

# **3He spin structure and intrinsic isobars**

**Vadim Guzey**



Petersburg Nuclear Physics Institute (PNPI),  
National Research Center “Kurchatov Institute”,  
Gatchina, Russia



## **Outline:**

- Nuclear effects in He-3 spin structure function  $g_1^{3\text{He}}(x, Q^2)$
- Possible presence of  $\Delta(1232)$  isobar in He-3 wave function and  $g_1^{3\text{He}}(x, Q^2)$
- Nuclear shadowing and antishadowing in  $g_1^{3\text{He}}(x, Q^2)$
- Extraction of the neutron  $g_{1n}(x, Q^2)$  from He-3 data
- Summary
- Based on [Frankfurt, Guzey, Strikman, PLB 381 \(1996\) 379](#); [Boros, Guzey, Strikman, Thomas, PRD 64 \(2001\) 014025](#); [Bissey, Guzey, Strikman, Thomas, PRC 65 \(2002\) 064317](#)

**Exploring QCD with light nuclei at EIC, Stony Brook University, Jan 21-24, 2020  
(remote presentation)**

# Nuclear effects in He-3 spin structure function

## $g_1^{3\text{He}}(x, Q^2)$

- Inclusive deep inelastic scattering (DIS) of longitudinally polarized leptons on longitudinally polarized targets (**p**, **D**, **He-3**, **Li-6**, **Li-7**) → spin structure function of the target  $g_1(x, Q^2)$  → polarized quark and gluon distributions.
- Besides their own interest, polarized nuclear targets (D and He-3) are used as a source of polarized neutrons.
- The neutron  $g_{1n}(x, Q^2)$  is needed for
  - flavor separation of quark polarized distributions
  - tests of various spin sum rules (Bjorken, Jaffe-Manohar, Burkhardt-Cottingham, Gerasimov-Drell-Hearn)
- Various nuclear effects make  $g_{1n}(x, Q^2) \neq g_1^{3\text{He}}(x, Q^2)$ . They include:
  - nucleon spin depolarization
  - nuclear binding and Fermi motion
  - off-shell effects
  - potential presence of  $\Delta(1232)$  isobar in He-3 wave function
  - nuclear shadowing and antishadowing

# Standard picture of $g_1^{3\text{He}}(x, Q^2)$

- The effects of spin depolarization, binding and Fermi motion are traditionally described within the framework of the convolution approach:

$$g_1^{3\text{He}}(x, Q^2) = \int_x^3 \frac{dy}{y} \Delta f_{n/3\text{He}}(y) g_1^n(x/y, Q^2) + \int_x^3 \frac{dy}{y} \Delta f_{p/3\text{He}}(y) g_1^p(x/y, Q^2)$$

Nucleon light-cone momentum distributions from spectral functions = the probability to find spins of the nucleon and the nucleus aligned minus that to find their spins anti-aligned

Ciofi degli Atti, Scopetta, Pace, Salme, PRC 48 (1993) R968; Schulze, Sauer, PRC 48 (1993) 38; Bissey, Thomas, Afnan, PRC 64 (2001) 024004

Free, on-shell, nucleon structure function, Gluck, Reya, Stratmann, Wogelsang, PRD 63 (2001) 094005

- To a very good approximation,  $\Delta f_{N/3\text{He}}(y) = P_N \delta(1-y)$ ,

$$g_1^{3\text{He}}(x, Q^2) = P_n g_1^n(x, Q^2) + 2P_p g_1^p(x, Q^2) \quad \text{Eq. (2)}$$

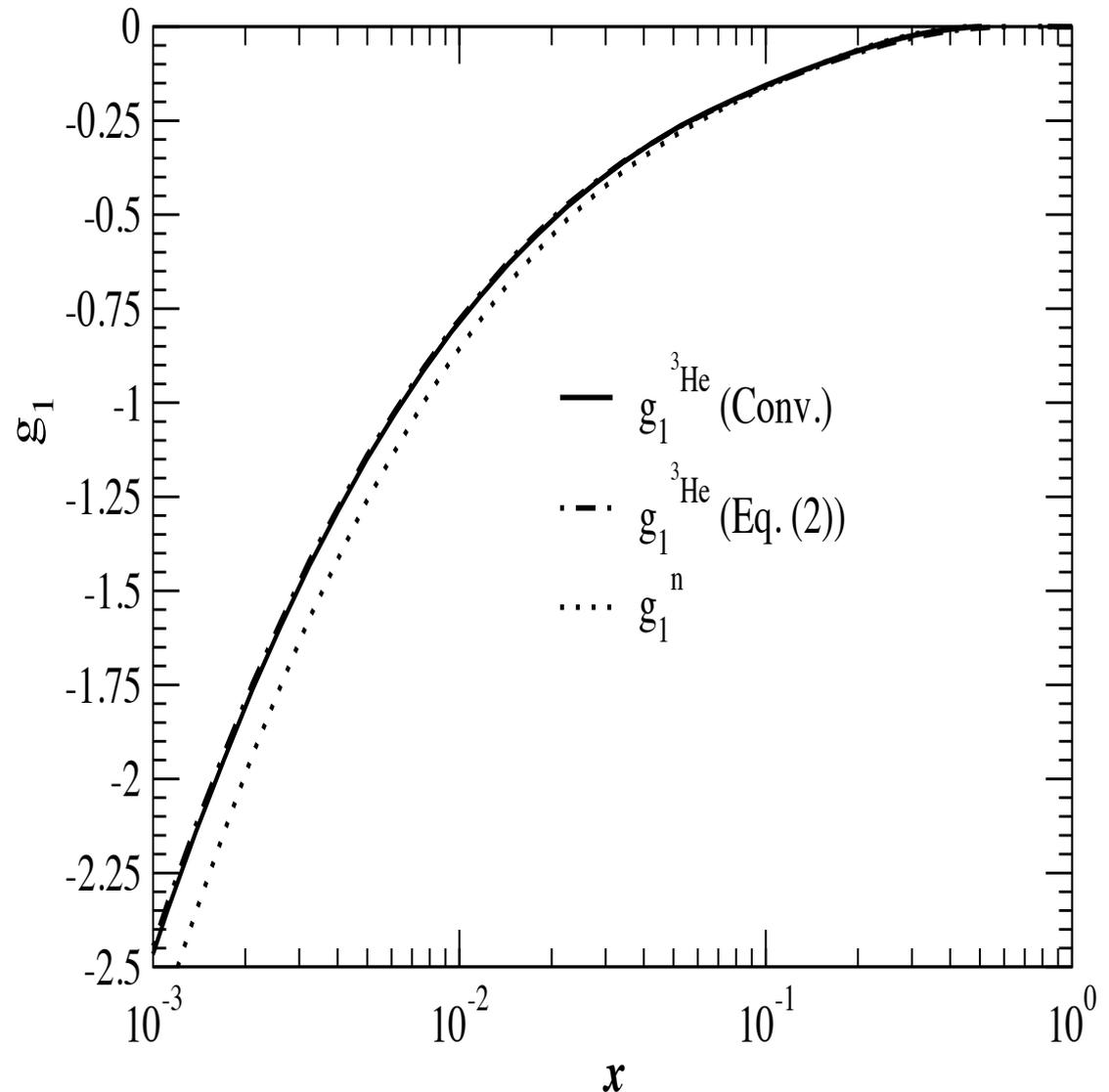
Effective n and p polarizations, include the effect of the tensor component of NN force:  $P_n = 0.979$  and  $P_p = -0.021$ .

# Standard picture of $g_1^{3\text{He}}(x, Q^2)$ - Cont.

- Off-shell corrections for light nuclei are expected to be small. We used the results of the Quark-Meson Coupling model, [Steffens, Tsushima, Thomas, Saito, PLB 447 \(1999\) 233](#).

- The spin structure function  $g_1^{3\text{He}}(x, Q^2)$  at  $Q^2=4 \text{ GeV}^2$ , [Bissey, Guzey, Strikman, Thomas, PRC 65 \(2002\) 064317](#)

- Eq. (2) approximates very well the full result for  $x < 0.1$ . For larger  $x$ , the differences are sizable.



# Possible presence of $\Delta(1232)$ isobar in He-3 wave function

- The description of nuclei as collections of proton and neutrons may be incomplete.
- Consider the ratio of the Bjorken sum rules for the **A=3** and **A=1** systems:

$$\frac{\int_0^3 \left( g_1^{3\text{H}}(x, Q^2) - g_1^{3\text{He}}(x, Q^2) \right) dx}{\int_0^1 \left( g_1^p(x, Q^2) - g_1^n(x, Q^2) \right) dx} = \frac{g_A|_{\text{triton}}}{g_A} = 0.956 \pm 0.004$$

From triton beta-decay, Budick, Chen, Lin, PRL 67 (1991) 2630

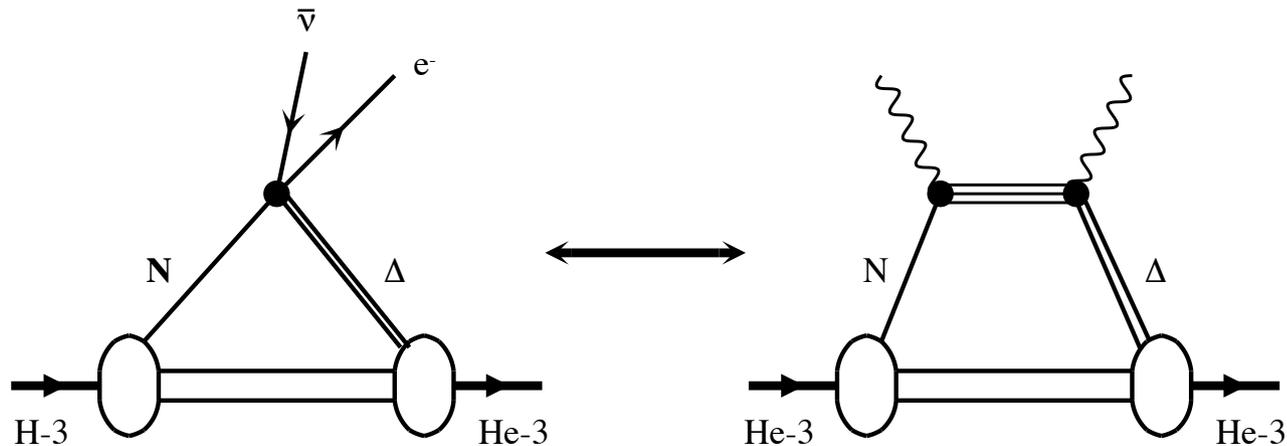
- Using the convolution formula:

$$\frac{\int_0^3 \left( g_1^{3\text{H}}(x, Q^2) - g_1^{3\text{He}}(x, Q^2) \right) dx}{\int_0^1 \left( g_1^p(x, Q^2) - g_1^n(x, Q^2) \right) dx} = \left( P_n - 2P_p \right) \frac{\tilde{\Gamma}_p - \tilde{\Gamma}_n}{\Gamma_p - \Gamma_n} = 0.921 \frac{\tilde{\Gamma}_p - \tilde{\Gamma}_n}{\Gamma_p - \Gamma_n}$$

- a **3.5%** deficit!

# Possible presence of $\Delta(1232)$ isobar in He-3 (2)

- It has been known for a long time that non-nucleonic dof's (pions, vector mesons,  $\Delta$ ) play important role in calculations of low-energy nuclear physics.
- In particular, two-body exchange currents involving  $\Delta(1232)$  increase the theoretical description for the axial-vector coupling constant of triton by  $\sim 4\%$ ,  
[Saito, Wu, Ishikawa, Sasakawa, PLB 242 \(1990\) 12](#); [Carlson, Riska, Schiavilla, Wiringa, PRC 44 \(1991\) 619](#)
- $\rightarrow$  it is natural to assume that the same mechanism is present also in polarized DIS on  $^3\text{He}$  and  $^3\text{H}$ , [Frankfurt, Guzey, Strikman, PLB 381 \(1996\) 379](#)



Triton beta decay

Polarized DIS on He-3

# Possible presence of $\Delta(1232)$ isobar in He-3 (3)

- The contribution of  $\Delta$ -isobar to  $g_1^{3\text{He}}(x, Q^2)$ :

$$g_1^{3\text{He}} = \int_x^3 \frac{dy}{y} \Delta f_{n/3\text{He}}(y) \tilde{g}_1^n(x/y, Q^2) + \int_x^3 \frac{dy}{y} \Delta f_{p/3\text{He}}(y) \tilde{g}_1^p(x/y, Q^2) + 2P_{n \rightarrow \Delta^0} g_1^{n \rightarrow \Delta^0} + 4P_{p \rightarrow \Delta^+} g_1^{p \rightarrow \Delta^+}$$

- The new interference structure functions can be estimated using SU(6) wave functions, [Close, Thomas, PLB 212 \(1988\) 227](#); [Boros, Thomas, PRD 60 \(1999\) 074017](#)

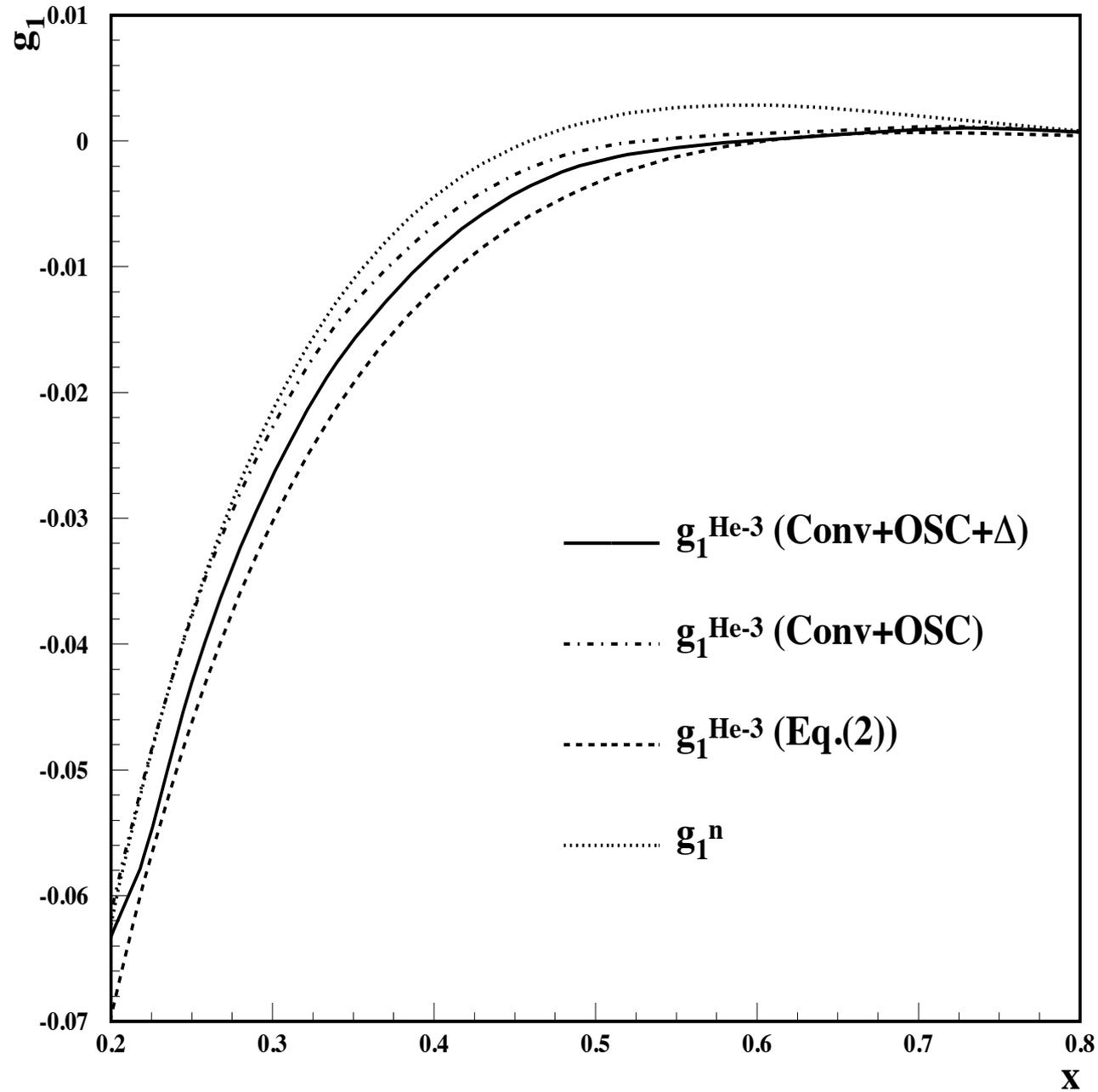
$$g_1^{n \rightarrow \Delta^0} = g_1^{p \rightarrow \Delta^+} = \frac{2\sqrt{2}}{5} (g_1^p - 4g_1^n)$$

- Requiring that theory reproduces the experimental value of  $g_{A|\text{triton}}/g_A$ , we determine the effective polarizations:  $2(P_{n \rightarrow \Delta^0} + 2P_{p \rightarrow \Delta^+}) = -0.025$

- $g_1^{3\text{He}}(x, Q^2)$  including the effects of the nucleon spin depolarization, binding, Fermi motion, off-shellness, and the intrinsic  $\Delta$ -isobar:

$$g_1^{3\text{He}} = \int_x^A \frac{dy}{y} \Delta f_{n/3\text{He}}(y) \tilde{g}_1^n(x/y, Q^2) + \int_x^A \frac{dy}{y} \Delta f_{p/3\text{He}}(y) \tilde{g}_1^p(x/y, Q^2) - 0.014 (\tilde{g}_1^p(x, Q^2) - 4\tilde{g}_1^n(x, Q^2)) .$$

# Possible presence of $\Delta(1232)$ isobar in He-3 (4)



# Nuclear shadowing in $g_1^{3\text{He}}(\mathbf{x}, Q^2)$

- The **small-x coherent** nuclear effects of **shadowing and antishadowing** have so far been ignored in analyses of DIS of polarized nuclear targets.
- In the target rest frame, the photon interacts coherently with all target nucleons by fluctuating into  $h_{\text{eff}} \rightarrow$  the **destructive interference** of scattering amplitudes with  $N=1, 2,$  and  $3$  nucleons leads to the suppression of the nuclear cross section:

$$g_1^{3\text{He}} \propto \sigma_{\gamma^* A}^{\uparrow\downarrow} - \sigma_{\gamma^* A}^{\uparrow\uparrow} \propto \sigma_{h_{\text{eff}} A}^{\uparrow\uparrow} - \sigma_{h_{\text{eff}} A}^{\uparrow\downarrow}$$

- Using the Gribov-Glauber shadowing formalism:

$$\Delta\sigma_{h_{\text{eff}} A} \equiv \sigma_{h_{\text{eff}} A}^{\uparrow\uparrow} - \sigma_{h_{\text{eff}} A}^{\uparrow\downarrow} = P_n \Delta\sigma_n + 2P_p \Delta\sigma_p - \frac{\sigma_{\text{eff}}}{4\pi B} (\Delta\sigma_n \Phi_n + \Delta\sigma_p \Phi_p) + \frac{\sigma_{\text{eff}}^2}{48\pi^2 (\alpha_{3\text{He}} + B)^2} \Delta\sigma_n$$

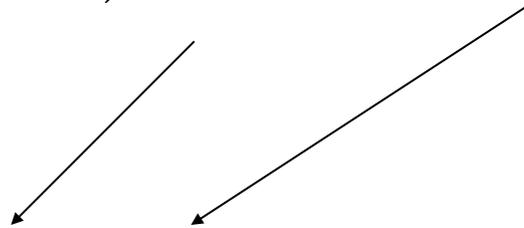
Effective cross section driven by spin-dependent diffraction or diffraction due to Pomeron-Reggeon interference - unknown

Calculated using the ground-state  $3\text{He}$  wf

# Nuclear antishadowing in $g_1^{3\text{He}}(x, Q^2)$

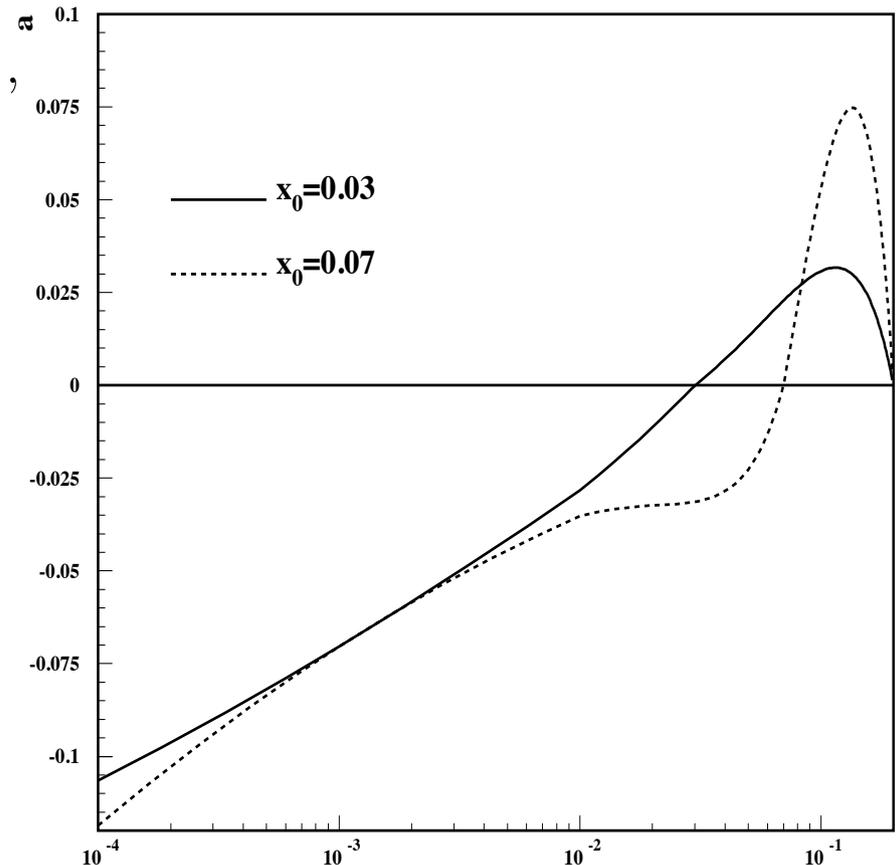
- In unpolarized DIS on nuclear targets, the suppression of the nuclear cross section due to shadowing is followed by some **enhancement (antishadowing)**.
- We assume the same for  $g_1^{3\text{He}}(x, Q^2)$  and require that both effects **compensate each other** in the Bjorken sum rule:

$$g_1^{3\text{He}} = \int_x^3 \frac{dy}{y} \Delta f_{n/3\text{He}}(y) \tilde{g}_1^n(x/y) + \int_x^3 \frac{dy}{y} \Delta f_{p/3\text{He}}(y) \tilde{g}_1^p(x/y) - 0.014 \left( \tilde{g}_1^p(x) - 4\tilde{g}_1^n(x) \right) + a(x)g_1^n(x) + b(x)g_1^p(x),$$

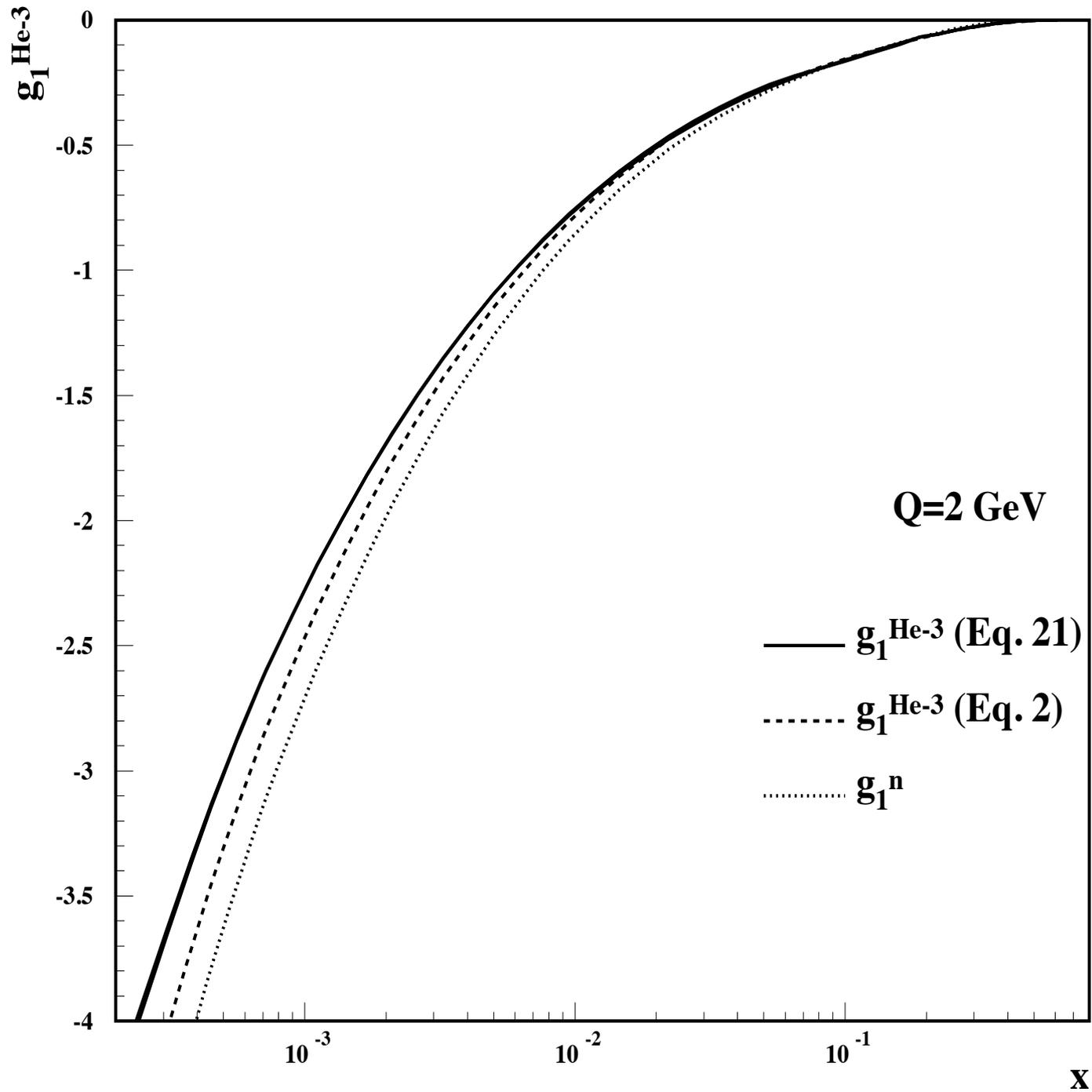


Calculated using Gribov-Glauber model for small  $x < 0.03-0.07$  and modeled for large  $x \rightarrow$

The height and shape of antishadowing depends on the assumed **cross-point  $x_0$** .



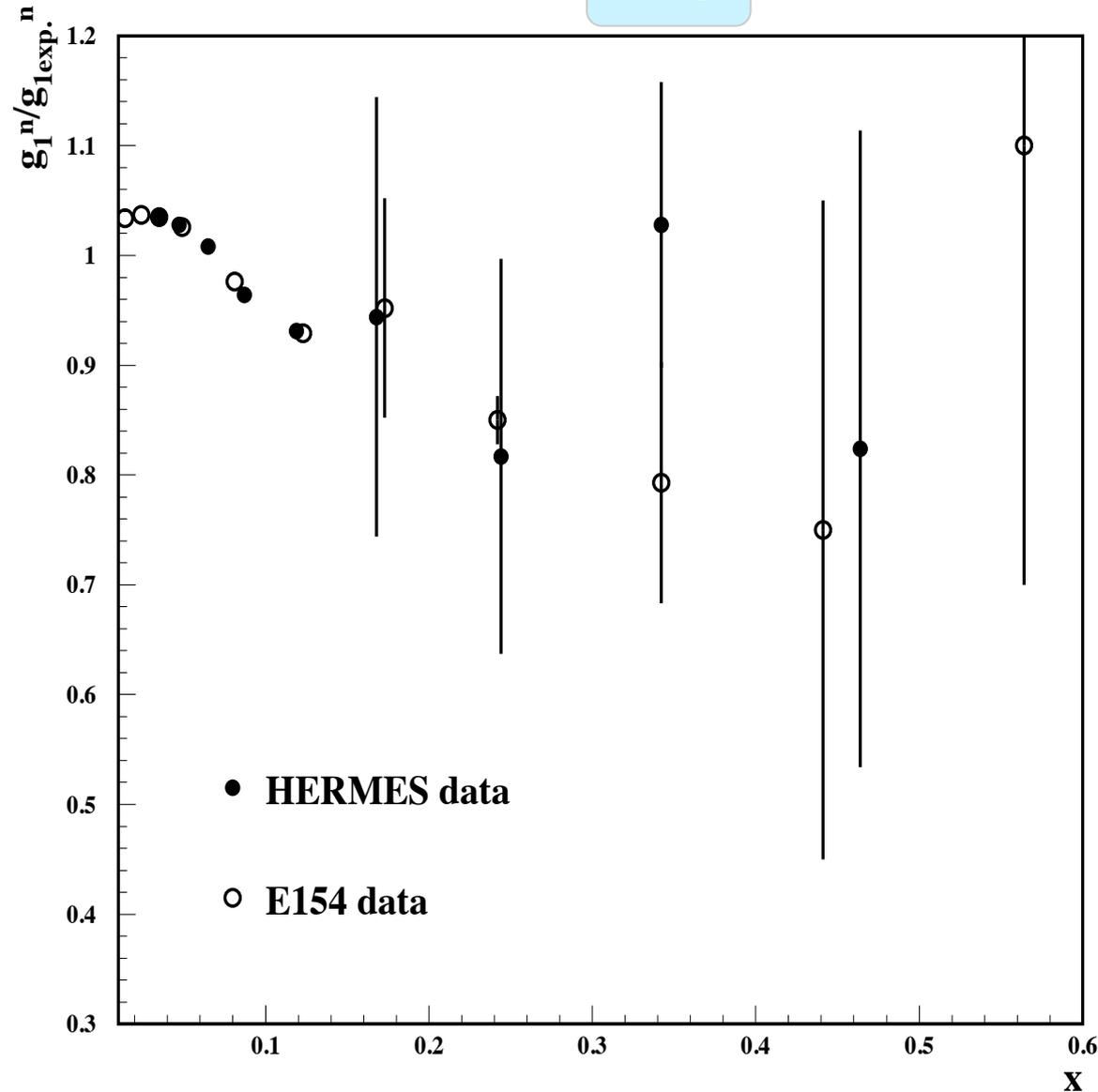
# Full result for $g_1^{3\text{He}}(x, Q^2)$



# Extraction of neutron $g_{1n}(x, Q^2)$ from $^3\text{He}$ data

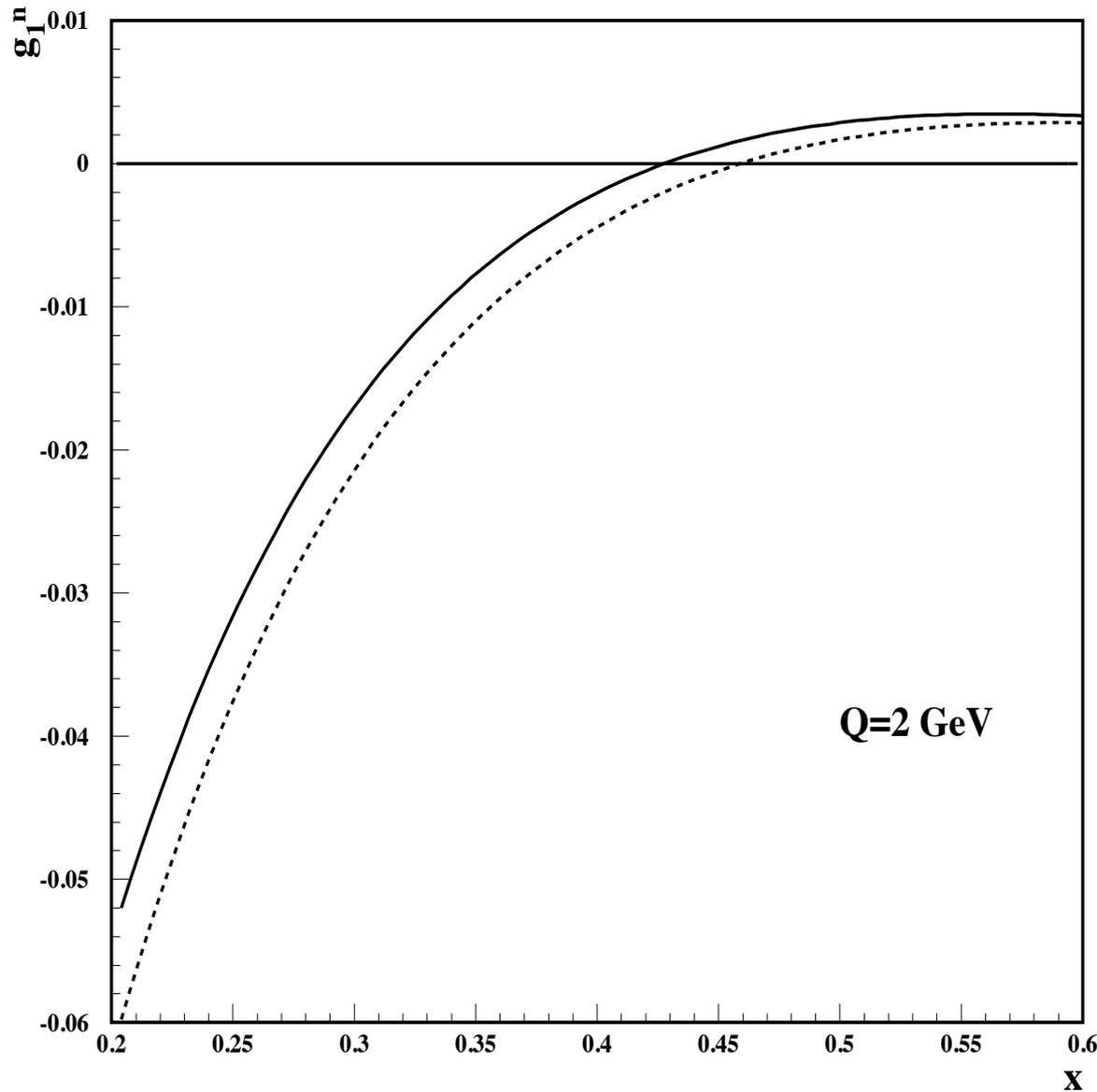
- Correction factor due to  $\Delta$  isobar, shadowing and antishadowing:

$$\frac{g_1^n}{g_{1\text{exp}}^n} = \frac{P_n + g_1^p/g_{1\text{exp}}^p (0.014 - b(x))}{P_n + 0.056 + a(x)}$$



# Extraction of neutron $g_{1n}(x, Q^2)$ from $^3\text{He}$ data (2)

•  $g_{1n}(x, Q^2)$  from 
$$\frac{g_1^n}{g_{1\text{exp}}^n} = \frac{P_n + g_1^p/g_{1\text{exp}}^n (0.014 - b(x))}{P_n + 0.056 + a(x)}$$



Solid  $g_{1n}(x, Q^2)$   
Dotted  $g_{1n}^{\text{exp}}(x, Q^2)$

# Summary

- Comprehensive picture of nuclear effects in DIS on polarized He-3 over a wide range of  $x$ ,  $10^{-4} < x < 0.8$ : nucleon spin depolarization, presence of  $\Delta$  isobar, Fermi motion and binding, nuclear shadowing and antishadowing.
- **Nucleon spin depolarization**, present for all  $x$ . Especially important at  $x=0.4-0.5$ , where  $g_{1n} \approx 0$ . Well-understood and used in analyses of He-3 data to extract the neutron  $g_{1n}$ .
- **Presence of  $\Delta$  isobar**, present for all  $x$ , but modeled here only for valence quarks,  $0.2 < x < 0.8$ : **15-25% effect** on  $g_1^{3\text{He}}$  and  $g_{1n}$ ; lowers  $x$ , where  $g_{1n}$  changes sign.
- **Shadowing**,  $10^{-4} < x < 0.03-0.07$ , by analogy with unpolarized DIS: **10%** effect on  $g_1^{3\text{He}}$  at  $10^{-4}$  and **4%** effect on  $g_{1n}$  at  $x=0.01$ .
- **Antishadowing**,  $0.03-0.07 < x < 0.2$ , modeled to preserve Bjorken sum rule, depends on the cross-over point  $x_0$ , **7%** effect on  $g_1^{3\text{He}}$  and  $g_{1n}$  at  $x=0.12-0.13$ .
- **Fermi motion and binding** become sizable for  $x > 0.1$  (c.f. [Ciofi degli Atti, Scopetta, Pace, Salme, PRC 48 \(1993\) R968](#)) and very significant for  $x > 0.8$ .