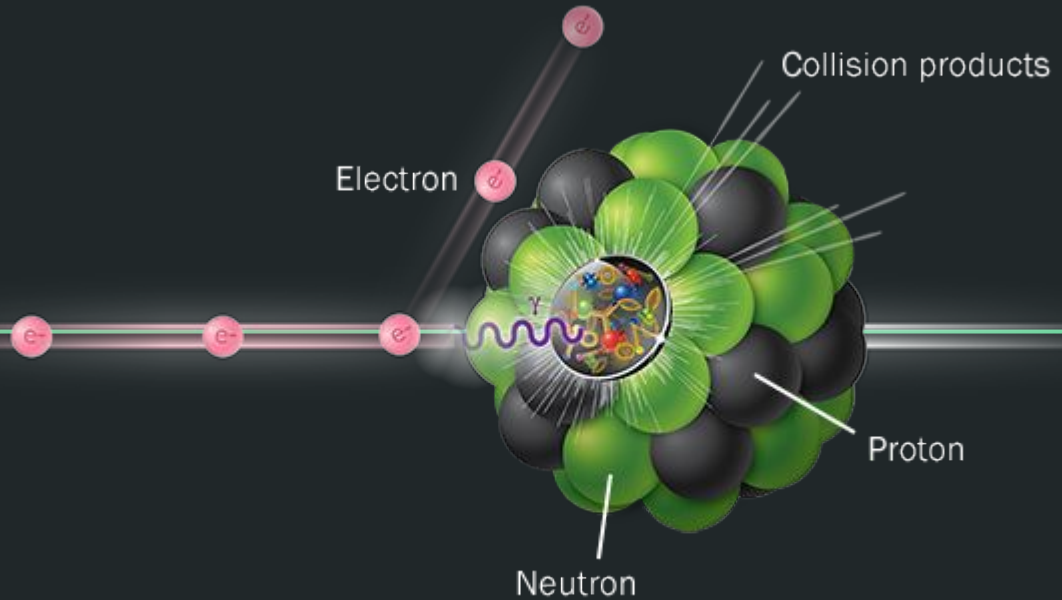


Experimental Measurements at the EIC



Renee Fatemi
University of Kentucky

Lecture IV

There is so much more to the proton!

We spent a lot of time talking about helicity distributions in Lectures I & II because they gave us a nice platform to investigate how to detect, reconstruct and analyse inclusive and semi-inclusive DIS events.

With those tools in our toolbox, let's take a step back and think about the many dimensions of the proton.

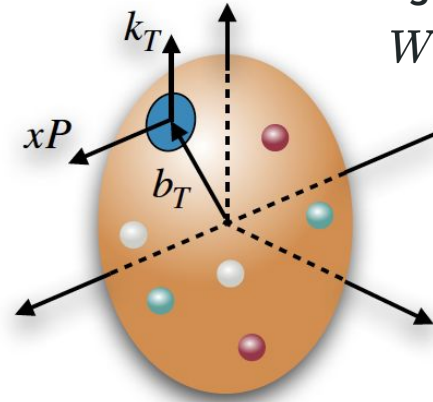


CS370413

SADLY THE CHARACTERS ARE STILL ONE-DIMENSIONAL.

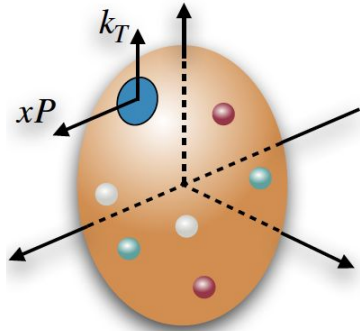
Wigner Functions

$$W(x, k_T, b_T)$$



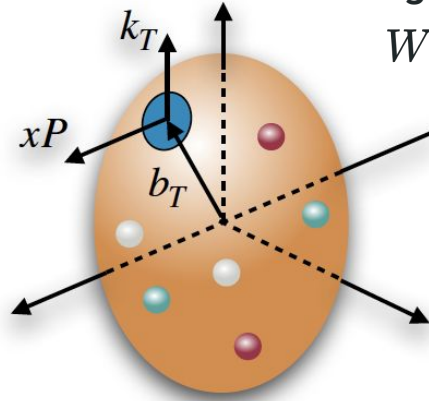
**Transverse Momentum
Distributions**

$$f(x, k_T)$$

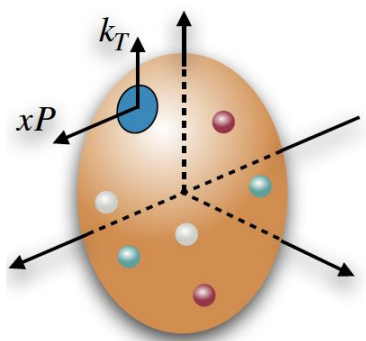


Wigner Functions

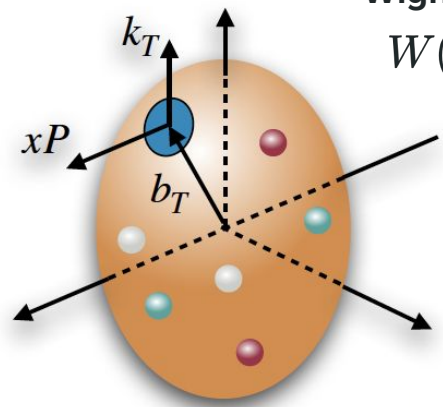
$$W(x, k_T, b_T)$$



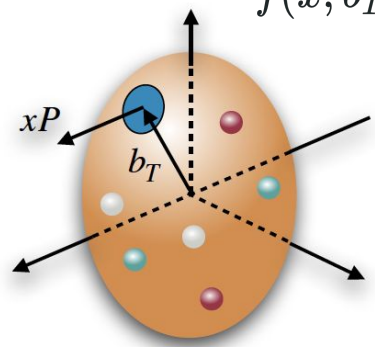
TMDs
 $f(x, k_T)$



Wigner Functions
 $W(x, k_T, b_T)$

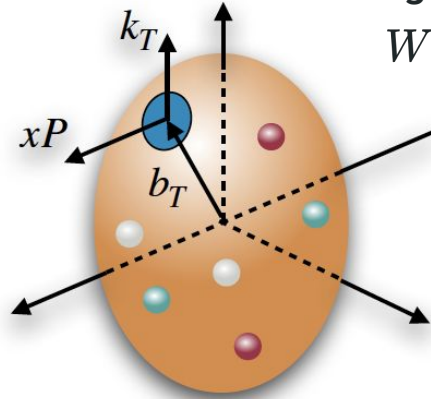


Fourier Transform of
Generalized Parton
Distributions
 $f(x, b_T)$



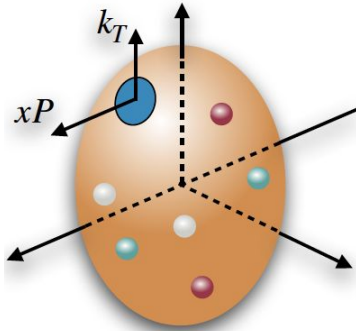
Wigner Functions

$$W(x, k_T, b_T)$$



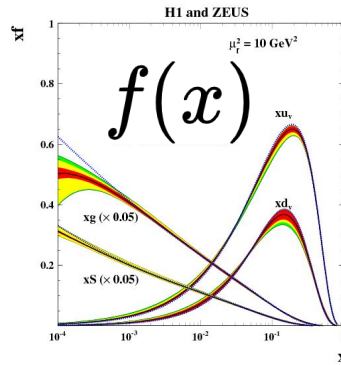
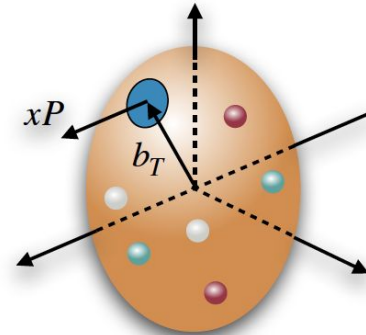
TMDs

$$f(x, k_T)$$



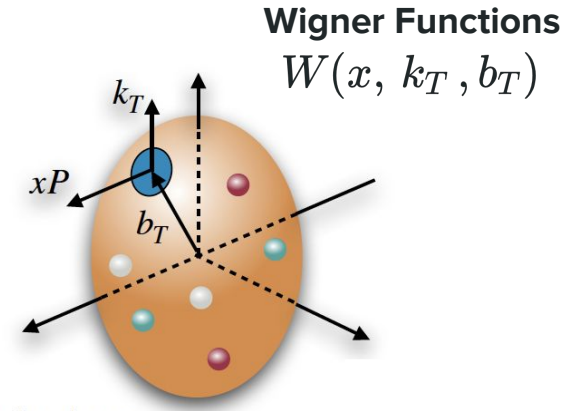
Fourier Transform of GPDs

$$f(x, b_T)$$

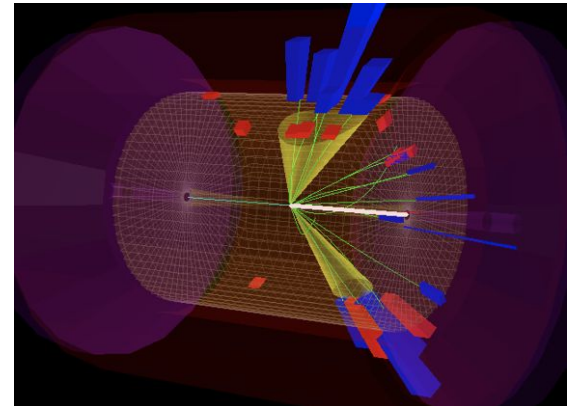


Can we measure a Wigner Function?

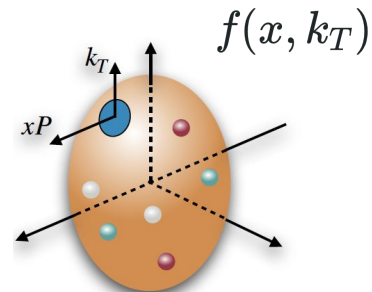
- Five years ago this question would have been met with silence.
- In 2016 **Hatta, Xiao and Yuan** proposed using diffractive dijet production at the EIC to probe the fourier transform of the gluon Wigner distribution.
- Requires reconstruction of dijet, with a rapidity gap, ie no activity between the jet and the hadron beam.
- Sensitive to k_T via the dijet relative $P_T = \frac{(P_{T1} - P_{T2})}{2}$
- Sensitive to b_T via the proton transverse recoil:
$$\Delta x_T = -(P_{T1} + P_{T2})$$
- Azimuthal correlations between P_T and Δx are sensitive to correlations between k_T and b_T in the Wigner distribution.



Theory is rapidly evolving - promising new experimental channels are being developed.

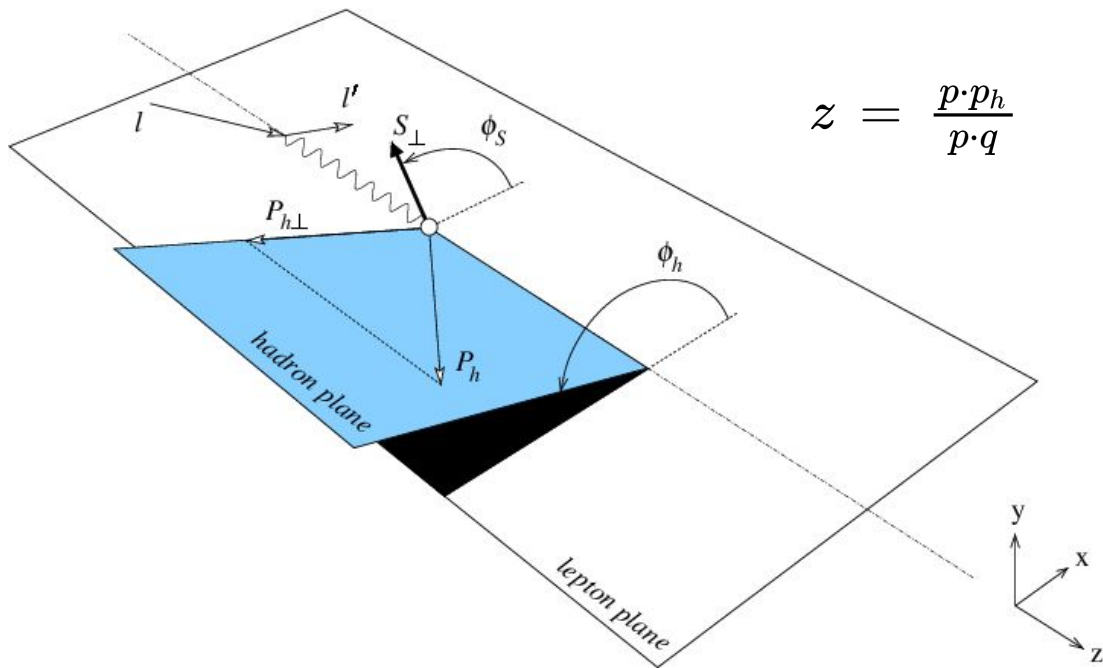


TMD parton distribution functions

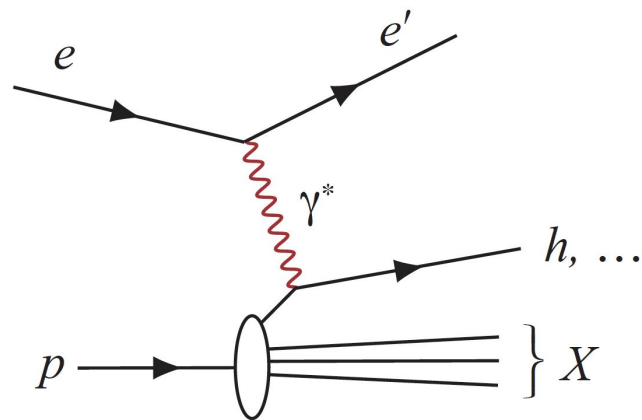


		Quark Polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1(x, k_T^2)$		$h_1^\perp(x, k_T^2)$ <i>Boer-Mulders</i>
	L		$g_1(x, k_T^2)$ <i>Helicity</i>	$h_{1L}^\perp(x, k_T^2)$ <i>Long-Transversity</i>
	T	$f_1^\perp(x, k_T^2)$ <i>Sivers</i>	$g_{1T}(x, k_T^2)$ <i>Trans-Helicity</i>	$h_1(x, k_T^2)$ <i>Transversity</i> $h_{1T}^\perp(x, k_T^2)$ <i>Pretzelosity</i>

TMDs require SIDIS



$$z = \frac{p \cdot p_h}{p \cdot q}$$



In addition to standard DIS kinematic variables it is necessary to measure:

- $P_{h\perp}$ the transverse momentum of the reconstructed hadron
- ϕ_h the angle between the hadron and scattering plane
- ϕ_S the angle between the nucleon spin and the scattering plane.

Lepton-Hadron Cross-section

$F_{XY,Z}$

- X is polarization of electron beam WRT to \mathbf{y}^*
- Y is the polarization of proton beam WRT \mathbf{y}^*
- Z is the polarization of the virtual photon

$$\begin{aligned}
 \frac{d^6\sigma}{dx dy dz d\phi d\phi_S dP_{h\perp}^2} &= \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} \right. \\
 &+ \sqrt{2\epsilon(1+\epsilon)} \cos\phi F_{UU}^{\cos\phi} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi F_{LU}^{\sin\phi} \\
 &+ S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin\phi F_{UL}^{\sin\phi} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\
 &+ S_L \lambda_e \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos\phi F_{LL}^{\cos\phi} \right] \\
 &+ |S_T| \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi - \phi_S)} + \epsilon F_{UT,L}^{\sin(\phi - \phi_S)} \right) \right. \\
 &+ \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi + \phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi - \phi_S)} \\
 &\left. + \sqrt{2\epsilon(1+\epsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi - \phi_S)} \right] \\
 &+ |S_T| \lambda_e \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi - \phi_S)} + \sqrt{2\epsilon(1-\epsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 &\left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi - \phi_S)} \right] \left. \right\}.
 \end{aligned}$$

Lepton-Hadron Cross-section

$F_{XY,Z}$

- X is polarization of electron beam WRT to \mathbf{y}^*
- Y is the polarization of proton beam WRT \mathbf{y}^*
- Z is the polarization of the virtual photon

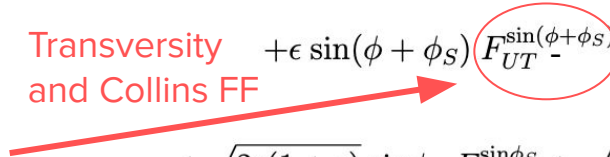
$$F_{UT}^{\sin(\phi+\phi_S)} = C \left[-\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} \delta q H_1^\perp \right]$$

and

$$F_{UT,T}^{\sin(\phi-\phi_S)} = C \left[-\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_{1T}^\perp D_1 \right]$$

$$\begin{aligned} \frac{d^6\sigma}{dx dy dz d\phi d\phi_S dP_{h\perp}^2} &= \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ F_{UU,T} + \epsilon F_{UU,L} \right. \\ &+ \sqrt{2\epsilon(1+\epsilon)} \cos\phi F_{UU}^{\cos\phi} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi F_{LU}^{\sin\phi} \\ &+ S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin\phi F_{UL}^{\sin\phi} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ &+ S_L \lambda_e \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos\phi F_{LL}^{\cos\phi} \right] \\ &+ |S_T| \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \right. \\ &\quad \left. + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \right. \\ &\quad \left. + \sqrt{2\epsilon(1+\epsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right] \\ &+ |S_T| \lambda_e \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} + \sqrt{2\epsilon(1-\epsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\ &\quad \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \left. \right\}. \end{aligned}$$

Transversity
and Collins FF



Lepton-Hadron Cross-section

$F_{XY,Z}$

- X is polarization of electron beam WRT to \mathbf{y}^*
- Y is the polarization of proton beam WRT \mathbf{y}^*
- Z is the polarization of the virtual photon

$$F_{UT}^{\sin(\phi+\phi_S)} = \mathcal{C} \left[-\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} \delta q H_1^\perp \right]$$

and

$$F_{UT,T}^{\sin(\phi-\phi_S)} = \mathcal{C} \left[-\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_{1T}^\perp D_1 \right]$$

Sivers and
spin
independent
FF

$$\begin{aligned} \frac{d^6\sigma}{dx dy dz d\phi d\phi_S dP_{h\perp}^2} &= \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ F_{UU,T} + \epsilon F_{UU,L} \right. \\ &+ \sqrt{2\epsilon(1+\epsilon)} \cos\phi F_{UU}^{\cos\phi} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi F_{LU}^{\sin\phi} \\ &+ S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin\phi F_{UL}^{\sin\phi} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ &+ S_L \lambda_e \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos\phi F_{LL}^{\cos\phi} \right] \\ &+ |S_T| \left[\sin(\phi-\phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \right. \\ &+ \epsilon \sin(\phi+\phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi-\phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \\ &+ \sqrt{2\epsilon(1+\epsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi-\phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \left. \right] \\ &+ |S_T| \lambda_e \left[\sqrt{1-\epsilon^2} \cos(\phi-\phi_S) F_{LT}^{\cos(\phi-\phi_S)} + \sqrt{2\epsilon(1-\epsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\ &\left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi-\phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \left. \right\}. \end{aligned}$$

TMD extraction requires global analysis of both PDF and FF!!

Sivers \otimes FF

$$F_{UT,T}^{\sin(\phi-\phi_S)} = \mathcal{C} \left[-\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_{1T}^\perp D_1 \right]$$

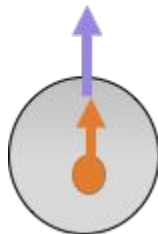


\otimes

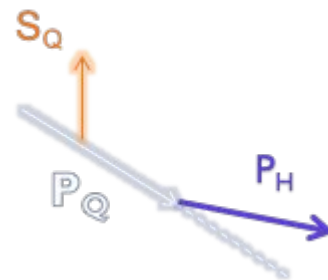


Transversity \otimes Collins

$$F_{UT}^{\sin(\phi+\phi_S)} = \mathcal{C} \left[-\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} \delta q H_1^\perp \right]$$



\otimes



$$A_{UT}^{\sin(\phi_h+\phi_s)}(x, y, z, P_T) = \frac{2(1-y)}{1+(1-y)^2} \frac{F_{UT}^{\sin(\phi_h+\phi_s)}}{F_{UU}} .$$

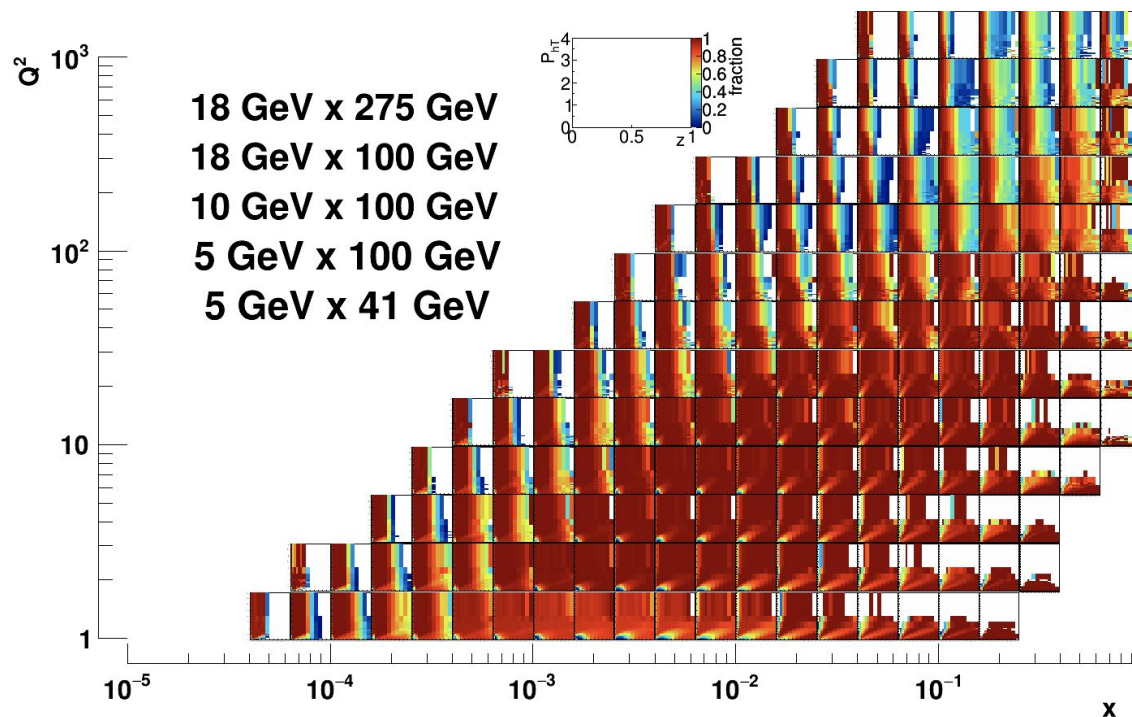
TMDs at the EIC

Yellow Report : 2103.05419

Hadron acceptance fractions
as a function of z and $P_{h\perp}$

Low acceptance at
intermediate x and high Q^2 is
do to limit PID capabilities.

This region is important
because ***TMD evolution is
not fully prescribed by
theory. There is a
non-perturbative component
that must be measured
experimentally.***



Affinity for TMD Factorization

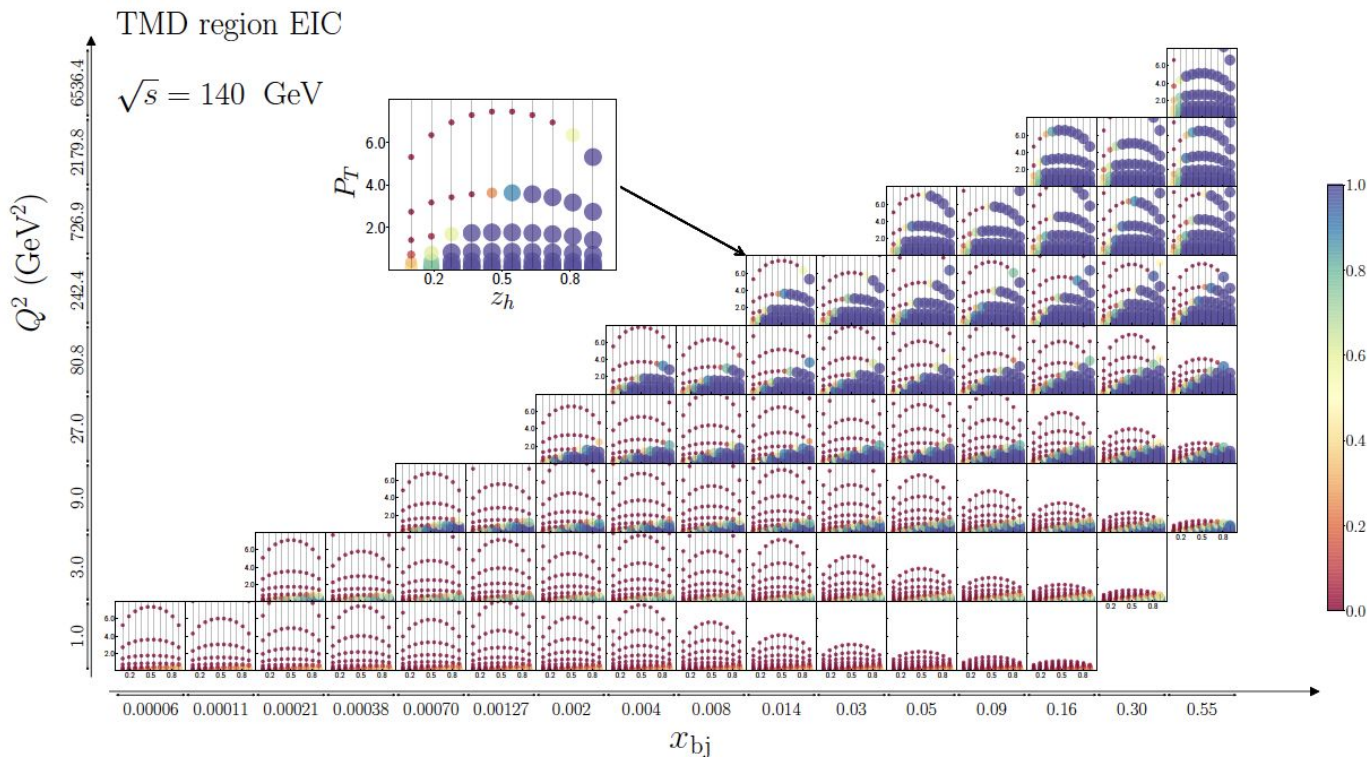
Yellow Report : 2103.05419

x - Q^2 plane for
future EIC
measurement at
 $\sqrt{s} = 140$ GeV.

Dot represent
affinity for
factorization.

$$\frac{P_T}{zQ} < 0.25$$

The sea of red at
low Q^2 excludes
many previous
measurements.



Affinity for TMD Factorization

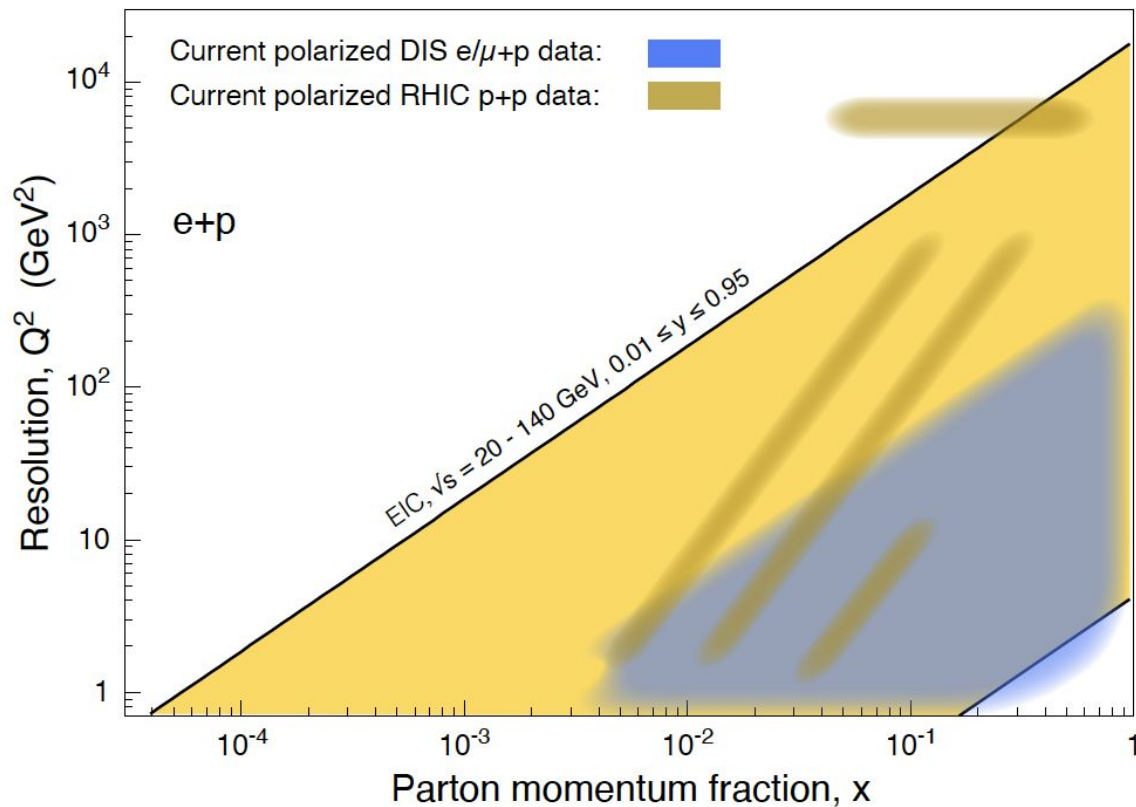
Yellow Report : 2103.05419

x - Q^2 plane for
future EIC
measurement at
 $\sqrt{s} = 140$ GeV.

Dots represent
affinity for
factorization.

$$\frac{P_T}{zQ} < 0.25$$

The sea of red at
low Q^2 excludes
many previous
measurements.



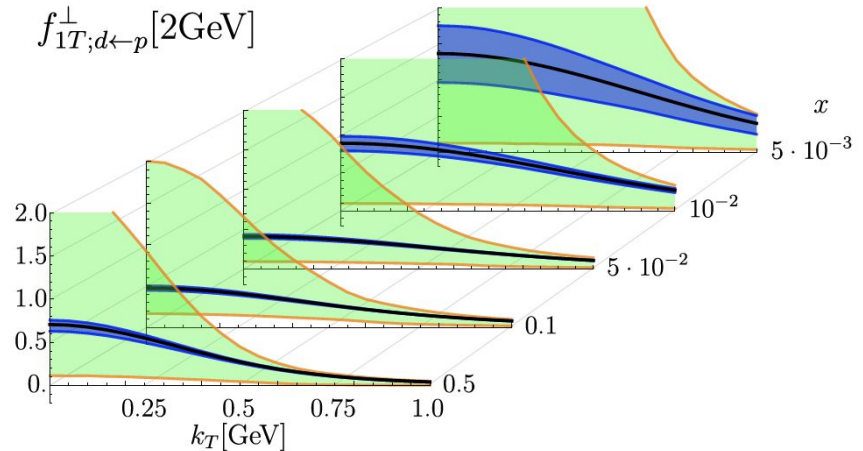
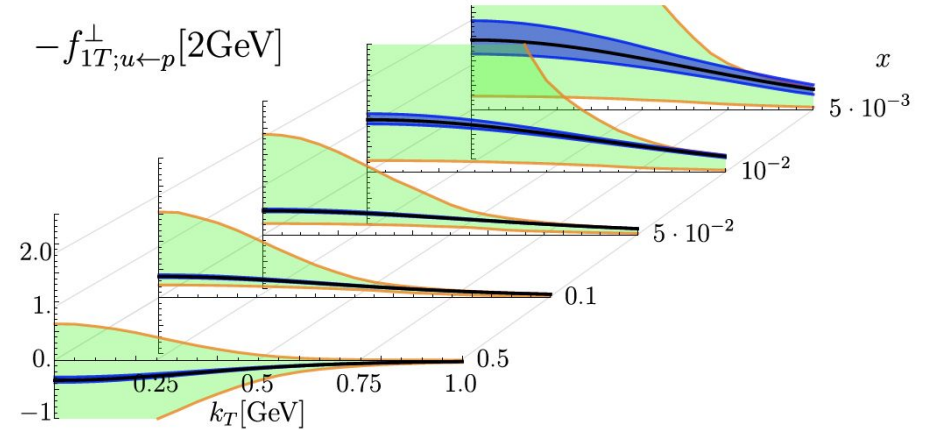
EIC impact on u/d Sivers

Current (green) and EIC (blue) constraints on the up and down Sivers functions.

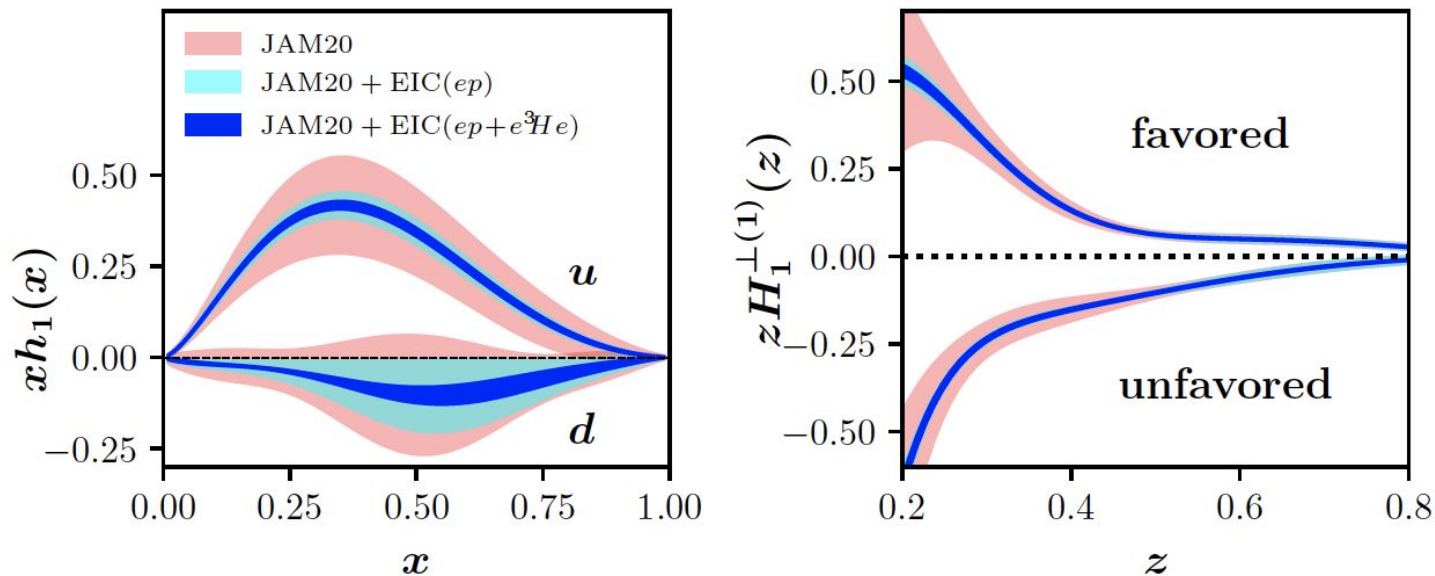
The size of the error bars is due to the limited subset of existing data that satisfies factorization conditions.

Uncertainties can be reduced by more than an order of magnitude for all flavors.

The wide range of hadron pT facilitates the mapping in kT



EIC Impact on Transversity and Collins Functions

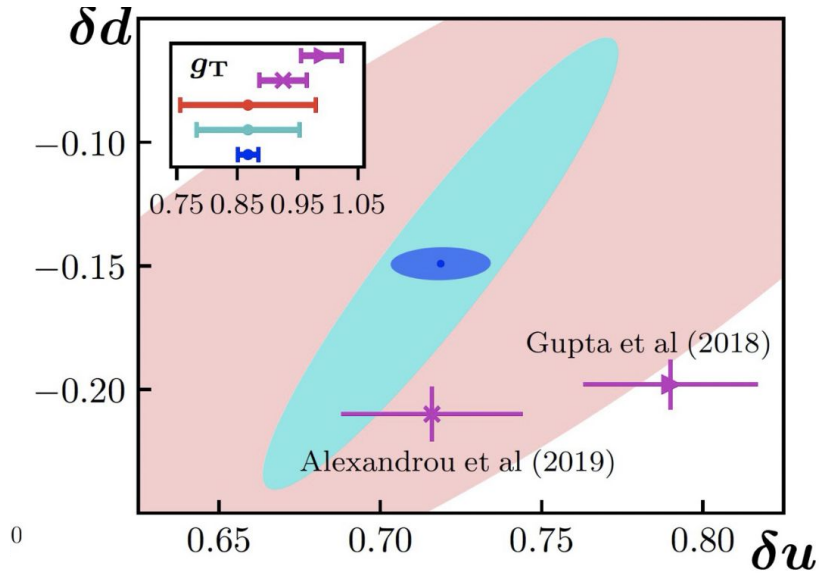


L. Gamberg, Z. Kang, D. Pitonyak, A. Prokudin, N. Sato Phys.Lett.B 816 (2021)

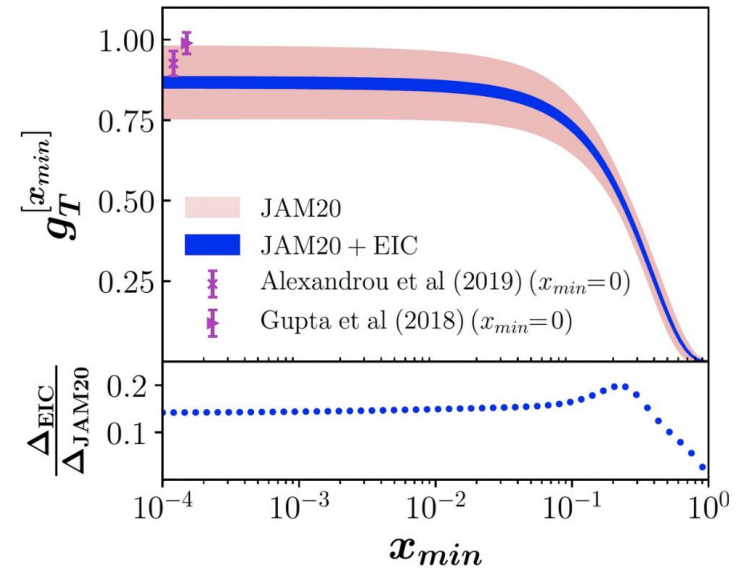
JAM20: Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato, Phys.Rev.D 102 (2020)

EIC constraints on tensor charge

$$\delta q(Q^2) \equiv \int_0^1 dx \left(h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2) \right).$$



$$g_T = \delta u - \delta d$$

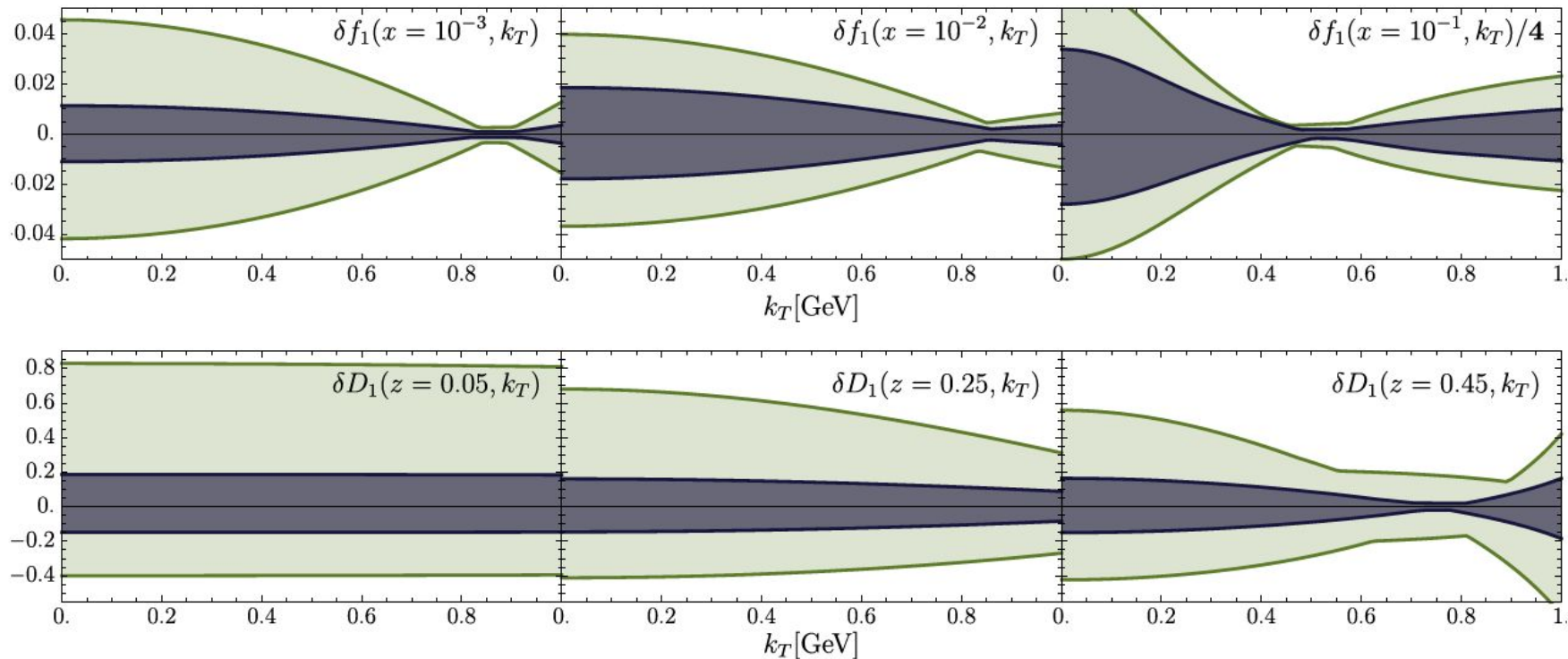


L. Gamberg, Z. Kang, D. Pitonyak, A. Prokudin, N. Sato Phys.Lett.B 816 (2021)

JAM20: Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato, Phys.Rev.D 102 (2020)

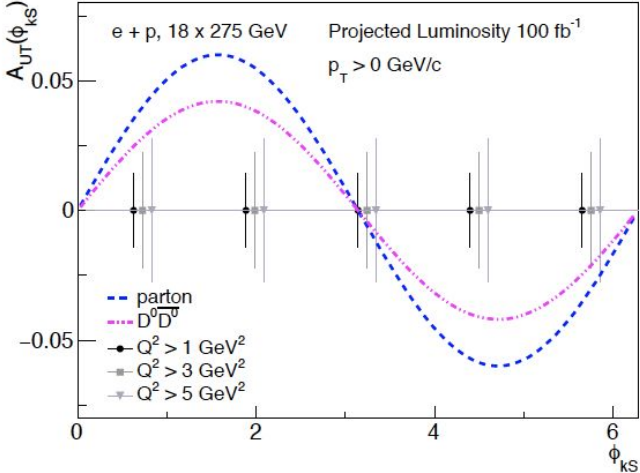
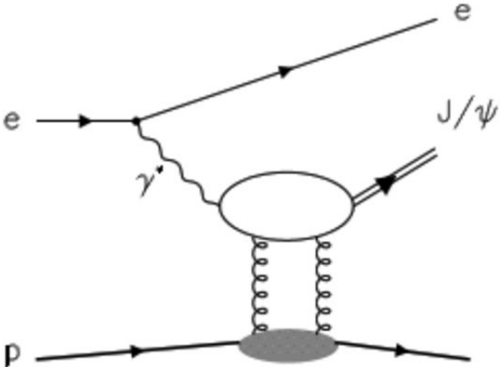
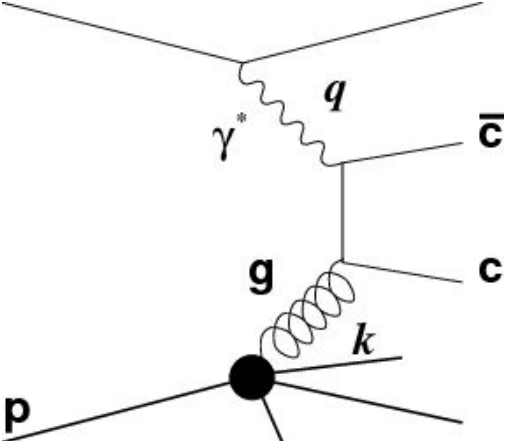
EIC impact on Unpolarized TMD PDFs and FF

Impact on unpolarized up quark TMD PDF and unpolarized u-pi TMD FF/



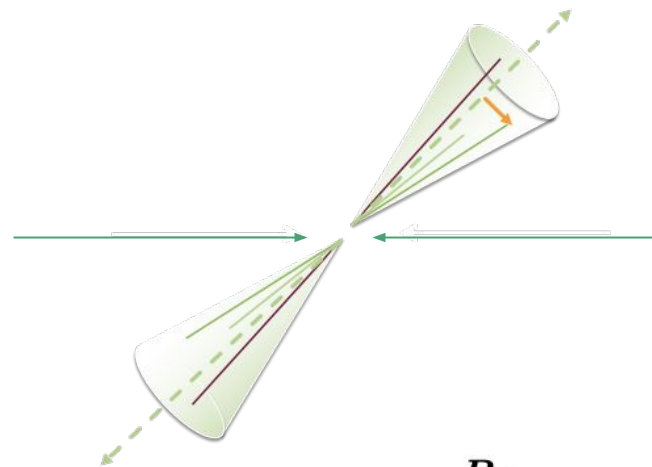
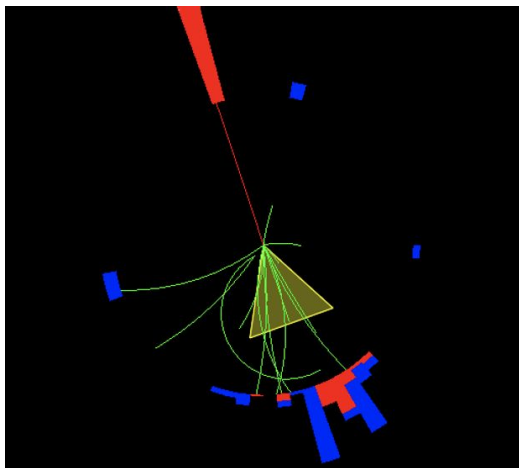
Gluon TMDs at the EIC

- Gluon TMDs are nearly unconstrained
- Can access at an EIC via
 - Quarkonium production
 - Open charm production
 - Charm jet production



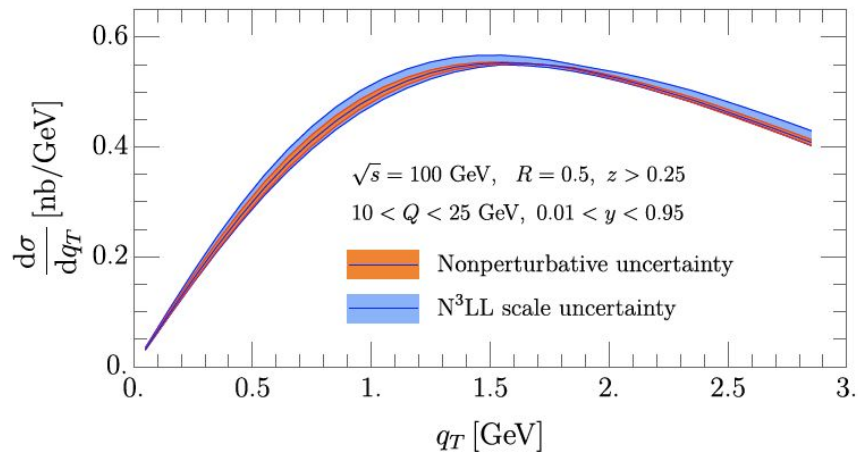
Using Jets to access TMDs

- Jets are classic collider tools
- Natural to extend to an EIC
- Jet q_T measurement probes TMD PDFs and is independent of TMD FF
- Hadron in jet measurements are sensitive to transversity + Collins



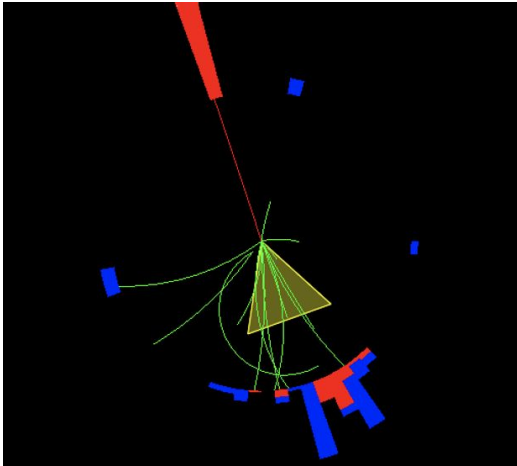
$ep \rightarrow e \text{ jet } X$

$$\mathbf{q} = \frac{\mathbf{P}_J}{z} + \mathbf{q}_{\text{in}},$$

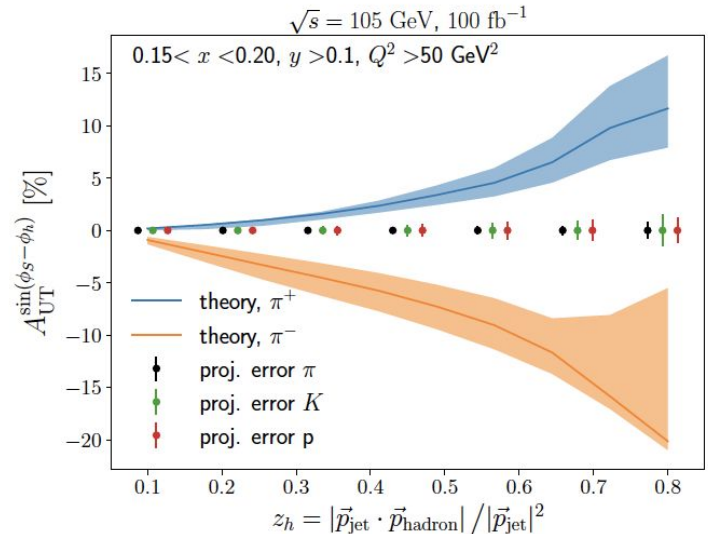
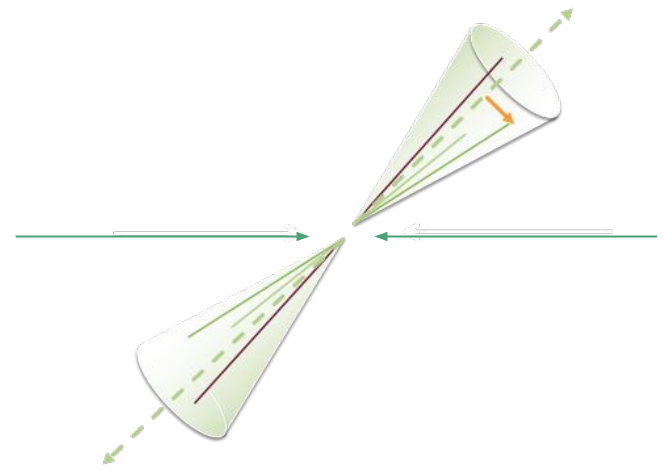


Using Jets to access TMDs

- Jets are classic collider tools
- Natural to extend to an EIC
- Jet qT measurement probes TMD PDFs and is independent of TMD FF
- Hadron in jet measurements are sensitive to transversity + Collins



Bands are current uncertainty on transversity and Collins functions. Points are projected statistical errors.



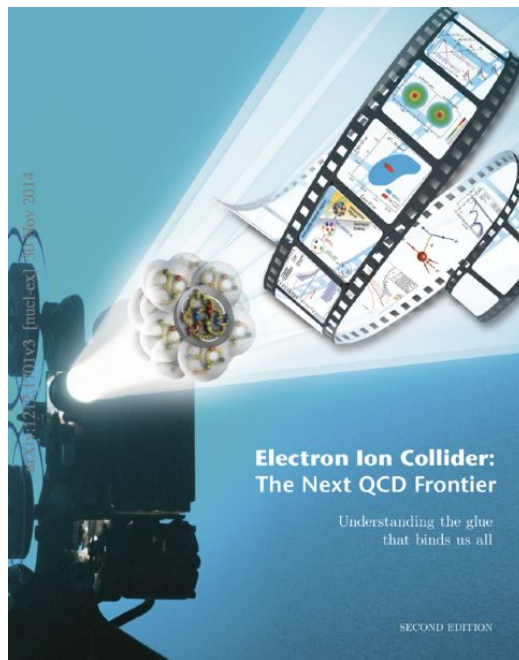
There is so much more!

I encourage you to take a look at the EIC White & Yellow papers.

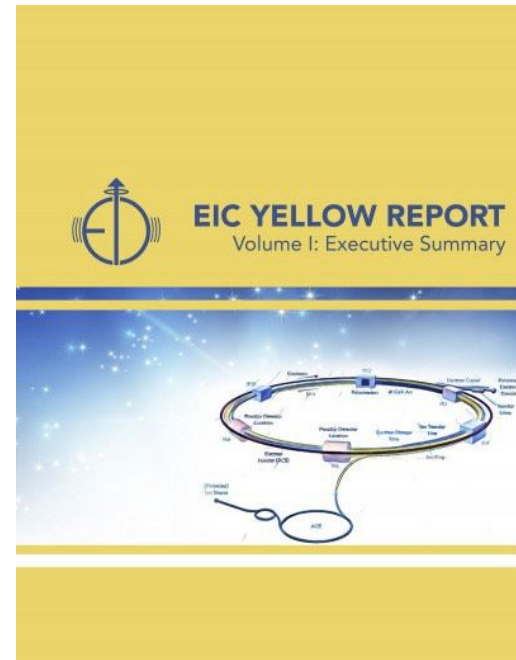
Many more topics to study:

- Origin of Proton Mass
- GPDs vis DVCS
- Nuclear PDFs
- Gluon Saturation
- Charged Lepton Flavor Violation

Thank you!



arXiv:1212:1701



arXiv:2103.05419