

Lido for inclusive jet analysis

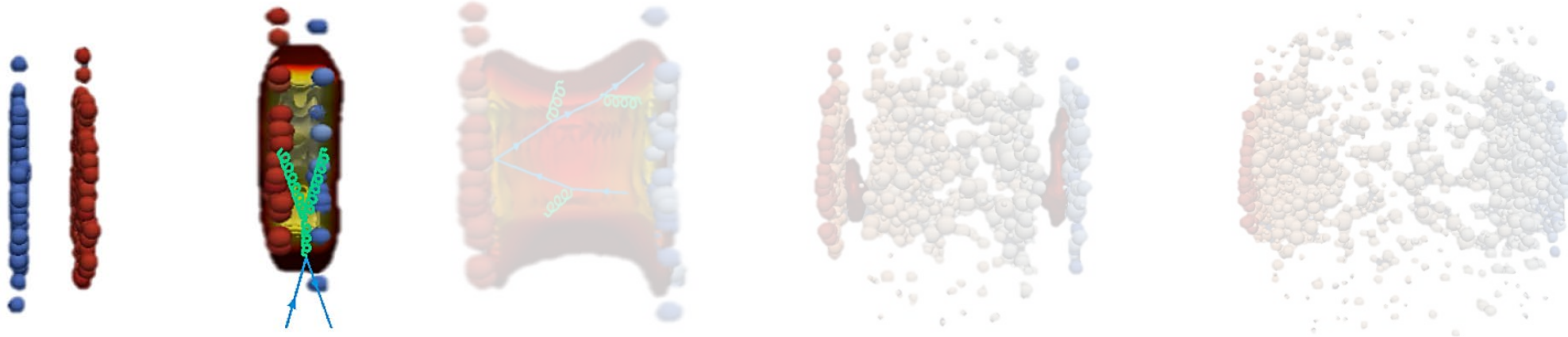
Wenkai Fan¹, Weiyao Ke², Steffen A. Bass¹

1. Duke University

2. University of California, Berkeley

- The simulation pipeline
- The Lido transport model
- Jet and Jet Substructure
- Summary & Outlook

AuAu collision @ 200GeV, figure credit: Hannah Petersen



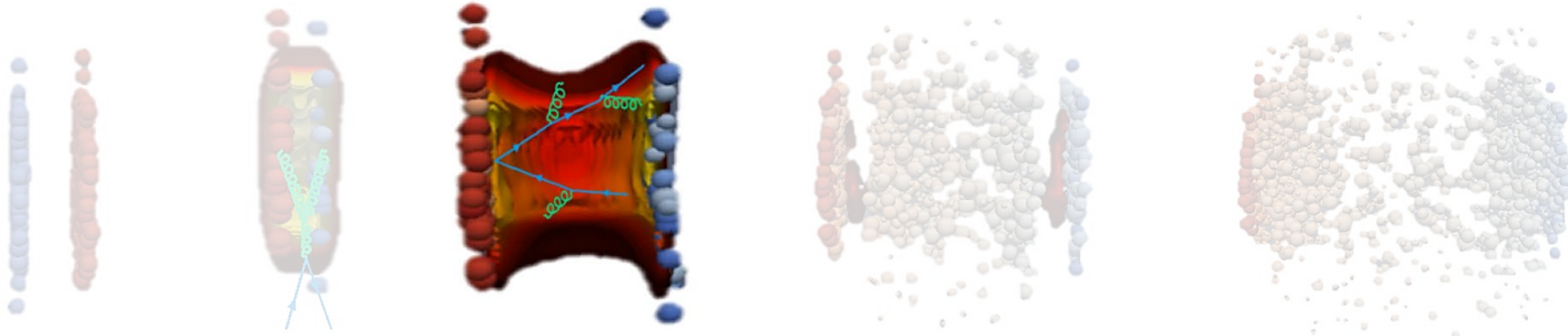
Soft matter:

- Multiple nucleon collision
- TRENTO: parametrized entropy deposition
- Free streaming approximation

Hard parton:

- TRENTO: sample nucleon positions
- Momentum distribution: Pythia with nuclear PDF
- Free streaming approximation

AuAu collision @ 200GeV, figure credit: Hannah Petersen



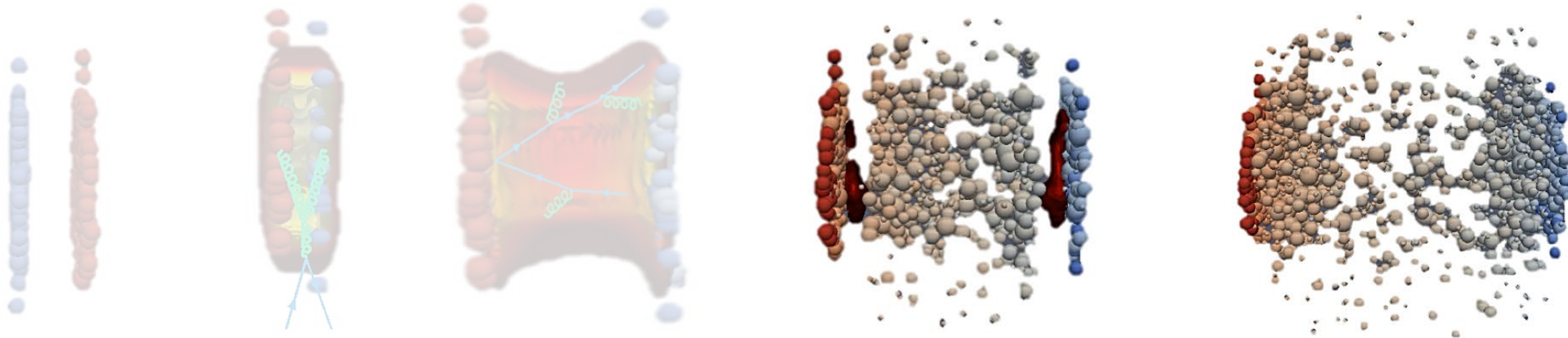
Soft matter:

- Hydrodynamical expansion
- Near local equilibrium
- Equation of State from Lattice QCD
- Shear and bulk viscosity $\frac{\eta}{s}(T), \frac{\zeta}{s}(T)$

Hard parton:

- Transport models - Lido
- Collisional & radiational energy loss
-> jet quenching

AuAu collision @ 200GeV, figure credit: Hannah Petersen



Soft matter:

- Particlization at T_{switch}
- Hadronic rescattering (UrQMD)

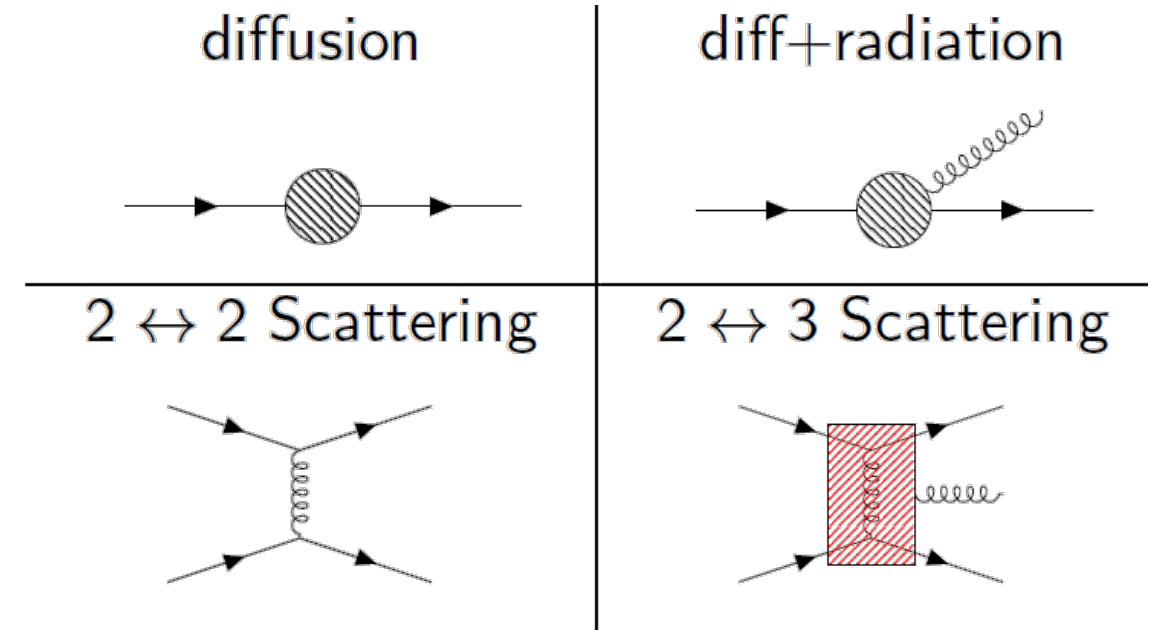
Hard parton:

- Recombination + fragmentation
- Hadronic rescattering (UrQMD)

The evolution of hard parton distribution functions are described by Boltzmann transport equation:

$$\frac{df}{dt} = \mathcal{D}[f] + c^{1\leftrightarrow 2}[f] + c^{2\leftrightarrow 2}[f] + c^{2\leftrightarrow 3}[f]$$

We further divide the interaction kernels into large and small momentum transfer q ones, where the switching scale Q_{cut} should obey $gT \ll Q_{cut} \ll T$.



Ke, Weiyao, Yingru Xu, and Steffen A. Bass. *arXiv:1810.08177 (2018)*.

1. Elastic and large q collisions (vacuum QCD matrix element)

$$R = \frac{g_i}{2E_1} \int \frac{d^3 p_2}{2E_2 (2\pi)^3} f_0(p_2) 2\hat{s} \sum_i \int_{-\hat{s}}^0 \frac{d\sigma_i}{d\hat{t}} d\hat{t}$$

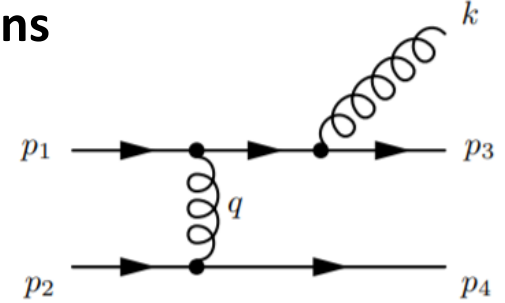
2. Elastic and small q diffusion

$$\begin{cases} \frac{dx_i}{dt} = \frac{p_i}{E} \\ \frac{dp_i}{dt} = -\eta_D p_i + \xi_i(t) \end{cases}$$

The reverse inelastic process rates $R_{3 \rightarrow 2}$ and $R_{2 \rightarrow 1}$ can be written down by the requirement of detailed balance but are omitted in the current setup due to their small contribution to the total collision rate.

3. Inelastic and large q collisions

The matrix elements for $2 \rightarrow 3$ processes are derived under the limits $k, q \ll \sqrt{s}$.

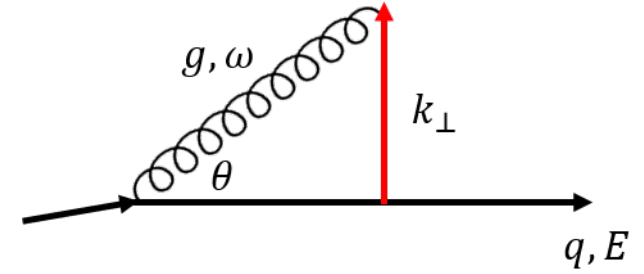


4. Inelastic and small q collisions

$$R_{1 \rightarrow 2} = \kappa_T \int d\mathbf{k}^2 dx \frac{\alpha_s P(x)}{2\pi(\mathbf{k}^2 + m_D^2/2)}$$

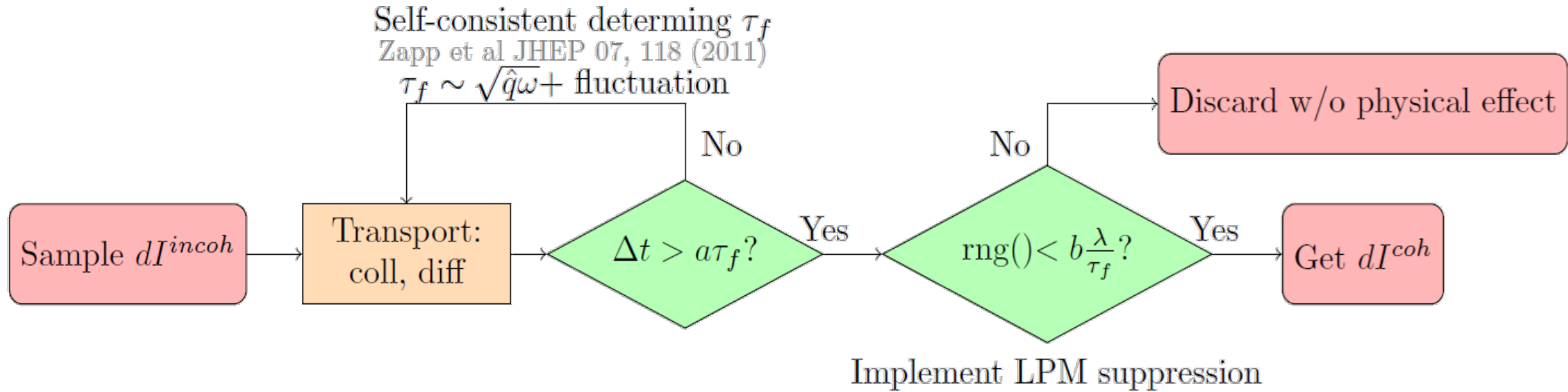
The formation time for a certain splitting is

$$\tau_f \approx \frac{2}{\omega\theta^2}$$



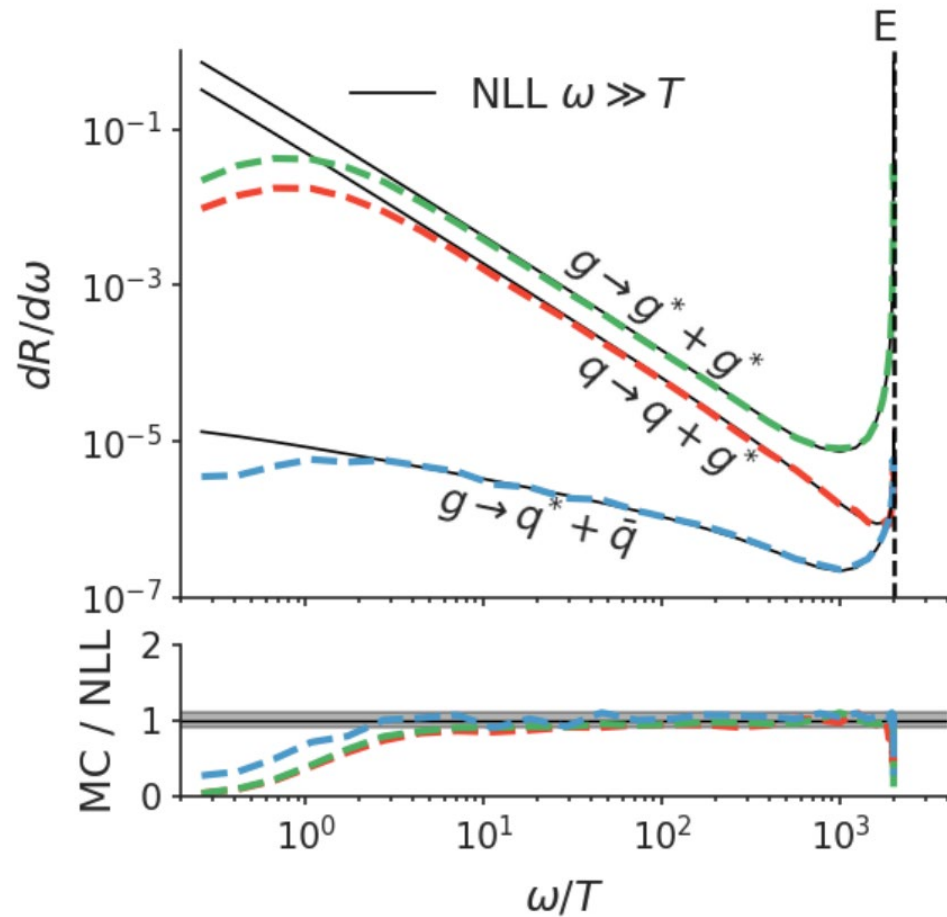
τ_f can be much bigger than the mean free path $\lambda \approx 1/g^2T$ for **hard and colinear** splitting.

- When this is the case, theoretical calculations indicates the radiation rate is suppressed by a factor proportional to λ/τ_f (deep LPM regime) compared to the incoherent limit.
- When formation time is short, the incoherent limit rate recovers and is called the Bethe-Heitler regime.
- Need a Monte-Carlo method that interpolates these two regimes and can be extended to a dynamic medium.

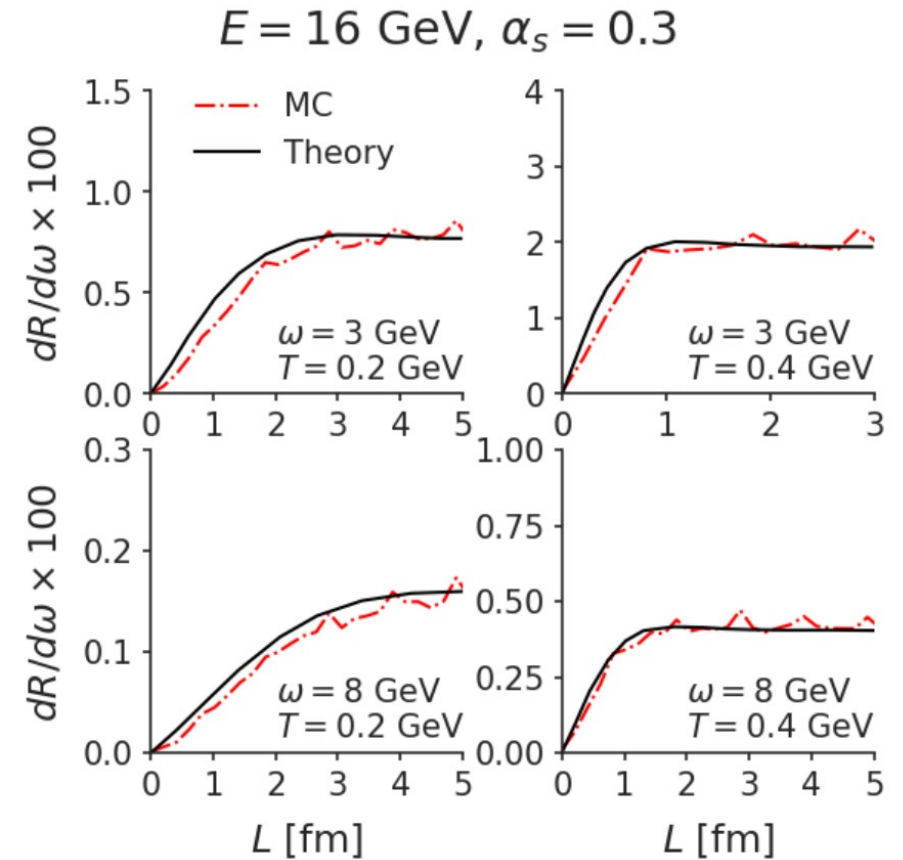


A “non-local” Boltzmann Equation. Figure credit: Weiyao Ke

(The factors a and b are used to match to NLL calculations in a infinite medium)



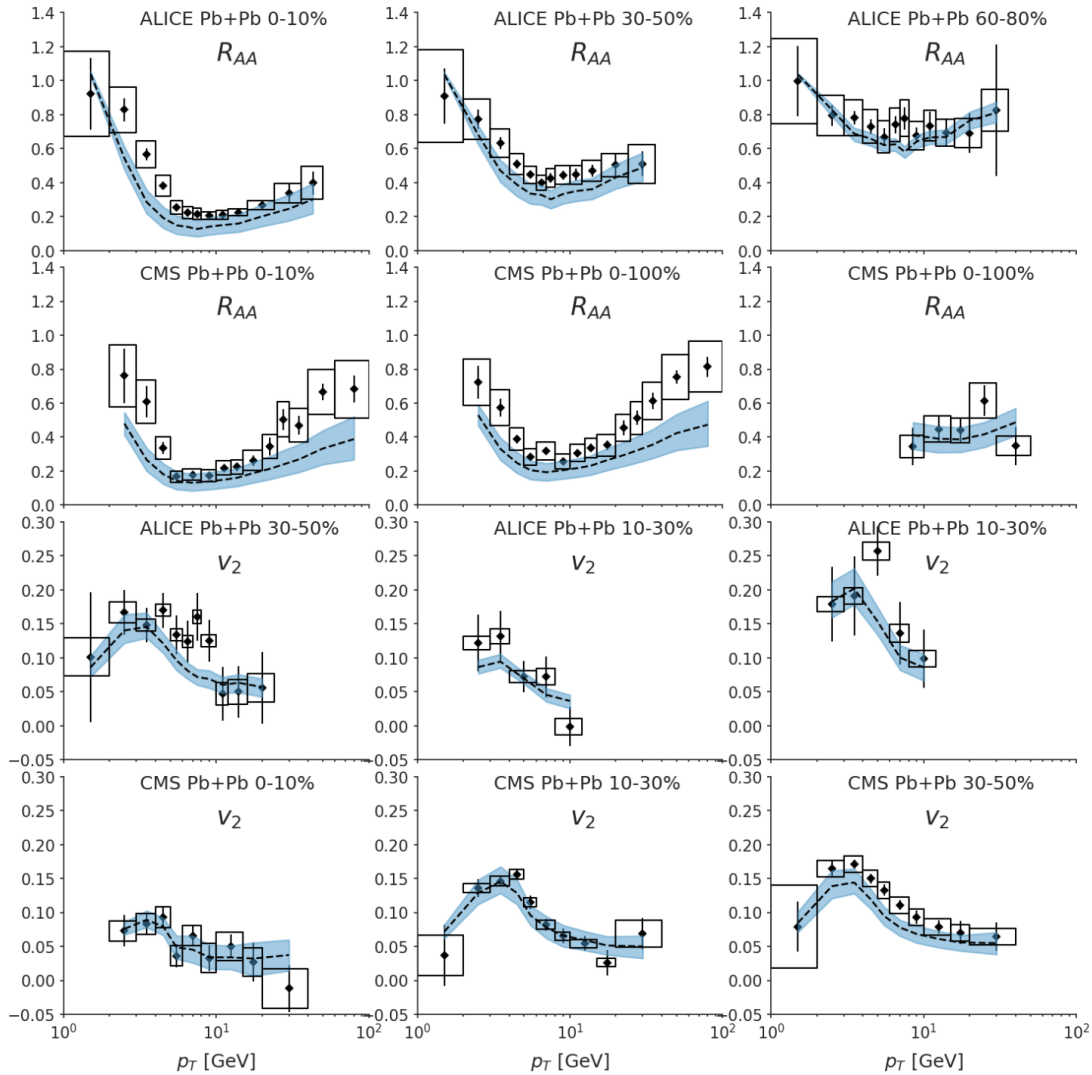
Comparison with AMY formalism in an infinite medium



Splitting rate in a finite medium

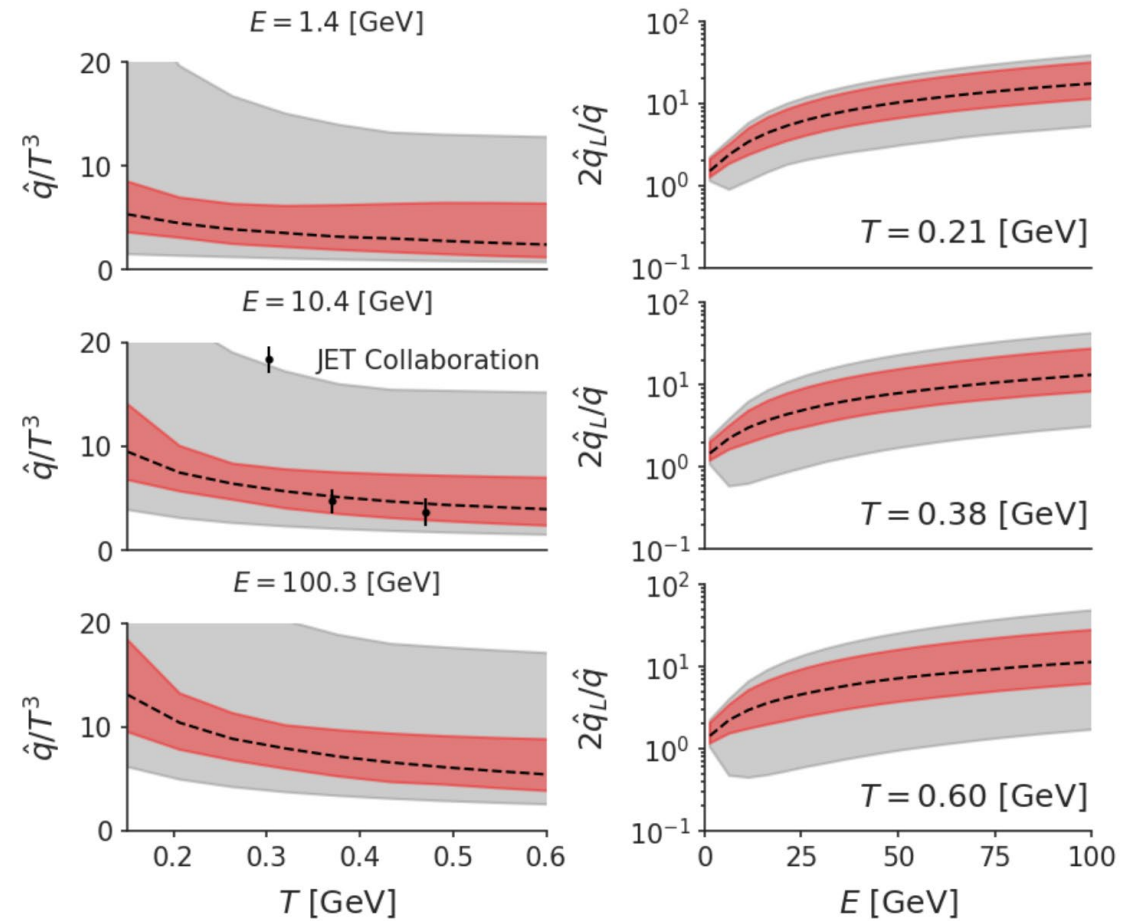
PART 2

Lido Transport Model – Open-Heavy Flavor Results



Calibrated results on open heavy flavor observables

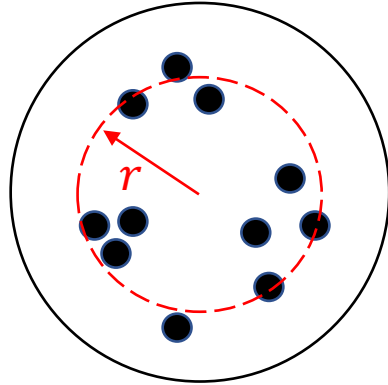
Ke, Weiya. arXiv preprint arXiv:2001.02766 (2020).



90% CL of transport coefficients

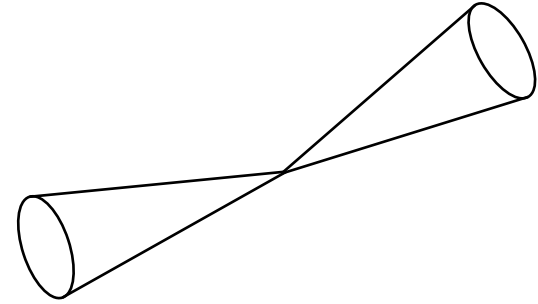
Jet shape:

$$\rho(r) = \frac{1}{\delta r} \frac{1}{N_{jet}} \sum_{jets} \frac{\sum_i p_{i,T}}{p_T^{jet}}$$



Dijet asymmetry:

$$A_J = \frac{p_{T1} - p_{T2}}{p_{T1} + p_{T2}}, \Delta\phi > \frac{\pi}{2}$$

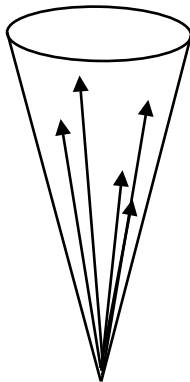


Jet fragmentation function:

$$z = p_T \cos\Delta R / p_T^{jet}$$

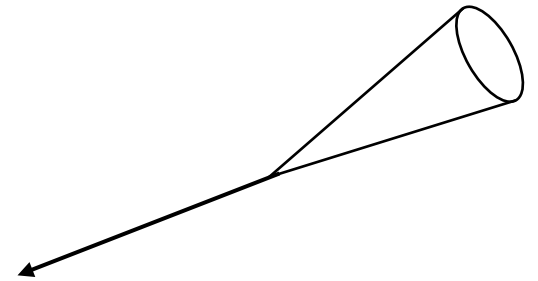
$$D(z) = \frac{1}{N_{jet}} \frac{dn_{ch}}{dz}$$

$$D(p_T) = \frac{1}{N_{jet}} \frac{dn_{ch}}{dp_T}$$

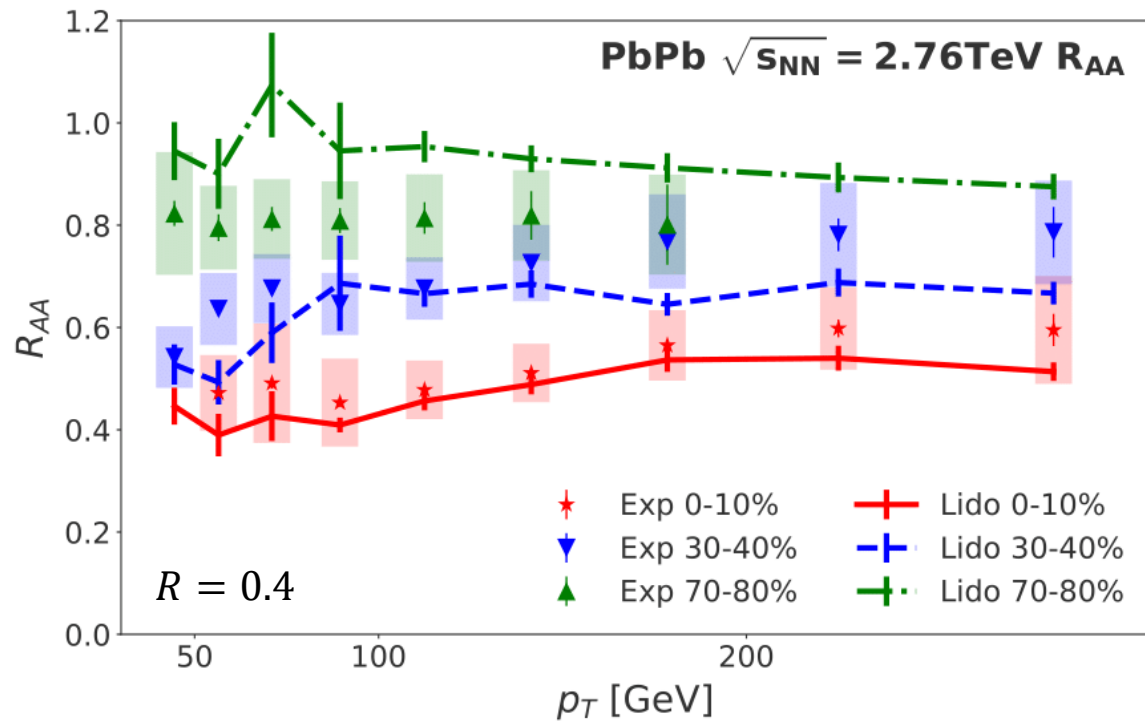


Z/γ tagged jets:

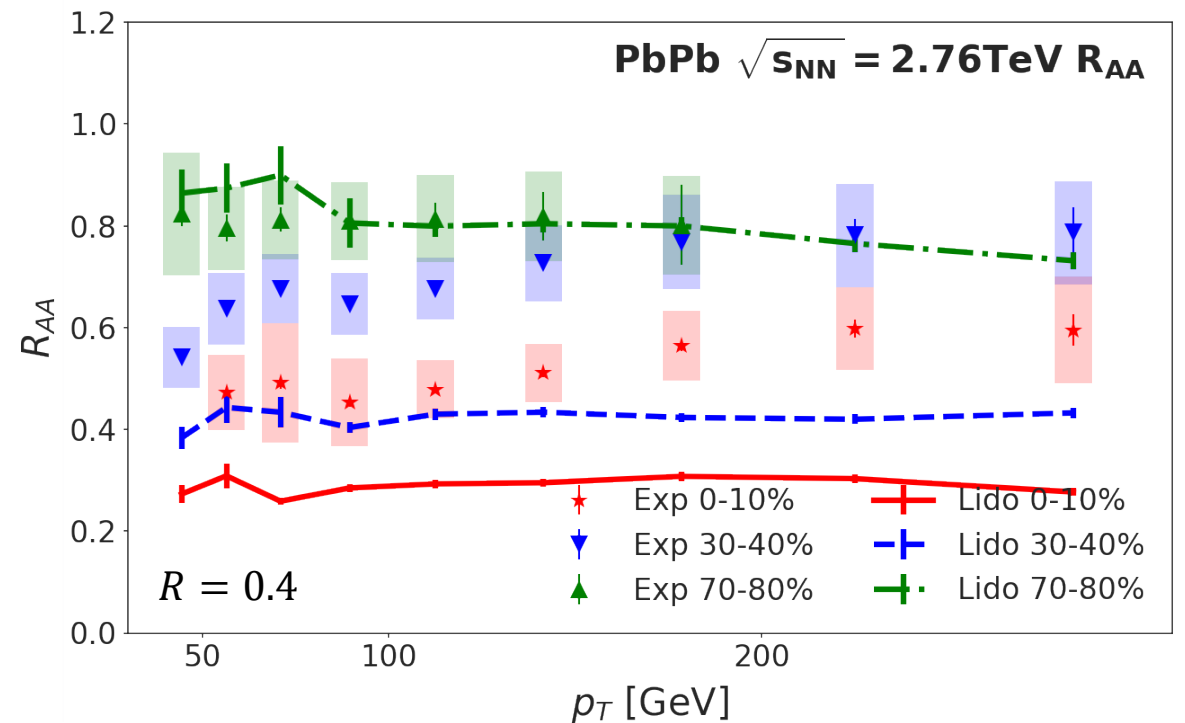
$$\frac{1}{N_\nu} \frac{dN_{j\nu}}{dx_{j\nu}}$$



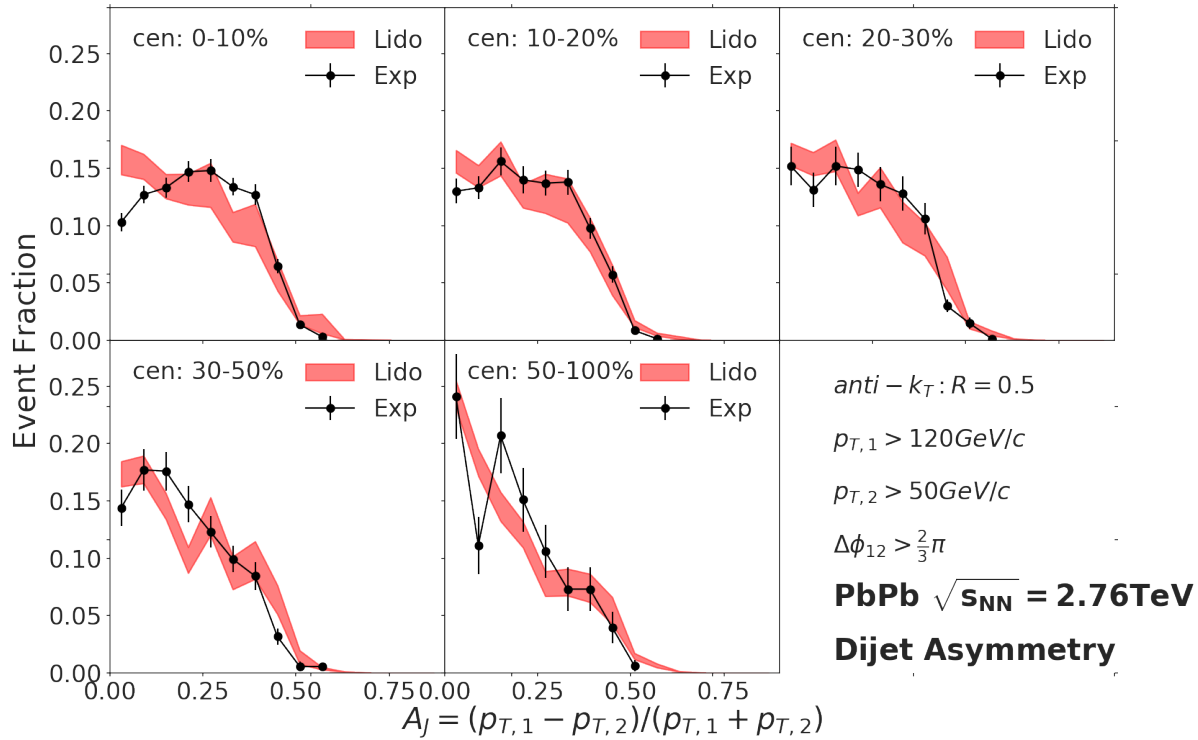
The hydrodynamic simulation is event-averaged and jets are clustered at the parton level. We also compare the results with recoil partons from the medium and without.



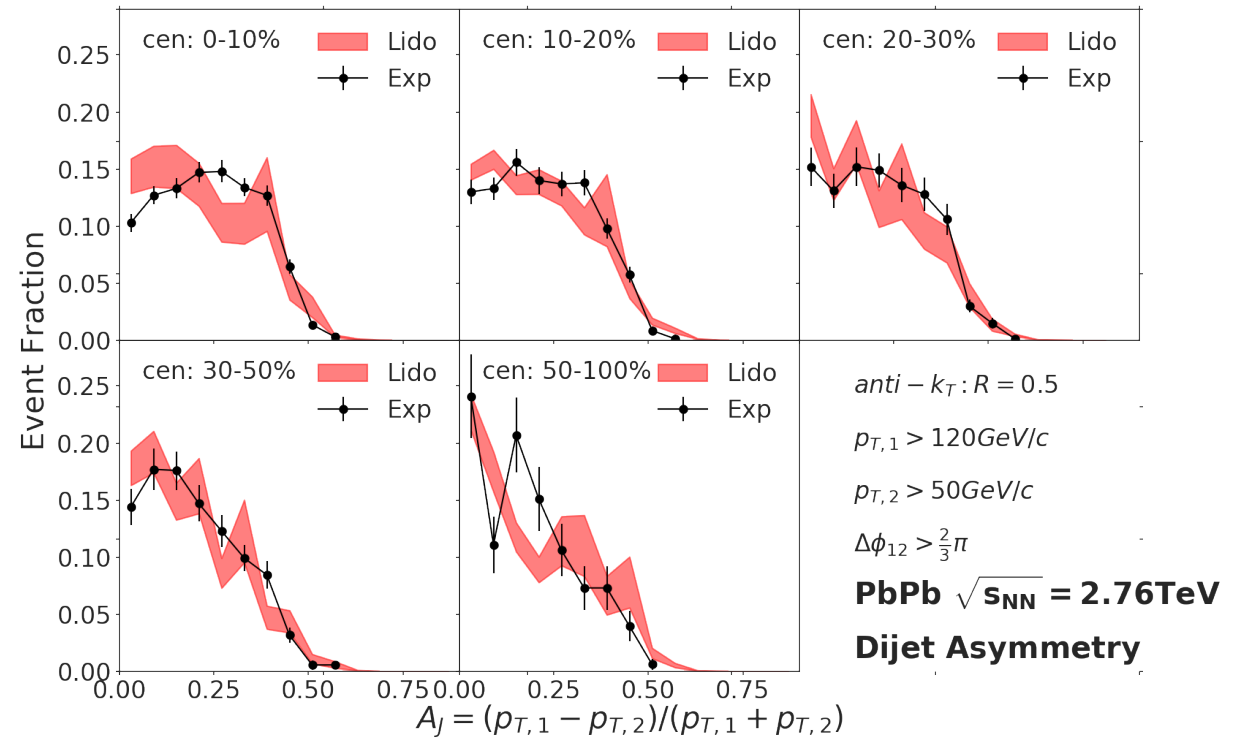
R_{AA} with recoil



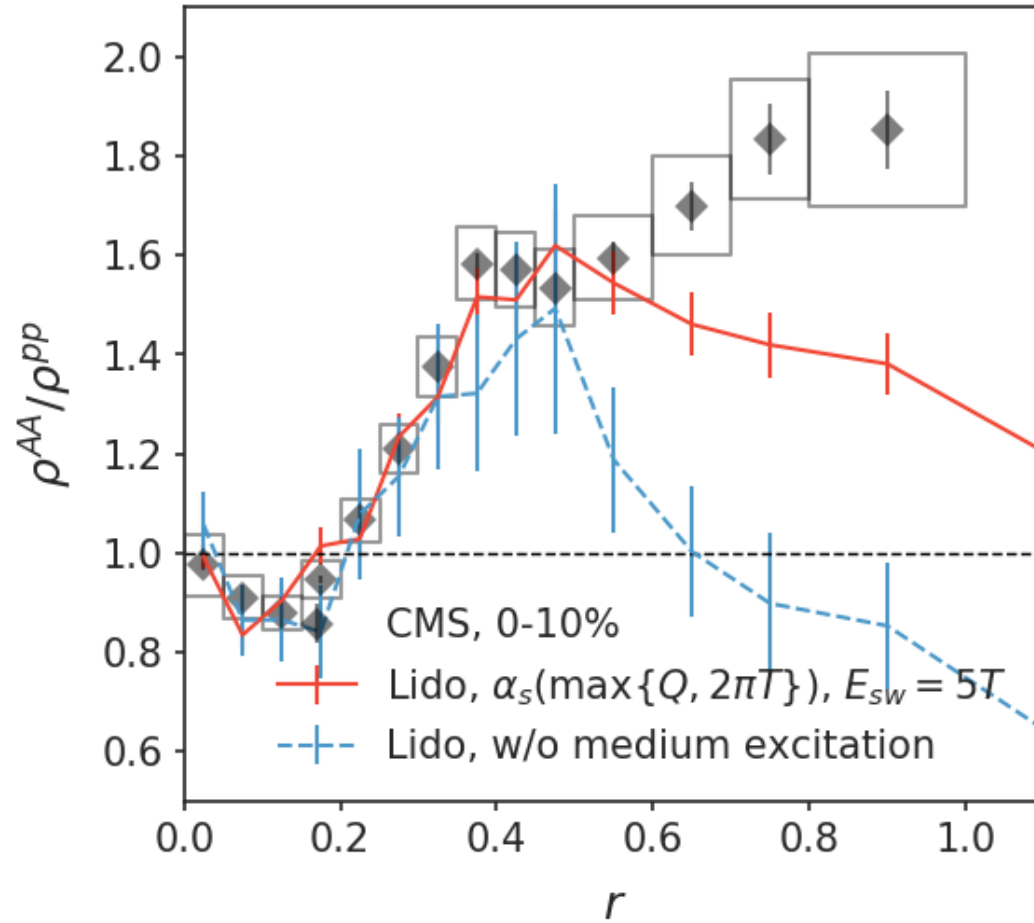
R_{AA} without recoil



Dijet asymmetry with recoil



Dijet asymmetry without recoil

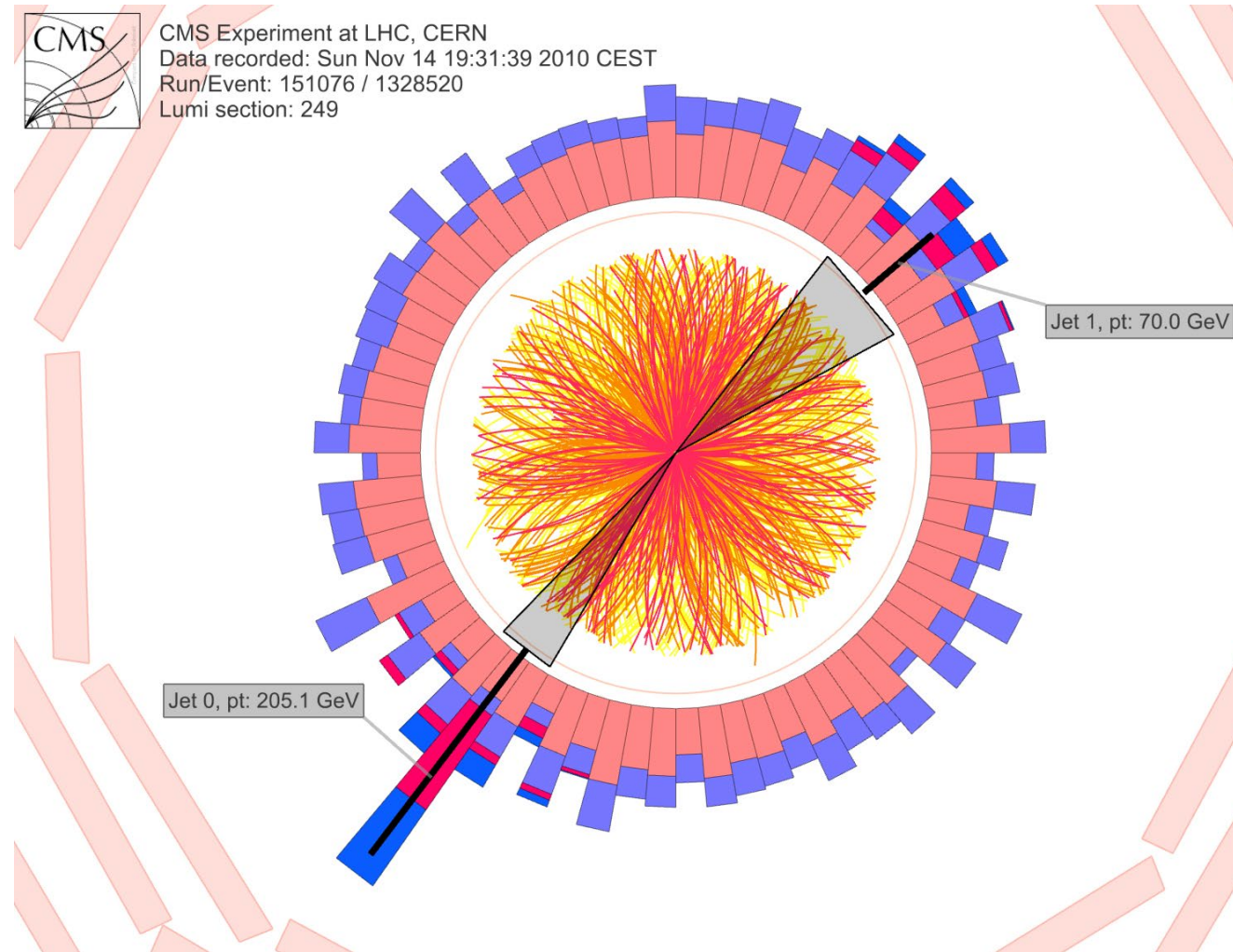


Preliminary W Ke, XN Wang, work in progress

- Lido is a hybrid transport model for both **light** and **heavy** parton transport.
- Jet observables are powerful tools for probing the QGP medium which reveal both longitudinal and transversal parton-medium interactions.
- Considering the progress we are making, we think it is a promising project towards **heavy jet** analysis.
- After including *event-by-event hydro, medium response, hadronization and background subtraction*, we will apply a Bayesian analysis on the transport coefficients and compare with previous results.
- Adaption of JETSCAPE 3.0 in the near future.

Thank you!

- Collimated ensemble of highly energetic particles usually created by initial hard scatterings
- Reconstructed by jet algorithm
- Quenching (energy loss) observed → QGP transport properties



Jet algorithms should be infra-red safe and collinear safe. We adopt the sequential clustering algorithm:

- d_{ij} (distance between particle i and particle j) and d_{iB} (distance between particle i and beam B) are defined as:

$$d_{ij} = \min(k_{\perp i}^{2p}, k_{\perp j}^{2p}) \frac{\Delta_{ij}^2}{R^2}$$

$$d_{iB} = k_{\perp i}^{2p}$$

where $\Delta_{ij} = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$, $k_{\perp i}$ is the transverse momentum, y_i is the rapidity and ϕ_i is the azimuthal angle.

- p is a input parameter, $p = 1$ is the k_T algorithm, $p = 0$ is the Cambridge/Aachen algorithm and $p = -1$ is the anti- k_T algorithm.
- At each step, the minimum among all the values of d_{ij} and d_{iB} is found. If the smallest element is d_{ij} , combine i and j . If the smallest element is d_{iB} , i is labeled as a jet and removed from the list.

Nuclear modification factor:

$$R_{AA}^{jet} = \frac{\left. \frac{d^2 N_{jet}}{dp_T dy} \right|_{AA}}{\langle N_{bin} \rangle \left. \frac{d^2 N_{jet}}{dp_T dy} \right|_{pp}}$$

Nuclear modified jet shape:

$$\rho_{AA}(r) / \rho_{pp}(r)$$

Because there are soft contributions from the bulk medium within the jet cone that we are generally not interested, background subtraction are often required to remove those low p_T particles (jet grooming and re-clustering are also used in experimental analysis). However the implementations might differ for different experiments. How to ensure an apple-to-apple comparison with experiments is what we need to pay attention to.

1. Elastic and large q collisions

$$R = \frac{g_i}{2E_1} \int \frac{d^3 p_2}{2E_2 (2\pi)^3} f_0(p_2) 2 \hat{s} \sum_i \int_{-\hat{s}}^0 \frac{d\sigma_i}{d\hat{t}} d\hat{t}$$

2. Elastic and small q diffusion

$$\begin{cases} \frac{dx_i}{dt} = \frac{p_i}{E} \\ \frac{dp_i}{dt} = -\eta_D p_i + \xi_i(t) \end{cases}$$

where $\langle \xi_i(t) \rangle = 0$, $\langle \xi_i(t) \xi_j(t') \rangle = (\kappa_L \frac{p_i p_j}{p^2} + \kappa_T \left(\delta_{ij} - \frac{p_i p_j}{p^2} \right)) \delta(t - t')$

$$\kappa_T = \int_0^{Q_{cut}^2} dq^2 \frac{\alpha_s m_D^2 T}{q^2 (q^2 + m_D^2)}$$

$$\kappa_L = \int_0^{Q_{cut}^2} dq^2 \frac{\alpha_s (m_D^2/2) T}{q^2 (q^2 + m_D^2/2)}$$

$$\eta_D = \frac{\kappa_L}{2ET} - \frac{\kappa_L - \kappa_T}{p^2} - \frac{\partial \kappa_L}{\partial p^2}$$

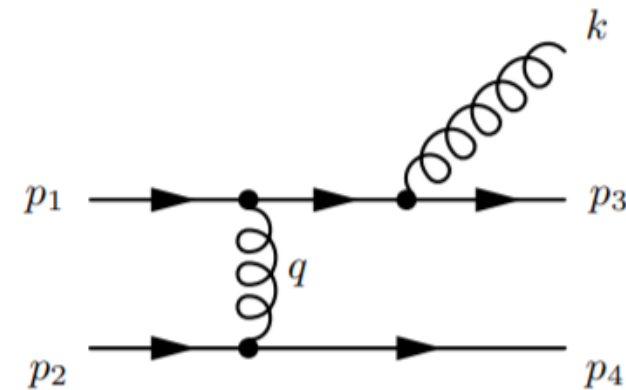
3. Inelastic and large q collisions

The matrix elements for $2 \rightarrow 3$ processes are derived under the limits $k, q \ll \sqrt{s}$ and can be found in the appendix.

4. Inelastic and small q collisions

$$R_{1 \rightarrow 2} = \kappa_T \int d\mathbf{k}^2 dx \frac{\alpha_s P(x)}{2\pi(\mathbf{k}^2 + m_D^2/2)}$$

The reverse inelastic process rates $R_{3 \rightarrow 2}$ and $R_{2 \rightarrow 1}$ can be written down by the requirement of detailed balance but are omitted in the current setup due to their small contribution to the total collision rate.



1. When a splitting happens at t_0 , final state partons b and c are not immediately treated as physical objects to the system. The parent parton can carry arbitrary numbers of such “preformed” final-state copies.
2. Evolve from t to $t + \Delta t$ the “preformed” final state partons in each copy with only elastic processes. While the parent parton is evolved under the full Boltzmann equation.
3. Recalculate formation time τ_f for those “preformed” partons after each time step.
4. Repeat steps 1 to 3 until $t - t_0 > a\tau_f(t)$ is satisfied.
5. Then, the “preformed” final state is considered to become the physical final state with probability $p =$

$$\min\left\{1, \frac{ab\lambda(t)}{\tau_f}\right\}.$$

(The factors a and b are used to match to NLL calculations in a infinite medium)

Light parton scattering:

$$\begin{aligned} \overline{|M_{q_1 q_2 \rightarrow q_1 q_2}|^2} &= \frac{64\pi^2 \alpha_s^2}{9} \frac{s^2 + u^2}{t^2} \\ \overline{|M_{gg \rightarrow gg}|^2} &\approx 72\pi^2 \alpha_s^2 \frac{-su}{t^2} \\ \overline{|M_{qg \rightarrow qg}|^2} &\approx 16\pi^2 \alpha_s^2 \frac{s^2 + u^2}{t^2} \end{aligned}$$

Heavy parton scattering:

$$\begin{aligned} \overline{|M_{Qq \rightarrow Qq}|^2} &= \frac{64\pi^2 \alpha_s^2}{9} \frac{(M^2 - u)^2 + (s - M^2)^2 + 2M^2 t}{t^2} \\ \overline{|M_{Qq \rightarrow Qq}|^2} &= \pi^2 \left\{ 32\alpha_s^2 \frac{(s - M^2)(M^2 - u)}{t^2} \right. \\ &+ \frac{64}{9} \alpha_s^2 \frac{(s - M^2)(M^2 - u) + 2M^2(s + M^2)}{(s - M^2)^2} \\ &+ \frac{64}{9} \alpha_s^2 \frac{(s - M^2)(M^2 - u) + 2M^2(u + M^2)}{(M^2 - u)^2} \\ &+ \frac{16}{9} \alpha_s^2 \frac{M^2(4M^2 - t)}{(M^2 - u)(s - M^2)} \\ &+ 16\alpha_s^2 \frac{(s - M^2)(M^2 - u) + M^2(s - u)}{t(s - M^2)} \\ &\left. - 16\alpha_s^2 \frac{(s - M^2)(M^2 - u) - M^2(s - u)}{t(M^2 - u)} \right\} \end{aligned}$$

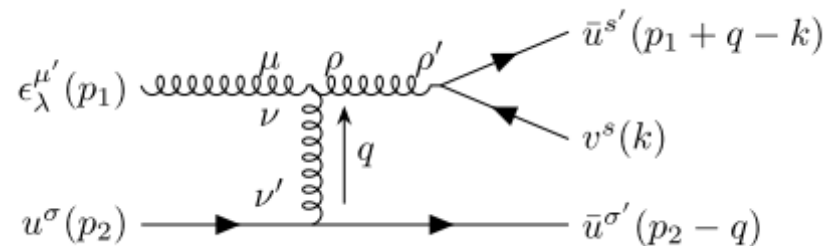
Collinear approximation: $k_{\perp}^2, q_{\perp}^2 \ll x(1-x)\hat{s}$, $x = k^+/\sqrt{s}$

The matrix-element is factorized into an amplitude for the splitting process (approximated in the collinear limit) times the amplitude for two-body collision with the medium parton.

$$\overline{|M^2|}_{g+i \rightarrow g+g+i} = \overline{|M^2|}_{g+i \rightarrow g+i} P_{gg}^{g(0)} D_{gg}^g,$$

$$\overline{|M^2|}_{g+i \rightarrow q+\bar{q}+i} = \frac{C_F d_F}{C_A d_A} \overline{|M^2|}_{g+i \rightarrow g+i} P_{q\bar{q}}^{g(0)} D_{q\bar{q}}^g,$$

$$\overline{|M^2|}_{q+i \rightarrow q+g+i} = \overline{|M^2|}_{q+i \rightarrow q+i} P_{qg}^{q(0)} D_{qg}^q.$$



$$P_{gg}^{g(0)} = g^2 C_A \frac{1 + x^4 + (1-x)^4}{x(1-x)},$$

$$P_{qg}^{q(0)} = g^2 C_F \frac{1 + (1-x)^4}{x},$$

$$P_{q\bar{q}}^{g(0)} = g^2 \frac{N_f}{2} (x^2 + (1-x)^4).$$

$$D_{q\bar{q}}^g = C_A(\mathbf{a} - \mathbf{b})^2 + C_A(\mathbf{a} - \mathbf{b})^2$$

$$- C_A(\mathbf{a} - \mathbf{b}) \cdot (\mathbf{a} - \mathbf{c}),$$

$$D_{q\bar{q}}^g = C_F(\mathbf{a} - \mathbf{b})^2 + C_F(\mathbf{a} - \mathbf{b})^2$$

$$- (2C_F - C_A)(\mathbf{a} - \mathbf{b}) \cdot (\mathbf{a} - \mathbf{b}),$$

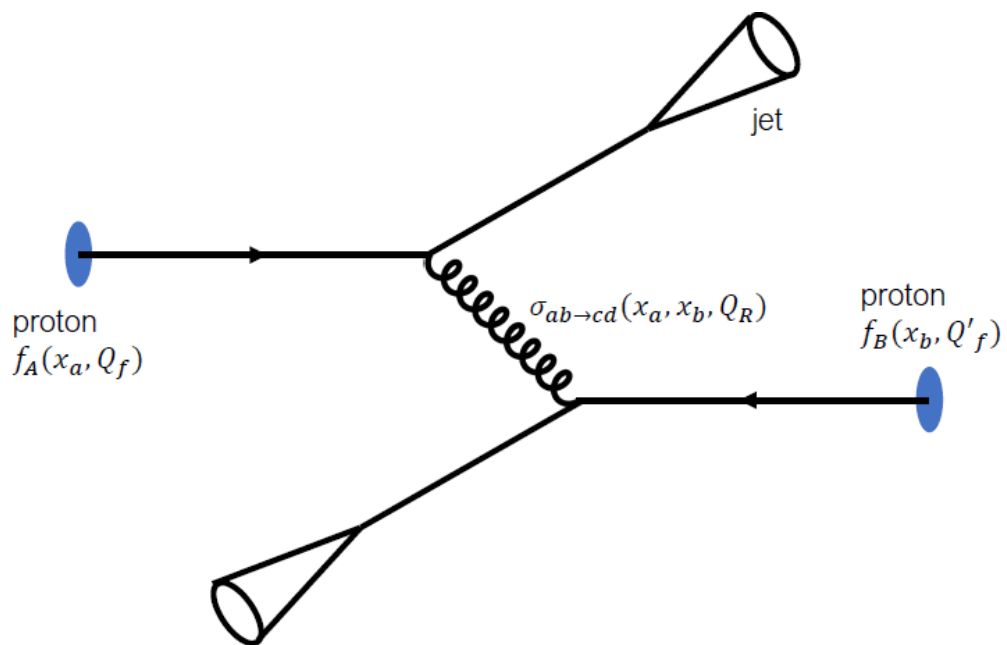
$$D_{qg}^q = C_F(\mathbf{c} - \mathbf{a})^2 + C_F(\mathbf{c} - \mathbf{b})^2$$

$$- (2C_F - C_A)(\mathbf{c} - \mathbf{a}) \cdot (\mathbf{c} - \mathbf{b}).$$

$$\mathbf{a} = \frac{\mathbf{k} - x\mathbf{q}}{(\mathbf{k} - x\mathbf{q})^2}, \mathbf{b} = \frac{\mathbf{k} - \mathbf{q}}{(\mathbf{k} - \mathbf{q})^2}, \mathbf{c} = \frac{\mathbf{k}}{\mathbf{k}^2}.$$

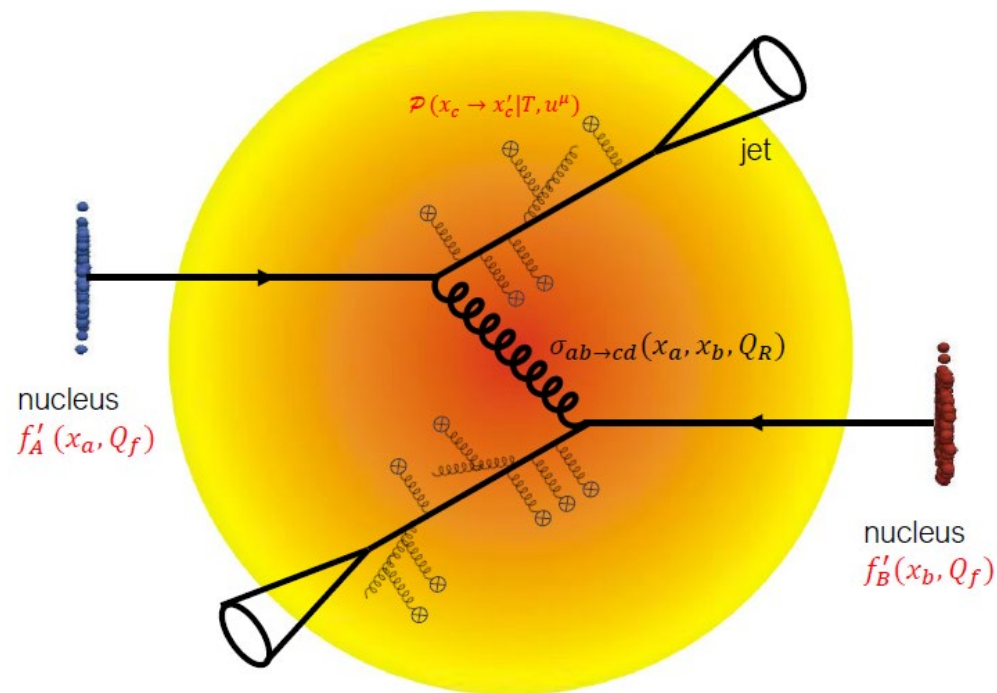
$$\sigma^{AB \rightarrow X + jet}$$

$$= \sum_{abcd} f_A(x_a, Q_f) \otimes f_B(x_b, Q_f) \otimes \sigma_{ab \rightarrow cd}(x_a, x_b, Q_R)$$



$$\sigma^{AB \rightarrow X + jet} = \int_{\text{geometry}} \sum_{abcd} f'_A(x_a, Q_f) \otimes f'_B(x_b, Q_f)$$

$$\otimes \sigma_{ab \rightarrow cd}(x_a, x_b, Q_R) \otimes \mathcal{P}(x_c \rightarrow x'_c | T, u^\tau)$$



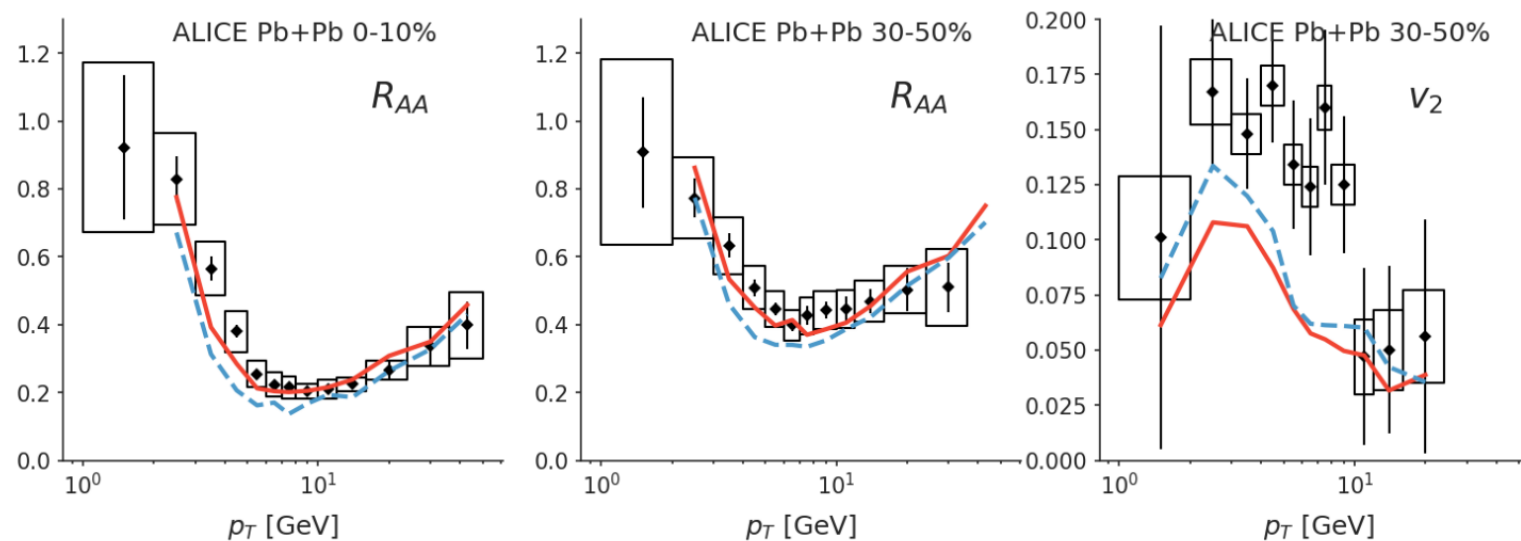
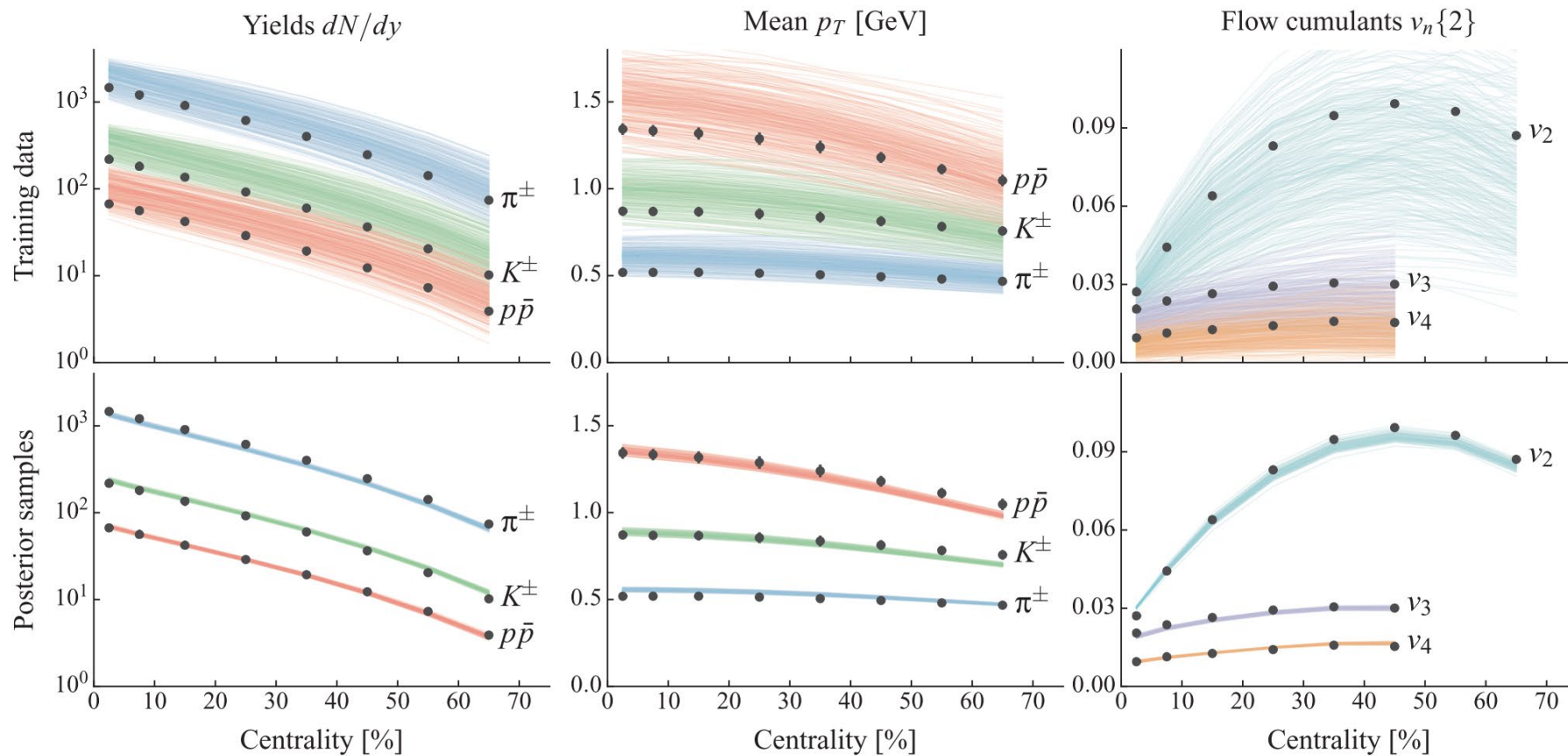
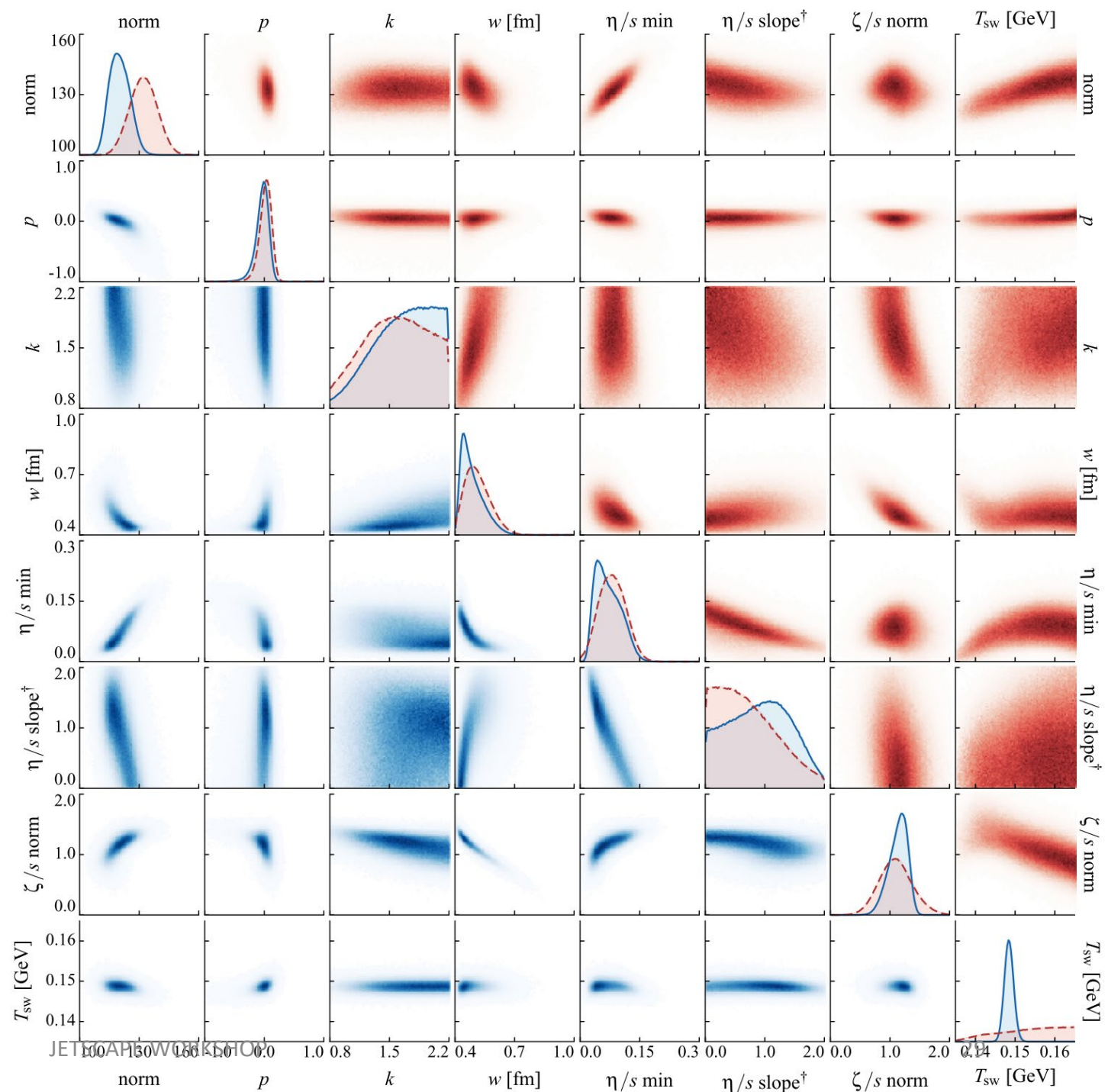
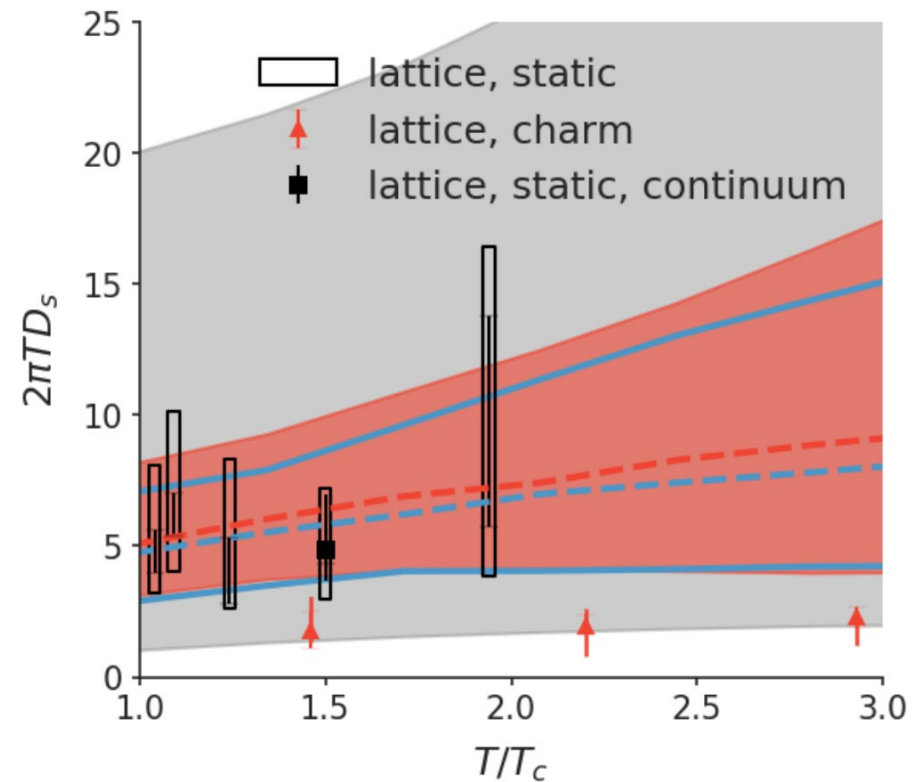
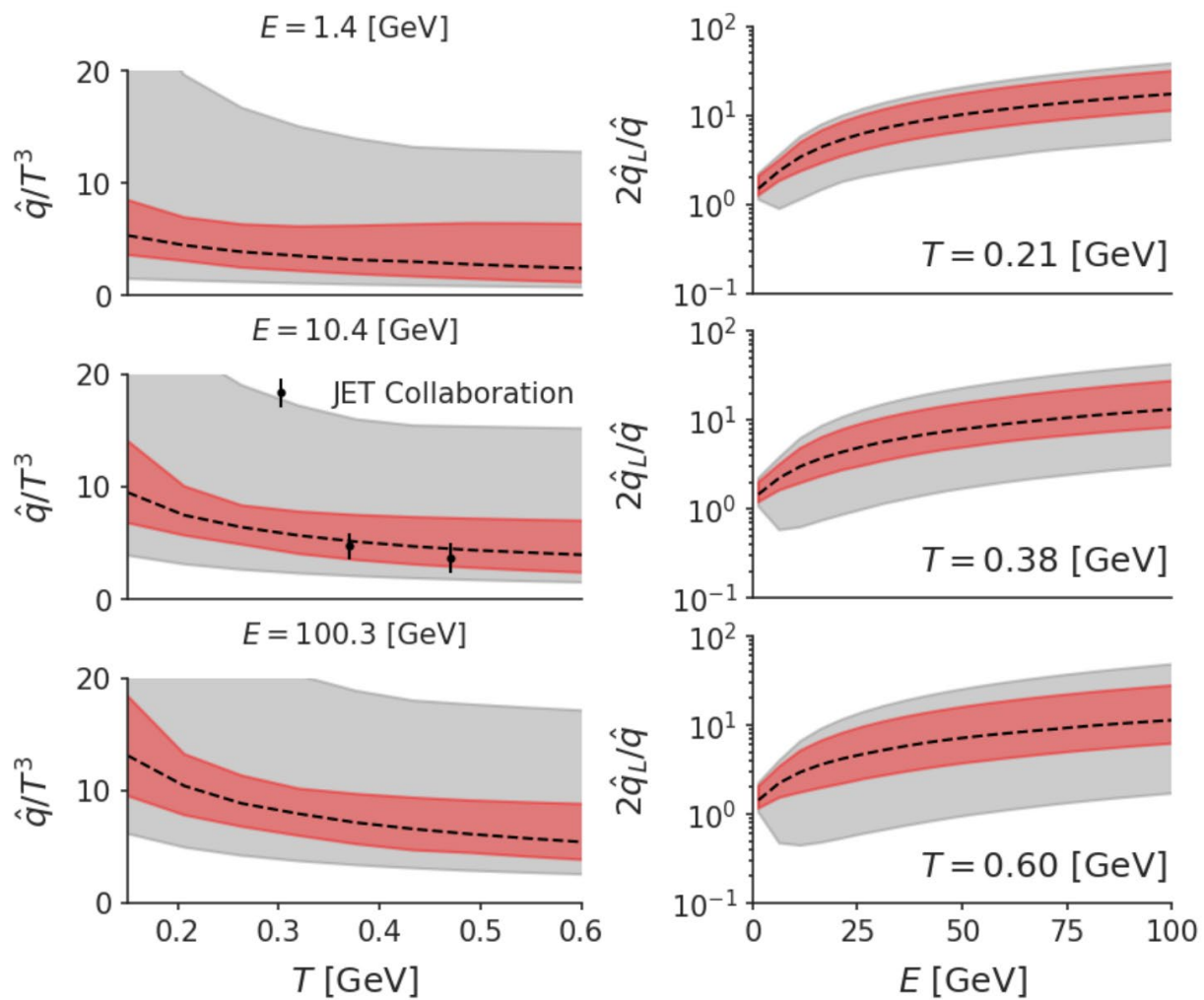
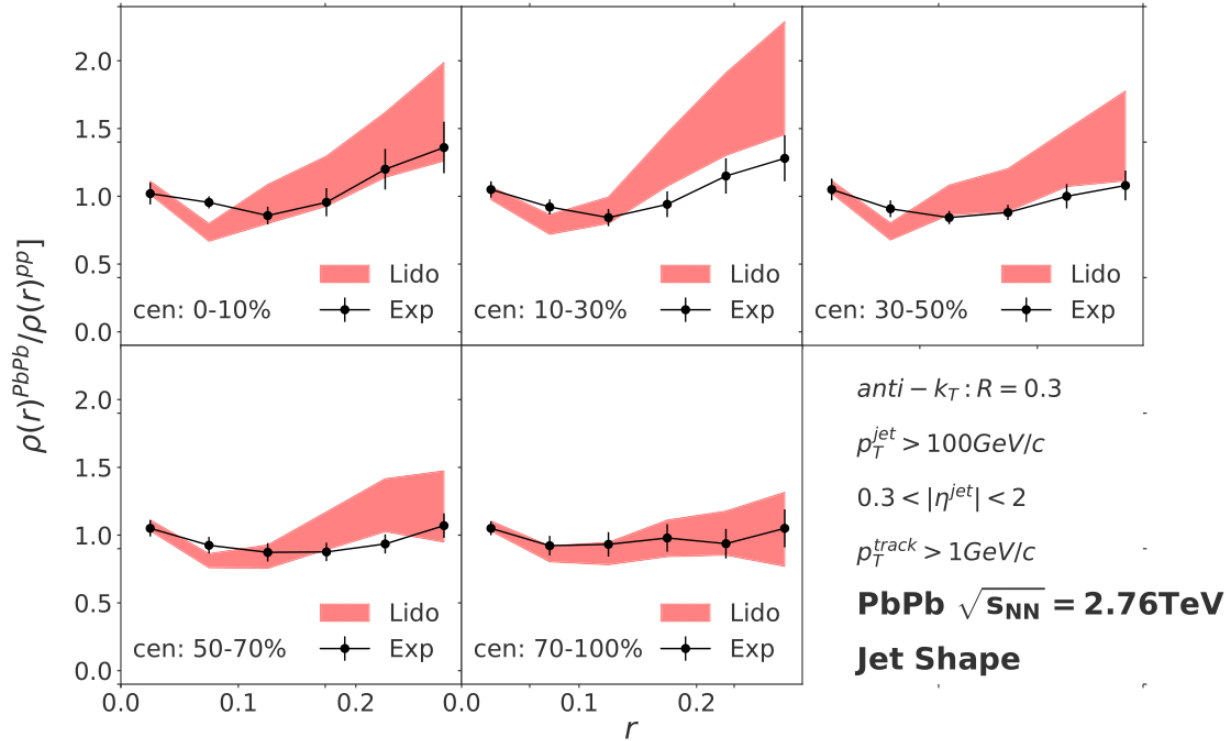


Figure 4.9 Effect of changing the switch scale between small- Q diffusion modeling and large- Q scattering modeling. $\mu = 2$ is used. The red solid lines used a switching scale at $Q_{switch}^2 = 4m_D^2$, and the blue dashed lines uses $16m_D^2$.

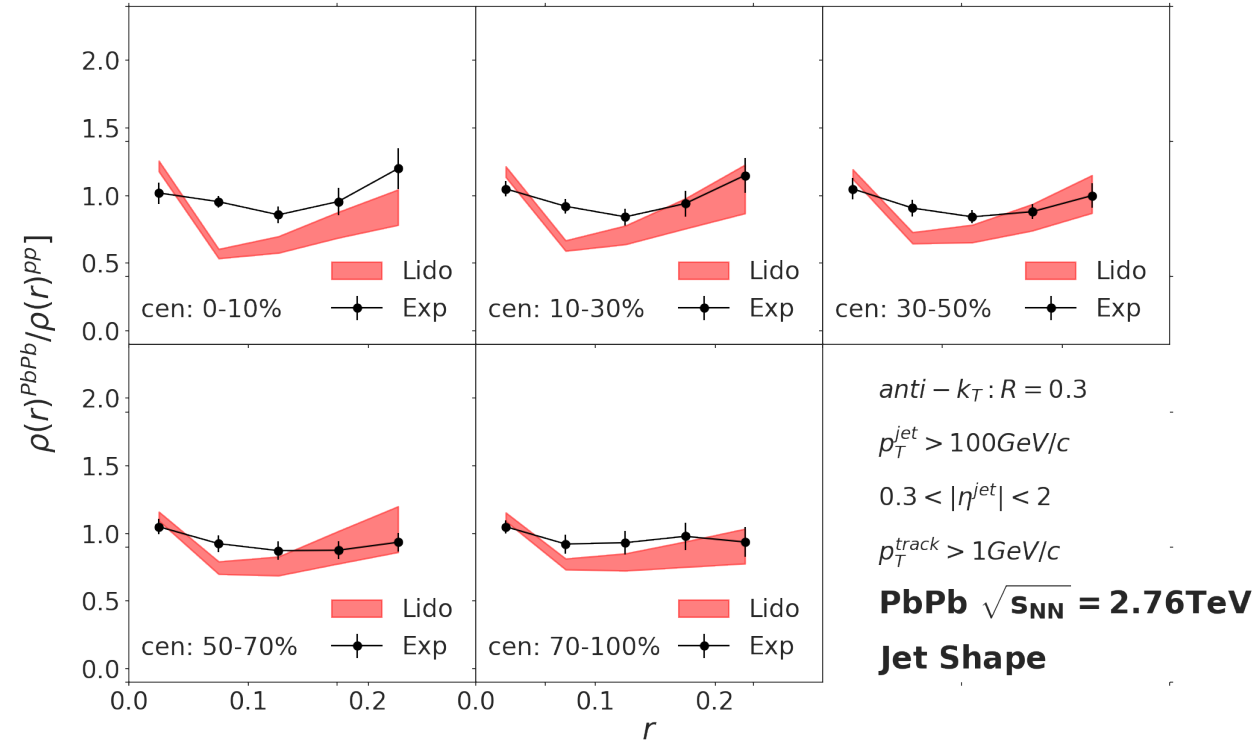








Jet shape with recoil



Jet shape without recoil