

# **Deuteron breakup kinematics in BeAGLE event generator**

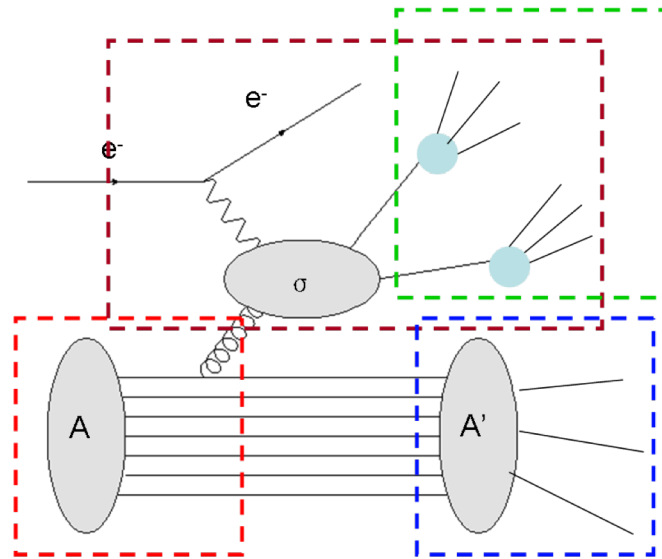
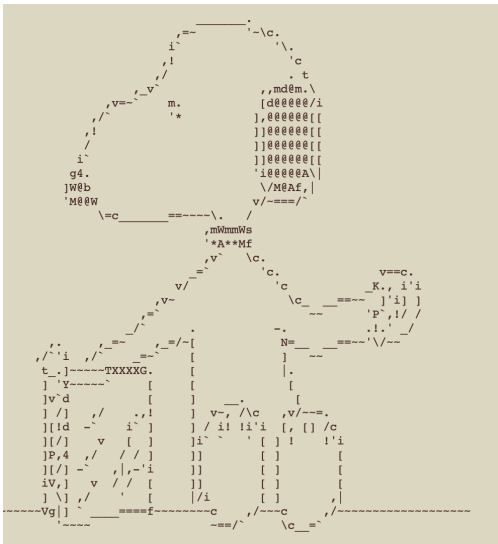
Kong Tu

BNL

03.06.2020

# BeAGLE

- Initiated by M.Baker, E. Aschenauer, JH. Lee, Z. Liang.
- Now new developers/maintainers, e.g., Kong Tu, Mathieu Ehrhart, ...
- Many users from Jlab, BNL, and other institutes, and becoming more.
- Pythia 6 + DPMJet + Fluka - embed an elementary eN collision into a nuclear environment, <https://wiki.bnl.gov/eic/index.php/BeAGLE>



A hybrid model consisting of DPMJet and PYTHIA with nPDF EPS09.

Nuclear geometry by DPMJet and nPDF provided by EPS09.

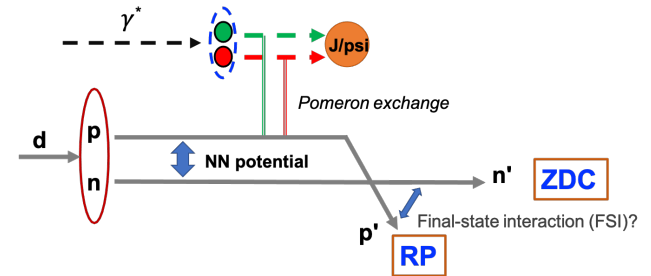
Parton level interaction and jet fragmentation completed in PYTHIA.

Nuclear evaporation ( gamma dexcitation/nuclear fission/fermi break up ) treated by DPMJet

Energy loss effect from routine by Salgado&Wiedemann to simulate the nuclear fragmentation effect in cold nuclear matter

# Status

- One process:



was implemented in BeAGLE, which consists of realistic deuteron wavefunction and LF kinematics of the struck and spectator nucleons.

- Useful for both EIC physics and detector requirements studies with spectator tagging.
  - Short-range nuclear correlations in deuteron.
  - Incoherent diffractive VM production.
  - DVCS on deuteron (incoherent)
  - ...
- Replace  $J/\psi$  with any particle of one's interest, the tagging is still valid.
- This study overlaps with other subgroups of YR effort. *Take what you need and/or tell us what you need.*
- In this talk, the study is done with  $J/\psi$ , but it can apply to any VM or photon or dijet or ...

# Observables and detectors

Physics observables:

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. $p'$ and $n'$ )	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
theta' ( $n'$ polar angle w.r.t gamma*)	✓		
$p_T$ of VM (e.g., J/psi, photon, dijets, etc)		✓	✓

...

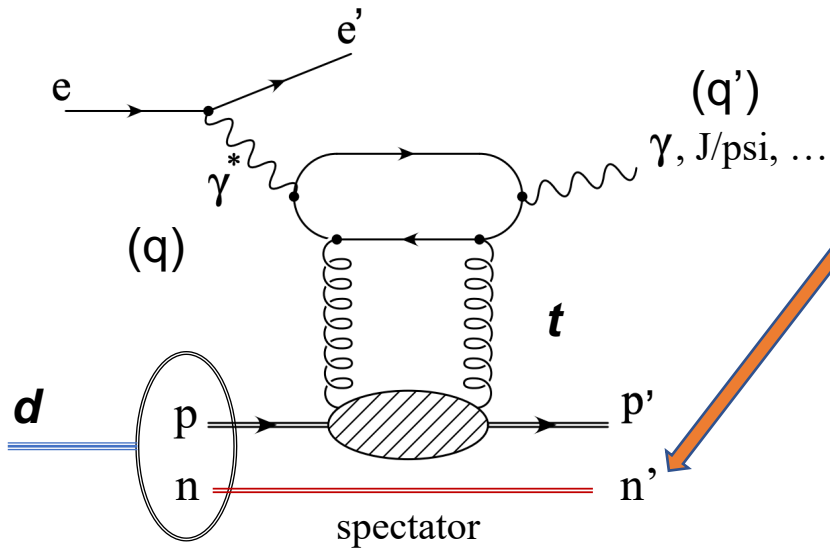
Toy EIC forward detectors

Detectors	Neutron det.	Proton det.
Energy reso.	$\frac{50\%}{\sqrt{E}} + 5\%$	
Angular reso. (mrad)	0.3	
Momentum reso.		$\frac{dp_T}{p_T} = 3\%$
Acceptance (mrad)	5	(0,5) (7,22)

# BeAGLE parameters

- 18 GeV electron scattering off 135 GeV deuteron
  - Other available energy configurations for EIC, e.g., 5x20, 10x50 GeV
  - Deuteron wavefunction for  $\mathbf{k}$ , where  $\mathbf{k}$  is momentum of nucleon in p+n frame. Taken from [ [Phys. Rev. C 53, 1689](#) ]
  - LC kinematics of nucleons in deuteron, taken from [Strikman & Weiss \[Phys.Rev. C97 \(2018\) no.3, 035209\]](#)
  - BeAGLE still has a small momentum nonconservation issue, will be resolved soon hopefully.
- 
- 1M events with incoherent diffractive J/psi production  
(optional, BeAGLE can keep J/psi decay or not decay to lepton pairs)
- 
- $Q^2 > 1 \text{ GeV}^2$
  - $0.05 < y < 0.85$

# Kinematic variables

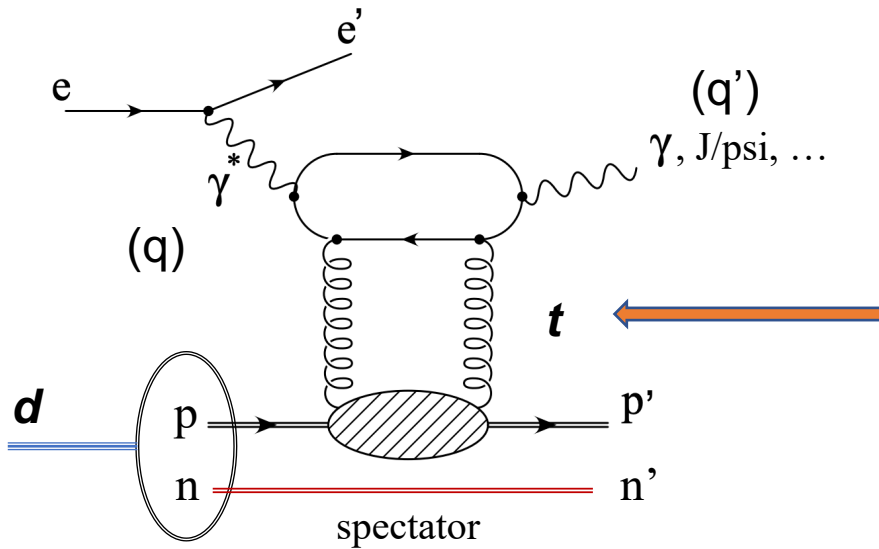


$p_m, p_t, p_z$ :

Total, transverse, and longitudinal momentum of spectator nucleon in  $d$  rest frame

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. $p'$ and $n'$ )	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
theta' ( $n'$ polar angle w.r.t gamma*)	✓		
$p_T$ of VM (e.g., J/psi, photon, dijets, etc)		✓	✓

# Kinematic variables



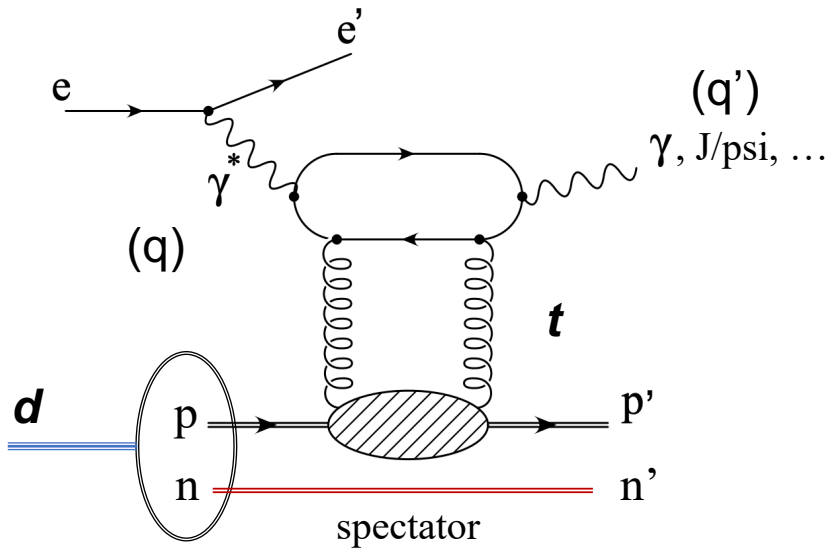
$$t = (e' - e + V)^2 = (p' - n'')^2$$

Momentum transfer from virtual photon to the struck nucleon

$n'' = p$ , the initial momentum of the struck nucleon

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. $p'$ and $n'$ )	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
theta' ( $n'$ polar angle w.r.t gamma*)	✓		
$p_T$ of VM (e.g., J/psi, photon, dijets, etc)		✓	✓

# Kinematic variables



alpha:

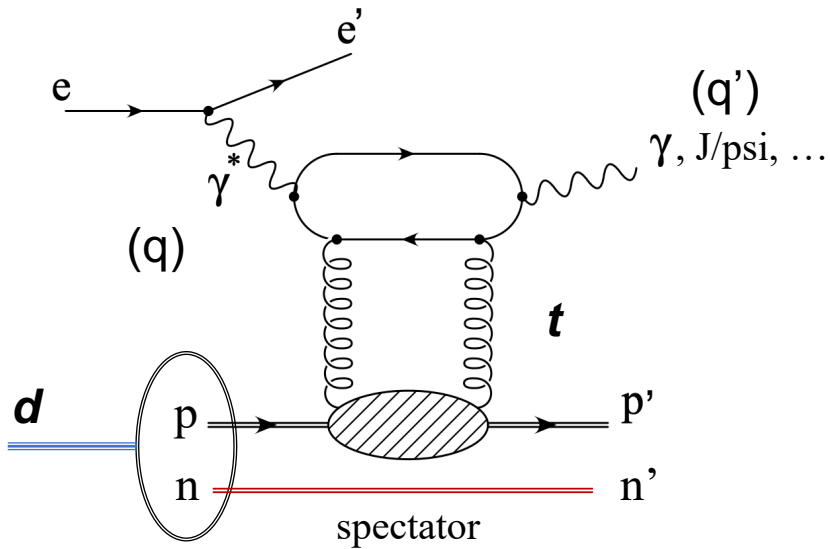
Light cone momentum fraction

$$\alpha = \frac{2p_{n'}^+}{p_d^+}$$

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. p' and n')	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
theta' (n' polar angle w.r.t gamma*)	✓		
$p_T$ of VM (e.g., J/psi, photon, dijets, etc)		✓	✓



# Kinematic variables

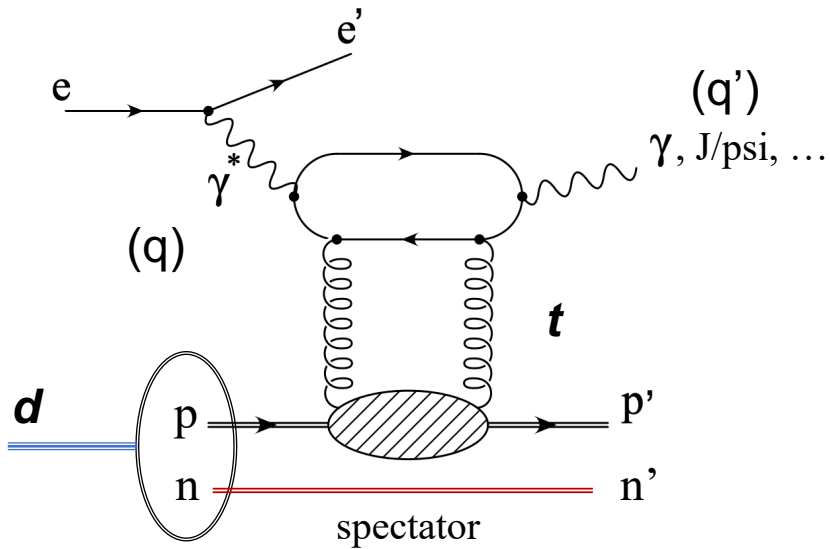


$S_{PN}$ :

Center-of-mass energy between  
proton and neutron squared  
 $(p' + n')^2$

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. $p'$ and $n'$ )	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
theta' ( $n'$ polar angle w.r.t gamma*)	✓		
$p_T$ of VM (e.g., J/psi, photon, dijets, etc)		✓	✓

# Kinematic variables

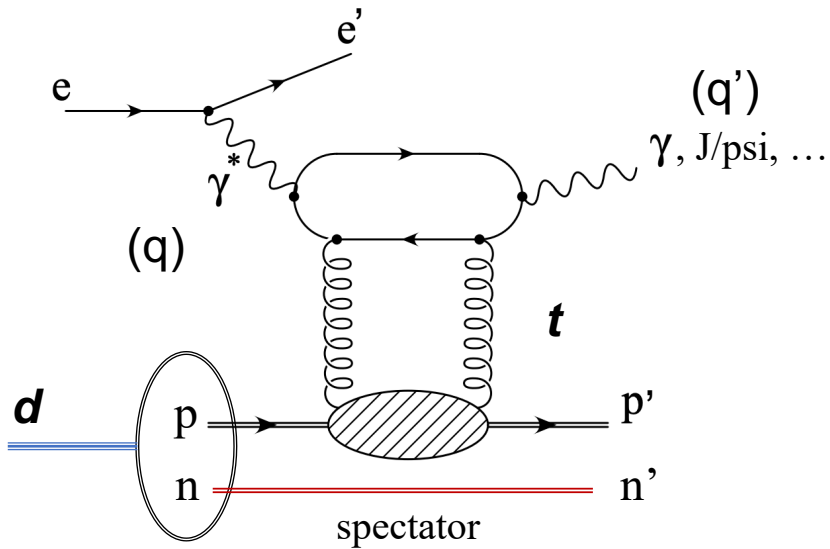


$$t' = (n' - d)^2 - M^2 :$$

effective struck nucleon off-shellness

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. $p'$ and $n'$ )	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
theta' ( $n'$ polar angle w.r.t gamma*)	✓		
$p_T$ of VM (e.g., J/psi, photon, dijets, etc)		✓	✓

# Kinematic variables

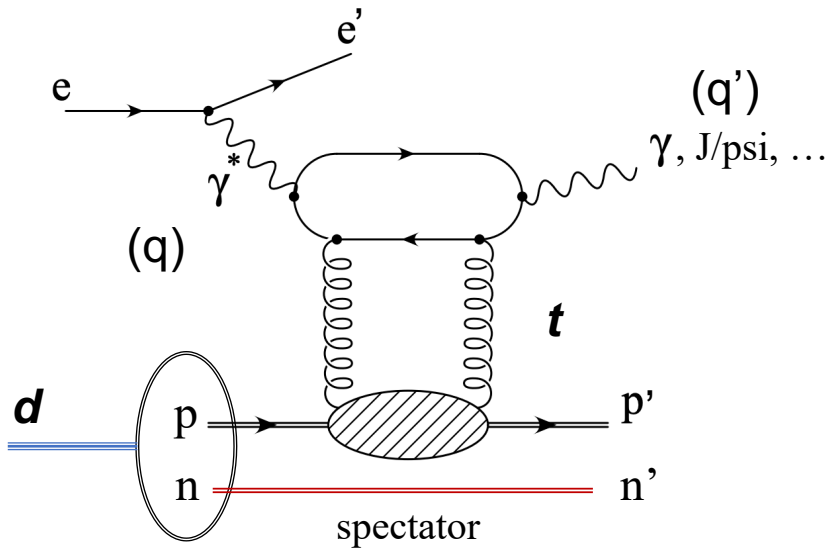


$\theta'$ :

Spectator nucleon polar angle  
w.r.t virtual photon direction in  
target rest frame

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. $p'$ and $n'$ )	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
$\theta'$ ( $n'$ polar angle w.r.t $\gamma^*$ )	✓		
$p_T$ of VM (e.g., $J/\psi$ , photon, dijets, etc)		✓	✓

# Kinematic variables



$p_T$  of VM:

Transverse momentum of VM,  
e.g.,  $J/\psi$ ,  $\rho^0$ , or other  
particles like real photon ..

Observables	SRC	DVCS	VMP
$p_m$ (GeV) $p_T, p_z$ (GeV)	✓		✓
$t$ (GeV <sup>2</sup> ) $= (e' - e + V)^2$		✓	✓
alpha (LC mom. frac.)	✓		✓
$S_{PN}$ (GeV <sup>2</sup> ) (s btw. $p'$ and $n'$ )	✓		✓
$t'$ (GeV <sup>2</sup> ) $= (n' - d)^2 - M^2$	✓	✓	✓
theta' ( $n'$ polar angle w.r.t gamma*)	✓		
$p_T$ of VM (e.g., $J/\psi$ , photon, dijets, etc)		✓	✓

# PWIA

Introduction: D(e,e'p) in PWIA

$$\frac{d^5\sigma}{d\omega d\Omega_e d\Omega_p} = k\sigma_{ep}\rho(p_r)$$

**Plane Wave IA:**

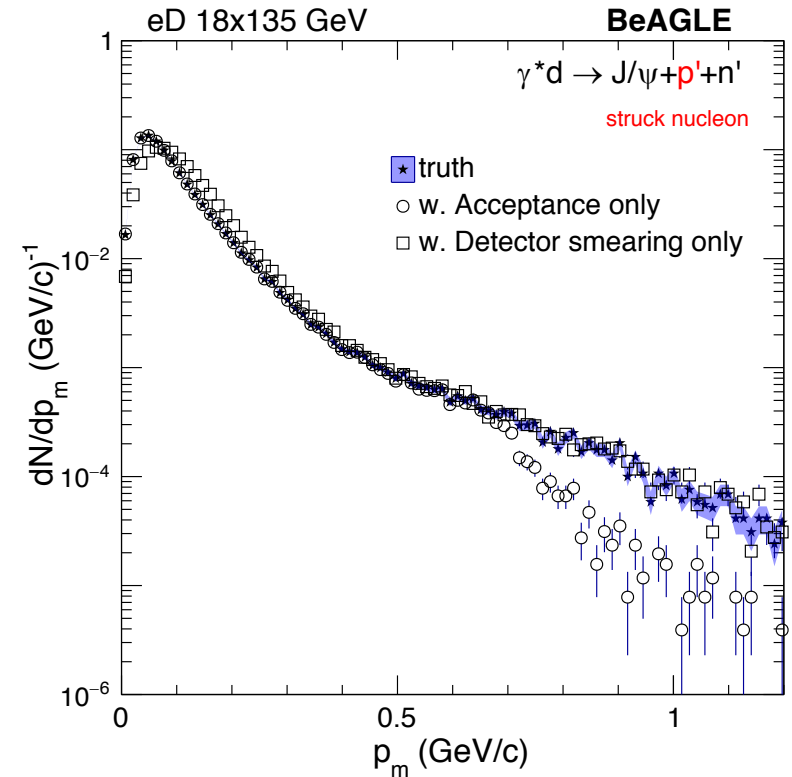
- Hit nucleon does not interact with the recoiling system
- Described by a plane wave

Experimental Momentum distributions:

$$\rho(p_r)_{exp} = \sigma_{red} = \frac{\sigma_{exp}}{k\sigma_{ep}}$$

also called reduced cross sections

1/21/20 Exploring QCD with light nuclei at EIC 5

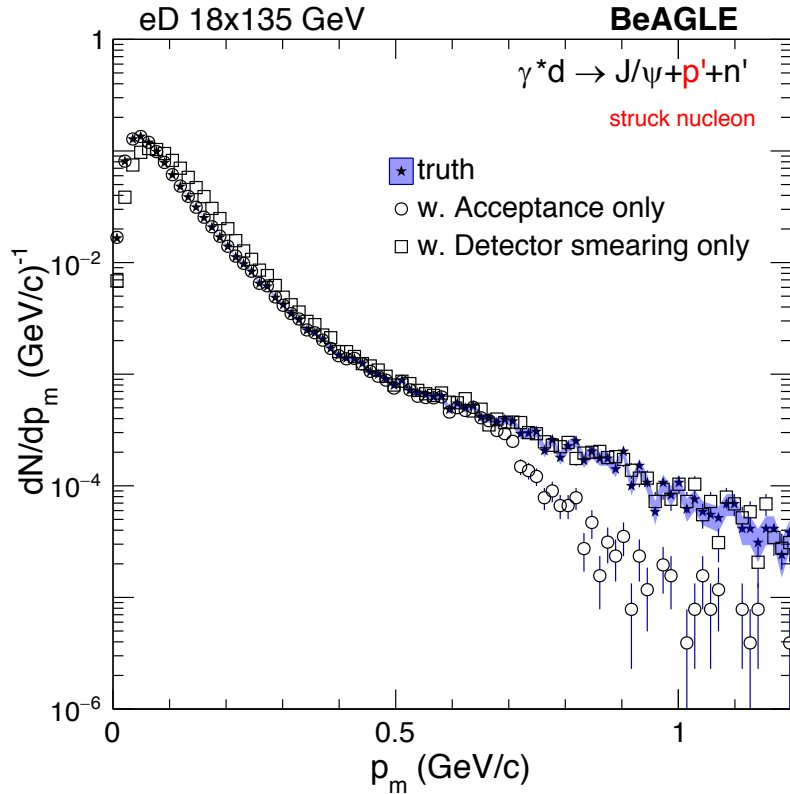


Deuteron SRC 101 by W. Boeglin  
Workshop on Light Ion (CFNS)

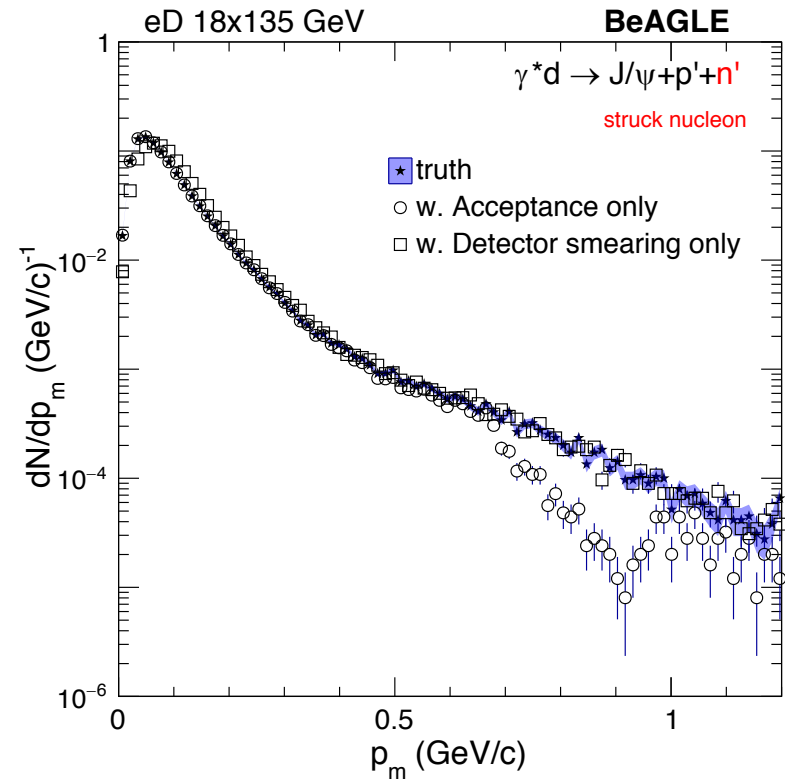
- Low momentum limited by resolution
- High momentum limited by acceptance

Shown this before, next is to compare each observables by tagging protons or neutrons

# $P_m$



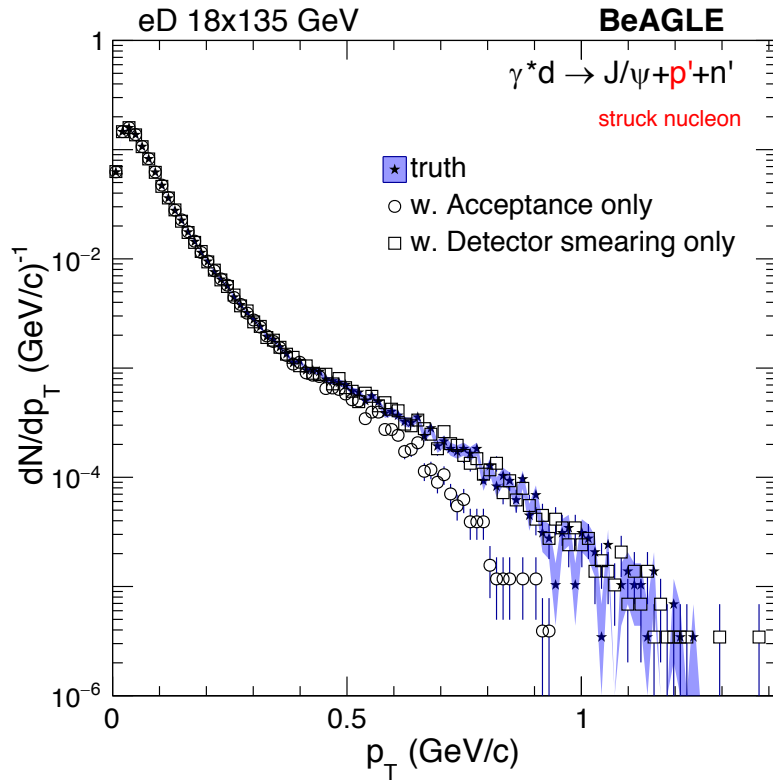
Neutron spectator tagging



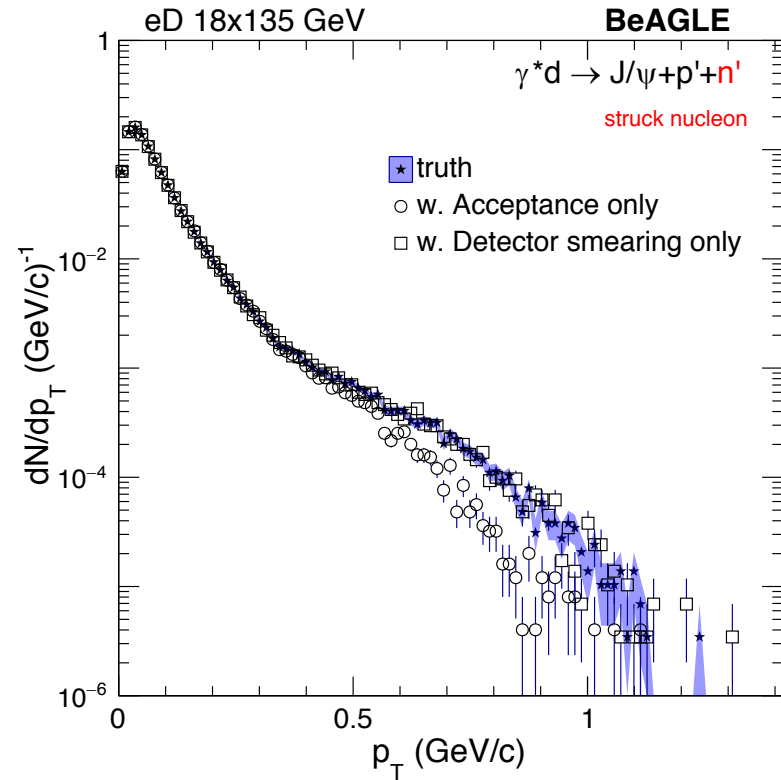
Proton spectator tagging

- Both acceptance and detector resolutions are checked, separately.
- Given the current assumption of detector, tagging proton seems to be better

# $P_T$



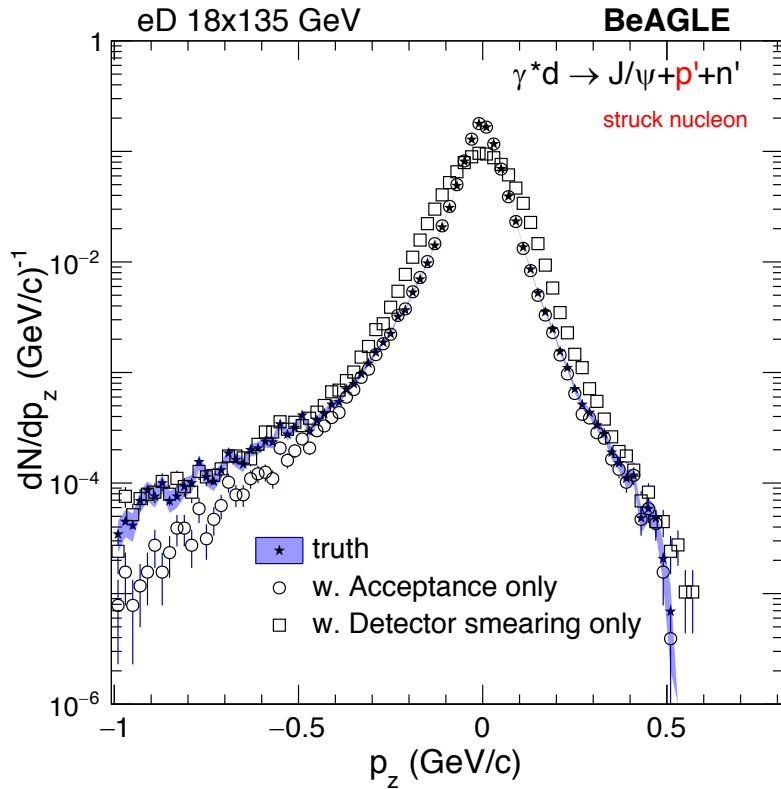
Neutron spectator tagging



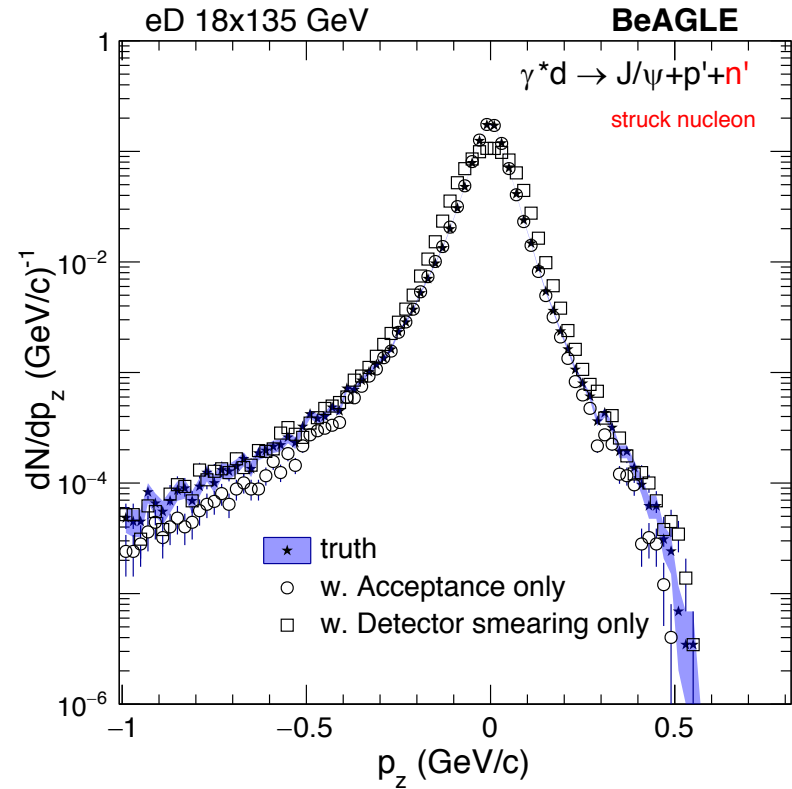
Proton spectator tagging

- There is no significant difference, and the transverse momentum is much less sensitive to detector resolution

$p_z$



Neutron spectator tagging

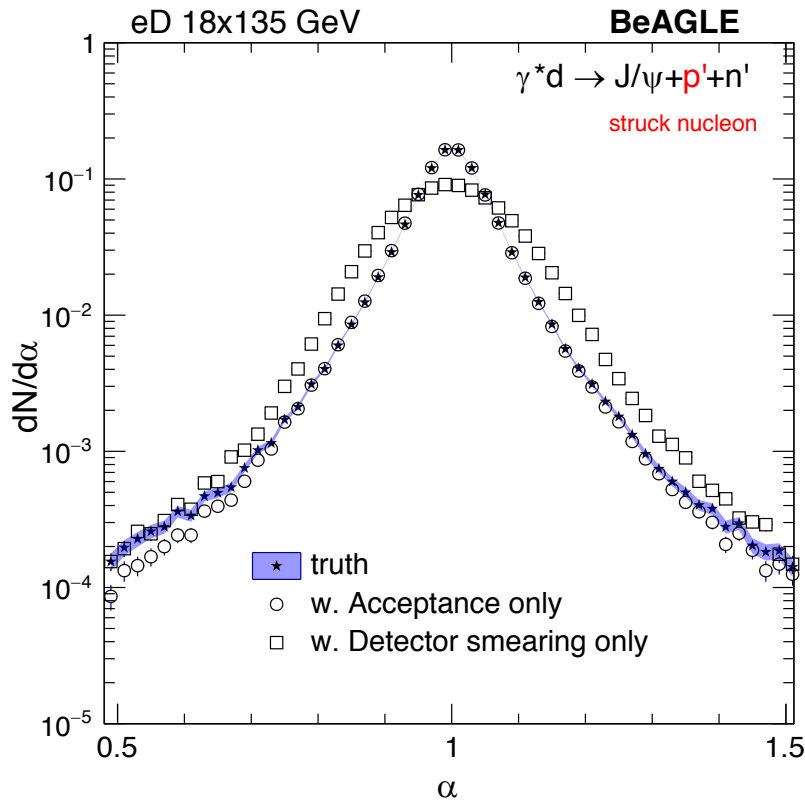


Proton spectator tagging

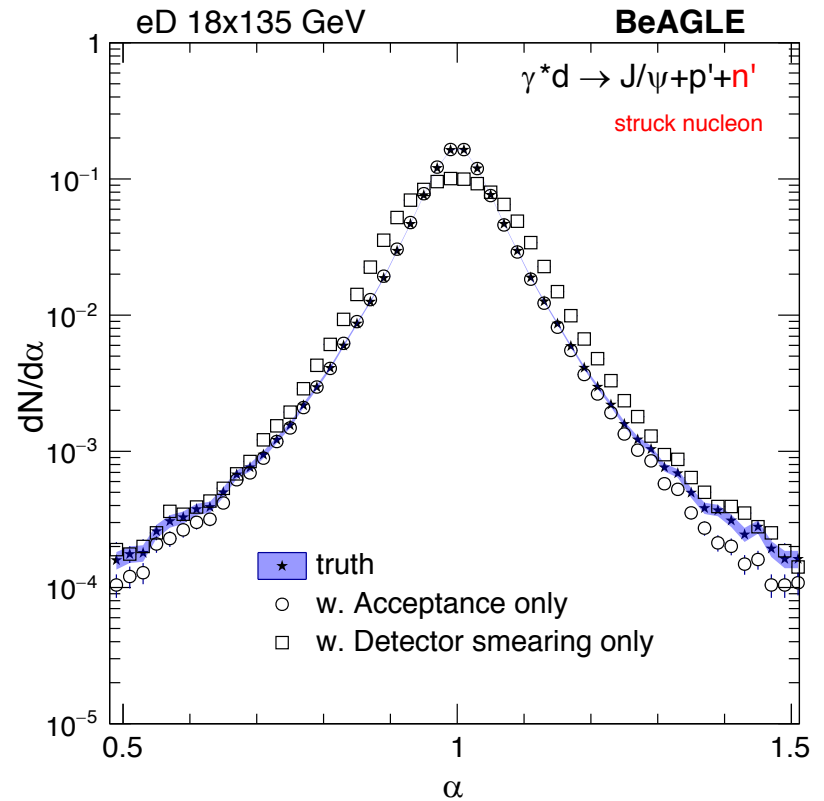
- Given the current assumption of detector, tagging proton seems to be better



# alpha



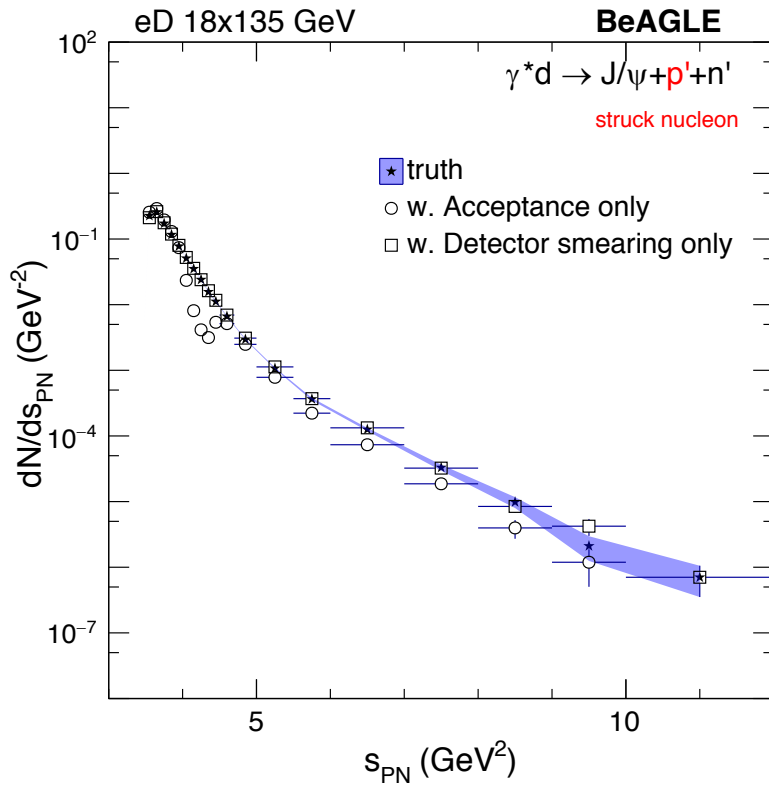
Neutron spectator tagging



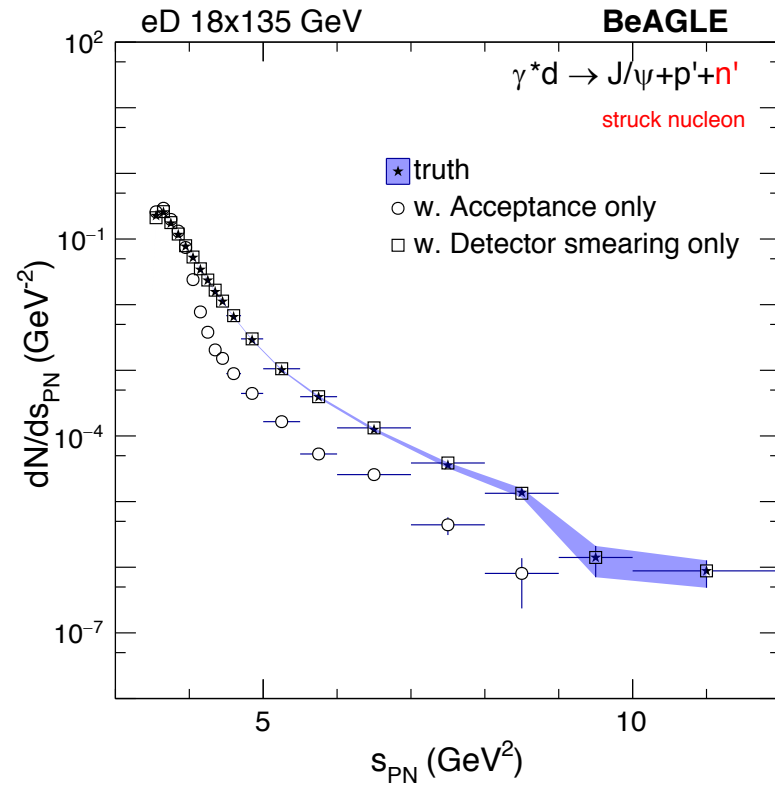
Proton spectator tagging

- Given the current assumption of detector, tagging proton seems to be better but not much..

# SPN



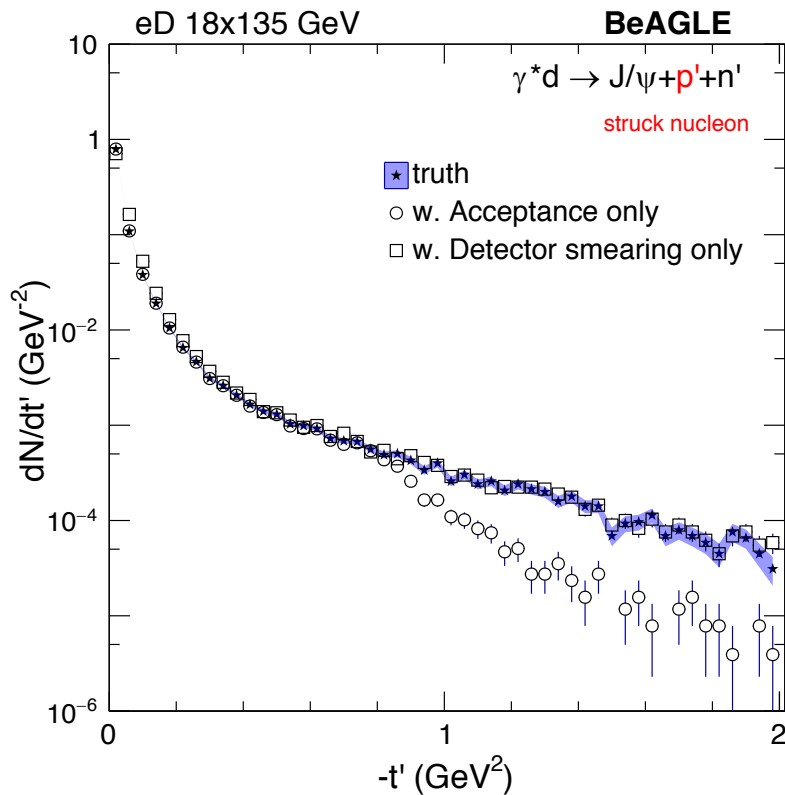
Neutron spectator double tagging



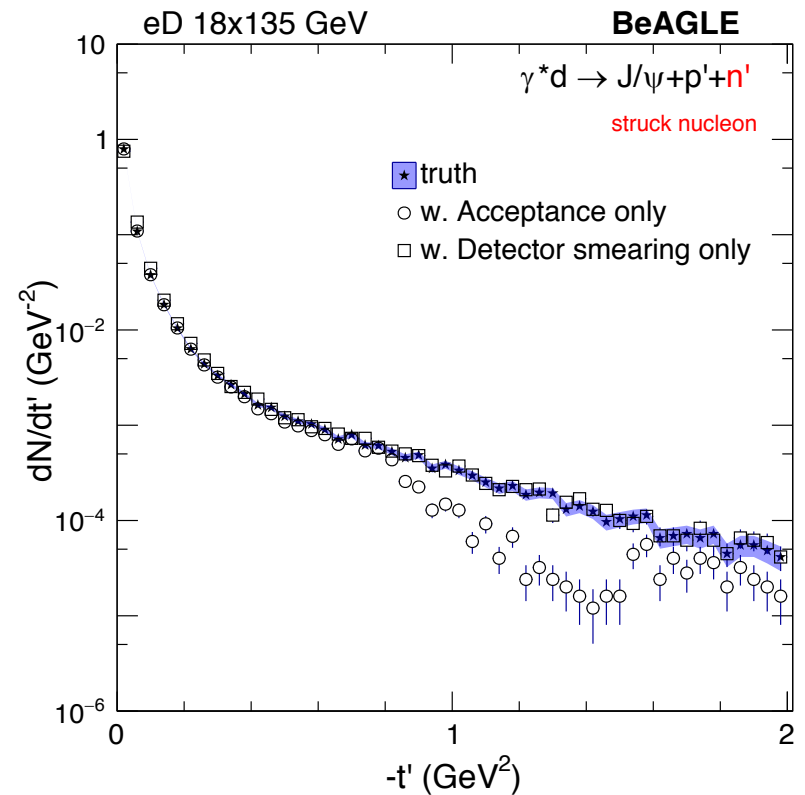
Proton spectator double tagging

- This observable is not so sensitive to the resolution because the lower bound starts at  $(M_p + M_n)^2$ , so  $\sim 100$  MeV smearing is not dominant at low  $s$ .

$t'$



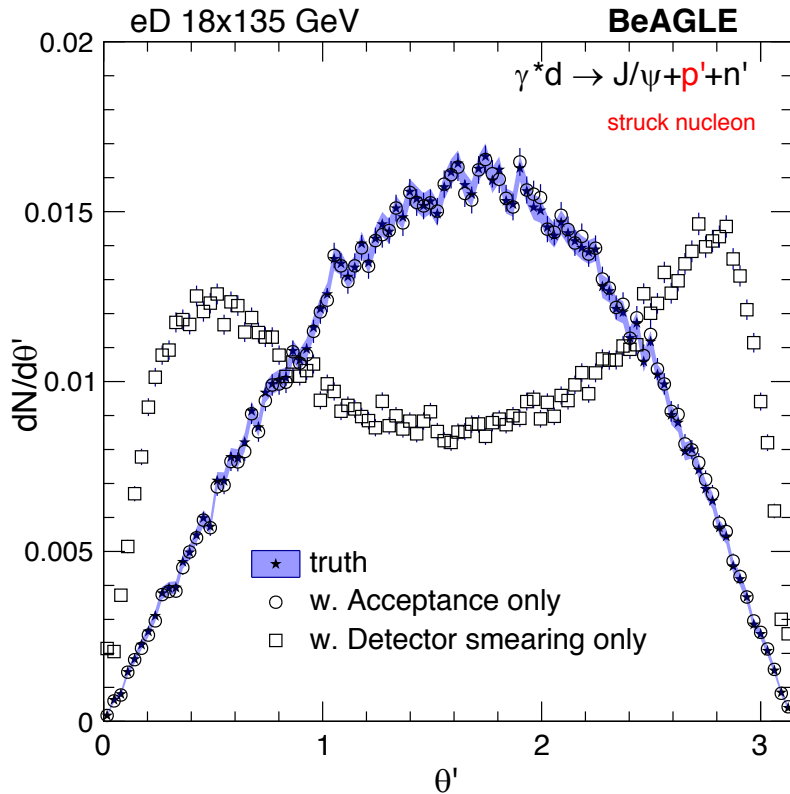
### Neutron spectator tagging



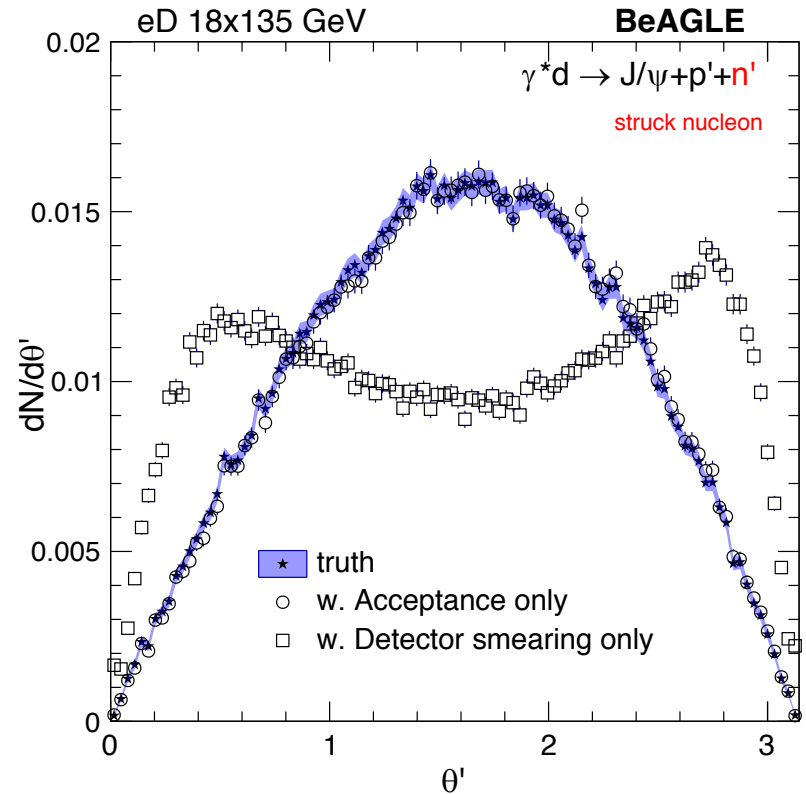
### Proton spectator tagging

- Important observable to extract free neutron xxx (PDF, GPD, ..)
- Intuitively, this is the struck nucleon off-shellness, and on-shell extrapolation will be needed for certain analysis, so low- $t'$  is essential.

# theta'



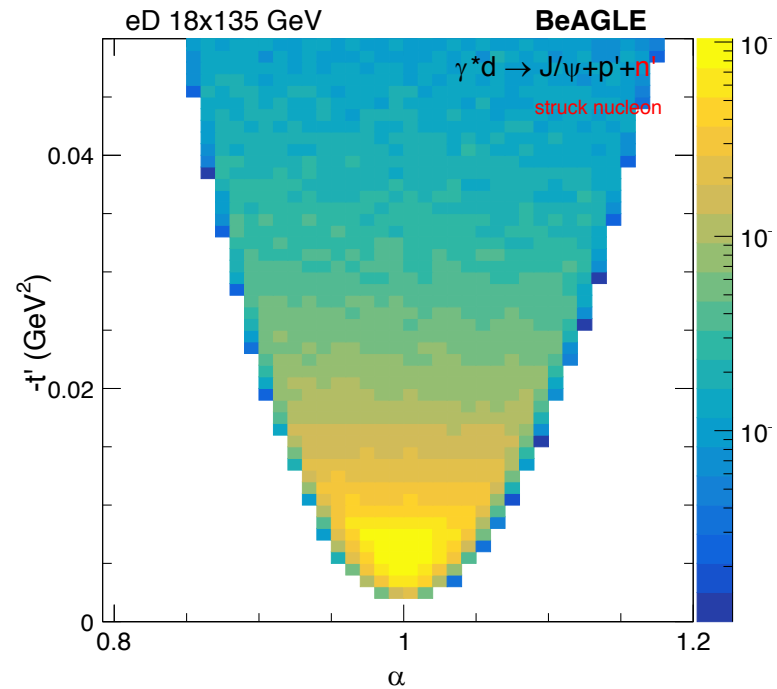
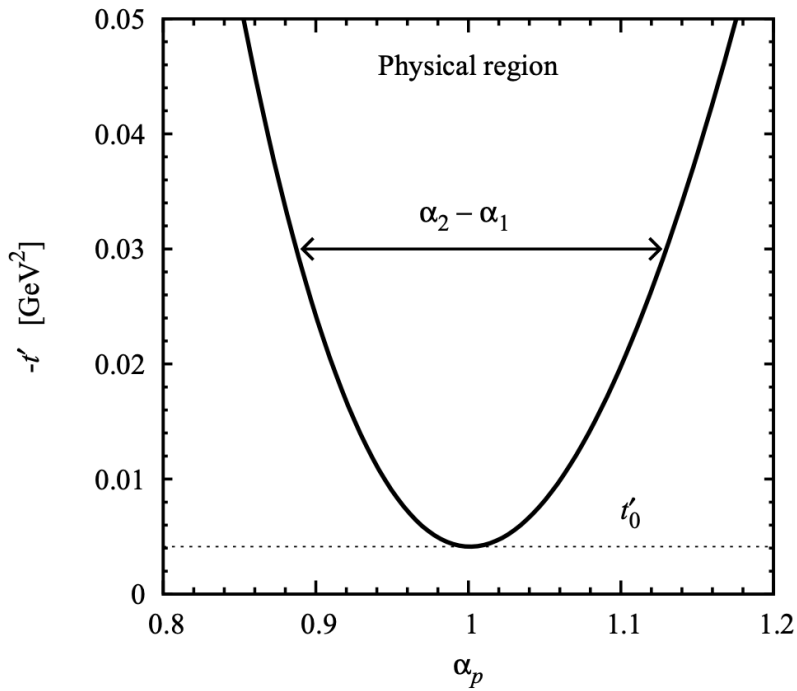
Neutron spectator tagging



Proton spectator tagging

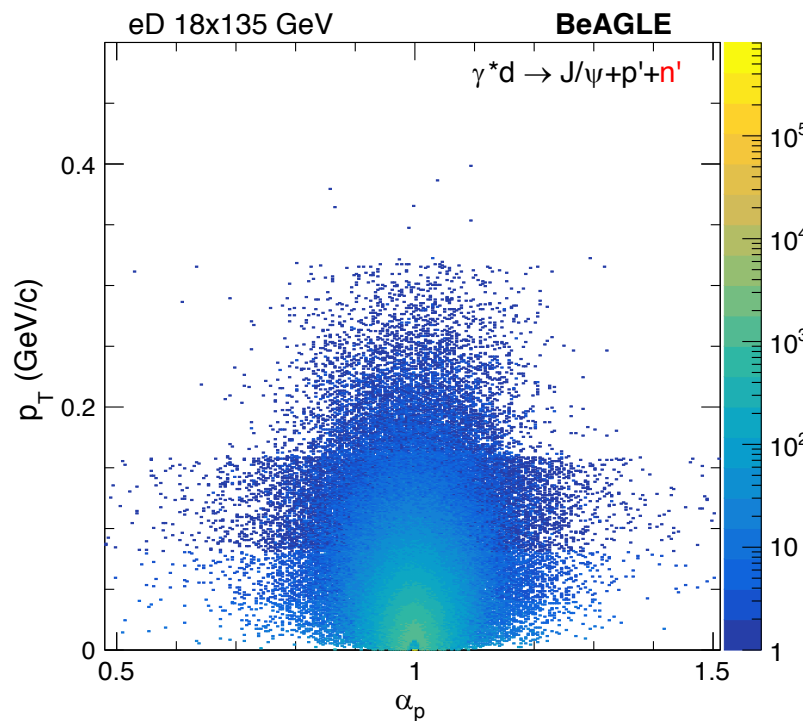
- Most dramatic smearing in this observable.
- In the  $d$  rest frame, the angle between photon and spectator nucleon.

# $t'$ vs alpha

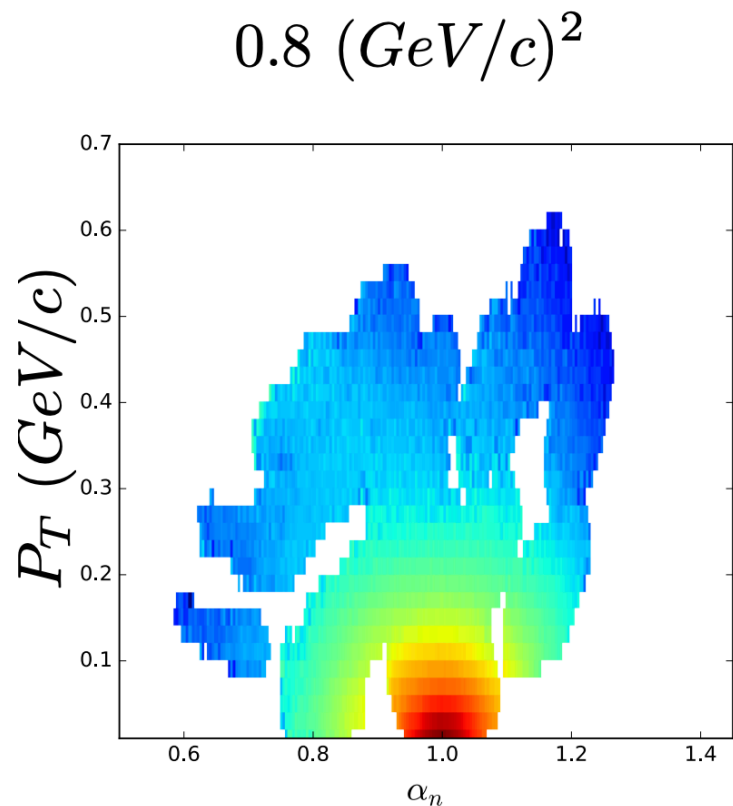


Kinematic limits and physical regions are well reproduced!  $t_{\min} \sim 0.004$   
Based on Strikman & Weiss paper, <https://arxiv.org/abs/1706.02244>

# Spectral function $S_d(\alpha, \mathbf{p}_T)$



Proton spectator tagging  
Acceptance only

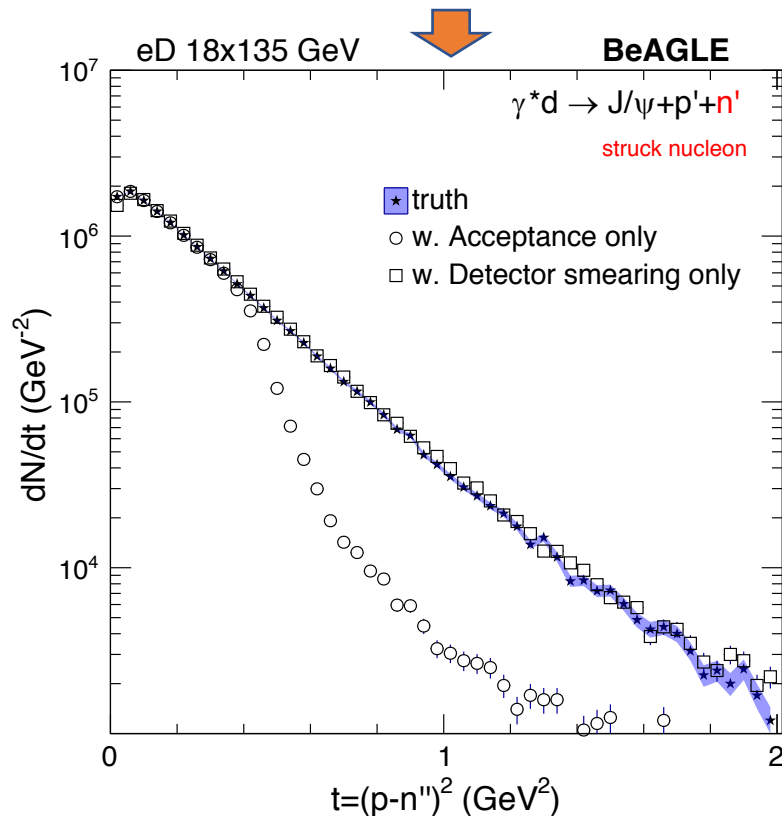
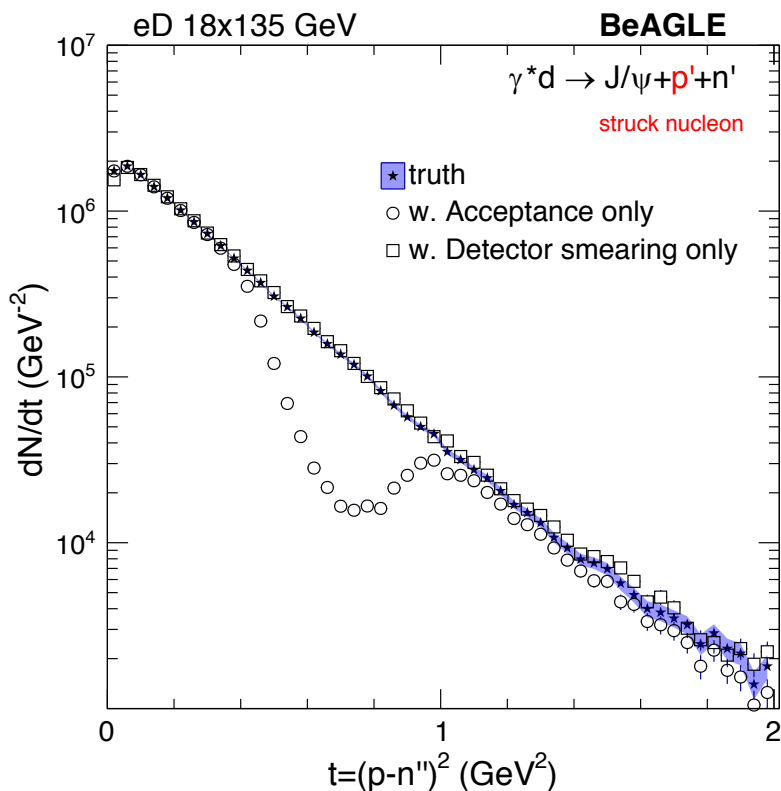


New results from Jlab preliminary data

Seems to have a better acceptance for alpha comparing to fixed target experiment?

**t**

## DVCS on neutron

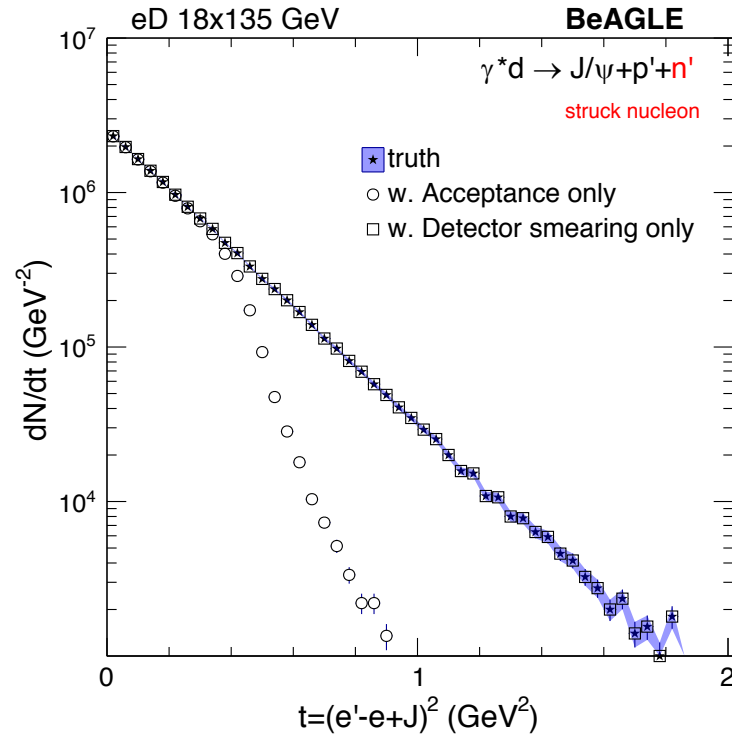
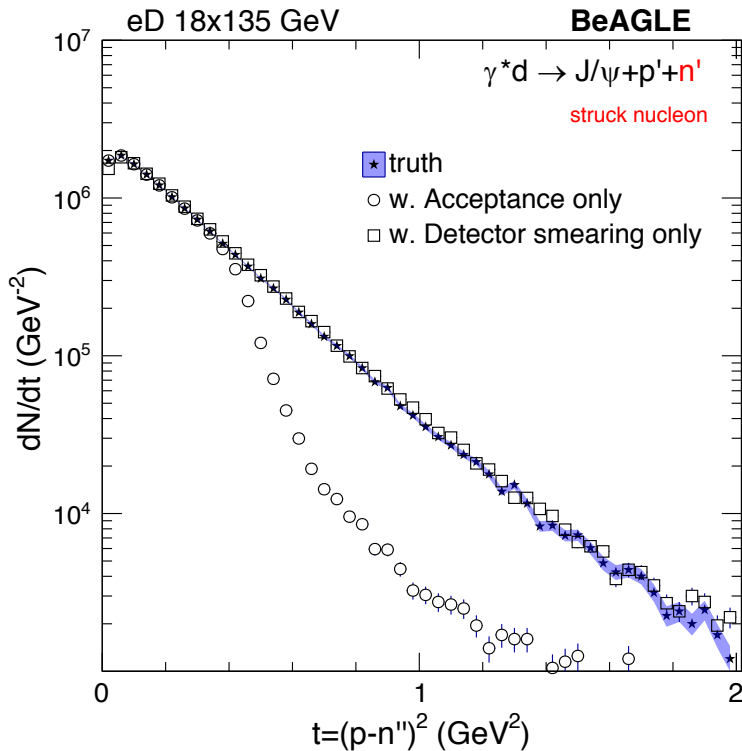


## Neutron spectator double tagging

## Proton spectator double tagging

- Acceptance is much more important than detector resolution. This method requires double tagging, most of high  $t$  is lost by acceptance.
- A dip structure is observed at low  $t$ , might be related to the difference between this method and  $t = (e' - e + J)^2$  in BeAGLE.

# t compare

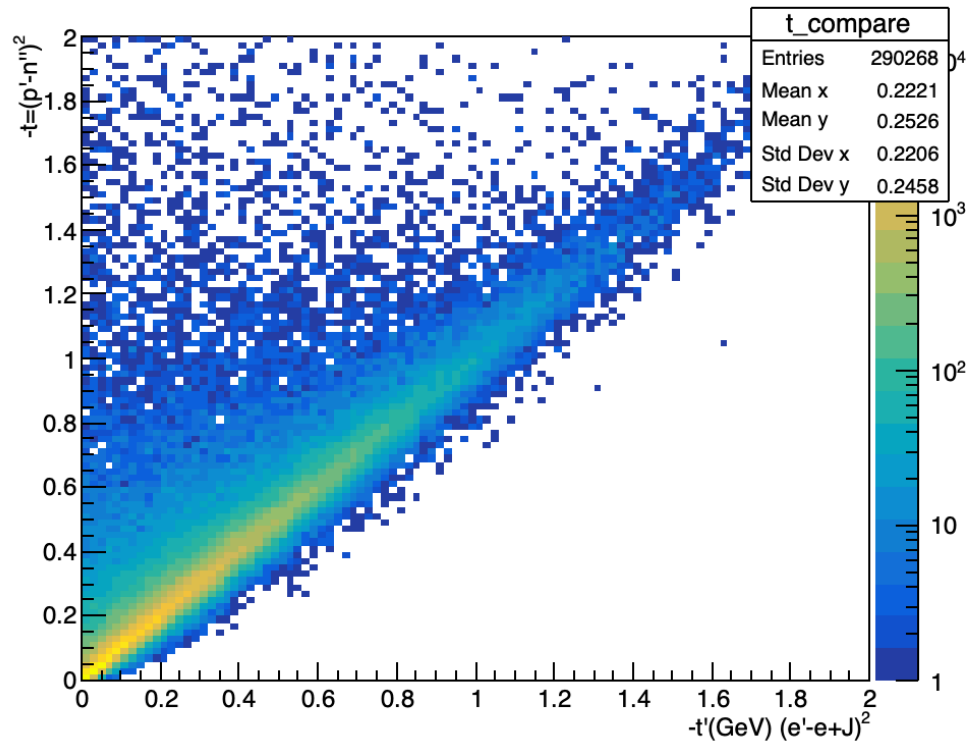


## Proton spectator double tagging

- The true  $t$  in BeAGLE is not the physical  $t$ ! The kinematics was given by Pythia, ignoring the fact that nucleon has fermi motion/SRC
- Correcting this kinematics is not so trivial, need to think about it.
- The slopes of these two are slightly different.



# t compare



- This is not a resolution effect, it's because of inconsistency in BeAGLE.
- However, for detector requirements, it doesn't matter much.

# Comparison

- Neutron detector

Neutron Det.	Default	V1	V2
Acceptance	5 mrad	6 mrad	7 mrad
Energy reso.	$\frac{50\%}{\sqrt{E}} + 5\%$	$\frac{30\%}{\sqrt{E}} + 5\%$	$\frac{100\%}{\sqrt{E}} + 5\%$

- Proton detector

- Acceptance: (0,5) + (7-22) mrad (default)

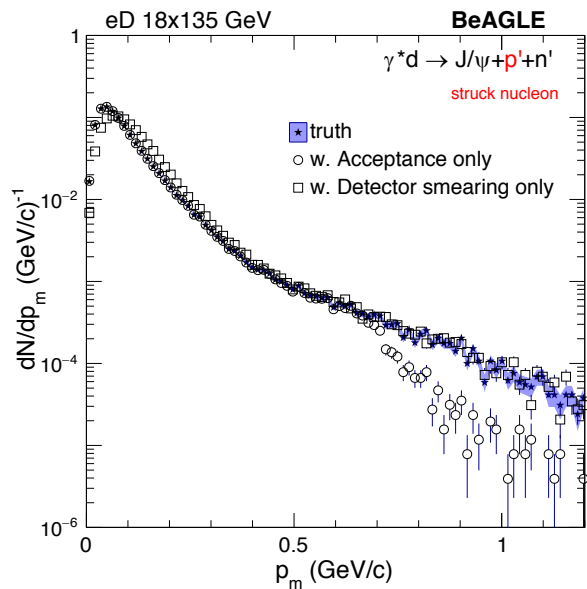
Proton Det.	Default	V1	V2
Momentum reso.	$\frac{dp_T}{p_T} = 3\%$	$\frac{dp_T}{p_T} = 5\%$	$\frac{dp_T}{p_T} = 10\%$

- Energy configurations:

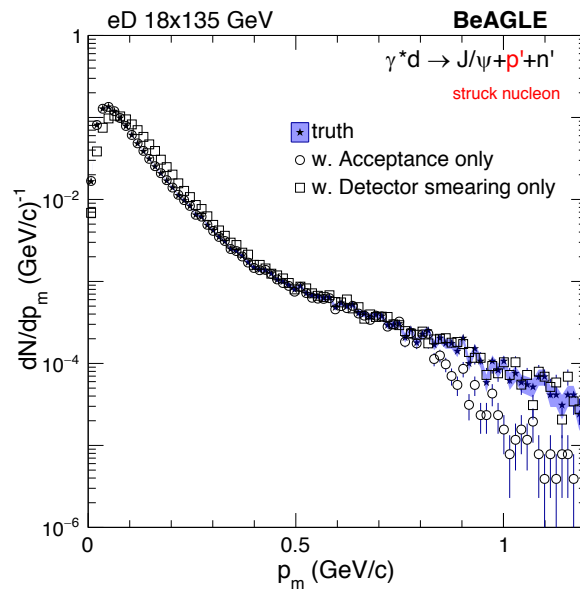
- 18 x 135 GeV (default)
- 10 x 50 GeV
- 5 x 20 GeV

# **Neutron detector acceptance**

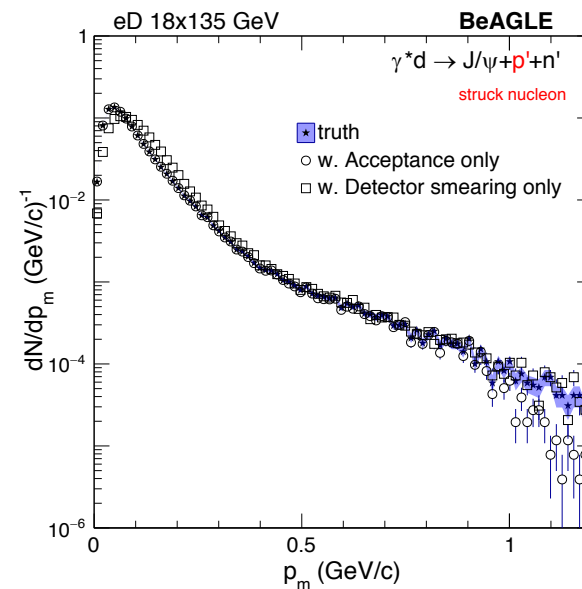
# Neutron detector acceptance - $p_m$



5 mrad



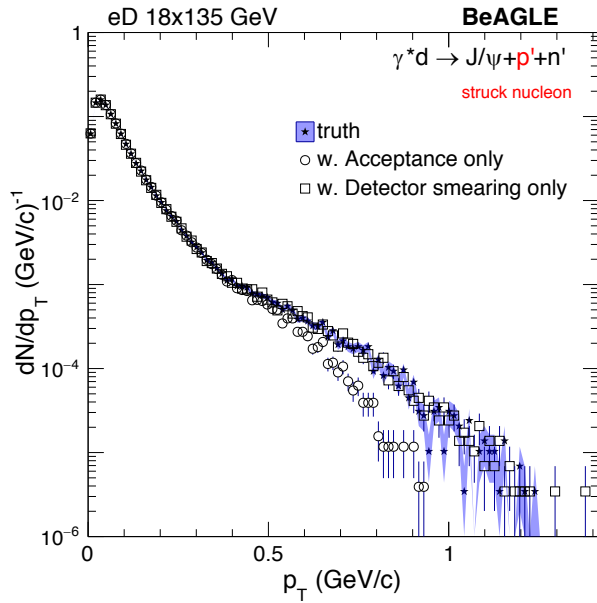
6 mrad



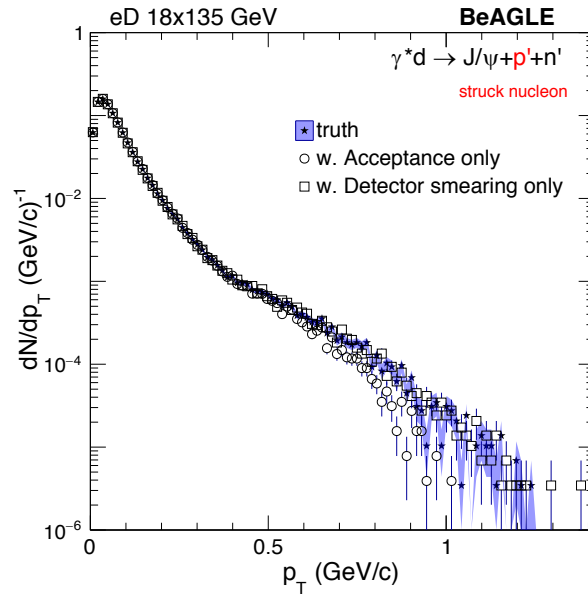
7 mrad

High momentum tail gradually comes back when increase the size of neutron detector

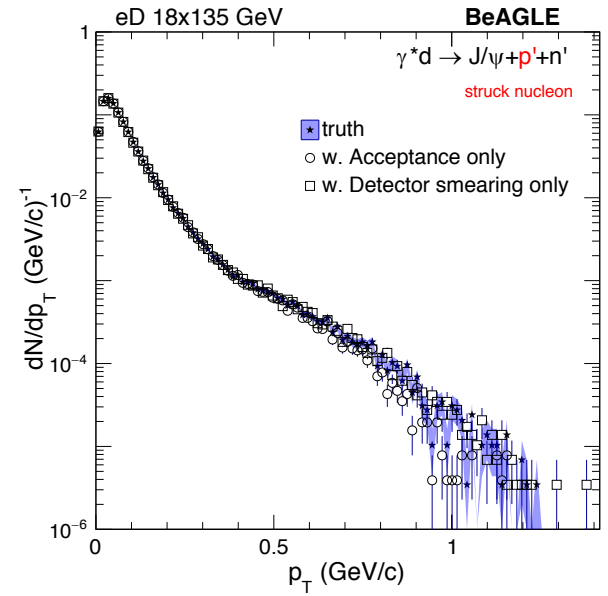
# Neutron detector acceptance - $p_T$



5 mrad



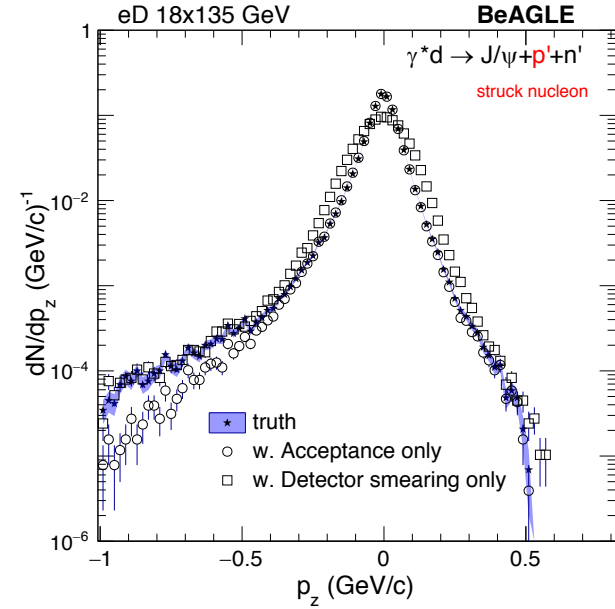
6 mrad



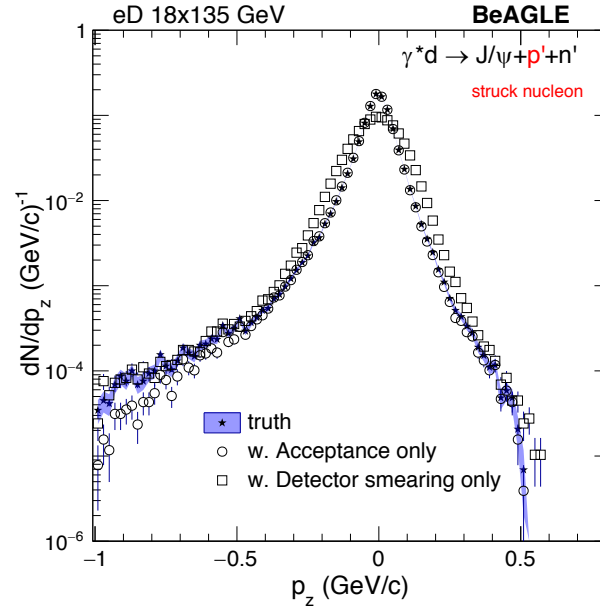
7 mrad

High momentum tail gradually comes back when increase the size of neutron detector

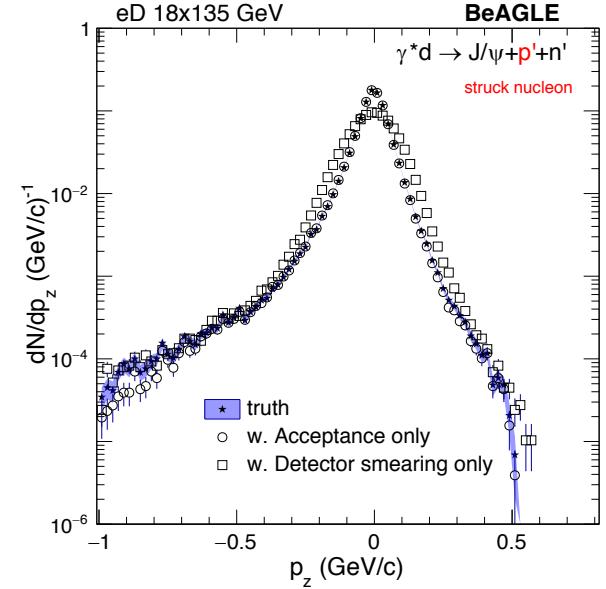
# Neutron detector acceptance - $p_z$



5 mrad



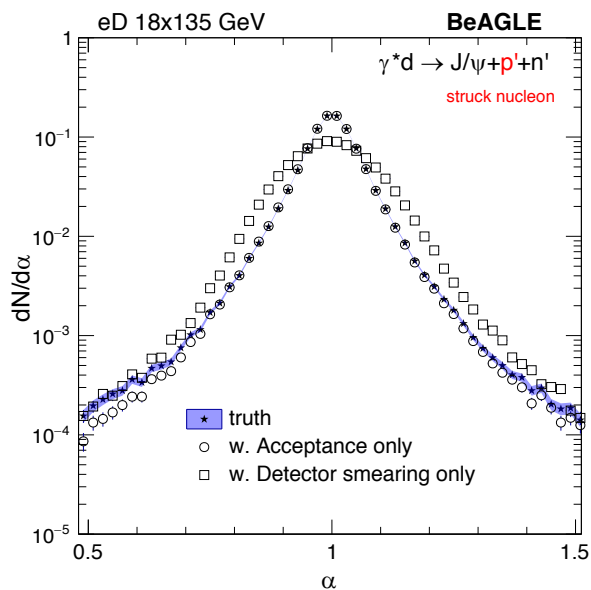
6 mrad



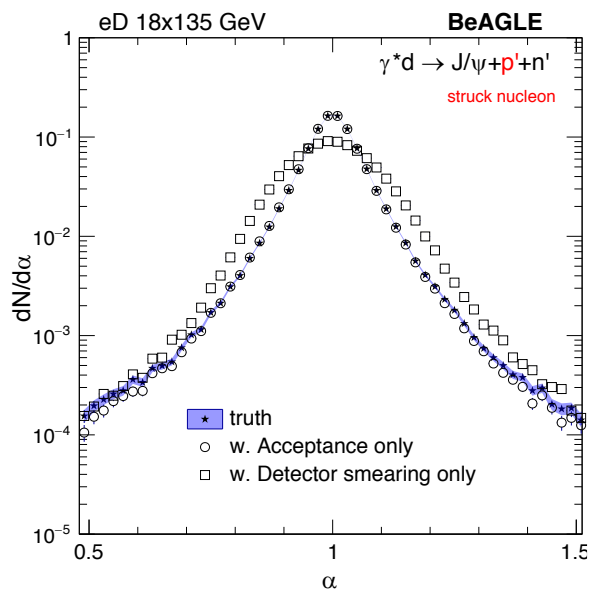
7 mrad

High momentum tail gradually comes back when increase the size of neutron detector

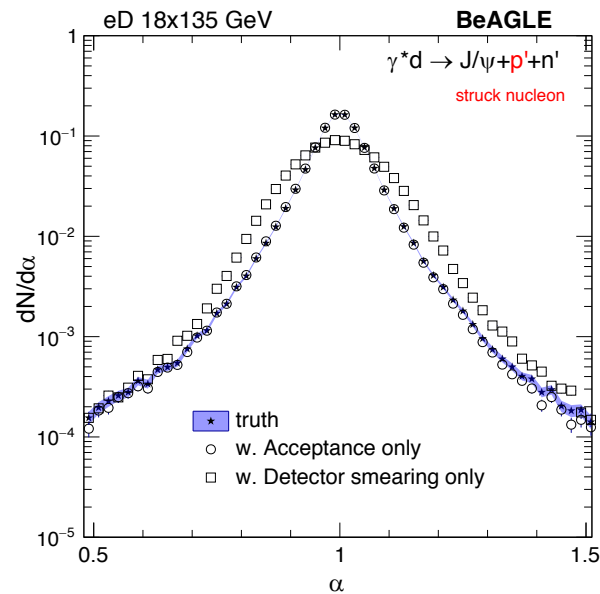
# Neutron detector acceptance - alpha



5 mrad



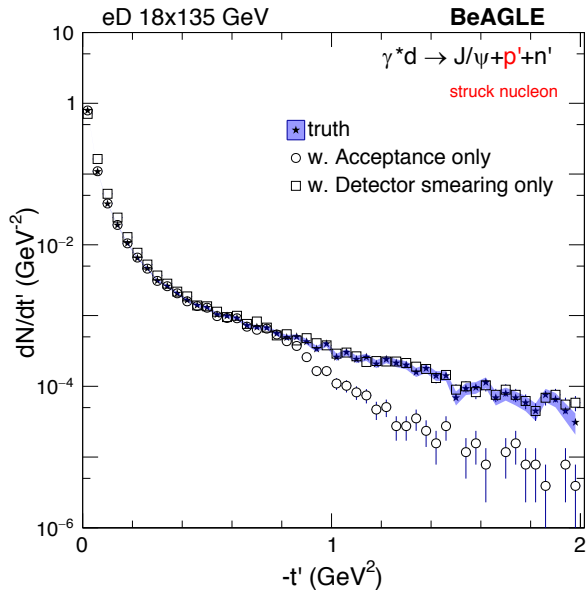
6 mrad



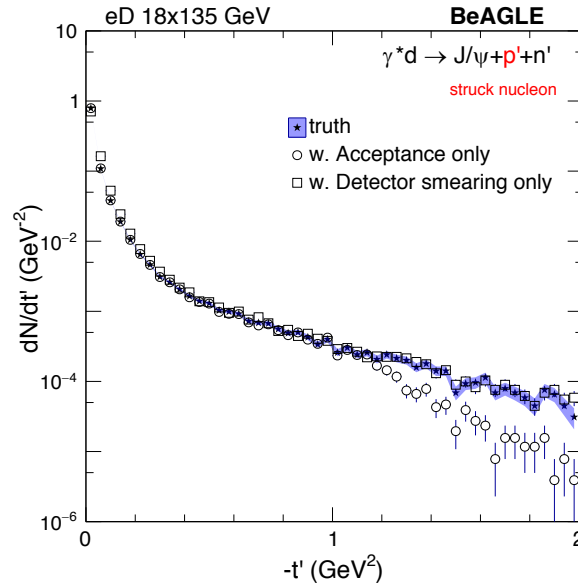
7 mrad

High momentum tail gradually comes back when increase the size of neutron detector

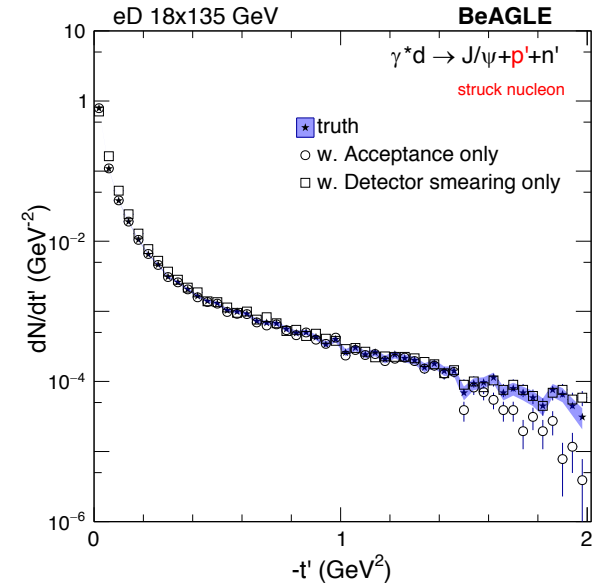
# Neutron detector acceptance – t'



5 mrad



6 mrad



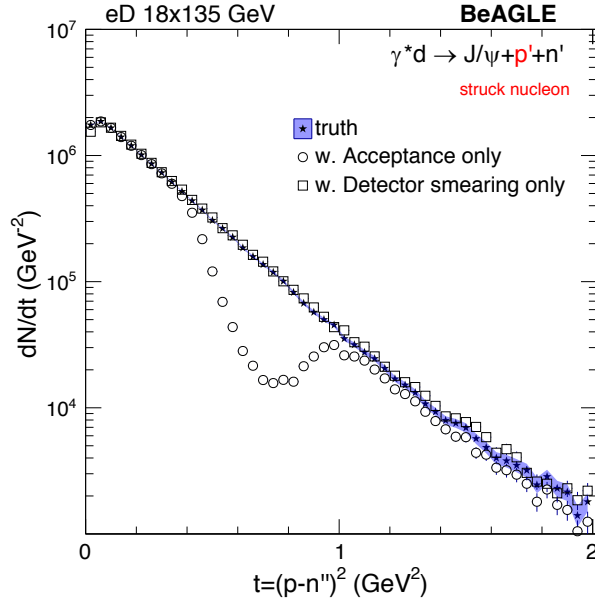
7 mrad

Neutron spectator tagging

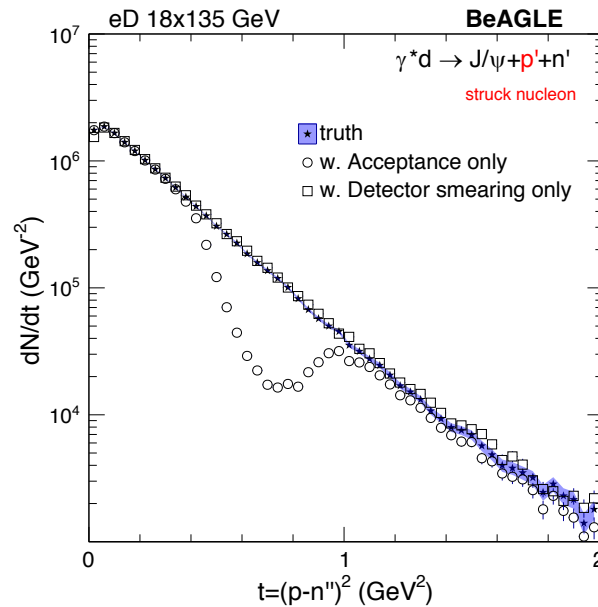
High  $t'$  gradually comes back when increase the size of neutron detector



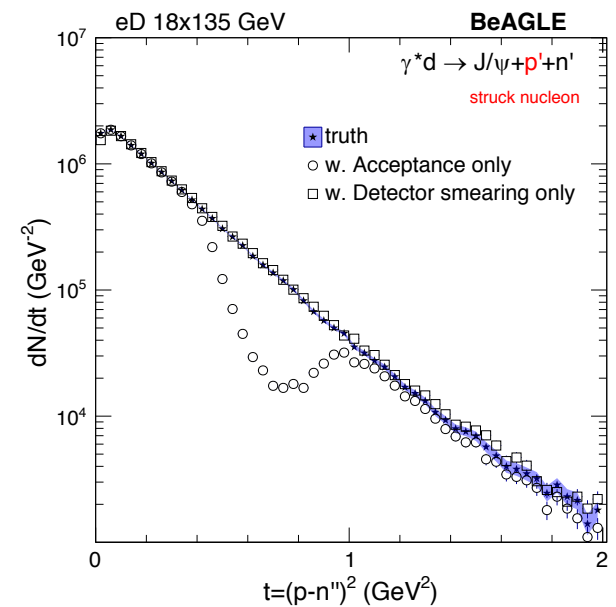
# Neutron detector acceptance – t



5 mrad



6 mrad

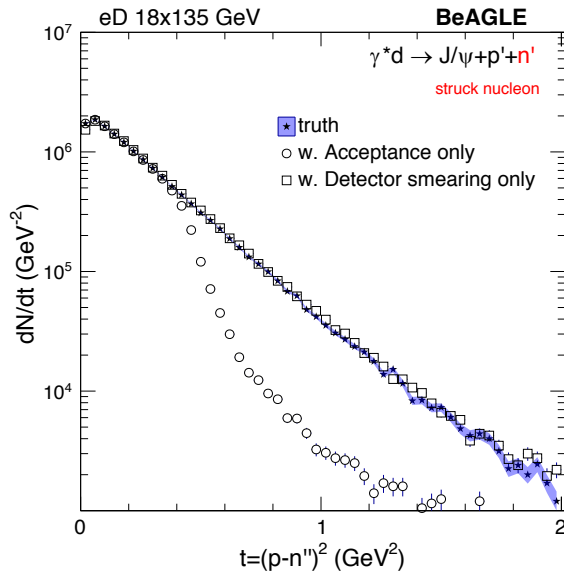


7 mrad

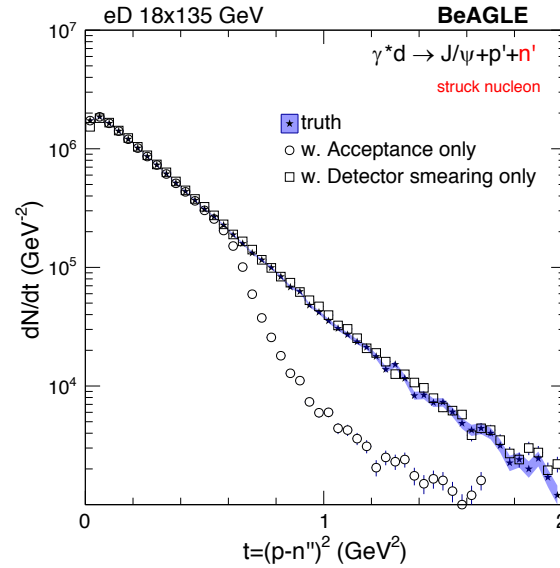
Neutron spectator double tagging

- Very small differences, because most of spectator neutron are within acceptance of 5 mrad, only gain at some very high momentum tail.
- For DVCS, we are interested in hitting neutron. See next slide.

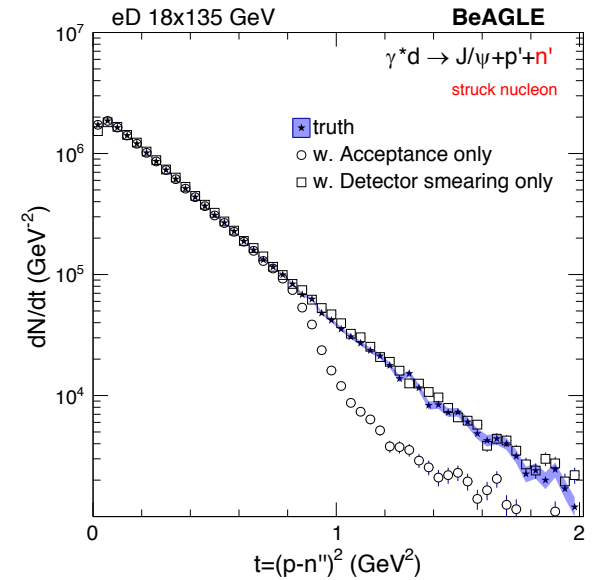
# Neutron detector acceptance – t



5 mrad



6 mrad



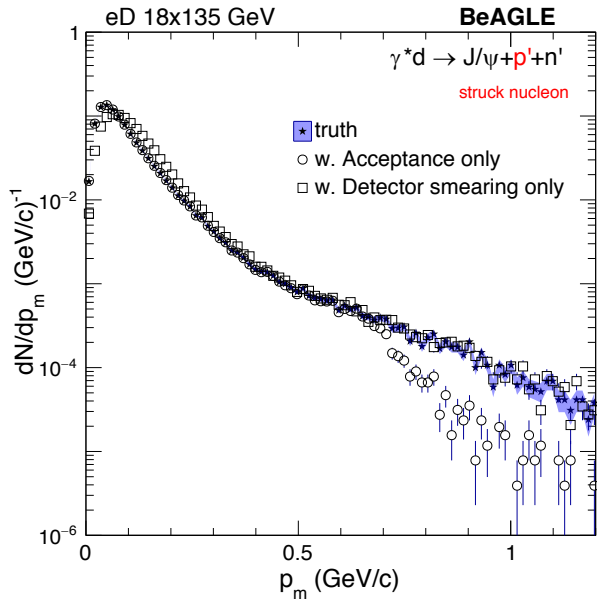
7 mrad

## Proton spectator double tagging

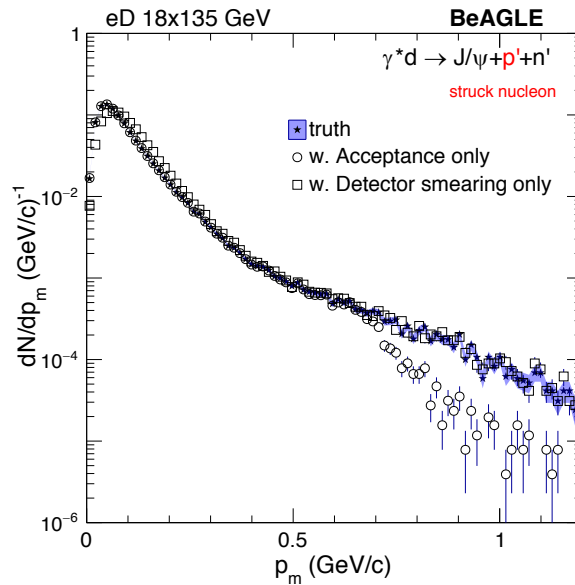
- Significant differences are observed. Full acceptance in  $t$  up to 800  $\text{MeV}^2$  for 7 mrad.
- More physics impact studies might be needed to justify for large neutron detector?

# **Neutron detector energy resolution**

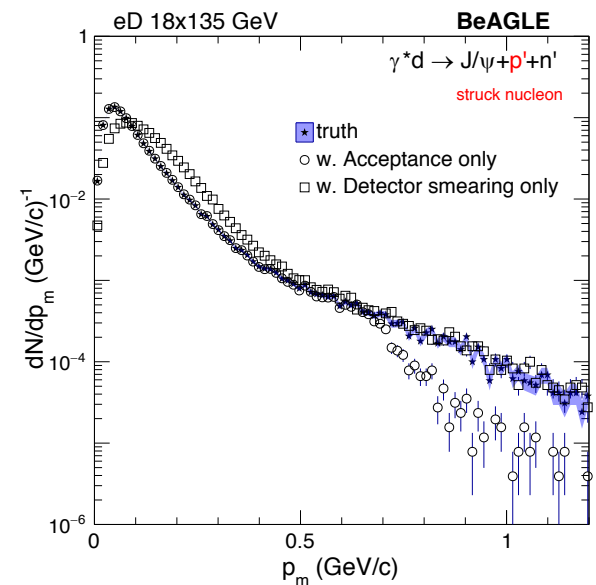
# Neutron detector energy resolution - $p_m$



50%/sqrt(E)



30%/sqrt(E)

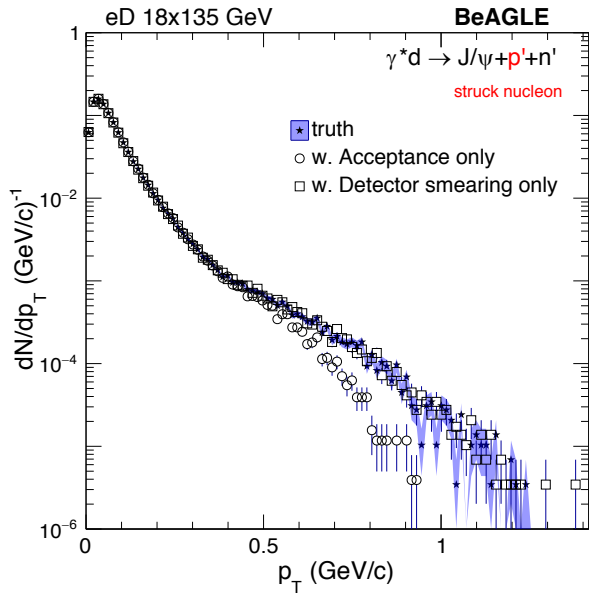


100%/sqrt(E)

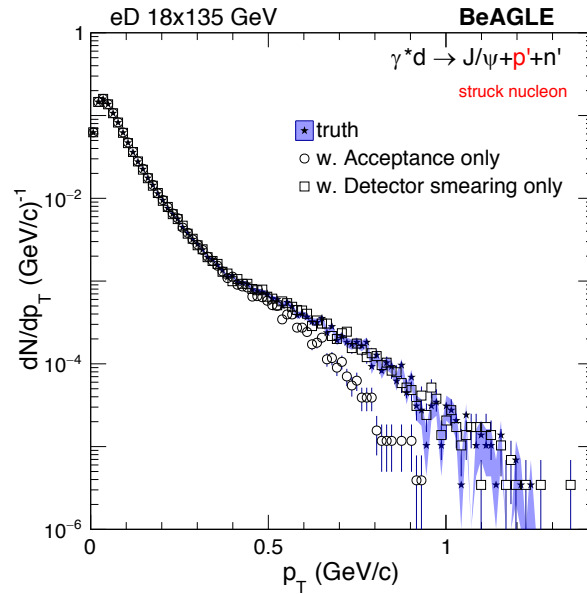
- The worst scenario is still better than the STAR ZDC since the constant term here is 5%. The STAR ZDC has  $\sim 10\%$  for the constant term.
- Low momentum has stronger smearing for poorer resolution.
- High momentum tails are fine.

Reference: STAR ZDC 85%/sqrt(E) + 9.1%, ZEUS ZDC 35%/sqrt(E) + 2% 36

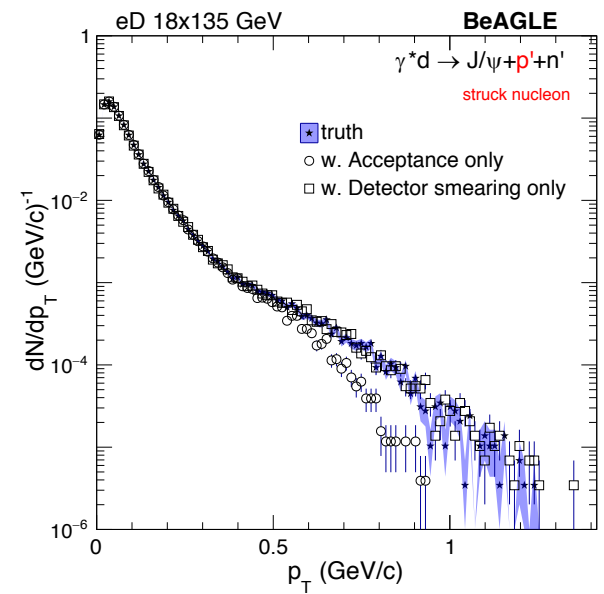
# Neutron detector energy resolution - $p_T$



50%/sqrt(E)



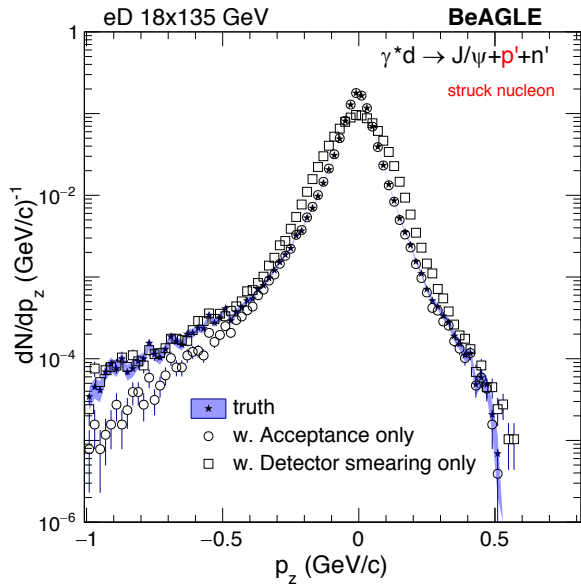
30%/sqrt(E)



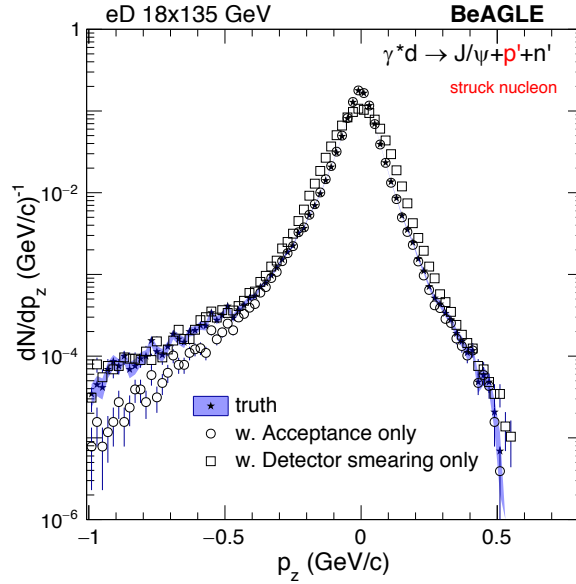
100%/sqrt(E)

- No difference is observed for  $p_T$

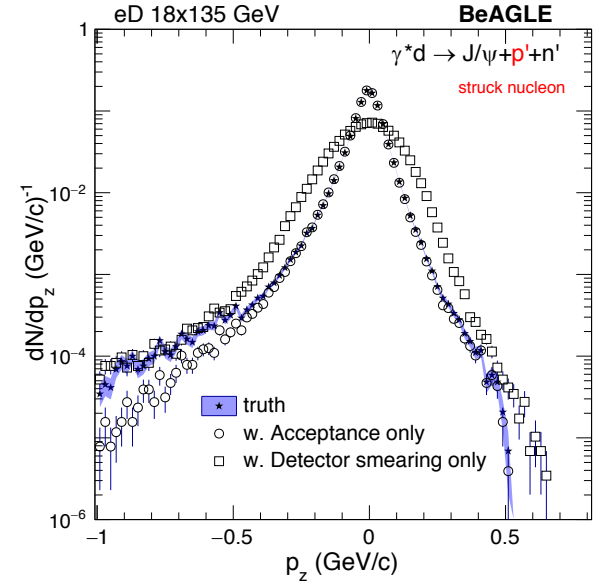
# Neutron detector energy resolution - $p_z$



50%/sqrt(E)



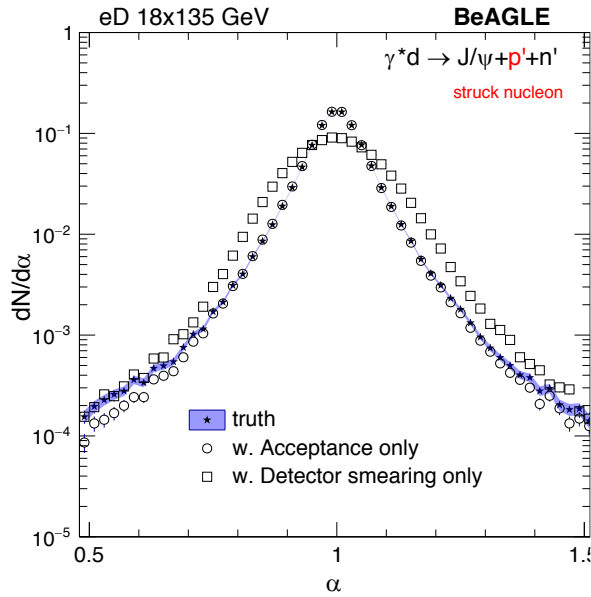
30%/sqrt(E)



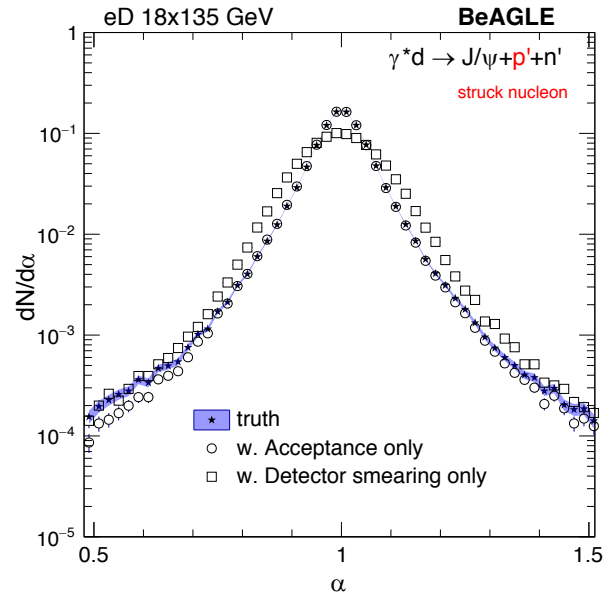
100%/sqrt(E)

- Like  $p_m$  where difference is obvious.

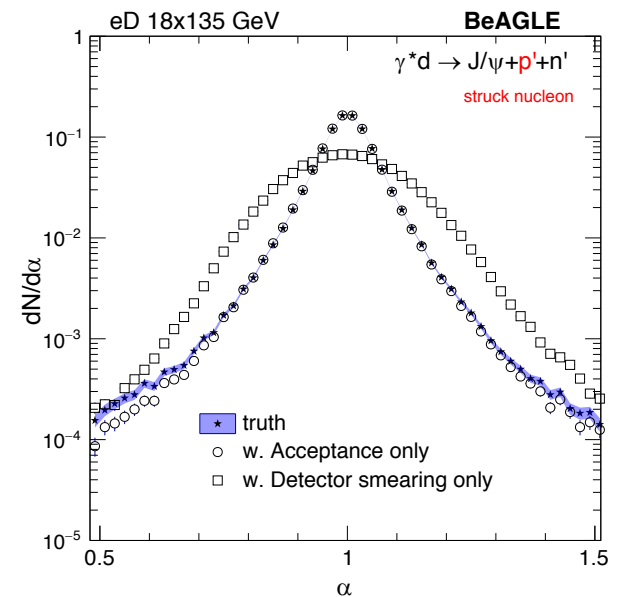
# Neutron detector energy resolution - alpha



50%/sqrt(E)



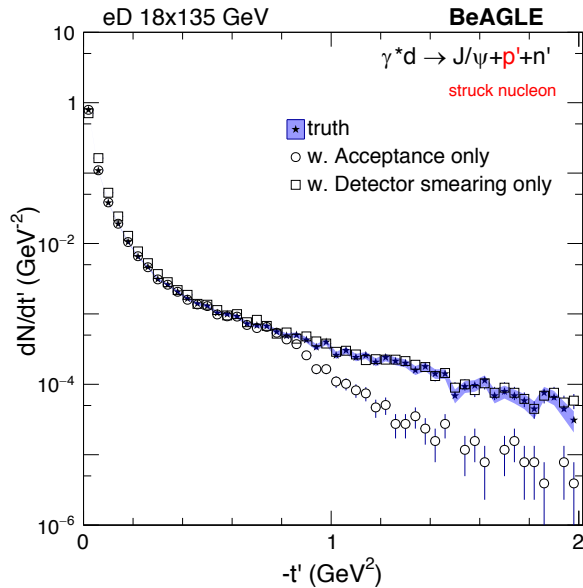
30%/sqrt(E)



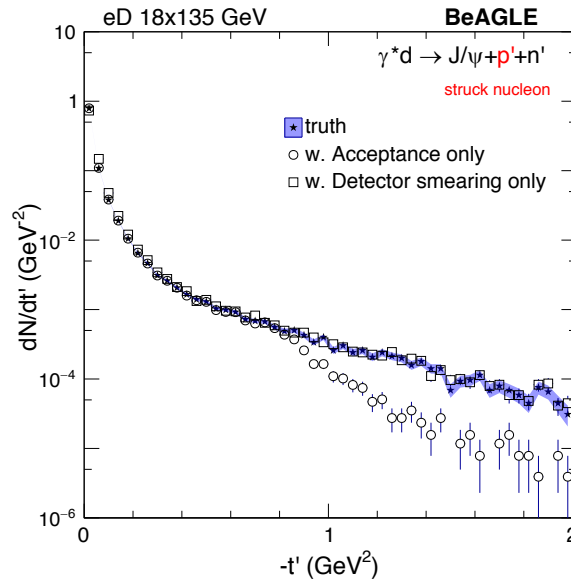
100%/sqrt(E)

- Like  $p_m$  where difference is obvious.

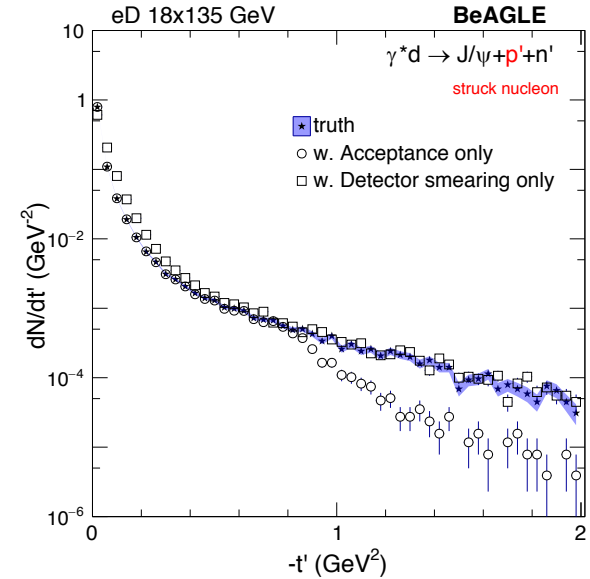
# Neutron detector energy resolution – $t'$



50%/sqrt(E)



30%/sqrt(E)

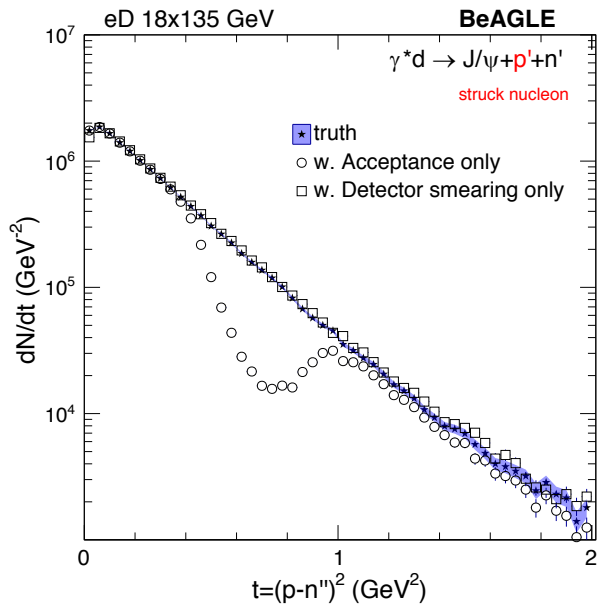


100%/sqrt(E)

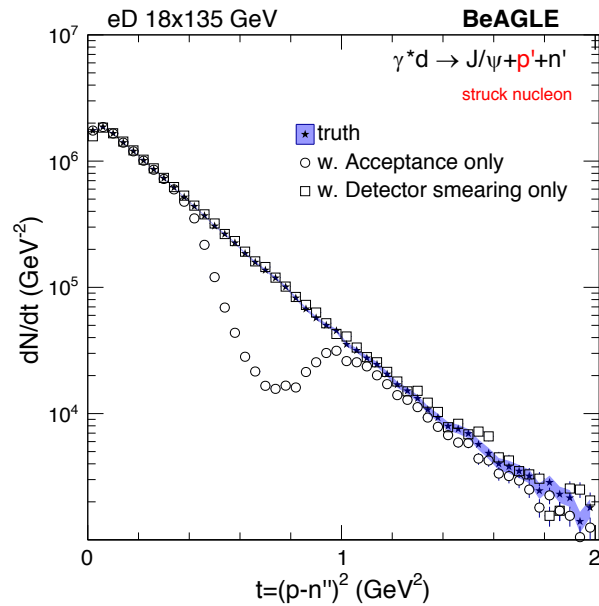
- See some difference at low  $t'$ . This will significantly affect the low  $t'$  extrapolation. Unfolding technique needs to be applied for analysis anyway, but its uncertainty is correlated to how good the resolution is



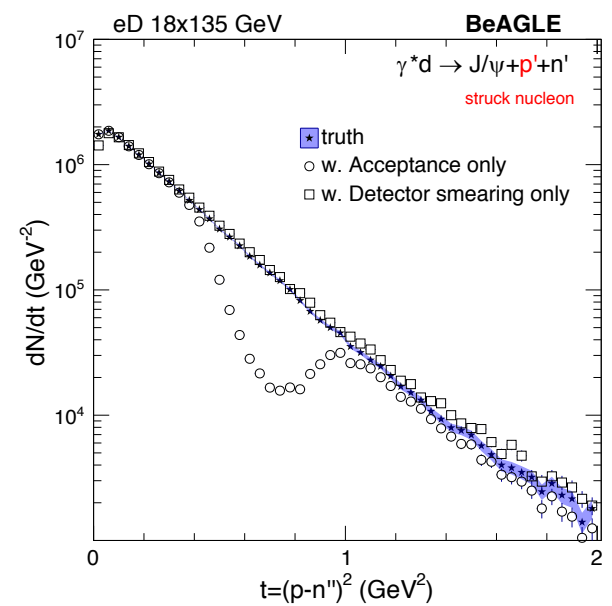
# Neutron detector energy resolution – t



50%/sqrt(E)



30%/sqrt(E)



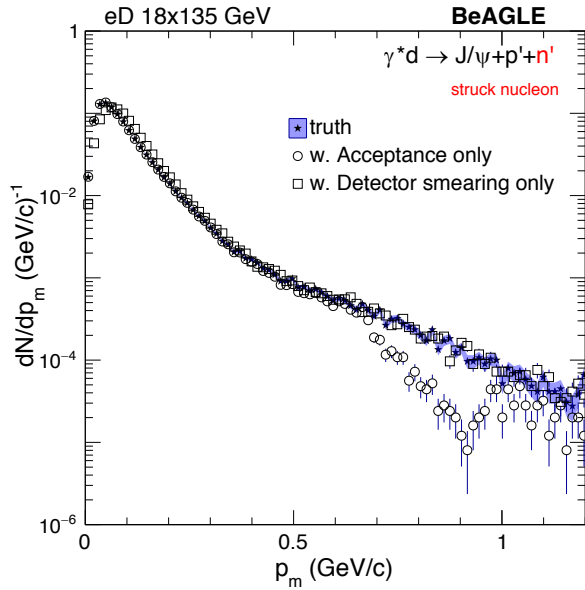
100%/sqrt(E)

Neutron spectator double tagging

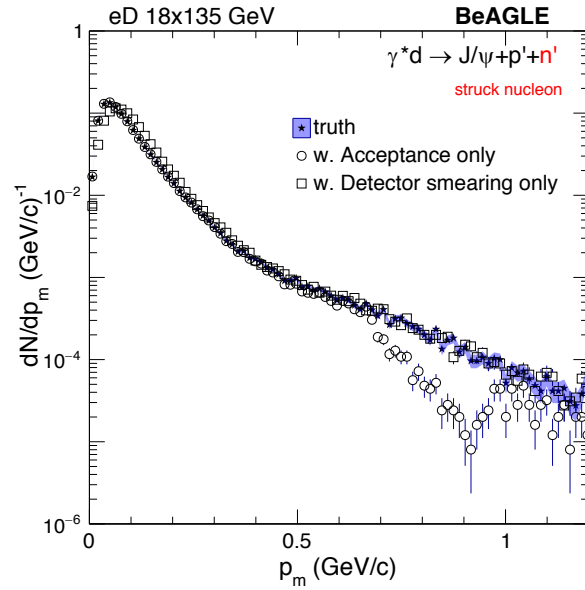
- Some small difference can be seen.
- In the resolution study, proton spectator double tagging case is just the same.

# **Proton detector momentum resolution**

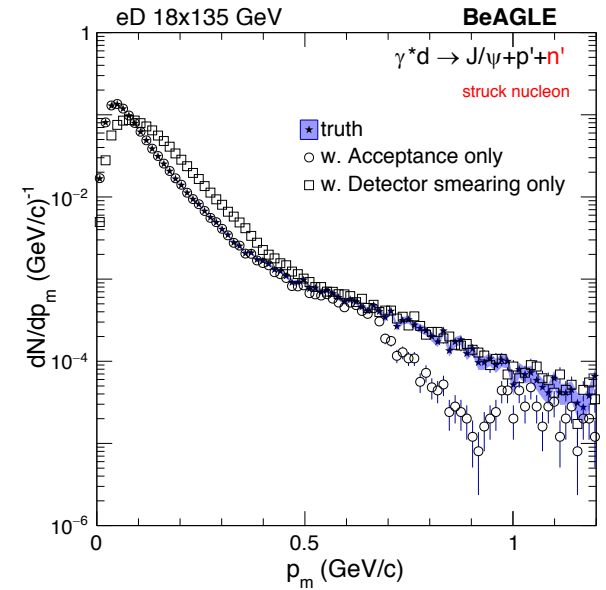
# Proton detector momentum resolution - $p_m$



dpt/pt = 3%



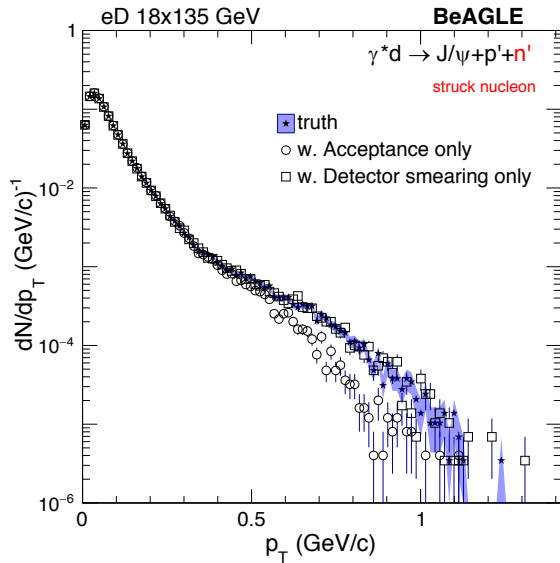
dpt/pt = 5%



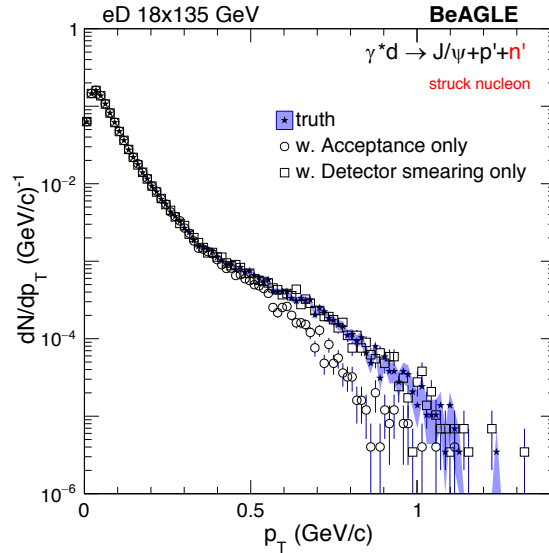
dpt/pt = 10%

- Same conclusion as for neutron detector energy resolution study

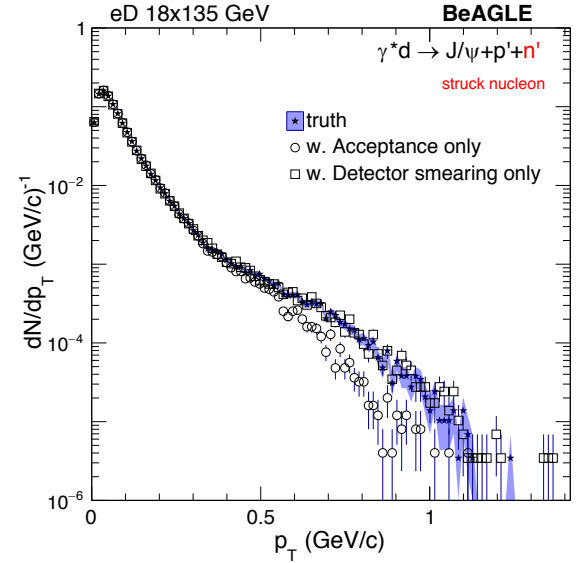
# Proton detector momentum resolution - $p_T$



dpt/pt = 3%



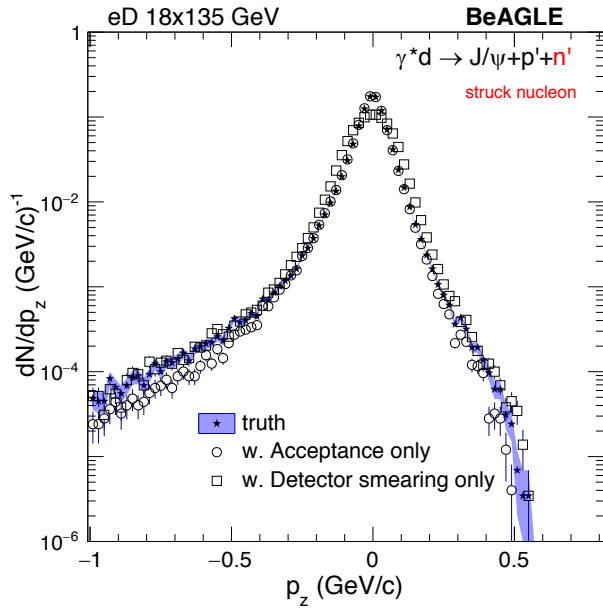
dpt/pt = 5%



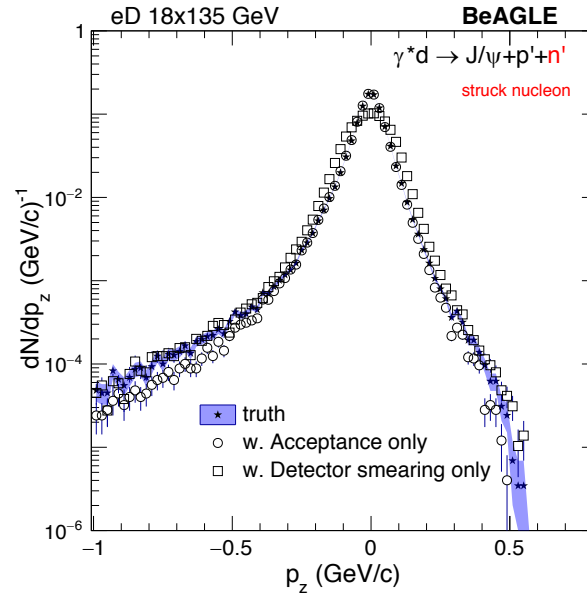
dpt/pt = 10%

- Still very robust on the  $p_T$

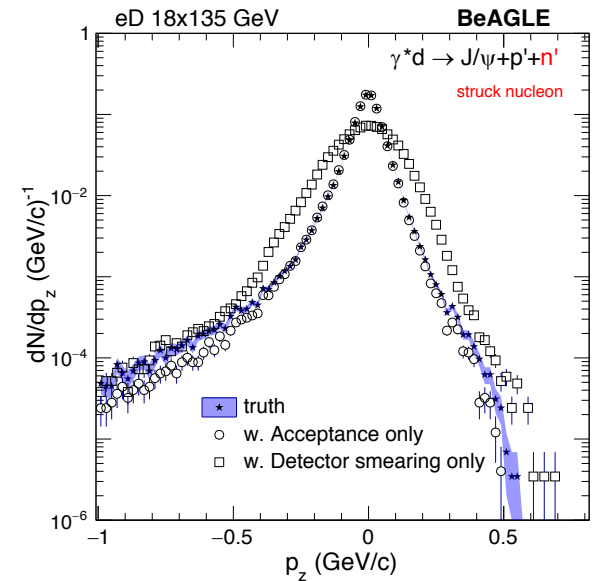
# Proton detector momentum resolution - $p_z$



dpt/pt = 3%



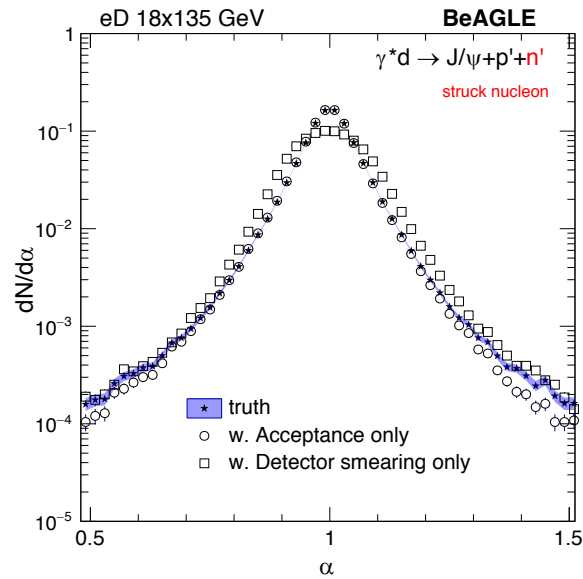
dpt/pt = 5%



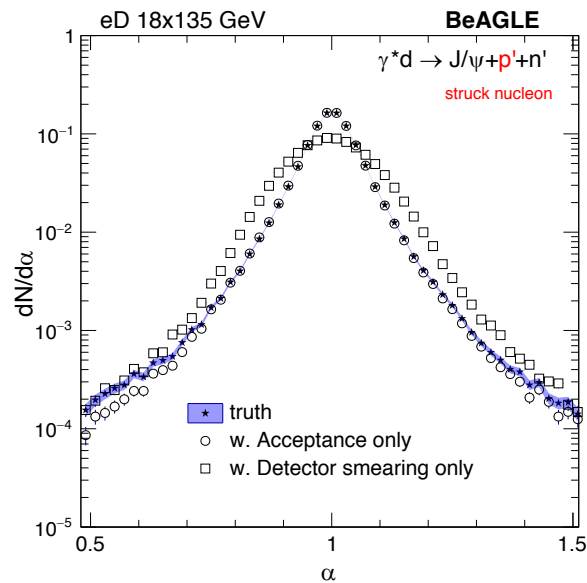
dpt/pt = 10%

- Same conclusion as for neutron detector energy resolution study

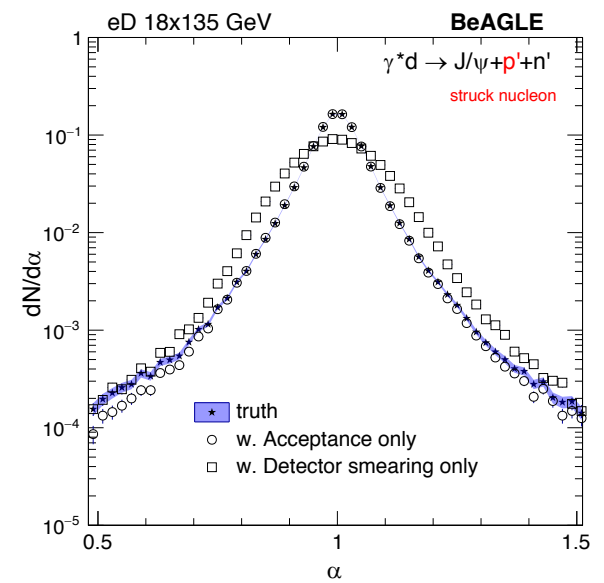
# Proton detector momentum resolution - alpha



dpt/pt = 3%



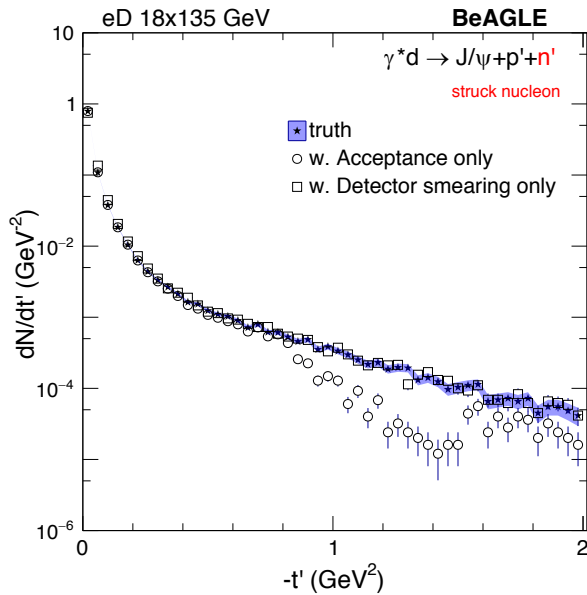
dpt/pt = 5%



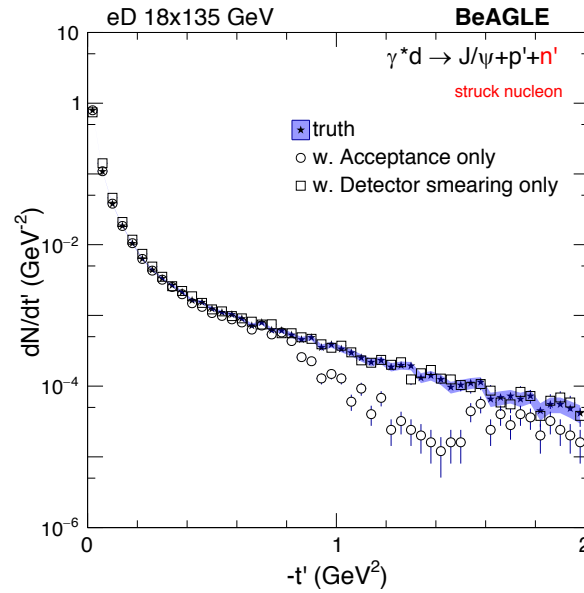
dpt/pt = 10%

- Same conclusion as for neutron detector energy resolution study

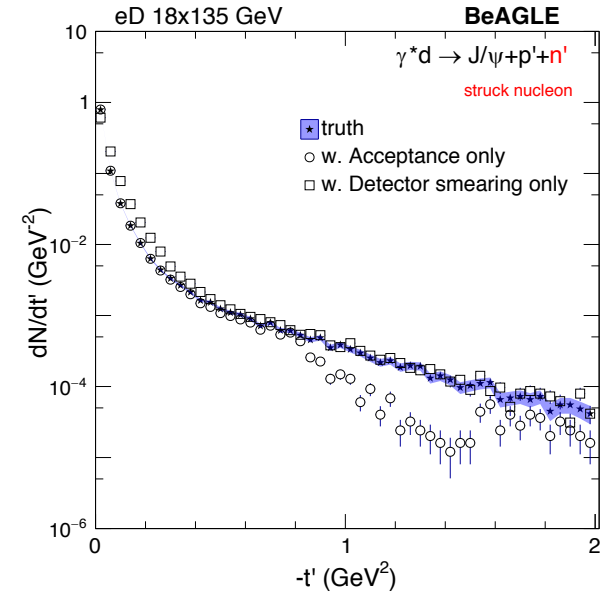
# Proton detector momentum resolution – $t'$



dpt/pt = 3%



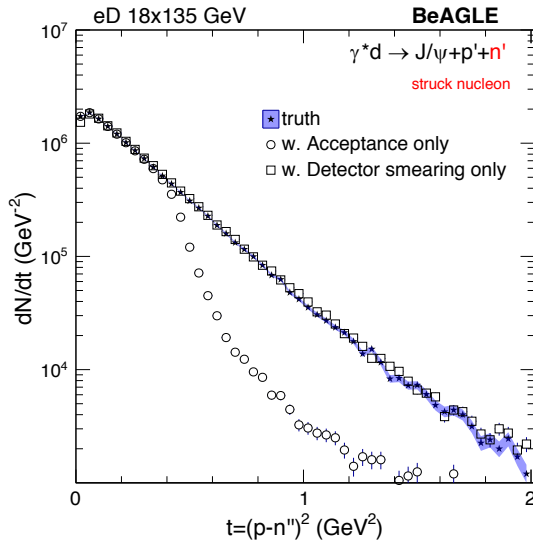
dpt/pt = 5%



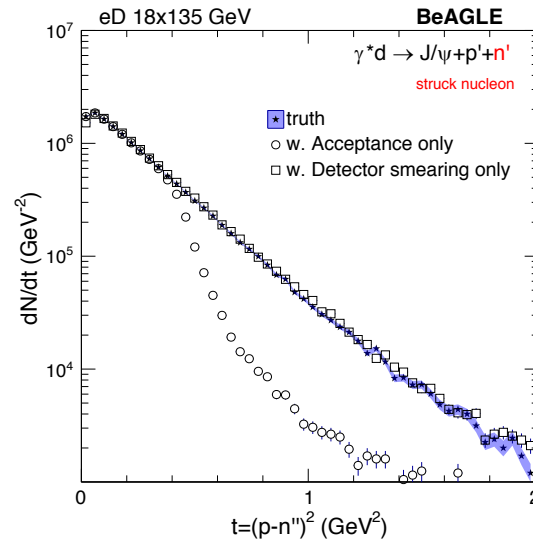
dpt/pt = 10%

- Same conclusion as for neutron detector energy resolution study

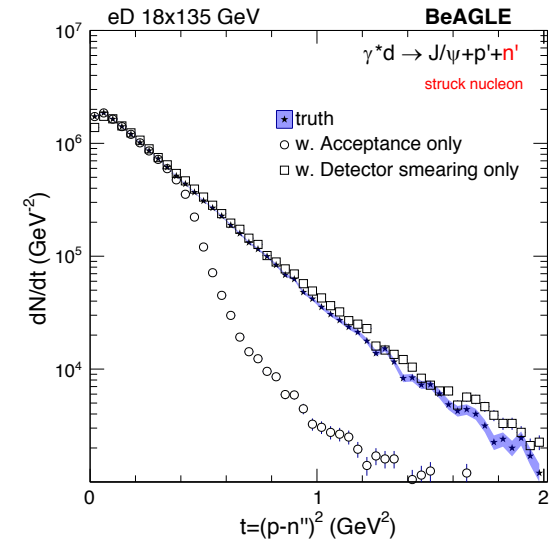
# Proton detector momentum resolution – t



dpt/pt = 3%



dpt/pt = 5%



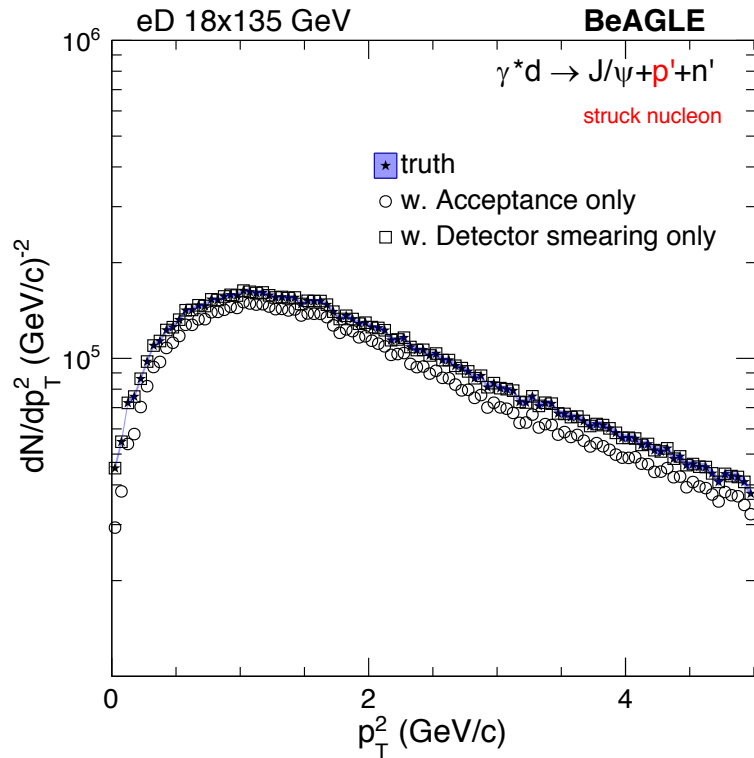
dpt/pt = 10%

Proton spectator double tagging

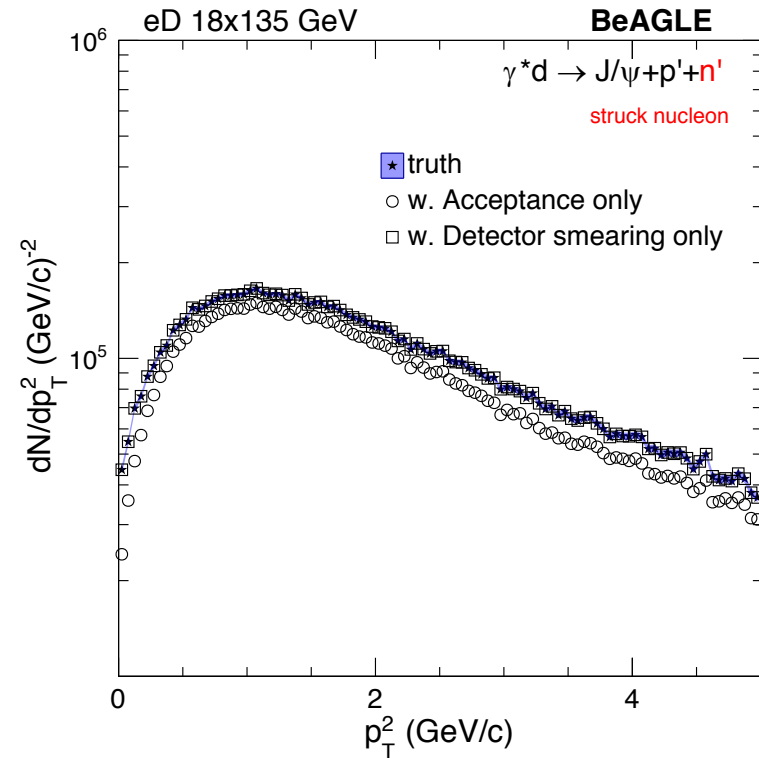
- Same conclusion as for neutron detector energy resolution study



# Jpsi distributions – no detector effect



Neutron spectator double tagging



Proton spectator double tagging

- Acceptances are on protons and neutrons only, the shift is due to requirement of double tagging

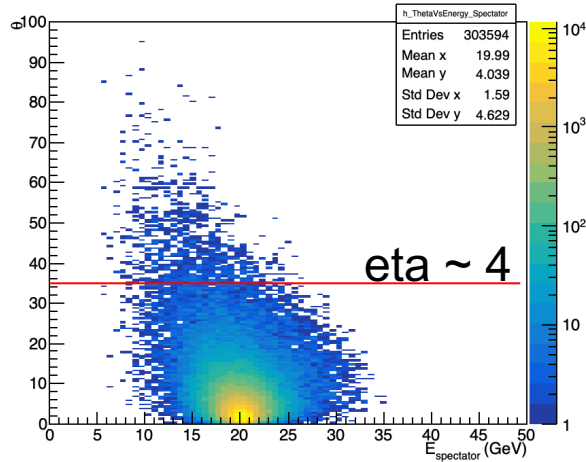
# Energy configurations comparisons

Disclaimer:

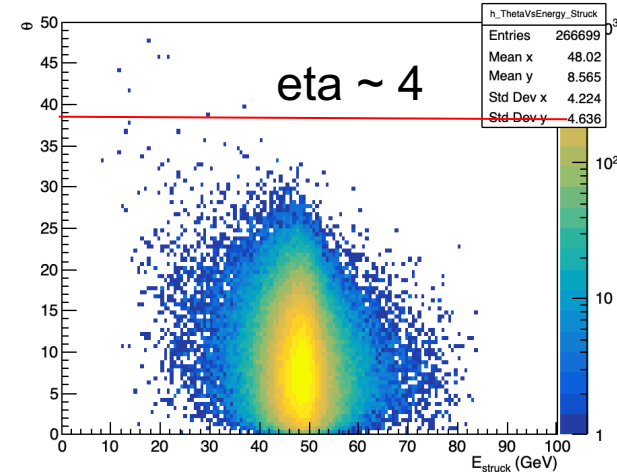
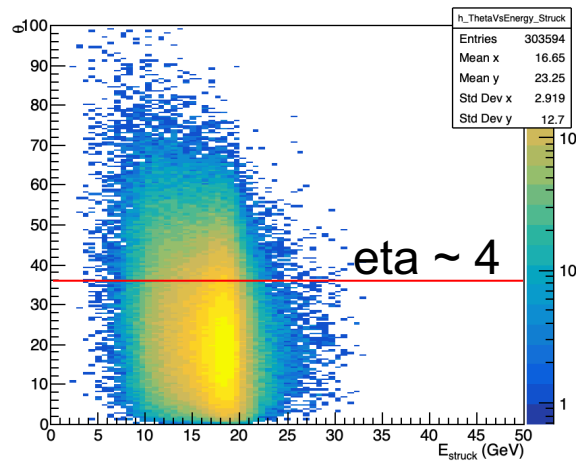
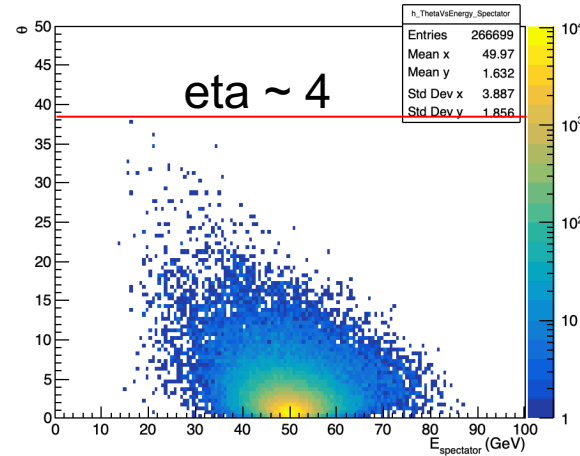
- No central detector is included
- Proton and neutron detectors use default settings

# where are protons and neutrons

5x20 GeV



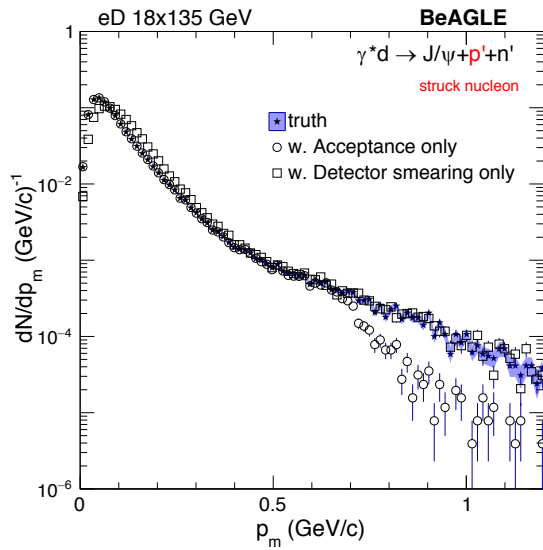
10x50 GeV



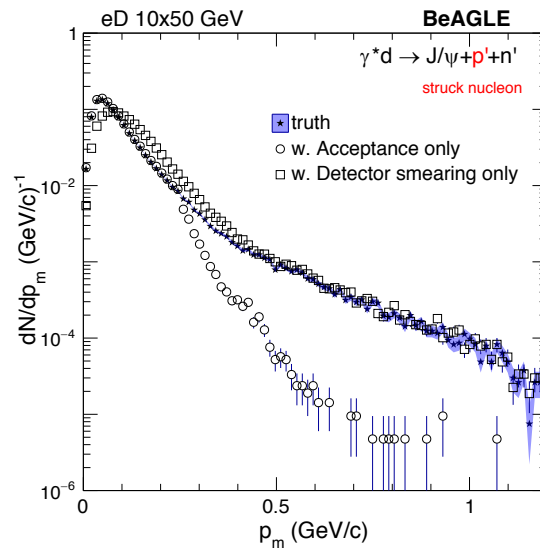
- For low enough energy, nucleons could be in the central tracker!
- Might be a benefit for extreme SRC studies?

# **Neutron spectator**

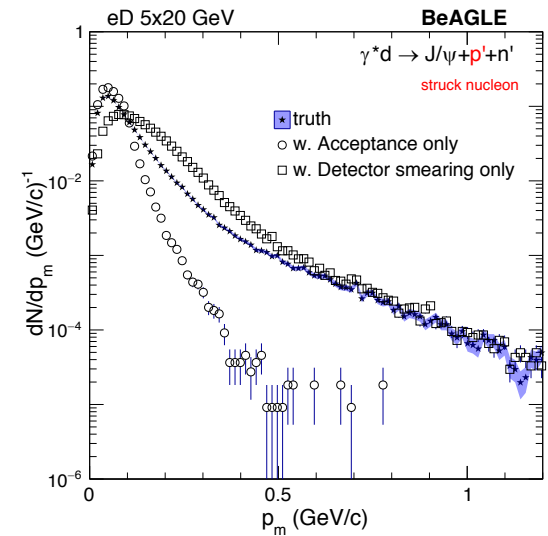
# Neutron spectator - $p_m$



18x135 GeV



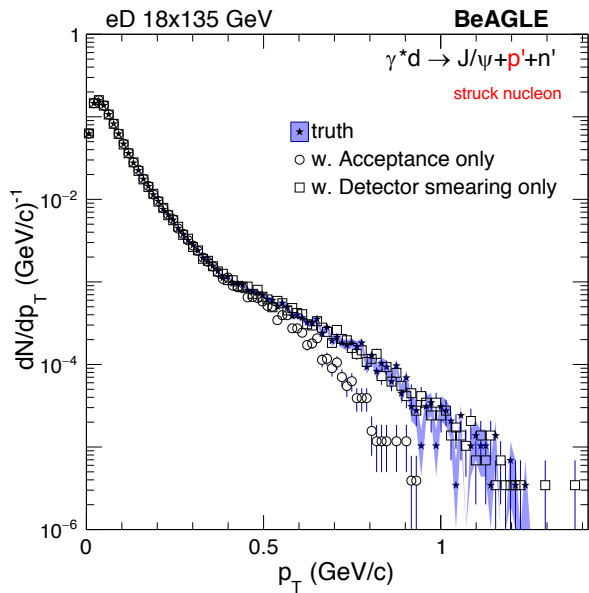
10x50 GeV



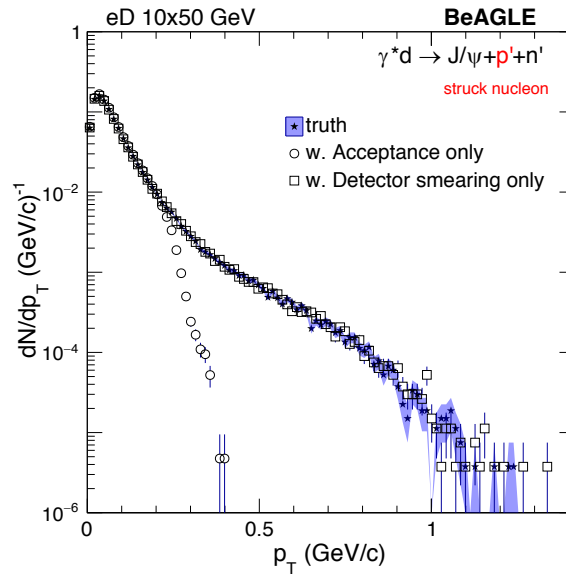
5x20 GeV

- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration

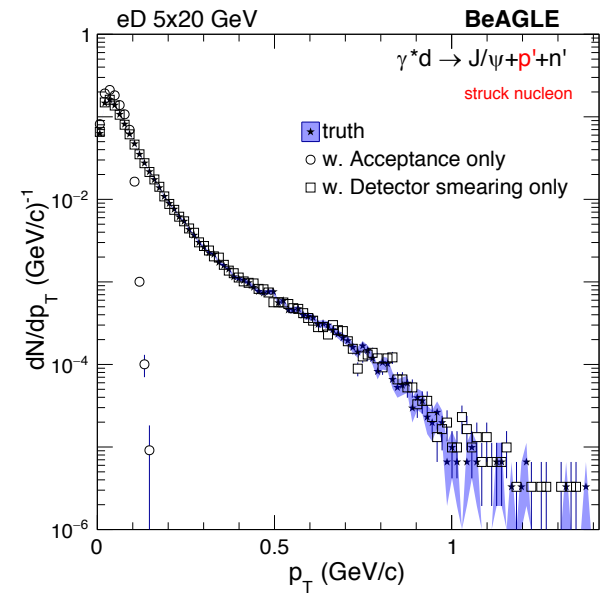
# Neutron spectator - $p_T$



18x135 GeV



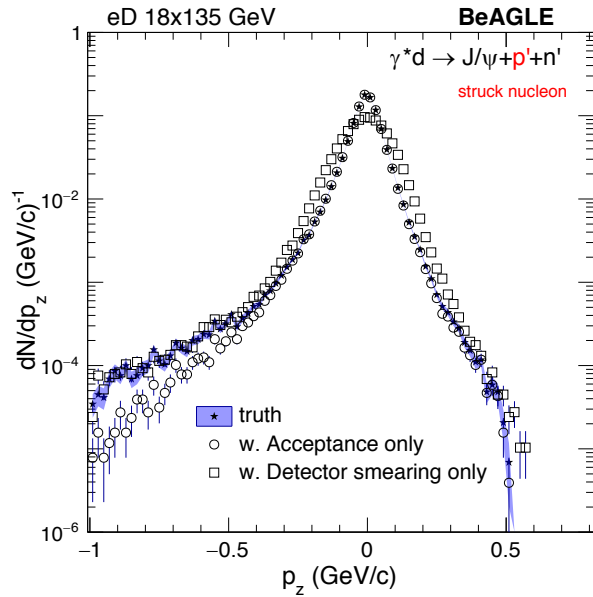
10x50 GeV



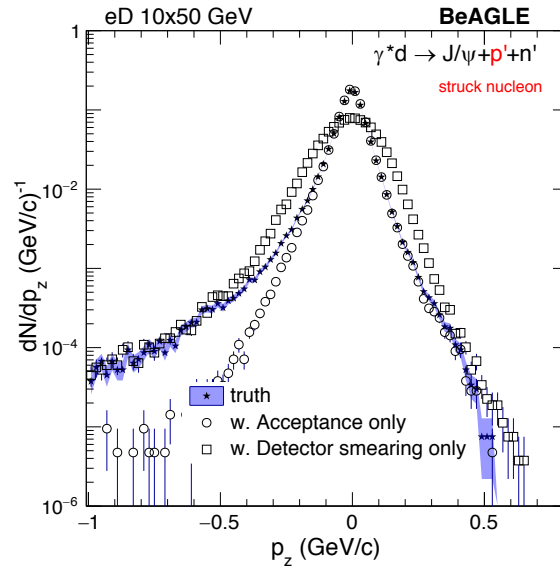
5x20 GeV

- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration

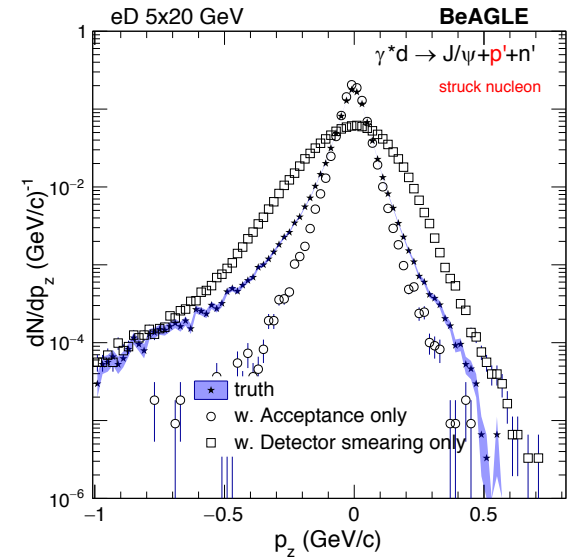
# Neutron spectator - $p_z$



18x135 GeV



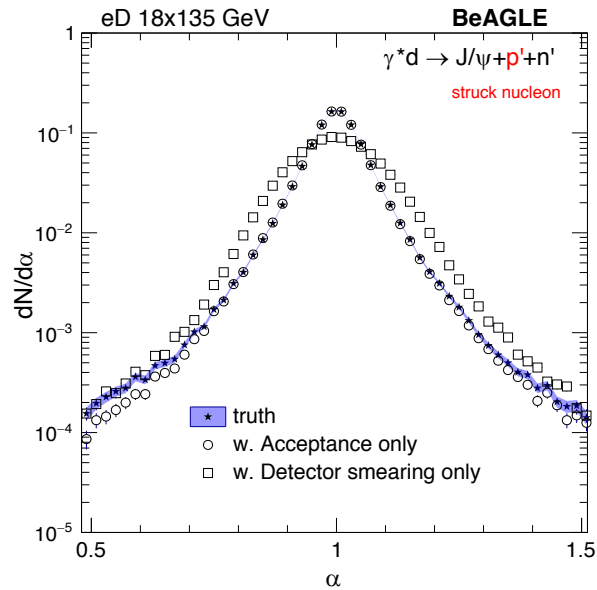
10x50 GeV



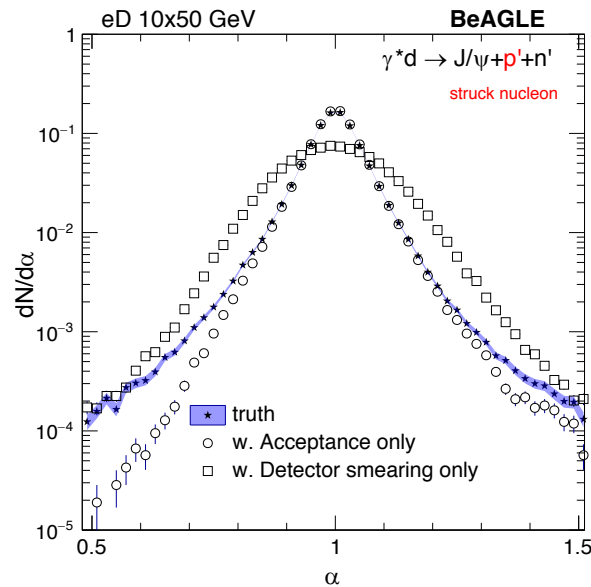
5x20 GeV

- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration

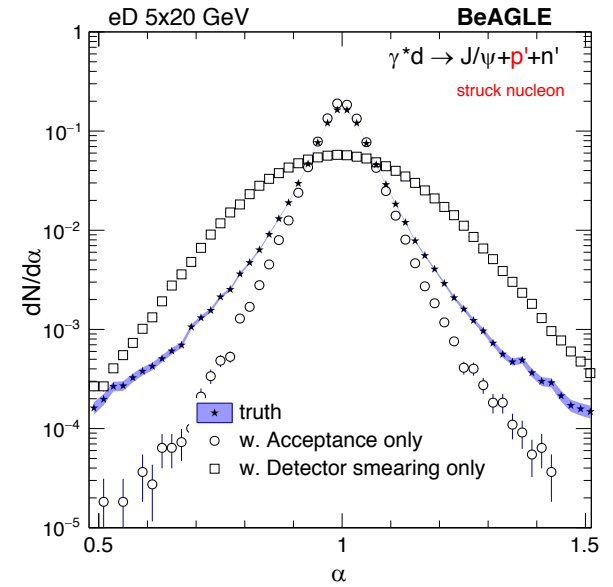
# Neutron spectator - alpha



18x135 GeV



10x50 GeV

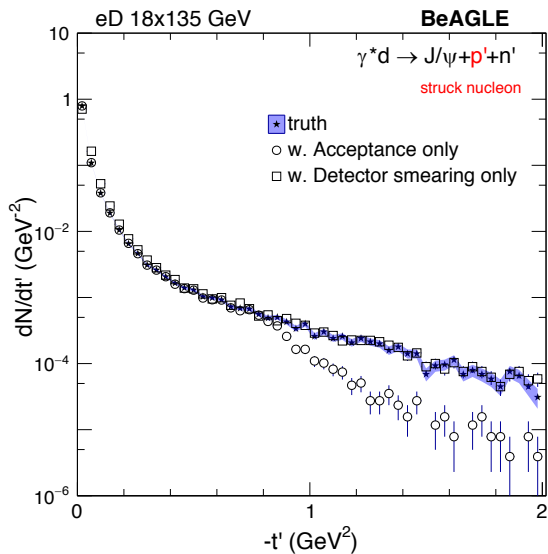


5x20 GeV

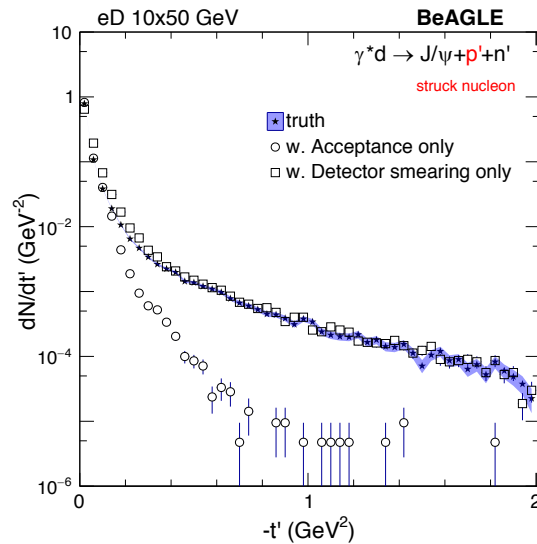
- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration



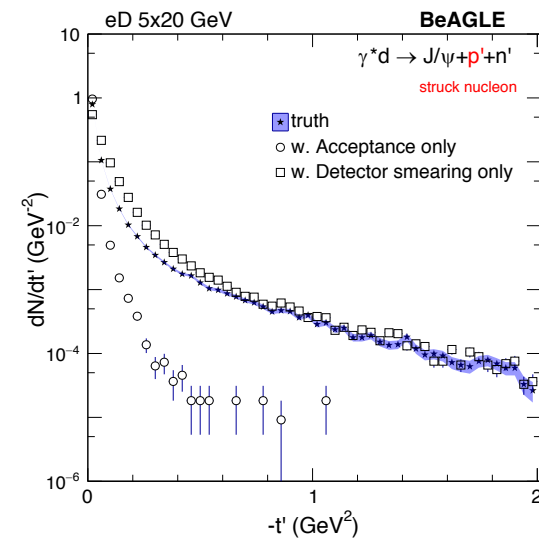
# Neutron spectator – t'



18x135 GeV



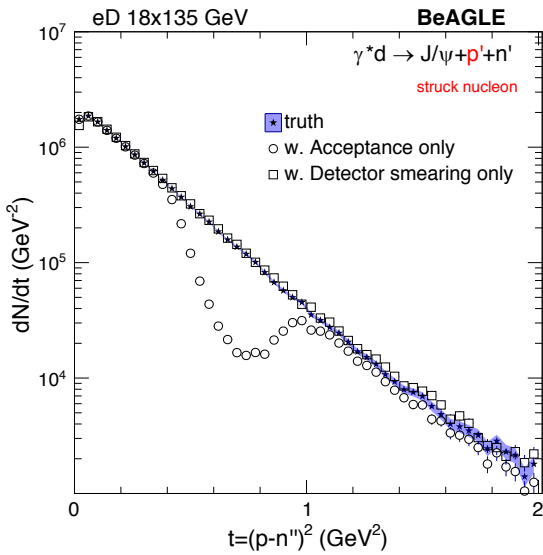
10x50 GeV



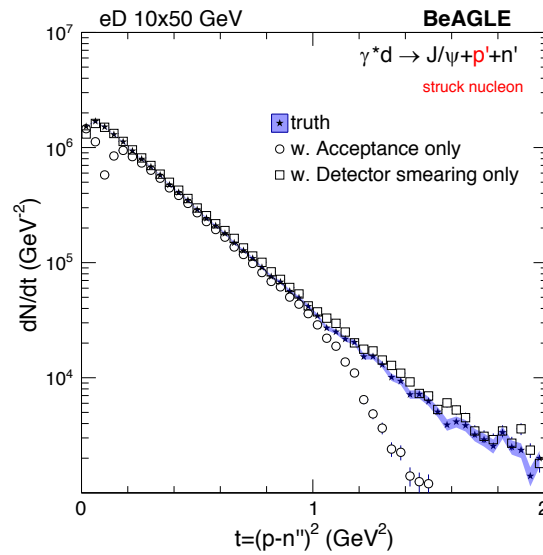
5x20 GeV

- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration

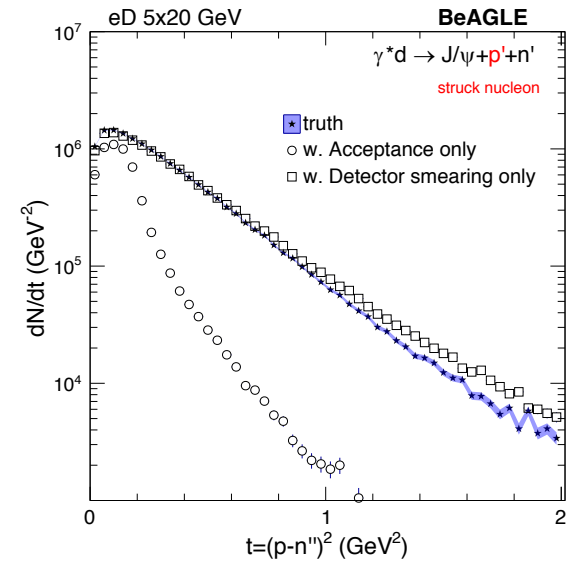
# Neutron spectator – t



18x135 GeV



10x50 GeV

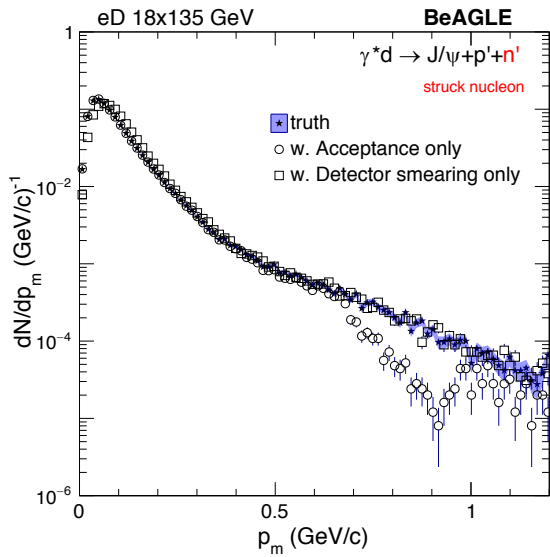


5x20 GeV

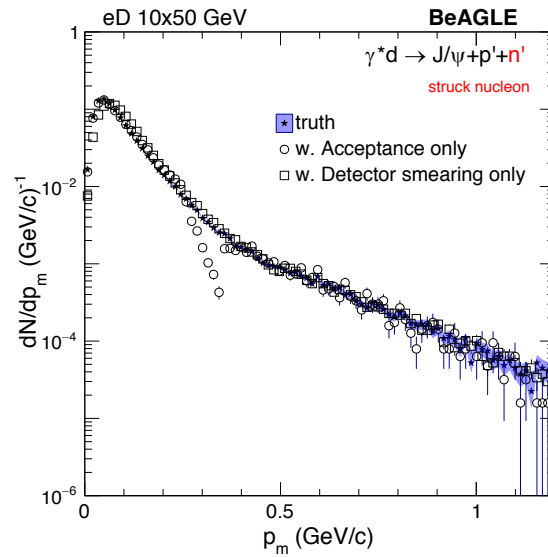
- Significant difference towards low energies.

# Proton spectator

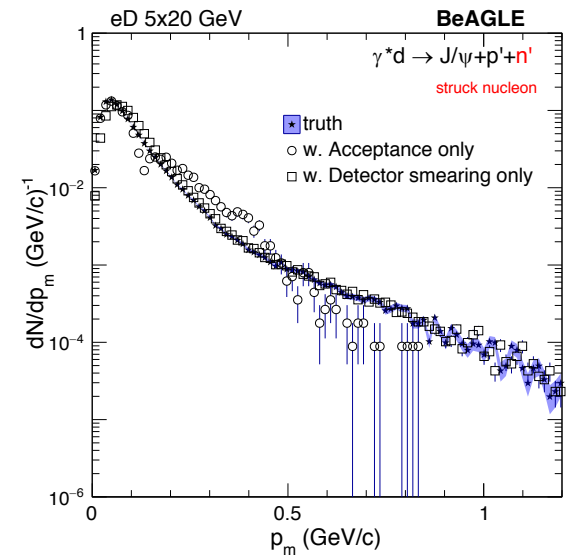
# Proton spectator - $p_m$



18x135 GeV



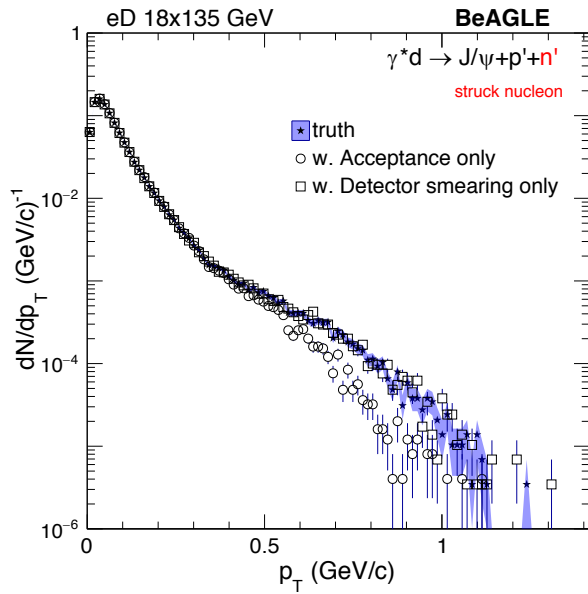
10x50 GeV



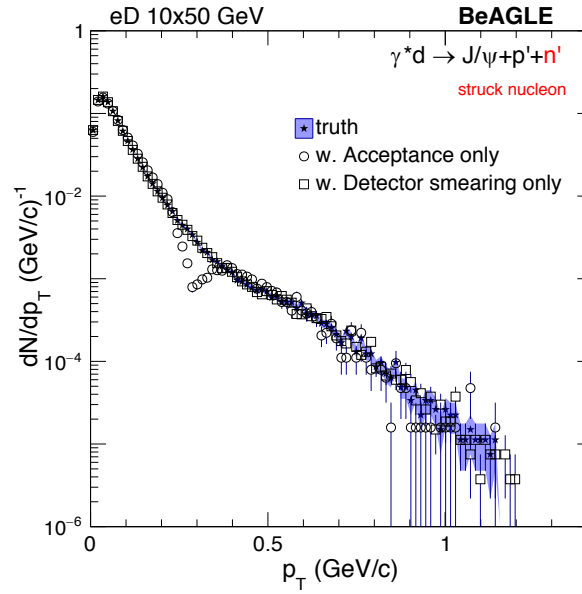
5x20 GeV

- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration

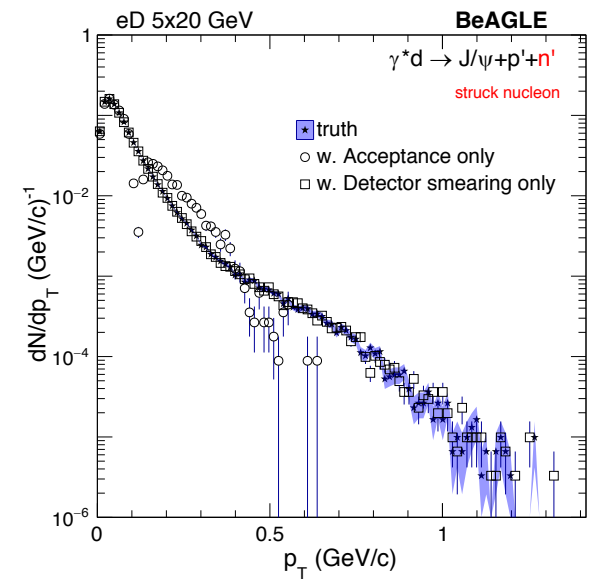
# Proton spectator - $p_T$



18x135 GeV



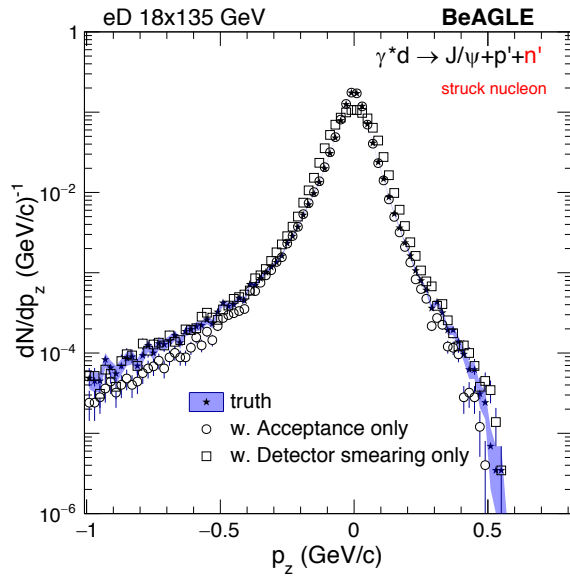
10x50 GeV



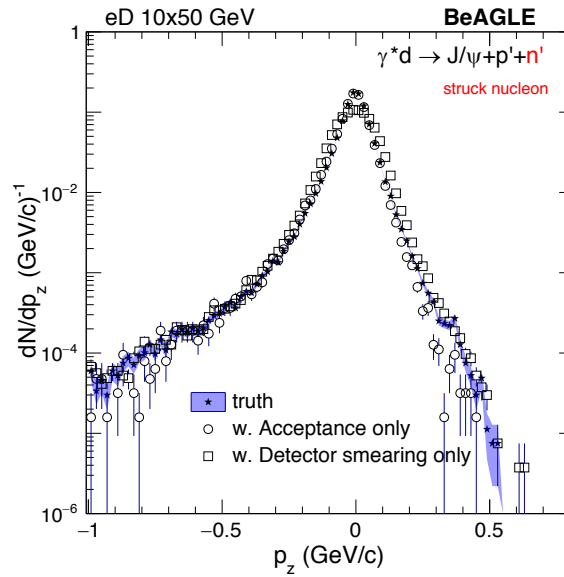
5x20 GeV

- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration

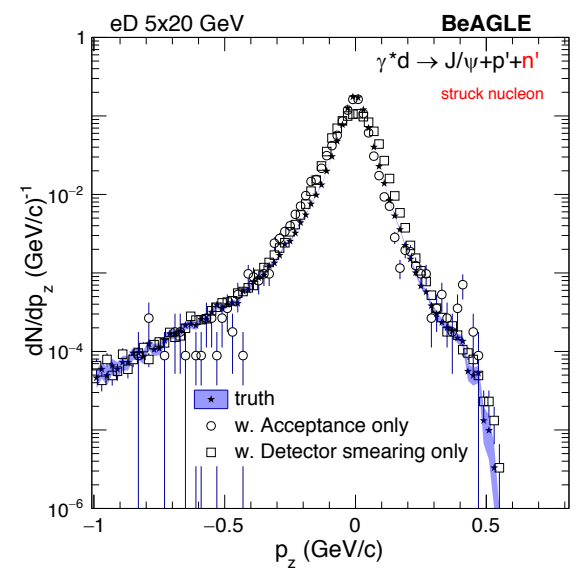
# Proton spectator - $p_z$



18x135 GeV



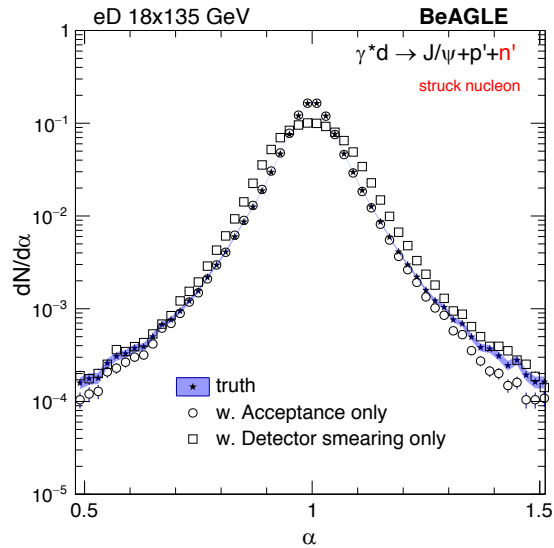
10x50 GeV



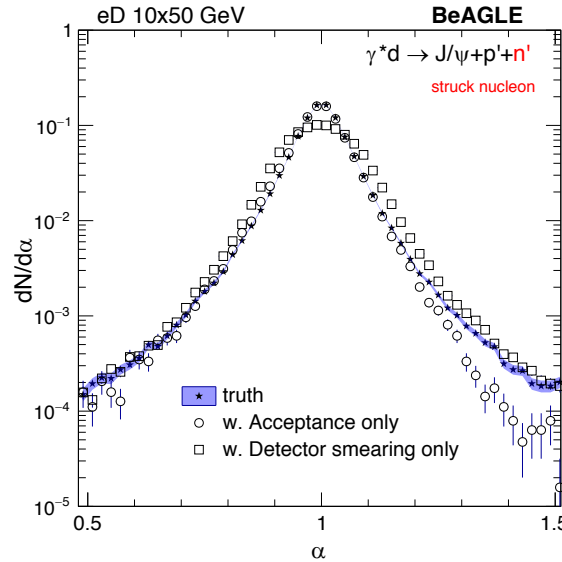
5x20 GeV

- Significant difference towards low energies.
- Starting to see more asymmetries for lower energies.
- SRC studies seem to be better off with higher energy configuration

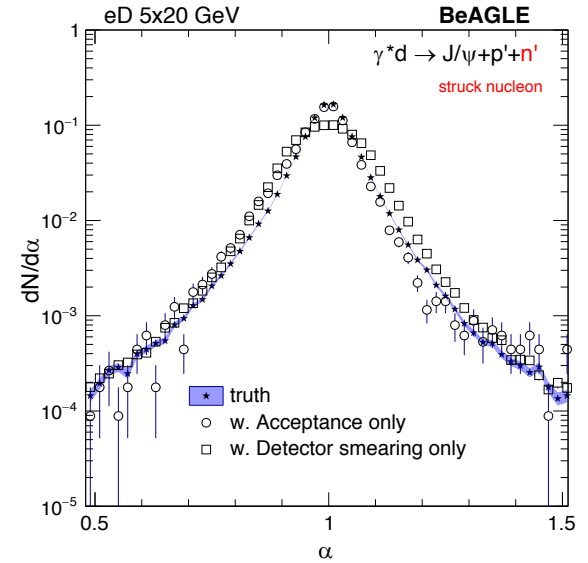
# Proton spectator - alpha



18x135 GeV



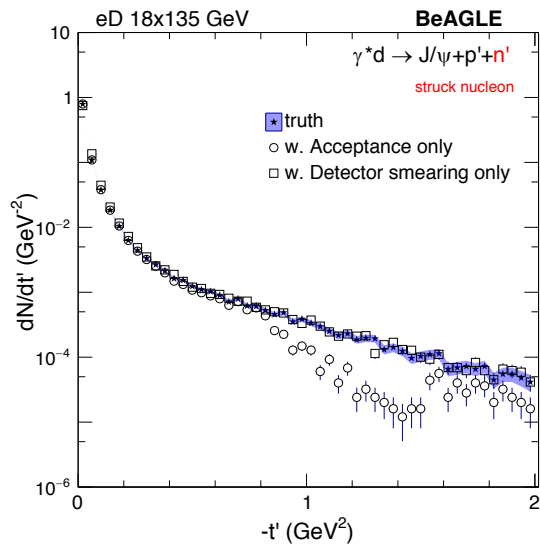
10x50 GeV



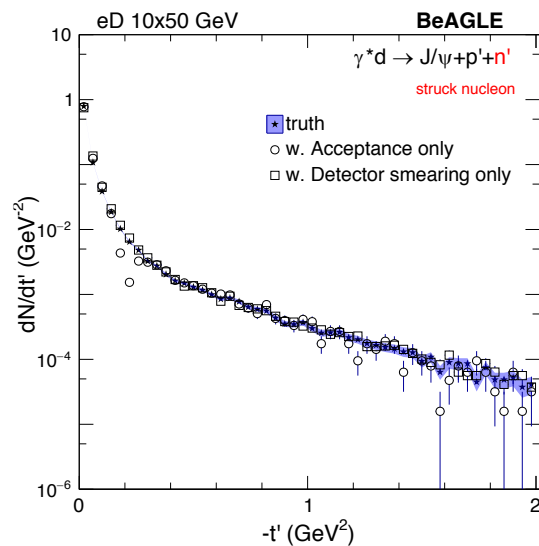
5x20 GeV

- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration

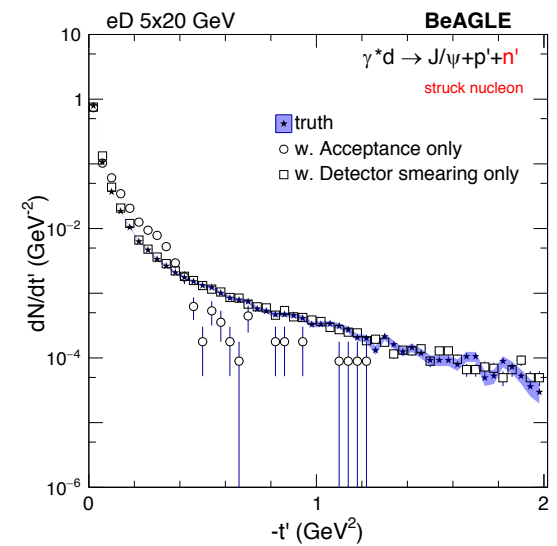
# Proton spectator – t'



18x135 GeV



10x50 GeV

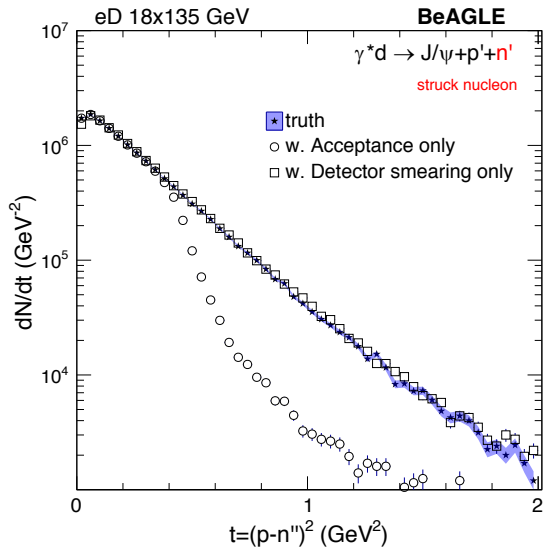


5x20 GeV

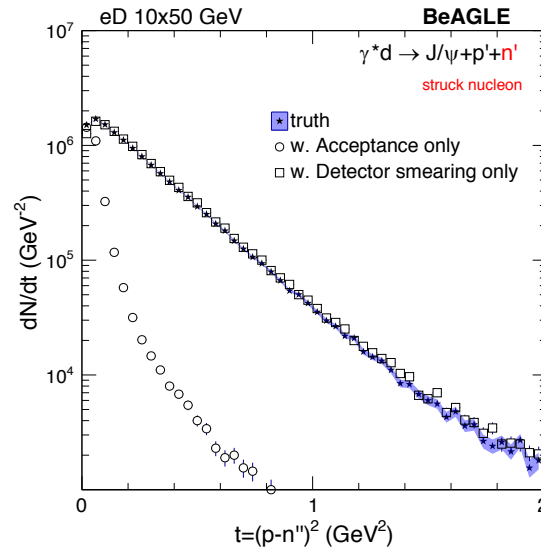
- Significant difference towards low energies.
- SRC studies seem to be better off with higher energy configuration



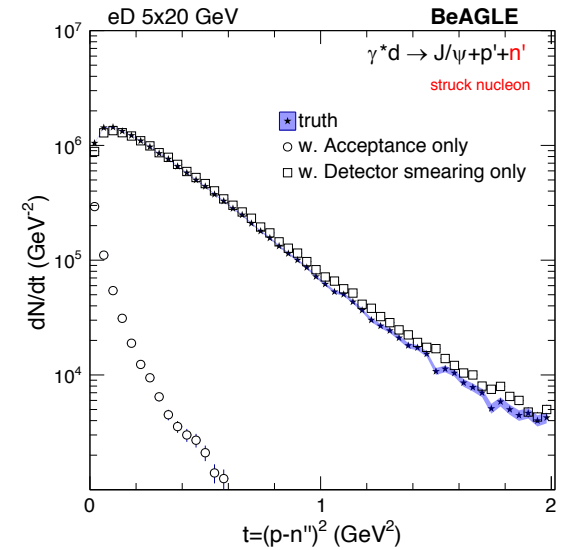
# Proton spectator – t



18x135 GeV



10x50 GeV



5x20 GeV

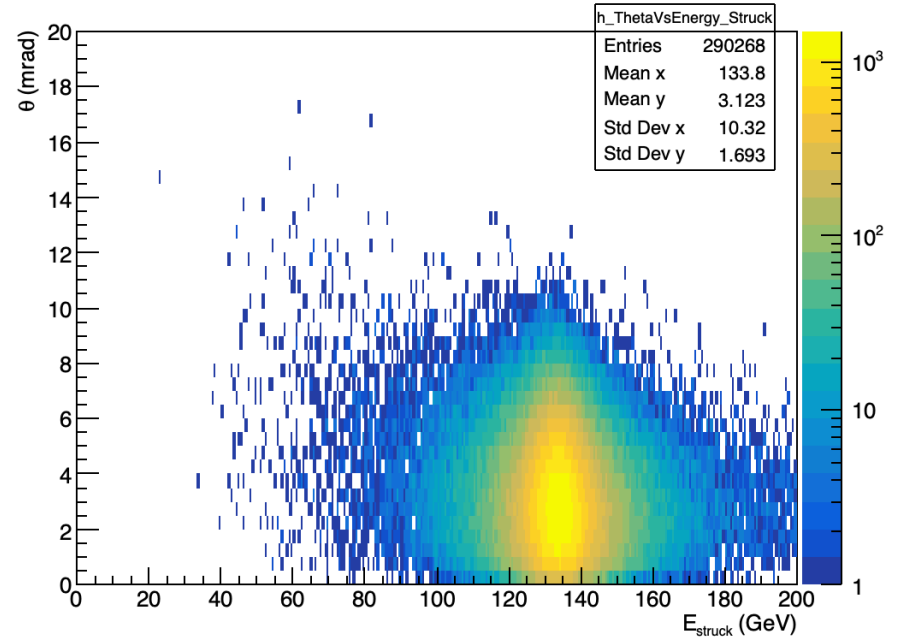
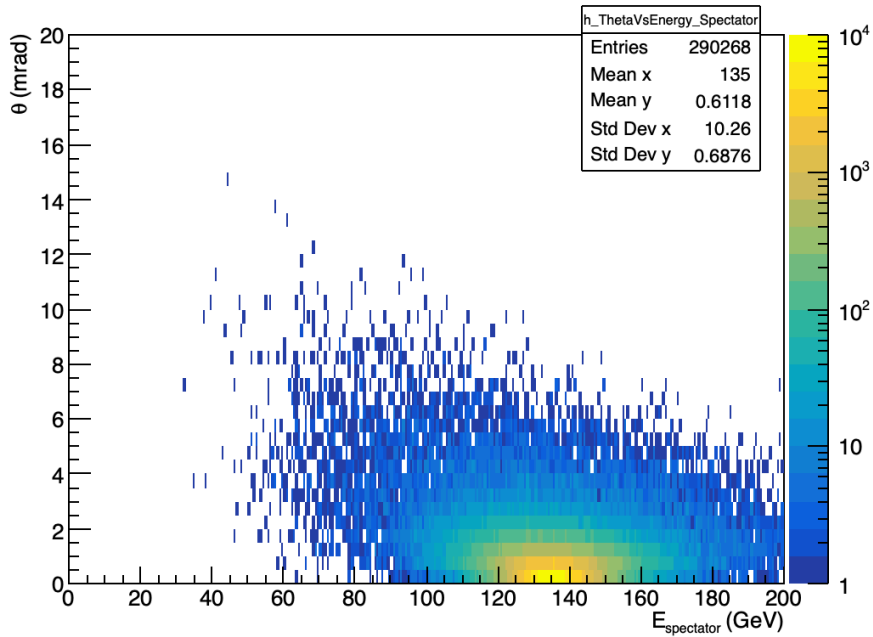
- Significant difference towards low energies.
- Very bad acceptance at low energy but don't forget this might be recovered by main detector

# Summary

- Spectator tagging in deuteron breakups have been investigated with toy forward detectors.
- Tagging spectator protons and neutrons are done separately.
- Some observables are more sensitive to energy/momentum resolutions, while some are more acceptance hungry.
- Many more physics cases can be studied using BeAGLE, however for coherent VMP off deuteron, it might be easier to go to *Satre*. Will need more investigations.
  
- *Will need to think about how to combine all above information*
  
- Realistic simulations are done by Alex Jentsch et al, which includes more effects for the detector and IR/Machine designs, e.g., momentum spread of the beam, crab cavity, angular divergence, etc.

# Backup

# theta vs E



No detector acceptance or resolution was applied.