

Recent $|Vub|$ results from semi-leptonic B decays at *BABAR*

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on behalf of the *BABAR* Collaboration

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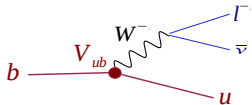
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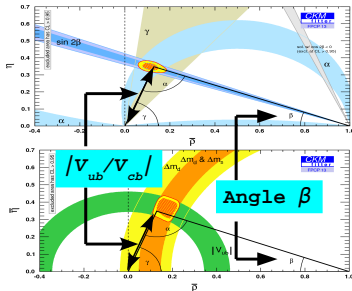
THE CKM MATRIX AND THE ROLE OF $|V_{ub}|$

$$V_{\text{CKM}} \equiv \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



- In the SM, CKM matrix \Rightarrow flavor-mixing
- $|V_{ub}|$ is one of the smallest and most difficult elements to measure
- Semi-leptonic (SL) $b \rightarrow u\ell\bar{\nu}_\ell$ transition $\Rightarrow |V_{ub}|$

- Unitarity triangle:** side opposite to angle β is $\propto |V_{ub}|/|V_{cb}|$
- Both β and $|V_{cb}|$ known to better than 3%
- Measurement of $|V_{ub}|$ places strong constraints on CKM framework



SEMI-LEPTONIC B DECAYS

- **Cleanest** source of $B\bar{B}$ pairs for studying SL B decays:

$$e^+e^- \rightarrow \Upsilon(4S) \xrightarrow{>96\%} B\bar{B}, \sqrt{s} = 10.58 \text{ GeV}$$

- PEP-II collider and **BABAR** detector: asymmetric e^+e^- B -factory at SLAC.

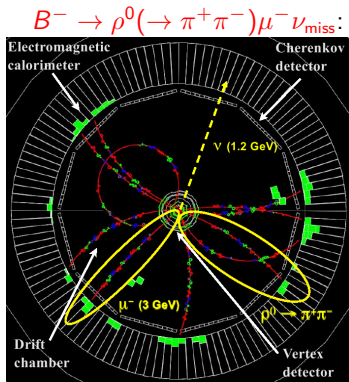
- Full “on-peak” dataset: $\sim 470 \text{ M } B\bar{B}$

- Initial 4-momentum fully known. **Tag** the “other” B , to reconstruct B_{sig}

- Two discriminating variables:

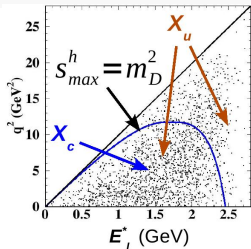
$$\Delta E = E_B^* - \sqrt{s}/2 (\sim 0 \text{ for signal})$$

$$m_{\text{ES}} = \sqrt{s/4 - |\vec{p}_B^*|^2} (\sim m_B \text{ for signal})$$

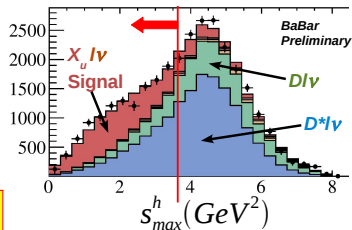


INCLUSIVE $B \rightarrow X_u \ell \nu$ WITH s_H^{MAX} CUT (UNTAGGED)

- Challenge: $50\times$ larger $B \rightarrow X_c \ell \nu$ background
- $\sqrt{q^2} \Rightarrow W^*(\ell \bar{\nu}_\ell)$ mass; $E_\ell \Rightarrow$ lepton energy
- $s_h^{\text{max}} \equiv m_X^2 < 3.52 \text{ GeV}^2$: **remove** dominant **charm** background in $m_X > m_D$



- Update on PRL **95** 111801 (2005): **full dataset**, improved $D^* \ell \nu$ suppression (neural net cut) and **systematics**
- For $E_e^* > 2 \text{ GeV}$, $s_h^{\text{max}*} < 3.5 \text{ GeV}^2$:



$$\Delta\mathcal{B} = \left(3.98 \pm 0.22 \left|_{\text{stat}} \begin{array}{c} +0.27 \\ -0.20 \end{array} \right|_{\text{sys}} \begin{array}{c} +0.17 \\ -0.05 \end{array} \right) \times 10^{-4}$$

EXTRACTION OF $|V_{ub}|$

- To get $|V_{ub}|$ from partial BF: $|V_{ub}| = \sqrt{\Delta\mathcal{B}/(\tau_B \Delta\Gamma_{\text{theory}})}$
- Several QCD calculations available for $d\Gamma/(dE_\ell^* dq^2 dm_X)$:
 - BLNP (NPB 699,335 (2004))
 - GGOU (JHEP 0710,058 (2007))
 - DGE (JHEP 0601,096 (2006))
 - ADFR (EPJC 59,831 (2009))

Measurement	$ V_{ub} $ (10^{-3})			
	BLNP	GGOU	DGE	ADFR
<i>BABAR</i> untagged $(E_{e^*s_h}^{\max})$ (2005)	$4.66 \pm 0.31^{+0.31}_{-0.36}$	–	$4.32 \pm 0.29^{+0.24}_{-0.29}$	$3.82 \pm 0.26^{+0.17}_{-0.18}$
<i>BABAR</i> untagged $(E_{e^*s_h}^{\max})$ (2013)	$4.44^{+0.16}_{-0.21} \pm 0.31$	–	$4.11^{+0.15+0.23}_{-0.20-0.27}$	$3.62^{+0.13}_{-0.18} \pm 0.17$
<i>BABAR</i> tagged (m_X, q^2) (2012)	$4.28 \pm 0.24^{+0.09}_{-0.11}$	$4.35 \pm 0.24^{+0.09}_{-0.11}$	$4.40 \pm 0.24^{+0.12}_{-0.13}$	$4.29 \pm 0.24^{+0.18}_{-0.19}$
<i>Belle</i> tagged (m_X, q^2) (2010)	$4.47 \pm 0.27^{+0.19}_{-0.21}$	$4.54 \pm 0.27^{+0.10}_{-0.11}$	$4.60 \pm 0.27^{+0.11}_{-0.13}$	$4.48 \pm 0.30^{+0.19}_{-0.19}$

- New *BABAR* untagged $E_{e^*s_h}^{\max}$ results to be submitted to PRD
- Consistent with hadronic tagged ($p_\ell^* > 1$ GeV, 2-D fit in (m_X, q^2))

INCLUSIVE $|V_{ub}|$ SUMMARY

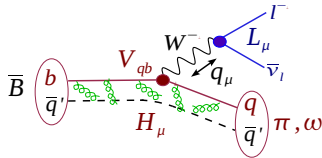
- **Best** measurements (Belle and *BABAR*) from **hadronic tag**
- Arithmetic average over 4 QCD calculations:

$$|V_{ub}|_{\text{incl}} = (4.41 \pm 0.15_{\text{exp}} \pm 0.17_{\text{th}}) \times 10^{-4}$$

- **Systematic errors** mostly from $B \rightarrow X_u \ell \nu$ and background Monte Carlo **simulations**

EXCLUSIVE $B \rightarrow \{\pi, \omega\} \ell \nu$ AND FORM-FACTORS

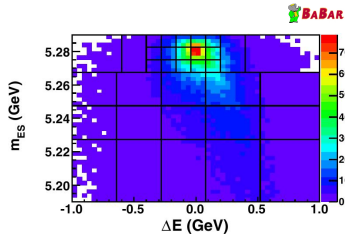
- **Leptonic** (L_μ) and **hadronic** (H_μ) sides factorize
- **Vector-meson**: 3 helicity amplitudes $H_{\{0,\pm\}}$ and 3 form-factors (A_1, A_2, V)
- **Pseudo-scalars**: single H_0 amplitude, 1 FF (f_+)
- **Theory** predictions of FF's based on: **quark models**, light cone sum rules (**LCSR**), **lattice** calculations, with different q^2 regions of validity.
- Model-independent series expansions from **dispersion relations** \Rightarrow **data-driven** way to fix q^2 dependence



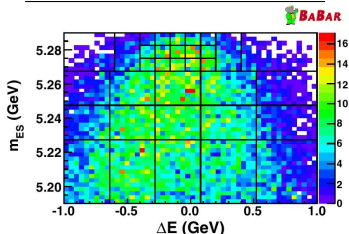
UNTAGGED $B \rightarrow \pi \ell \nu$ PRD **86**, 092004 (2012)

- Update on PRD **83**, 052011 (2011): full dataset, improvement at high q^2
- $Y \equiv (\pi \ell)$ and c.m. frame variable: $\cos \theta_{BY} = \frac{2E_B E_Y - m_B^2 - m_Y^2}{2|\vec{p}_B||\vec{p}_Y|}$
- Loose ν reconstruction: $|\cos \theta_{BY}| \leq 1$;
- Combined fit to π^+ and π^0 samples assuming **isospin** relations
- $m_{ES} - \Delta E - q^2$ fits using **signal** + **5 background** categories of PDF's from MC

Signal $\pi \ell \nu$:

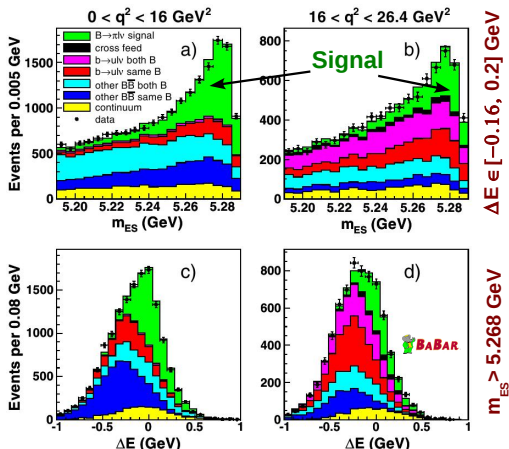


$e^+ e^- \rightarrow q \bar{q} (\gamma)$ Continuum:



UNTAGGED $B \rightarrow \pi \ell \nu$ PRD 86, 092004 (2012) (CNTD.)

- π^+/π^0 combined fit projections:



- Isospin-constrained: $\mathcal{B}(B \rightarrow \pi \ell \nu) = (1.45 \pm 0.04_{\text{stat}} \pm 0.06_{\text{sys}}) \times 10^{-4}$

BCL EXPANSION FIT

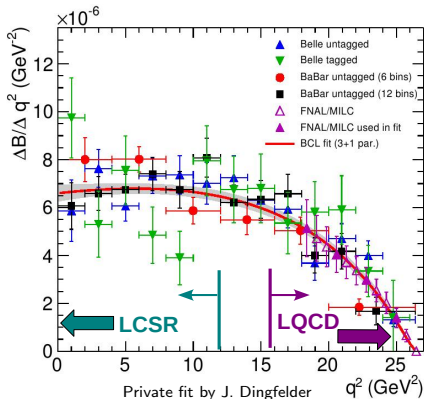
- BCL (Bourrely *et al.*, PRD **79**, 013008 (2009)) **simple pole** form:

$$f_+(q^2) = \frac{1}{1 - q^2/m_{B^*}^2} \sum_k^{k_{\max}} \tilde{a}_k z^k(q^2)$$

- Measured **data** \Rightarrow **shape**.
Normalization towards q_{\max}^2 from
LQCD (only 4/12 points)

$$|V_{ub}|_{\text{fit}} = (3.28 \pm 0.29) \times 10^{-3}$$

BABAR PRD **83**, 032007 (2011) Belle PRD **83**, 071101 (2011)
 BABAR PRD **86**, 092004 (2012) Belle arXiv:1306.2781 (2013)



- Compare $f_+(0)_{\text{fit}} = 0.28 \pm 0.03$ with $f_+(0)_{\text{LCSR}} = 0.28 \pm 0.02$

$|V_{ub}|$ SUMMARY FOR $B \rightarrow \pi \ell \nu$

- Form-factor calculations

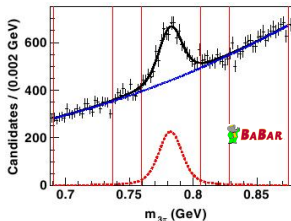
- 1 LCSR, Khodjamirian *et al.*, PRD **83**, 094031 (2011)
- 2 HPQCD (lattice), PRD **73** 074502 (2005)
- 3 FNAL/MILC (lattice), PRD **79**, 054507 (2009)

Measurement	LCSR ¹	HPQCD ²	FNAL/MILC ³ fit
	$q^2 \in [0, 12]$ GeV ²	$q^2 \in [16, 26.4]$ GeV ²	$q^2 \in [16, 26.4]$ GeV ²
	$ V_{ub} $ (10^{-3})		
<i>BABAR</i> 6 q^2 -bins (2011)	$3.54 \pm 0.12^{+0.38}_{-0.33}$	$3.22 \pm 0.15^{+0.55}_{-0.37}$	2.98 ± 0.31
<i>BABAR</i> 12 q^2 -bins (2011)	$3.46 \pm 0.10^{+0.37}_{-0.32}$	$3.26 \pm 0.19^{+0.56}_{-0.37}$	3.22 ± 0.31
<i>BABAR</i> 12 q^2 -bins (2012)	$3.46 \pm 0.10^{+0.37}_{-0.32}$	$3.47 \pm 0.13^{+0.60}_{-0.39}$	3.25 ± 0.31
Belle 13 q^2 -bins (2011)	$3.44 \pm 0.10^{+0.37}_{-0.32}$	$3.60 \pm 0.13^{+0.61}_{-0.41}$	3.43 ± 0.33
Avg. untagged	$3.47 \pm 0.06^{+0.37}_{-0.32}$	$3.43 \pm 0.09^{+0.59}_{-0.39}$	3.21 ± 0.31
Belle hadronic tag (2013)	$3.40 \pm 0.16^{+0.37}_{-0.32}$	$3.81 \pm 0.24^{+0.66}_{-0.43}$	3.52 ± 0.29

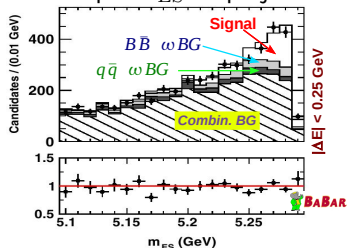
- Untagged $B \rightarrow \pi \ell \nu$ measurements still the most precise for exclusive $|V_{ub}|$. Error dominated by theory uncertainties.

UNTAGGED $B \rightarrow \omega l\nu$ PRD **87**, 032004 (2013)

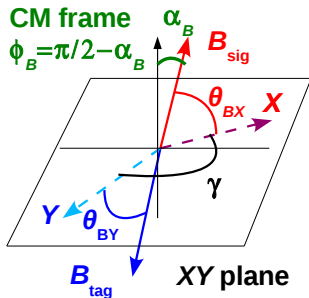
- **New** untagged on full *BABAR* dataset, with $-1.2 < \cos \theta_{\text{BY}} < 1.1$
- **Neural network** based selection for $q\bar{q}$ and $B \rightarrow X_c l\nu$ suppression
- Binned LH fit in **5** q^2 and **20** ΔE - m_{ES} bins
- Combinatoric BG *fixed* using $m_{3\pi}$ sidebands in Data



- Sample m_{ES} fit projection:

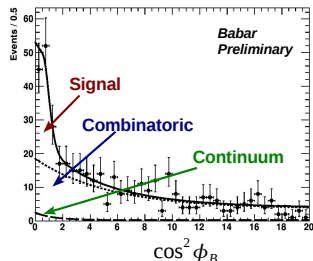


$$\mathcal{B}(B \rightarrow \omega l\nu) = (1.21 \pm 0.14_{\text{stat}} \pm 0.08_{\text{sys}}) \times 10^{-4}$$

SEMI-LEPTONICALLY TAGGED $B \rightarrow \omega l \nu$ (NEW!)

- $\mathcal{B}(B \rightarrow D^{(*)} \nu) \sim 8\% \Rightarrow$ tag efficiency
 $\sim 4.4\%$ is higher than hadronic tags.
- Binned LH fits to $\cos^2 \phi_B$ shape

$$\mathcal{B}(B \rightarrow \omega l \nu) = (1.35 \pm 0.21_{\text{stat}} \pm 0.11_{\text{sys}}) \times 10^{-4}$$



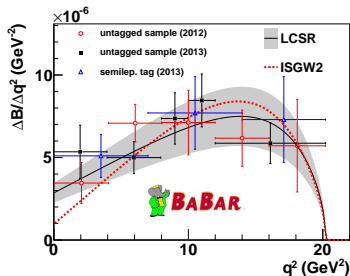
$|V_{ub}|$ FROM $B \rightarrow \omega l \nu$

References:

PRD **86**, 092004 (2012)PRD **87**, 032004 (2013)

arXiv:1308.2589 (2013)

- $\frac{dB}{dq^2}$ compared to form-factor models:

LCSR valid at $q^2 \rightarrow 0$ HQE based ISGW2 valid at $q^2 \rightarrow q_{\max}^2$ 

Measurement	$ V_{ub} $ (10^{-3})		
	LCSR $q^2 \in [0, 12]$	LCSR $q^2 \in [0, 21]$	ISGW2 $q^2 \in [0, 21]$
<i>BABAR</i> untag. 2012		$3.22 \pm 0.24^{+0.45}_{-0.27}$	
<i>BABAR</i> untag. 2013	$3.37 \pm 0.23 \pm 0.38$	$3.23 \pm 0.22 \pm 0.38$	3.25 ± 0.22
<i>BABAR</i> SL tag. 2013		$3.41 \pm 0.31 \pm 0.38$	3.43 ± 0.31
<i>BABAR</i> avg.	$3.37 \pm 0.23 \pm 0.38$	$3.27 \pm 0.18 \pm 0.38$	3.3 ± 0.18
Belle had. tag (2013)	$3.08 \pm 0.31^{+0.44}_{-0.31}$		3.03 ± 0.26

SUMMARY AND INCLUSIVE/EXCLUSIVE “TENSION”

- Several new *BABAR* measurements, both **inclusive** and **exclusive**. Results fully consistent with previous measurements.
- Current world averages for $|V_{ub}|$:

$$|V_{ub}|_{\text{incl.}} = (4.37 \pm 0.20_{\text{exp}} \pm 0.15_{\text{th}}) \times 10^{-4}$$

$\sim 2.9\sigma$
tension

$$|V_{ub}|_{\text{excl.}} = (3.21 \pm 0.17_{\text{exp}} \pm 0.26_{\text{th}}) \times 10^{-4}$$

- **Inclusive**: latest *BABAR*/Belle (q^2, m_X) tagged. Sum over 4 QCD calculations.
- **Exclusive**: only untagged $\pi\ell\nu$ and 4 LQCD points.
- Uncertainties have been reduced, but tension persists.
- Smaller, but non-zero tension in $|V_{cb}|$ as well

FUTURE IMPROVEMENTS

- Better understanding of BG composition/dynamics of incl. $X_{\{c,u\}}\ell\nu$ and $q\bar{q}$
- MVA-based (instead of cut-based) **hadronic tagging** algorithms, with larger (40× data) MC samples to study efficiencies of tag-modes with small BF's
- Full **angular-fit** for exclusive $B \rightarrow V\ell\nu$ to make use of correlations
- Improved QCD calculations with **wider q^2** coverage for exclusive
- **Global fits** to m_X moments in $B \rightarrow X_u\ell\nu$ and E_γ spectrum in $B \rightarrow X_s\gamma$ to extract shape-function parameters and $|V_{ub}|$
- If tension is not due to measurements, ... **New Physics?** – RH currents, additional scalar and tensor terms in the effective Lagrangian