

# Jet Clustering for DIS in the Breit Frame

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[arXiv:2006.10751](https://arxiv.org/abs/2006.10751)

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Supported by the FELLINI project and the European Commission



# Breit Frame kinematics

$$n^\mu = (1, 0, 0, +1) \quad \bar{n}^\mu = (1, 0, 0, -1)$$

Proton

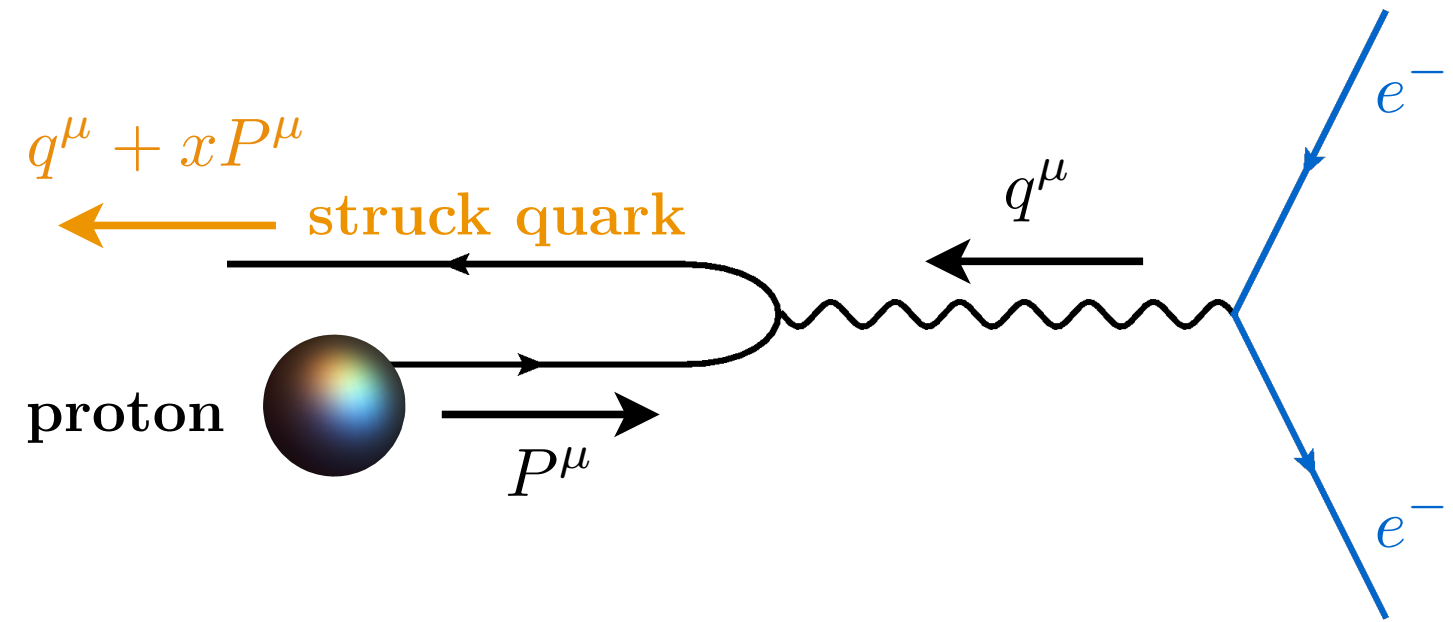
$$P^\mu = \frac{Q}{2x_B} n^\mu$$

Photon

$$q^\mu = \frac{Q}{2} (n^\mu - \bar{n}^\mu)$$

Struck quark

$$p^\mu = q^\mu + xP^\mu = \frac{Q}{2} \bar{n}^\mu$$



Hadronization of the struck quark will generate a jet close to the (anti-)beam axis. These configurations are the majority of the events and offer vast range of applications. The jets found away from beam remnant provide “clean” jets similar to those found in lepton-lepton colliders (but with dynamical  $Q$ ).

# The backward jet

## Jet observables

- Energy (fraction) distributions
- Hadron-in-jet
- Jet substructure (e.t.c. Angularities)

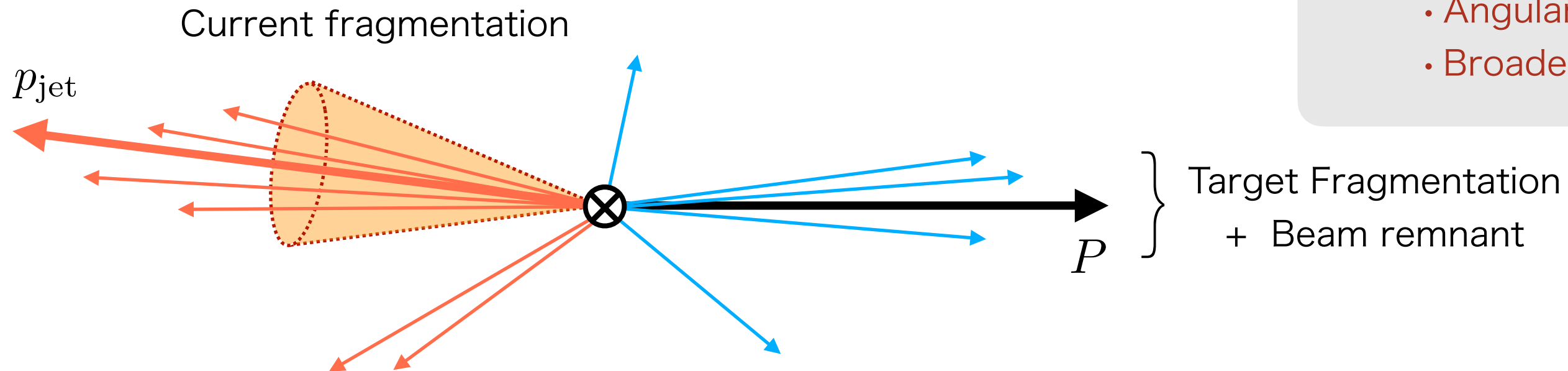
## TMDs

- unpolarized TMDs
- Sivers (quark)
- Hadron-in-jet

The only frame for which TMDPDFs are universal to conventional TMDs.  
(i.e., the soft function involves Wilson-lines in the back-to-back direction)

## Event shapes (in BF)

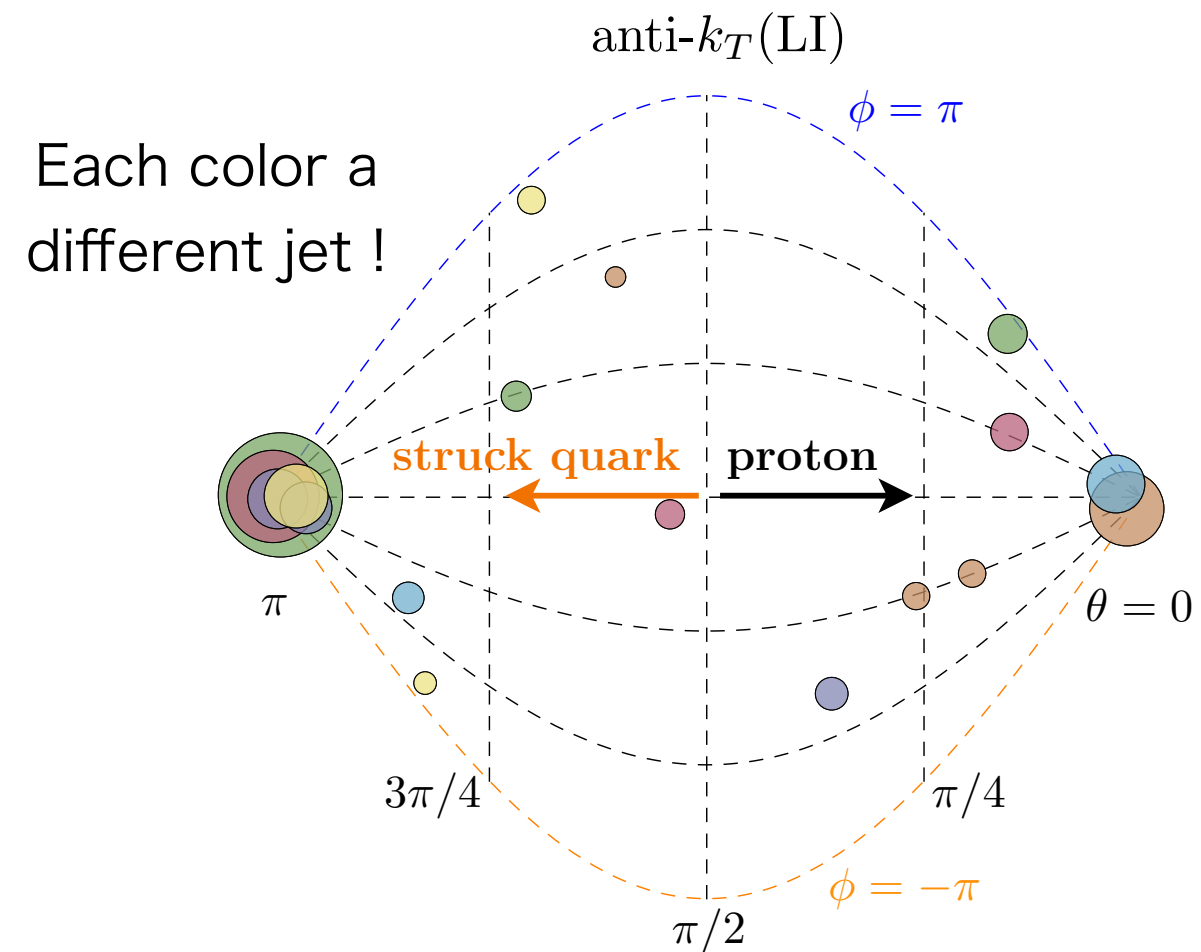
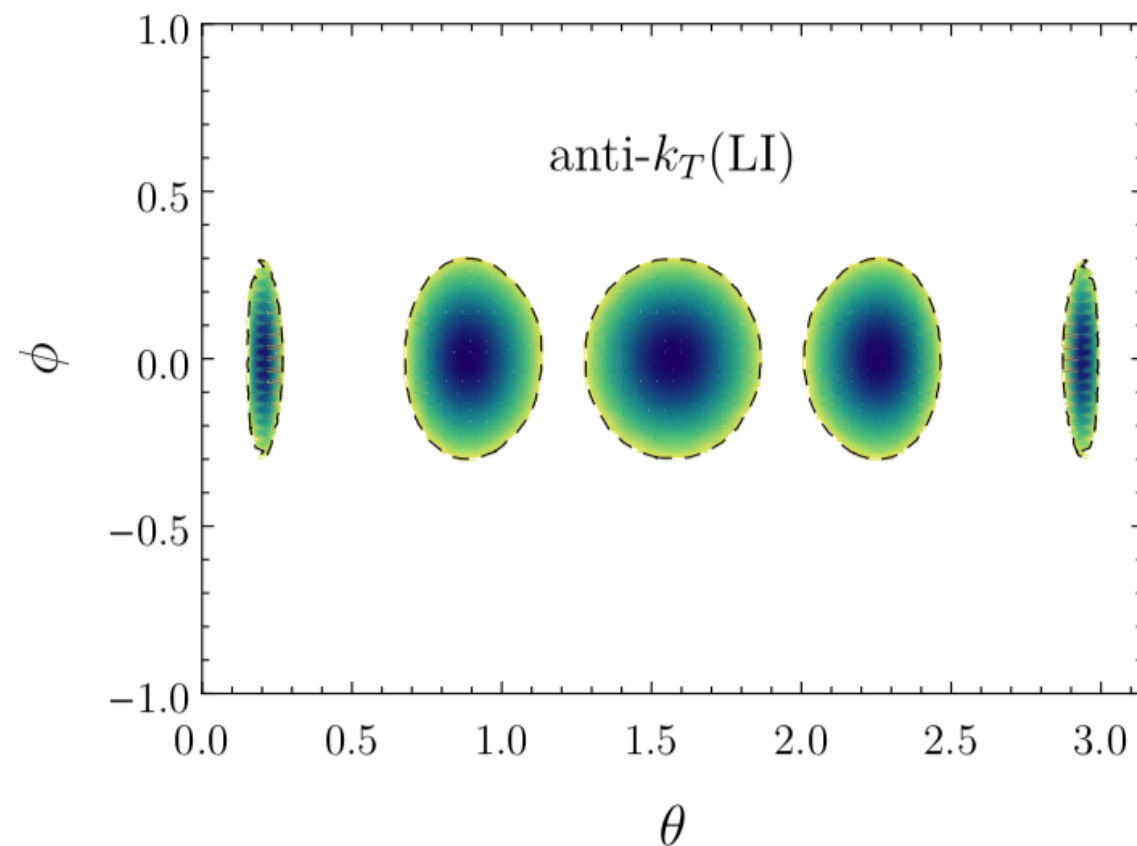
- 1-jettiness
- Angularities
- Broadening



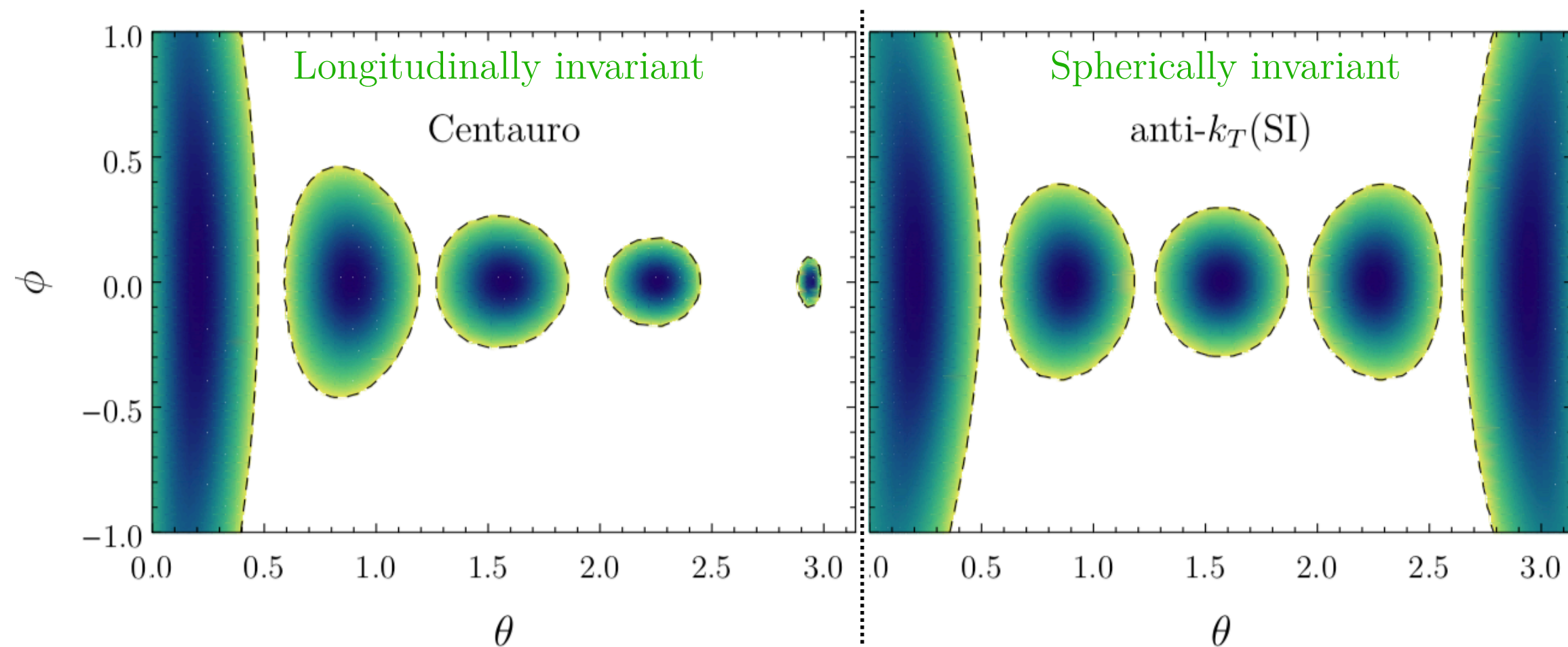
# Longitudinally invariant algorithms

k<sub>T</sub>-type jet algorithms (and particularly anti-k<sub>T</sub>) dominate the hadronic physics market. Are well known and well behaved algorithms in the LAB frame.

However, in Breit Frame since they cluster in the  $y - \phi$  space, they fail to capture hadrons in the very backward direction, where we are looking for one.



# Alternatives



$$d_{ij} = \left[ (\Delta f_{ij})^2 + 2f_i f_j (1 - \cos \Delta\phi_{ij}) \right] / R^2$$

Asymmetric measure is necessary

$$f(x) = x + \mathcal{O}(x^2)$$

$$\bar{\eta}_i = -\frac{2Q}{\bar{n} \cdot q} \frac{p_i^\perp}{n \cdot p_i}$$

$$\bar{\eta}_i(\text{BF}) = 2p_i^\perp / p_i^+$$

$$d_{ij} = \min(E_i^{2p}, E_j^{2p}) \frac{1 - \cos \theta_{ij}}{1 - \cos R}$$

Here we use:

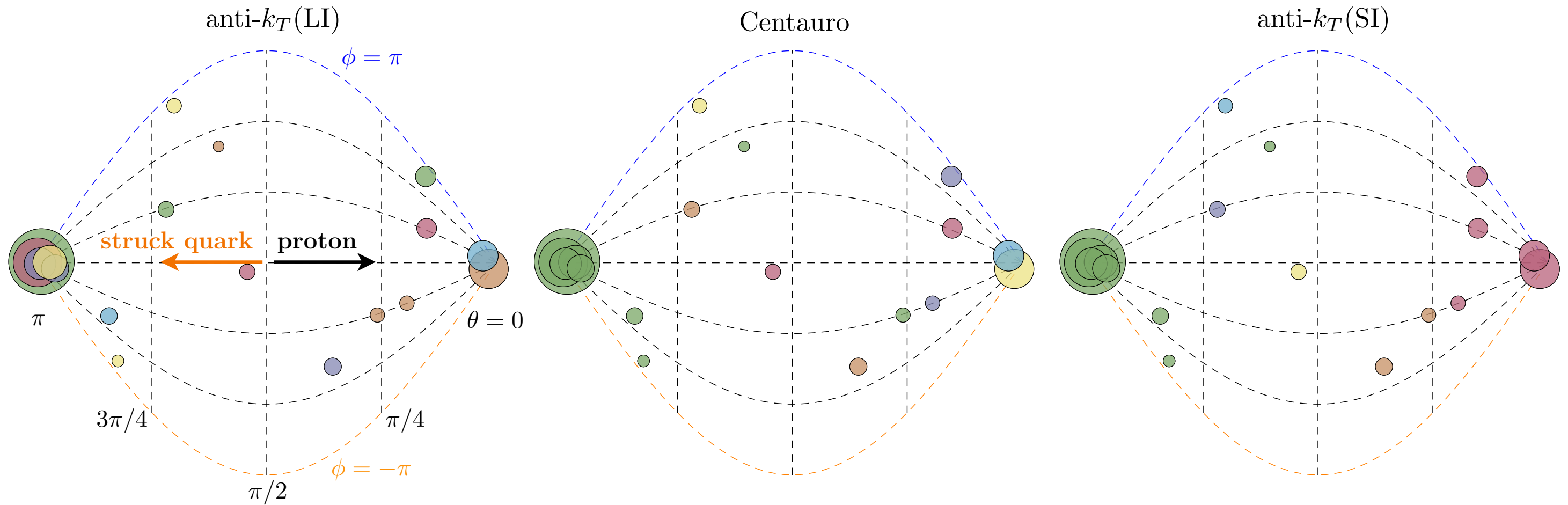
$$d_{iB} = E_i^{2p}$$

$$p = -1$$

Similar algorithm for DIS by:

S. Catani, Y. L. Dokshitzer, and B. Webber, (1992)

# Alternatives

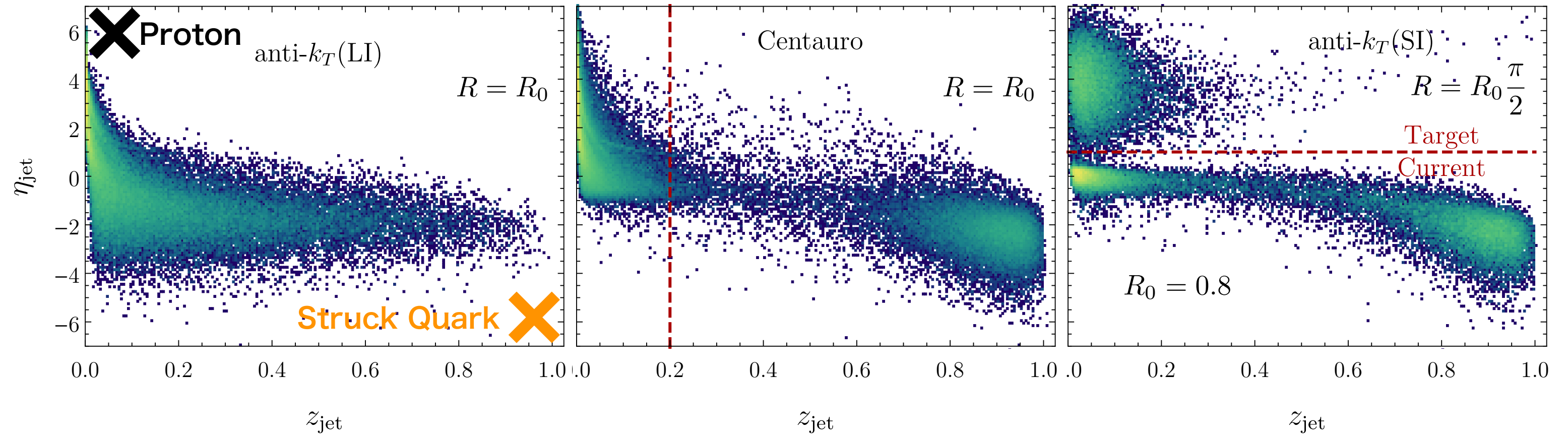


Longitudinally invariant  
Symmetric

Longitudinally invariant  
Asymmetric

Spherically invariant  
Symmetric

# First look



$$z_{\text{jet}} = \frac{P \cdot p_{\text{jet}}}{P \cdot q}$$

$$z_{\text{jet}}(\text{Breit frame}) = p^+ / Q$$

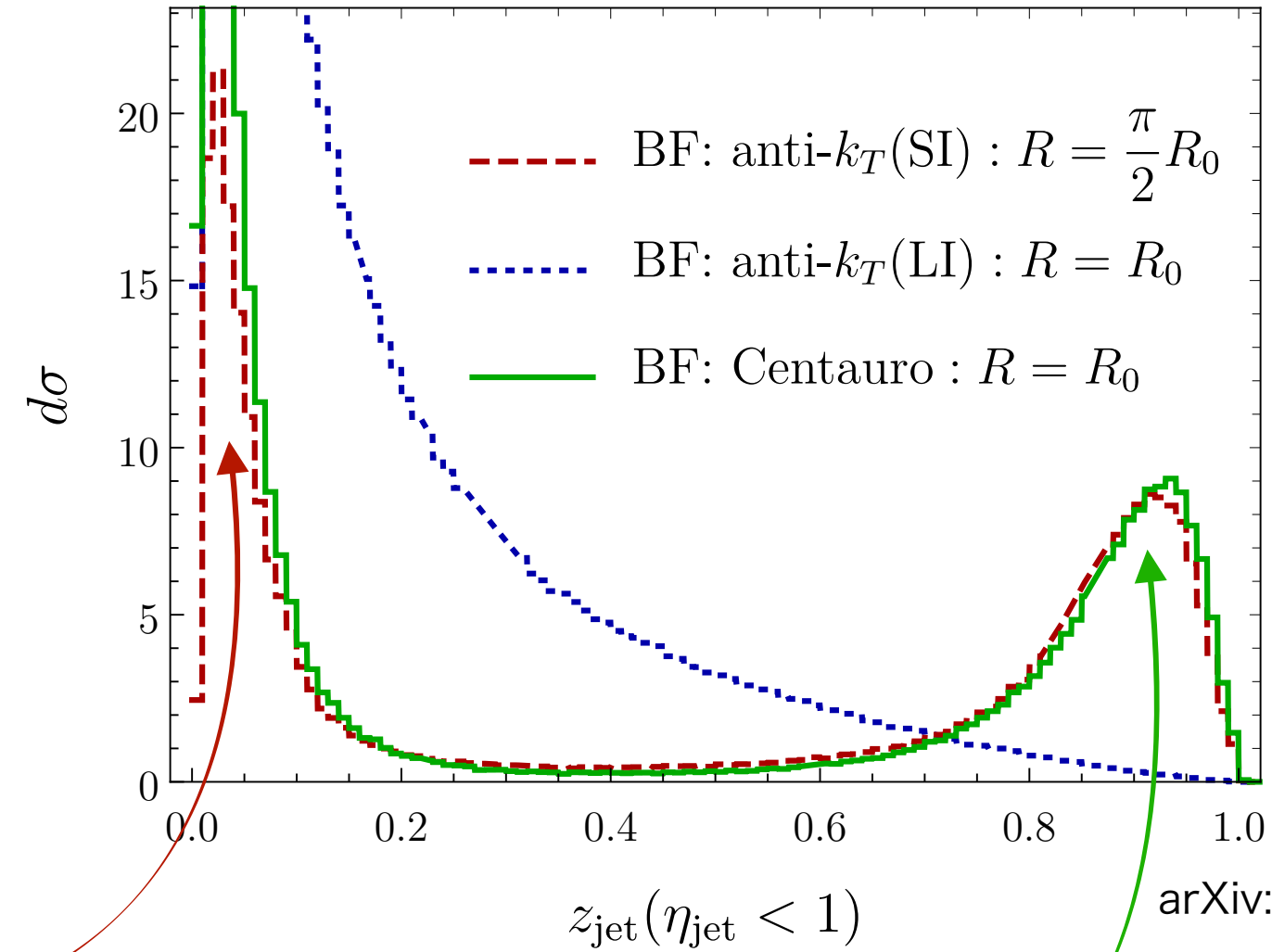
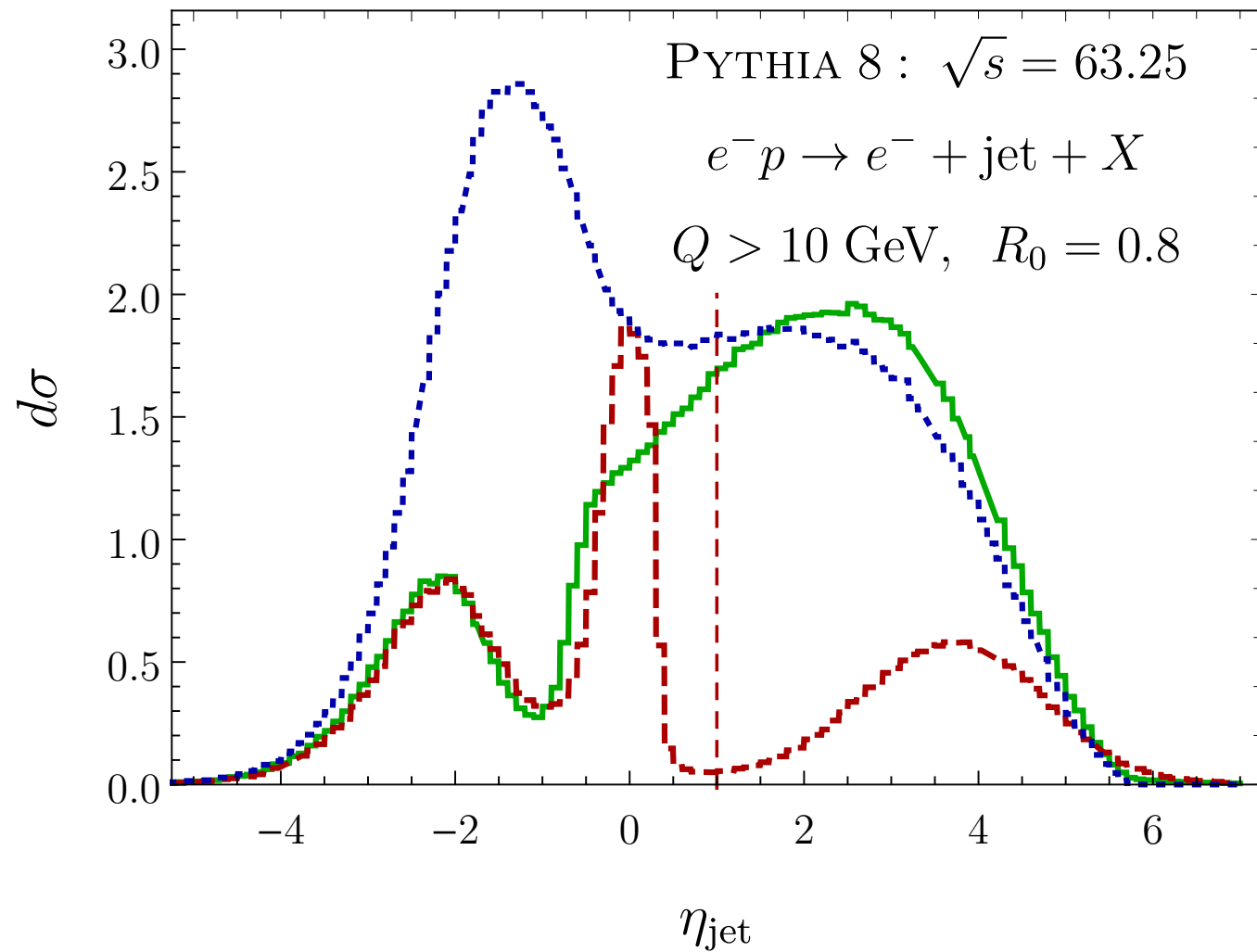
$$z_{\text{jet}} > 0$$

$$z_{\text{jet}} = \sum_{i \in \text{jet}} z_i$$

$$z_{\text{jet}} \leq 1$$

$$\sum_{\text{jet} \in \text{event}} z_{\text{jet}} \leq \sum_{i \in \text{event}} z_i = 1$$

# Pseudo-rapidity and Energy fraction



Rapidity cutoff to remove target fragmentation in SI allows for studies of the full z-spectrum. Other wise only possible in hadronic colliders

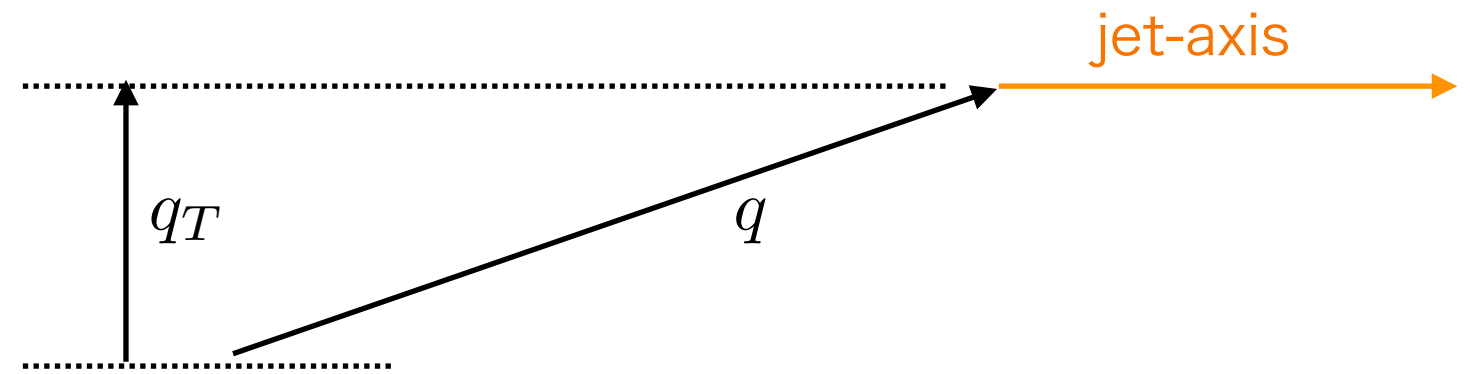
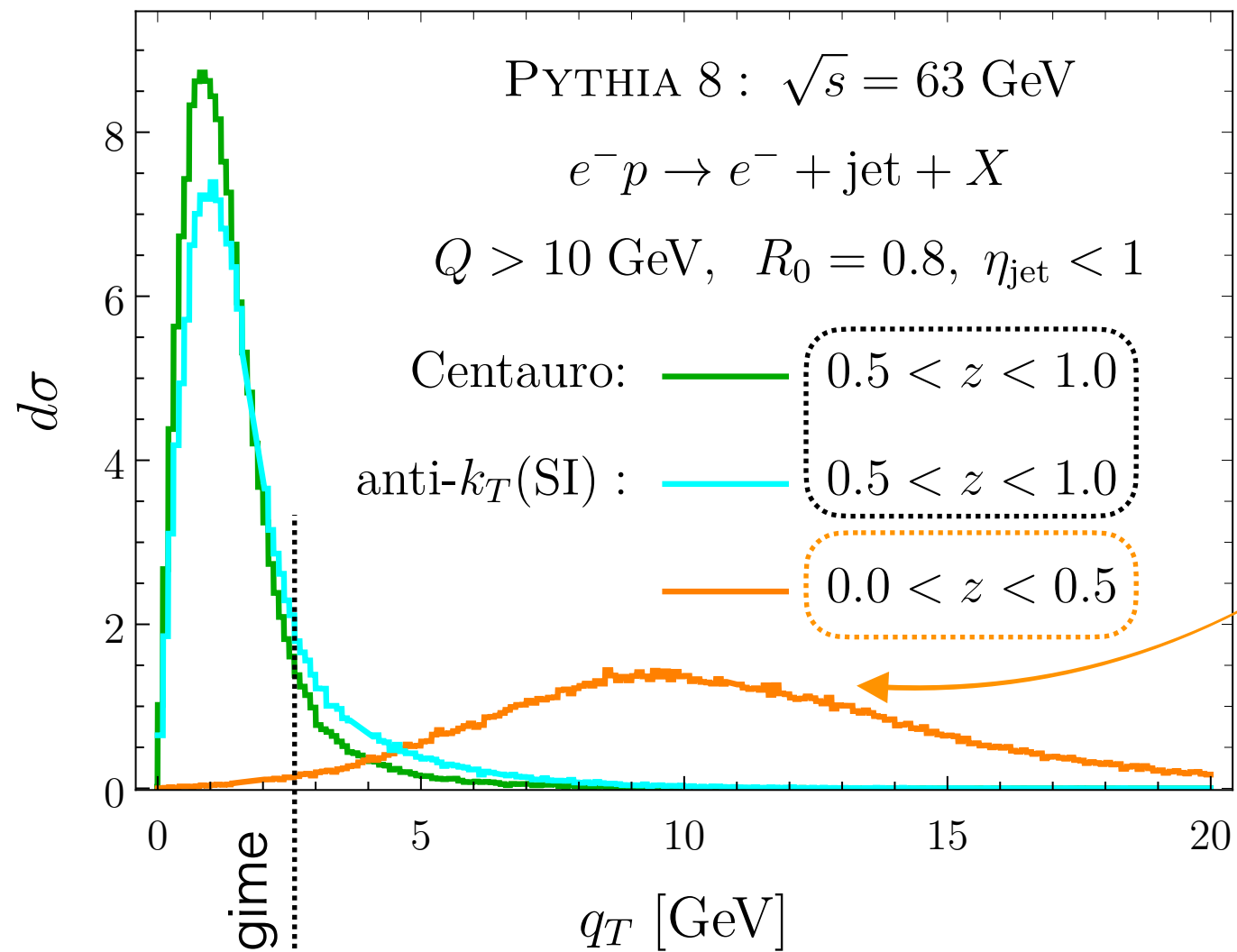
arXiv:2003.02275

Endpoint distribution associated with the energetic jets requires threshold analysis. Hadronization effects for Centauro are universal to event-shape observables

arXiv:1701.05660



# TMDs



New regime from current fragmentation at small transverse momentum that is not studied theoretically yet.

The  $z$ -cut at 0.5 it is arbitrary and can be relaxed within the region 0.2 - 0.6 inducing only minor effects.

arXiv:1807.07573

arXiv:1904.04259 arXiv:1907.05896

# Implementation with Fastjet::contrib

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by Miguel A.

The necessary files can be found here:

<https://github.com/miguelignacio/CentauroJetAlgorithm>

We plan to include this code in the standard fastjet-contrib release. To install it, you should copy this folder as "CentauroPlugin" in your fastjet contrib folder (<https://fastjet.hepforge.org/contrib/>) along with all the other plugings. Then do:

```
./configure --only=CentauroPlugin --fastjet-config=YOURPATH/fastjet-install/bin/fastjet-  
config CXXFLAGS=-fPIC CFLAGS=-fPIC  
  
make  
  
make install
```

You can then run an example with:

```
./example < ../data/single-epDIS-event.dat
```

# How to use in Pythia 8

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```
#include "fastjet/contrib/CentauroPlugin.hh"
```

```
·  
·  
·
```

```
fastjet::contrib::CentauroPlugin * centauro_plugin = new fastjet::contrib::CentauroPlugin(0.8);
```

```
JetDefinition centauro(centauro_plugin);
```

```
ClusterSequence clustSeqCentauro(fjInputsBF, centauro);
```

```
inclusiveJetsCentauro = clustSeqCentauro.inclusive_jets(0);
```

```
JetsCentauro = sorted_by_E(inclusiveJetsCentauro);
```

↑  
minimum pT for jets

↑  
jet Radius

# Outlook

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(1) **In progress** - Energy spectrum: projections for the EIC and HERA

+

Theory predictions including  
threshold resummation and  
hadronization corrections

(2) Look the behavior of Centauro in di-jet configurations and consider simultaneous analysis for single and di-jet cross sections.

(3) Theory + pheno. study of the quark-Sivers function from jets in the Breit Frame

(4) Integration in the FastJet framework: effects of soft radiation in the threshold region (Grooming and/or use of soft-recoil free axis)

(5) Applications in event and jet shape observables

**Thank you**

# Leading order processes in the LAB

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