

# Is the Chiral Magnetic Effect fast enough ?



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**Phys. Rev. D. 104 (2021) 046009**  
**2105.05855 [hep-ph]**

**With: J. Ghosh, S. Grieneringer, S. Morales-Tejera**



# Outline

- CME and equilibrium
- Out-of-equilibrium CME in Holography
  - Generic model properties
  - Matching to QCD
- Conclusions & Outlook

# CME @ HIC

Axial anomaly (QED):

$$\partial_\mu J_5^\mu = c \epsilon^{\mu\nu\rho\lambda} F_{\mu\nu} F_{\rho\lambda}$$

CME:

$$\vec{J} = 8c \mu_5 \vec{B}$$

[Fukushima, Kharzeev, Warringa]

[Vilenkin] 1980

[Alekseev, Chaianov, Fröhlich]

[Giovannini, Shaposhnikov],...

Equilibrium quantity, not the chiral charge !

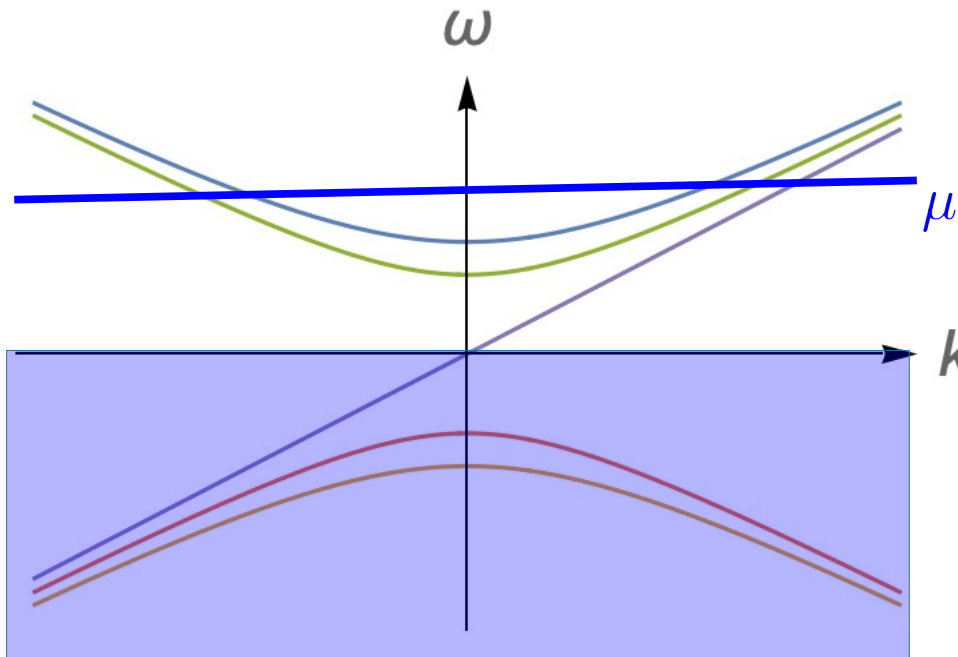
Lifetime!

Theory subtleties (covariant vs. consistent anomalies)

[Gynther, K.L., Pena-Benitez, Rebhan], 1005.2587 [K.L. 1610.04413]

$$\vec{J} = 8c(\mu_5 - A_5^0) \vec{B}$$

Chiral fermion in (very strong) magnetic field:



Lowest Landau Level:

$$J = \frac{eB}{2\pi} \int_0^\infty \frac{dk}{2\pi} [n_F(\mu, T) - n_F(-\mu, T)] = \frac{\mu}{4\pi^2} eB$$

Higher Landau Levels:

$$J = \frac{eB}{2\pi} \int_{-\infty}^{+\infty} \frac{dk}{2\pi} \frac{\partial \epsilon}{\partial k} (n_F(\mu, T, k^2)) = 0$$

CME current stems from LLL only

arXiv.org > nucl-th > arXiv:1608.00982

## Nuclear Theory

*[Submitted on 2 Aug 2016 (v1), last revised 12 Aug 2016 (this version, v2)]*

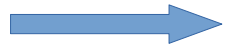
# Chiral Magnetic Effect Task Force Report

Vladimir Skokov, Paul Sorensen, Volker Koch, Soeren Schlichting, Jim Thomas, Sergei Voloshin, Gang Wang, Ho-Ung Yee

## Theory Uncertainties:

A) the initial distribution of axial charges,

B) the evolution of the magnetic field,



C) the dynamics of the CME during the pre-equilibrium stage,



D) the uncertainties in the hadronic phase and the freeze-out.

## How long does it take to build up the CME current if one starts out with $J=0$ ?

- Quark Gluon Plasma: strongly coupled fluid
  - One of the success stories of holography
  - Especially successful for CME, CVE
- Shear viscosity:  $\frac{\eta}{s} = \frac{1}{4\pi}$  [Policastro, Son, Starinets]
- Equilibration, isotropisation times:  $\tau \approx 0.5 fm/c$  [Chesler, Yaffe]

[Newman], [Yee], [Erdmenger, Kaminski, Haack, Yarom], [Banerjee, Bhattacharya, Bhattacharyya, Dutta, Loganayagam, Surowka]  
[Rebhan, Schmitt, Stricker], [Gynther, K.L., Pena-Benitez, Rebhan], [K.L., Megias, Melgar, Pena-Benitez],  
[Ammon, Grienering, Hernandez, Kaminski, Koirala, Leiber, Wu], ...

Investigate this question in a holographic setup

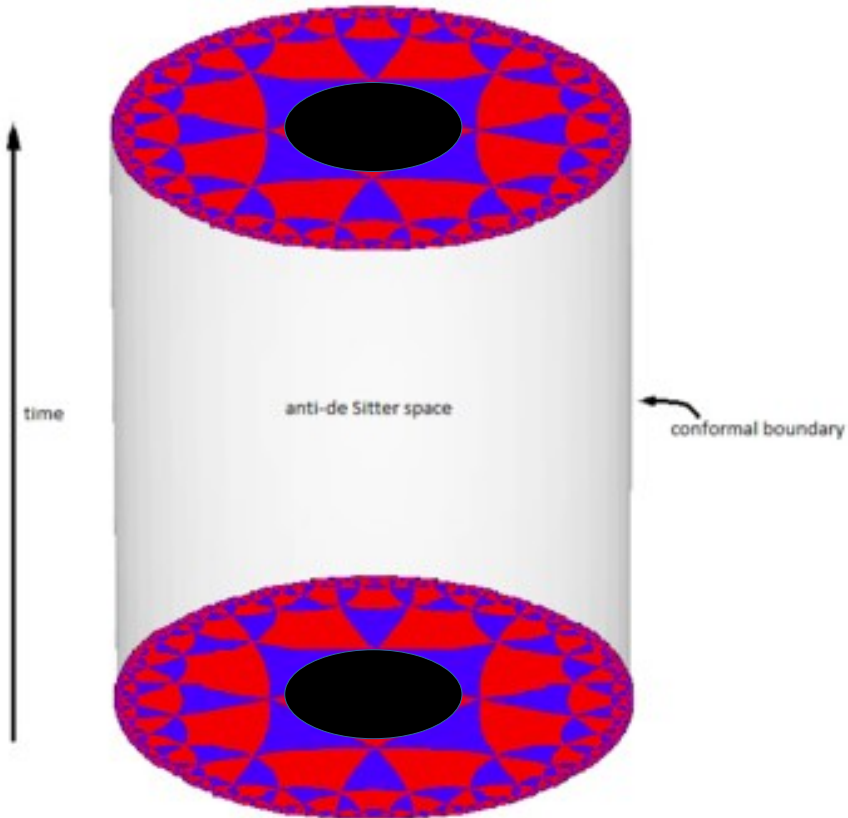
[Lin, Yee], [Ammon, Grienering, Jimenez-Alba, Malcedo, Melgar], [K.L., Lopez, Milans del Bosch],  
[Fernandez-Pendas, K.L.], [Morales-Tejera, K.L.], [Cartwright]

Quantum simulation approach 2D model: [Kharzeev, Kikuchi]

TALKS at this conference: *M.Kaminski* and *C.Cartwright*

# Holography

Gravity in asymptotically AdS = QFT



## Holographic Dictionary

Metric	Energy Momentum Tensor
Gauge field	Conserved current = symmetry
Scalar field	Scalar operator
<b>Boundary value</b>	<b>Coupling</b>
<b>Black Hole</b>	<b>Temperature</b>

# Holography

Holographic bottom-up approach: chose symmetries, simplest Lagrangian

$$S = \frac{1}{2\kappa^2} \int d^5x \sqrt{-g} \left[ R + \frac{12}{L^2} - \frac{1}{4} F_V^2 - \frac{1}{4} F_A^2 + \frac{\alpha}{3} \epsilon^{\mu\nu\rho\lambda\sigma} A_\mu (3F_{\nu\rho}^V F_{\lambda\sigma}^V + F_{\nu\rho}^A F_{\lambda\sigma}^A) \right]$$

**Ansatz:**  $ds^2 = -f(v, u)dv^2 - \frac{2L^2}{u^2} dvdu + \frac{2}{u^2} h(v, u)dvdz + \Sigma(v, u)^2 \left[ e^{\xi(v, u)}(dx^2 + dy^2) + e^{-2\xi(v, u)} dz^2 \right]$

$$V_\mu = (0, 0, -y B/2, x B/2, V_z(v, u)) \quad , \quad A_\mu = (-Q_5(v, u), 0, 0, 0, 0)$$

Asymptotic expansion:

$$Q_5(v, u) = \frac{u^2}{2} q_5 + \mathcal{O}(u^3),$$

$$V_z(v, u) = u^2 V_2(v) + \mathcal{O}(u^3),$$

$$\Sigma(v, u) = \frac{1}{u} + \lambda(v) + \mathcal{O}(u^5),$$

$$\xi(v, u) = u^4 \left( \xi_4(v) - \frac{B^2}{12} \log(u) \right) + \mathcal{O}(u^5),$$

$$f(v, u) = \left( \frac{1}{u} + \lambda(v) \right)^2 + u^2 \left( f_2 + \frac{B^2}{6} \log(u) \right) - 2\dot{\lambda}(v) + \mathcal{O}(u^3).$$

Operators:

$$J_z = \frac{1}{\kappa^2} V_2(v)$$

$$J_5^0 = \frac{1}{2\kappa^2} q_5$$

$$T_v^v = \frac{1}{4\kappa^2} [6f_2 - B^2 \log(\mu L)]$$

$$T_x^x = T_y^y = -\frac{1}{8\kappa^2} [B^2 + 4f_2 - 16\xi_4(v) - 2B^2 \log(\mu L)]$$

$$T_z^z = -\frac{1}{4\kappa^2} [2f_2 + 16\xi_4(v) + B^2 \log(\mu L)]$$



# Holography

- Initial state:
- Energy and axial charge corresponding to  $(T, \mu_5)$  in final state
  - Magnetic field is uniform and constant in time
  - Dynamical pressure anisotropy vanishes  $\xi = 0$
  - CME current is absent  $V_z = 0$

- Final state:
- Dynamical pressure anisotropy determined by magnetic field
  - CME current has approached equilibrium expression

- Compare to:
- [Chesler, Yaffe] 2010 “Isotropization”, no magnetic field
- [Fuini, Yaffe] 2016 Magnetic field, no chiral charge, no CME

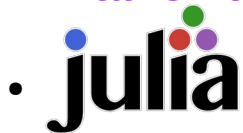
# Holography

## Numerical Methods:

- Pseudo-spectral methods
- Chebyshev Polynomials
- Chebyshev-Lobatto grid  $x_n = \cos(n\pi/N)$
- Keep apparent horizon fixed  $\lambda(v)$
- Subtract logs for better convergence
- Time evolution 4<sup>th</sup> order Runge-Kutta [Chesler, Yaffe] JHEP 07 (2014) 086

## Implementation:

- Mathematica (original code, somewhat slow)

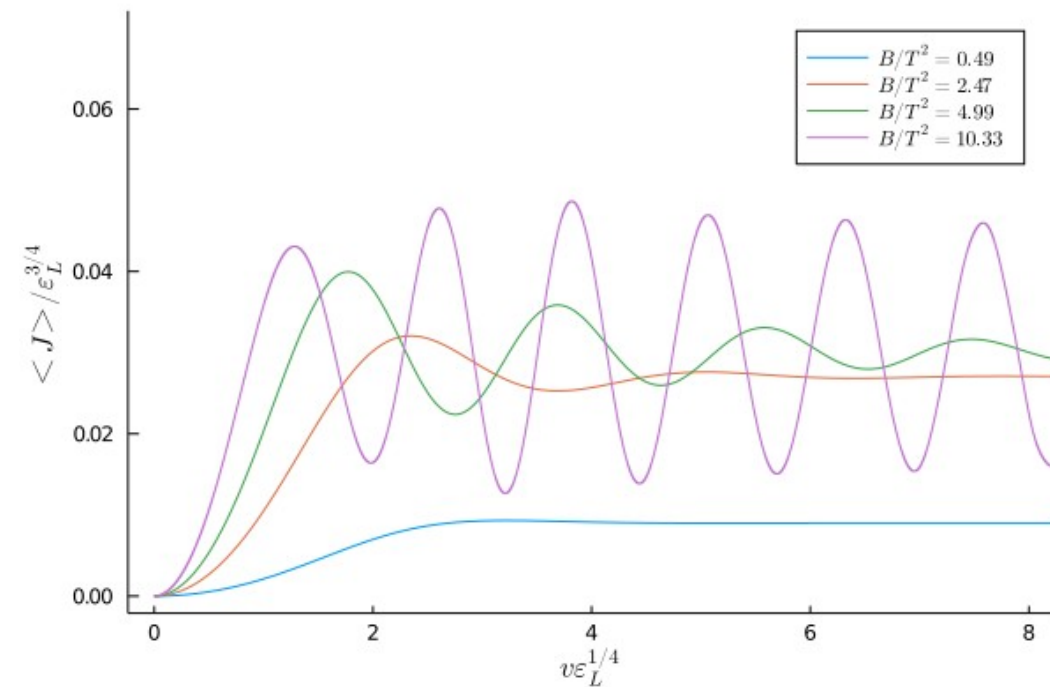


## Renormalization scale:

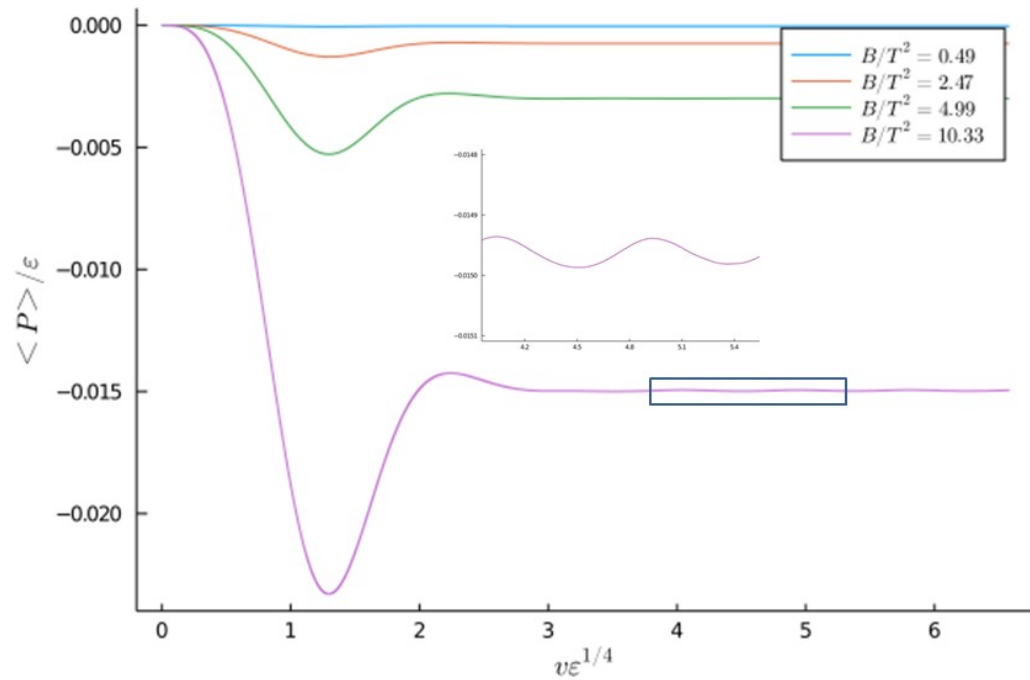
- Numerics  $\mu = 1/L$
  - Physics  $\mu = \sqrt{B}$
- $$\frac{\epsilon_B}{B^2} = \frac{\epsilon_L}{B^2} + \frac{1}{4} \log(BL^2)$$

# Holography

B-field dependence:  $q_5 = 0.2$  ,  $\alpha = 1.5$



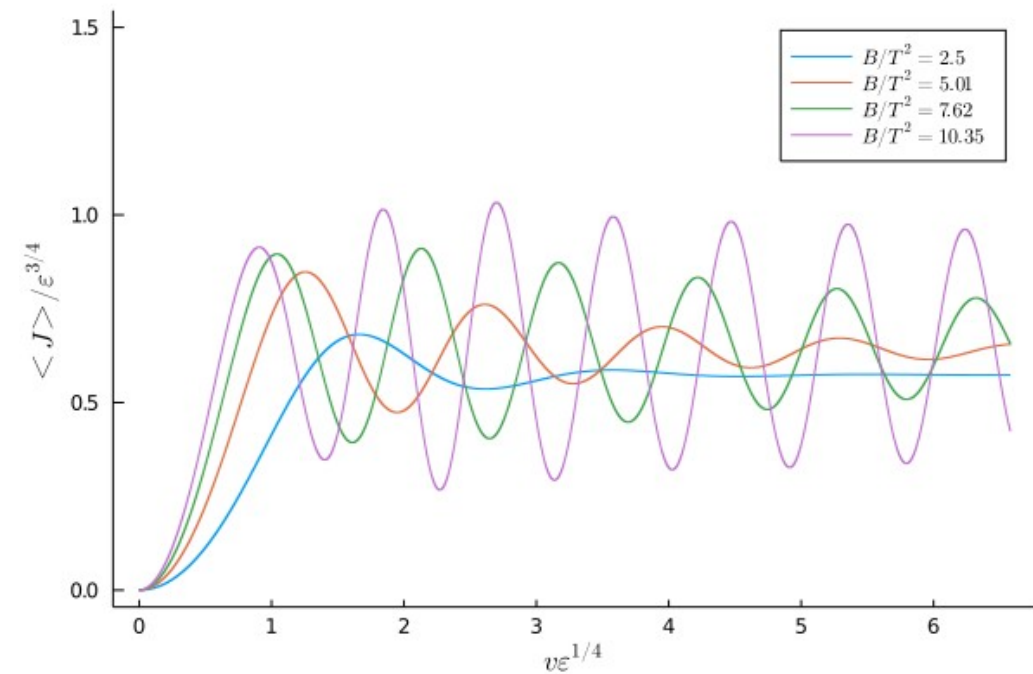
Current



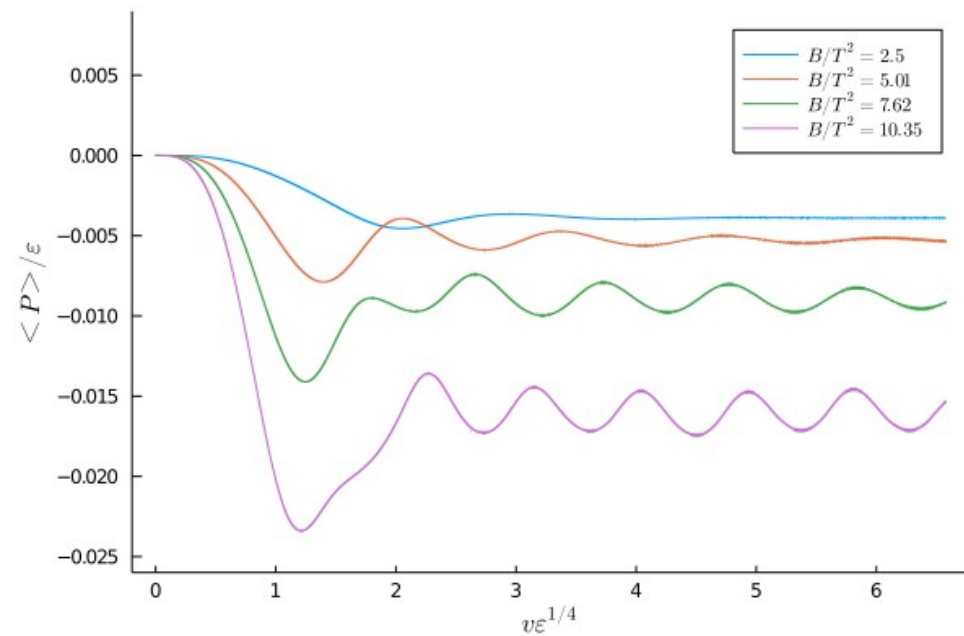
Pressure anisotropy

# Holography

B-field dependence:  $q_5 = 1.5$  ,  $\alpha = 1.5$



Current



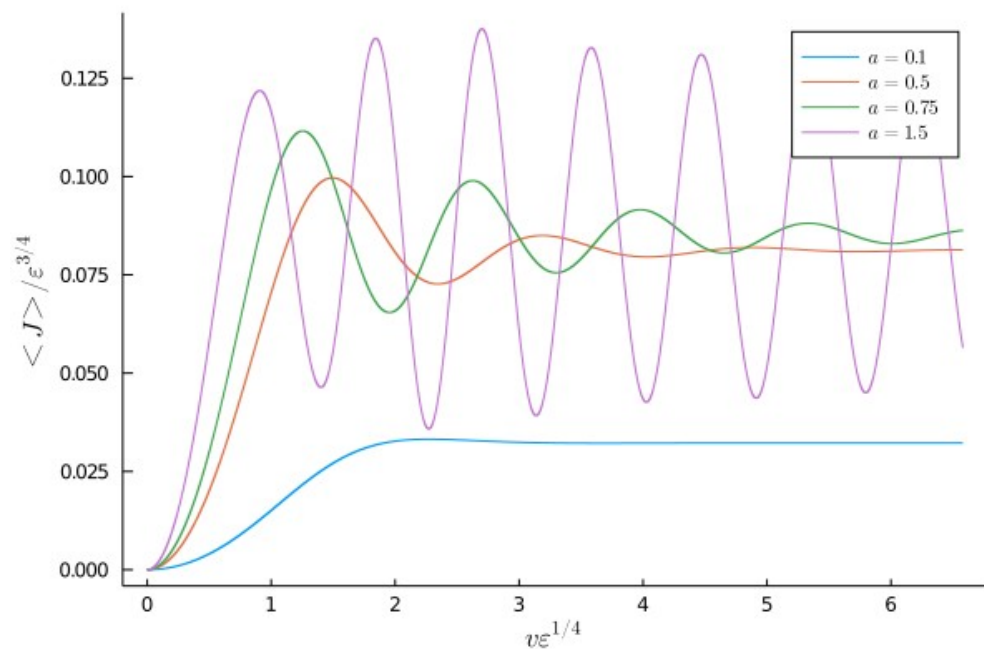
Pressure anisotropy

# Holography

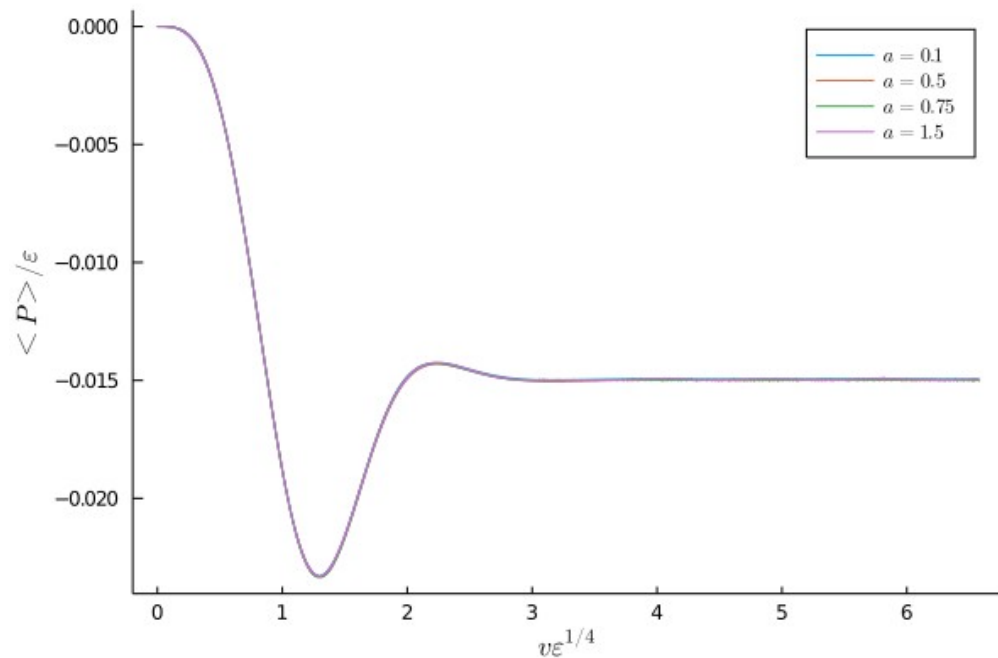
- Almost undamped oscillations: QNMs near the real axis  
[Ammon, Grieninger, Jimenez-Alba, Malcedo, Melgar]
- Define build up time to first maximum
- Observation: faster for larger magnetic field
- Lowest Landau Level: 2D physics! Operator relation  $J_5^\mu = \epsilon^{\mu\nu} J_\nu$

# Holography

Anomaly dependence:  $q_5 = 0.2$  ,  $B = 2$



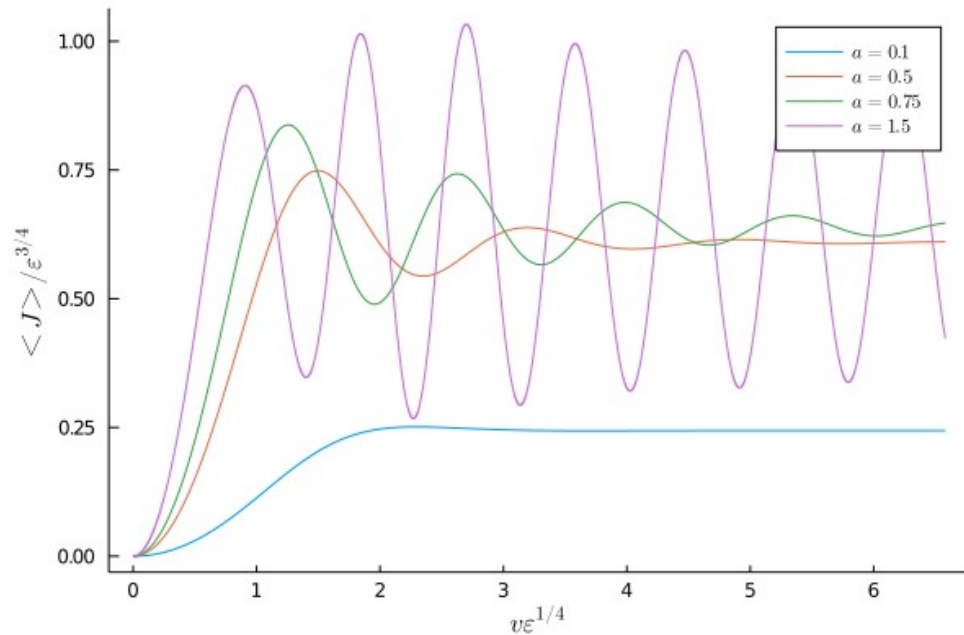
Current



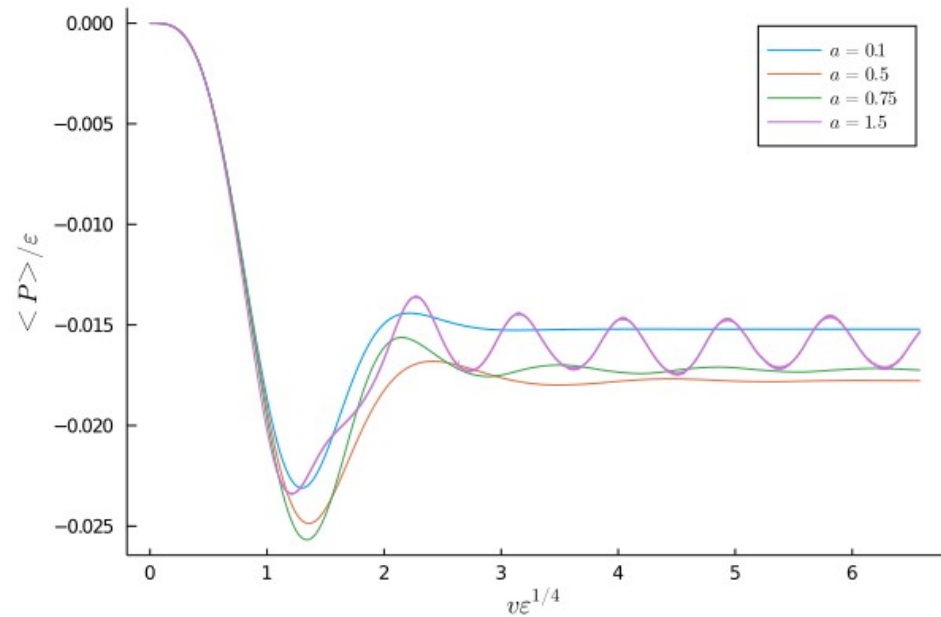
Pressure anisotropy

# Holography

Anomaly dependence:  $q_5 = 1.5$  ,  $B = 2$



Current



Pressure anisotropy

# Holography

## Matching couplings to QCD:

→ Gravitational coupling: match to entropy

$$s_{BH} = \frac{4\pi^2 T^3}{2\kappa^2} \quad s_{SB} = 4 \left( \nu_b + \frac{7}{4}\nu_f \right) \frac{\pi^2 T^3}{90}$$

$$s_{BH} = \frac{3}{4} s_{SB} \quad \Rightarrow \quad \kappa^2 \approx 12.5$$

→ Chern Simons coupling: match to anomaly

$$\frac{\alpha}{2\kappa^2} = \mathcal{A}_{QCD} = \frac{1}{8\pi^2} \quad \Rightarrow \quad \alpha \approx 0.316$$



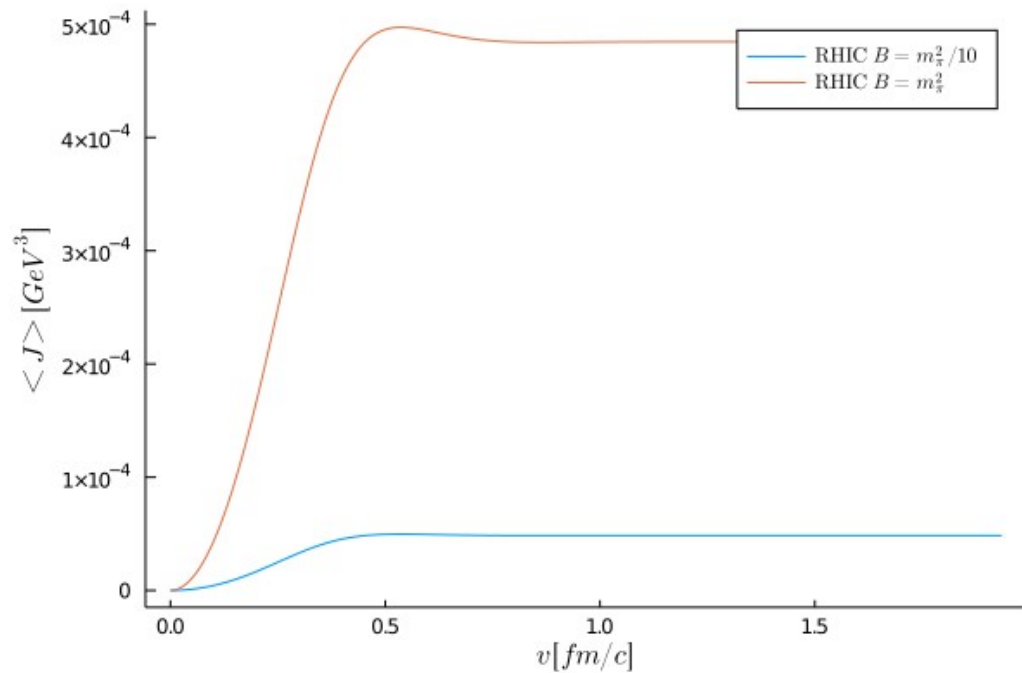
# Holography

Physical parameters:

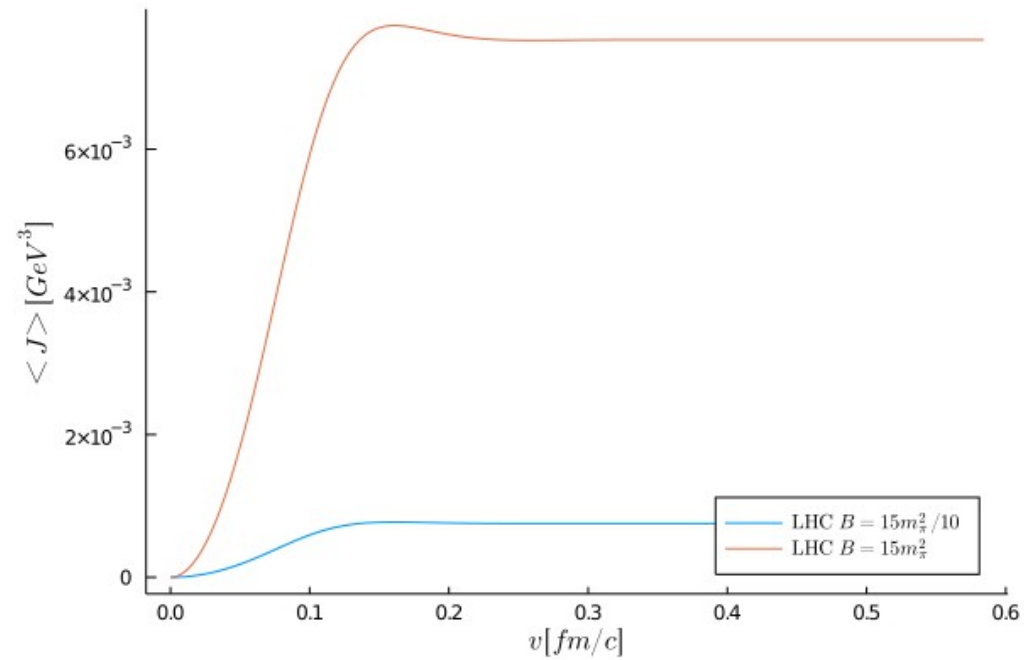
	“RHIC”	“LHC”
T	300MeV	1000MeV
$\mu_5$	10 (100) MeV	10 (100) MeV
B	1 (0.1) $m_\pi^2$	15 (1.5) $m_\pi^2$

# Holography

## CME current



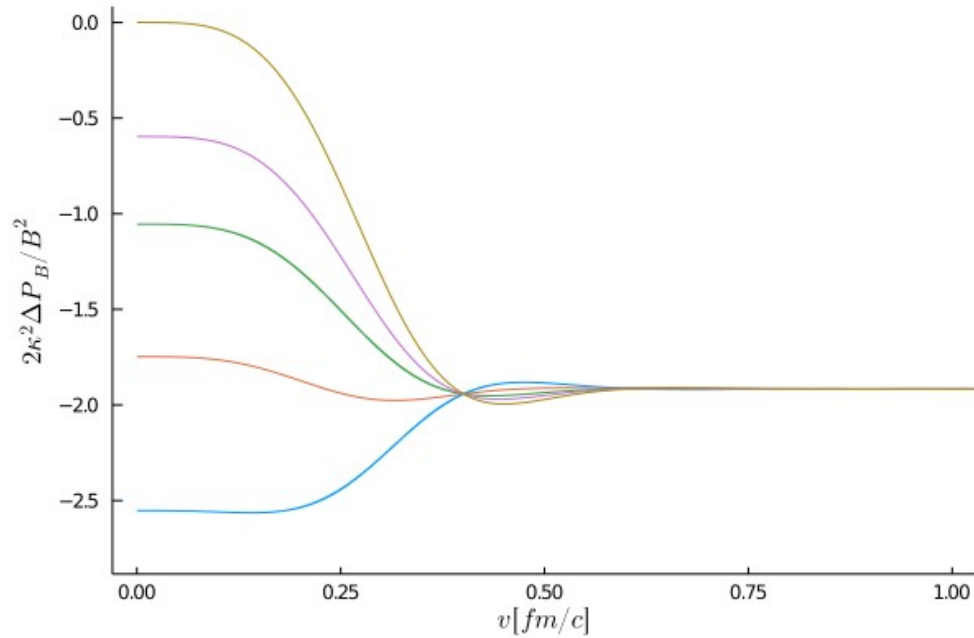
RHIC



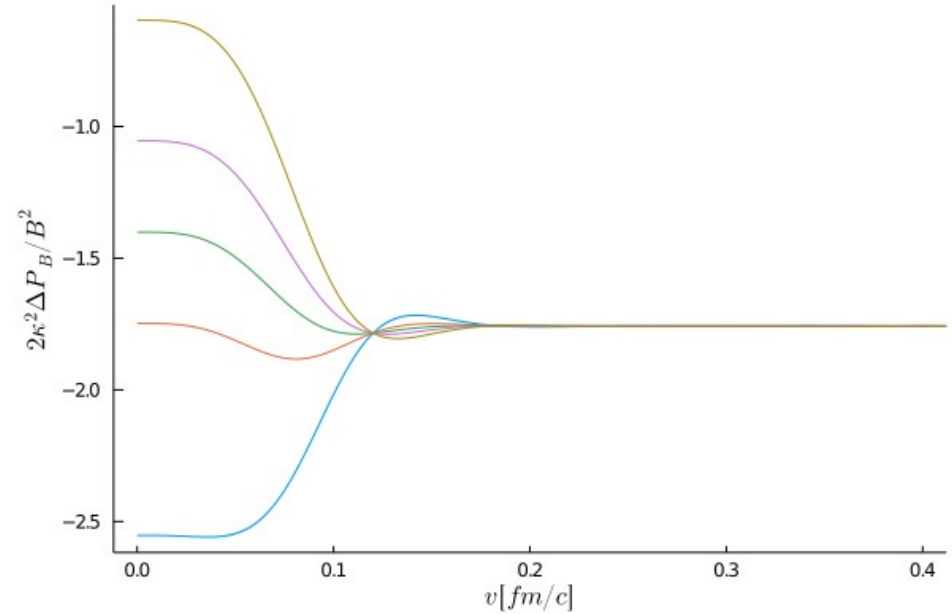
LHC

# Holography

Pressure anisotropy (large B)



RHIC



LHC

$$2\kappa^2 \frac{\Delta P_B}{B^2} = 12 \frac{\xi_4(v)}{B^2} + \frac{1}{2} \log(BL^2) - \frac{1}{4}$$

$$4\kappa^2 \frac{\epsilon_B}{B^2} = 6 \frac{f_2}{B^2} - \frac{1}{2} \log(BL^2)$$

# Holography

- No oscillations !
- Equilibration time: within 10% of final value [Chesler, Yaffe]

RHIC  $B = m_\pi^2$

$\delta P_i$	-2.55	-1.75	-1.05	-0.60	0.00
$v_{\text{eq}}^{\langle J \rangle}$ in [fm/c]	0.380	0.380	0.380	0.380	0.380
$v_{\text{eq}}^{\langle \Delta P \rangle}$ in [fm/c]	0.383	0.418	0.334	0.344	0.350

RHIC  $B = 0.1 m_\pi^2$


$\delta P_i$	-3.70	-2.90	-2.55	-2.21	-1.75
$v_{\text{eq}}^{\langle J \rangle}$ in [fm/c]	0.380	0.380	0.380	0.380	0.380
$v_{\text{eq}}^{\langle \Delta P \rangle}$ in [fm/c]	0.383	0.418	0.310	0.334	0.344

LHC  $B = 15 m_\pi^2$

$\delta P_i$	-2.55	-1.75	-1.40	-1.05	-0.60
$v_{\text{eq}}^{\langle J \rangle}$ in [fm/c]	0.114	0.114	0.114	0.114	0.114
$v_{\text{eq}}^{\langle \Delta P \rangle}$ in [fm/c]	0.114	0.187	0.085	0.098	0.103

LHC  $B = 1.5 m_\pi^2$

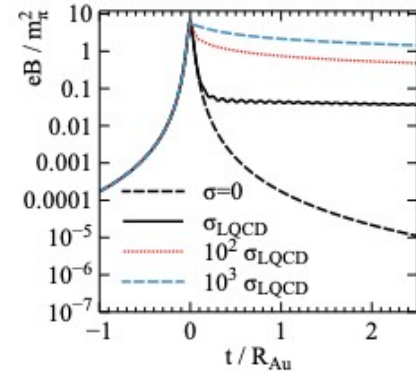
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$v_{\text{eq}}^{\langle \Delta P \rangle}$ in [fm/c]	0.114	0.187	0.085	0.098	0.103

Compare to  Without anomaly [Chesler, Yaffe]:  $\tau \sim 0.5$  fm/c  
Experimental estimate [U. Heinz]:  $\tau \sim 0.3$  fm/c

# Holography

## Lifetime of magnetic field

- Highly uncertain
- Rapid decay in vacuum
- Medium effects can prolong lifetime considerably
- Many different estimates in literature



[McLerran, Skokov] ] Nucl.Phys.A 929 (2014) 184

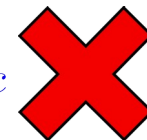
Latest available estimate: [Guo, Feng, Liao, Shi] Phys.Lett.B 798 (2019) 134929

$$\tau_B = \frac{117}{\sqrt{s}} \text{GeV fm}/c$$

$$\tau_B^{RHIC} \approx 0.6 \text{fm}/c$$



$$\tau_B^{LHC} \approx 0.02 \text{fm}/c$$



# Summary and Outlook

- *Holography allows to address important issues for CME@HIC*
- *Even simple models give interesting results*
- *Indicates that*
  - *CME@LHC is not effective*
  - *CME@RHIC is save*
- *Many model improvements are possible*

*(Dynamical B-field, expanding plasma, finite axial lifetime, ...)*



C. Cartwright's talk on Friday

**THANKS!**