

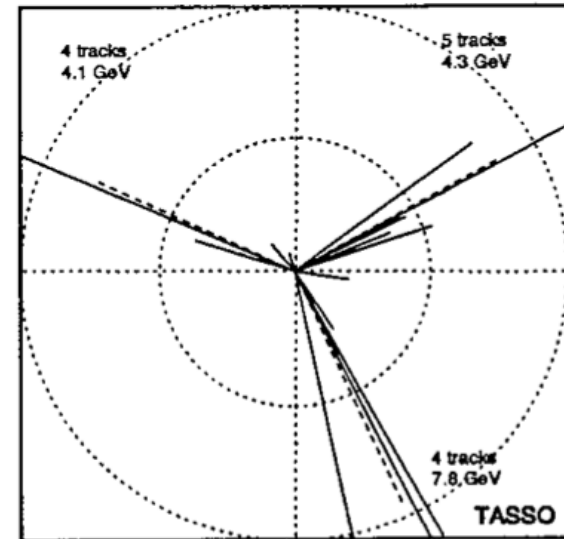
20+5

Jets in e^+e^- (TMD FFs in jets at the B-factories)

Anselm Vossen

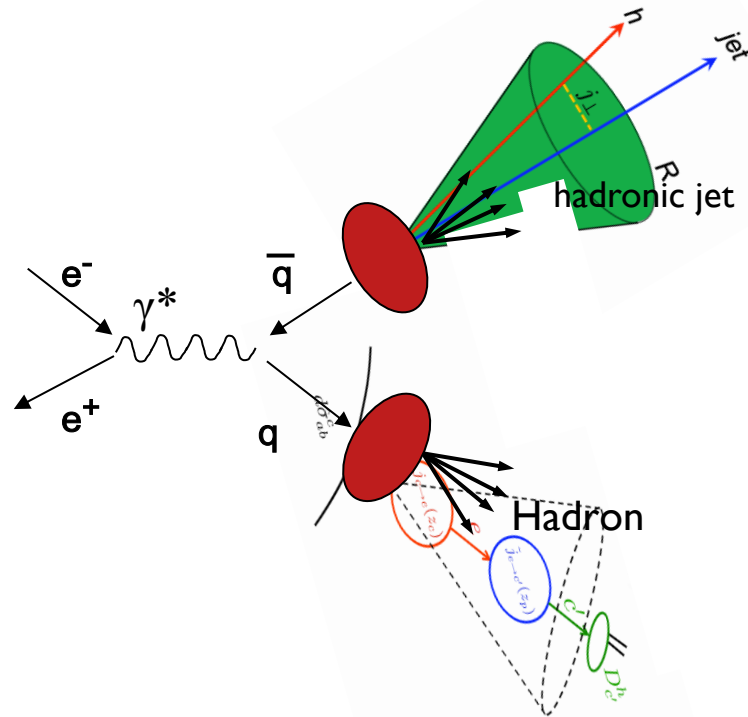
Long history of jet/hadronization studies in e^+e^- at DESY, SLAC, KEK, CERN

- Gluon discovery at TASSO, PLUTO, MARK-J, JADE at DESY
- Verification of LUND string model of fragmentation looking at activity between quarks and gluons
- α_S determination...
- Gluon vs quark jets...



Three jet event at TASSO

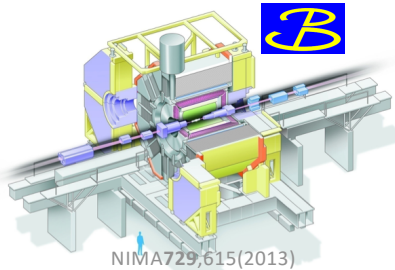
More recently: Interest in determining TMD FFs from Hadrons in Jets



Kaufmann, Mukherjee, Vogelsang,
Phys.Rev. D92 (2015) no.5, 054015

B-factories provide the necessary statistics...

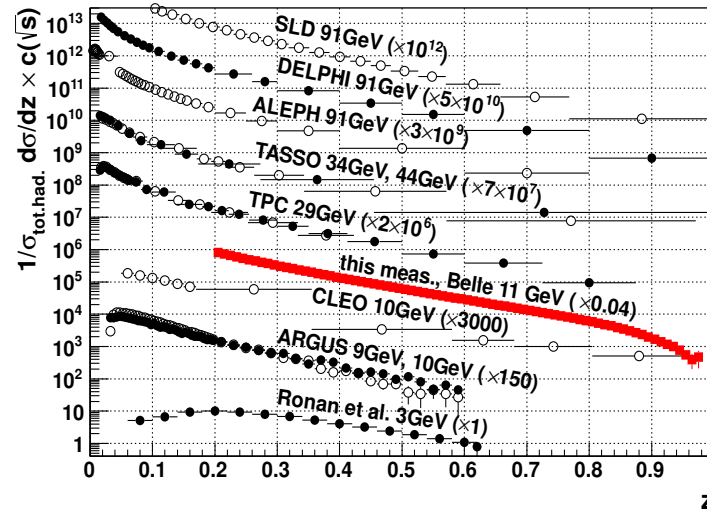
- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.425$
- $L \sim 1 \text{ ab}^{-1}$



NIMA729,615(2013)

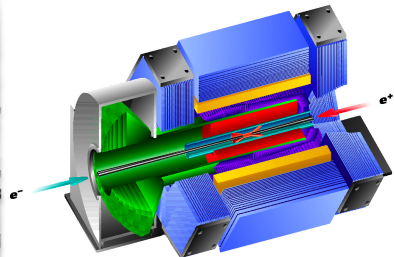
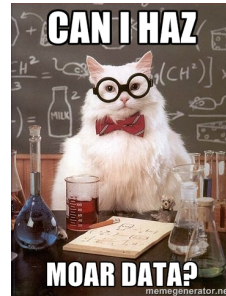
NIMA479,117(2007) **BABAR**

World Data (Sel.) for $e^+e^- \rightarrow \pi^\pm + X$ Production

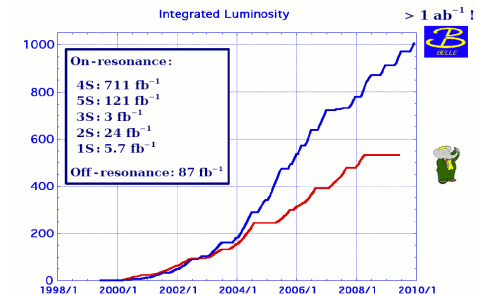


- Dominated by B factories
- Limited lever arm in $\sqrt{s}$ in particular at high z
- Precision data includes charged single hadrons π , K , p , D , Λ , charmed baryons...

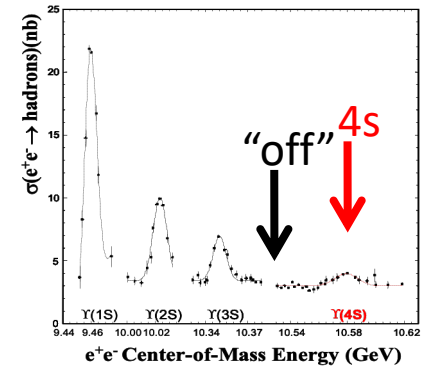
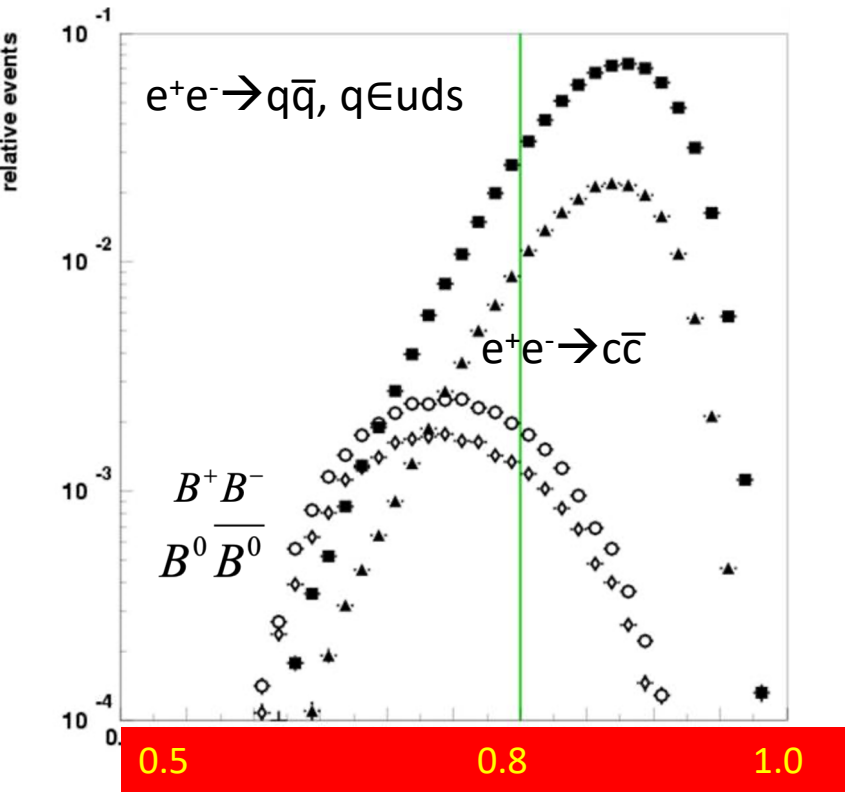
Phys.Rev.Lett. 111 (2013) 062002 (Belle)
Phys.Rev. D88 (2013) 032011 (BaBar)



- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.65$
- $L \sim 500 \text{ fb}^{-1}$

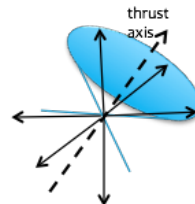


Lots of data off resonance, easy to remove resonance background

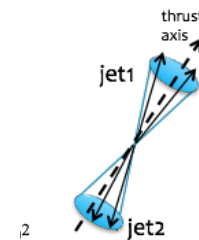


- small B contribution (<1%) in high thrust sample
- >75% of X-section continuum under $\Upsilon(4S)$ resonance
- $\sim 100 \text{ fb}^{-1} \rightarrow \sim 1000 \text{ fb}^{-1}$

$$\text{Thrust: } T = \frac{\sum_i |p_i \cdot \hat{n}|}{\sum_i |p_i|}$$



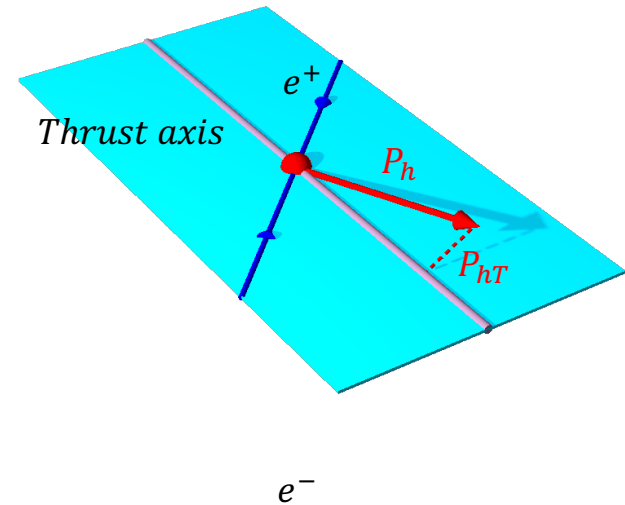
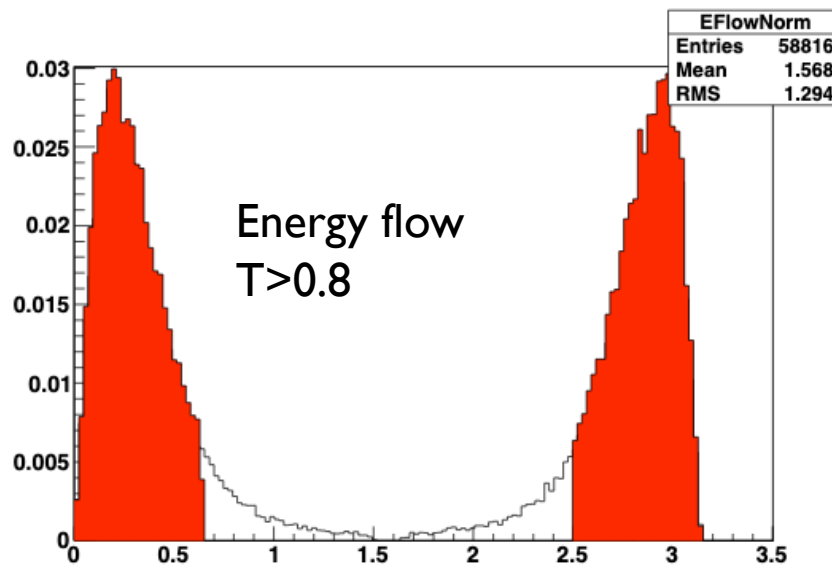
$T \sim 0.5$



$T \sim 1$

Use thrust as proxy to $q\bar{q}$ axis

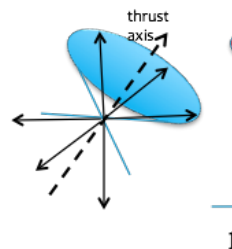
- No phase space for >2 jet events
- **Transverse momentum measured with respect to thrust axis**



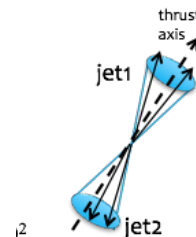
$$T = \sum_i \frac{|\mathbf{P} \cdot \hat{\mathbf{n}}|}{|\mathbf{P}|}$$

thrust axis $\equiv \hat{\mathbf{n}}$

$$0.5 \leq T \leq 1$$



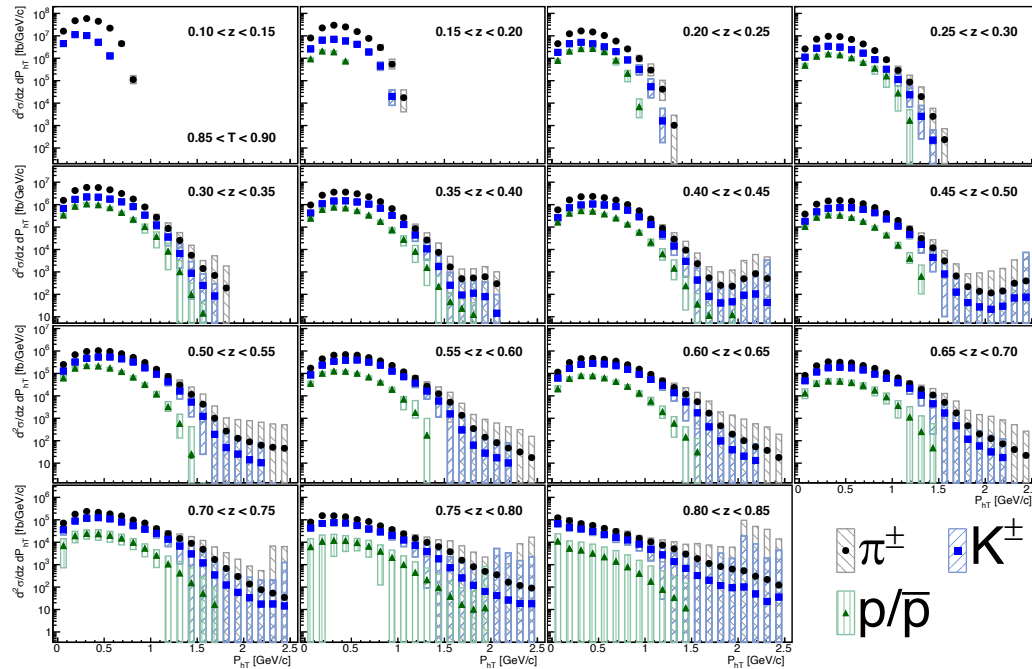
$T \sim 0.5$



$T \sim 1$

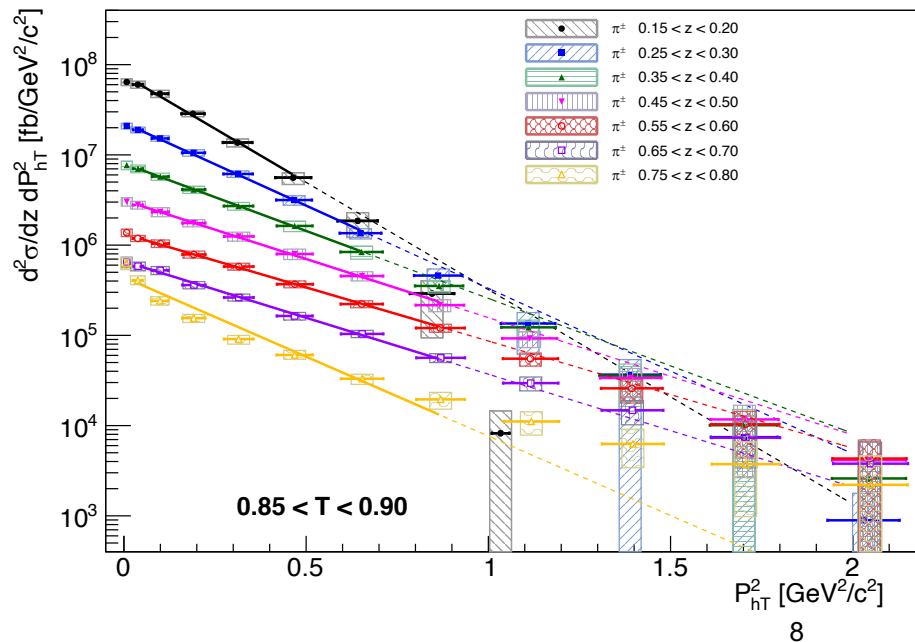
Transverse momentum distributions

- $0.85 < \text{Thrust } T < 0.9$
 - Transverse momenta mostly Gaussian
 - Possible deviations for large P_{hT} tails, but also large uncertainties



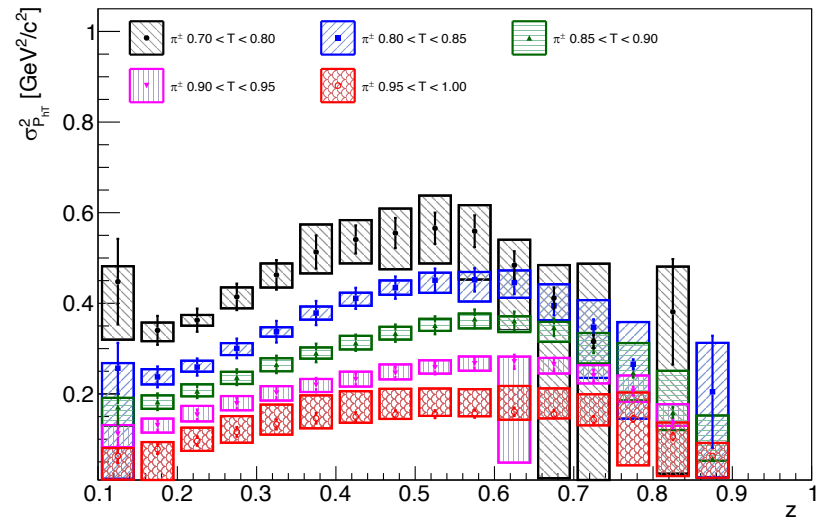
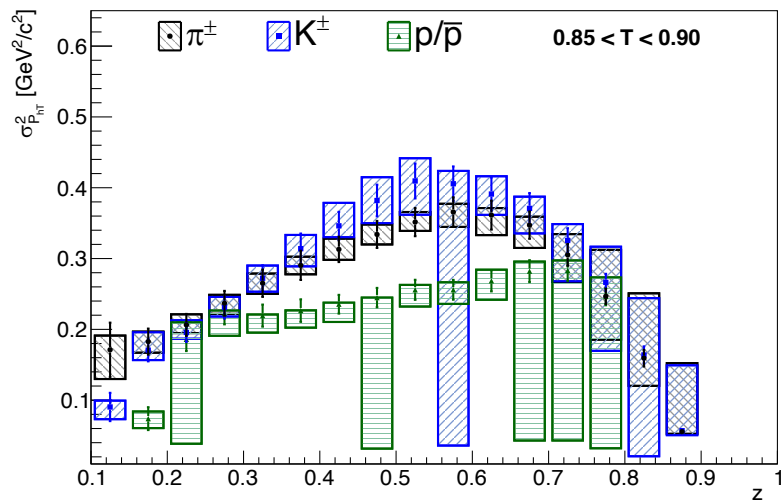
Transverse Momentum: Gaussian widths

- $0.85 < T < 0.9$
 - Fit Gauss to low P_{hT} data
 - Mostly well described with possible exception at high z
 - Deviation from Gauss at large P_{hT}
 - Clear increase in width with z for low values of z



Gaussian Width as a function of z and T

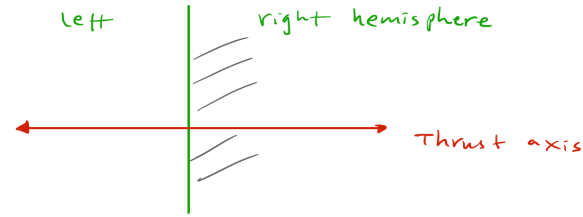
- General increase with z with turnover at larger values of z for mesons
- Protons with smaller width and more linear rise with z



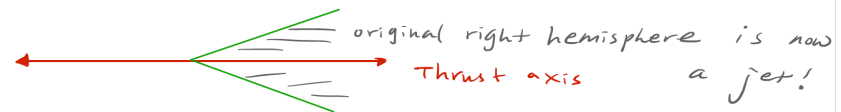
- General increase with z with turnover at larger values of z for mesons
- Clear decrease of widths with increase of T
 - Particles more and more collimated

New theoretical insights: Thrust and Jet measurements are closely related

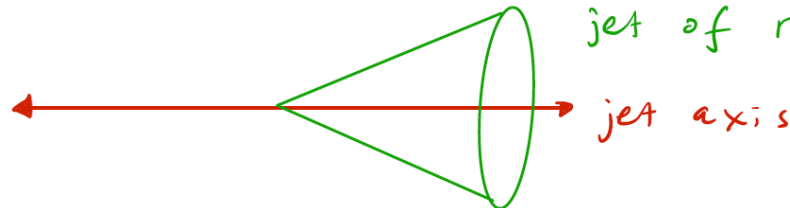
- Motivated by gaussian p_T spectrum as expected from jet measurement
- M. Boglione, A. Simonelli, "Factorization of $e^+e^- \rightarrow HX$ cross section, differential in z_h, P_T and thrust, in the 2-jet limit", 2011.07366 [hep-ph]
- Z. Kang, D. Shao, F. Zhao, "QCD resummation on single hadron transverse momentum distribution with the thrust axis", 2007.14425 [hep-ph]



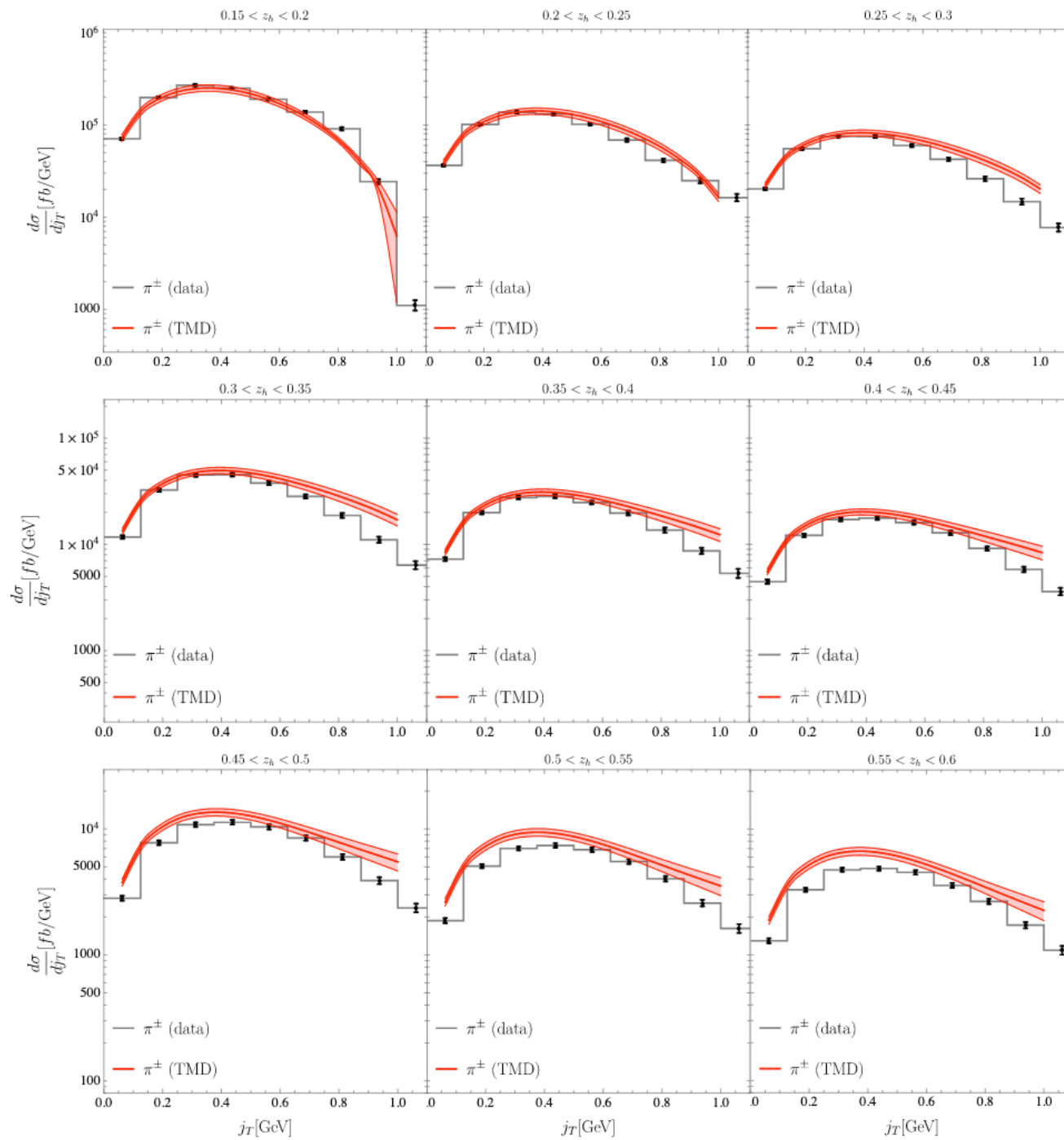
⇓ Lorentz boost along thrust axis



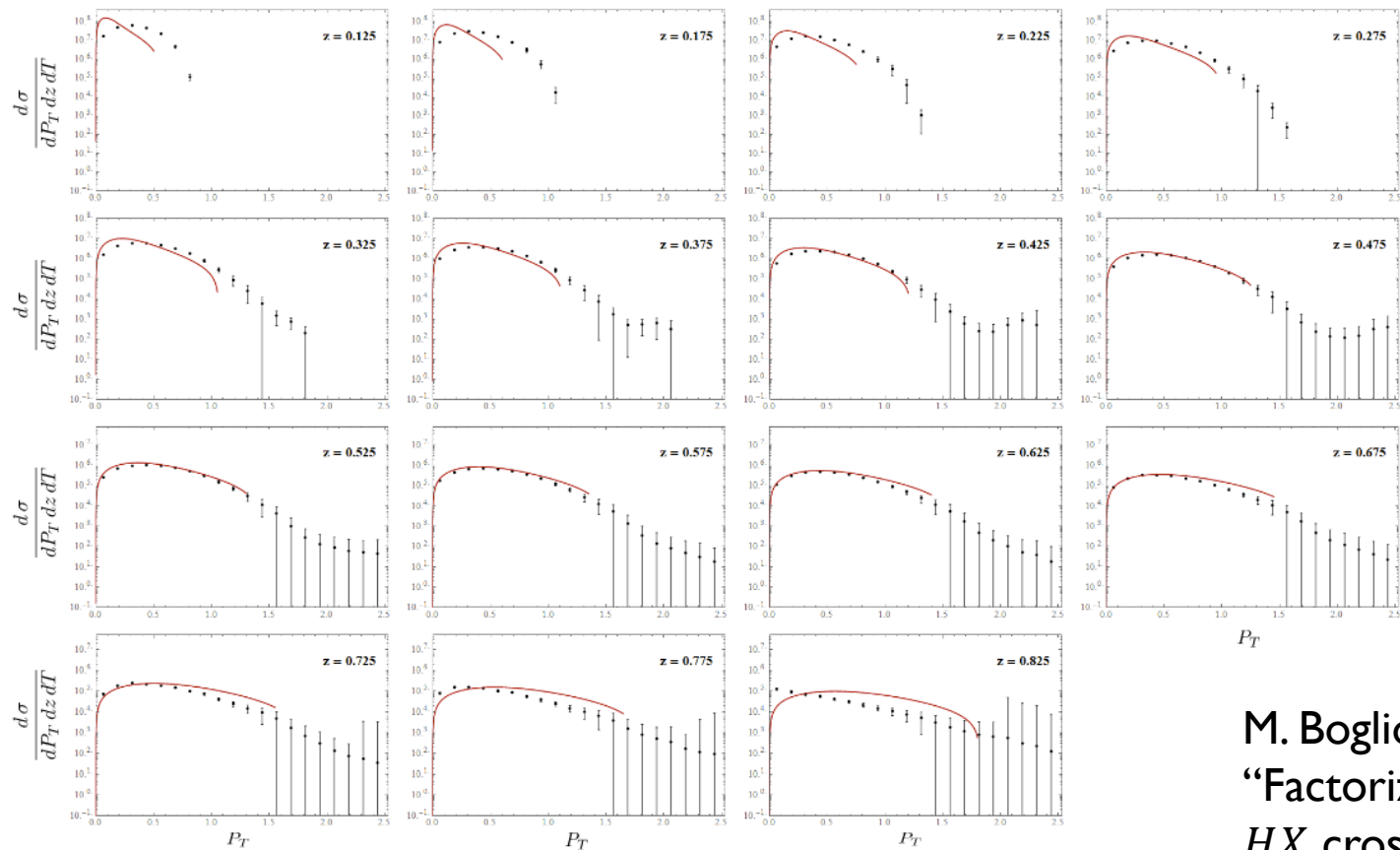
⇓ thus is equivalent to jet of radius R



Drawing by Zhong-Bo Kang

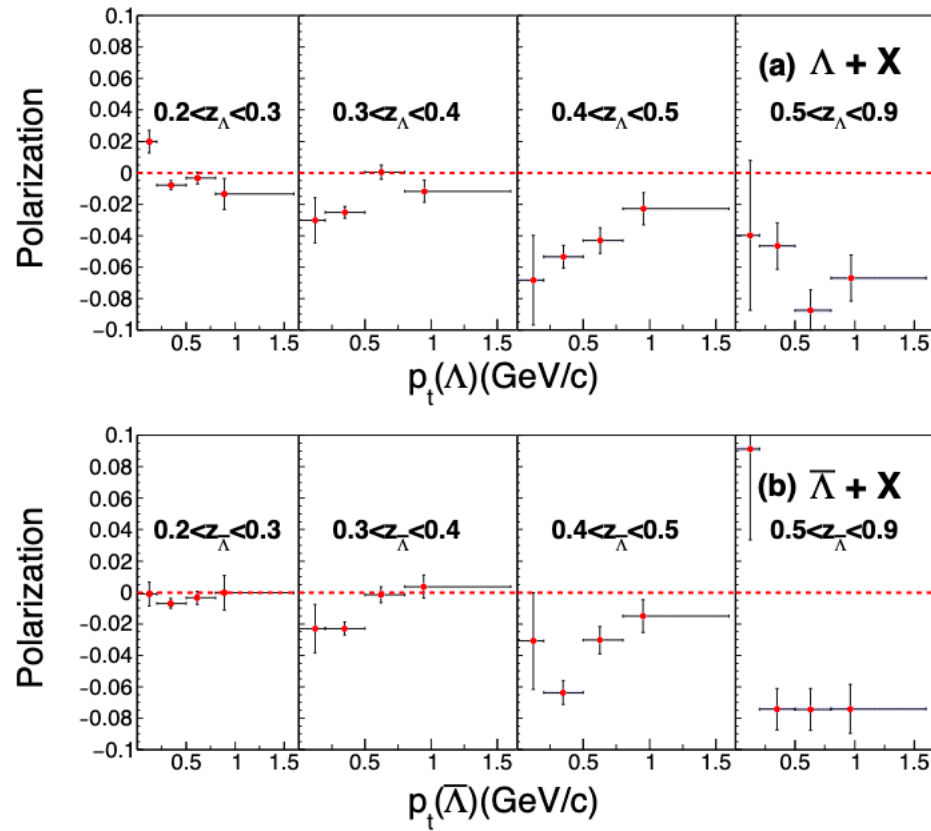


Z. Kang, D. Shao, F. Zhao, “QCD resummation on single hadron transverse momentum distribution with the thrust axis”, 2007.14425 [hep-ph]



M. Boglione, A. Simonelli,
 “Factorization of $e^+e^- \rightarrow$
 HX cross section,
 differential in z_h, P_T and
 thrust, in the 2-jet limit”,
 2011.07366 [hep-ph]

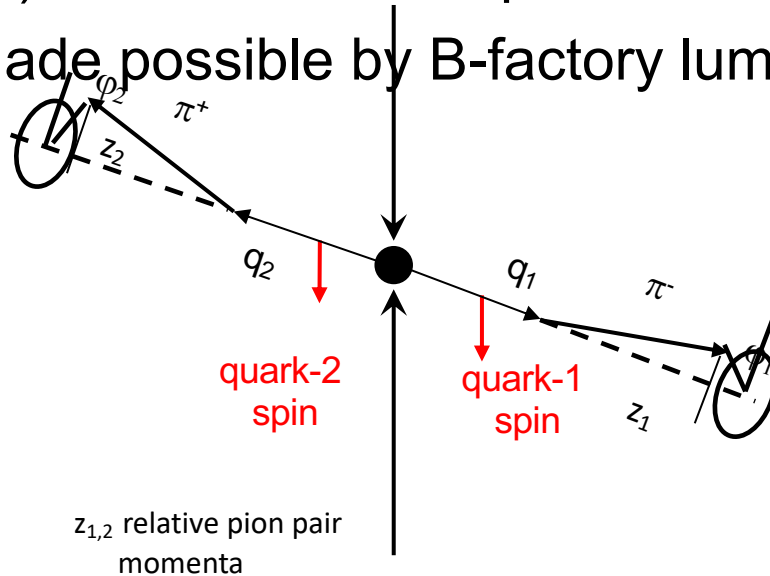
$\Lambda^\uparrow$ in jets



Phys.Rev.Lett. 122 (2019) 4, 042001

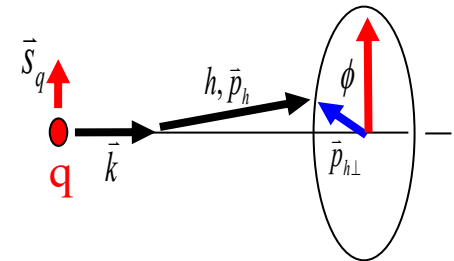
Polarized FFs from Correlation Measurements in e^+e^-

- Access spin dependence and p_T dependence (convolution or in jet) without PDF complication
- Made possible by B-factory luminosities

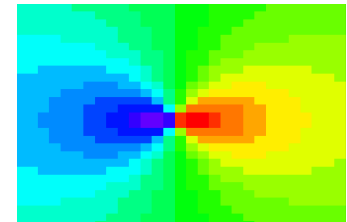


J. Collins, Nucl. Phys. B396, (1993) 161

$$D_{q\uparrow}^h(z, P_{h\perp}) = D_{1,q}^h(z, P_{h\perp}^2) + H_{1,q}^{\perp h}(z, P_{h\perp}^2) \frac{(\hat{\mathbf{k}} \times \mathbf{P}_{h\perp}) \cdot \mathbf{S}_q}{zM_h}$$



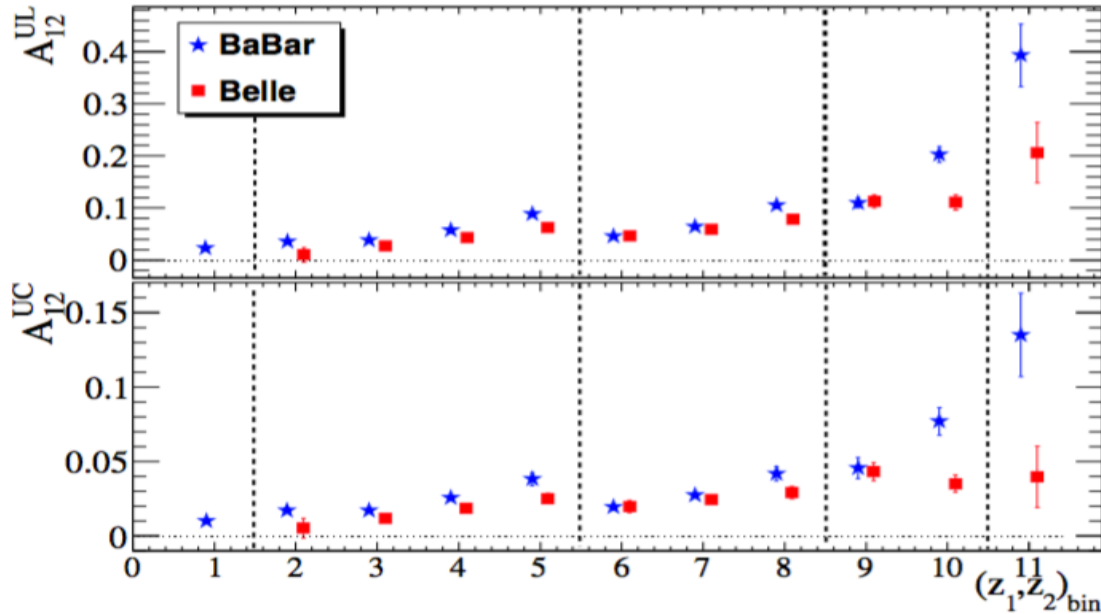
$$\text{Cross-section } e^+e^- \rightarrow (h_1 h_2)(\overline{h_1} \overline{h_2}) + X \\ \propto D_1^\perp \overline{D_1^\perp} + H_1^\perp \overline{H_1^\perp} \cos(\phi_1 + \phi_2)$$



Collins Effect vs (z_1, z_2) : comparisons

EPJA, 52, 1-15 (2016)

Unlike/Likesign
Unlike/Charged
Ratios to cancel
acceptance effects
Unlike:
 $\text{fav}^* \text{fav} + \text{dis}^* \text{dis}$
Like:
 $\text{fav}^* \text{dis}$



- Symmetric (z_1, z_2) bins are used for the comparisons: results falling in the same large (z_1, z_2) interval are averaged taking into account statistical and systematic uncertainties
- A_0 : very good agreement between BaBar and Belle data; larger asymmetry for BESIII in the last bin ($z_{1,2} > 0.5$)
- A_{12} : some tensions between BaBar and Belle,
 - $z < 0.9$ for BaBar, $z < 1$ for Belle

- First non-zero independent measurement of the Collins effect for pion pairs in e^+e^- annihilation by Belle Collaboration @ $\sqrt{s} \sim 10.6$ GeV (PRL 111,062002(2008), PRD 88,032011(2013)) leads to first extraction of transversity (Phys.Rev. D75 (2007) 054032) from SIDIS and e^+e^-
 - Confirmed by BaBar @ $\sqrt{s} \sim 10.6$ GeV (PRD 90,052003 (2014); PRD 92,111101(R)(2015) for KK and $K\pi$)
 - Measured at BESIII @ $\sqrt{s} = 3.65$ GeV (PRL 116,42001(2016))

New Pt dependence from Belle

- Trend consistent with BaBar
- Direct comparison difficult due to different correction schemes (thrust vs $q\bar{q}$ -axis)

Unlike/Likesign

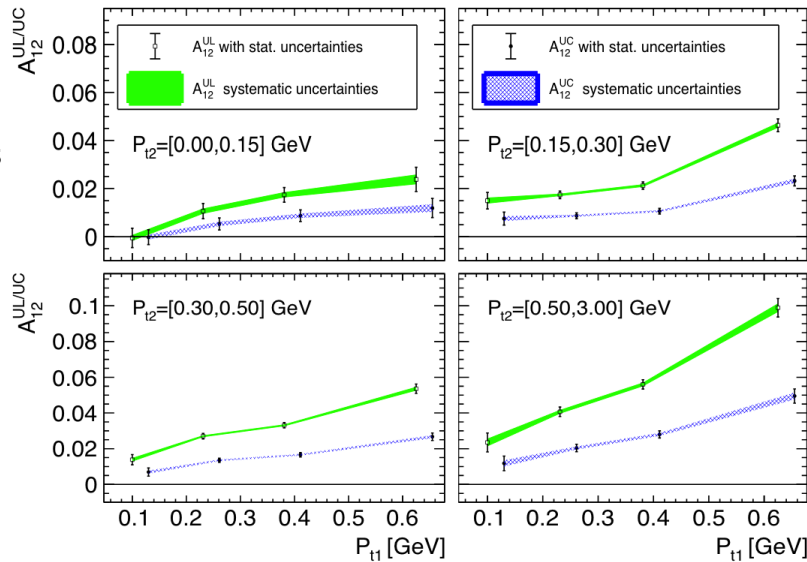
Ratios to cancel acceptance effects

Unlike:

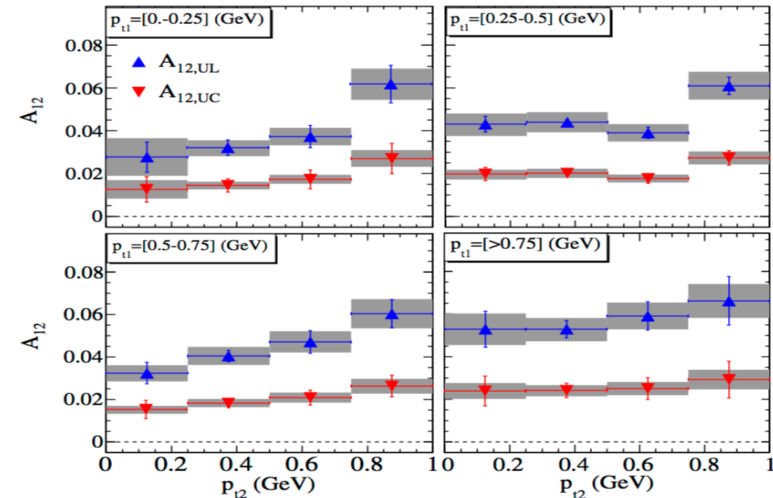
$\text{fav}^* \text{fav} + \text{dis}^* \text{dis}$

Like:

$\text{fav}^* \text{dis}$



BaBar

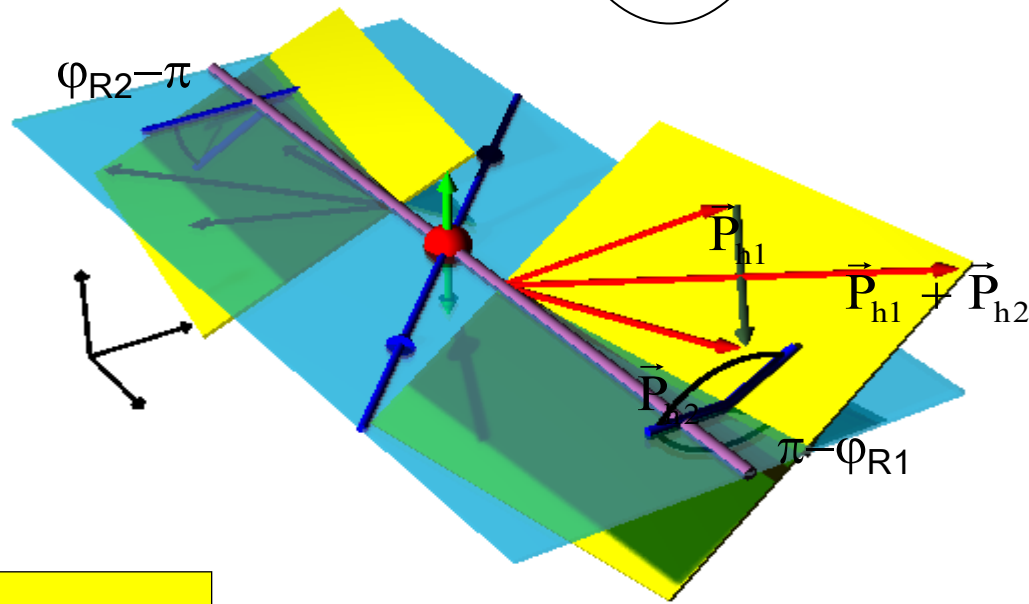
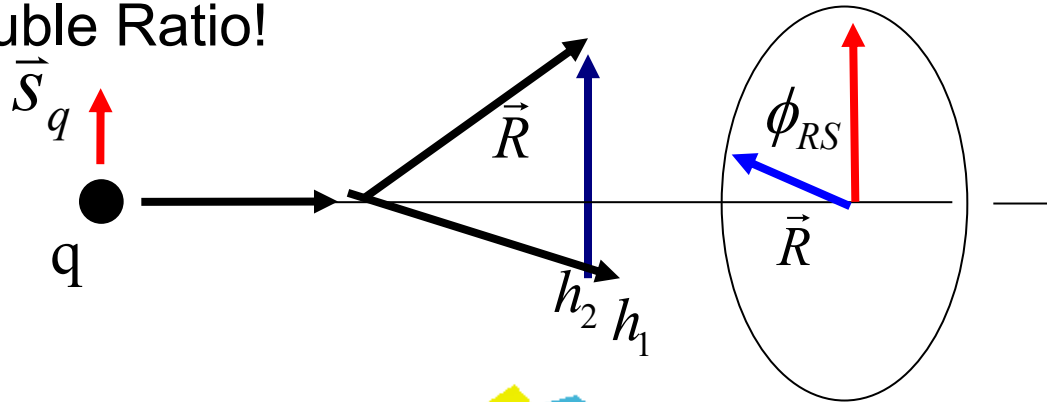


Phys.Rev.D 100 (2019) 9, 092008

Kaon, π^0 , η , π^0 -charged averaged also available (see backup)

Di-Hadron Fragmentation

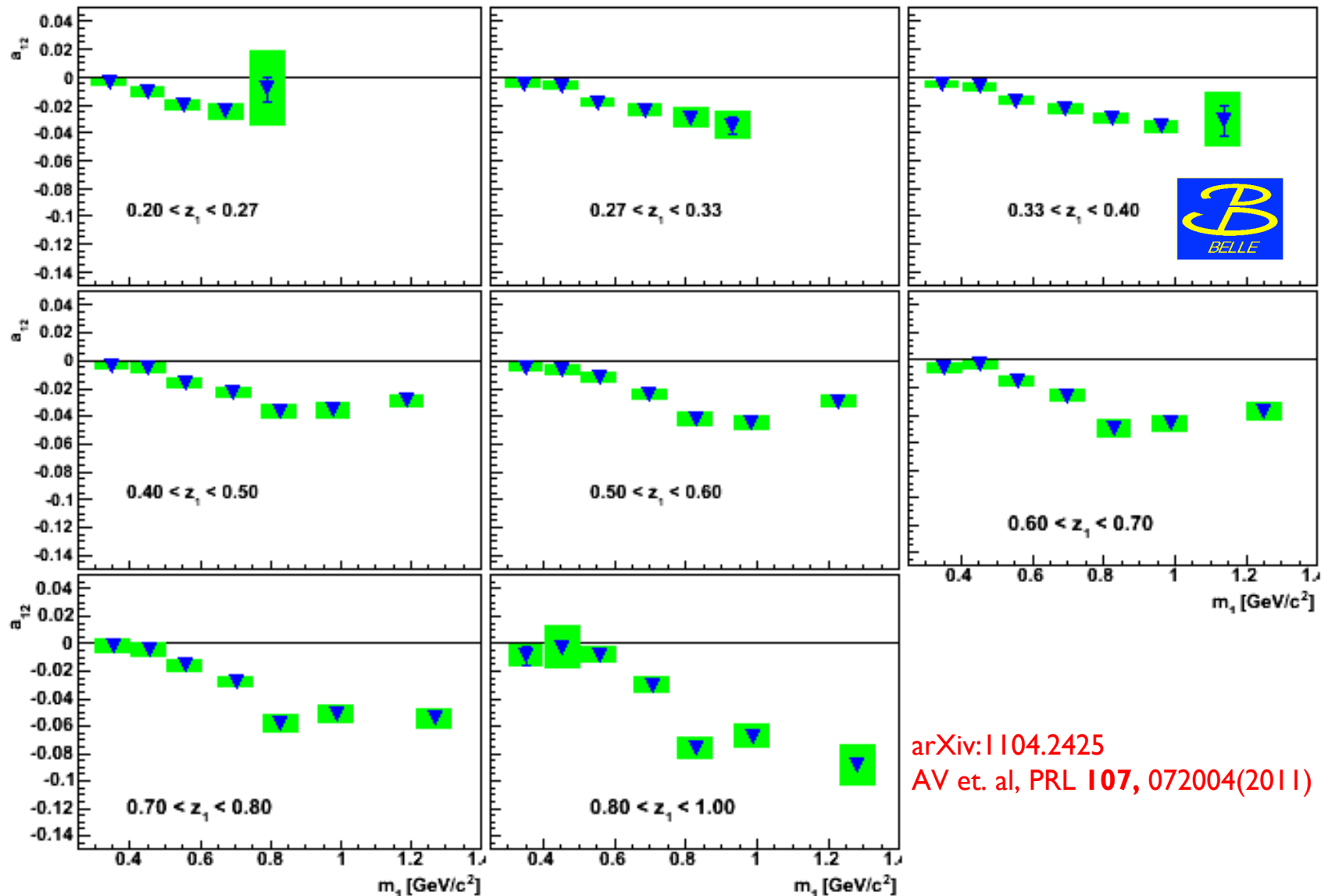
- No Double Ratio!



$$\sigma \propto H_1^\perp \cdot \bar{H}_1^\perp$$

First measurement of Interference Fragmentation Function

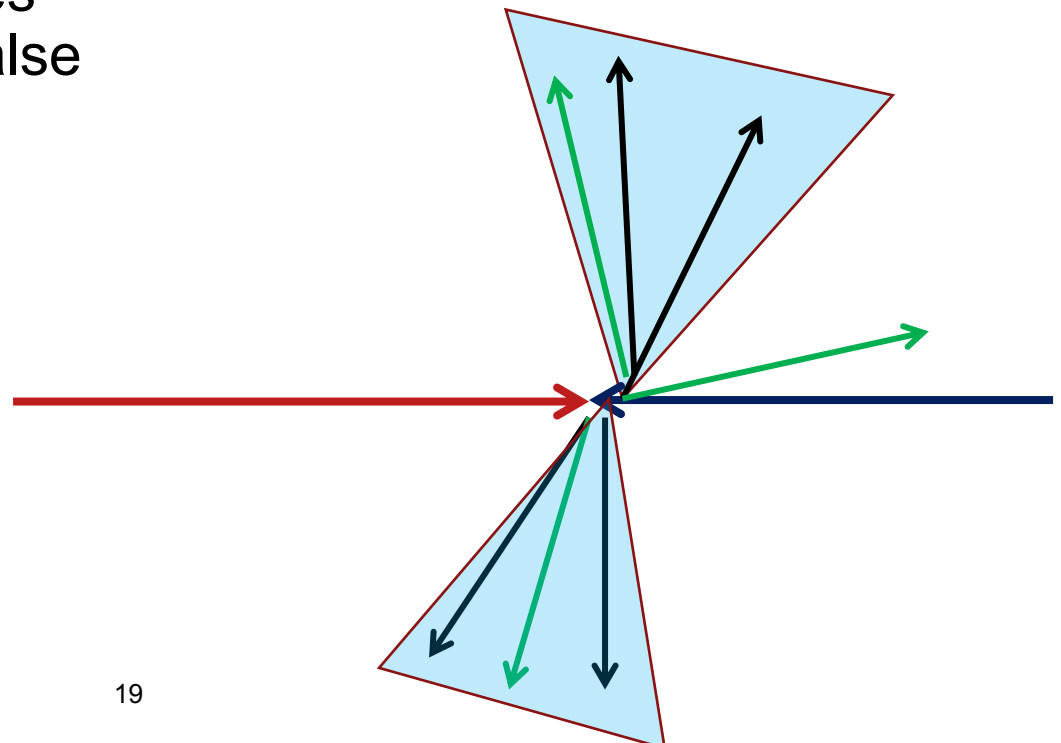
$$a_{12} \propto H_1^< * H_1^<$$



arXiv:1104.2425
 AV et. al, PRL **107**, 072004(2011)

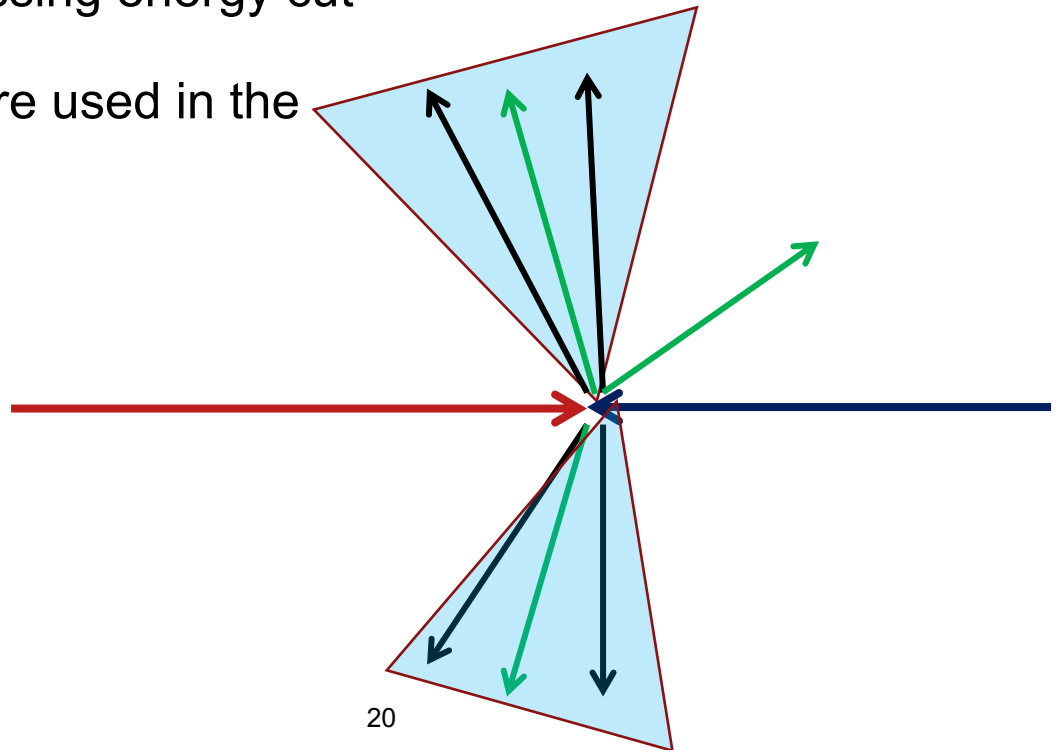
Extraction of $\phi_1 - \phi_2$ Asymmetries

- *Phys.Rev.D* 67 (2003) 094003:
 $\cos(2(\phi_1 - \phi_2))$ asymmetries are
proportional to $G_1^\perp \cdot \bar{G}_1^\perp$
- Fixed thrust axis correlates
hemispheres leading to false
asymmetries



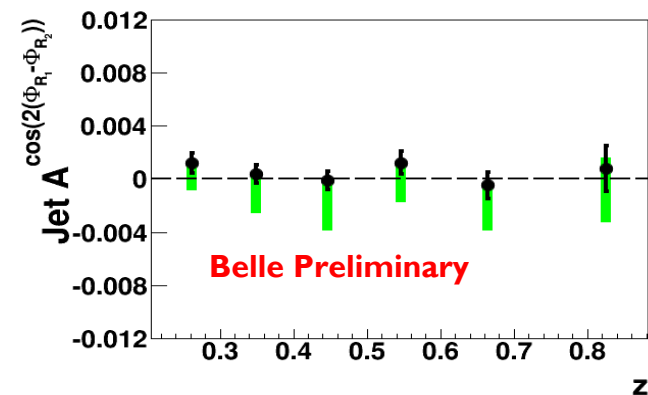
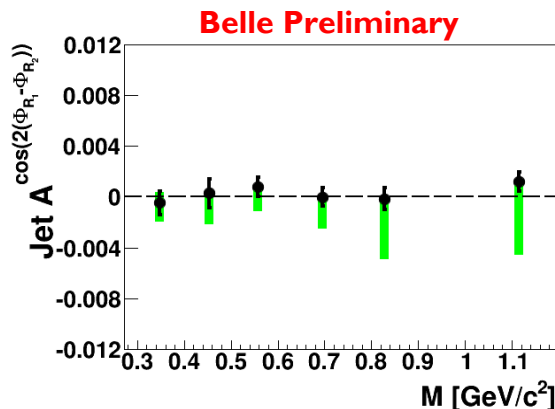
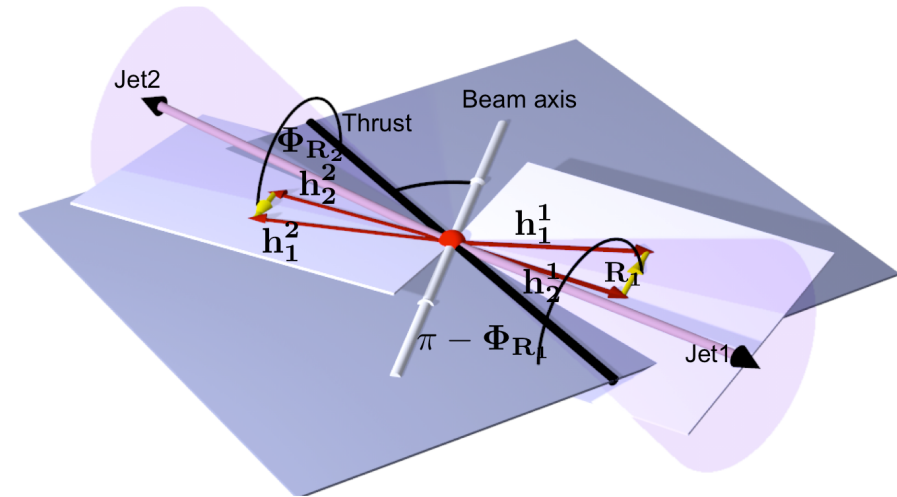
Jet Reconstruction at Belle

- Robust vs. final state radiation
- **De-correlate axis between hemispheres**
- We use anti-kT algorithm implemented in fastjet
- Cone radius $R=1.0$
- Min energy per jet 3.75 GeV $\rightarrow$ suppress weak τ decays
- Only allow events with 2 jets passing energy cut (dijet events)
- Only particles that form the jet are used in the asymmetry calculation

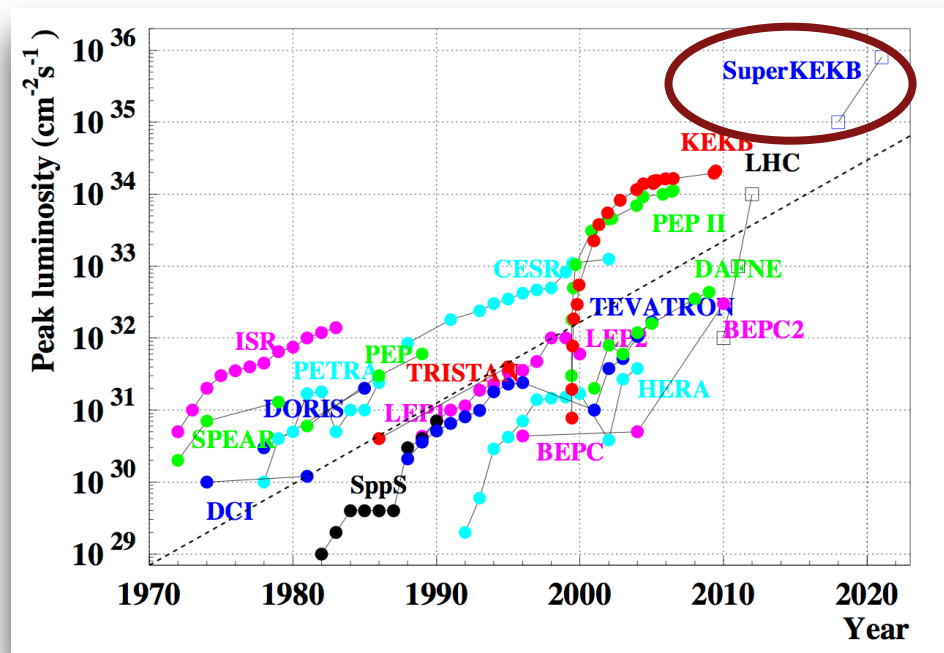


Asymmetries for $\text{Cos}(2(\phi_{R1}-\phi_{R2}))$ ($G_1^\perp$) small

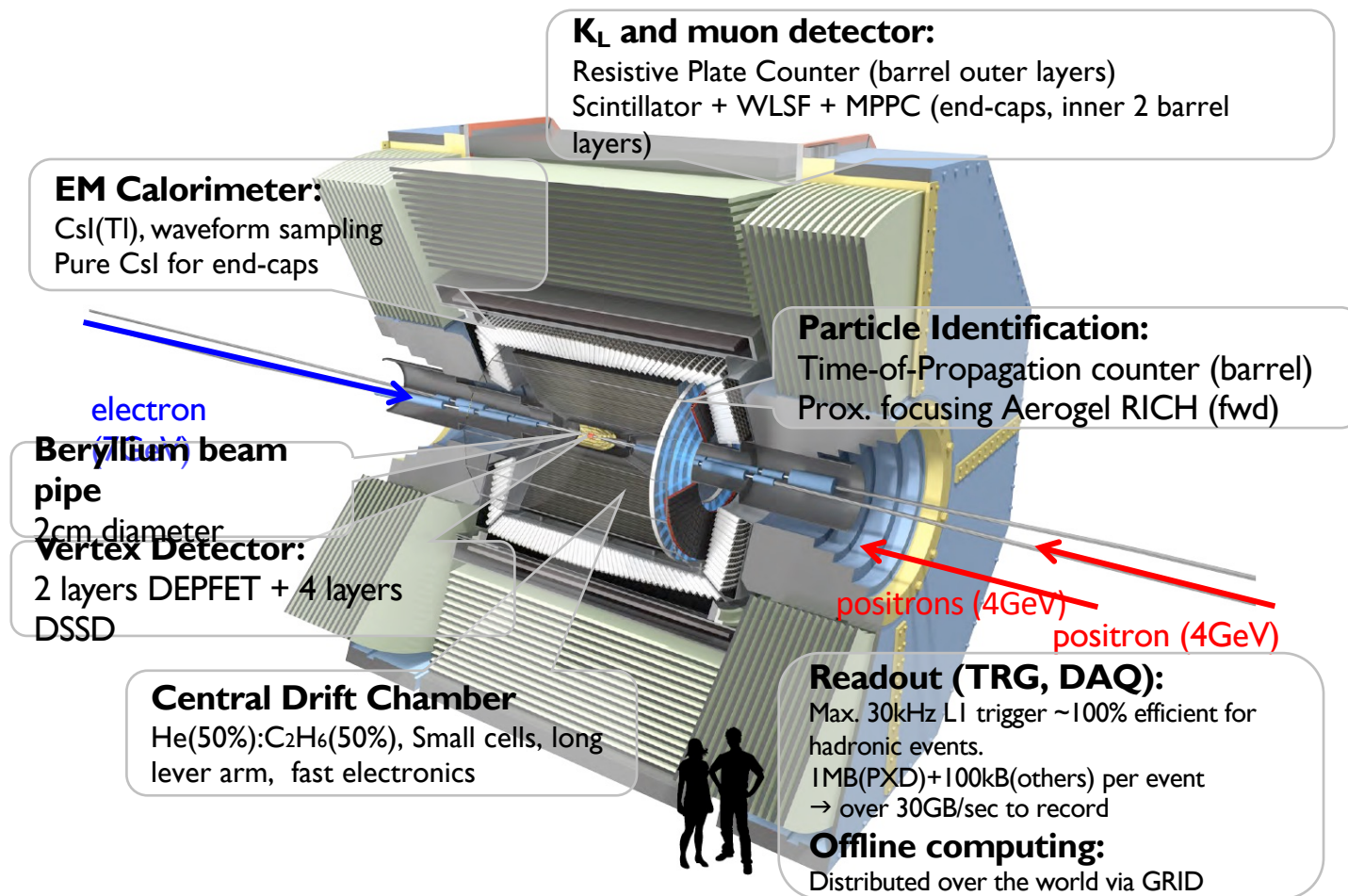
- Turned out that the asymmetry is projected to be $\equiv 0$



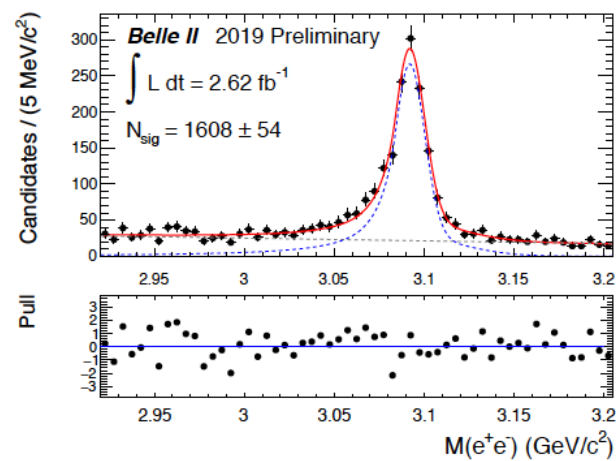
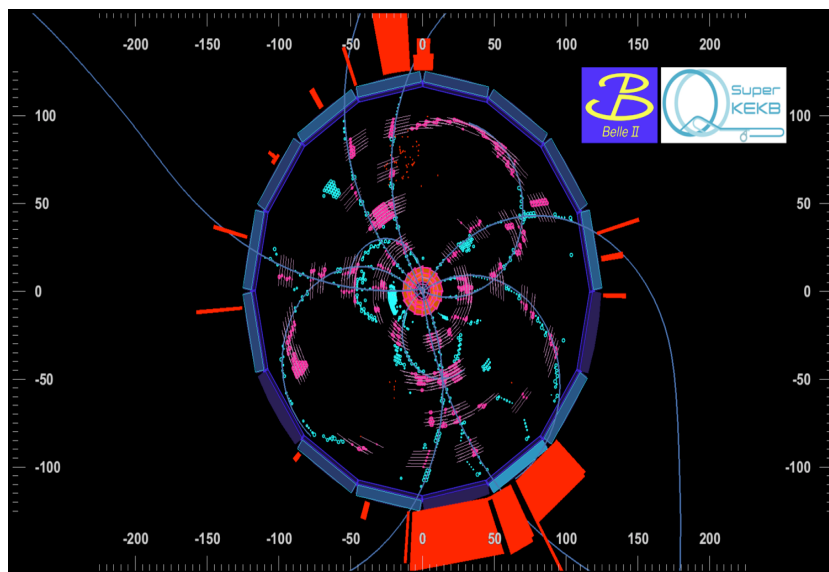
The future is now: Next Generation B factory SuperkeB



Cut view of Belle II Detector



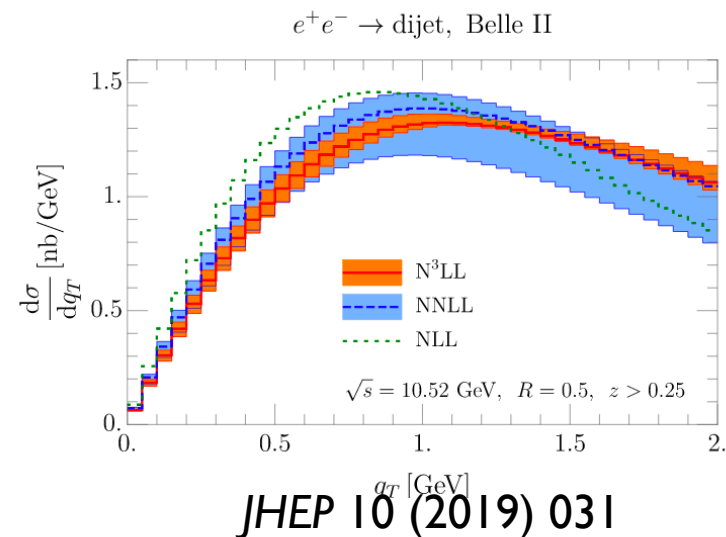
2019: First Collisions in Phase 3, the Physics Run



Clear signals for $B \rightarrow J/\psi X$ in $\sim 1/2$ of Phase 3 data.

Summary

- (Super) B-factories great place to study jets
- Focus so far on in-jet fragmentation using thrust axis
 - Unpolarized, p_T dependence
 - $\Lambda^\uparrow$ in jet
 - Collins/IFF
- First dijet measurement extracting $A^{\cos(2(\phi_1-\phi_2))}$
- Future: dedicated program on jets at Belle II
 - E.g. measuring dijet correlations

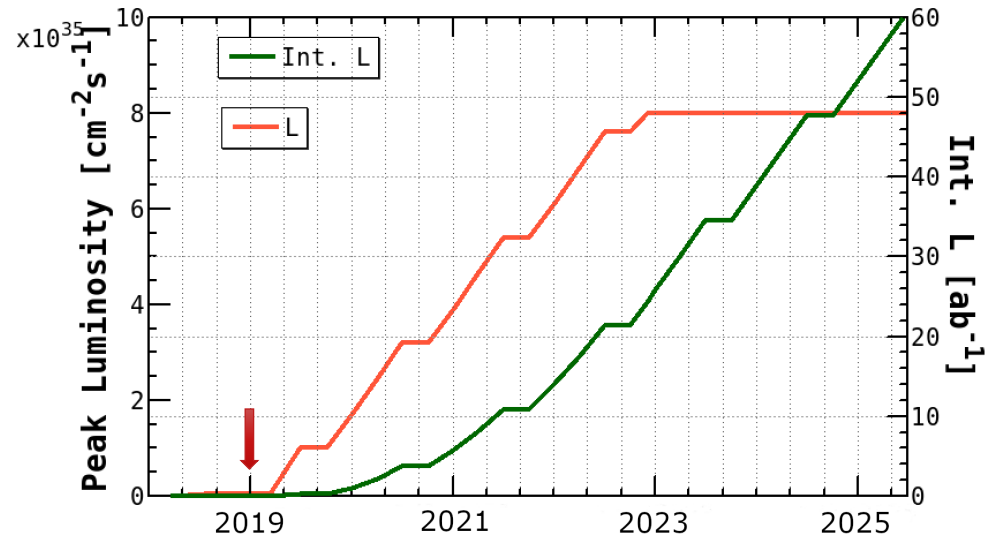


SuperKEKB/Belle II Luminosity Profile

Belle/KEKB recorded $\sim 1000 \text{ fb}^{-1}$. Now have to change units on the y-axis to ab^{-1}

Beam currents *only* a factor of two higher than KEKB ($\sim \text{PEP-II}$)

“nano-beams” are the key; vertical beam size is **50nm** at the IP



Invitation to participate in the Snowmass Whitepaper

Snowmass 2021 Letter of Interest: QCD and Hadronization Studies at Belle II

on behalf of the U.S. Belle II Collaboration

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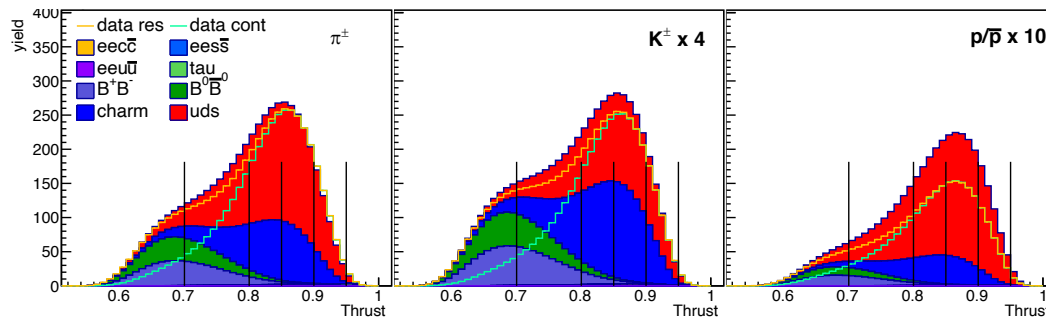
Thematic Area(s):

- (EF05) QCD and strong interactions: Precision QCD
- (EF06) QCD and strong interactions: Hadronic structure and forward QCD
- (RF03) Fundamental Physics in Small Experiments

1 Hadron and Jet Fragmentation Studies at Belle II as input for the EIC

Use thrust as proxy to $q\bar{q}$ axis

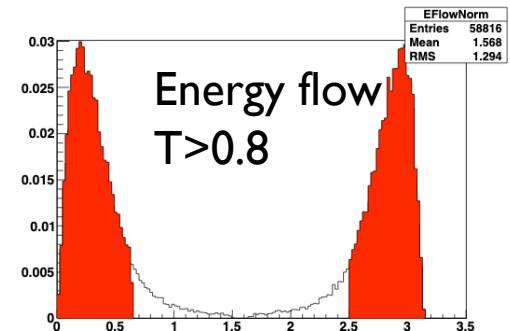
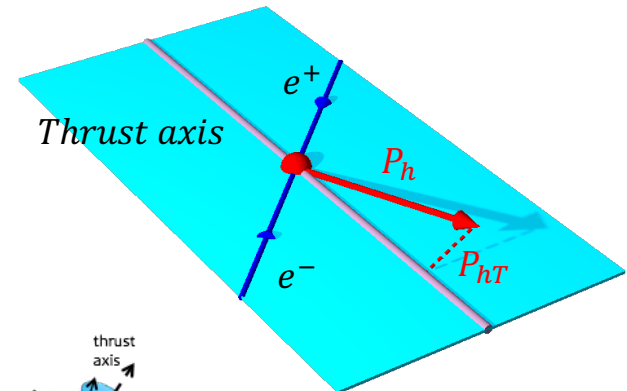
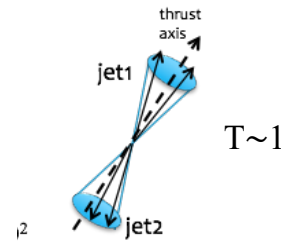
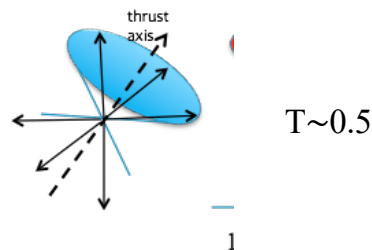
- No phase space for >2 jet events
- **Transverse momentum measured with respect to thrust axis**



$$T = \sum_i \frac{|\mathbf{P} \cdot \hat{\mathbf{n}}|}{|P|}$$

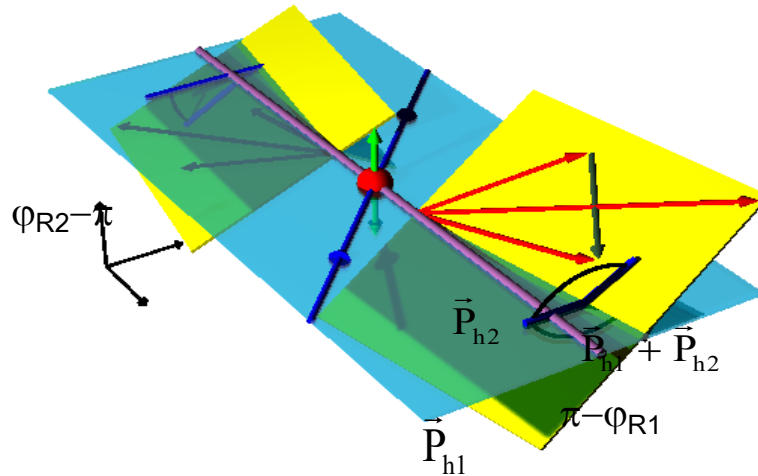
thrust axis $\equiv \hat{\mathbf{n}}$

$$0.5 \leq T \leq 1$$



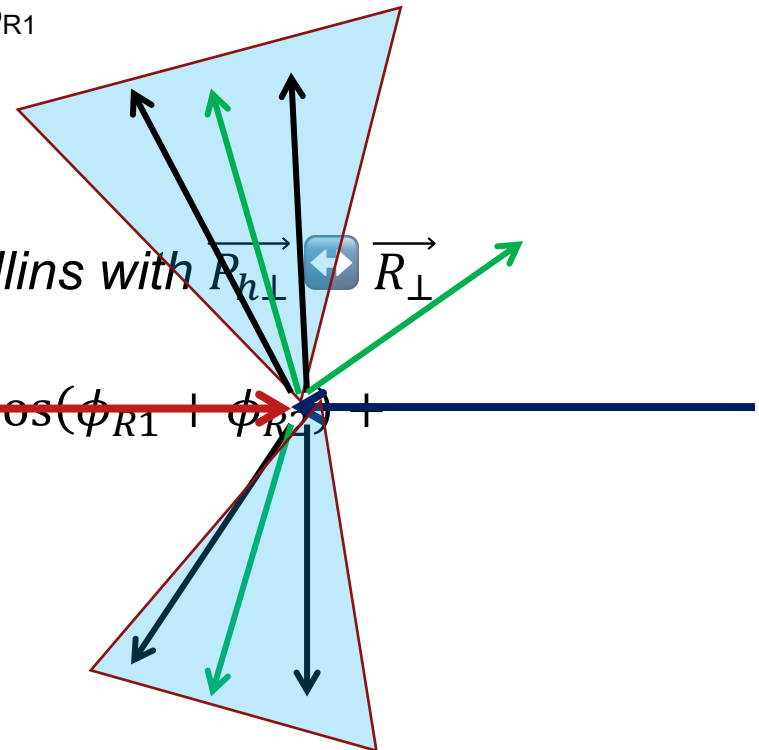
BaBar
Belle
~~BESIII~~

Di-hadron asymmetries

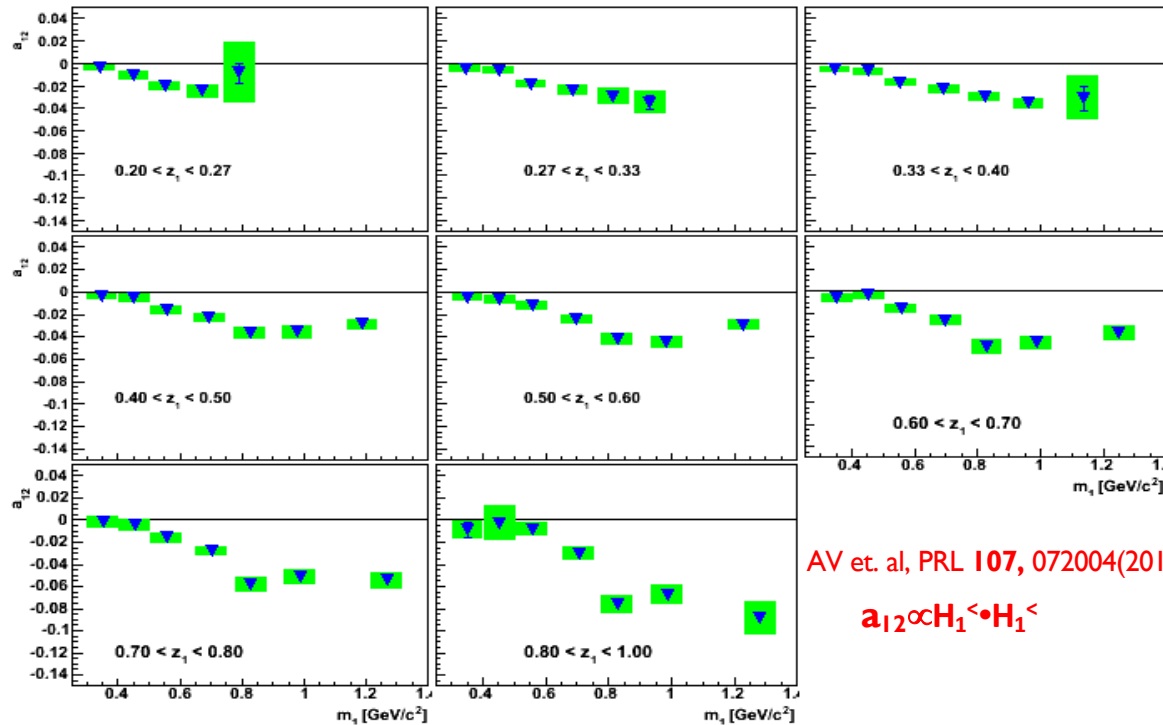


- Conceptually similar measurement as Collins with $\vec{p}_{h\perp} \leftrightarrow \vec{R}_{\perp}$
- Normalized cross section:

$$e^+e^- \rightarrow (h_1 h_2)(\overline{h_1} \overline{h_2}) + X \propto 1 + H_1^\perp \overline{H_1^\perp} \cos(\phi_{R1} + \phi_{R2}) + G_1^\perp \overline{G_1^\perp} \cos(2(\phi_{R1} - \phi_{R2}))$$
- See talks by Aram and Marco



First measurement of Interference Fragmentation Function



See Marco's talk about
Transversity extraction
From di-hadrons

AV et. al, PRL **107**, 072004(2011)

$$a_{12} \propto H_1^< \bullet H_1^<$$

Backup

Long history of e⁺e⁻ colliders: First generation for FF measurements

– DESY:

- DORIS I (3-5) DORIS II (7-10 GeV)
- PETRA 14-46 GeV (1978-86)
: TASSO (34pb⁻¹ (34/44 GeV))

– SLAC:

- PEP@29GeV 1980-1990
(TPC 140 pb⁻¹), HRS, MARK

– KEK:

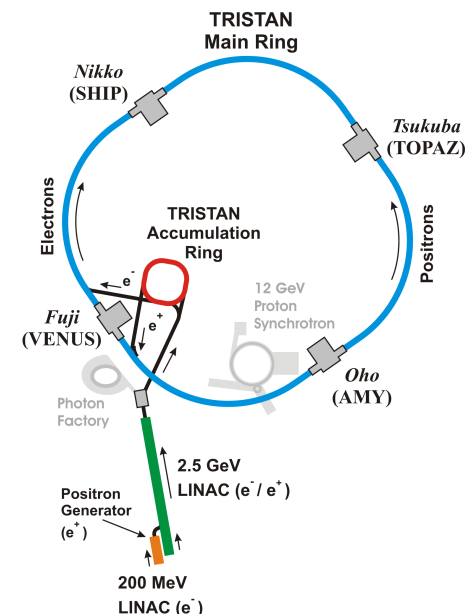
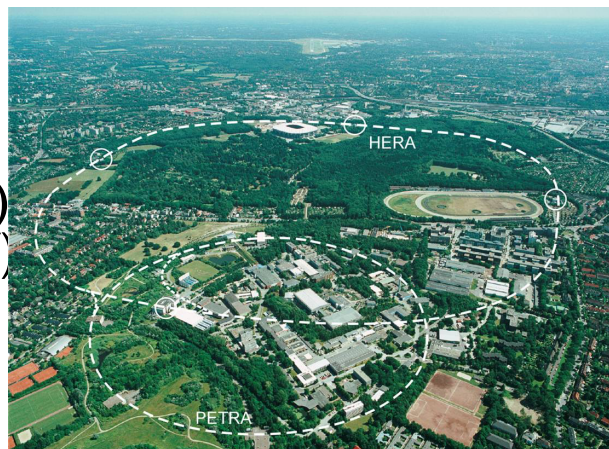
- Tristan @ 50-64 : TOPAZ, AMY (278pb⁻¹)

– SLC @ M_Z (20p⁻¹)

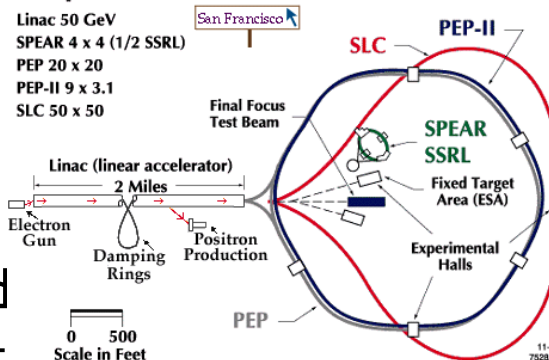
– SLD+MARK II @ M_Z (500k evts $Z \rightarrow qq$), long polarized

– LEP I : 160pb⁻¹, LEP-II 700pb⁻¹

- ~50x SLC

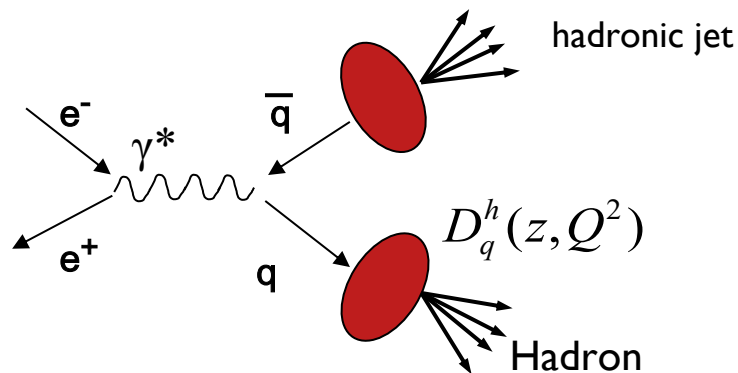


Experimental Areas at SLAC



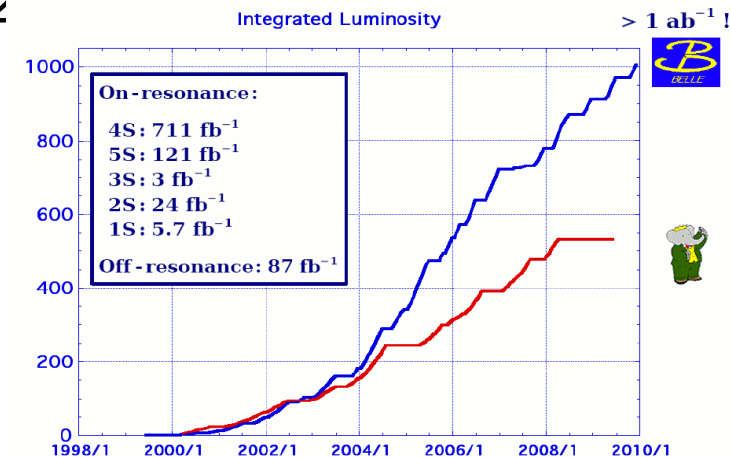
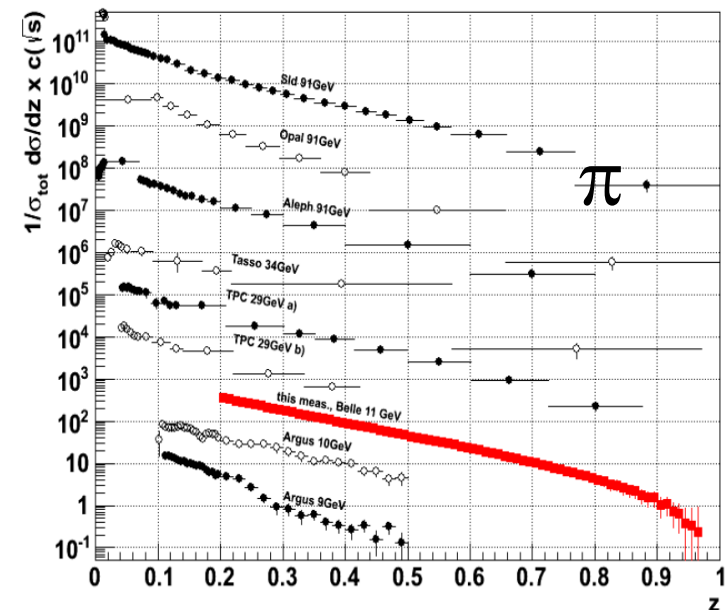
Where to Study?

- e^+e^- cleanest way to access FFs



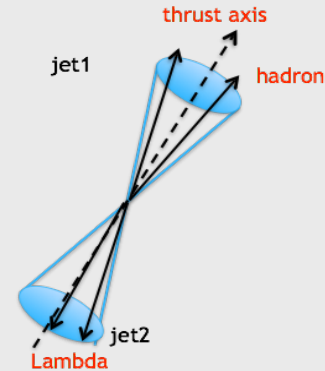
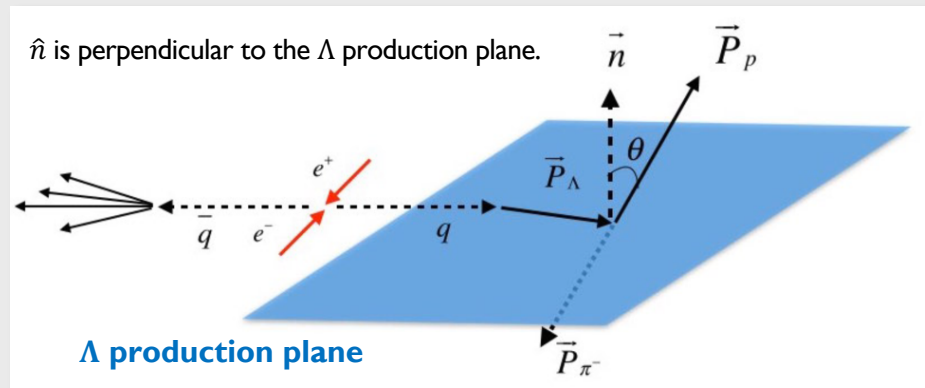
- B factories

- close in energy to SIDIS (100 GeV^2 vs 2 GeV^2)
- Large integrated lumi!, high z reach



Observables in Λ Restframe

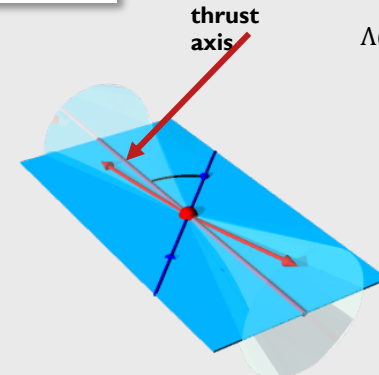
36



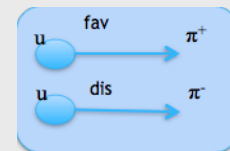
- Self-analyzing decay leads to polarization dependent distribution

$$\frac{1}{N} \frac{dN}{d\cos\theta} = 1 + \alpha P \cos\theta$$

- where α is the decay parameter: $\alpha_+ = 0.642 \pm 0.013$ for Λ and $\alpha_- = -0.71 \pm 0.08$ for $\bar{\Lambda}$ (PDG).
- The p_t is measured as the transverse momentum of Λ relative to the **thrust axis**



$\Lambda(u\bar{d}s); \pi^+(u\bar{d}); K^+(u\bar{s})$



Thrust

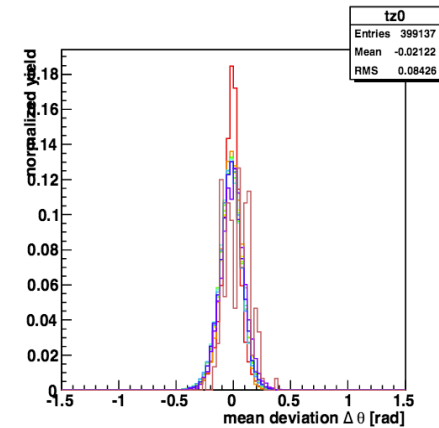
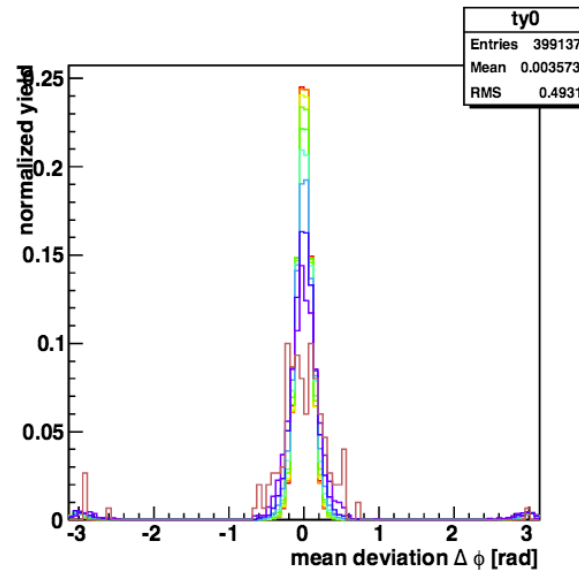
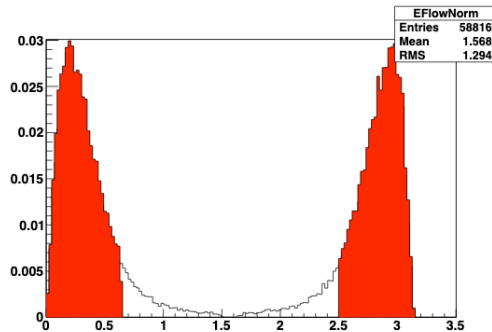
- → at Belle energies 2 jet events, connection to di-jet events

Seminal measurements, Collins IFF

G1\perp

Jet vs Thrust vs $q\bar{q}$ axis

- Non-negligible resolution effects
- In terms of k_T multiply by $\sim z^{*0.5}\sqrt{s}$, e.g. for typical RMS of 0.1 rad RMS ~ 100 MeV RMS for p_T (Similar as BaBar)



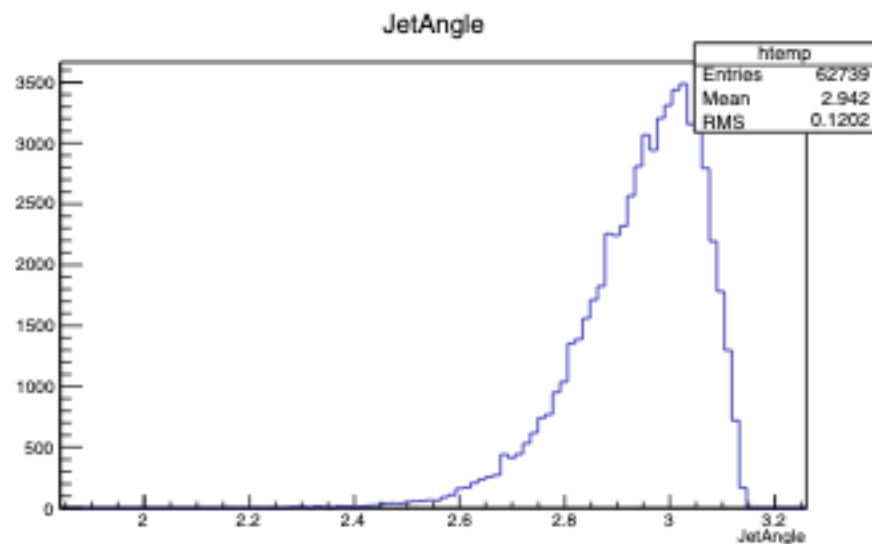


FIG. 12. The angle between two jets in 4π Monte Carlo simulation.

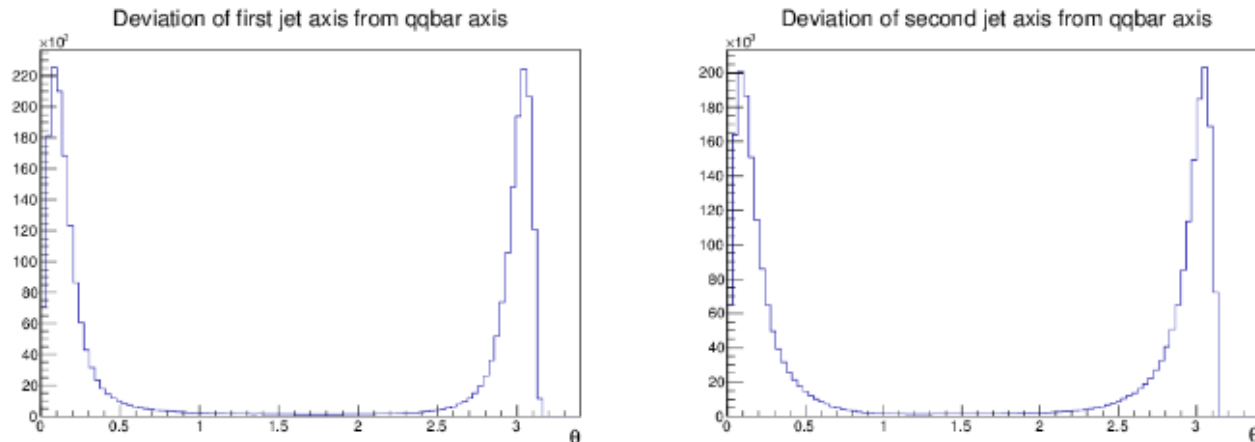
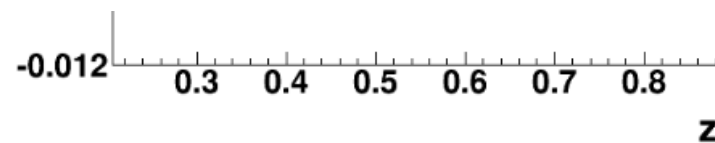
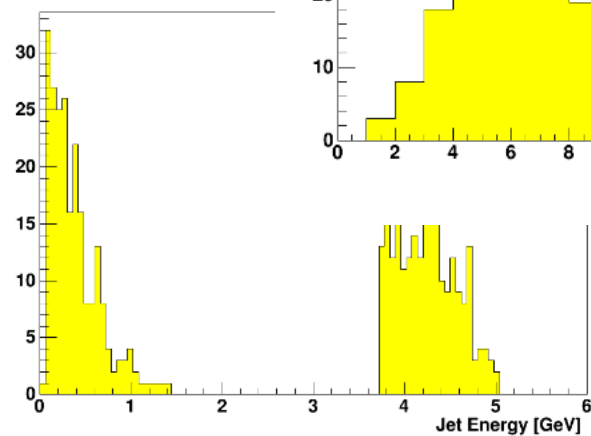
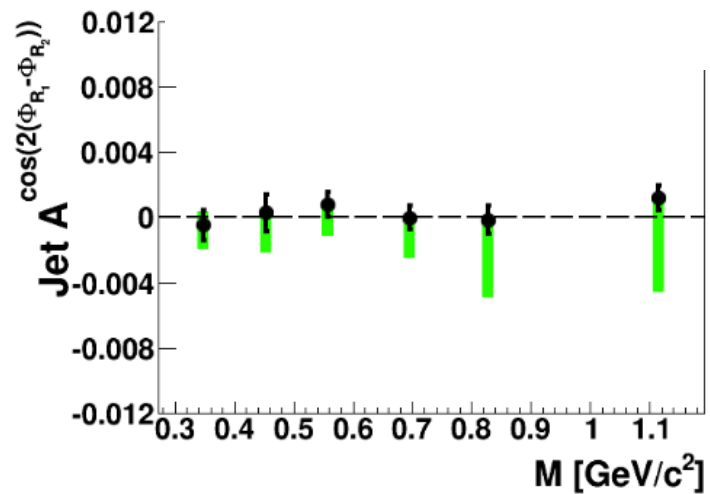
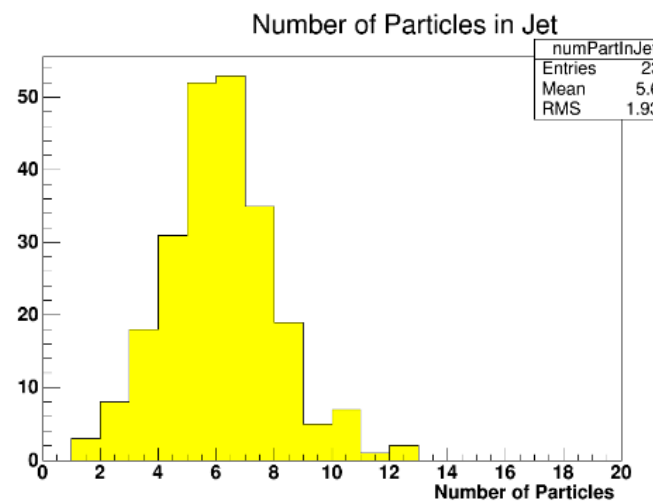
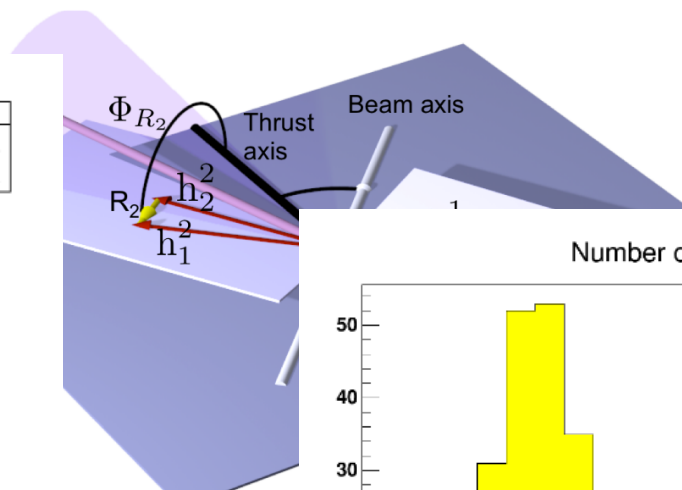
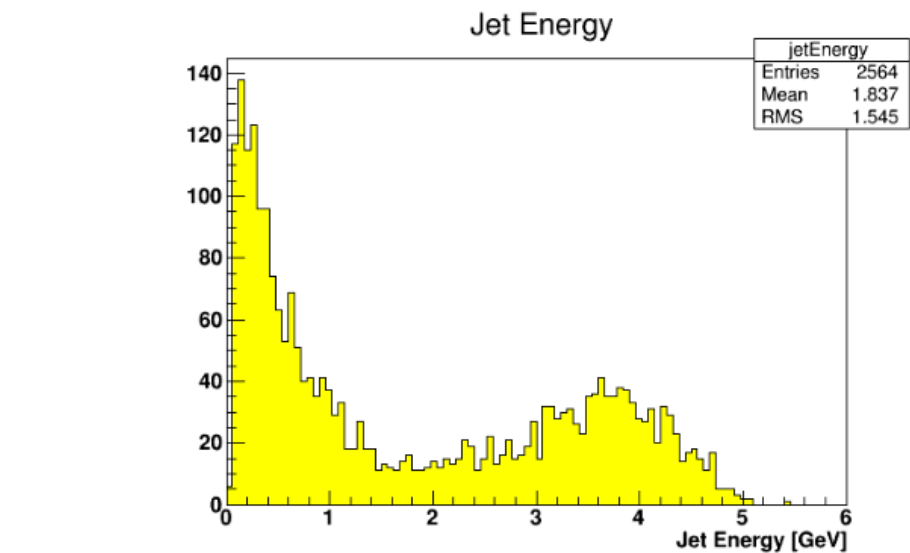


FIG. 14. The angle between jet and initial $q\bar{q}$ -pair axes. The left plot shows the deviation for the jet with the higher momentum in the pair and the right one with the lower momentum. The deviation for the lower momentum jet is larger, since less energy of the parent quark is reconstructed in the jet. In the analysis the order is randomly assigned.



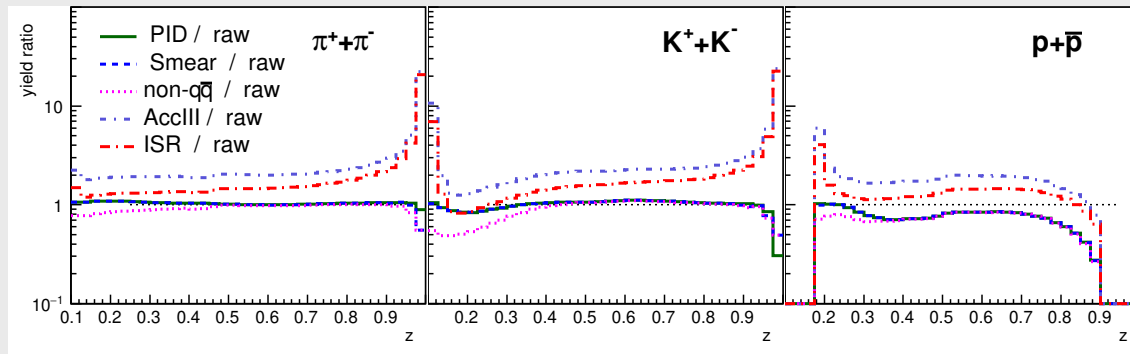
Latest: TMD FF

From Hadron yields to Cross-sections

- **Hadron yields undergo a series of corrections**
 - Particle (mis) identification [e.g. not every identified pion was a pion]
 - Smearing unfolding [e.g. measured and true momentum might differ]
 - Non $\bar{q}q$ -processes [e.g. two photon processes, $\Upsilon \rightarrow B\bar{B}\dots$]
 - “ 4π ”-correction [selection criteria and limited acceptance]
 - QED radiation [initial-state radiation (ISR)]
- **Collins asymmetries also corrected for false asymmetries and axis (mis)reconstruction**

From Hadron ⁴⁷ yields to Cross-sections

- **Example: single hadron inclusive cross-sections**
 - Largest effect for mesons **from acceptance and ISR corrections**
 - Larger PID correction for protons than for mesons

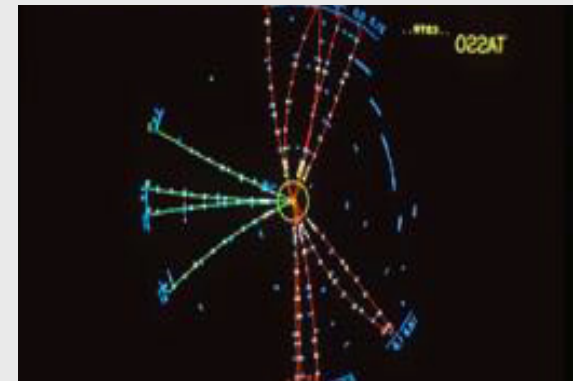
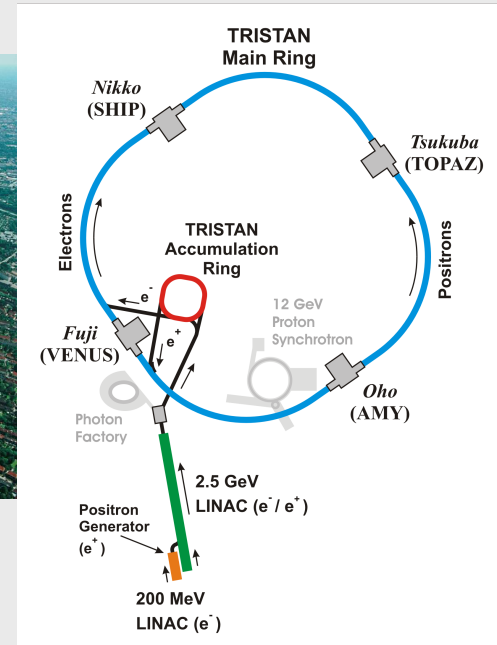
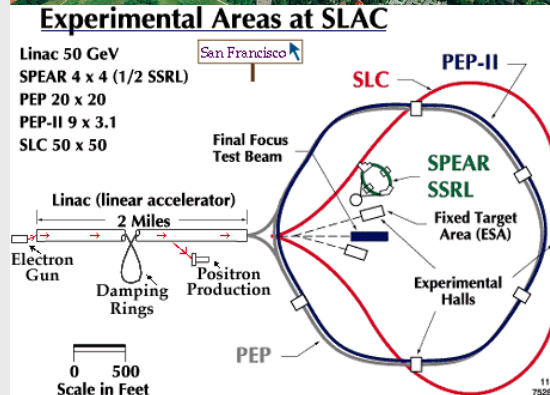


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Long history of e⁺e⁻ colliders: First generation for FF measurements

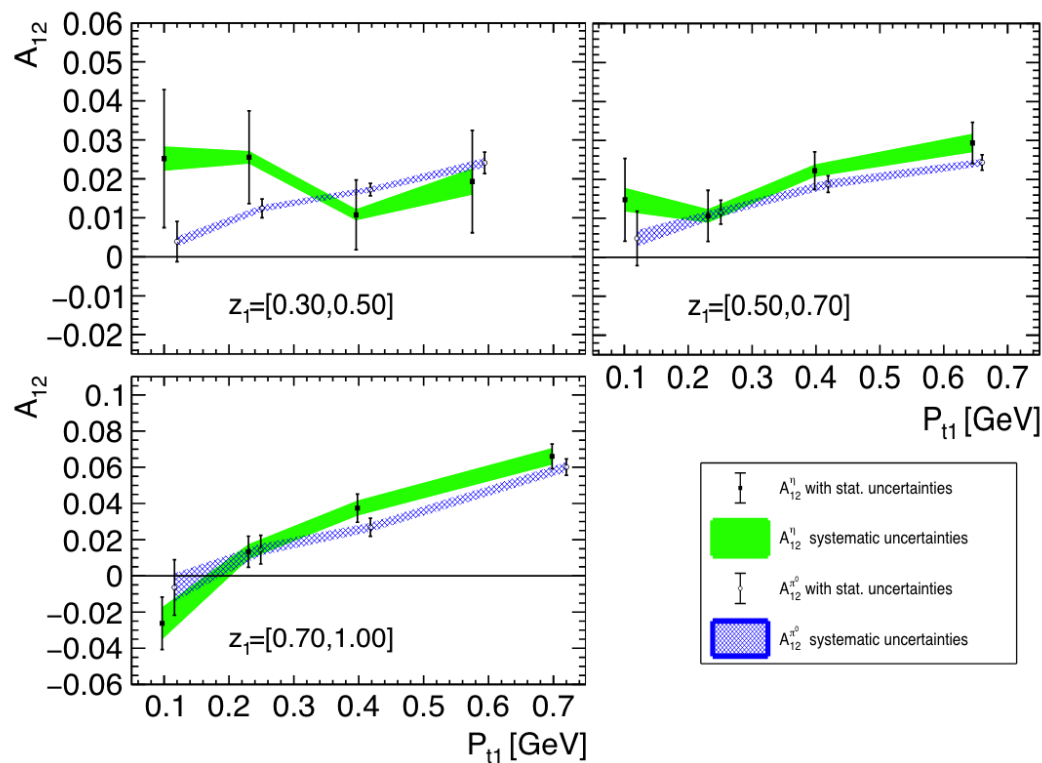
48

- X-section below M_{Z^0}
- DESY:
 - DORIS I (3-5) DORIS II (7-10 GeV)
 - PETRA 14-46 GeV (1978-86) : TASSO (34pb⁻¹ (34/44 GeV)
- SLAC:
 - PEP@29GeV 1980-1990 (TPC 140 pb⁻¹), HRS, MARK I
- KEK:
 - Tristan @ 50-64 : TOPAZ, AMY (278pb⁻¹)



Outlook to Belle II

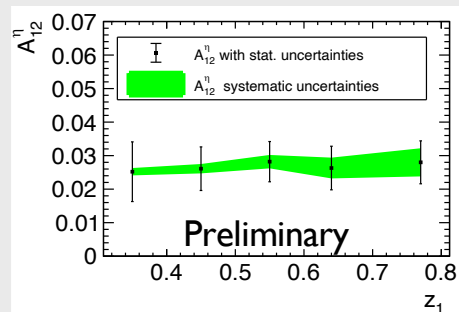
New π^0/η from Belle



$$\mathcal{R}_{12}^{\pi^0} = \frac{R_{12}^{0\pm}}{R_{12}^L} = \frac{\pi^0\pi^+ + \pi^0\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

$$\mathcal{R}_{12}^{\eta} = \frac{R_{12}^{\eta\pm}}{R_{12}^L} = \frac{\eta\pi^+ + \eta\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

- **Rise with $z_{1,2}$, similar to charged pions**



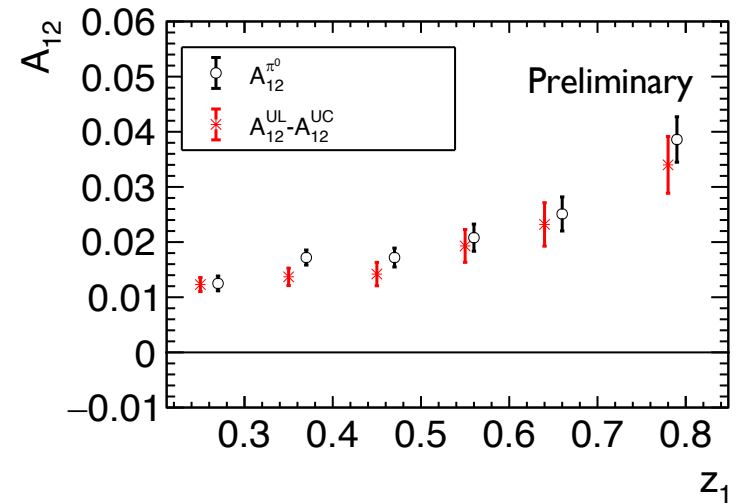
- η almost flat except large z

Consistency between Neutral and charged pions

$$\mathcal{R}_{12}^{\pi^0} = \frac{R_{12}^{0\pm}}{R_{12}^L} \approx 1 + \cos(\phi_{12}) \frac{\sin^2(\theta)}{1 + \cos^2(\theta)}$$

$$\times \left\{ \frac{5(H_1^{\perp, fav} + H_1^{\perp, dis}) \otimes (H_1^{\perp, fav} + H_1^{\perp, dis}) + 4H_{1,s \rightarrow \pi}^{\perp, dis} \otimes H_{1,s \rightarrow \pi}^{\perp, dis}}{5(D_1^{fav} + D_1^{dis}) \otimes (D_1^{fav} + D_1^{dis}) + 4D_{1,s \rightarrow \pi}^{dis} \otimes D_{1,s \rightarrow \pi}^{dis}} - \frac{10H_1^{\perp, fav} \otimes H_1^{\perp, dis} + 2H_{1,s \rightarrow \pi}^{\perp, dis} \otimes H_{1,s \rightarrow \pi}^{\perp, dis}}{10D_1^{fav} \otimes D_1^{dis} + 2D_{1,s \rightarrow \pi}^{dis} \otimes D_{1,s \rightarrow \pi}^{dis}} \right\}.$$

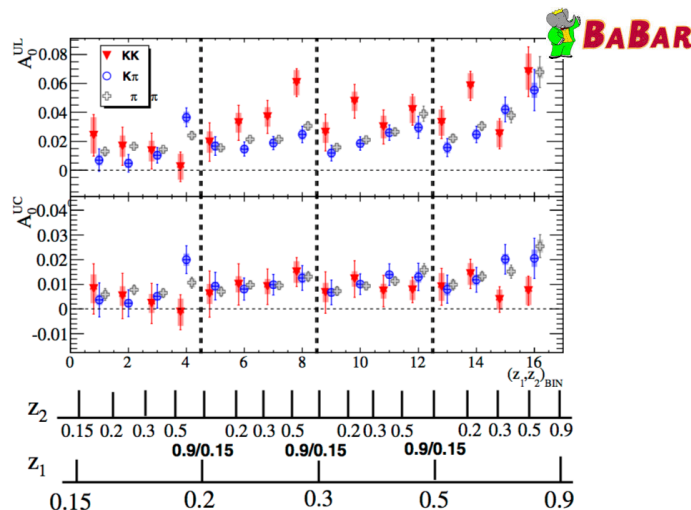
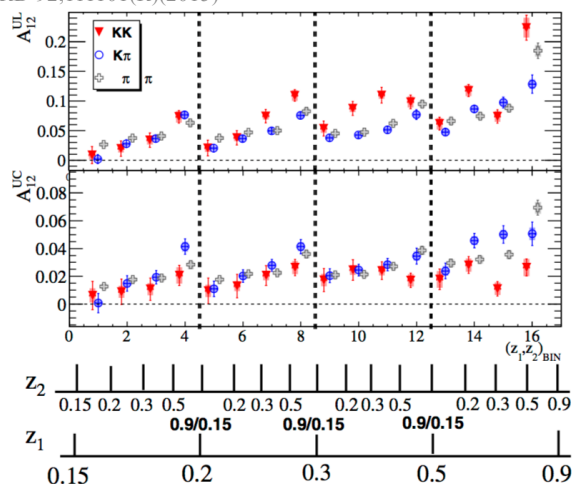
$= A_{12}^{UL} - A_{12}^{UC}$ (Isospin)



Collins effect for kaon/pion pairs

Simultaneous measurement of KK, K π and $\pi\pi$ Collins asymmetries from BaBar data

PRD 92,111101(R)(2015)



- Rising of the asymmetry as a function of z :
 - more pronounced for U/L
- A^{UL} KK asymmetry slightly higher than pion asymmetry for high z
- KK asymmetry consistent with zero at lower z
- $\pi\pi$ asymmetries consistent with previous measurements (PRD90, 052003)

- Analysis performed differentially in bins of $z, P_{hT}, Thrust$
($18 \times 20 \times 6$)