

Probing Gluon TMDs at EIC

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Various types of TMDs

		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \odot$		$h_1^\perp = \uparrow - \downarrow$ Boer-Mulders
	L		$g_{1L} = \rightarrow - \rightarrow$ Helicity	$h_{1L}^\perp = \rightarrow - \rightarrow$
	T	$f_{1T}^\perp = \odot - \ominus$ Sivers	$g_{1T}^\perp = \uparrow - \uparrow$	$h_{1T}^\perp = \downarrow - \uparrow$ Transversity

		gluon pol.		
		U	L	linear
nucleon pol.	U	f_1^g		$h_1^{\perp g}$
	L		g_{1L}^g	$h_{1L}^{\perp g}$
	T	$f_{1T}^{\perp g}$	g_{1T}^g	$h_1^g, h_{1T}^{\perp g}$

- Probe unpolarized TMDs via h and hh .
- From spin-asymmetries, we can study spin-dependent TMDs such as the Sivers function f_{1T}^\perp .

A Tale of Two Gluon Distributions

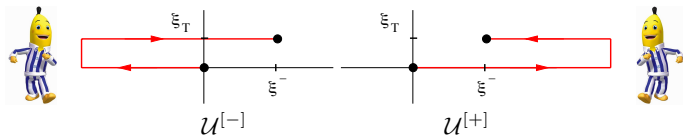
In terms of operators (TMD def. [Bomhof, Mulders and Pijlman, 06]), two **gauge invariant** gluon definitions: [Dominguez, Marquet, Xiao and Yuan, 11]

I. **Weizsäcker Williams** gluon distribution:

$$xG_{\text{WW}}(x, k_{\perp}) = 2 \int \frac{d\xi^{-} d\xi_{\perp}}{(2\pi)^3 P^{+}} e^{ixP^{+}\xi^{-} - ik_{\perp} \cdot \xi_{\perp}} \text{Tr} \langle P | F^{+i}(\xi^{-}, \xi_{\perp}) \mathcal{U}^{[+]\dagger} F^{+i}(0) \mathcal{U}^{[+]} | P \rangle.$$

II. **Color Dipole** gluon distributions:

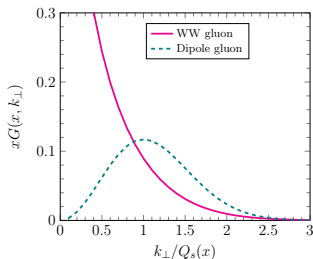
$$xG_{\text{DP}}(x, k_{\perp}) = 2 \int \frac{d\xi^{-} d\xi_{\perp}}{(2\pi)^3 P^{+}} e^{ixP^{+}\xi^{-} - ik_{\perp} \cdot \xi_{\perp}} \text{Tr} \langle P | F^{+i}(\xi^{-}, \xi_{\perp}) \mathcal{U}^{[-]\dagger} F^{+i}(0) \mathcal{U}^{[-]} | P \rangle.$$



- The WW gluon distribution is the **conventional gluon distributions**.
- The dipole gluon distribution has no such interpretation.
- Two topologically different gauge invariant definitions.
- Same after integrating over k_{\perp} ;

A Tale of Two Gluon Distributions

Measuring the gluon distributions in various processes I. **Weizsäcker Williams** gluon distribution; II. **Color Dipole** gluon distributions.



■ Modified Universality for Gluon Distributions:

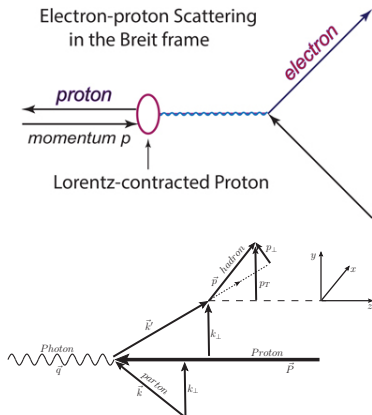
	Inclusive	Single Inc	DIS dijet	γ +jet	dijet in pA
xG_{WW}	×	×	✓	×	✓
xG_{DP}	✓	✓	×	✓	✓

× ⇒ Do Not Appear.

✓ ⇒ Appear.

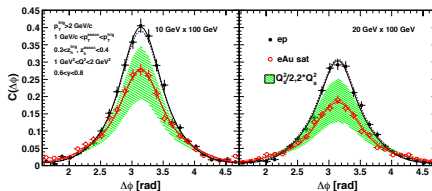
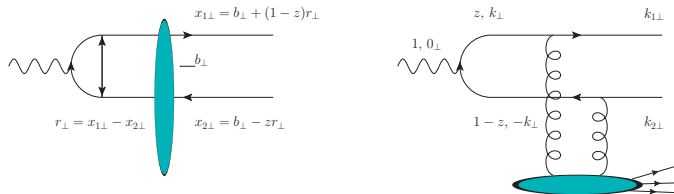
Semi-Inclusive DIS

Study unpolarized quark TMDs in the Breit frame ('brick wall' frame) in SIDIS



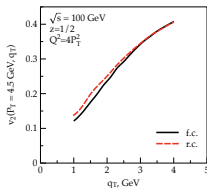
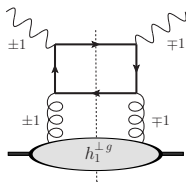
- In the Breit frame $q^\mu = (0, 0, 0, -Q)$, $k = (k_0, k_\perp, k_3 = Q/2)$, $z_h \equiv \frac{p \cdot P}{q \cdot P}$.
- We need to measure the recoiled electron to reconstruct the incoming virtual momentum.

Dijet production in DIS



- Back-to-back correlation measurement $C(\Delta\phi)$: [Zheng, Aschenauer, Lee and BX, 14] **Unique golden measurement** for the **Weizsäcker Williams** gluon distributions.
- **EIC** will be a **perfect machine** to study gluon saturation inside protons/nuclei.

Linearly Polarized Gluon distribution



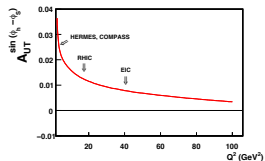
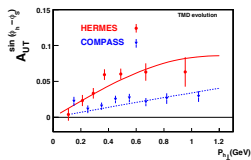
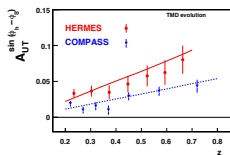
$$\frac{d\sigma}{dy_1 dy_2 dy dx_B d^2\mathbf{q}_T d^2\mathbf{K}_\perp} = \delta(1 - z_1 - z_2) \times \frac{\alpha^2 \alpha_s}{\pi s M_\perp^2} \frac{(1 + y x_B)}{y^5 x_B} \left[A + \frac{\mathbf{q}_T^2}{M^2} B \cos 2(\phi_T - \phi_\perp) \right].$$

$$B^{eh \rightarrow eQ\bar{Q}X} = \sum_Q e_Q^2 h_1^+g(x, \mathbf{q}_T^2) \mathcal{B}^{eg \rightarrow eQ\bar{Q}},$$

- [Boer, Brodsky, Mulders, Pisano, 11; Metz, Zhou, 11]
Probing the Linearly Polarized Gluon distribution $h_1^+g(x, \mathbf{q}_\perp^2)$ at EIC.
- Due to linearly polarized gluon distribution, there could be the analog of elliptic flow v_2 in DIS as well. [Dumitru, Lappi, Skokov, 15]

Transverse single spin asymmetry (SSA) in SIDIS

Extracting the quark Sivers function via SSA in SIDIS

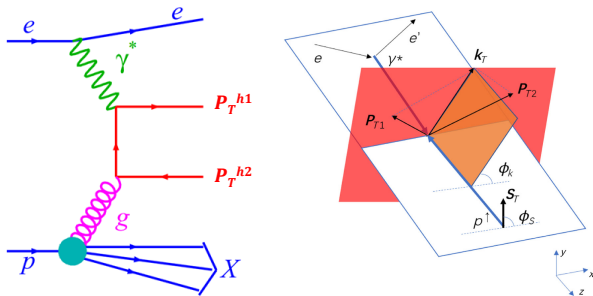


- [Aybat, Prokudin and Rogers, 12] indicates a couple of percent of SSA at EIC.
- SSA in SIDIS as a probe to the quark Sivers function f_{1T}^\perp

$$A_{UT}^{\sin(\phi_h - \phi_S)} = \frac{\int d\phi_h d\phi_S 2 \sin(\phi_h - \phi_S) (\sigma(\phi_h, \phi_S) - \sigma(\phi_h, \phi_S + \pi))}{\int d\phi_h d\phi_S (\sigma(\phi_h, \phi_S) + \sigma(\phi_h, \phi_S + \pi))}$$

Transverse single spin asymmetry (SSA) in SIDIS

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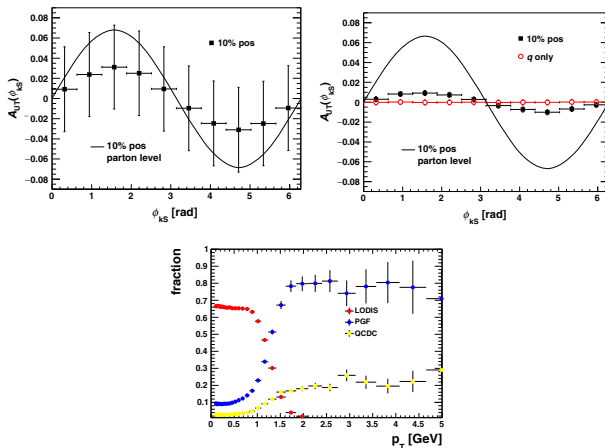


- [BX, Diehl, 12; Zheng, Aschenauer, Lee, Xiao, Yin, 18] indicates a couple of percent of SSA at EIC.
- SSA in this process as a probe to the gluon Sivers function f_{1T}^\perp

$$A_{UT}(\phi_{kS}, k_T) = \frac{d\sigma^\uparrow(\phi_{kS}, k_T) - d\sigma^\downarrow(\phi_{kS}, k_T)}{d\sigma^\uparrow(\phi_{kS}, k_T) + d\sigma^\downarrow(\phi_{kS}, k_T)} \propto \frac{\Delta^N f_{g/p^\uparrow}(x, k_\perp)}{2f_{g/p}(x, k_\perp)},$$

Transverse single spin asymmetry (SSA) in SIDIS

Extracting the gluon Sivers function via SSA in SIDIS



$$f_{1T}^{\perp g} = -\frac{2\sigma M_p}{k_{\perp}^2 + \sigma^2} f_g(x, k_{\perp}), \quad \sigma = 0.8 \text{ GeV},$$