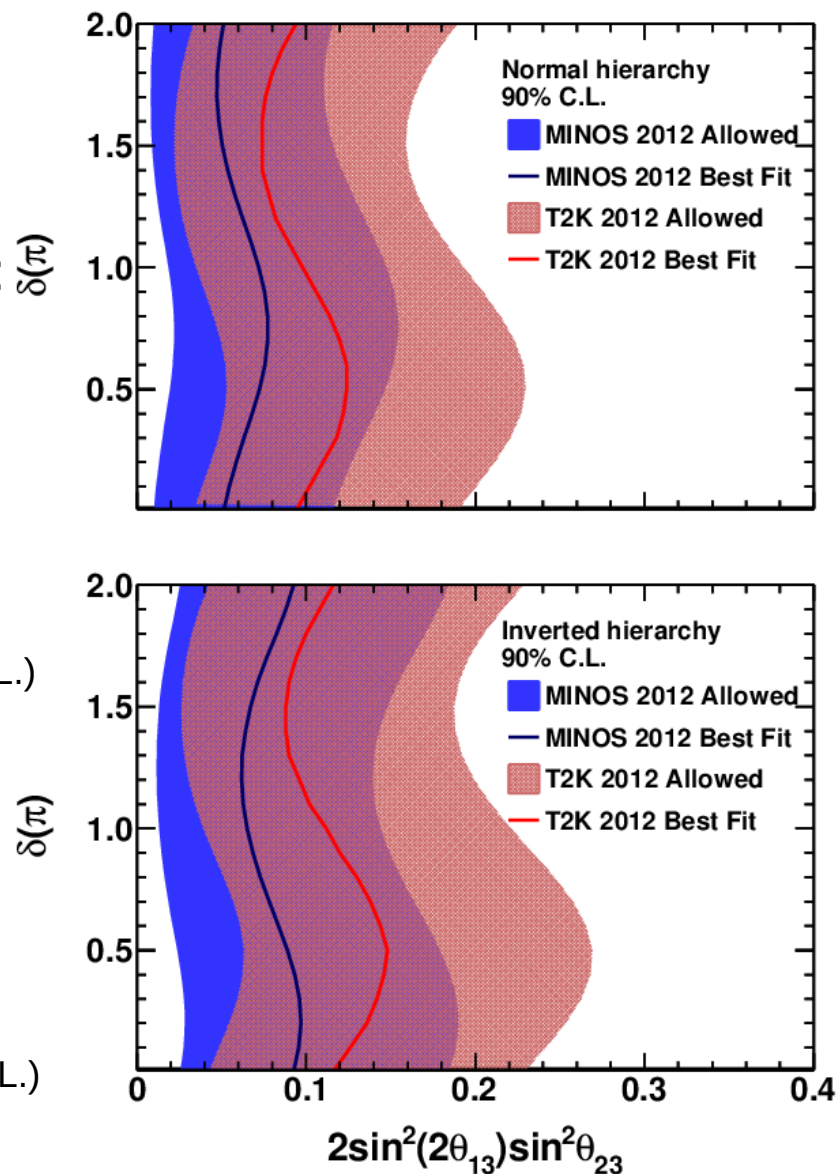
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$$0.01 < 2 \sin^2(2\theta_{13}) \sin^2(\theta_{23}) < 0.12 \text{ (90\% C.L.)}$$

- Assuming inverted hierarchy:

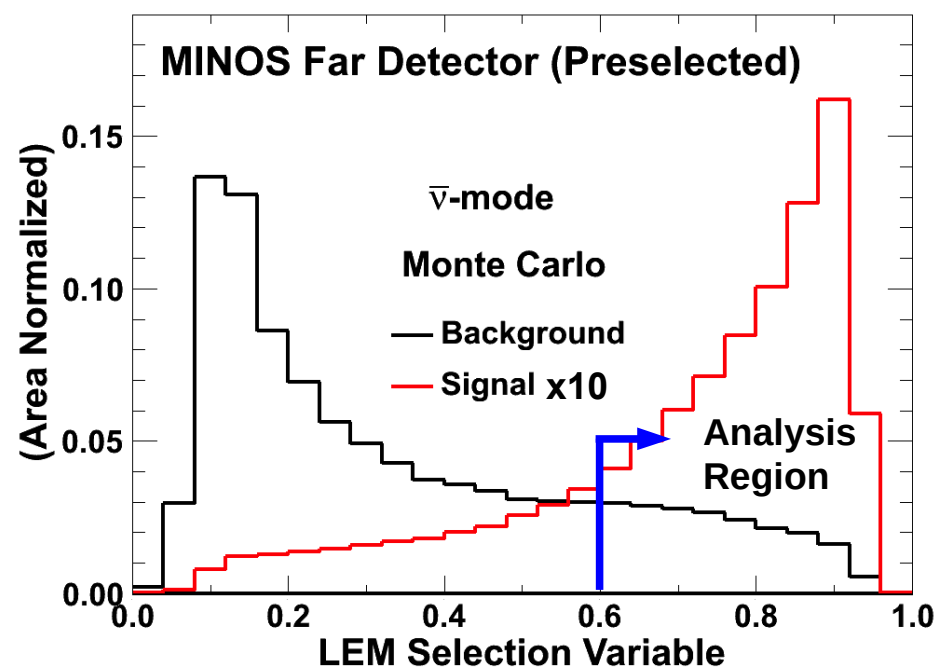
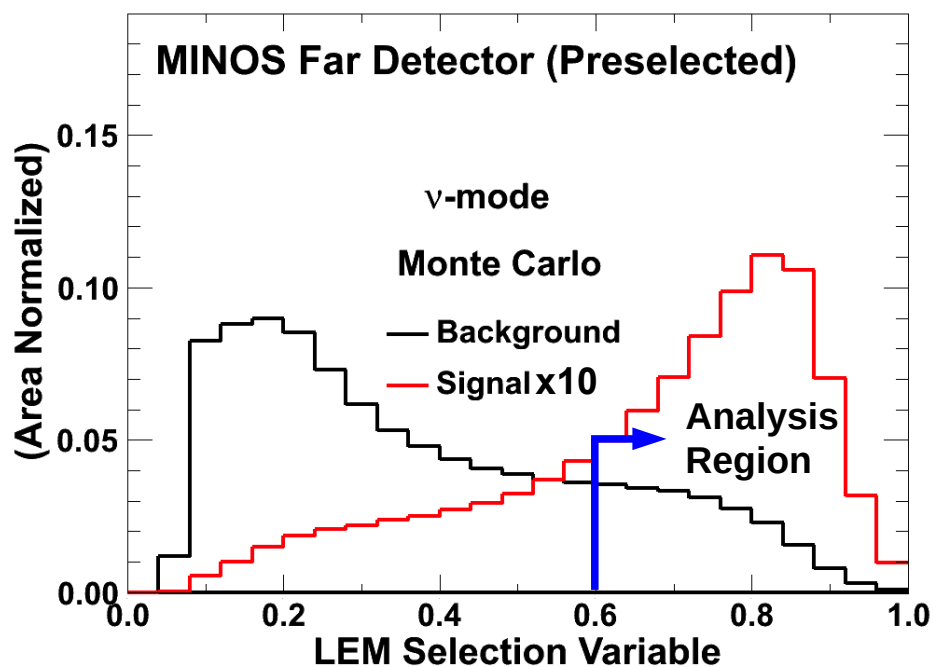
$$2 \sin^2(2\theta_{13}) \sin^2(\theta_{23}) = 0.093^{+0.054}_{-0.049}$$

$$0.03 < 2 \sin^2(2\theta_{13}) \sin^2(\theta_{23}) < 0.18 \text{ (90\% C.L.)}$$



Electron Neutrino Appearance

- MINOS detector granularity makes ν_e CC identification challenging
- Compare candidate events to a library of MC using “Library Event Matching” (LEM)
- Compute discriminating variables based on truth information from library events that best match the candidate



Combined Beam and Atmospheric Neutrino Disappearance Best Fit

	Parameter	Best fit	Confidence limits
Normal hierarchy	$ \Delta m_{32}^2 /10^{-3}\text{eV}^2$	2.35	2.27 – 2.45 (68% C.L.)
	$\sin^2 \theta_{23}$	0.41	0.35 – 0.68 (90% C.L.)
Inverted hierarchy	$ \Delta m_{32}^2 /10^{-3}\text{eV}^2$	2.41	2.31 – 2.53 (68% C.L.)
	$\sin^2 \theta_{23}$	0.62	0.34 – 0.68 (90% C.L.)

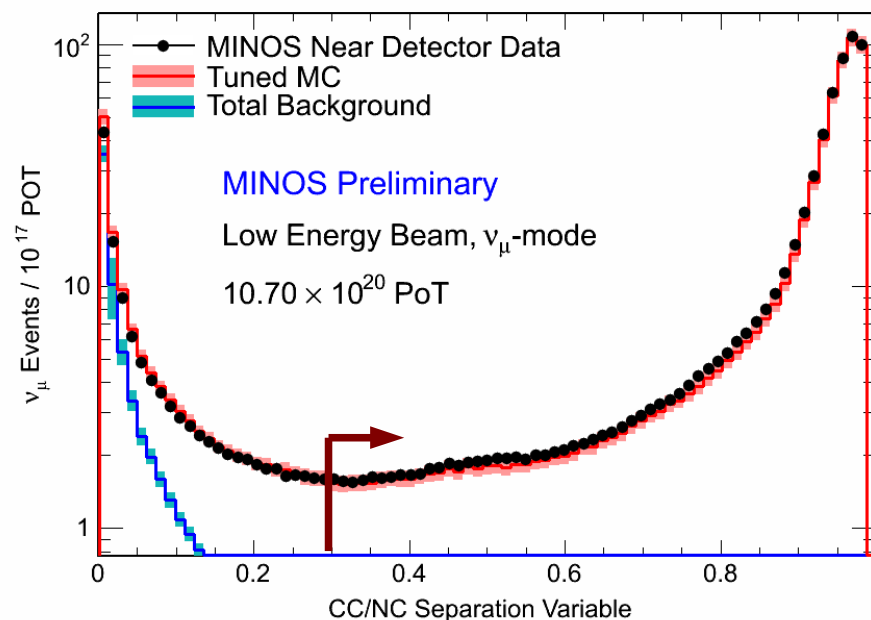
Preference for inverted hierarchy: $-2\Delta \log L = 0.25$

Preference for higher octant: $-2\Delta \log L = 0.20$

Exclusion of maximal mixing: $-2\Delta \log L = 1.79 (\Rightarrow 82\% \text{ C.L.})$

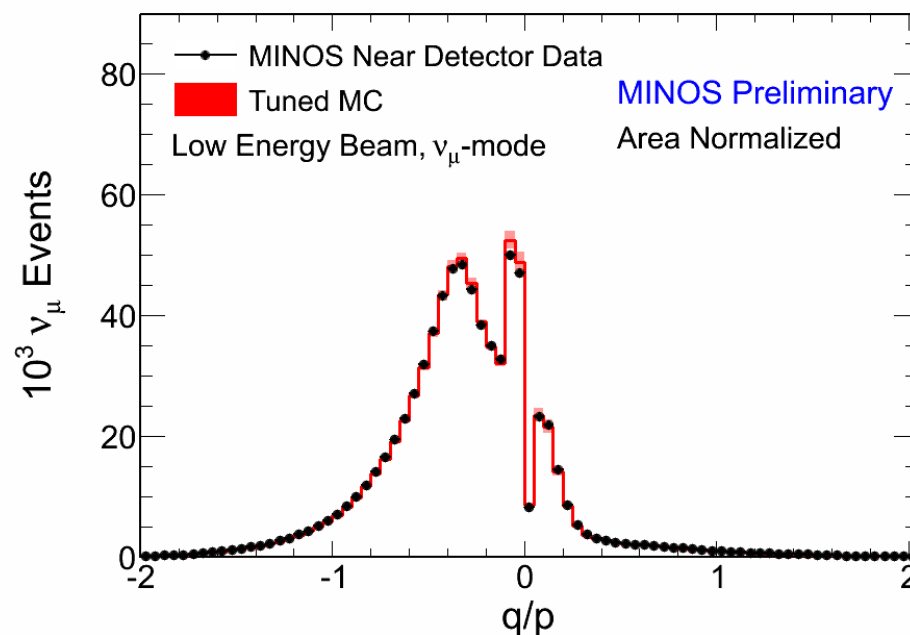
MINOS: Selection I

- The actual analysis selection can be broken down into two main parts.
- The first is the selection of muon like events by using a kNN (k nearest neighbour) algorithm. This takes advantage of the way muon tracks deposit energy, specifically:
 - Track Length.
 - Mean signal in track planes.
 - Transverse track profile.
 - Signal fluctuation in the track.

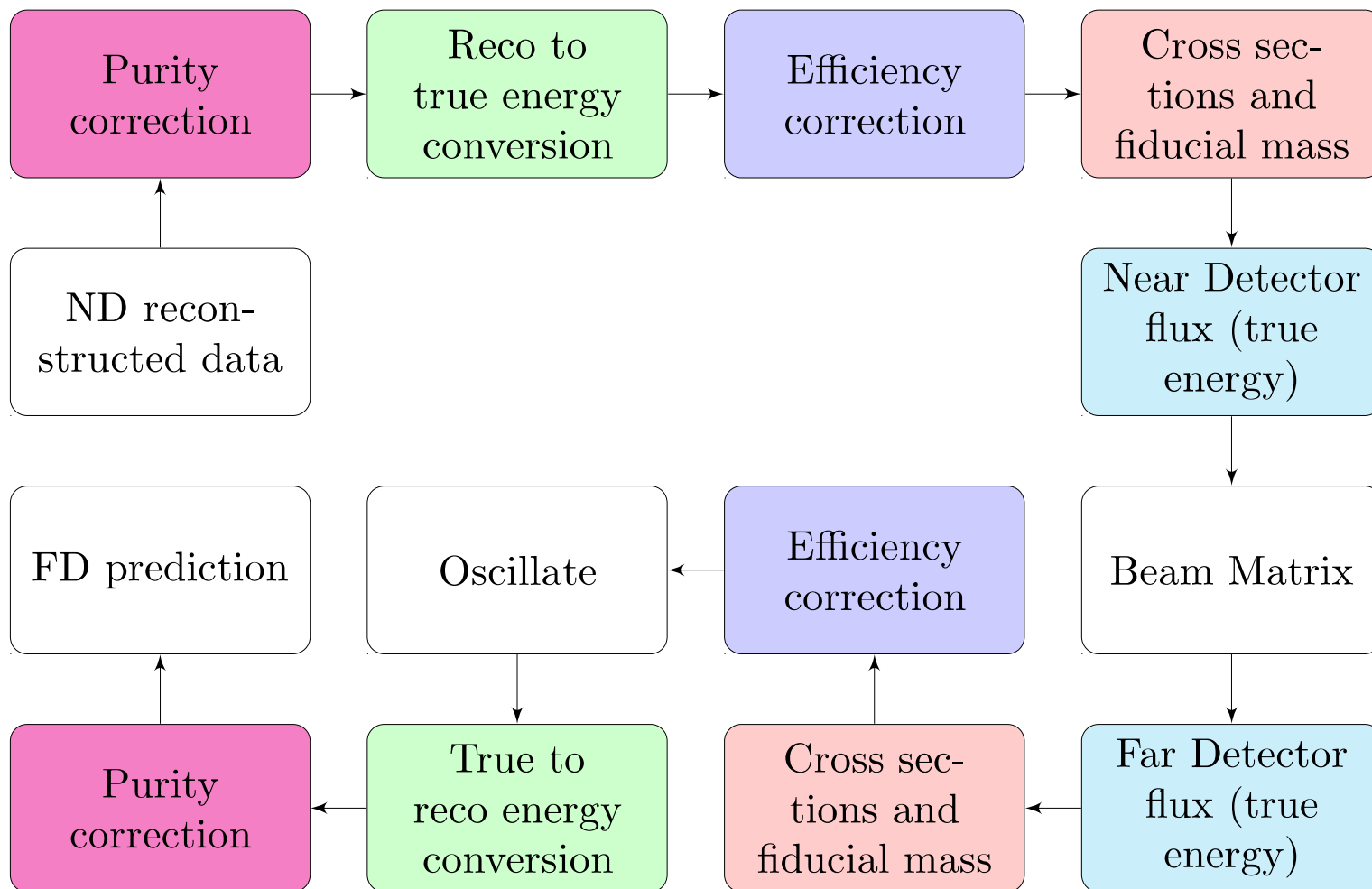


MINOS: Selection II

- The next is charge sign selection, judged by looking at the q/p of the track.
- Particularly important in the anti-neutrino analysis which aims to perform its fit with only anti-neutrinos.
- Less important for the 2 parameter analysis which includes positive sign CC events in its sample.

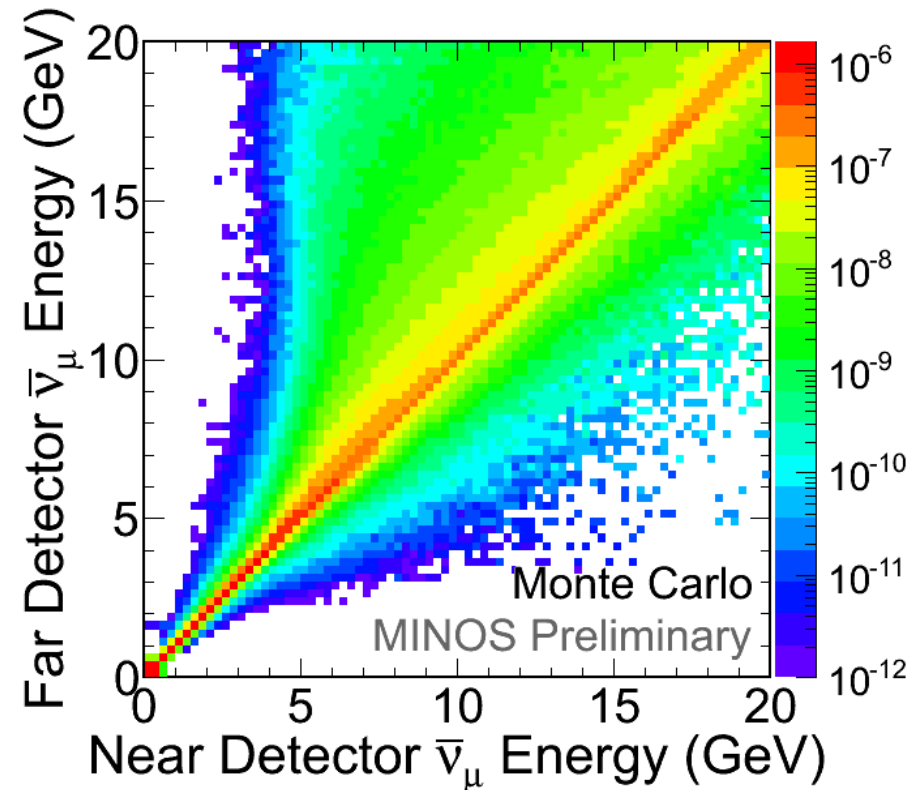


Near to Far Extrapolation



Beam Matrix

- To achieve this we use the a beam matrix
- This matrix describes the energy dependant differences in the neutrino flux seen at the near and far detector.
- $\pi/K/\mu$ producing events of a given energy in the near detector produce a range of energies in the far detector, yielding the energy smearing seen.



Selected Disappearance Events

Data Set	Simulation		Events
	No osc.	With osc.	Observed
ν_μ from ν_μ beam	3201	2543	2579
$\bar{\nu}_\mu$ from ν_μ beam	363	324	312
Non-fiducial μ from ν_μ beam	3197	2862	2911
$\bar{\nu}_\mu$ from $\bar{\nu}_\mu$ beam	313	227	226
Atm. contained-vertex $\nu_\mu + \bar{\nu}_\mu$	1100	881	905
Atm. non-fiducial $\mu^- + \mu^+$	570	467	466
Atm. showers	727	724	701

Library Event Matching (LEM)

Find best matches from a library of MC Events

Judge how signal-like an event is based on those best matches.

Matching is done using only strip info (location and charge)

No dependence on high level reconstructed quantities

