

Axion-like-particles @ Kaon experiments

Stefania Gori
UC Santa Cruz

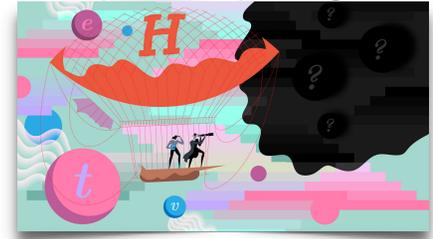


High Energy / Nuclear Theory / RIKEN seminars,
BNL

June 24, 2020

Outline

from symmetry magazine



1. Introduction

2. Kaon experiments: status and prospects

- * Measurement of the very rare $K \rightarrow \pi \nu \nu$ decays
- * KOTO (K_L) anomaly
- * How to address the anomaly

3. Testing ALPs at Kaon experiments

- * New proposed searches for the KOTO and NA62 experiments ($K \rightarrow \pi \gamma \gamma$)
- * Interpretation in terms of ALP simplified models (aGG, aWW)
- * Complementarity with other experiments (highlight: precision pion experiments)

Main references for this seminar

SG, G. Perez, K. Tobioka, 2005.05170

(W. Altmannshofer, SG, D. Robinson, 1909.00005)

Focus:

ALPs with masses
above the MeV scale

High intensity experiments & dark sectors

1. Several **flavor experiments** are coming online/will collect very large datasets in the coming years.
2. Several **fixed target experiments** are proposed for the near future.

All of these facilities can be used to search for light dark sector particles

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Many Standard Model (SM) **flavor violating processes** will be measured for the first time in the coming years:

For example:

$K \rightarrow \pi \nu \nu$ (KOTO and NA62)

$B \rightarrow K^{(*)} \nu \nu$ (Belle-II)

$B_d \rightarrow \mu\mu$ (LHCb)

As we will demonstrate, (some of) these decays can be easily affected by the presence of MeV and above axion-like-particles (ALPs)

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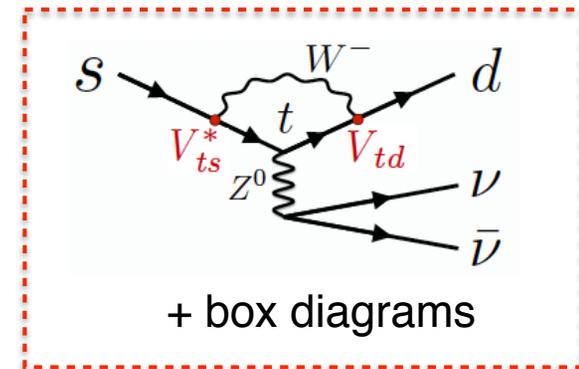
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Kaon rare decays in the SM: $K \rightarrow \pi \nu \nu$

$$\mathcal{H}_{\text{SM}} = g_{\text{SM}}^2 \sum_{\ell=e,\mu,\tau} [V_{cs}^* V_{cd} X(x_c) + V_{ts}^* V_{td} X(x_t)] \underbrace{(\bar{s}_L \gamma_\mu d_L)(\bar{\nu}_\ell \gamma^\mu \nu_\ell)}_{\text{Only operator in the SM}}$$



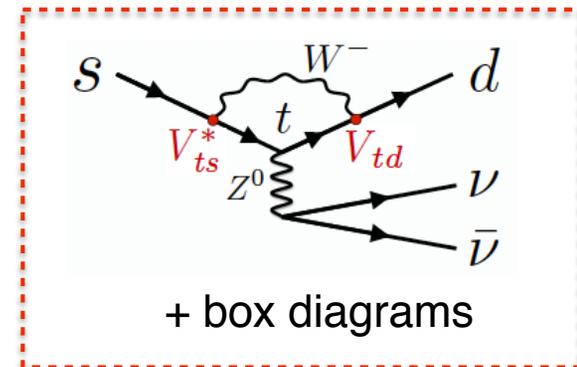
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Very clean decays (mainly short distance contribution)

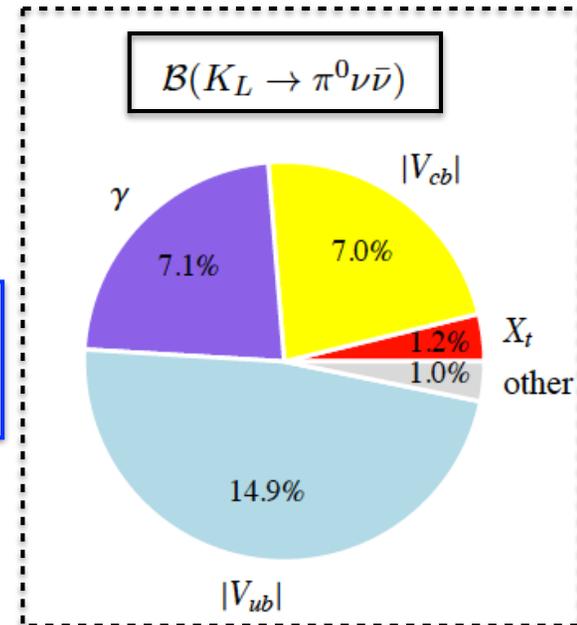
$$\left\{ \begin{array}{l} \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \simeq \kappa_+ \left| \frac{V_{ts}^* V_{td}}{\lambda^5} X(x_t) + \frac{V_{cs}^* V_{cd}}{\lambda} \left(\frac{X(x_c)}{\lambda^4} + \delta P \right) \right|^2 \\ \text{CP-conserving} \\ \mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \simeq \kappa_L \text{Im} \left(\frac{V_{ts}^* V_{td}}{\lambda^5} X(x_t) \right)^2 \\ \text{CP-violating} \end{array} \right.$$

Long-distance contributions



$$\left\{ \begin{array}{l} \text{BR}(K^+ \rightarrow \pi^+ \bar{\nu} \nu) = (9.11 \pm 0.72) \times 10^{-11} \\ \text{BR}(K_L \rightarrow \pi^0 \bar{\nu} \nu) = (3.4 \pm 0.6) \times 10^{-11} \end{array} \right.$$

Very rare!
→ Access to NP



Brod, Gorbahn, Stamou 1009.0947;
Buras, Buttazzo, Girbach-Noe, Kneijens, 1503.02693

The Grossman-Nir (GN) bound

Beyond the Standard model theories can easily induce a New Physics (NP) effect in these very rare Kaon decays.

Generically, the NP effects in the K^+ and in the K_L decay are highly correlated.

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From an EFT perspective:

$$\mathcal{H}_{\text{eff}} = \frac{c_1}{\Lambda^2} (\bar{s}_L \gamma_\mu d_L) (\bar{\nu}_\ell \gamma^\mu \nu_\ell) + \frac{c_2}{\Lambda^2} (\bar{s}_R \gamma_\mu d_R) (\bar{\nu}_\ell \gamma^\mu \nu_\ell)$$

SM operator

$$\mathbf{X} = \frac{\lambda_t}{\lambda^5} \mathbf{X}(x_t) + \frac{\text{Re}(\lambda_c)}{\lambda} P_{c,u} + \frac{1}{\lambda^5} (c_1 + c_2)$$

$$\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \propto F_0 (\text{Im} \mathbf{X})^2$$

$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \propto F_+ |\mathbf{X}|^2$$

because of the isospin symmetry,
the form factors: $F_0 \sim F_+$

Grossman-Nir bound
(model independent):

$$\frac{\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu})}{\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu})} < 4.3$$

[hep-ph/9701313](https://arxiv.org/abs/hep-ph/9701313)

The Grossman-Nir (GN) bound

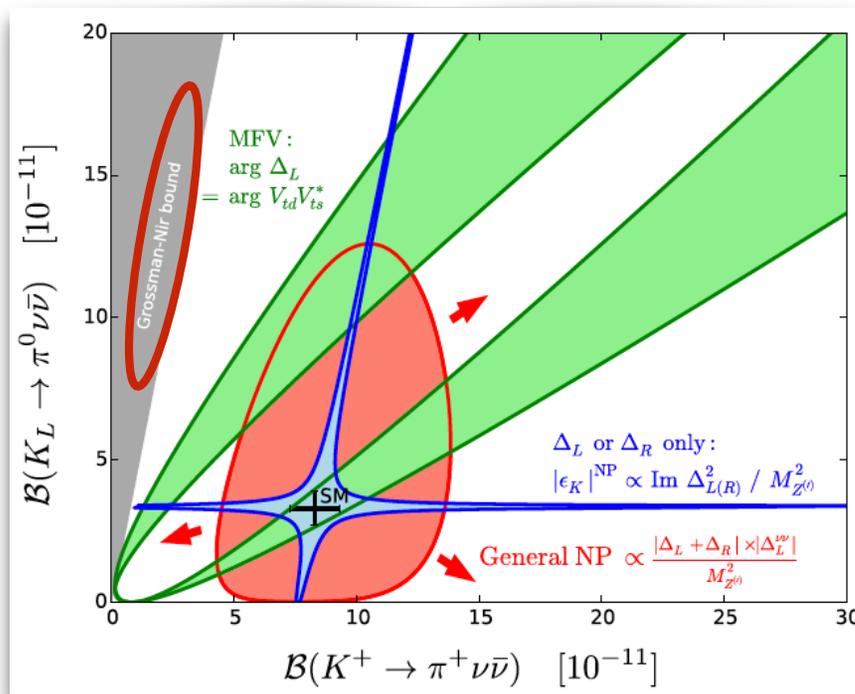
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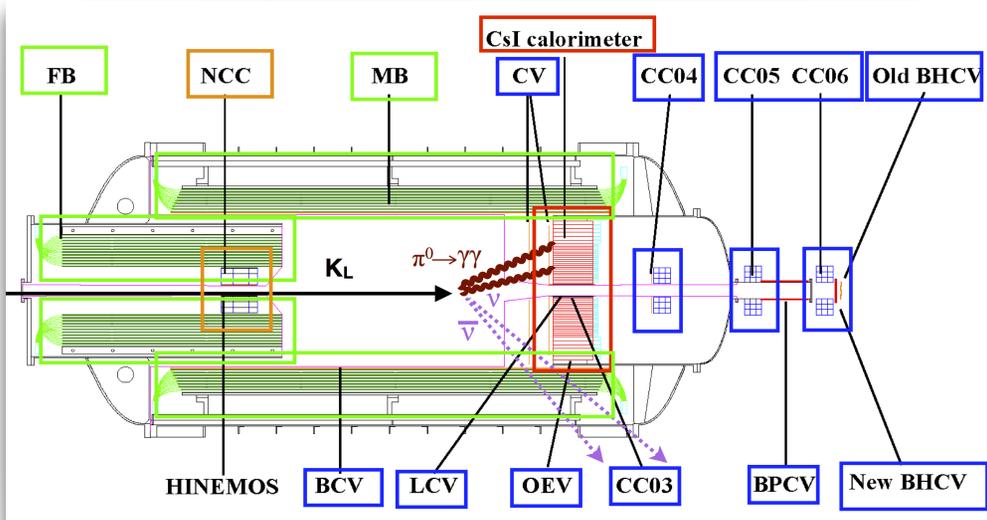
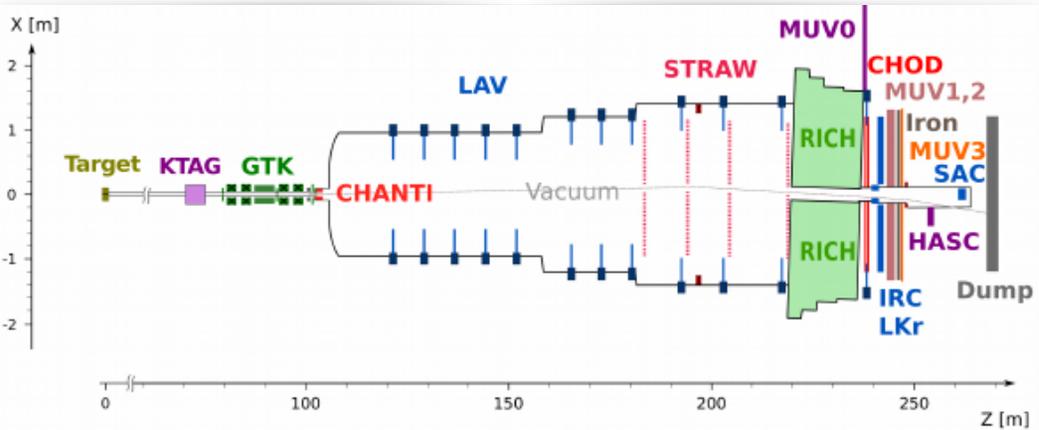
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Brief look: NA62 & KOTO

Only calorimetry, no tracking



NA62

KOTO

future goals

	NA62	KOTO
POT	10^{19} (400 GeV)	10^{21} (30 GeV)
# Kaons	10^{13}	10^{13}
K-Energy	75 GeV	1.5 GeV
Length	300 m	10 m
Decay region	150 m	3-4 m

In comparison,
CHARM
(beam dump experiment):
 $\sim 10^{18}$ POT

Status of the NA62 experiment (K⁺)

* E949 experiment: [0903.0030](#)

$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (17.3_{-10.5}^{+11.5}) \times 10^{-11}$$

* Analysis of the full 2016 data

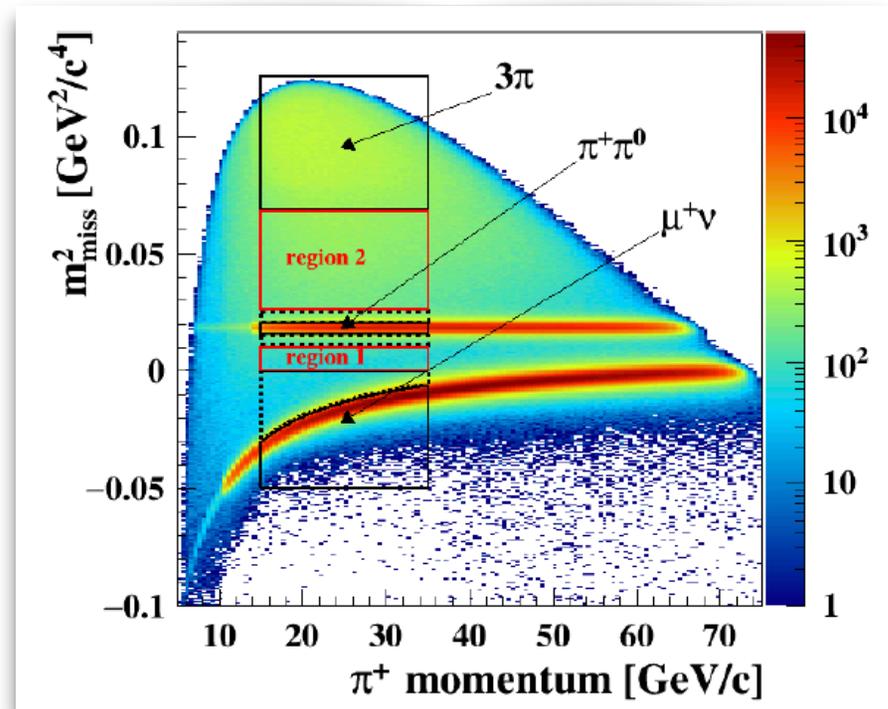
Optimized to suppress backgrounds from leading Kaon decay modes

$$15 < P_{\pi^+} < 35 \text{ GeV}/c$$

$$m_{\text{miss}}^2 = (P_K - P_{\pi^+})^2$$

1 event seen! (0.3 expected)

[Published analysis, 1811.08508](#)



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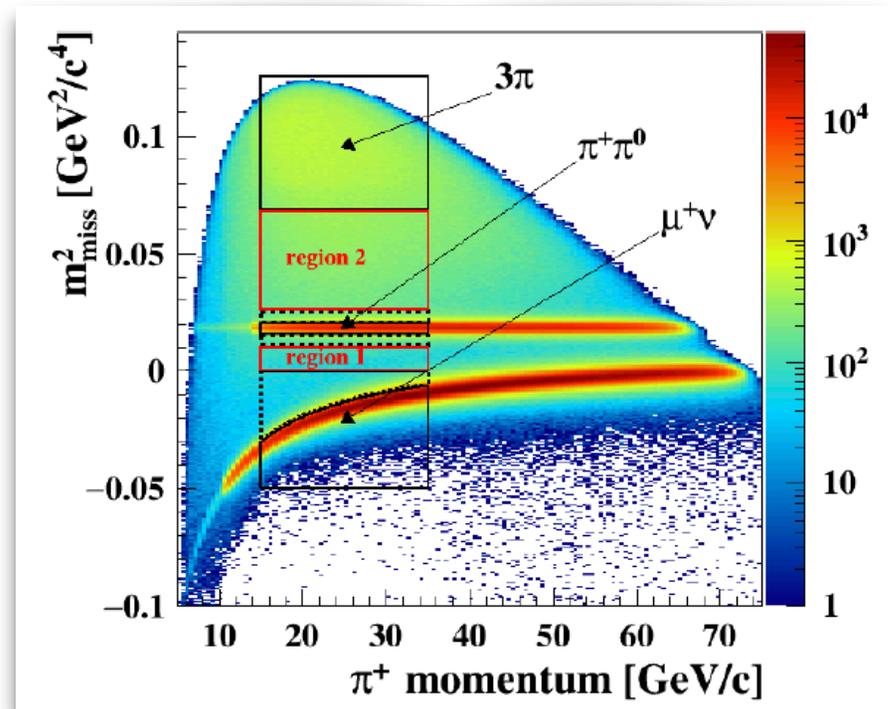
* Analysis of the 2016-2017 data
(preliminary)

3 event observed

$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 1.85 \times 10^{-10} \quad 90\% \text{ C.L.}$$

$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (4.7^{+7.2}_{-4.7}) \times 10^{-11}$$

[see e.g. talk by Volpe, pheno 2020](#)



Final NA62 goal:
measurement of the SM BR
with ~10% uncertainty

Status of the KOTO experiment (K_L)

Experimental challenges associated to the signature (2 photons+nothing)

* Initial physics data taken in 2013

$$\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 5.1 \times 10^{-8}$$

(1609.03637)

* 2015 run: ~ 20 times more data

$$\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9}$$

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* Indirect bound:

(using Grossman-Nir)

$$\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{GN}} < 7.96 \times 10^{-10}$$

Final KOTO goal (~100 times more data)
measurement of/evidence for
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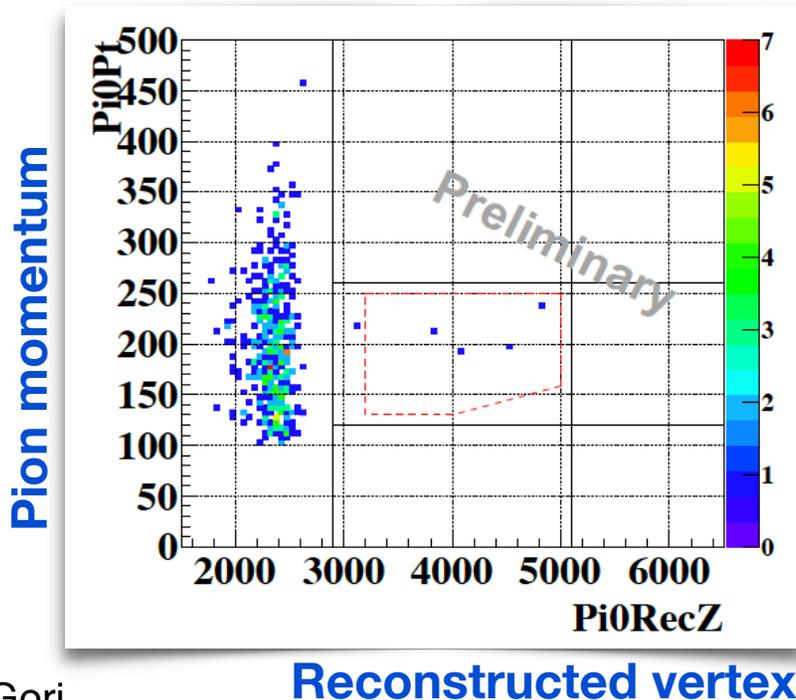
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- * 2016-2018 run: ~ 50% more data

- * Indirect bound:
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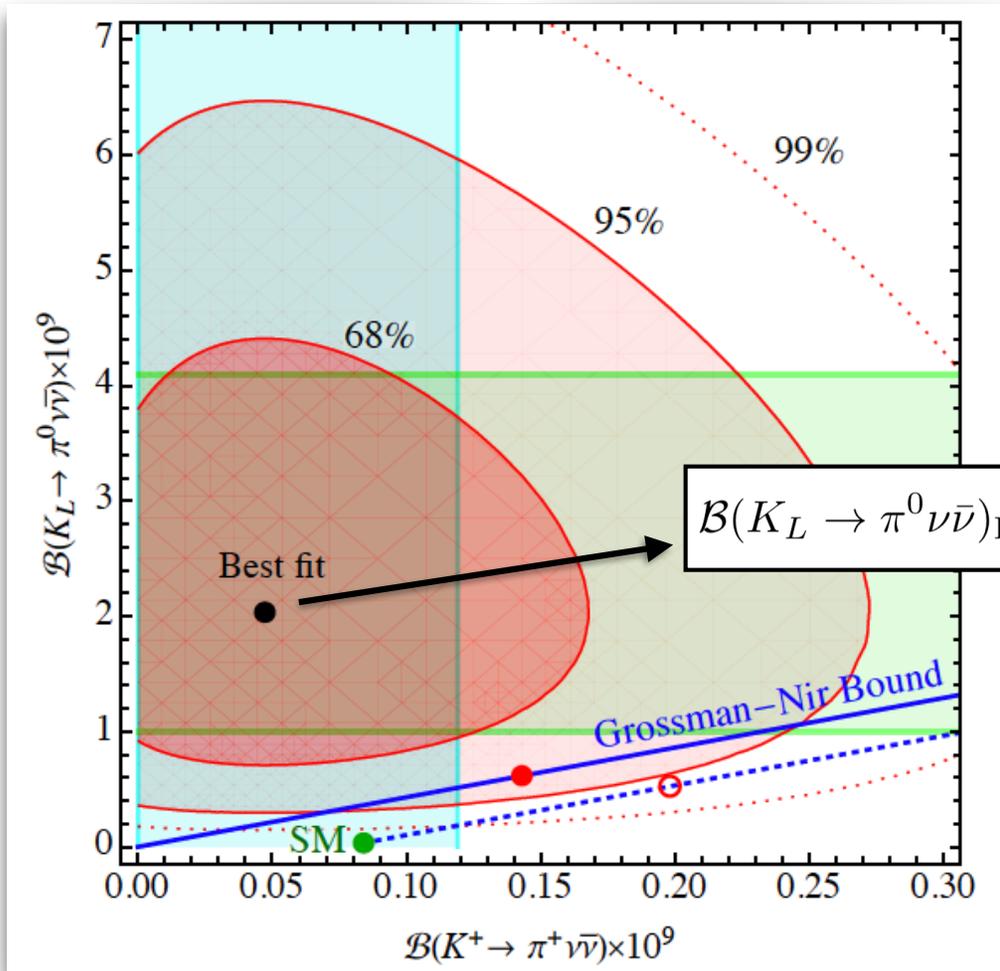
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4-events in the signal region!
Expected number of events: 0.05 ± 0.02

Final KOTO goal (~100 times more data)
 measurement of/evidence for
 the SM BR with ~?% uncertainty
 $\text{BR}(K_L \rightarrow \pi^0 \bar{\nu} \nu) = (3.4 \pm 0.6) \times 10^{-11}$

Compatibility NA62/KOTO?



$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{KOTO}} = 2.1_{-1.1}^{+2.0 (+4.1)} \times 10^{-9}$$

(theory interpretation)

- ~ 2σ tension (interference with the SM)
- ~ 3σ tension (no interference with the SM)

Kitahara et al., 1909.11111

Class of models addressing the anomaly

* Heavy New Physics described by a EFT framework



* Light New Physics (X) that satisfies the GN bound:



- X is “long-lived enough” for KOTO, but not for NA62

$K \rightarrow \pi$ (X \rightarrow invisible) for KOTO, but NOT for NA62

Preferred lifetime: $O(0.1-0.01)\text{ns}$

- X has a mass in (100-160) MeV (close to the pion mass)

NA62 has large $K^+ \rightarrow \pi^+ \pi^0$ in this region. (Fuyuto et al, 1412.4397)

(based on the observation that NA62 is effectively larger than KOTO:

$$L_{\text{NA62}}/p_{\text{NA62}} > L_{\text{KOTO}}/p_{\text{KOTO}})$$

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* Light New Physics (X) that breaks the GN bound: (see next slide)

* Exotics:

e.g. New particle, ϕ , produced at the target and that decays $\phi \rightarrow \gamma\gamma$ inside the KOTO fiducial

An incomplete list of pheno interpretations:

Kitahara et al. 1909.11111; Egana-Ugrinovic et al. 1911.10203; Dev et al. 1911.12334

Jho et al. 2001.06572; Liu et al. 2001.06522; He et al. 2002.05467; Ziegler et al. 2005.00451 Liao et al.

2005.00753; Hostert et al. 2005.07102; Datta et al. 2005.08920; Altmannshofer et al. 2006.05064

(Strongly) Breaking the GN bound

One can avoid the Grossman-Nir bound in models with **only neutral New Physics particles**.

Based on an idea by M. Pospelov

Let us suppose to have a new decay:

$$K_L \rightarrow \sigma\chi, \quad \chi = \text{Im}(\phi), \quad \sigma = \text{Re}(\phi)$$

This would dominate the 3-body final states of the charged Kaon:

$$K^+ \rightarrow \pi^+\chi\chi, \quad K^+ \rightarrow \pi^+\sigma\sigma$$

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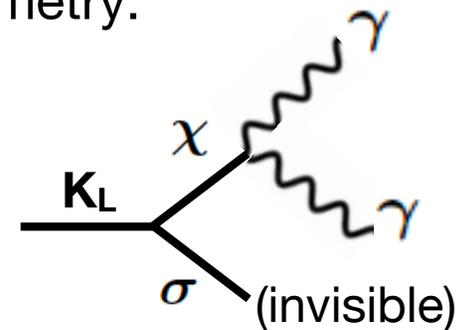
This would dominate the 3-body final states of the charged Kaon:

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A working model based on an approximate strange flavor symmetry:

$$\left\{ \begin{array}{l} y_1 H \bar{Q}_1 s \phi^2 / \Lambda^2 \text{ and/or } y_2 H \bar{Q}_2 d \phi^2 / \Lambda^2 + h.c. \\ \mathcal{L}_\chi \supset \frac{\chi}{\Lambda_\chi} F_{\mu\nu} \tilde{F}^{\mu\nu} \end{array} \right.$$

SG, Perez, Tobioka,
2005.05170



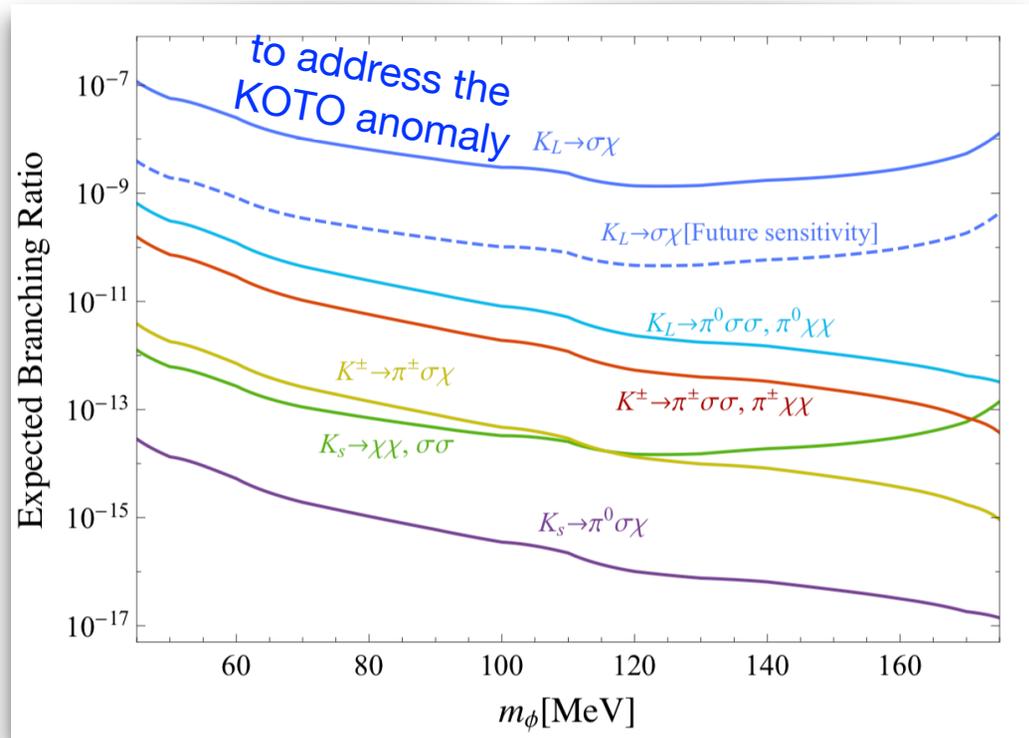
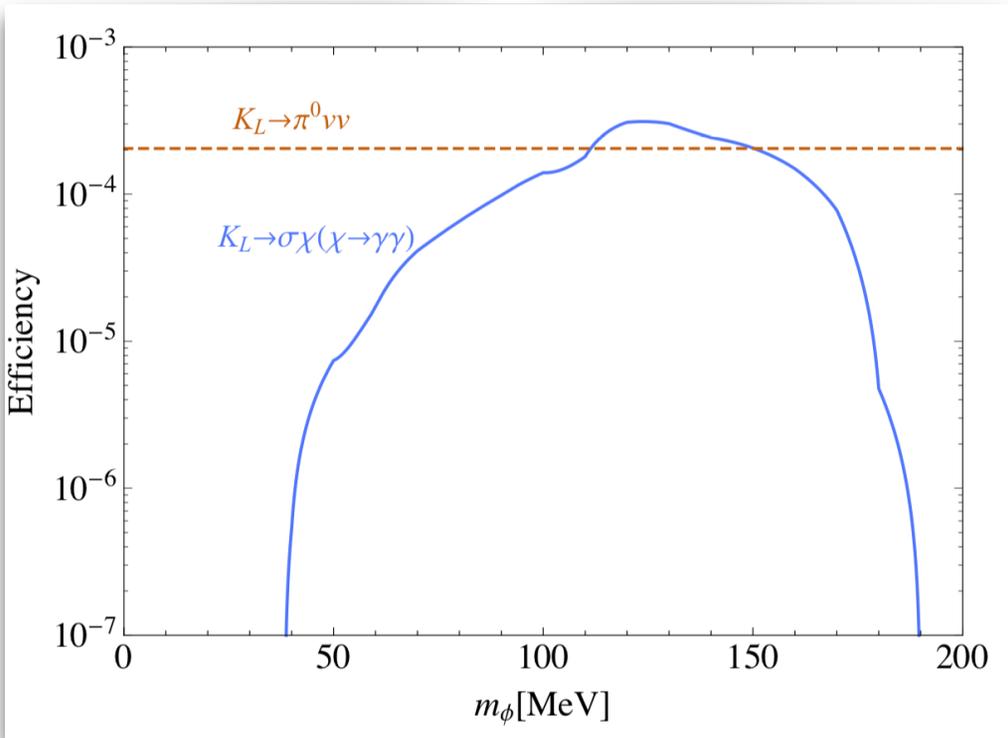
$$\Gamma(K_L \rightarrow \chi\sigma) \sim M_K \left| \frac{y_{1,2} v}{\Lambda^2} \right|^2 \times F_\pi^2$$

Depending on the ϕ mass,
this decay can
fall into the KOTO signal region

Predictions for Kaon experiments

$$\frac{v}{\Lambda_{\text{GNV}}^2} \phi^2 \frac{F_\pi^2 B_0}{2} \text{Tr}[y_1 \lambda_{sd} \Sigma] + \frac{v}{\Lambda_{\text{GNV}}^2} \phi^2 \frac{F_\pi^2 B_0}{2} \text{Tr}[y_2 \lambda_{sd}^\dagger \Sigma] + h.c.$$

$$\Sigma \equiv \exp[2i\Pi/F_\pi] \quad \Pi \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -2\frac{\eta_8}{\sqrt{6}} \end{pmatrix}, \quad \lambda_{sd} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix}$$



Other New Physics searches we can do at these two Kaon experiments?

$K \rightarrow \pi X$ with a visible X



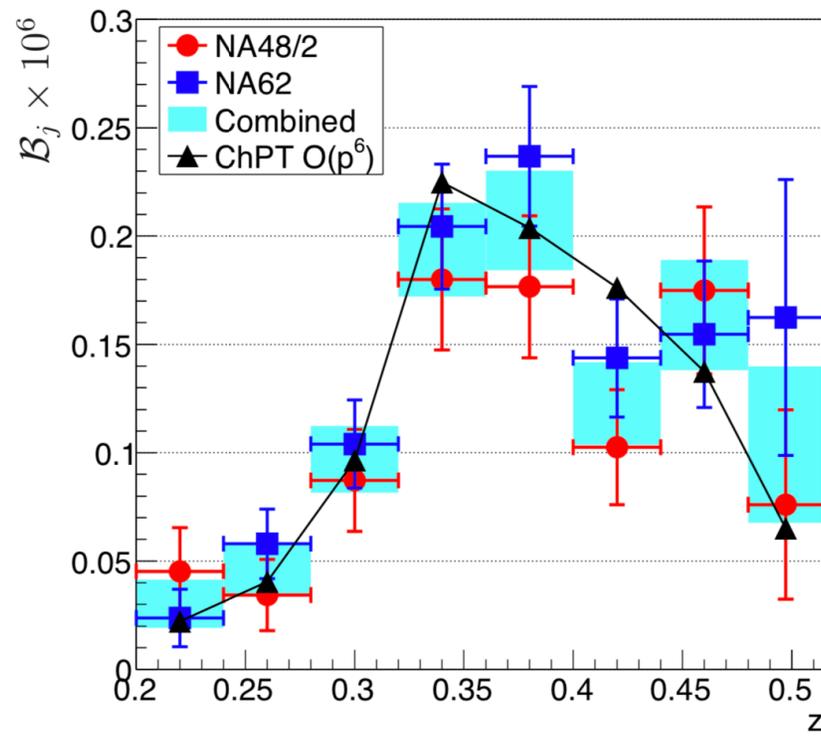
$K \rightarrow \pi \gamma \gamma$ (charged mode)

$K^+ \rightarrow \pi^+ \gamma \gamma$ has been searched for at:

* **E949** with the requirements ([hep-ex/0505069](https://arxiv.org/abs/hep-ex/0505069))

- Photons originate within 80 cm of the stopped Kaon
- $p_{\pi^+} > 213$ MeV

* at the **NA62/48** experiment ([1402.4334](https://arxiv.org/abs/1402.4334))



$\sim 10^9$ K^+ in the fiducial region

NA62 did not perform the search (yet).
In the following, we will rescale the NA48/62 bound with \sqrt{L} considering a downscaling trigger factor of 400.

$$220 \text{ MeV} \lesssim m_{\gamma\gamma} \lesssim 350 \text{ MeV}$$

$$z = (m_{\gamma\gamma}/m_K)^2$$

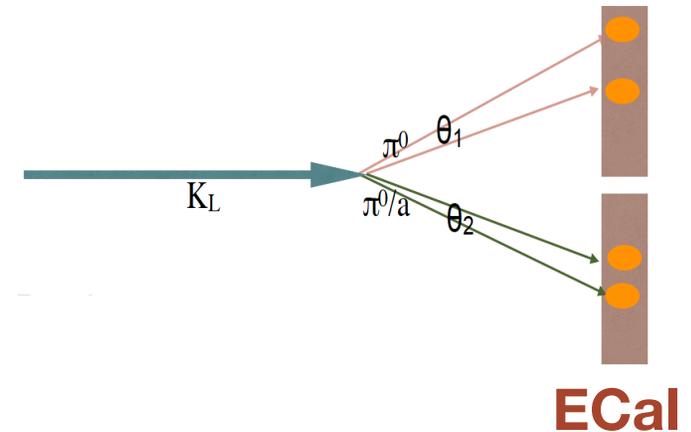
$K \rightarrow \pi \gamma \gamma$ (neutral mode)

$$K_L \rightarrow \pi^0 a \rightarrow 4\gamma$$

Our new proposed search

Challenges of the search:

- the decay point is unknown (only ECal, no tracker)
- combinatorics of $\gamma\gamma$ pairs



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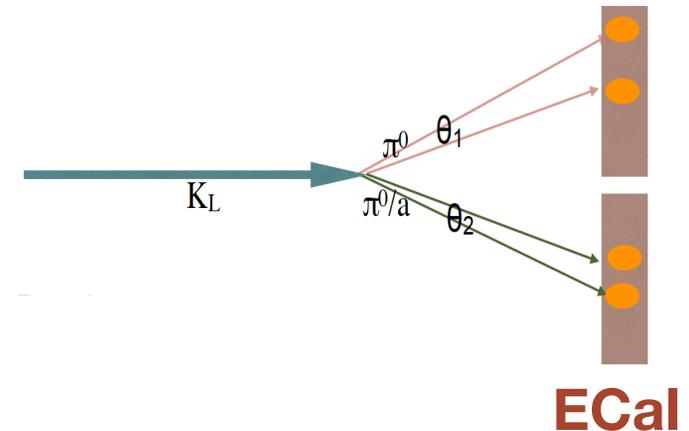
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Main ingredients :

1. We derive the K_L decay vertex location of the 6 possible di-photon pair combinations, assuming

$$m_{\gamma_i \gamma_j}^2 = m_{\pi^0}^2$$

2. Require $m_{4\gamma} \simeq m_{K_L}$ to find a correct pair



Importance of a good vertex resolution! ($\sim 5\text{cm}$) and small energy smearing ($\sim 2\%$)

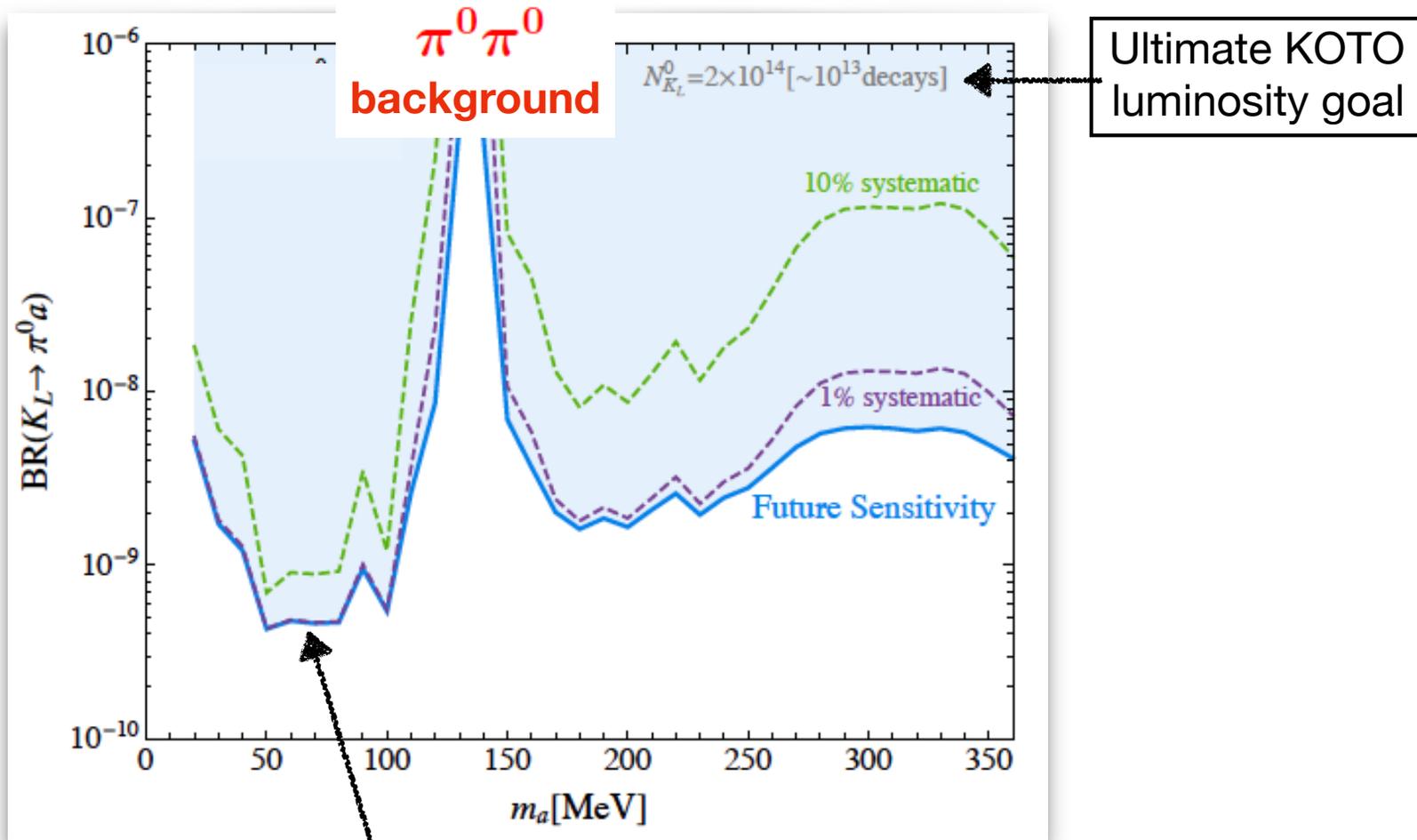
We simulate the **main sources of background**:

$$K_L \rightarrow \pi^0 \pi^0, \quad K_L \rightarrow \pi^0 \gamma \gamma$$

mainly for $m_a \sim m_{\text{pion}}$

The KOTO reach

$$K_L \rightarrow \pi^0 a \rightarrow 4\gamma$$

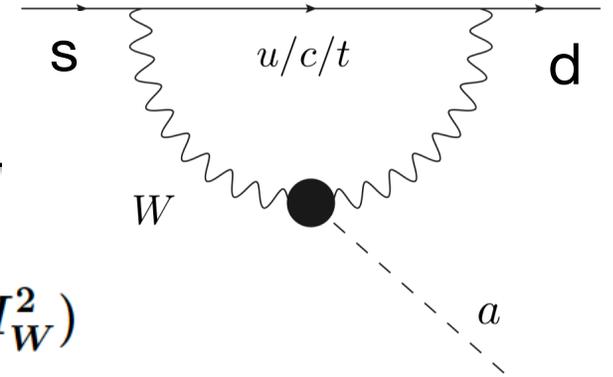


Interpretation in terms of New Physics models

1. $\frac{g_{aW}}{4} a W_{\mu\nu}^a \tilde{W}^{a\mu\nu}$ (SU(2) gauge bosons)
2. $\frac{\alpha_s}{8\pi F_a} a G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$ (gluons)

1. WW coupled ALP simplified model

$$\frac{g_{aW}}{4} a W_{\mu\nu}^a \tilde{W}^{a\mu\nu}$$



$$g_{ads} \equiv -\frac{3\sqrt{2}G_F M_W^2 g_{aW}}{16\pi^2} \sum_{\alpha \in c,t} V_{\alpha d} V_{\alpha s}^* f(M_\alpha^2/M_W^2)$$

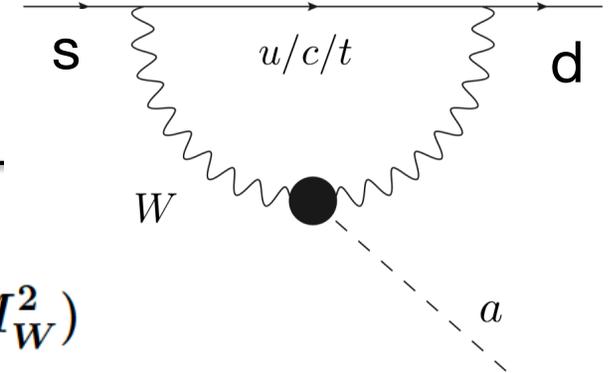
$$\Gamma(K_L \rightarrow \pi^0 a) = \frac{M_{K_L}^3}{64\pi} \left(1 - \frac{M_{\pi^0}^2}{M_{K_L}^2}\right)^2 \text{Im}(g_{asd})^2 \lambda_{\pi^0 a}^{1/2}$$

This coupling will induce the decay of the ALP into two photons:

$$\frac{g_{a\gamma}}{4} a F_{\mu\nu} \tilde{F}^{\mu\nu}, \quad g_{a\gamma} = g_{aW} \sin^2 \theta$$

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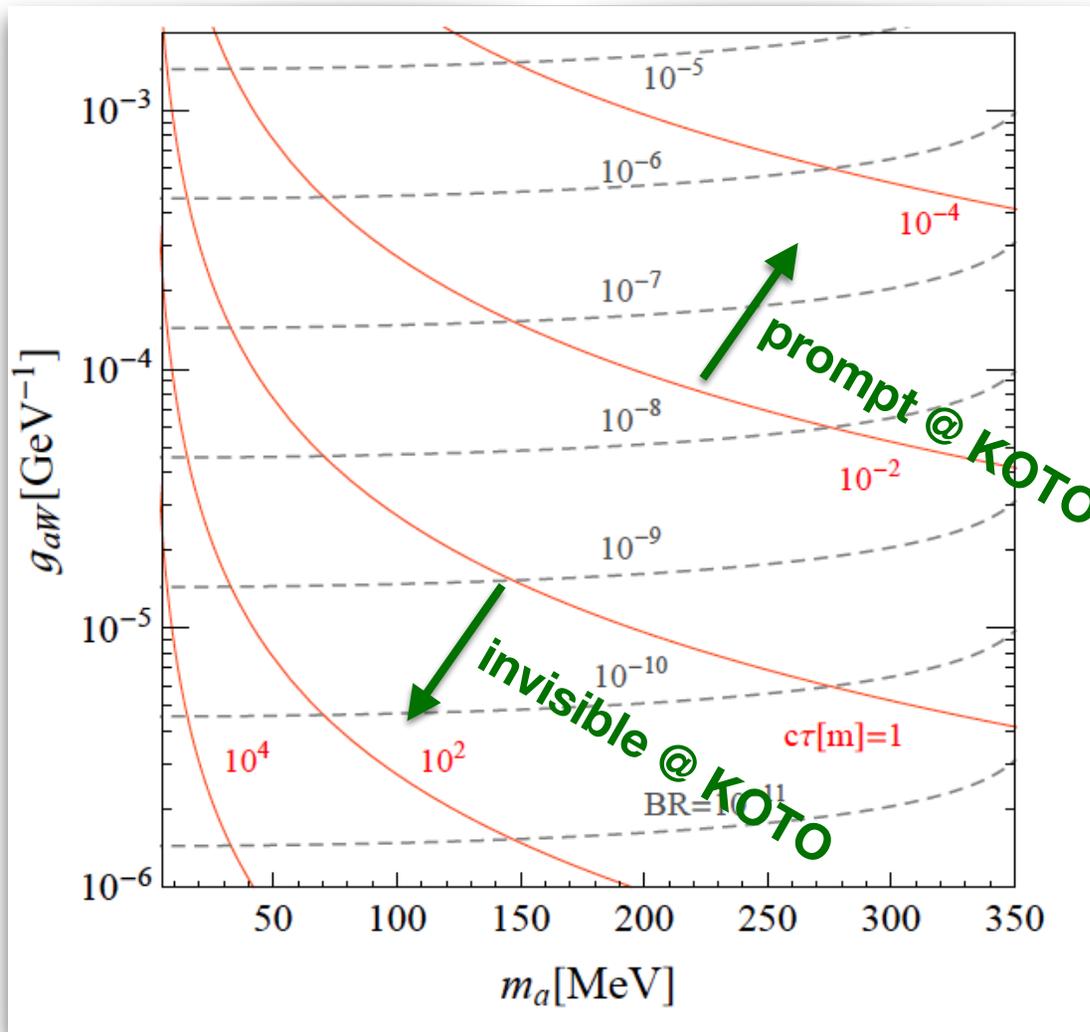
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According to the Grossman-Nir bound, we expect an effect also in the K^+ decay. Indeed:

$$\Gamma(K^+ \rightarrow \pi^+ a) = \frac{M_{K^+}^3}{64\pi} \left(1 - \frac{M_{\pi^+}^2}{M_{K^+}^2}\right)^2 |g_{asd}|^2 \lambda_{\pi^+ a}^{1/2}$$

WW coupled ALP pheno

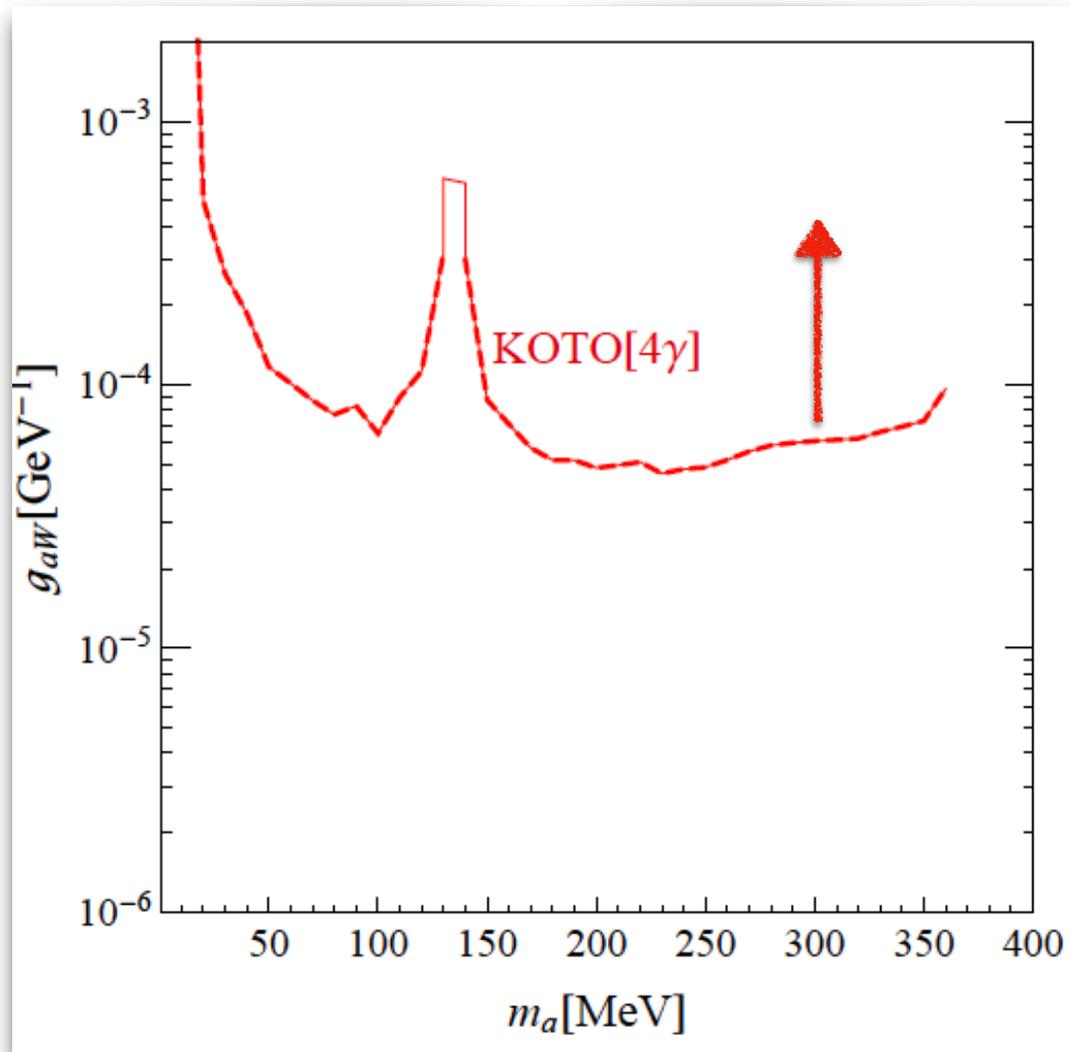


ALP lifetime (in meters)

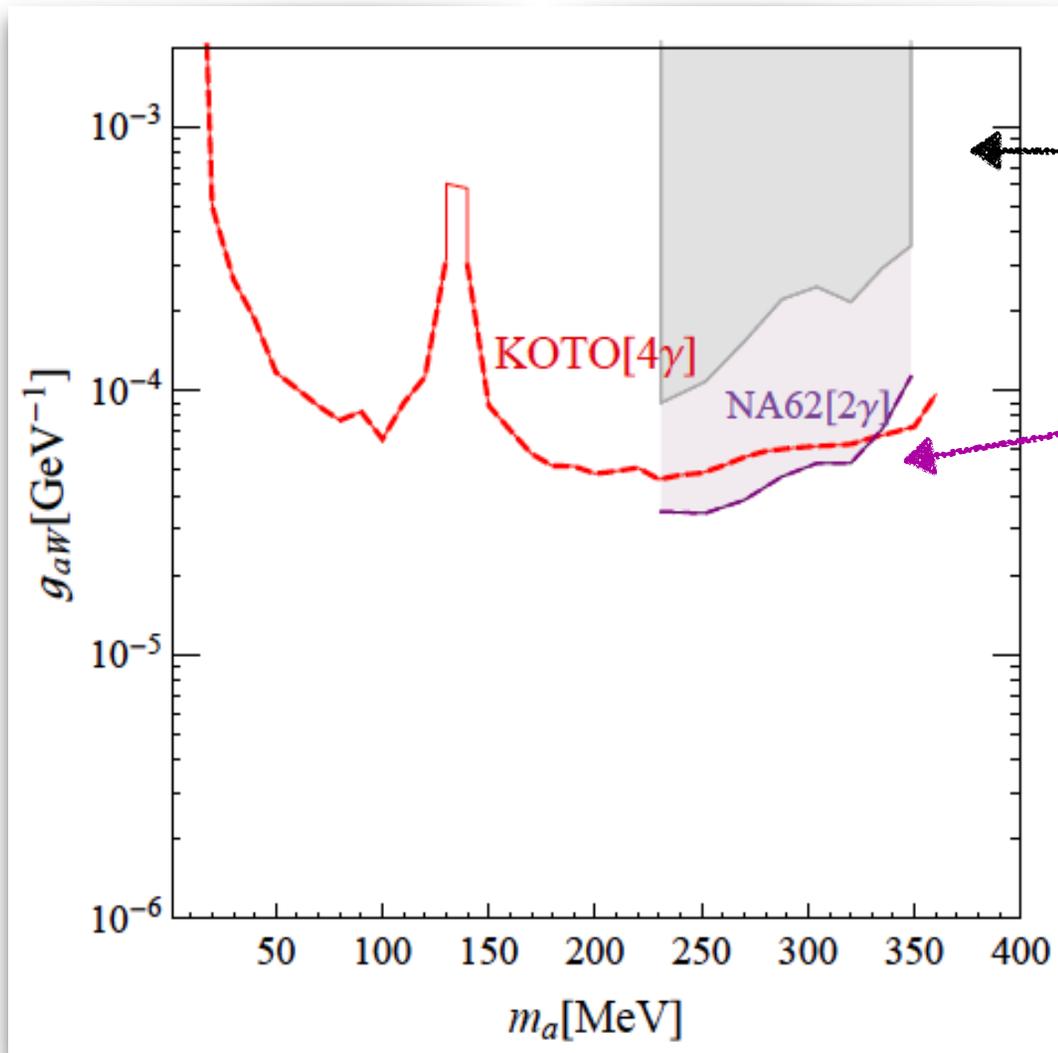
$\text{BR}(K_L \rightarrow \pi a)$

$$\text{BR}(K^+ \rightarrow \pi^+ a) \sim 1.8 \text{ BR}(K_L \rightarrow \pi a)$$

$aW\tilde{W}$ at KOTO



$aW\tilde{W}$ at KOTO and NA62 (visible)



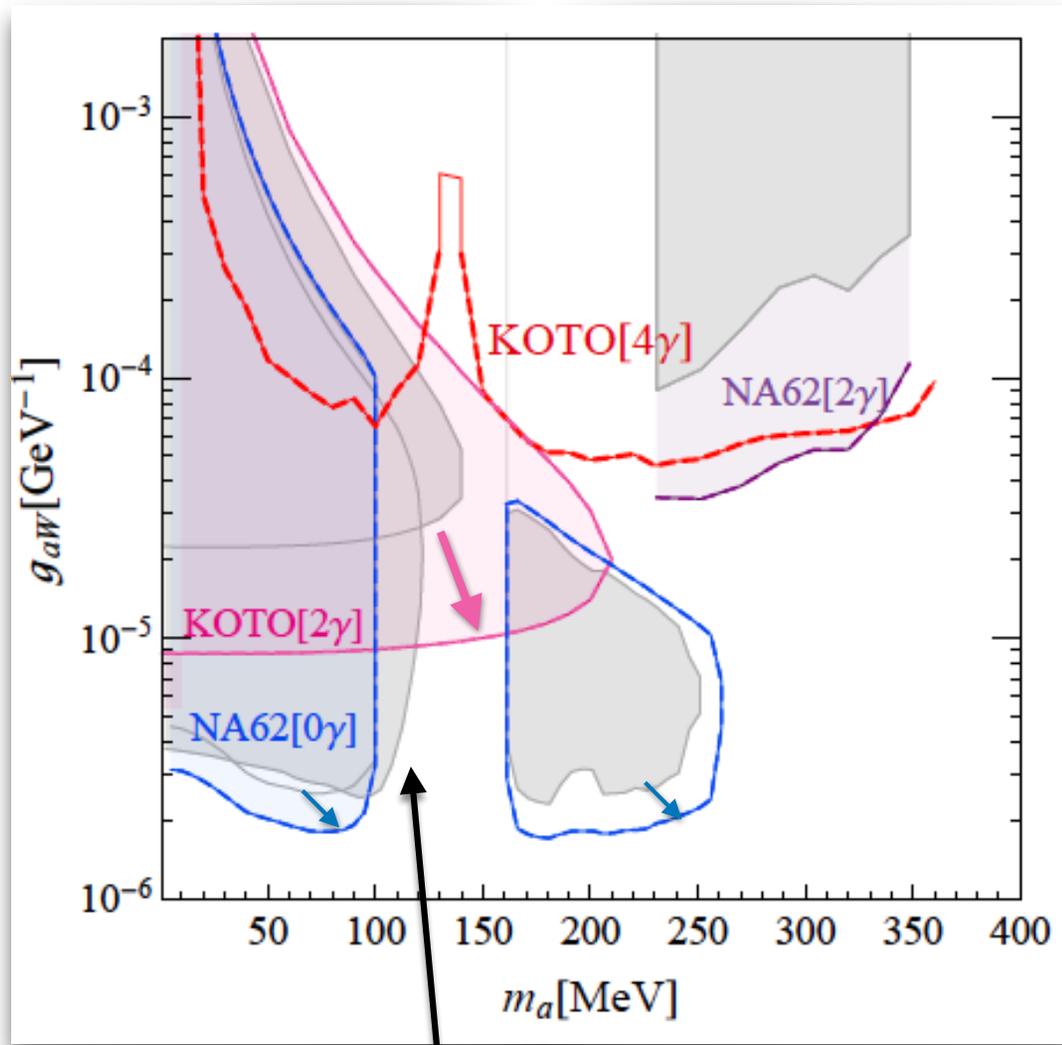
NA48/62 search for

$$K^+ \rightarrow \pi^+ a, a \rightarrow \gamma\gamma$$

Izaguirre, Lin, Shuve, 1611.09355

projection with
the full NA62 luminosity

$aW\tilde{W}$ at KOTO and NA62



E949 invisible

Longer life-time

Both **NA62** and **KOTO**
can search for
 $K \rightarrow \pi + \text{invisible}$

(the ALP is long lived
enough to decay after
the detector)

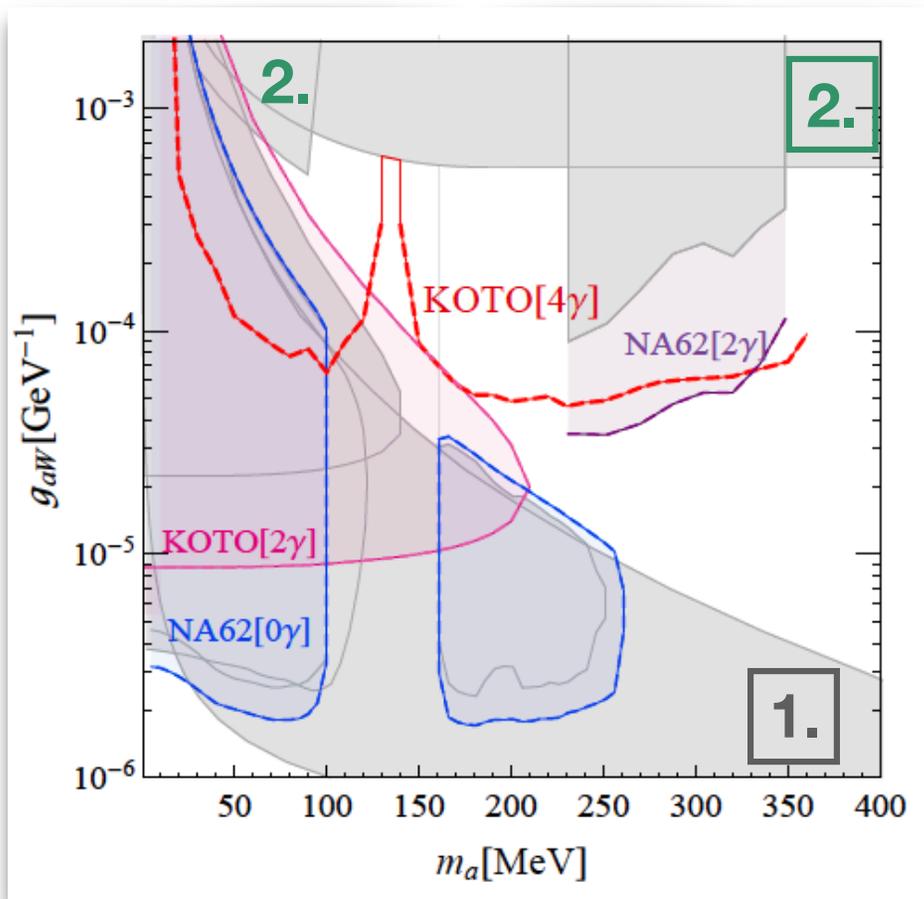
Complementarity with other experiments

This specific model ($aW\tilde{W}$) also predicts a coupling of the ALP with photons

 Several other experiments can probe the parameter space

Complementarity with other experiments

This specific model ($aW\tilde{W}$) also predicts a coupling of the ALP with photons
➔ Several other experiments can probe the parameter space



1. Beam dump experiments
2. LEP ($e^+e^- \rightarrow \gamma a$ or $Z \rightarrow \gamma a \rightarrow \gamma\gamma(\gamma)$)
+ CDF ($Z \rightarrow \gamma a \rightarrow \gamma\gamma$)

Additional opportunities at B-factories?
(Belle-II) [Izaguirre, Lin, Shuve, 1611.09355](#)

Note, however, that NA62 and KOTO will have **~ 3 orders of magnitude more** Kaons than the number of B-mesons at Belle-II!

2. GG coupled ALP simplified model

$$\frac{\alpha_s}{8\pi F_a} a G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

$$\mathcal{L}_{eff} = \frac{iF_\pi^2}{4} \frac{\partial_\mu a}{F_a} \text{Tr}[\tilde{\kappa}_q (\Sigma^\dagger D^\mu \Sigma - \Sigma D^\mu \Sigma^\dagger)] + \frac{F_\pi^2}{2} B_0 \text{Tr}[\Sigma \mathbf{m}^\dagger + \mathbf{m}^\dagger \Sigma^\dagger]$$

Kinetic mixing

Mass mixing

$$\mathbf{m} = \exp\left(i\kappa_q \frac{a}{2F_a} \gamma_5\right) \cdot m_q \cdot \exp\left(i\kappa_q \frac{a}{2F_a} \gamma_5\right) \quad \tilde{\kappa}_q = \text{diag}(\kappa_q), \quad \kappa_q = \frac{1}{m_q} / \sum_{q'} \left(\frac{1}{m_{q'}}\right)$$

$$\left\{ \begin{array}{l} \theta_{\pi a} \simeq \frac{F_\pi}{2F_a} (\kappa_u - \kappa_d) \frac{m_a^2}{m_a^2 - m_{\pi^0}^2} \quad \text{Kinetic mixing with the pion of the SM} \\ \theta_{\eta a} \simeq \frac{F_\pi \sqrt{2} m_a^2 [\kappa_u + \kappa_d - 2\kappa_s] \cos \theta_{\eta\eta'} - 2 (m_a^2 [\kappa_u + \kappa_d + \kappa_s] - 6\Delta m_{\pi^0}^2) \sin \theta_{\eta\eta'}}{2\sqrt{6} (m_a^2 - m_\eta^2)} \end{array} \right.$$

Kinetic mixing and mass mixing with the eta of the SM

(mass mixing is due to the eta-eta' mixing, $\theta_{\eta\eta'}$)

Theory prediction for $K \rightarrow \pi a$

The ALP-pion and ALP-eta mixing will induce

- * an effective K - π -ALP coupling ($K \rightarrow a\pi$)
- * a ALP coupling to photons ($a \rightarrow \gamma\gamma$)

Theory prediction for $K \rightarrow \pi a$

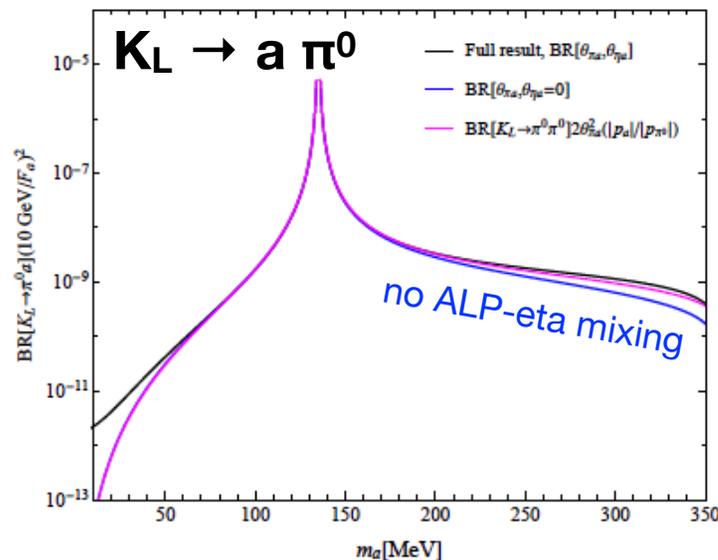
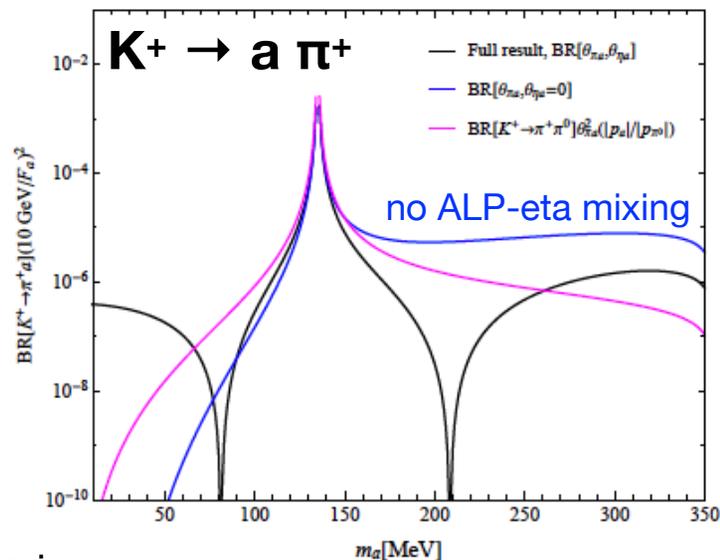
The ALP-pion and ALP-eta mixing will induce

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At low energy, the two operators responsible for $\Delta S = 1$ transitions are

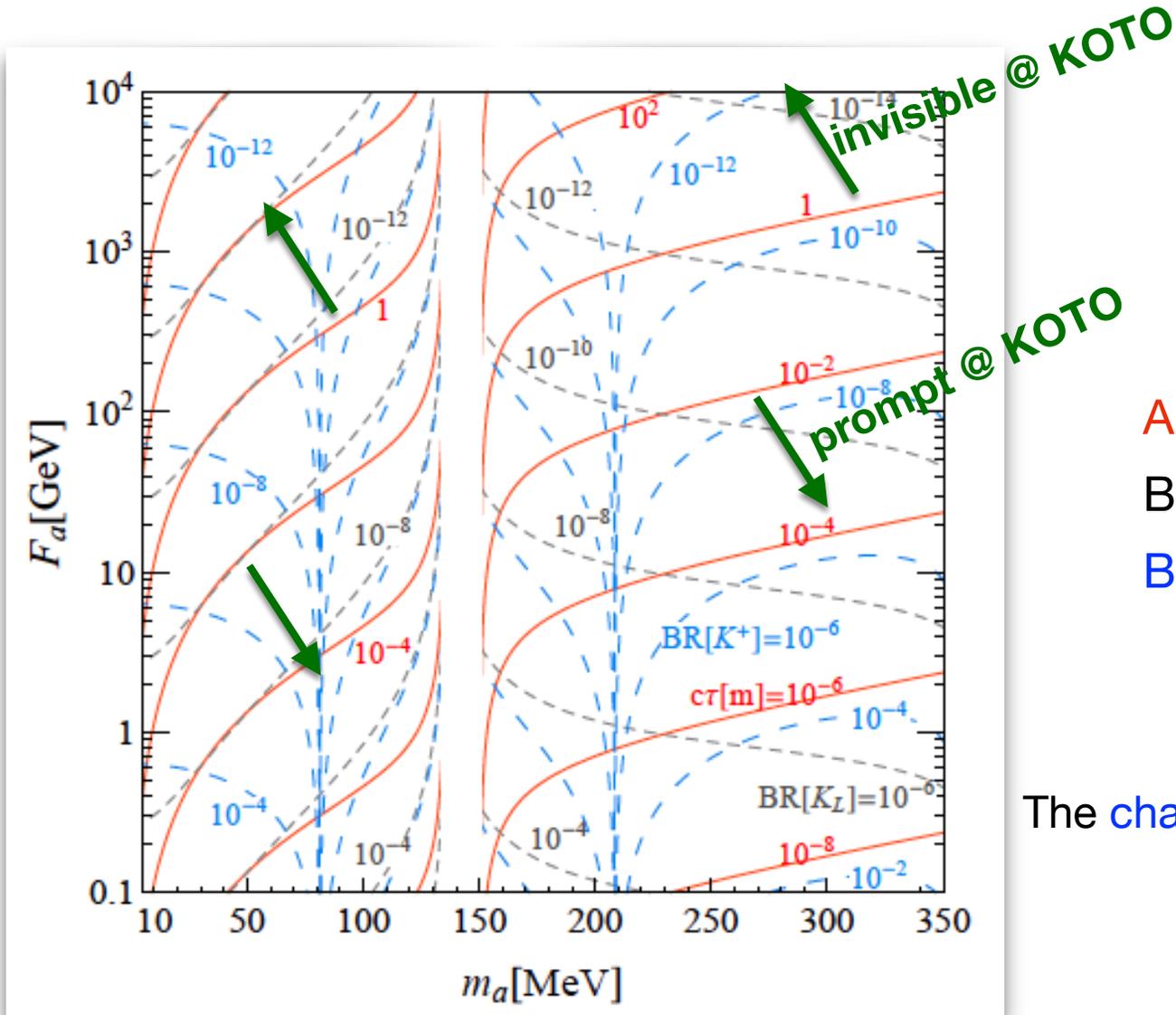
$$\mathcal{L}_{\Delta S=1} = G_8 F_\pi^4 \text{Tr}[\lambda_{sd} D^\mu \Sigma^\dagger D_\mu \Sigma] + G_{27} F_\pi^4 \left(L_{\mu 23} L_{11}^\mu + \frac{2}{3} L_{\mu 21} L_{13}^\mu \right) + h.c.$$

$$\begin{aligned} \pi^0 &\rightarrow \pi_{\text{phy}}^0 + \theta_{\pi a} a_{\text{phy}} \\ \eta &\rightarrow \eta_{\text{phy}} + \theta_{\eta a} a_{\text{phy}} \end{aligned} \quad L_\mu \equiv i\Sigma^\dagger D_\mu \Sigma, \quad \lambda_{sd} \equiv \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix}$$



Note:
possible additional
UV contributions

GG coupled ALP pheno



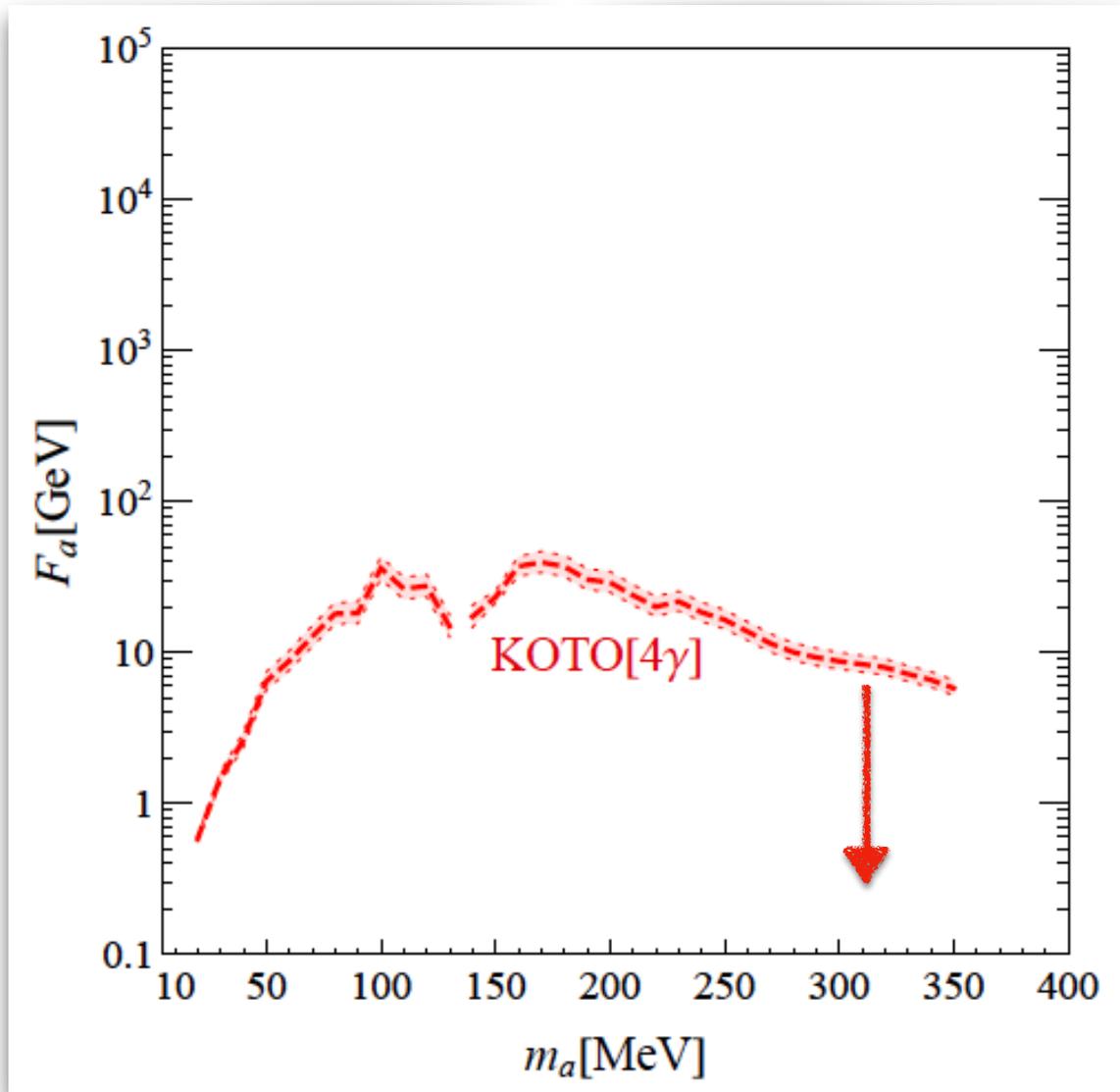
ALP lifetime (in meters)

$BR(K_L \rightarrow \pi a)$

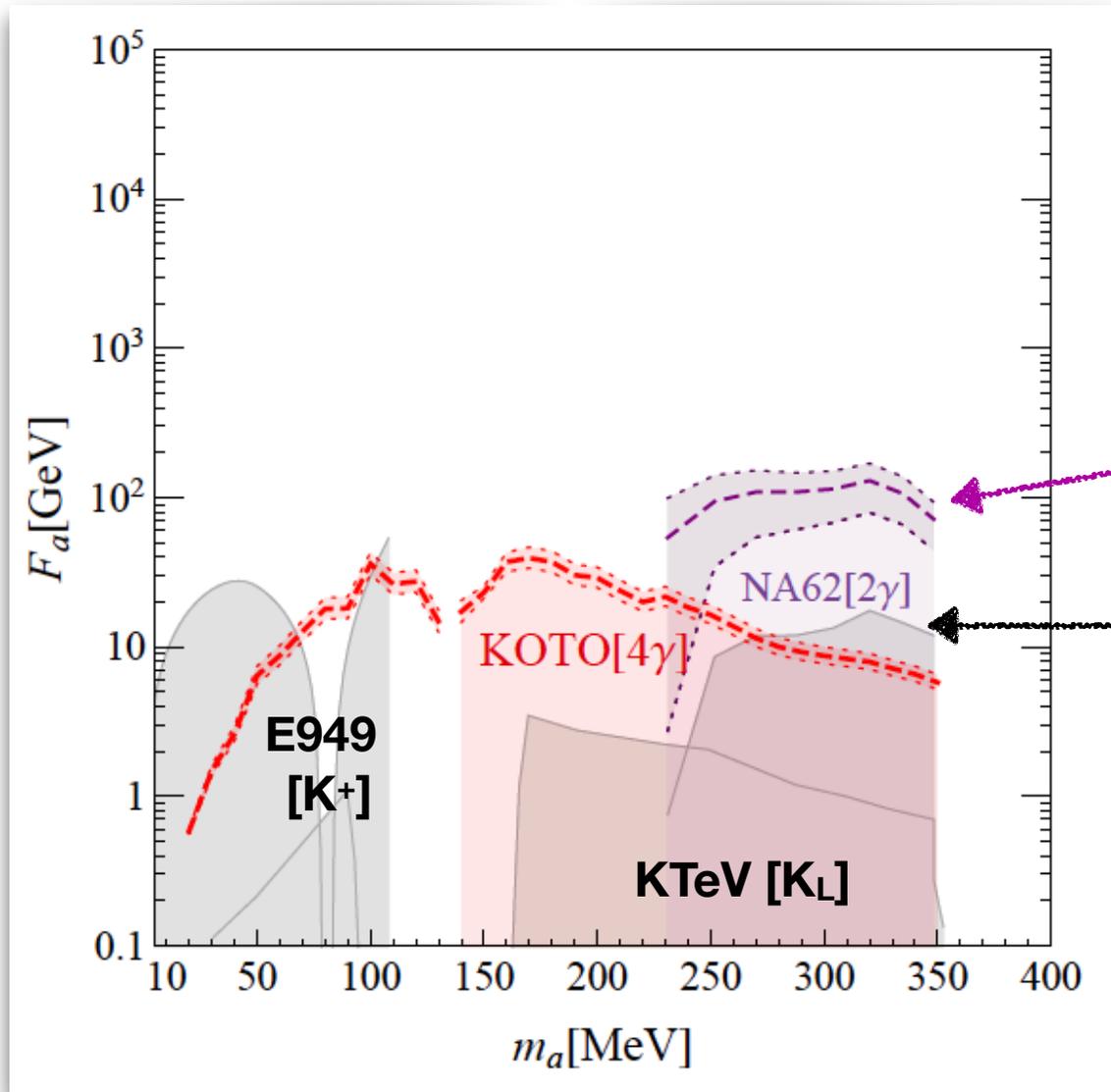
$BR(K^+ \rightarrow \pi^+ a)$

The charged BR is typically larger

$aG\tilde{G}$ at KOTO



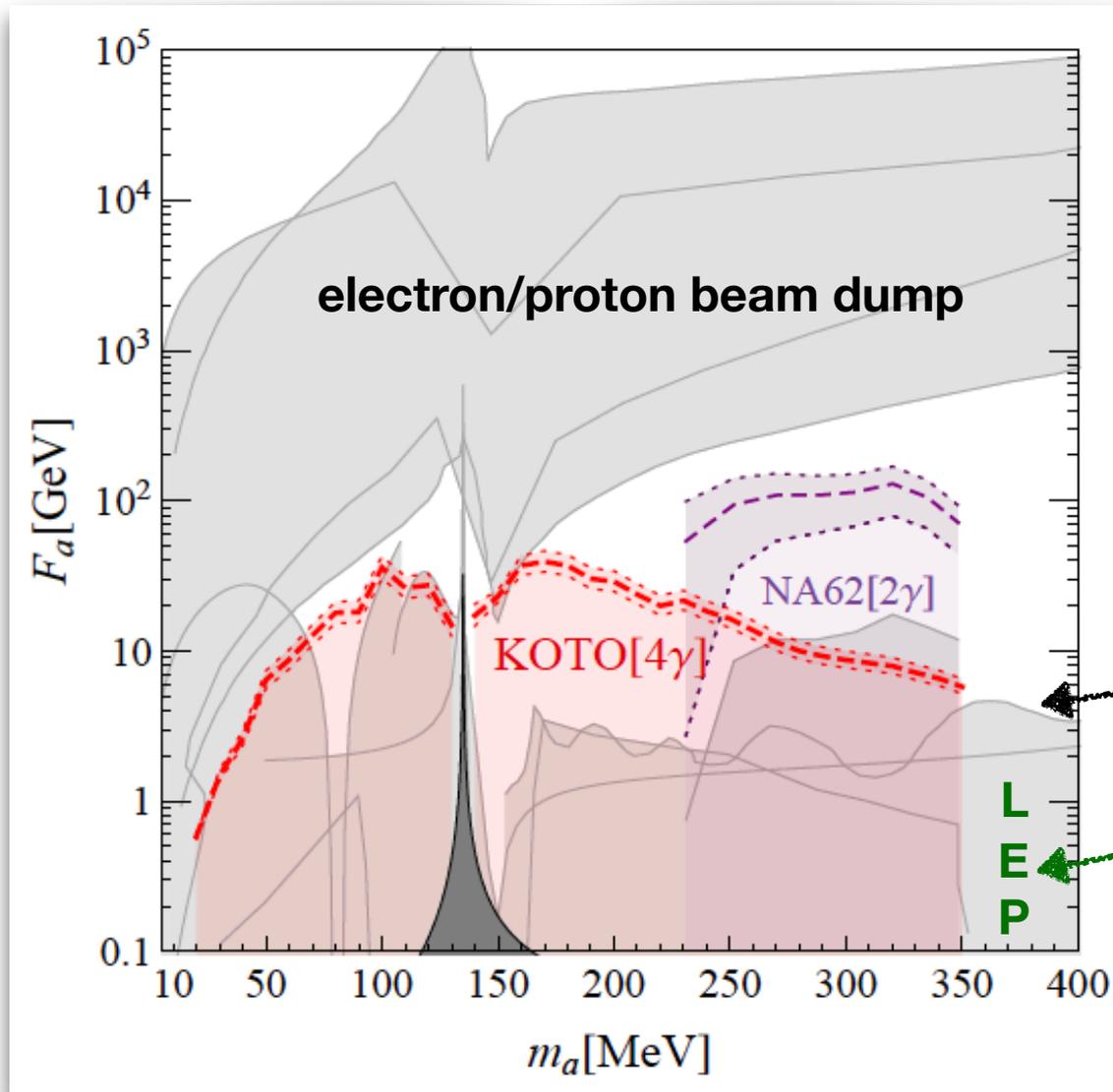
$aG\tilde{G}$ at KOTO and NA62 (visible)



projection with
the full NA62 luminosity

NA48/62 search for
 $K^+ \rightarrow \pi^+ a, a \rightarrow \gamma\gamma$

Complementarity with other experiments

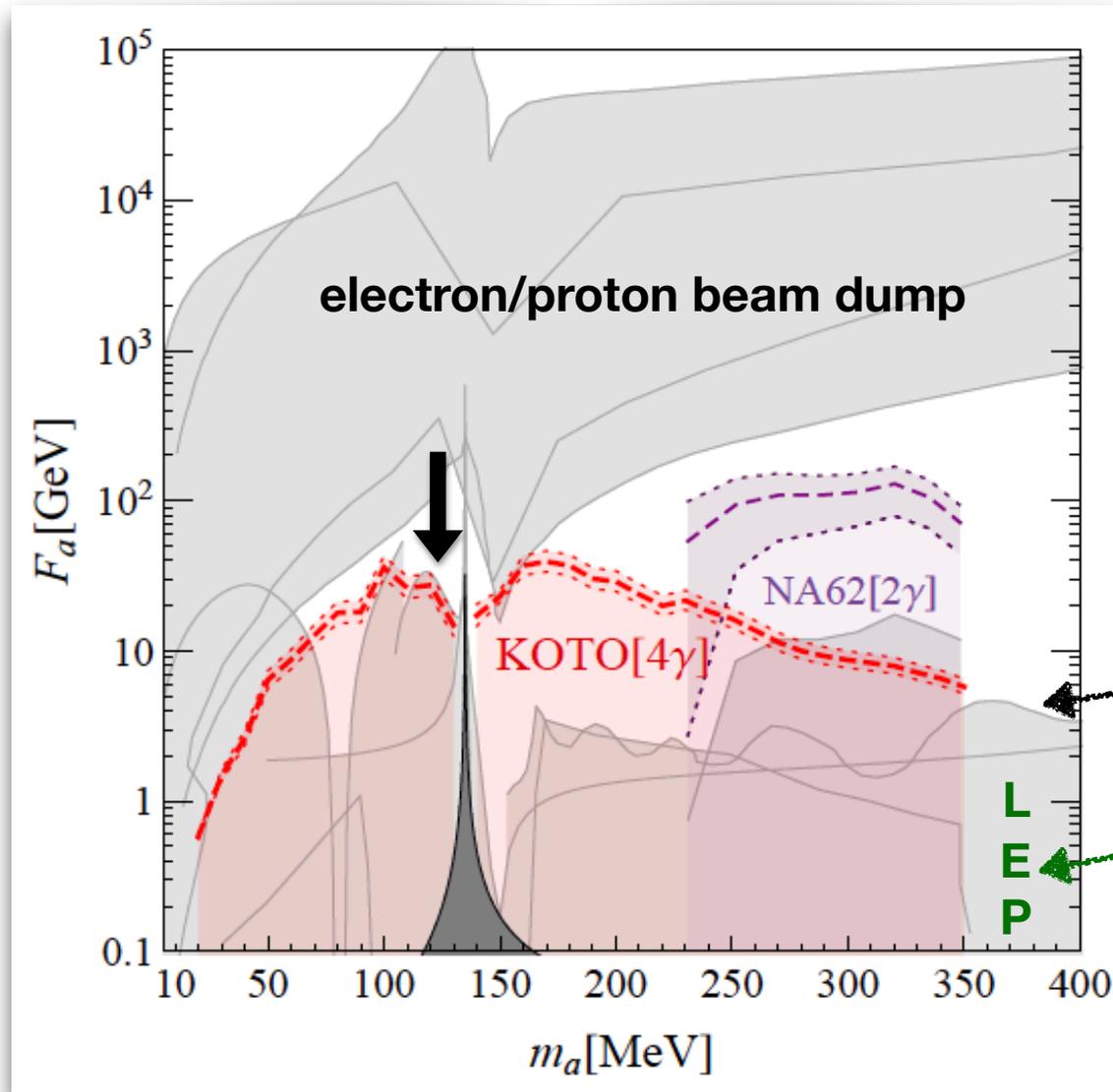


In gray,
we show all present constraints

GlueX,
Aloni et al., 1903.03586

$e^+e^- \rightarrow \gamma a, a \rightarrow \gamma\gamma$
(collimated)

Complementarity with other experiments



In gray,
we show all present constraints

→ This bound comes from
precision pion experiments
W. Altmannshofer, SG, D. Robinson,
1909.00005

GlueX,
Aloni et al., 1903.03586

$e^+e^- \rightarrow \gamma a, a \rightarrow \gamma\gamma$
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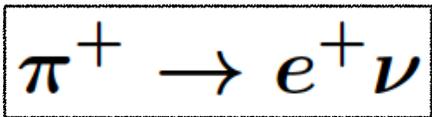
Precision pion experiments

Several (past and present) small-scale experiments built to measure π^+ rare decays

Precision pion experiments

Several (past and present) small-scale experiments built to measure π^+ rare decays

Among the most interesting:



$$\text{BR} \sim \frac{m_e^2 (m_\pi^2 - m_e^2)^2}{m_\mu^2 (m_\pi^2 - m_\mu^2)^2}$$

Helicity suppressed decay

Most precise measurement:

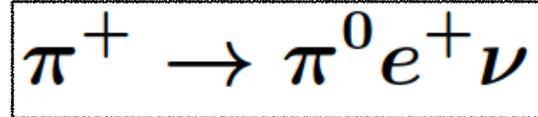
PIENU experiment @ TRIUMF

$$\text{BR}^{\text{exp}} = (1.234 \pm 0.004) \times 10^{-4}$$

Mainly stat. uncertainty

Theoretical uncertainty

~1 order of magnitude smaller!



$$\text{BR} \sim \frac{(m_{\pi^\pm} - m_{\pi^0})^5 m_{\pi^\pm}^3}{f_\pi^2 m_\mu^2 (m_{\pi^\pm}^2 - m_\mu^2)^2}$$

Phase space suppressed decay

Most precise measurement:

PIBETA experiment @ PSI

$$\text{BR}^{\text{exp}} = (1.036 \pm 0.006) \times 10^{-8}$$

Comparable stat. and sys. uncertainties

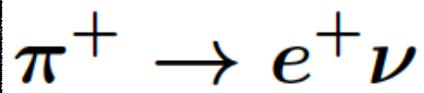
Theoretical uncertainty

a factor of ~2 smaller

Precision pion experiments

Several (past and present) small-scale experiments built to measure π^+ rare decays

Among the most interesting:



$$\text{BR} \sim \frac{m_e^2}{m_\mu^2} \frac{(m_\pi^2 - m_e^2)^2}{(m_\pi^2 - m_\mu^2)^2}$$

Helicity suppressed decay

Most precise measurement:

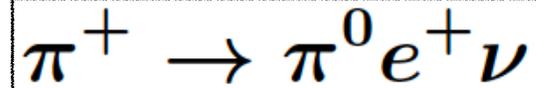
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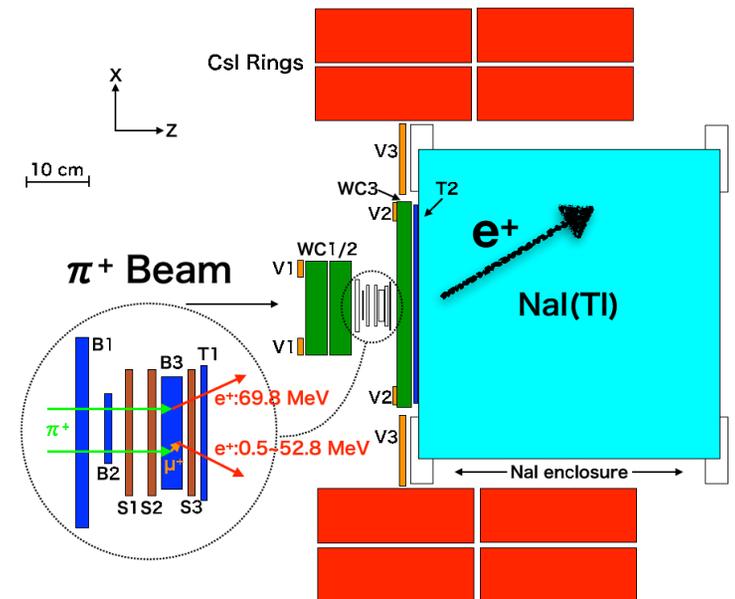
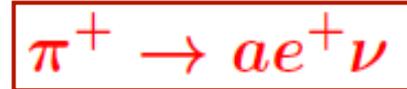
Theoretical uncertainty

a factor of ~2 smaller

$\pi^+ \rightarrow a e^+ \nu$ is not suppressed!

ALPs @ PIENU

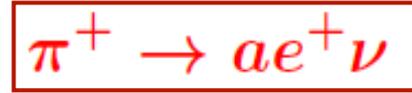
The production of the ALP will affect the energy spectrum measured by the calorimeter



Courtesy of D.Bryman

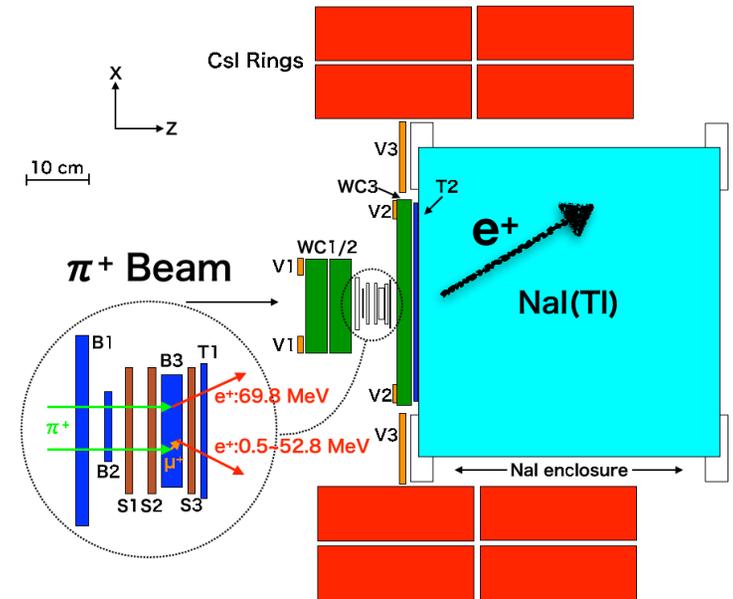
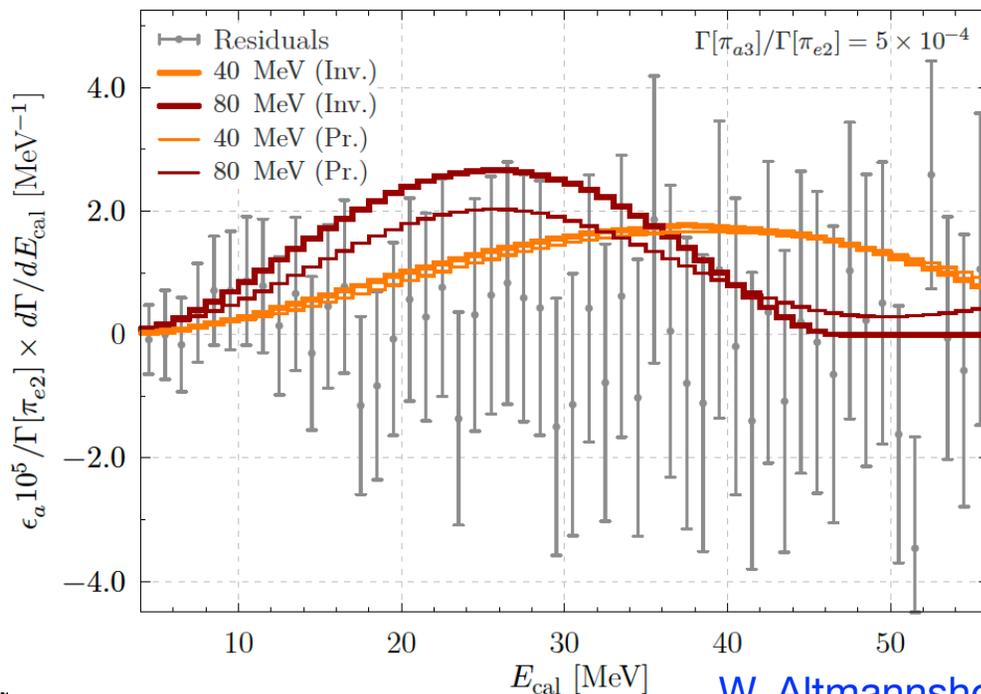
ALPs @ PIENU

The production of the ALP will affect the energy spectrum measured by the calorimeter



2. Invisible regime: the energy spectrum of the positron depends on the ALP mass.

1. Prompt regime: the energy measured by the calorimeter can get a contribution from the photons produced from the ALP decay ($a \rightarrow \gamma\gamma$).



Courtesy of D. Bryman

ALPs @ PiBeta

$$\pi^+ \rightarrow \pi^0 e^+ \nu$$

vs.

$$\pi^+ \rightarrow a e^+ \nu$$

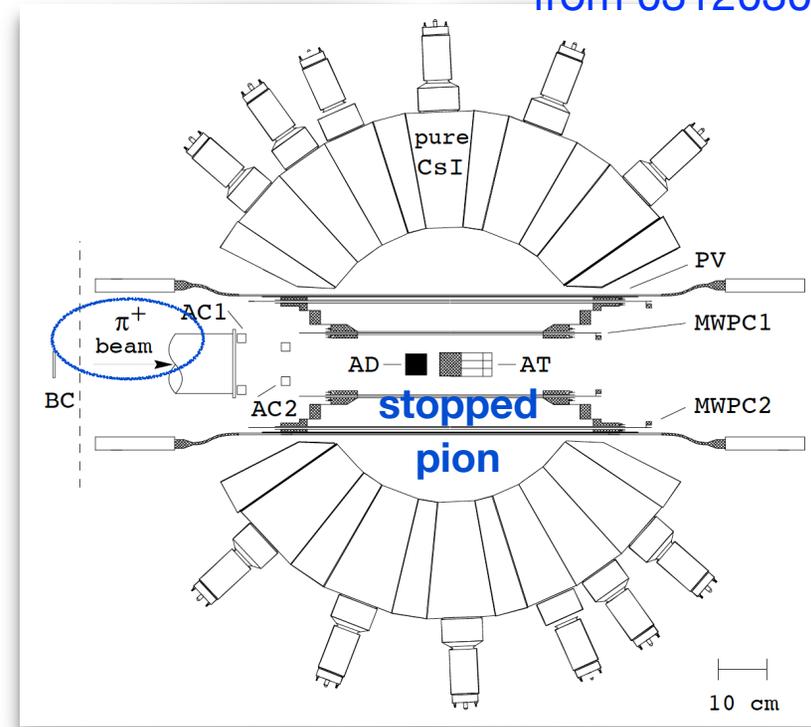
$$\pi^0 \rightarrow \gamma\gamma$$

will be produced
~ back to back

$$a \rightarrow \gamma\gamma$$

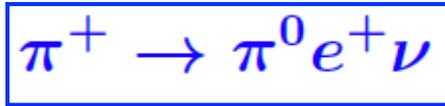
will have a smaller
opening angle

from 0312030

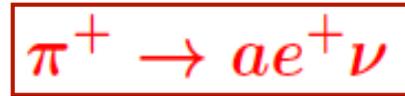


$$-1 \leq \cos \theta_{\gamma\gamma} \leq -1 + 2 \left(\frac{m_{\pi^+}^2 - m_a^2}{m_{\pi^+}^2 + m_a^2} \right)^2$$

ALPs @ PiBeta



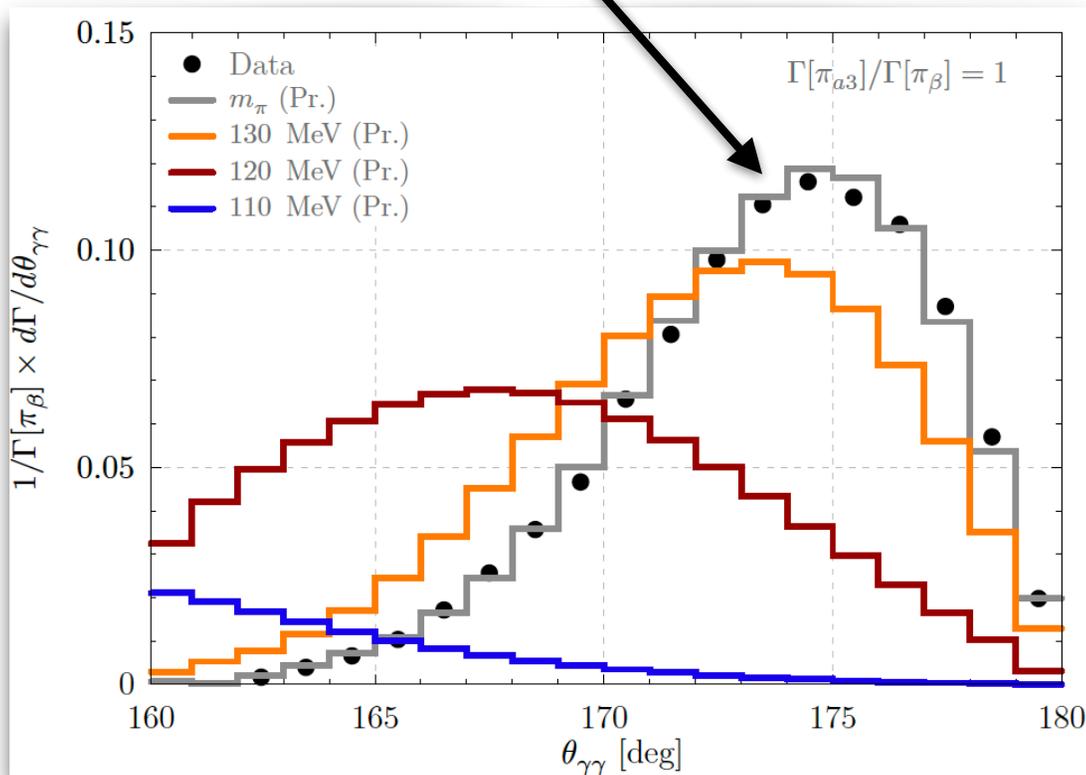
vs.



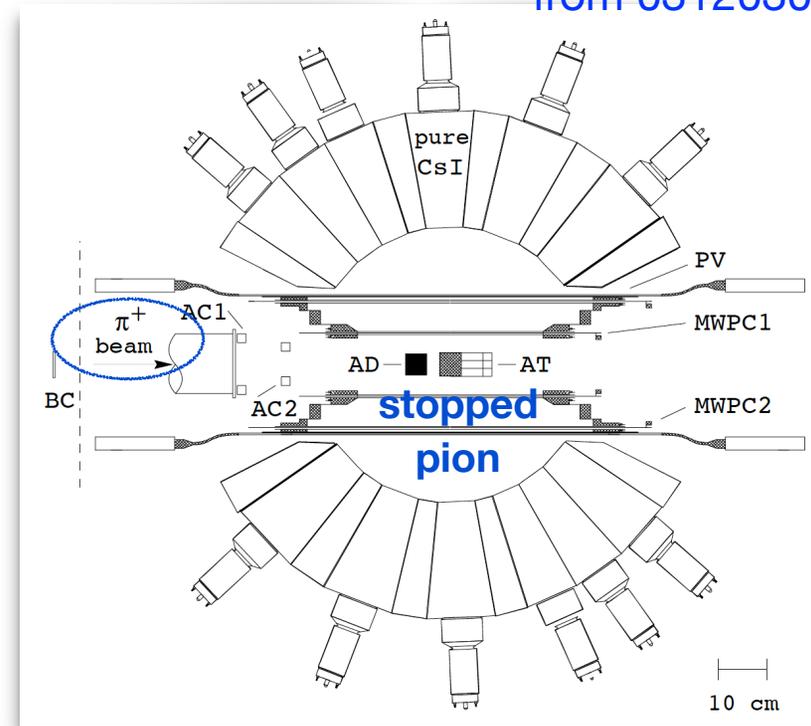
will be produced
~ back to back



will have a smaller
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from 0312030

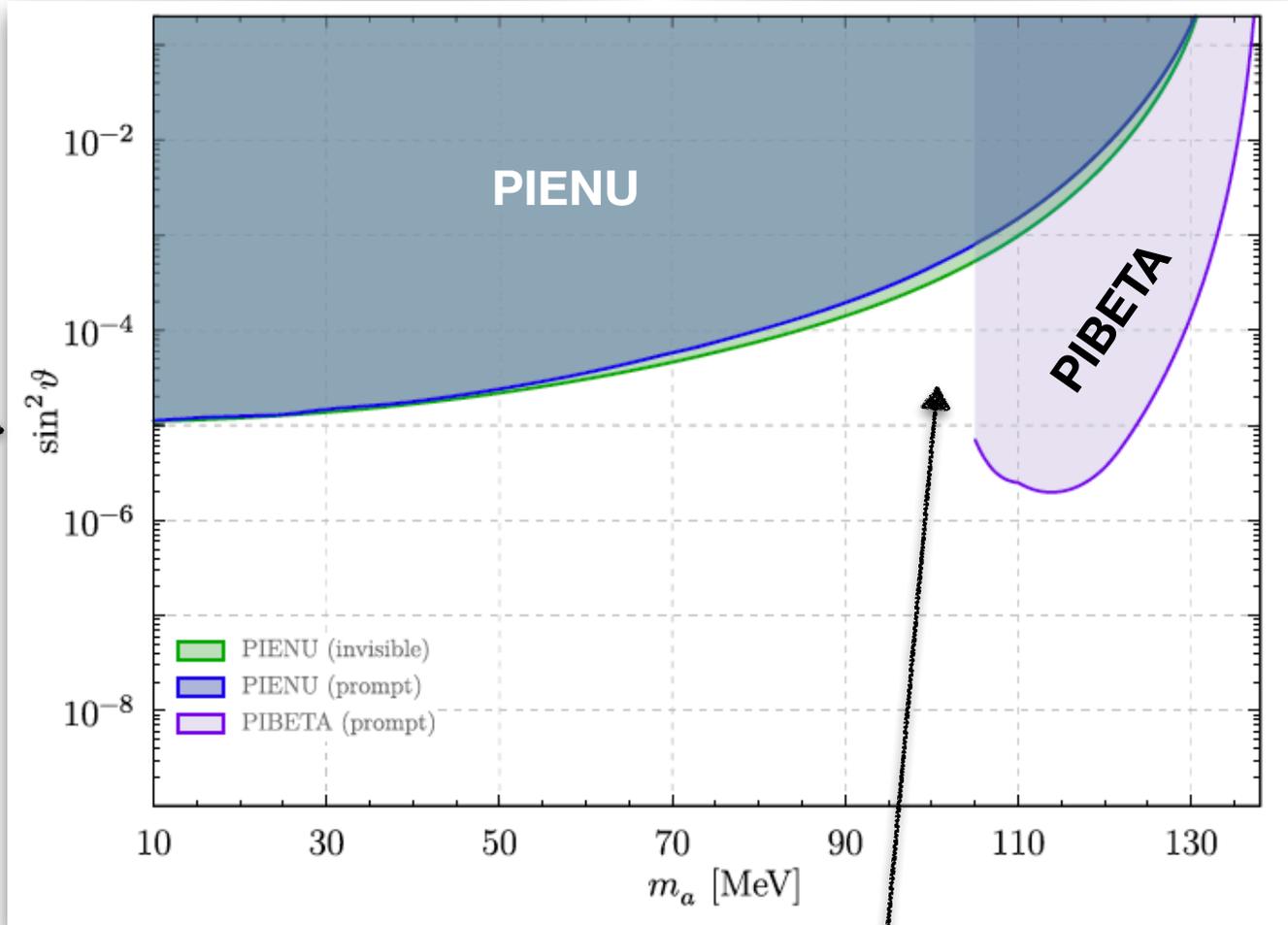


$$-1 \leq \cos \theta_{\gamma\gamma} \leq -1 + 2 \left(\frac{m_{\pi^+}^2 - m_a^2}{m_{\pi^+}^2 + m_a^2} \right)^2$$

ALP bounds from PIENU and PiBeta

W. Altmannshofer, SG, D. Robinson, 1909.00005

ALP-pion
mixing angle



Possibility to go to lower masses
at future experiments
(data at smaller angles!)



Conclusions & Outlook

Interesting times for flavor physics:
anomalies + several experiments ramping up

**Plenty of opportunities to test dark sectors
at these experiments**

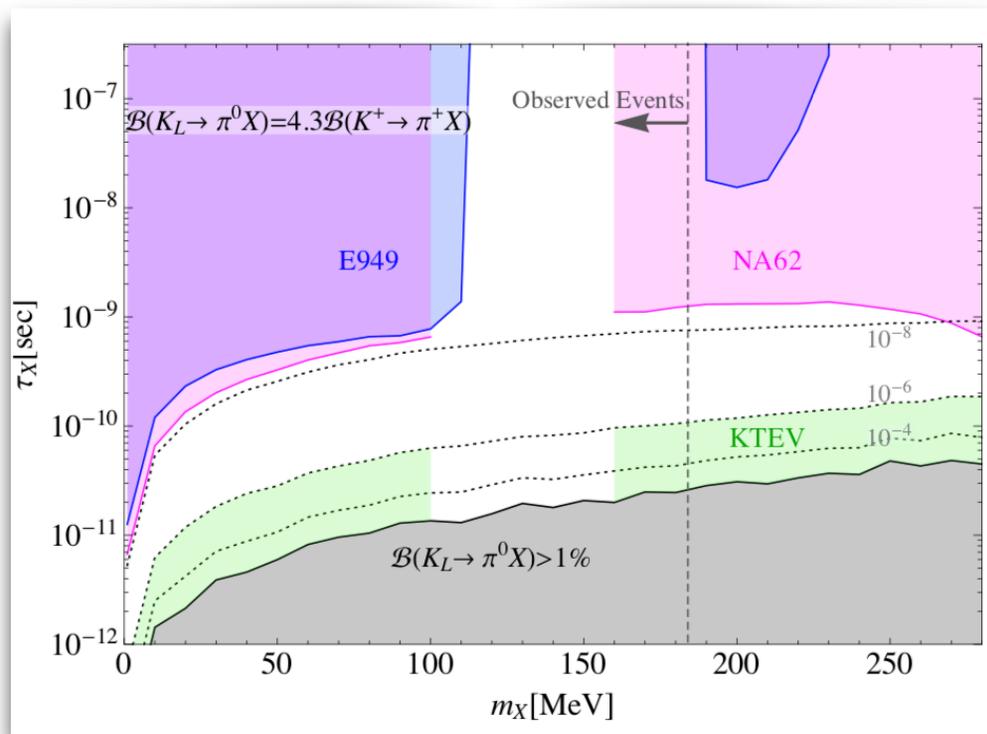
For this seminar:

testing ALPs Kaon experiments

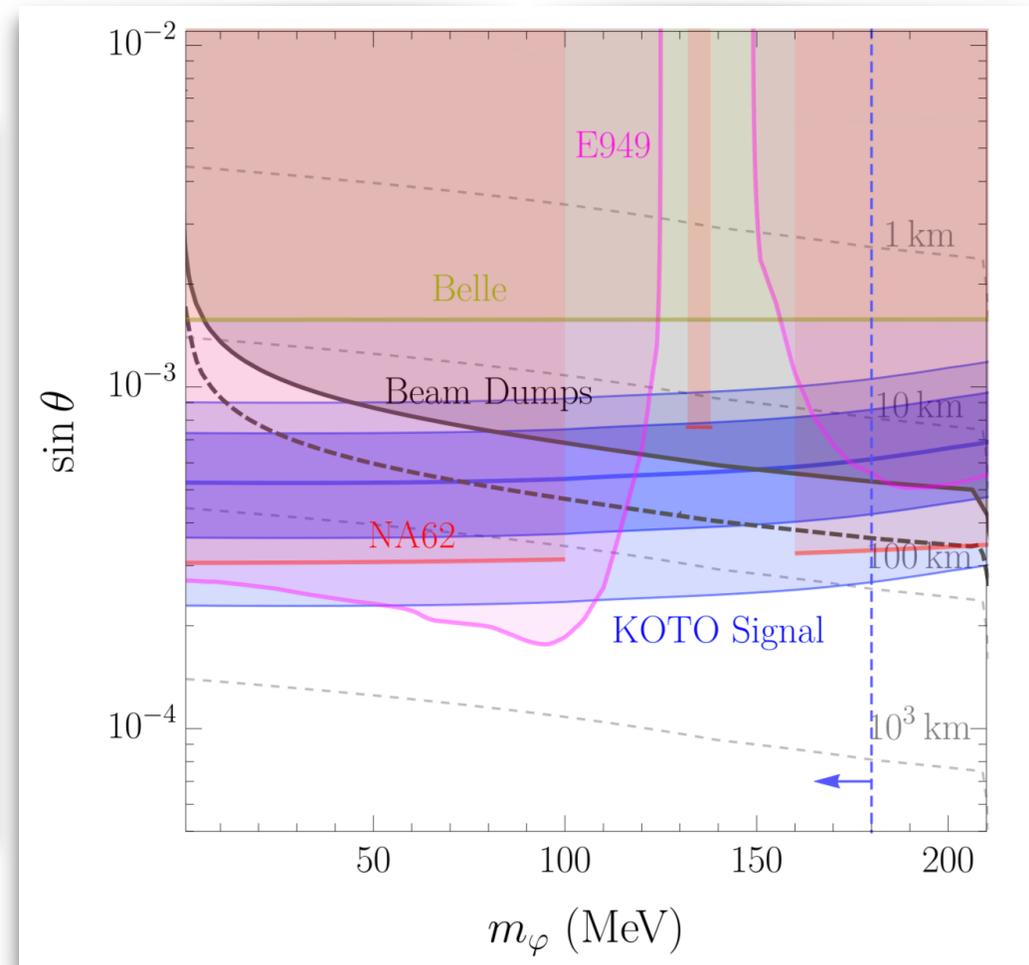
- * The KOTO anomaly
- * New proposed search ($K \rightarrow \pi a$, $a \rightarrow \gamma \gamma$)
and its model interpretation
- * Complementarity with other experiments
(highlight: precision pion experiments)

Models addressing the KOTO anomaly

(light new physics satisfying the GN bound)



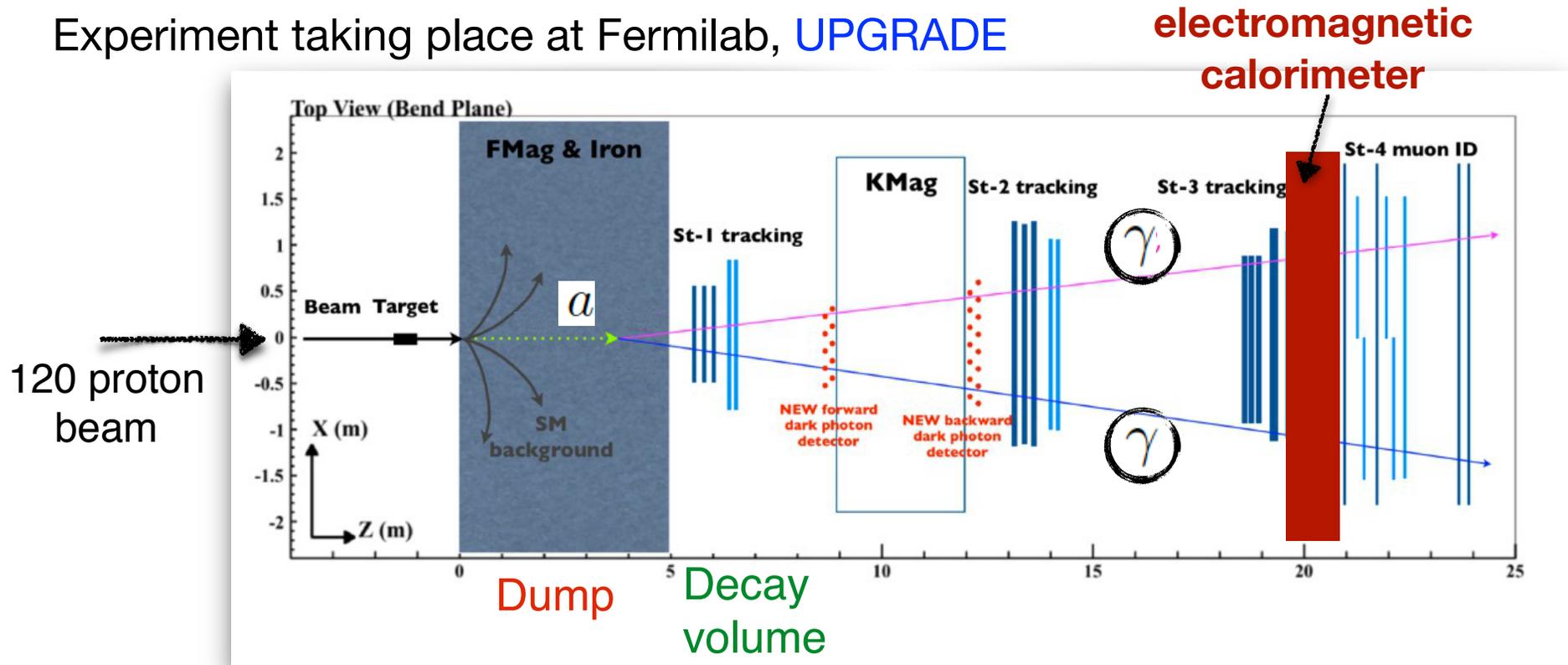
Kitahara et al., 1909.11111



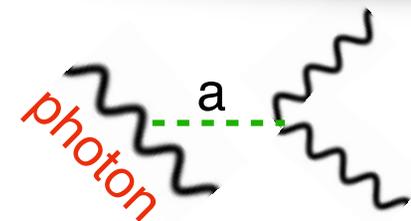
Egana-Ugrinovic et al, 1911. 10203

More new measurements coming up? DarkQuest

Experiment taking place at Fermilab, **UPGRADE**



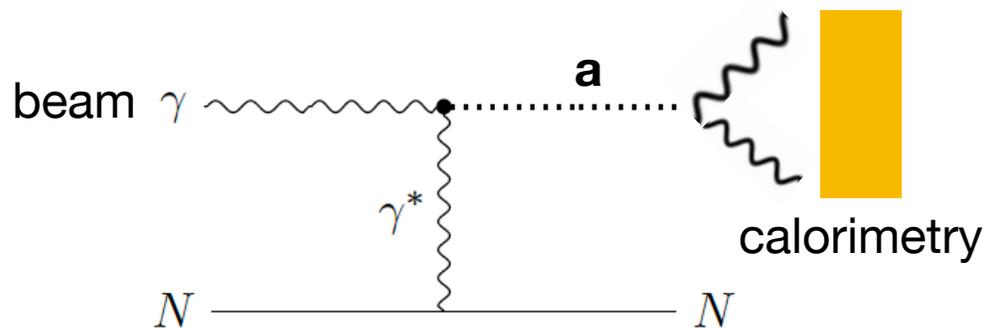
Proposed running after 2022. $\sim 10^{20}$ protons on target.
Displaced electromagnetic objects (including photons)



axions radiated from secondary photons produced in the collisions

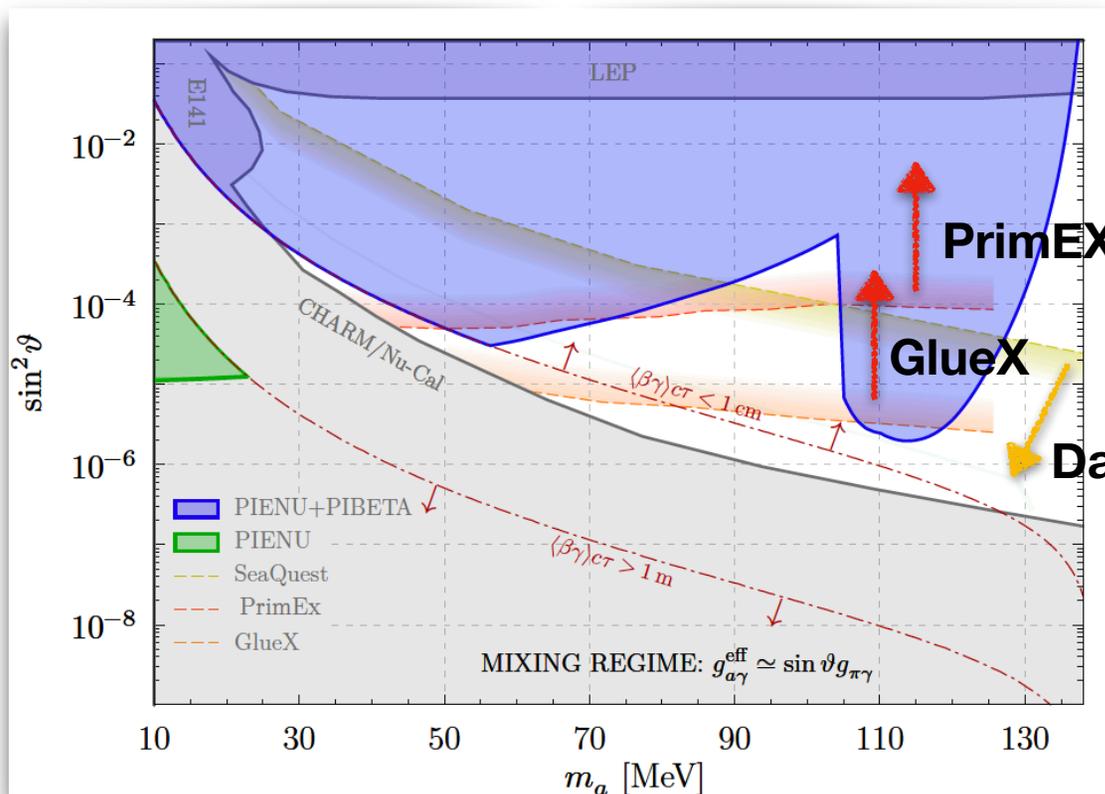
More new measurements coming up?

PrimEX, GlueX



Proposed upgrades for the PrimEX and GlueX experiments at JLAB

$$\gamma N \rightarrow a N \rightarrow \gamma \gamma$$

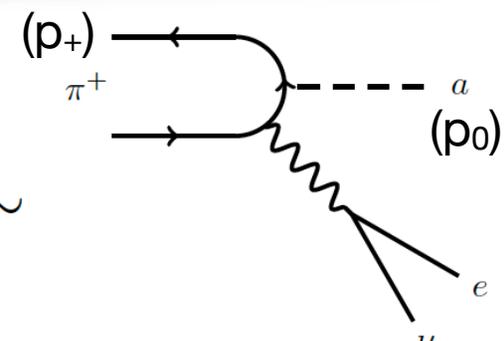


The parameter space for ALPs with mass below the pion mass (and above a few MeV) could be fully covered!

Producing ALPs in pion decays

$$\pi^+ \rightarrow ae^+\nu$$

Not helicity suppression, nor phase space suppression!



$\mathcal{A}[\pi^+ \rightarrow ae\nu] \sim$

$\mathcal{A}^\mu \simeq \langle a | \pi^{*0} \rangle \langle \pi^{*0} | \bar{d} \gamma^\mu u | \pi^+ \rangle$
 $\equiv \sin \vartheta \langle \pi^{*0} | \bar{d} \gamma^\mu u | \pi^+ \rangle$

$$\langle \pi^{*0} | \bar{d} \gamma^\mu u | \pi^+ \rangle = c_\pi \left[\underbrace{f_+}_{\text{form factors}} (p_+^\mu + p_0^\mu) + (f_0 - f_+) \frac{m_+^2 - m_0^2}{q^2} \underbrace{(p_+^\mu - p_0^\mu)}_{q^\mu} \right]$$

ALP mass

$f_+(q^2) \simeq 1$ as long as q^2 is small $\Rightarrow m_0 > \sim 10$ MeV

Theory: better understanding of form factors is needed to probe lighter ALPs!

$$\frac{\text{BR}[\pi^+ \rightarrow ae^+\nu]}{\text{BR}[\pi^+ \rightarrow e^+\nu]} \sim \frac{m_0^4 \sin^2 \vartheta}{f_\pi^2 m_\mu^2 (1 - m_e^2/m_+^2)^2} \times \int_1^{\frac{(m_0^2 + m_+^2)}{2m_0 m_+}} (w^2 - 1)^{3/2} dw$$

$$w = \frac{m_+^2 + m_0^2 - q^2}{2m_+ m_0}$$

ALP-pion & ALP-eta mixing

$$\mathcal{L}_{eff} = \frac{iF_\pi^2}{4} \frac{\partial_\mu a}{F_a} \text{Tr}[\tilde{\kappa}_q(\Sigma^\dagger D^\mu \Sigma - \Sigma D^\mu \Sigma^\dagger)] + \frac{F^2}{2} B_0 \text{Tr}[\Sigma \mathbf{m}^\dagger + \mathbf{m}^\dagger \Sigma^\dagger],$$

$$\left\{ \begin{array}{l} \mathbf{m} = \exp\left(i\kappa_q \frac{a}{2F_a} \gamma_5\right) \cdot m_q \cdot \exp\left(i\kappa_q \frac{a}{2F_a} \gamma_5\right) \\ \tilde{\kappa}_q = \text{diag}(\kappa_q), \quad \kappa_q = \frac{1}{m_q} / \sum_{q'} \left(\frac{1}{m_{q'}}\right) \end{array} \right.$$

$$\Sigma \equiv \exp[2i\Pi/F_\pi], \quad \Pi \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} + \frac{\eta_0}{\sqrt{3}} & & & \\ & \pi^- & & \\ & & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} + \frac{\eta_0}{\sqrt{3}} & \\ & & & K^- & & \\ & & & & \bar{K}^0 & \\ & & & & & -2\frac{\eta_8}{\sqrt{6}} + \frac{\eta_0}{\sqrt{3}} \end{pmatrix} \begin{matrix} \pi^+ \\ K^0 \\ K^+ \end{matrix}$$

$$\begin{pmatrix} \eta \\ \eta' \end{pmatrix} = \begin{pmatrix} \cos \theta_{\eta\eta'} & -\sin \theta_{\eta\eta'} \\ \sin \theta_{\eta\eta'} & \cos \theta_{\eta\eta'} \end{pmatrix} \begin{pmatrix} \eta_8 \\ \eta_0 \end{pmatrix}$$

$$\theta_{\eta\eta'} \subset -(10 - 20)^\circ$$

Large uncertainties

← this is decoupled

The precision frontier @ flavor factories

A big jump in luminosity is expected in the coming years

Past/Present

Future

B-factories

LHCb: more than $\sim 10^{12}$ b quarks produced so far;

Belle (running until 2010):
 $\sim 10^9$ BB-pairs were produced.

~ 40 times more b quarks will be produced by the end of the LHC;

~ 50 times more BB-pairs will be produced by **Belle-II**.

.....

Kaon-factories

E949 at BNL: $\sim 10^{12}$ K^+
(decay at rest experiment);

E391 at KEK: $\sim 10^{12}$ K_L

NA62 at CERN: $\sim 10^{13}$ K^+
by the end of its run
(decay in flight experiment);

KOTO at JPARC: $\sim 10^{14}$ K_L
by the end of its run

.....

Pion-factories

PIENU experiment at TRIUMF:
 $\sim 10^{11}$ π^+ (still analyzing data)

?