

# Charmonium and Bottomonium Hybrid States

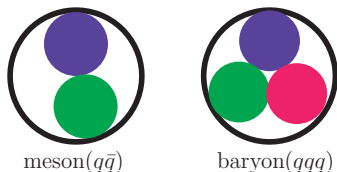
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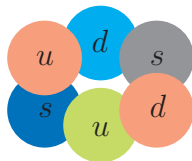
DPF 2013, UC Santa Cruz, August 16, 2013

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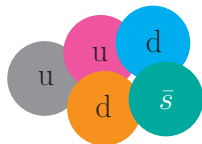


- **Quark model** is quite successful in the classification of hadrons:  $J^{PC}$  quantum numbers and flavour quantum numbers;
- However, the hadron structures are more complicated in **QCD**. It may allow for hadrons which lie **outside the naive quark model**;
- Mesons with **exotic  $J^{PC}$  quantum numbers**:  
 $J^{PC} = 0^{--}, 0^{+-}, 1^{-+}, 2^{+-}, \dots$
- Baryons with **exotic flavour quantum numbers**:  
**dibaryon, pentaquark, ...**

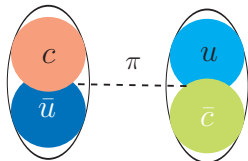
# Many possible candidates of exotic hadrons in QCD:



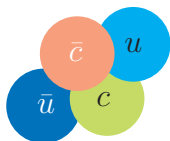
dibaryon



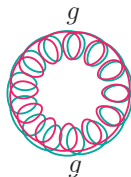
pentaquark



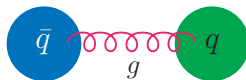
molecule



tetraquark

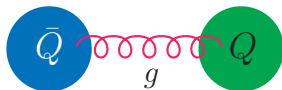


glueball



hybrid

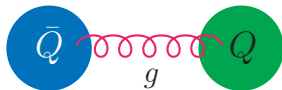
# Hybrid Mesons:



- The existence of hybrids was suggested by Jaffe and Johnson in 1976;
- Hybrid mesons were studied in MIT bag model, flux tube model, LQCD, QCD sum rule and so on;
- Heavy quarkonium hybrids were originally studied in QCD sum rule:
  - J. Govaerts et al., Nucl. Phys. B258, 215 (1985);
  - J. Govaerts et al., Nucl. Phys. B262, 575 (1985);
  - J. Govaerts et al., Nucl. Phys. B284, 674 (1987).

Only dimension-4 condensate contributions were studied to the correlation functions. Many channels are unstable!

# Heavy Quarkonium Hybrids:



- The  $1^{--}, 1^{++}, 0^{-+}$  channels have been re-analyzed by including the tri-gluon condensate:
  - C. F. Qiao et al., J. Phys. G39, 015005 (2012);
  - D. Harnett et al., J. Phys. G39, 125003 (2012);
  - R. Berg et al., Phys. Rev. D86, 034002 (2012).
- We study the effects of the dimension six condensates on remaining channels:  $J^{PC} = 0^{++}, 0^{--}, 0^{+-}, 1^{-+}, 1^{+-}, 2^{-+}$  and  $2^{++}$ ;
- We confirm the hybrid supermultiplet structures.

# Hybrid Sum Rules

Two-point Correlation Function:

$$\Pi_{\mu\nu}(q^2) = i \int d^4x e^{iq \cdot x} \langle 0 | T [J_\mu(x) J_\nu^\dagger(0)] | 0 \rangle,$$

where  $J_\mu(x)$  is the hybrid interpolating currents

$$J_\mu = g_s \bar{Q} \frac{\lambda^a}{2} \gamma^\nu G_{\mu\nu}^a Q, \quad J^{PC} = 1^{-+}, 0^{++},$$

$$J_\mu = g_s \bar{Q} \frac{\lambda^a}{2} \gamma^\nu \gamma_5 G_{\mu\nu}^a Q, \quad J^{PC} = 1^{+-}, 0^{--},$$

$$J_{\mu\nu} = g_s \bar{Q} \frac{\lambda^a}{2} \sigma_\mu^\alpha \gamma_5 G_{\alpha\nu}^a Q, \quad J^{PC} = 2^{-+}, 1^{++}, 1^{-+}, 0^{-+},$$

By replacing  $G_{\mu\nu}^a$  with  $\tilde{G}_{\mu\nu}^a = \frac{1}{2} \epsilon_{\mu\nu\alpha\beta} G^{\alpha\beta,a}$ , we obtain the corresponding currents with opposite parities.

- Hadron level: Dispersion relation

$$\Pi(q^2) = (q^2)^N \int_{4m^2}^{\infty} \frac{\rho(s)}{s^N (s - q^2 - i\epsilon)} ds + \sum_{n=0}^{N-1} b_n (q^2)^n,$$

- Quark-gluon level:  $\Pi(q^2)$  can be calculated via the OPE method;
- Hybrid sum rules: Quark-hadron duality and Borel transform

$$f_X^2 m_X^{8+2k} e^{-m_X^2/M_B^2} = \int_{4m^2}^{s_0} ds s^k \rho(s) e^{-s/M_B^2} = \mathcal{L}_k(s_0, M_B^2),$$

where  $s_0$  and  $M_B$  are threshold parameter and Borel mass respectively.

- Hybrid mass:

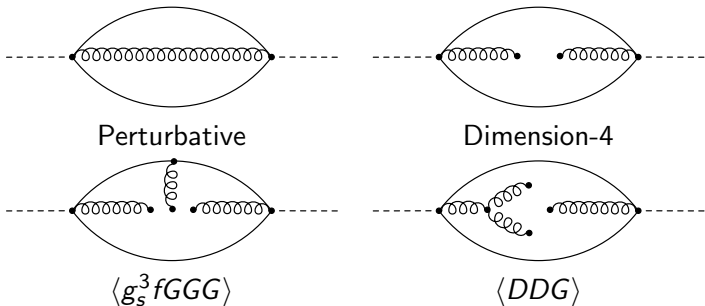
$$m_X^2 = \frac{\mathcal{L}_1(s_0, M_B^2)}{\mathcal{L}_0(s_0, M_B^2)}.$$



# Correlation Function and Spectral Density

- Quark-gluon level:  $\Pi(q^2)$  and  $\rho(s)$  are calculated up to dimension six:

$$\rho(s) = \rho^{\text{pert}}(s) + \rho^{\langle GG \rangle}(s) + \rho^{\langle GGG \rangle} + \rho^{\langle jj \rangle},$$



# Working Regions of $M_B$ and $s_0$ :

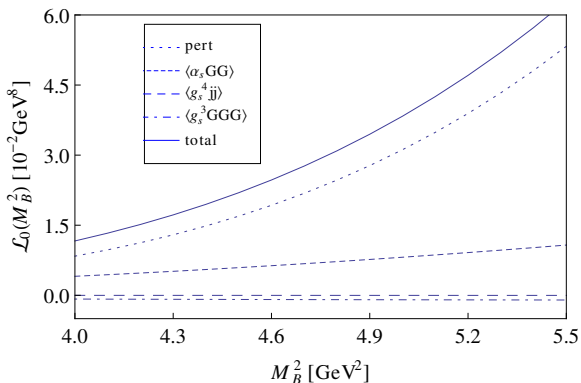
## Limitations of the parameters:

- OPE convergence: gluon condensate is less than one third of the perturbative term while tri-gluon condensate is less than one third of the gluon condensate;
- Upper bound on  $M_B^2$  is obtained by requiring PC be larger than 10%;
- We fix on the value of  $s_0$  around which the variation of  $m_X$  with  $M_B^2$  is minimum;
- The Borel curves should be stable.

## Pole Contribution(PC):

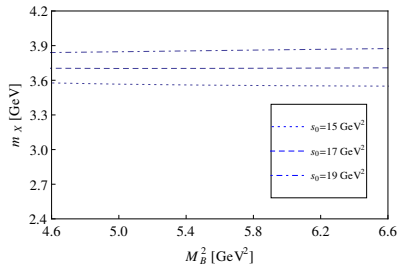
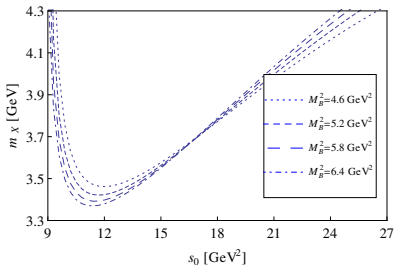
$$\text{PC}(s_0, M_B^2) = \frac{\int_{4m_c^2}^{s_0} ds e^{-s/M_B^2} \rho(s)}{\int_{4m_c^2}^{\infty} ds e^{-s/M_B^2} \rho(s)}.$$

The OPE convergence for  $1^{-+} \bar{c}Gc$  hybrid:

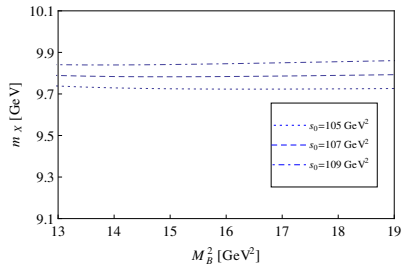
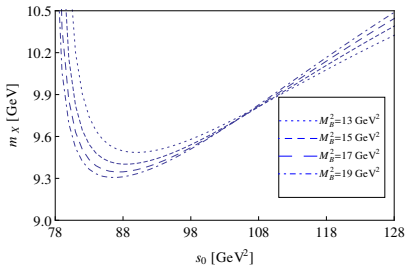


$$M_B^2 \geq 4.6 \text{ GeV}^2$$

### The Borel curves for $1^{-+} \bar{c}Gc$ hybrid:



### The Borel curves for $1^{-+} \bar{b}Gb$ hybrid:



# Numerical results for $\bar{c}Gc$ charmonium hybrids

$J^{PC}$	$s_0(\text{GeV}^2)$	$[M_{\min}^2, M_{\max}^2](\text{GeV}^2)$	$m_X(\text{GeV})$	PC(%)
1 <sup>--</sup>	15	2.5 ~ 4.8	$3.36 \pm 0.15$	18.3
0 <sup>-+</sup>	16	5.6 ~ 7.0	$3.61 \pm 0.21$	15.4
1 <sup>-+</sup>	17	4.6 ~ 6.5	$3.70 \pm 0.21$	18.8
2 <sup>-+</sup>	18	3.9 ~ 7.2	$4.04 \pm 0.23$	26.0
0 <sup>+-</sup>	20	6.0 ~ 7.4	$4.09 \pm 0.23$	15.5
2 <sup>++</sup>	23	3.9 ~ 7.5	$4.45 \pm 0.27$	21.5
1 <sup>+-</sup>	24	2.5 ~ 8.4	$4.53 \pm 0.23$	33.2
1 <sup>++</sup>	30	4.6 ~ 11.4	$5.06 \pm 0.44$	30.4
0 <sup>++</sup>	34	5.6 ~ 14.6	$5.34 \pm 0.45$	36.3
0 <sup>--</sup>	35	6.0 ~ 12.3	$5.51 \pm 0.50$	31.0

- **Unstable channels** are stabilized and the mass predictions are reliable!
- **1<sup>++</sup> charmonium hybrid** is much heavier than **X(3872)**, which seems to preclude a pure charmonium hybrid interpretation for this state;

# Numerical results for $\bar{b}Gb$ bottomonium hybrids

$J^{PC}$	$s_0(\text{GeV}^2)$	$[M_{\min}^2, M_{\max}^2](\text{GeV}^2)$	$m_X(\text{GeV})$	PC(%)
1 <sup>--</sup>	105	11 ~ 17	$9.70 \pm 0.12$	17.2
0 <sup>-+</sup>	104	14 ~ 16	$9.68 \pm 0.29$	17.3
1 <sup>-+</sup>	107	13 ~ 19	$9.79 \pm 0.22$	20.4
2 <sup>-+</sup>	105	12 ~ 19	$9.93 \pm 0.21$	21.7
0 <sup>+-</sup>	114	14 ~ 19	$10.17 \pm 0.22$	17.6
2 <sup>++</sup>	120	12 ~ 20	$10.64 \pm 0.33$	19.7
1 <sup>+-</sup>	123	10 ~ 21	$10.70 \pm 0.53$	28.5
1 <sup>++</sup>	134	13 ~ 27	$11.09 \pm 0.60$	27.7
0 <sup>++</sup>	137	13 ~ 31	$11.20 \pm 0.48$	30.0
0 <sup>--</sup>	142	14 ~ 25	$11.48 \pm 0.75$	24.1

We have confirmed the hybrid supermultiplet structure:

- **Lightest hybrid supermultiplet:** negative-parity states with  $J^{PC} = 1^{--}, (0, 1, 2)^{-+}$ ;
- **Heavier hybrid supermultiplet:** positive-parity states with  $J^{PC} = (0, 1)^{+-}, (0, 1, 2)^{++}$ ;
- **Heaviest 0<sup>--</sup> hybrid** may suggest a highly excited gluonic structure.

# Possible Decay Patterns: $\bar{c}Gc$ charmonium hybrids

$J^G J^{PC}$	S-wave	P-wave
$0^- 1^{--}$	—	—
$0^+ 0^{++}$	$\eta_c(1S)f_0(600)$	—
$0^+ 1^{+-}$	—	$\eta_c(1S)\eta, J/\psi\omega(782)$
$0^+ 2^{++}$	—	$D\bar{D}^*, J/\psi\omega(782)$
$0^- 0^{+-}$	—	$J/\psi f_0(600)$
$0^+ 2^{++}$	$J/\psi\omega(782), J/\psi\phi(1020),$ $\chi_{c2}(1P)f_0(600)$	$D\bar{D}_1, D\bar{D}_2^*, D^*\bar{D}_0^*, D^*\bar{D}_1, D^*\bar{D}_0^*, J/\psi h_1(1170),$ $\eta_c(1S)f_1(1285), \eta_c(1S)f_2(1270), \chi_{c(1,2)}(1P)\eta$
$0^- 1^{+-}$	$D\bar{D}^*, J/\psi\eta, \psi(2S)\eta, \chi_{c0}(1P)h_1(1170)$	$D\bar{D}_0^*, D\bar{D}_1, D\bar{D}_2^*, D^*\bar{D}_0^*, D^*\bar{D}_2^*, D^*\bar{D}_1, \eta_c(1S, 2S)h_1(1170)$
$0^+ 1^{++}$	$D\bar{D}^*, D_0^*\bar{D}_1, D_1\bar{D}_2^*, J/\psi\omega(782),$ $J/\psi\phi(1020), \chi_{c0}(1P)f_1(1285),$ $\chi_{c1}(1P)f_0(600), \chi_{c2}(1P)f_1(1285)$	$D\bar{D}_0^*, D\bar{D}_1, D\bar{D}_2^*, D^*\bar{D}_0^*, D^*\bar{D}_2^*, D^*\bar{D}_1,$ $\eta_c(1S, 2S)f_0(600), \eta_c(1S, 2S)f_0(980), J/\psi h_1(1170),$ $\eta_c(1S)f_1(1285), \eta_c(1S)f_2(1270), \chi_{c(0,1,2)}(1P)\eta$
$0^+ 0^{++}$	$J/\psi\omega, J/\psi\phi, \eta_c(1S, 2S)\eta, \chi_{c0}(1P)f_0(600),$ $\chi_{c0}(1P)f_0(980), \chi_{c1}(1P)f_1(1285)$	$D\bar{D}_1, D^*\bar{D}_0^*, D^*\bar{D}_1, D^*\bar{D}_2^*, \eta_c(1S, 2S)f_1(1285),$ $J/\psi h_1(1170), \psi(2S)h_1(1170), \chi_{c1}(1P)\eta$
$0^- 0^{--}$	$D\bar{D}_0^*, D^*\bar{D}_1, J/\psi f_1(1285),$ $\psi(2S)f_1(1285), \chi_{c1}(1P)\omega(782)$	$D\bar{D}^*, D_0^*\bar{D}_1, D_1\bar{D}_2^*, J/\psi\eta, \psi(2S)\eta,$ $\eta_c(1S)\omega(782), \eta_c(2S)\omega(782), \chi_{c(0,1,2)}(1P)h_1(1170)$

S + P-wave selection rule:  $D^{(*)}\bar{D}_0^*$  and  $D^{(*)}\bar{D}_1$  are dominant decay modes!

Could be a strong signature at future experiments, especially BESIII, PANDA and LHCb!

## Correlation function and spectral density:

- We calculate the correlation functions and spectral densities by including dimension six condensates.

## Mass predictions of the $\bar{c}Gc$ and $\bar{b}Gb$ hybrids:

- Unstable channels are stabilized by the dimension six condensates;
- Predict the masses of the exotic hybrid channels:  $1^{-+}, 0^{+-}, 0^{--}$ ;
- Pure hybrid interpretation of  $X(3872)$  seems to be precluded;
- We confirm the supermultiplet structure of the hybrid spectrum.

## Possible decay patterns:

- $D^{(*)}\bar{D}_0^*$ ,  $D^{(*)}\bar{D}_1$  and  $D_s^{(*)}\bar{D}_{s0}^*$ ,  $D_s^{(*)}\bar{D}_{s1}$  are dominant decay modes;
- A strong signature at BESIII, PANDA and LHCb in the future.



THANK YOU VERY MUCH!