

Hadron-in-jet in EIC: Factorization and Resummation

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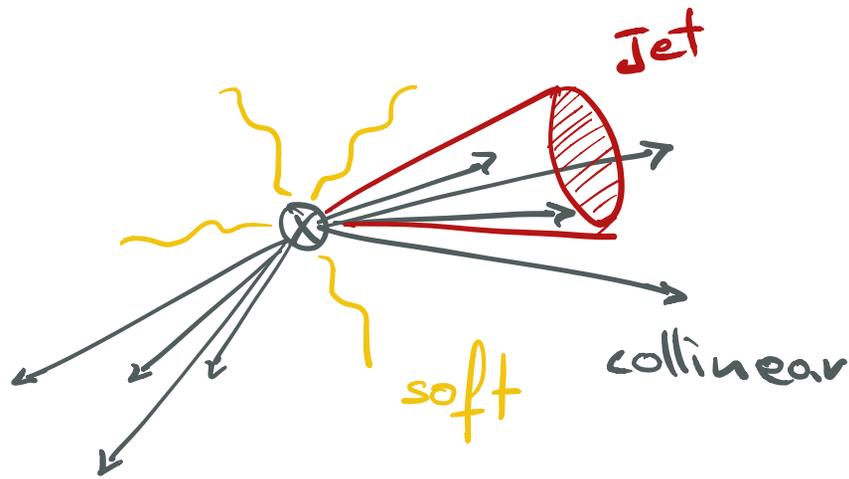
Outline

①

- Types of jets (semi-inclusive, exclusive, jet-axis, etc.)
- Phenomenology - Observables
 - Hadron-in-jet / Angularities / Energy fractions
 - TMDs + Groomed-jets
 - Heavy mesons in jets (threshold - logs)
- Factorization in EIC

Types of jets (exclusive vs semi-inclusive) (2)

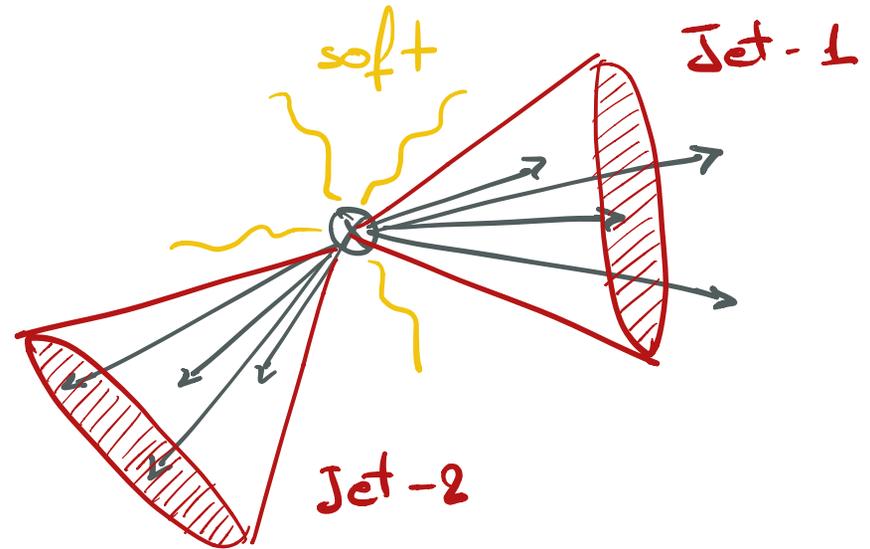
Semi-Inclusive



Example. $l+p \rightarrow l+jet+X$

Energetic radiation close to the jet axis can escape the jet.
Appropriate for small $-R$

Exclusive



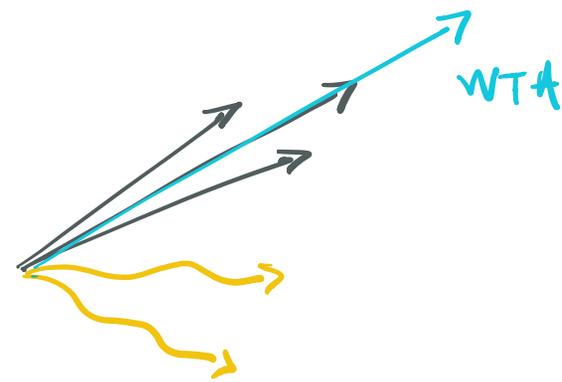
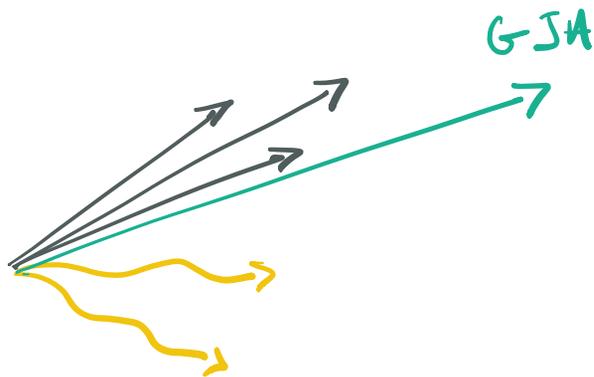
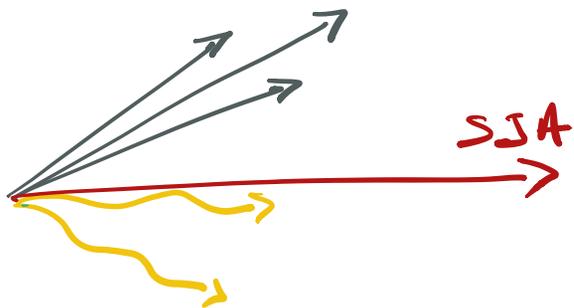
$l+p \rightarrow l+N-jets+X_{soft}$

$N=1,2,3,\dots$

Captures all energetic radiation
Works well with large $-R$

Types of jets (Modified vs Standard)

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Standard jet axis (SJA)

- located at the center of the jet and is given by the sum of all radiation in the jet

* Event-based axis: Thrust axis

Modified axis

- Examples : Groomed jet axis (GJA)
Jet broadening axis
Winner-Take-All (WTA)

Particularly relevant

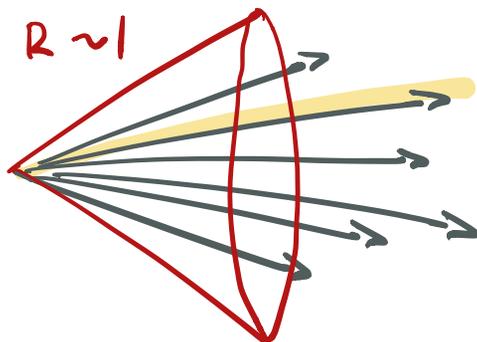
for TMDs

- Probes collinear radiation and is given by a sub-set of particles

Observables

Hadron-in-jet at FIC:

$$l+p \rightarrow l+jet(h)+X$$



identified hadron (h)

The hadron is member of the jet

Measurements on the hadron w.r.t. the jet

Measurements on the jet substructure

Energy fractions (eg. $z = E_h/E_{jet}$)

Jet energy

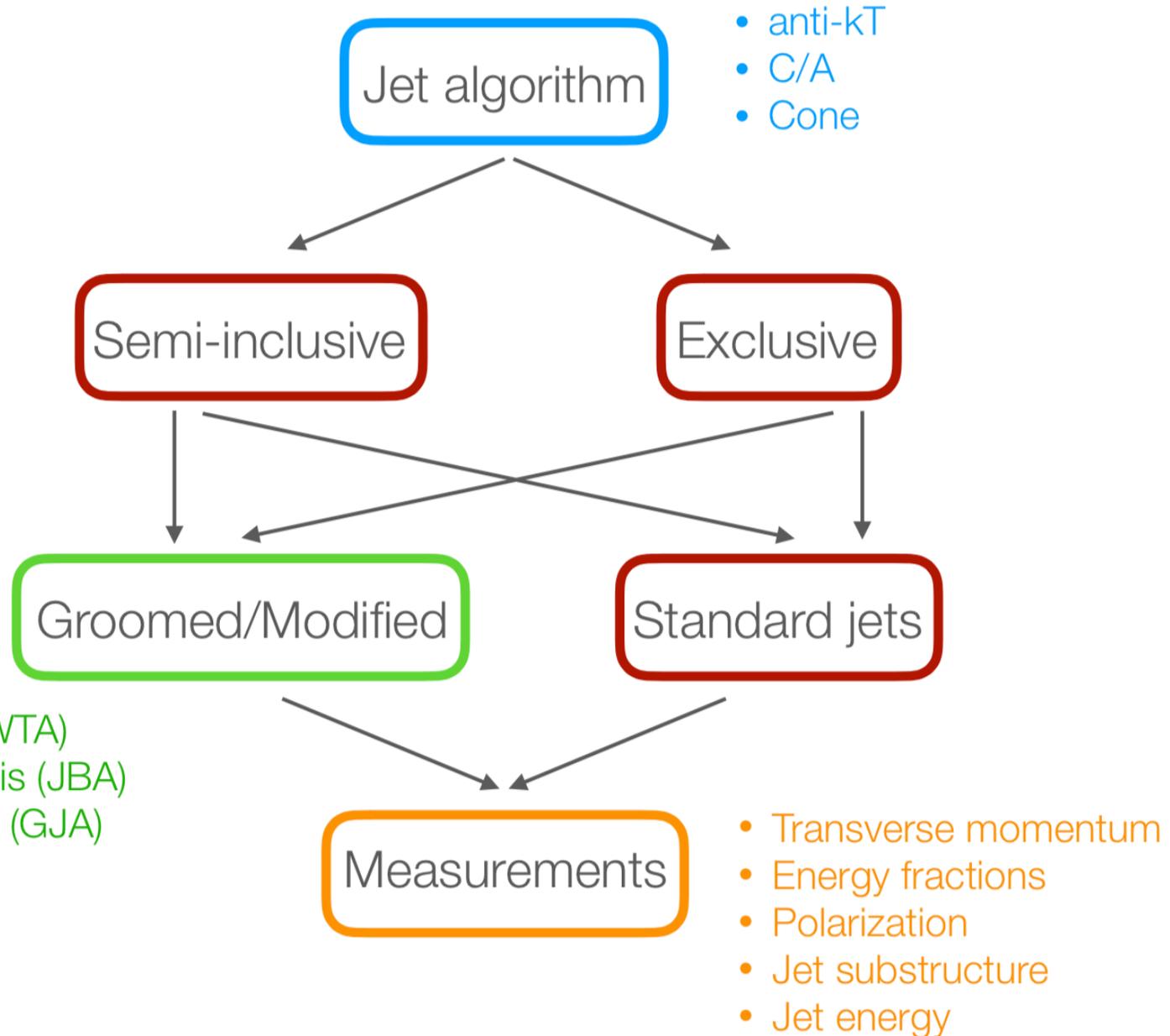
Transverse momentum w.r.t. jet
↳ choice of axis

Angularities / Thrust / jet mass

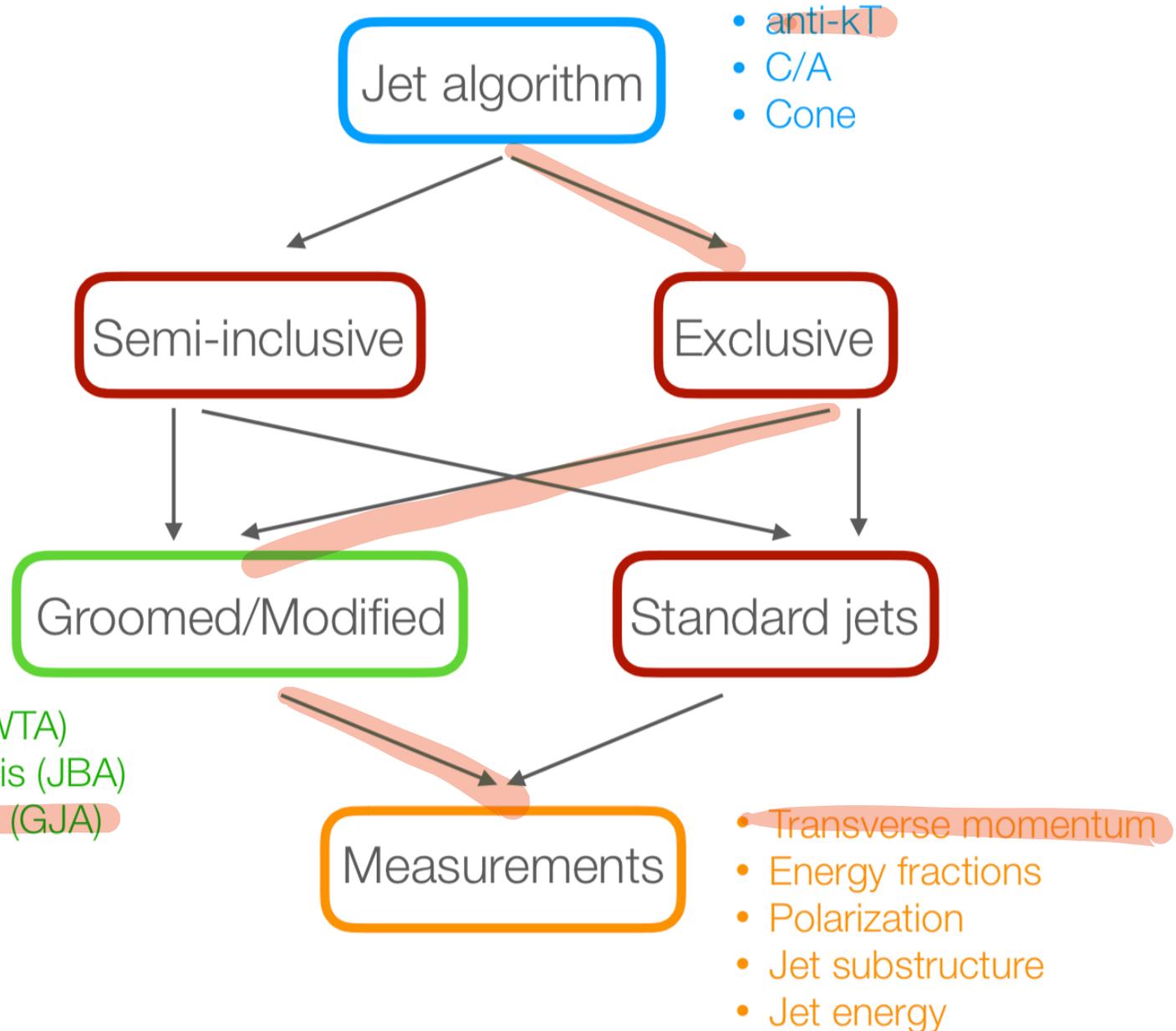
Polarization

Other jet substructure observables

Definition of jets



Definition of jets



Factorization at EIC

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Fragmenting-Jet-Functions (Measurement

Exclusive jets

$$\frac{d\sigma}{dzdM} = H_{ij}(Q; \mu) S(\Lambda; \mu) B_{i/P}(Q, M; \mu) G_{j/h}^E(z, Q, M; \mu)$$

dependent
Functions)

Semi-Inclusive jets

$$\frac{d\sigma}{dzdM} = \left[\frac{d\sigma}{dzdM}(lp \rightarrow j) \right] \otimes G_{j/h}^{S.I.}(z, Q, M, \mu)$$

- process specific part of the factorization

Universal functions
The formalism for lepton-lepton colliders can be easily incorporated for EIC!

Re-Factorization of FJFs

Refactorization is important for resumming large logarithms

Exclusive ↙ matching coefficient

$$G_{i/h}^E = C_S \otimes_M \tilde{f}_{i/j} \otimes_z D_{j/h}(z, h) \leftarrow \begin{matrix} \text{collinear fragmentation} \\ \text{functions} \end{matrix}$$

↑ collinear-soft matrix element

Semi-Inclusive

$$G_{i/h}^{S.I.} = H_i \times C_S \otimes_M \tilde{f}_{i/j} \otimes_z D_{j/h}(z, h)$$

↑ additional matching term

Energy fractions (only)

** Mass corrections;

Dai, Kim, Leibovich arXiv:1805.06014

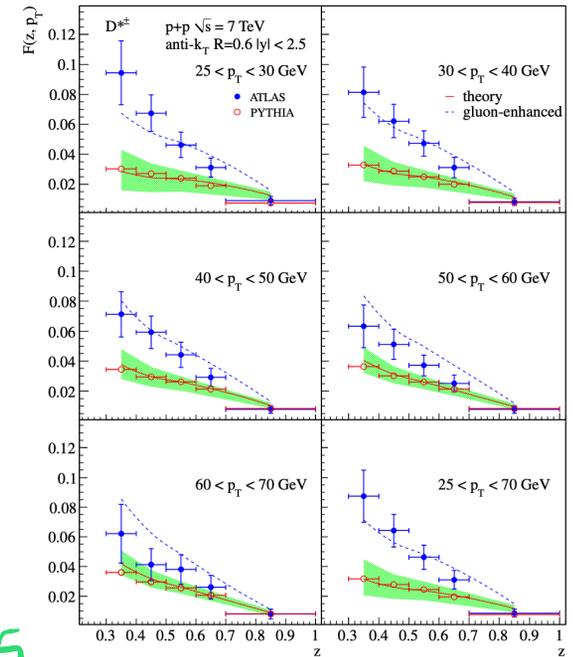
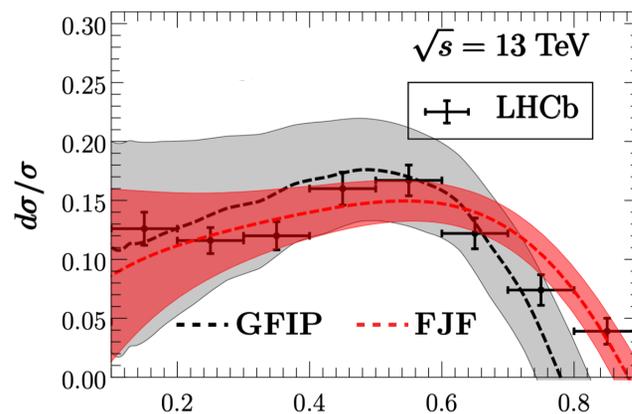
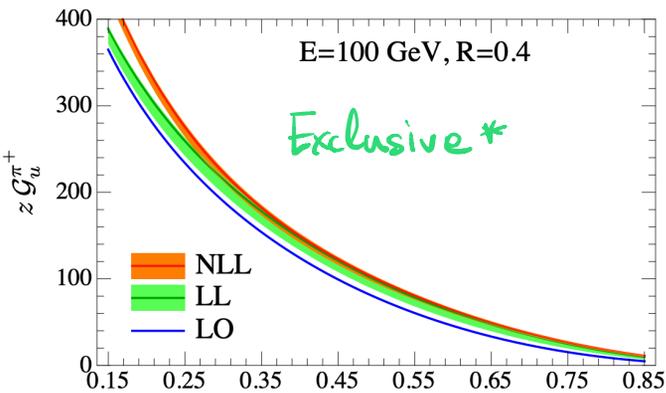
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The simplest observable is to measure the energy fraction of the hadron w.r.t. the jet

Light mesons (π)

Quarkonia (J/ψ)

Heavy mesons (D)



Procura, Waalewijn

arXiv: 1111.6605

Bain et al

arXiv: 1702.05525

* For semi-inclusive jets: Kaufmann et al. arXiv: 1506.01415

Threshold effects: Kaufmann et al. arXiv 1910.11746

Chien et al.

arXiv: 1512.06851

Thrust and Angularities

* full mass dependence
by Bauer, Merigheiti arXiv:1312.5605

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$$I(\alpha) = \frac{1}{2E_{jet}} \sum_{i \in jet} (P_i^+)^{1-\alpha/2} (P_i^-)^{\alpha/2}$$

← Sensitive to all radiation in the jet

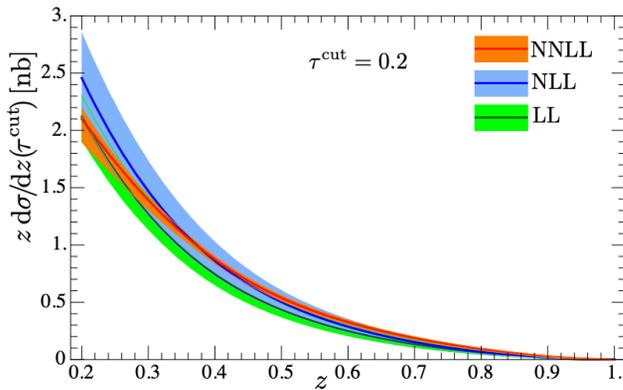
$\alpha < 2$ $I(\alpha=0) \sim \text{thrust (jet)}$

Angularities + Hadron-in-jet observables

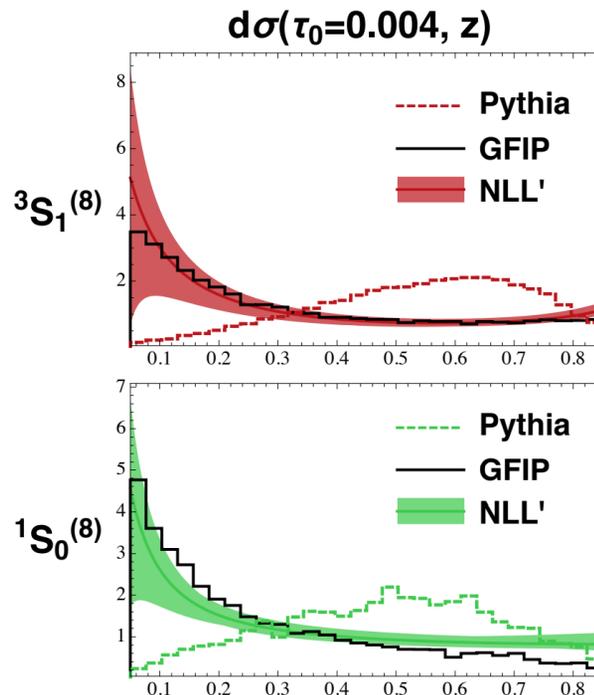
Light mesons (π)

Quarkonia (ψ/ϕ)

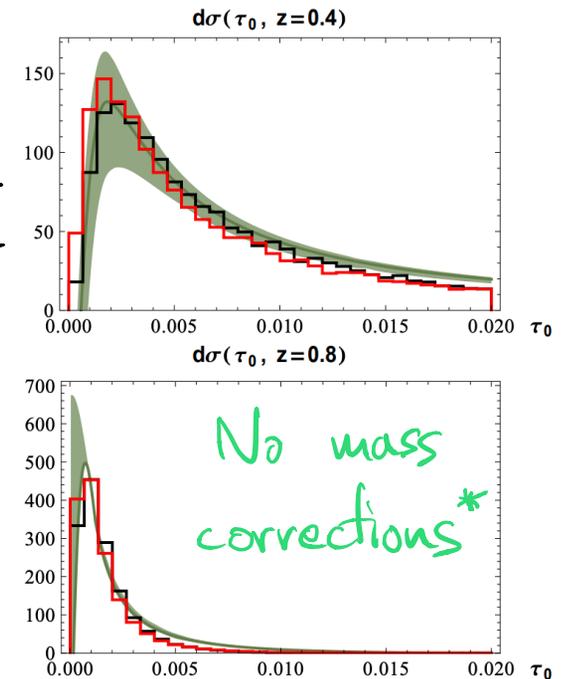
Heavy Mesons (B)



Jain, Procura, Waabeswiji
arXiv:1101.4953



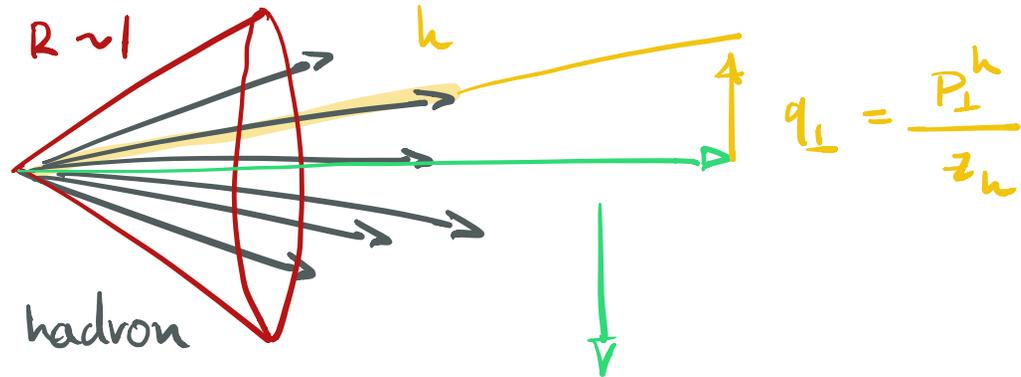
Bain et al.
arXiv:1603.06921



Transverse momentum dependent observables

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Measurement :



the transverse momentum of the hadron

is measured w.r.t. to the jet

jet axis (SJA, GJA, WTA, ...)

and rescaled by the energy fraction.

Exclusive (SJA) : Bain et.al. arXiv:1610.06508

Semi-inclusive (SJA) : Kang et.al. arXiv:1705.08443/1707.00913

Groomed-jets : Makris et.al. arXiv:1712.07653/1807.09805

Winner-take-all : Neil et.al. arXiv:1612.04817/1810.12915

What have we learned from these studies?

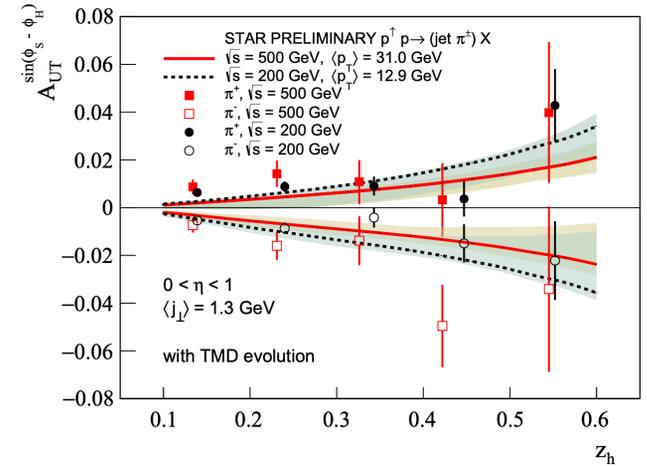
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① Hadron-in-jet can provide a TMD-factorization in isolation

$$\frac{d\sigma}{dzdM} = \boxed{\frac{d\sigma}{dzdM}(1p \rightarrow j)} \otimes G_{j/h}^{S.I.}(z, Q, M, k)$$

collinear factorization

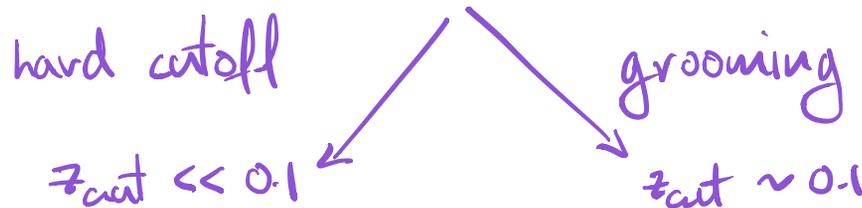
TMD factorization.



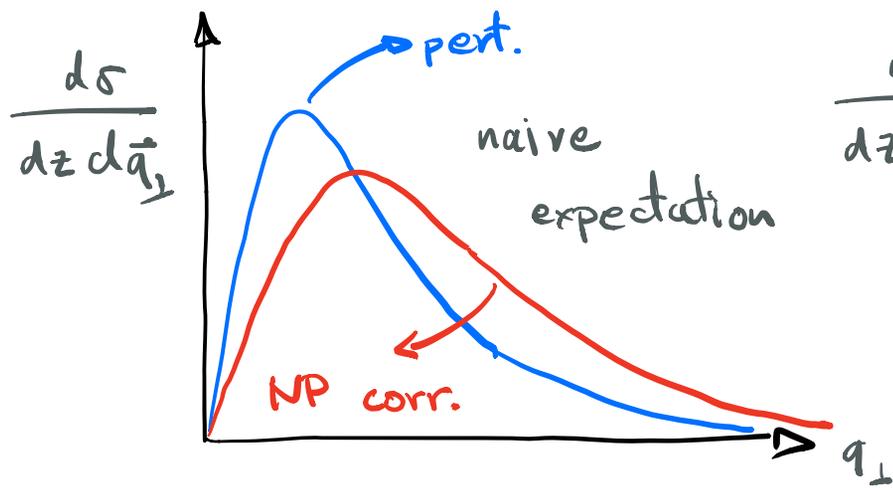
Kang et al.

arXiv: 1707.00913

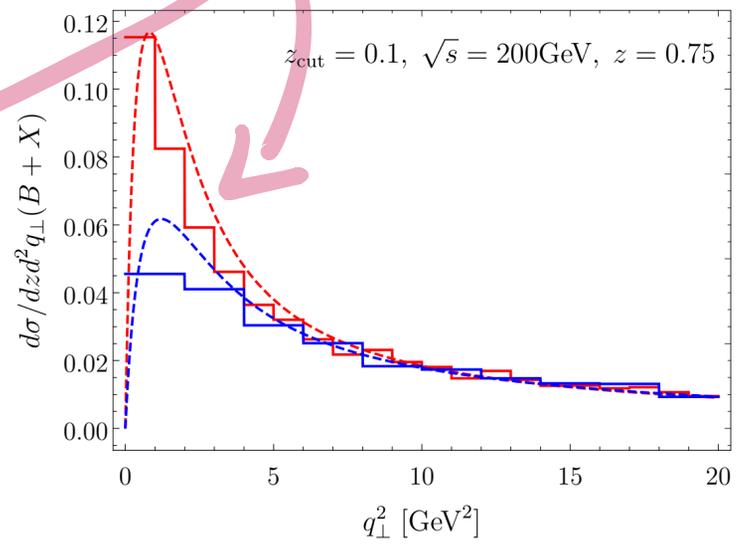
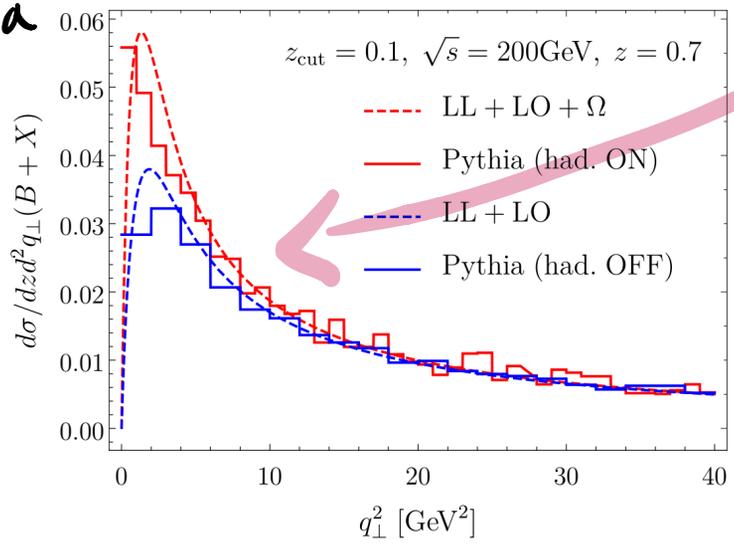
② Small z_h coming from underlying event can generate q_{\perp} contribution in the TMD region



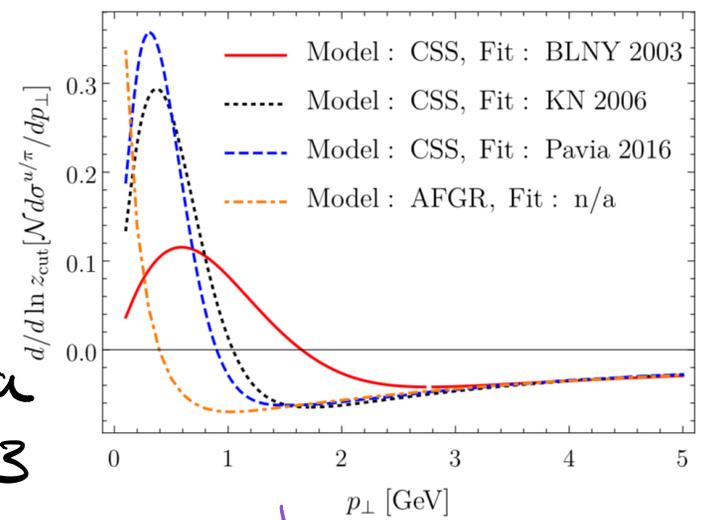
③ A more careful look at the heavy meson production at threshold ¹³ is needed. Heavy mesons in jet could provide a novel approach to hadronization studies.



Matris, Vaidya
arXiv:
1807.09805



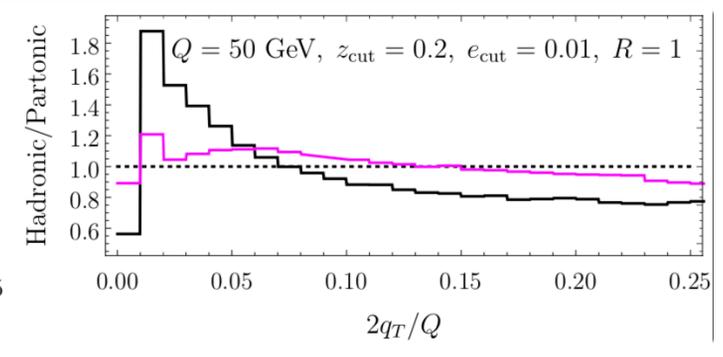
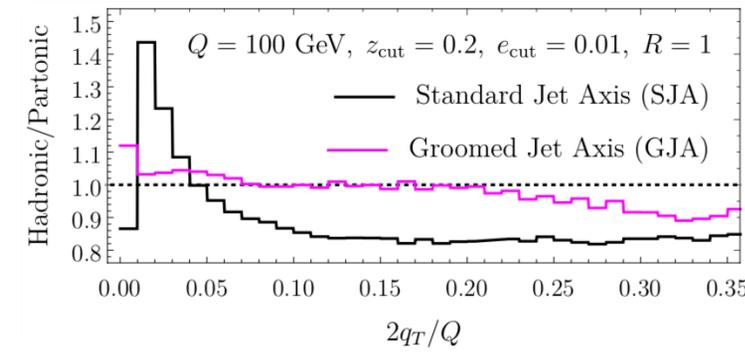
④ Grooming for light mesons can provide new observables for studying TMD-evolution



Mukris, Neil, Vaidya
arXiv: 1712.07653

⑤ Warning! Jet-algorithm dependent matrix elements introduce new non-perturbative corrections. No jet axis is insensitive to hadronization.

Reyes et.al
arXiv: 1907.05896

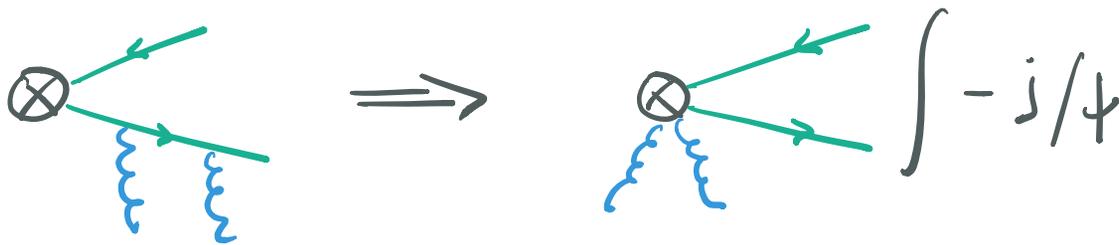


⑥ Not all hadron-in-jet q_{\perp} measurements result in TMD-like factorization. Examples are WTA and heavy mesons ($z_h \rightarrow 1$)

TMDs - Quarkonia

Quarkonia studies in soft background:

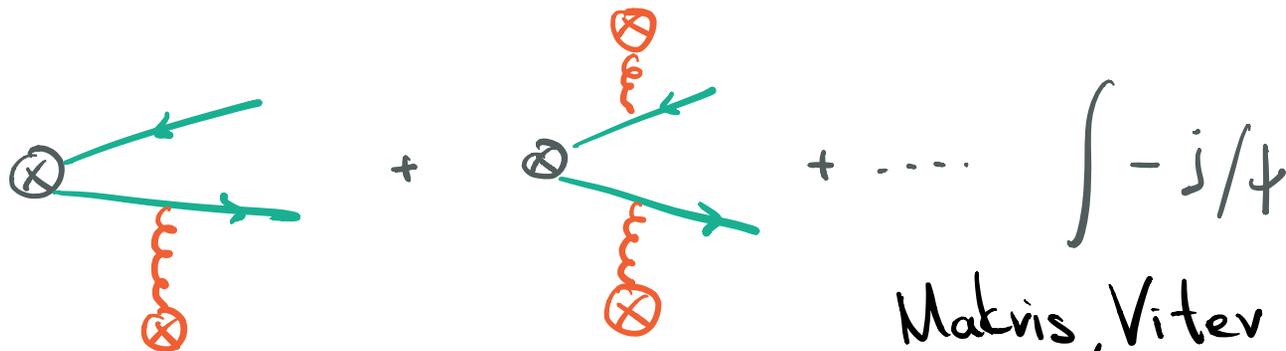
$SLET_Q$: Real - soft radiation



Fleming, Makris, Mehen

arXiv:1910.03586

$NRQCD_G$: Virtual - soft interactions.



Makris, Vitev

arXiv:1906.04186

Work in progress (15)

(1) Medium induced transitions (Ivan V.)

(2) Quarkonium photo / lepto - production (Sean F., Thomas M.)

(3) Quarkonium TMD - fragmentation (Ignazio S. Miguel E.)
(in-jet TMDs)

Summary

① Rapid evolution of the topic hadron-in-jet

② Better understanding of the possibilities and limitations

③ YR is a good reason to collaborate:

Categorize these limitations and to identify the key processes.

