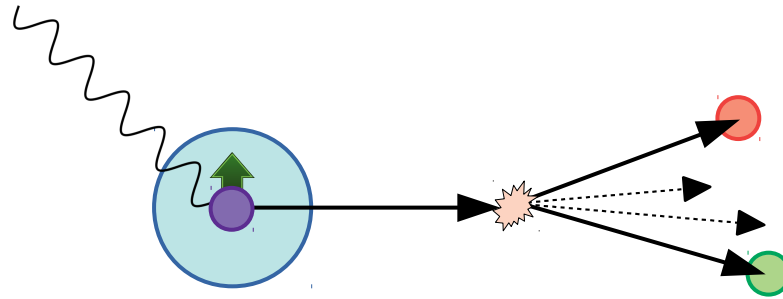


Dihadrons at the EIC



Christopher Dilks

Yellow Report Workshop Pavia

May 2020



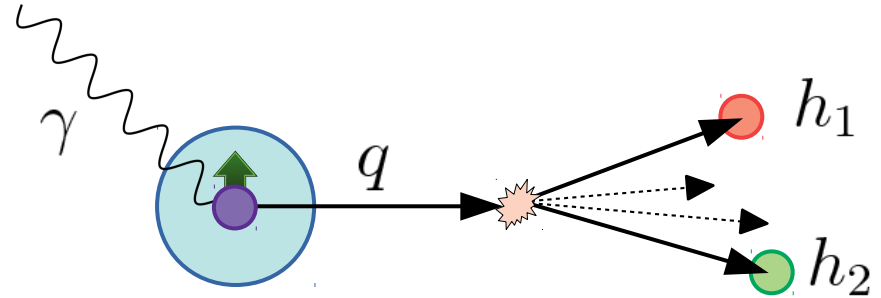
Outline

- ◆ Introduction
- ◆ Event Selection and Monte Carlo Details
- ◆ x, Q^2 planes and binning
- ◆ Effects of y cuts
- ◆ Polar plots
- ◆ Effects of acceptance limits
- ◆ Dihadron kinematics
- ◆ PID performance

Dihadrons: Probing Spin-Orbit Correlations in Hadronization

Unpolarized SIDIS:

- ◆ **Cahn Effect:** quark transverse momentum leads to azimuthal modulations of SIDIS cross section
- ◆ **Boer-Mulders Effect:** Non-collinear quarks in an unpolarized proton can have transverse polarization, also contributing azimuthal modulations



Boer-Mulders and Cahn effects are comparable in single hadron production

- HERMES and COMPASS data, e.g. Phys.Rev.D 81 (2010) 114026

Dihadrons can help decouple BM from Cahn

- Extra degree of freedom in dihadrons
 - Cahn effect impacts dihadron total momentum direction P_h
 - Utilize azimuthal angle about P_h , in addition to the azimuth about the virtual photon

Advantages from a broader and higher Q^2 range at an EIC

- Broader Q^2 range probes evolution effects
- Higher Q^2 suppresses Cahn effect in single-hadron asymmetries (Cahn is twist-4)
- Lower Q^2 for overlap with other SIDIS experiments

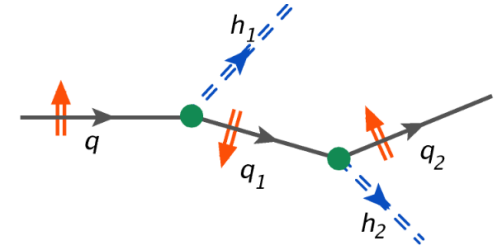
Dihadrons: Probing Spin-Orbit Correlations in Hadronization

Longitudinally polarized SIDIS:

■ Helicity DiFF G_1^{\perp} :

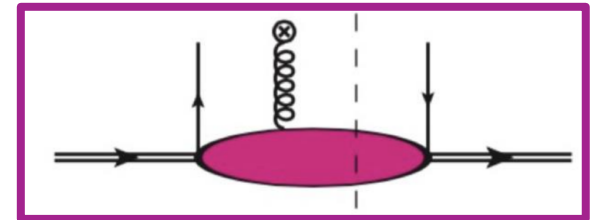
- Not yet constrained by data!
- Spin-orbit correlations in hadronization
- Fragmenting quark acquires transverse polarization via ‘wormgear’ splitting in the quark-jet hadronization model
- Preliminary CLAS12 data indicate **significant effect**, dependent on invariant mass

$$G_1^{\perp} = \text{[Diagram: A quark } q \text{ with a blue circular arrow indicating spin, emitting two black arrows representing hadrons. This is followed by a minus sign and another quark } q \text{ with a blue circular arrow indicating spin, emitting two black arrows representing hadrons.]}$$



■ Collinear Twist-3 PDFs $e(x)$ and $h_L(x)$:

- CLAS6 data provided the first $e(x)$ extraction, consistent with models; CLAS12 data are in agreement
- Physical Interpretation via moments of $e(x)$:
 - Transverse color-force on a transversely polarized struck-quark, in an unpolarized proton
 - πN sigma terms:
 - Quark mass contribution to proton mass
 - Quark chromomagnetic dipole moment \rightarrow CP-odd π -N coupling
- No experimental constraints yet for $h_L(x)$



Dihadrons: Probing Spin-Orbit Correlations in Hadronization

Transversely polarized SIDIS:

Access to several additional **TMDs**:

- Transversity** → Tensor Charge

$$\delta q = \int_{-1}^1 dx h(x) = \int_0^1 dx [h(x) - \bar{h}(x)]$$

- Quark EDM contribution to nucleon EDM → CP violation
- Comparisons with lattice QCD calculation
- Sivers Function**
- Kotzinian-Mulders (wormgear) Function**
- Pretzelosity**
- Twist-3 TMDs**

$$F_{UT} \begin{array}{lll} f_{1T}^\perp \otimes D_1 + g_{1T} \otimes G_1 & f_T \otimes D_1 & h_T \otimes H_1 \\ h_1 \otimes H_1 & f_T^\perp \otimes D_1 & h_T^\perp \otimes H_1 \\ h_{1T}^\perp \otimes H_1 & & \end{array}$$

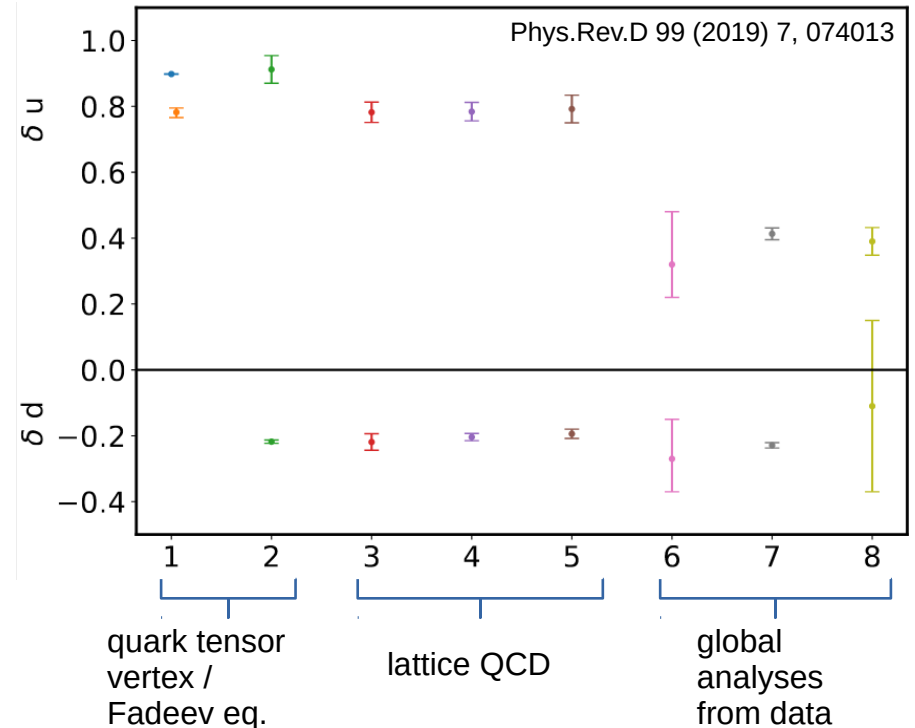
$$F_{LT} \begin{array}{lll} g_{1T} \otimes D_1 + f_{1T}^\perp \otimes G_1 & g_T \otimes D_1 & e_T \otimes H_1 \\ & g_T^\perp \otimes D_1 & e_T^\perp \otimes H_1 \end{array}$$

Twist-2 TMDs

N/q	U	L	T
U	f_1		h_1^\perp
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_{1T}, h_{1T}^\perp

Twist-3 TMDs

N/q	U	L	T
U	f^\perp	g^\perp	h, e
L	f_L^\perp	g_L^\perp	h_L, e_L
T	f_T, f_T^\perp	g_T, g_T^\perp	$h_T, e_T, h_T^\perp, e_T^\perp$

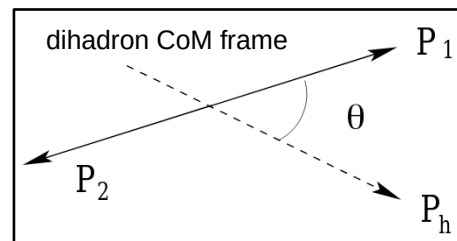


Dihadron Fragmentation and Partial Waves

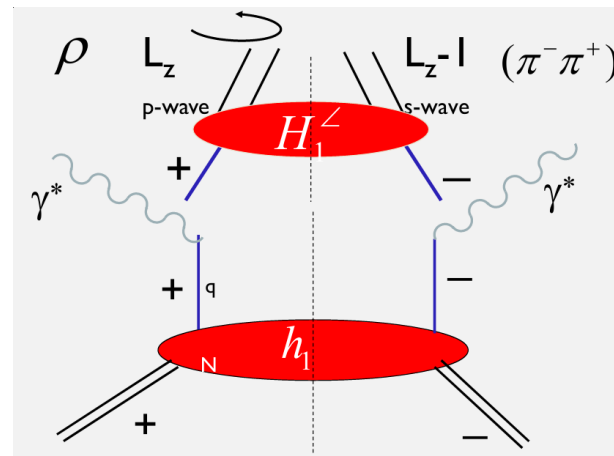
$$H_1^\perp = \sum_{\ell=0}^{\ell_{\max}} \sum_{m=-\ell}^{\ell} \underline{P_{\ell,m}(\cos \vartheta)} e^{im(\phi_{R_\perp} - \phi_p)} H_1^{\perp|\ell,m\rangle}(z, M_h, |\mathbf{p}_T|)$$

Dihadron Fragmentation Functions (DiFFs)

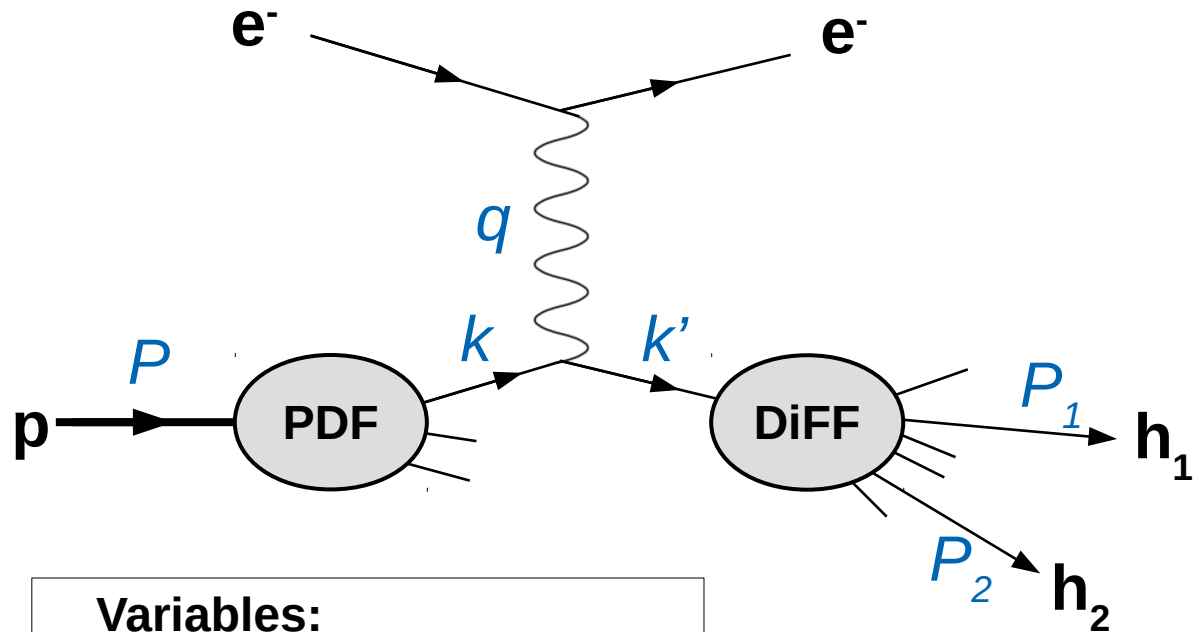
$h_1 h_2 / q$	U	L	T
UU	$D_{1,00}$		$H_{1,00}^\perp$
LU	$D_{1,0L}$		$H_{1,0L}^\perp$
LL	$D_{1,LL}$		$H_{1,LL}^\perp$
TU	$D_{1,OT}$	$G_{1,OT}^\perp$	$\begin{cases} H_{1,OT}^\perp & \text{if } m < 0 \\ H_{1,OT}^\triangleleft & \text{if } m > 0 \end{cases}$
TL	$D_{1,LT}$	$G_{1,LT}^\perp$	$\begin{cases} H_{1,LT}^\perp & \text{if } m < 0 \\ H_{1,LT}^\triangleleft & \text{if } m > 0 \end{cases}$
TT	$D_{1,TT}$	$G_{1,TT}^\perp$	$\begin{cases} H_{1,TT}^\perp & \text{if } m < 0 \\ H_{1,TT}^\triangleleft & \text{if } m > 0 \end{cases}$



- DiFFs expand in partial waves
- Access to interference between dihadrons with relative angular momenta
 - ss, sp, pp interference



Dihadron Kinematics



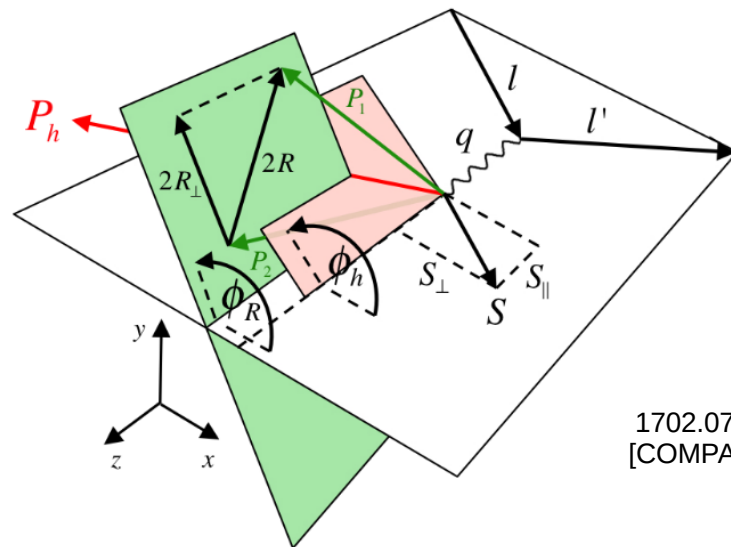
Variables:

- Scale: Q^2
- Bjorken-x: x
- Feynman-x: x_F
- Invariant Mass: M_h
- Fragmentation fraction: z
- Missing Mass: M_X

Momenta and Angles

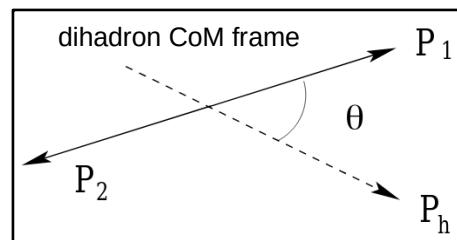
$$P_h = P_1 + P_2 \quad \Rightarrow \quad \phi_h$$

$$R = \frac{1}{2} (P_1 - P_2) \quad \Rightarrow \quad \phi_R$$



Sirtl
1702.07317
[COMPASS]

Dihadron CoM
production angle:



Monte Carlo

Energies:

- 5x41 $\sqrt{s} = 28.7$ GeV
- 5x100 $\sqrt{s} = 44.7$ GeV
- 10x100 $\sqrt{s} = 63.3$ GeV
- 18x275 $\sqrt{s} = 140.7$ GeV

▣ Event Generation

- Pythia6 (via pythiaeRHIC)
 - 1M events
 - Radiative corrections using RADGEN attempted, but was unsuccessful
 - Using steer file obtained from Elke
- Kinematic maps below focus on low and high CoM energy: 5x41 and 18x275

▣ Fast Simulation

- `eic_smear` with the `handbook` detector setting (via eJANA)
- Require the electron and hadron E and P to be smeared (in tracker+calorimeter)

▣ Analysis

- DIS kinematics reconstructed using highest-energy scattered electron
- Pions and Kaons are paired inclusively
- PID studies
- Architecture for asymmetry fits / projections is ready
 - Uses same code for a parallel analysis at CLAS
 - Projections for partial wave amplitudes is also possible

Event Selection

$Q^2 > 1 \text{ GeV}^2$ cut for event generator

$W > 3 \text{ GeV}$ exclude elastic / resonance region

$0.01 < y < 0.95$ lower bound is to avoid region in which calculating x , Q^2 , etc. via the e' momentum may be insufficient

$x_{F_h} > 0$ help ensure hadrons are produced in the current fragmentation region

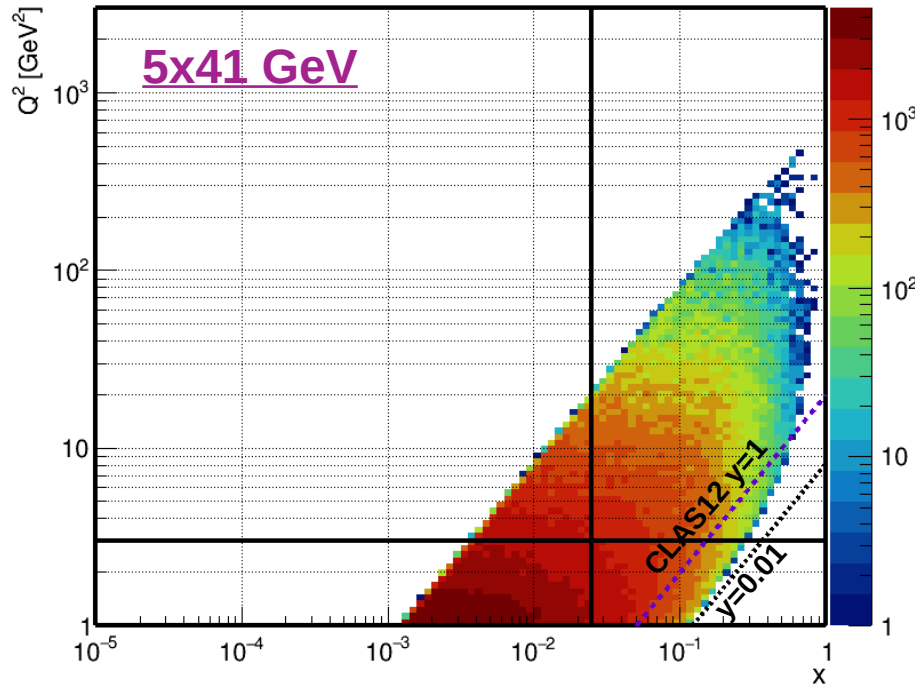
$z_h > 0.01$ cuts out long M_h tail at $z \sim 0$ peak (need to think about...)

$z_{h_1 h_2} < 0.95$ helps avoid exclusive region

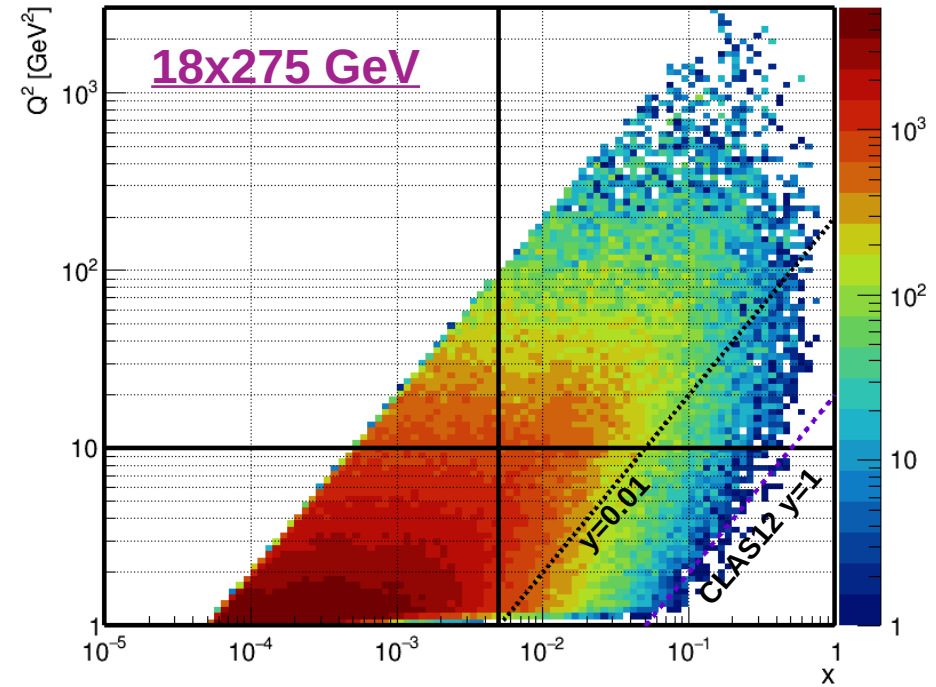
Focusing on $\pi^+\pi^-$ channel

(x, Q^2) Planes, with Binning

Q^2 vs. x for selected dihadrons



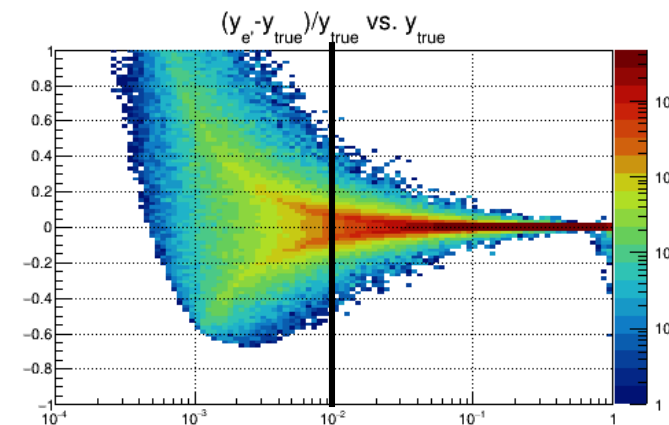
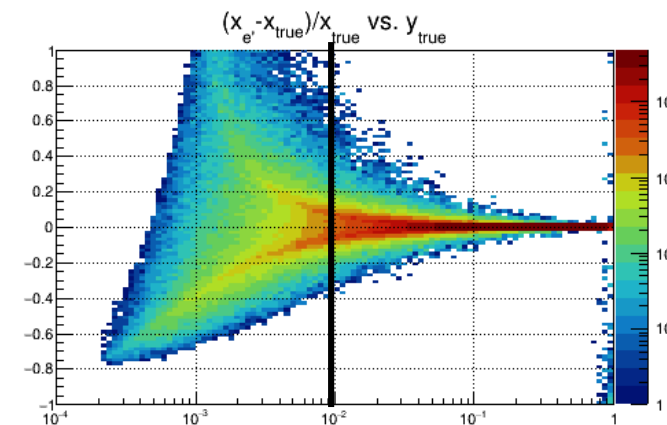
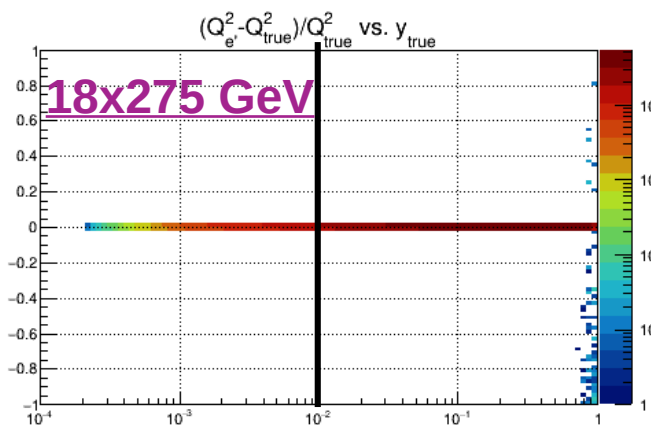
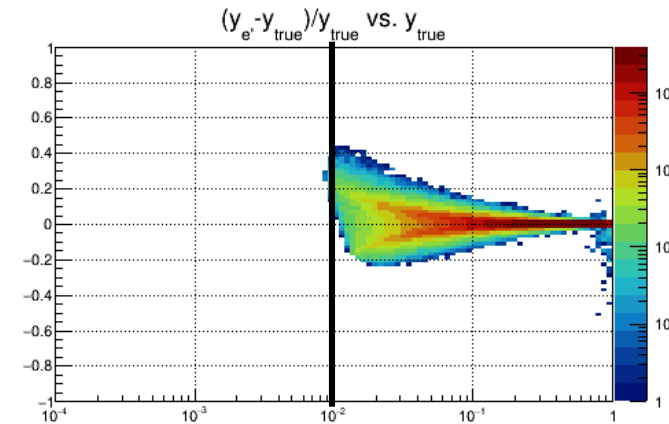
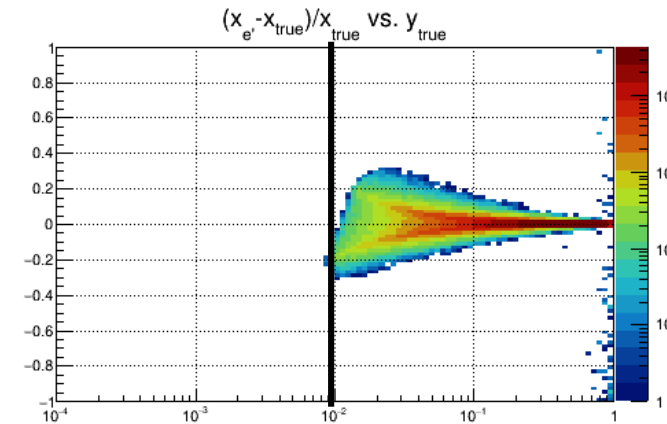
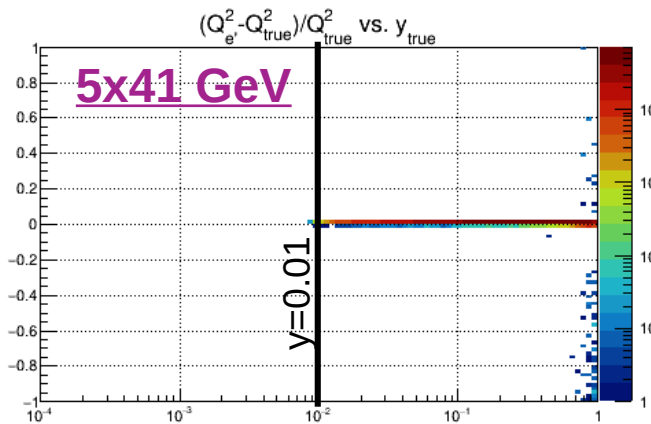
Q^2 vs. x for selected dihadrons



- Diagonal lines show y contour at the cut of 0.01, along with the CLAS12 upper limit ($y=1$)
 - 18x275 plot includes data with $y < 0.01$
 - Kinematic reach of 5x41 with $Q^2 > 1$ does not extend to $y < 0.01$, but overlaps with CLAS12
- Vertical / horizontal lines demarcate (x, Q^2) bin boundaries, used in the following slides
- Next slides show matrices of plots corresponding to these bins

Low-y Studies: effects of y cuts

Smearing Disabled



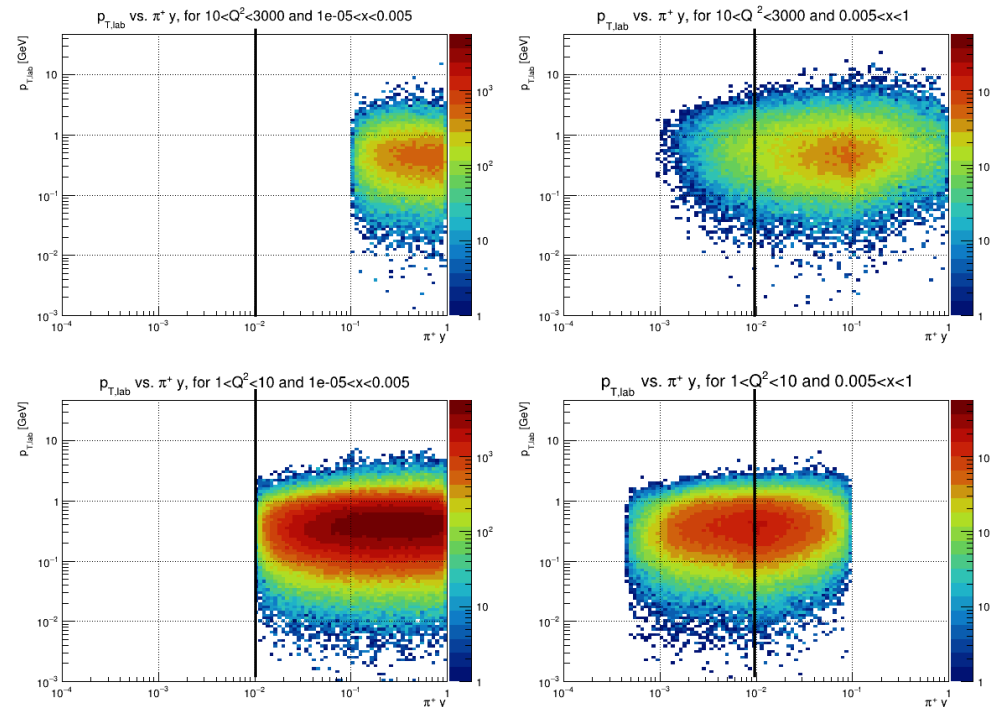
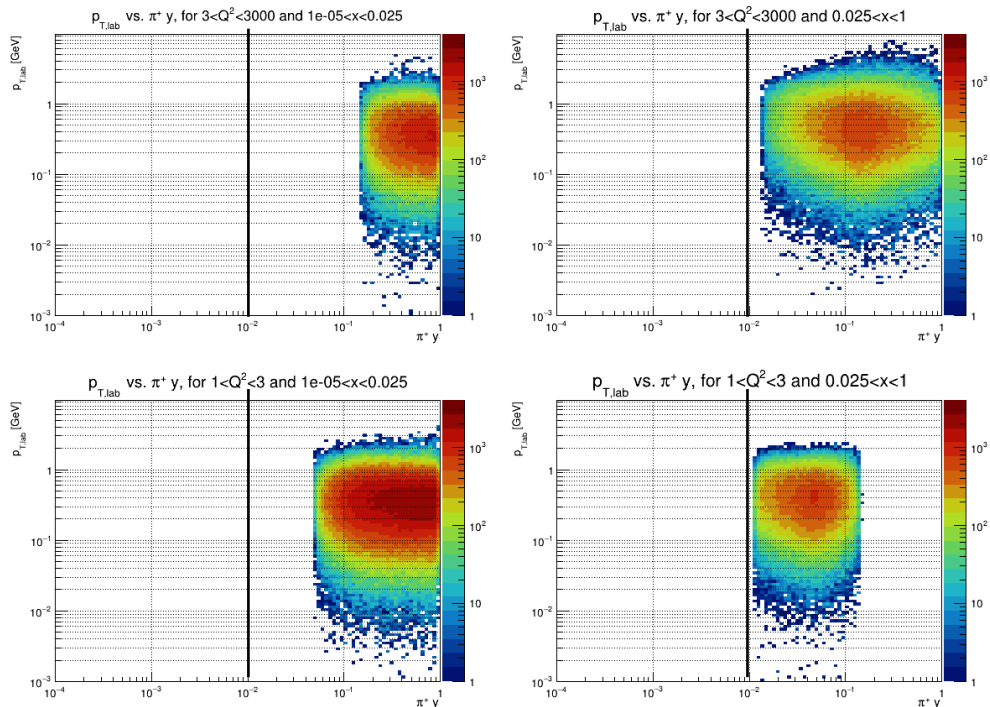
- DIS kinematics calculated using scattered electron are not reliable for $y < 0.01$
- By $y = 0.1$, there are already differences up to 15%
- (small fraction of high-y discrepancies not studied)

Effects of y cut on p_T

Smearing Disabled

5x41 GeV

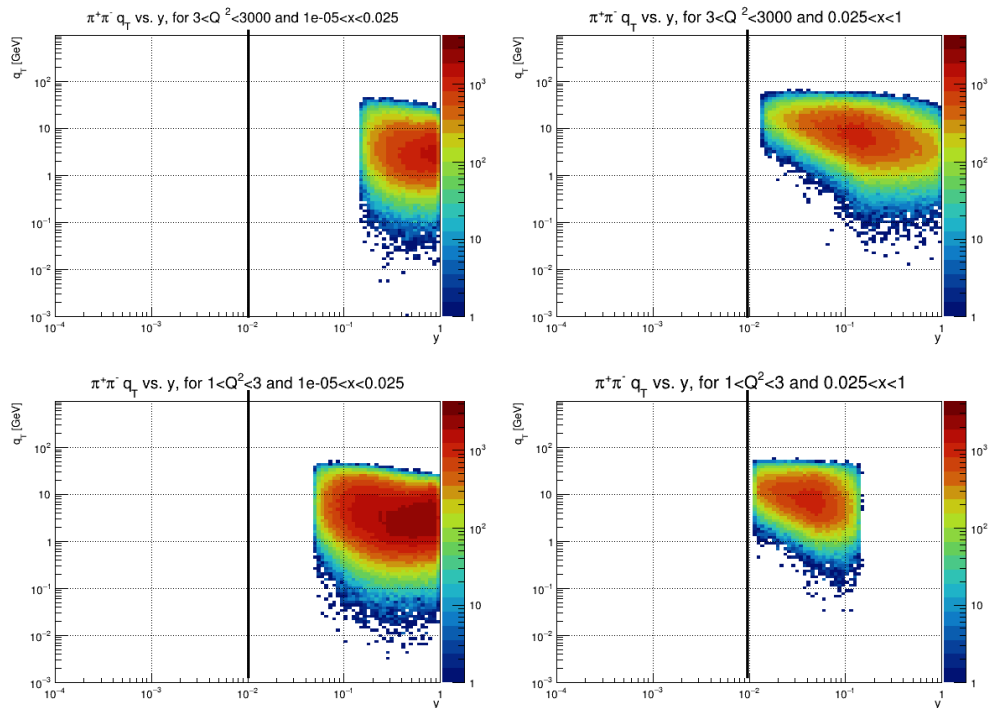
18x275 GeV



- This shows $\pi^+ p_T$ versus y ; black line indicates $y=0.01$
- 4 plot matrix corresponds to binning shown on (x, Q^2) planes above
- The impact of $y > 0.01$ cut is negligible
- Higher y cuts may start to shave away low p_T at high- x and low Q^2

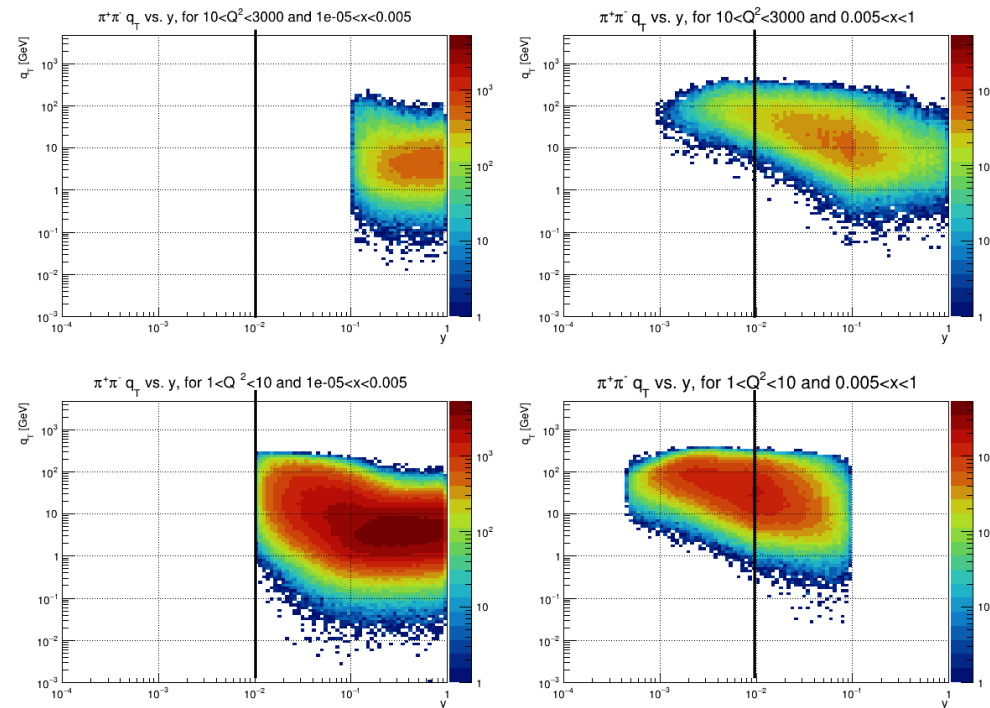
Effects of y cut on $q_T (=P_h^\perp/z_{\text{pair}})$

5x41 GeV



Smearing Disabled

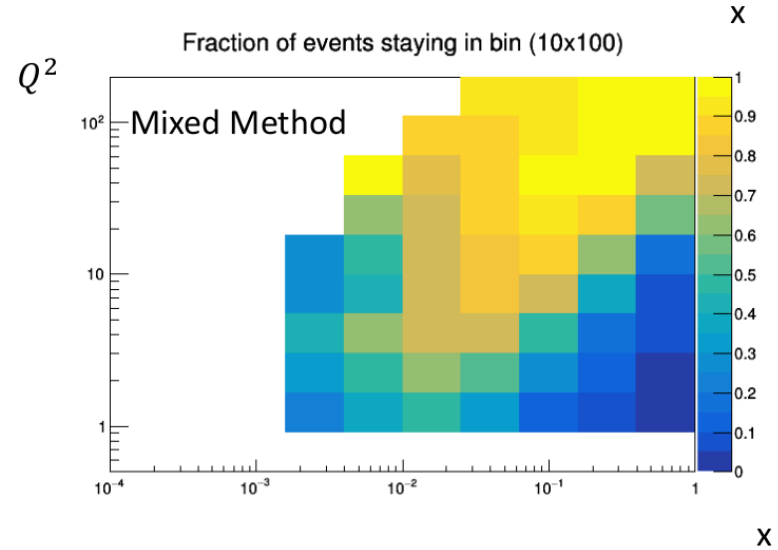
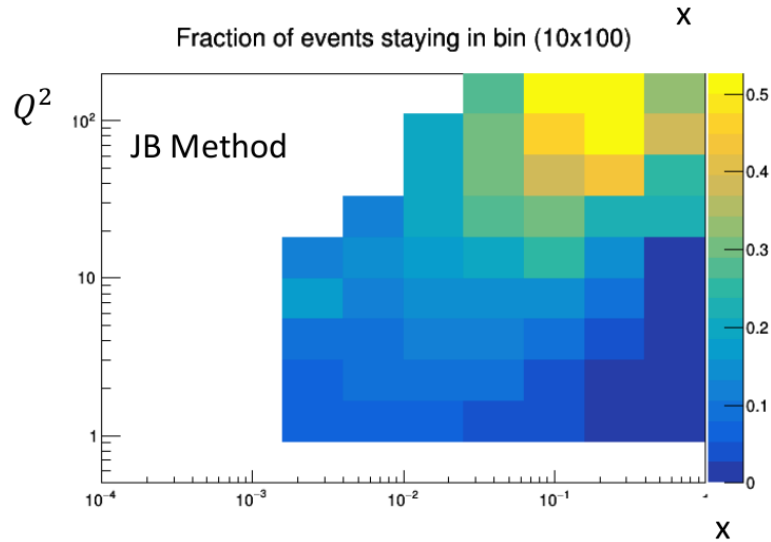
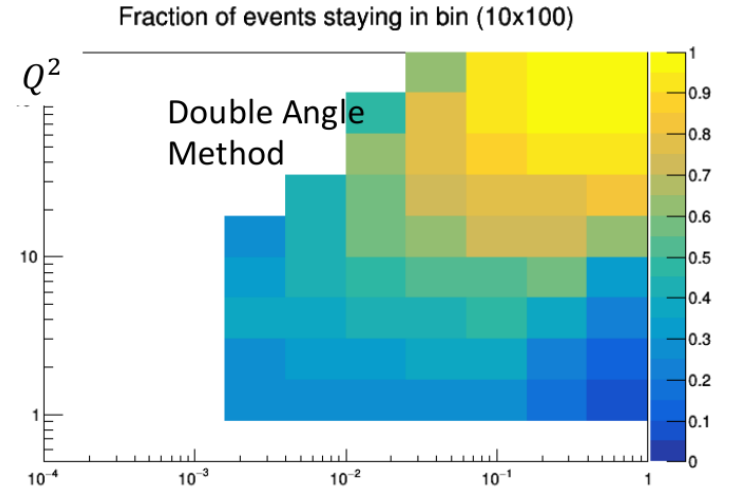
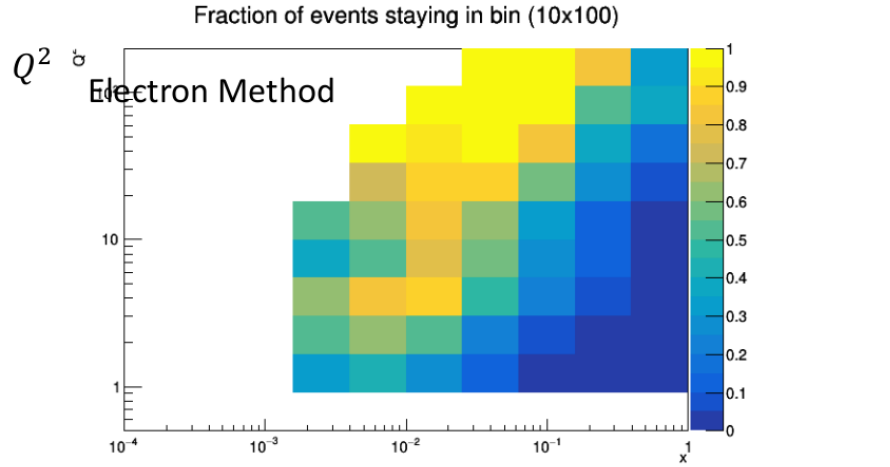
18x275 GeV



- Compare to q_T versus y ; black line indicates $y=0.01$
- Mean q_T will decrease a bit as y cut is increased

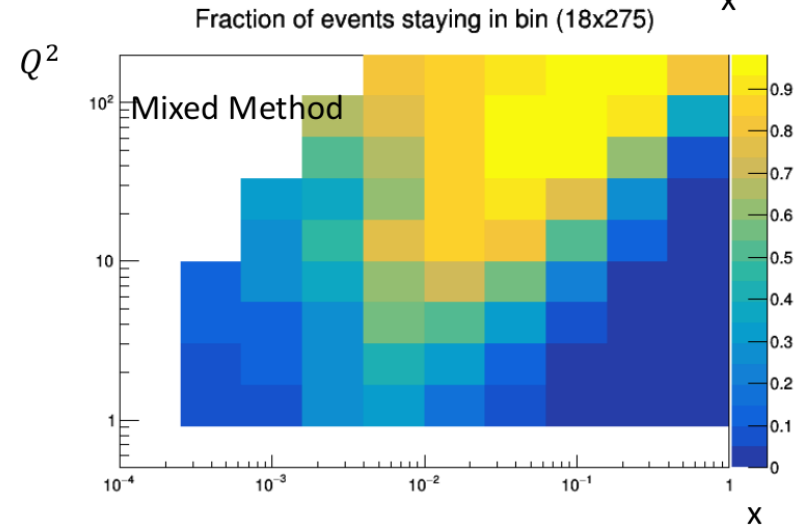
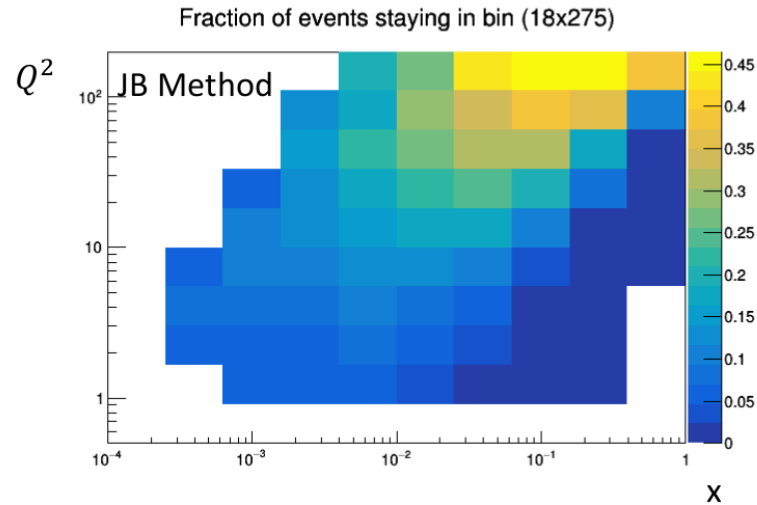
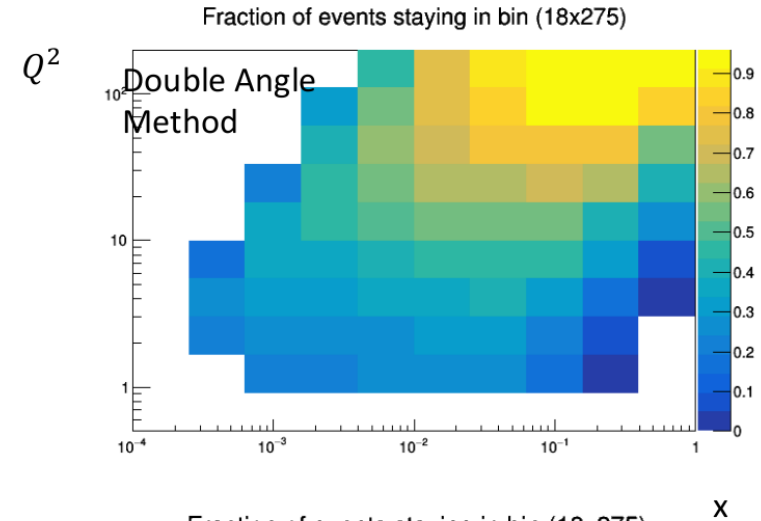
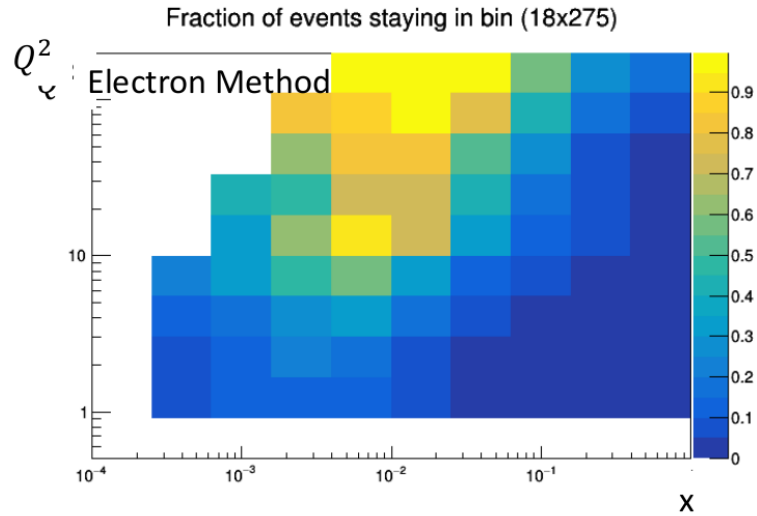
Aside: Alternative methods for calculating (x, Q^2)

Study from Anselm



Aside: Alternative methods for calculating (x, Q^2)

Study from Anselm

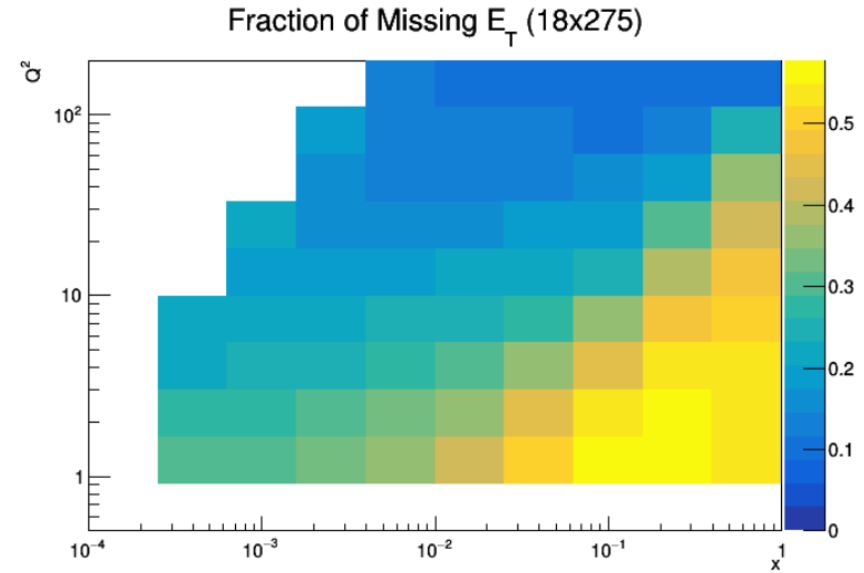
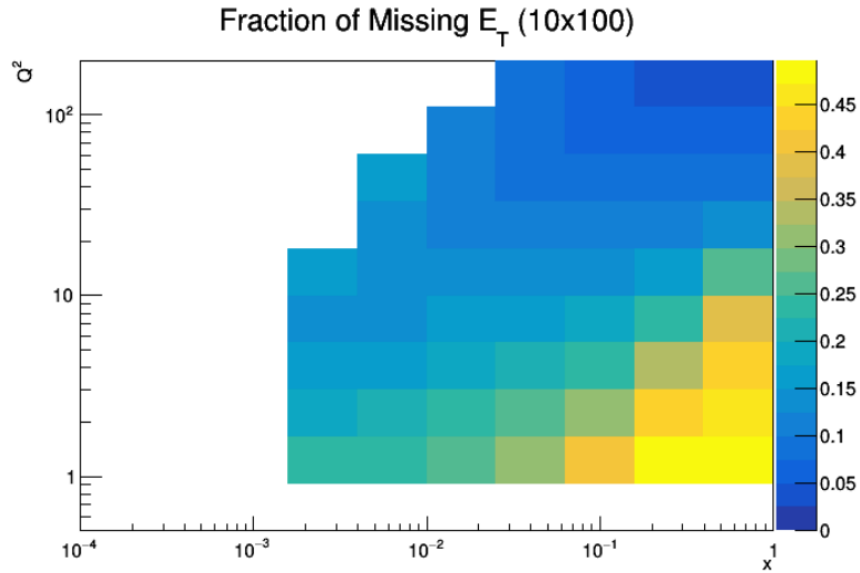


Aside: Alternative methods for calculating (x, Q^2)

Study from Anselm

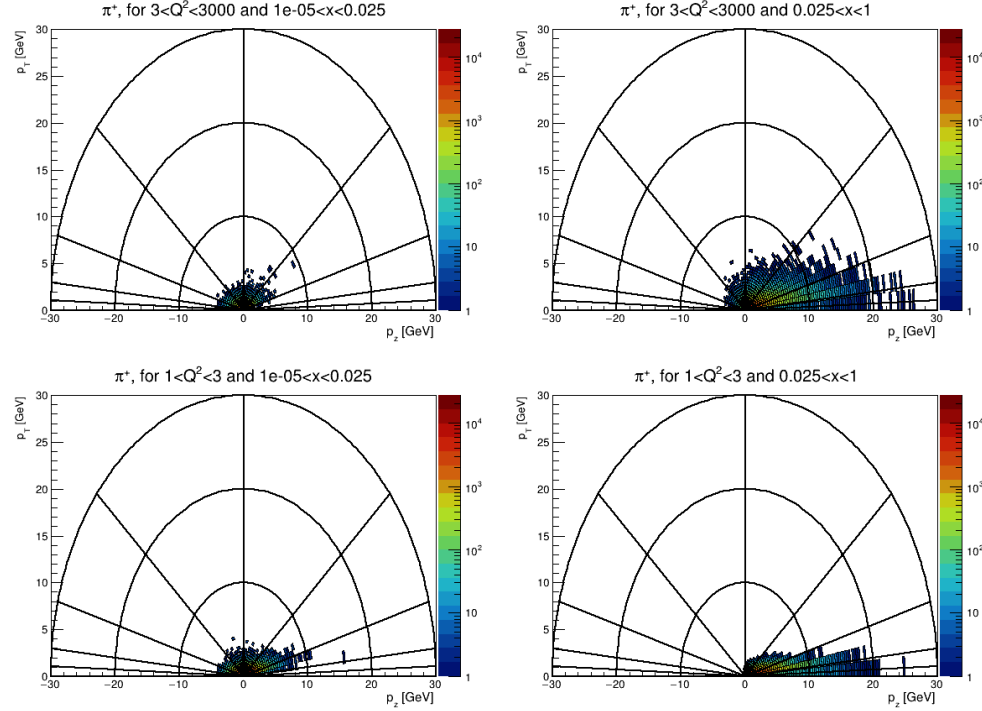
Fraction of missing energy, from acceptance limits

Larger fraction at low- y \rightarrow correlates to inaccuracy of (x, Q^2)

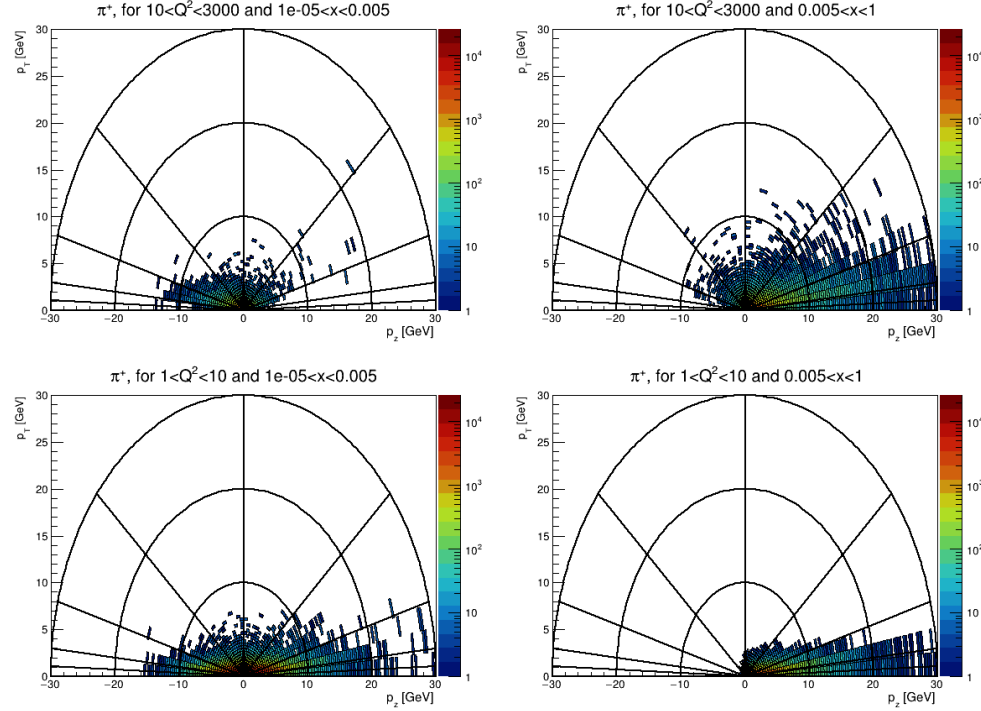


Pion Momentum

5x41 GeV



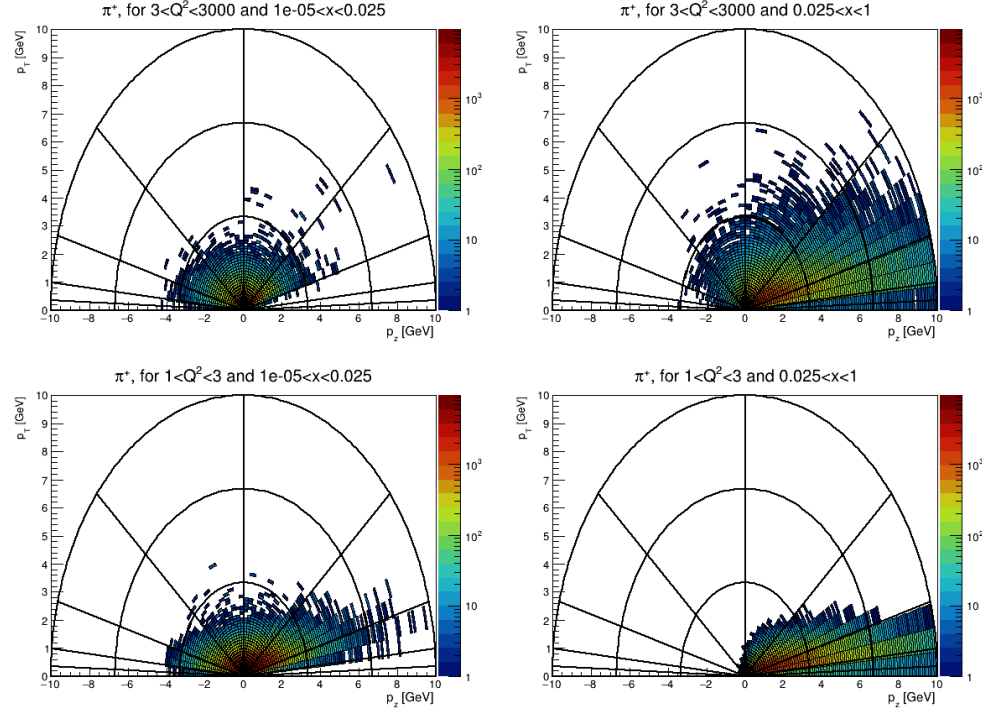
18x275 GeV



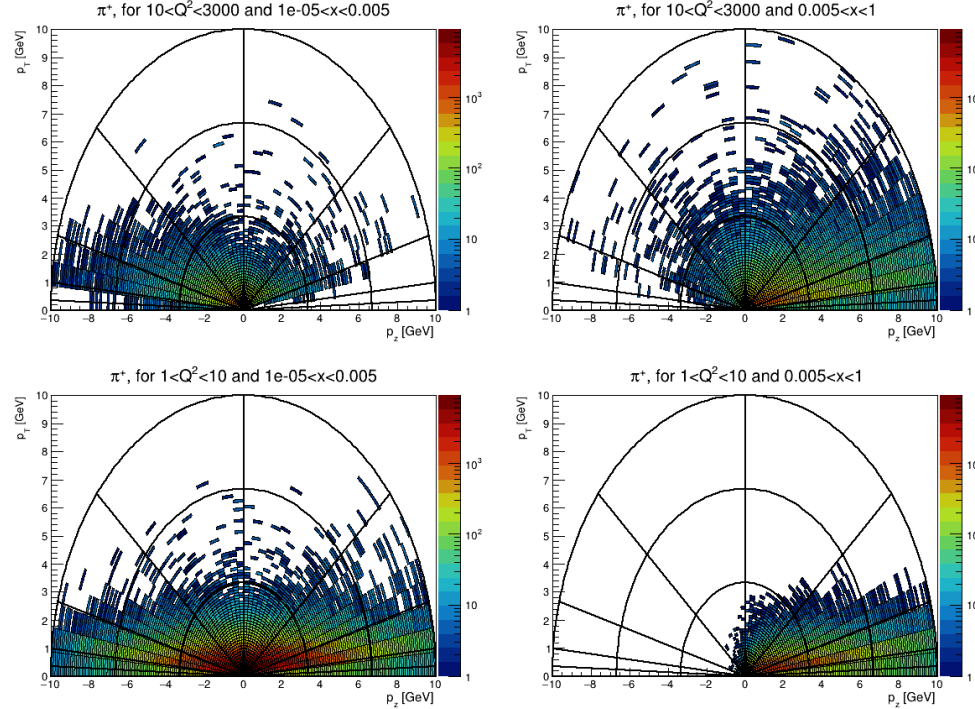
- Radius set at 30 GeV; compare to next slide's zoomed plot
- Smearing with eic-smear enabled → acceptance cuts at $|\eta|=3.5$
- This is for π^+ of $\pi^+\pi^-$ dihadrons, but the π^- looks the same

Pion Momentum

5x41 GeV



18x275 GeV



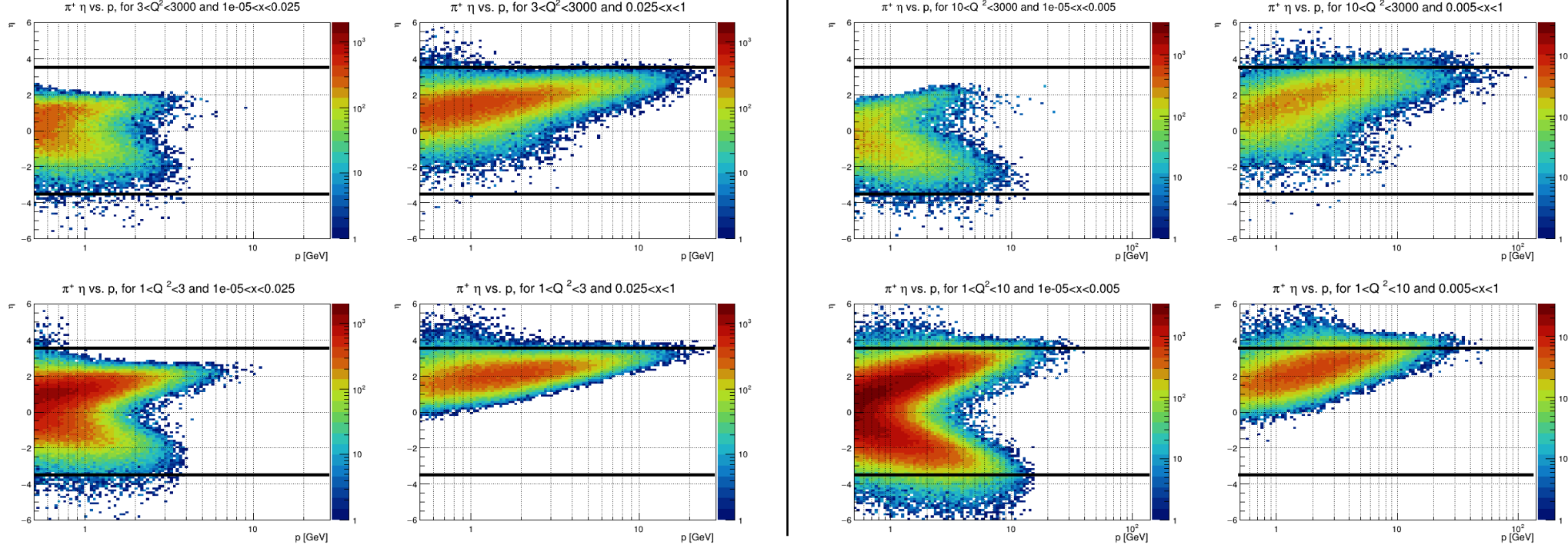
- Radius set at 10 GeV
- Smearing with eic-smear enabled → acceptance cuts at $|\eta|=3.5$
- This is for π^+ of $\pi^+\pi^-$ dihadrons, but the π^- looks the same
- Some backward production at low x

Pion Momentum vs. Pseudorapidity

Smearing Disabled

5x41 GeV

18x275 GeV



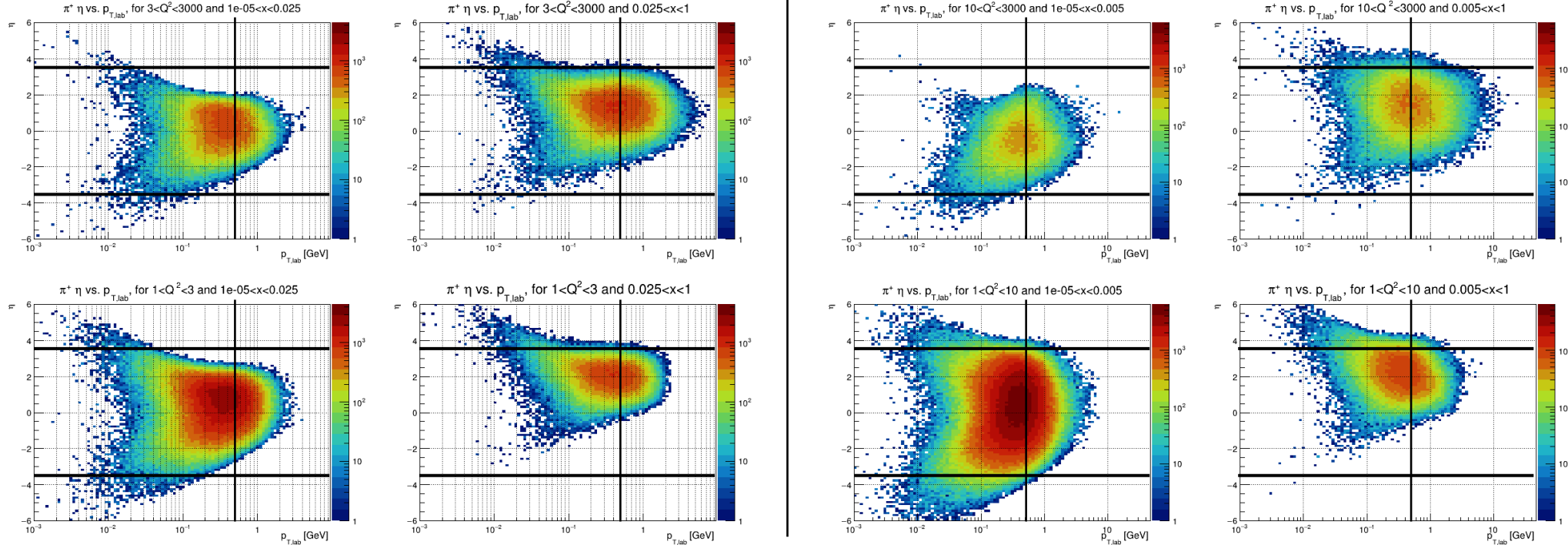
- Smearing disabled, to show activity beyond acceptance cuts
 - Enabling smearing does not alter the shape of the distributions much
- Lines for $|\eta|=3.5$ are shown
- Acceptance cuts only effect $p < \sim 4$ GeV
- $\pi/K/p$ separation up to $p \sim 8$ GeV is sufficient

Pion Transverse Momentum vs. Pseudorapidity

Smearing Disabled

5x41 GeV

18x275 GeV



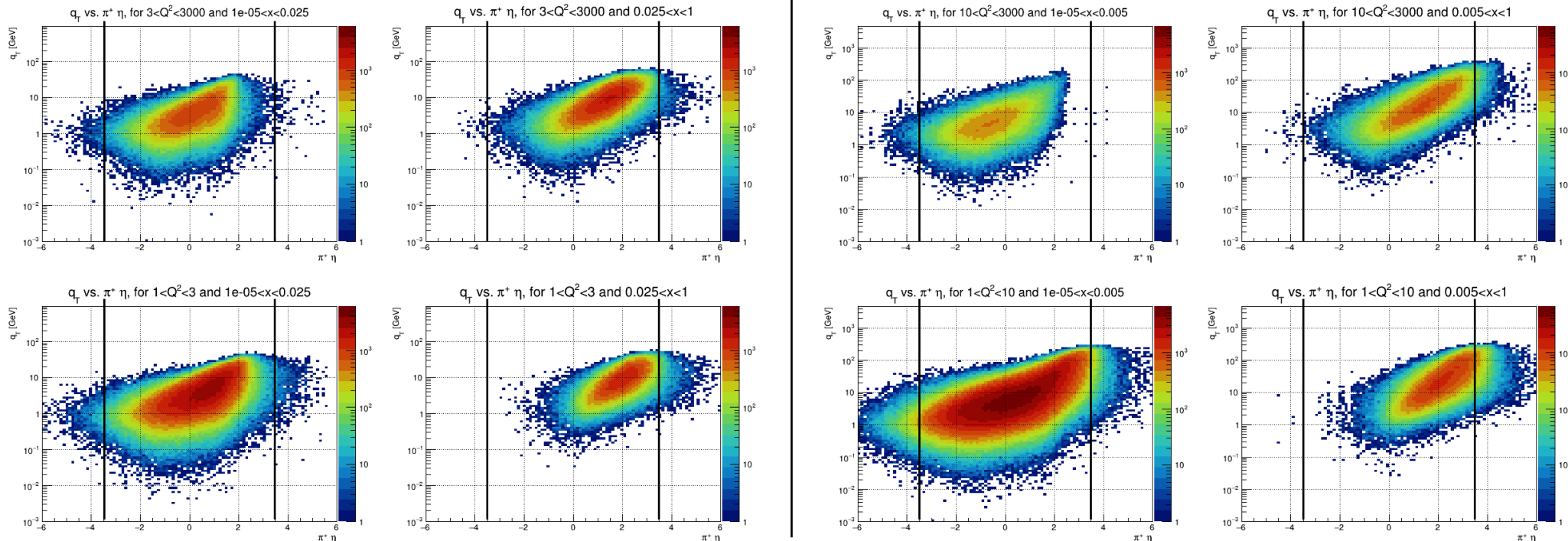
- Smearing disabled, to show activity beyond acceptance cuts
 - Enabling smearing does not alter the shape of the distributions much
- Horizontal lines for $|\eta|=3.5$
- Impact of acceptance cuts is primarily on low p_T , well below the 500 MeV threshold (vertical lines)

Effects of η cuts on q_T

Smearing Disabled

5x41 GeV

18x275 GeV

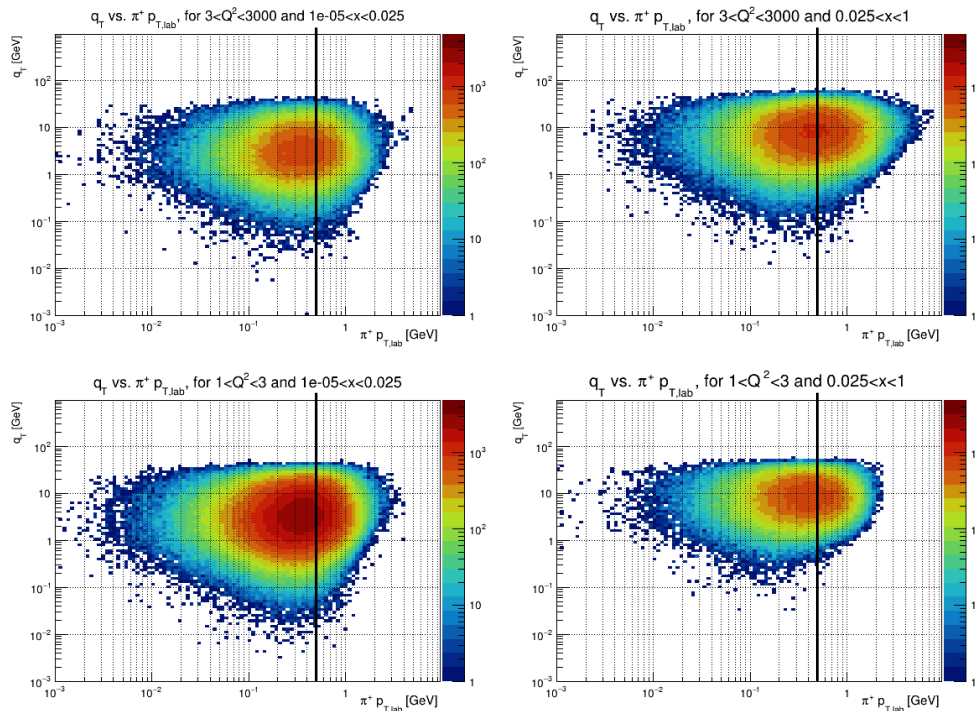


- Plots show $q_T = P_h^\perp / z_{\text{pair}}$ vs. η of π^+
- Smearing disabled, to show activity beyond acceptance cuts
- Vertical lines for $|\eta|=3.5$
- Little impact of acceptance cuts on q_T

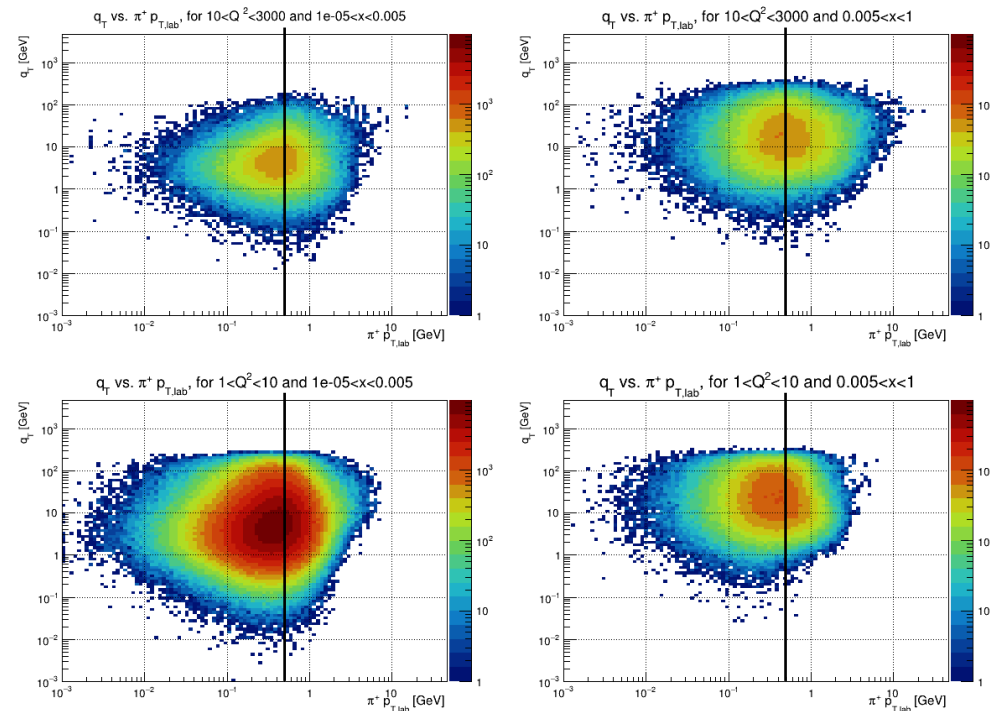
Effects of p_T cuts on q_T

Smearing Disabled

5x41 GeV



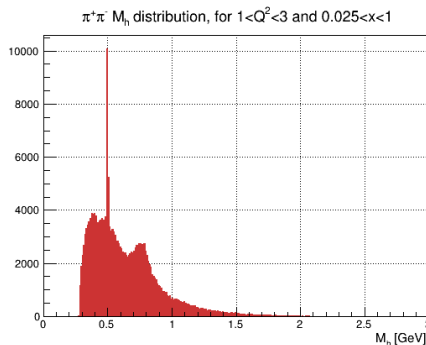
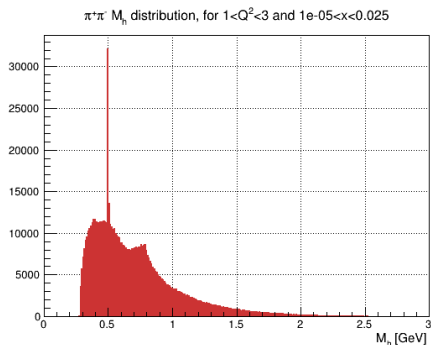
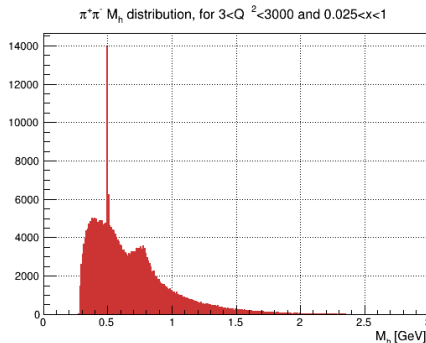
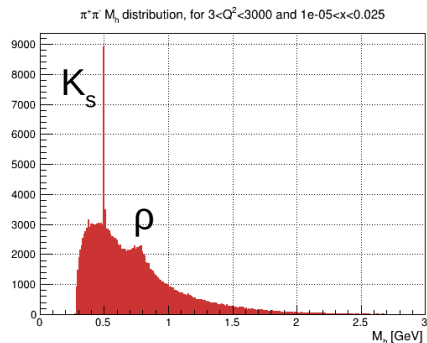
18x275 GeV



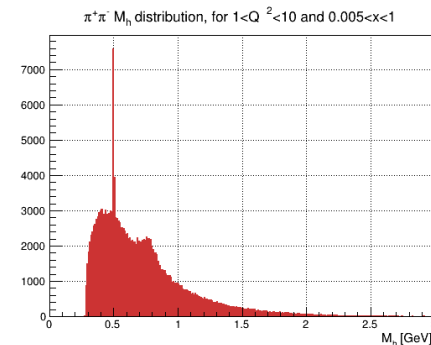
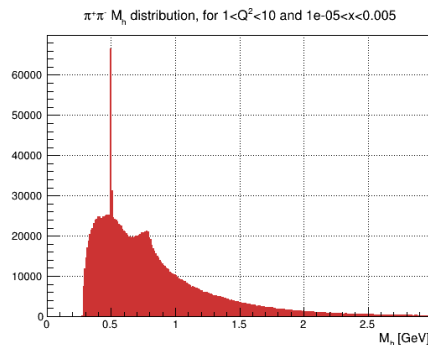
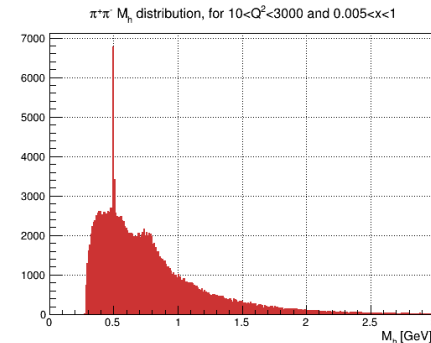
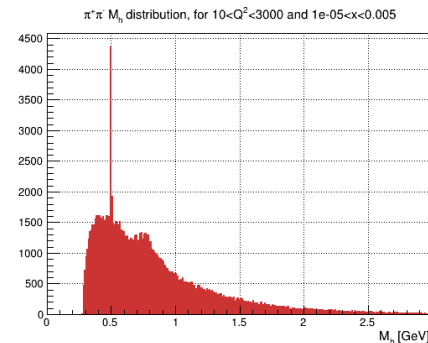
- Plots show q_T vs. p_T of π^+
- Smearing disabled, to show activity beyond acceptance cuts
- Vertical lines $p_T = 500$ MeV
- Higher p_T cuts may have mild impact at low q_T

Dihadron Kinematics: Invariant Mass

5x41 GeV

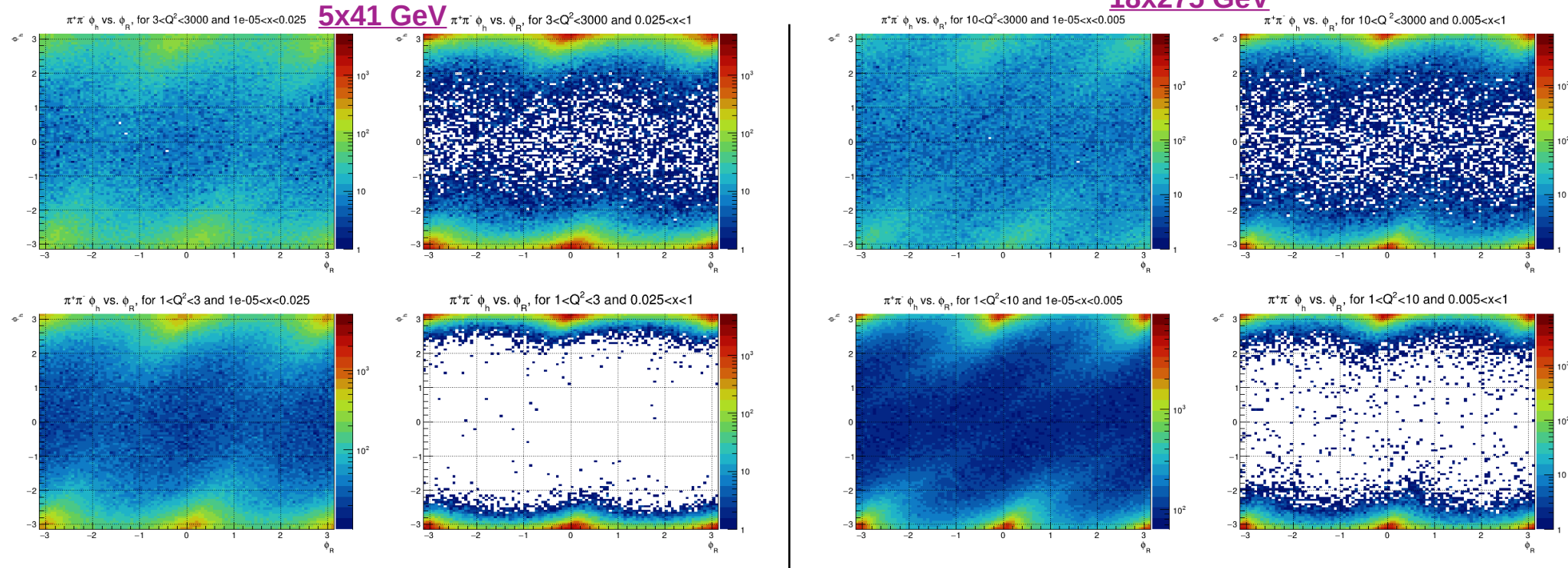


18x275 GeV



- Strong K_S peak seen, not smeared very much
- ρ peak also visible
- Not much dependence on x , Q^2 , or \sqrt{s}

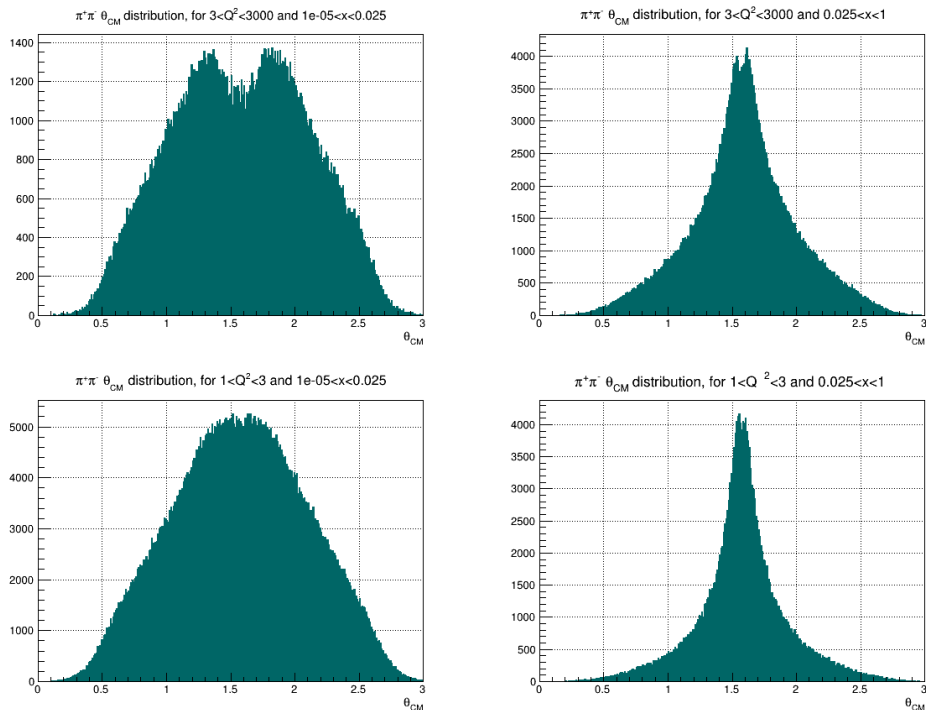
Dihadron Kinematics: Azimuthal correlations ϕ_h vs. ϕ_R



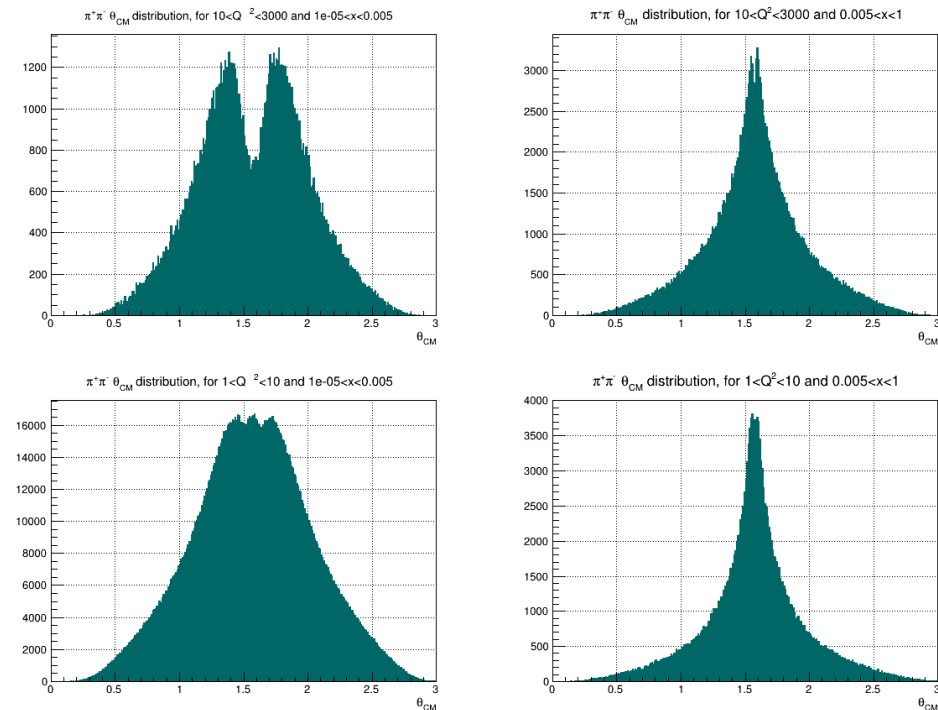
- ϕ_h peaks at $\pm\pi$ indicate a strong tendency of dihadron momentum sum P_h to be in lepton scattering plane, with P_h^\perp opposite of p_e^\perp , where “ \perp ” denotes the plane transverse to q
 - Similar shape seen in ϕ_h of single hadrons
- ϕ_R peaks at $\pm\pi$ and 0 indicate the hadrons also tend to be within the lepton scattering plane
- These shapes are also present in the generated (not smeared) sample

Dihadron Kinematics: CoM Frame Production Angle

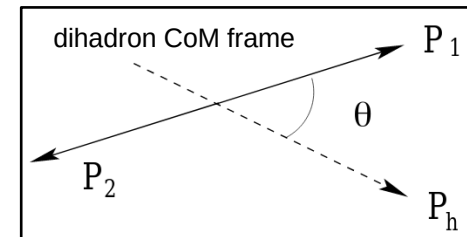
5x41 GeV



18x275 GeV

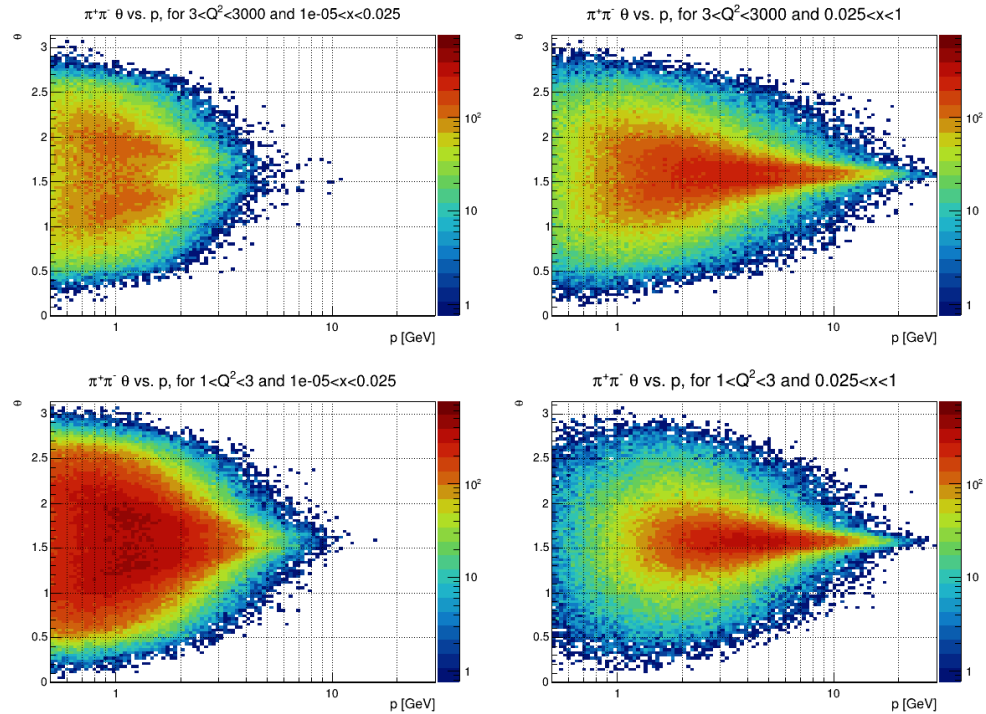


- θ represents the “decay” angle of the hadron pair, in the rest frame of the dihadron
- Dihadron Fragmentation Functions are expanded in partial waves, parameterized by θ
 - Sensitivity to ss, sp, pp interference of dihadroproduction
- Ideal distribution follows a $\sin\theta$ shape
- Double peaking visible at low- x and high Q^2

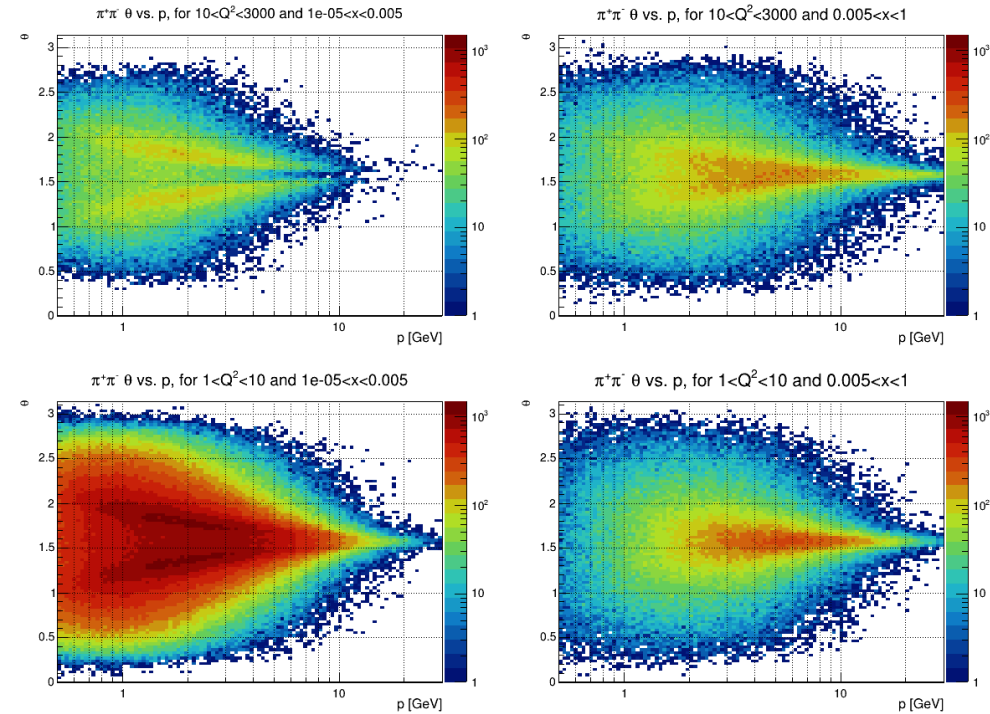


Dihadron Kinematics: θ vs. P_h

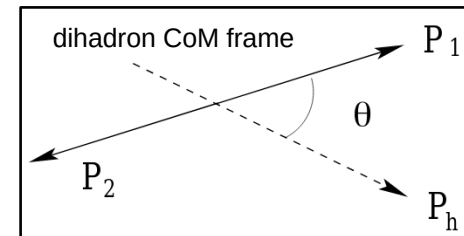
5x41 GeV



18x275 GeV



- Plots show correlation between θ and the hadron momentum sum P_h
- Double peak separation correlates with P_h

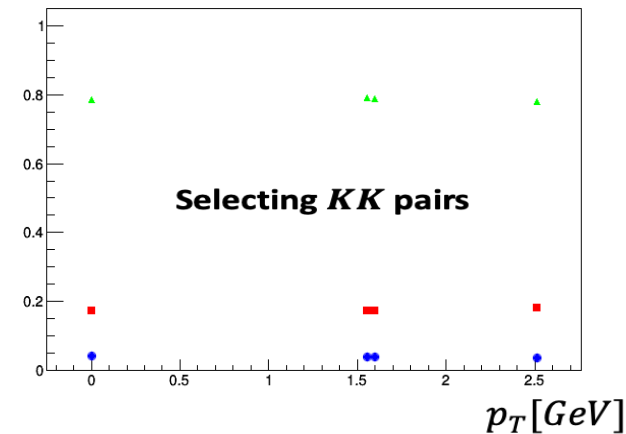
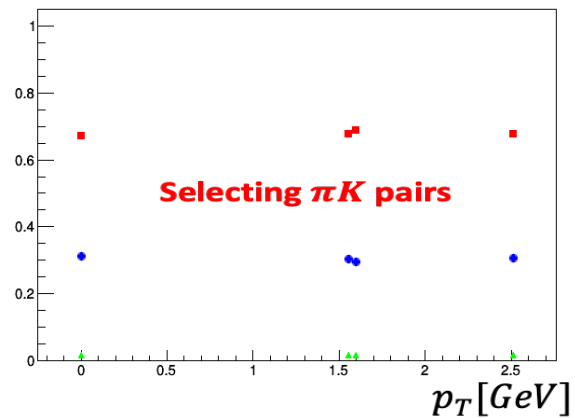
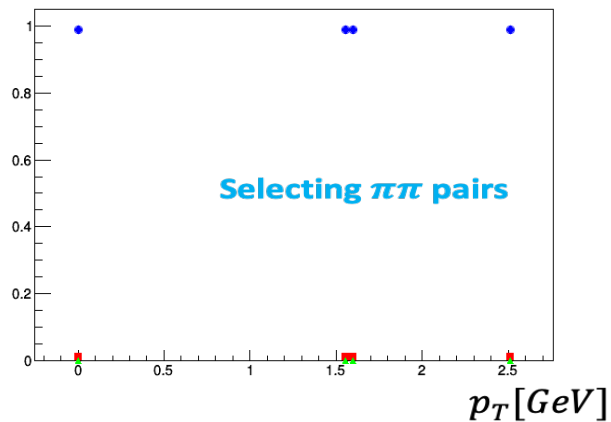


PID Performance

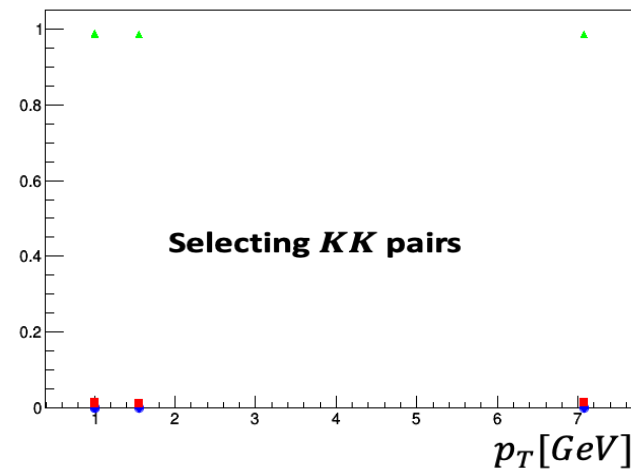
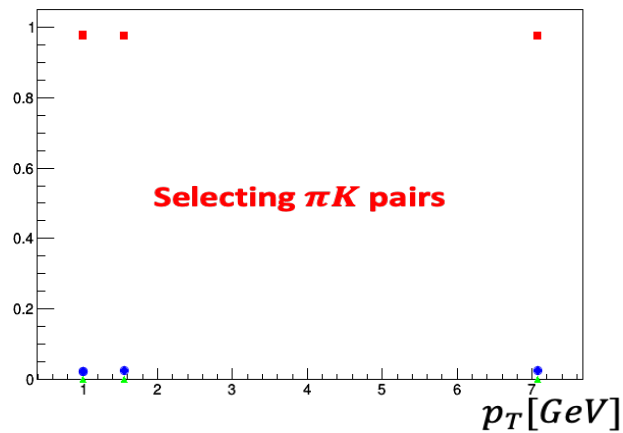
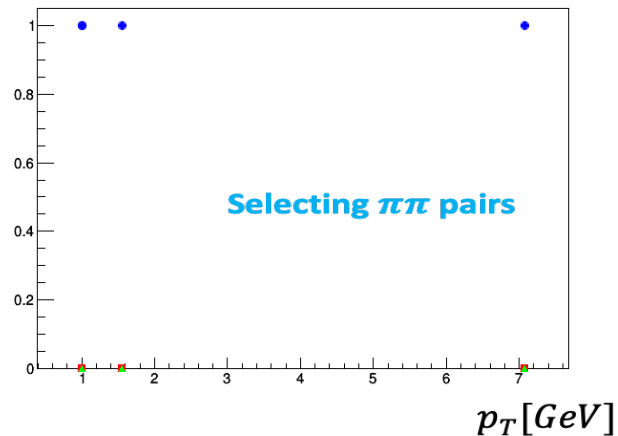
- Fraction of reconstructed $\pi\pi$ pairs
- Fraction of reconstructed πK pairs
- Fraction of reconstructed KK pairs

Study from Anselm

Using 2σ separation:



Using 3σ separation:

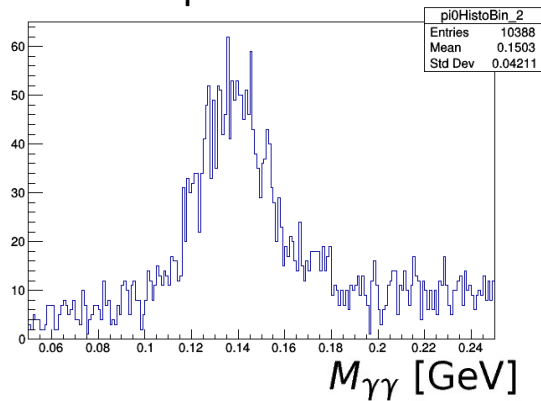


PID Performance

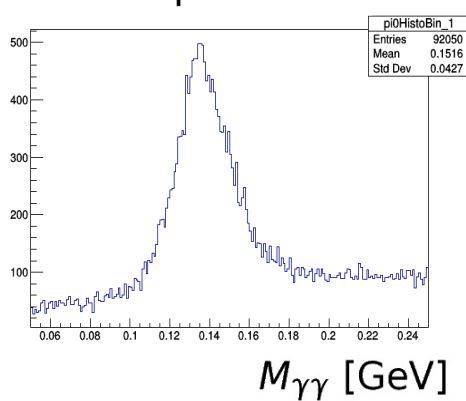
Study from Anselm

π^0 Reconstruction with $E_\gamma > 200$ MeV

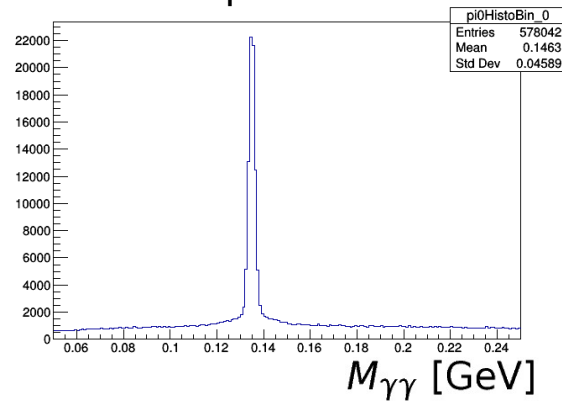
$-4.5 < \eta < -0.5$



$-0.5 < \eta < 1.5$

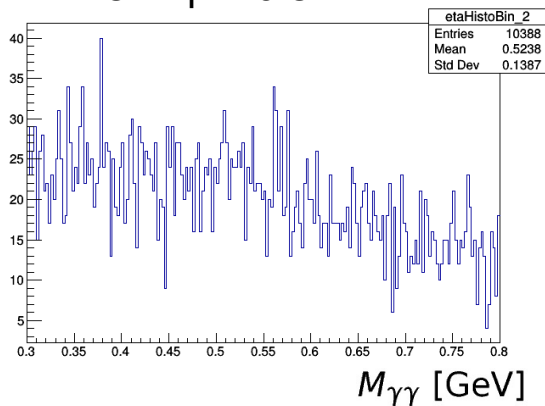


$1.5 < \eta < 4.5$

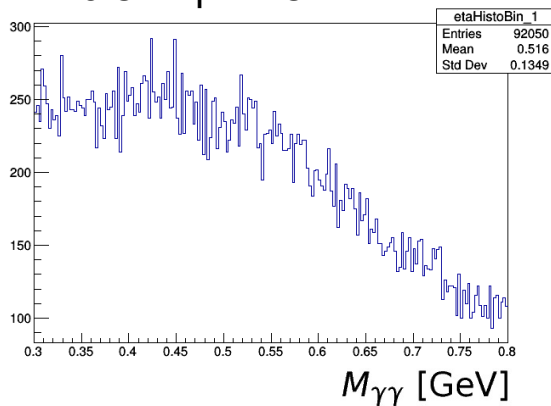


η Reconstruction with $E_\gamma > 200$ MeV

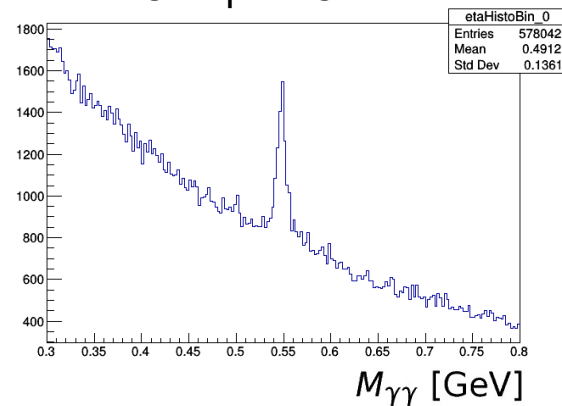
$-4.5 < \eta < -0.5$



$-0.5 < \eta < 1.5$



$1.5 < \eta < 4.5$



Summary and Outlook

- Dihadrons access several aspects of the nucleon:
 - Spin-momentum correlations in hadronization
 - Transverse-momentum dependent PDFs
 - Twist-3 TMD PDFs
- EIC simulation studies are well underway
- Next Steps:
 - Asymmetry projections, including partial wave sensitivity
 - Study other dihadron channels, including kaons