

Is the muon just a heavy electron?

01/10/20

HET Lunch Talk

An update on LFUV

outline

- **This is mostly a progress report supplemented with some interesting developments of past some months**
- **+ Some implications for the HEF and for the IF**

Anomalies galore!

- RD(*) $\sim 46(?)$; ALSO $R_4 \sim 26$ LHCL
- RK(*) : $2.66(R_K)$; 2.2 $\rightarrow 2.56$ $R_K^+ \Rightarrow \sim 3.56$
- g -2...BNL \Rightarrow FNAL expt... ~ 3.66 *main lattice progress*
- \mathcal{E}' : a personal obsession....for a long^{^3} time \Rightarrow 'cause of the strong belief that it is super-sensitive to NP
 216[PRL 2015] \Rightarrow ~ 1400 of which ~ 740 g c analyzed
 $[2.1\sigma \Rightarrow ??]$ few more months to new results
- **Notice in each case, because of the omnipresence of non-perturbative effects, lattice methods provide crucial info for experiments to be able to use the data in the most economical manner**

Why lattice is needed?

expt measurement $\sim f[G_K, m_\pi, V_{CKM} \Sigma C_i \langle O_i \rangle]$

$(2.232 \pm 0.007) \times 10^{-3}$
BNL '64 Nobel

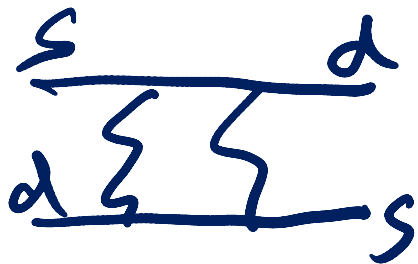
Nonpert ME

$$|\epsilon_K| = \frac{G_F^2 m_W^2 f_K^2 m_K}{12\sqrt{2}\pi^2 \Delta m_K^{\text{exp}}} \hat{B}_{K\epsilon} \text{Im} \left(\eta_1 S_0(x_c) (V_{cs} V_{cd}^*)^2 + 2\eta_3 S_0(x_c, x_t) V_{cs} V_{cd}^* V_{ts} V_{td}^* \right.$$

$$\left. + \eta_2 S_0(x_t) (V_{ts} V_{td}^*)^2 \right).$$

$$\langle K | (\bar{s} \gamma_\mu d) | K \rangle \quad (2.3)$$

MUST HAVE THIS
TO ALL orders in d_s



A.S. in Proceedings of Lattice '85 (FSU)..1st Lattice meeting ever attended

The matrix elements of some penguin operators control in the standard model another CP violation parameter, namely ϵ'/ϵ .^{6,8)} Indeed efforts are now underway for an improved measurement of this important parameter.¹⁰⁾ In the absence of a reliable calculation for these parameters, the experimental measurements, often achieved at tremendous effort, cannot be used effectively for constraining the theory. It is therefore clearly important to see how far one can go with MC techniques in alleviating this old but very difficult

With C. Bernard
[UCLA]

Theo Summary; 16th FPCP; A Soni

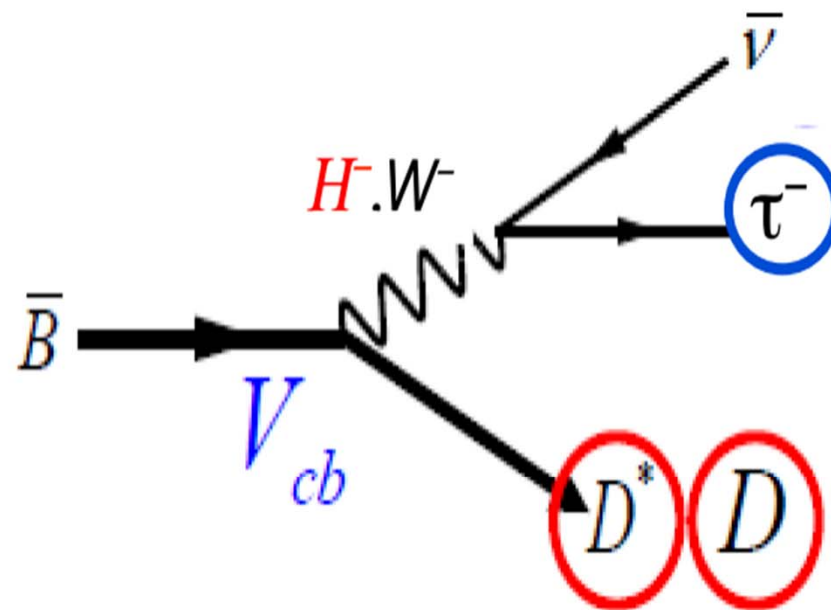
$$\epsilon' \sim 10^{-6}$$



**[SEEMINGLY] BEST CHANCE IN A LONG
TIME FOR POSSIBLE SIGHTINGS OF NEW
PHYSICS**



Exclusive $B \rightarrow D^{(*)}\tau\nu$



RA LUTH (BABAR)

'CP May 2012
(HEFEI, China)

MANUEL FRANCO
SEVILLA
PhD Thesis

Independent of
 V_{cb} !

- To test the SM Prediction, we measure

$$R(D) = \frac{\Gamma(\bar{B} \rightarrow D\tau\nu)}{\Gamma(\bar{B} \rightarrow D\ell\nu)} \quad R(D^*) = \frac{\Gamma(\bar{B} \rightarrow D^*\tau\nu)}{\Gamma(\bar{B} \rightarrow D^*\ell\nu)}$$

Leptonic τ
decays only

Several experimental and theoretical uncertainties cancel in the ratio!

- DD events are fully reconstructed.

some expt + also some
The only errors tend to cancel

$l = \mu$ or e

Improving constraints on $\tan\beta/m_H$ using $B \rightarrow D \tau \bar{\nu}$

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(Received 12 June 1997)

We study the q^2 dependence of the exclusive decay mode $B \rightarrow D \tau \bar{\nu}$ in type-II two Higgs doublet models (2HDM's) and show that this mode may be used to put stringent bounds on $\tan\beta/m_H$. There are currently rather large theoretical uncertainties in the q^2 distribution, but these may be significantly reduced by future measurements of the analogous distribution for $B \rightarrow D(e, \mu) \bar{\nu}$. We estimate that this reduction in the theoretical uncertainties would eventually (i.e., with sufficient data) allow one to push the upper bound on $\tan\beta/m_H$ down to about 0.06 GeV^{-1} . This would represent an improvement on the current bound by about a factor of 7. We

11/15



the SM ←

- 10

Semileptonic B decays

BaBar measured an excess of $B^0 \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau$ (**3 σ away from SM!**) [PRD 88 (2013) 072012]
[Nature 546 (2017) 227]

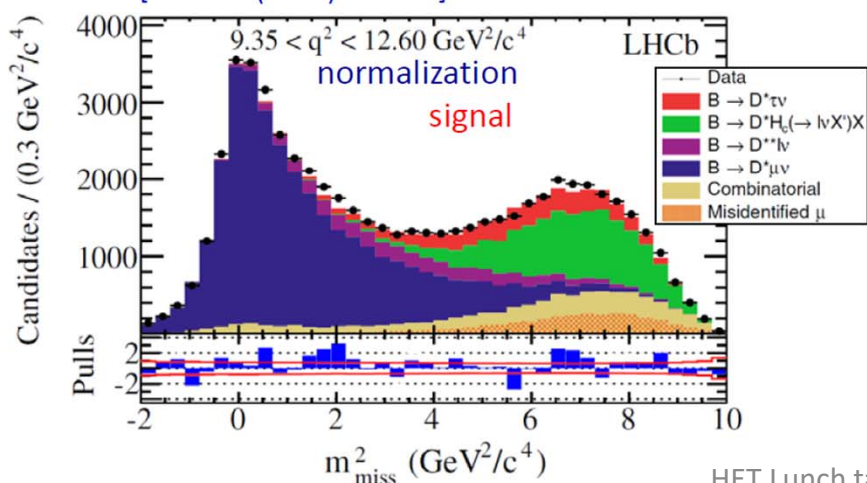
LHCb:

- $R(D^*)$
 - $B^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$, with $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$ [PRL 115 (2015) 111803]
 - $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$, with $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ (\pi^0) \bar{\nu}_\tau$ [PRL 120 (2018) 171802]
- $R(J/\psi)$
 - $B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau$, with $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$ [PRL 120 (2018) 121801]

■ Using $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$

Information from the missing mass squared $m_{\text{miss}}^2 = (P_B - P_{D^*} - P_\mu)^2$ and muon energy

[PRL 115 (2015) 111803]

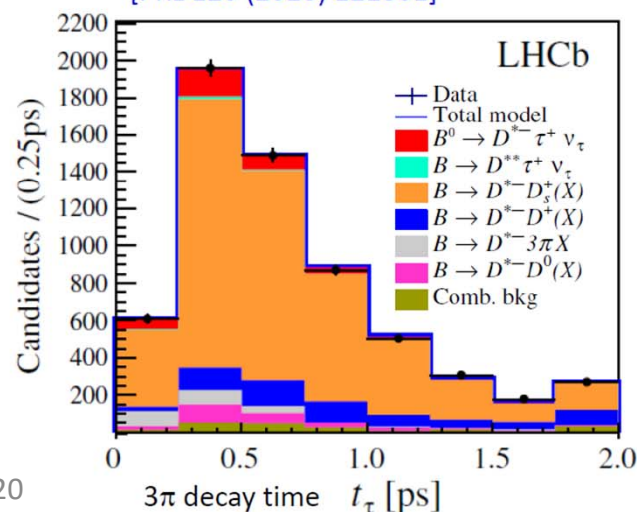


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■ Using $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau$

Information from the position of the pions. Normalized to $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$

[PRL 120 (2018) 121801]

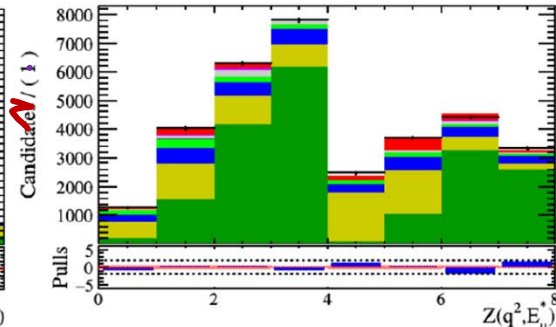
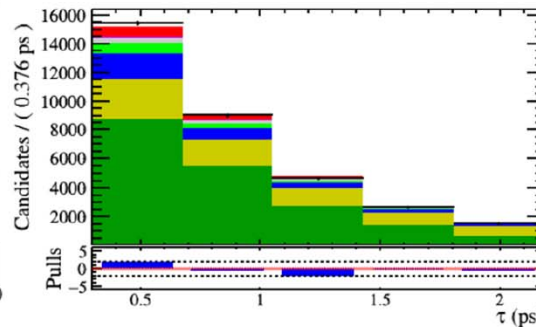
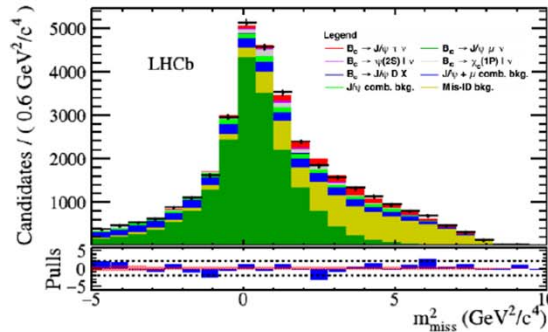


$$B_c \rightarrow J/\psi \tau \nu$$

2 PM Jan 2018

Greg Ciezarek,
on behalf of the LHCb collaboration

$$B_c \rightarrow \frac{b \rightarrow W \tau \nu}{\tau \rightarrow \mu \nu} \mu \nu$$



- $R_{J/\psi} \equiv B_c \rightarrow J/\psi \tau \nu / B_c \rightarrow J/\psi \mu \nu$
- Measured using very similar techniques to $\mathcal{R}(D^*)$, on run 1 data
- $R_{J/\psi} = 0.71 \pm 0.17 \pm 0.18$

- $\sim 2\sigma$ from SM

- But nearly as far from consistency with $\mathcal{R}(D^*)$

- LHCb-PAPER-2017-035 (Run 1 data)

SM $R_{J/\psi} \sim 0.265 \pm 0.025$

QUITE ROBUST!

ESSENTIALLY A NR BOUND STATE

C ALSO MARK SMITH PAPER 2018

REMAINING ISSUES

PRIMARY EXPTAL

1. Stat 2. D^{**} 3. $\tau \rightarrow h c l + 2 \nu$

Bc => psi tau(l) nu...Th/ph

PHYSICAL REVIEW D **98**, 094026 (2018)

Model-independent determination of $B_c^+ \rightarrow \eta_c \ell^+ \nu$ form factors

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(Received 31 August 2018; published 27 November 2018)

We derive model-independent bounds on the form factors for the decay $B_c^+ \rightarrow \eta_c \ell^+ \nu$ including full mass effects, i.e., $\ell = e, \mu$, and τ . The bounds are obtained by using the Boyd-Grinstein-Lebed parametrization for the form factors, and fitting to the preliminary lattice data of the HPQCD Collaboration. Our main result after bounding the form factors is the Standard Model prediction for the ratio of branching fractions $R(\eta_c) = \mathcal{B}(B_c^+ \rightarrow \eta_c \tau^+ \nu_\tau) / \mathcal{B}(B_c^+ \rightarrow \eta_c \mu^+ \nu_\mu)$. We find $R(\eta_c)|_{\text{SM}} = 0.31^{+0.04}_{-0.02}$, and argue that a measurement of $R(\eta_c)$ is within the reach of LHCb during the high-luminosity run of the LHC. In addition, using the heavy-quark spin symmetry of the B_c meson we relate our results for $B_c^+ \rightarrow \eta_c \ell^+ \nu$ to those for $B_c^+ \rightarrow J/\psi \ell^+ \nu$ yielding the estimate $R(J/\psi)|_{\text{SM}} = 0.26 \pm 0.02$ in good agreement with other determinations.

R_ψ

0.26 ± 0.02

Ref

Murphy
+ Soni

0.29 ± 0.07 Ivanov

+ Issaadykov
PLB'18

0.283 ± 0.045

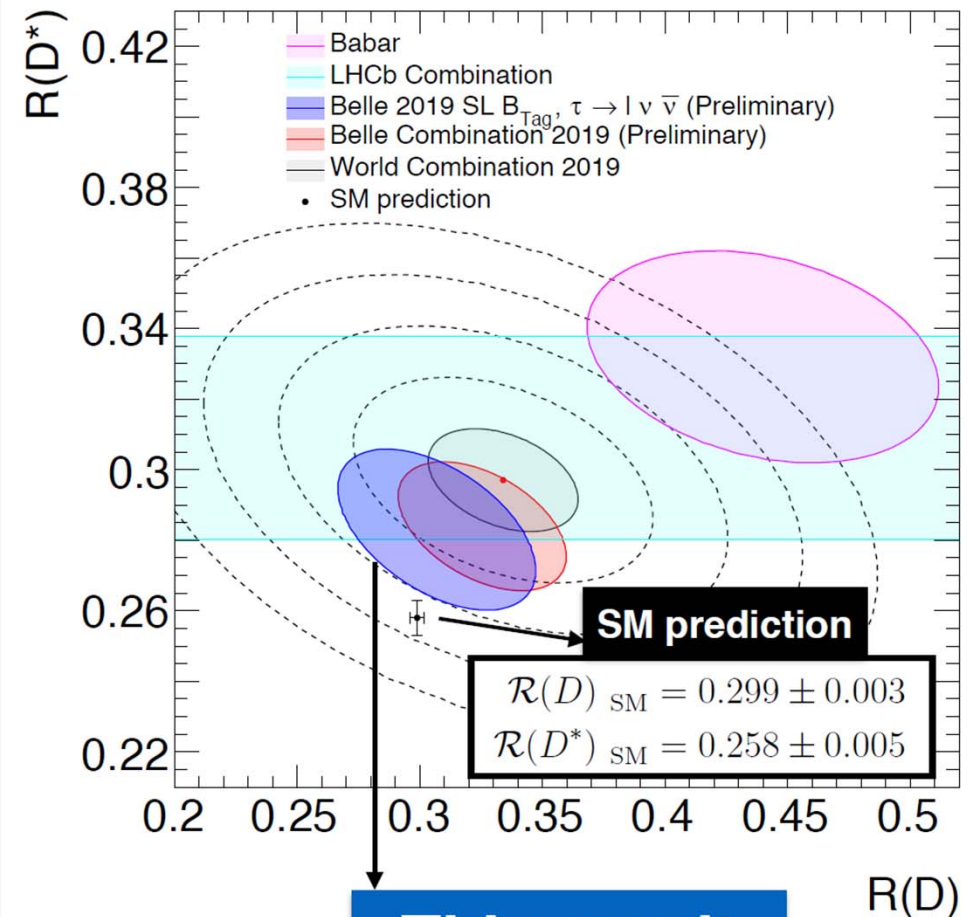
Watanabe
PLB'18

JHEP'18

< also Berns + Lamm

Conclusion / Preliminary $R(D^{(*)})$ averages

- **Most precise measurement** of $R(D)$ and $R(D^*)$ to date
- First **$R(D)$** measurement performed with a **semileptonic tag**
- Results **compatible with SM** expectation within **1.2σ**
- **$R(D) - R(D^*)$ Belle average** is now within **2σ** of the SM prediction
- **$R(D) - R(D^*)$ exp. world average** tension with SM expectation **decreases from 3.8σ to 3.1σ**



This result

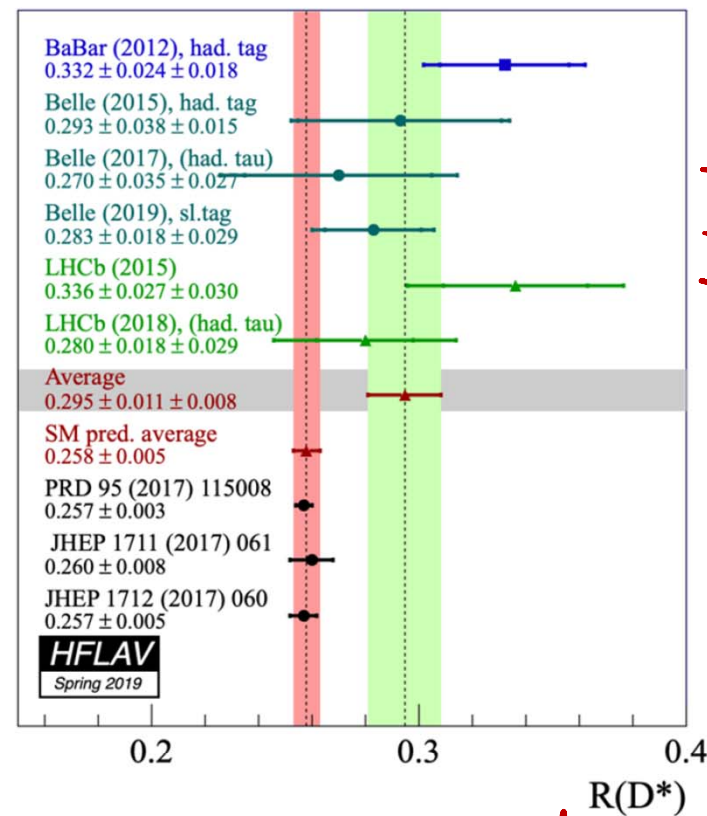
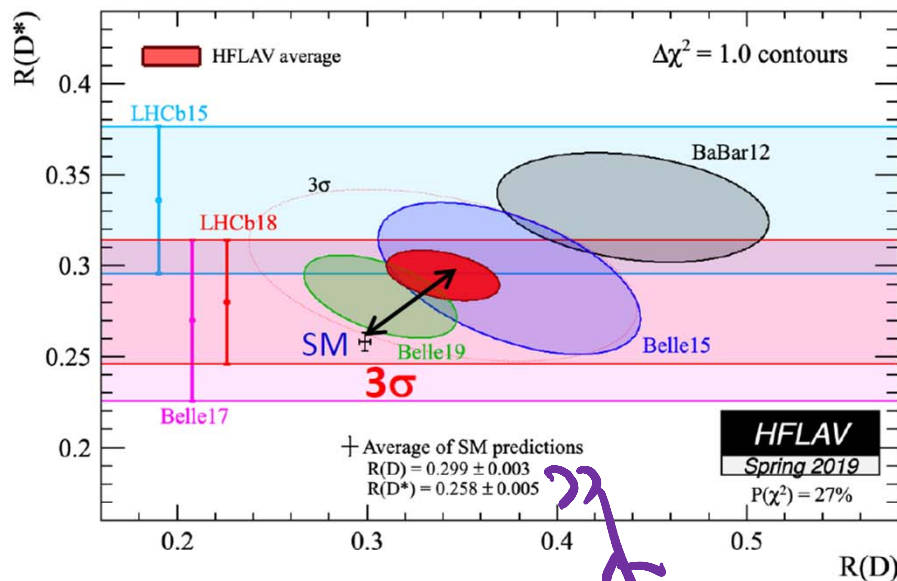
$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016$$
$$\mathcal{R}(D^*) = 0.283 \pm 0.018 \pm 0.014$$

Semileptonic B decays

6 R_{D^*} measurements

New results (Moriond 2019) from Belle:

- Global picture of R_D and R_{D^*}



→ New results from Belle: $4\sigma \rightarrow 3\sigma$ deviation from SM

R_D : 3 BaBar, + Belle

↑↑

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$B \rightarrow D^*$ Form factors from Lattice still cooking

The bottom line

Therefore, it is an excellent approximation to combine the LHCb and B factory results as done in section II. In that case we find

$$\frac{R_D}{R_D^{\text{SM}}} = \frac{R_{D^*}}{R_{D^*}^{\text{SM}}} = 1.15 \pm 0.04 , \quad \text{✂} \quad (24)$$

both for the LHCb and the B-factory expressions in Eqs. (21,22).

FACT OR FARCE?

1) Exptal results (not all independent), AhL central values above Theory!

4

experiment	tag method	τ decay mode	R_D	R_D^*	R_ψ
Babar (2012)[1]	hadronic	$1 \nu \nu$	$0.440 \pm 0.058 \pm 0.042$	$0.332 \pm 0.024 \pm 0.018$	
Belle (2015)[2]	hadronic	$1 \nu \nu$	$0.375 \pm 0.064 \pm 0.026$	$0.293 \pm 0.038 \pm 0.015$	
LHCb (2015)[5]	hadronic	$1 \nu \nu$	-	$0.336 \pm 0.027 \pm 0.030$	
Belle (2016)[2]	semileptonic	$1 \nu \nu$	-	$0.302 \pm 0.030 \pm 0.011$	
Belle (2017)[4]	hadronic	$\pi(\rho)\nu$	-	$0.270 \pm 0.035 \pm 0.027$	
LHCb (2017)[6]	hadronic	$3\pi\nu$	-	$0.291 \pm 0.019 \pm 0.029$	
Belle (2019)[7]	semileptonic	$1 \nu \nu$	$0.307 \pm 0.037 \pm 0.016$	$0.283 \pm 0.018 \pm 0.014$	
LHCb(2016) [9]	hadronic	$1 \nu \nu$	-	-	$0.71 \pm 0.17 \pm 0.18$
SM	-	-	0.299 ± 0.011	0.260 ± 0.008	0.26 ± 0.02

TABLE I: All experimental results announced to date on R_D , R_{D^*} and on R_ψ versus the predictions of those for the SM

ALTMANNSTHOFER, DEVI+AS, YICONG SUO (in prep)

Excellent 9.5

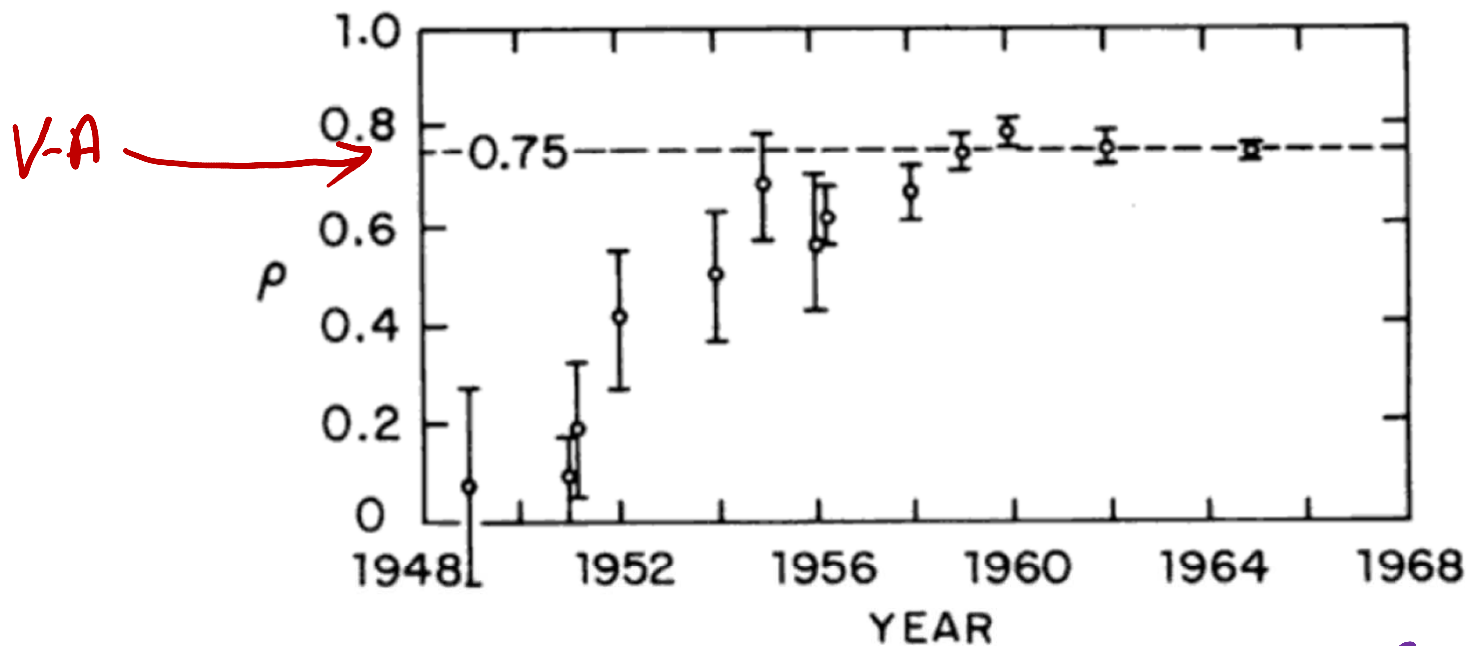
RECAP

- 3 different major B-experiments
 - 3 with $B \Rightarrow D$
 - 7 with $B \Rightarrow D^*$
 - 1 with $B_c \Rightarrow \psi$
 - 9 with $\tau \Rightarrow l$ ($l=\mu$ or e) $\nu \nu'$
 - 2 with $\tau \Rightarrow \text{hadron} + \nu$
-
- Each and everyone of the 11 experimental results seem to imply tau is NOT just a heavy muon(electron) as dictated by SM.

PAUSE

**CAN THERE BE SOME EXPERIMENTAL
ISSUE(S) CAUSING THIS DEVIATION?**

Imp. Historical ~~Aside~~ CAUTION



FROM M PUROHIT

Figure 16. The change of the Michel parameter ρ from year to year.

From T. D. Lee's text

Cs Wu & T.D. Lee defn of rho

20200108_095440.jpg

448

LEE & WU

$$\begin{aligned} i\psi_l^\dagger \gamma_4 \gamma_\lambda (C_V - C_A \gamma_5) \psi_{\nu_l} &= (C_V - C_A) i\psi_l^\dagger \gamma_4 \gamma_\lambda \psi_{\nu_l} \\ &= (C_V - C_A) i\psi_l^\dagger \gamma_4 \gamma_\lambda \gamma_5 \psi_{\nu_l} \end{aligned}$$

Insofar as μ decay is concerned, there is no difference between a $(V-A)$ interaction and a, say, $(V+10A)$ interaction, provided the two-component theory holds for both ν_e and ν_μ . At present, all experimental evidences in μ decay are in excellent agreement with the above form of $(V-A)$ interaction.

1. *The electron spectrum and the Michel parameter.*—The decay electron momentum spectrum from μ decay is

$$N(x) = x^2 \left\{ \left(2 - \frac{4}{3} \rho \right) - \left(2 - \frac{16}{9} \rho \right) x \right\}$$

where

$$x = \frac{|\mathbf{p}_e|}{m_\mu/2}$$

The constant ρ is called the Michel parameter. If the conservation laws of lepton numbers L_e and L_μ hold and if the two-component theory is valid for both ν_e and ν_μ , then [independent of whether the μ -decay interaction consists of (V, A) or (S, P) couplings]

$$\rho = 3/4$$



Flag 2019: sample [Nf=2 +1]

- $BK^{\text{hat}} = 0.7625(97) \dots 1.5\%$

- $f_B = 192.0 (4.3) \text{ MeV} \dots 2.2 \%$

- $\xi = 1.206 (17) \dots 1.5\%$

$\rightarrow SU(3) \text{ breaking}$

- $B \Rightarrow D, \delta[\text{sl FF } (q^2)] \sim 10\%$

- $RD \sim 4\%$

- $B \Rightarrow D^* [\text{incomp}]$

$\rangle\rangle$ Need lot more
work esp due
expts on the
horizon

Semileptonic $B \rightarrow \pi \ell \nu$, $B \rightarrow D \ell \nu$, $B_s \rightarrow K \ell \nu$, and $B_s \rightarrow D_s \ell \nu$ decays

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We present updates for our nonperturbative lattice QCD calculations to determine semileptonic form factors for exclusive $B \rightarrow \pi \ell \nu$, $B \rightarrow D \ell \nu$, $B_s \rightarrow K \ell \nu$, and $B_s \rightarrow D_s \ell \nu$ decays. Our calculation is based on RBC-UKQCD's set of $2+1$ -dynamical-flavor gauge field ensembles. In the valence sector we use domain wall fermions for up/down, strange and charm quarks, whereas bottom quarks are simulated with the relativistic heavy quark action. The continuum limit is based on three lattice spacings. Using kinematical z expansions we aim to obtain form factors over the full q^2 range. These form factors are the basis for predicting ratios addressing lepton flavor universality or, when combined with experimental results, to obtain CKM matrix elements $|V_{ub}|$ and $|V_{cb}|$.

arXiv:1912.09946v1 [hep-lat] 20 Dec 2019

	$L^3 \times T$	a^{-1} / GeV	am_l	M_π / MeV	# Configurations	# Time Sources
C1	$24^3 \times 64$	1.784	0.005	338	1636	1
C2	$24^3 \times 64$	1.784	0.010	434	1419	1
M1	$32^3 \times 64$	2.383	0.004	301	628	2
M2	$32^3 \times 64$	2.383	0.006	362	889	2
M3	$32^3 \times 64$	2.383	0.008	411	544	2
F1	$48^3 \times 96$	2.774	0.002144	234	98	24

Table 1: The RBC-UKQCD 2+1 domain-wall fermion ensembles used in this work [50–53]. The F ensemble is a new element of the RBC/UKQCD b -physics project analysis and is a key difference between this work and the prior analysis. Presently the properties of the F1 ensemble are re-evaluated and may change slightly.

m_π, m_K physics not yet complete

$B_n(B \rightarrow \mu \nu \gamma_{hard}) \sim 12$

Radiative leptonic decays on the lattice



↑ hard
"γ"
cures
helicity
supp

$B_n(B \rightarrow \mu \nu)$
Atwood, ED
AS 64

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Adding a hard photon to the final state of a leptonic pseudoscalar-meson decay lifts the helicity suppression and can provide sensitivity to a larger set of operators in the weak effective Hamiltonian. Furthermore, radiative leptonic B decays at high photon energy are well suited to constrain the first inverse moment of the B -meson light-cone distribution amplitude, an important parameter in the theory of nonleptonic B decays. We demonstrate that the calculation of radiative leptonic decays is possible using Euclidean lattice QCD, and present preliminary numerical results for $D_s^+ \rightarrow \ell^+ \nu \gamma$ and $K^- \rightarrow \ell^- \bar{\nu} \gamma$.

g.s excellent

NON-LOCAL ME

//el efflat: our Roman friends: G.M. et al

Lepton universality tests

- In the SM, ratios

$\bar{b} \rightarrow \bar{u} \mu^+ \mu^-$
 $\bar{b} \rightarrow \bar{u} e^+ e^-$

$$R_K = \frac{\int d\Gamma[B^+ \rightarrow K^+ \mu^+ \mu^-]/dq^2 \cdot dq^2}{\int d\Gamma[B^+ \rightarrow K^+ e^+ e^-]/dq^2 \cdot dq^2}$$

LHCb introduced such & well defined ratios

only differ from unity by phase space — the dominant SM processes couple equally to the different lepton flavours.

- Theoretically clean since hadronic uncertainties cancel in the ratio.
- Experimentally challenging due to differences in muon/electron reconstruction (in particular Bremsstrahlung from the electrons).
 - Take double ratios with $B \rightarrow J/\psi X$ decays to cancel possible sources of systematic uncertainty.
 - Correct for migration of events in q^2 due to FSR/Bremsstrahlung using MC (with PHOTOS).

LHCb

Lepton Flavour Universality

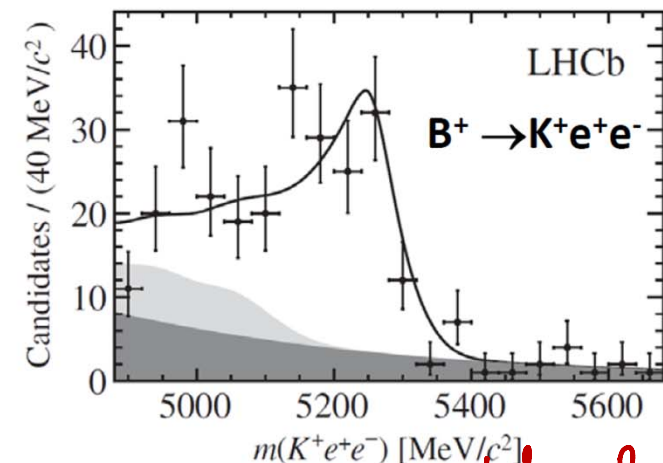
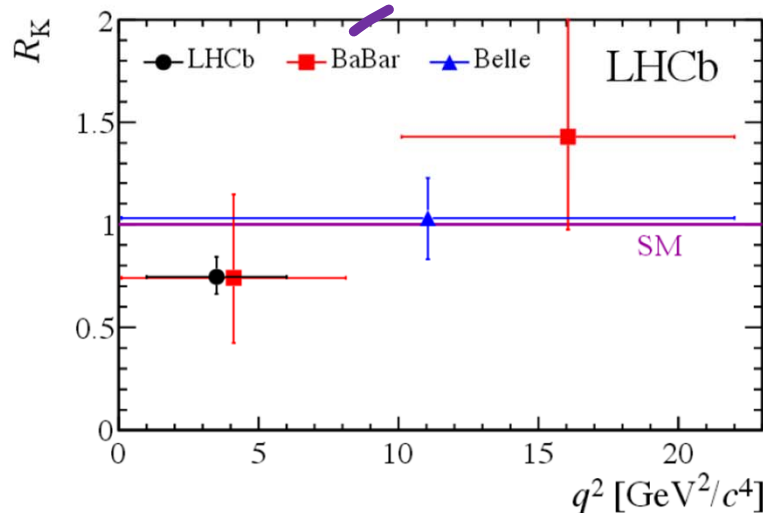
Arantza Oyanguren

- In the SM all leptons are expected to behave in the same way

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)} = 1.000 + \mathcal{O}(m_\mu^2/m_b^2) \text{ (SM)}$$

[PRL 113 (2014) 151601]

- Experimentally, use the $B^+ \rightarrow K^+ J/\psi (\rightarrow e^+ e^-)$ and $B^+ \rightarrow K^+ J/\psi (\rightarrow \mu^+ \mu^-)$ to perform a double ratio
- Precise theory prediction due to **cancellation of hadronic form factor uncertainties**



$1 \text{ GeV} < q^2 < 6 \text{ GeV}$ *should be safe from Rad Corr*

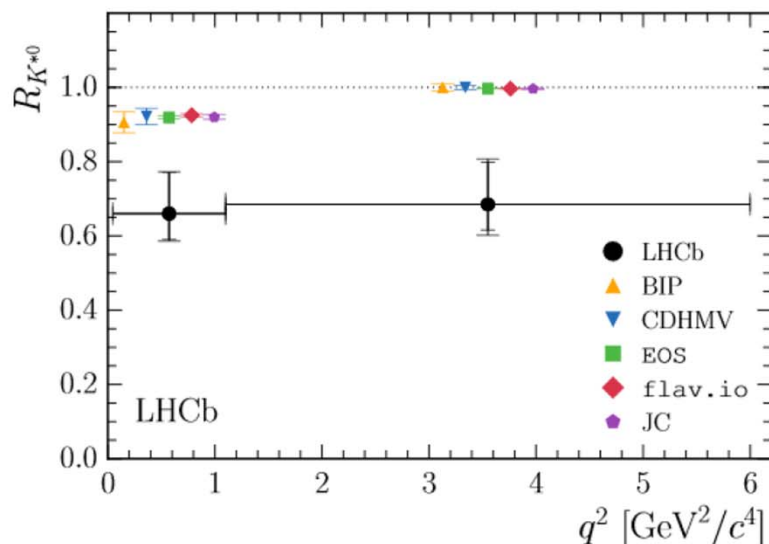
$$R_K = 0.745^{+0.090}_{-0.074} (\text{stat}) \pm 0.036 (\text{syst})$$

→ Consistent, but lower, than the SM at **2.6σ**

LHCb Lepton Flavour Universality

• Results:

LHCb, JHEP08(2017)055



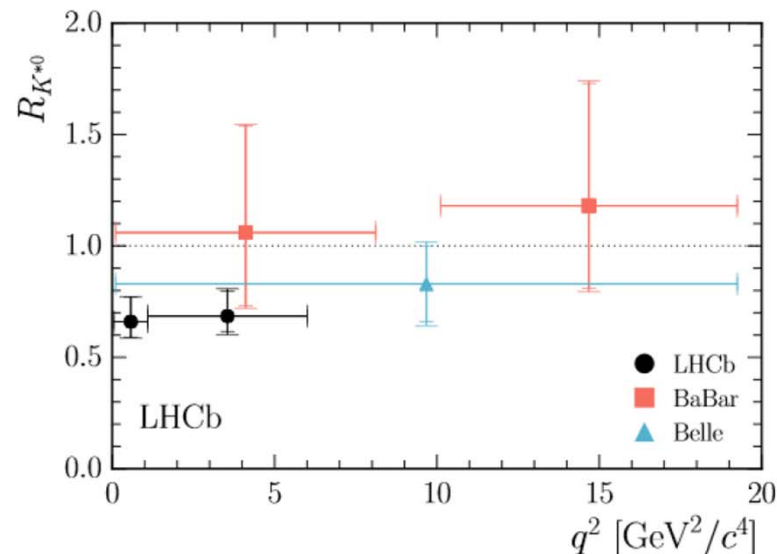
- ▲ BIP [EPJC 76 (2016) 440]
- ▼ CDH MV [JHEP 04 (2017) 016]
- EOS [PRD 95 (2017) 035029]
- ◆ flav.io [EPJC 77 (2017) 377]
- JC [PRD 93 (2016) 014028]

Low q^2 [0.045-1.1 GeV²]: $SM_{\nabla} = 0.922(22)$

$$R_{K^{*0}} = 0.66 \pm 0.11 \text{ (stat)} \pm 0.03 \text{ (syst)}$$

Central q^2 : [1.1-6 GeV²]: $SM_{\nabla} = 1.000(6)$

$$R_{K^{*0}} = 0.69 \pm 0.11 \text{ (stat)} \pm 0.05 \text{ (syst)}$$



- LHCb [PRL 113 (2014) 151601]
- ▲ Belle [PRL 103 (2009) 171801]
- BaBar [PRD 86 (2012) 032012]

$\approx 3.4\sigma$

→ Consistent, but lower than the SM at **2.1-2.3 σ** (low q^2) and **2.4-2.5 σ** (central q^2)

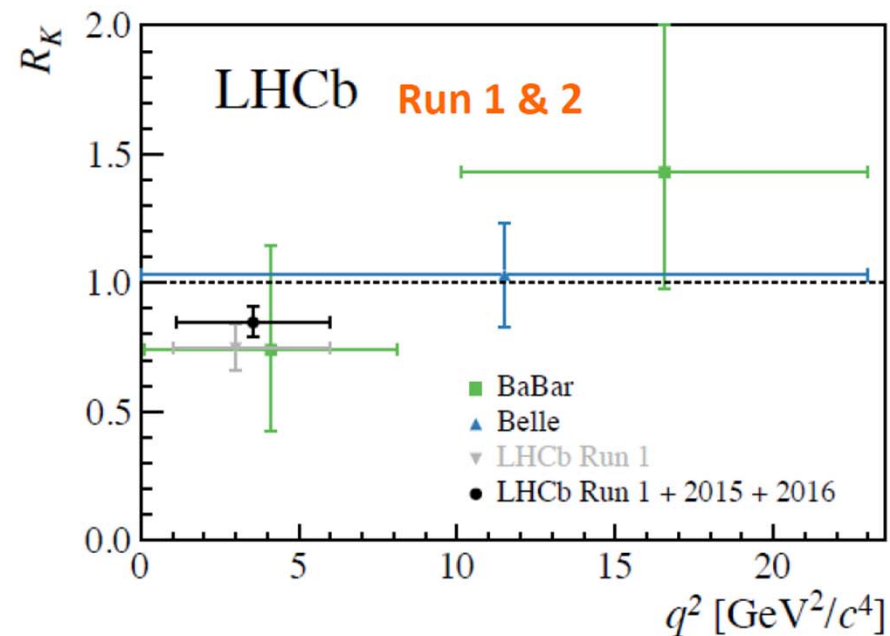
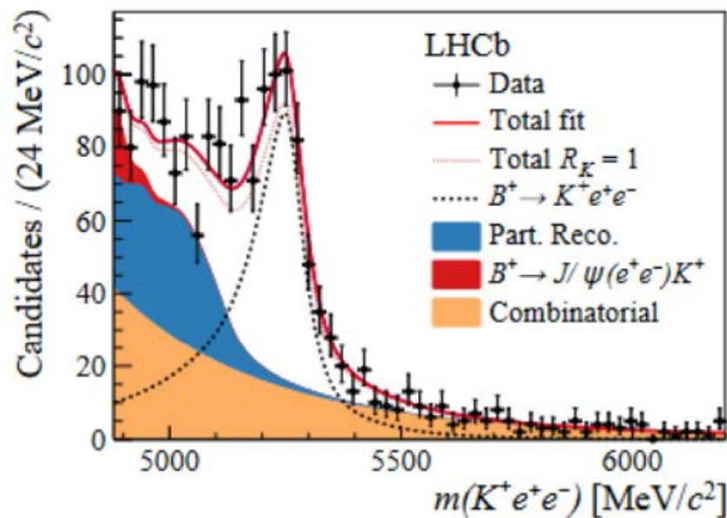
Rare B decays: R_K

New results (Moriond 2019):

Including partial sample of
Run2 (2fb^{-1})

[LHCb, *PRL* 122 (2019) 191801]

With improved reconstruction and
re-optimized analysed strategy



$1.1 \text{ GeV} < q^2 < 6 \text{ GeV}$

$$R_K = 0.846^{+0.060}_{-0.054}(\text{stat.})^{+0.016}_{-0.014}(\text{syst.})$$

→ Still consistent, lower, than the SM at 2.5σ

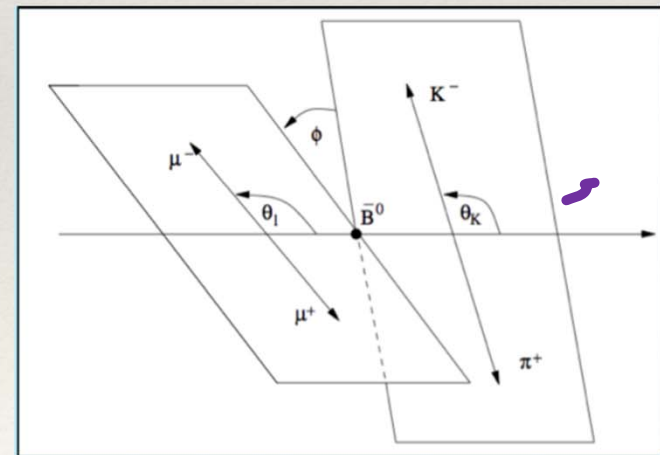
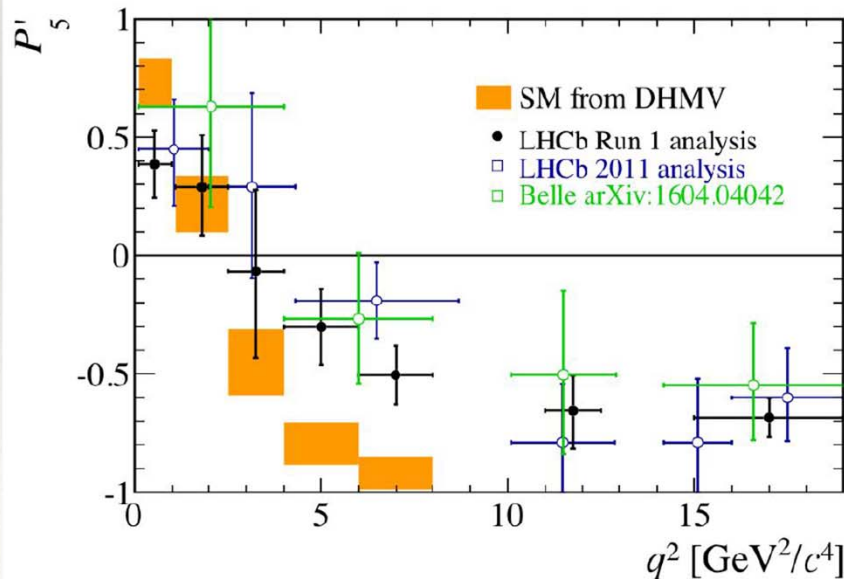
Not confirmed, not ruled out...

B-flavor anomalies: P_5' $B \rightarrow K \mu \mu$

REMAIN CONCERNED
ABOUT NON-local
contributions

Much LESS clean esp
in low q^2

- ❖ Several angular observables measured as functions of q^2
- ❖ Some, like P_5' , are optimized to be insensitive to hadronic uncertainties: [\[Descotes-Genon, Matias, Ramon, Virto: 1207.2753\]](#)



LHCb also finds deficit in
observed $B_s \rightarrow \phi \mu \mu$ compared to "SM"
 $\sim 2.5 \sigma$
Less reliable
due to LD contamination

URGENTLY Needed! $\Rightarrow R_\phi \equiv \frac{B_s \rightarrow \phi \mu \mu}{B_s \rightarrow \phi e e}$
FROM LHCb

MUON (G-2) ANOMALY....VERY SPECIAL FOR BNL

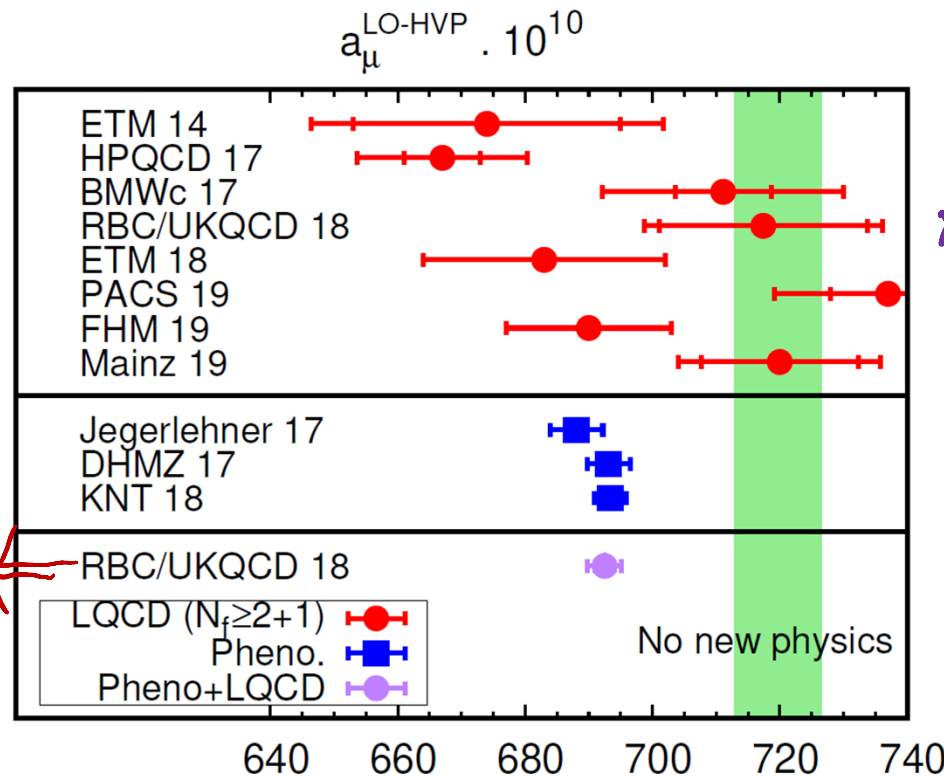
A. El-Khadra's talk at Seattle INT workshop.

Sept 2019

$(g-2)_\mu$

[prepared by K. Miura for WP]

[V.]

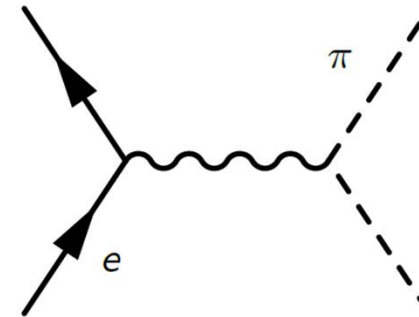
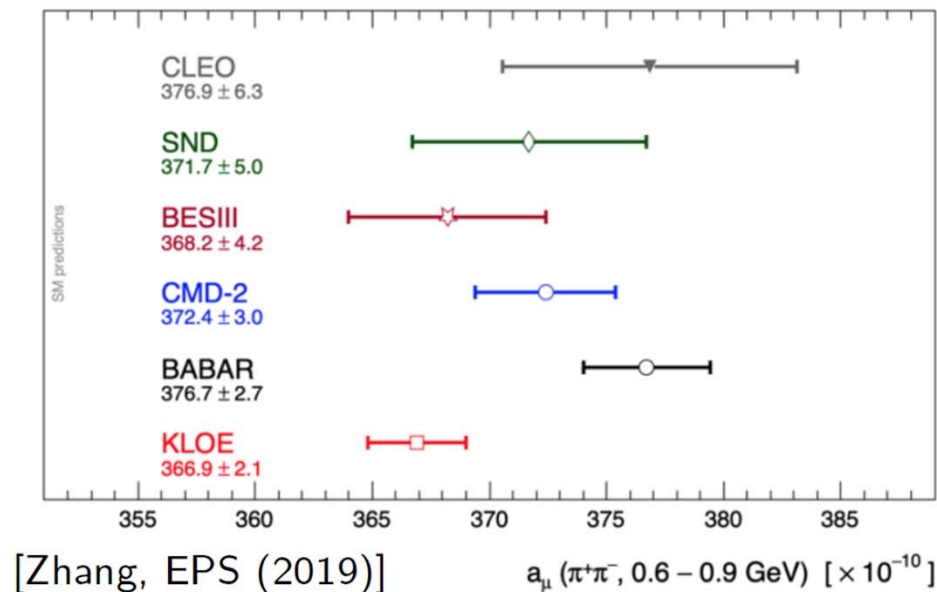


x 1/3 reduction
in errors
very soon by
RBC-UKQCD
[CL]

C. Let al \neq

Lattice work started by Tom Blum
EBNL '04

Tensions in Experiment



R-ratio data for $ee \rightarrow \pi\pi$ exclusive channel, $\sqrt{s} = 0.6 - 0.9$ GeV region

Tension between most precise measurements (BABAR/KLOE)

R-ratio a_μ^{HVP} uncertainty $<$ difference in this channel

Avoid tension by computing precise lattice-only estimate of a_μ^{HVP}

Use lattice QCD to inform experiment, resolve discrepancy

speculation

Ist gem not
sensitive to
NP
+

$(g-2)_\mu$
 $R_K(x)$
+
 $R_D(x)$

-

Table 1

Constraints on lepton-flavor violating and conserving processes. For the last four observables, the experimental null results are given in terms of a dimension-6 operator, suppressed by two orders of Λ , which can be interpreted as the nominal scale of new physics.

Observable	Limit
$\text{Br}(\mu \rightarrow 3e)$	$< 1.0 \times 10^{-12}$ [1]
$\text{Br}(\mu \rightarrow e\gamma)$	$< 5.7 \times 10^{-13}$ [1]
$\text{Br}(\tau \rightarrow 3e)$	$< 2.7 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow e^- \mu^+ \mu^-)$	$< 2.7 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow e^+ \mu^- \mu^-)$	$< 1.7 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow \mu^- e^+ e^-)$	$< 1.8 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow \mu^+ e^- e^-)$	$< 1.5 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow 3\mu)$	$< 2.1 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow \mu\gamma)$	$< 4.4 \times 10^{-8}$ [1]
$\text{Br}(\tau \rightarrow e\gamma)$	$< 3.3 \times 10^{-8}$ [1]
μ - e conversion	$\Lambda \gtrsim 10^3 \text{ TeV}$ [5]
$e^+ e^- \rightarrow e^+ e^-$	$\Lambda \gtrsim 5 \text{ TeV}$ [3]
$e^+ e^- \rightarrow \mu^+ \mu^-$	$\Lambda \gtrsim 5 \text{ TeV}$ [3]
$e^+ e^- \rightarrow \tau^+ \tau^-$	$\Lambda \gtrsim 4 \text{ TeV}$ [3]

KILC, KOBACH
+ AS
PRD2015

Possibly interesting inter-related story reg. LUV evolving over the past ~15 years

- μ on (g-2).....BNL ~2004; FermiL ~2017=>?
- $RD(*)$ BaBar, Belle, LHCb~2012-----→
- $RK(*)$ LHCb ~2014-----→
- Intriguing rather long tell- tale signs of LUV or few sigma flukes?
- Fortunately, wont have to wait too long < ~ 2 years due to FermiL, LHCb & Belle-II AND LATTICE

MODEL INDEPENDENT TESTS AT HIGH PT

- In a nut-shell B-experiments seem to find anomalous behavior in the underlying $b \Rightarrow c \text{ tau } \nu$
- This necessarily [by XSym] implies there should be analogous anomaly in $g + c \Rightarrow b \text{ tau } \nu \dots \Rightarrow \text{pp} \Rightarrow b \text{ tau } \nu$
- *Thus it immediately leads to inescapable search channels for possible NP at the high energy frontier for ATLAS & CMS and these are urgently urged*

Low pt \Leftrightarrow high pt interplay

- XS of $b \Rightarrow c \tau \nu$ \Rightarrow $g + b \Rightarrow b \tau \nu$
 - XS of $b \Rightarrow s \ell \ell$ \Rightarrow $g + s \Rightarrow b \ell \ell$
 - C Altmannshofer, Dev, AS, PRD 2017
- $g \equiv \text{gluon}$

IF
exptl hints stay then



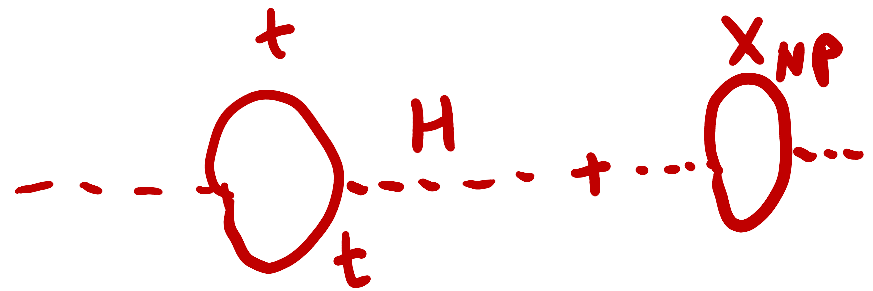
Altmanmshofer, Dev, A.S. 2017
+WIP

**ANOMALIES: POSSIBLY A HINT FOR
(NATURAL) SUSY-WITH RPV3**

then RPV - SUSY extremely well
motivated - -
+ New

- ASSUMING the anomaly is REAL & HERE TO STAY [BIG ASSUMPTION due to caveats mentioned]
- Anomaly involves simple tree-level semi-leptonic decays
- Also $b \Rightarrow \tau$ (3rd family)
- **Speculate: May be related to Higgs naturalness**
- Seek minimal solution: perhaps 3rd family super-partners(a lot) lighter than other 2 gens > proton decay concerns may not be relevant=> RPV [“natural” SUSY]
- **RPV natural setting for LUV ...can accommodate g-2, RK(*) if needs be**
- Collider signals tend to get a lot harder than (usual-RPC) SUSY
- RPV makes leptoquarks natural [and respectable]
- Moreover, RPV should be viewed as an umbrella i.e. under appropriate limits other models are incorporated

$$m_H \approx 126 \text{ GeV}$$



RPV_3 preserves gauge coupling unification irrespective of # of effective gens. 1, 2 or 3.

ADS-PD'17

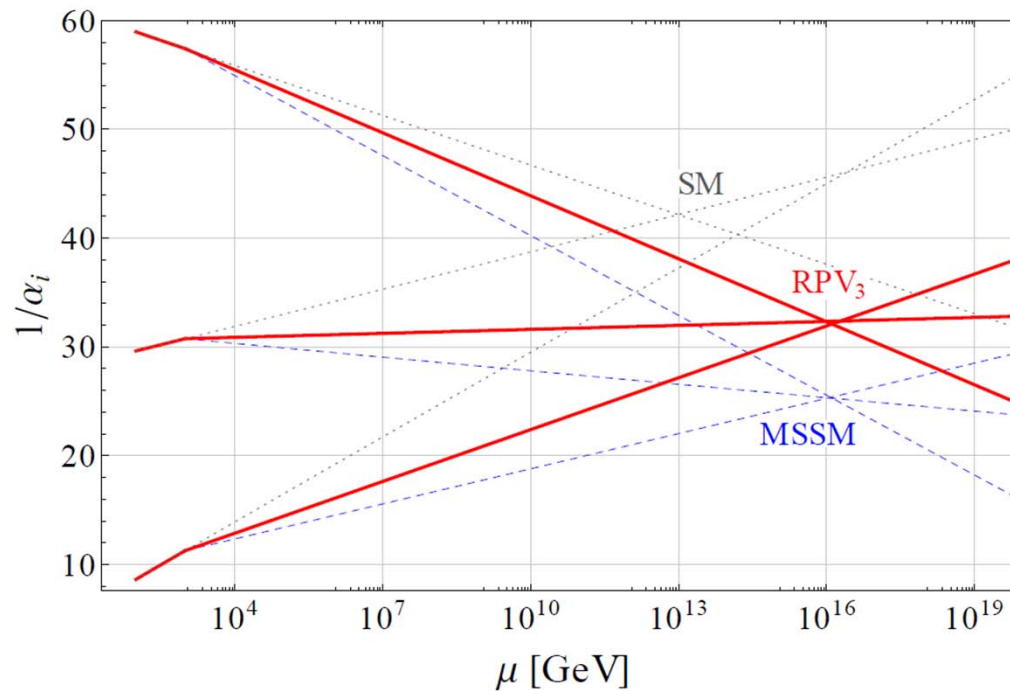


FIG. 2. RG evolution of the gauge couplings in the SM, MSSM and with partial supersymmetrization.

Unification scale stays same, only value of couplings shifts

For pheno relevant terms:

ADS'PRD 2017

$$\mathcal{L} = \lambda'_{ijk} [\tilde{\nu}_{iL} \bar{d}_{kR} d_{jL} + \tilde{d}_{jL} \bar{d}_{kR} \nu_{iL} + \tilde{d}_{kR}^* \bar{\nu}_{iL}^c d_{jL} \\ - \tilde{e}_{iL} \bar{d}_{kR} u_{jL} - \tilde{u}_{jL} \bar{d}_{kR} e_{iL} - \tilde{d}_{kR}^* \bar{e}_{iL}^c u_{jL}] + \text{H.c.}$$

Analogous
of
 G_F
 $\sqrt{2}$

$$\mathcal{L}_{\text{eff}} \supset \frac{\lambda'_{ijk} \lambda'^*_{mnk}}{2m_{\tilde{d}_{kR}}^2} \left[\bar{\nu}_{mL} \gamma^\mu \nu_{iL} \bar{d}_{nL} \gamma_\mu d_{jL} \right. \\ \left. - \nu_{mL} \gamma^\mu e_{iL} \bar{d}_{nL} \gamma_\mu \left(V_{\text{CKM}}^\dagger u_L \right)_j + \text{h.c.} \right] \\ - \frac{\lambda'_{ijk} \lambda'^*_{mjn}}{2m_{\tilde{u}_{jL}}^2} \bar{e}_{mL} \gamma^\mu e_{iL} \bar{d}_{kR} \gamma_\mu d_{nR} ,$$

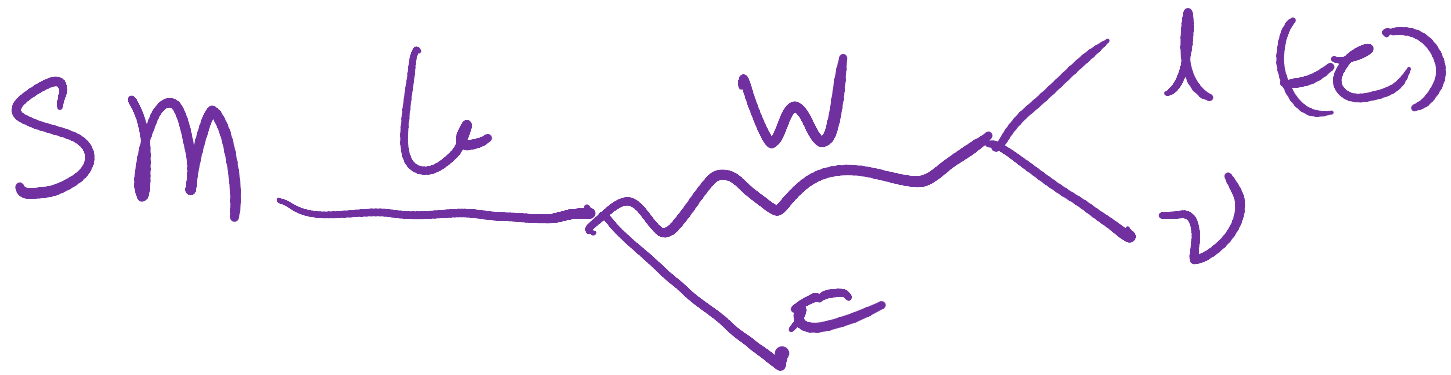
) RPV₃ interaction

← Dim-6

→ $f_n \Gamma_D(x)$

NOTE:

ITS
SM-like!



RPV

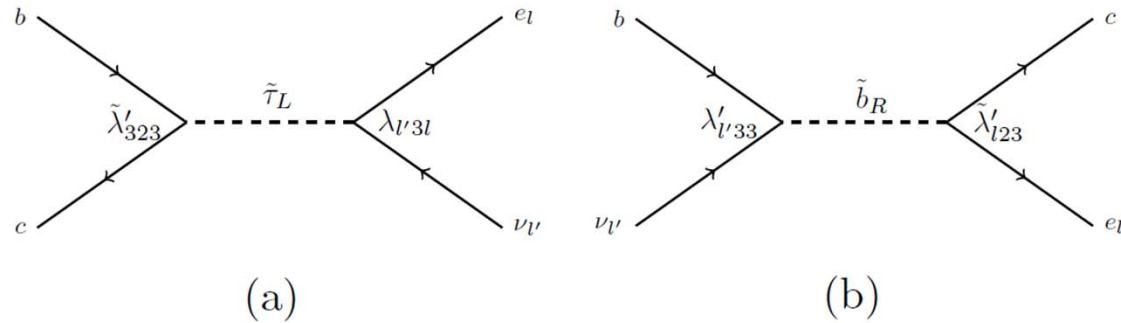


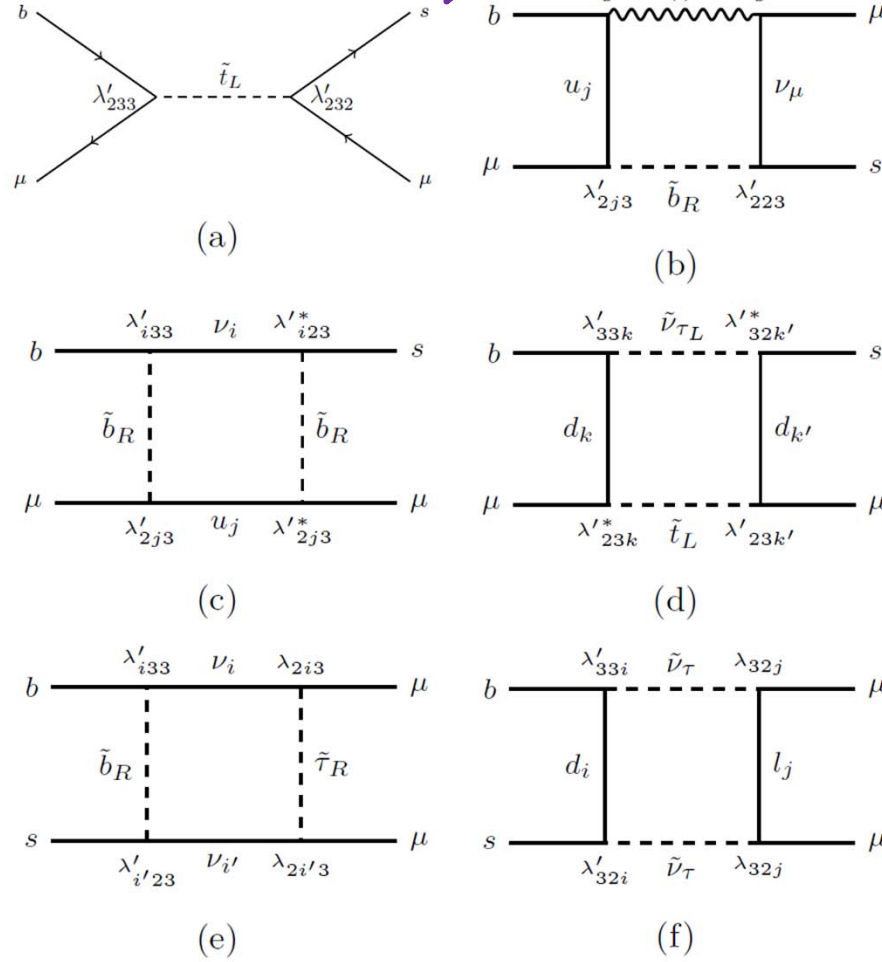
FIG. 3: Contribution to the R_D and R_{D^*} from λ' and λ in RPV SUSY. (a) both LLE and LQD; (b) LQD only.

LLE

only 3g

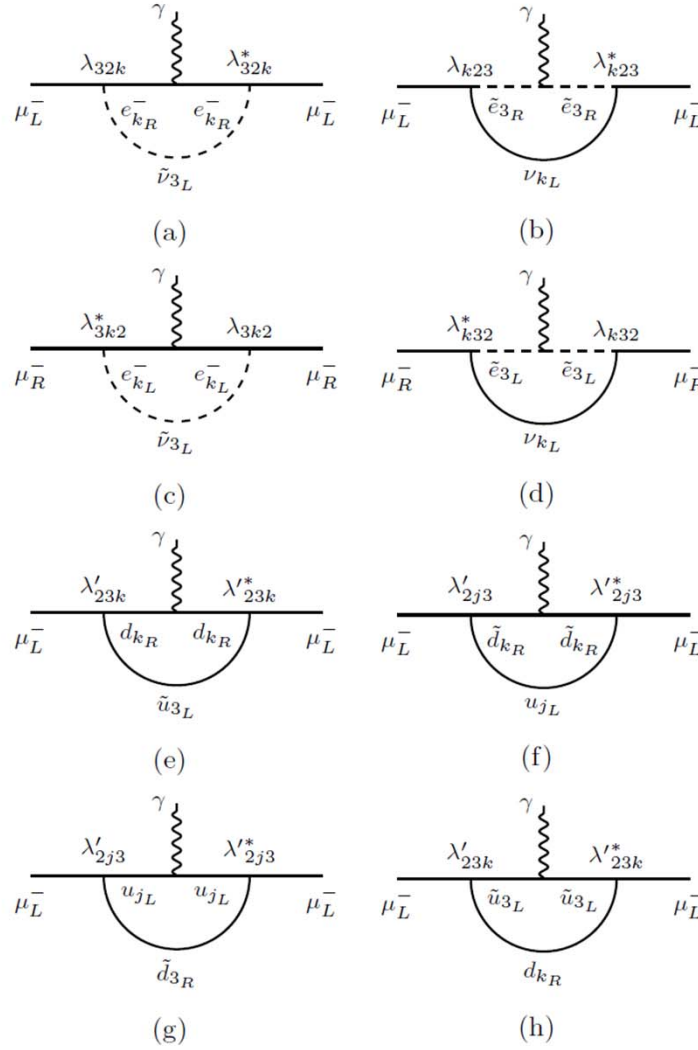
$$\mathcal{L}_{\text{LLE}} = \frac{1}{2} \lambda_{ijk} \left[\tilde{\nu}_{iL} \bar{e}_{kR} e_{jL} + \tilde{e}_{jL} \bar{e}_{kR} \nu_{iL} + \tilde{e}_{kR}^* \bar{\nu}_{iL}^c e_{jL} \right. \\ \left. - (i \leftrightarrow j) \right] + \text{H.c.} . \quad (19)$$

R_K, R_K^*



SM W Z ν_i $\nu_{i'}$

FIG. 4: Different classes of contribution to the $b \rightarrow s \ell \ell$ transitions in RPV SUSY. a) tree level stop exchange; b) sbottom- W boson loops; c) sbottom loops; d) stop-sneutrino loops; e) sbottom-stau loops; f) sneutrino loops.



$(g-2)_\mu$

FIG. 5: Contribution to the $(g-2)_\mu$ from λ in RPV SUSY. a, c $\tilde{\nu}$ loop with different external handedness; b, d \tilde{e}_3 loop.

List of important constraints imposed

- $B \Rightarrow K(\pi) \nu \nu$
- $Z \Rightarrow \tau \tau / Z \Rightarrow l l$
- $\tau \Rightarrow l \nu \nu$
- $B \Rightarrow \tau \nu$
- $B_c \Rightarrow \tau \nu$
- B_s mixing
- \vdash many more
- As a result parameter space of RPV3 gets significantly constrained (see below)

PRD'17

ALTMANNSHOFER, BHUPAL DEV, and SONI

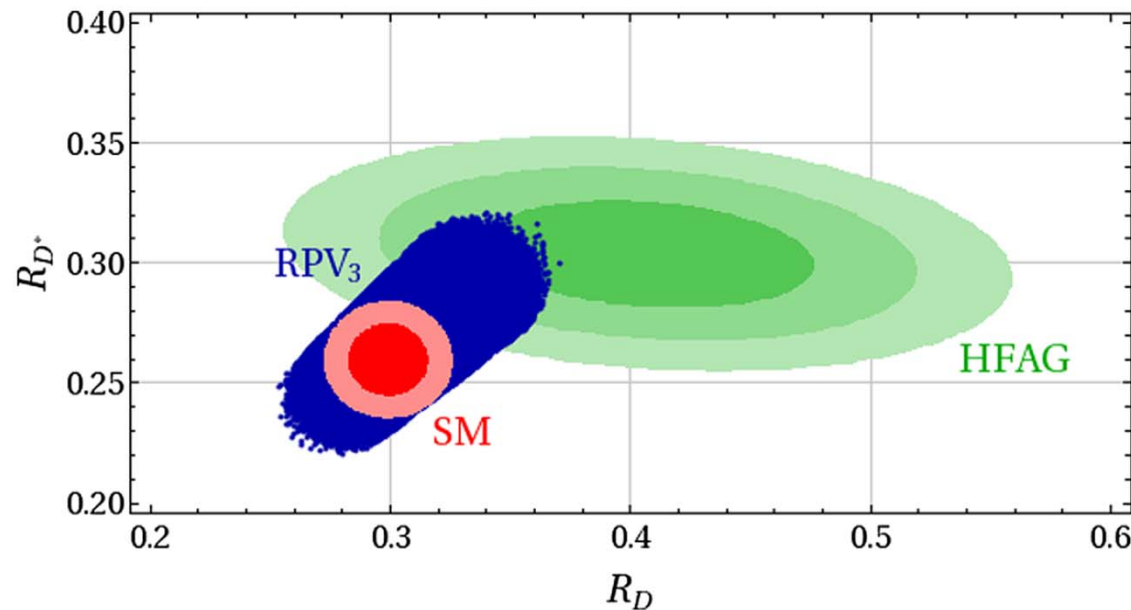


FIG. 4. The SM predictions (red), experimental world average (green), and accessible values in our RPV-SUSY scenario (blue) in the R_D vs. R_{D^*} plane. For the SM, bearing in mind recent works [17,20,22] we are taking $(R_D^{\text{SM}}, R_{D^*}^{\text{SM}}) = (0.299 \pm 0.011, 0.260 \pm 0.010)$.

Because of numerous constraints, despite huge # of param
 RPV_3 "barely survives"

Recent developments

- For $B=D^* \tau(l) \nu$, Belle has provided $l.q^2$ distribution [not just the integrated rate],
II. the D^* polarization and III τ polarization (though the last one has rather large errors). These additional info are very useful for discriminating amongst models
- Very nice model independent analysis by [Clara Murgui](#), [Ana Peñuelas](#) , [Martin Jung](#) & [Antonio Pich](#), arXiv:1904.09311
- For R_K and R_K^* both are larger compare to SM.
- This positive correlation rather than anti is of particular importance for telling us about the Lorentz structure of the currents

2 Theoretical framework

2.1 Effective Hamiltonian

We adopt the most general $SU(3)_C \otimes U(1)_Q$ -invariant effective Hamiltonian describing $b \rightarrow c \ell \bar{\nu}_\ell$ transitions at the bottom quark scale, not considering the possibility of light right-handed neutrinos:

$$\mathcal{H}_{\text{eff}}^{b \rightarrow c \ell \bar{\nu}} = \frac{4G_F}{\sqrt{2}} V_{cb} [(1 + C_{V_L}) \mathcal{O}_{V_L} + C_{V_R} \mathcal{O}_{V_R} + C_{S_R} \mathcal{O}_{S_R} + C_{S_L} \mathcal{O}_{S_L} + C_T \mathcal{O}_T] + \text{h.c.} \quad (2.1)$$

The above fermionic operators are given by⁴

$$\mathcal{O}_{V_{L,R}} = (\bar{c} \gamma^\mu b_{L,R}) (\bar{\ell}_L \gamma_\mu \nu_{\ell L}), \quad \mathcal{O}_{S_{L,R}} = (\bar{c} b_{L,R}) (\bar{\ell}_R \nu_{\ell L}), \quad \mathcal{O}_T = (\bar{c} \sigma^{\mu\nu} b_L) (\bar{\ell}_R \sigma_{\mu\nu} \nu_{\ell L}), \quad (2.2)$$

Very useful work includes constraints from $B \rightarrow (\pi, \rho, \dots)$, q^2 distribution, $B^0 \rightarrow \pi^0 \ell^+ \ell^-$, $B_c \rightarrow \tau \nu$

not only

$C_{V_L} \neq 0 \Rightarrow$ corresponds to our RPV3
MURGULETOL
1964.09311
MARTIN J.

MURCH et al

- On the other hand, considering scenarios with only a single Wilson coefficient present, there is a clear preference for C_{V_L} : removing the other three Wilson coefficients increases χ^2 only by 1.4, corresponding to 0.14σ . Hence, Min 1 is well compatible with a global modification of the SM, that is, C_{V_L} being the only non-zero coefficient.

Grac. Belle EWMoniod

central values do change. Again all individual coefficients are roughly compatible with zero at 1σ . C_{V_L} alone also still provides an excellent fit to all the data, now with a smaller central value of ~ 0.08 . Interestingly, the fit with only C_T is improved by the new results, which,

A striking endorsement for RPV₃. IFNP is needed!

**But in the current context any NP solution
needs to be accompanied by a concern**

[relevant ^{only} for small non-vanishing CVL]

- It may just be SM + (expt + theory) errors
- **This is why further reduction in errors of both experiment AND theory are highly desirable...**
- **THIS IS THE MOTIVATION DRIVING OUR LATTICE EFFORT**
- Belle-II and LHCb in the next few years are of course going to provide better experimental numbers
- **Assuming** NP is needed then RPV3 is a very good candidate

ADSS'
(WIP)

$R_K(x)$

Try to fit N.P. need via
shifts in W.C

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \frac{e^2}{16\pi^2} \sum_{i=9,10} \left((C_i)^\ell (Q_i)^\ell + (C'_i)^\ell (Q'_i)^\ell \right), \quad (30)$$

with the operators

$$(Q_9)^\ell = (\bar{s} \gamma_\alpha P_L b) (\bar{\ell} \gamma^\alpha \ell), \quad (Q_{10})^\ell = (\bar{s} \gamma_\alpha P_L b) (\bar{\ell} \gamma^\alpha \gamma_5 \ell), \quad (31)$$

and $Q'_{9,10}$ are obtained from $Q_{9,10}$ by $P_L \rightarrow P_R$. Fits of R_K and R_{K^*} show that the observed pattern can be accommodated with new physics in the coefficients $(C_9)^e$, $(C_{10})^e$, $(C_9)^\mu$, $(C_{10})^\mu$. New physics in the primed coefficients is disfavored as it leads to an anti-correlated effect in R_K and R_{K^*} , contradicting the current data.

Global fits of all relevant data on rare B decays finds a particular consistent new physics picture which is characterized by non-standard effects in muonic coefficients in the combination of Wilson coefficients $(C_9)^\mu = -(C_{10})^\mu$ [49] (see also [50–54]). As we will see below, our RPV SUSY scenario will generate contributions to both $(C_9)^\mu = -(C_{10})^\mu$ and $(C'_9)^\mu = -(C'_{10})^\mu$. Such a scenario provides an excellent fit to the data for the following values [49]

$$(C_9)^e \simeq (C_{10})^e \simeq (C'_9)^e \simeq (C'_{10})^e \simeq 0, \quad (32)$$

$$(C_9)^\mu = -(C_{10})^\mu \simeq -0.55 \pm 0.10, \quad (33)$$

$$(C'_9)^\mu = -(C'_{10})^\mu \simeq 0.20 \pm 0.11. \quad (34)$$

Note that the combination $(C_9)^\mu \simeq -(C_{10})^\mu$ corresponds to new physics that mainly affects left-handed muons. All other coefficients are compatible with zero at the 2σ level. The correction to the SM values of the Wilson coefficients $C_9^{\text{SM}} \simeq -C_{10}^{\text{SM}} \simeq 4$ is at the level of -15%. The

Data
Needs
 $C_9^\mu = -C_{10}^\mu$
No change
in e

Effectⁿ
15% in
amplitude

2 + 's & 1-

- q^2 distribution in sIB of NP seems similar to SM...+
- RK and RK^* are positively correlated as in SM....+
- But because the q^2 distribution in sIB is SM-like $\Rightarrow D^*$ polarization must stay as in SM;
current Belle data disfavors SM at 1.6 sigma

LHCb, BELLE-II input would be crucial

Sequel to our work on
 R_{UV_3}
nearly completion

Addressing B -anomalies, muon $g - 2$ and ANITA anomaly in a Minimal R -parity violating supersymmetric framework

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g.s@wustl

IN CLOSING: A REMINDER

Importance of the “IF”: score card

- Beta decay $\Rightarrow G_f \Rightarrow W \dots$
- Huge suppression of $KL \Rightarrow \mu \mu$; miniscule $\Delta m_K \Rightarrow$ charm
- $KL \Rightarrow 2 \pi$ but very rarely; mostly to $3 \pi \Rightarrow$ CP violation \Rightarrow 3 families
- Largish B_d –mixing \Rightarrow large top mass
- etc.....
- \Rightarrow extremely unwise to put all eggs in HEF
- info from IF complementary to HEF can be a crucial guide
for pointing to new thresholds as well as to provide important clues
to the nature of the signals there from

History may repeat yet again!

Summary + Outlook

- Hints of LUV are extremely interesting, intriguing and important. *There is nothing we know of that tells us that these hints cannot be true.*
- While these indications are rather serious, **personally I don't find them compelling enough weighing in the fact that they ask for too radical a departure from conventional understanding so it is best we exercise extreme caution and care before accepting them. Moreover, in each of the 3 cases there are features that cause some concern.**
- Fortunately significant experimental/theoretical progress on these issues should occur in $< \sim 2$ years and is eagerly awaited.
- Anticipate new $g-2$ results from Fermilab in 2020; improved results from LHCb in 2020 & 2021 and Belle-II results starting ~ 2021 and many improved theory results from Lattice
- **IF** the current hints survive further scrutiny, RPV3, with 3g more amenable to NP, is not only interesting and has significant theoretical appeal, this early on there appears to be some important experimental support for it.
- **Given all the above hints, may be with some luck the IF will lead us to the gem of NP and once again, as many times in the past, guide collider physics et al**

Revisiting R-parity violating interactions as an explanation of the B-physics anomalies

Sokratis Trifinopoulos^{*1}

"S-T" sym

¹*Physik-Institut, Universität Zürich, CH-8057 Zürich, Switzerland*

introduces a nice formal sym argument to implement
 Ok RPV₃ [3rd gen \bar{s} lightest]
 ↑ → Abstract

In the last few years, the ratios $R_{D^{(*)}}$ and of $R_{K^{(*)}}$ have reportedly exhibited significant deviations from the relevant Standard Model predictions, hinting towards a possible violation of Lepton Flavor Universality and a window to New Physics. We investigate to what extent the inclusion of R-parity violating couplings in the Minimal Supersymmetric Standard Model can provide a better fit to the anomalies simultaneously. We perform this analysis employing an approximate, non-abelian $\mathcal{G}_f = U(2)_q \times U(2)_\ell$ flavour symmetry, which features a natural explanation of the appropriate hierarchy of the R-parity violating couplings. We show that, under the requirement of a supersymmetric spectrum with much heavier left-handed doublet superpartners, our assumption favors a considerable enhancement in the tree-level charged-current $B \rightarrow D^{(*)} \tau \bar{\nu}$, while the anomalies induced by $b \rightarrow s \ell^+ \ell^-$ receive up to an approximate 30% improvement. The consistency with all relevant low-energy constraints is assessed.

BACK TO LOW PT: NOTABLE LFV DECAYS OF TAU AND B [IN RPV3]

LFV of τ & q B 's
 \rightarrow 3-g centric RPV_3 : Altmannshofer
 Dev, AS, YS

* Impreg

Mode	Model dependent BR	Current bound
$\tau \rightarrow \mu \phi$	2×10^{-10}	8×10^{-8}
$\tau \rightarrow \mu K K$	3×10^{-11}	4×10^{-8}
$\tau \rightarrow \mu K_s^0$	6×10^{-11}	2×10^{-8}
$\tau \rightarrow 3\mu$	1.5×10^{-10}	2×10^{-8}
$\tau \rightarrow \mu \gamma$	1.1×10^{-11}	4×10^{-8}
$\tau \rightarrow \mu l^+ l^-$	6×10^{-12}	2×10^{-8}
$b \rightarrow s \mu \tau$	7×10^{-7}	4.5×10^{-5}
$B_s \rightarrow \tau \mu$	1.3×10^{-8}	N/A

TABLE I: Few examples of lepton flavor violating decay modes of τ and of B - mesons. Shown are also loop decays $\tau \rightarrow \mu \gamma$ and $\tau \rightarrow \mu l^+ l^-$; see text

$B_u[B \rightarrow K^* \mu \tau \sim 10^{-7}]!$ \Leftarrow Recall $B \rightarrow X_c \ell \nu$
 $\propto V_{cb} \sim \alpha^2$
 $\& B \rightarrow K \tau \tau$ also deserves attention

Implications of anomaly for colliders

At low energies, the effective 4-fermion Lagrangian for the quark-level transition $b \rightarrow c\tau\bar{\nu}$ in the SM is given by

$$-\mathcal{L}_{\text{eff}} = \frac{4G_F V_{cb}}{\sqrt{2}} (\bar{c}\gamma_\mu P_L b) (\bar{\tau}\gamma^\mu P_L \nu_\tau) + \text{H.c.}, \quad (4) \quad \text{SM}$$

"V"
"S" ←

BSM

DIM 6 OPS

$$\mathcal{O}_{V_{R,L}} = (\bar{c}\gamma^\mu P_{R,L} b) (\bar{\tau}\gamma_\mu P_L \nu) \quad (5)$$

$$\mathcal{O}_{S_{R,L}} = (\bar{c}P_{R,L} b) (\bar{\tau}P_L \nu), \quad (6)$$

$$\mathcal{O}_T = (\bar{c}\sigma^{\mu\nu} P_L b) (\bar{\tau}\sigma_{\mu\nu} P_L \nu). \quad (7)$$

- - - - -

skip 4 now

ADD!

$R_{D^{(*)}}$ ANOMALY: A POSSIBLE HINT FOR ...

PHYSICAL REVIEW D **96**, 095010 (2017)

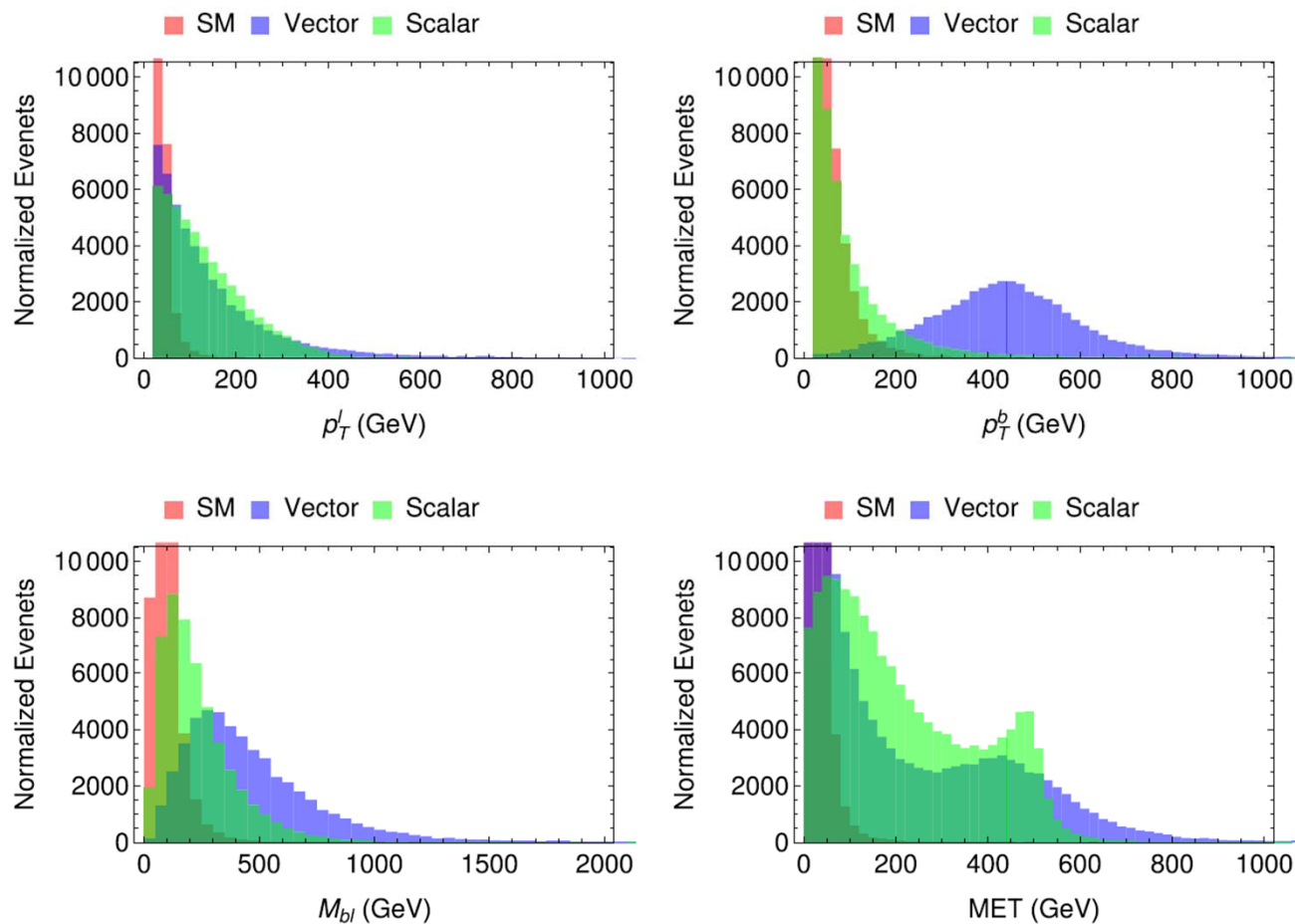


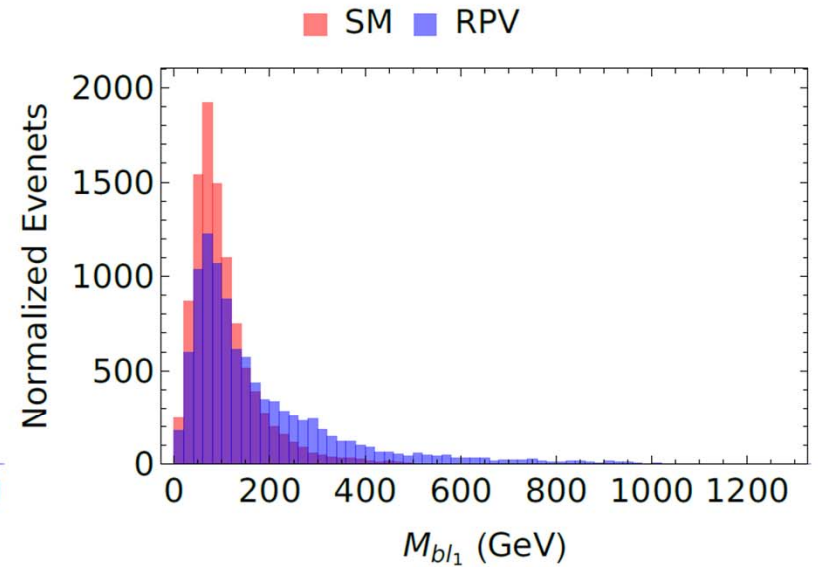
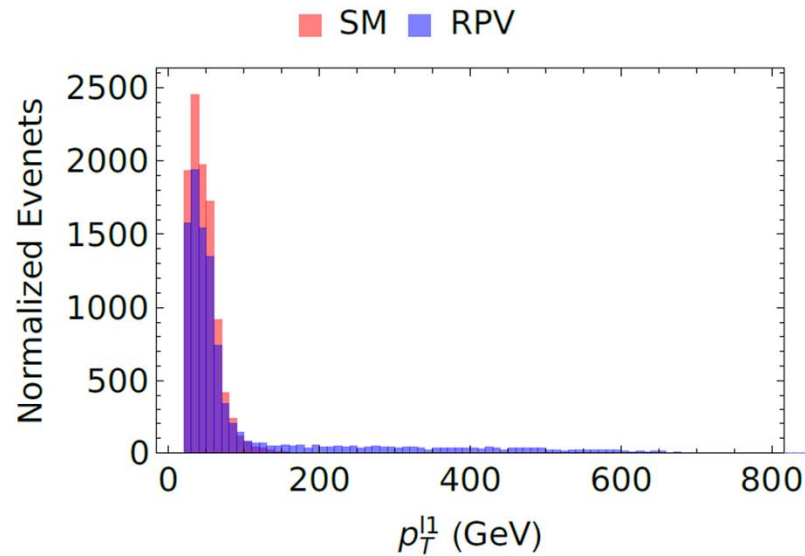
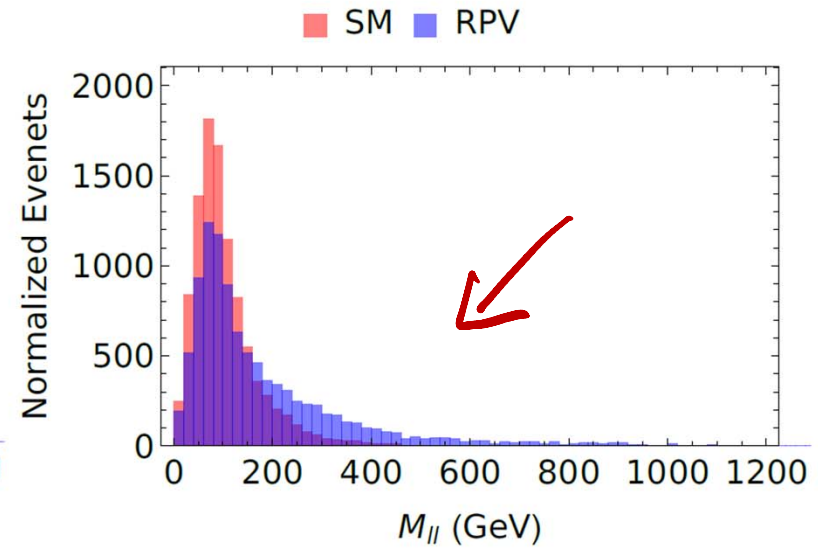
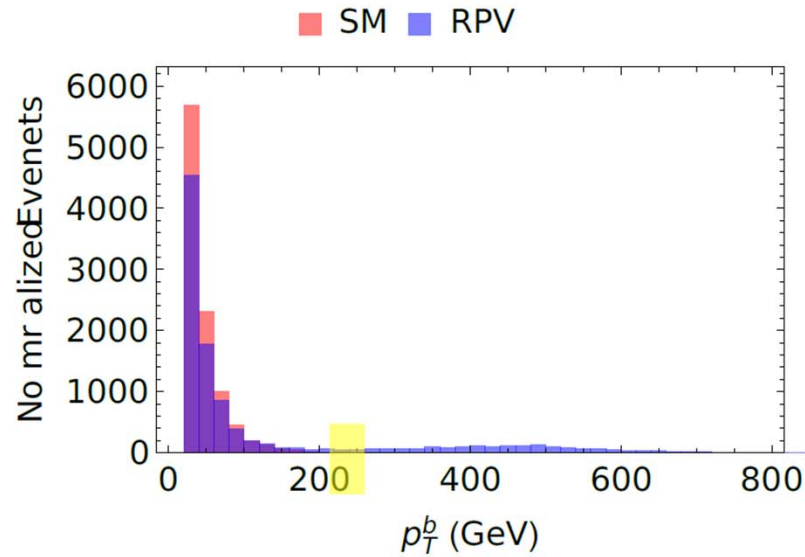
FIG. 1. Normalized kinematic distributions for the $pp \rightarrow b\tau\nu \rightarrow b\ell + \cancel{E}_T$ signal and background.

EXPECT DISTINCTIVE NP CONTRIBUTIONS IN COLLIDERS

Following $RK(*) \Rightarrow$ model independent high pt implications

- In a similar vein to the charged current case
- $B=K(*) \ell \ell \dots RK(*)$ anomaly
- $b \Rightarrow s \ell \ell$
- $g + b \Rightarrow s \ell \ell$
- $g + s \Rightarrow b \ell \ell$ \leftarrow Most suited due signal, backgrounds & such

Thus collider searches for NP in $pp \rightarrow b \ell \ell$ are urged...



we have used the minimal trigger cuts: $p_T^{j,b\ell} > 20$ GeV, $|\eta^{j,b,\ell}| < 2.5$ and $\Delta R^{\ell\ell} > 0.4$ and an average b -tagging efficiency of 70%. ~~From the distributions (give cut flow~~

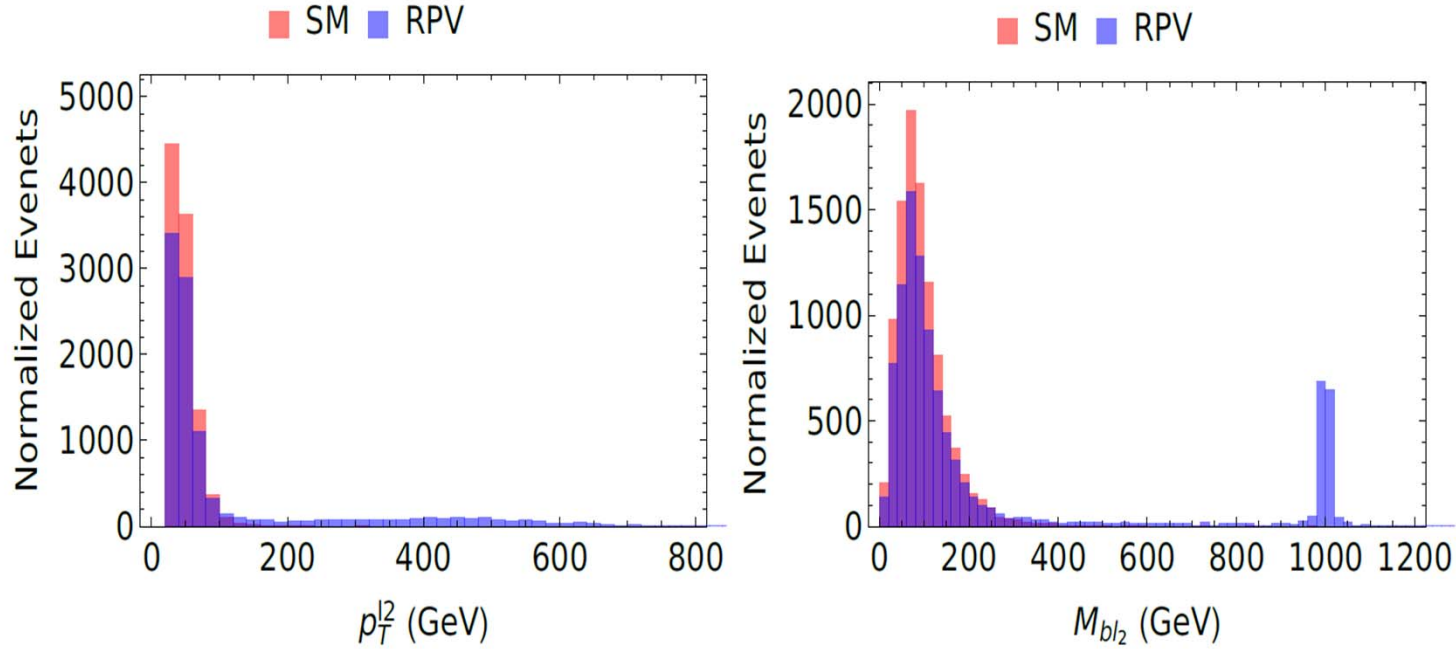
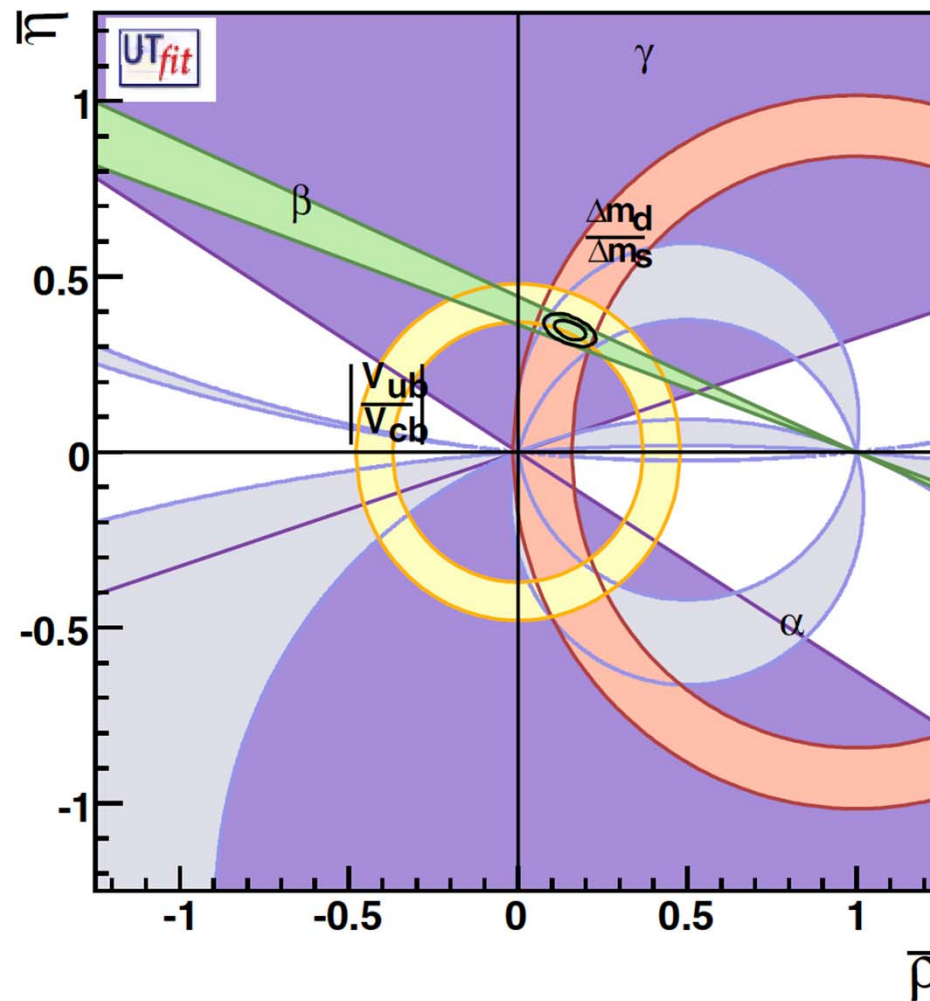


FIG. 2: Kinematic distributions for the $pp \rightarrow b\ell\ell$ signal in the RPV model (blue) and the corresponding SM background (red). The left panels show the transverse momentum distributions for the bottom quark and the two charged leptons, whereas the right panel shows the invariant mass distributions for the dilepton and the two bottom quark-lepton combinations. In the RPV model under consideration, the right combination of M_{bl} gives a peak at the squark mass, as shown in the last plot. Minimal trigger cuts have been imposed here.

In passing, a side remark, please

- QCD and therefore non-perturbative dynamics critically effects SM and or BSM
- In almost all of these “IF” experiments, quantitative understanding of non-perturbative [non-P] effects is of crucial importance to make most economical use of experimental data, often obtained at huge cost. **The non-P methods do not just need humungous computing hardware, (wo)man power needs are also very large. Given their vital use, they deserve greater support from the (experimental) community.**

PRL **97**, 151803 (2006)



MARCELLA BONA ~2007

COUPLINGS BETWEEN CWB+ AS & PBM ET AL

**ALL 11 EXPERIMENTAL CENTRAL
VALUES ARE ABOVE THEORY!**

$(g-2)_\mu \oplus R_D^{(*)} \oplus R_K^{(*)} + \text{ANITA anomalies}$

10 +
ALL known
exptal
constraints

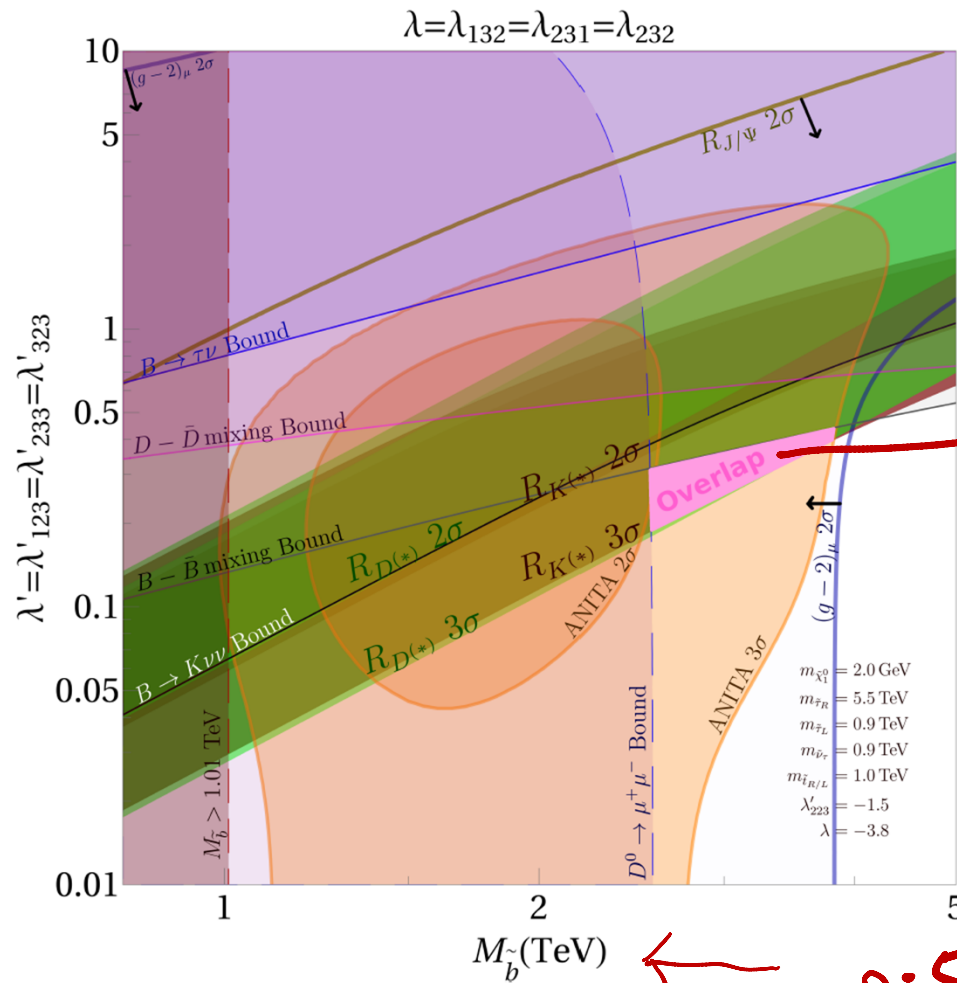


FIG. 4: Benchmark scenario with overlapping $R_D^{(*)}$, $R_{J/\Psi}$, $R_K^{(*)}$, $(g-2)_\mu$ and ANITA regions. The total overlap is shown as pink area. $R_D^{(*)}$ $2, 3\sigma$ flavored regions are denoted as green regions; $R_K^{(*)}$ $2, 3\sigma$ flavored regions are shown in red regions; $(g-2)_\mu$ and $R_{J/\Psi}$ 2σ flavored region is marked by thick blue and dark yellow edges, respectively, with arrows pointing inwards to the allowed regions; ANITA anomaly $2, 3\sigma$ flavored regions are shown in orange regions.

$B \rightarrow K\nu\nu$ bound is shown as dark gray curve with forbidden region indicated as dark gray region while $B - \bar{B}$ mixing bound shown as gray curve with forbidden region in gray; $D \rightarrow \mu\mu$ is shown as dashed light purple curve with forbidden region in light pink. $D - \bar{D}$ mixing bound is shown as the pink curve with forbidden region in light pink.

