Spectroscopy: overview and theory

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Temple University, March 19th, 2020





Istituto Nazionale di Fisica Nucleare

QCD spectrum



The spectrum of hadron excitations is incredibly rich

Several new observations beyond the minimal quark content







Color confinement Manifestation of gluonic degrees of freedom Non-perturbative dressing effects Light-q vs. heavy-q «The Electron Ion Collider will act like an enormous microscope»

We want to use it to study «human-size» hadrons!

Building the EIC spectroscopy community



Castello di Trento ("Trint"), watercolor 19.8 x 27.7, painted by A. Dürer on his way back from Venice (1495). British Museum

The Spectroscopy Program at EIC and Future Accelerators

Trento, December 19-21, 2018

Main Topics - Multiquark Spectroscopy - Ghuonic States - Diffractive production - Interaction of Heavy Flavor with media

Conveners Feng-Kun Guo (C.4.S-ITP), Ryan Mitcheil (Indiana Univ.), Nora Brambilla (TUM), Umberto Tamponi (INFN Torino), Wolfgang Schäfer (INP Erskow), Ronan McNulty (UCD), Christian Weiss (ILab), Giuseppe Bruno (Università di Bart & INFN)

> Organizers M. Battaglieri (INFN Genova), A. Pilloni (J.Lab & ECT*), A. Szczepaniak (Indiana Univ. & J.Lab)

Director of the ECT*: Professor Jochen Wambach (ECT*)

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Goals

- Demonstrate a strong physics case for a hadron spectroscopy program at EIC (to be part of the next EIC physics book)
- Study the impact on EIC design (machine and detectors)

Working groups

- Multiquark & Gluonic states conveners: F.K. Guo, R. Mitchell
- Diffractive production
 - conveners: W. Schafer, R. McNulty
- Heavy flavor in media conveners: C. Weiss, G. Bruno

Quarkonium orthodoxy & exotic

Esposito, AP, Polosa, Phys.Rept. 668



A host of unexpected resonances have appeared

Hardly reconciled with usual charmonium interpretation

(Cornell potential) Effective theories (HQET, NRQCD, pNRQCD...) approximate heavy quark

 $V(r) = -\frac{C_F \alpha_s}{r} + \sigma r$

spin symmetry (HQSS) Integrate out heavy DOF

spectrum, decay & production rates

X(3872)



Sizeable prompt production at hadron colliders, $\sim 5\%$ of $\psi(2S)$

 $\sigma_{PR} \times B(X \rightarrow J/\psi \pi \pi) =$ (1.06 ± 0.11 ± 0.15) nb @CMS

• Discovered in $B \to K X \to K J/\psi \pi \pi$

- Quantum numbers 1⁺⁺
- Very close to DD* threshold
- Too narrow for an abovetreshold charmonium
- Isospin violation too big $\frac{\Gamma(X \to J/\psi \ \omega)}{\Gamma(X \to J/\psi \ \rho)} \sim 0.8 \pm 0.3$
- Mass prediction not compatible with $\chi_{c1}(2P)$

$$\begin{split} M &= 3871.68 \pm 0.17 \; \text{MeV} \\ M_X - M_{DD^*} &= -3 \pm 192 \; \text{keV} \\ \Gamma &< 1.2 \; \text{MeV} @ 90\% \end{split}$$

Charged *Z* states: $Z_c(3900), Z'_c(4020)$

Charged quarkonium-like resonances have been found, 4q needed



Pentaquarks!





Quantum numbers $J^{P} = \begin{pmatrix} 3^{-}, 5^{+} \\ \frac{5}{2}, \frac{5^{+}}{2} \end{pmatrix} \text{ or } \begin{pmatrix} 3^{+}, 5^{-} \\ \frac{5}{2}, \frac{5^{+}}{2} \end{pmatrix} \text{ or } \begin{pmatrix} 5^{+}, 3^{-} \\ \frac{5^{+}}{2}, \frac{3^{-}}{2} \end{pmatrix}$

LHCb, PRL 122, 222001

Higher statistics analysis revealed a twopeak structure of the narrow state, plus a new lighter one Quantum numbers still unknown

Models

Compact

Extended

Hybrids Containing gluonic degrees of freedom Multiquark Several (cluster) of valence quarks





Hadroquarkonium

Heavy core interacting with a light cloud via Van der Waals forces

Rescattering effects

Structures generated by cross-channel rescattering, very process-dependent



Molecule

Bound or virtual state generated by long-range exchange forces

What at the EIC?

- High energy in the CoM, possibility to study heavy flavors charm sector well explored, little is known for the bottom sector
 - Meson(-like) spectroscopy: X_{b,c}, Z_{b,c}
 - Baryon(-like) spectroscopy: P_{b,c}
- Coupling to (virtual) photons can provide more information about their nature
- Interaction of exotic with nuclear media can complement the study in AA and pA

Need for cross section estimates of signal + irreducible background



Reactions to be studied for the YR

- Exclusive *P_c* photoproduction: C. Fanelli, A. Hiller Blin, D. Winney,
- Exclusive X, \tilde{X}, Z photoproduction: M. Albaladejo
- Diffractive semi-inclusive ph.production: V. Mathieu, A. Szczepaniak
- Semi-inclusive X production: AP, X. Yao
- (study of the scalar exotics in $\gamma\gamma$ fusion)
- (production of hybrids and doubly heavy)



- all to be extended to the $b\overline{b}$ sector
- Partial overlap with Exclusive and Diffractive WG

Exclusive P_c photoproduction



At Jlab12 measurements of direct P_c production are being performed

Using VMD, BR($P_c \rightarrow J/\psi p$) ~ 1%





Exclusive P_c photoproduction



At EIC energies the direct production is negligible, backward region dominated by u-channel P_c exchange Main bkg is due to ordinary N^{*} exchanges OZI suppressed

All couplings are known or related to the GlueX BR estimate

Polarized P_c photoproduction



 $\sim s^{\alpha(u)}$

Sensitivity of Polarization observables to 5q parameters at SBS Easily extended for the EIC

D. Winney, C. Fanelli, AP et al. (JPAC), PRD100, 034019

Exclusive X, Z_c photoproduction



 Z_c^+ production has been studied in the literature Lin, Liu, Xu PRD88, 114009

VMD + saturation of the width by measured decay modes provide rigid prediction

Vector meson exchange is well known, and leads to rigid prediction for the *X*



COMPASS claimed the existence of a state degenerate with the X(3872), but with C = 1

Large photoproduction cross section

Another \tilde{X} ?



COMPASS claimed the existence of a state degenerate with the X(3872), but with C = 1

Large photoproduction cross section

Diffractive semi-inclusive Z_c ph.



Large rapidity gap

If the target fragments are separated from the beam ones, one can invoke Regge factorization Diffractive semi-inclusive Z_c ph.



If the target fragments are separated from the beam ones, one can invoke Regge factorization Quark-Regge duality allows to replace the intermediate hadrons with a Pomeron exchange Triple Pomeron vertex well known Model needed for $Z_c^0 \gamma \mathbb{P}$ coupling

Semi-inclusive *X* production

For large Q^2 one can invoke NRQCD factorization to describe quarkonium(-like) production

$$d\sigma(e^- + p \to H + X) = \sum d\sigma(e^- + p \to Q\overline{Q}(n) + X) \langle \mathcal{O}^H(n) \rangle$$

Н

X

n

Perturbative partonic matrix element, calculable

> Nonperturbative transition matrix element $Q\overline{Q} \rightarrow H$ fitted from data

Semi-inclusive X production

One can assume the same NRQCD factorization for exotics, independent of their internal structure

$$\sigma[X(3872)] = \sum_{n} \hat{\sigma}[c\bar{c}_{n}] \langle \mathcal{O}_{n}^{X} \rangle,$$

 $Br[X \to J/\psi \pi^{+}\pi^{-}] \left(\langle \mathcal{O}_{8}^{X}(^{3}S_{1}) \rangle + 0.159 \ \langle \mathcal{O}_{8}^{X}(^{1}S_{0}) \rangle + 0.085 \ \langle \mathcal{O}_{1}^{X}(^{1}S_{0}) \rangle \right.$ $\left. + 0.00024 \ \langle \mathcal{O}_{1}^{X}(^{3}S_{1}) \rangle \right) = (2.7 \pm 0.6) \times 10^{-4} \text{ GeV}^{3}$ Artoisenet and Braaten, PRD81, 114018 from Tevatron data

If one consider the first term only, it leads to

$$Br[X \to J/\psi \pi^+ \pi^-] \sigma(X(3872), Q^2 > 1 \text{ GeV}) \approx 2.6 \text{ pb}$$
 $\sqrt{s} = 100 \text{ GeV}$

Production of other exotics

Other cross sections have been estimated, generally quite large

Guo et al. EPJC74, 9, 3063 Guo et al. CTP, 61, 354

	$Z_b(10610)$	$Z_b(10650)$	$Z_{c}(3900)$	$Z_{c}(4020)$
Tevatron	0.26(0.47)	0.06(0.17)	11(13)	1.7(2.0)
LHC 7	4.8(8.0)	1.2(3.0)	187(211)	29(31)
LHCb 7	0.76(1.3)	0.18(0.47)	33(39)	5.5(5.8)
LHC 8	5.9(9.5)	1.4(3.5)	220(240)	34(36)
LHCb 8	0.9(1.4)	0.22(0.56)	40(48)	6.3(6.9)
LHC 14	11(17)	2.6(6.5)	382(423)	61(63)
LHCb 14	1.9(3.0)	0.52(1.2)	84(88)	14(14)

X_b	$E_{X_b} = 24 \text{ MeV}(\Lambda = 0.5 \text{ GeV})$	$E_{X_b} = 66 \text{ MeV}(\Lambda = 1 \text{ GeV})$
Tevatron	0.08(0.18)	0.61(1.4)
LHC 7	1.5(3.1)	12(23)
LHCb 7	0.25(0.49)	1.9(3.7)
LHC 8	1.8(3.6)	14(27)
LHCb 8	0.3(0.62)	2.2(4.7)
LHC 14	3.2(6.8)	24(51)
LHCb 14	0.65(1.3)	4.9(9.7)



Estimates can be given using MC generators, using coalescence model and assuming a molecular nature for the exotics

Summary

- Exclusive *P_c* photoproduction: C. Fanelli, A. Hiller Blin, D. Winney,
- Exclusive X, \tilde{X}, Z photoproduction: M. Albaladejo
- Diffractive semi-inclusive ph.production: V. Mathieu, A. Szczepaniak
- Semi-inclusive *X* production: AP, X. Yao

BACKUP



Multiscale system

 $m_0 \gg m_0 v \gg m_0 v^2$ Systematically integrate $m_b \sim 5 \text{ GeV}, m_c \sim 1.5 \text{ GeV}$ out the heavy scale, $v_h^2 \sim 0.1, v_c^2 \sim 0.3$ $m_0 \gg \Lambda_{OCD}$ Full QCD ---- NRQCD ----- pNRQCD 3.5 BELLE data: √s = 10.6 GeV 60 GeV < W < 240 GeV dơ/dp_T(pp→J/γ+X) × B(J/γ→μμ) [nb/GeV] ATLAS data: √s = 7 TeV 0.8 10 0.3 < z < 0.9CS+CO, NLO: Butenschön et al. |y| < 0.75 3 $Q^2 < 2.5 \text{ GeV}^2$ $d\sigma(ep \rightarrow J/\psi + X)/dp_T^2 \ [nb/GeV^2]$ 0.6 10 CDF data: √s = 1.96 TeV √s = 319 GeV 2.5 2 2 [dd] (X+/n/)(← 9+0)Ω 1 0.4 10 |y| < 0.60.2 $\lambda_{\theta}(p_T)$ 10⁻² ŦŦ Ŧ 10 0 Į -0.2 10-2 10⁻³ -0.4 1 10^{-3} $p\bar{p} \rightarrow J/\psi + X$, helicity frame data: HERA1 10-4 -0.6 H1 data: HERA2 CDF data: $\sqrt{s} = 1.96$ TeV, |y| < 0.60.5 10 -0.8 CS+CO, NLO: Butenschön et al. S+CO, NLO: Butenschön et al. +CO, NLO: Butenschön et al 10^{-t} 0 10² 40 25 35 10 15 20 10 15 20 25 30 (b)¹ (**d**) **(a)** 10 (c) $p_T^2 [GeV^2]$ p_T [GeV] p_T [GeV]

Factorization (to be proved) of universal LDMEs

Good description of many production channels, some known puzzles (polarizations)

Comparison: EIC vs. others

Too late (?) for charm physics 😕

Flexibility in the production mechanism \checkmark Flexibility in energy (no Λ_b) \checkmark Less clean environment *

Same luminosity ✓ Lower cross sections ≭ Better efficiencies for neutrals (?) ✓

Polarized electron & ion beams 🗸

BEST





Hybrid production



Suprisingly, no calculation for heavy hybrid production has been carried out so far

The only example for B decays is Petrov et al. PRD58, 034013

Room for improvement and inclusion of the large number of gluons at small x

Doubly heavy



Lots of attention recently on tetraquark and baryons with two heavy quarks, driven by LHCb and lattice results

> Quigg and Eicthen, PRL119, 202002 Esposito, AP et al. PRD88, 054029 Karliner and Rosner, PRD90, 094007 Karliner and Rosner, PRL119, 202001 Francis et al. PRL118, 142001

MC code available, GENXICC2.0, which implements the heavy diquark in Pythia NRQCD approach in e^+e^- collisions in Chen et al. JHEP1412, 018

X(3872)

Large prompt production at hadron colliders $\sigma_B / \sigma_{TOT} = (26.3 \pm 2.3 \pm 1.6)\%$

 $\sigma_{PR} \times B(X \rightarrow J/\psi \pi \pi)$ = (1.06 ± 0.11 ± 0.15) nb

CMS, JHEP 1304, 154



B decay mode	X decay mode	product branchin	g fraction $(\times 10^5)$	B_{fit}	R_{fit}
K^+X	$X \to \pi \pi J/\psi$	0.86 ± 0.08	$(BABAR, \frac{26}{25} Belle^{25})$	$0.081^{+0.019}_{-0.031}$	1
		$0.84 \pm 0.15 \pm 0.07$	BABAR ²⁶		
		$0.86 \pm 0.08 \pm 0.05$	Belle^{25}		
$K^0 X$	$X \to \pi \pi J\!/\!\psi$	0.41 ± 0.11	$(BABAR, 26 Belle^{25})$		
		$0.35 \pm 0.19 \pm 0.04$	BABAR ²⁶		
		$0.43 \pm 0.12 \pm 0.04$	Belle^{25}		
$(K^+\pi^-)_{NR}X$	$X \to \pi \pi J\!/\!\psi$	$0.81 \pm 0.20^{+0.11}_{-0.14}$	Bellc ¹⁰⁶		
$K^{*0}X$	$X \to \pi \pi J / \psi$	< 0.34, 90% C.L.	Belle^{106}		
KX	$X ightarrow \omega J/\psi$	$R=0.8\pm0.3$	BABAR ³³	$0.061^{+0.024}_{-0.036}$	$0.77^{+0.28}_{-0.32}$
K^+X		$0.6\pm0.2\pm0.1$	BABAR ³³		
$K^0 X$		$0.6\pm0.3\pm0.1$	BABAR ³³		
KX	$X \to \pi \pi \pi^0 J/\psi$	$R=1.0\pm0.4\pm0.3$	Belle^{32}		
K^+X	$X \to D^{*0} \bar{D}^0$	8.5 ± 2.6	$(BABAR, \frac{38}{38} Belle^{37})$	$0.614^{+0.166}_{-0.074}$	$8.2^{+2.3}_{-2.8}$
		$16.7\pm3.6\pm4.7$	BABAR ³⁸		
		$7.7\pm1.6\pm1.0$	$\operatorname{Belle}^{\overline{37}}$		
$K^0 X$	$X \to D^{*0} \bar{D}^0$	$f 12\pm4$	$(BABAR, \frac{38}{38} Belle^{37})$		
		$22\pm10\pm4$	BABAR ³⁸		
		$9.7\pm4.6\pm1.3$	Belle ³⁷		
K^+X	$X \to \gamma J/\psi$	0.202 ± 0.038	$(BABAR, \frac{35}{35} Bellc \frac{34}{35})$	$0.019^{+0.005}_{-0.009}$	$0.24_{-0.06}^{+0.05}$
K^+X		$0.28 \pm 0.08 \pm 0.01$	BABAR ³⁵		
		$0.178^{+0.048}_{-0.044} \pm 0.012$	Bellc ³⁴		
$K^0 X$		$0.26 \pm 0.18 \pm 0.02$	BABAR ³⁵		
		$0.124^{+0.076}_{-0.061} \pm 0.011$	Belle^{34}		
K^+X	$X \to \gamma \psi(2S)$	0.44 ± 0.12	BABAR ³⁵	$0.04^{+0.015}_{-0.020}$	$0.51^{+0.13}_{-0.17}$
K^+X		$0.95 \pm 0.27 \pm 0.06$	BABAR ³⁵		
		$0.083^{+0.198}_{-0.183} \pm 0.044$	Belle^{34}		
		$R' = 2.46 \pm 0.64 \pm 0.29$	LHCb ³⁶		
$K^0 X$		$1.14 \pm 0.55 \pm 0.10$	BABAR ³⁵		
		$0.112^{+0.357}_{-0.290} \pm 0.057$	$\operatorname{Bellc}^{34}$		
K^+X	$X \to \gamma \chi_{c1}$	$< 9.6 \times 10^{-3}$	Belle^{23}	$< 1.0 \times 10^{-3}$	< 0.014
K^+X	$X \to \gamma \chi_{c2}$	< 0.016	Belle ²³	$< 1.7 \times 10^{-3}$	< 0.024
KX	$X \to \gamma \gamma$	$< 4.5 \times 10^{-3}$	Belle^{111}	$< 4.7 \times 10^{-4}$	$< 6.6 \times 10^{-3}$
KX	$X \to \eta J/\psi$	< 1.05	BABAR ¹¹²	< 0.11	< 1.55
K^+X	$X \to p\bar{p}$	$< 9.6 \times 10^{-4}$	LHCb ¹¹⁰	$< 1.6 \times 10^{-4}$	$< 2.2 \times 10^{-3}$

Prompt production of *X*(3872)

The question is:



«Are large prompt production cross sections at hadron colliders compatible with a loosely bound molecule interpretation?»

 $M = 3871.69 \pm 0.17 \text{ MeV}$ $E_B = M_{DD^*} - M_X = 10 \pm 200 \text{ keV (PDG)}$ $\Gamma < 1.2 \text{ MeV @90\%}$

The width of the D^* and of the X(3872) are neglected, according to Weinberg's spirit The X(3872) is considered a (stable) bound state of (stable) $\overline{D}{}^0 D^{*0}$

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$$k_B = \sqrt{2\mu E_B} \sim 20$$
 MeV, $R = \frac{1}{k_B} \sim 10$ fm

Hadronic molecules with MC simulations

We aim to evaluate prompt production cross section at hadron colliders via Monte-Carlo simulations

Q. What is a molecule in MC? A. «Coalescence» model



Estimating k_{max}

The choice of k_{max} is crucial. By phase space argument, the cross section scales as k_{max}^3 , small changes have huge impacts on the results



Alternative, one can model the binding potential.

For example, a simple square well with this corresponds to:

 $\frac{\sqrt{\langle k^2 \rangle}}{\sqrt{\langle r^2 \rangle}} \approx 50 \text{ MeV},$ $\frac{\sqrt{\langle r^2 \rangle}}{\sqrt{\langle r^2 \rangle}} \approx 10 \text{ fm}$

2009 Results



We tune our MC to reproduce CDF distribution of $\frac{d\sigma}{d\Delta\phi}(p\bar{p} \rightarrow D^0 D^{*-})$ We get $\sigma(p\bar{p} \rightarrow DD^*|k < k_{max}) \approx 0.1$ nb $@\sqrt{s} = 1.96$ TeV Experimentally $\sigma(p\bar{p} \rightarrow X(3872)) \approx 30 - 70$ nb!!!

Bignamini, Grinstein, Piccinini, Polosa, Sabelli PRL103 (2009) 162001

Estimating k_{max} -- Part II

A solution can be Final State Interactions (rescattering of DD^*) Artoisenet and Braaten, PRD81, 114018

$$\mathcal{M} = -NA_{prod}^{on} \cdot \frac{e^{i\delta}\sin\delta}{ka_{NN}}$$

Watson-Migdal model for FSI, the on-shell elastic scattering matrix multiplies the production amplitude

$$\sigma(p\bar{p} \to X(3872)) \to \sigma(p\bar{p} \to DD^* | k < k_{max}) \times \frac{6\pi\sqrt{2\mu E_B}}{k_{max}}$$

Estimating k_{max} -- Part II

A solution can be Final State Interactions (rescattering of DD^*) Artoisenet and Braaten, PRD81, 114018

$$\mathcal{M} = -NA_{prod}^{on} \cdot \frac{e^{i\delta}\sin\delta}{ka_{NN}}$$



Watson-Migdal model for FSI, the on-shell elastic scattering matrix multiplies the production amplitude

To take into account the rescattering correctly, one needs to integrate up to the scale of the mediator,

 $\sigma_{FSI}(p\bar{p} \to DD^* | k < 2m_{\pi}) \approx 23 \text{ nb}$ $\sigma(p\bar{p} \to DD^* | k < 5m_{\pi}) \approx 230 \text{ nb}$

Estimating k_{max} -- Part III & IV

Watson-Migdal approach requires the DD^* to recoil onto some debrys. The theorem is challenged by the presence of pions that interfere with DD^* propagation

Bignamini, Grinstein, Piccinini, Polosa, Riquer, Sabelli, PLB684, 228-230

FSI saturate unitarity bound, the D and D^* only talk with each other Artoisenet and Braaten, PRD83, 014019

What is the role of 2-body unitarity in a 100-body high energy collision?

A new mechanism?

In a more billiard-like point of view, the comoving pions can elastically interact with $D(D^*)$, and slow down the DD^* pairs



Esposito, Piccinini, AP, Polosa, JMP 4, 1569 Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

The mechanism also implies: *D* mesons actually "pushed" inside the potential well (the classical 3-body problem!)

X(3872) is a real, negative energy bound state (stable) It also explains a small width $\Gamma_X \sim \Gamma_{D^*} \sim 100 \text{ keV}$



By comparing hadronization times of heavy and light mesons, we estimate up to ~ 3 collisions can occur before the heavy pair to fly apart

We get $\sigma(p\bar{p} \rightarrow X(3872)) \sim 5$ nb, still not sufficient to explain all the experimental cross section



Estimating k_{max} -- Part V

$$\begin{split} \sigma(\bar{p}p \to X) &\sim \left| \int d^{3}\mathbf{k} \langle X|D^{0}\bar{D}^{*0}(\mathbf{k})\rangle \langle D^{0}\bar{D}^{*0}(\mathbf{k})|\bar{p}p\rangle \right|^{2} \\ &\simeq \left| \int_{\mathcal{R}} d^{3}\mathbf{k} \langle X|D^{0}\bar{D}^{*0}(\mathbf{k})\rangle \langle D^{0}\bar{D}^{*0}(\mathbf{k})|\bar{p}p\rangle \right|^{2} \\ &\leq \int_{\mathcal{R}} d^{3}\mathbf{k} \left| \Psi(\mathbf{k}) \right|^{2} \int_{\mathcal{R}} d^{3}\mathbf{k} \left| \langle D^{0}\bar{D}^{*0}(\mathbf{k})|\bar{p}p\rangle \right|^{2} \\ &\leq \int_{\mathcal{R}} d^{3}\mathbf{k} \left| \langle D^{0}\bar{D}^{*0}(\mathbf{k})|\bar{p}p\rangle \right|^{2} \end{split}$$

The estimate of the k_{max} has been brought back

Albaladejo et al. arXiv:1709.09101

The essence of the argument is that one has to look at the integral of the wave function

$$\int_R d^3 \mathbf{k} \, \psi(\mathbf{k})$$



Estimating k_{max} -- Part VI

However, the integral of the wave function may not be well defined. For example, if one considers the wave function in the scattering length approximation,

 $\psi(\mathbf{k}) = \frac{1}{\pi} \frac{a^{3/2}}{a^2 k^2 + 1}$ it's not integrable

Esposito, AP et al. arXiv:1709.09631

A physical value should rather be based on expectation values which involve $|\psi({f k})|^2$

For example, an estimate using the virial theorem gives $k \sim 100$ MeV for the deuteron



Estimating k_{max} -- Part VI

An accurate calculation using several deuteron *S*-wave functions available on the market (for example <u>https://www.phy.anl.gov/theory/research/av18/deut.wfk</u>) give

$$d^{3}\mathbf{k} |\psi(\mathbf{k})|^{2} = 90\%$$
 for $k_{max} = 110$ MeV

This also show that this region is well controlled by pion exchange - universal



Light nuclei at ALICE

In 2015, ALICE published data on production of light nuclei in Pb-Pb and *pp* collisions

These might provide a benchmark for *X*(3872) production



Nuclear modification factors

We can use deuteron data to extract the values of the nuclear modification factors (caveat: for RAA data have different \sqrt{s})



Light nuclei at ALICE

Esposito, Guerrieri, Maiani, Piccinini, AP, Polosa, Riquer, PRD92, 034028

We assume a pure Glauber model (RAA = 1) and a value RAA = 5 to rescale Pb-Pb data to pp



Light nuclei at ALICE vs. X(3872)

Esposito, Guerrieri, Maiani, Piccinini, AP, Polosa, Riquer, PRD92, 034028

We assume a pure Glauber model (RAA = 1) and a value RAA = 5 to rescale Pb-Pb data to pp

The X(3872) is way larger than the extrapolated cross section



Light nuclei at ALICE vs. X(3872)

If the production is long-distance dominated, that's pretty much it.

0.8

7 TeV

If it's short-distance dominated, one can think on an effect related to the number of quarks involved, in the spirit of constituent counting rules

> Brodsky and Lebed, PRD91, 114025 Guo et al., CPC41, 053108 Voloshin, PRD94, 074042 Wang, CPC42, 043103

However, it is not easy to make sense of constituent counting rules in inclusive reactions, where you cannot track the energy carried by each quark

0.2 o(pp-Based on LHCb data in JHEP 1705 (2017) 074 0 2 3 5 7 6 p_t (GeV) S. Stone

 Λ_{c}^{+}/D^{+}

They seem to spectacularly fail

8

Production of Y(4260) and $P_c(4450)$

Given the new lineshape by BESIII, we need to rethink the binding energy of the Y(4260)J. Nys and AP, to appear

	Constituents	Bind. Energy	Bind. Mom.	Mediator
X(3872)	$\overline{D}{}^0D^{*0}$	~100 keV	~50 MeV	1π (~300 MeV)
Y(4260)	$\overline{D}D_1$	~70 MeV	~400 MeV	2π (~600 MeV)
$P_{c}(4450)$	$\overline{D}^*\Sigma_c$	~10 MeV	~150 MeV	1π (~300 MeV)

If the states are purely hadron molecule, all the properties depend on the position of the pole with respect to threshold – all the features are universal

Production of Y(4260) and $P_c(4450)$

We can use Pythia to simulate the production of event, and calculate the relative production of Y(4260) and $P_c(4450)$ with respect to the X(3872) J. Nys and AP, to appear



Production of Y(4260) and $P_c(4450)$

Naively, the fragmentation function of the D_1 is 1/10 of the D^* , but the cross section scales as k_{max}^3



J. Nys and AP, to appear

Conclusions

- An Electron Ion Collider is going to be a challenge from any point of view
- The spectroscopy program requires an intense effort from the theory side, to exploit all the unique features of the new machine
- The working group just started working, some estimates are on the way.
 We need people and ideas!
- We aim to have a workshop in December, and to wrap up the white book in ~ 1 year from now

Thank you

Charged *Z* states: $Z_b(10610), Z'_b(10650)$



If the amplitude is a free complex number, in each bin of $m_{\psi'\pi^-}^2$, the resonant behaviour appears as well

Charged Z states: Z(4430)



Flavored *X*(5568)





- A flavored state seen in $B_s^0 \pi$ invariant mass by D0 (both $B_s^0 \rightarrow J/\psi \phi$ and $\rightarrow D_s \mu \nu$),
- not confermed by LHCb or CMS
- (different kinematics? Compare differential distributions)

Controversy to be solved

Joint Physics Analysis Center

- Joint effort between theorists and experimentalists to work together to make the best use of the next generation of very precise data taken at JLab and in the world
- Created in 2013 by JLab & IU agreement
- It is engaged in education of further generations of hadron physics practitioners



A. Pilloni – JPAC program for Hadron Spectroscopy

P_c photoproduction

To exclude any rescattering mechanism, we propose to search the $P_c(4450)$ state in photoproduction.



 $\langle \lambda_{\psi} \lambda_{p'} | T_r | \lambda_{\gamma} \lambda_p \rangle = \frac{\langle \lambda_{\psi} \lambda_{p'} | T_{\text{dec}} | \lambda_R \rangle}{M_r^2 - W^2 - \mathrm{i}\Gamma_r M_r} \frac{\langle \lambda_R | T_{\text{em}}^{\dagger} | \lambda_{\gamma} \lambda_p \rangle}{M_r^2 - W^2 - \mathrm{i}\Gamma_r M_r}$

Hadronic part

- 3 independent helicity couplings,
 - \rightarrow approx. equal, $g_{\lambda_{\psi},\lambda_{p'}} \sim g$
- g extracted from total width and (unknown) branching ratio

Vector meson dominance relates the radiative width to the hadronic width

$$\Gamma_{\gamma} = 4\pi\alpha \,\Gamma_{\psi p} \left(\frac{f_{\psi}}{M_{\psi}}\right)^2 \left(\frac{\bar{p}_i}{\bar{p}_f}\right)^{2\ell+1} \times \frac{4}{6}$$

Hiller Blin, AP et al. (JPAC), PRD94, 034002

Background parameterization

The background is described via an Effective Pomeron, whose parameters are fitted to high energy data from Hera



$$\begin{split} \lambda_{\psi}\lambda_{p'}|T_P|\lambda_{\gamma}\lambda_p\rangle &= \\ iA \left(\frac{s-s_t}{s_0}\right)^{\alpha(t)} e^{b_0(t-t_{\min})}\delta_{\lambda_p\lambda_{p'}}\delta_{\lambda_{\psi}\lambda_{\gamma}} \end{split}$$

Asymptotic + Effective threshold

Helicity conservation

Hiller Blin, AP et al. (JPAC), PRD94, 034002



Pentaquark photoproduction



Vector Y states



Lots of unexpected $J^{PC} = 1^{--}$ states found in ISR/direct production (and nowhere else!) Seen in few final states, mostly $J/\psi \pi\pi$ and $\psi(2S) \pi\pi$

Not seen decaying into open charm pairs Large HQSS violation



A. Pilloni – Amplitude analysis for exotic states

Vector *Y* states in BESIII

BESIII, PRL118, 092002 (2017)

BESIII, PRL118, 092001 (2017) $e^+e^- \rightarrow J/\psi \pi \pi$



Parameters	Solution I	Solution II
$\Gamma_{e^+e^-} \mathcal{B}[\psi(3770) \to \pi^+\pi^- J/\psi]$		$0.5 \pm 0.1 \; (0$
$\Gamma_{e^+e^-} \mathcal{B}(R_1 \to \pi^+\pi^- J/\psi)$	$8.8^{+1.5}_{-2.2} (\cdots)$	$6.8^{+1.1}_{-1.5} (\cdots)$
$\Gamma_{e^+e^-} \mathcal{B}(R_2 \to \pi^+\pi^- J/\psi)$	$13.3 \pm 1.4 \ (12.0 \pm 1.0)$	$9.2\pm 0.7~(8.9\pm 0.6)$
$\Gamma_{e^+e^-} \mathcal{B}(R_3 \to \pi^+\pi^- J/\psi)$	$21.1 \pm 3.9 \ (17.9 \pm 3.3)$	$1.7^{+0.8}_{-0.6} \ (1.1^{+0.5}_{-0.4})$
ϕ_1	$-58 \pm 11 \ (-33 \pm 8)$	$-116^{+9}_{-10} \ (-81^{+7}_{-8})$
ϕ_2	$-156 \pm 5 (-132 \pm 3)$	$68 \pm 24 \ (107 \pm 20)$

New BESIII data show a peculiar lineshape for the Y(4260)

The state appear lighter and narrower, compatible with the ones in $h_c \pi \pi$ and $\chi_{c0} \omega$ A broader old-fashioned Y(4260) is appearing in $\overline{D}D^*\pi$, maybe indicating a $\overline{D}D_1$ dominance

 $M(Y(4320)) = (4224.8 \pm 3.8 \pm 4.0) \text{ MeV}(2, \Gamma(Y(4220))) = (72.3 \pm 3.1 \pm 0.5) \text{ MeV}.$ $M(Y(4390)) = (4400.1 \pm 9.3 \pm 2.1) \text{ MeV}(2, \Gamma(Y(4220))) = (181.7 \pm 16.9 \pm 7.4) \text{ MeV}.$



Charged *Z* states: $Z_c(3900), Z'_c(4020)$

Charged quarkonium-like resonances have been found, 4q needed



Pentaquarks!



LHCb, PRL 115, 072001 LHCb, PRL 117, 082003 Two states seen in $\Lambda_b \rightarrow (J/\psi p) K^-$, evidence in $\Lambda_b \rightarrow (J/\psi p) \pi^ M_1 = 4380 \pm 8 \pm 29 \text{ MeV}$

 $\Gamma_1 = 205 \pm 18 \pm 86 \text{ MeV}$ $M_2 = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$ $\Gamma_2 = 39 \pm 5 \pm 19 \text{ MeV}$

Quantum numbers $J^{P} = \left(\frac{3}{2}^{-}, \frac{5}{2}^{+}\right) \operatorname{or}\left(\frac{3}{2}^{+}, \frac{5}{2}^{-}\right) \operatorname{or}\left(\frac{5}{2}^{+}, \frac{3}{2}^{-}\right)$

Opposite parities needed for the interference to correctly describe angular distributions, low mass region contaminated by Λ^* (model dependence?)

No obvious threshold nearby

A. Pilloni – Spectroscopy: overview and theory

State	M (MeV)	Γ (MeV)	J^{PC}	Process (mode)	Experiment $(\#\sigma)$	State	M (MeV)	Γ (MeV)	J^{PC}	Process (mode)	Experiment $(\#\sigma)$
X(3823)	3823.1 ± 1.9	< 24	??-	$B \to K(\chi_{c1}\gamma)$	$Belle^{23}(4.0)$	Y(4220)	4196^{+35}_{-30}	39 ± 32	1	$e^+e^- \rightarrow (\pi^+\pi^-h_c)$	BES III data ^{63,64} (4.5)
X(3872)	3871.68 ± 0.17	< 1.2	1^{++}	$B \to K(\pi^+\pi^- J/\psi)$	Belle $24,25$ (>10), BABAR 26 (8.6)	Y(4230)	4230 ± 8	38 ± 12	1	$e^+e^- \to (\chi_{c0}\omega)$	BES $III_{65}^{65}(>9)$
				$p\bar{p} \rightarrow (\pi^+\pi^- J/\psi) \dots$	$CDF^{27,28}(11.6), D0^{29}(5.2)$	$Z(4250)^+$	4248^{+185}_{-45}	177^{+321}_{-72}	$?^{?+}$	$\bar{B}^0 \to K^-(\pi^+\chi_{c1})$	Belle ⁵⁴ (5.0), BABAR ⁵⁵ (2.0)
				$pp \rightarrow (\pi^+\pi^- J/\psi) \dots$	LHCb ^{30,31} (np)	Y(4260)	4250 ± 9	108 ± 12	1	$e^+e^- \rightarrow (\pi\pi J/\psi)$	$BABAR^{66,67}(8), CLEC^{68,69}(11)$
				$B \to K(\pi^+\pi^-\pi^0 J/\psi)$	$Belle^{32}(4.3), BABAR^{33}(4.0)$	· /					Belle ^{41,53} (15), BES III ⁴⁰ (np)
				$B \to K(\gamma J/\psi)$	$Belle^{34}(5.5), BABAR^{35}(3.5)$					$e^+e^- \rightarrow (f_0(980)J/\psi)$	$BABAR^{67}$ (np), $Belle^{41}$ (np)
					LHCb ³⁶ (> 10)					$e^+e^- \to (\pi^- Z_c(3900)^+)$	BES III ⁴⁰ (8), Belle ⁴¹ (5.2)
				$B \to K(\gamma\psi(2S))$	$BABAR^{35}(3.6), Belle^{34}(0.2)$					$e^+e^- \rightarrow (\gamma X(3872))$	BES $III^{70}(5.3)$
					$LHCt^{36}(4.4)$	Y(4290)	4293 ± 9	222 ± 67	1	$e^+e^- \rightarrow (\pi^+\pi^-h_c)$	BES III data ^{63,64} (np)
				$B \to K(D\bar{D}^*)$	Belle ^[37] (6.4), BABAR ^[38] (4.9)	X(4350)	$4350.6^{+4.6}$	13^{+18}	$\frac{1}{0/2^{?+}}$	$e^+e^- \rightarrow e^+e^-(\phi Jhh)$	$\frac{B}{B} = \frac{B}{B} $
$Z_c(3900)^+$	3888.7 ± 3.4	35 ± 7	1^{+-}	$Y(4260) \to \pi^- (D\bar{D}^*)^+$	BES III ³⁹ (np)	V(4360)	4354 ± 11	$\frac{10-10}{78+16}$	1	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	$Bell_{4}^{71}(8) BABAB^{72}(np)$
				$Y(4260) \to \pi^-(\pi^+ J/\psi)$	BES III ⁴⁰ (8), Belle ⁴¹ (5.2)	$Z(4300)^+$	4504 ± 11 4478 ± 17	180 ± 31	1+-	$\bar{R}^0 \rightarrow K^-(\pi^+ \psi(2S))$	$Belle^{73},74 (6.4) BABAP^{75} (2.4)$
					CLEO data ⁴²¹ (>5)	2(4400)	4470 ± 11	100 ± 51	1	$D \rightarrow R (\pi^+ \psi(2D))$	$L H C \frac{76}{12.0}$
$Z_c(4020)^+$	4023.9 ± 2.4	10 ± 6	1+-	$Y(4260) \to \pi^-(\pi^+ h_c)$	BES III 43 (8.9)					$\bar{D}0 \rightarrow W^{-}(-\pm I/h)$	$D_{1100} = (15.9)$
				$Y(4260) \to \pi^- (D^* D^*)^+$	BES III ⁴⁴ (10)	V(4cno)	4004+9	00+41	1	$D^{\circ} \to K (\pi^+ J/\psi)$ + - $(\Lambda^+ \bar{\Lambda}^-)$	$\frac{\text{Dell}^{22}}{12}(4.0)$
Y(3915)	3918.4 ± 1.9	20 ± 5	0^{++}	$B \to K(\omega J/\psi)$	Belle ⁴⁵ (8), BABAR ^{33,46} (19)	Y(4030)	4034_{-11}	92_{-32}^{+}	1	$e^+e^- \rightarrow (\Lambda_c^+ \Lambda_c^-)$	Belle (8.2)
				$e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle ⁴⁷ (7.7), BABAR ⁴⁸ (7.6)	Y (4660)	4005 ± 10	53 ± 14	1	$e^+e^- \to (\pi^+\pi^-\psi(2S))$	Bellett (5.8), BABAH (5)
Z(3930)	3927.2 ± 2.6	24 ± 6	2++	$e^+e^- \rightarrow e^+e^-(DD)$	$\operatorname{Bell}_{\operatorname{d49}}(5.3), \operatorname{BABAR}_{\operatorname{D01}}(5.8)$	$Z_b(10610)^+$	10607.2 ± 2.0	18.4 ± 2.4	1+-	$\Upsilon(5S) \to \pi(\pi\Upsilon(nS))$	$\operatorname{Bell}_{\bullet}^{(\circ_1(\circ_1))}(>10)$
X(3940)	3942^{+9}_{-8}	37^{+21}_{-17}	?:+	$e^+e^- \rightarrow J/\psi \ (DD^*)$	$\operatorname{Bell}_{6}^{51,52}(6)$					$\Upsilon(5S) \to \pi^-(\pi^+ h_b(nP))$	$\text{Belle}^{78}(16)$
Y(4008)	3891 ± 42	255 ± 42	1	$e^+e^- \rightarrow (\pi^+\pi^- J/\psi)$	Bell(41,53)(7.4)					$\Upsilon(5S) \to \pi^- (B\bar{B}^*)^+$	$\text{Bell}_{(8)}^{(8)}$
$Z(4050)^+$	4051^{+24}_{-43}	82^{+51}_{-55}	?(+	$B^0 \to K^-(\pi^+\chi_{c1})$	$Belle^{54}(5.0), BABAR^{55}(1.1)$	$Z_b(10650)^+$	10652.2 ± 1.5	11.5 ± 2.2	1+-	$\Upsilon(5S) \to \pi^-(\pi^+\Upsilon(nS))$	$\operatorname{Belle}^{\overline{78}}(>10)$
Y(4140)	4145.6 ± 3.6	14.3 ± 5.9	?(+	$B^+ \to K^+(\phi J/\psi)$	$CDF^{50}[57](5.0), Belle^{58}(1.9),$					$\Upsilon(5S) \to \pi^-(\pi^+ h_b(nP))$	$Belle^{\overline{78}}(16)$
					LHCH ^{59} (1.4), CMS ^{60} (>5)					$\Upsilon(5S) \to \pi^- (B^* \bar{B}^*)^+$	Belle80(6.8)
	1.00	119	-91	1	$\mathbb{D} \mathscr{O}^{61}(3.1)$						
X(4160)	4156^{+29}_{-25}	139^{+113}_{-65}	?:+	$e^+e^- \rightarrow J/\psi \ (D^*D^*)$	$Belle_{52}(5.5)$						

 $\text{Belle}^{62}(7.2)$

Esposito, AP, Polosa, Phys.Rept. 668 Guerrieri, AP, Piccinini, Polosa, IJMPA 30, 1530002

 1^{+-}

 $\bar{B}^0 \to K^-(\pi^+ J/\psi)$

 370^{+99}_{-110}

 4196^{+35}_{-30}

 $Z(4200)^+$

Tuning of MC

Monte Carlo simulations A. Esposito

• We compare the $D^0 D^{*-}$ pairs produced as a function of relative azimuthal angle with the results from CDF:



Such distributions of charm mesons are available at Tevatron No distribution has been published (yet) at LHC

Prompt production of *X*(3872)

X(3872) is the Queen of exotic resonances, the most popular interpretation is a $D^0 \overline{D}^{0*}$ molecule (bound state, pole in the 1st Riemann sheet?)

We aim to evaluate prompt production cross section at hadron colliders via Monte-Carlo simulations

Q. What is a molecule in MC? A. «Coalescence» model



This should provide an upper bound for the cross section

Bignamini, Piccinini, Polosa, Sabelli PRL103 (2009) 162001 Kadastic, Raidan, Strumia PLB683 (2010) 248 64

Estimating *k*_{max}

The binding energy is $E_B \approx -0.16 \pm 0.31$ MeV: very small! In a simple square well model this corresponds to:

 $\sqrt{\langle k^2 \rangle} \approx 50 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 10 \text{ fm}$

binding energy reported in Kamal Seth's talk is $E_B \approx -0.013 \pm 0.192$ MeV: $\sqrt{\langle k^2 \rangle} \approx 30$ MeV, $\sqrt{\langle r^2 \rangle} \approx 30$ fm

to compare with deuteron: $E_B = -2.2 \text{ MeV}$

$$\sqrt{\langle k^2 \rangle} \approx 80 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 4 \text{ fm}$$

We assume $k_{max} \sim \sqrt{\langle k^2 \rangle} \approx 50$ MeV, some other choices are commented later

2009 results



We tune our MC to reproduce CDF distribution of $\frac{d\sigma}{d\Delta\phi}(p\bar{p} \rightarrow D^0 D^{*-})$ We get $\sigma(p\bar{p} \rightarrow DD^*|k < k_{max}) \approx 0.1$ nb $@\sqrt{s} = 1.96$ TeV Experimentally $\sigma(p\bar{p} \rightarrow X(3872)) \approx 30 - 70$ nb!!!

Estimating *k*_{max}

A solution can be FSI (rescattering of DD^*), which allow k_{max} to be as large as $5m_{\pi} \sim 700$ MeV $\sigma(p\bar{p} \rightarrow DD^*|k < k_{max}) \approx 230$ nb Artoisenet and Braaten, PRD81, 114018

However, the applicability of Watson theorem is challenged by the presence of pions that interfere with DD^* propagation Bignamini, Grinstein, Piccinini, Polosa, Riquer, Sabelli, PLB684, 228-230

> FSI saturate unitarity bound? Influence of pions small? Artoisenet and Braaten, PRD83, 014019

Guo, Meissner, Wang, Yang, JHEP 1405, 138; EPJC74 9, 3063; CTP 61 354 use $E_{max} = M_X + \Gamma_X$ for above-threshold unstable states

With different choices, 2 orders of magnitude uncertainty, limits on predictive power

A new mechanism?

In a more billiard-like point of view, the comoving pions can elastically interact with $D(D^*)$, and slow down the pairs DD^*



Esposito, Piccinini, AP, Polosa, JMP 4, 1569 Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

The mechanism also implies: *D* mesons actually "pushed" inside the potential well (the classical 3-body problem!)

X(3872) is a real, negative energy bound state (stable) It also explains a small width $\Gamma_X \sim \Gamma_{D^*} \sim 100 \text{ keV}$



By comparing hadronization times of heavy and light mesons, we estimate up to ~ 3 collisions can occur before the heavy pair to fly apart

We get $\sigma(p\bar{p} \rightarrow X(3872)) \sim 5 \text{ nb}$, still not sufficient to explain all the experimental cross section

