

# TMD measurements with jets

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1st EIC Yellow Report Workshop

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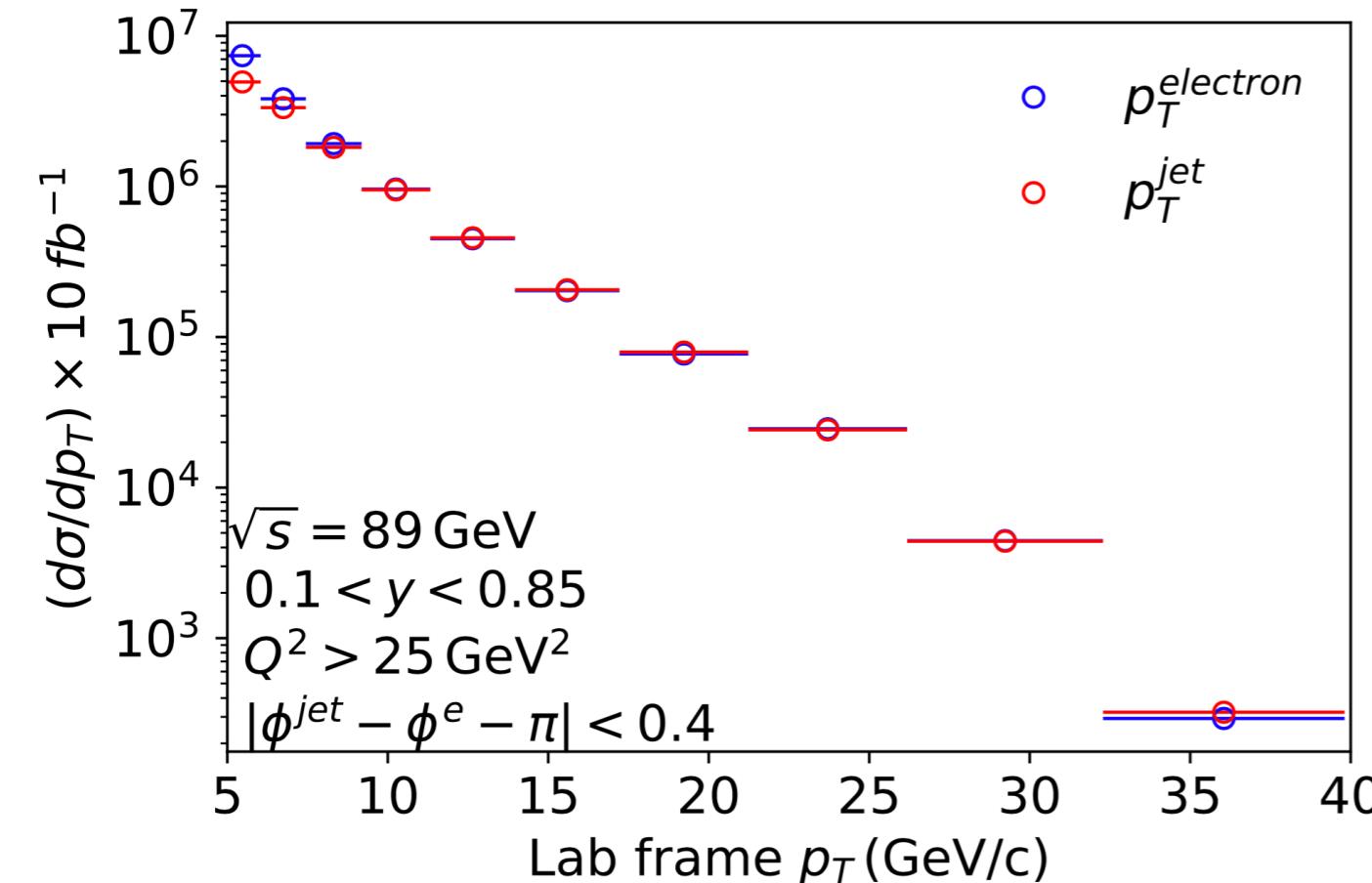
Berkeley  
UNIVERSITY OF CALIFORNIA



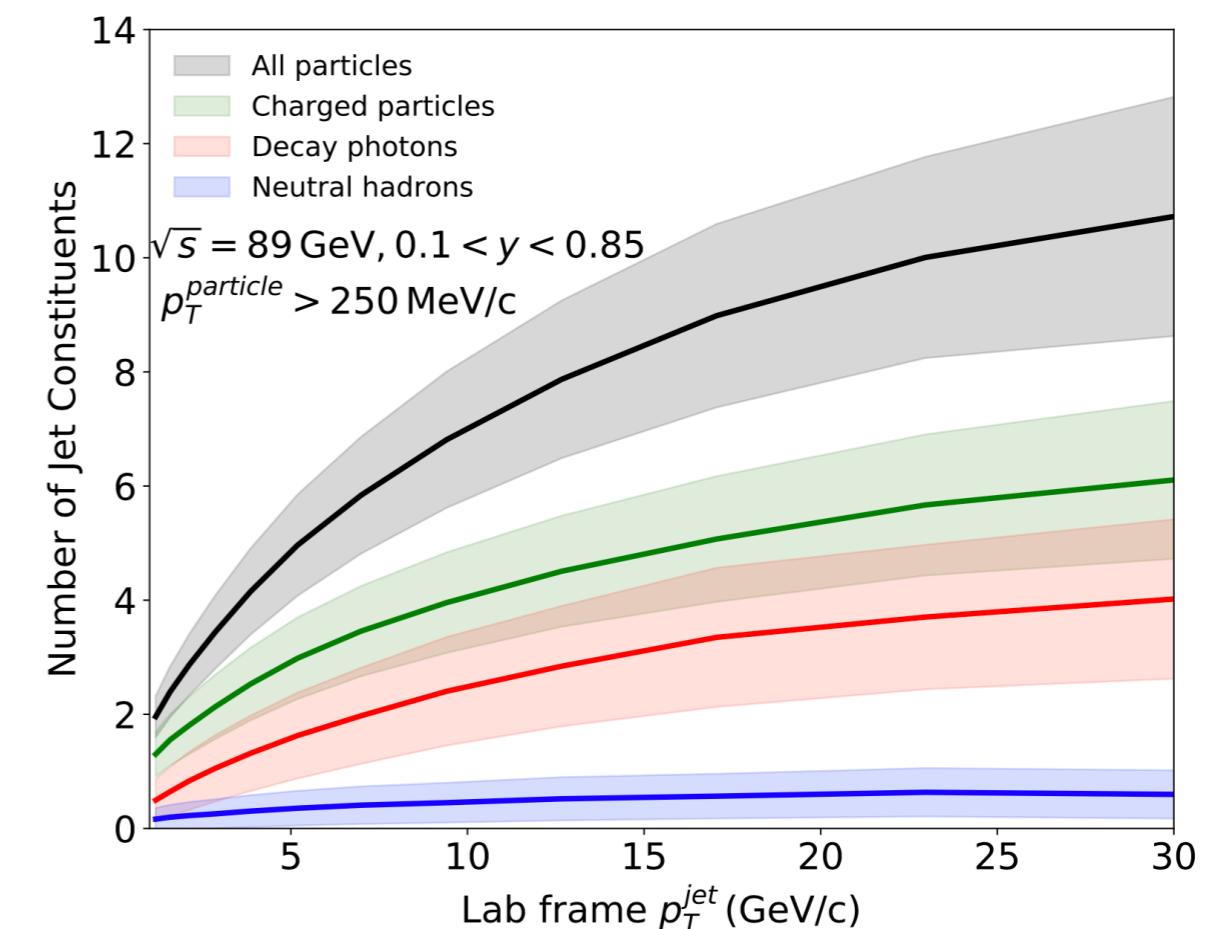
# Jets at the Electron-Ion Collider

Arratia, Jacak, FR, Song '19  
see also: Aschenauer, Chu, Page '19

Jet transverse momentum  $p_T$



Number of particles in the jet



Jet radius  $R = 1.0$

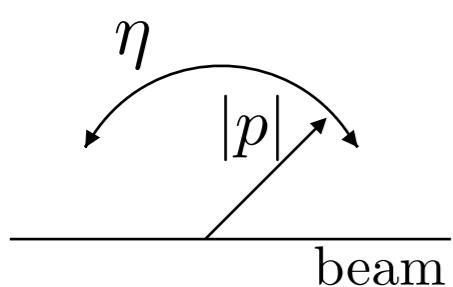
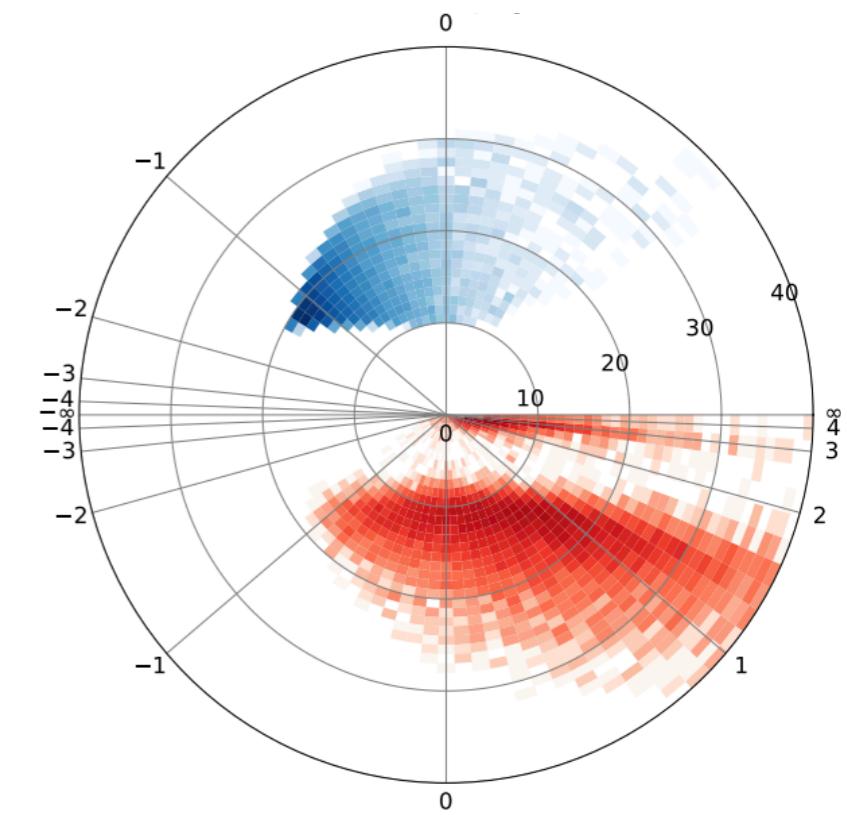
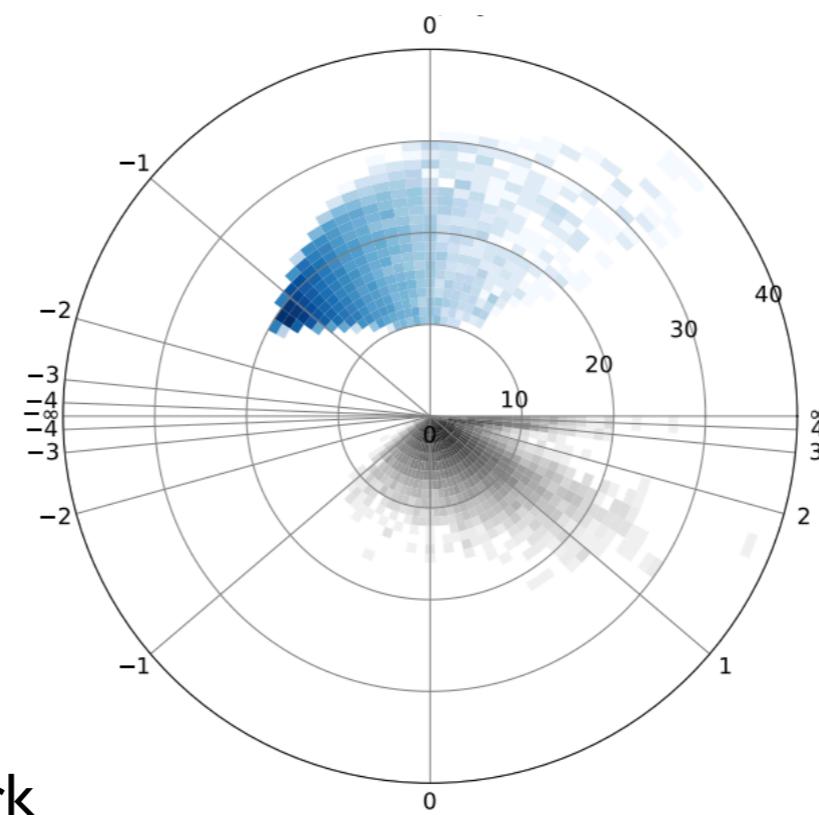
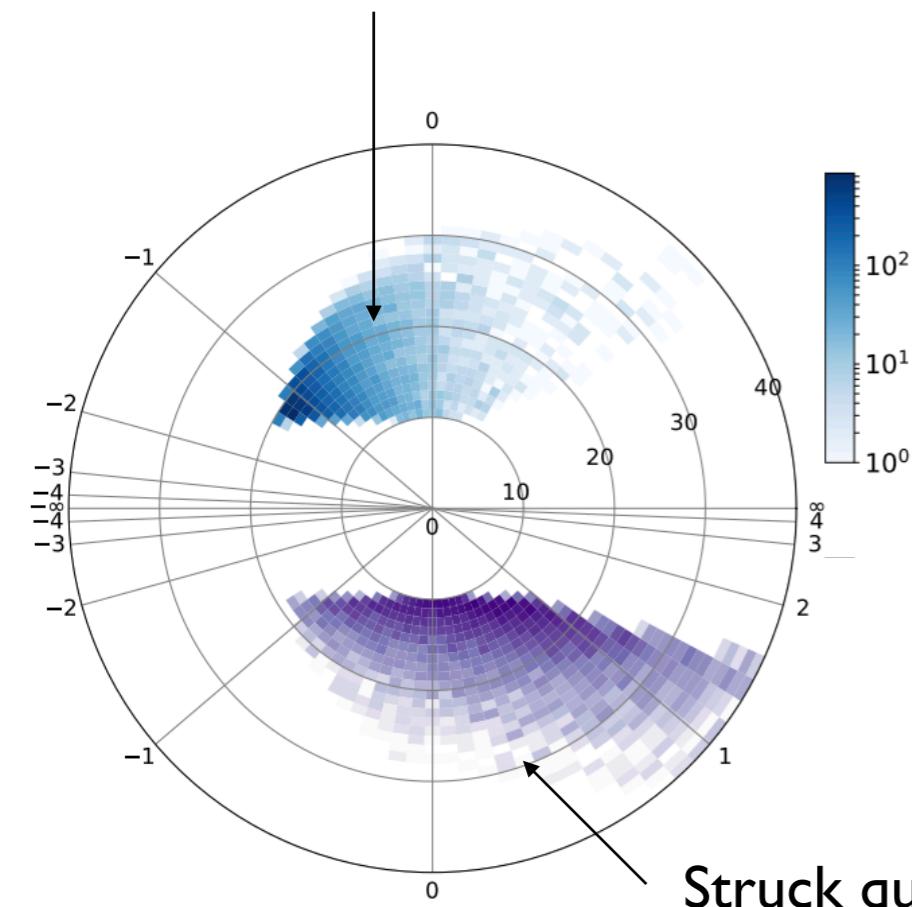
Deep Inelastic Scattering

# Hadrons and jets at the EIC

$Q^2 > 100 \text{ GeV}^2$ ,  $\sqrt{s} = 89 \text{ GeV}$

$10 < p_T^e < 30 \text{ GeV}$ ,  $0.1 < y < 0.85$

Scattered electron



Arratia, Jacak, FR, Song '19



- Initial and final state shower
- Hadronization

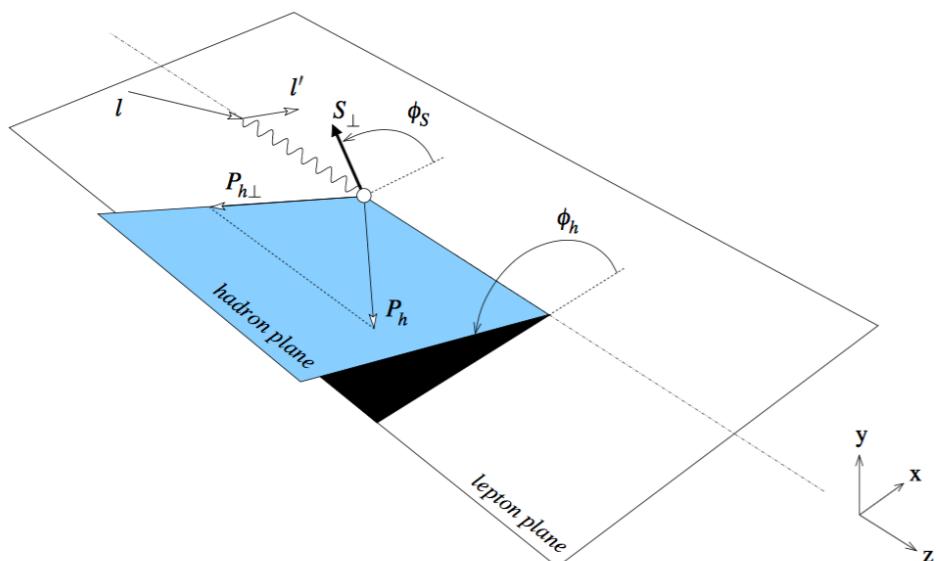


- Initial and final state shower
- Hadronization
- Jet reconstruction
- Lab frame, anti- $k_T$

# Measurement of TMDs at the EIC

e.g. Bacchetta, Diehl, Goeke, Metz, Mulders '07

- Semi-Inclusive Deep-Inelastic Scattering
- Measure hadrons with low transverse momentum



$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xy Q^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} \right. \\ \left. + \dots \right.$$

→ Sensitivity to (polarized) TMD PDFs and FFs

- Complementary processes using jets — universality?
- Study TMD evolution
- Clean environment at the EIC

# Outline

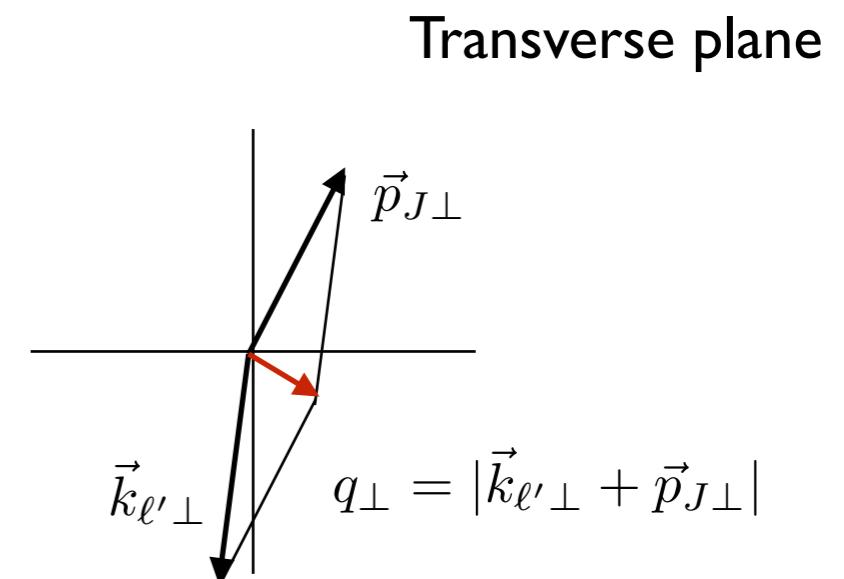
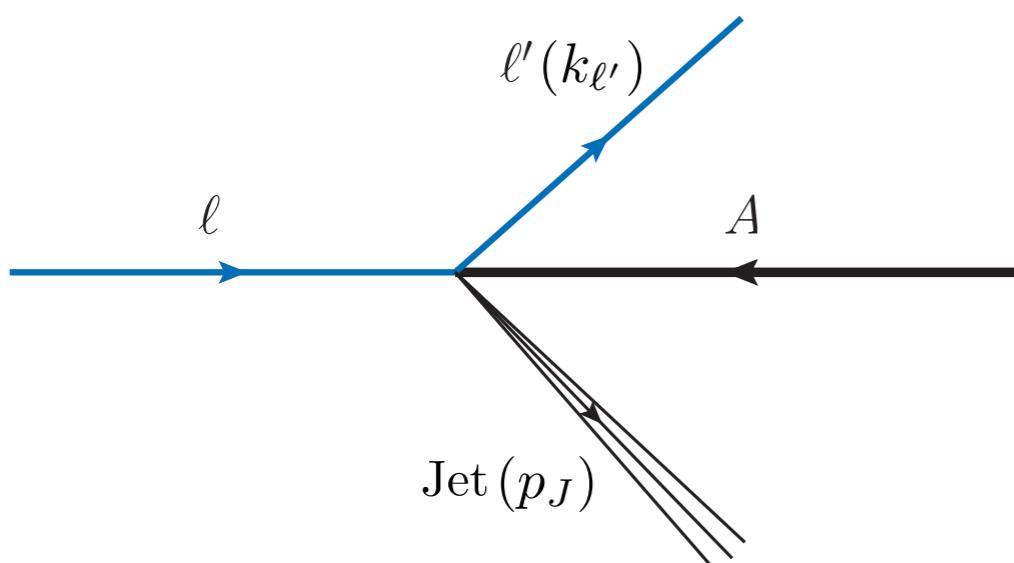
- Introduction
- Jet correlations
- Jet substructure
- Conclusions and outlook

# Electron-jet correlations

Liu, FR, Vogelsang, Yuan '18

- Require high  $p_T$  jet
- Measure imbalance  $q_\perp$  between lepton and jet in the lab frame

$$\frac{d\sigma}{d\eta_{\ell'} d^2 k_{\perp \ell'} d^2 q_\perp}$$



- Close analogy to proton-proton collisions at RHIC
- No TMD fragmentation
- Test of universality

Boer, Vogelsang '04

Vogelsang, Yuan '05

Bomhof, Mulders, Vogelsang, Yuan '07

# Electron-jet correlations

Liu, FR, Vogelsang, Yuan '18

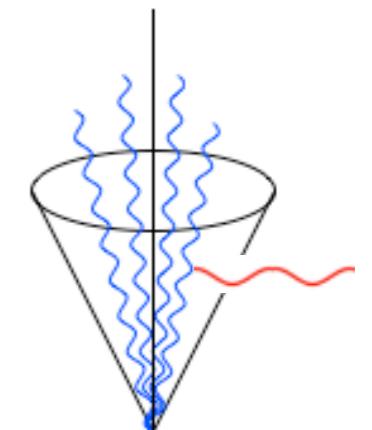
- Factorization

$$\frac{d\sigma}{d\eta_{\ell'} d^2 k_{\perp \ell'} d^2 q_{\perp}} = \sigma_0 \int \frac{d^2 b_{\perp}}{(2\pi)^2} e^{iq_{\perp} \cdot b_{\perp}} x f_q(x, b_{\perp}, \zeta_c, \mu_F) S_J(b_{\perp}, \mu_F) H_{\text{TMD}}(Q, \mu_F)$$

Large radius advantageous  $R \sim 1$

- Non-global logarithms

$$S_{\text{NGL}}^{(2)}(b_{\perp}) = -C_F \frac{C_A}{2} \left(\frac{\alpha_s}{\pi}\right)^2 \frac{\pi^2}{24} \ln^2 \left(\frac{k_{\ell \perp}^2 b_{\perp}^2}{c_0^2}\right)$$

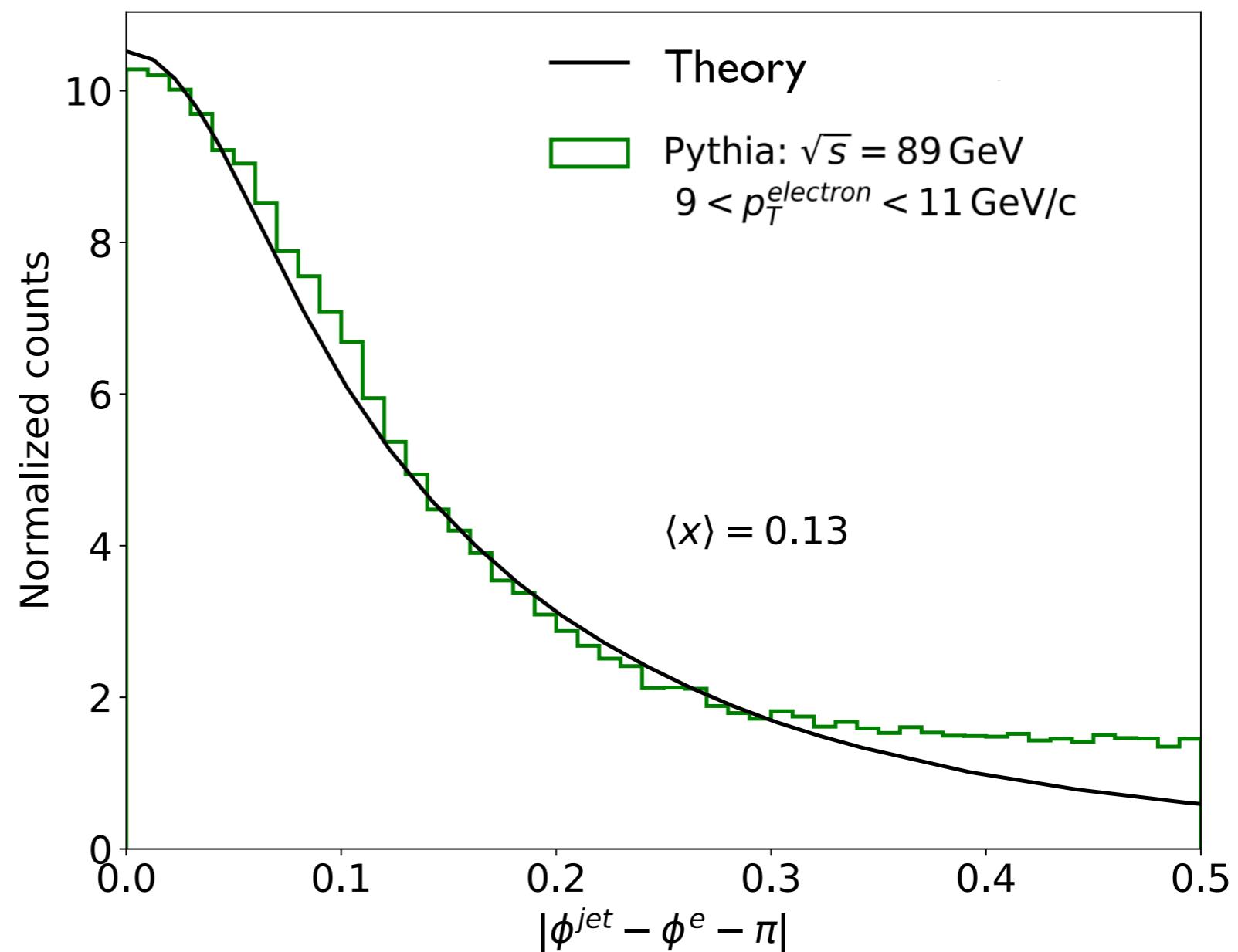
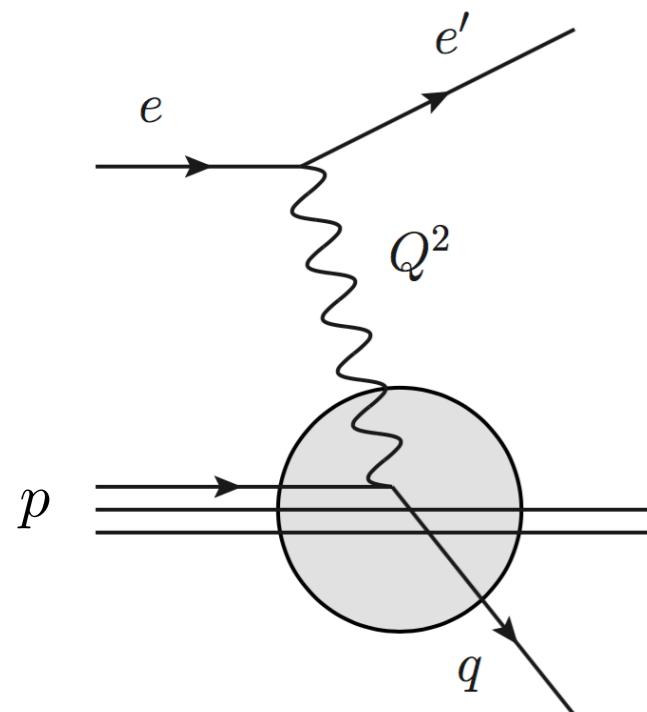


Contributes at NLL, included at leading color, at most a 5% effect

Dasgupta, Salam '01

# Results for the EIC

Liu, FR, Vogelsang, Yuan '18  
 Arratia, Jacak, FR, Song '19



Comparison to Pythia 8  
 HERA, EIC

Studies using Pythia 6 see: Aschenauer, Lee, Page, FR '19  
 See Brian Page's talk

# Direct measurement of the Sivers effect

Liu, FR, Vogelsang, Yuan '18

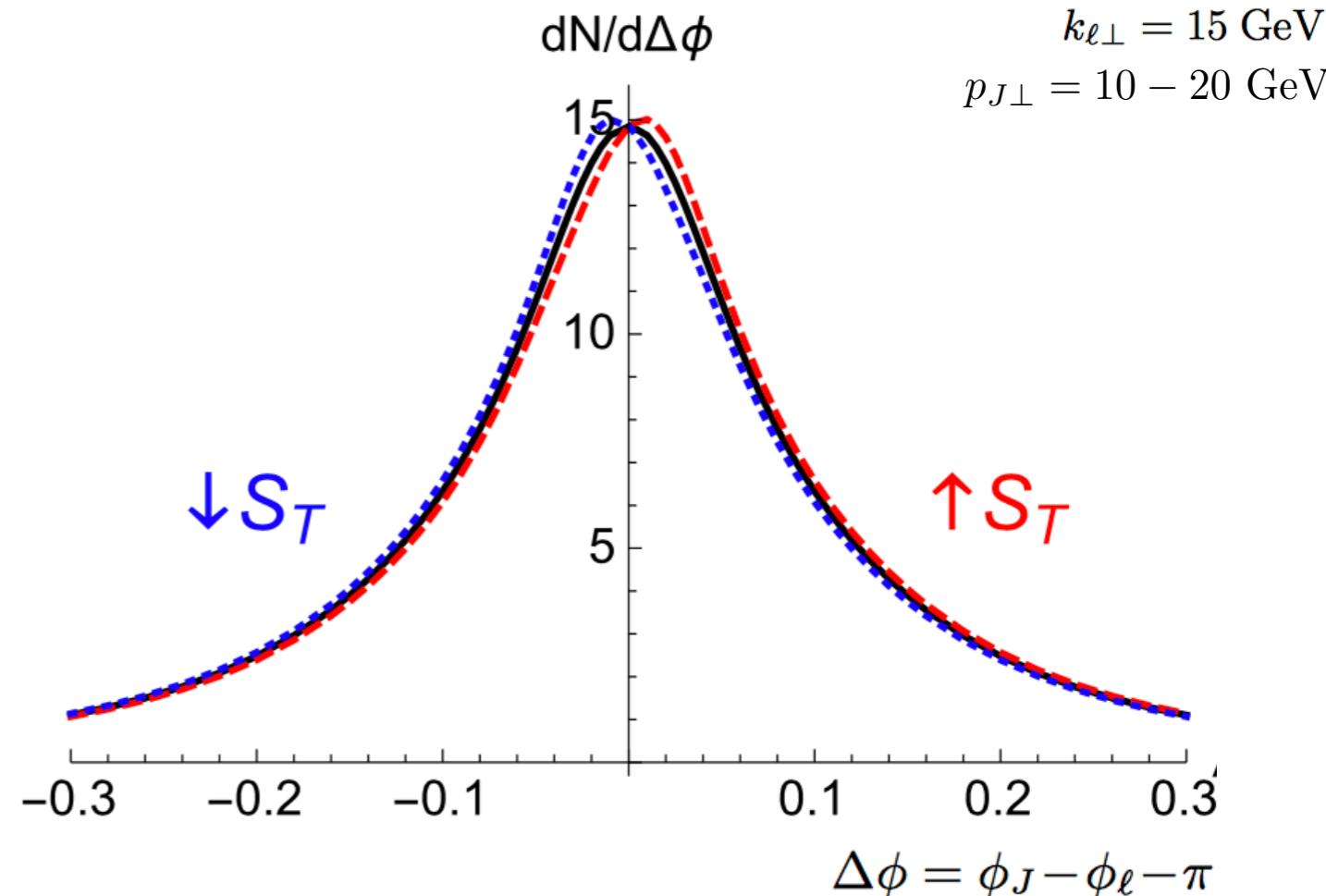
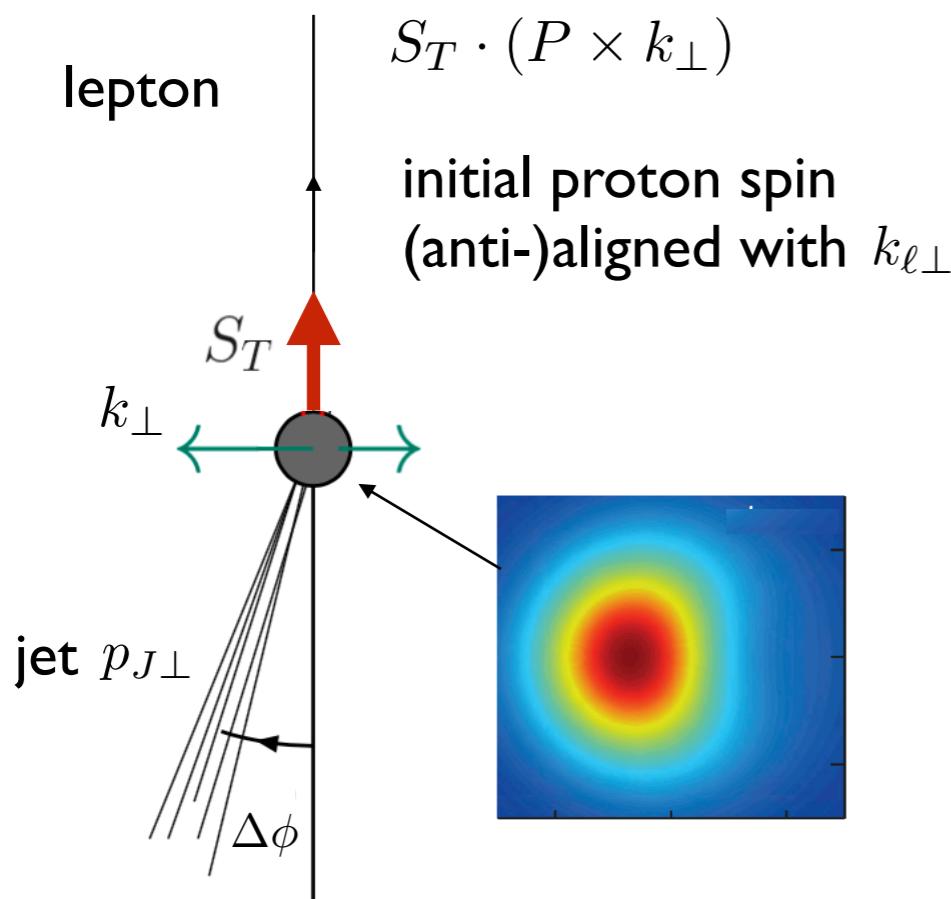
- $H(Q^2, R) f_q(q_\perp) \otimes_\perp S_q(q_\perp, R)$

$$y_\ell = y_J = 1$$

$$\sqrt{S_{ep}} = 80 \text{ GeV}$$

$$k_{\ell\perp} = 15 \text{ GeV}$$

$$p_{J\perp} = 10 - 20 \text{ GeV}$$



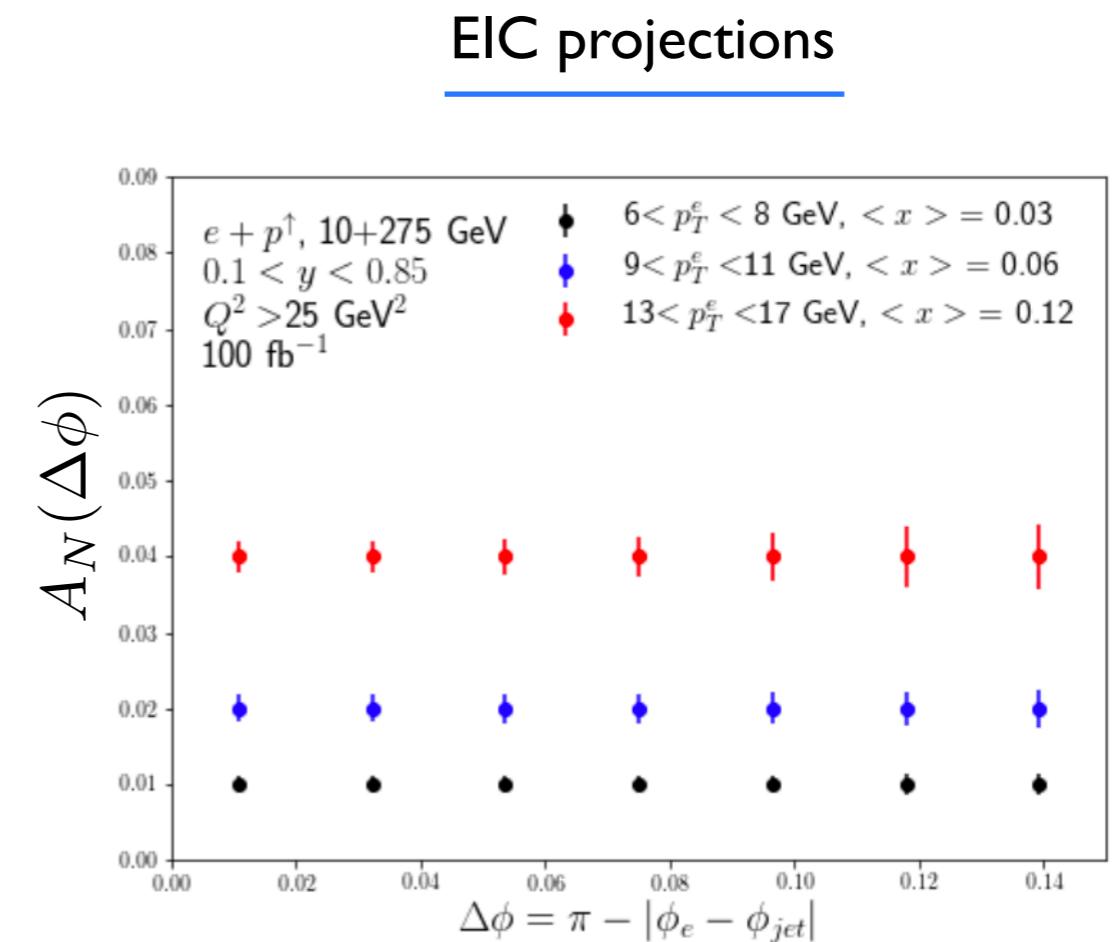
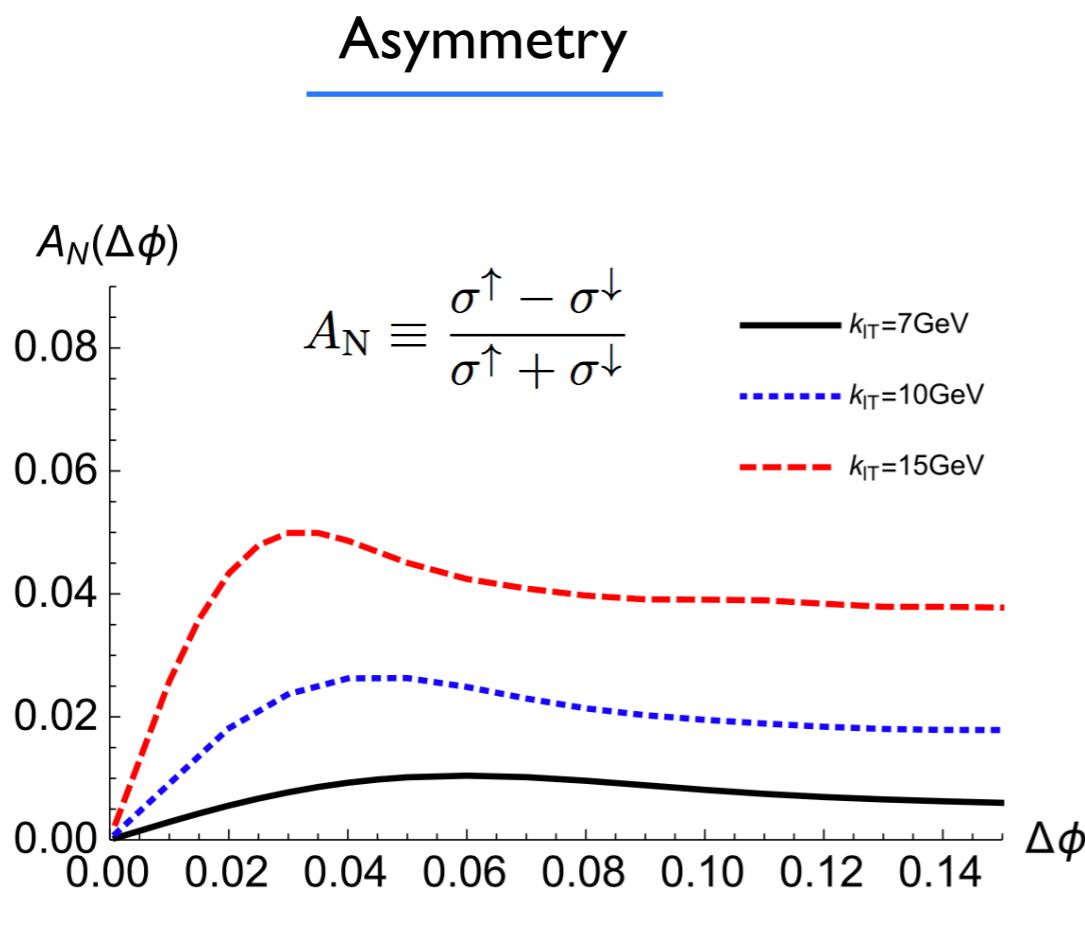
- Sensitivity to the Sivers TMD PDF extraction from Sun, Yuan '13
- Test of universality and factorization breaking effects, see RHIC measurements STAR, PRL 99 (2007) 142003

# Direct measurement of the Sivers effect

Liu, FR, Vogelsang, Yuan '18

- TMD factorization

$$H(Q^2, R) \ f_q(q_\perp) \otimes_\perp S_q(q_\perp, R)$$



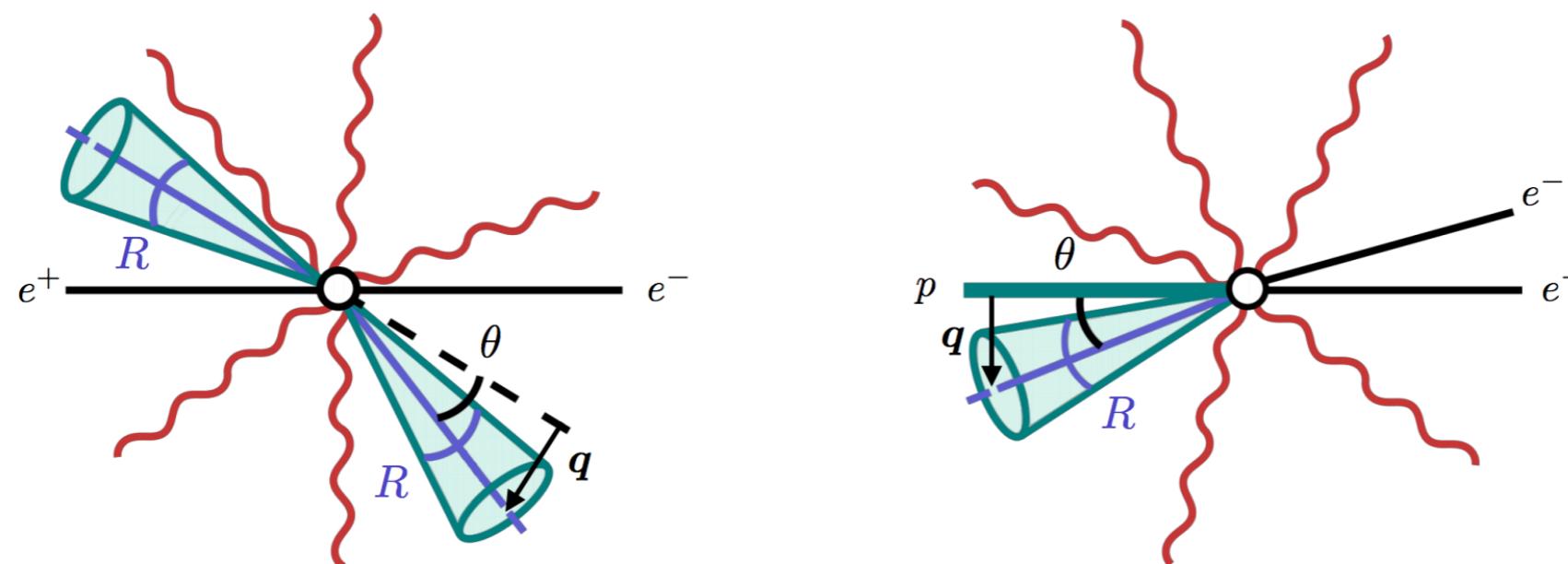
see Miguel Arratia's talk

- Sensitivity to the Sivers TMD PDF extraction from Sun, Yuan '13
- Test of universality and factorization breaking effects, see RHIC measurements STAR, PRL 99 (2007) 142003

# Proton-jet correlations

- Semi-Inclusive Deep Inelastic Scattering
- Breit frame
- Initial and final state TMD factorization

Gutierrez-Reyes, Scimemi, Waalewijn, Zoppi '18, '19  
 Gutierrez-Reyes, Makris, Vaidya, Scimemi, Zoppi '20



- Soft function with back-to-back Wilson lines
- TMD fragmentation function  $\longrightarrow$  perturbative TMD jet functions. Close connection to  $e^+e^-$
- Winner-take-all jets, different jet radii

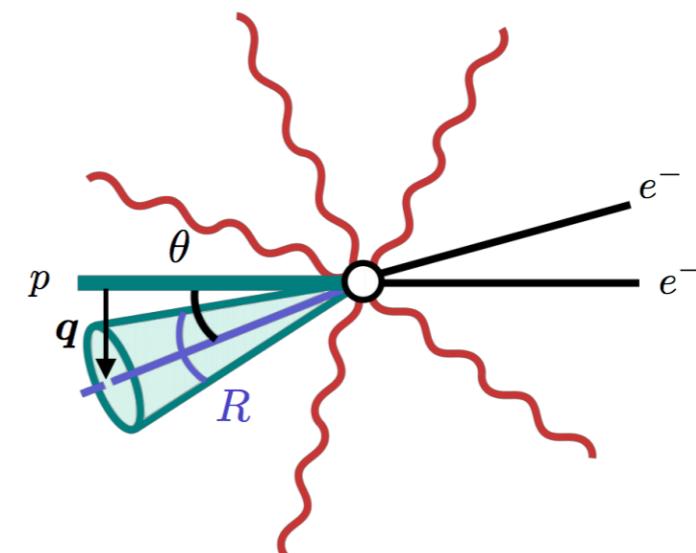
# Proton-jet correlations

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Gutierrez-Reyes, Scimemi, Waalewijn, Zoppi '18, '19  
 Gutierrez-Reyes, Makris, Vaidya, Scimemi, Zoppi '20

$$\frac{d\sigma_{ep \rightarrow eJX}}{dQ^2 dx dz dq} = \sum_q \sigma_{0,q}^{\text{DIS}}(x, Q^2) H_{\text{DIS}}(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b} \cdot \mathbf{q}} F_q(x, \mathbf{b}, \mu, \zeta) J_q\left(z, \mathbf{b}, \frac{QR}{2}, \mu, \zeta\right)$$

$$\mathbf{q} = \frac{\mathbf{P}_J}{z} + \mathbf{q}_{\text{in}} \quad z = 2E_J/Q$$

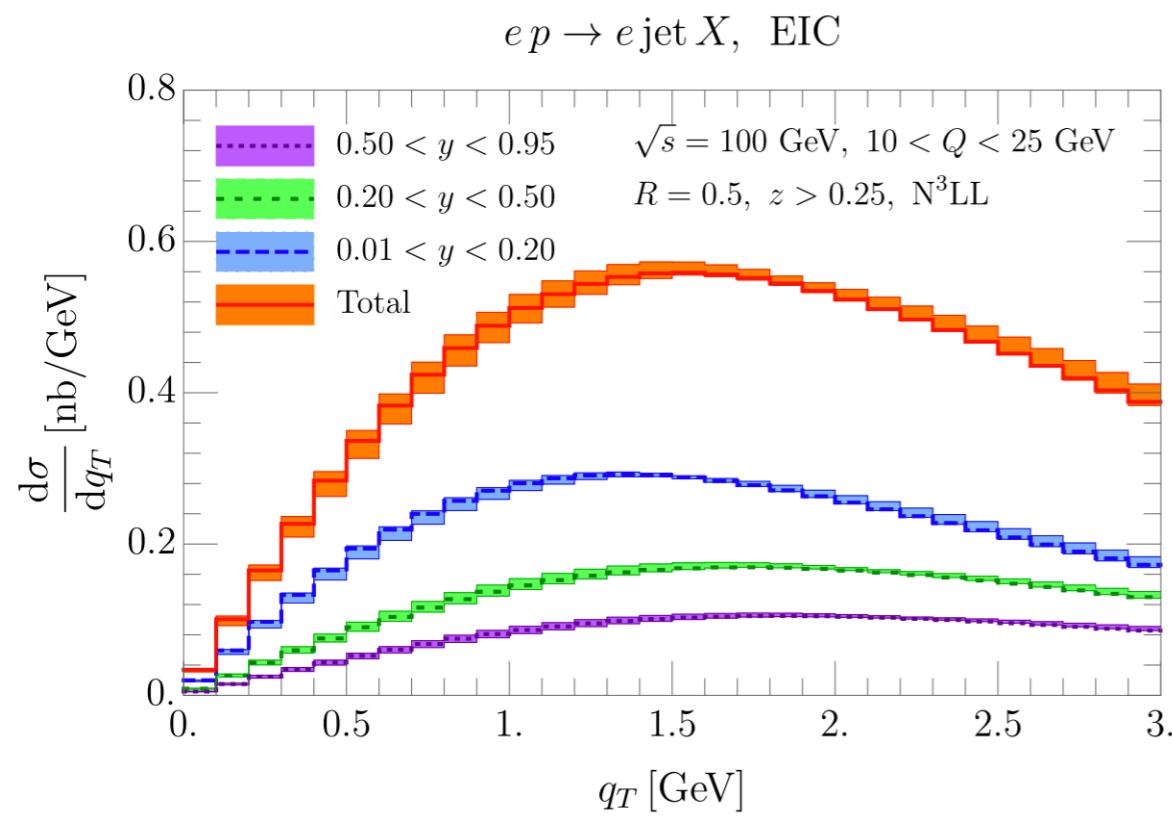


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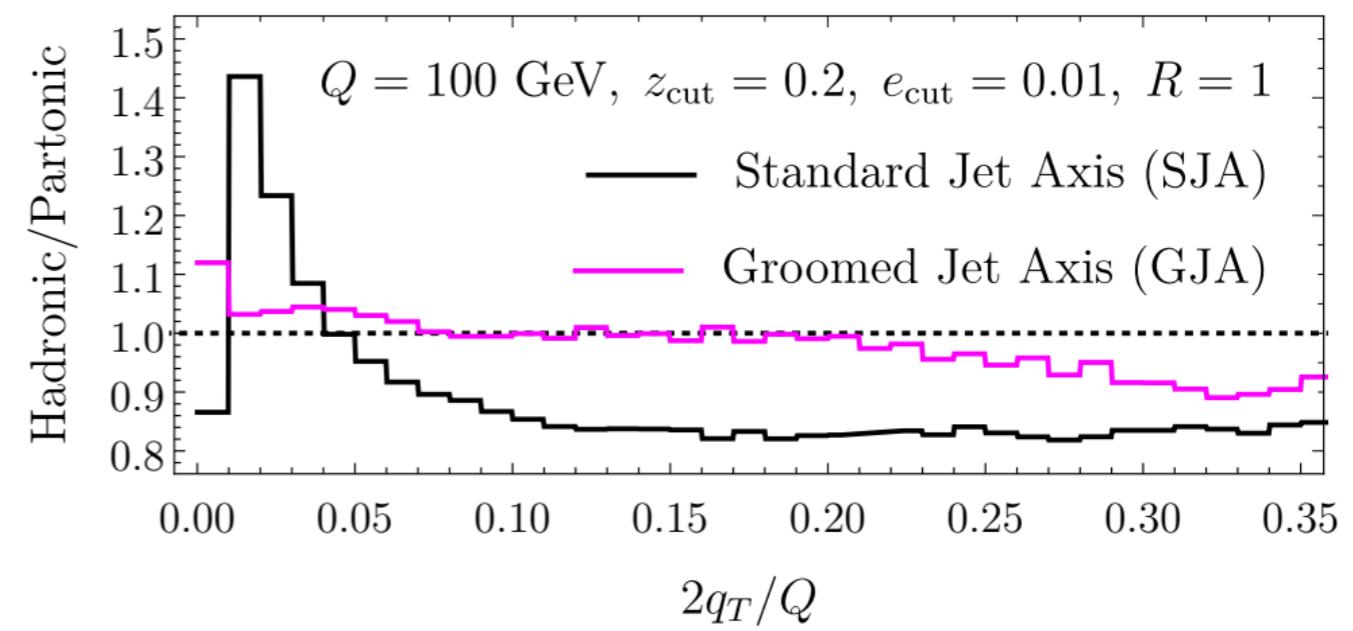
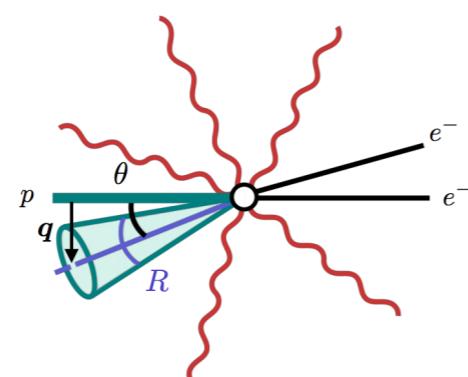
# Proton-jet correlations

- Semi-Inclusive Deep Inelastic Scattering
- Breit frame

Gutierrez-Reyes, Scimemi, Waalewijn, Zoppi '18, '19  
 Gutierrez-Reyes, Makris, Vaidya, Scimemi, Zoppi '20



WTA-axis



Soft drop groomed jet axis

- Reduction of hadronization effects
- Mitigate effect of non-global logarithms

# Outline

- Introduction
- Jet correlations
- Jet substructure
- Conclusions and outlook

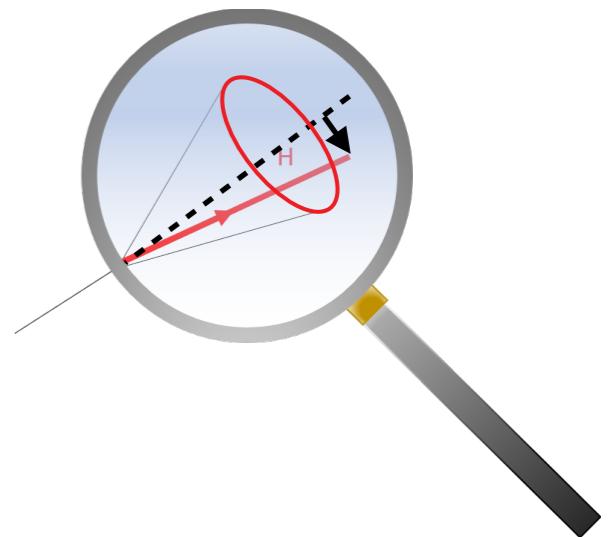
# TMD in-jet distributions

see also Yiannis Makris' talk

The hadron distribution inside jets  $p_T, \eta$

- Measure additional two variables:

- Longitudinal momentum fraction  $z_h = p_T^h/p_T$
- Relative transverse momentum wrt. to a predetermined axis  $\mathbf{j}_\perp$



$$F(z_h, \mathbf{j}_\perp; \eta, p_T, R) = \frac{d\sigma^{pp \rightarrow (\text{jet}+h)X}}{dp_T d\eta dz_h d^2 j_\perp} \Bigg/ \frac{d\sigma^{pp \rightarrow \text{jet } X}}{dp_T d\eta}$$

## I. Collinear factorization

$$\frac{d\sigma^{pp \rightarrow (\text{jet}+h)X}}{dp_T d\eta dz_h d^2 j_\perp} = \sum_{a,b,c} f_a(x_a, \mu) \otimes f_b(x_b, \mu) \otimes H_{ab}^c(x_a, x_b, \eta, p_T/z, \mu) \otimes \boxed{\mathcal{G}_c^h(z, z_h, \mathbf{j}_\perp, p_T R, \mu)} + \mathcal{O}(R^2)$$

## 2. Refactorization ...

- EIC — Switch out hard functions

# Different TMD in-jet distributions

- Overview: The choice of the jet axis

Standard jet axis

Bain, Makris, Mehen '16  
Kang, Liu, FR, Xing '17  
Kang, Lee, Terry, Xing '19

Recoil free axis  
e.g. Winner-take-all

Neill, Scimemi, Waalewijn '17  
Neill, Papaefstathiou, Waalewijn, Zoppi '18

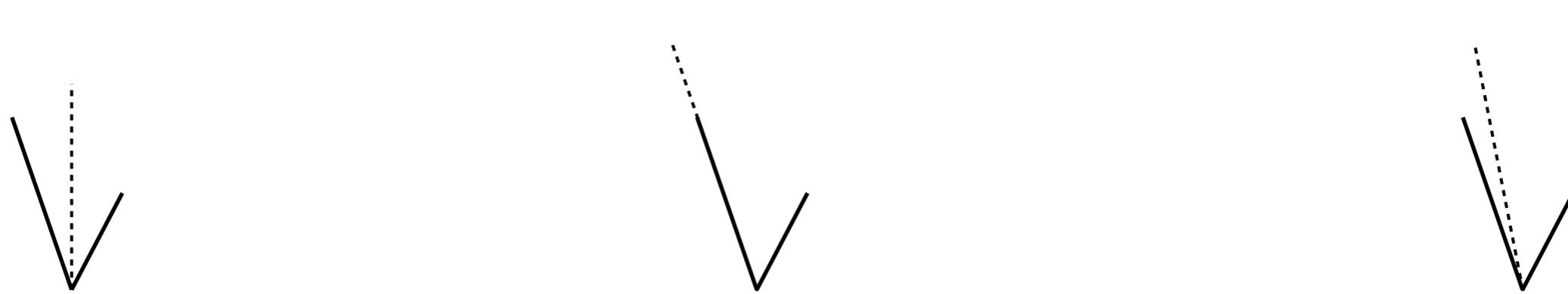
Groomed jet axis

Makris, Neill, Vaidya '17

TMD factorization

Collinear factorization

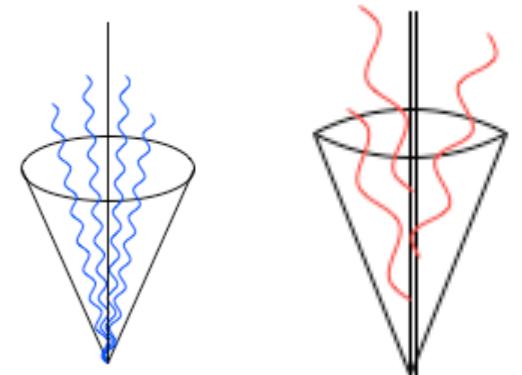
TMD factorization



# In-jet TMD distributions

Bain, Makris, Mehen '16  
Kang, Liu, FR, Xing '17

$$\begin{aligned} \mathcal{G}_c^h(z, z_h, p_T R, \mathbf{j}_\perp, \mu) &= \mathcal{H}_{c \rightarrow i}(z, p_T R, \mu) \int d^2 \mathbf{k}_\perp d^2 \boldsymbol{\lambda}_\perp \delta^2(z_h \boldsymbol{\lambda}_\perp + \mathbf{k}_\perp - \mathbf{j}_\perp) \\ &\times D_{h/i}(z_h, \mathbf{k}_\perp, \mu, \nu) S_i(\boldsymbol{\lambda}_\perp, \mu, \nu R) \end{aligned}$$



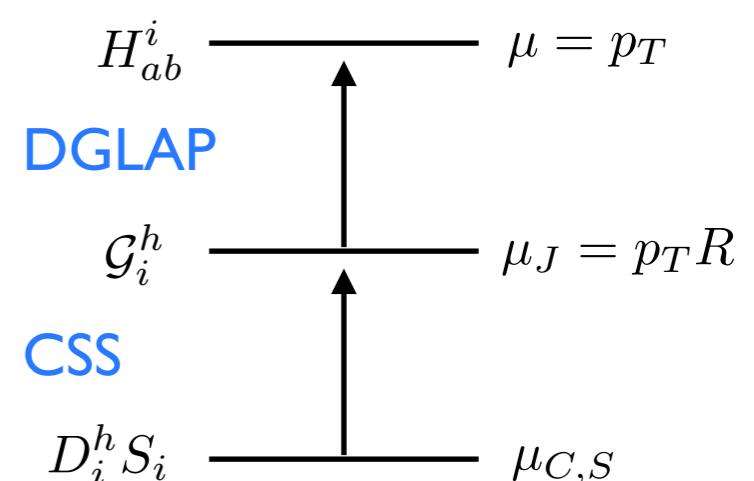
- TMD evaluated at the jet scale

$$\hat{D}_{h/i}(z_h, \mathbf{j}_\perp; \mu_J) = \frac{1}{z_h^2} \int \frac{b db}{2\pi} J_0(j_\perp b/z) C_{j \leftarrow i} \otimes D_{h/j}(z_h, \mu_{b_*}) e^{-S_{\text{pert}}^i(b_*, \mu_J) - S_{\text{NP}}^i(b, \mu_J)}$$

At NLL usual TMD Sudakov Collins, Soper, Sterman '85

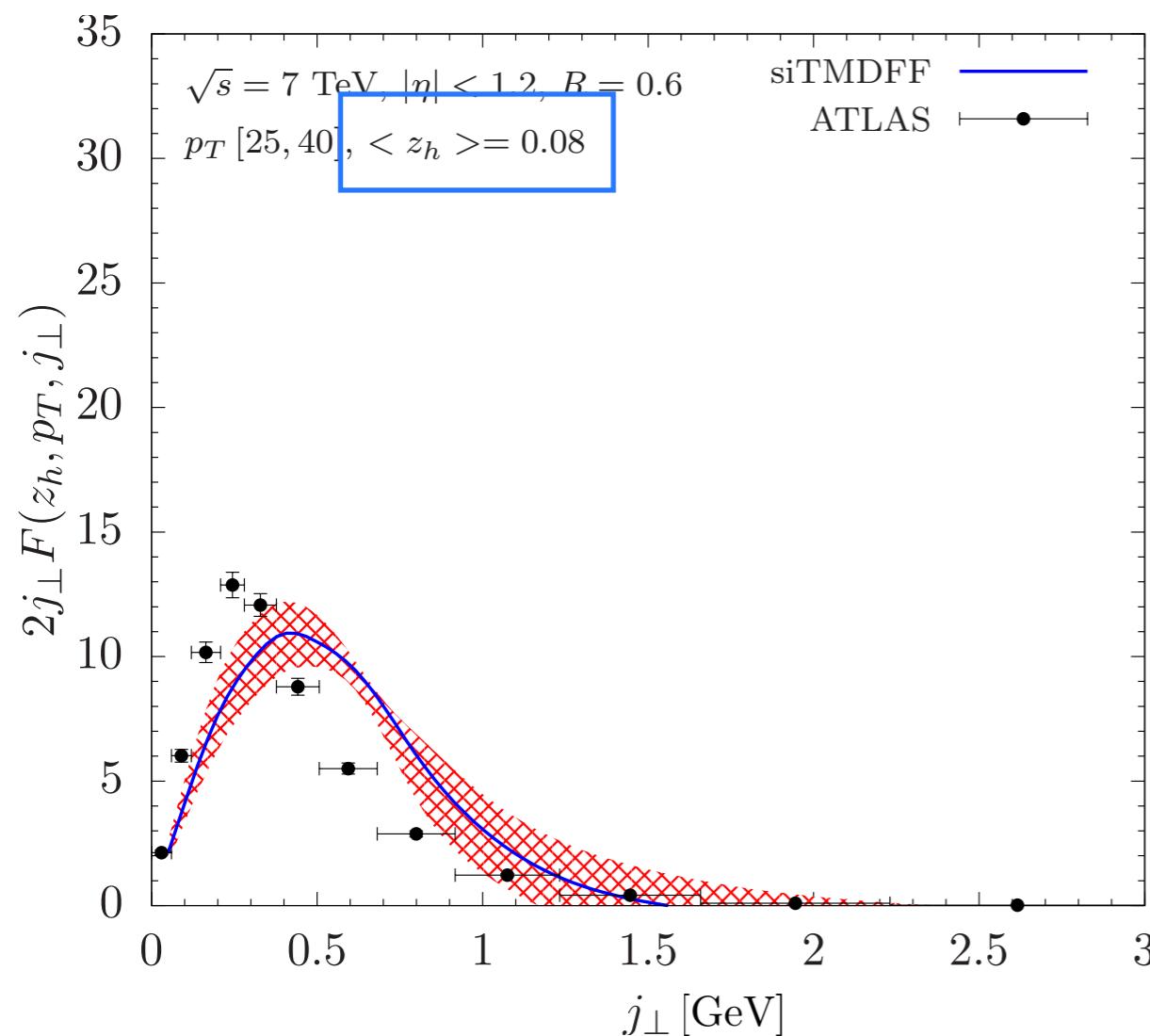
- Non-perturbative input from Sun, Isaacson, Yuan, Yuan '14

RG evolution



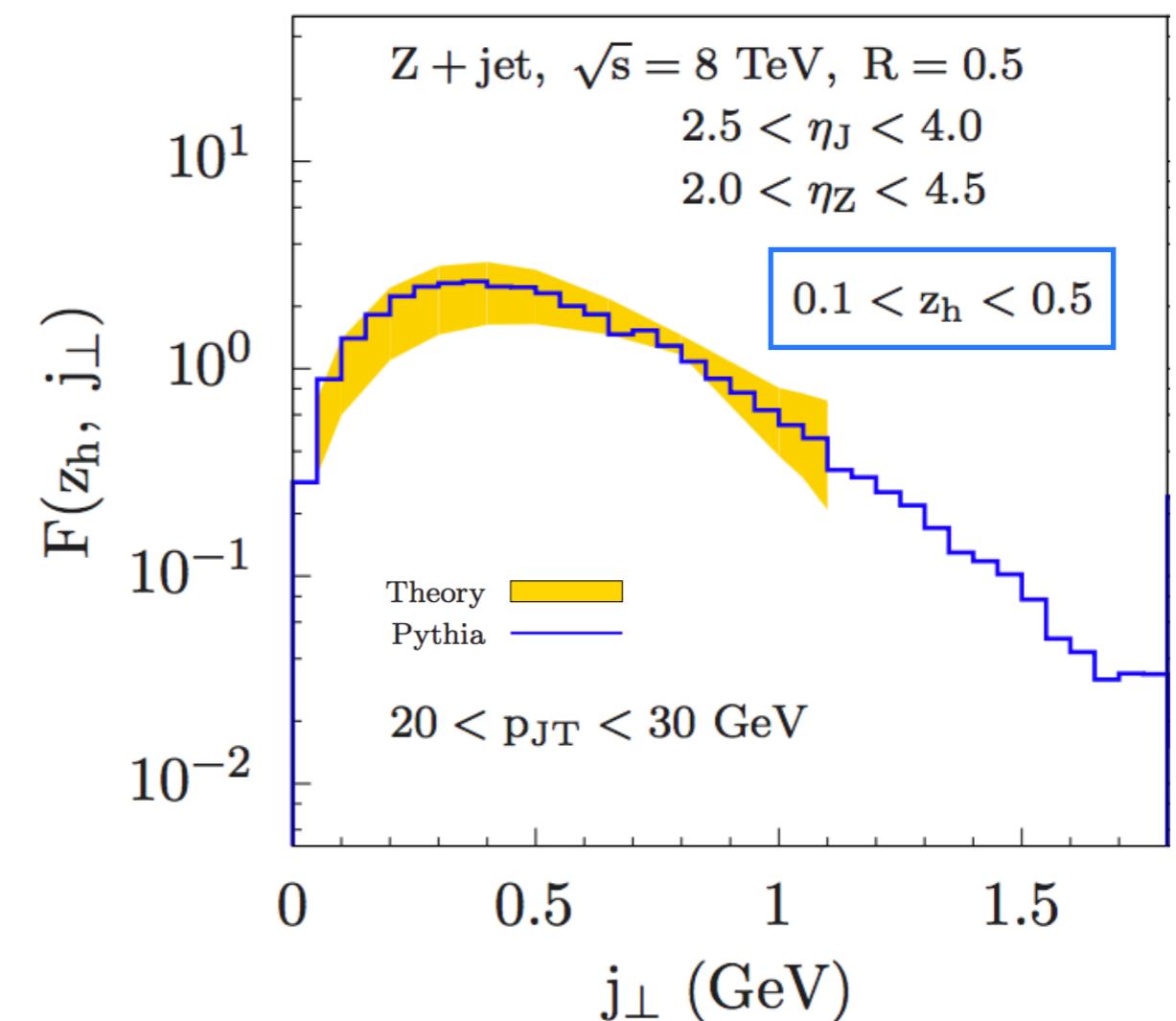
# The TMD hadron-in-jet distribution

Inclusive jets, comparison to ATLAS data



Kang, Liu, FR, Xing '17

Z tagged jets, comparison to Pythia



Kang, Lee, Terry, Xing '19

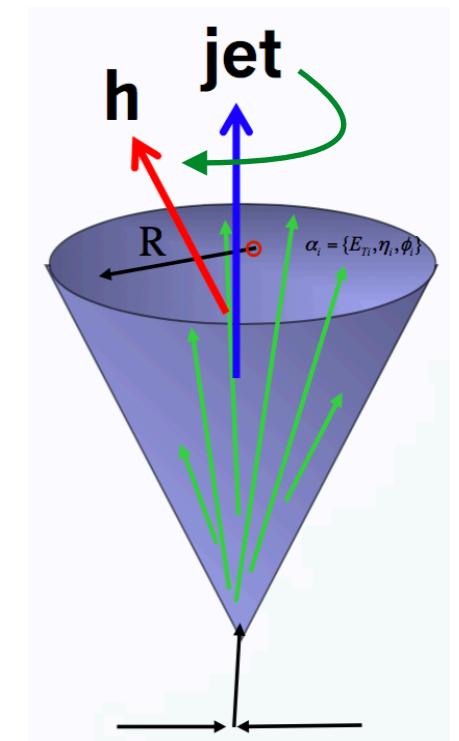
# Including spin effects

- Transversely polarized pp collisions

$$p^\uparrow(P_A, S_T, \phi_S) + p(P_B) \rightarrow \text{jet}(\eta, p_T) h(z_h, j_\perp, \phi_H) + X$$

$$\frac{d\sigma^{pp \rightarrow (\text{jet}+h)X}}{dp_T d\eta dz_h d^2 j_\perp} = F_{UU} + \sin(\phi_S - \phi_H) F_{UT}^{\sin(\phi_S - \phi_H)}$$

- Collinear transversity
- Collins TMDFF



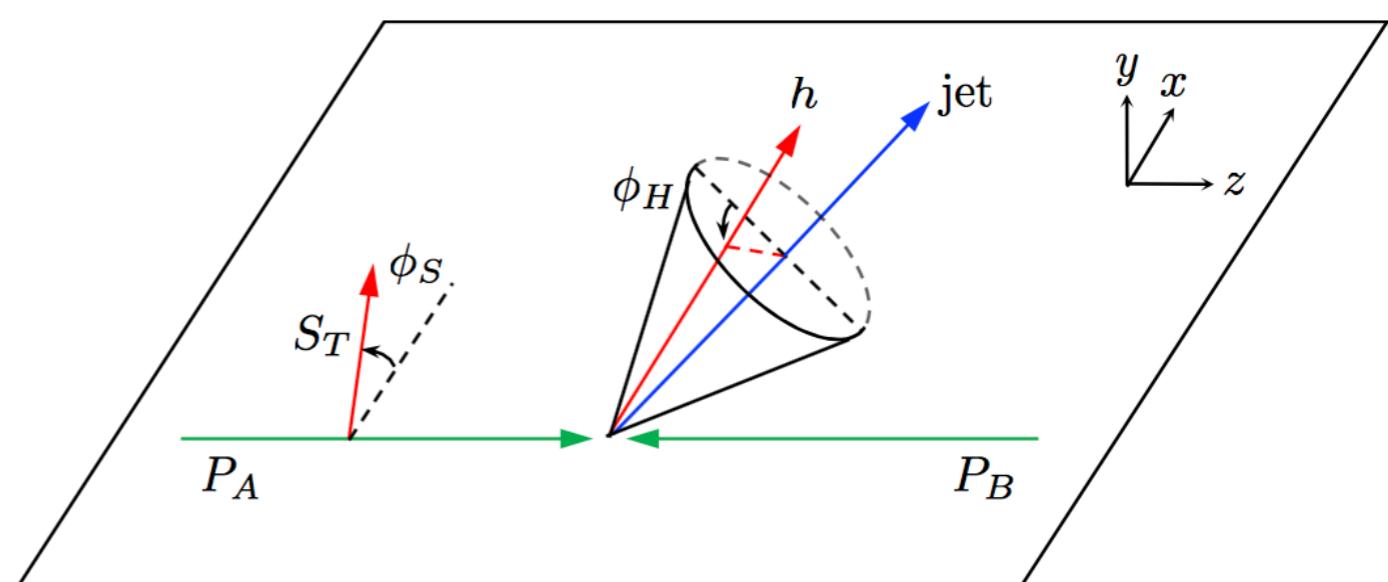
## Spin asymmetry

$$A_{UT}^{\sin(\phi_S - \phi_H)}(z_h, j_\perp; \eta, p_T) = \frac{F_{UT}^{\sin(\phi_S - \phi_H)}}{F_{UU}}$$

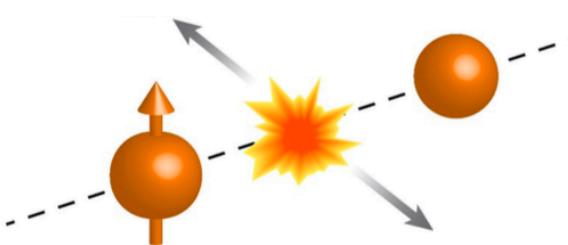
Yuan '08

Kang, Prokudin, FR, Yuan '17

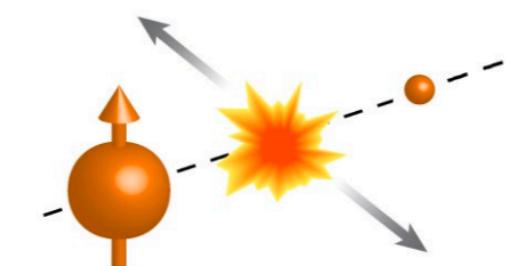
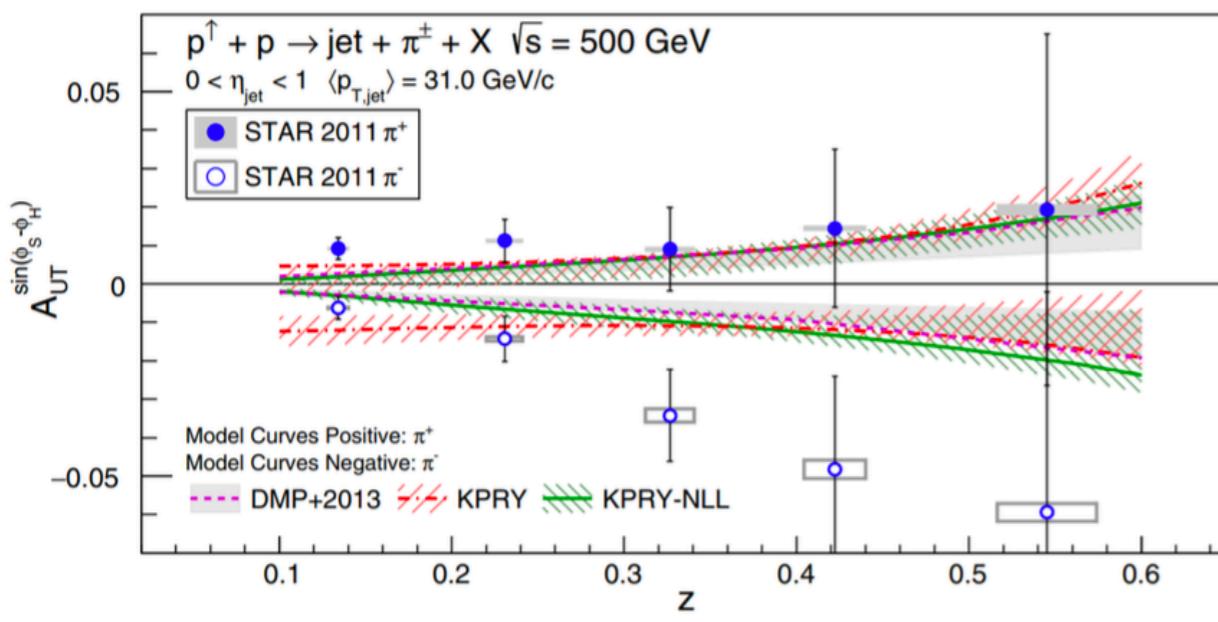
see also: D'Alesio, Murgia, Pisano '11, '17



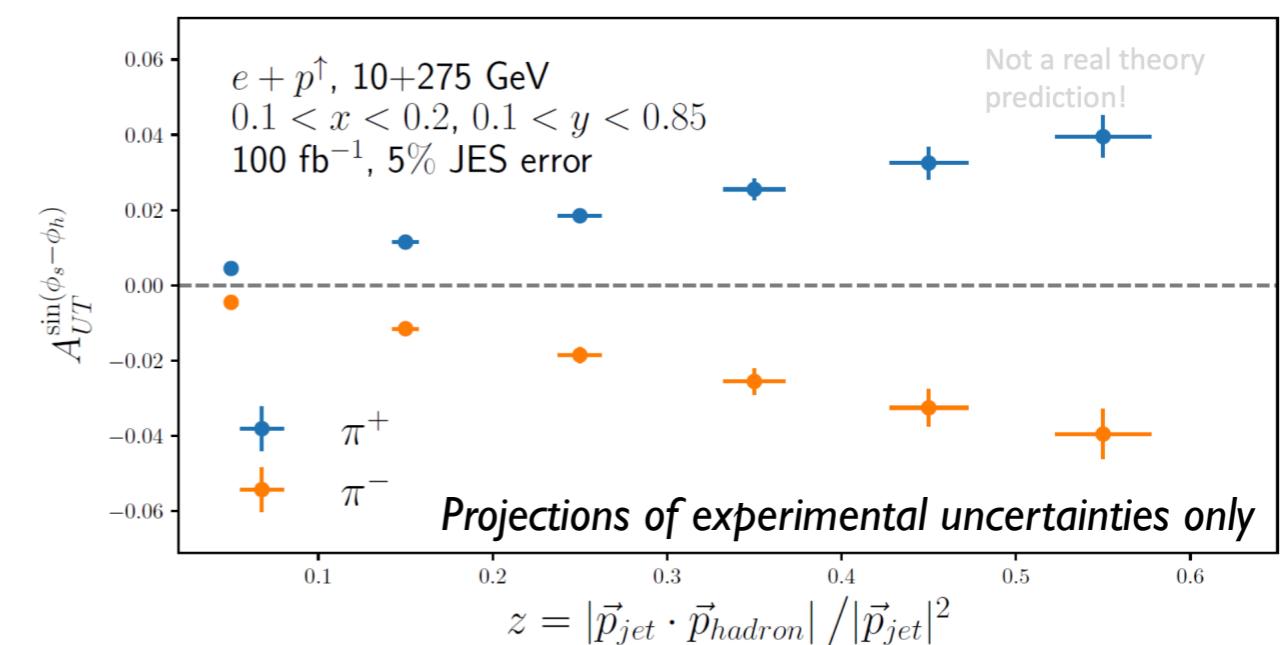
# Transversity and Collins fragmentation



RHIC



EIC

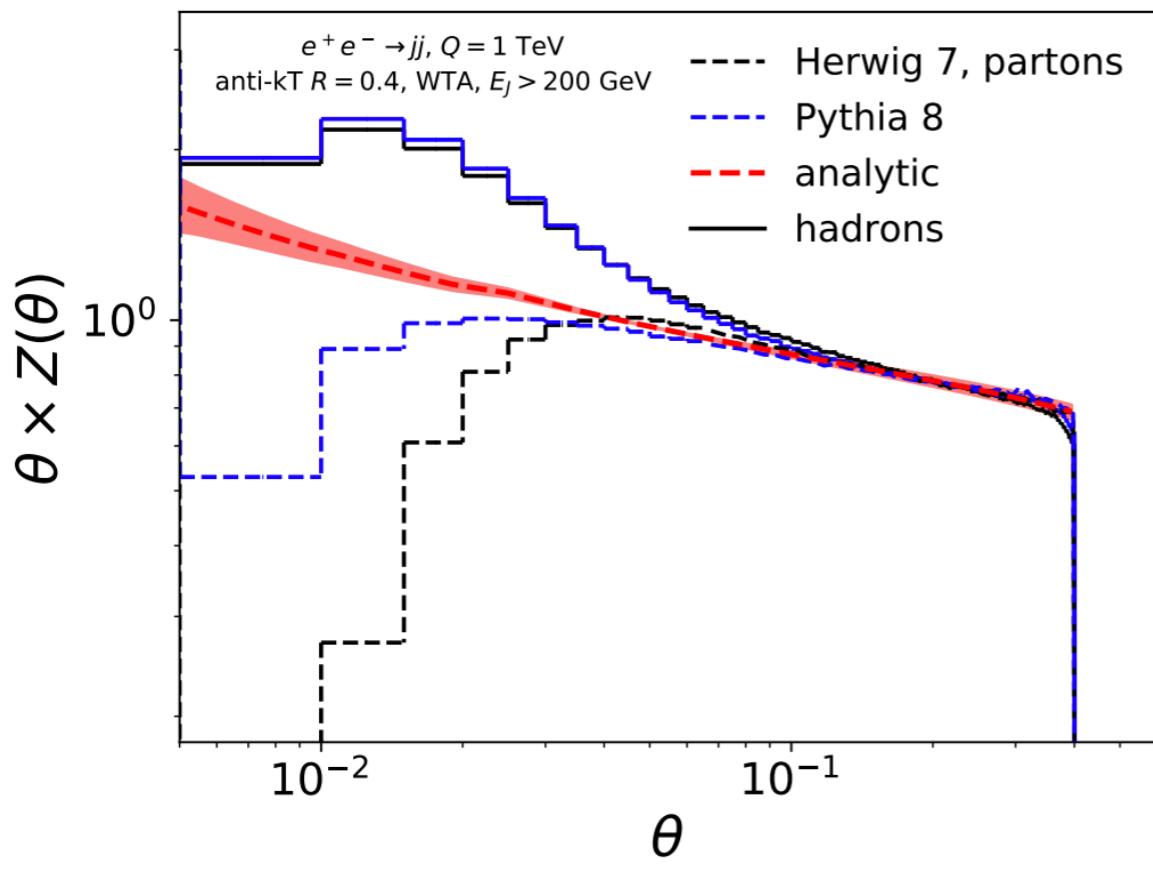


Kang, Prokudin, FR, Yuan '17  
STAR, PRD 97 032004 (2018)

see Miguel Arratia's talk

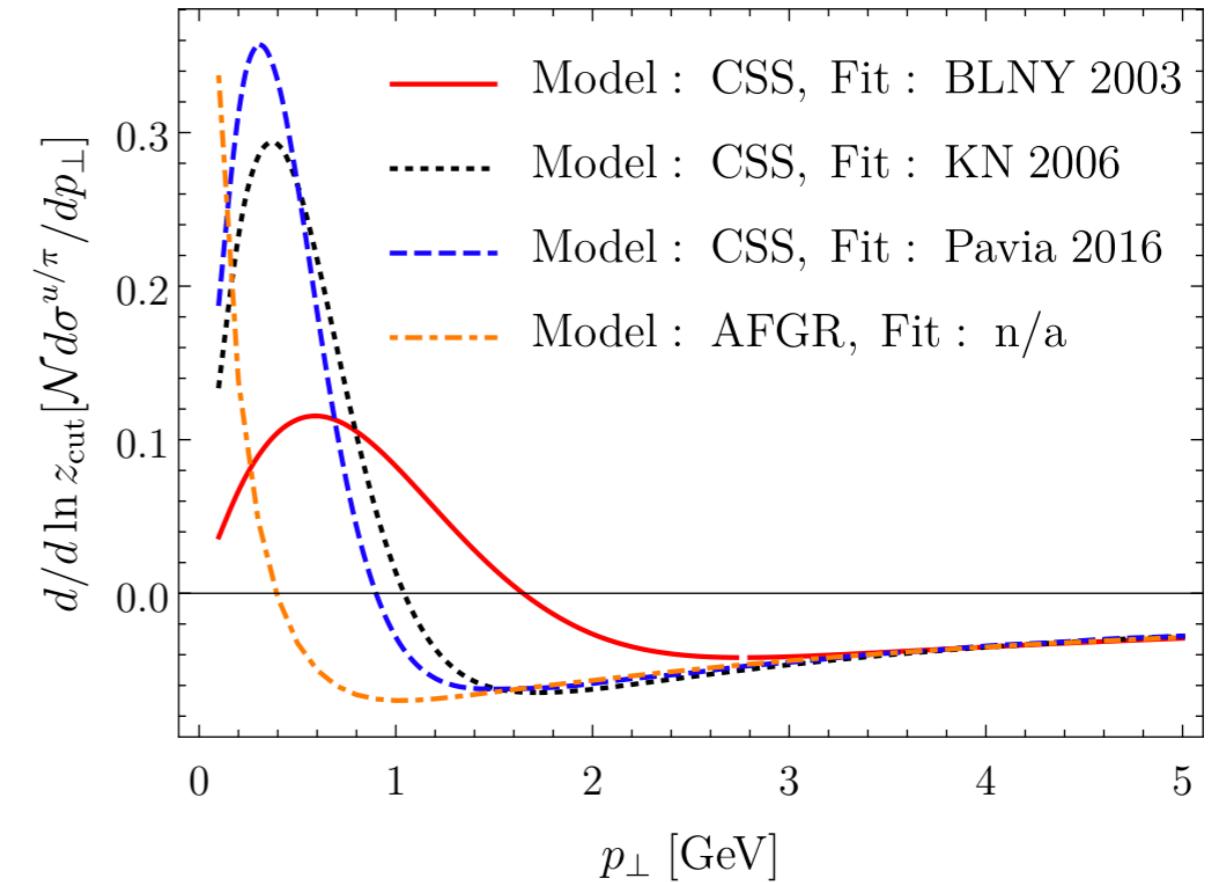
# The WTA axis and groomed jets

$$\theta = j_\perp / p_T$$



Nonperturbative effects  
very important at small angles,  $j_\perp$

Neill, Scimemi, Waalewijn '17  
Neill, Papaefstathiou, Waalewijn, Zoppi '18



Constraints on the nonperturbative  
part of the rapidity anomalous dimension

Makris, Neill, Vaidya '17

# Angles between jet axes

Cal, Neill, FR, Waalewijn '19  
see also: Makris, Neill, Vaidya '18

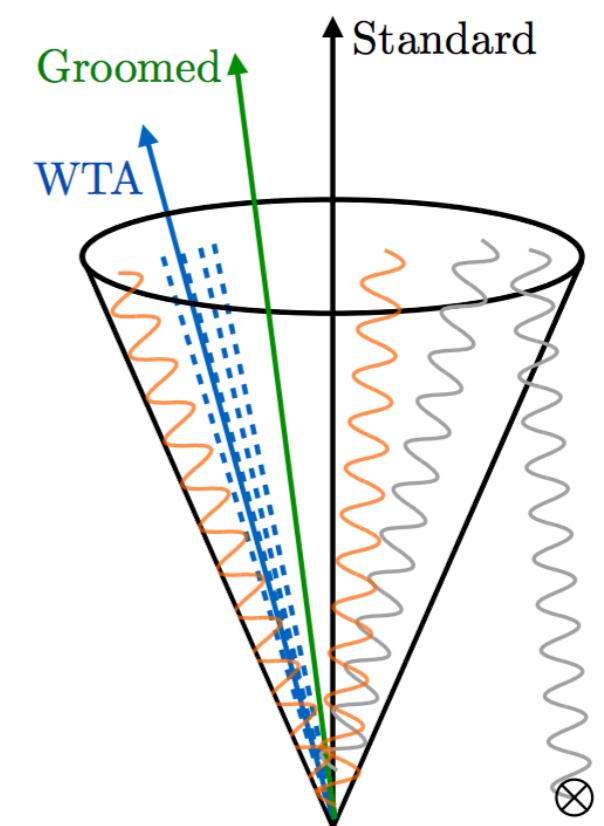
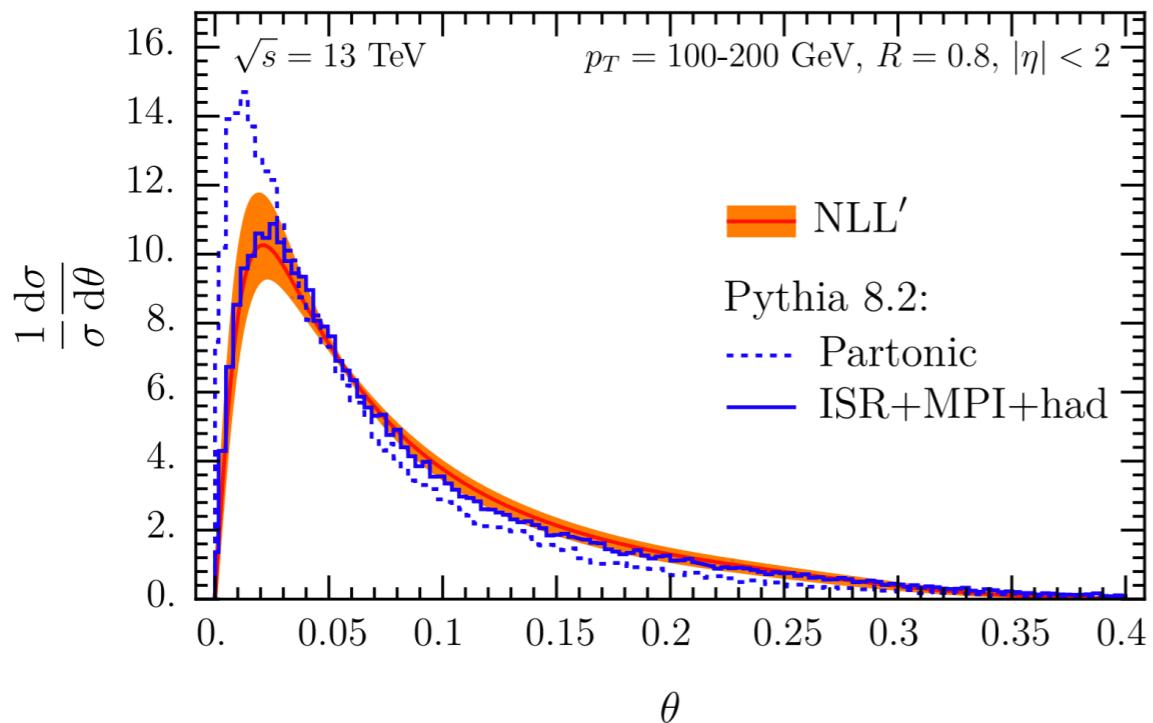
- IRC safe observables

- Probe of TMD evolution

$$\exp(-g_K \ln(\mu/\mu_0)) \quad \text{e.g.} \quad \exp \left[ -g_K(b_\perp, b_*) \frac{1}{1+\beta} \ln \frac{z_{\text{cut}} p_T R}{\mu_b} \right]$$

Nonperturbative part of the rapidity anomalous dimension

- Ideal observable at low energies such as the EIC



Soft drop parameters  $z_{\text{cut}}, \beta$

# Outline

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- Conclusions and outlook

# Overview

## Jet correlations

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Lepton-jet, Lab frame

IS-TMD

ST,WTA, GR

Proton-jet, Breit frame

IS&FS-TMD

ST,WTA, GR

Di-jet, Breit frame

IS-TMD

ST,WTA, GR

## Jet substructure

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Hadron-ST,GR axes

FS-TMD

Hadron-WTA axis

Jet axes-ST,WTA, GR or Jet shape

FS-TMD

*IS-Initial state, FS-Final state*

*TMD-Rapidity evolution, ST-Standard, WTA-Winner-take-all,  
GR-Soft drop groomed jet axis*

*Other choices of the jet axes possible*

# Conclusions

- Recent significant progress of TMD-jet observables
- Important observables at the EIC
- Jet substructure and jet correlations
- Non-global logarithms
- Include in fits
- EIC detector requirements

