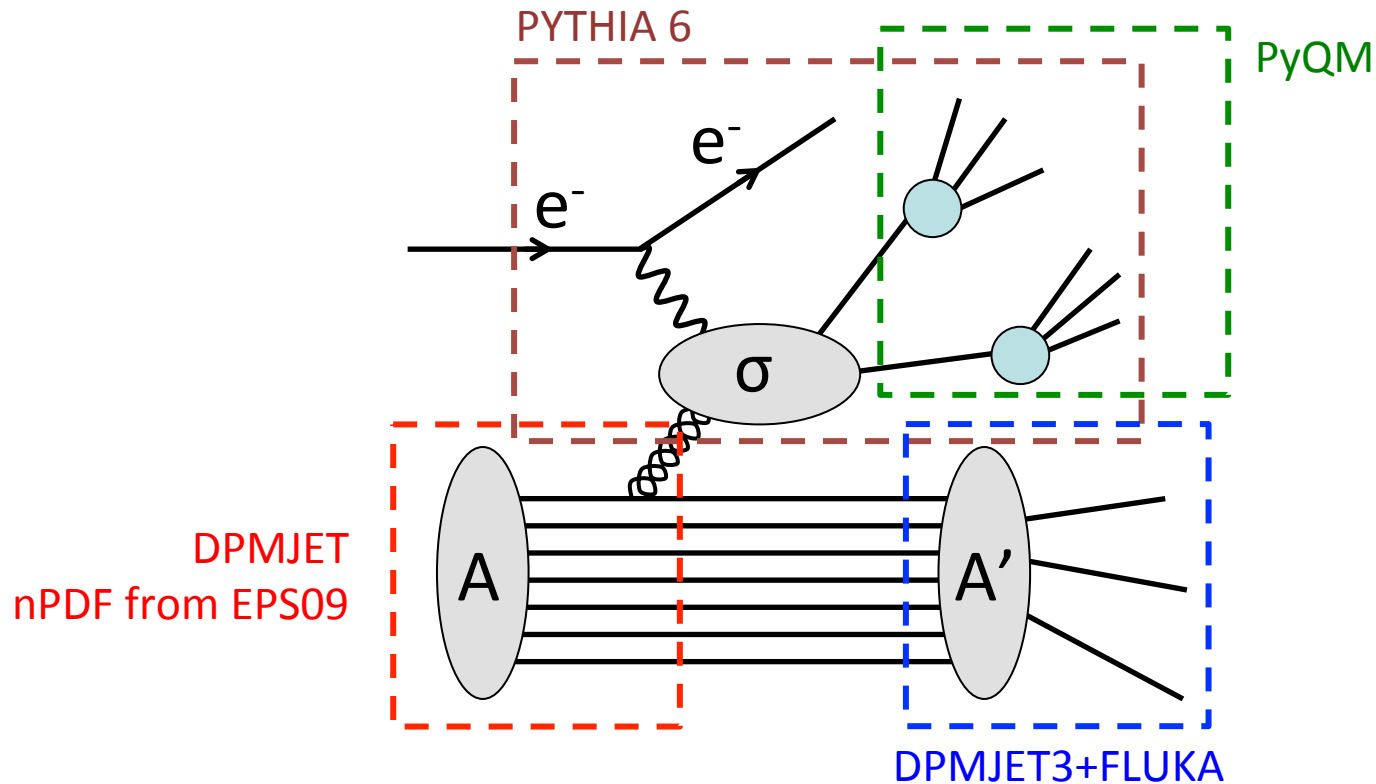


BeAGLE

- Benchmark eA Generator for Leptoproduction
- general purpose EIC eA Monte-Carlo generator

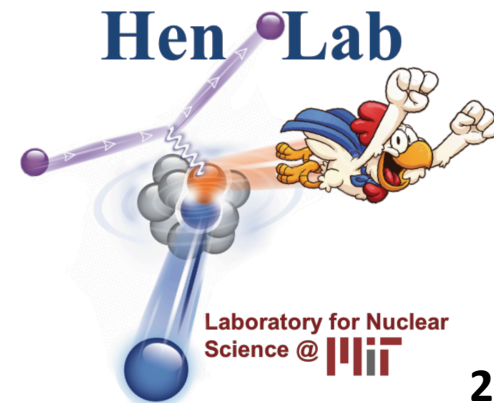


Quasi-Elastic scattering off SRC nucleons:
Generalized Contact Formalism (GCF)

Contact Formalism and SRC universality

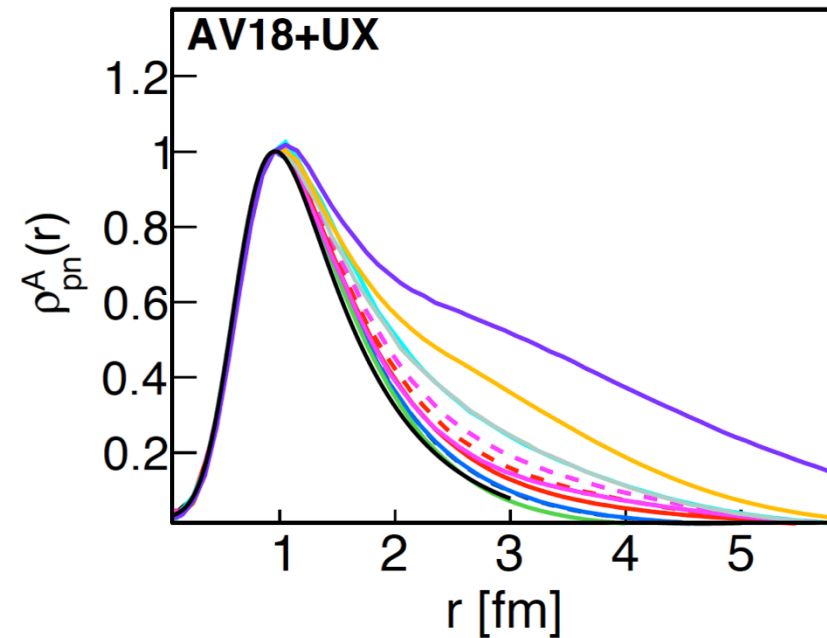


Reynier Cruz Torres
Exploring QCD with light nuclei at EIC
January 22nd, 2020



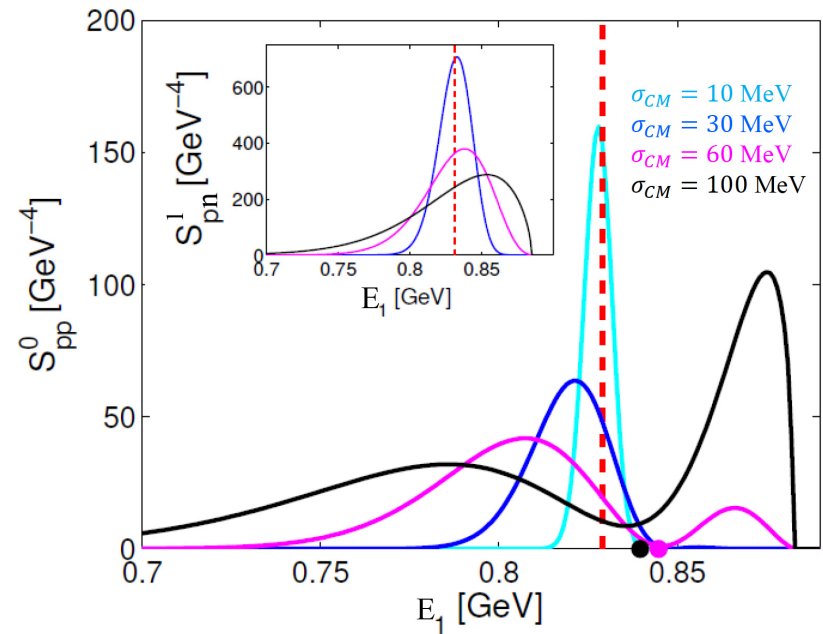
Summary & Conclusions

- GCF describes the many-body nuclear wave-function where SRCs dominate.



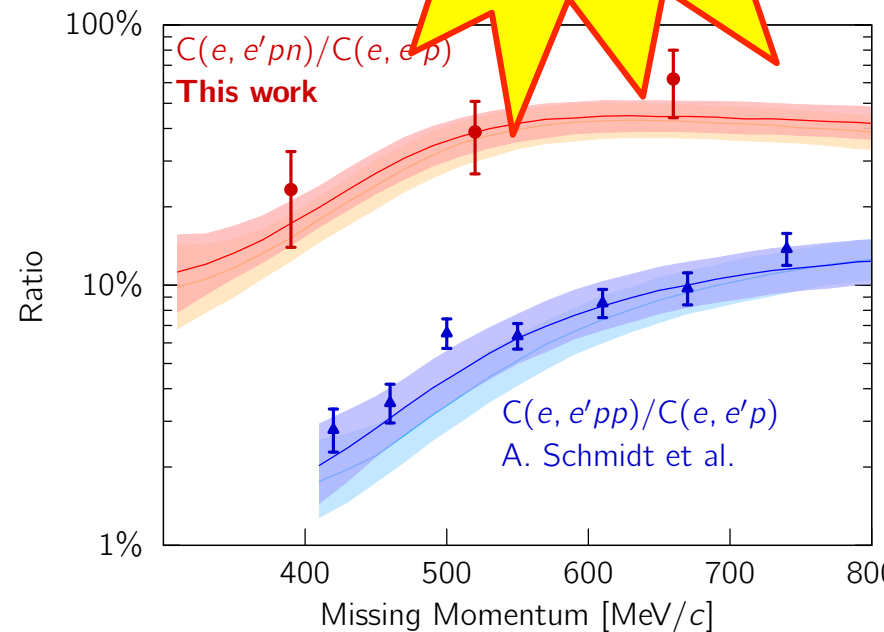
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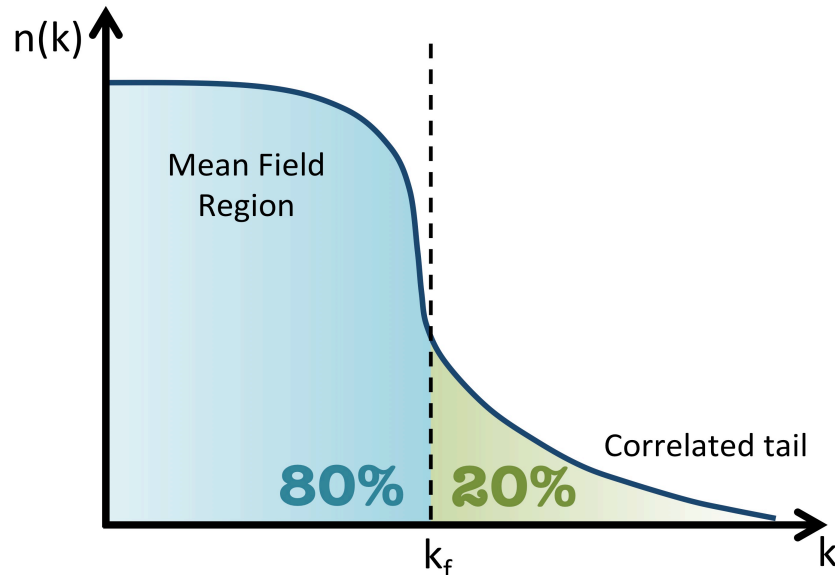


Summary & Conclusions

- GCF describes the many-body nuclear wave-function where SRCs dominate.
- GCF offers prescription for SRC spectral functions.
- This allows us to calculate QE electron-scattering cross sections and other observables.



SRC 101



Account for $\sim 20\%$ of all nucleons in any nucleus.

Dominate the momentum distribution above the Fermi momentum (k_F).

Relative momentum $\gg$ center-of-mass and Fermi momenta.

Predominantly pn pairs.

O. Hen et al., Science 364 (2014) 614.

Korover et al., PRL 113 (2014) 022501.

N. Fomin et al., PRL 108, 092502 (2012).

R. Subedi et al., Science 320 (2008) 1476.

K. Sh. Egiyan et al., PRC 68, 014313 (2003).

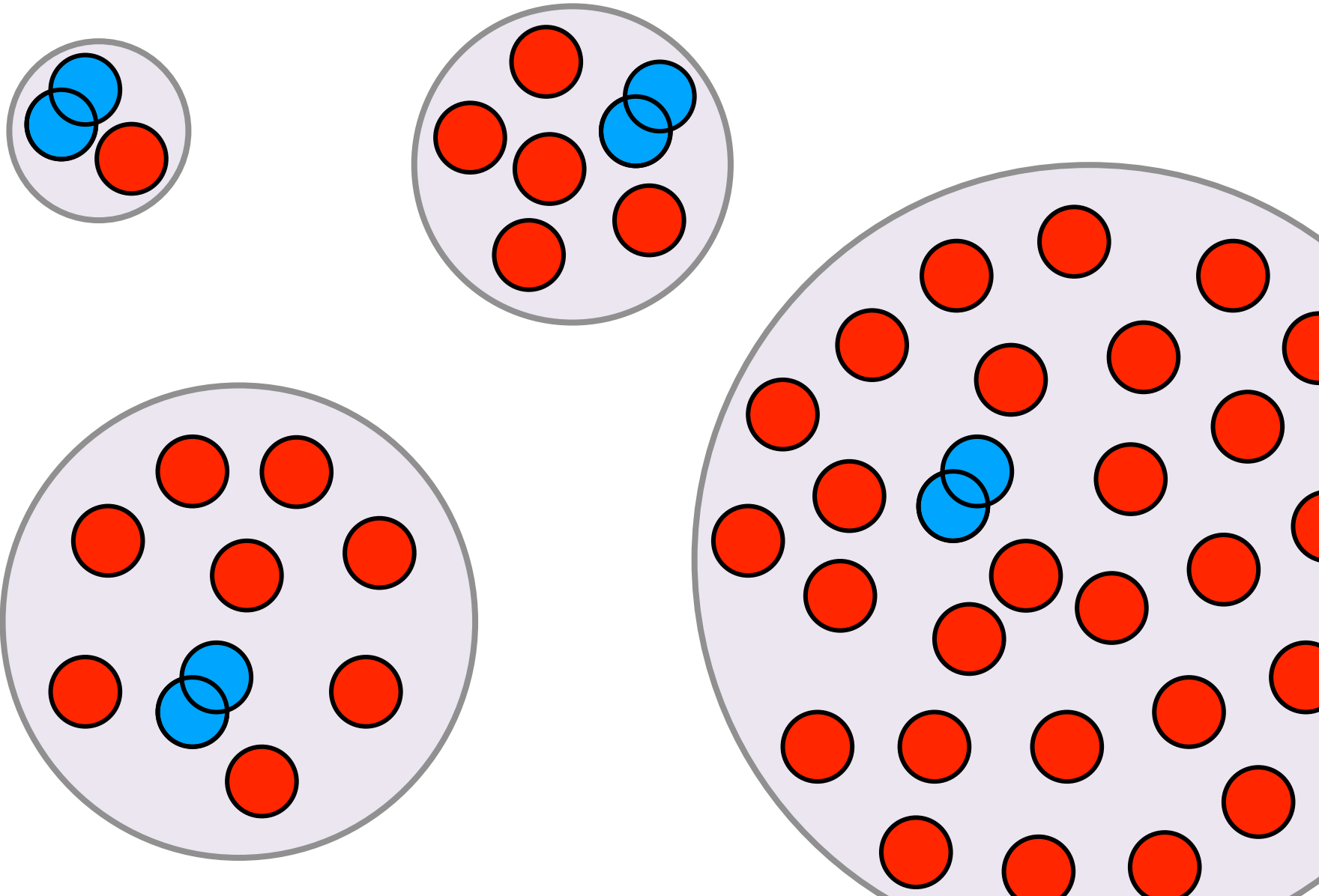
H. Baghdasaryan et al., PRL 105, 222501 (2010).

O. Hen, L. B. Weinstein, E. Piasetzky, *et al.*, PRC 92, no. 4, 045205 (2015).

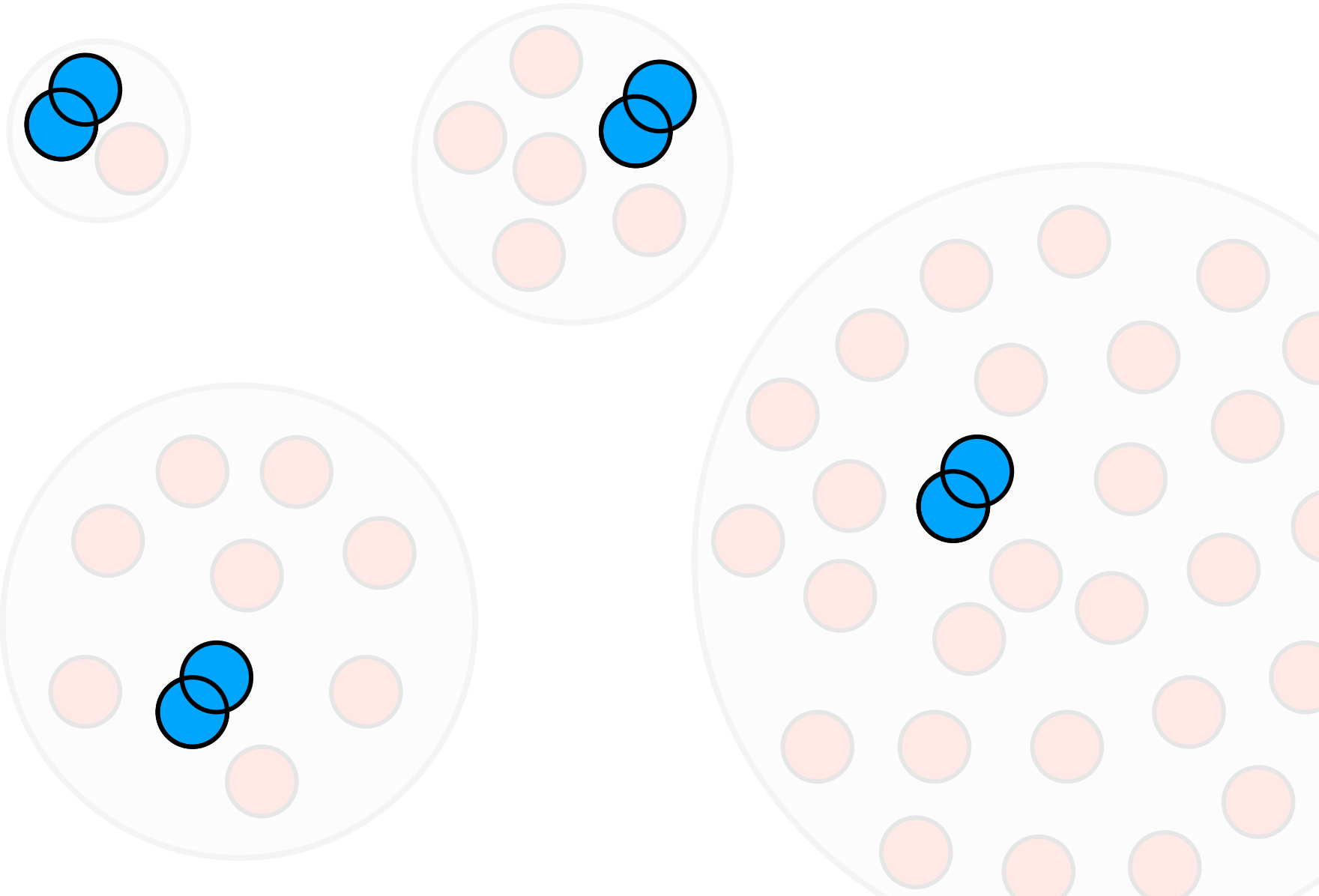
Why effective theories for SRC?

- Complicated NN interaction & large nuclear density
- Ab-initio calculations are limited to light-medium nuclei
 - Mean-Field theories don't include SRCs

Scale Separation in Nuclear Systems

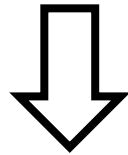


Scale Separation in Nuclear Systems

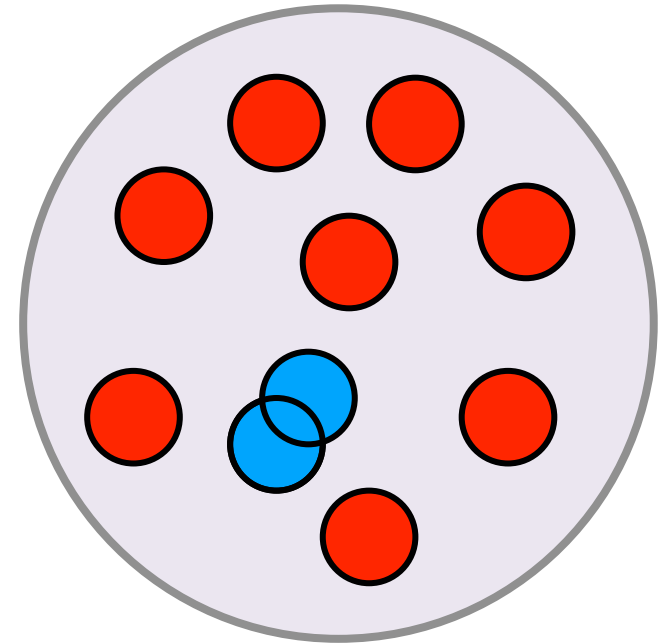


Factorization in nuclear systems

Scale separation at short distances

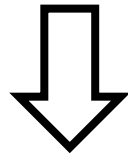


Factorization of the nuclear
wavefunction

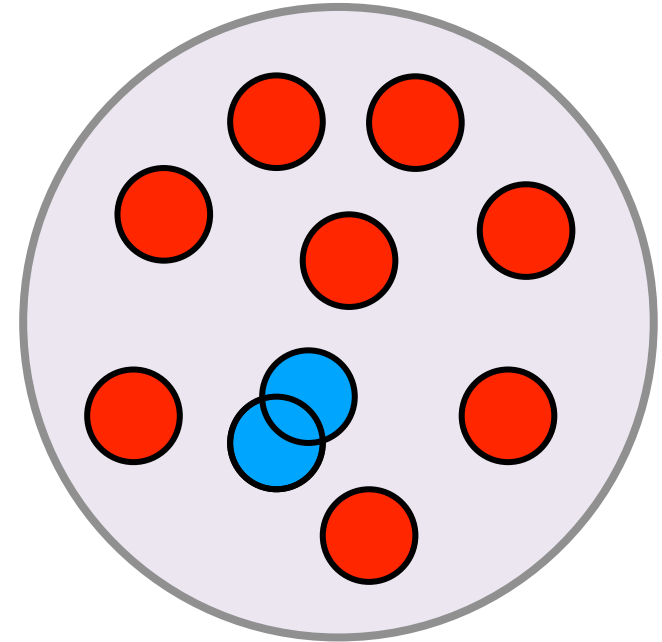


Factorization in nuclear systems

Scale separation at short distances



Factorization of the nuclear wavefunction



$$\Psi \xrightarrow{r_{ij} \rightarrow 0} \varphi(r_{ij}) \times A_{ij}(R_{ij}, \{r\}_{k \neq ij})$$

Many-body
nuclear wave-
function

two-body
wave-
function

A-2 residual
system

Short-r 2-body density in the GCF

$$\rho_A^{NN,\alpha}(\mathbf{r}) = c_A^{NN,\alpha} \times |\varphi_{NN}^{\alpha}(\mathbf{r})|^2$$

Short-r 2-body density in the GCF

$$\rho_A^{NN,\alpha}(\mathbf{r}) = C_A^{NN,\alpha} \times |\varphi_{NN}^{\alpha}(\mathbf{r})|^2$$

Many-body density

constant

Contacts

(nucleus dependent)

2-body density

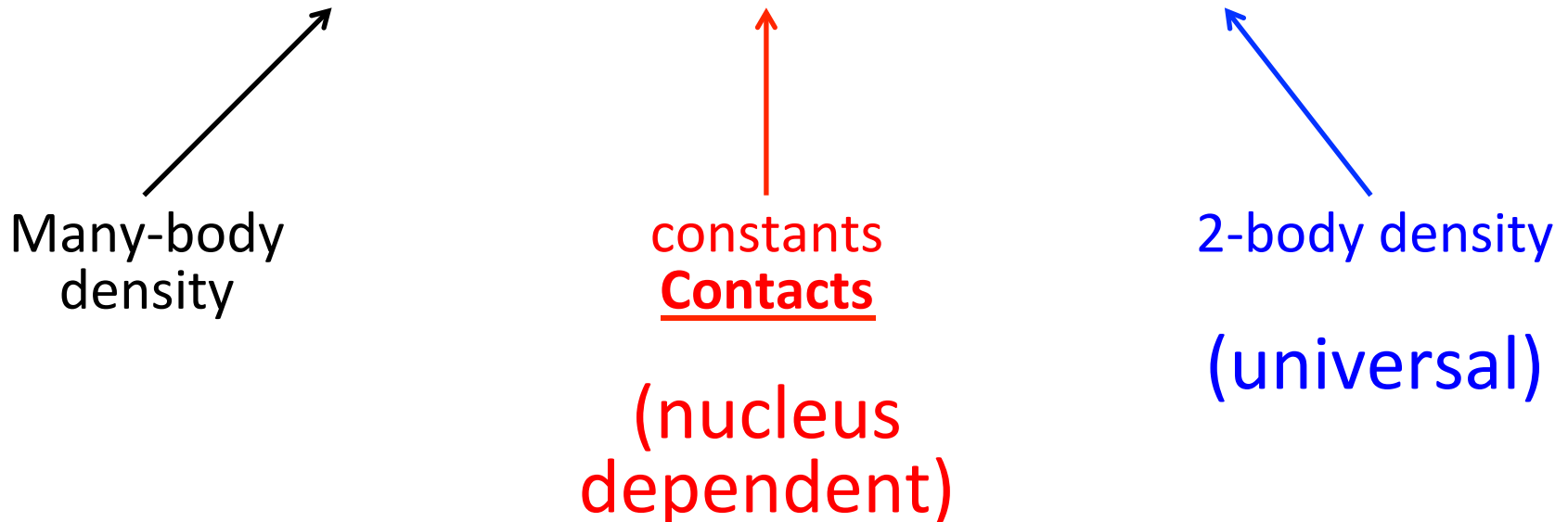
(universal)

High-k 2-body density in the GCF

$$\rho_A^{NN,\alpha}(\mathbf{r}) = C_A^{NN,\alpha} \times |\varphi_{NN}^{\alpha}(\mathbf{r})|^2$$

$$\rho_A^{NN,\alpha}(\mathbf{q}) = C_A^{NN,\alpha} \times |\varphi_{NN}^{\alpha}(\mathbf{q})|^2$$

Many-body
density



constants
Contacts

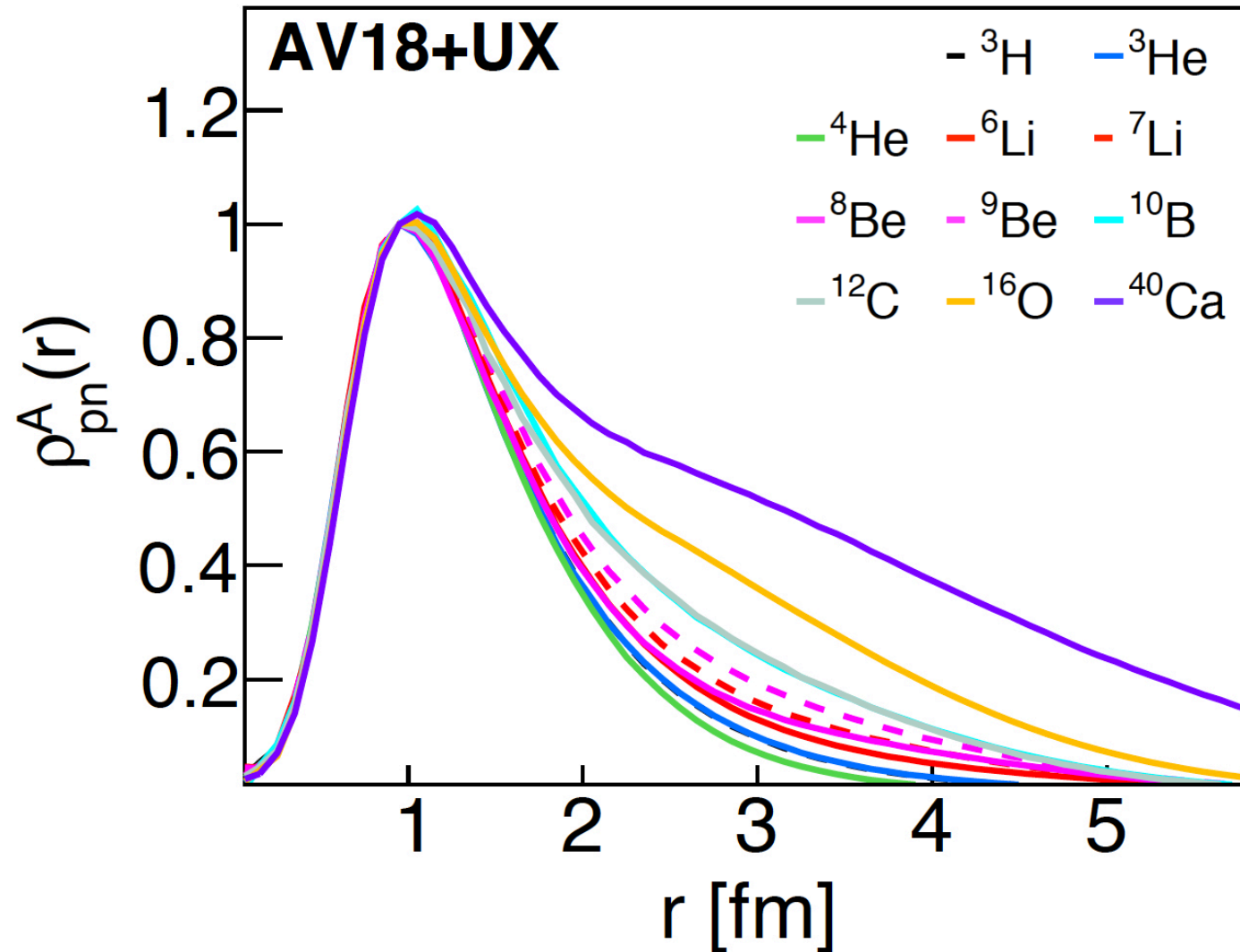
(nucleus
dependent)

2-body density
(universal)

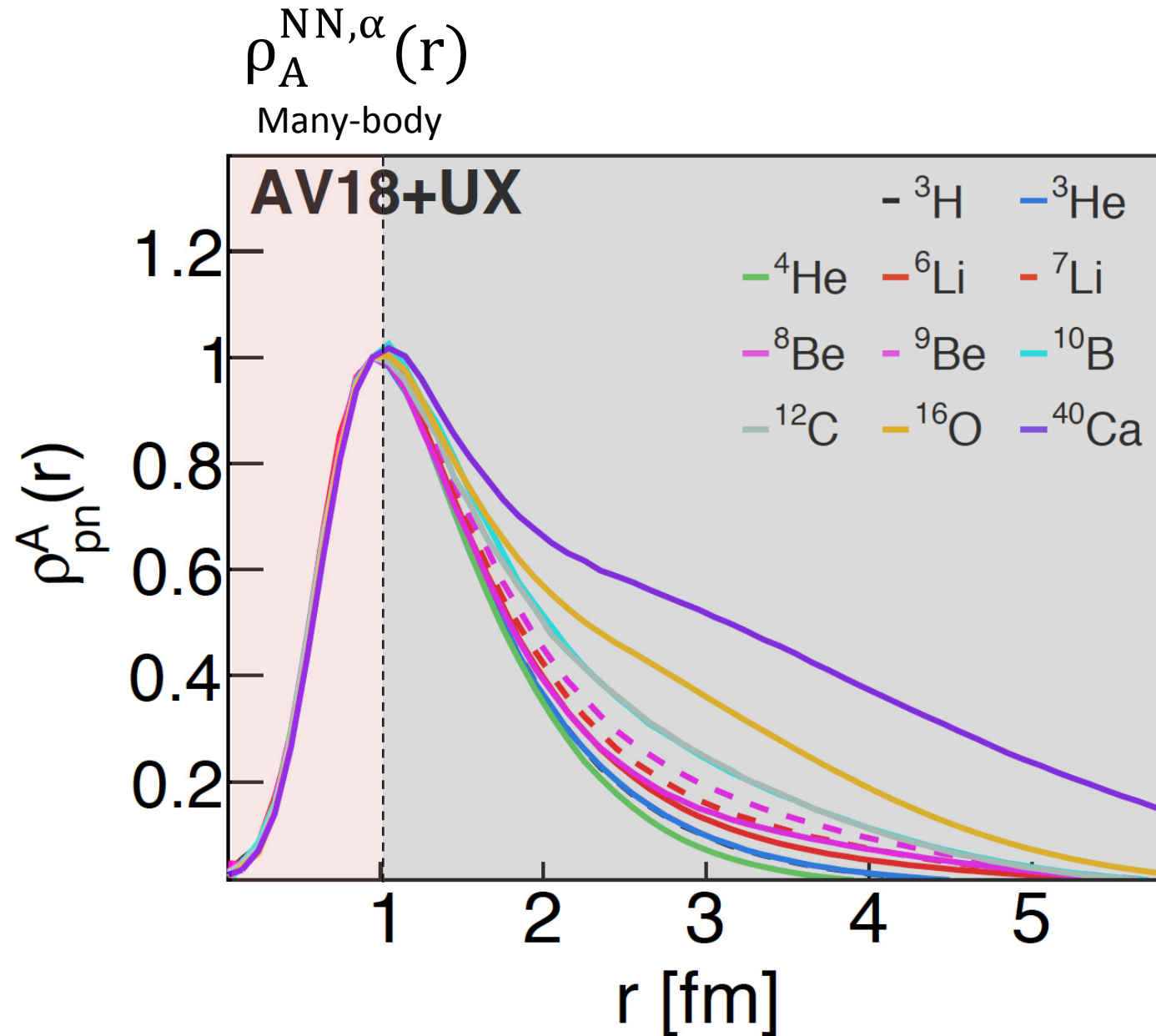
Small-r universality

$$\rho_A^{NN,\alpha}(r)$$

Many-body

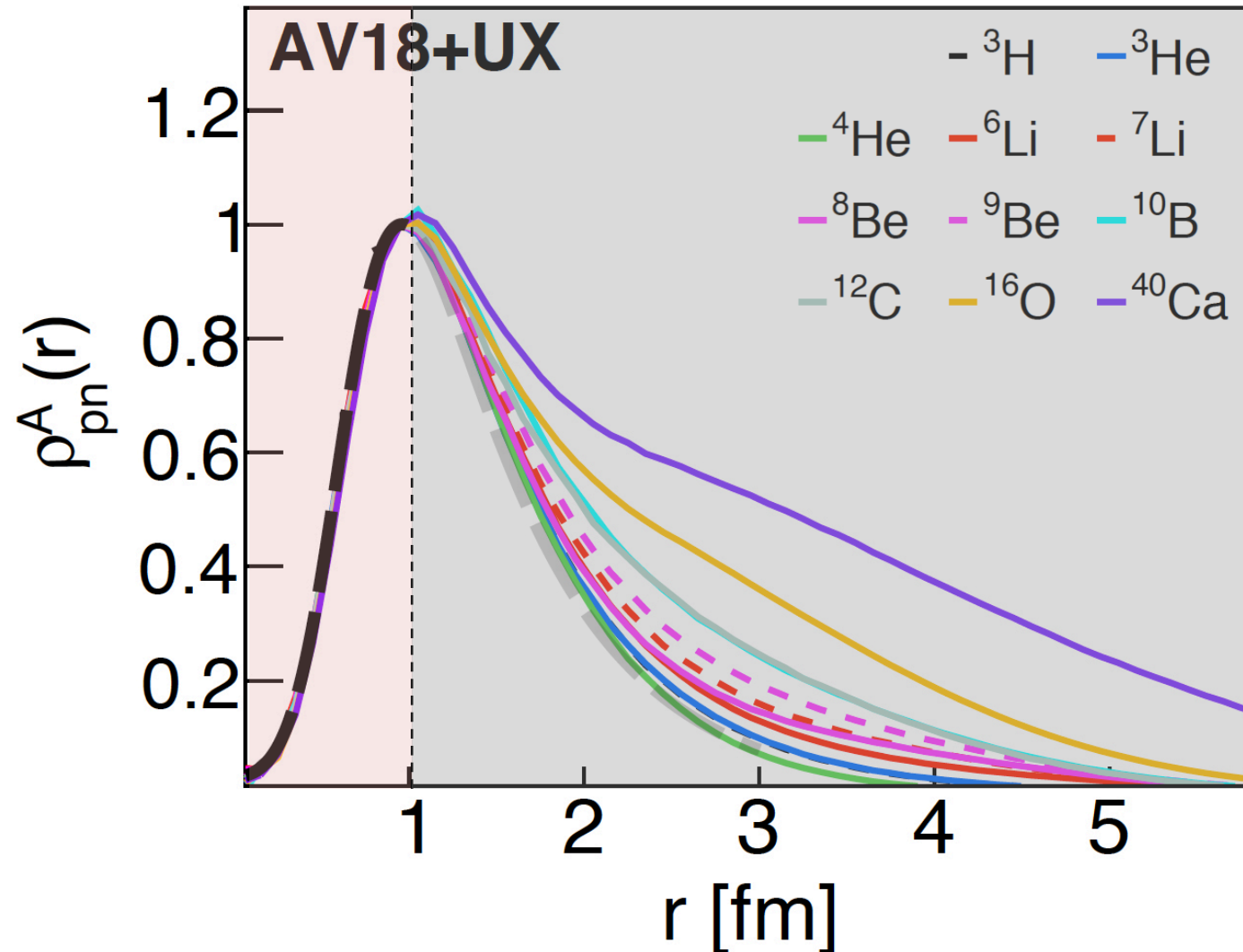


Small-r universality



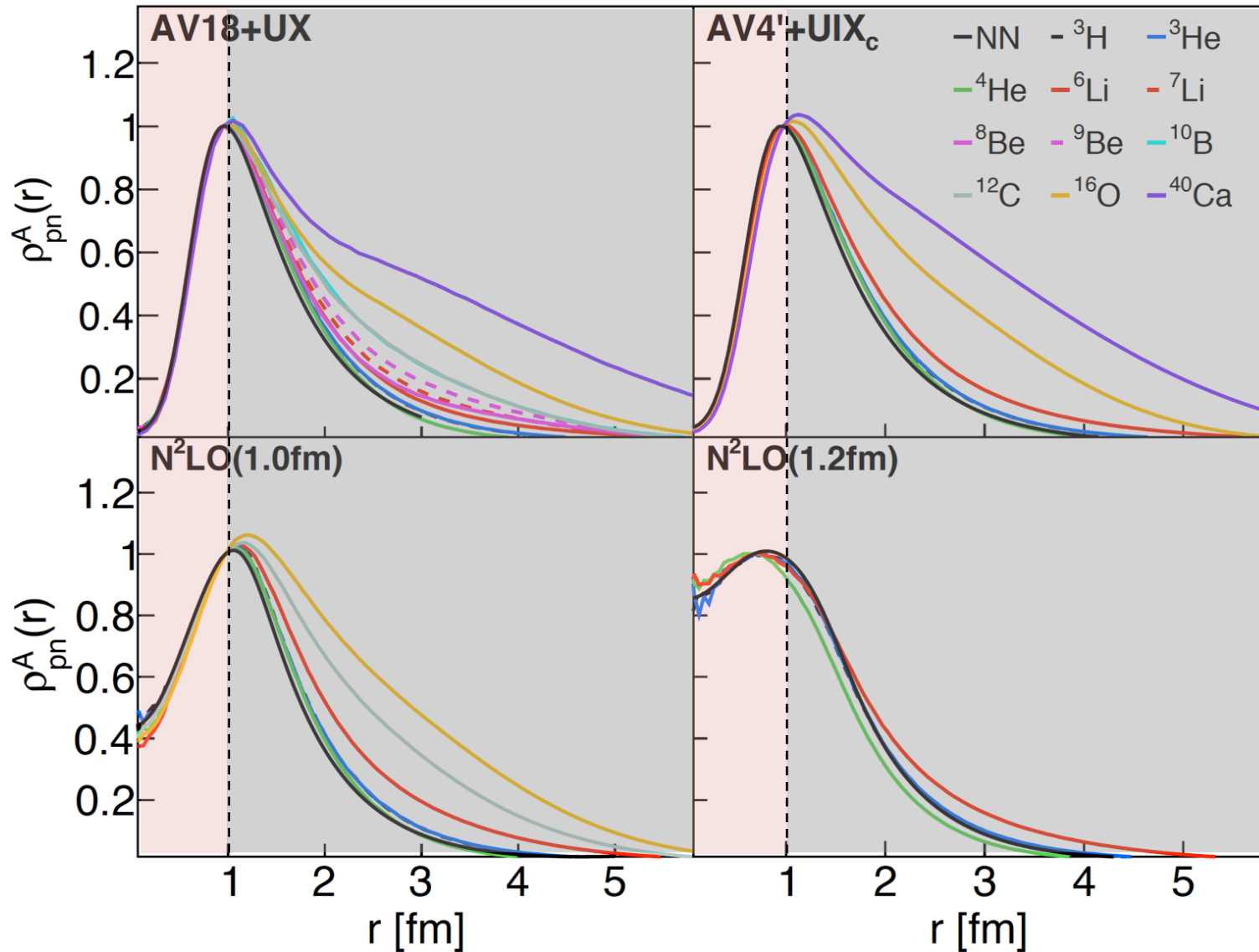
The Generalized Contact Formalism

$$\rho_A^{\text{NN},\alpha}(r) = \underset{\text{Many-body}}{C_A^{\text{NN},\alpha}} \times \underset{\text{Pair}}{|\varphi_{\text{NN}}^{\alpha}(r)|^2}$$



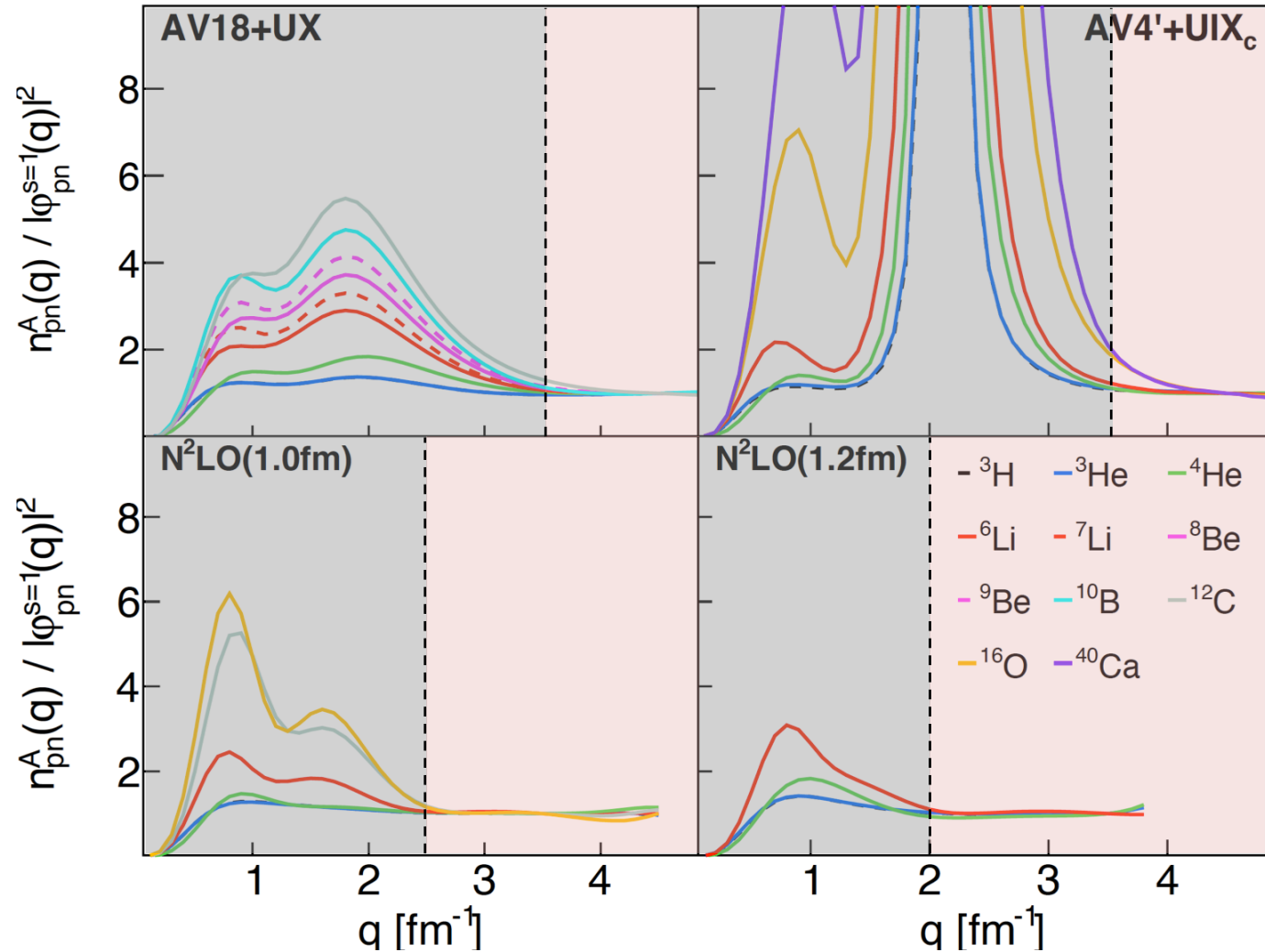
Small-r universality and the GCF

$$\rho_A^{NN,\alpha}(r) = C_A^{NN,\alpha} \times |\varphi_{NN}^{\alpha}(r)|^2$$



High-k universality and the GCF

$$\frac{\rho_A^{NN,\alpha}(q)}{|\varphi_{NN}^\alpha(q)|^2} = C_A^{NN,\alpha}$$



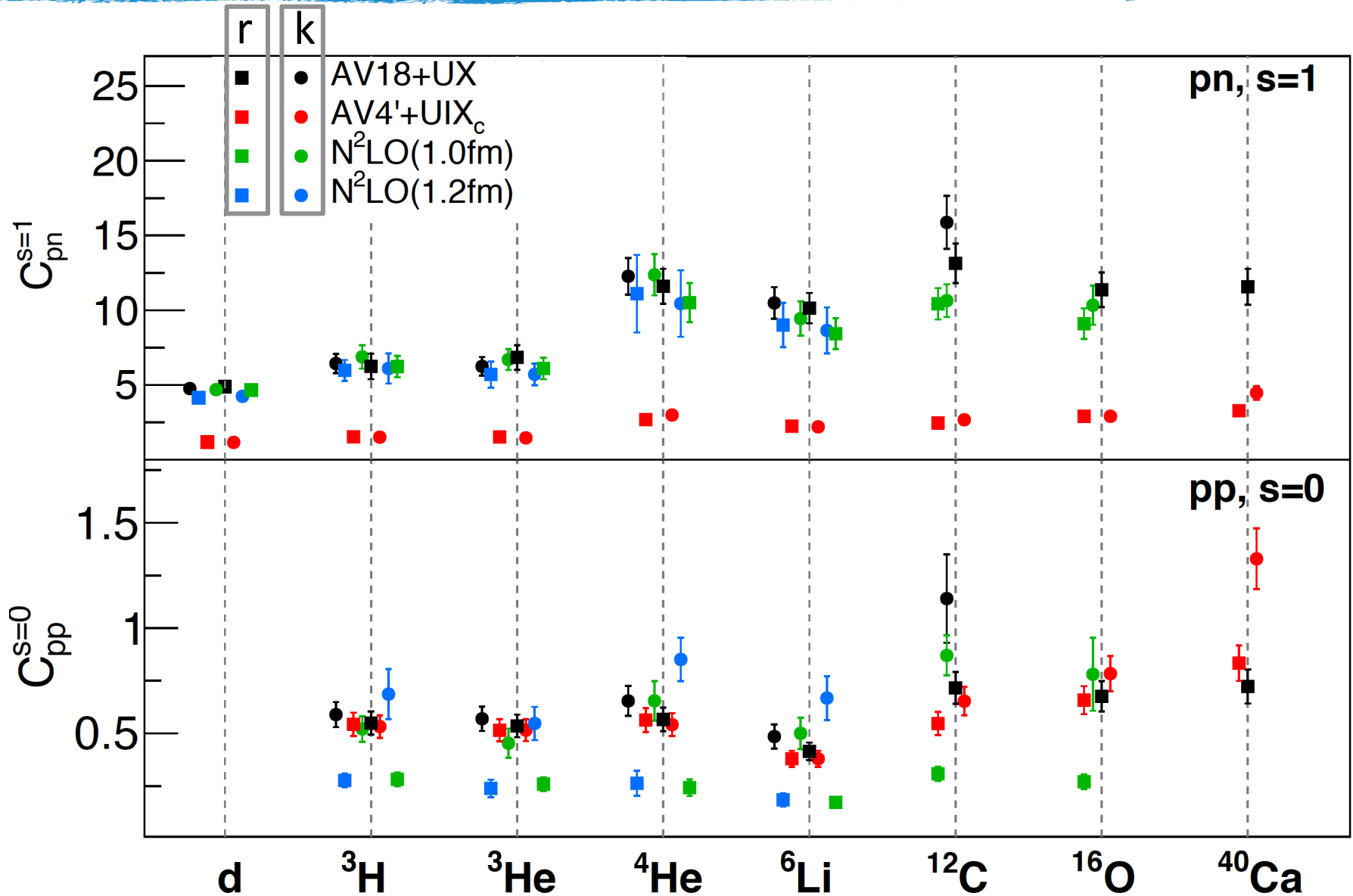
RW et al., Phys. Rev. C 92, 054311 (2015)

RW, **RCT** et al., PLB 780, 211 (2018)

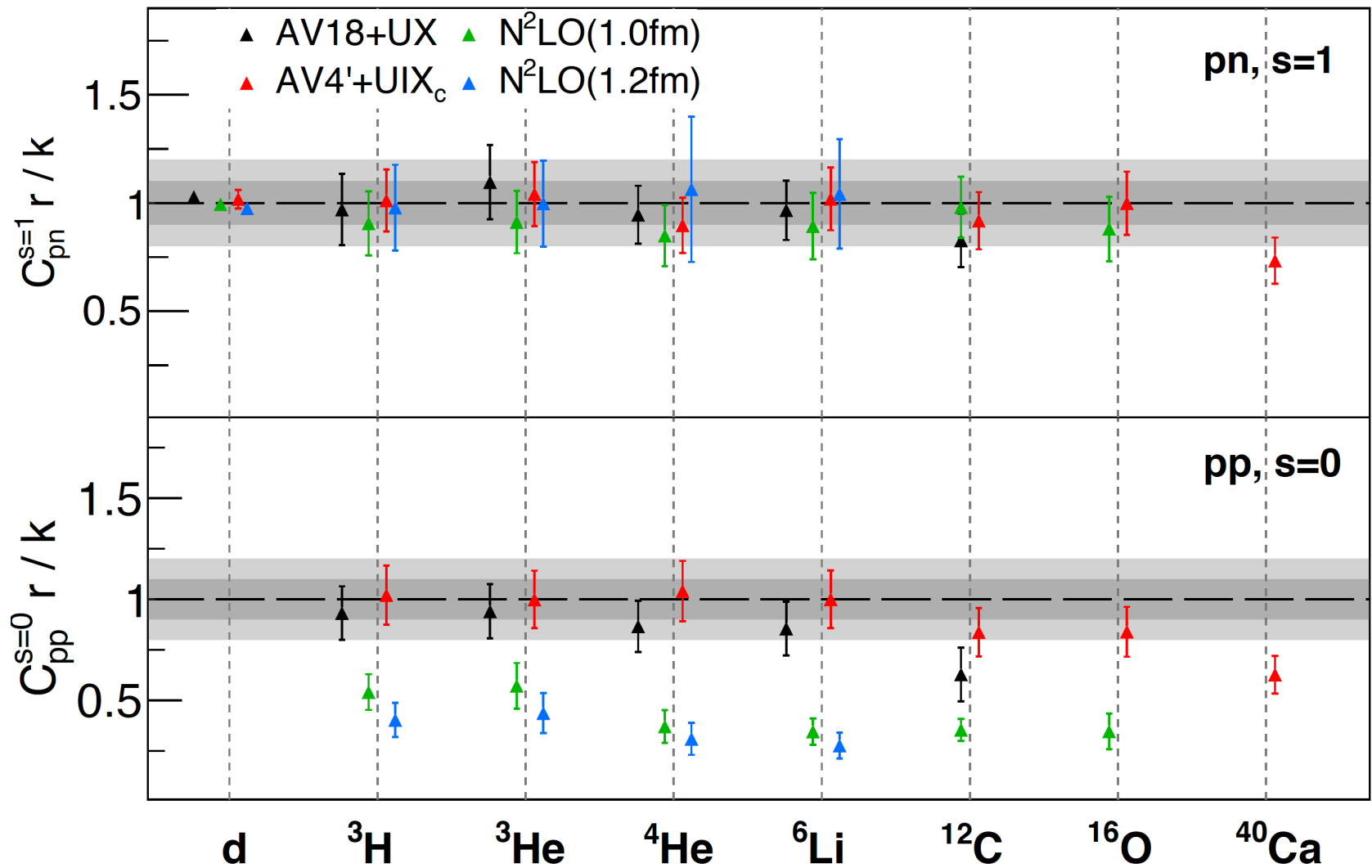
RCT, et al., PLB 785 304 (2018)

RCT, et al., arXiv:1907.03658 (2019), under review for Nature Physics

Nuclear Contacts



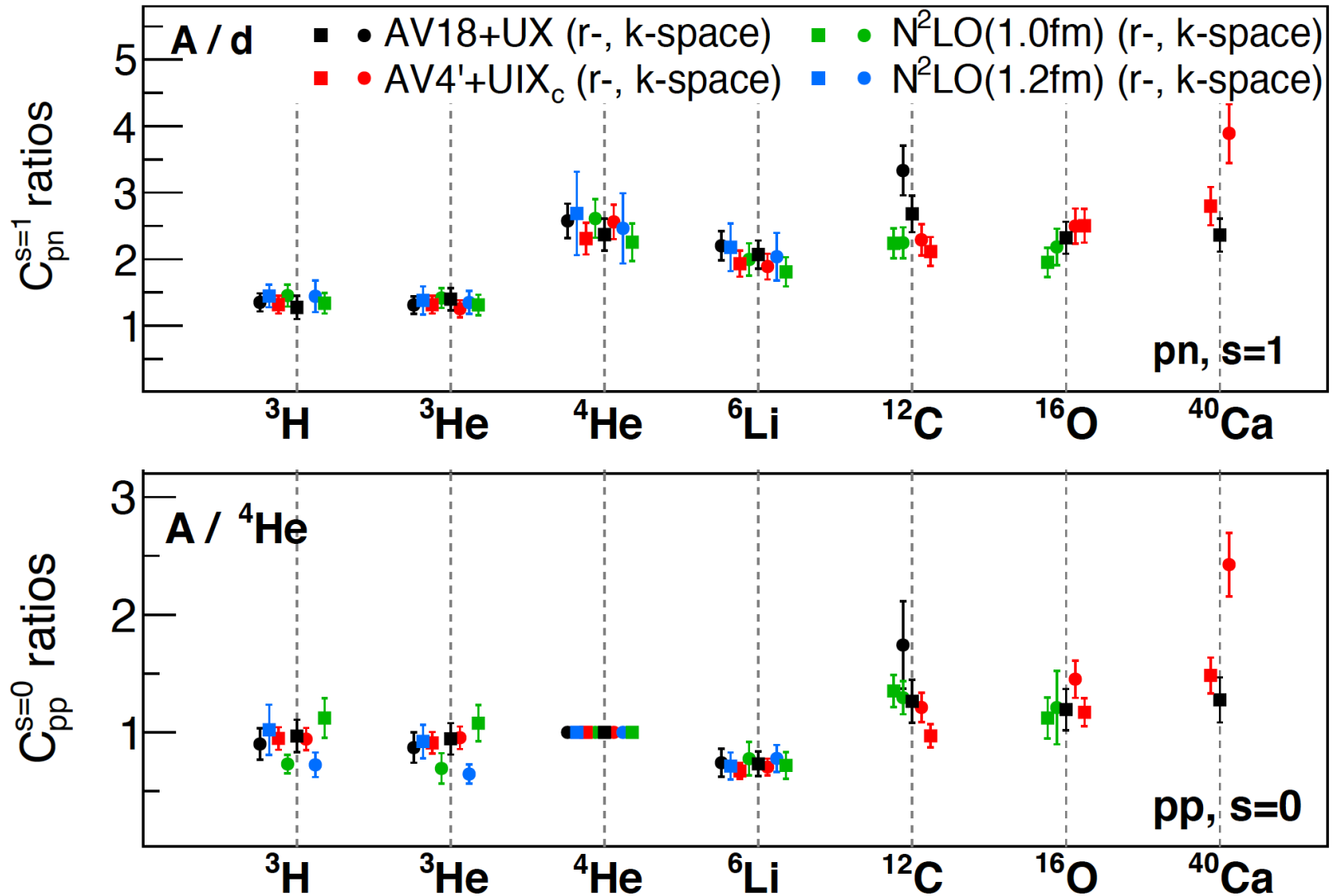
Coordinate – Momentum Equivalence



r/k ratio = 1 $\rightarrow$ coordinate-momentum equivalence

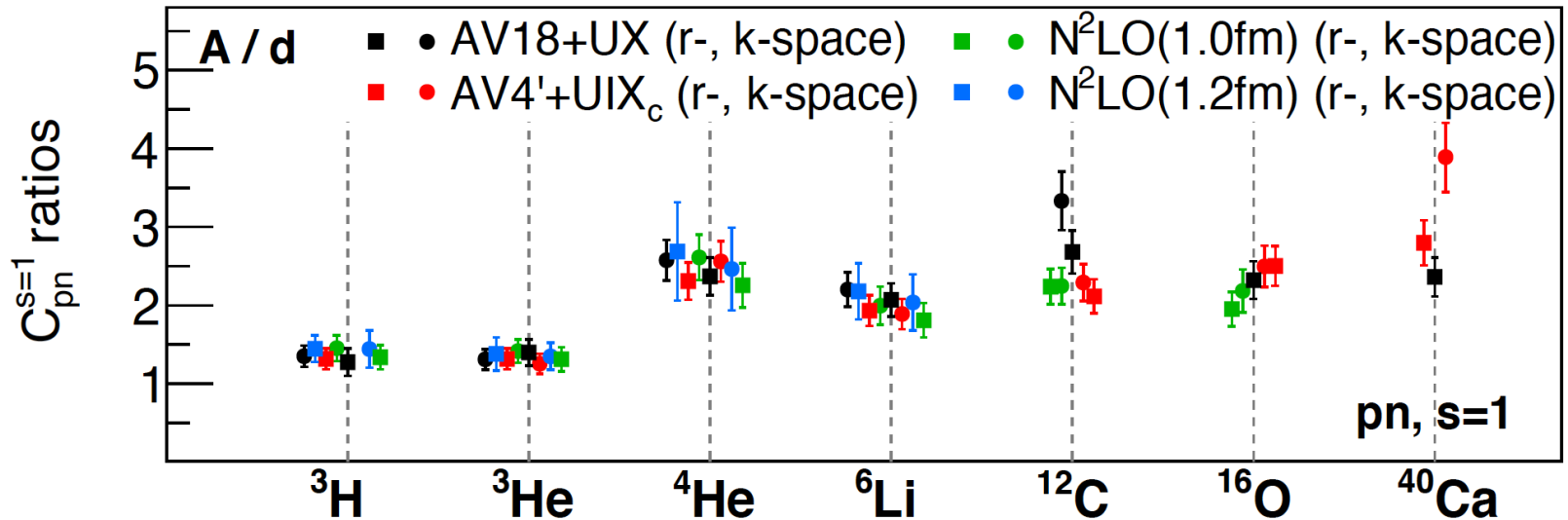
A/d: small-r and high-k scaling are IDENTICAL

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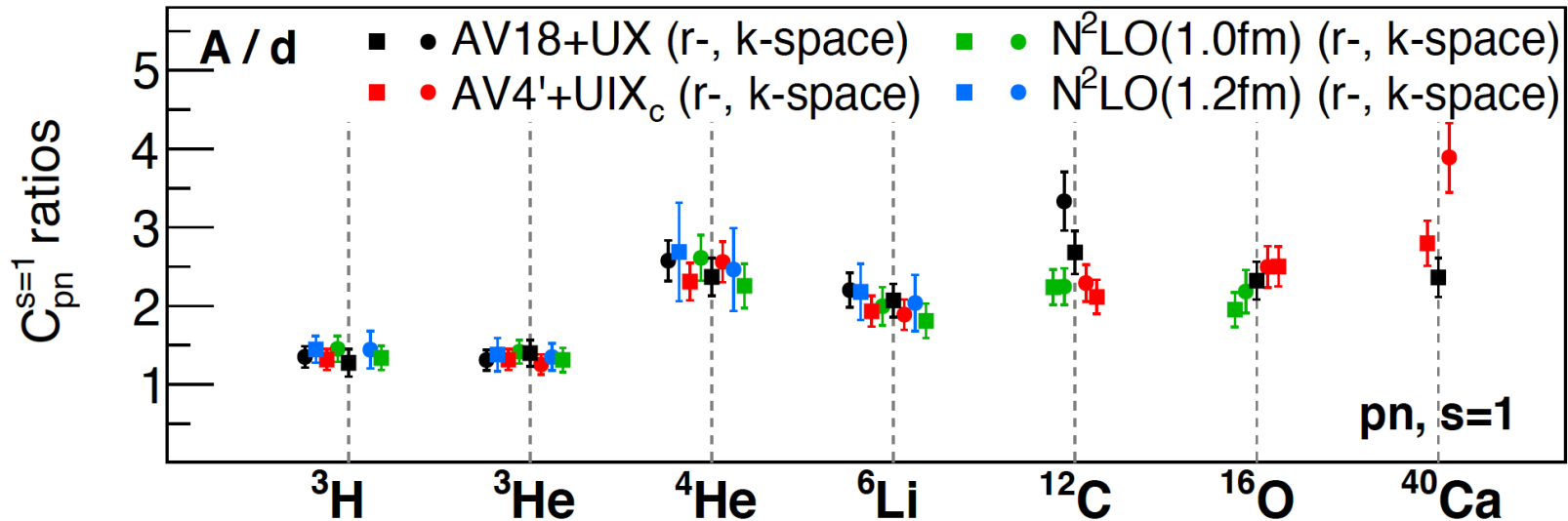
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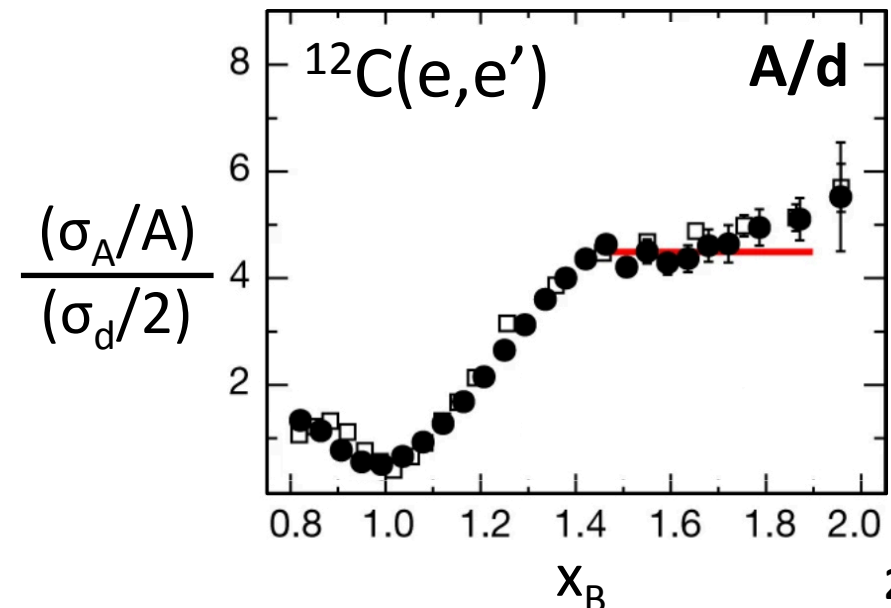
- SRC abundance is a Mean Field property.

A/d: small-r and high-k scaling are IDENTICAL

RCT, et al., arXiv:1907.03658 (2019), under review for Nature Physics.



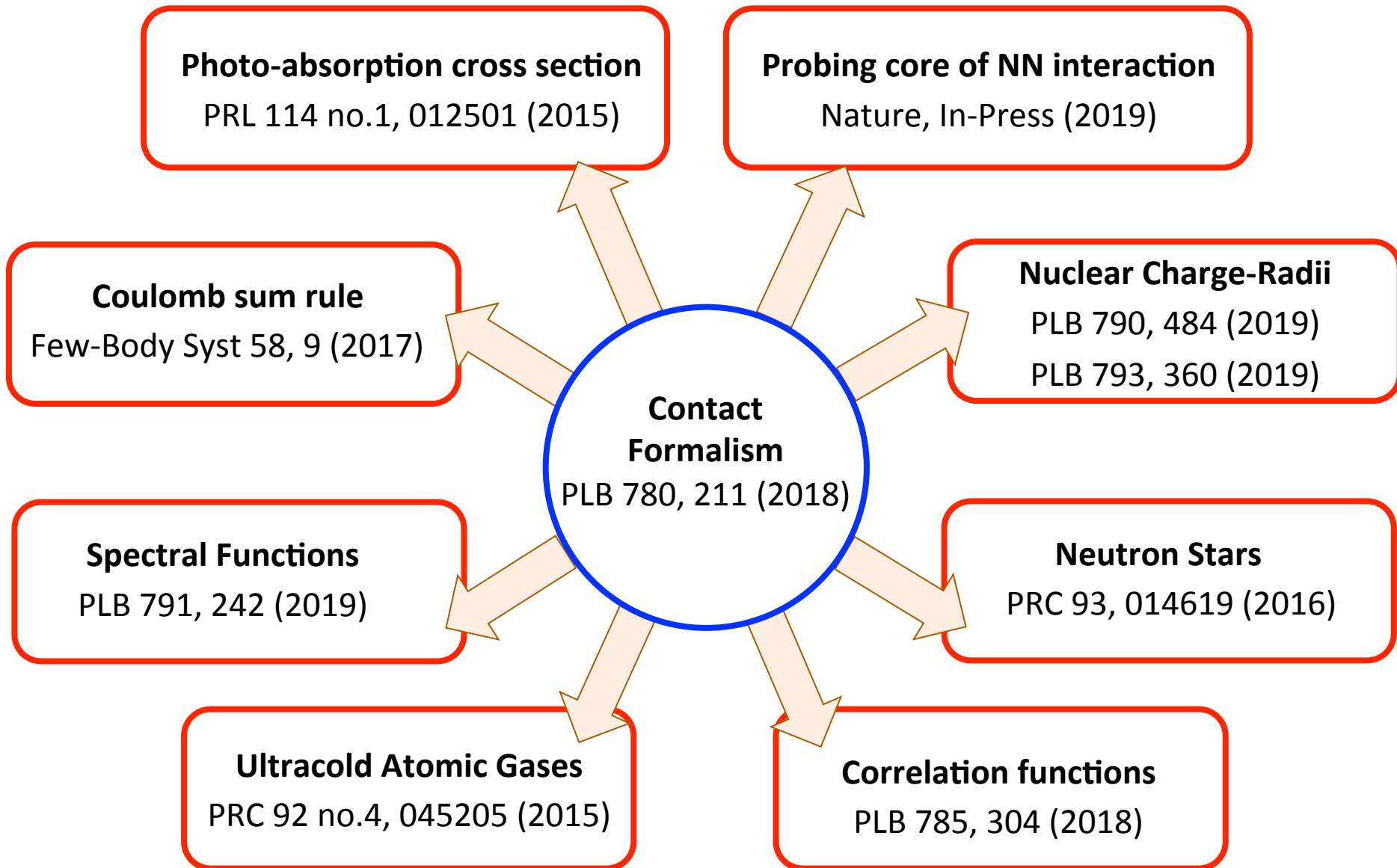
- SRC abundance is a Mean Field property.
- Inclusive ratios are insensitive to the NN interaction details at short distance.



Fomin et al., PRL 108, 092502 (2012).

B.Schmookler, et al., Nature 566, 354-358 (2019)

Applications of the GCF



Applications of the GCF

Photo-absorption cross section
PRL 114 no.1, 012501 (2015)

Probing core of NN interaction
Nature, In-Press (2019)

Coulomb sum rule
Few-Body Syst 58, 9 (2017)

Nuclear Charge-Radii
PLB 790, 484 (2019)
PLB 793, 360 (2019)

Contact Formalism
PLB 780, 211 (2018)

Spectral Functions
PLB 791, 242 (2019)

Neutron Stars
PRC 93, 014619 (2016)

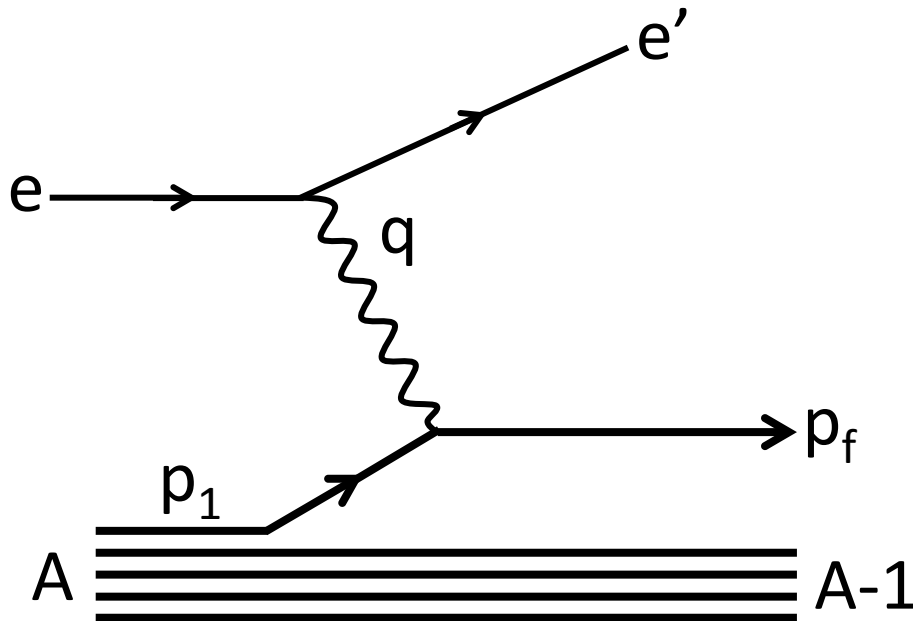
Ultracold Atomic Gases
PRC 92 no.4, 045205 (2015)

Correlation functions
PLB 785, 304 (2018)

Plane-Wave Impulse Approximation (PWIA)

Missing momentum

$$\vec{p}_{\text{miss}} \equiv \vec{p}_f - \vec{q}$$

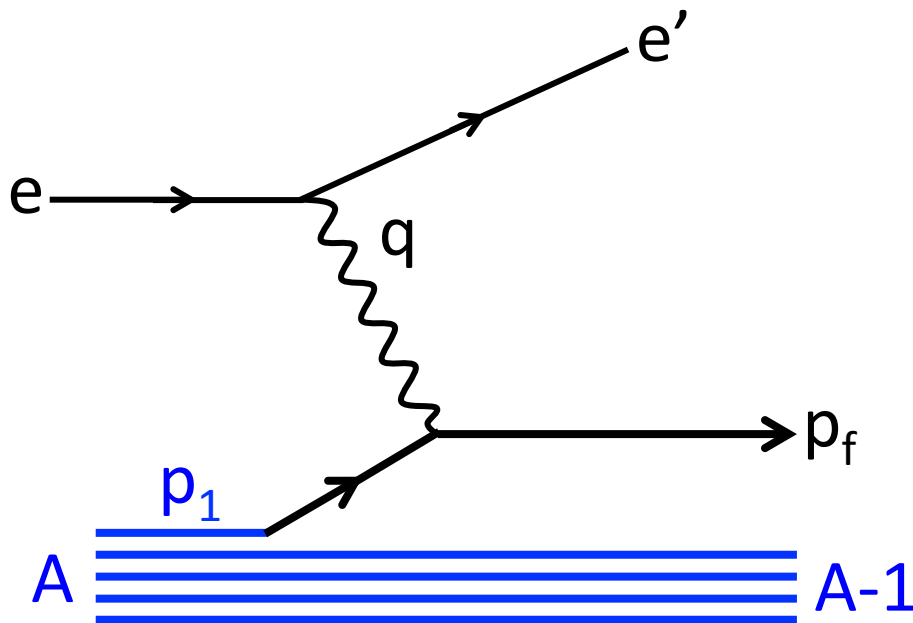


Assuming:

- 1) momentum transfer absorbed by a single nucleon.
- 2) knocked-out nucleon did not rescatter as it left the nucleus.

$$\vec{p}_{\text{miss}} = \vec{p}_1$$

High-Energy Factorization

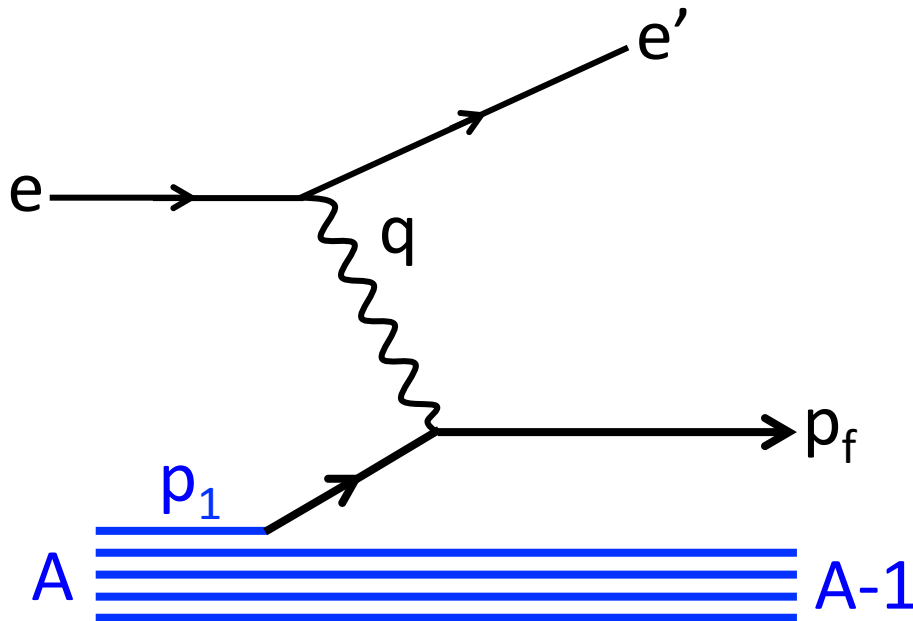


$$\sigma = \sigma_{eN} \cdot S(p_1, E_1)$$

Spectral function:
probability to find a
nucleon with
momentum p_1 and
energy E_1

High-Energy Factorization

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Spectral function:
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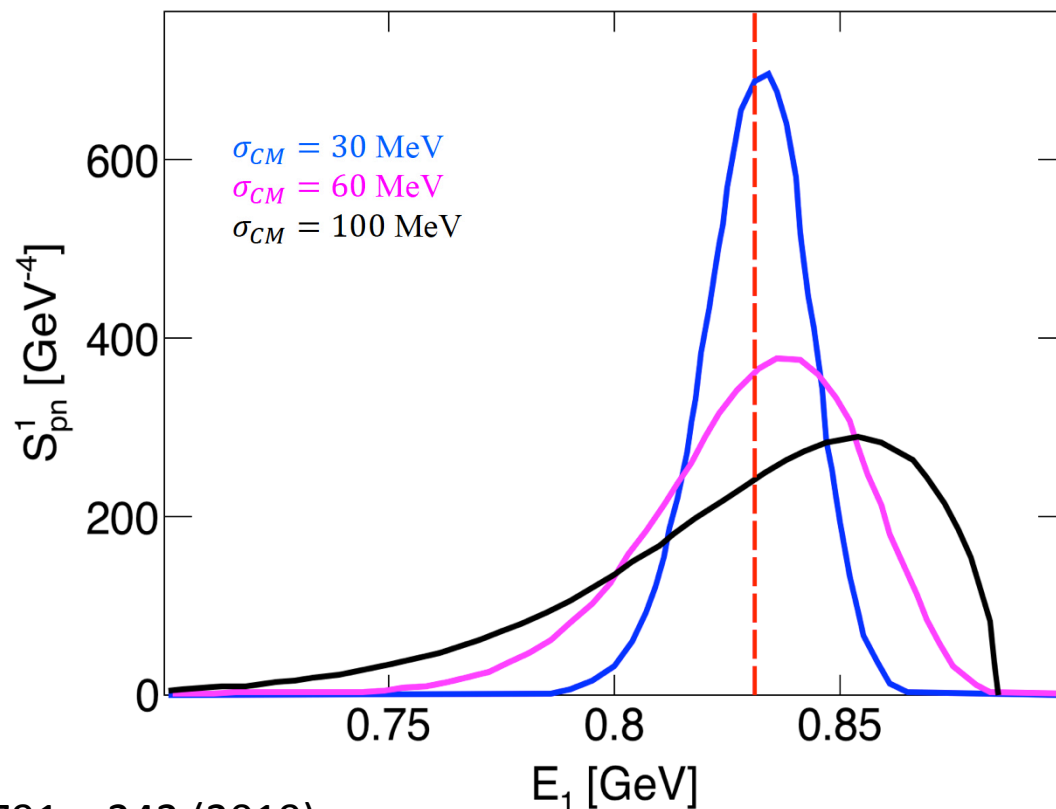


Calculated from traditional
effective models =>
lack SRC effects.

GFC (SRC) Spectral Function

$$\sigma = \sigma_{eN} \cdot S(p_1, E_1)$$

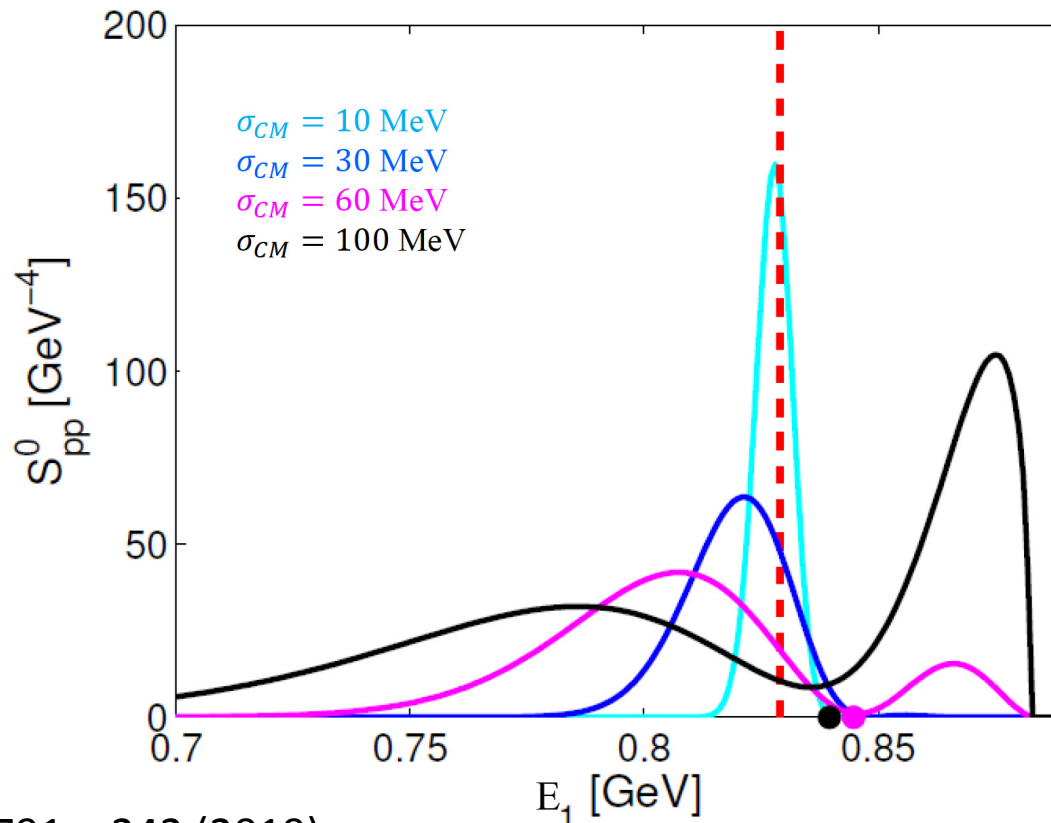
$$S(p_1, E_1) = \sum_{\alpha} C_A^{\alpha} \int \frac{d^3 p_2}{(2\pi)^3} |\varphi^{\alpha}(q)|^2 n(Q) \delta(f(p_2))$$



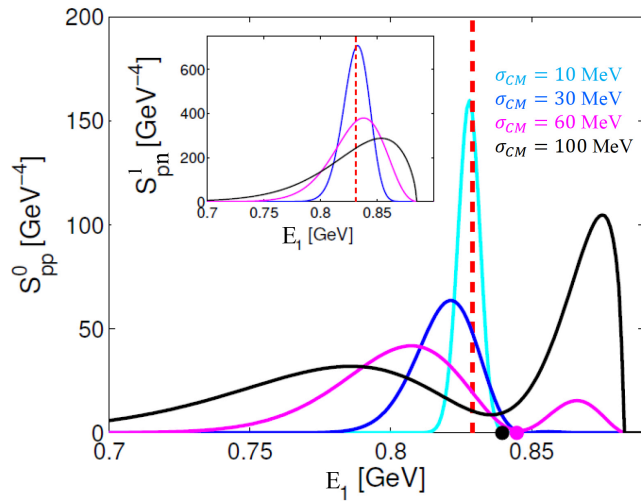
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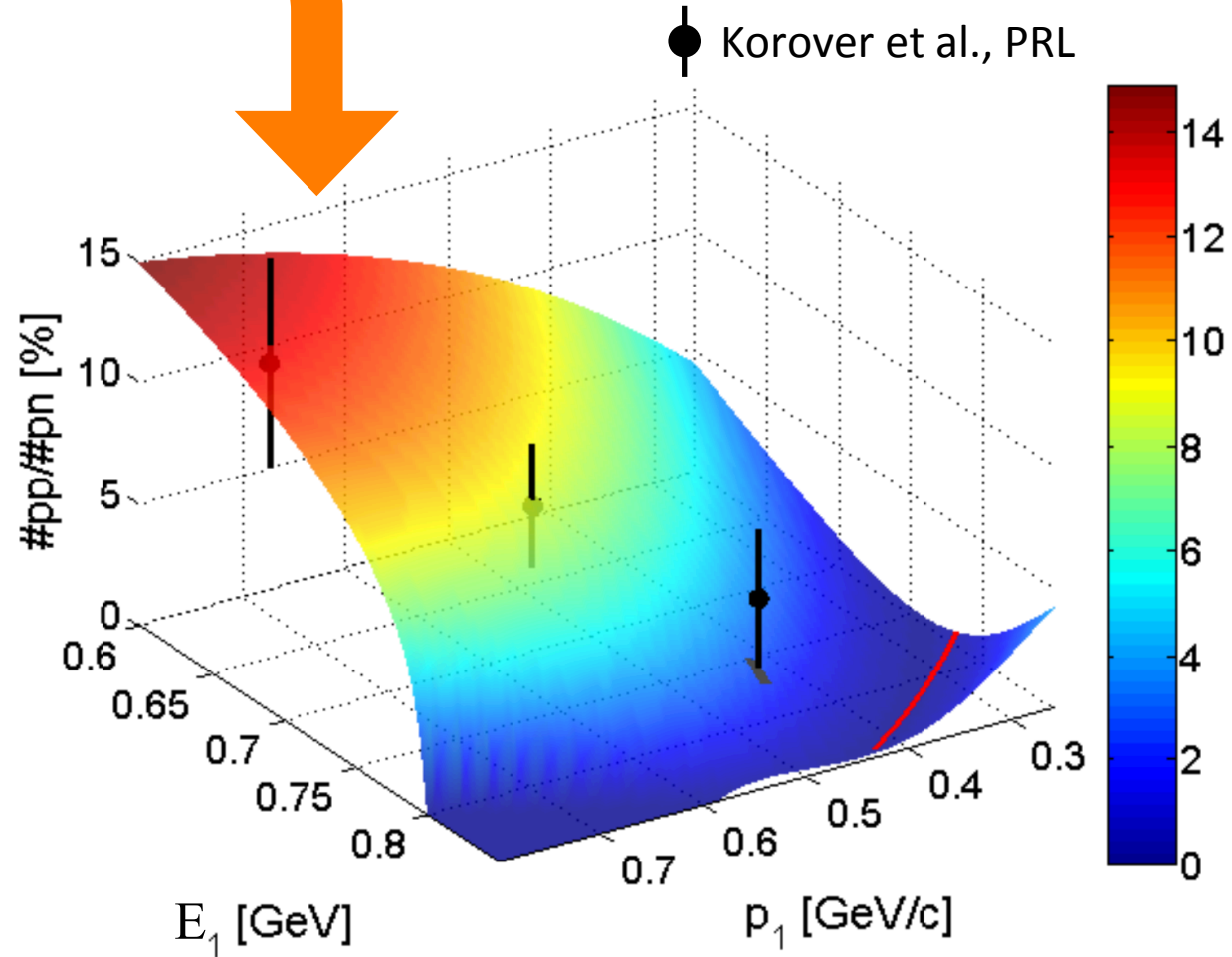
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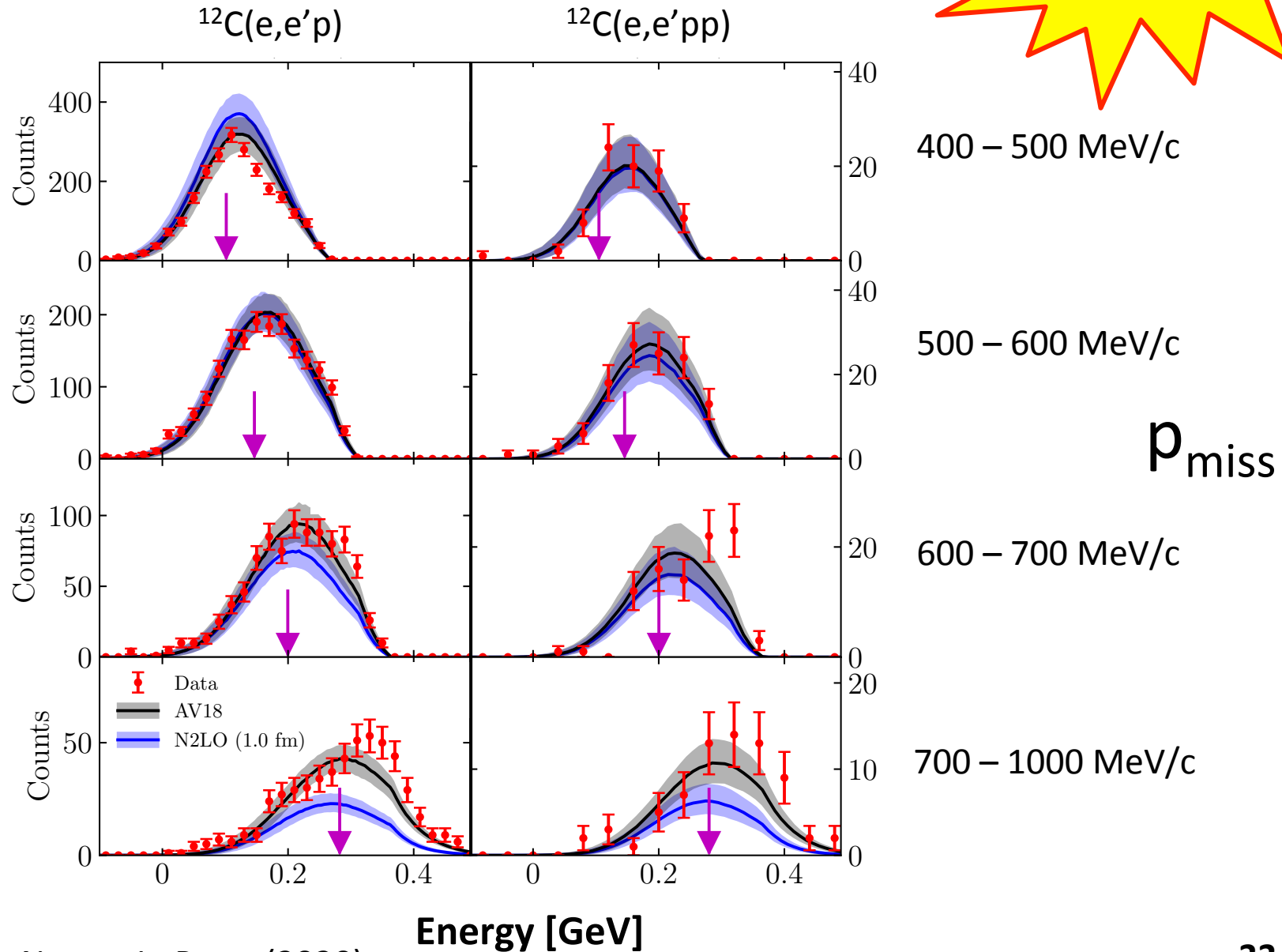


$$\frac{\#pp}{\#pn} = \frac{S_{pp}}{S_{pn}}$$



GFC (SRC) Spectral Function

see talk by
J. Pybus



Applications of the GCF

see talk by
J. Pybus

Photo-absorption cross section
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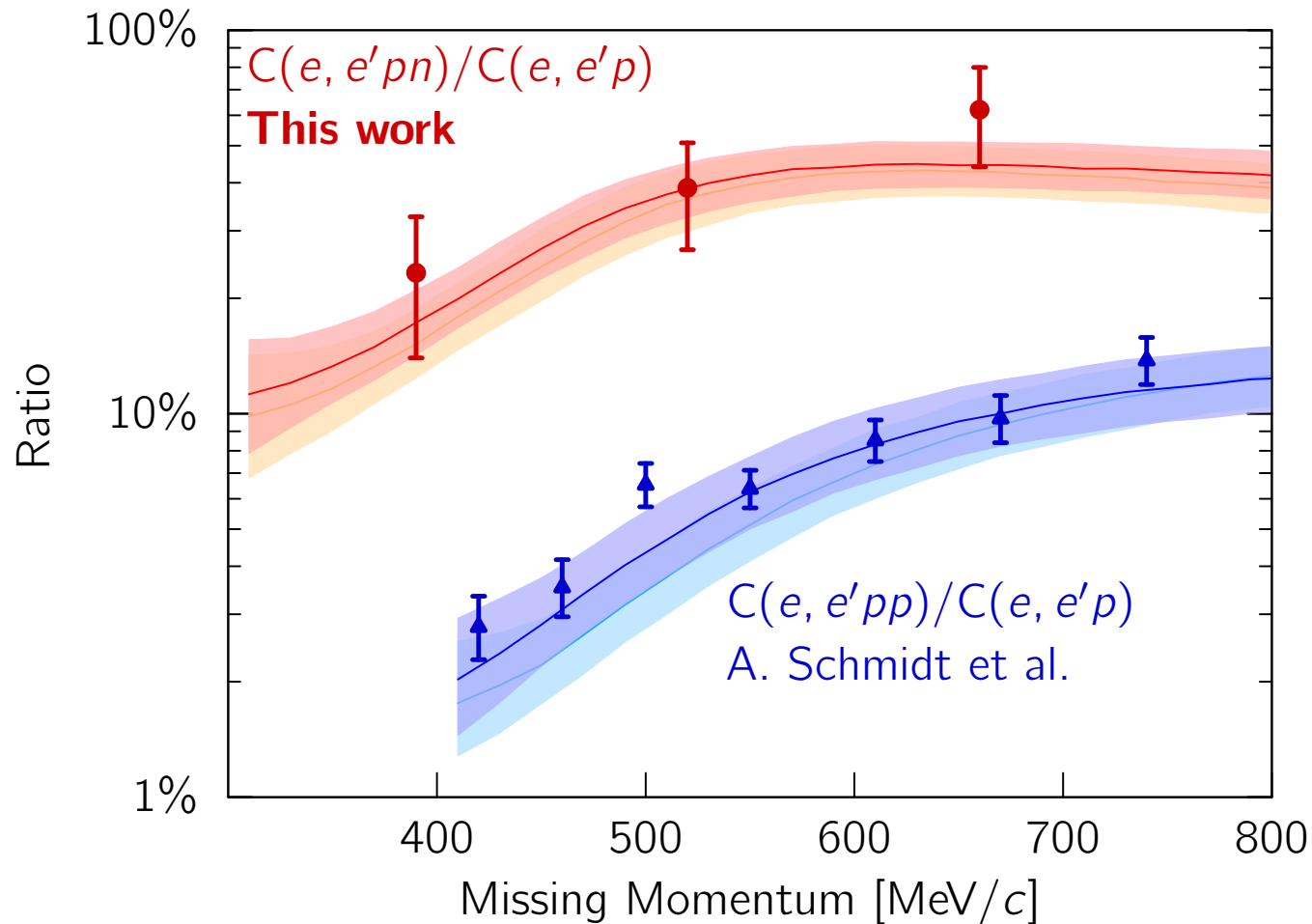
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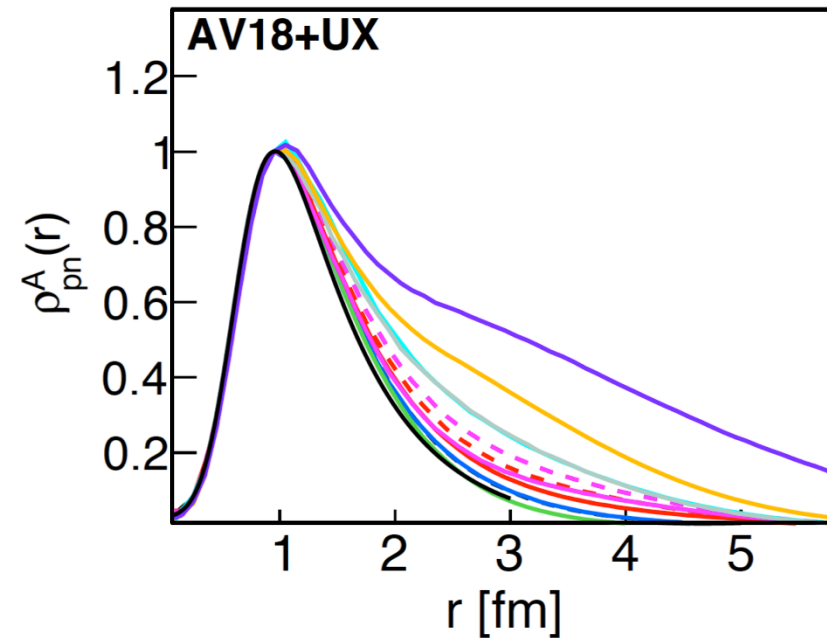
$(e,e'pN)/(e,e'p)$ ratio

see talk by
J. Pybus



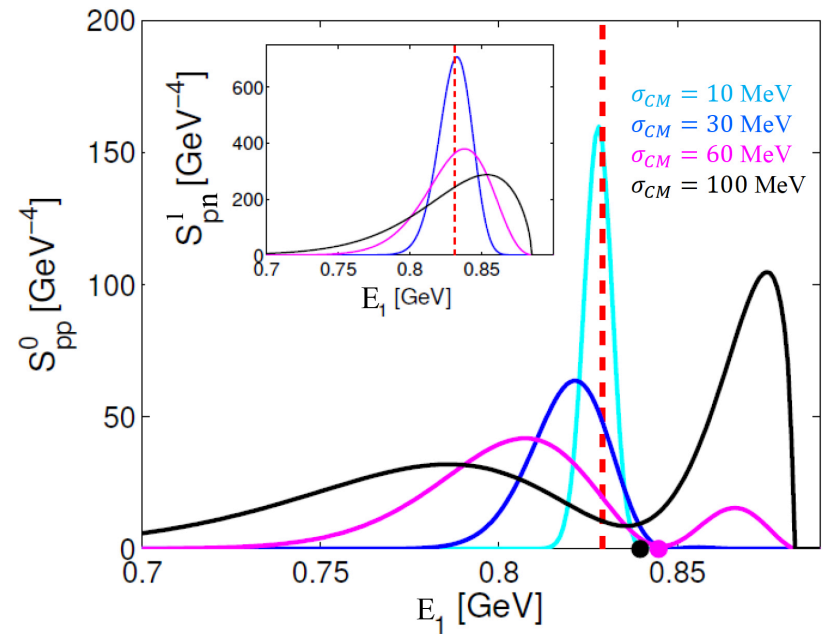
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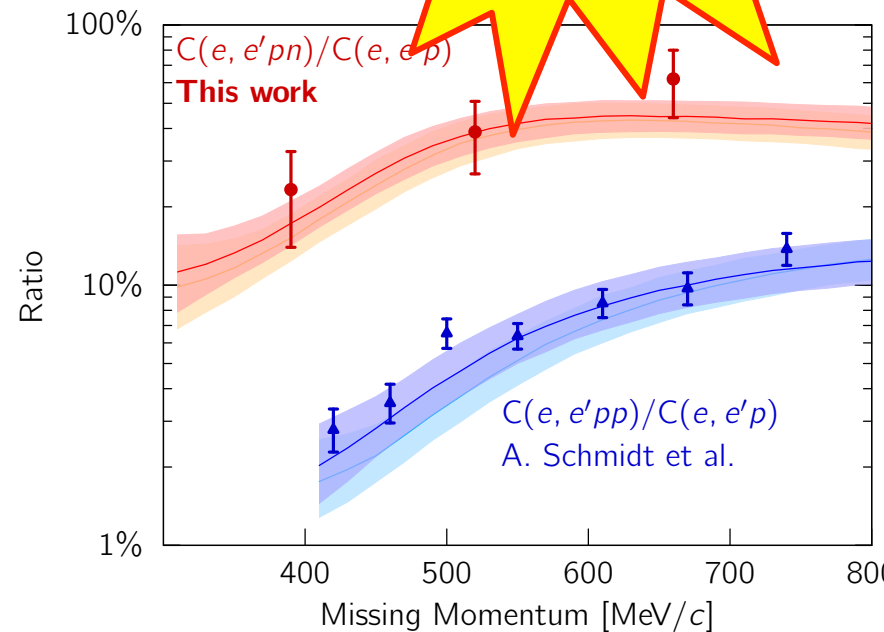
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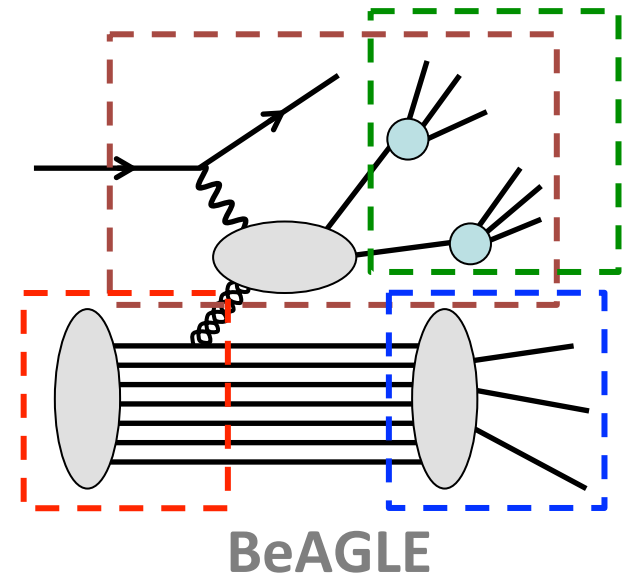
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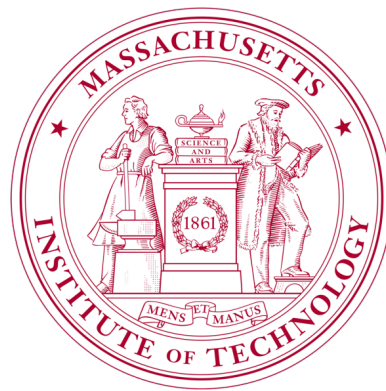
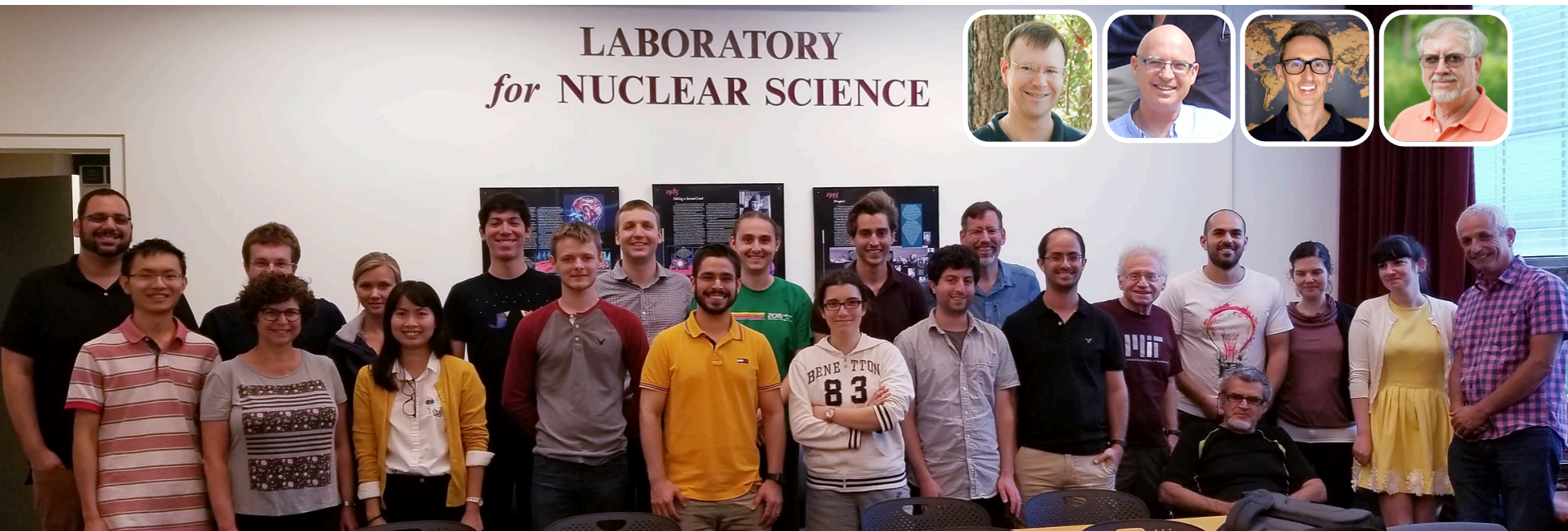


Summary & Conclusions

- GCF describes the many-body nuclear wave-function where SRCs dominate.
- GCF offers prescription for SRC spectral functions.
- This allows us to calculate QE electron-scattering cross sections and other observables.
- QE electron scattering off SRC nucleons implemented in EIC generator from GCF.

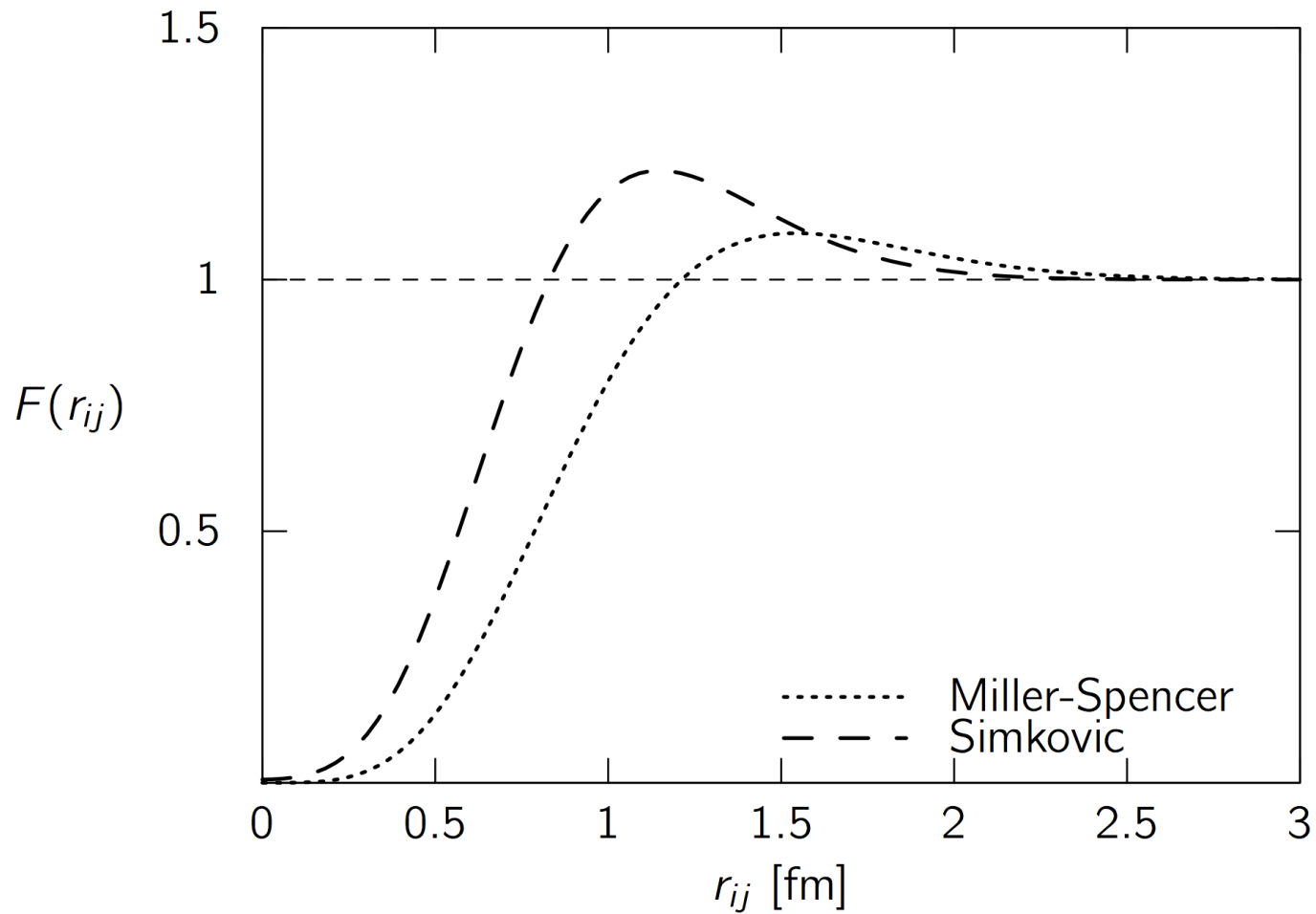


Thank you!



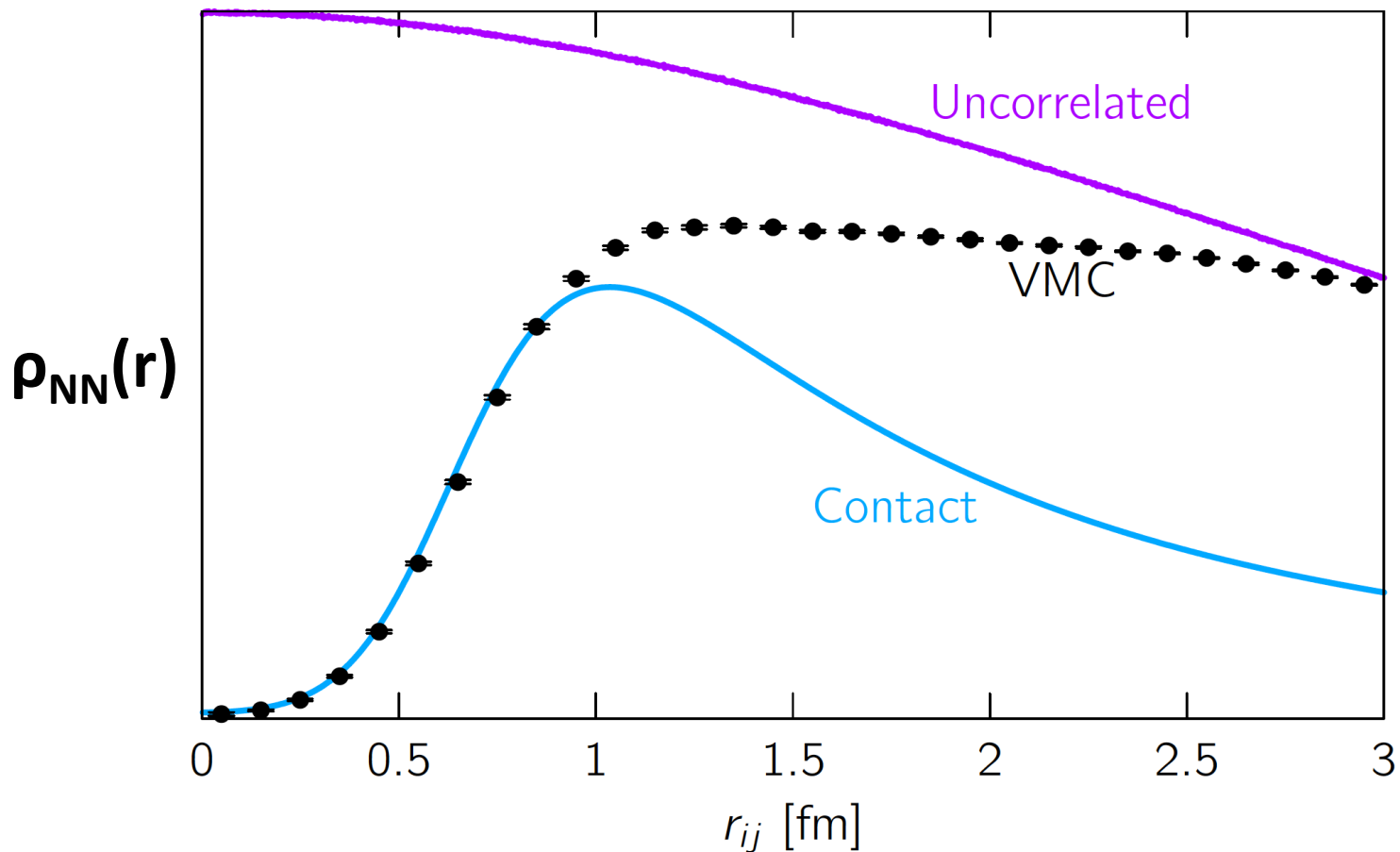
Backup

$$F(r) \equiv \frac{\text{Fully correlated}}{\text{Uncorrelated}}$$



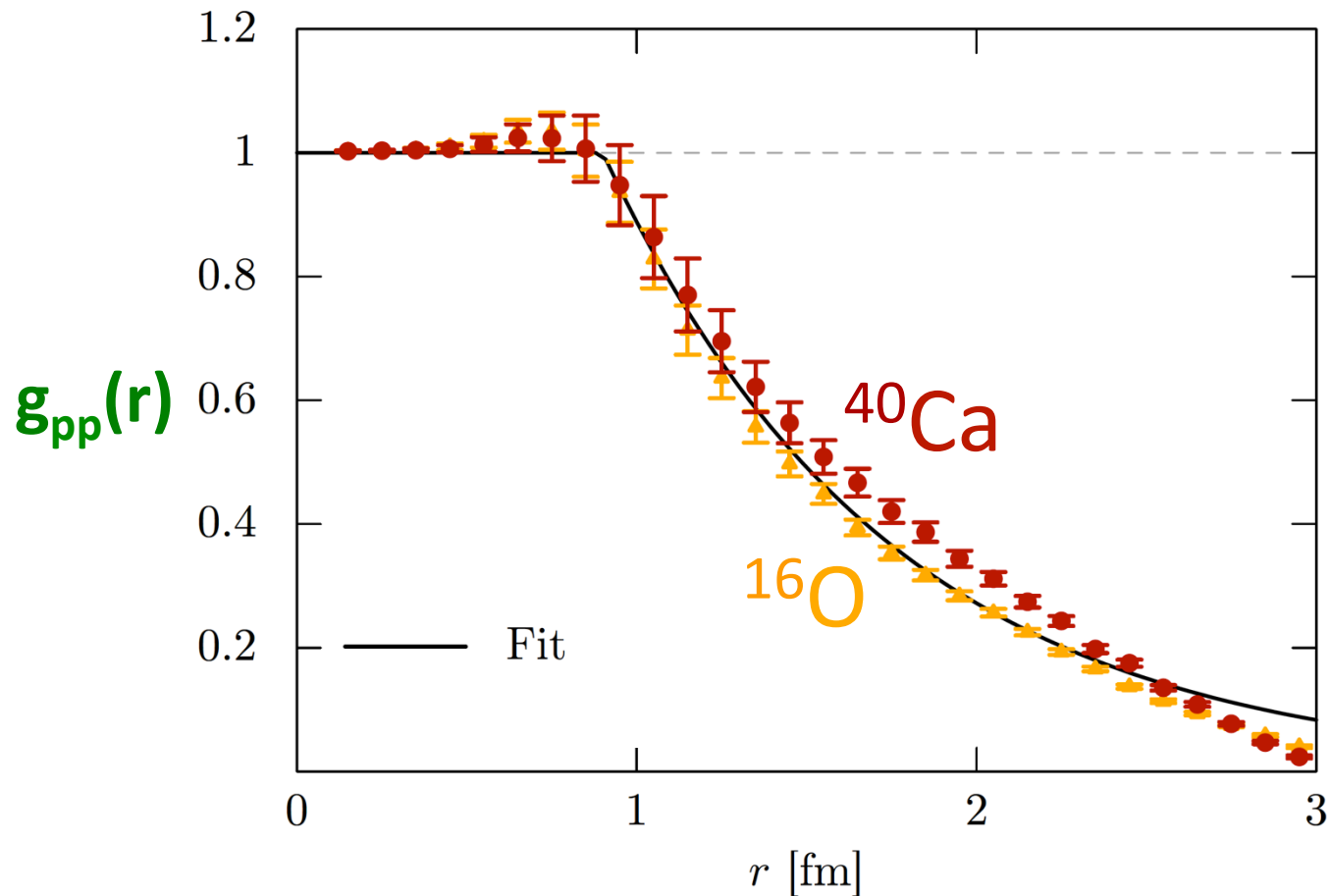
2 Component Blending Model

$$\rho_{NN}(r) = g_{NN}(r) \rho_{NN}^{(\text{contact})}(r) + \kappa(1 - g_{NN}(r)) \rho_{NN}^{(\text{Uncorrelated})}(r)$$

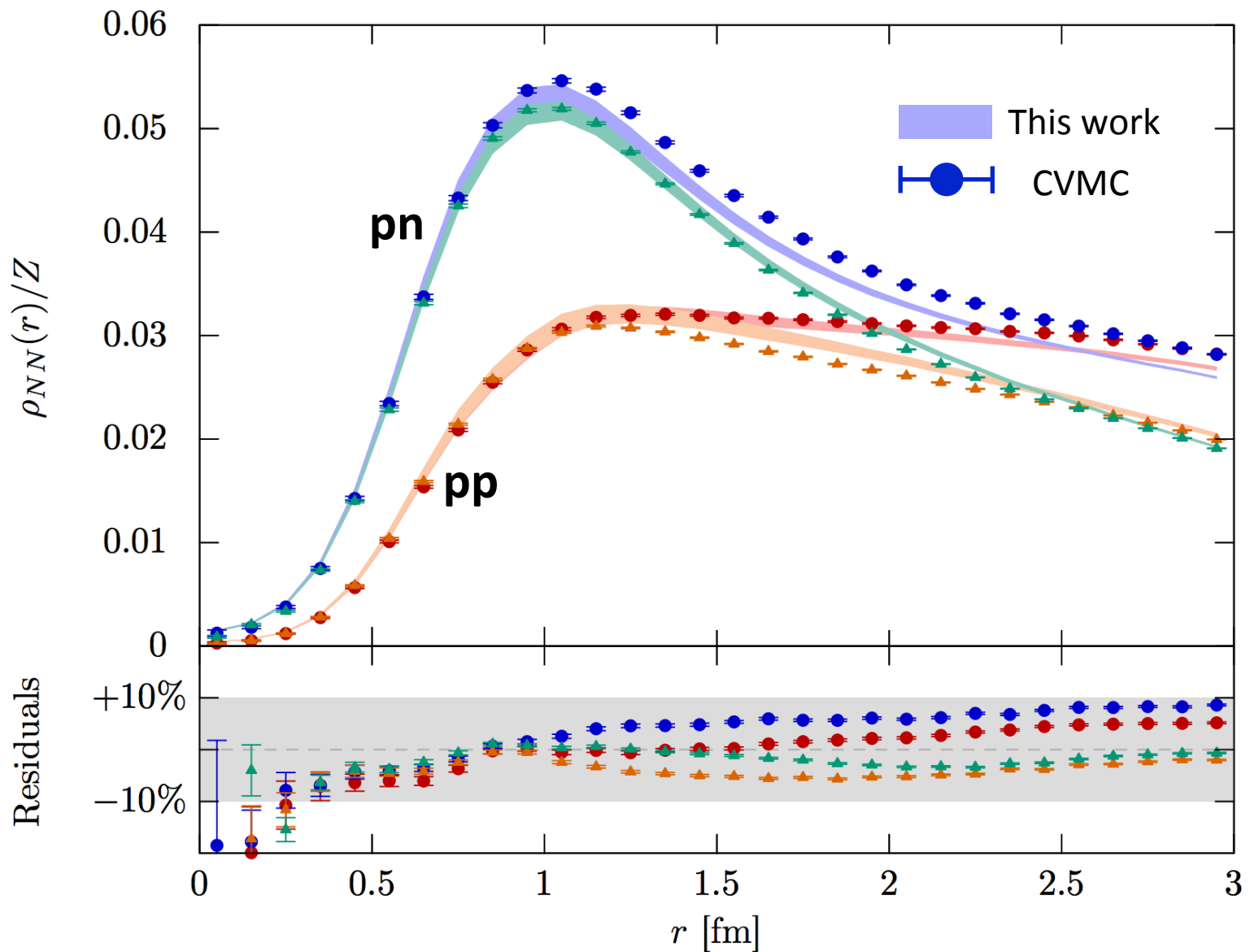


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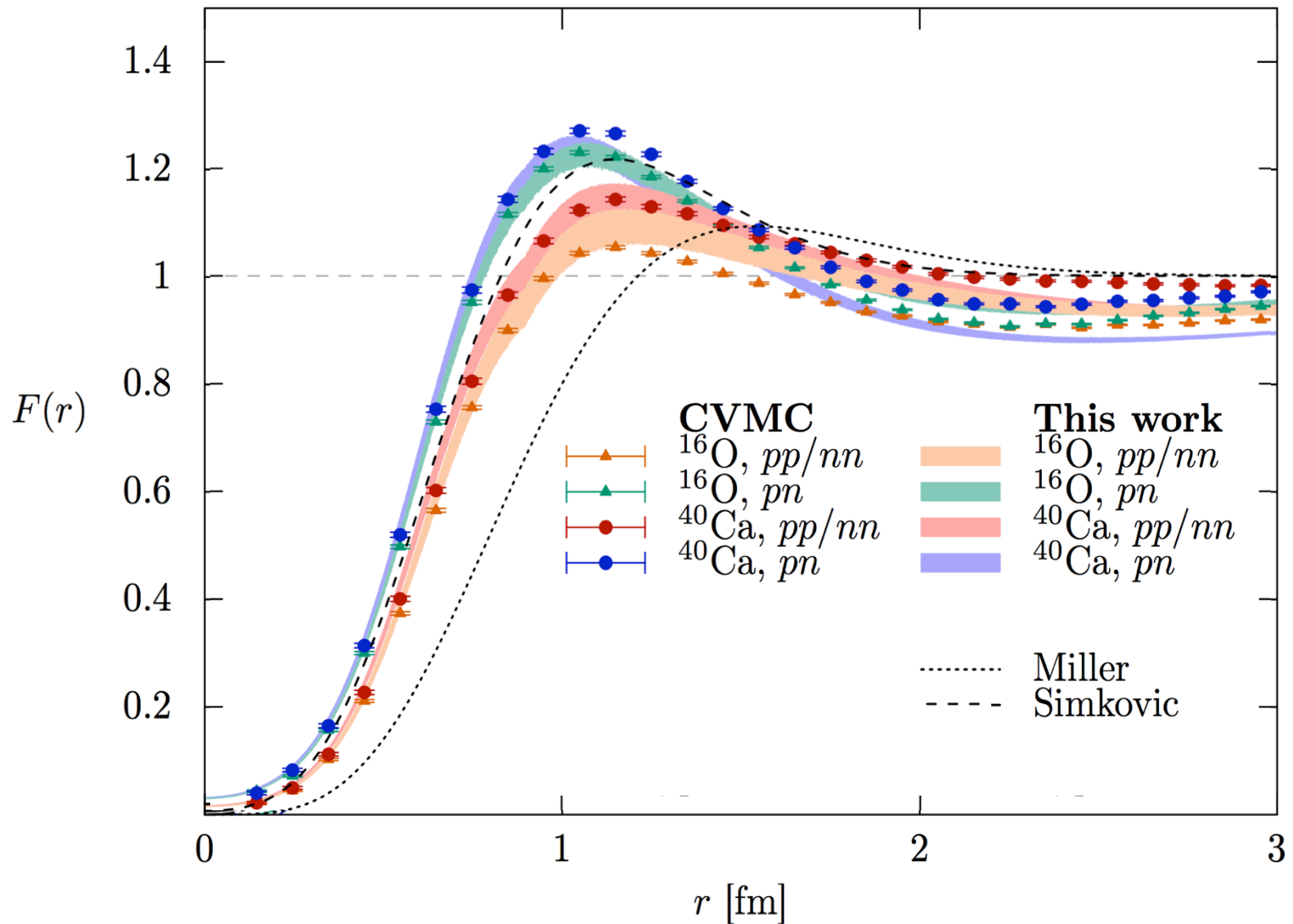
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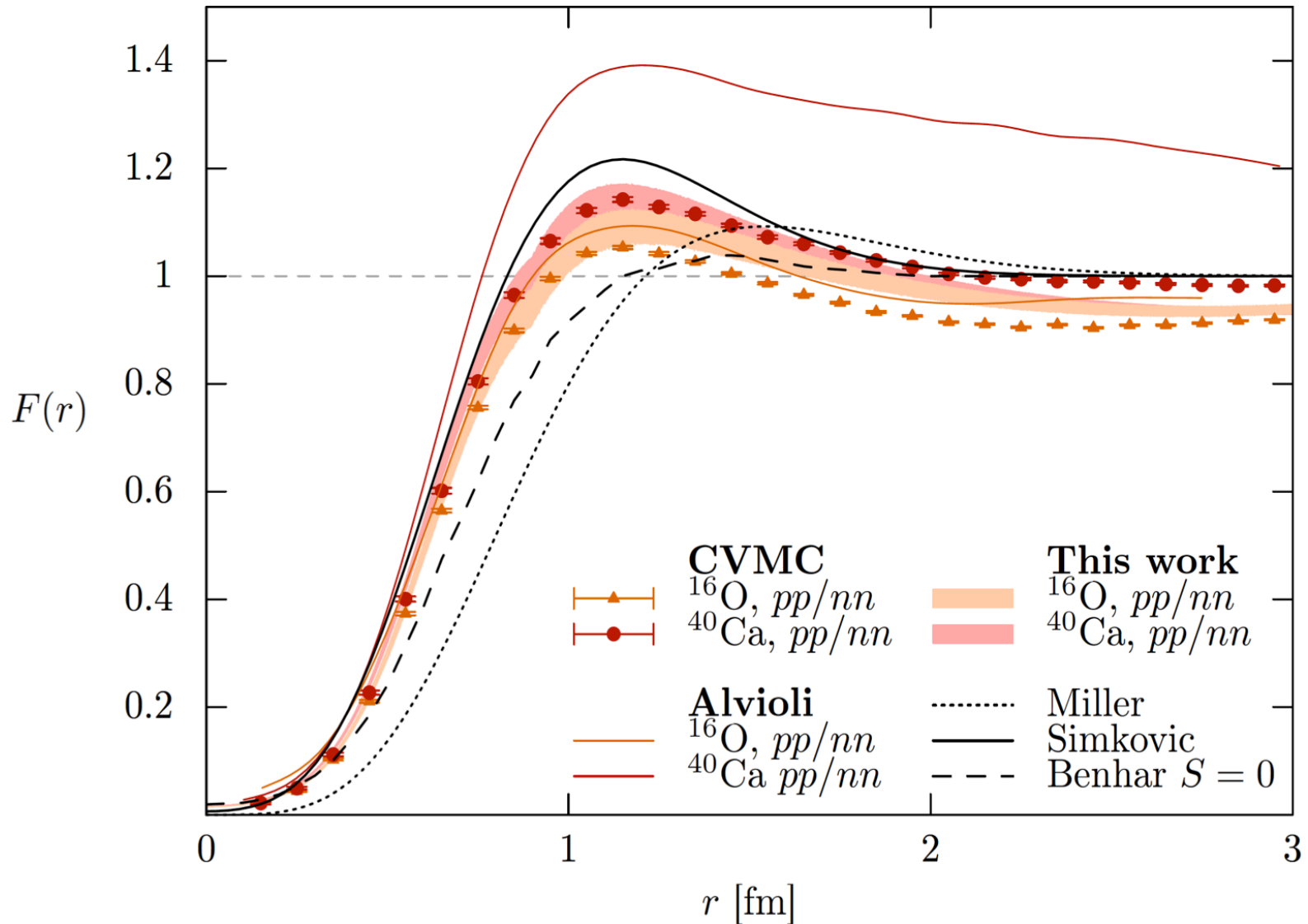
Test: 2-Body Density ($A = 16$ & 40)



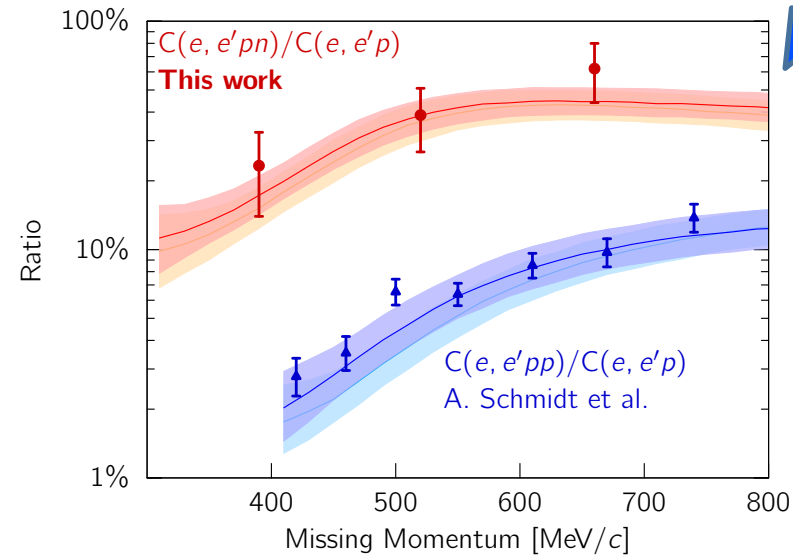
Correlation Functions



pp/nn Correlation Functions



$(e,e'pN)/(e,e'p)$ ratio



Inferred Strong Interaction Dynamics

