

Phenomenological Study of the Origin of SSAs and Extraction of the Tensor Charge



Daniel Pitonyak

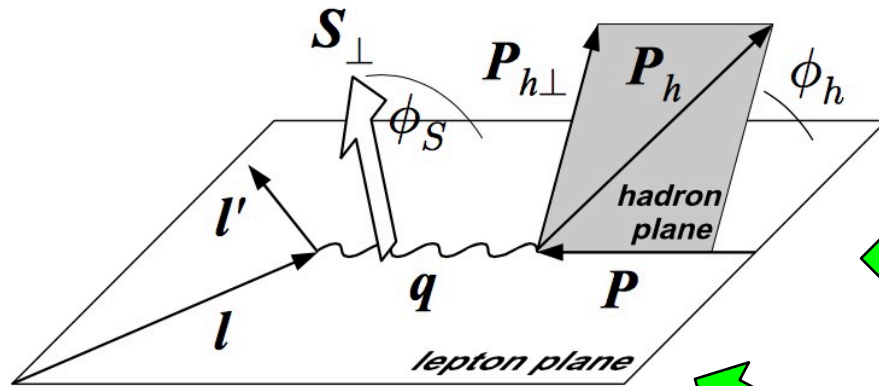
Lebanon Valley College, Annville, PA, USA



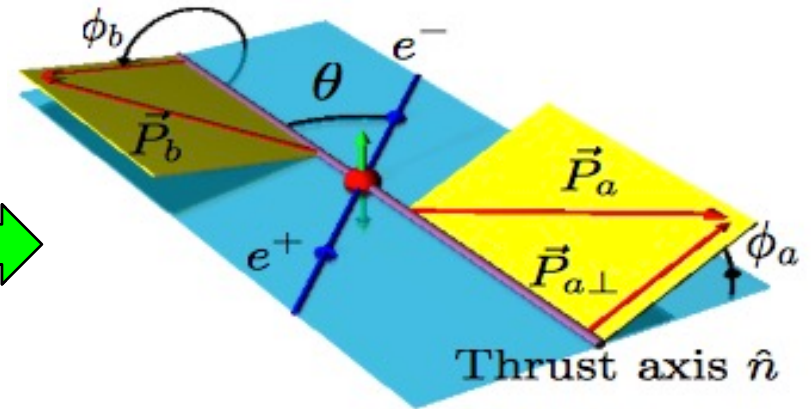
QCD Evolution Workshop

May 13, 2021

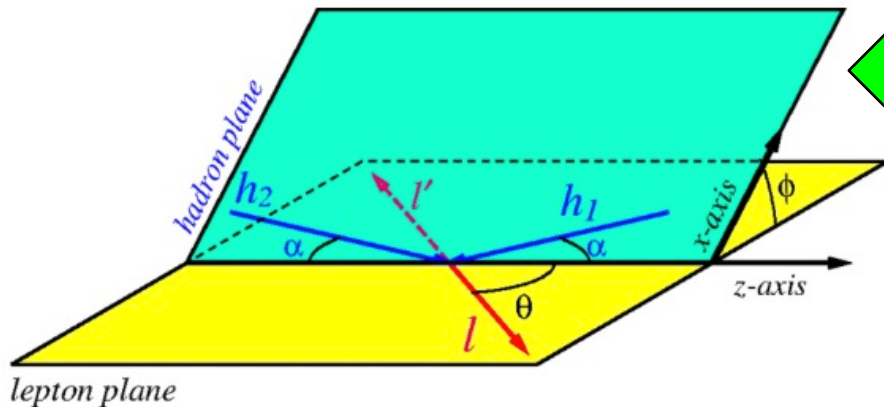
Cammarota, Gamberg, Kang, Miller, DP, Prokudin, Rogers, Sato, PRD **102** (2020)



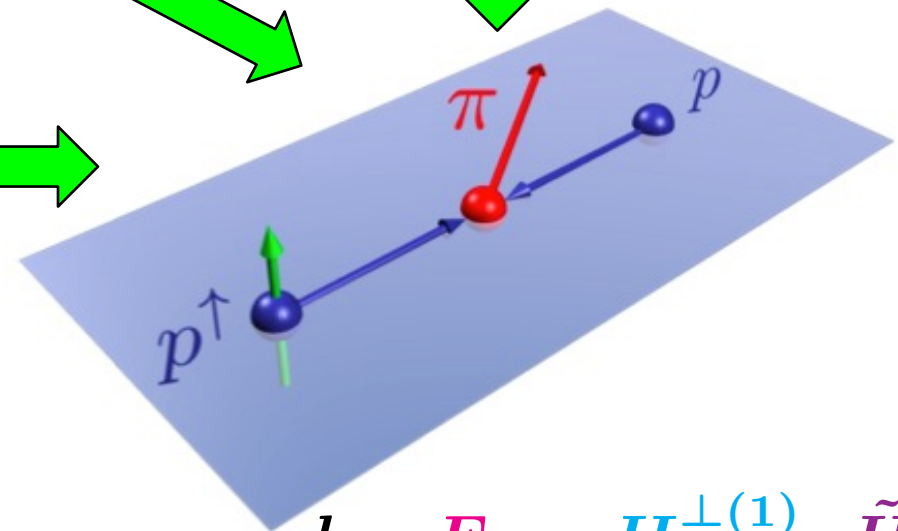
$h_1, F_{FT}, H_1^{\perp(1)}$



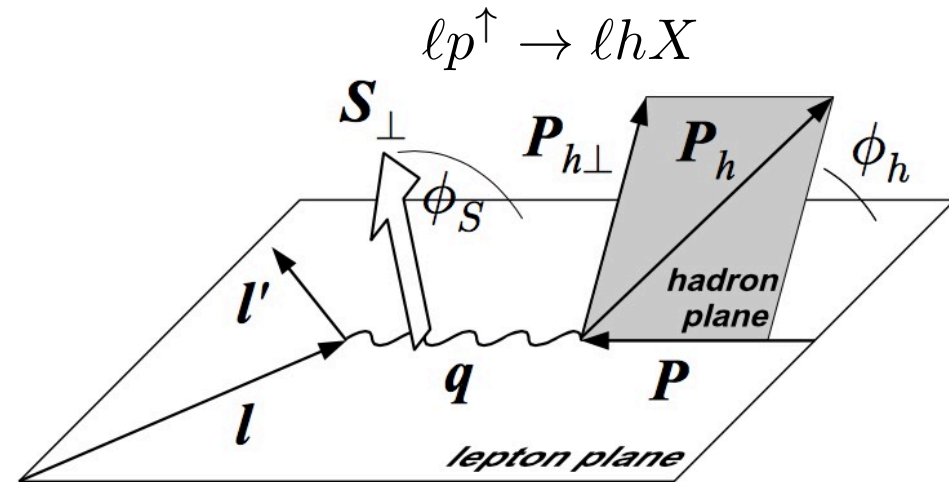
$H_1^{\perp(1)}$



F_{FT}

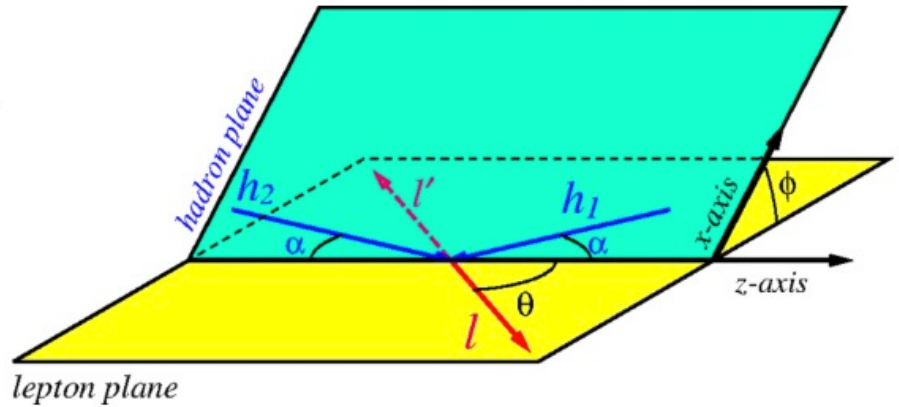


$h_1, F_{FT}, H_1^{\perp(1)}, \tilde{H}$



$$F_{UT}^{\sin(\phi_h - \phi_S)} = \mathcal{C} \left[-\frac{\hat{h} \cdot \vec{k}_T}{M} \mathbf{f}_{1T}^\perp D_1 \right]$$

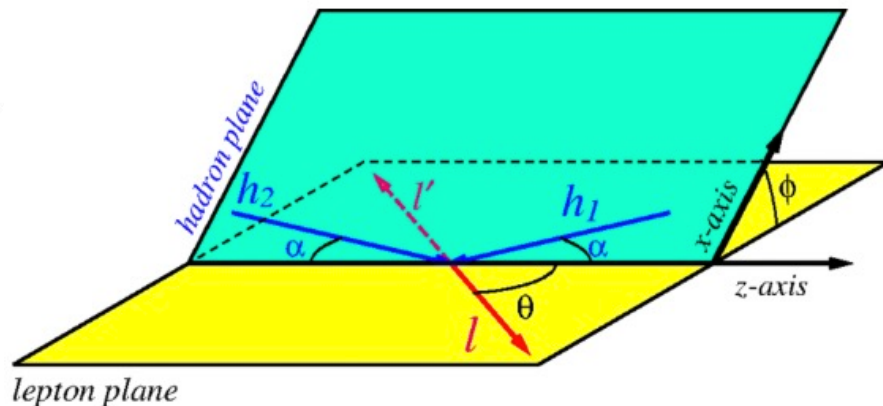
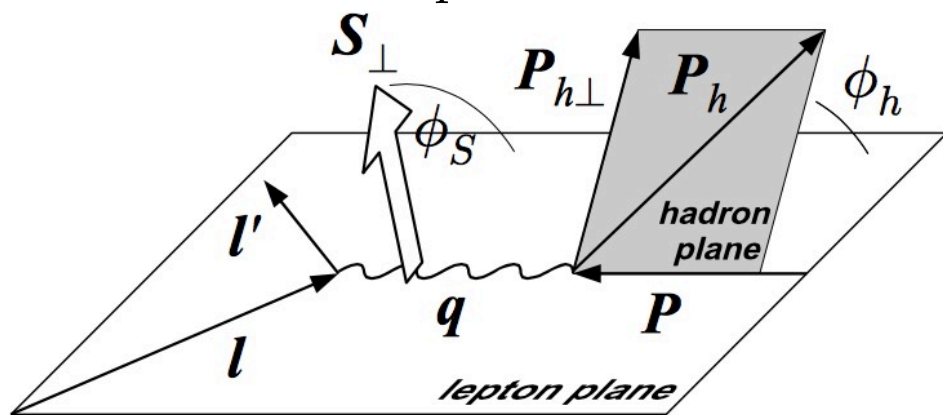
$$\{\pi, p\} p^\uparrow \rightarrow \{\ell^+ \ell^-, W^\pm, Z\} X$$



$$F_{TU}^{\sin \phi} = \mathcal{C} \left[-\frac{\hat{h} \cdot \vec{k}_{aT}}{M_a} \mathbf{f}_{1T}^\perp \bar{f}_1 \right]$$

$$\ell p^\uparrow \rightarrow \ell h X$$

$$\{\pi, p\} p^\uparrow \rightarrow \{\ell^+ \ell^-, W^\pm, Z\} X$$



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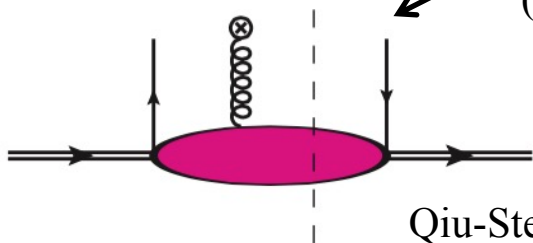
$$\tilde{f}_{1T}^{\perp(1)}(x, b_T; Q^2, \mu_Q) \sim F_{FT}(x, x; \mu_{b_*}) \exp \left[-S_{pert}(b_*(b_T); \mu_{b_*}, Q, \mu_Q) - S_{NP}^{f_{1T}^\perp}(b_T, Q) \right]$$

OPE

(NLO available from
Scimemi, Tarasov,
Vladimirov (2019))

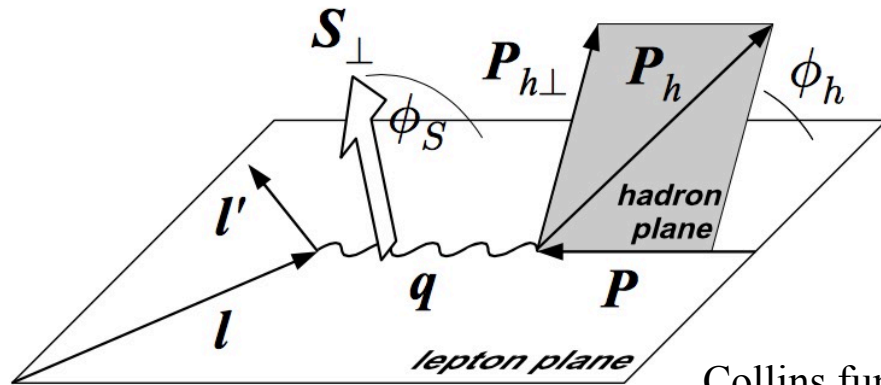
$$g_{f_{1T}^\perp}(x, b_T) + g_K(b_T) \ln(Q/Q_0)$$

(Aybat, et al. (2012); Echevarria, et al. (2014))



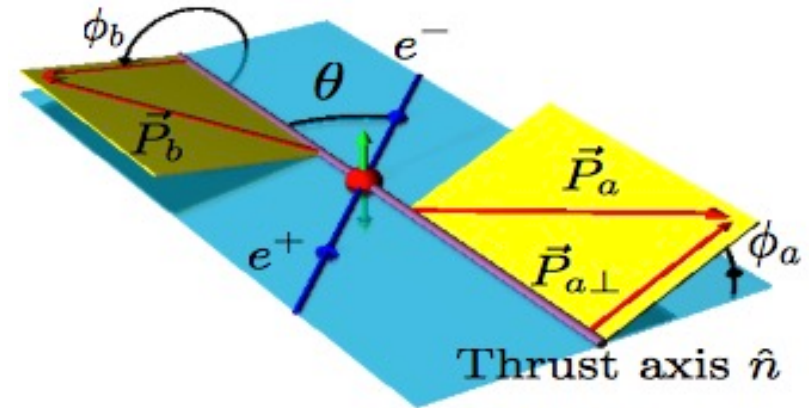
Qiu-Sterman
function

$$\ell p^\uparrow \rightarrow \ell h X$$



Collins function

$$e^+ e^- \rightarrow h_1 h_2 X$$



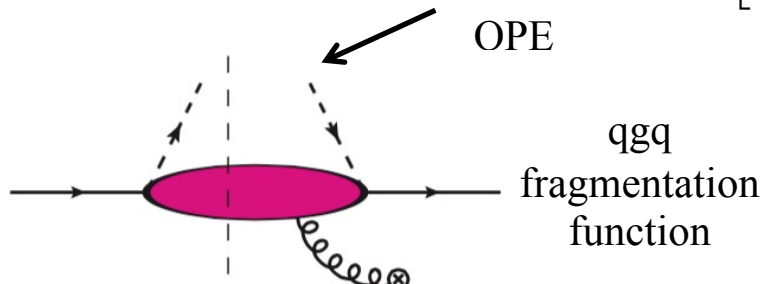
Thrust axis $\hat{n}$

$$F_{UT}^{\sin(\phi_h + \phi_S)} = C \left[-\frac{\hat{h} \cdot \vec{p}_\perp}{M_h} h_1 H_1^\perp \right] \quad F_{UU}^{\cos(2\phi_0)} = C \left[\frac{2\hat{h} \cdot \vec{p}_{a\perp} \hat{h} \cdot \vec{p}_{b\perp} - \vec{p}_{a\perp} \cdot \vec{p}_{b\perp}}{M_a M_b} H_1^\perp \bar{H}_1^\perp \right]$$

$$\tilde{h}_1(x, b_T; Q^2, \mu_Q) \sim h_1(x; \mu_{b_*}) \exp[-S_{pert}(b_*(b_T); \mu_{b_*}, Q, \mu_Q) - S_{NP}^{h_1}(b_T, Q)]$$

$$\tilde{H}_1^{\perp(1)}(z, b_T; Q^2, \mu_Q) \sim H_1^{\perp(1)}(z; \mu_{b_*}) \exp[-S_{pert}(b_*(b_T); \mu_{b_*}, Q, \mu_Q) - S_{NP}^{H_1^\perp}(b_T, Q)]$$

OPE



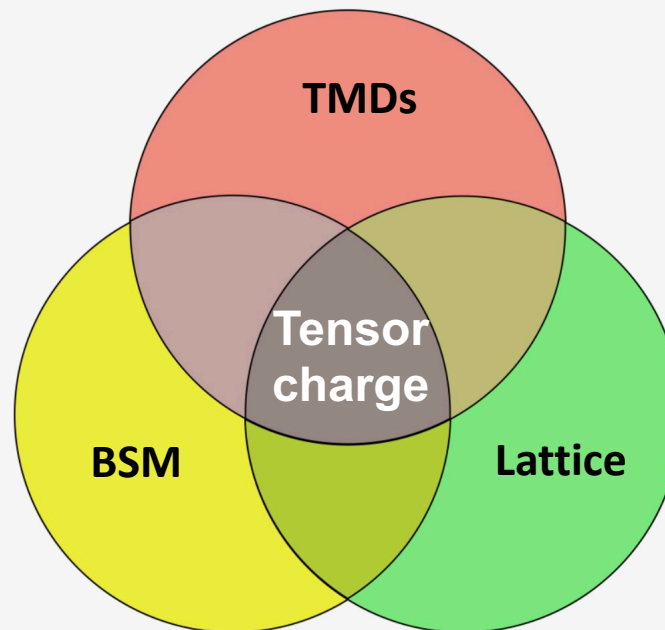
(Kang, et al. (2016))

$$\delta q \equiv \int_0^1 dx [h_1^q(x) - h_1^{\bar{q}}(x)] \quad g_T \equiv \delta u - \delta d$$

The tensor charge of the nucleon is one of its fundamental charges and is important for BSM studies in, e.g., beta decays (Gonzalez-Alonso, et al. (2018),...)

Processes sensitive to TMDs can play an important role in these efforts (Courtoy, et al. (2015); Yamanaka, et al. (2017), Liu, et al. (2018),...)

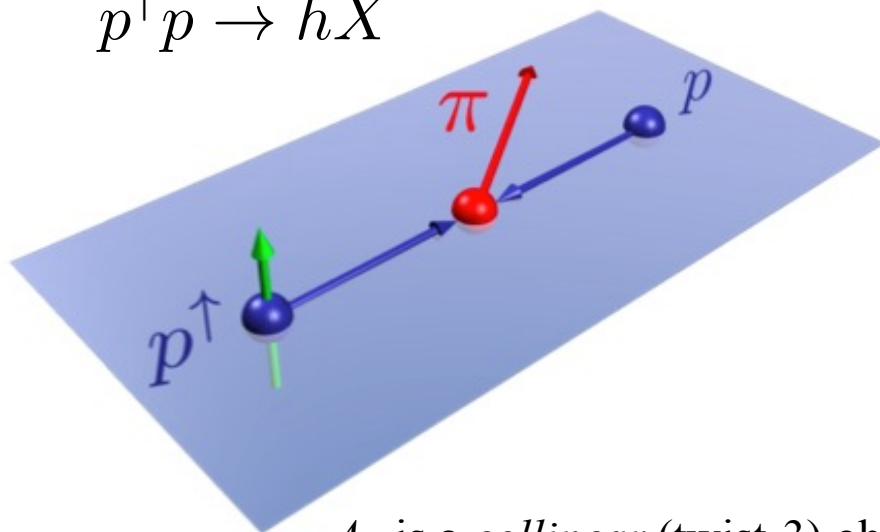
Lattice QCD has also calculated the tensor charges with great precision (Gupta, et al. (2018); Hasan, et al. (2019), Alexandrou, et. (2019),...)



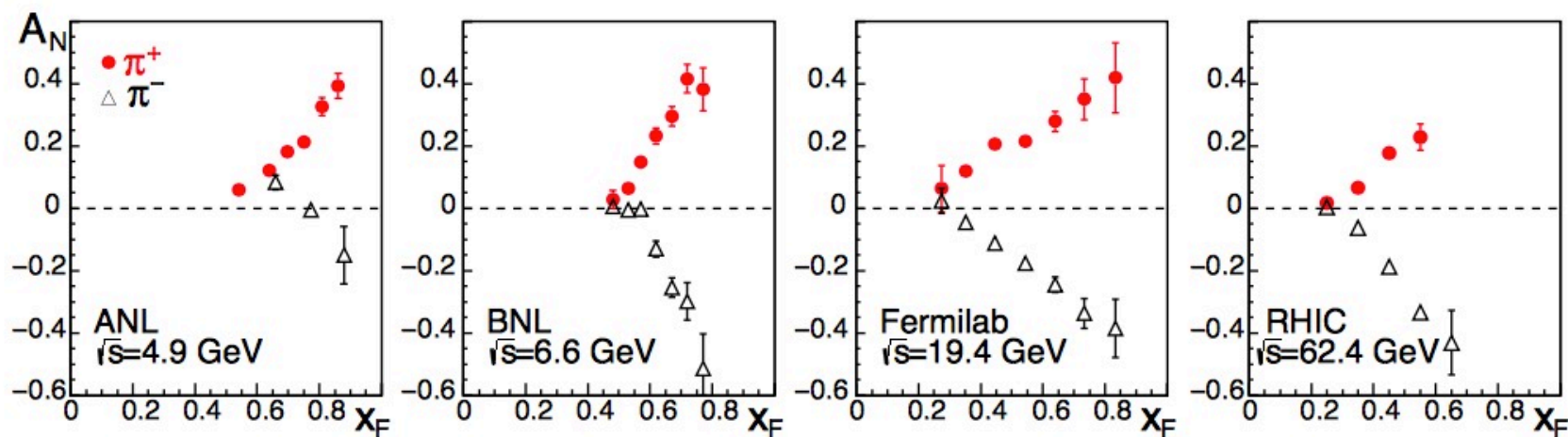
$$p^\uparrow p \rightarrow hX$$

$$d\Delta\sigma(S_T) \sim \underbrace{H_{QS} \otimes f_1 \otimes \mathbf{F}_{FT} \otimes D_1}_{\text{Qiu-Sterman term}}$$

$$+ \underbrace{H_F \otimes f_1 \otimes \mathbf{h}_1 \otimes \left(\mathbf{H}_1^{\perp(1)}, \tilde{\mathbf{H}} \right)}_{\text{Fragmentation term}}$$

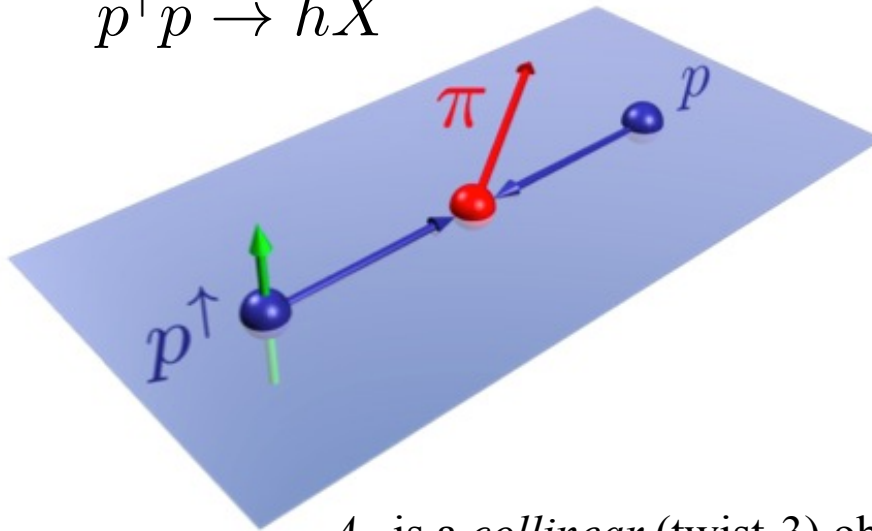


A_N is a *collinear* (twist-3) observable



1976 →

$$p^\uparrow p \rightarrow hX$$

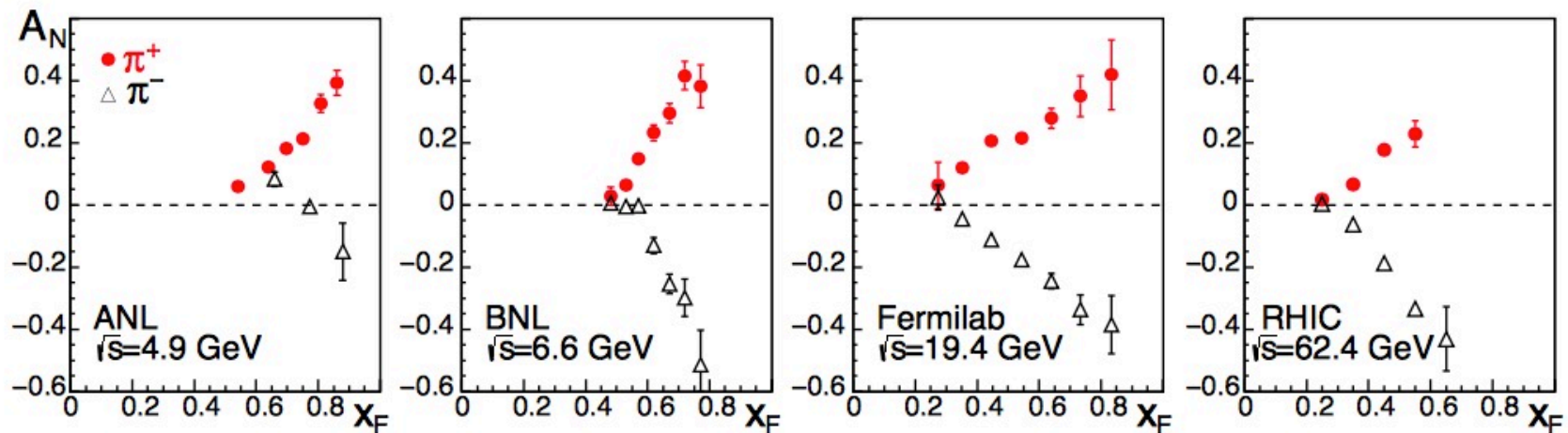


$$d\Delta\sigma(S_T) \sim \underbrace{H_{QS} \otimes f_1 \otimes \mathbf{F}_{FT} \otimes D_1}_{\text{Qiu-Sterman term}}$$

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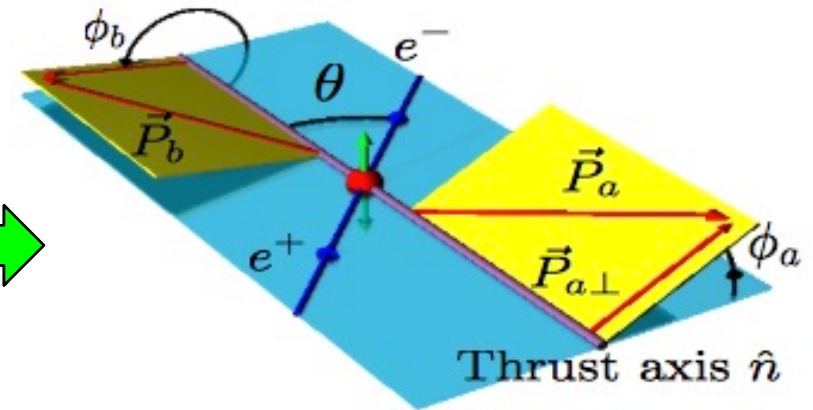
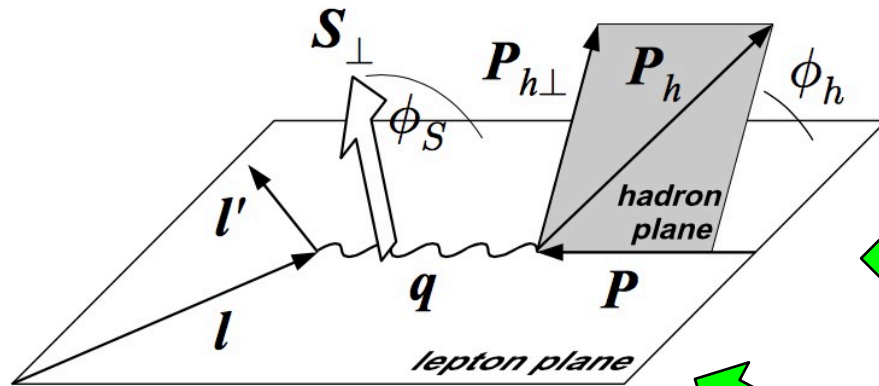
(Metz, DP (2012); Kanazawa, et al. (2014);
Gamberg, et al. (2017); Cammarota, et al. (2020))

A_N is a *collinear* (twist-3) observable



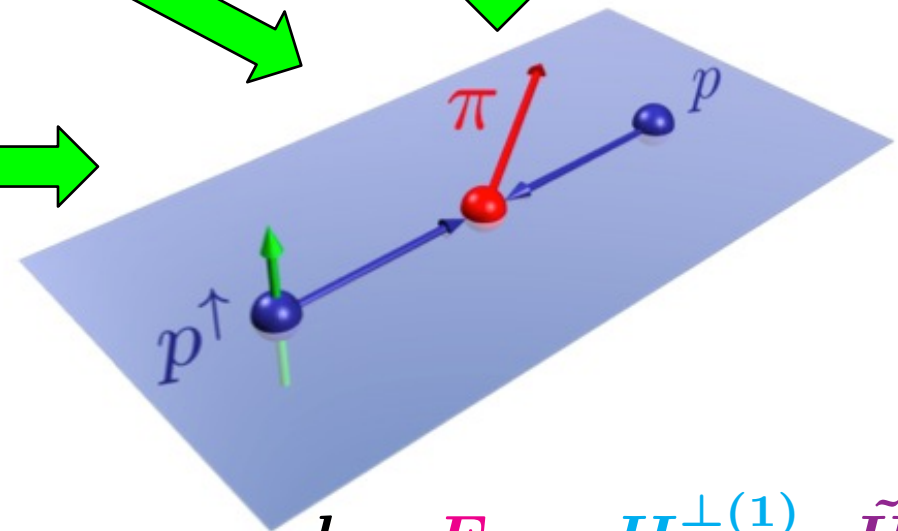
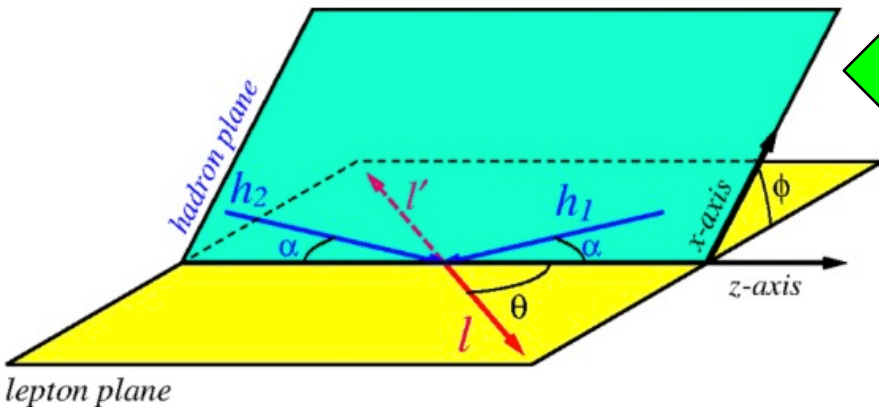
1976 →

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$h_1, F_{FT}, H_1^{\perp(1)}$

$H_1^{\perp(1)}$



F_{FT}

$h_1, F_{FT}, H_1^{\perp(1)}, \tilde{H}$

- We have performed the first global analysis of SSAs in SIDIS, Drell-Yan, e^+e^- annihilation, and proton-proton collisions and extracted a universal set of non-perturbative functions

$$h_1(x), F_{FT}(x, x), H_1^{\perp(1)}(z), \hat{H}(z) \quad \text{noise in the fit – need } A_{UT}^{\sin \phi_S}$$

along with the relevant transverse momentum widths for the Sivers, transversity, and Collins functions: $\langle k_T^2 \rangle_{f_1^\perp}, \langle k_T^2 \rangle_{h_1}, \langle p_\perp^2 \rangle_{H_1^\perp}^{fav}, \langle p_\perp^2 \rangle_{H_1^\perp}^{unf}$

- We use a Gaussian ansatz: $F(x, k_T^2) \sim F(x) e^{-k_T^2 / \langle k_T^2 \rangle}$ where

$$F^q(x) = \frac{N_q x^{a_q} (1-x)^{b_q} (1 + \gamma_q x^{\alpha_q} (1-x)^{\beta_q})}{B[a_q+2, b_q+1] + \gamma_q B[a_q+\alpha_q+2, b_q+\beta_q+1]}$$

NB: $\{\gamma, \alpha, \beta\}$ only used for Collins function

- DGLAP-type evolution for the collinear functions analogous to Duke & Owens (1984): double-log Q^2 -dependent term explicitly added to the parameters

Observable	Reactions	Non-Perturbative Function(s)	$\chi^2/N_{\text{pts.}}$
$A_{\text{SIDIS}}^{\text{Siv}}$	$e + (p, d)^{\uparrow} \rightarrow e + (\pi^+, \pi^-, \pi^0) + X$	$f_{1T}^{\perp}(x, k_T^2)$	150.0/126 = 1.19
$A_{\text{SIDIS}}^{\text{Col}}$	$e + (p, d)^{\uparrow} \rightarrow e + (\pi^+, \pi^-, \pi^0) + X$	$h_1(x, k_T^2), H_1^{\perp}(z, z^2 p_{\perp}^2)$	111.3/126 = 0.88
$A_{\text{SIA}}^{\text{Col}}$	$e^+ + e^- \rightarrow \pi^+ \pi^- (UC, UL) + X$	$H_1^{\perp}(z, z^2 p_{\perp}^2)$	154.5/176 = 0.88
$A_{\text{DY}}^{\text{Siv}}$	$\pi^- + p^{\uparrow} \rightarrow \mu^+ \mu^- + X$	$f_{1T}^{\perp}(x, k_T^2)$	5.96/12 = 0.50
$A_{\text{DY}}^{\text{Siv}}$	$p^{\uparrow} + p \rightarrow (W^+, W^-, Z) + X$	$f_{1T}^{\perp}(x, k_T^2)$	31.8/17 = 1.87
A_N^h	$p^{\uparrow} + p \rightarrow (\pi^+, \pi^-, \pi^0) + X$	$h_1(x), F_{FT}(x, x) = \frac{1}{\pi} f_{1T}^{\perp(1)}(x), H_1^{\perp(1)}(z)$	66.5/60 = 1.11

- 18 observables and 6 non-perturbative functions (Sivers up/down; transversity up/down; Collins favored/unfavored)

**Test of
universality!**

- Broad kinematical coverage:

$$\text{SIDIS: } x \lesssim 0.3 \quad 0.2 \lesssim z \lesssim 0.6 \quad 2 \lesssim Q^2 \lesssim 40 \text{ GeV}^2$$

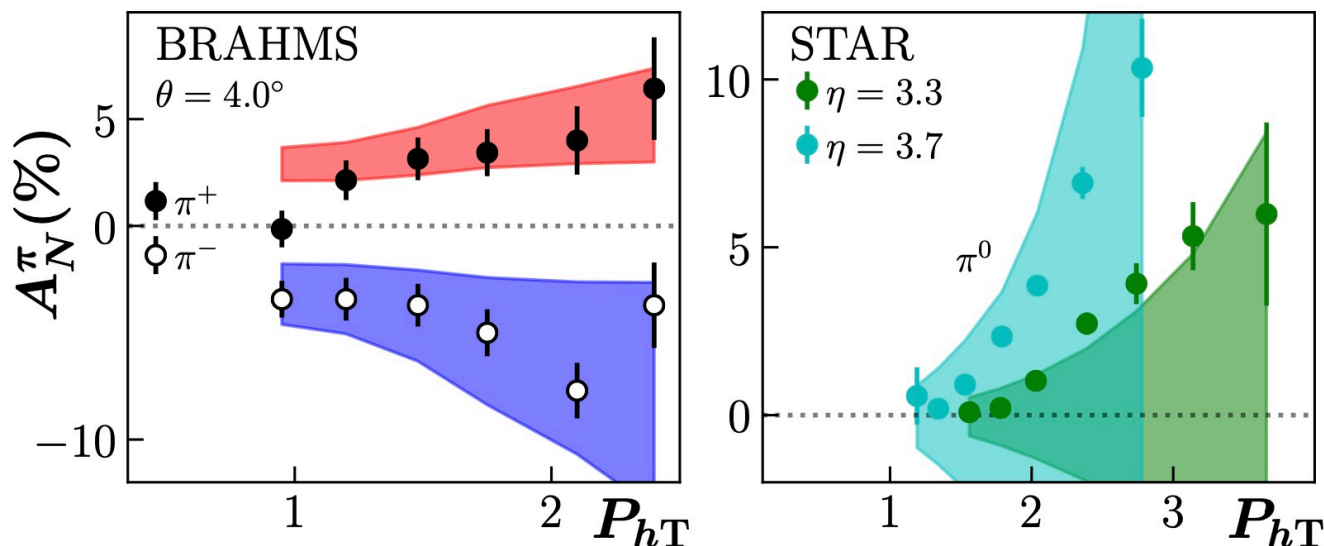
$$\text{SIA: } 0.2 \lesssim z \lesssim 0.8 \quad Q^2 \approx 13 \text{ GeV}^2 \text{ or } 110 \text{ GeV}^2$$

$$\text{DY: } 0.1 \lesssim x \lesssim 0.35 \quad Q^2 \approx 30 \text{ GeV}^2 \text{ or } (80 \text{ GeV})^2$$

$$A_N^h: 0.2 \lesssim (x_{\min}, z_{\min}) \lesssim 0.7 \quad 1 \lesssim Q^2 \lesssim 13 \text{ GeV}^2$$

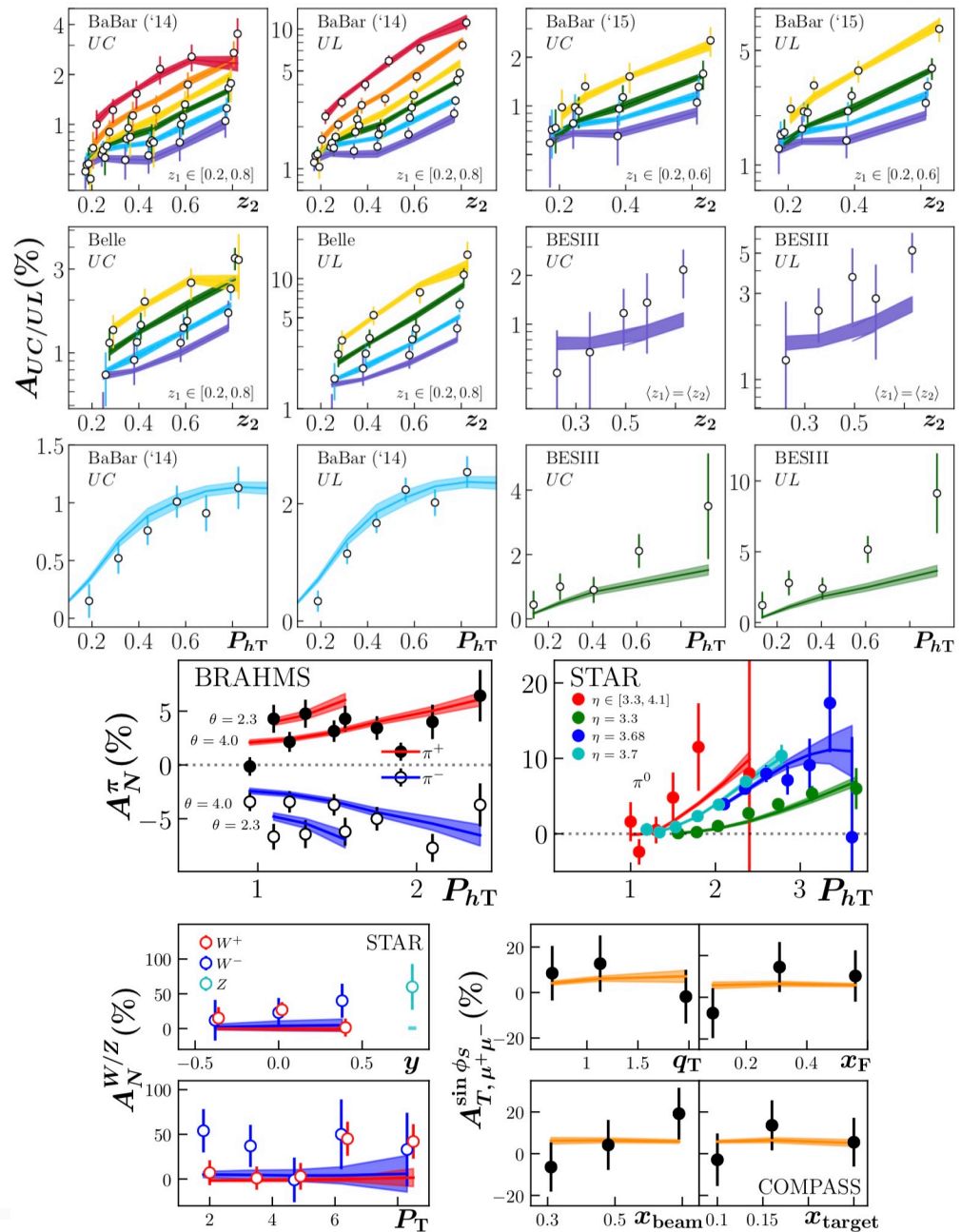
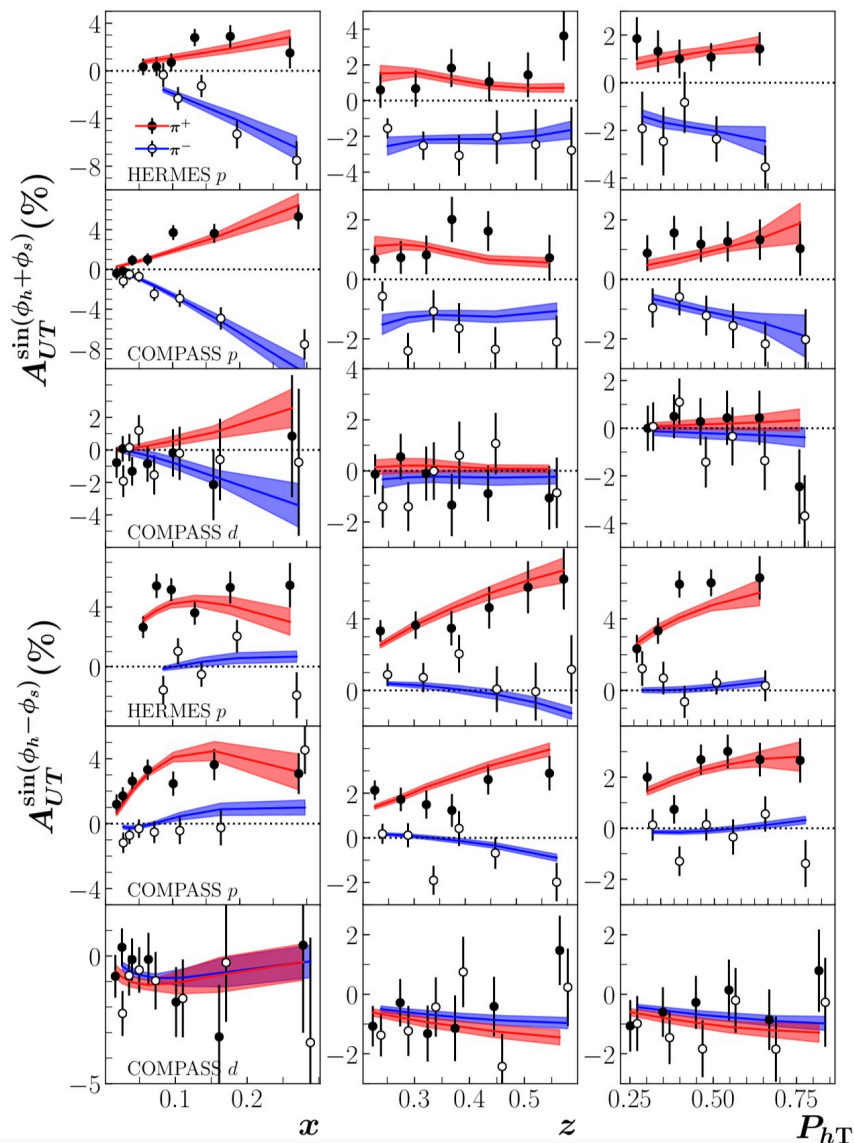
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$A_{\text{SIDIS}}^{\text{Col}}$	$e + (p, d)^{\uparrow} \rightarrow e + (\pi^+, \pi^-, \pi^0) + X$	$h_1(x, k_T^2), H_1^{\perp}(z, z^2 p_{\perp}^2)$	111.3/126 = 0.88
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➤ Predictions of A_N using a fit of only TMD observables

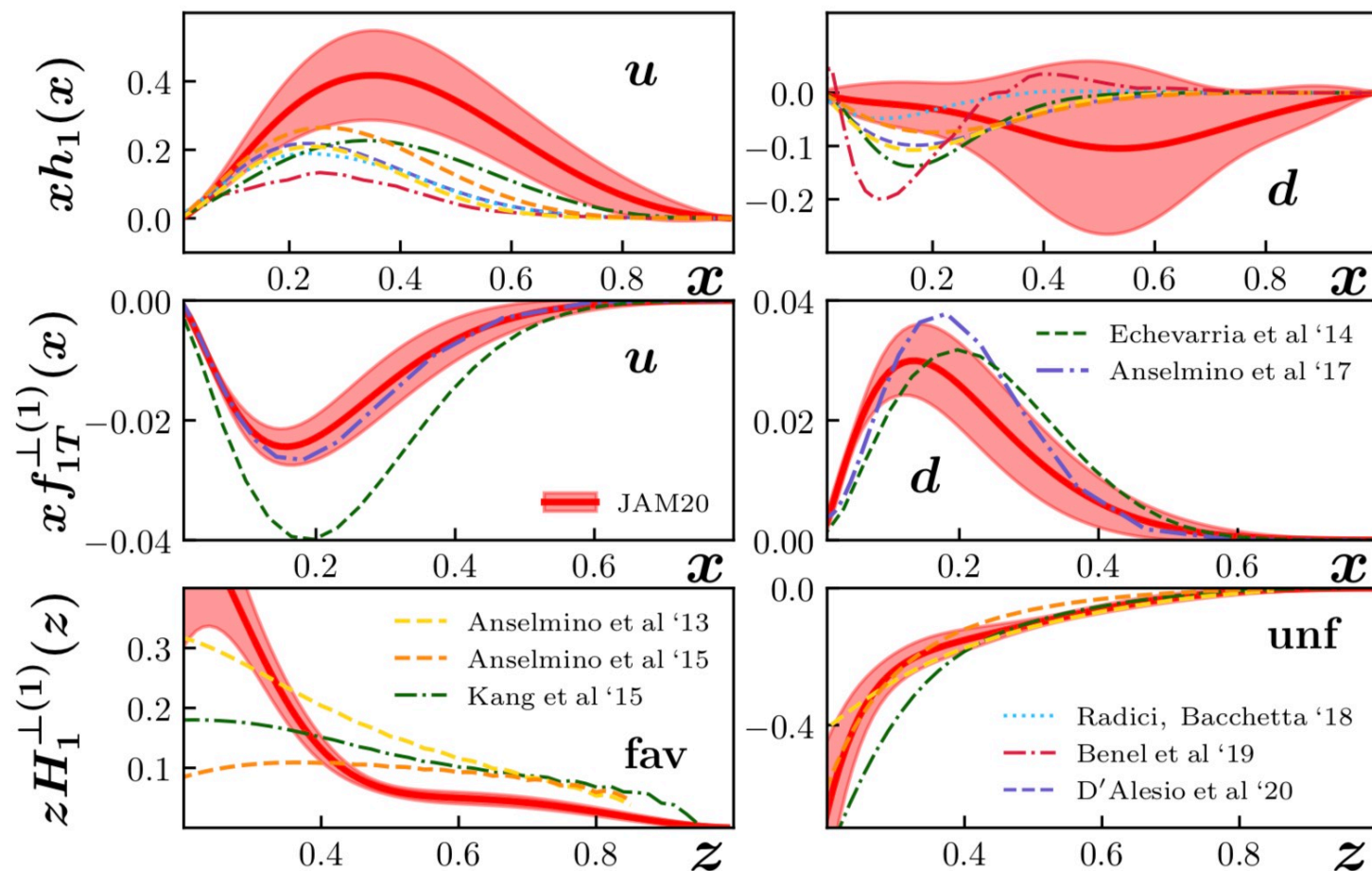


**Test of
universality!**

$$\chi^2/N_{\text{pts.}} = 520/517 = 1.01$$



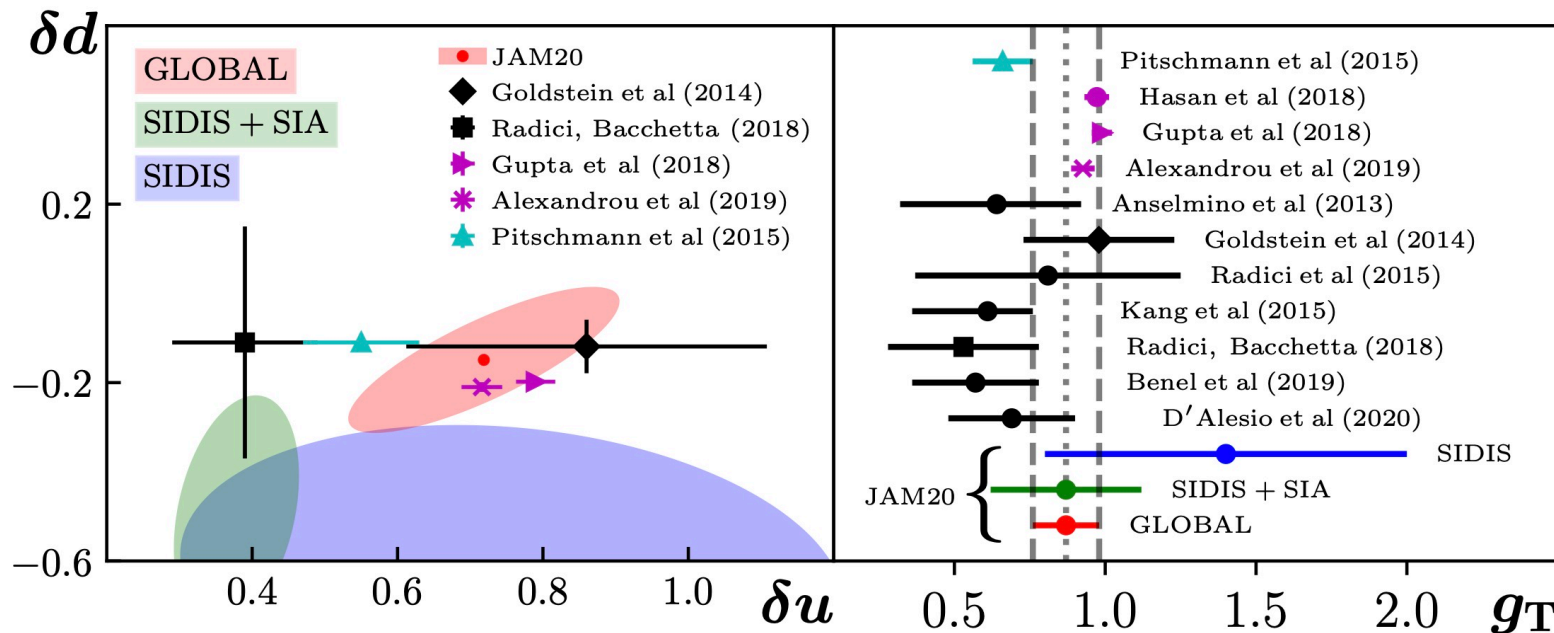
JAM3D



Transversity

Sivers first moment
(QS function)

Collins first moment



Cammarota, Gamberg, Kang, Miller, DP, Prokudin, Rogers, Sato, PRD **102** (2020)

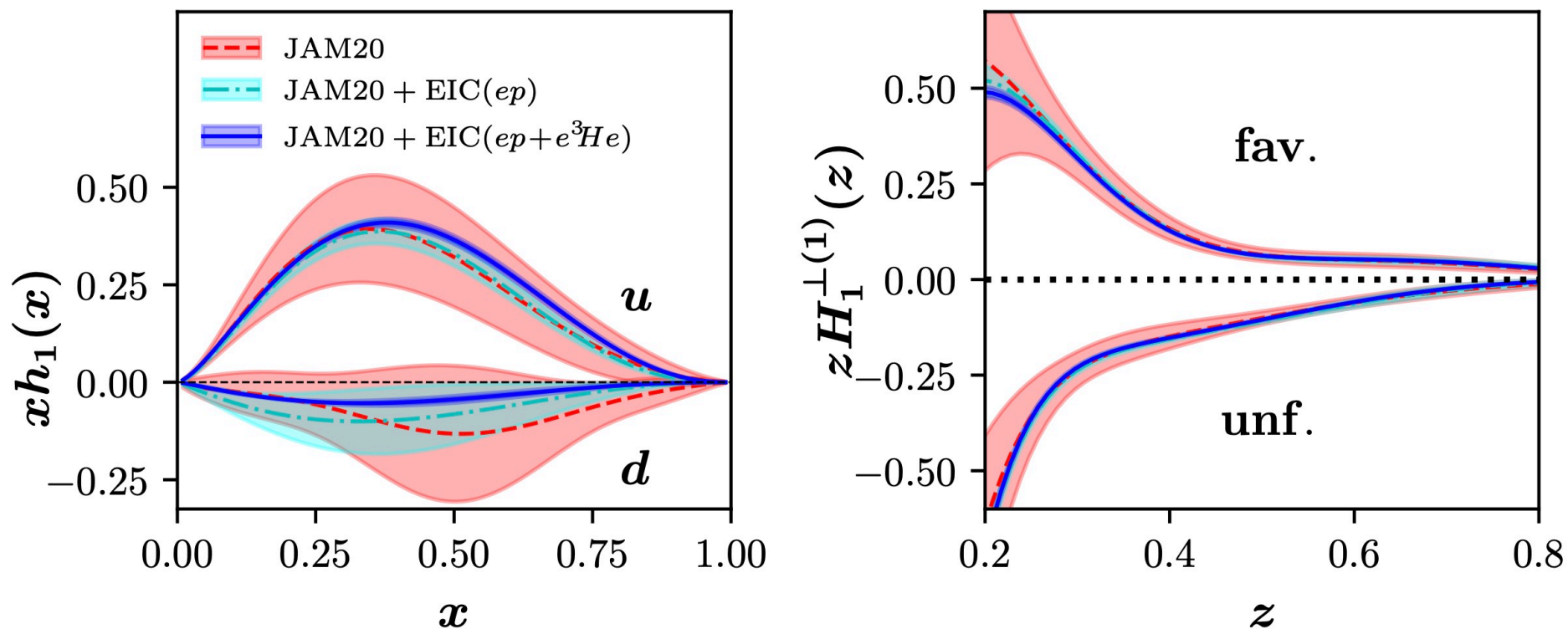
Only after a *simultaneous* QCD global analysis of SSAs does the phenomenological extraction of the tensor charges agree with lattice, *but still with large uncertainties*.

Gamberg, Kang, DP, Prokudin, Sato, Seidl, PLB **816** (2021)

EIC Pseudo-data			
Observable	Reactions	CM Energy ($\sqrt{s}$)	$N_{\text{pts.}}$
Collins (SIDIS)	$e + p^\uparrow \rightarrow e + \pi^\pm + X$	141 GeV	756 (π^+) 744 (π^-)
		63 GeV	634 (π^+) 619 (π^-)
		45 GeV	537 (π^+) 556 (π^-)
		29 GeV	464 (π^+) 453 (π^-)
	$e + {}^3\text{He}^\uparrow \rightarrow e + \pi^\pm + X$	85 GeV	647 (π^+) 650 (π^-)
		63 GeV	622 (π^+) 621 (π^-)
		29 GeV	461 (π^+) 459 (π^-)
	Total EIC $N_{\text{pts.}}$		8223

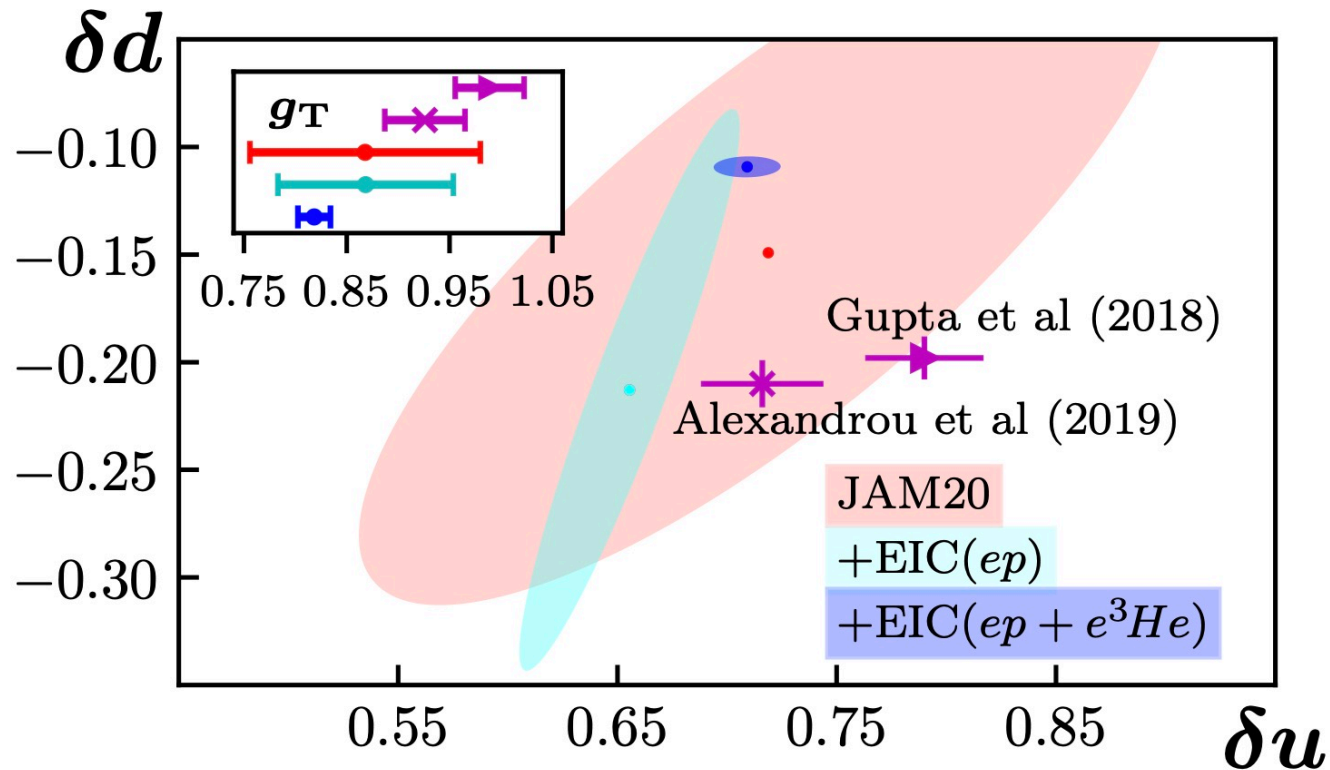
Assumed accumulated luminosities of 10 fb^{-1} , 70% polarization, conservatively accounted for detector smearing and acceptance effects

Gamberg, Kang, DP, Prokudin, Sato, Seidl, PLB **816** (2021)



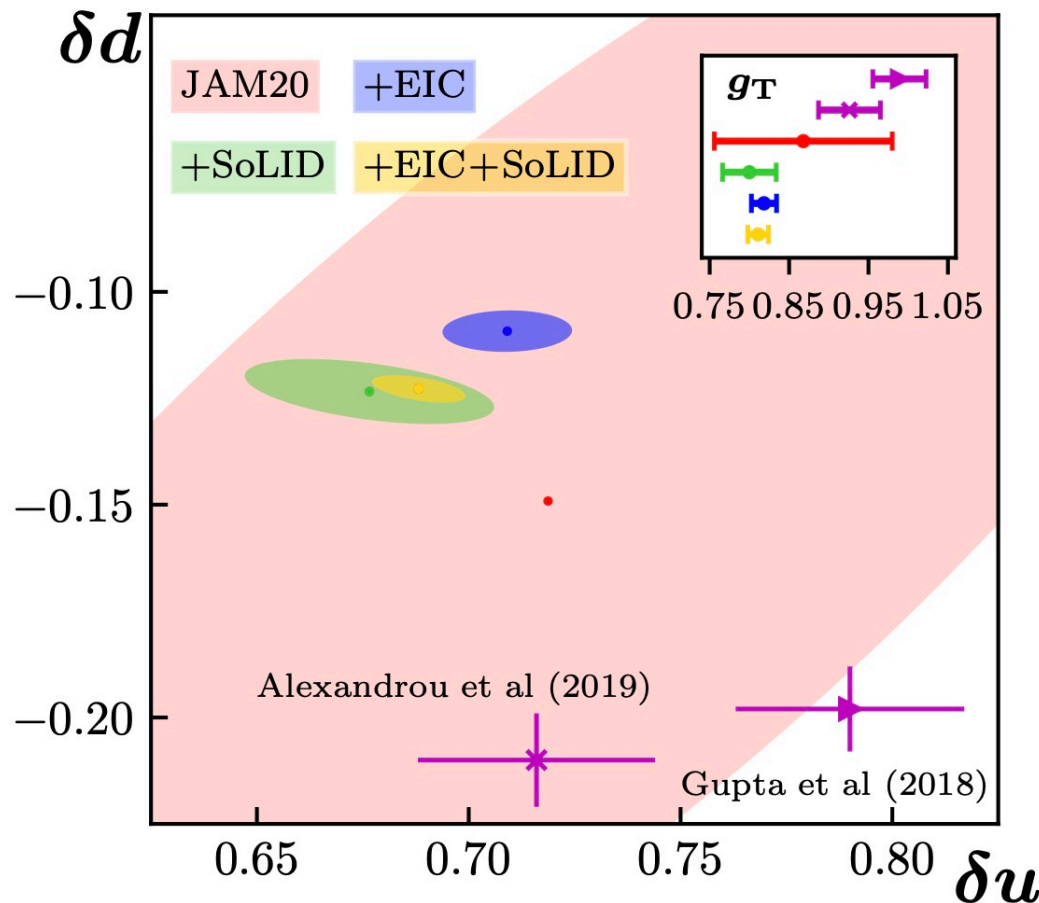
EIC data on the Collins effect will significantly reduce the uncertainties in extractions of the transversity PDF (as well as the Collins FF)

Gamberg, Kang, DP, Prokudin, Sato, Seidl, PLB **816** (2021)



EIC data will allow phenomenological extractions of the tensor charge to become as precise as current lattice calculations. ^3He data is especially important to decorrelate the extraction of δu and δd .

Gamberg, Kang, DP, Prokudin, Sato, Seidl, PLB **816** (2021)



SoLID at JLab will also provide important constraints on the tensor charges. The combined analysis with EIC data gives the most precise phenomenological determination of them.

- We have performed the first global analysis of SSAs in SIDIS, DY, e^+e^- annihilation, and proton-proton collisions and extracted a universal set of non-perturbative functions, showing a common origin of SSAs.
- First agreement with lattice QCD on the tensor charges of the nucleon was obtained, but still with large uncertainties.
- EIC data on the Collins effect will allow for phenomenological extractions of the tensor charge to be as precise as current lattice calculations. SoLID at JLab will also provide important constraints.