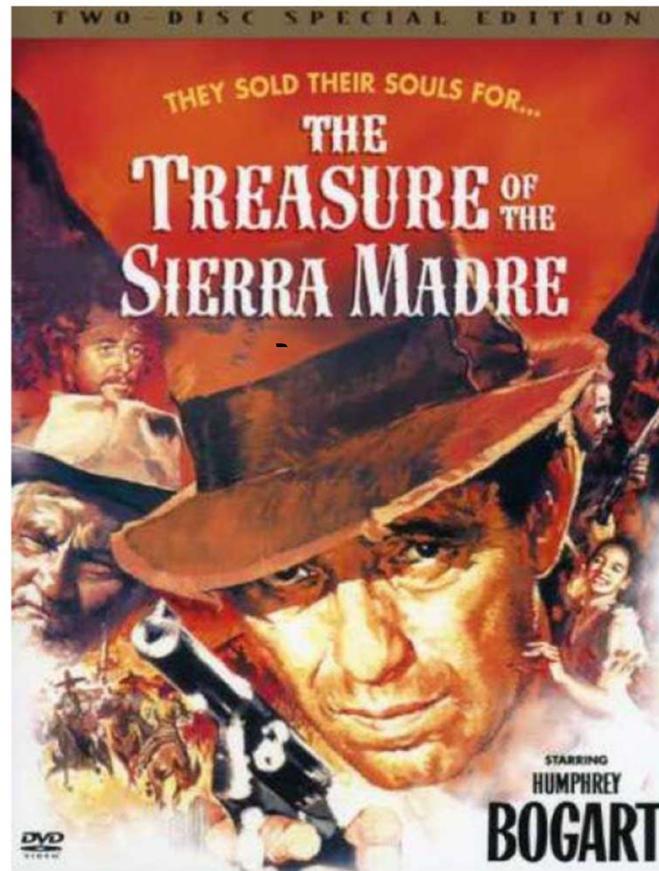


# Amarjit Soni

HET Lunch Seminar 07/17/20

- 1)[More ] Treasures from Kaons**
- 2) RPV3 & the anomalies**

# *[More] Treasures from Kaons*



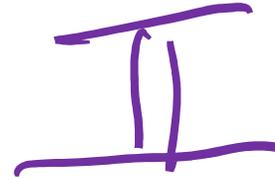
# Outline

I

- Unforgettable Memories!
- Exciting history .....
- Bagged 2 Nobels for BNL!
- Magics of  $\text{-QM-mixings-K0}$
- A very important consequence of the QM mixing: **K\_LONG...**
- Delta  $M_k$  constraints  $\Rightarrow$  stirs up flavor and CP puzzles of the SM
- Lattice BK  $\Rightarrow$  Epsilon\_K  $\Rightarrow$  precision constraints on the modern day UT fit
- Another important consequence of Delta\_mk  $\Rightarrow$  BK<sup>BSM</sup> vs BK<sub>SM</sub>

An extremely powerful tool!

# outline

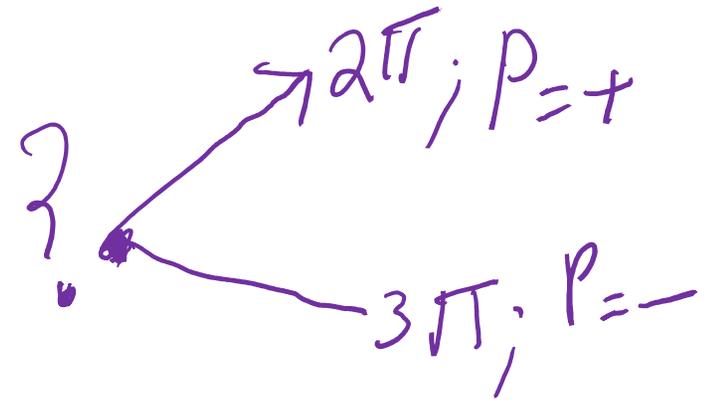


- Basics of Direct CP in  $K \Rightarrow \pi\pi$  i.e.  $\epsilon'$
- Early attempt(s), hurdles & resolution
- I. Breakthrough: Domain wall & chiral symmetric formulation
- II. Another key development: Lellouch-Lüscher method
- 1<sup>st</sup> completion ~2015 & indication of difficulty ←
- Improved stats & systematic  $\Rightarrow$  new result
- some implications
- Summary + Outlook

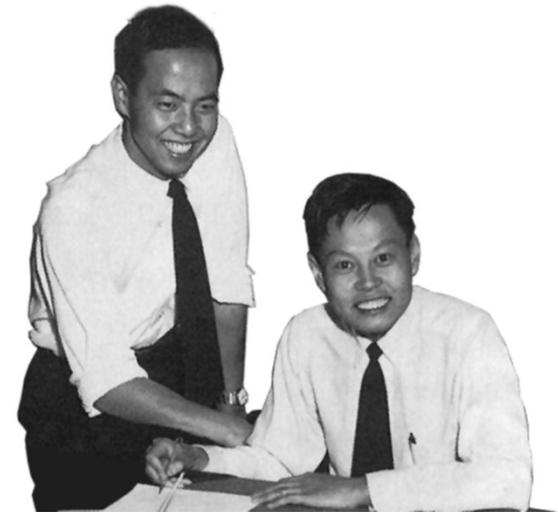
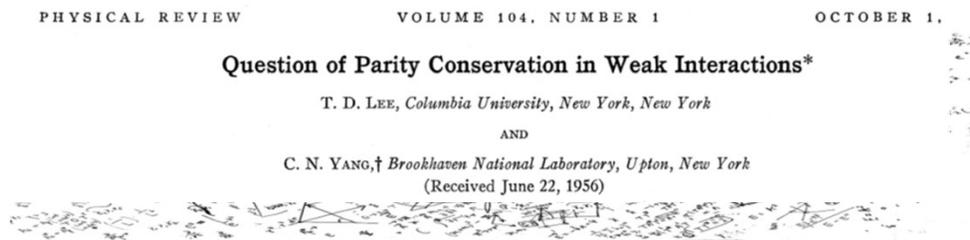
# $\Delta m_K^{\text{expt}}$ vs $\Delta m_K^{\text{theory}}$

- $\Delta m_K^{\text{expt}}$  extremely precise  $\rightarrow [3.484 \pm 0.006] \times 10^{-12}$  MeV
- $\Delta m_K^{\text{theory}}$   $\rightarrow$  part heavy NLO  
 $O(50\%)$  errors.....LD, non-local, 4-q OP as OPE is NOT valid  
 ....intermediate  $\pi\pi$  states make significant contribution.
- Historically, therefore, the very well known experimental # cannot be used as **a precision** tool for constraining SM or BSM
- RBC-UKQCD past ~5 years with new lattice methodology is working to change this situation...CU PhD students 1. JiangLei Yu 2.Ziyuan Bai , 3. Bigeng Wang [NOW] .... $\delta(\Delta m_K^{\text{theory}}) \sim O(20\%)$ .....checks underway NOW

# What an exciting history!

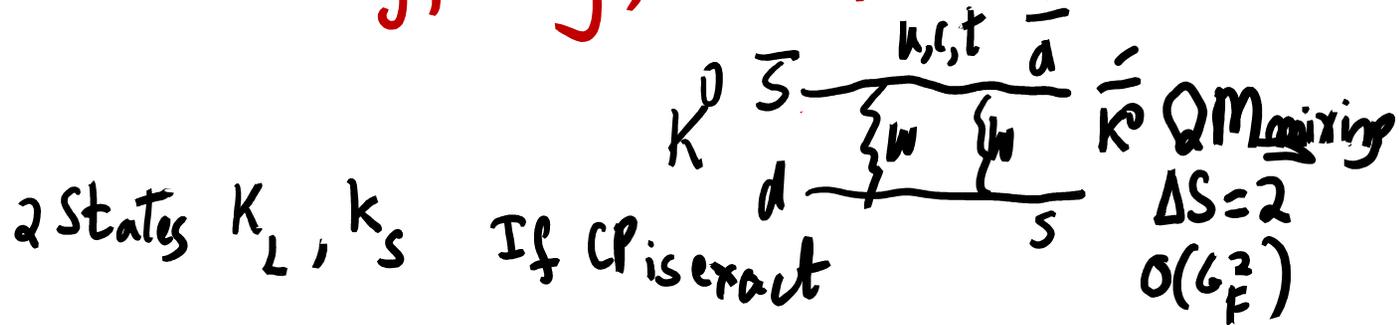


- Theta – tau puzzle.....Nature does care about L vs R
- ... the Nobel goes to Kids!



*K* decay violates P!

## II $K^0 - \bar{K}^0$ Mixing, Decay, Indirect CP violation



$$K_L \equiv \frac{K^0 - \bar{K}^0}{\sqrt{2}} \quad ; \quad K_S \equiv \frac{K^0 + \bar{K}^0}{\sqrt{2}}$$

CP-  $\rightarrow 3\pi$   
 $\not\rightarrow 2\pi$

CP+  $\rightarrow 2\pi$   
 $\not\rightarrow 3\pi$

The long life time of  $K_L$  a very important blessing; led to one of the most important discoveries in Particle Physics ie CP violation

$$\frac{\Delta m_K}{m_K} \sim 7 \times 10^{-15}$$

$$\text{But } \tau_{K_L} / \tau_{K_S} \sim O(500) \gg 1$$

$$C \tau \sim 15 \text{ nm!}$$

### III Indirect CP violation

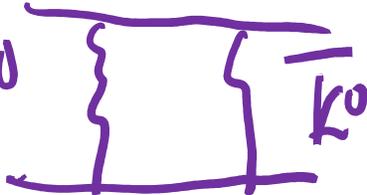
BNL 1964 Fitch, Cronin, Christensen + Turlay

NOBLE  
CRONIN  
+  
FITCH

$$\frac{A(K_L \rightarrow \pi\pi)}{A(K_S \rightarrow \pi\pi)} \neq 0 !$$

$\epsilon_K \rightarrow \sim 2.23 \times 10^{-3}$

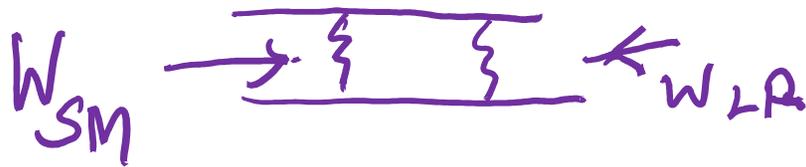


$K^0$    $\bar{K}^0$  CPV in state mixing,  $\Delta S=2$  Heff

# $\Delta m_K$ : a powerful constraint on BSM

In SM  $\Delta S=2$   $\frac{s \rightarrow d}{u, c, t \rightarrow s}$

An explicit illustration: LRSM, Beall + Baander  
+ AS PR 1982



$$\left(\frac{\Delta m_K}{m_K}\right)^{\text{expt}} \approx 10^{-14}!!$$

$$\Rightarrow m_R \gtrsim 1.6 \text{ TeV}$$

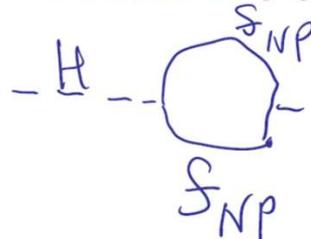
$\Rightarrow$  precision to flavor & CP problem

## MR > ~20 MW

- A remarkable story of several factors of a few all going in one direction
- Starting point was factor of O(5) from  $LXR = -2 [S+P]X[S-P]$
- Initial Black Board intuitive argument  $M_{LR} \Rightarrow \text{Const}$  as  $m_q \Rightarrow 0$  whereas  $M_{LL}$  i.e. SM  $\Rightarrow 0$  as  $m_q \Rightarrow 0$  with grad student Greg Beall in field theory class
- GB comes back later with X2 from graphs X  $\log[M_R/M_W]$ ...
- Very soon these factors pile up to O(20)
- NLO QCD enhances also  $\Rightarrow$  a PRL is born

## Outstanding Th.puzzles of our times

- Hierarchy puzzle



$$-H \text{---} \text{---} \text{---} H \text{---} \sim \frac{g_{NP}^2}{16\pi^2} \Lambda_{NP}^2 \Rightarrow \Lambda_{NP} \lesssim \text{TeV}$$

to avoid fine tuning  $m_H$

- Flavor puzzle

$\Delta \text{flavor} = 2$  e.g.



$$\sim \frac{g_{NP}^2}{\Lambda_{NP}^2} \Rightarrow \Lambda_{NP} \gtrsim 10^3 \text{ TeV}$$

to avoid constraint from  $\Delta c m_K$

"NO  
LOSE  
Thm"  
IGNORE  
FLAVOR

# The Randall-Sundrum (RS) idea

**Island Universes in Warped Space-Time**

According to string theory, our universe might consist of a three-dimensional "brane," embedded in higher dimensions. In the model developed by Lisa Randall and Raman Sundrum, gravity is much weaker on our brane than on another brane, separated from us by a fifth dimension. (Time is the unseen fourth dimension.)

**GRAVITY BRANE**  
(where gravity is concentrated)

**Fifth dimension**  
Space is warped by energy throughout five-dimensional space-time. As a result, gravity is much weaker on our brane.

**Gravitons,**  
which transmit gravity, are closed strings, which are not confined to either brane.

**Warped space-time**  
Because space-time is warped, things are exponentially bigger and lighter closer to our brane.

The ends of **open strings**, whose oscillations are particles and forces other than gravity, are stuck to our brane.

**BRANE**  
(our universe)

(Wikipedia)

[stolen from Newt+]

9/13/13 A. Soni HET-BNL

13

### Flavor structure of warped extra dimension models

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(Received 14 September 2004; published 6 January 2005)

We recently showed that warped extra-dimensional models with bulk custodial symmetry and few TeV Kaluza-Klein (KK) masses lead to striking signals at *B* factories. In this paper, using a spurion analysis, we systematically study the flavor structure of models that belong to the above class. In particular we find that the profiles of the zero modes, which are similar in all these models, essentially control the underlying flavor structure. This implies that our results are robust and model independent in this class of models. We discuss in detail the origin of the signals in *B* physics. We also briefly study other new physics signatures that arise in rare *K* decays ( $K \rightarrow \pi\nu\nu$ ), in rare top decays [ $t \rightarrow c\gamma(Z, \text{gluon})$ ], and the possibility of *CP* asymmetries in *D*<sup>0</sup> decays to *CP* eigenstates such as  $K_S\pi^0$  and others. Finally we demonstrate that with light KK masses,  $\sim 3$  TeV, the above class of models with anarchic 5D Yukawas has a “*CP* problem” since contributions to the neutron electric dipole moment are roughly 20 times larger than the current experimental bound. Using AdS/CFT correspondence, these extra-dimensional models are dual to a purely 4D strongly coupled conformal Higgs sector thus enhancing their appeal.

DOI: 10.1103/PhysRevD.71.016002

PACS numbers: 11.25.Wk, 11.30.Hv

In both cases as in SUSY-like & most BSM, the LxL of SM ΔS=2 becomes LxR-like as in LRSM leading to enhanced ME<sub>S</sub> for K-K̄



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### The little Randall–Sundrum model at the large hadron collider

“LRS”

Hooman Davoudiasl<sup>a,\*</sup>, Gilad Perez<sup>b</sup>, Amarjit Soni<sup>a</sup>

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#### ABSTRACT

We present a predictive warped model of flavor that is cut off at an ultraviolet scale  $O(10^3)$  TeV. This “Little Randall–Sundrum (LRS)” model is a volume-truncation, by a factor  $y \approx 6$ , of the RS scenario and is holographically dual to dynamics with number of colors larger by  $y$ . The LRS couplings between Kaluza–Klein states and the Standard Model fields, including the proton constituents, are explicitly calculable without *ad hoc* assumptions. Assuming separate gauge and flavor dynamics, a number of unwanted contributions to precision electroweak,  $Zb\bar{b}$  and flavor observables are suppressed in the LRS framework, compared with the corresponding RS case. An important consequence of the LRS truncation, independent of precise details, is a significant enhancement of the clean (golden) di-lepton LHC signals, by  $O(y^3)$ , due to a larger “ $\rho$ -photon” mixing and a smaller inter-composite coupling.

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### Little Randall–Sundrum models: $\epsilon_K$ strikes again

M. Bauer, S. Casagrande, L. Gründer, U. Haisch and M. Neubert  
Institut für Physik (THEP), Johannes Gutenberg-Universität, D-55099 Mainz, Germany  
(Dated: November 22, 2008)

A detailed phenomenological analysis of neutral kaon mixing in “little Randall–Sundrum” models is presented. It is shown that the constraints arising from the CP-violating quantity  $\epsilon_K$  can, depending on the value of the ultra-violet cutoff, be even stronger than in the original Randall–Sundrum scenario addressing the hierarchy problem up to the Planck scale. The origin of the enhancement is explained, and a bound  $\Lambda_{UV} > \text{several } 10^3 \text{ TeV}$  is derived, below which vast corrections to  $\epsilon_K$  are generically unavoidable. Implications for non-standard  $Z^0 \rightarrow b\bar{b}$  couplings are briefly discussed.

PACS numbers: 11.10.Kk, 12.60.-i, 12.90.+b, 13.20.Eb, 13.38.Dg

**Constraint on the Mass Scale of a Left-Right-Symmetric Electroweak Theory from the  $K_L$ - $K_S$  Mass Difference**

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and

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(Received 21 December 1981)

The  $K_L$ - $K_S$  mass difference provides a stringent constraint on the mass ( $M_R$ ) of the charged right-handed gauge field occurring in a "manifest" left-right-symmetric electroweak theory, yielding  $M_R \approx 1.6$  TeV. Taken in the context of a grand-unifying gauge theory, e.g.,  $O(10)$ , such a large bound on  $M_R$ , along with the measured value of  $\sin^2 \theta_w$ , implies that  $M_R \approx 10^9$  GeV.

PACS numbers: 12.10.Ck, 11.30.Ly, 14.80.Er

$$A_{LR}(d\bar{s} - \bar{d}s) = \left(\frac{g}{\sqrt{2}}\right)^4 \left(\frac{O_{LR}}{8\pi^2 M_R^4}\right) \sum_{i,j=u,c,t} \sum_{i',j'=u,c,t} m_i U_{is}^{R*} U_{id}^L m_j U_{js}^L U_{jd}^{R*} \times \left[ \frac{\beta \ln \beta}{(1-\beta)(\epsilon_i - \beta)(\epsilon_j - \beta)} + \frac{\epsilon_i \ln \epsilon_i}{(1-\epsilon_i)(\beta - \epsilon_i)(\epsilon_j - \epsilon_i)} + \frac{\epsilon_j \ln \epsilon_j}{(1-\epsilon_j)(\beta - \epsilon_j)(\epsilon_i - \epsilon_j)} \right], \quad (2)$$

$$O_{LR} = [\bar{\psi}_s^\alpha \gamma_5 \frac{1}{2} (1 - \gamma_5) \psi_d^\alpha] [\bar{\psi}_s^\beta \frac{1}{2} (1 + \gamma_5) \psi_d^\beta]$$

$$\frac{M_{LRM}}{M_{SM}} \sim 7.7$$

$$O_{LL} = [\bar{\psi}_s^\alpha \gamma_\mu \frac{1}{2} (1 - \gamma_5) \psi_d^\alpha] [\bar{\psi}_s^\beta \gamma^\mu \frac{1}{2} (1 - \gamma_5) \psi_d^\beta].$$

$$\mathfrak{N}_{LL} \simeq \mathfrak{N}_{LL}^{vac} = \frac{2}{3} f_K^2 m_K^2 / 2m_K.$$

← SM

(5)

To evaluate the LR contribution we also use the divergence equation  $\bar{\psi}_1 \gamma_5 \psi_2 = -i \partial_\mu (\bar{\psi}_1 \gamma^\mu \gamma_5 \psi_2) / (m_1 + m_2)$  to obtain

$$\mathfrak{N}_{LR} \simeq \mathfrak{N}_{LR}^{vac} = \frac{1}{2} [m_K^2 / (m_s + m_d)^2 + \frac{1}{6}] f_K^2 m_K^2 / 2m_K \simeq 7.7 \mathfrak{N}_{LL}^{vac},$$

7.7

(6)

⇒

← LR SM

↑  
used  $m_s = 150 \text{ meV}$   
PRL 1981-82

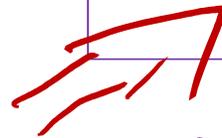
P. Boyle et al 1812.04981

the five operators  $O_i$ . In our framework we are interested only in the parity-even operators. In the so-called SUSY basis introduced in [2], the parity-even operators are,

$$\begin{aligned}
 O_1 &= (\bar{s}_a \gamma_\mu (1 - \gamma_5) d_a) (\bar{s}_b \gamma_\mu (1 - \gamma_5) d_b) \quad \Leftarrow \text{SM} \\
 O_2 &= (\bar{s}_a (1 - \gamma_5) d_a) (\bar{s}_b (1 - \gamma_5) d_b) \\
 O_3 &= (\bar{s}_a (1 - \gamma_5) d_b) (\bar{s}_b (1 - \gamma_5) d_a) \\
 O_4 &= (\bar{s}_a (1 - \gamma_5) d_a) (\bar{s}_b (1 + \gamma_5) d_b) \quad \Rightarrow \text{LRM} \\
 O_5 &= (\bar{s}_a (1 - \gamma_5) d_b) (\bar{s}_b (1 + \gamma_5) d_a).
 \end{aligned}
 \tag{1.2}$$

$$\frac{M_{\text{BSM}}}{M_{\text{SM}}}$$

$\sqrt{1/2}$



LRM is an extremely interesting extension of SM  $\Rightarrow m_2 \neq 0$

Table 3: Comparison of the results of this work in  $\overline{\text{MS}}(\mu = 3\text{GeV})$  alongside our collaboration's previous results presented in [5].

	RBC-UKQCD16[5]	This Work
$N_f =$	2+1	2+1
scheme	RI-SMOM	RI-SMOM
$R_2$	-19.48(44)(52)	-18.83(17)(55)
$R_3$	6.08(15)(23)	5.815(63)(125)
$R_4$	43.11(89)(230)	41.58(37)(119)
$R_5$	10.99(20)(88)	10.81(9)(37)

II.  $K \Rightarrow \pi\pi$ ,  $\Delta I = \frac{1}{2}$  Rule &  $\varepsilon'$

Delta I=1/2 rule (puzzle): a challenge for generations  $I=0,2$

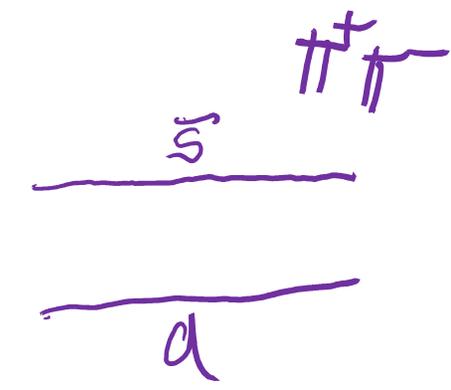
MAIN MODES

•  $K_S$

$\pi^+ \pi^-$

$\tau \sim 0.9 \times 10^{-10} \text{ s}$   
 $\Delta I = 1/2, 3/2$

$K^0$

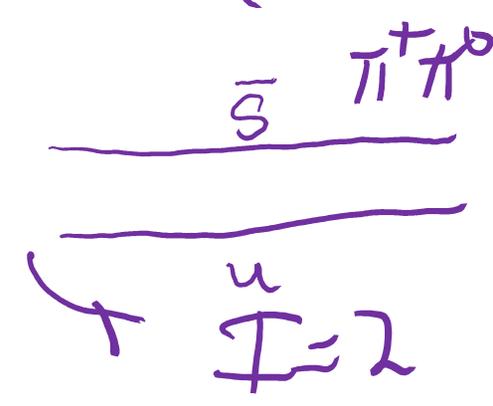


•  $K^+$

$\pi^+ \pi^0$

$\Delta I = 3/2$   
 $\sim 1.2 \times 10^{-8} \text{ s}$

$K^+$



$K_L$

$\pi^+ \pi^- \pi^0$

$\sim 5 \times 10^{-8} \text{ s}$

phase space suppressed

IV:  $\epsilon'$  /  $\epsilon$ : Direct CPV **EXPERIMENTAL ROUTE**

$$\eta_{+-} = |\eta_{+-}| e^{i\phi_{+-}} = \frac{A(K_L \rightarrow \pi^+\pi^-)}{A(K_S \rightarrow \pi^+\pi^-)}$$

$$\eta_{00} = |\eta_{00}| e^{i\phi_{00}} = \frac{A(K_L \rightarrow \pi^0\pi^0)}{A(K_S \rightarrow \pi^0\pi^0)}$$

$$\eta_{+-} = \epsilon + \epsilon', \quad \eta_{00} = \epsilon - 2\epsilon'$$

$$\epsilon' = \frac{1}{3} (\eta_{+-} - \eta_{00}) \Rightarrow 0(10^{-3}) - 0(10^{-3}) \Rightarrow 10^{-6}$$

$$\epsilon = \frac{1}{3} (2\eta_{+-} + \eta_{00})$$

10

# BSM-CP: Theoretical motivation

- To the extent that SM is not a complete theory, BSM-CP phase(s) are exceedingly likely to exist
- Adding fermions, scalars or gauge bosons as a rule entails new phase(s)
- Explicit examples: 4G SM: + 2; LRS : at least + 1; 2HDM : neutral scalar sector

as well as charged sector can have new phases; SUSY or WEXD [see e.g. Agashe, Perez & AS, PRD '04; c also Neubert et al'08; Buras et al '08] : tens of new O(1) CP-odd phases arise *naturally*

→ MORE BIT later

- SM cannot account for baryogenesis....CKM CP not enough
- Due to all of the above (and some more), searching for BSM CP-phase(s) is just about the most powerful way to look for NP....*an early realization & a driving force for past few decades*

→ not a compelling argument, *Naturalness is compelling!*

$K \rightarrow 2\pi$

$$\text{Re}\left(\frac{\epsilon'}{\epsilon}\right) = \text{Re}\left\{\frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\epsilon} \left[ \frac{\text{Im}A_2}{\text{Re}A_2} - \frac{\text{Im}A_0}{\text{Re}A_0} \right]\right\}$$

$\uparrow$   $I=2$        $\uparrow$   $I=0$

Use lattice to calculate 6 quantities:  
 ReA0, ReA2 known from expt;  $\delta_0, \delta_2$  via  
 ChPT etc.. So very good checks;  
 ImA, ImA2 unknown

$\omega \equiv \text{Re}A_2 / \text{Re}A_0$   
 $\sim 0.045$

Indirect CP

$|\epsilon| = 2.228(11) \times 10^{-3}$

$\text{Re}(\epsilon'/\epsilon) = 1.65(26) \times 10^{-3}$

DIRECT CP

$\epsilon' \ll \epsilon$        $\epsilon' \sim 10^{-6}!$

## A.S. in Proceedings of Lattice '85 (FSU)..1<sup>st</sup> Lattice meeting ever attended

The matrix elements of some penguin operators control in the standard model another CP violation parameter, namely  $\epsilon'/\epsilon$ .<sup>6,8)</sup> Indeed efforts are now underway for an improved measurement of this important parameter.<sup>10)</sup> In the absence of a reliable calculation for these parameters, the experimental measurements, often achieved at tremendous effort, cannot be used effectively for constraining the theory. It is therefore clearly important to see how far one can go with MC techniques in alleviating this old but very difficult

**With C. Bernard  
[UCLA]**

HET-Lunch-071720

Serves as a template for the need of Lattice calculations for more economical use of almost all experimental data  
From IF



ODE to YESTERYEARS!

## ***MOTHER of all (lattice) calculations to date: A Personal Perspective***

- Calculation  $K \Rightarrow \pi$  &  $\epsilon'$  were the reasons I went into lattice over 1/3 of a century ago!
- 9 + (3 new) PhD thesis: Terry Draper (UCLA'84), George Hockney(UCLA'86), Cristian Calin (Columbia=CU'01), Jack Laiho(Princeton'04), Sam Li(CU'06), Matthew Lightman(CU'09), Elaine Goode(Southampton'10), Qi Liu(CU'12), Daiqian Zhang(CU'15)+ [new ones starting from CU, U Conn and Southampton] + many PD's & junior facs.. obstacles & challenges (and of course "mistakes"!) ad infinitum.....

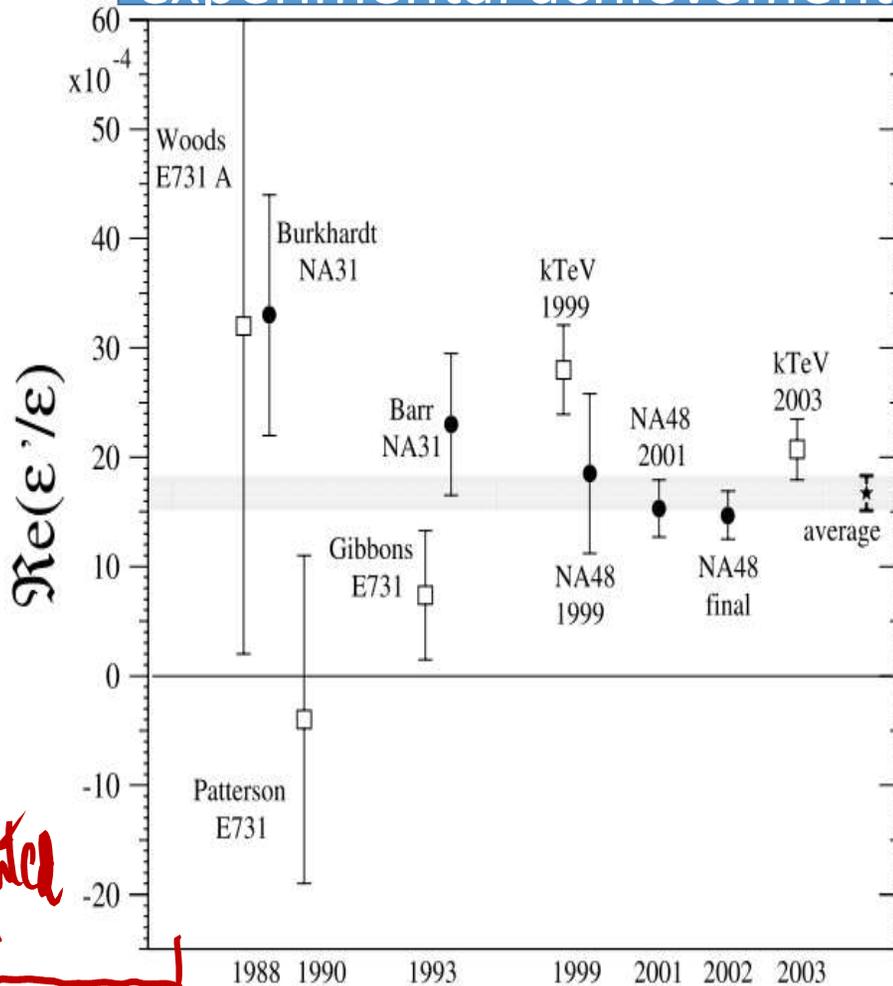
Tianle WANG,  
Dan Hoying

A key point to emphasize is that overcoming  
each major obstacle led to significant  
application to phenomenology and/or lattice  
**[necessity is the parent of.....]**

# EXTREMELY valuable inputs from countless:

- **Fred Gilman and Mark Wise**
- **Andrzej Buras et al**
- **Guido Martinelli et al**
- **Yigal Shamir**
- **Laurent Lellouch + Martin Luscher**
- .....
- .....
- .....

A monumental experimental achievement!



Komrad  
kleinknecht  
"Uncertainty CPV"

$16.6(2.3) \times 10^{-4}$   
PDG 2014

LATTICE  
WORK STARTED

# *Basic calculational framework*

$\Delta S=1 H_W$

W L b NLO

Buchalla, Buras, Lautenbacher  
RMP 196; Cirigliani et al 95

$$H_W = \frac{G_F}{\sqrt{2}} V_{us}^* V_{ud} \sum_{i=1}^{10} [z_i(\mu) + \tau y_i(\mu)] Q_i(\mu).$$

$m_i = \langle k | Q_i | \pi \pi \rangle$   
Needed

$$\tau = -V_{ts}^* V_{td} / V_{us}^* V_{ud}$$

to all orders in  $L_S$

Station

Tree

$$Q_1 = (\bar{s}_\alpha d_\alpha)_L (\bar{u}_\beta u_\beta)_L,$$

$$Q_2 = (\bar{s}_\alpha d_\beta)_L (\bar{u}_\beta u_\alpha)_L,$$

$$Q_3 = (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\beta)_L,$$

$$Q_4 = (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\alpha)_L,$$

$$Q_5 = (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\beta)_R,$$

$$Q_6 = (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} (\bar{q}_\beta q_\alpha)_R,$$

$$Q_7 = \frac{3}{2} (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\beta)_R,$$

$$Q_8 = \frac{3}{2} (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\alpha)_R,$$

$$Q_9 = \frac{3}{2} (\bar{s}_\alpha d_\alpha)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\beta)_L,$$

$$Q_{10} = \frac{3}{2} (\bar{s}_\alpha d_\beta)_L \sum_{q=u,d,s} e_q (\bar{q}_\beta q_\alpha)_L,$$

QCDP

$I=0 \Rightarrow$

$\rightarrow 0$   
 $m_q \rightarrow 0$

$\rightarrow \text{const}$   
 $m \rightarrow 0$

$\frac{S M_d}{e_g}$   
 $\frac{S M_u}{e_g}$   
QCDP

$\frac{S M_d}{e_g}$   
 $\frac{S M_u}{e_g}$   
EWP

EWP

$I=2$

## Why EWK cannot be neglected: 3 Reasons

- Despite  $\alpha_{\text{QED,EWK}} \ll \alpha_{\text{QCD}}$ , EWK contributions are extremely important and CANNOT be neglected:
- EWK are (8,8) and QCD are (8,1), and (8,8) go to constant whereas (8,1) vanish in the chiral limit
- EWK, i.e. those due Z exch have Wilson coeff that go as  $mt^2/mW^2$

• In  $\mathcal{E}'$  they enter as  $\overset{\text{EWP}}{\left[ \frac{\text{Im}A_2}{\text{Re}A_2} - \frac{\text{Im}A_0}{\text{Re}A_0} \right]}$   $\overset{\text{QCDP}}{\rightarrow}$

$$\frac{\text{Re}A_0}{\text{Re}A_2} \sim 22$$

small  $\leftarrow$

$\rightarrow$  large

## Why EWK cannot be neglected: 3 Reasons

- Despite  $\alpha_{\text{QED,EWK}} \ll \alpha_{\text{QCD}}$ , EWK contributions are extremely important and CANNOT be neglected:
- EWK are (8,8) and QCD are (8,1), and (8,8) go to constant whereas (8,1) vanish in the chiral limit
- EWK, i.e. those due Z exch have Wilson coeff that go as  $mt^2/mW^2$

• In  $\mathcal{E}'$  they enter as  $\overset{\text{EWP}}{\left[ \frac{\text{Im}A_2}{\text{Re}A_2} - \frac{\text{Im}A_0}{\text{Re}A_0} \right]}$   $\overset{\text{QCDP}}{\rightarrow}$

$\frac{\text{Re}A_0}{\text{Re}A_2} \sim 22$

small  $\leftarrow$

$\rightarrow$  large

For simplicity: 1st strategy via ChPT

PHYSICAL REVIEW D

VOLUME 32, NUMBER 9

1 NOVEMBER 1985

Application of chiral perturbation theory to  $K \rightarrow 2\pi$  decays

LEFFT

BDS PW-85

Claude Bernard, Terrence Draper,\* and A. Soni

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Department of Physics, California Institute of Technology, Pasadena, California 91125

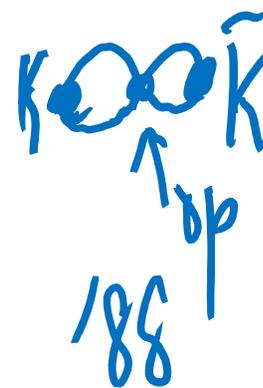
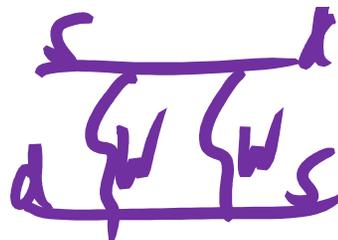
(Received 3 December 1984)

Chiral perturbation theory is applied to the decay  $K \rightarrow 2\pi$ . It is shown that, to quadratic order in meson masses, the amplitude for  $K \rightarrow 2\pi$  can be written in terms of the unphysical amplitudes  $K \rightarrow \pi$  and  $K \rightarrow 0$ , where 0 is the vacuum. One may then hope to calculate these two simpler amplitudes with lattice Monte Carlo techniques, and thereby gain understanding of the  $\Delta I = \frac{1}{2}$  rule in  $K$  decay. The reason for the presence of the  $K \rightarrow 0$  amplitude is explained: it serves to cancel off unwanted renormalization contributions to  $K \rightarrow \pi$ . We make a rough test of the practicability of these ideas in Monte Carlo studies. We also describe a method for evaluating meson decay constants which does not require a determination of the quark masses.

12/20/2017

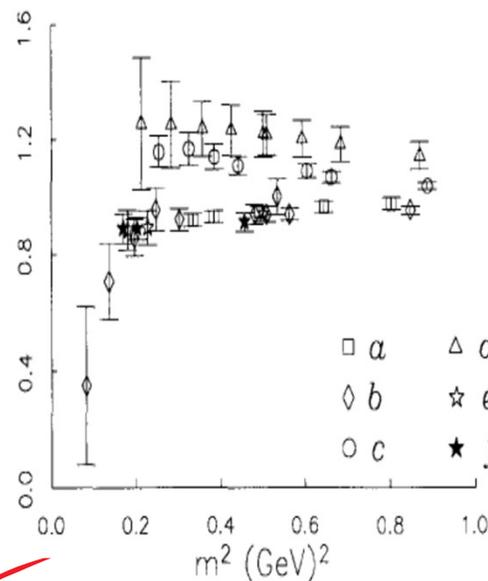
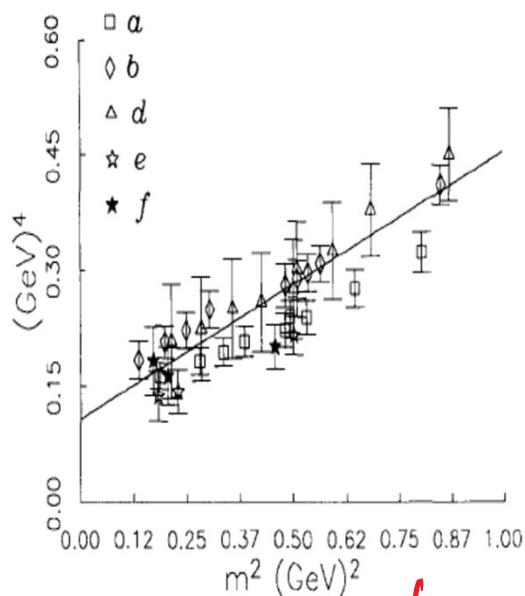
USED extensively on lattice for ~20 years  $\Rightarrow$  NLD J. LAIHO PhD Thesis ~ '03

$$\langle \pi | (\bar{s} \gamma_{\mu} d)^2 | \bar{K} \rangle$$



162

C. Bernard, A. Soni / Weak matrix elements on the lattice



$\chi S$  violation by  $K-\bar{K} \Rightarrow$  FINE TUNING PROBLEM

**Lattice computation of the decay constants of B and D mesons**

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James N. Labrenz  
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Amarjit Soni  
*Department of Physics, Brookhaven National Laboratory, Upton, New York 11973*  
(Received 1 July 1993)

PHYSICAL REVIEW D

VOLUME 45, NUMBER 3

1 FEBRUARY 1992

**Lattice study of semileptonic decays of charm mesons into vector mesons**

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Aida X. El-Khadra  
*Theory Group, Fermi National Accelerator Laboratory, P.O. Box 500, Batavia, Illinois 60510*

Amarjit Soni  
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(Received 30 September 1991)

We present our lattice calculation of the semileptonic form factors for the decays  $D \rightarrow K^*$ ,  $D_s \rightarrow \phi$ , and  $D \rightarrow \rho$  using Wilson fermions on a  $24^3 \times 39$  lattice at  $\beta=6.0$  with 8 quenched configurations. For  $D \rightarrow K^*$ , we find for the ratio of axial form factors  $A_1(0)/A_0(0) = 0.70 \pm 0.16$ . Results for other form factors and ratios are also given.

**PIONEERING WORKS leading to modern Day UT**

12/20/2017

IMSC; HE

**Semileptonic decays on the lattice: The exclusive  $0^-$  to  $0^-$  case**

Claude W. Bernard\*  
*Institute for Theoretical Physics, University of California, Santa Barbara, California 93106*

Aida X. El-Khadra  
*Theory Group, Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, Illinois 60510*

Amarjit Soni  
*Institute for Theoretical Physics, University of California, Santa Barbara, California 93106*  
*and Department of Physics, Brookhaven National Laboratory, Upton, New York 11973*  
(Received 21 December 1990)

PHYSICAL REVIEW D, VOLUME 58, 014501

**SU(3) flavor breaking in hadronic matrix elements for  $B-\bar{B}$  oscillations**

*Later SMs CDF, DCP*

C. Bernard  
*Department of Physics, Washington University, St. Louis, Missouri 63130*

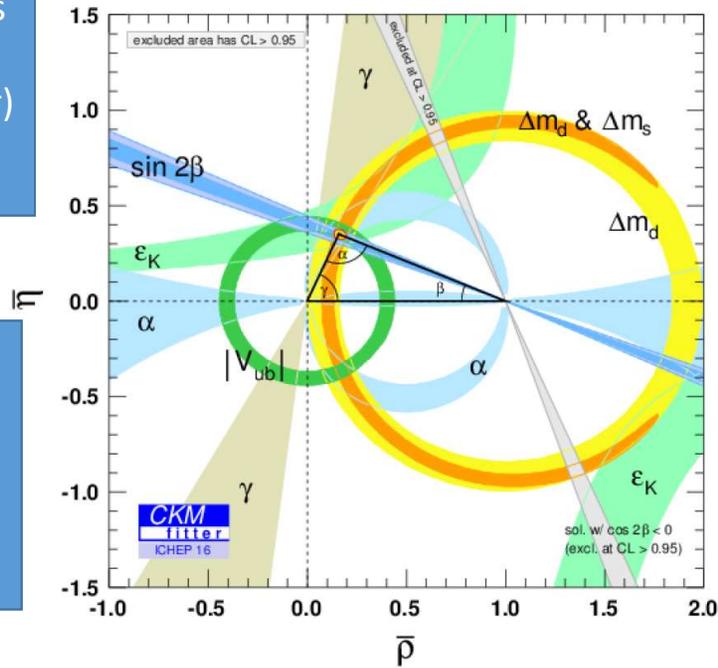
T. Bhuni and A. Soni  
*Department of Physics, Brookhaven National Laboratory, Upton, New York 11973*  
(received 28 January 1998; published 5 May 1998)

Use exptal data + lattice WME to test SM & search for new physics

<http://ckmfitter.in2p3.fr>  
 see also <http://www.utfit.org>

Looks great; but looks  
 can be deceiving...  
 In fact at level of  $O(2\sigma)$   
 tension(s) exist

$O(10-15\%)$  new  
 physics is possible  
 and is HUGE!



Latt      Expt

$f_B$        $\Delta m_B$

$\frac{f_{B_s}}{f_B} \dots \frac{\Delta m_{B_s}}{\Delta m_B}$

$f(\vec{v}) / f_0(\vec{v}) \rightarrow B \text{ or } \pi$

$B_K > \epsilon_K$

---

$\Delta m_K$  NOT used

### QCD with domain wall quarks

T. Blum\* and A. Soni†

Department of Physics, Brookhaven National Laboratory, Upton, New York 11973

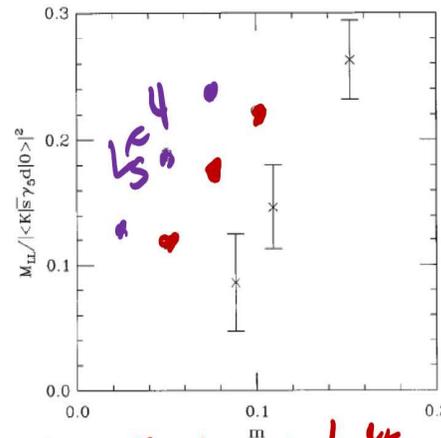
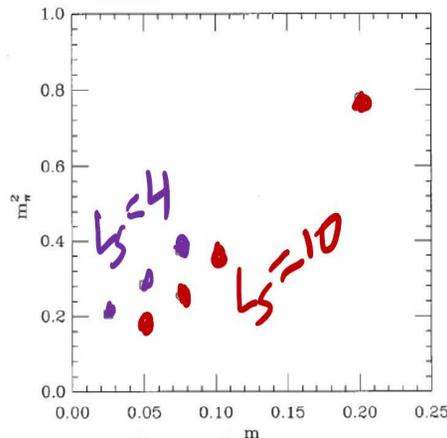
(Received 27 November 1996)

Two key papers

1st Simulation with DWQ

9th '97

We present lattice calculations in QCD using Shamir's variant of Kaplan fermions which retain the continuum  $SU(N)_L \times SU(N)_R$  chiral symmetry on the lattice in the limit of an infinite extra dimension. In particular, we show that the pion mass and the four quark matrix element related to  $K_0-\bar{K}_0$  mixing have the expected behavior in the chiral limit, even on lattices with modest extent in the extra dimension, e.g.,  $N_5=10$ . [S0556-2821(97)00113-6]



Excellent Chiral Symmetry with ~10 sites in 5th dim.

12/20/2017

MAJOR BREAK THROUGH FOR K-PI Lattice Calculations

i.e. NoChPT

CMP / OI.  
a new method

another major  
development  
for  $K \rightarrow K\pi$   
on lattice

Direct  $K \rightarrow \pi\pi$  (a la Lellouch-Luscher), using finite  
volume correlation\* functions, [i.e. w/o  
ChPT] RBC initiates around 2006

CONTINUED BY RBC-UKQCD (mostly) Edinburgh -  
Southampton

\* Allows to bypass Maini-Testa theorem

COMMON interest: use of DWA for simulations

# Relating lattice ME to physical amplitudes

$$A_{2/0} = F \frac{G_F}{\sqrt{2}} V_{ud} V_{us} \sum_{i=1}^{10} \sum_{j=1}^7 \left[ \left( z_i(\mu) + \tau y_i(\mu) \right) Z_{ij}^{\text{lat} \rightarrow \overline{\text{MS}}} M_j^{\frac{3}{2}/\frac{1}{2}, \text{lat}} \right]$$

F is the Lellouch-Luscher factor which relates finite volume ME to the infinite volume

$$A = \frac{1}{\pi q} \sqrt{\frac{\partial \phi}{\partial q} + \frac{\partial \delta}{\partial q}} \sqrt{m_K} E_{\pi\pi} L^{2/3} M$$

A/M is LL factor F

$$q = \frac{pL}{2\pi}$$

$$\hookrightarrow \propto \frac{\delta}{L} \text{ for small } p$$

$\phi$  is a somewhat complicated function of  $q$  and boundary Conditions [See Daiqian Zhang thesis]

12/20/2017

IMSC; HET-BNL;soni

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RBC-UKQCD  
PRL 2015

Results for  
 $\epsilon'$

- Using  $\text{Re}(A_2)$  and  $\text{Re}(A_0)$  from experiment and our lattice value for  $\text{Im}(A_2)$  and  $\text{Im}(A_0)$  and the phase shifts  $\delta_2$  and  $\delta_0$

*EWP*  
*QCDP*  
*orig. Central Value*

$$\text{Re} \left( \frac{\epsilon'}{\epsilon} \right) = \text{Re} \left\{ \frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\epsilon} \left[ \frac{\text{Im}A_2}{\text{Re}A_2} - \frac{\text{Im}A_0}{\text{Re}A_0} \right] \right\}$$

LARGE CANCELLATION!!

RBC-UKQCD PRL'15  
EDITOR'S CHOICE

$$= 1.38(5.15)(4.43) \times 10^{-4},$$

$$16.6(2.3) \times 10^{-4}$$

Bearing in mind the largish errors in this first calculation, we interpret that our result are consistent with experiment at  $\sim 2\sigma$  level



$$\omega = \frac{\text{Re}A_2}{\text{Re}A_0} \sim 0.145$$

with expt  
Computed  $\text{Re}A_0$  good agreement with expt  
Offered an "explanation" of the Delta I=1/2 enhancement

# A UNIQUE ASPECT OF THIS CALCULATION

- **REAL  $A_0$ , the strong phase ( $\delta_0$ ) and Im  $A_0$  are being calculated simultaneously from 1<sup>st</sup> principles in the same calculation**
- **Re  $A_0$  is also known from EXPERIMENT...& strong phase deduced via ChPT + expt**
- **So those provide a powerful check [amongst many] of what we are doing**
- **If a non-perturbative calculation of Im $A_0$  and of  $\epsilon_{\text{ps}}$ ' is done w/o also calculating Re $A_0$  &  $\delta_0$  in the same framework, then its repercussions for  $\epsilon_{\text{ps}}$ ' (in the very least) raises questions.**

# A possible difficulty: strong phases

- The continuum and our lattice determinations of strong phase

differ

$$\phi_{\epsilon'} = \delta_2 - \delta_0 + \frac{\pi}{2} = \begin{cases} (42.3 \pm 1.5)^\circ & \text{RBC [2]} \\ (54.6 \pm 5.8)^\circ & \text{RBC [47, 48]} \end{cases}$$

*Colangelo et al  
ChPT etc*

*RBC-UKQCD*

*OK*  $\rightarrow$  *off by  $\approx 2\sigma \Rightarrow$  a concern*

## Statistics increase C Kedy / LAT / 18

- Original goal was a 4x increase in statistics over 216 configurations used in 2015 analysis.
- 4x reduction in configuration generation time obtained via algorithmic developments (exact one-flavor implementation) → D Murphy
- Large-scale programme performed involving many machines:

SCs  
over  
3  
continents

Source	Determinant computation	Independent configs.
Blue Waters	RHMC	34+18+4+3
KEKSC	RHMC	106
BNL	RHMC	208
DiRAC	RHMC	151
KEKSC	EOFA	275+215
BNL	EOFA	245
		1259 total

- Measurements performed using IBM BG/Q machines at BNL and the Cori computer (Intel KNL) at NERSC largely complete.
- Including original data, now have 6.7x increase in statistics!

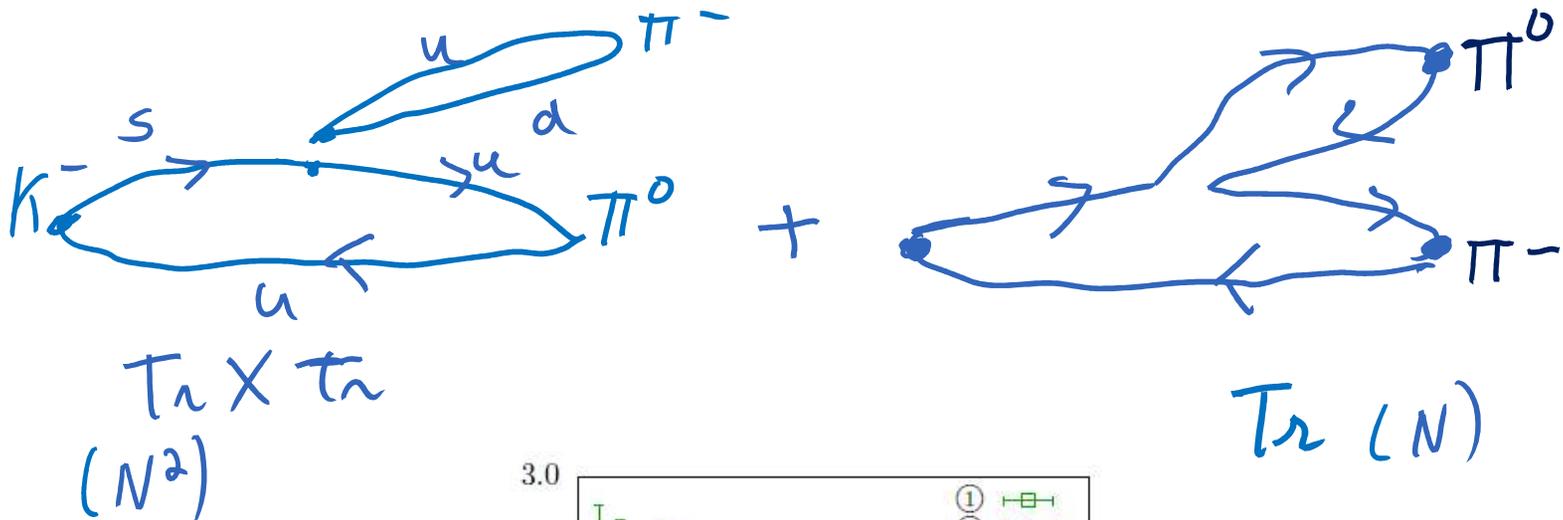
NOW  $\approx 14409.6$

## Implications for $K \rightarrow \pi\pi$ and resolution

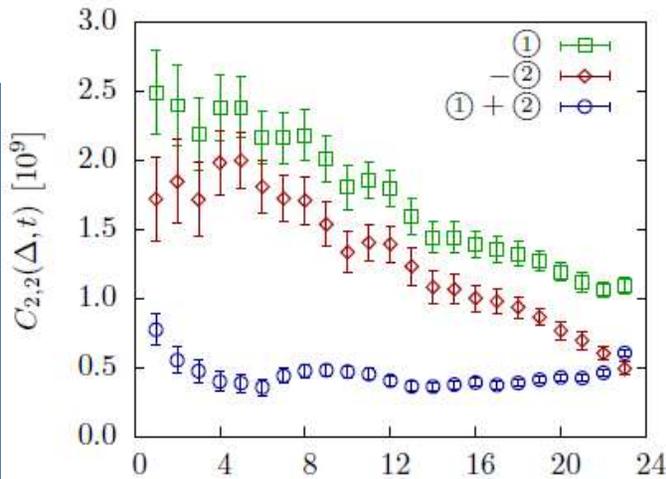
- Despite vast increase in statistics, *this second state cannot be resolved from the time dependence using only a single  $\pi\pi$  operator.*
- Possibly a significant underestimate of excited state systematic error in  $K \rightarrow \pi\pi$  calculation that can only be resolved by adding additional operators.
- In response we have **expanded the scope of the calculation:**
  - Added  $K \rightarrow \sigma$  matrix elements
  - Added  $K \rightarrow \pi\pi$  matrix element of new  $\pi\pi$  operator with larger relative pion momenta (still  $p_{\text{CM}}=0$ )
- Result is **3x increase in the number of  $l=0$   $\pi\pi$  operators in  $K \rightarrow \pi\pi$  calc.**
- Also added  $\pi\pi$  2pt functions with non-zero total  $\pi\pi$  momenta.  
Calculate phase shift at several (smaller) additional center-of-mass energies.
  - Additional points that can be compared to dispersive result / experiment
  - **Improve ~11% systematic** on Lellouch-Luscher factor associated with slope of phase shift.
- Currently have 152 measurements with new operators! *Adding ~100/month*

# Unravelling the $\Delta I=1/2$ rule

Dissecting (the much easier)  $\Delta I=3/2$  [ $I=2$   $\pi\pi$ ] Amp on the lattice: 2 contributing topologies only

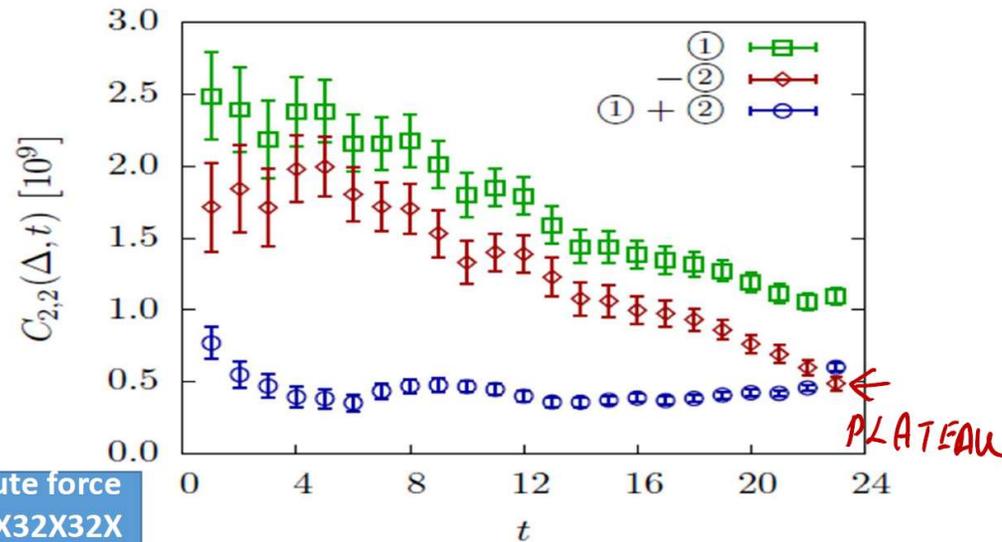


Simplest basic step is significantly different from phenomenological expectations!



DRAMATIC CANCELLATION!  
( $m_\pi \approx 140$  MeV)

RBC-UKQCD PRL 2012: Unravelling the origin of the textbook Delta I=1/2 Puzzle: Unnatural (“accidental”) suppression of ReA2 at  $m_{\pi} \sim 140$  MeV



Brute force  
32X32X32X  
64X16

FIG. 2: Contractions (1), -(2) and (1) + (2) as functions of  $t$  from the simulation at physical kinematics and with  $\Delta = 24$ .

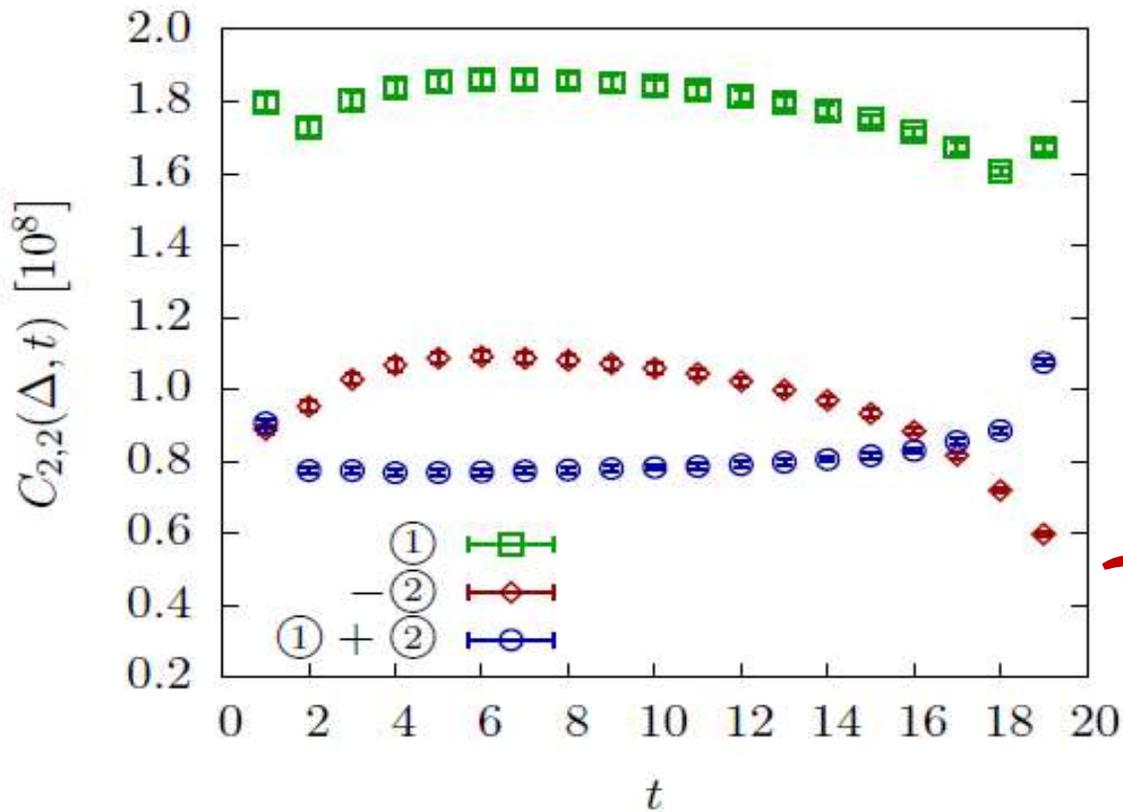
QCDOC 10 Tf

12/20/2017

IMSC; HET-BNL;soni

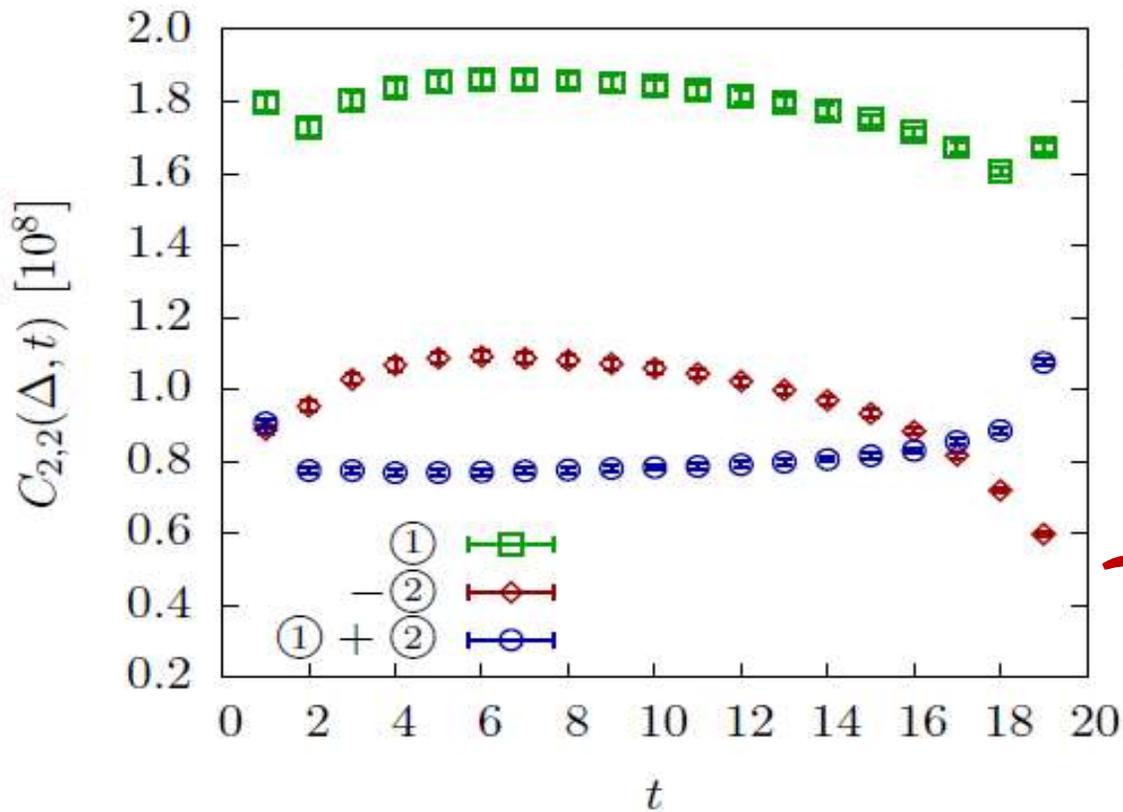
96

UNLIKE WHAT TEXT BOOKS SAY, INFAC T NAÏVE  
FACTORIZATION FAILS IN I=2 K=> 2 pi decays



For heavier  $\pi$ ,  
 $m_\pi \sim 330 \text{ MeV}$   
 less cancellation  
 bet.  $N^2$  &  $N$   
 Large  $N$  begins  
 to improve!

FIG. 3: Contractions ①, -② and ① + ② as functions of  $t$  from the simulation at threshold with  $m_\pi \simeq 330 \text{ MeV}$  and  $\Delta = 20$ .



For heavier  $\pi$ ,  
 $m_\pi \sim 330 \text{ MeV}$   
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 bet.  $N^2$  &  $N$   
 Large  $N$  begins  
 to improve!

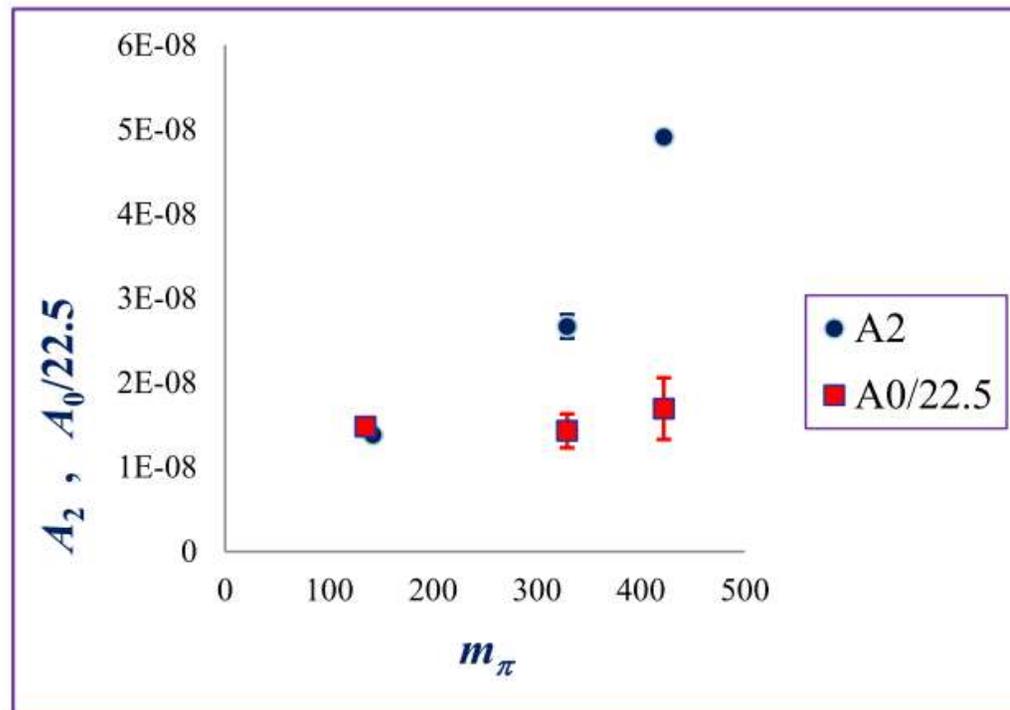
FIG. 3: Contractions ①, -② and ① + ② as functions of  $t$  from the simulation at threshold with  $m_\pi \simeq 330 \text{ MeV}$  and  $\Delta = 20$ .

Because of mass dependent cancellation

$\text{Re}A_2$  changes with  $m_\pi$  dramatically.

$\text{Re}A_0$  is mild

## Compare $A_2$ and $A_0/22.5$



NHCE  
KITP,  
Aug 15

# Net effect

- **This large cancellation between  $N^2$  and  $N$  [ $N=3$ , for QCD] leads to a reduction in  $\text{ReA2}$  compared to “naïve expectations” by a factor of about 4 to 5 in the original effect of around 22.5**
- **Then there is a factor of 2 to 3 from renorm...=> bringing the total to [8 to 15] of the needed 22.5**
- **The remaining factor of  $\sim$  [ 1.5 to 2.8] ... comes from  $\text{ReA0}$  over “naïve expectations”**

## More on A0

$$Q_2 \equiv \overline{s} \gamma_\mu d \overline{u} \gamma^\mu u$$

- Another important fact about  $\text{Re } A_0$  is that at a scale of  $\sim 1.3$  GeV or more, the contribution from penguin operators,  $Q_3, Q_4, Q_5, Q_6$ , is negligibly small.
- Indeed,  $\sim 85\%$  of  $\text{Re } A_0$  originates at these scales from  $Q_2$  which is just the original Weak interaction 4-q operator:  $[\overline{s} \gamma_\mu d] X [\overline{u} \gamma^\mu u]$ , which originates from integrating out the W-boson.
- The essential moral is that if you take the original weak interaction 4q operator and non-perturbatively compute its matrix element between K to  $\pi \pi$  in the  $I=0$  channel then it accounts for most ( $\sim 85\%$ ) of  $\text{Re } A_0$ .....
- Lastly, but equally importantly, it should be stressed that the SVZ-penguin operator  $Q_6$  is in fact the dominant contributor to  $\text{Im } A_0$ .

Im A0 &  $\epsilon'$

arXiv:  
2004,  
09440



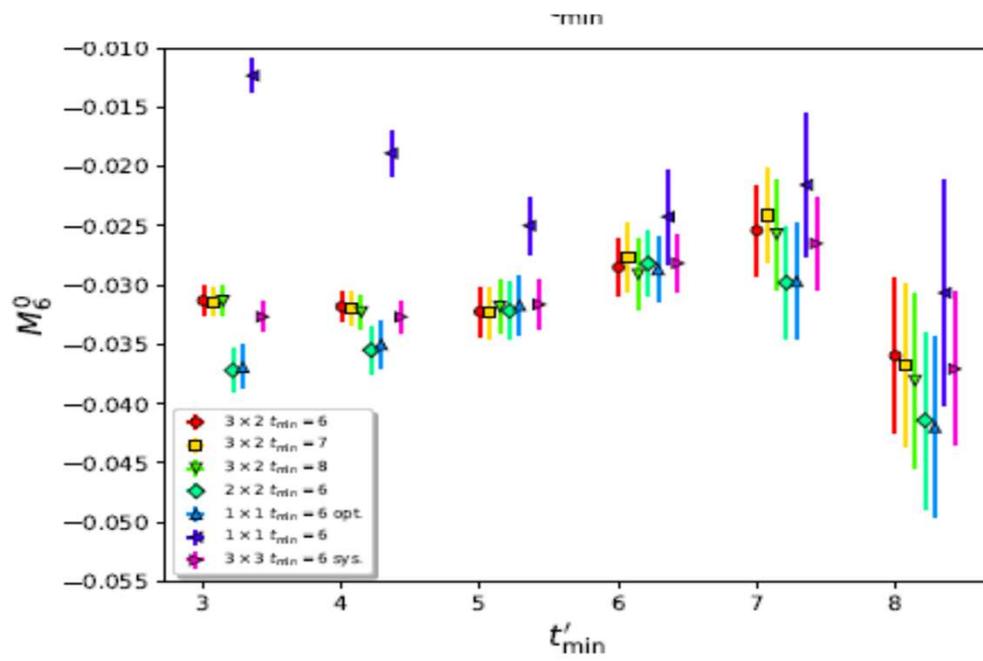
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RBL-  
UKQCD  
2020

Parameter	Value	
	2-state fit	3-state fit
Fit range	6-15	4-15
$A_{\pi\pi(111)}^0$	0.3682(31)	0.3718(22)
$A_{\pi\pi(311)}^0$	0.00380(32)	0.00333(27)
$A_{\sigma}^0$	-0.0004309(41)	-0.0004318(42)
$E_0$	0.3479(11)	0.35030(70)
$A_{\pi\pi(111)}^1$	0.1712(91)	0.1748(67)
$A_{\pi\pi(311)}^1$	-0.0513(27)	-0.0528(30)
$A_{\sigma}^1$	0.000314(17)	0.000358(13)
$E_1$	0.568(13)	0.5879(65)
$A_{\pi\pi(111)}^2$	—	0.116(29)
$A_{\pi\pi(311)}^2$	—	0.063(10)
$A_{\sigma}^2$	—	0.000377(94)
$E_2$	—	0.94(10)
p-value	0.314	0.092

TABLE III: Fit parameters in lattice units and the p-values for multi-operator fits to the  $I=0$   $\pi\pi$  two-point functions. Here  $E_i$  are the energies of the states and  $A_{\alpha}^i$  represents the matrix element of the operator  $\alpha$  between the state  $i$  and the vacuum, given in units of  $\sqrt{1 \times 10^{13}}$ . The second column gives the parameters for our primary fit which uses two-states and three operators. The third column shows a fit with the same three operators and one additional state that is used to probe the systematic effects of this third state on the  $K \rightarrow \pi\pi$  matrix element fits.





7-ops.

10-ops.

i	SMOM( $\not{q}, \not{q}$ ) (GeV <sup>3</sup> )	SMOM( $\gamma^\mu, \gamma^\mu$ ) (GeV <sup>3</sup> )	$\overline{\text{MS}}$ via SMOM( $\not{q}, \not{q}$ ) (GeV <sup>3</sup> )	$\overline{\text{MS}}$ via SMOM( $\gamma^\mu, \gamma^\mu$ ) (GeV <sup>3</sup> )
1	0.060(39)	0.059(38)	-0.107(22)	-0.093(18)
2	-0.125(19)	-0.106(16)	0.147(15)	0.143(14)
3	0.142(17)	0.128(14)	-0.086(61)	-0.053(44)
4	-	-	0.185(53)	0.200(40)
5	-0.351(62)	-0.313(48)	-0.348(62)	-0.311(48)
6	-1.306(90)	-1.214(82)	-1.308(90)	-1.272(86)
7	0.775(23)	0.790(23)	0.769(23)	0.784(23)
8	3.312(63)	3.092(58)	3.389(64)	3.308(63)
9	-	-	-0.117(20)	-0.114(19)
10	-	-	0.137(22)	0.123(19)

TABLE XIV: Physical, infinite-volume matrix elements in the SMOM( $\not{q}, \not{q}$ ) and SMOM( $\gamma^\mu, \gamma^\mu$ ) schemes at  $\mu = 4.006$  GeV given in the 7-operator chiral basis, as well as those converted perturbatively into the  $\overline{\text{MS}}$  scheme at the same scale in the 10-operator basis. The errors are statistical only.

2 schemes

$Q_i$

$\text{Re} A_0$

$\text{Im} A_0$

59

i	$\text{Re}(A_0)$		$\text{Im}(A_0)$	
	$(\not{q}, \not{q}) (\times 10^{-7} \text{ GeV})$	$(\gamma^\mu, \gamma^\mu) (\times 10^{-7} \text{ GeV})$	$(\not{q}, \not{q}) (\times 10^{-11} \text{ GeV})$	$(\gamma^\mu, \gamma^\mu) (\times 10^{-11} \text{ GeV})$
1	0.383(77)	0.335(64)	0	0
2	2.89(30)	2.81(28)	0	0
3	0.0081(58)	0.0050(42)	0.20(14)	0.12(10)
4	0.081(23)	0.088(17)	1.24(35)	1.34(27)
5	0.0380(68)	0.0339(53)	0.552(99)	0.492(77)
6	-0.410(28)	-0.398(27)	-8.78(60)	-8.54(57)
7	0.001863(56)	0.001900(56)	0.02491(75)	0.02540(75)
8	-0.00726(14)	-0.00708(13)	-0.2111(40)	-0.2060(39)
9	$-8.7(1.5) \times 10^{-5}$	$-8.5(1.4) \times 10^{-5}$	-0.133(22)	-0.128(21)
10	$2.37(38) \times 10^{-4}$	$2.13(32) \times 10^{-4}$	-0.0304(49)	-0.0273(41)
Total	2.99(32)	2.86(31)	-7.15(66)	-6.93(64)

TABLE XVIII: The contributions of each of the ten four-quark operators to  $\text{Re}(A_0)$  and  $\text{Im}(A_0)$  for the two different RI-SMOM intermediate schemes. The scheme and units are listed in the column headers. The errors are statistical, only.

Error source	Value
Excited state	-
Unphysical kinematics	5%
Finite lattice spacing	12%
Lellouch-Lüscher factor	1.5%
Finite-volume corrections	7%
Missing $G_1$ operator	3%
Renormalization	4%
Total	15.7%

TABLE XXV: Relative systematic errors on the infinite-volume matrix elements of  $\overline{\text{MS}}$ -renormalized four-quark operators  $Q_j$ .

Systematic errors

Re  $A_0$   
 $\downarrow$   
 $\sim 20\%$

Error source	Value	
	Re( $A_0$ )	Im( $A_0$ )
Matrix elements	15.7%	15.7%
Parametric errors	0.3%	6%
Wilson coefficients	12%	12%
Total	19.8%	20.7%

Im  $A_0$   
 $\downarrow$   
 $\sim 20\%$

TABLE XXVI: Relative systematic errors on  $\text{Re}(A_0)$  and  $\text{Im}(A_0)$ .

Quantity	Value
$\text{Re}(A_0)$	$2.99(0.32)(0.59) \times 10^{-7} \text{ GeV}$
$\text{Im}(A_0)$	$-6.98(0.62)(1.44) \times 10^{-11} \text{ GeV}$
$\text{Re}(A_0)/\text{Re}(A_2)$	19.9(2.3)(4.4)
$\text{Re}(\epsilon'/\epsilon)$	0.00217(26)(62)(50)

*Done I B  
See full pages*

TABLE I: A summary of the primary results of this work. The values in parentheses give the statistical and systematic errors, respectively. For the last entry the systematic error associated with electromagnetism and isospin breaking is listed separately as a third error contribution.

IB+EM effects.....not yet from  
lattice

We use

$$\frac{\epsilon'}{\epsilon} = \frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\epsilon} \left[ \frac{\text{Im}(A_2)}{\text{Re}(A_2)} - \frac{\text{Im}(A_0)}{\text{Re}(A_0)} \right]$$

→ isospin sym formula.

→  $\omega(17 \pm 9.1) \times 10^{-2}$

IB + EM eff

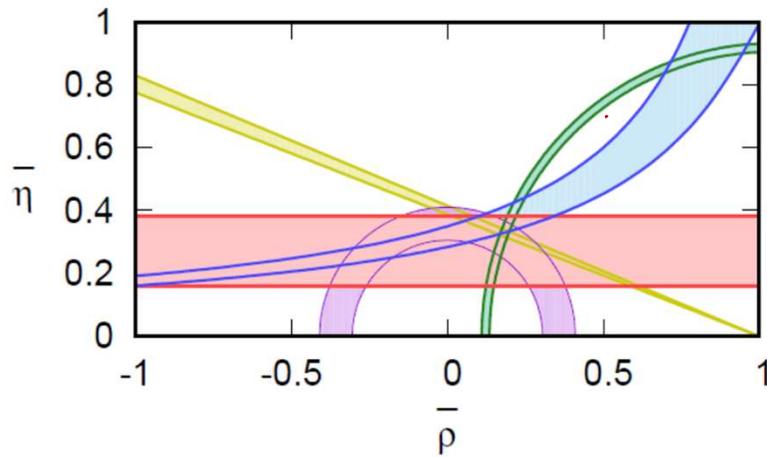


$$\frac{\epsilon'}{\epsilon} = \frac{i\omega_+ e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\epsilon} \left[ \frac{\text{Im}(A_2^{\text{emp}})}{\text{Re}(A_2^{(0)})} - \frac{\text{Im}(A_0^{(0)})}{\text{Re}(A_0^{(0)})} (1 - \hat{\Omega}_{\text{eff}}) \right]$$

See Cirigliano et al 1911.01359

THIS IS NOT our  $\omega_K$

WE CHOOSE to include THIS in our system



$\Delta M_s / \Delta M_d$  (green)  
 $\epsilon_K + |V_{cb}|$  (light blue)  
 $\sin 2\beta$  (yellow)  
 $|V_{ub}/V_{cb}|$  (purple)  
 $\epsilon'$  (pink)

→ current systematic ~ 35%  
 Aim to reduce this  
 in N3 MATO ~ 15%

FIG. 12: The horizontal-band constraint on the CKM matrix unitarity triangle in the  $\bar{\rho} - \bar{\eta}$  plane obtained from our calculation of  $\epsilon'$ , along with constraints obtained from other inputs [6, 70, 71]. The error bands represent the statistical and systematic errors combined in quadrature. Note that the band labeled  $\epsilon'$  is historically (e.g. in Ref. [72]) labeled as  $\epsilon'/\epsilon$ , where  $\epsilon$  is taken from experiment.

# *Naturalness: an important consideration*

*A firm believer in naturalness*

- **Used to be OSCILL8 (through the 80's while @UCLA)**

# Implications for NP & Naturalness

DRAWING STRONG CONCLUSIONS  
BASED ON 20% tests is  
TOO RISKY!

& Too Premature

OR 35%!

## A lesson from history (I)

"A special search at Dubna was carried out by E. Okonov and his group. They did not find a single  $K_L \rightarrow \pi^+ \pi^-$  event among 600 decays into charged particles [12] (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the Lab. The group was unlucky."

-Lev Okun, "The Vacuum as Seen from Moscow"

1964:  $BF = 2 \times 10^{-3}$

A failure of imagination? Lack of patience?

CHRISTENSEN,  
CANNON, FITCH  
& TURLAY  
BNL 1964

scalars'13; 9/13/13 A. Soni HET-BNL

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# Icing on the cake

**Direct CP violation and the  $\Delta I = 1/2$  rule in  $K \rightarrow \pi\pi$  decay from the  
Standard Model**

R. Abbott,<sup>1</sup> T. Blum,<sup>2,3</sup> P.A. Boyle,<sup>4,5</sup> M. Bruno,<sup>6</sup> N.H. Christ,<sup>1</sup>  
D. Hoying,<sup>3,2</sup> C. Jung,<sup>4</sup> C. Kelly,<sup>4</sup> C. Lehner,<sup>7,4</sup> R.D. Mawhinney,<sup>1</sup>  
D.J. Murphy,<sup>8</sup> C.T. Sachrajda,<sup>9</sup> A. Soni,<sup>4</sup> M. Tomii,<sup>2</sup> and T. Wang<sup>1</sup>

(RBC and UKQCD Collaborations)

<sup>1</sup>*Physics Department, Columbia University, New York, NY 10027, USA*

<sup>2</sup>*Physics Department, University of Connecticut, Storrs, CT 06269-3046, USA*

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<sup>5</sup>*SUPA, School of Physics, The University of Edinburgh, Edinburgh EH9 3JZ, UK*

<sup>6</sup>*Theoretical Physics Department, CERN, 1211 Geneve 23, Switzerland*

<sup>7</sup>*Universität Regensburg, Fakultät für Physik, 93040, Regensburg, Germany*

<sup>8</sup>*Center for Theoretical Physics, Massachusetts Institute of Technology, Boston, MA 02139, USA*

<sup>9</sup>*School of Physics and Astronomy, University of Southampton, Southampton SO17 1BJ, UK*

(Dated: April 21, 2020)

arXiv:2004.09440v1 [hep-lat] 20 Apr 2020

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Report of the Referee -- DS12692/Abbott  
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In their manuscript "Direct CP violation ...", Abbott et al present a new lattice calculation of the real and imaginary parts of the isospin 0,  $K \rightarrow \pi\pi$  amplitude,  $A_0$ . Combined with earlier results for the  $I=2$  amplitude,  $A_2$ , this calculation allows the authors to present new results for  $\epsilon'$ , the measure of direct CP-violation in  $K \rightarrow \pi\pi$  decays, and for the  $\Delta I=1/2$  enhancement ratio,  $\text{Re } A_0/\text{Re } A_2$ .

This is an impressive piece of work presented in a beautifully written manuscript. The paper reports on a hugely challenging lattice QCD calculation which is a near culmination of decades of developments and innovations from members of the team, as well as from the larger lattice QCD community. Its results also represent a landmark for particle physics: the first controlled calculation, in the standard model, of  $\epsilon'/\epsilon$ , whose measurement was evidence of direct CP violation and took over 20 years of experimental ingenuity to establish at the level of 5 standard deviations; the confirmation of their 2015 work on the standard model origin of the  $\Delta I=1/2$  enhancement.

The authors should also be highly commended for clearly debugging the result of their 2015 work on the same subject, and for showing how the many improvements which they have implemented allow them to get a much better handle on systematic errors. In that work, the team published a result for  $\text{Im } A_0$  that is 2.2 combined standard deviations (including possibly double counted errors) or 3.7 times smaller than the result presented here. They also had presented a result for the  $I=0$ ,  $\pi\pi$ -scattering phase shift,  $\delta_0^0$ , that is 1.6 combined standard deviations (including possibly double counted errors) smaller. While their 2015 results displayed some tension with experiment, their new result for  $\epsilon'/\epsilon$ , with a 40% error, and for  $\delta_0^0$ , with a 6% error, no longer do. The main aspect which is missing for this calculation to claim a full control over systematic errors is one, preferably two, finer lattices spacings for the matrix element calculations as well as a continuum limit for the step scaling.

Nonetheless, given the conservative errors on their final results, I can only very strongly recommend the publication of this manuscript in Physical Review D.

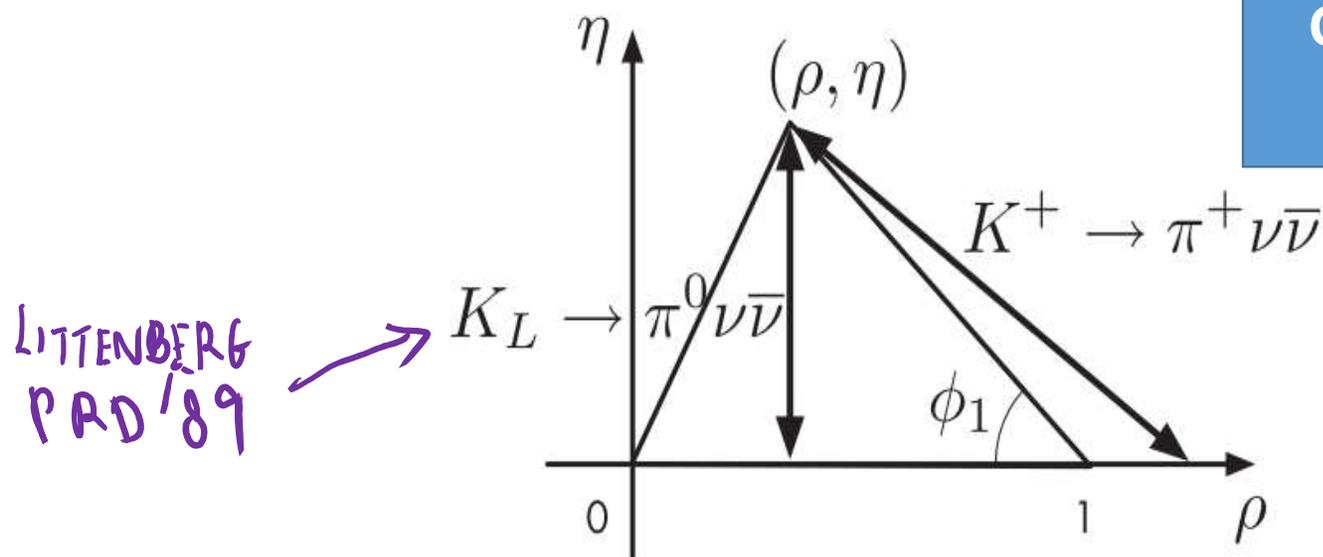
Relate to  $K_L \Rightarrow \pi^0 \nu \nu$ ;  $K^+$ ;  $\epsilon$ ,  $\epsilon'$  .....

- WIP with E Lunghi

# K-UT: A dream for some

Blucher, Winstein and Yamanaka '09; see also Buras

Construction of a Kaon UT



LITTENBERG  
PRD '89

Lehner+Luighi+AS  
PLB '2016

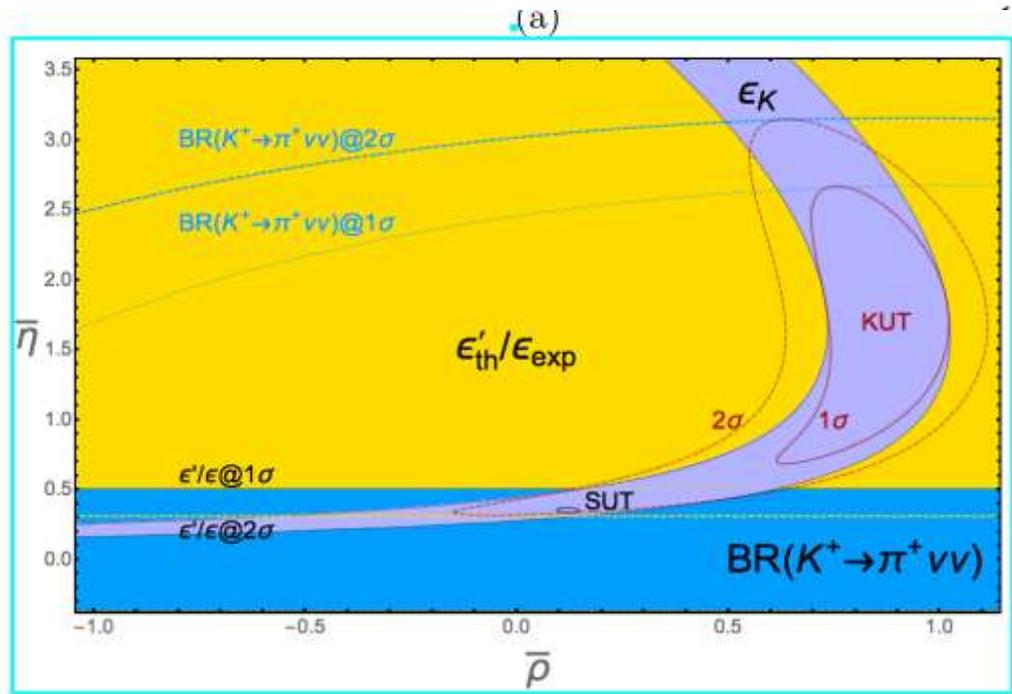
Fig. 14. Unitarity triangle.

Instead of [ $\sigma$  in addition to]  $K_L \rightarrow \pi^0 \nu \bar{\nu}$  can now plan on using  $\epsilon'/\epsilon$

Sketch of an emerging K-UT: 3 key Kaonic inputs

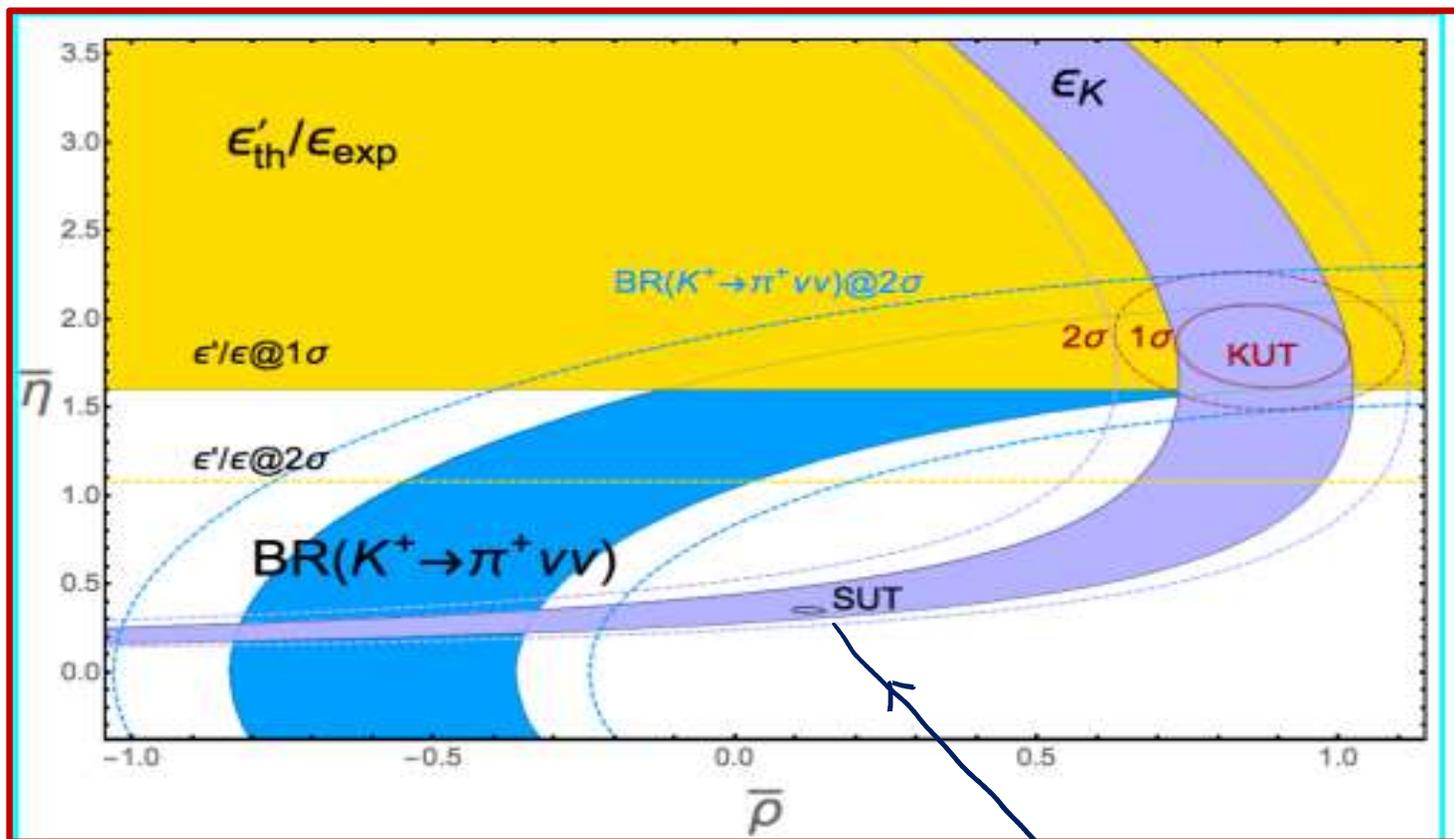
I  $\epsilon_K$  induced CP

II 
$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \begin{cases} (8.64 \pm 0.60) \times 10^{-11} & \text{SM} \\ (17.3^{+11.5}_{-10.5}) \times 10^{-11} & \text{E949 BNL} \end{cases}$$



III 
$$\text{Re} \left( \frac{\epsilon'}{\epsilon} \right)_K = \begin{cases} (16.7 \pm 1.6) \times 10^{-4} & \text{PDG 2015} \\ (1.36 \pm 5.21_{\text{stat}} \pm 4.49_{\text{syst}}) \times 10^{-4} & \text{ABC+UK(ACD)'15} \end{cases}$$

# POSSIBLE KUT CIRCA 2020: DUE NA62 + RBC-UKQCD



NO unique  
 $\rho, \eta$

Assumed: NA62, 100 events with  $\sim 7\%$  error  
RBC-UKQCD,  
 $\delta(\text{Im}A_0) \sim 18\%$   
[current  $\sim 60\%$ ]

Lehner, Lunghi + AS PLB'16

IMSC; HET-BNL;soni

"Standard" (B) UT

# Summary + Outlook

1 of 2 pages

- **After decades of effort, overcoming major hurdles, using DWQ with essentially continuum-like fermions along with improved renormalization methodology, cutting edge statistical analysis and algorithmic advances, RBC-UKQCD is presenting an updated result on  $SM\text{-}\epsilon_s' \sim 21.7(26)(62)(50) \times 10^{-4}$  which is compatible [within errors] with the measured value  $16.6(2.3) \times 10^{-4}$**
- **Bearing in mind that this is an extremely treacherous calculation loaded with numerous avenues of errors and oversights, an independent calculation has been in process for about  $\sim 3$  years within RBC-UKQCD. This effort is led by Tom Blum with (then g.s.) Dan Hoyer/Masaaki Tomii, U Conn-BNL, Taku Izubuchi et al. This path uses PBC unlike the currently finished result which used GPBC...we hope to have 1<sup>st</sup> results from PBC in  $\sim 2$  years.**
- **Also GPBC effort will be continued at other lattice spacing(s)**

# Summary + Outlook

- **Lattice efforts to incorporate IB + EM effects are being studied but have some ways to go before they can tackle  $K \Rightarrow \pi\pi$  and  $\epsilon\pi'$**
- **With physical pions, kaons and such first glance at lattice ChPT is quite encouraging, see RBC-UKQCD, David Murphy et al 2015 and DM, PhD thesis, Columbia Univ**
- **This begs the question that much simpler path could now be used via BDSPW [LO ChPT] and/or L+S [NLOChPT] to address  $\epsilon\pi'$ ...This could be tens of times simpler though at some cost in accuracy.....all this needs to be studied...Mattia Bruno, Christoph Lehner + AS et al**
- **Hope to have an improved result on  $\epsilon\pi'$  with  $O(15\%)$  errors in  $\sim 3$  years**

# EXTRAS

RBC

RIKEN-BNL Research Center

B = BNL-HET  
C = Columbia

The RBC & UKQCD collaborations

BNL and BNL/RBRC

Yasumichi Aoki (KEK)  
Taku Izubuchi  
Yong-Chull Jang  
Chulwoo Jung  
Meifeng Lin  
Aaron Meyer  
Hiroshi Ohki  
Shigemi Ohta (KEK)  
Amarjit Soni

UC Boulder

Oliver Witzel

CERN

Mattia Bruno

Columbia University

Ryan Abbot  
Norman Christ  
Duo Guo  
Christopher Kelly  
Bob Mawhinney  
Masaaki Tomii  
Jiqun Tu

Bigeng Wang  
Tianle Wang  
Yidi Zhao

University of Connecticut

Tom Blum  
Dan Hoying (BNL)  
Luchang Jin (RBRC)  
Cheng Tu

Edinburgh University

Peter Boyle  
Luigi Del Debbio  
Felix Erben  
Vera Gülpers  
Tadeusz Janowski  
Julia Kettle  
Michael Marshall  
Fionn Ó hÓgáin  
Antonin Portelli  
Tobias Tsang  
Andrew Yong  
Azusa Yamaguchi

UAM Madrid

Julien Frison

University of Liverpool

Nicolas Garron

MIT

David Murphy

Peking University

Xu Feng

University of Regensburg

Christoph Lehner (BNL)

University of Southampton

Nils Asmussen  
Jonathan Flynn  
Ryan Hill  
Andreas Jüttner  
James Richings  
Chris Sachrajda

Stony Brook University

Jun-Sik Yoo  
Sergey Syritsyn (RBRC)

UKQCD Subgroups that  
of UKQCD that uses  
D W @  
Edinburgh  
Southampton

**UDCSTBGZ      Has been since '89 (while @ BNL)**

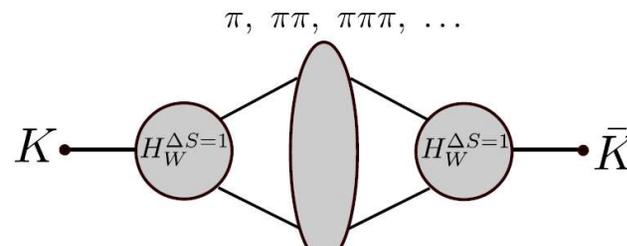
CKM '18

- Neutral kaon mixing induced by 2<sup>nd</sup> order weak processes gives rise to mass difference between  $K_L$  and  $K_S$

$$\Delta M_K = 2 \sum_n \frac{\langle \bar{K}^0 | H_W | n \rangle \langle n | H_W | K^0 \rangle}{M_K - E_n}$$

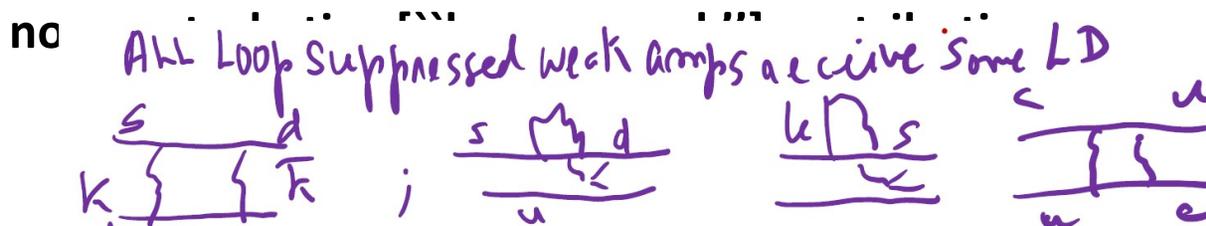
B. Wang @  
LAT '18

- FCNC → highly suppressed in SM due to GIM mechanism:  $\Delta m_K = 3.483(6) \times 10^{-12}$  MeV small and highly sensitive to new BSM FCNC.
- PT calc using weak EFT with  $\Delta S=2$  eff. Hamiltonian (charm integrated out) dominated by  $p \sim m_c$ : poor PT convergence at charm scale → **~36% PT sys error.**
- PT calc neglects **long-distance effects** arising when 2 weak operators separated by distance  $\sim 1/\Lambda_{\text{QCD}}$ .
- Use lattice to evaluate matrix element of product of  $H_W^{\Delta S=1, \text{eff}}$  directly:

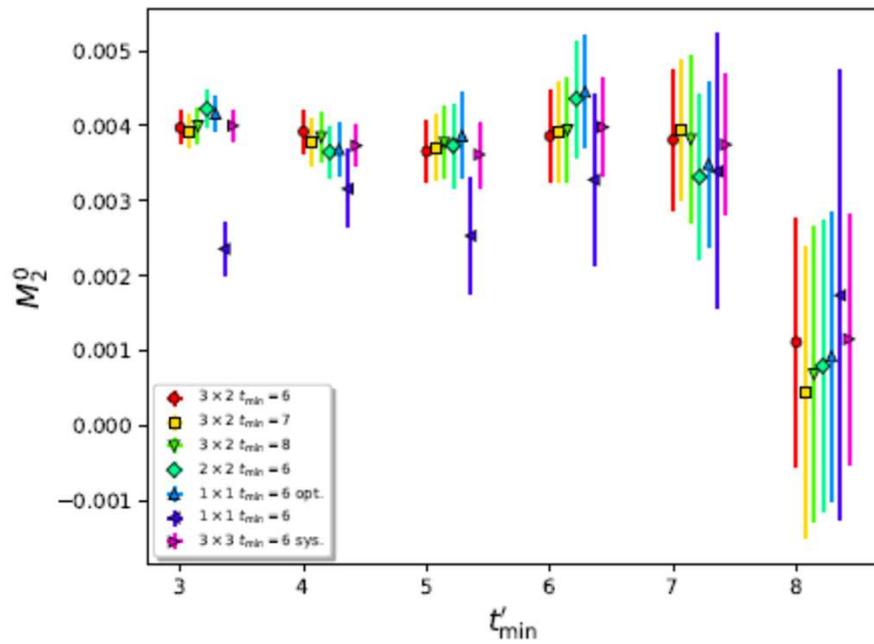


# Remarks

- In the past ~6 years, RBC-UKQCD developed methods for extended applications of Lellouch-Lusher method to 2 insertions of the weak operator for tackling non-local matrix elements [NLME]
- **ALL** loop suppressed transitions in the SM receive some



- $\Delta m_K$  extremely sensitive to BSM 'cause as a rule they contain [unlike SM] non-(V-A)<sup>2</sup>; see Beall, Bander, AS PRL'82 => 1<sup>st</sup> target of our effort for NLME has been therefore  $\Delta m_K$
- Pert. Theory @ NNLO [see Brod + Gorbahn, PRL 2012] estimates ~40% LD contamination; not reliable as NLO estimates [Herrlich + Nierste] were about the same...may well be indicating poor convergence of pert. Theory.



Quantity	Value
$\text{Re}(A_0)$	$2.99(0.32)(0.59) \times 10^{-7} \text{ GeV}$
$\text{Im}(A_0)$	$-6.98(0.62)(1.44) \times 10^{-11} \text{ GeV}$
$\text{Re}(A_0)/\text{Re}(A_2)$	$19.9(2.3)(4.4)$
$\text{Re}(\epsilon'/\epsilon)$	$0.00217(26)(62)(50)$

TABLE I: A summary of the primary results of this work. The values in parentheses give the statistical and systematic errors, respectively. For the last entry the systematic error associated with electromagnetism and isospin breaking is listed separately as a third error contribution.

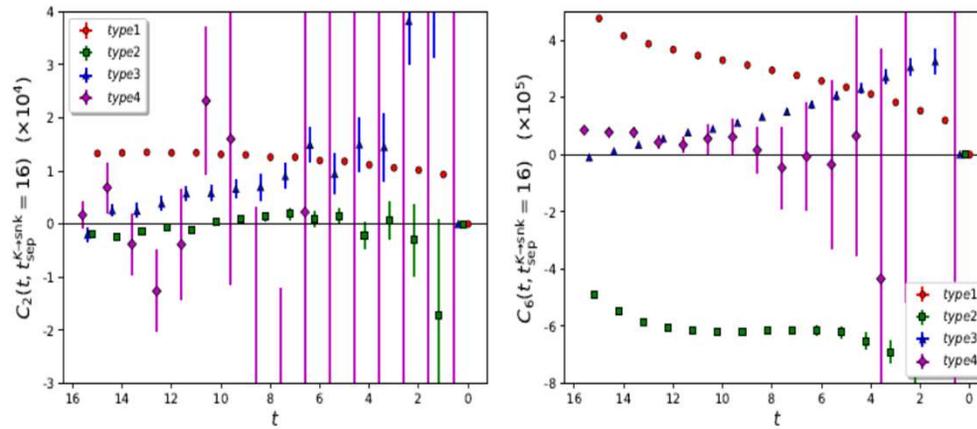


FIG. 3: The contributions of the four Wick contraction topologies *type1*-*type4* to the  $C_2$  (left) and  $C_6$  (right) three-point functions with the  $\pi\pi(111)$  sink operator, plotted as a function of the time separation between the kaon and the four-quark operator,  $t$ , at fixed  $t_{\text{sep}}^{K \rightarrow \text{snk}} = 16$ . For clarity we plot with an inverted x-axis such that the  $\pi\pi$  sink operator is on the left-hand side. These correlation functions include the subtraction of the pseudoscalar operator.

**SHOULD WE BE SHOCKED TO FIND THAT  
THE SCALE OF NEW PHYSICS IS NOT  $\sim 1$   
TEV & APPEARS TO BE HIGHER?**

scalars'13; 9/13/13 A. Soni HET-BNL

11

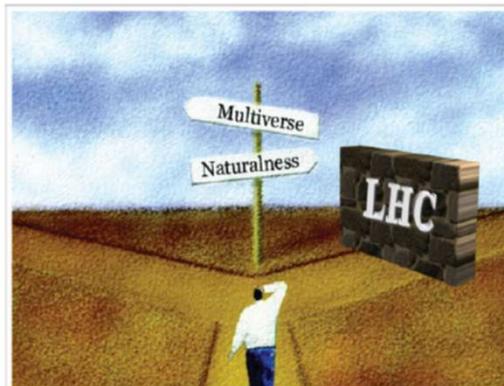
## Is Nature Unnatural?

Decades of confounding experiments have physicists considering a startling possibility: The universe might not make sense.

by: Natalie Wolchover

May 24, 2013

[email](#) [print](#)



Is the universe natural or do we live in an atypical bubble in a multiverse? Recent results at the Large Hadron Collider have forced many physicists to confront the latter possibility. (Illustration: Giovanni Villadoro)

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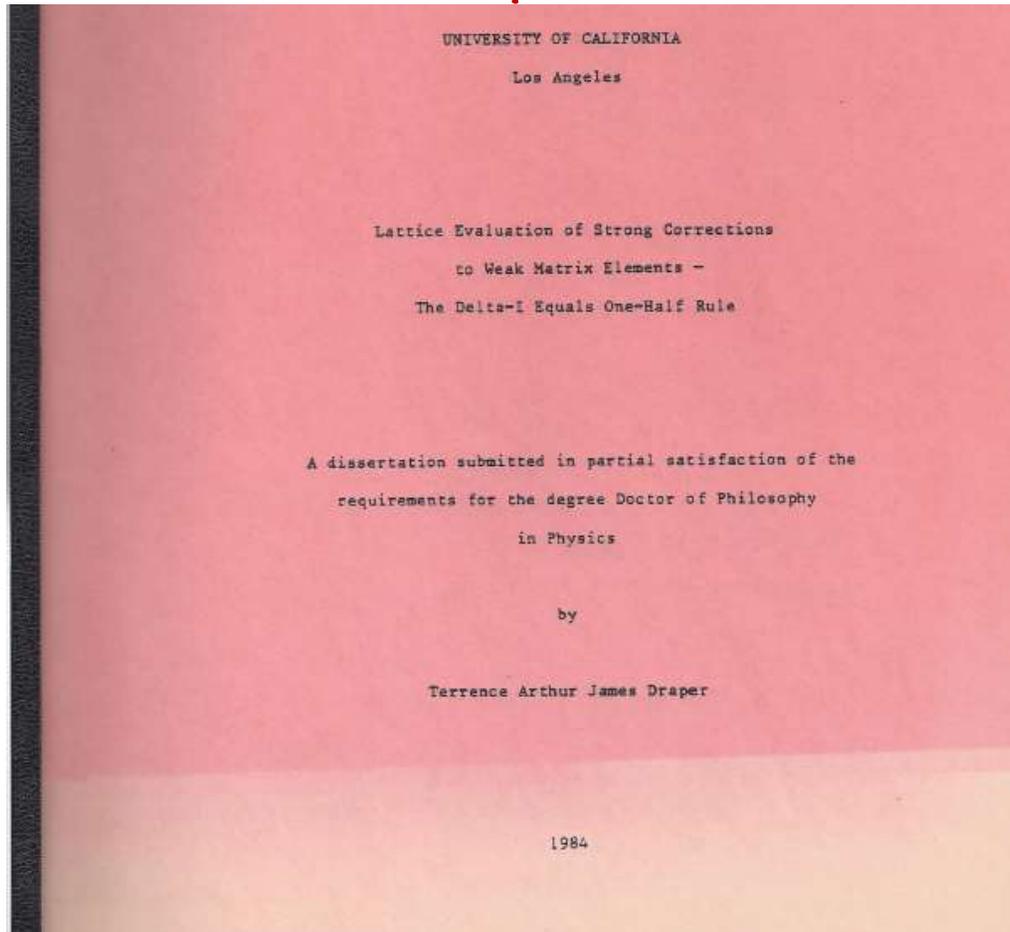
## Localization parameters of the 3-families of quarks

$$\begin{array}{lll} c_{Q_1} = -0.579, & c_{Q_2} = -0.517, & c_{Q_3} = -0.473 \\ c_{u_1} = -0.742, & c_{u_2} = -0.558, & c_{u_3} = +0.339 \\ c_{d_1} = -0.711, & c_{d_2} = -0.666, & c_{d_3} = -0.553 \end{array}$$

Table from  
M. Neubert  
@Moriond09

⇒ masses of the 6 quarks in RS!  
[HOWEVER, it does not predict masses]

The 1st  
Ph D  
Thesis



Grew from  
End of year  
Beer Party  
~ June 20, 1984!  
[UCLA]

Beware of  
End of year  
Beer Parties!

Fermion "geography" (localization) naturally explains:

Grossman&Neubert; Gherghetta&Pomarol; Davoudiasl, Hewett & Rizzo

- Why they are light (or heavy)
- FCNC for light quarks are severely suppressed automatically
- RS-GIM MECHANISM (Agashe, Perez, AS'04) flavor changing transitions though at the *tree level* (resulting from rotation from interaction to mass basis) are suppressed roughly to the same level as the loop in SM => CKM mixings (& mass) hierarchy.
- O(1) CP ubiquitous;.....nedm, in fact ALL DIR-CP [ $\varepsilon'/\varepsilon$ ,  $\gamma$ ,  $\Delta ACP(B \Rightarrow K\pi)$ ,  $\Delta(\text{Sin}2\beta)$ ;  $S[B \Rightarrow K^* \rho\gamma]$ ;  $\Delta ACP(D)$ ..] are an exceedingly important path to BSM-phase and new physics
- Most flavor violations are driven by the top

-> ENHANCED  $t \rightarrow cZ(h)$  .... A VERY IMPORTANT "GENERIC" PREDICTION. Agashe, Perez, AS'06  $\Rightarrow R_{SF,1} \sim 10^3 \text{ TeV}$

EXTENSIVE STUDIES by BURAS et al and by NEUBERT et al