

Lattice 2014

USQCD
ALCC

Higgs physics near the conformal window

Lattice Higgs Collaboration (LatHC)

Zoltan Fodor, Kieran Holland, Santanu Mondal,
Daniel Nogradi, Chik Him Wong

Julius Kuti

University of California, San Diego

Lattice 2014 Symposium, July 23-28, 2014

Talk is based on 6 publications, with an overview and added discussion of new developments

Szabolcs Borsanyi, [Zoltan Fodor](#), [Kieran Holland](#), [Julius Kuti](#), [Santanu Mondal](#), [Daniel Nogradi](#), [Chik Him Wong](#).
July 2014, in preparation

The lattice gradient flow at tree-level and its improvement

[Zoltan Fodor](#), [Kieran Holland](#), [Julius Kuti](#), [Santanu Mondal](#), [Daniel Nogradi](#), [Chik Him Wong](#). Jun 3, 2014. 14 pp.
e-Print: [arXiv:1406.0827](#) [hep-lat]

The chiral condensate from the Dirac spectrum in BSM gauge theories

[Zoltan Fodor](#), [Kieran Holland](#), [Julius Kuti](#), [Daniel Nogradi](#), [Chik Him Wong](#). Feb 24, 2014. 7 pp.
Conference: [C13-07-29.1 Proceedings](#)
e-Print: [arXiv:1402.6029](#) [hep-lat] | [PDF](#)

Can a light Higgs impostor hide in composite gauge models?

[Zoltan Fodor](#), [Kieran Holland](#), [Julius Kuti](#), [Daniel Nogradi](#), [Chik Him Wong](#). Jan 9, 2014. 7 pp.
Conference: [C13-07-29.1 Proceedings](#)
e-Print: [arXiv:1401.2176](#) [hep-lat] | [PDF](#)

The Yang-Mills gradient flow in finite volume

[Zoltan Fodor](#) ([Wuppertal U.](#) & [IAS, Julich](#) & [Eotvos U.](#)), [Kieran Holland](#) ([U. Pacific, Stockton](#) & [Bern U.](#)), [Julius Kuti](#) ([UC, San Diego](#)), [Daniel Nogradi](#) ([Eotvos U.](#)), [Chik Him Wong](#) ([UC, San Diego](#)). Aug 2012. 17 pp.
Published in **JHEP 1211 (2012) 007**
DOI: [10.1007/JHEP11\(2012\)007](#)
e-Print: [arXiv:1208.1051](#) [hep-lat] | [PDF](#)

Can the nearly conformal sextet gauge model hide the Higgs impostor?

[Zoltan Fodor](#) ([Wuppertal U.](#) & [IAS, Julich](#) & [Eotvos U.](#)), [Kieran Holland](#) ([U. Pacific, Stockton](#)), [Julius Kuti](#) ([UC, San Diego](#)), [Daniel Nogradi](#) ([Eotvos U.](#)), [Chris Schroeder](#) ([LLNL, Livermore](#)), [Chik Him Wong](#) ([UC, San Diego](#)). Sep 2012. 10 pp.
Published in **Phys.Lett. B718 (2012) 657-666**
DOI: [10.1016/j.physletb.2012.10.079](#)
e-Print: [arXiv:1209.0391](#) [hep-lat] | [PDF](#)

Outline

Near-conformal light Higgs?

light scalar (dilaton-like?) close to conformal window?
EW precision and S-parameter
scale setting and spectroscopy Wong's talk 2C

Running coupling

running (walking?) coupling from gradient flow
Nogradi 7E Thursday

Chiral condensate

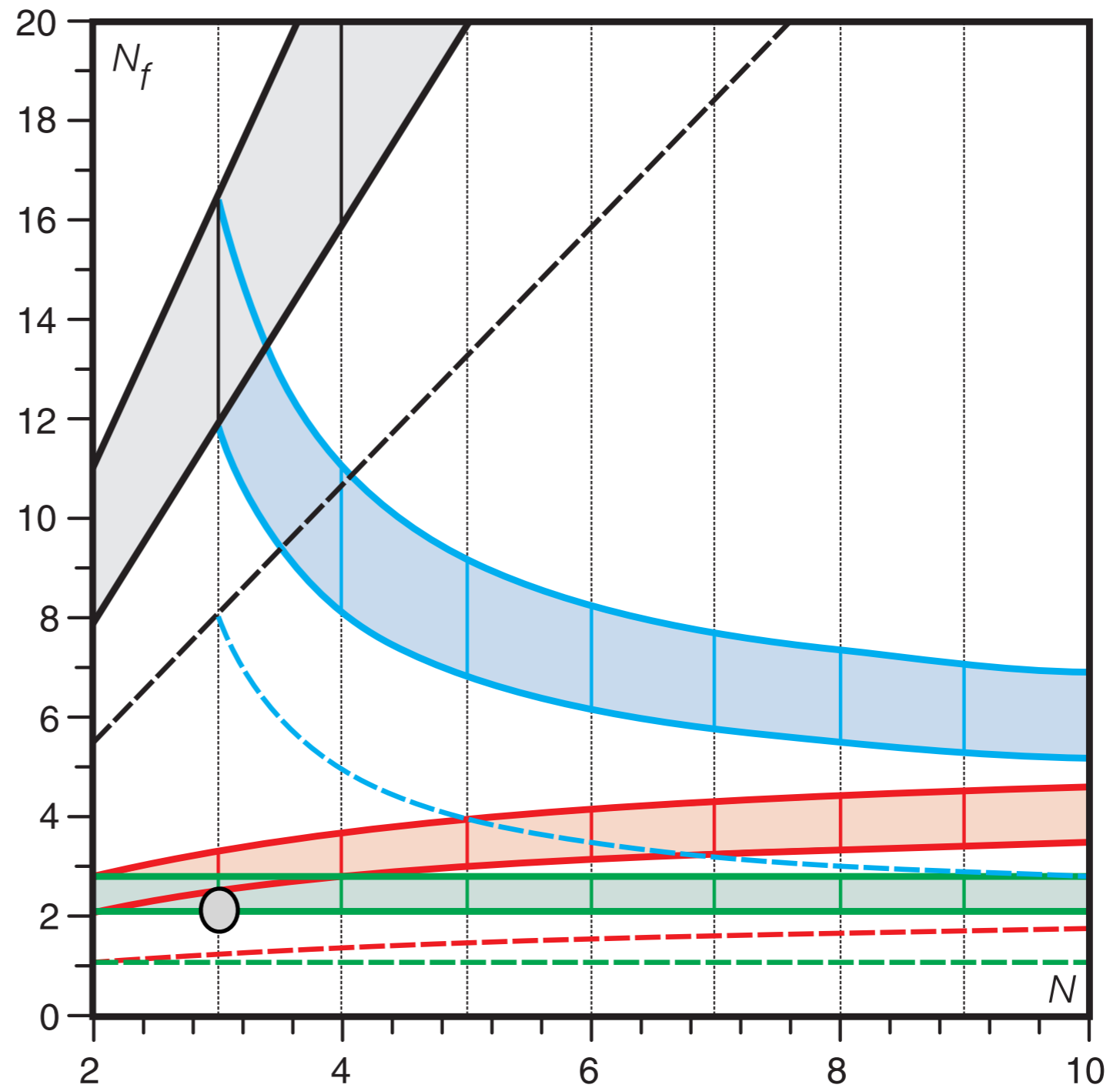
new stochastic method for spectral density
mode number
topology
anomalous dimension

Early universe

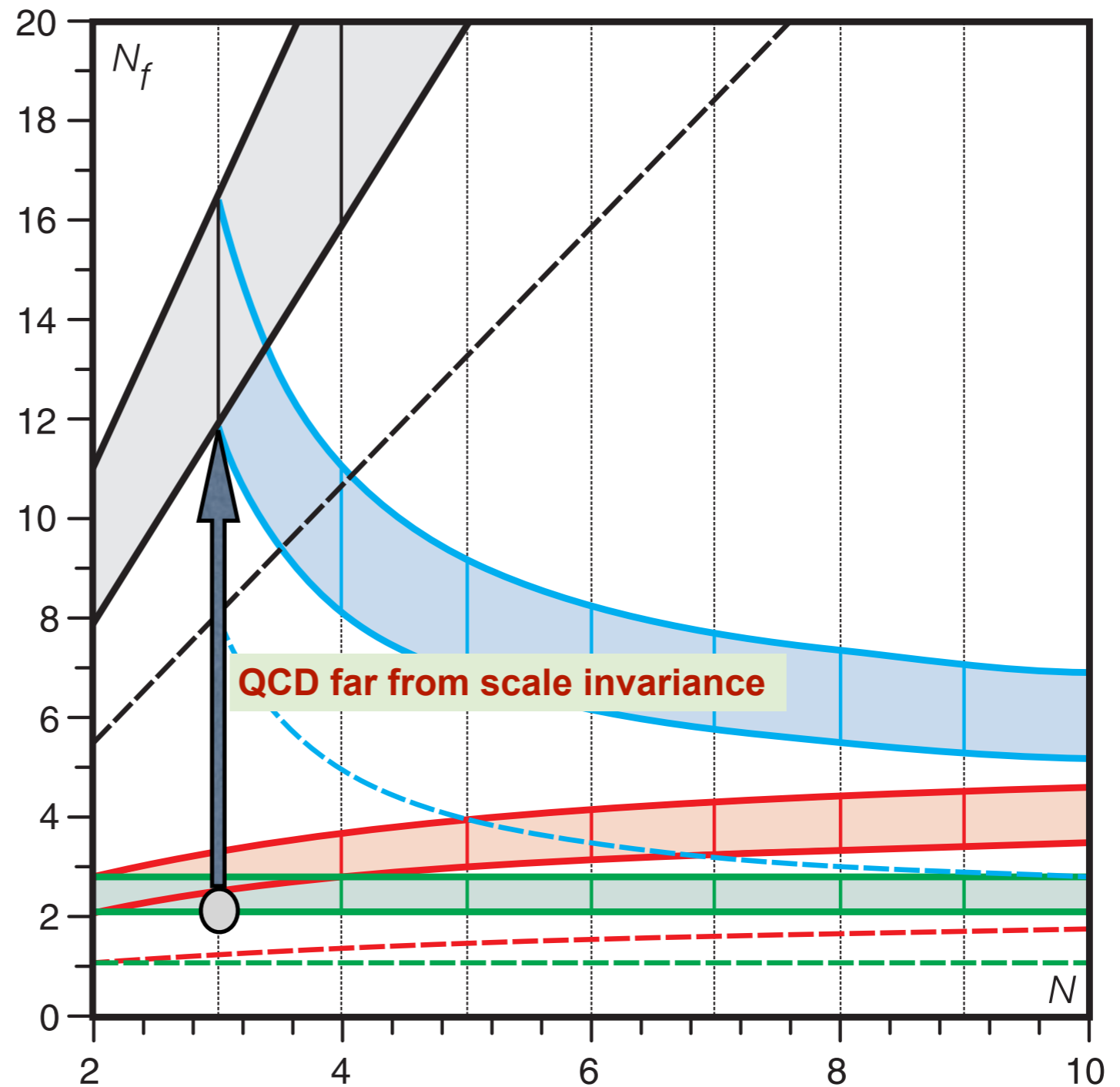
EW phase transition
dark matter Mondal 8C Friday

Summary and Outlook

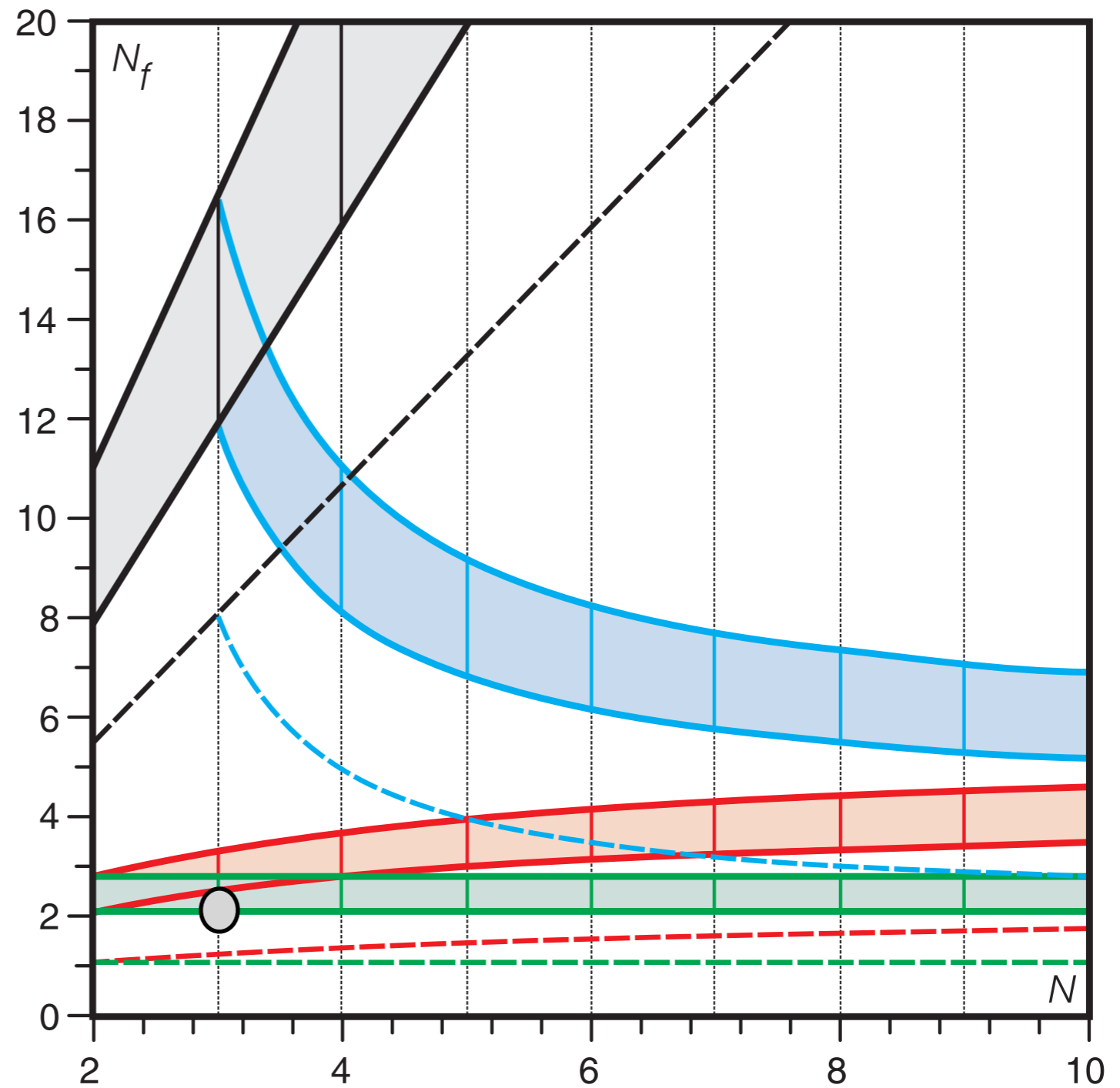
near-conformal light Higgs (dilaton-like?) sextet rep



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near-conformal light Higgs (dilaton-like?) sextet rep

to illustrate: sextet SU(3) color rep

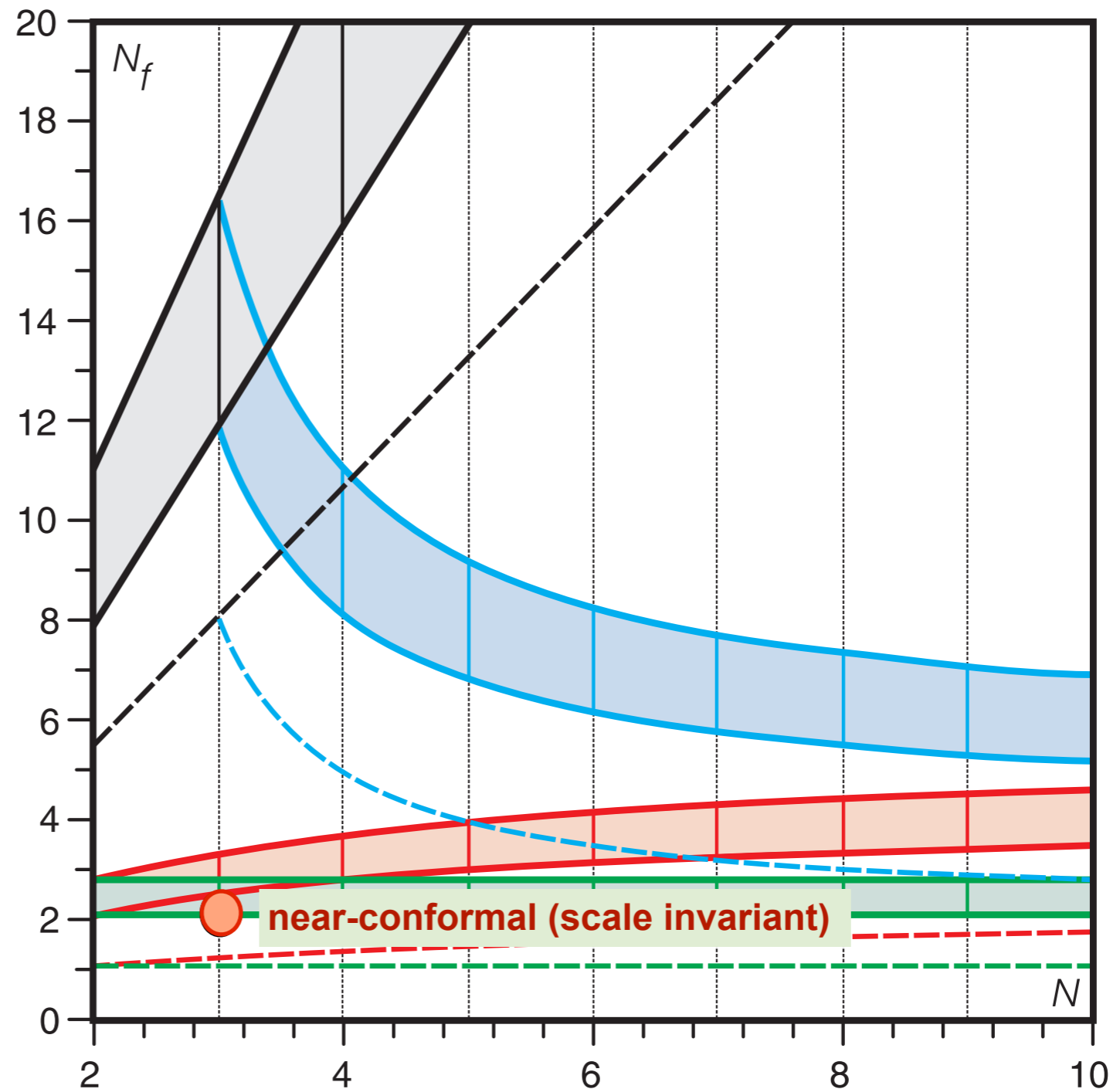
one massless fermion doublet $\begin{bmatrix} u \\ d \end{bmatrix}$

χ SB on $\Lambda \sim \text{TeV}$ scale

three Goldstone pions
become longitudinal
components of weak bosons

composite Higgs mechanism
scale of Higgs condensate
 $\sim F=250 \text{ GeV}$

conflicts with EW constraints?



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to apply QCD intuition to
near-conformal compositeness
is just plain wrong

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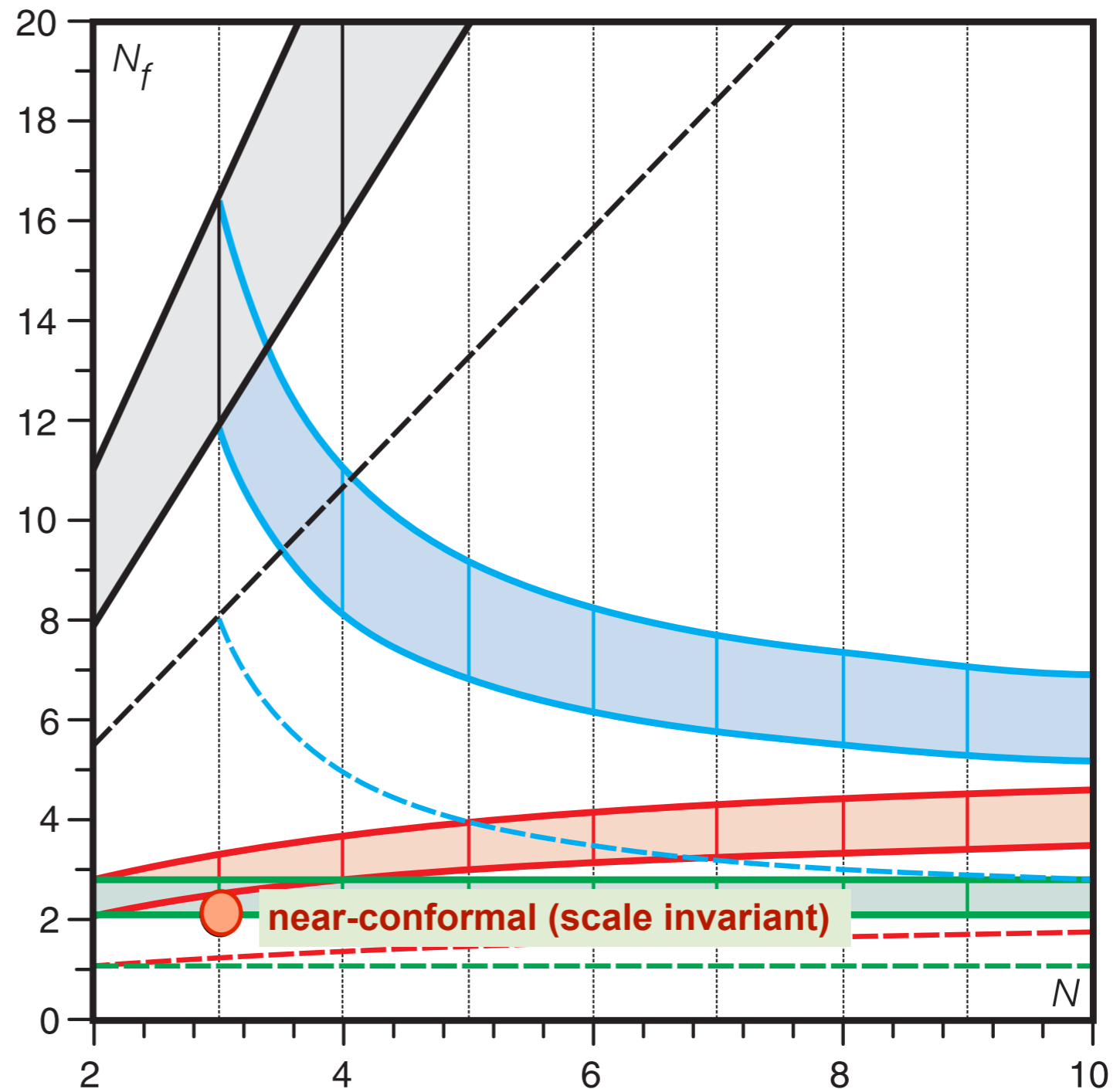
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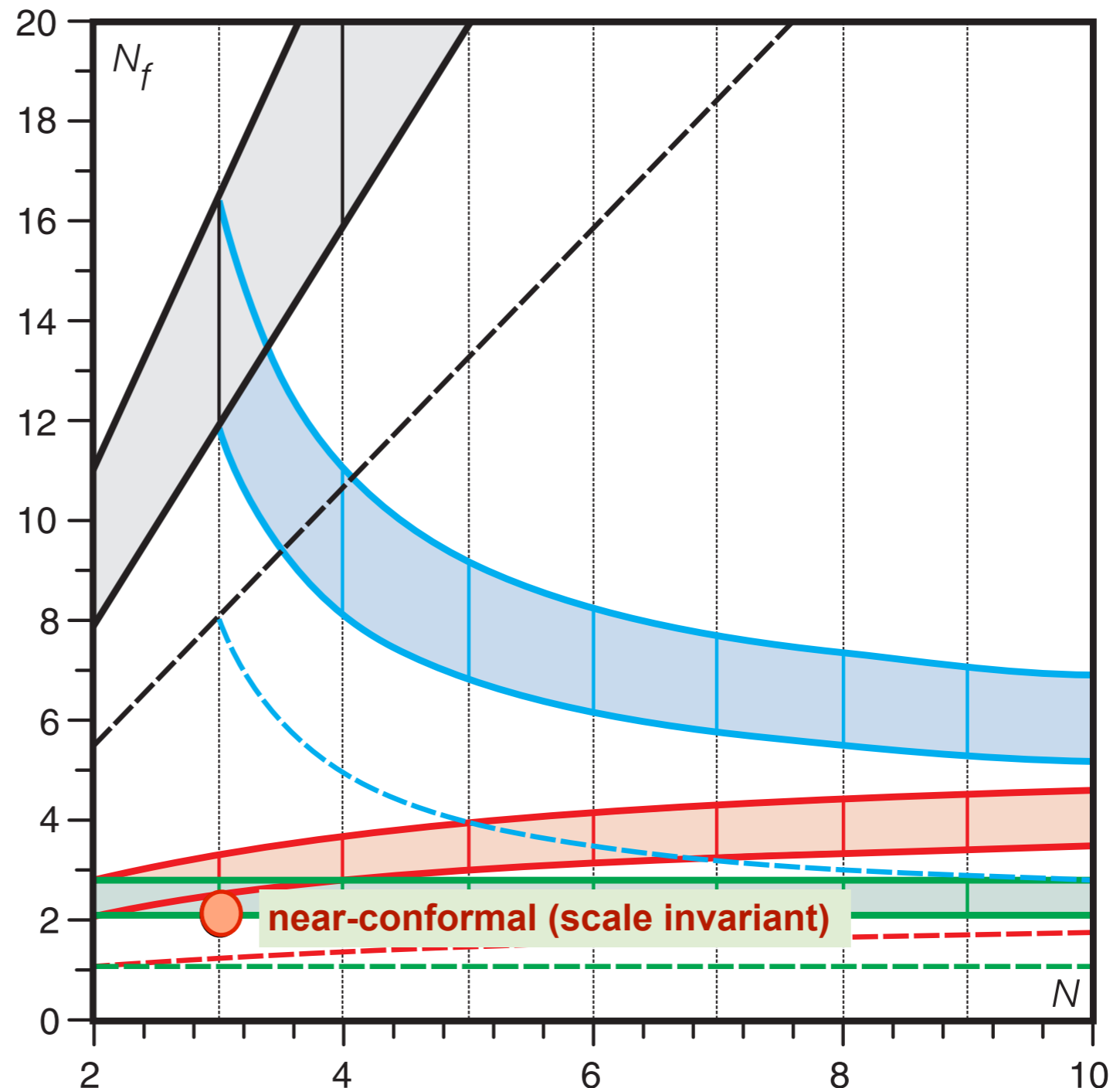
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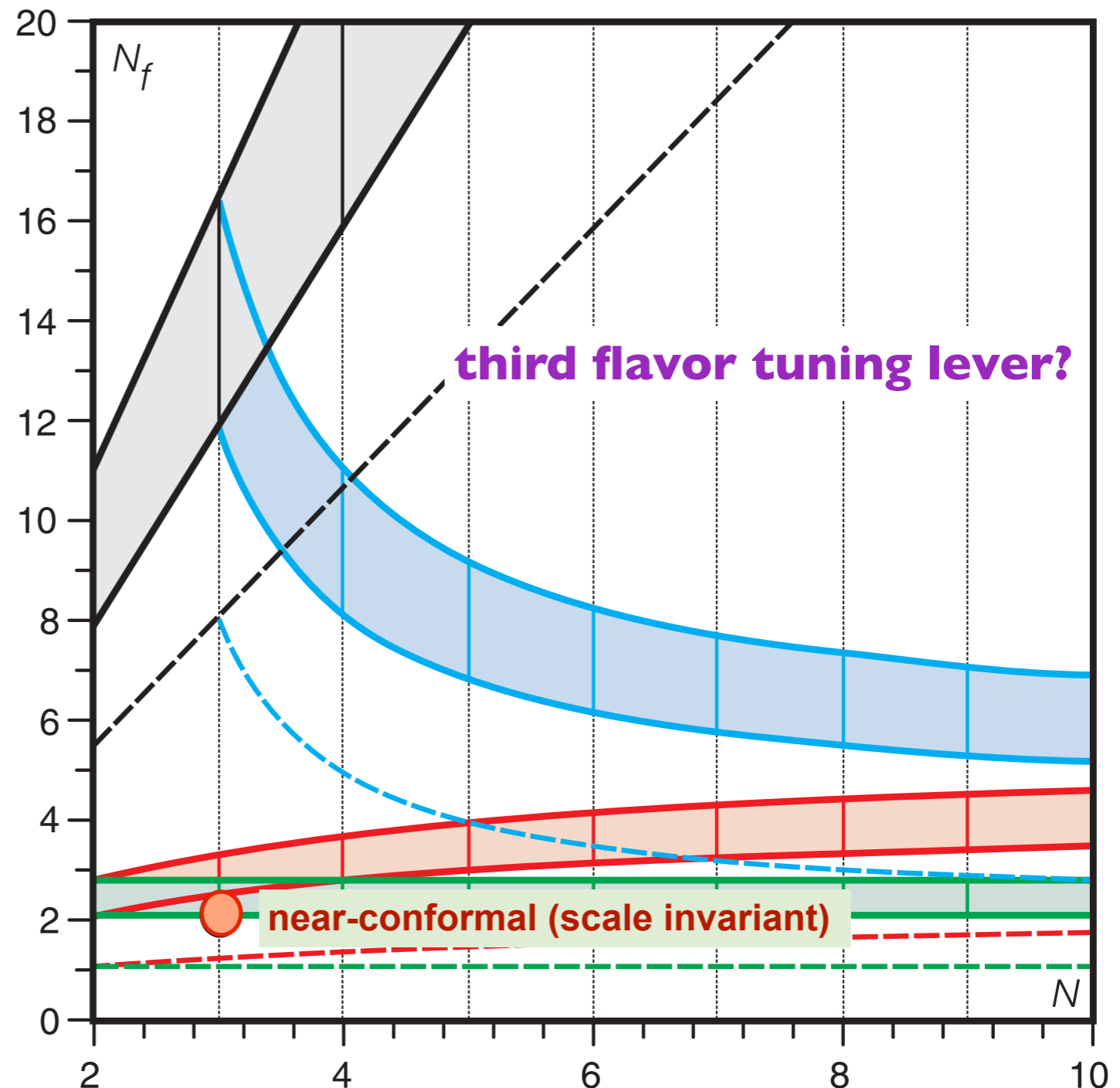
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Partially Conserved Dilatation Current (PCDC)

Will gradient flow based technology make the argument less slippery?

Dilatation current

Bardeen et al., Ellis, Yamawaki, Miransky, Appelquist, ...

$$m_\sigma^2 \simeq -\frac{4}{f_\sigma^2} \langle 0 | [\Theta_\mu^\mu(0)]_{NP} | 0 \rangle$$

$$\partial_\mu \mathcal{D}^\mu = \Theta_\mu^\mu = \frac{\beta(\alpha)}{4\alpha} G_{\mu\nu}^a G^{a\mu\nu}$$

$$\langle 0 | \Theta^{\mu\nu}(x) | \sigma(p) \rangle = \frac{f_\sigma}{3} (p^\mu p^\nu - g^{\mu\nu} p^2) e^{-ipx}$$

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$$[\Theta_\mu^\mu]_{NP} = \frac{\beta(\alpha)}{4\alpha} [G_{\mu\nu}^a G^{a\mu\nu}]_{NP} \quad \frac{m_\sigma}{f_\sigma} \rightarrow ?$$

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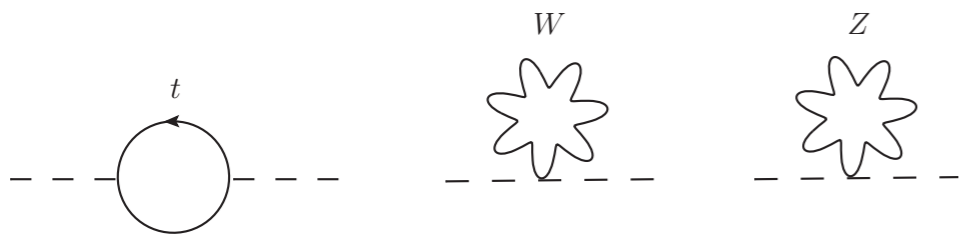
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light composite scalar, but
how light is light ?

few hundred GeV Higgs impostor?

Foadi, Frandsen, Sannino

open for spirited theory discussions



$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

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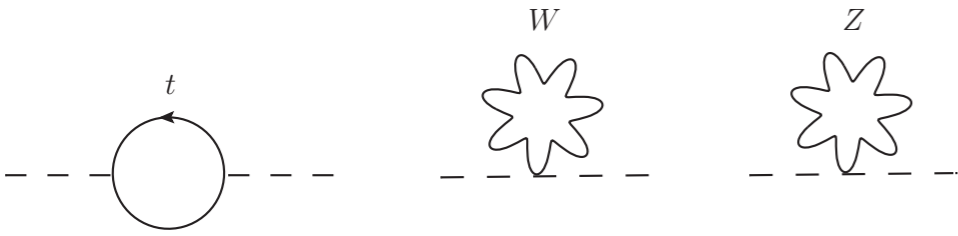
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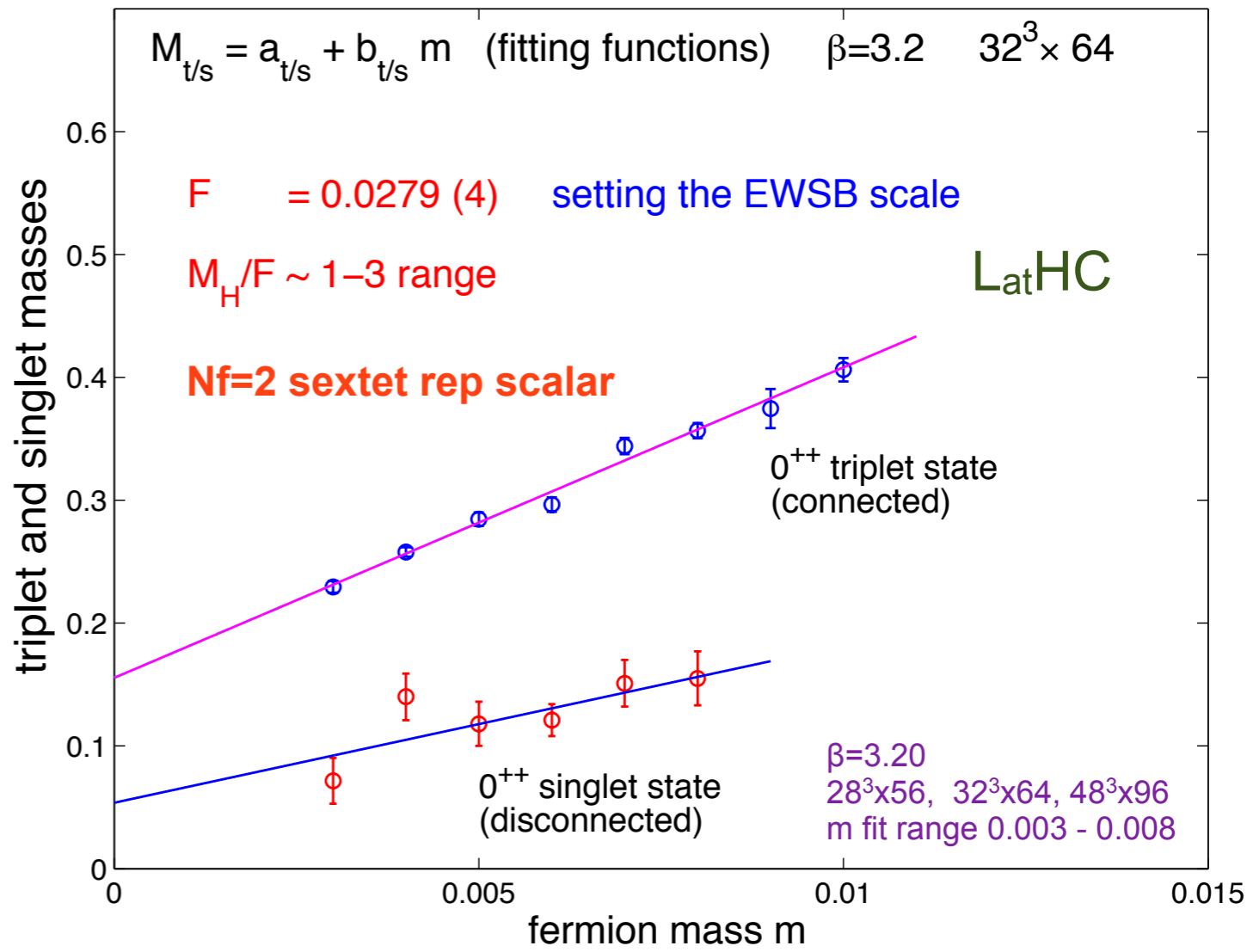
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Triplet and singlet masses from 0⁺⁺ correlators



near-conformal light Higgs (dilaton-like?) sextet rep

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“just a light scalar on the lattice, or perhaps dilaton like” ?

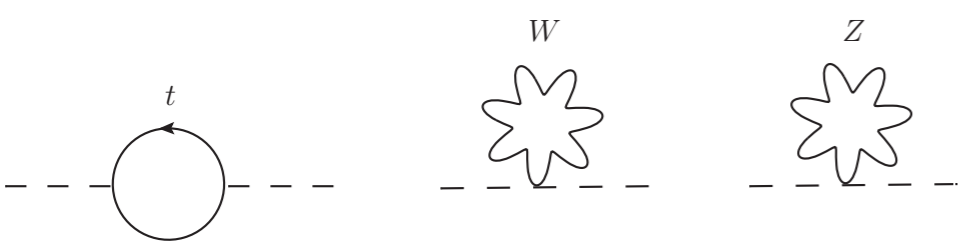
We started a second generation run set

first results in Wong’s talk

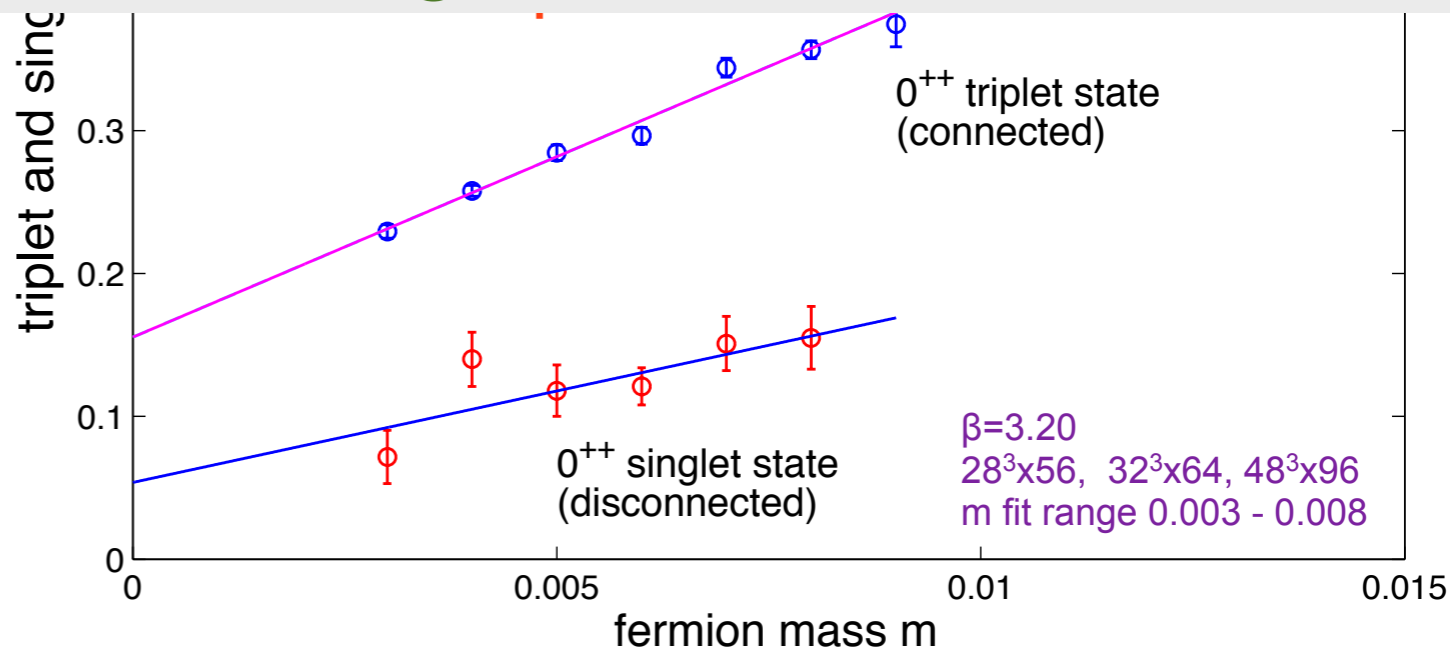
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new code (sextet Janos) is highly optimized **Borsanyi/Wong effort**
In production now to answer important questions in second generation run set:

1. Test of chiral perturbation theory below the scale of low mass scalar?

requires new effective action

how to test if light scalar is dilaton-like? effective theory of dilaton?

RMT and Dirac spectral density on two scales (m and λ)

2. Needs precise scale setting and resonance spectrum

S and T parameters of Electroweak precision tests

large volumes **$F \cdot L \sim 1$, or larger!**

slow topology?

We are in a second generation run set

$\beta=3.15, 3.20, 3.25, 3.30$ gauge couplings

$48^3 \times 96, 40^3 \times 80, 32^3 \times 64$ volumes

at least 3 fermion masses in each run

eventually we might need some $L=64$ runs

3. Running (walking?) coupling

volume-dependent running coupling

scale-dependent $L = \infty$ coupling in chiral limit

4. Consistent chiral condensate?

GMOR relation is still not quite consistent

new method for spectral density and mode number

anomalous dimension of chiral condensate

dependence on topology


TeV

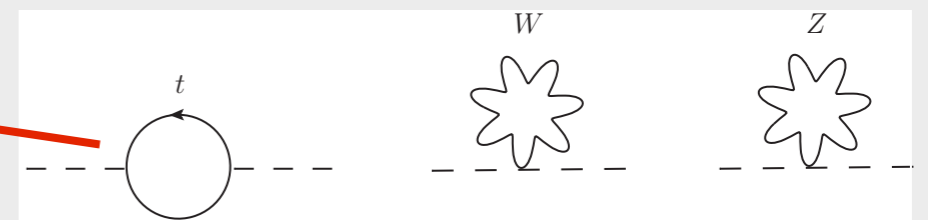
_____	N	~ 3.2 TeV
_____	A ₁	~ 2.7 TeV
=====	Rho	~ 1.9 TeV
=====	A ₀	~ 1.7 TeV

near-conformal resonance spectrum
separated from light scalar

within LHC14 reach

Wong's talk

_____ scalar impostor few hundred GeV?

 _____ EW self-energy shift
 _____ observed Higgs-like?

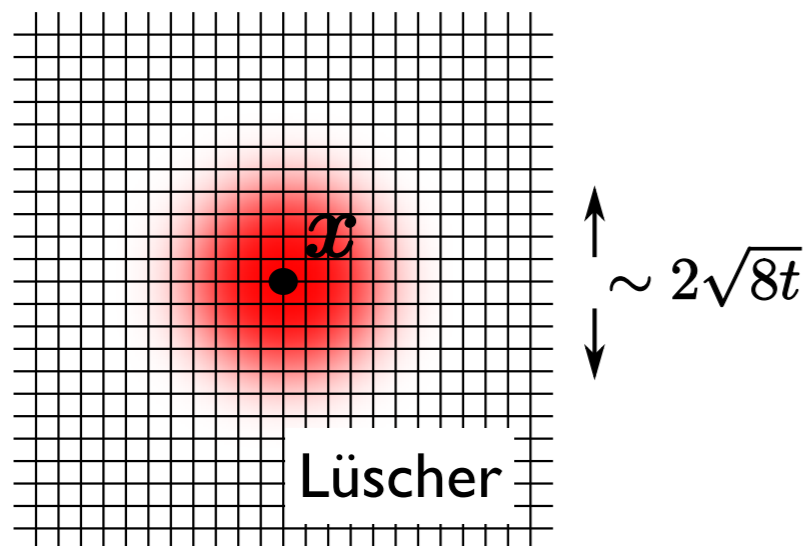
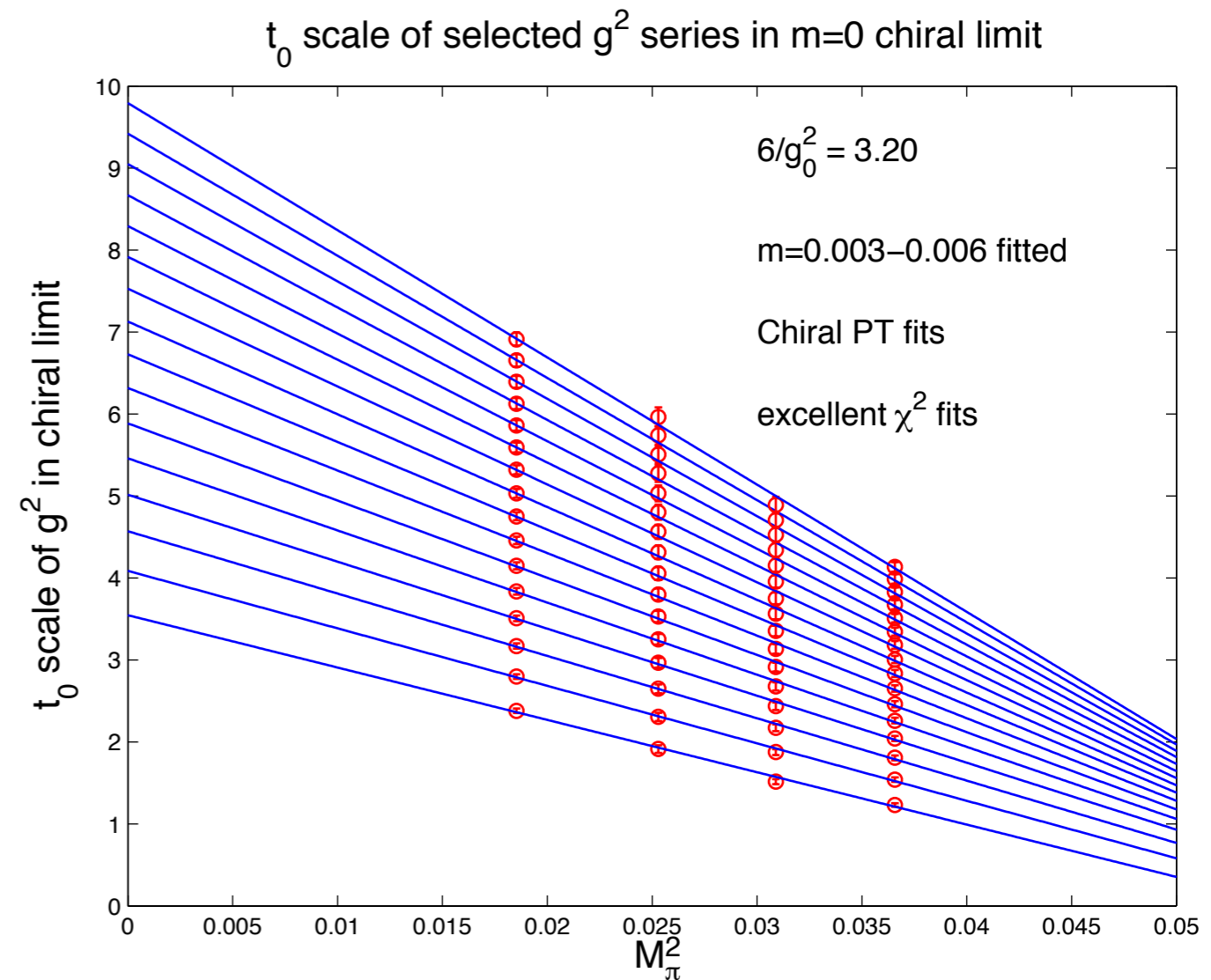
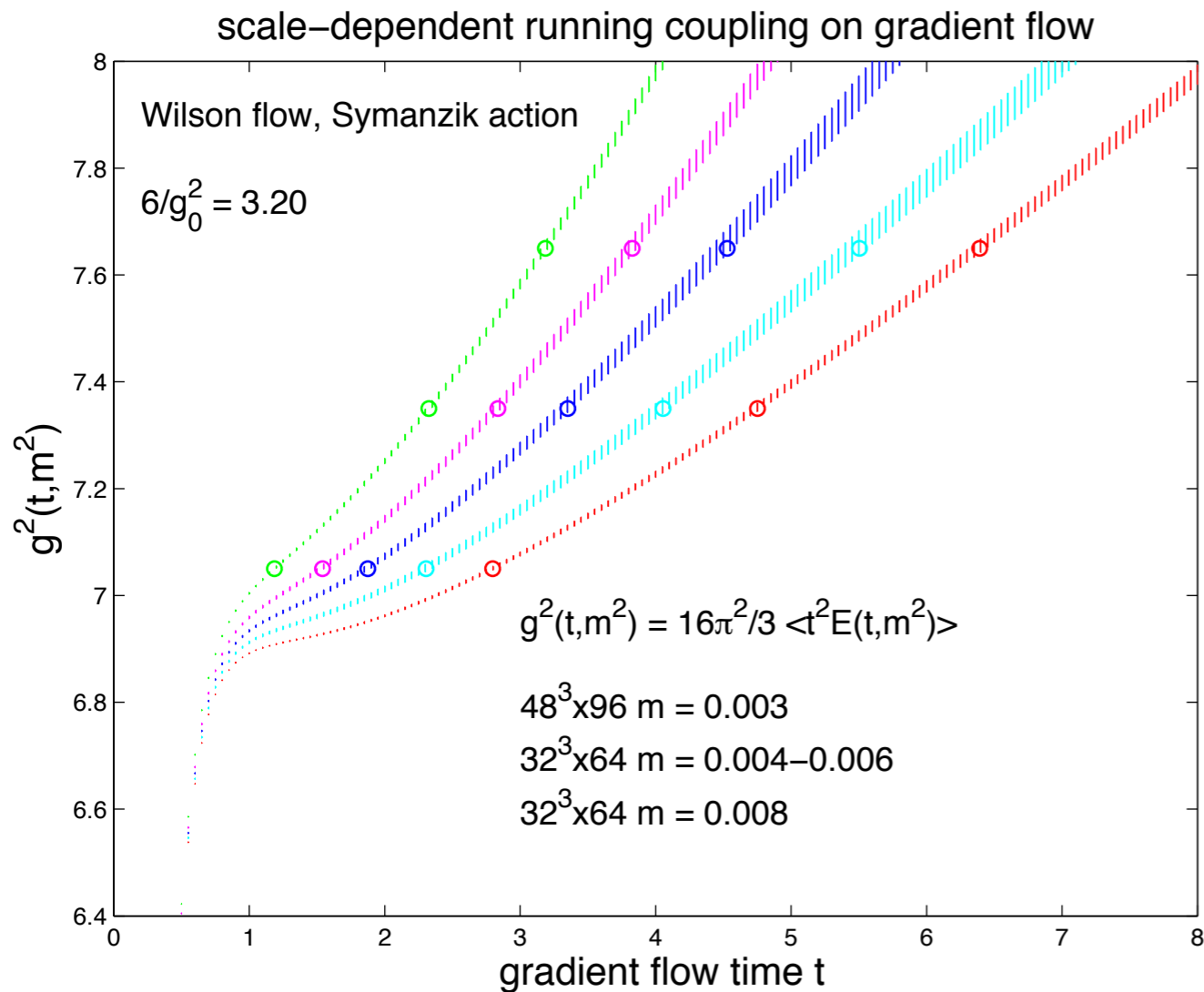


$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

We are in a second generation run set pushing the resonance spectrum somewhat higher

running coupling and beta function from gradient flow

sextet rep



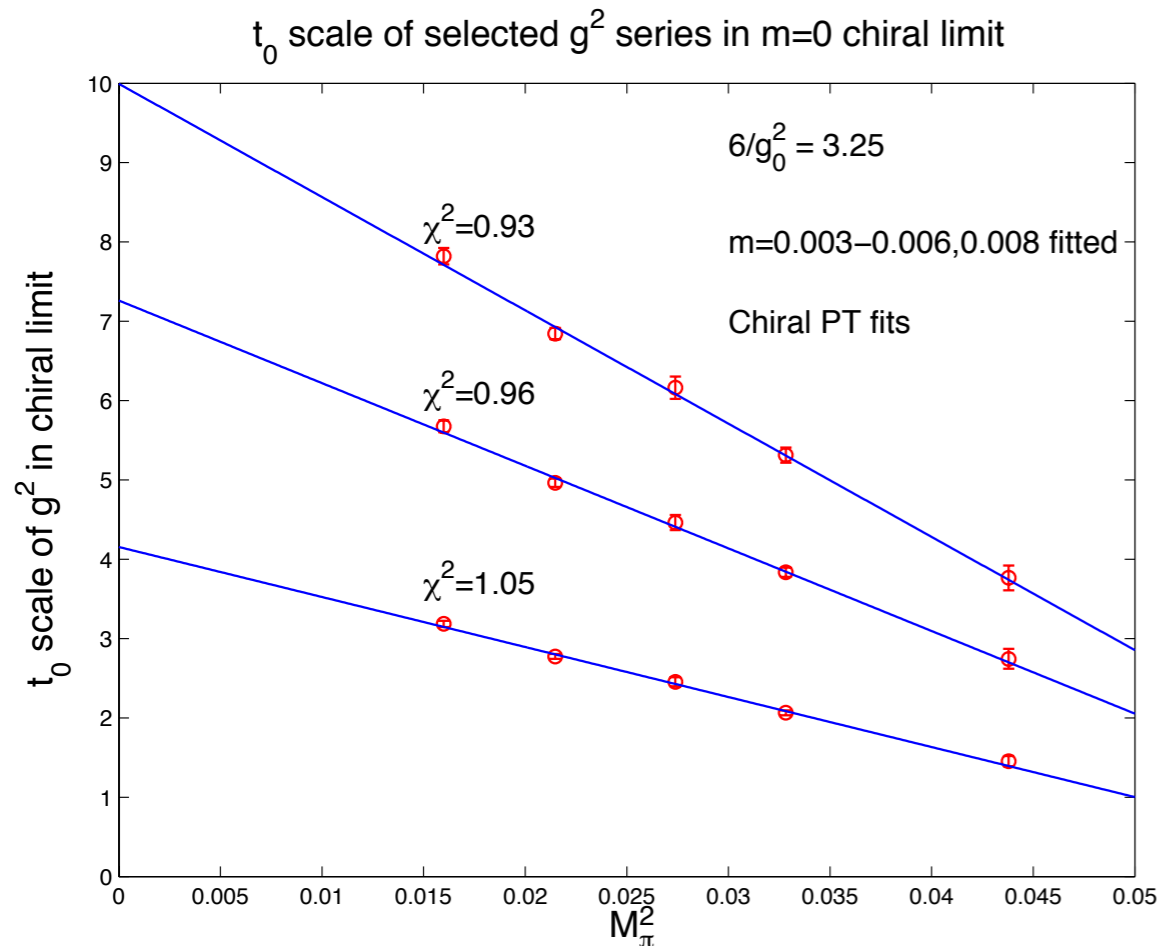
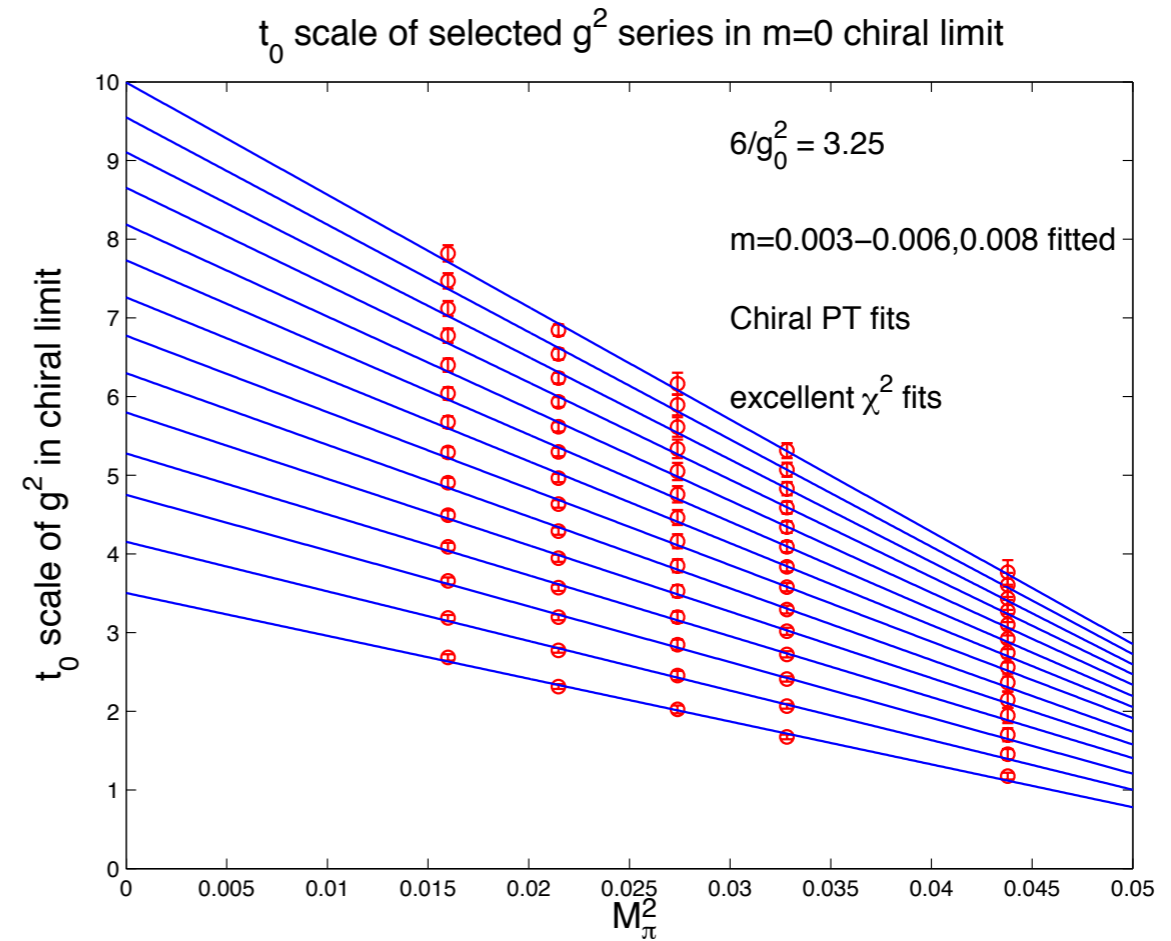
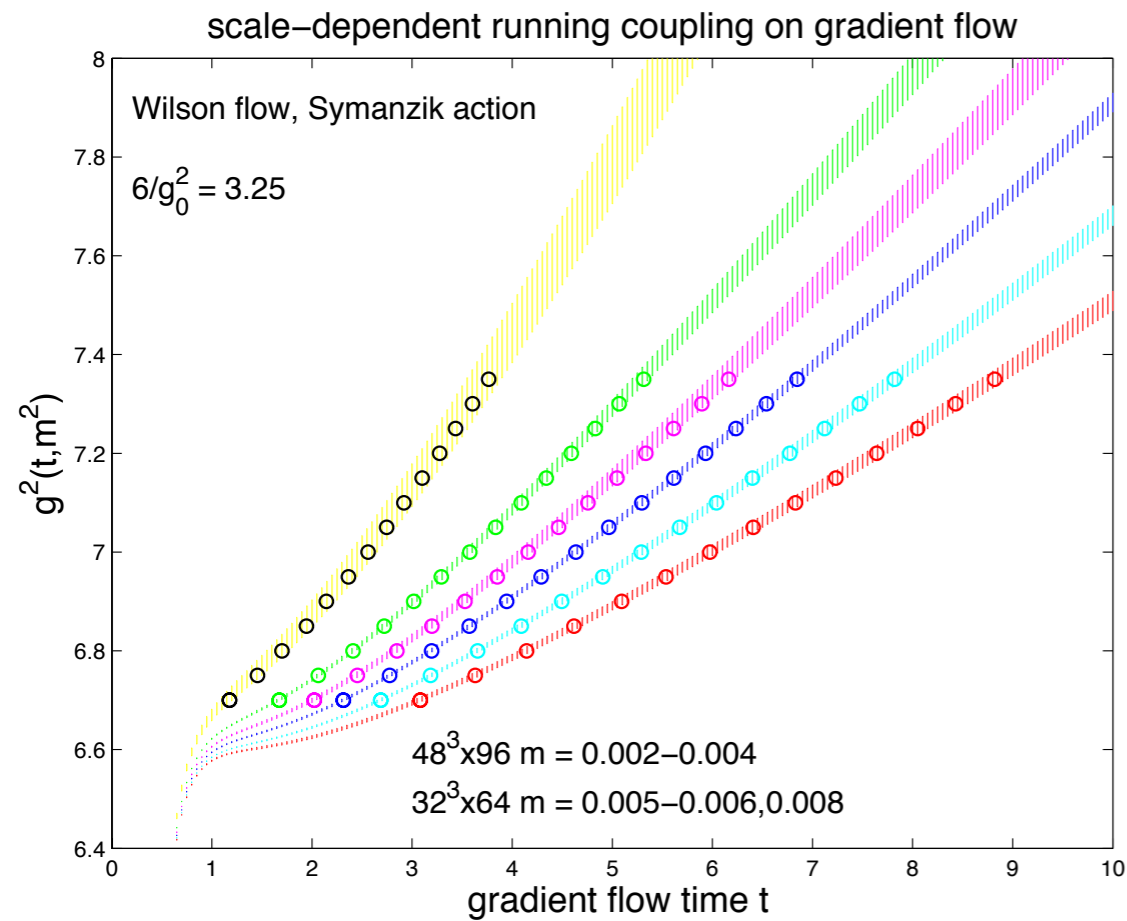
operator is quasi-point source of pions

controlled in chiPT

Bär and Golterman

fits of leading chiPT are excellent

running coupling and beta function from gradient flow sextet rep

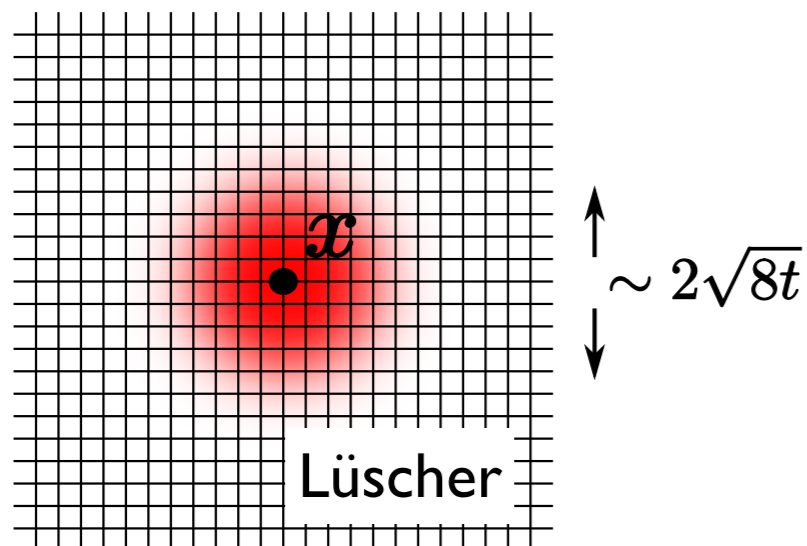
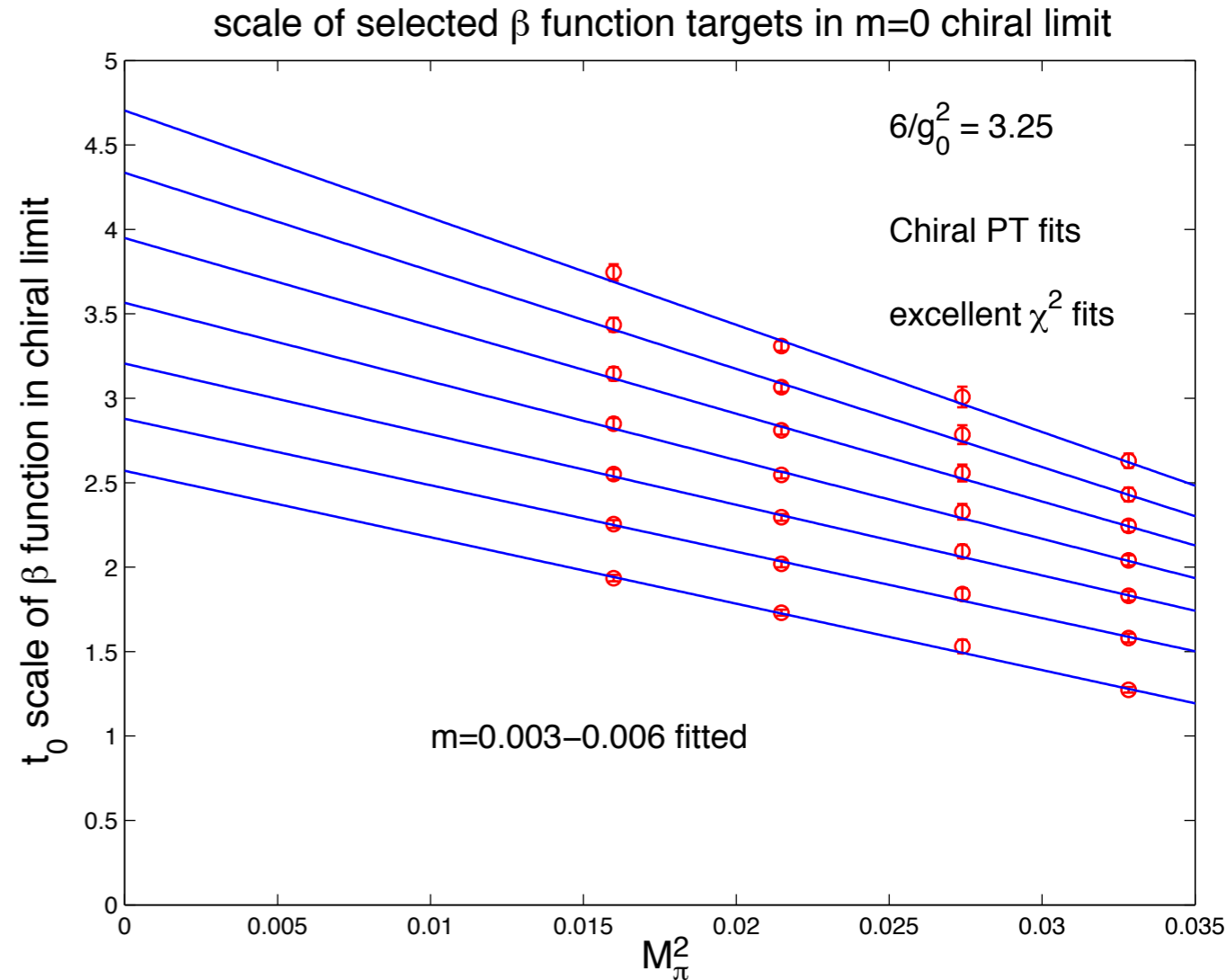
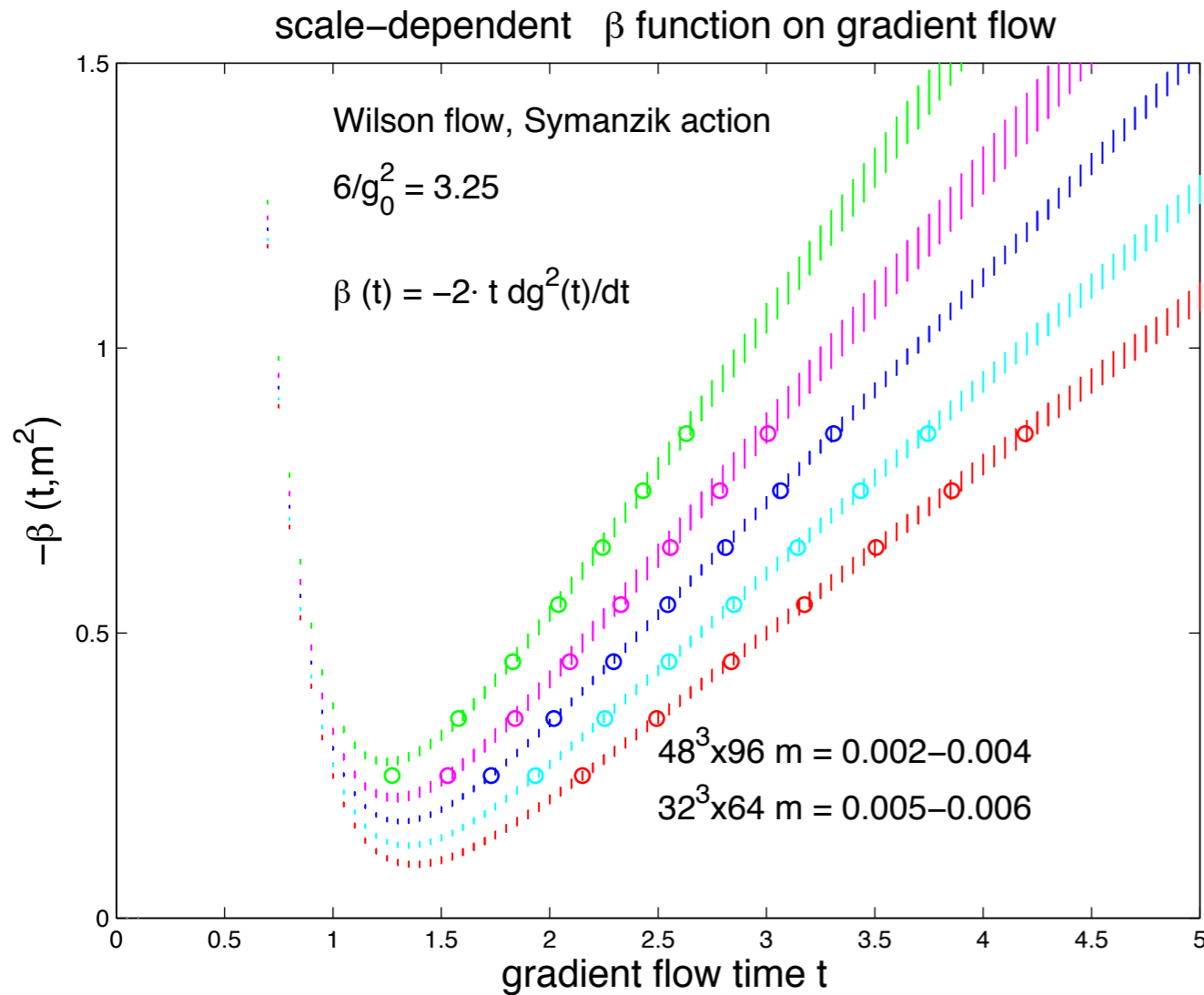


this is the second run set at $6/g_0^2 = 3.25$

two other sets at $6/g_0^2 = 3.15$ and $6/g_0^2 = 3.30$ are in the works

fits of leading chiPT are excellent

running coupling and beta function from gradient flow sextet rep



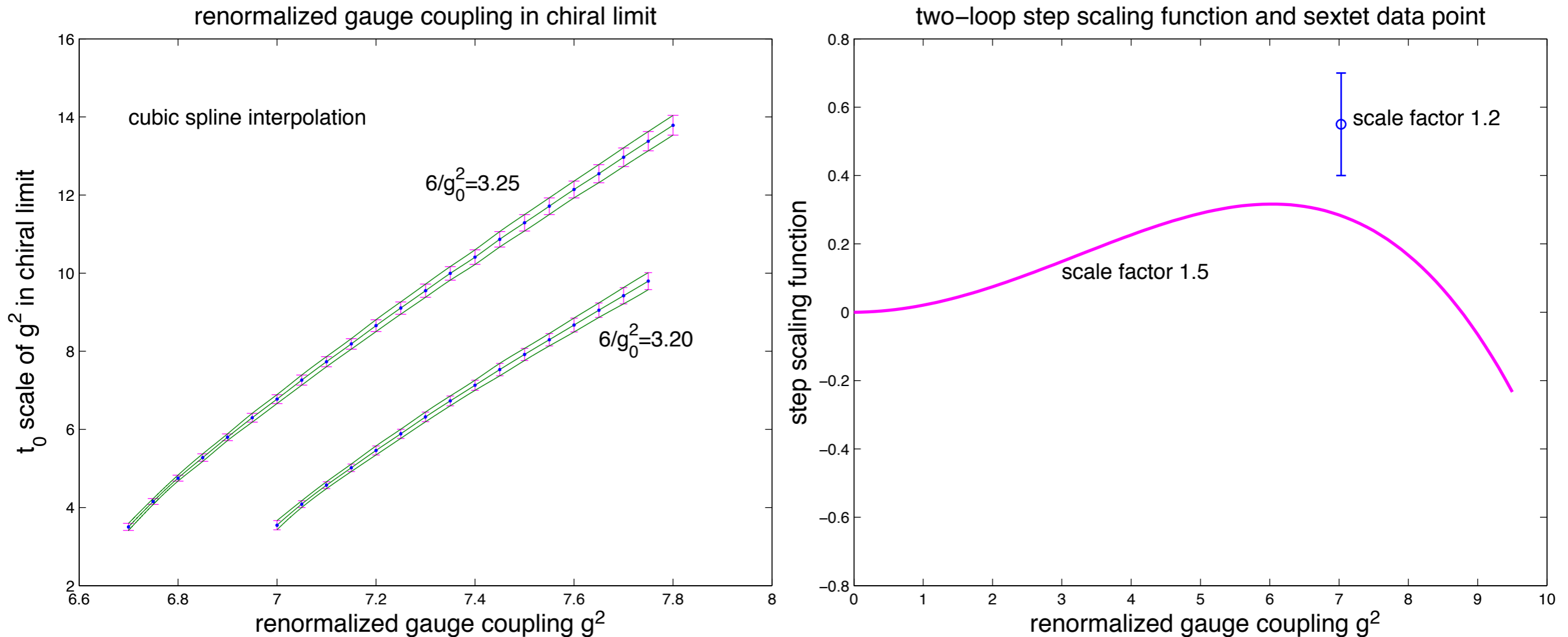
cross check on direct beta function at $6/g_0^2 = 3.25$

$\sim W_0$ of Wuppertal group

fits of leading chiPT are excellent again

running coupling and beta function from gradient flow

sextet rep



step function is larger than 2-loop (walking regime may or may not exist)

will have to be matched to perturbative running of finite volume $g^2(L)$

will tree-level improved analysis help when the operator is expanded in leading order of g^2 :

$$\langle t^2 E(t) \rangle = g_0^2 t^2 \int_{-\frac{\pi}{a}}^{\frac{\pi}{a}} \frac{d^4 p}{(2\pi)^4} \text{Tr} \left(e^{-t(\mathcal{S}^f + \mathcal{G})} (\mathcal{S}^g + \mathcal{G})^{-1} e^{-t(\mathcal{S}^f + \mathcal{G})} \mathcal{S}^e \right)$$

Nogradi 7E Thursday

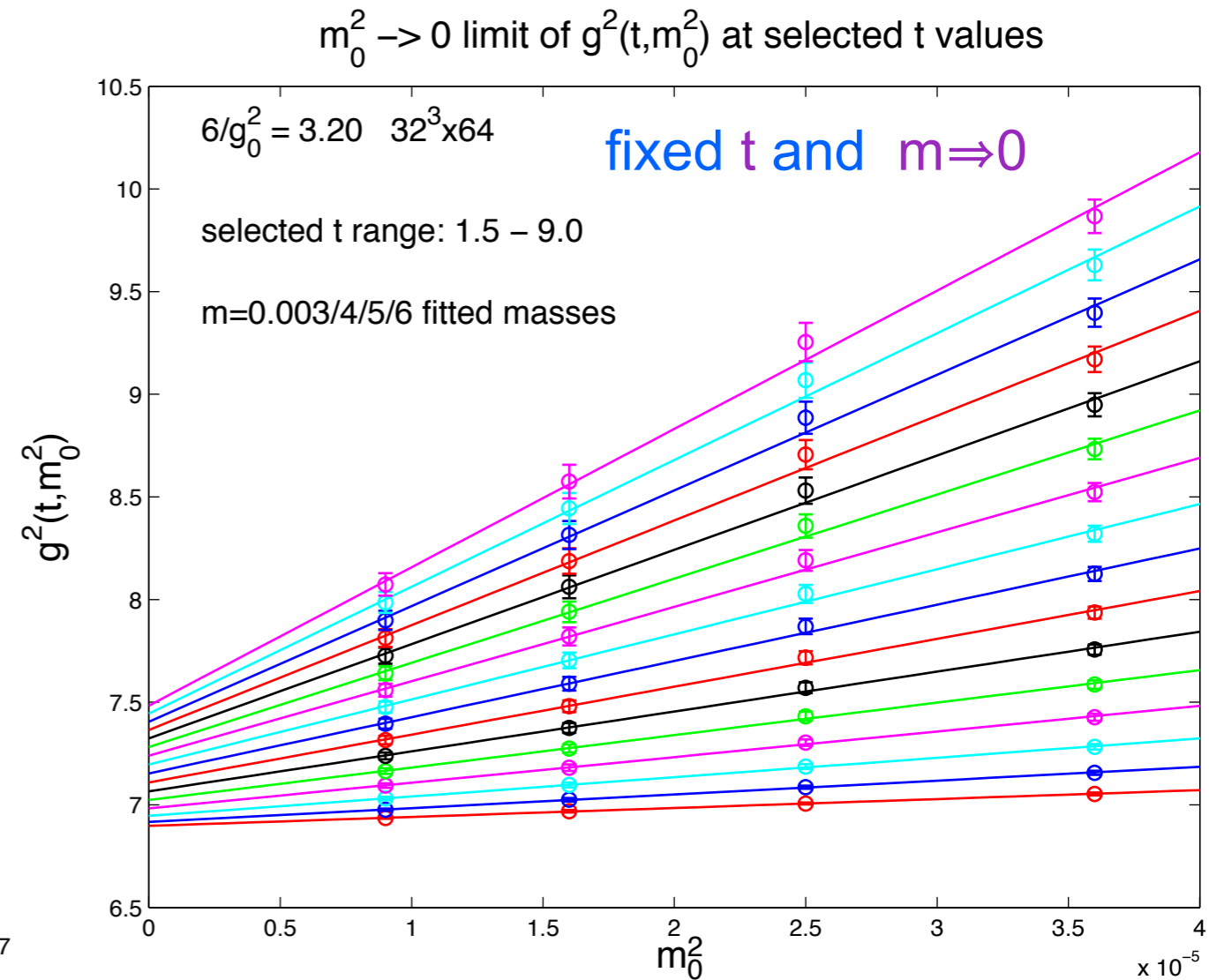
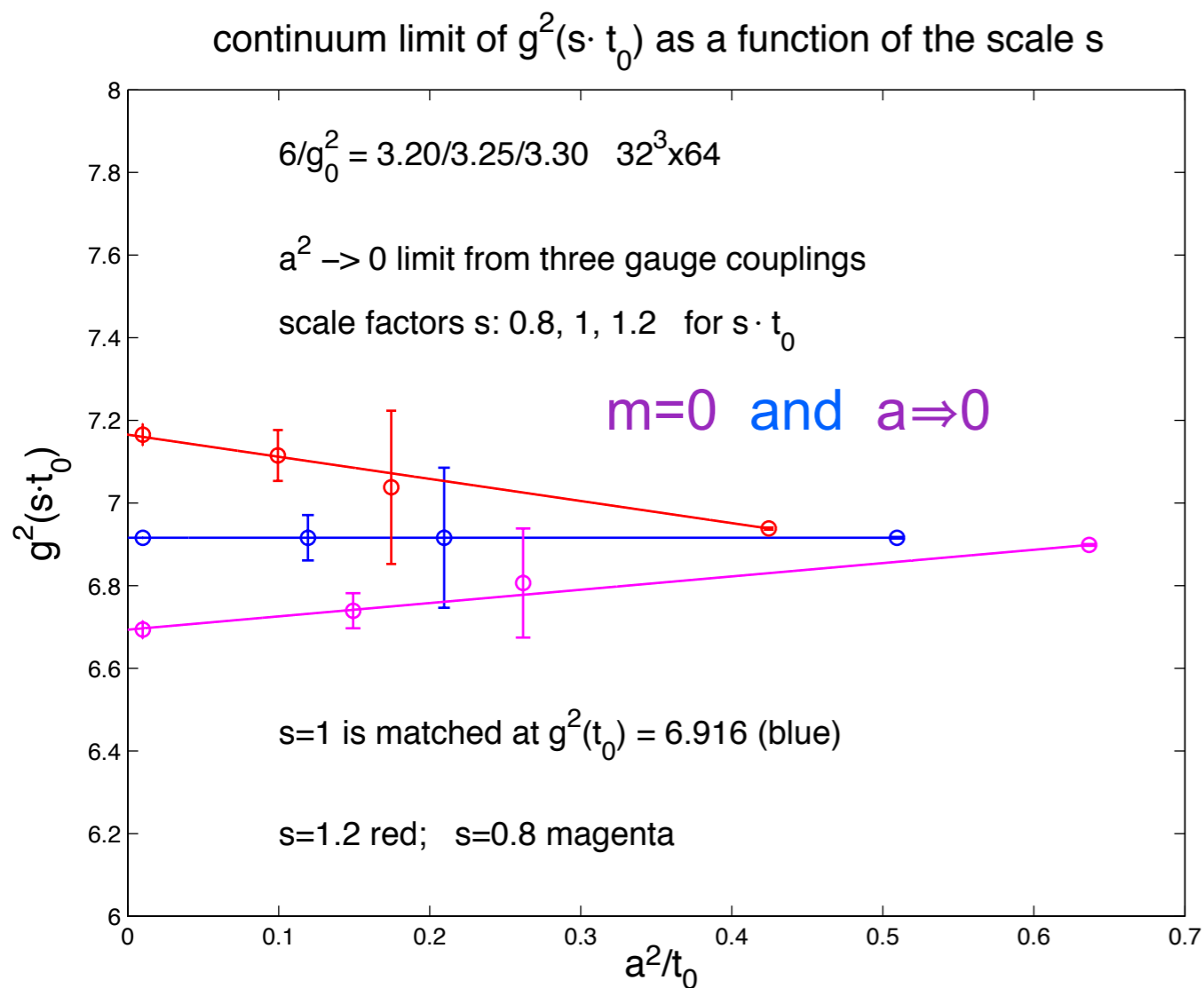
running coupling and beta function from gradient flow

sextet rep

complementing the analysis is the PT motivated procedure (JK SCGT14mini talk)

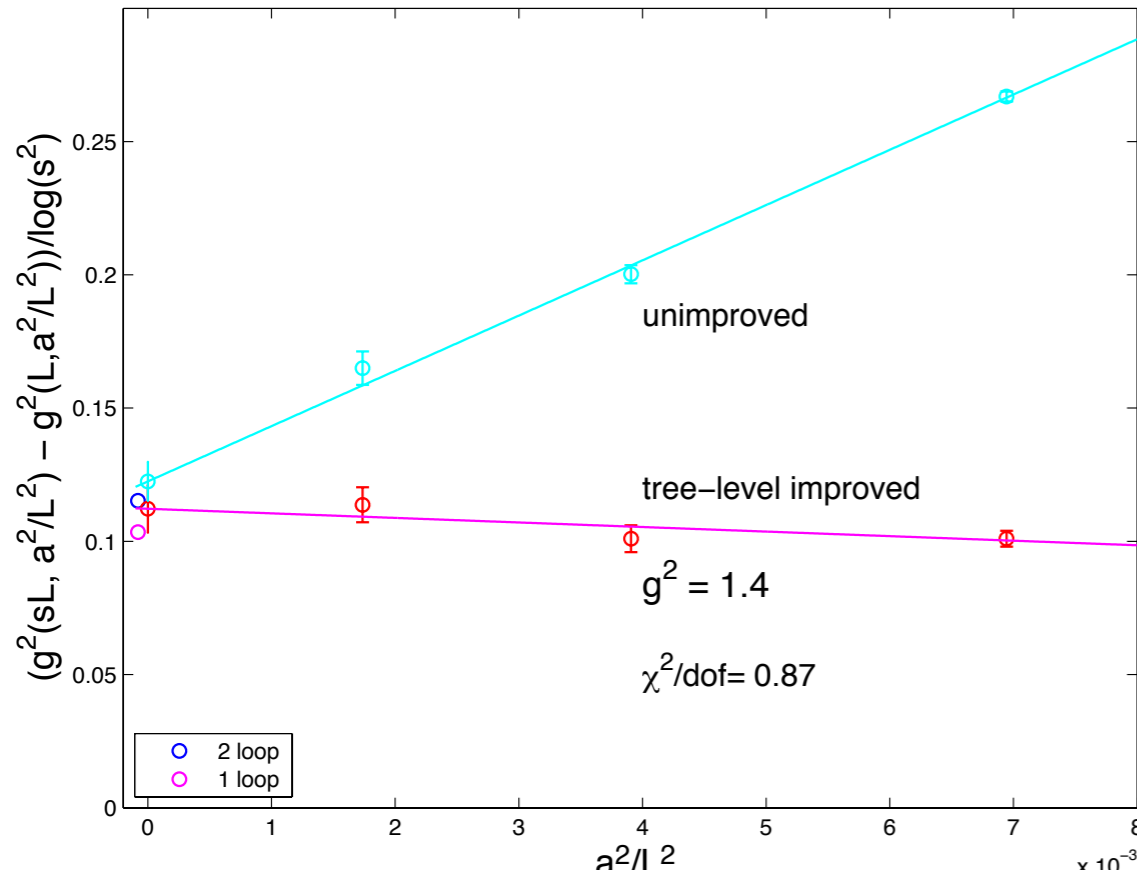
fixed t $m^2 \rightarrow 0$ extrapolation (3 gauge couplings)

results give a somewhat lower step scaling function, closer to walking
systematics to clean in both procedures

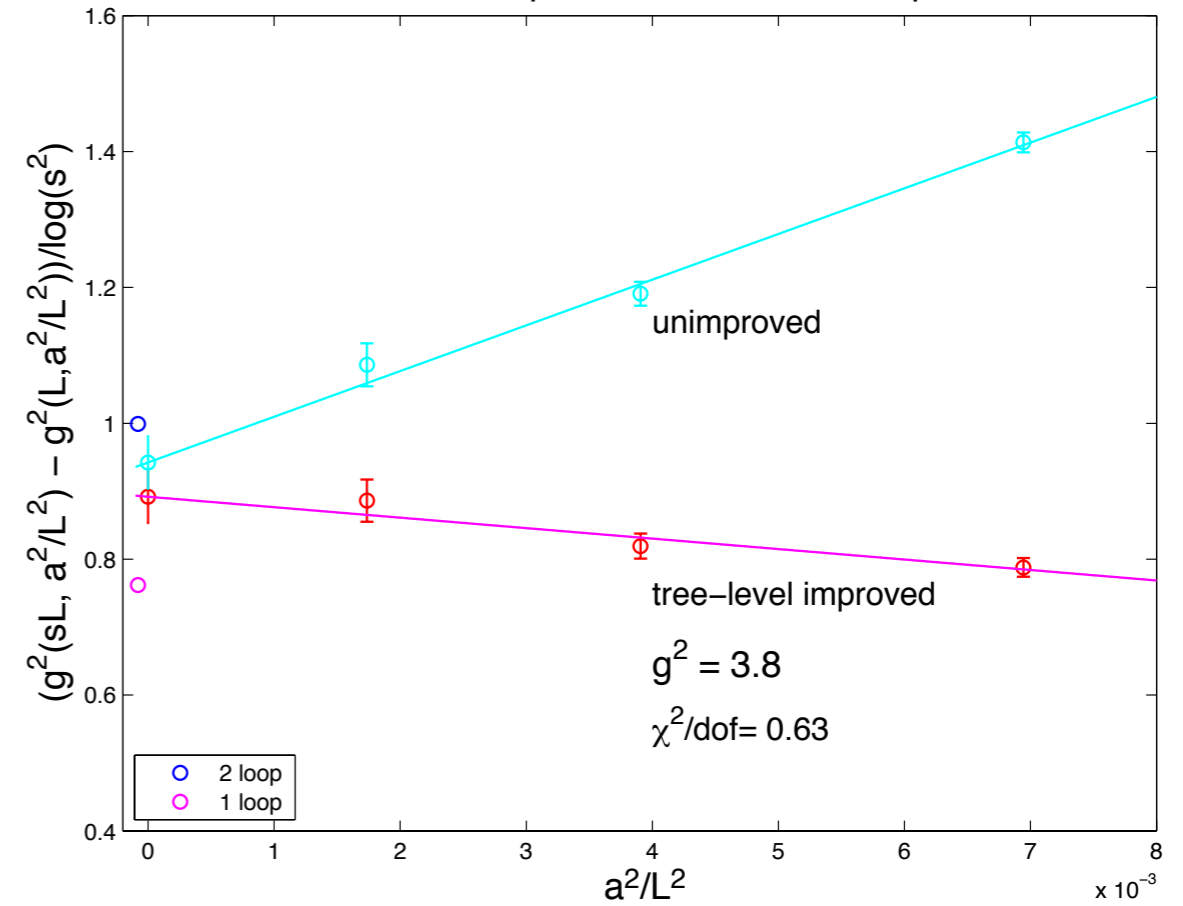


running coupling and beta function from gradient flow sextet rep

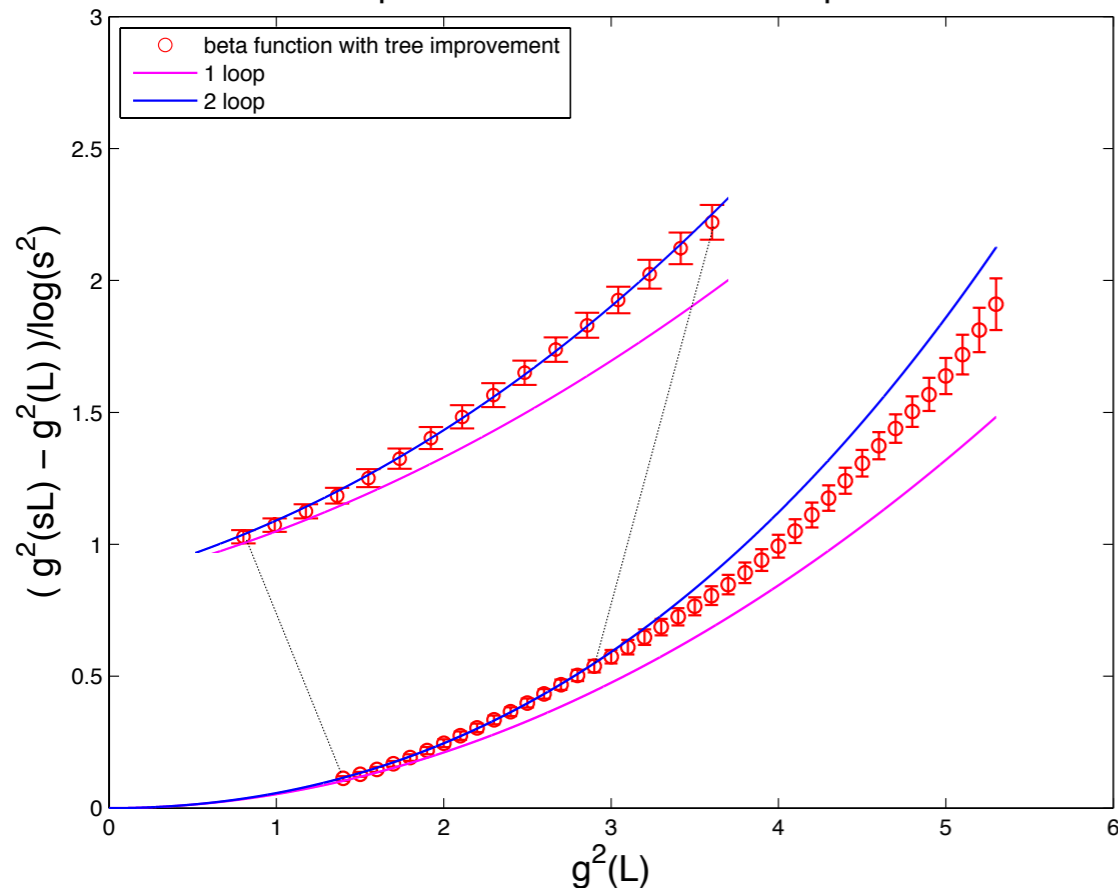
Nf=4 s=1.5 step function tree-level improved



Nf=4 s=1.5 step function tree-level improved



s=1.5 step function with tree-level improvement



works very well in Nf=4 fundamental rep test

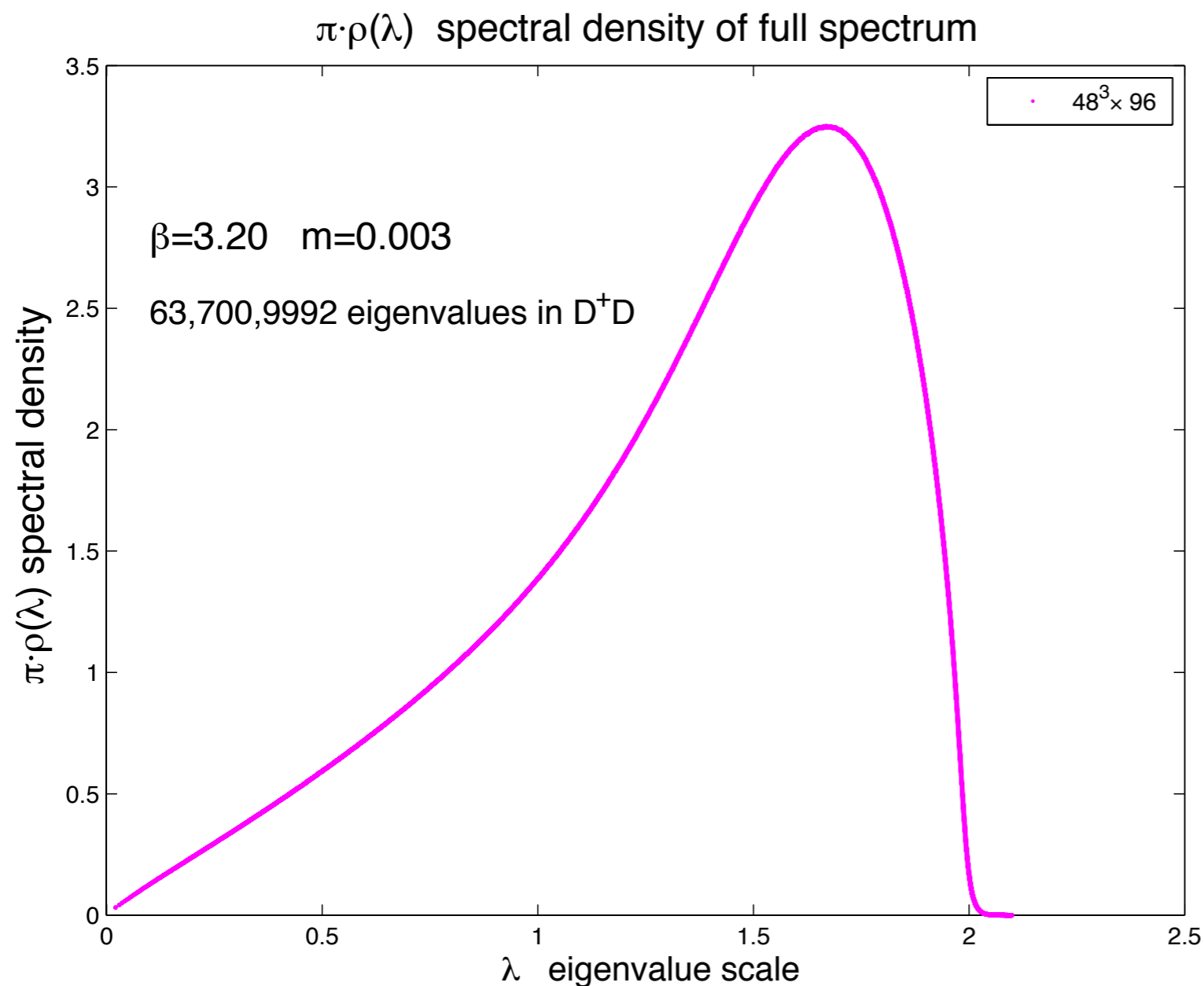
sextet rep and Nf=8,12 fundamental reps are in the works

The chiral (Higgs) condensate

- New stochastic method
- Direct determination of full spectral density and mode number distribution on gauge configurations
- To remove UV divergences at finite fermion mass
- To investigate internal (in)consistencies with GMOR relation
- To determine anomalous dimension of the chiral condensate
- To investigate dependence on slowly changing topology

The chiral condensate in the sextet theory

- new stochastic method **sextet Nf=2** code developed by Ricky Wong
- direct determination of full spectral density and mode number distribution
- based on Chebyshev polynomial resolution of spectral density



- typically Chebyshev order $\sim 3,000$
- Passed all tests so far
- example is from $48^3 \times 96$ lattices
- allows independent variation of m and λ **extended analysis!**
- topology dependence and the anomalous dimension of the chiral condensate

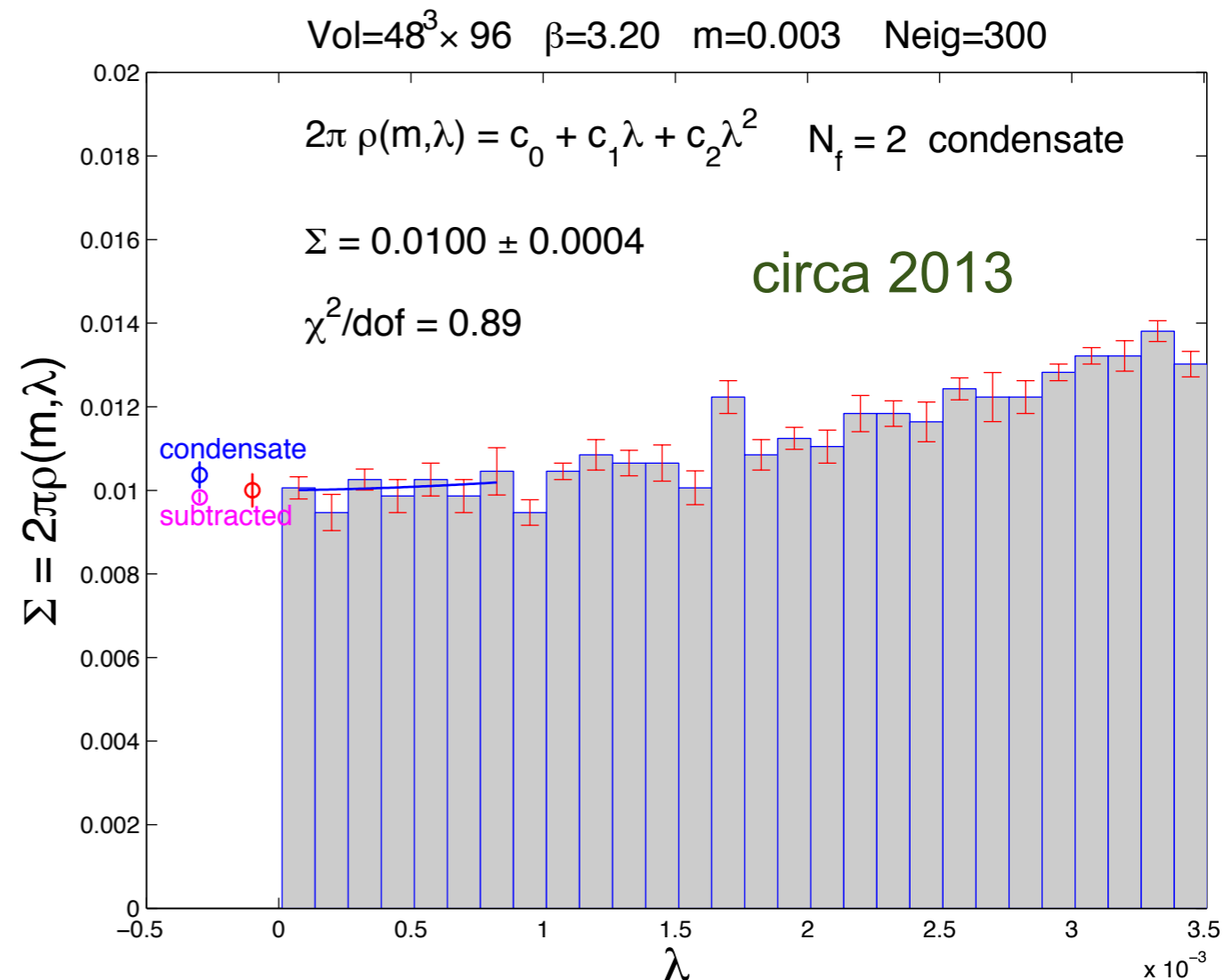
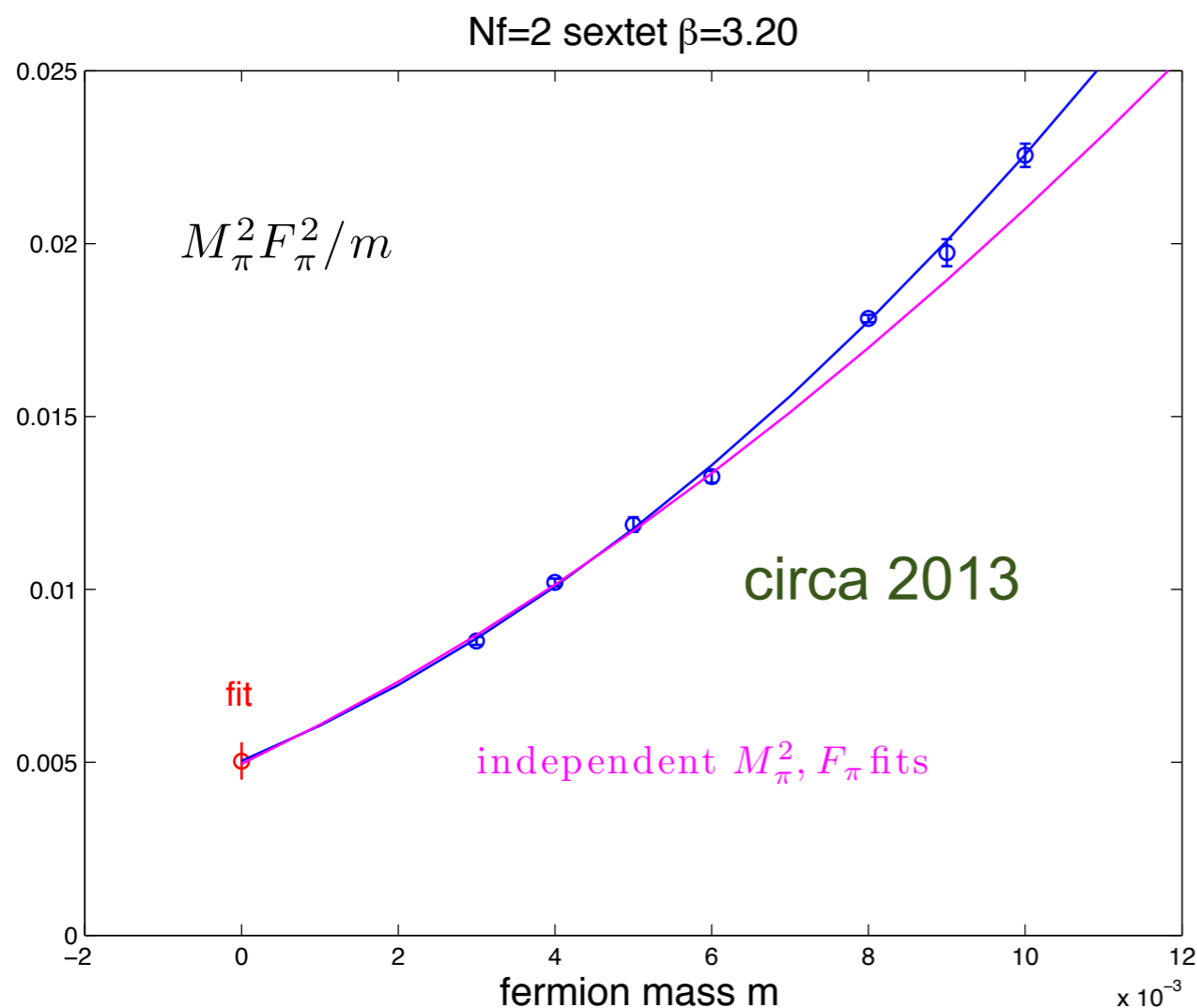
The chiral condensate in the sextet theory

control on UV divergences: mode number density of chiral condensate

$$\rho(\lambda, m) = \frac{1}{V} \sum_{k=1}^{\infty} \langle \delta(\lambda - \lambda_k) \rangle \quad \lim_{\lambda \rightarrow 0} \lim_{m \rightarrow 0} \lim_{V \rightarrow \infty} \rho(\lambda, m) = \frac{\Sigma}{\pi} \quad \text{spectral density}$$

$$\nu(M, m) = V \int_{-\Lambda}^{\Lambda} d\lambda \rho(\lambda, m), \quad \Lambda = \sqrt{M^2 - m^2} \quad \text{mode number density}$$

$$\nu_R(M_R, m_R) = \nu(M, m_q) \quad \text{renormalized and RG invariant} \quad (\text{Giusti and Luscher})$$



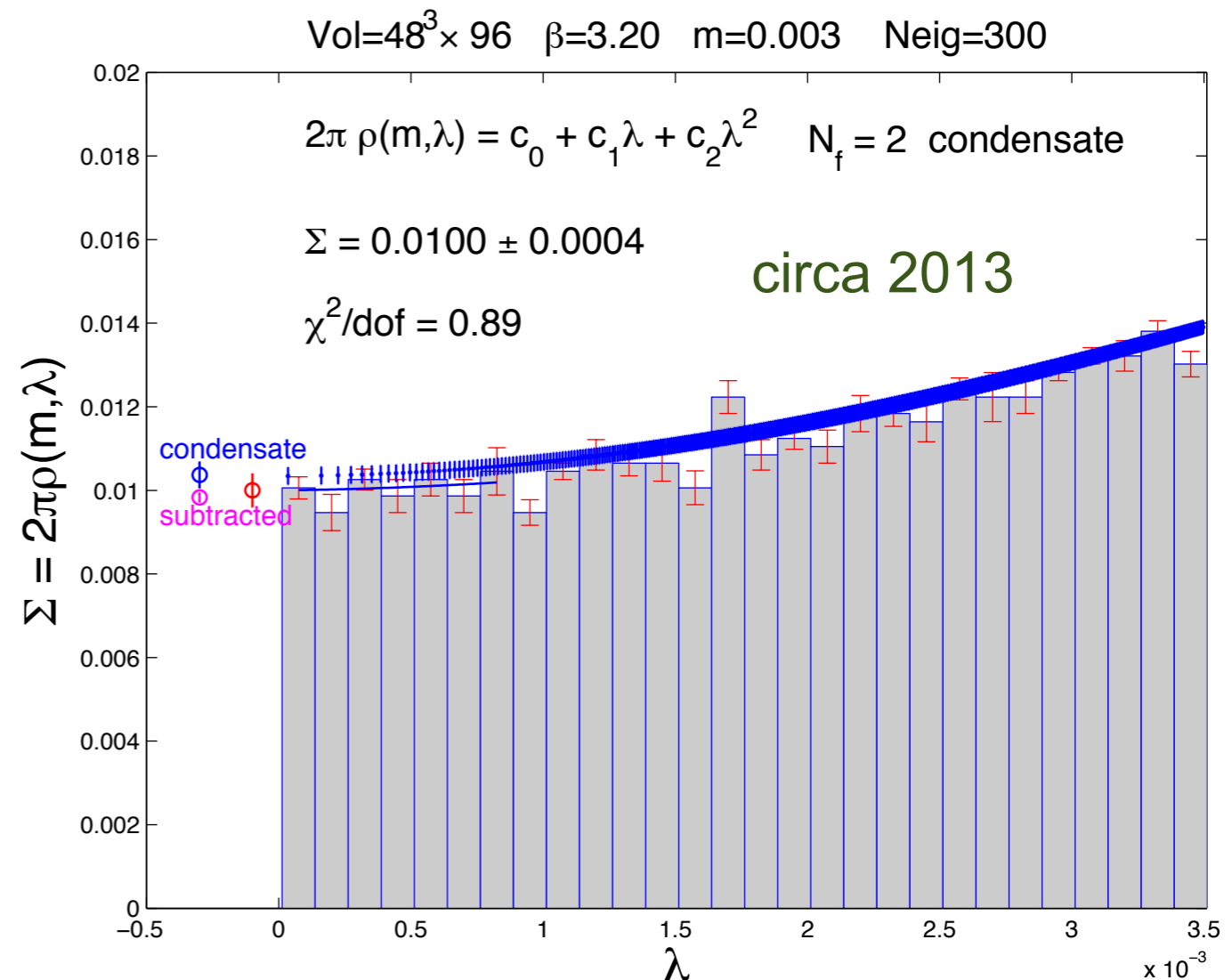
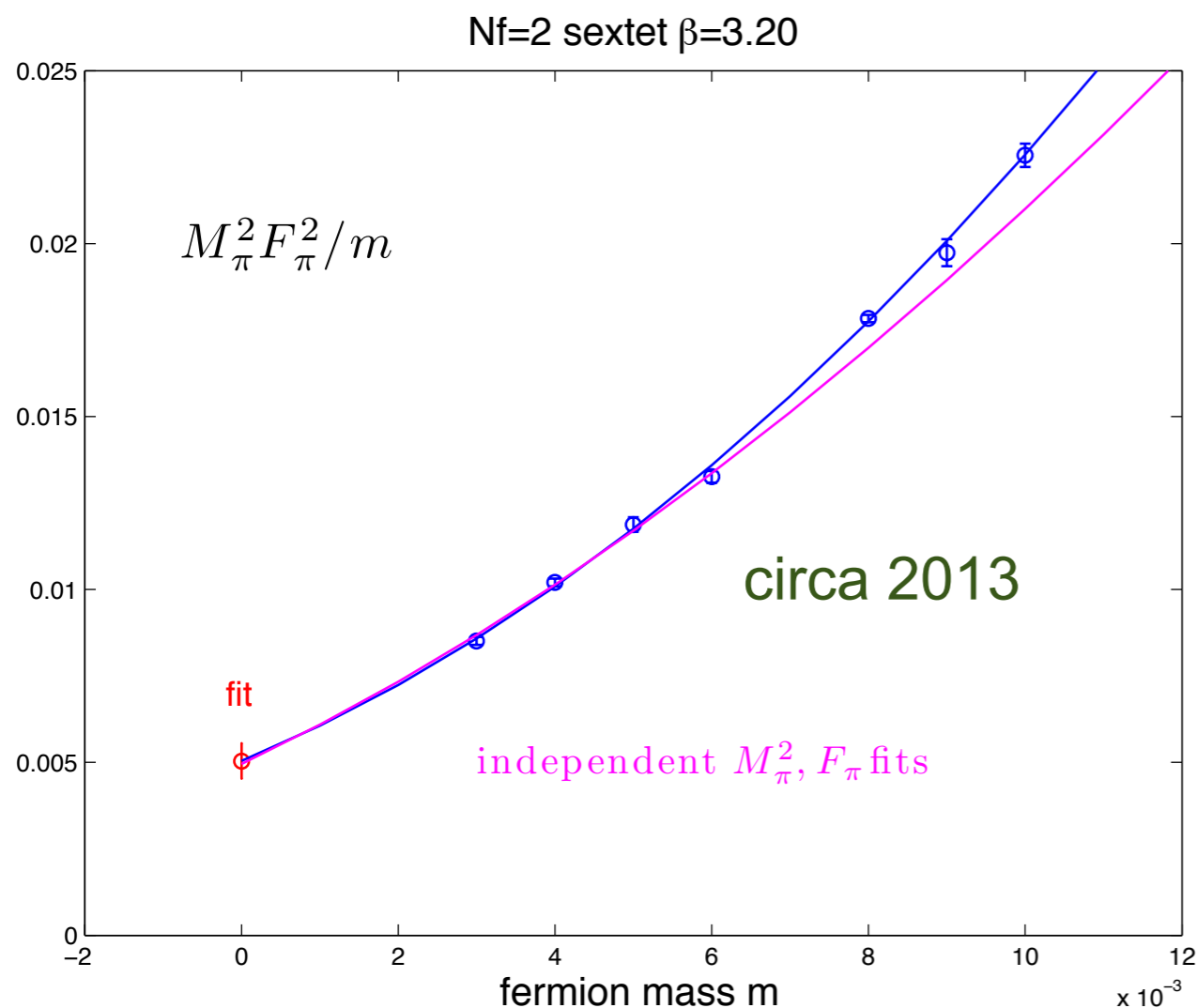
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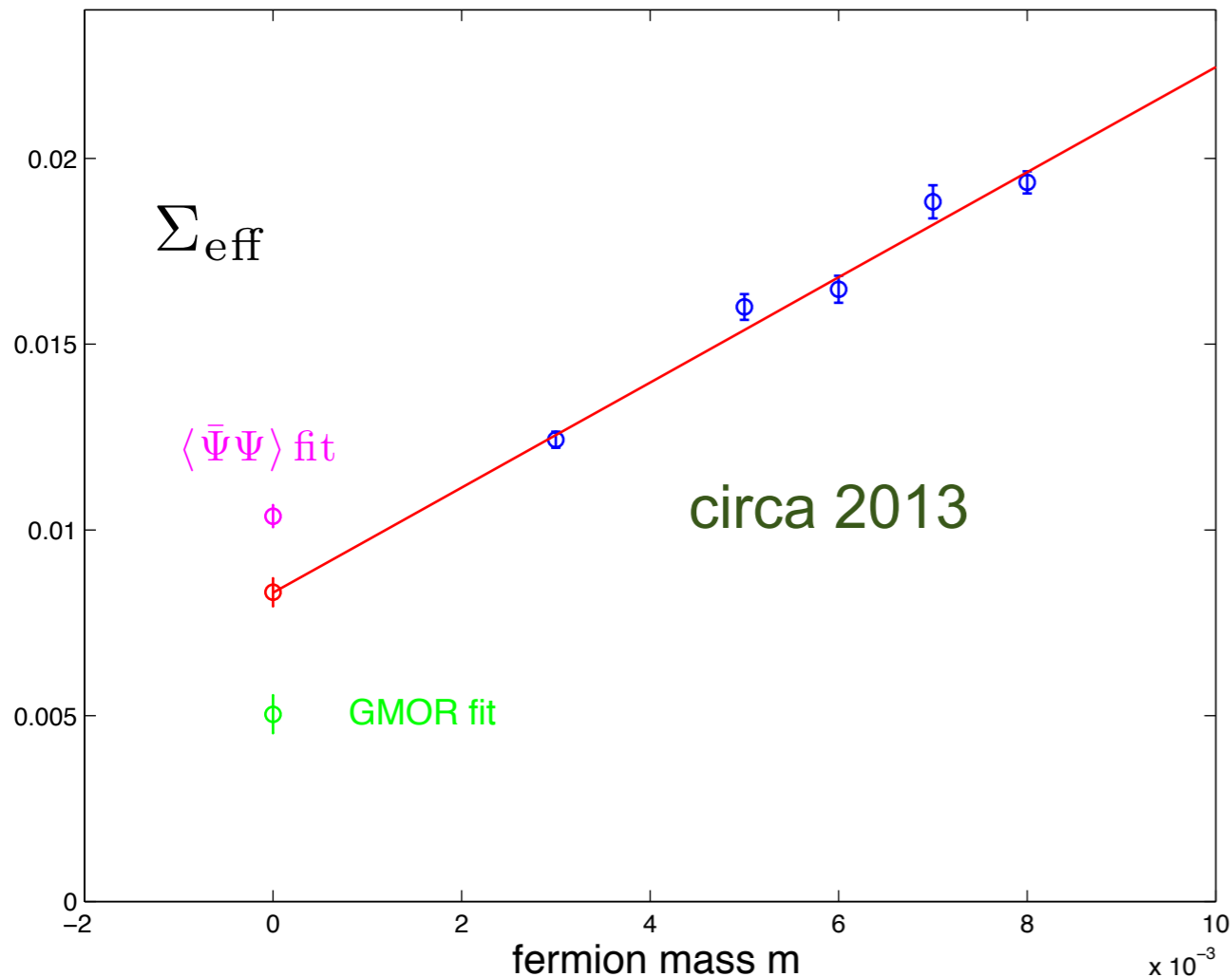
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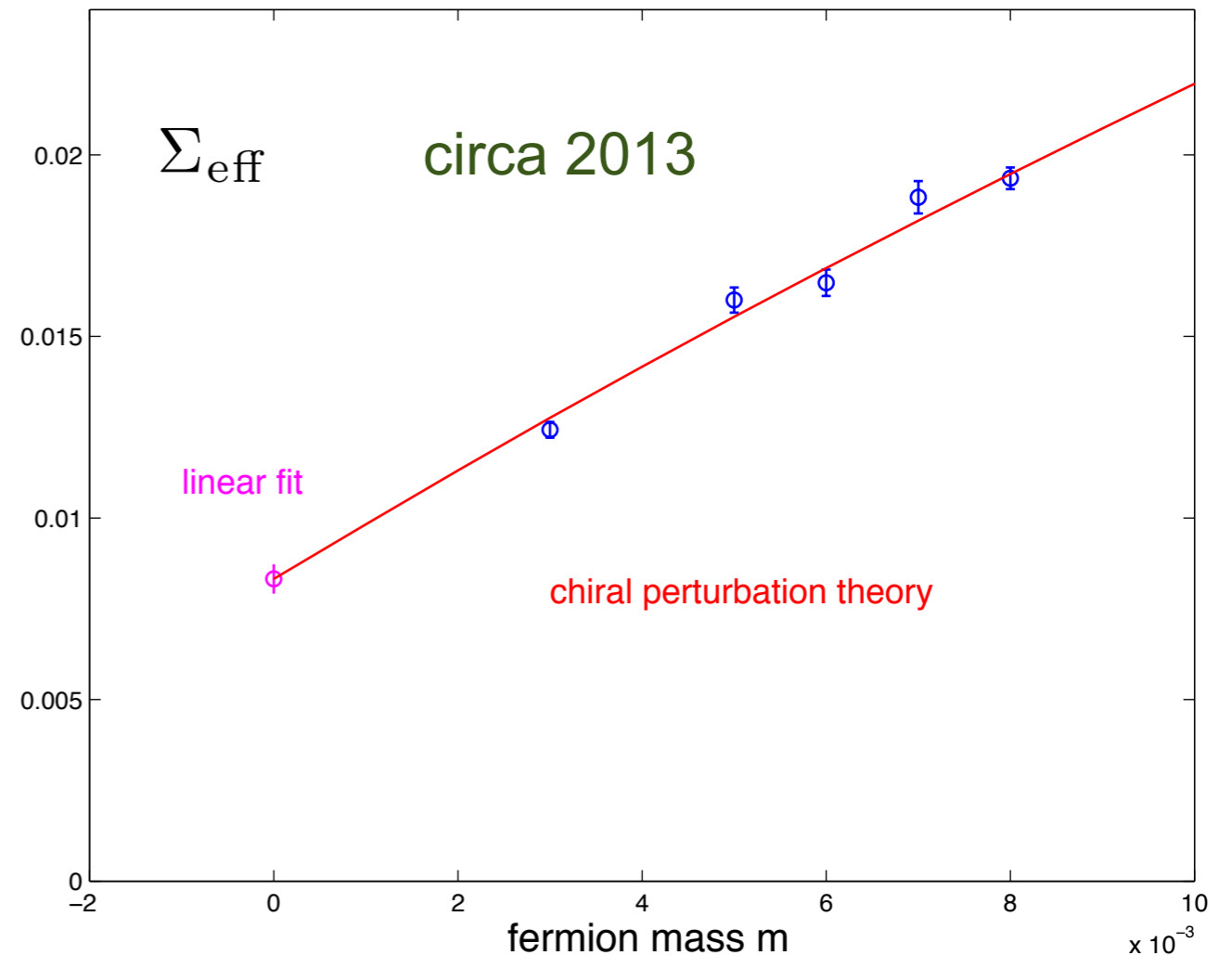


The chiral condensate in the sextet theory

Nf=2 sextet $\beta=3.20$ $\Lambda=0.003$



Nf=2 sextet $\beta=3.20$ $\Lambda=0.003$



$$\frac{\Sigma_{\text{eff}}}{\Sigma} = 1 + \frac{\Sigma}{32\pi^3 N_F F^4} \left[2N_F^2 |\Lambda| \arctan \frac{|\Lambda|}{m} - 4\pi |\Lambda| - N_F^2 m \log \frac{\Lambda^2 + m^2}{\mu^2} - 4m \log \frac{|\Lambda|}{\mu} \right]$$

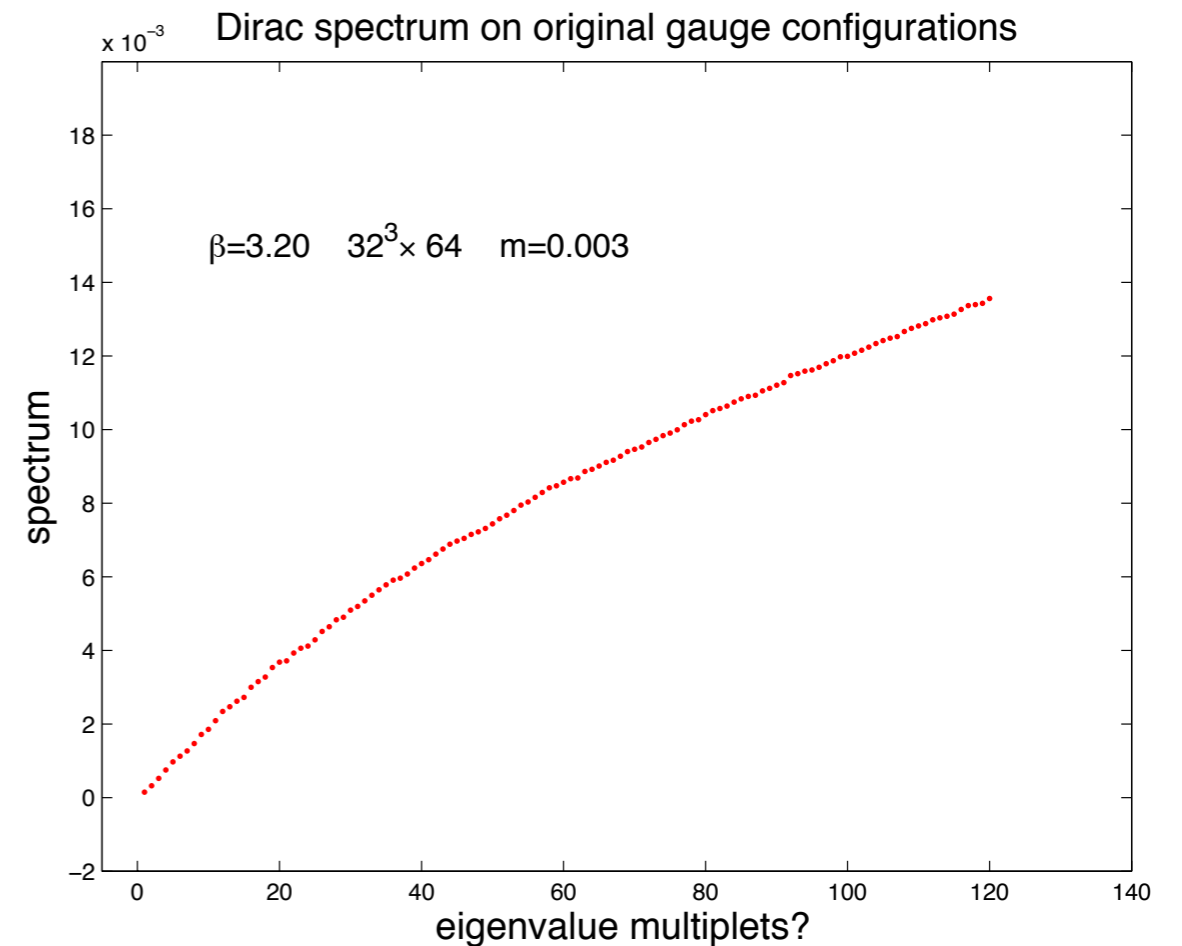
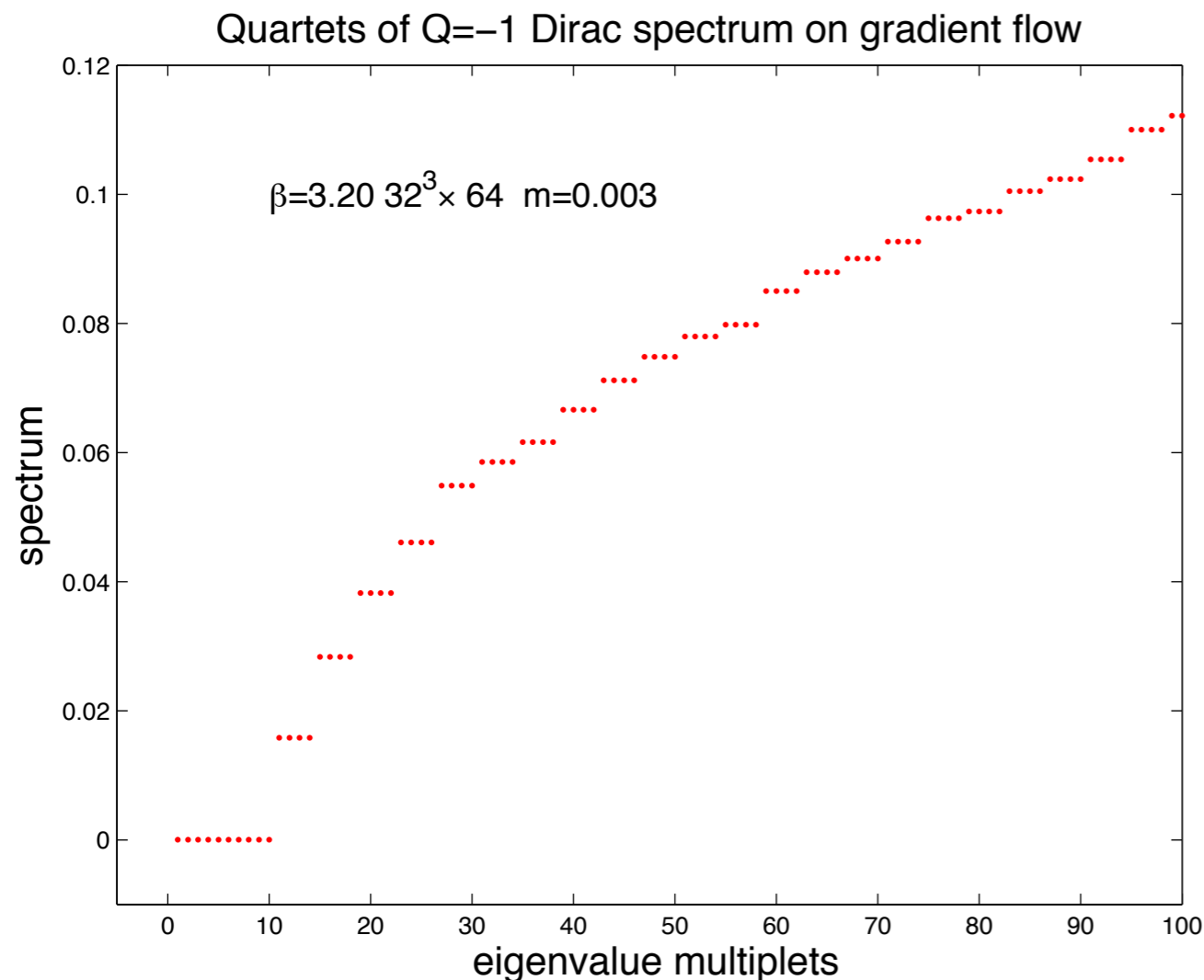
- new stochastic method allows the extension of chiPT analysis and study topology
- m and the scale on the spectrum can be tuned more freely in partial quenching

The chiral condensate in the sextet theory

analyzis of Dirac spectrum

building correlators

insight into $\sqrt{}$



$t=3$ on gradient flow

Dirac spectrum shows degenerate quartets

index theorem is perfect

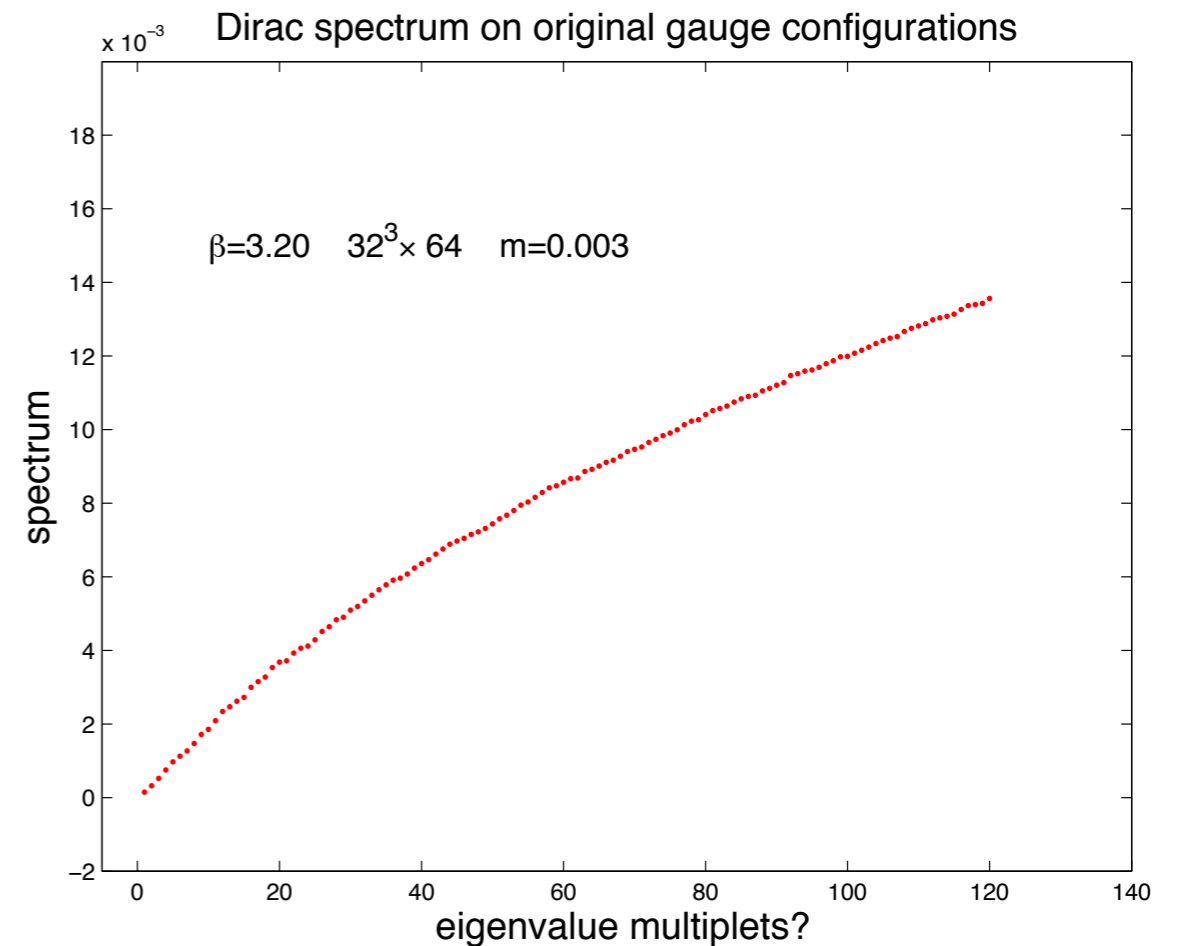
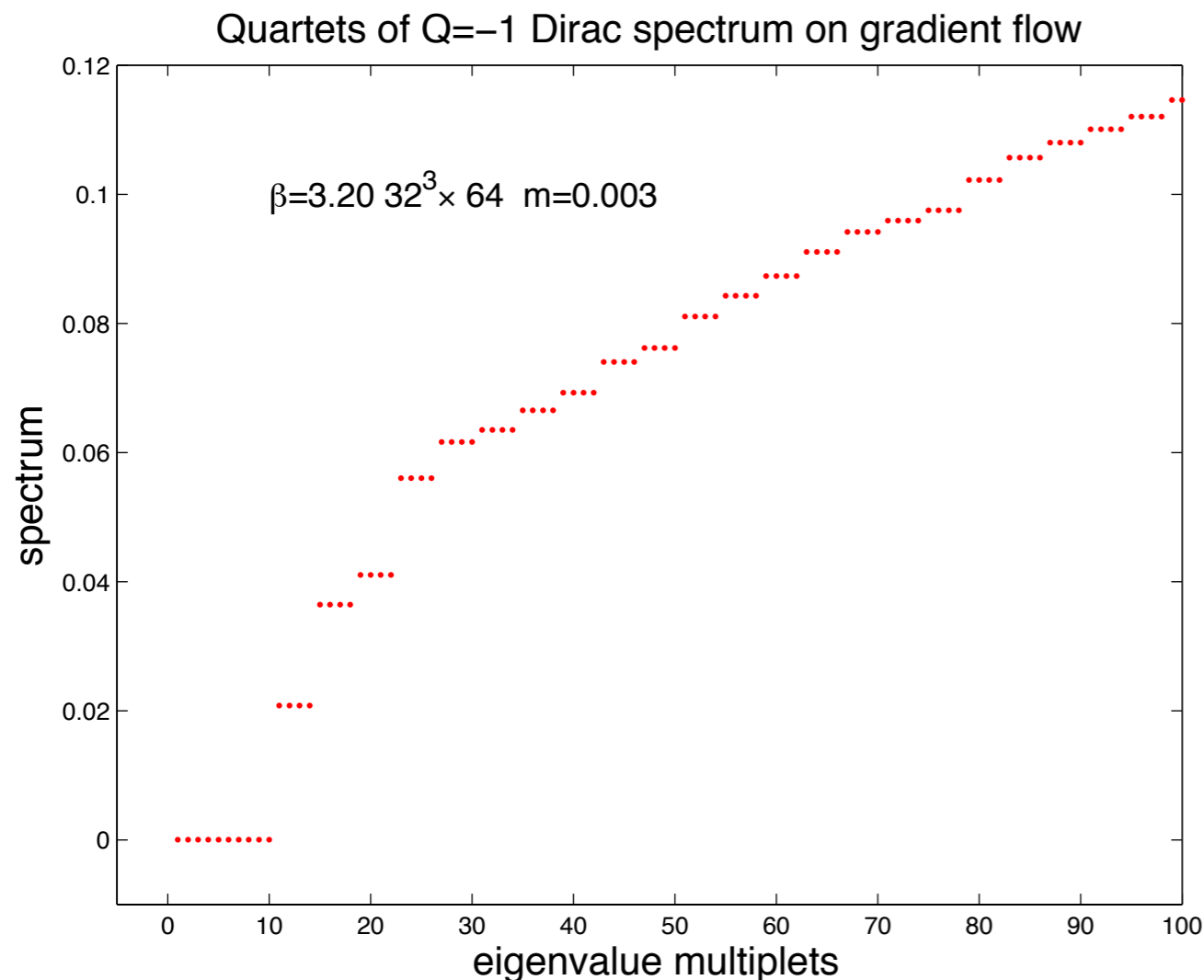
$10 \cdot Q$ zero modes in sextet $D^\dagger D$ op

The chiral condensate in the sextet theory

analyzis of Dirac spectrum

building correlators

insight into χ



$t=3$ on gradient flow

Dirac spectrum shows degenerate quartets

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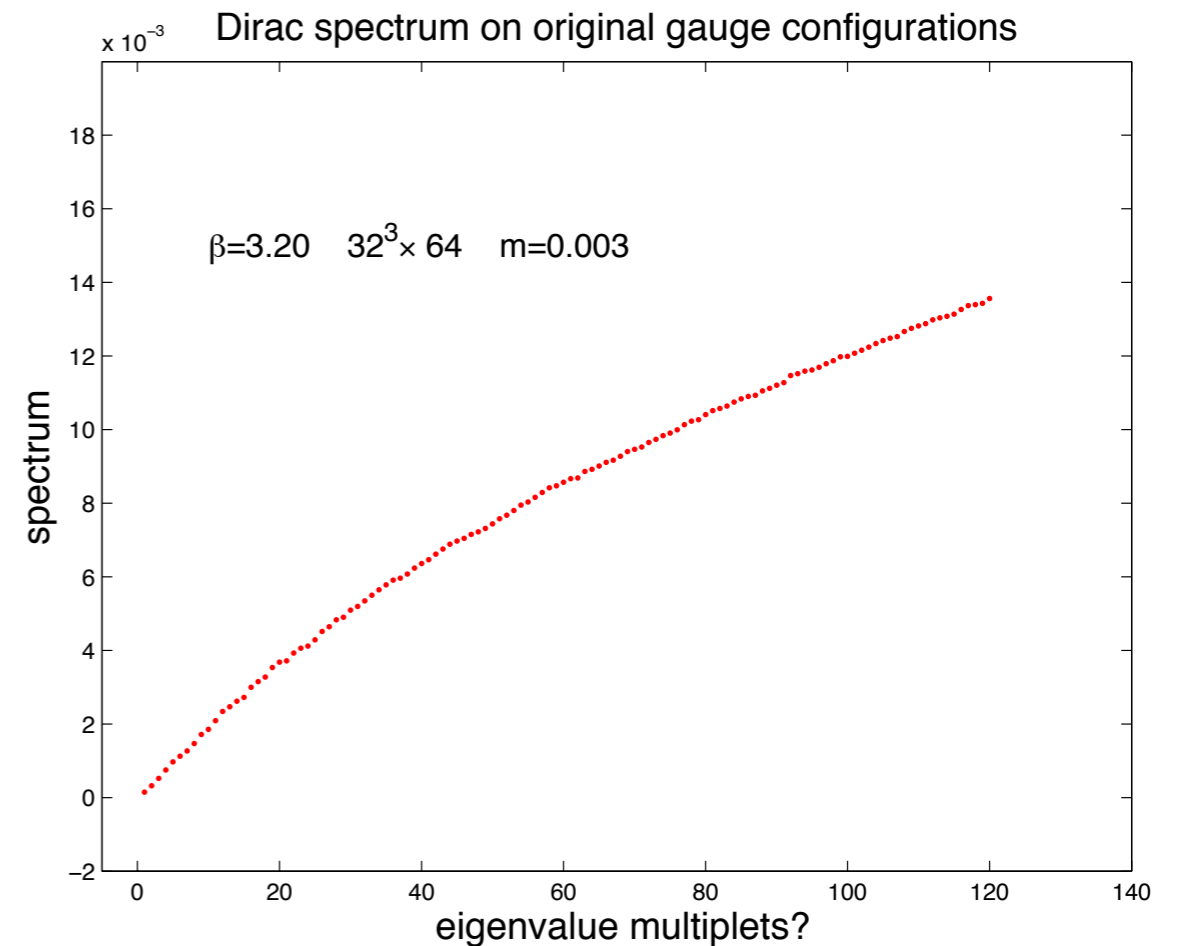
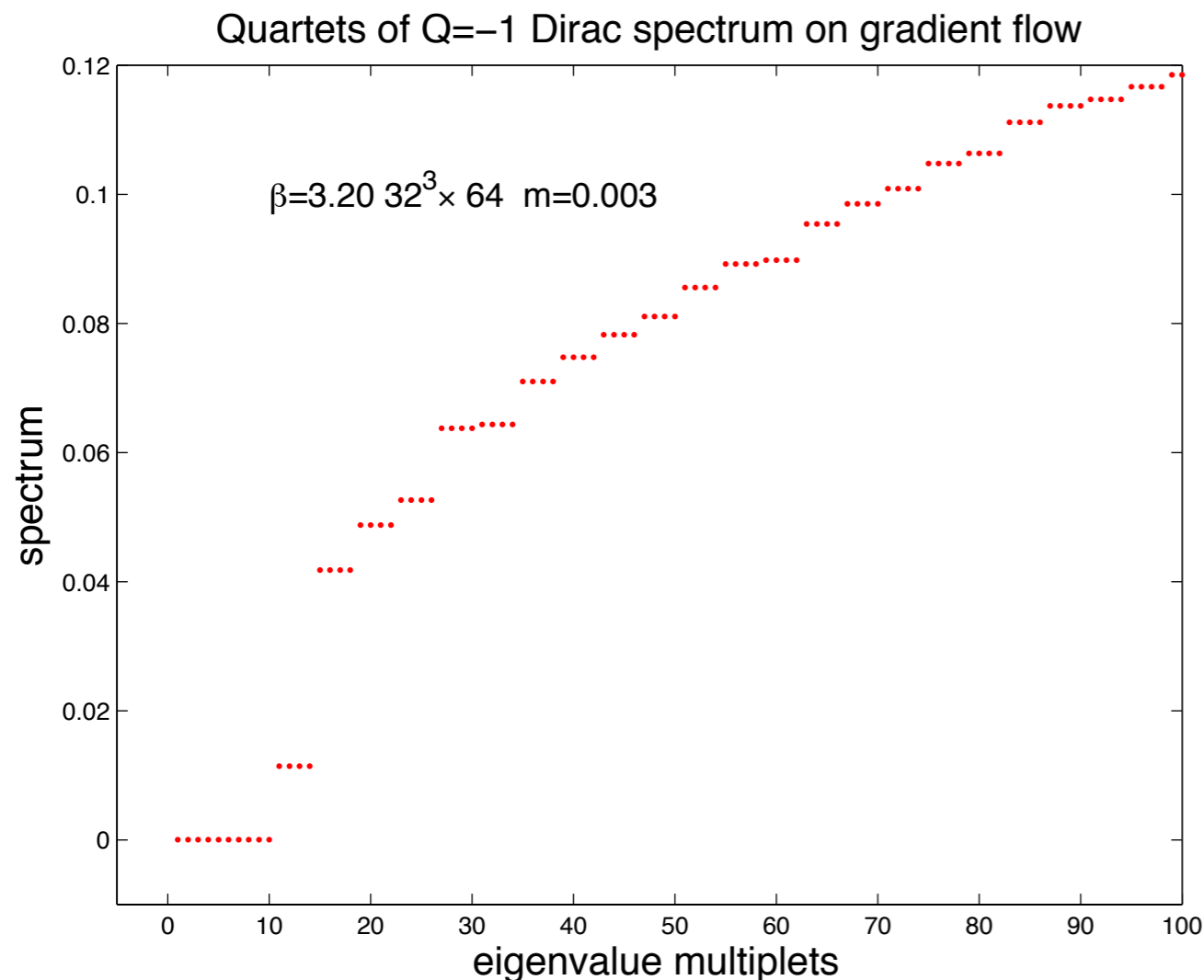
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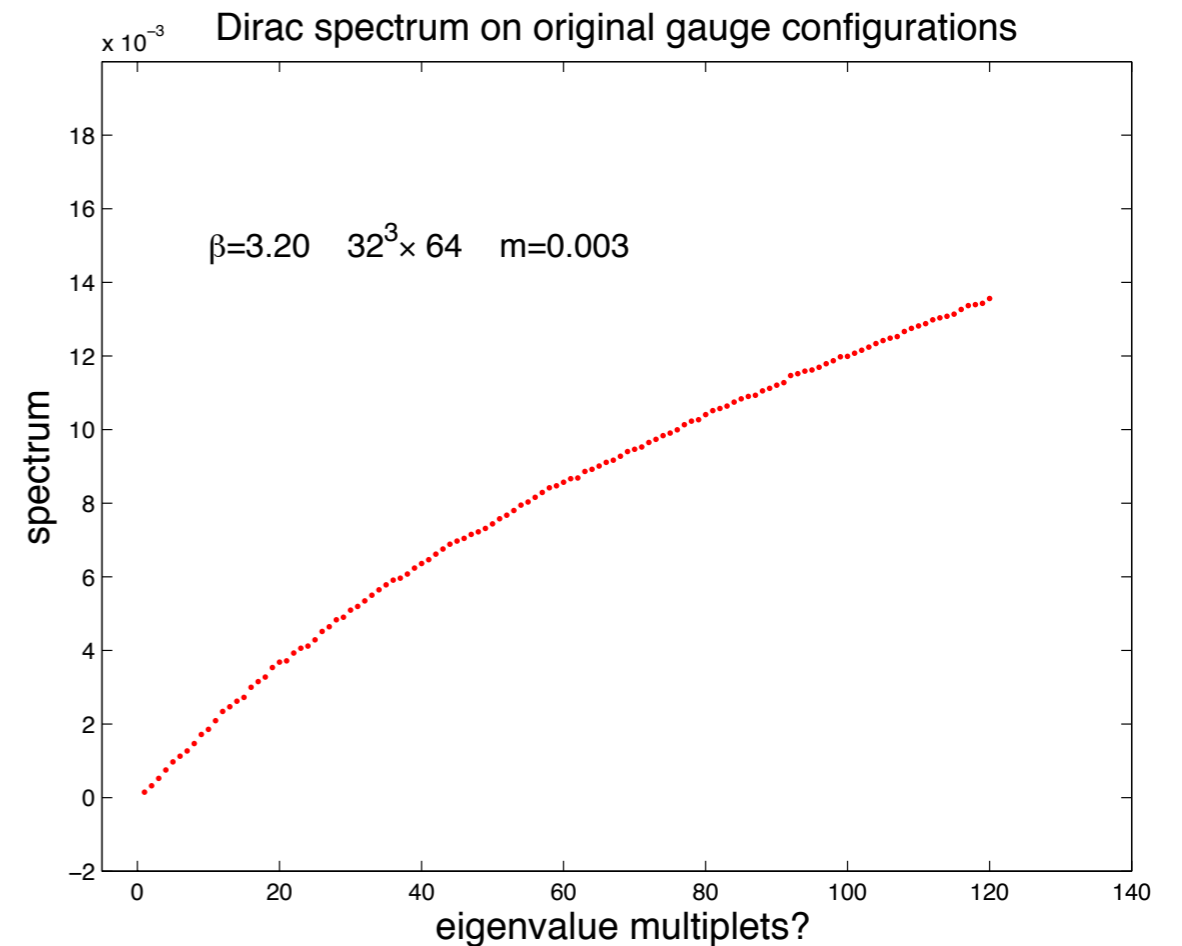
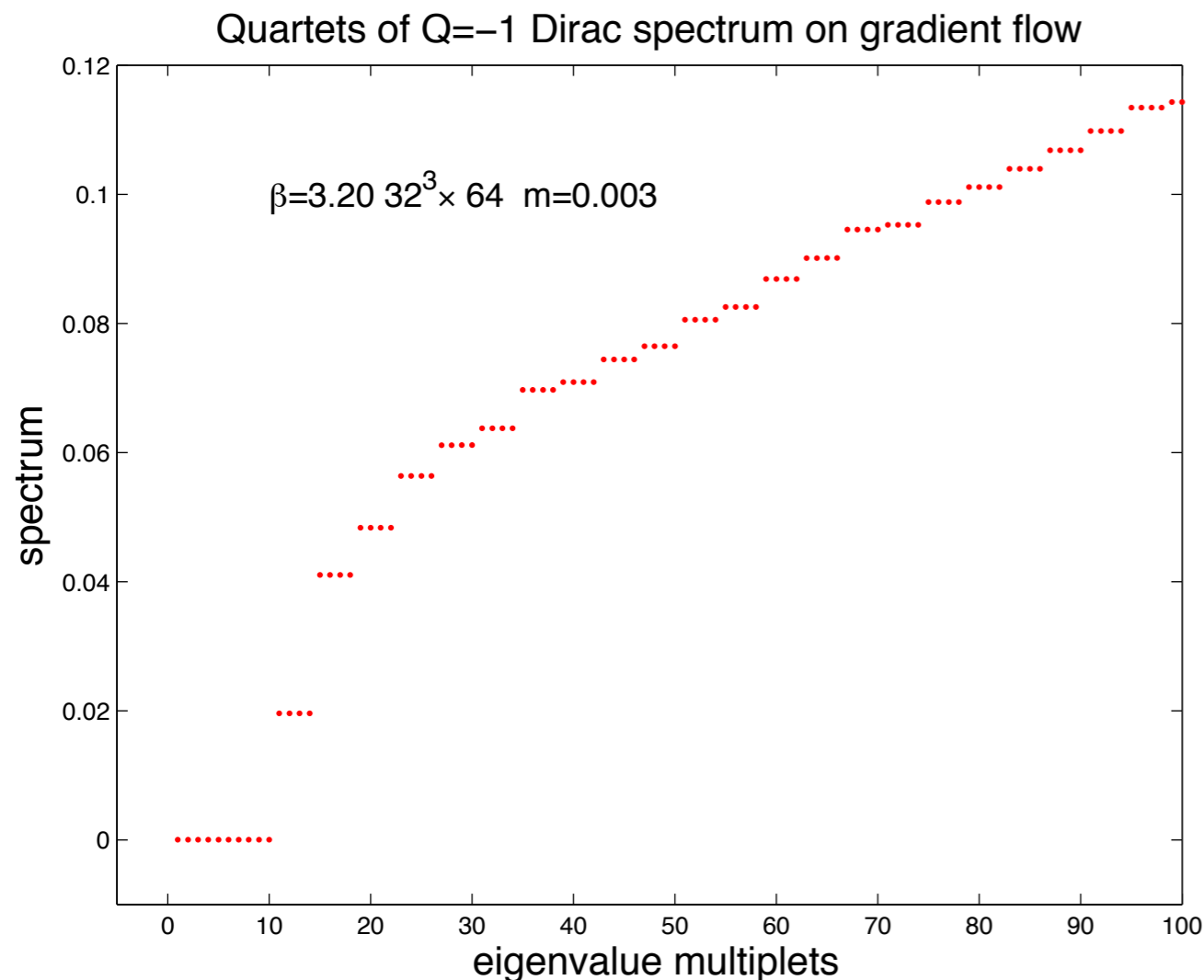
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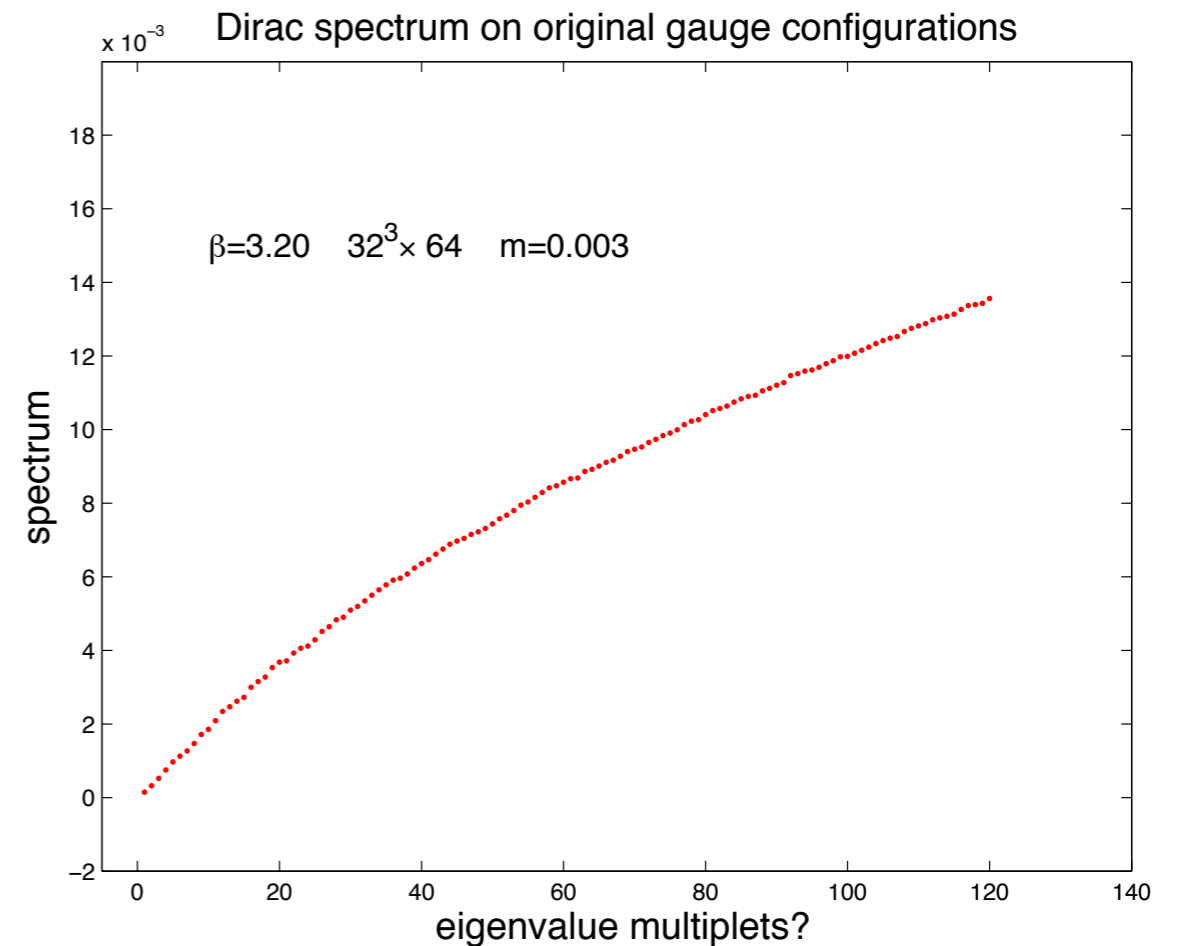
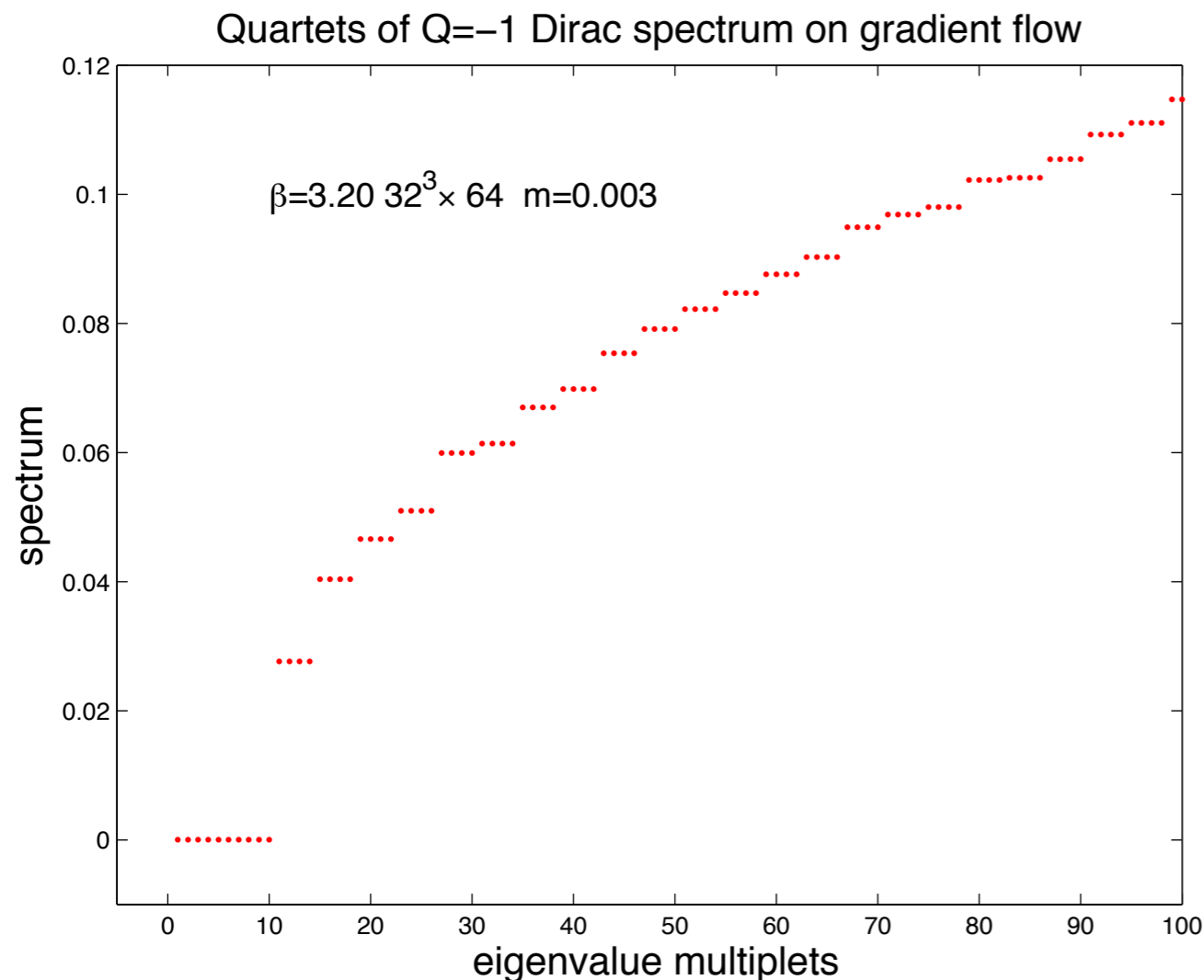
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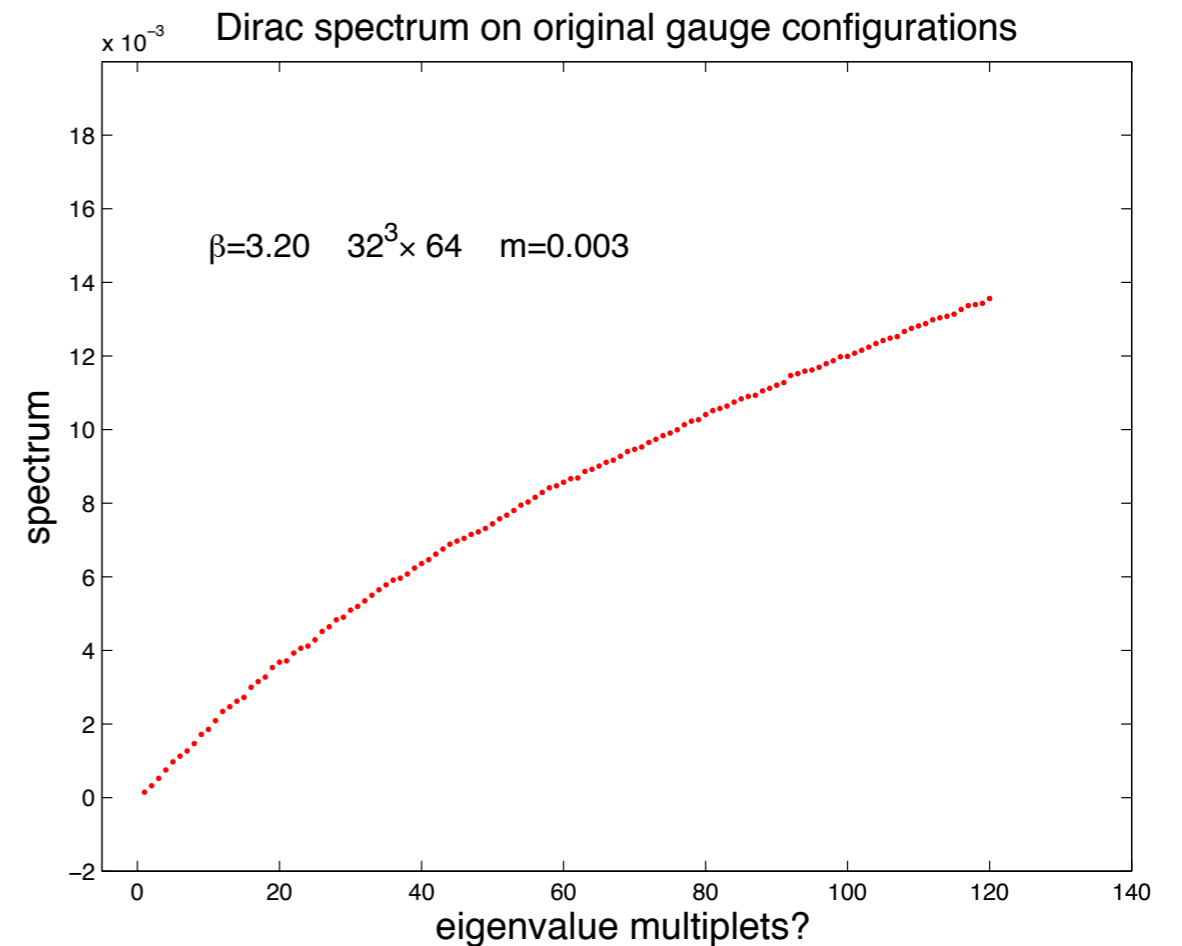
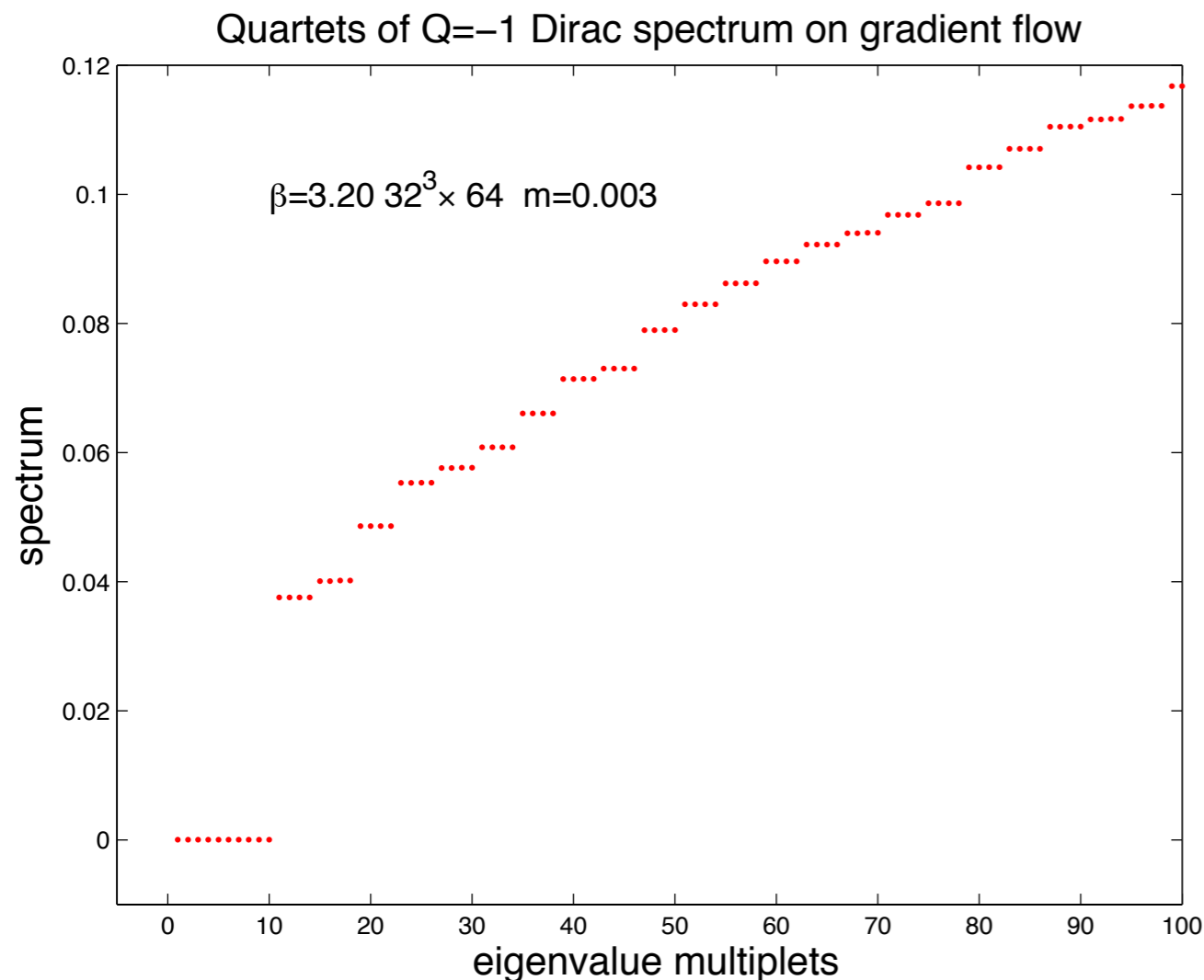
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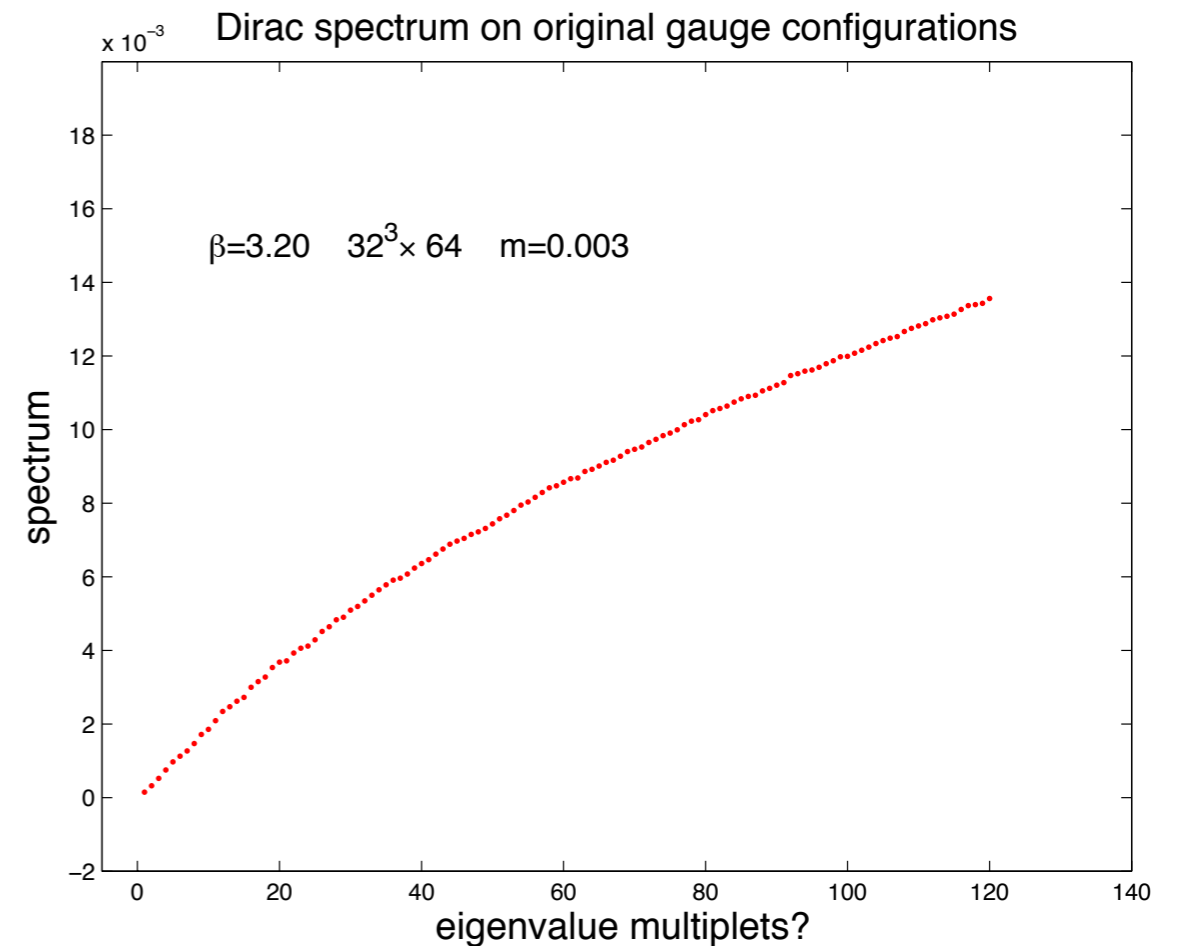
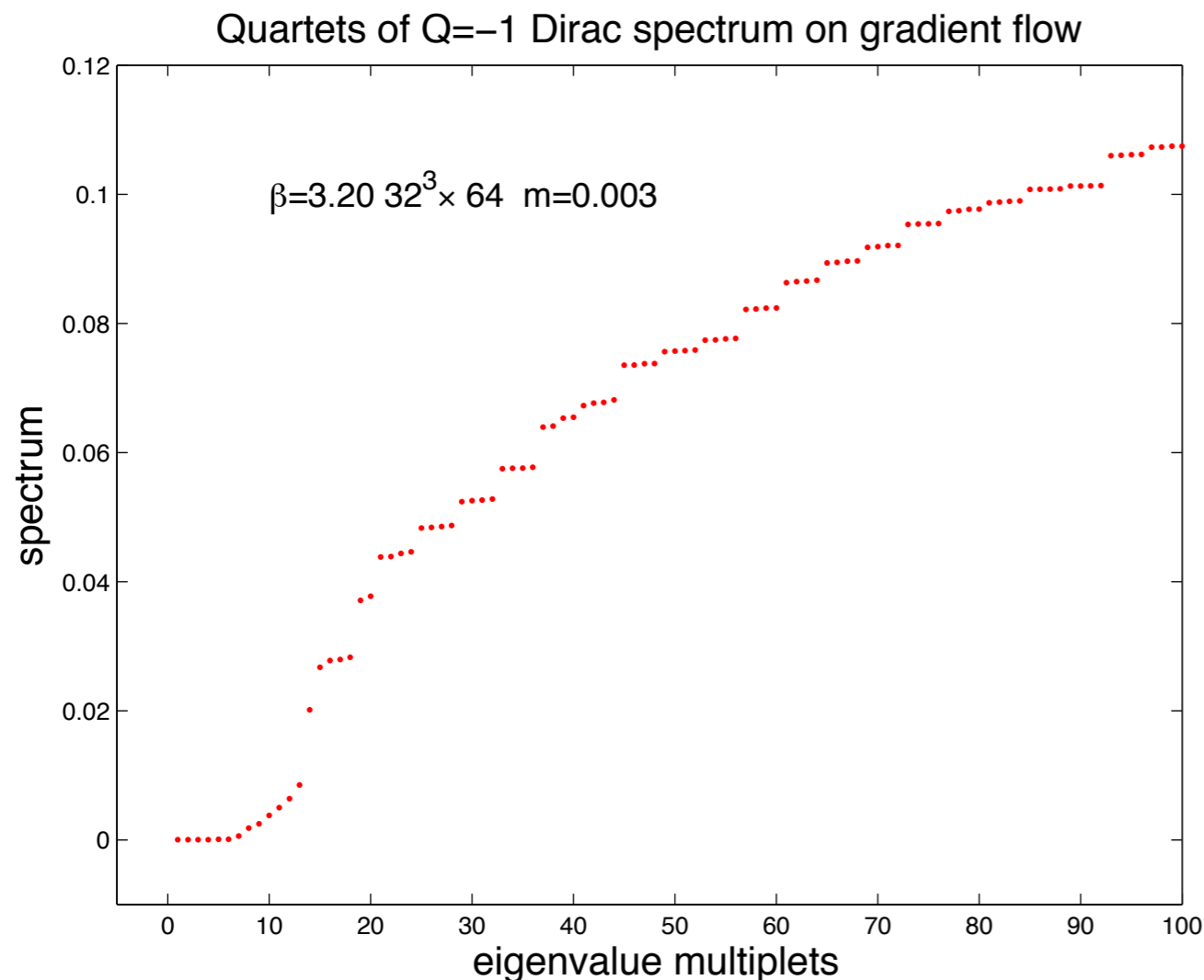
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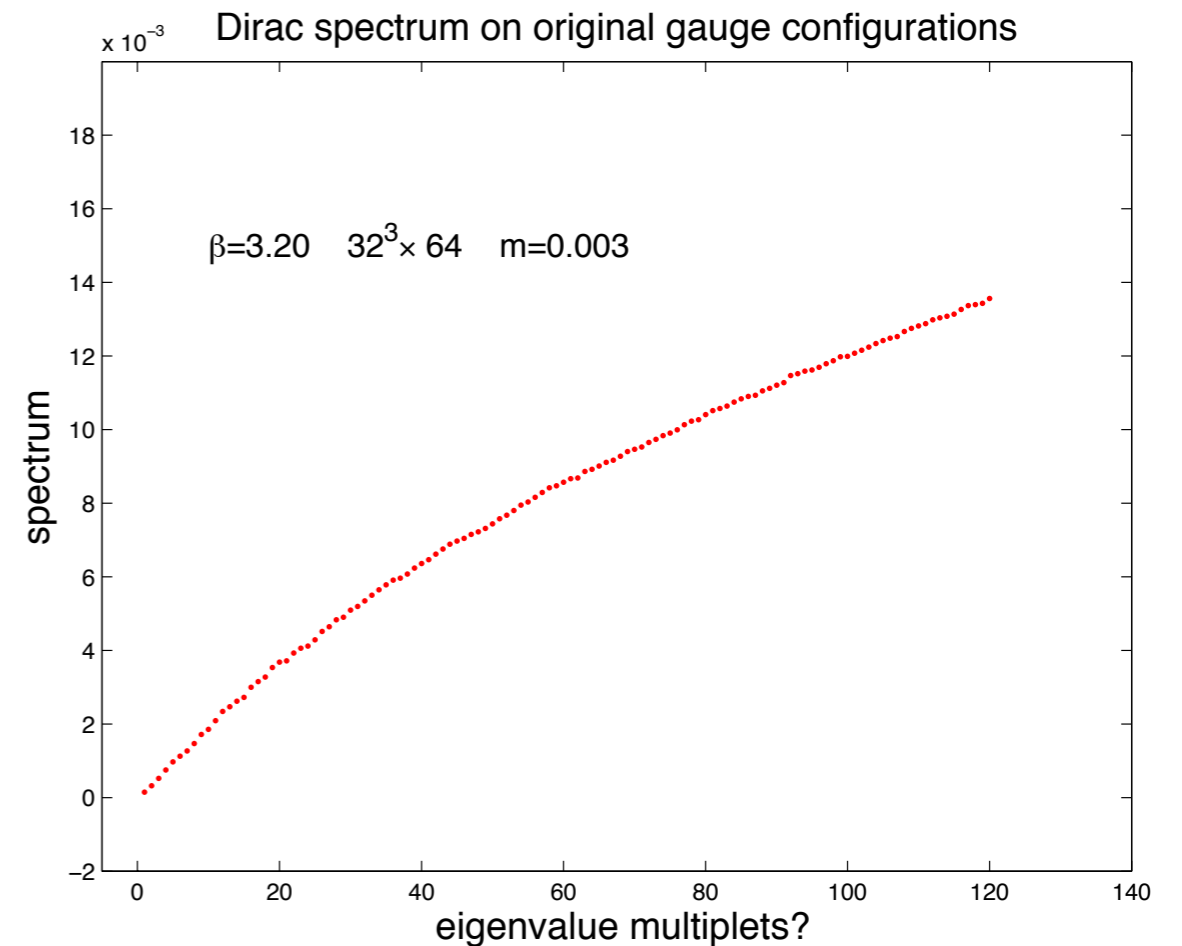
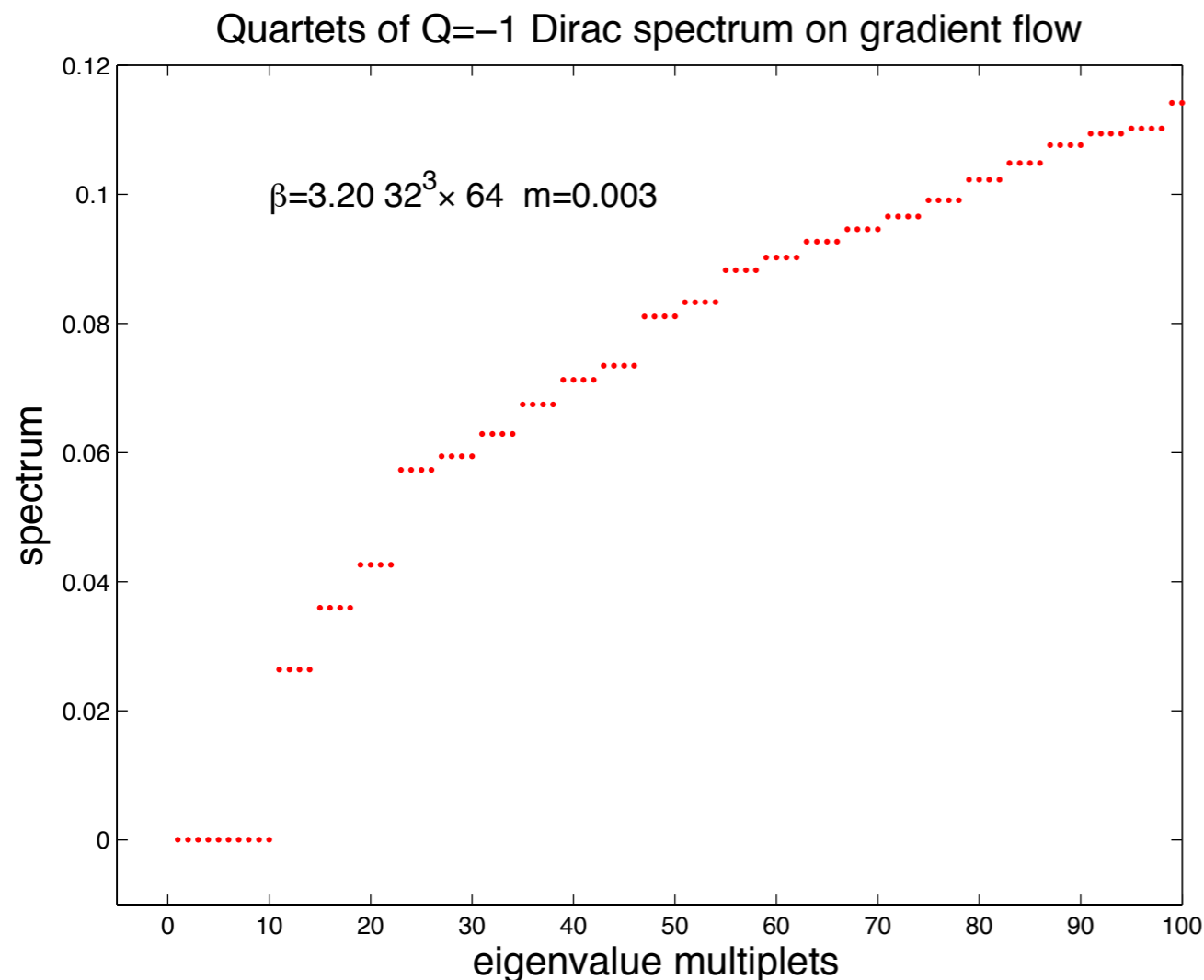
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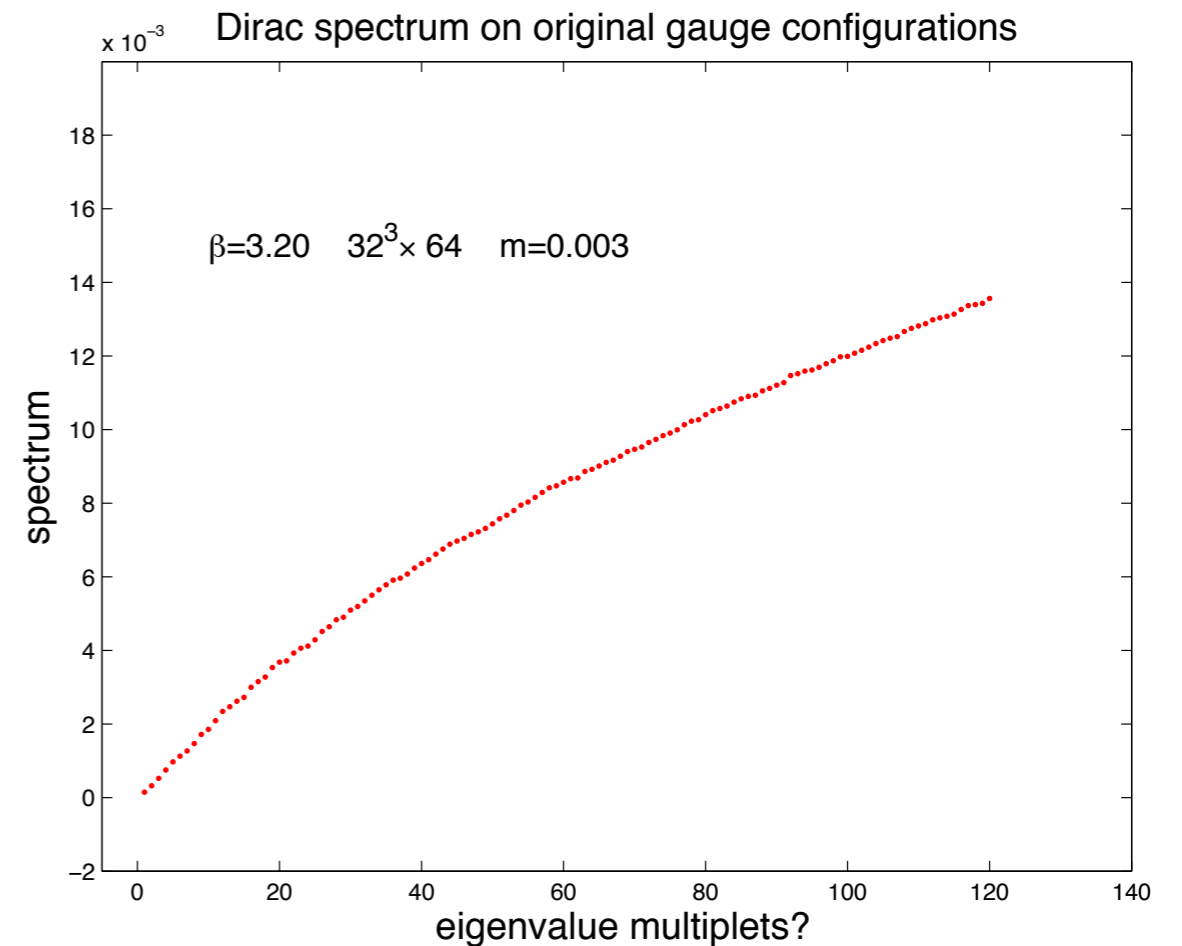
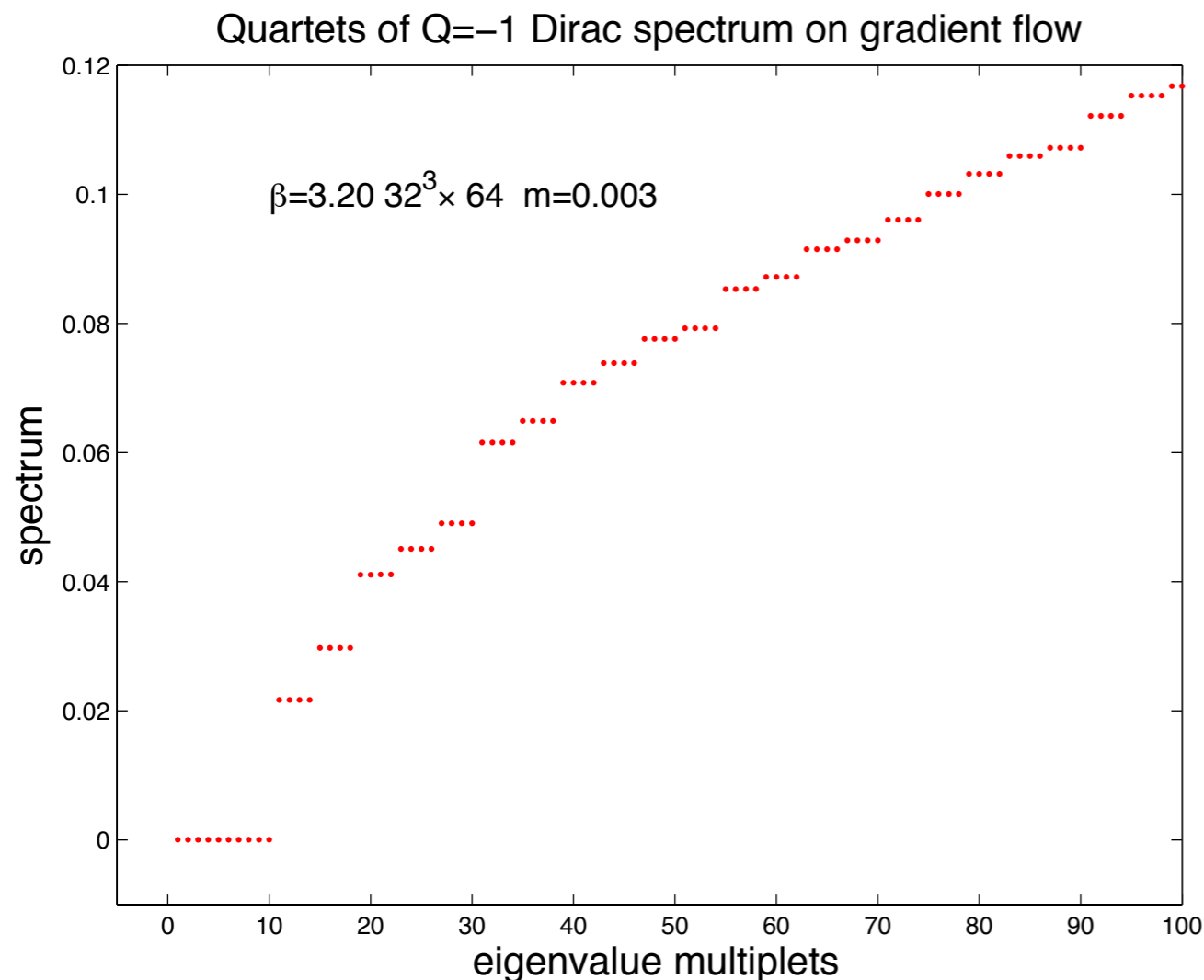
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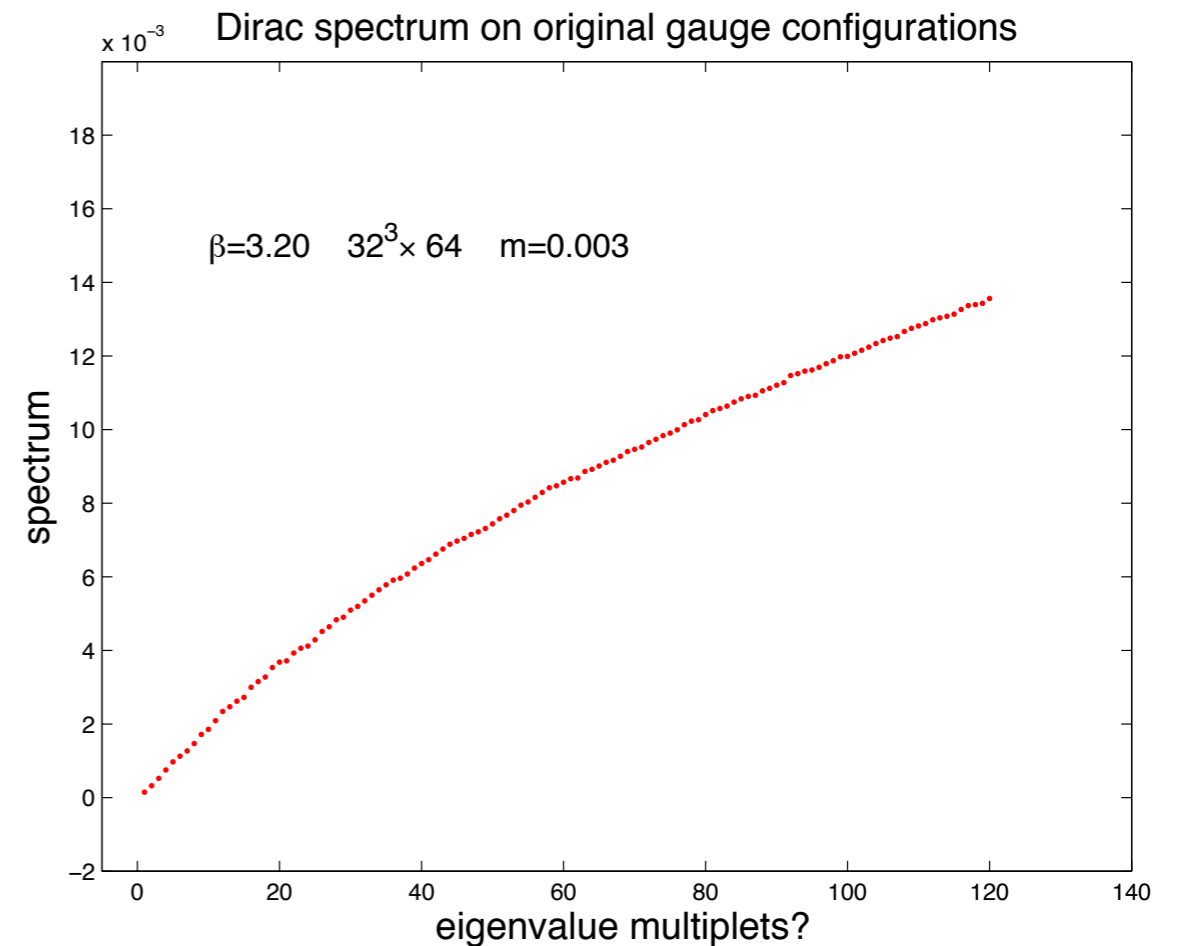
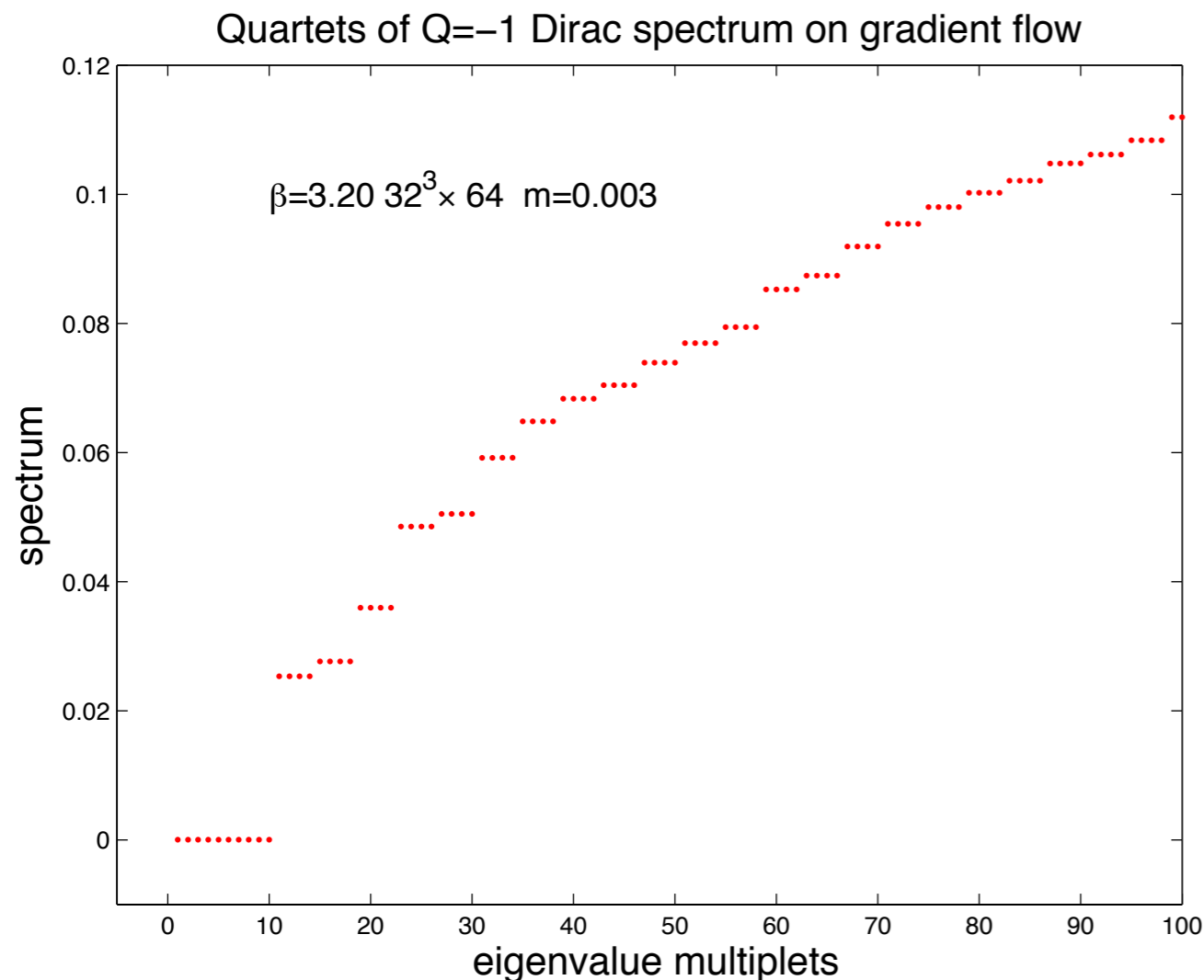
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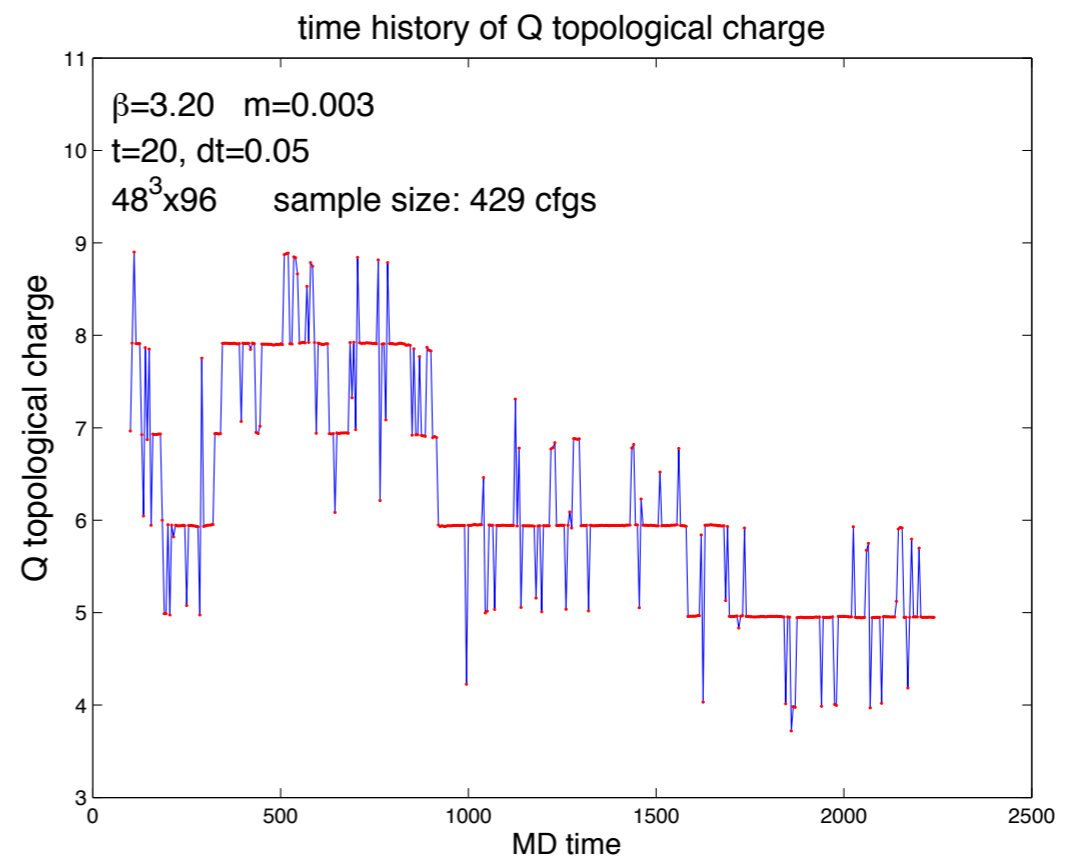
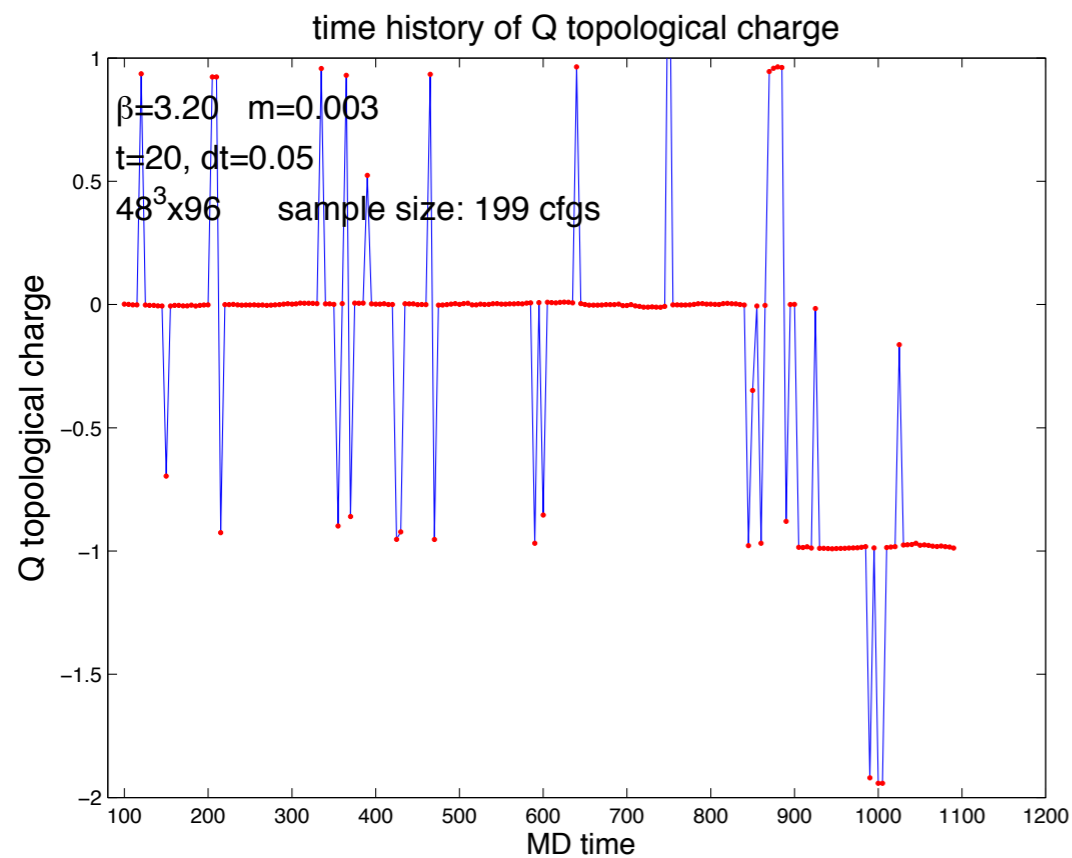
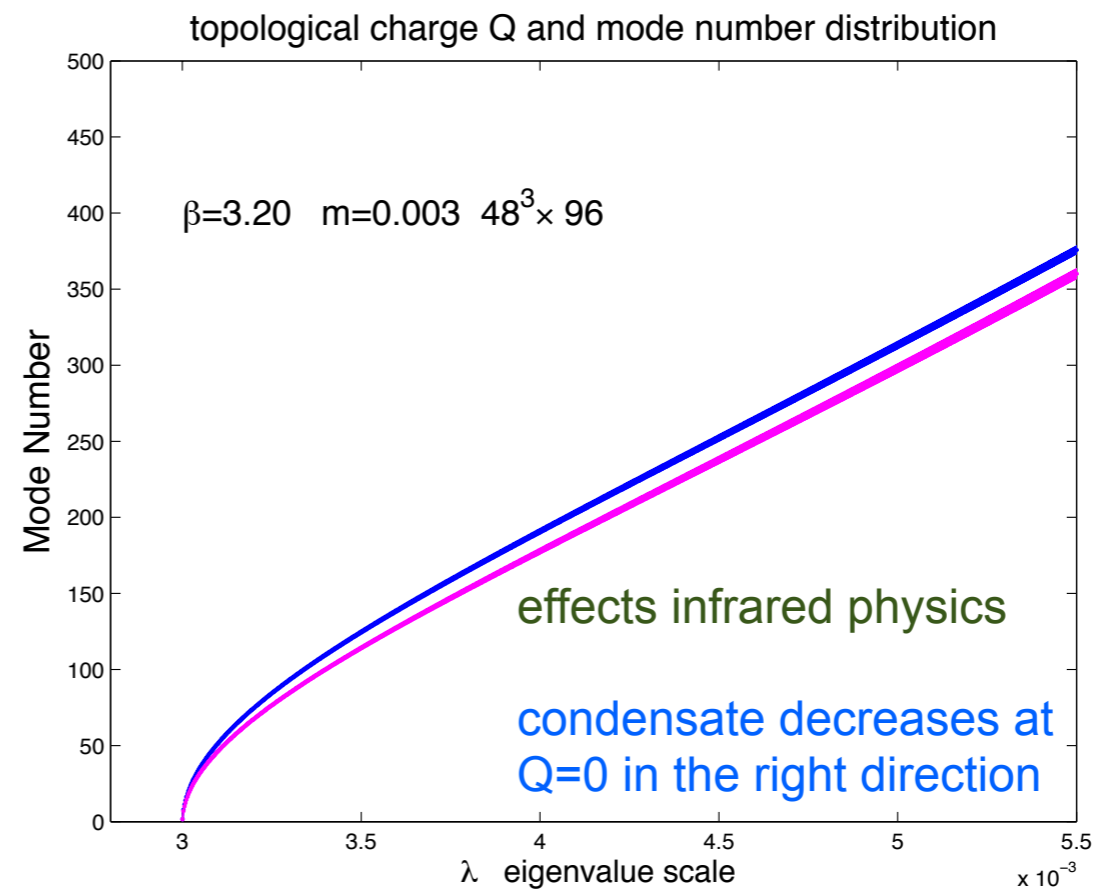
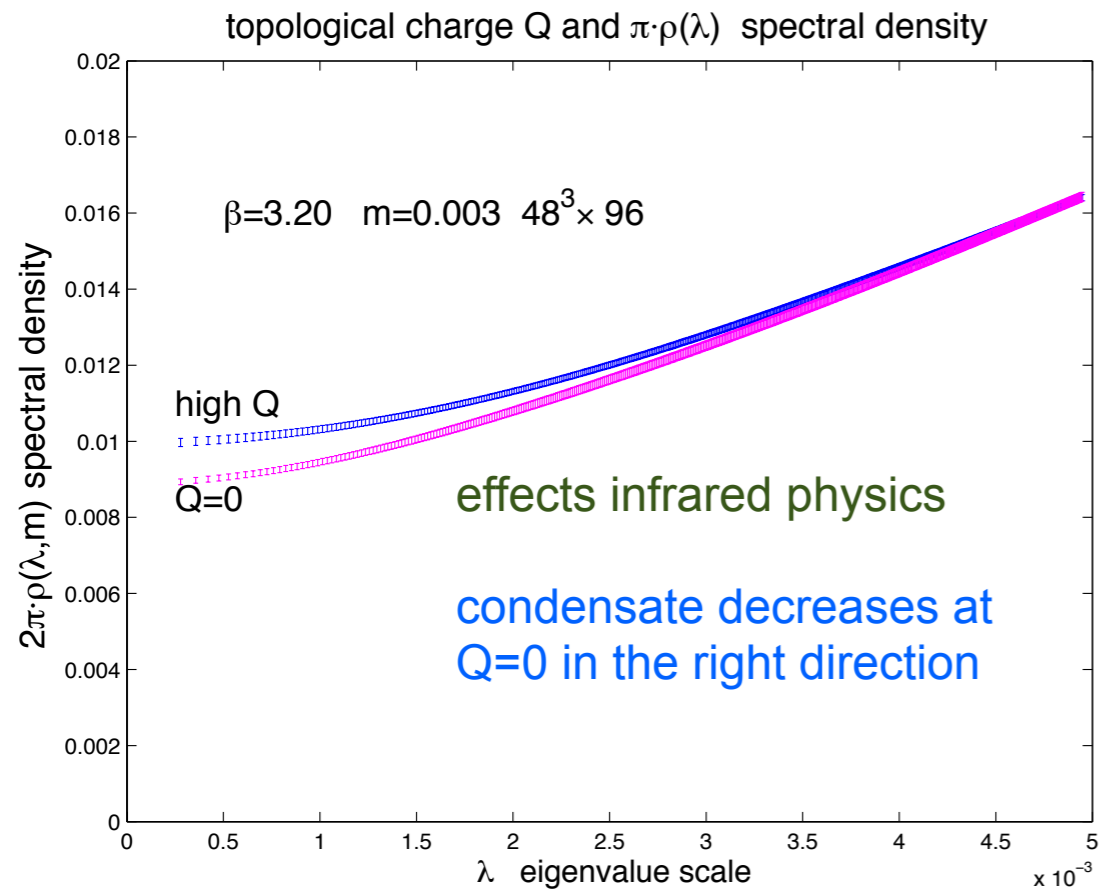
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Early universe

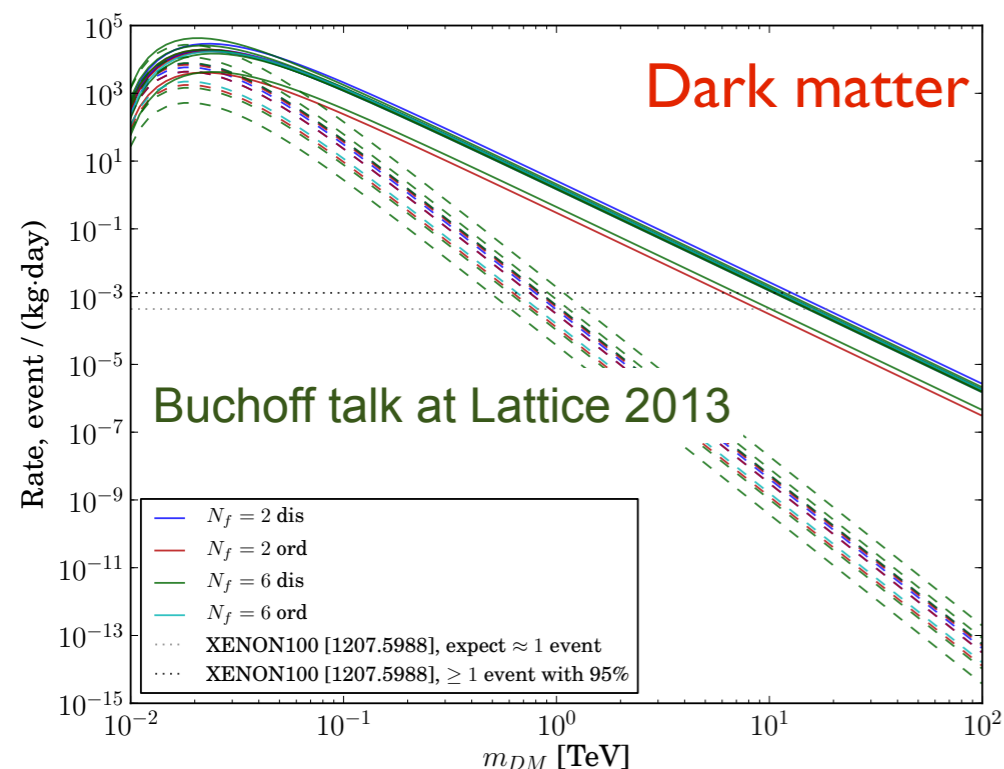
Kogut-Sinclair work finite temperature χ SB phase transition?
Relevance in early cosmology (order of the phase transition?)

The Total Energy of the Universe:

Vacuum Energy (Dark Energy) $\sim 67\%$
Dark Matter $\sim 29\%$
Visible Baryonic Matter $\sim 4\%$

Dark matter

self-interacting?
 $O(\text{barn})$ cross section would be challenging



- lattice BSM phenomenology of dark matter pioneering LSD work

- $N_f=2$ $Q_u=2/3$ $Q_d = -1/3$
udd neutral dark matter candidate

- dark matter candidate sextet $N_f=2$
electroweak active in the application

- there is room for third heavy fermion flavor as electroweak singlet

- rather subtle sextet baryon construction (symmetric in color)

Mondal 8C Friday

Summary and Outlook

Simplest composite scalar is light near conformality ?

light scalar (dilaton-like?) emerging

close to conformal window?

running (walking) coupling in progress

difficult, Gradient Flow is huge improvement

chiral condensate

new method is very promising

spectroscopy

emerging resonance spectrum $\sim 2\text{-}3\text{ TeV}$

dark matter

implications are intriguing
strong self-interactions?

Tuning with third flavor ?

We have a candidate for minimal Higgs impostor to make it fail !

Our job is not to oversell, but do everything we can to kill the model !

If we fail to kill, the model will speak for itself without naming rights

