

$$\Delta \ln P_i = \frac{\partial \ln P_i}{\partial \ln P_j^{\text{init}}} \Delta \ln P_j^{\text{init}} = G_{ij} \Delta \ln P_j^{\text{init}}$$