

GLISSANDO 3: GLauber Initial-State Simulation AND mOre, ver. 3[★]

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Abstract

We present ver. 3 of GLISSANDO, a versatile Monte-Carlo generator for Glauber-like models of the initial stages of ultra-relativistic heavy-ion collisions. The present version incorporates the wounded parton model, which is phenomenologically successful in reproducing multiplicities of particle production at the RHIC and the LHC. Within this model, one can study the nucleon substructure fluctuation effects, recently explored in p-A collisions. In addition, the code includes the possibility of investigating collisions of light nuclei, such as ^3He and ^3H , or the α -clustered $^7,9\text{Be}$, ^{12}C , and ^{16}O , where the deformation of the intrinsic wave function influences the transverse shape of the initial state. The current version, being down-compatible, retains the functionality of the previous releases, such as incorporation of various variants of Glauber-like models, a smooth NN inelasticity profile in the impact parameter obtained from a parametrization of experimental data, fluctuating strength of the entropy deposition, or realistic nuclear distributions of heavy nuclei with deformation. The code can provide output in the format containing the event-by-event source location, which may be further used in modeling the intermediate evolution phase, e.g., with hydrodynamics or transport models. The interface is simplified, such that in the control input file the user may supply only the very basic information, such as the collision energy, the mass numbers of the colliding nuclei, and the model type. GLISSANDO 3 is integrated with the CERN ROOT platform. The package includes numerous illustrative and useful ROOT scripts to compute and plot various results.

Key words: ultra-relativistic nuclear collisions, Monte Carlo generators, wounded quarks and nucleons, α -clusterization, LHC, RHIC, SPS

PROGRAM SUMMARY

Program Title: GLISSANDO 3 ver. 3.42

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Programming language: C++ with the ROOT libraries

Nature of problem: The code implements in a versatile way the Glauber modeling of the initial stages of ultra-relativistic nuclear collisions, including the wounded nucleon and wounded quark models, with possible admixture of binary collisions. A state-of-the art inelastic nucleon-nucleon collision profile is implemented. A statistical distribution of the strength of the sources can be overlaid. The α clustered structure of light nuclei is built in.

Solution method: Monte-Carlo simulation of nuclear collisions, analyzed off-line with numerous ROOT scripts. The software allows for a straightforward event-by-event analysis of eccentricity coefficients and their correlations, size fluctuations, or multiplicity distributions.

Additional comments including Restrictions and Unusual features: The input may consist only of the model type, the mass numbers of the nuclei and the collision energy. The output can also be used as initial conditions for further hydrodynamic studies.

* Supported by Polish National Science Centre, grants 2015/17/B/ST2/00101 (PB), 2015/19/B/ST2/00937 (WB), and 2016/23/B/ST2/00692 (MR)

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1 Introduction

We present an extended version of the package `GLISSANDO` – GLauber Initial-State Simulation AND mOre, previously described in [1] (ver. 1) and [2] (ver. 2), where the user is directed for a more detailed description of the underlying physics and the features which remain unchanged in the present version.

With the on-going efforts to understand the nature of the ultra-relativistic nuclear collisions, more ideas and models are being explored. Consequently, the dedicated open-access software should follow these efforts and supply useful analysis tools. Concerning the earliest stage of such collisions, modeling based on the so-called Glauber approach [3–5] has been commonly used, as it works well phenomenologically.

Another dedicated publicly available code implementing the Glauber approach is the PHOBOS Glauber Monte Carlo [6–8], provided as a `ROOT` package. The Glauber initial condition is also an option in the parameterizations of `TRENTo` code [9]. Many other ultra-relativistic nuclear collision codes, e.g., `HIJING` [10], `AMPT` [11], `URQMD` [12], or `EPOS` [13] use internally the Glauber approach to model the early stage of the collision.

A very successful variant of the Glauber model is based on *wounded quarks* [14–26] acting as the particle production sources, rather than the commonly used *wounded nucleons* [27,28] amended with *binary collisions* [29,30]). Implementation of the wounded quark (or, in general, *wounded parton*) model is the first major extension in `GLISSANDO 3`.

Second, collisions of small nuclei with non-uniform distribution of nucleons may offer further stringent tests of the geometry-flow transmutation mechanism, including the event-by-event fluctuations [13, 31–65]. Moreover, the heavy-light reactions may provide insight into the ground-state clusterization structure in light nuclei, as first proposed in [66,67] and further explored in [68–70]. We thus offer a possibility of simulating reactions with ${}^3\text{He}$ (studied experimentally in [71]) or ${}^3\text{H}$ nuclei, which may be thought of as small triangles, as well as collisions involving light α -clustered nuclei, such as ${}^7,9\text{Be}$ (dumbbell), ${}^{12}\text{C}$ (triangle), and ${}^{16}\text{O}$ (tetrahedron).

The nuclear configurations for ${}^3\text{He}$ and ${}^3\text{H}$ from [72,73], as supplied with the PHOBOS Glauber Monte Carlo input files [7], are used in `GLISSANDO 3` for simulations with $A = 3$ nuclei. Similarly, the user has an option to use the configurations for ${}^{12}\text{C}$ and ${}^{16}\text{O}$ from [72,73] as provided in [7].

The user interface to the code has been greatly simplified. In `GLISSANDO 3`, it suffices to provide the type of the model used (wounded nucleons or wounded

partons), the energy of the collision, and the mass numbers of the colliding nuclei. The appropriate NN inelastic cross section and its profile in the impact parameter are then automatically generated from interpolation formulas based on the experimental pp scattering data. Specifically, we use here the COMPETE model parametrization implemented in the Particle Data Group review [74], which offers statistically the best description on the pp and $p\bar{p}$ scattering data over a very broad range of the collision energies.

As in the previous releases, the output of GLISSANDO 3 is generated in two ways. The key features of the formed initial states are stored in a ROOT tree containing ready to use results in a compact form. In addition, a full event-by-event output can be generated for use in event-by-event studies of further evolution stages, such as hydrodynamics [35, 59, 75–81] or transport.

The new features implemented in GLISSANDO 3 include:

- State-of-the art nucleon-nucleon inelastic cross sections and their impact-parameter profiles.
- Implementation of the wounded quark (in general, wounded parton) model.
- Possibility of colliding ^3He and ^3H , with the distributions from external files.
- Inclusion of α -clustered structure of $^{7,9}\text{Be}$, ^{12}C , and ^{16}O nuclei.
- Possibility of studying the effect of the proton fluctuations in the framework of the wounded parton model.
- Simplified user interface.

The main retained features of the previous releases incorporate:

- Parametrization of distributions of all popular nuclei, in particular those used in the energy - system-size scan of the NA61/SHINE [82].
- Inclusion of the nuclear deformation [83–85].
- Possibility of using externally-generated (correlated) nuclear distributions, e.g., [86, 87] for ^{208}Pb , ^{197}Au or ^{40}Ca .
- Possibility of studying proton-nucleus and deuteron-nucleus collisions.
- Possibility of overlaying weights over the distribution of sources (Poisson, Gamma, negative binomial).
- Study of the core-corona effect [88–91].
- Output of the event-by-event data with location of the sources to a text file, to be used for initialization of hydrodynamics of transport codes.
- A reference manual generated with doxygen [92] may be useful for those who wish to tailor the code.

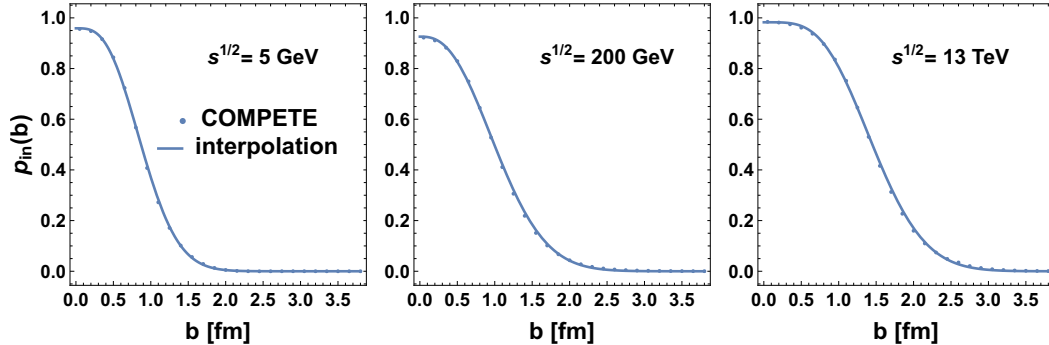


Fig. 1. The inelastic profile plotted as a function of the impact parameter for three sample pp collision energies \sqrt{s} . The points indicate the COMPETE model parametrization, whereas the lines show the interpolation according to Eq. (4).

2 New features in GLISSANDO 3

2.1 Inelastic cross sections and inelasticity profiles

With new measurements of the total, elastic, and differential elastic cross section, in particular at the LHC [93–95] and in cosmic rays [96], new parameterizations of the pp and $p\bar{p}$ scattering amplitudes became available. A standard description is provided by the COMPAS group within the COMPETE model, presented in Sec. 52 of the 2016 edition of the Review of Particle Physics [74], which parametrizes the pp and $p\bar{p}$ scattering data in a very accurate way. In GLISSANDO 3 we use this parameterization of the data as the most complete one.

The inelastic profile function, determining the probability of an inelastic NN collision at impact parameter b and collision energy \sqrt{s} is defined as

$$p_{\text{in}}(b, s) = \sigma_{\text{tot}}(b, s) - \sigma_{\text{el}}(b, s) = 4p_{\text{CM}} \text{Im} h(b, s) - 4p_{\text{CM}}^2 |h(b, s)|^2, \quad (1)$$

where $h(b, s)$ is the Fourier-Bessel transform of the pp elastic scattering amplitude $f(s, -q^2)$,

$$2p_{\text{CM}} h(b, s) = 2 \int_0^\infty q dq J_0(bq) f(s, -q^2), \quad (2)$$

with $p_{\text{CM}} = \sqrt{s/4 - m_N^2}$ denoting the CM momentum of the nucleon. Using the COMPETE model for $f(s, -q^2)$ with parametrization from [74], we thus obtain $\sigma_{\text{in}}(b, s)$. In the code, rather than using these long formulas involving a numerical integration in Eq. (2), we apply a simple parametrization of the inelastic profile of the form [97],

$$p_{\text{in}}(s, b) = G\Gamma\left(\frac{1}{\omega(s)}, \frac{\pi G(s)b^2}{\omega(s)\sigma_{\text{in}}(s)}\right) / \Gamma\left(\frac{1}{\omega(s)}\right), \quad (3)$$

where $\Gamma(a, z)$ denotes the incomplete Euler Γ function, $\sigma_{\text{in}}(s)$ is the inelastic cross section, and $G(s)$ and $\omega(s)$ are suitably adjusted parameters such that the COMPETE results are accurately reproduced. The values obtained from our fit can be efficiently represented with interpolating functions (which we use for $\sqrt{s} \geq 5$ GeV):

$$\begin{aligned} \sigma_{\text{in}}(s) &= [40.32(\sqrt{s}/\text{GeV} + 53.08)^{0.104} - 30.15 - 8.75/(\sqrt{s}/\text{GeV})] \text{ mb}, \quad (4) \\ G(s) &= \frac{33.82 + 1.27(\sqrt{s}/\text{GeV})^{0.85}}{32.10(\sqrt{s}/\text{GeV})^{0.063} + 1.28(\sqrt{s}/\text{GeV})^{0.85} - 10^{-8}}, \\ \omega(s) &= \frac{-3.97 + 4.41(\sqrt{s}/\text{GeV})^{0.24}}{1 + 4.41(\sqrt{s}/\text{GeV})^{0.40} - 0.27(\sqrt{s}/\text{GeV})^{0.24}}. \end{aligned}$$

Note that the applied expressions are for sheer numerical convenience and do not reflect physical mechanisms of high-energy pp scattering.

The quality of the interpolating formulas is illustrated in Fig. 1, where we compare the inelastic profile functions from the COMPETE model to Eq. (3) with parameters (4) for three selected collision energies. In the left panel of Fig. 2 we show the results of the COMPETE model for the total inelastic pp cross section $\sigma_{\text{in}}(s)$ (solid line) and our simple fit of Eq. (4). We also show (dotted line) the parametrization $A + B \ln^2(s/\text{GeV}^2)$, with $A = 25$ mb and $B = 0.146$ mb, used in [8]. We note that whereas at higher collision energies ($\sqrt{s} > 100$ GeV) this parametrization agrees with the COMPETE model (and thus with the data) accurately, for $\sqrt{s} < 100$ GeV the COMPETE parametrization, or our Eq. (4), is clearly advantageous. The interpolated dependence of parameters G and ω on the collision energy, as given by formulas (4), is displayed in the right panel Fig. 2.

We recall that the use of a realistic NN inelasticity profile (as opposed to sometimes used hard-sphere profile in older software, e.g., [10]) is phenomenologically important. First, it leads to proper elastic differential cross section in pp collisions, as shown above. Second, it yields sizable effects in standard observables in ultra-relativistic nuclear collisions. In particular, the effect on ellipticity of the fireball was discussed in detail in [98], where the use of a realistic (smooth) wounding profile led to a significant (10-20%) reduction for peripheral A-A collisions, compared to the case with a hard-sphere profile.

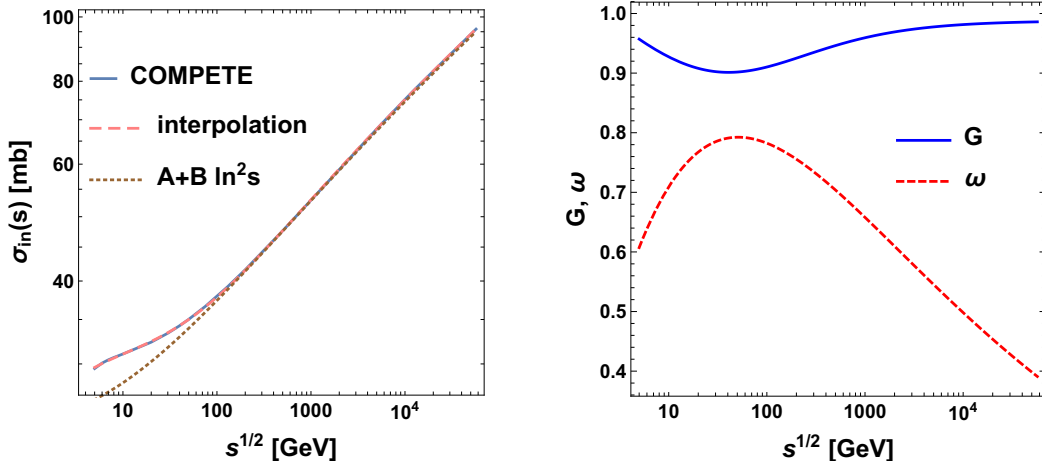


Fig. 2. The inelastic pp cross section (left) and parameters G and ω (right), plotted as functions of the collision energy. See the text for discussion.

2.2 Wounded partons

In the wounded quark model [14–17] the valence quarks play the role of elementary scatterers. The approach is implemented in `GLISSANDO 3`, as it has proved to be phenomenologically successful in describing the multiplicity of produced hadrons in a variety of reactions, with the linear scaling

$$\frac{dN_{\text{ch}}}{d\eta} \sim Q_{\text{W}} \quad (5)$$

well satisfied. Here N_{ch} denotes the observed charged hadrons, and Q_{W} the number of wounded quarks in a given reaction and centrality class. It was first noticed that the RHIC data follow the scaling [18], further explored at RHIC by the PHENIX Collaboration [20,21], as well as at the SPS [19]. See also [7, 20–26] for further developments.

Our implementation of the model is described in detail in [23]. The nucleon consists of p partons ($p = 3$ for the wounded quark model) distributed according to a radial density

$$\rho(r) = \text{const } r^2 \exp \left[-\sqrt{\frac{2}{3}} \left(1 - \frac{1}{p}\right) \frac{r}{r_0(s; p)} \right]. \quad (6)$$

The scale parameter $r_0(s; p)$ controls the size of the nucleon built of partons. The factor $1 - 1/p$ accounts for the center-of-mass corrections; a shift to the center of mass of the nucleon is carried out after randomly generating the positions of the centers of the partons. As r_0 is adjusted phenomenologically (see the following), the presence of the $1 - \frac{1}{p}$ factor in formula (6) is conventional.

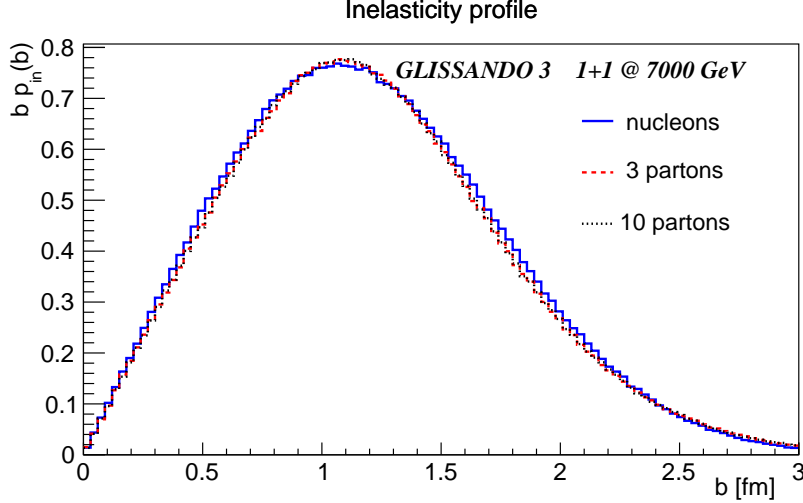


Fig. 3. The inelastic NN profiles (multiplied with b) obtained in the wounded nucleon and the wounded parton model for $p = 3$ and $p = 10$ (generated with script `inel_prof.C`).

In the wounded parton approach one needs to choose the parton-parton inelasticity profile. We take it in the Gaussian form

$$p_{\text{in}}^{qq}(s, b) = \exp \left[-\frac{\pi b^2}{\sigma_{\text{in}}^{qq}(s; p)} \right], \quad (7)$$

where $\sigma_{\text{in}}^{qq}(s)$ is the parton-parton inelastic cross section.

Thus our wounded parton model implementation brings in two parameters: $r_0(s; p)$ and $\sigma_{\text{in}}^{qq}(s; p)$. Their values are chosen in such a way that the resulting NN collision profile reproduces the COMPETE parametrization discussed in Sec. 2.1. In other words, we impose the desired feature that the NN inelasticity profile is the same if one uses nucleons or partons as elementary scatterers. With our chosen parameterizations of Eq. (6) and (7) this cannot be accomplished in an exact manner, but optimization leads to a close agreement (within a few percent). This can be seen in Fig. 3, where we compare the NN elasticity profiles (multiplied with b) obtained in the nucleon and parton models for $\sqrt{s} = 7$ TeV. The quality of agreement is similar at other collision energies or values of p .

The optimum values of the wounded parton model parameters are interpolated as follows for the parton-parton cross section and the parton distribution parameter:

$$\begin{aligned} \sigma_{\text{in}}^{qq}(s; p) &= [A_1 + A_2(\sqrt{s}/\text{GeV})^{A_3} + A_4/(\sqrt{s}/\text{GeV})] \text{ mb}, \\ A_1 &= -1.66 + 8.73/p + 0.11p, \quad A_2 = -1.58 + 9.03/p + 0.08p, \\ A_3 &= 0.22 - 0.07/p + 0.01p, \quad A_4 = -1.02 + 23.10/p - 0.05p, \end{aligned} \quad (8)$$

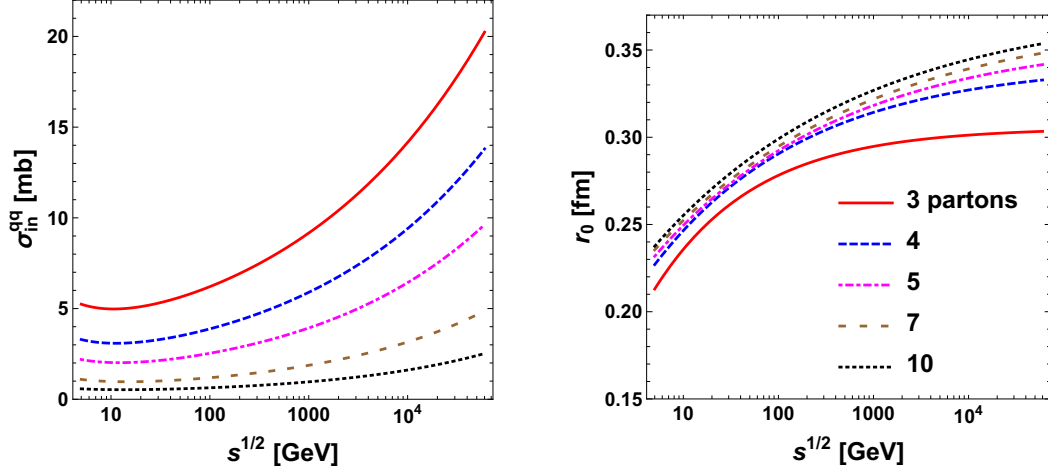


Fig. 4. The dependence of the inelastic parton-parton cross section (left) and the parton size distribution parameter r_0 (right) on the collision energy.

$$\begin{aligned}
 r_0(s; p) &= [B_1 + B_2(\sqrt{s}/\text{GeV})^{B_3}] \text{ fm}, \\
 B_1 &= 0.37 - 0.95/p^2 + 0.11, \quad B_2 = -0.21 - 0.39/p^2 + 0.22/p, \\
 B_3 &= -0.28 - 5.21/p^2 + 1.36p.
 \end{aligned}
 \tag{9}$$

The above parameterizations work for $3 \leq p \leq 10$. The dependence of $\sigma_{\text{in}}^{qq}(s; p)$ and $r_0(s; p)$ on \sqrt{s} is visualized in Fig. 4. We note that in our model the parton-parton cross section decreases with p , whereas the dependence of the size parameter r_0 exhibits a rather weak growth with p . We also note that an approximate scaling $\sigma_{\text{in}}^{qq}(s; p) \sim 1/p^2$ holds, which is accurate to a few percent for $p > 3$.

As in previous releases of our code, centers of nucleons in a nucleus are distributed according to a Woods-Saxon density with additional NN repulsion [1], or are taken from external calculations, *e.g.*, [86] of [7]. Nuclear shape deformation [83, 84, 99, 100] is implemented for deformed nuclei, such as ^{63}Cu , ^{197}Au , or ^{238}U , in the same manner as in GLISSANDO 2.

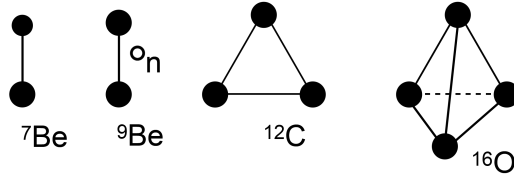


Fig. 5. Cartoon of the geometry of light clustered nuclei (from [69]). The bigger filled blobs represent the α cluster, the smaller filled blob the ^3He cluster, and the empty blob the extra neutron in ^9Be .

Table 1

Parameters of the distribution of light clustered nuclei used in GLISSANDO 3.

Nucleus	l [fm]	r_α [fm]	$r_{3\text{He}}$ [fm]	r_n [fm]
${}^7\text{Be}$	3.2	1.2	1.4	-
${}^9\text{Be}$	3.6	1.1	-	1.9
${}^{12}\text{C}$	2.8	1.1	-	-
${}^{16}\text{O}$	3.2	1.1	-	-

2.3 Reactions with light clustered nuclei

GLISSANDO 3 offers a possibility to collide nuclei whose structure exhibits clustering. Specifically, we implement ${}^7\text{Be}$ as $\alpha+{}^3\text{He}$, ${}^9\text{Be}$ as $2\alpha+\text{neutron}$, ${}^{12}\text{C}$ as 3α , and ${}^{16}\text{O}$ as 4α (see Fig. 5). The details of our fixing of geometric parameters of the distributions are presented in [69]. The parameters are adjusted in such way that the one-body nuclear distributions [72, 73] are matched. We first arrange the positions of clusters as in Fig. 5, separating the centers by the distance l . The distribution of the centers of nucleons in each cluster is randomly generated according to a Gaussian

$$f_i(\vec{r}) = \text{const} \exp\left(-\frac{3}{2} \frac{(\vec{r} - \vec{c}_i)^2}{r_c^2}\right), \quad (10)$$

where \vec{r} denotes the coordinate of the nucleon and \vec{c}_i is the position of the center of the cluster i . The width of the cluster is controlled with r_c , the rms radius of the cluster. Then the positions of the nucleons are generated sequentially, switching between clusters 1, 2, ..., 1, 2, ..., until all the needed nucleons are placed.

For the case of ${}^9\text{Be}$ we place the extra neutron on top of the two α clusters. The distribution is

$$f_n(\vec{r}) = \text{const} r^2 \exp\left(-\frac{3}{2} \frac{r^2}{r_n^2}\right), \quad (11)$$

and it exhibits a hole in the middle.

The values of parameters used in the code for the cluster model are collected in Table 1.

One may do many physical studies with light clustered nuclei, in particular looking for clusterization signatures in harmonic flow patterns [66, 67, 69, 101]. In Fig. 6 we present an example of a quantity, the symmetric cumulant of

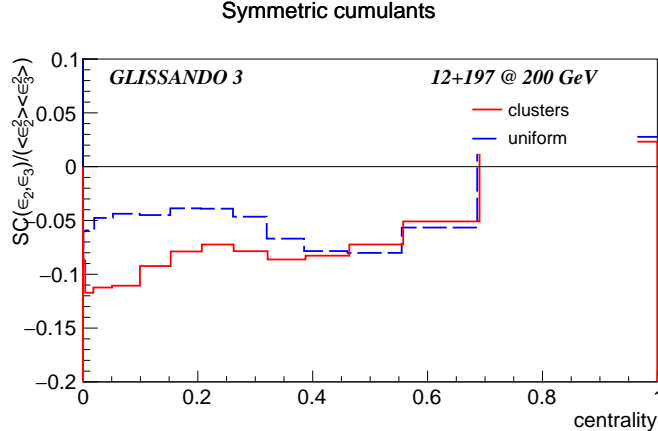


Fig. 6. The scaled symmetric cumulant of eccentricities in collisions of clustered and uniform ^{12}C nucleus with ^{197}Au . The symmetric cumulant is defined as $SC(a, b) = \langle a^2 b^2 \rangle - \langle a^2 \rangle \langle b^2 \rangle$ (generated with script `sc_comp.C`).

elliptic and triangular flows, which displays different behavior on the model with clusters compared to the case without clusters (uniform).

2.4 Smearing of sources

The Monte Carlo Glauber model provides, event-by event, the positions of point-like sources (wounded objects) in the transverse plane. Physically, the sources must have transverse size, which is accomplished by *smoothing* them, typically with a Gaussian form

$$\Delta(x, y; x_i, y_i) = \frac{1}{\pi\sigma^2} \exp \left[-\frac{(x - x_i)^2 + (y - y_i)^2}{\sigma^2} \right], \quad (12)$$

where (x, y) are the transverse coordinates and (x_i, y_i) gives the location of the i th source, and σ is the smearing width. Smearing is necessary, *i.a.*, in forming the initial condition for subsequent hydrodynamic evolution. Moreover, smearing increases the size of the fireball and reduces the eccentricities, which are its basic characteristics. The effect is particularly relevant for small systems. The effects of Gaussian smearing (12) are simple to implement, as the corresponding expressions are analytic.

The eccentricity of rank n ($n \geq 2$) in a given event, ϵ_n , and the corresponding angle of the principal axis (the event-plane angle), Ψ_n , are defined in the standard way as

$$\epsilon_n e^{i\Psi_n} \equiv -\frac{\int dx dy s(x, y) \rho^n e^{in\phi}}{\int dx dy s(x, y) \rho^n}, \quad (13)$$

where $s(x, y)$ is the transverse entropy distribution, and we have introduced the polar coordinates via $x = \rho \cos \phi$, $y = \rho \sin \phi$. When the sources are point-like, then $s(x, y) = \sum_i \delta(x - x_i) \delta(y - y_i)$ and

$$\epsilon_n e^{i\Psi_n} = -\frac{\sum_i \rho_i^n e^{in\phi_i}}{\sum_i \rho_i^n}, \quad (14)$$

where i runs over all the sources in the event, and $x_i = \rho_i \cos \phi_i$, $y_i = \rho_i \sin \phi_i$. With Gaussian smearing (12), we have $s(x, y) = \sum_i \Delta(x, y; x_i, y_i)$ and, correspondingly,

$$\epsilon_n e^{i\Psi_n} = -\frac{\sum_i N_i^{(n)}}{\sum_i D_i^{(n)}}, \quad (15)$$

$$N_i^{(n)} = \int dx dy \Delta(x, y; x_i, y_i) \rho^n e^{in\phi}, \quad D_i^{(n)} = \int dx dy \Delta(x, y; x_i, y_i) \rho^n.$$

In polar coordinates we may write explicitly

$$N_i^{(n)} = \frac{1}{\pi\sigma} \int \rho d\rho \int d\phi \exp\left(-\frac{\rho^2 + \rho_i^2 - 2\rho\rho_i \cos(\phi - \phi_i)}{\sigma^2}\right) \rho^n e^{in(\phi - \phi_i)} e^{in\phi_i}. \quad (16)$$

Integration over ϕ yields

$$N_i^{(n)} = \frac{2}{\sigma^2} \int \rho d\rho \rho^{n+1} e^{-\frac{\rho^2 + \rho_i^2}{\sigma^2}} I_n\left(\frac{2\rho\rho_i}{\sigma^2}\right) e^{in\phi_i}, \quad (17)$$

and integration over ρ

$$N_i^{(n)} = \rho_i^n e^{in\phi_i}, \quad (18)$$

which means that the numerator with smearing in Eq. (16) is exactly the same as for point-like sources in Eq. (14).

Repeating the above steps for the denominator yields

$$\begin{aligned}
D_i^{(n)} &= \frac{1}{\pi\sigma} \int \rho d\rho \int d\phi \exp\left(-\frac{\rho^2 + \rho_i^2 - 2\rho\rho_i \cos(\phi - \phi_i)}{\sigma^2}\right) \rho^n \\
&= \frac{2}{\sigma^2} \int \rho d\rho \rho^{n+1} e^{-\frac{\rho^2 + \rho_i^2}{\sigma^2}} I_0\left(\frac{2\rho\rho_i}{\sigma^2}\right) = \sigma^n \Gamma\left(\frac{n}{2} + 1\right) L_{\frac{n}{2}}\left(-\frac{\rho_i^2}{\sigma^2}\right),
\end{aligned} \tag{19}$$

where $\Gamma(z)$ is the Euler Gamma function and $L_a(z)$ is the Laguerre polynomial. The forms of $D_i^{(n)}$ for the first few even values of n are

$$\begin{aligned}
D_i^{(2)} &= \rho_i^2 + \sigma^2, \\
D_i^{(4)} &= \rho^4 + 4\rho_i^2\sigma^2 + 2\sigma^4, \\
D_i^{(6)} &= \rho_i^6 + 9\rho_i^4\sigma^2 + 18\rho_i^2\sigma^4 + 6\sigma^6, \\
&\dots
\end{aligned} \tag{20}$$

For odd values of n

$$\begin{aligned}
D_i^{(3)} &= \frac{1}{4\sigma} \sqrt{\pi} e^{-\frac{\rho_i^2}{2\sigma^2}} \left[2\rho_i^2 (\rho_i^2 + 2\sigma^2) I_1\left(\frac{\rho_i^2}{2\sigma^2}\right) \right. \\
&\quad \left. + (2\rho_i^4 + 6\rho_i^2\sigma^2 + 3\sigma^4) I_0\left(\frac{\rho_i^2}{2\sigma^2}\right) \right], \\
D_i^{(5)} &= \frac{1}{8\sigma} \sqrt{\pi} e^{-\frac{\rho_i^2}{2\sigma^2}} \left[\rho_i^2 (4\rho_i^4 + 24\rho_i^2\sigma^2 + 23\sigma^4) I_1\left(\frac{\rho_i^2}{2\sigma^2}\right) \right. \\
&\quad \left. + (4\rho_i^6 + 28\rho_i^4\sigma^2 + 45\rho_i^2\sigma^4 + 15\sigma^6) I_0\left(\frac{\rho_i^2}{2\sigma^2}\right) \right], \\
&\dots
\end{aligned} \tag{21}$$

where $I_{0,1}(z)$ are the modified Bessel functions of the first kind. It is apparent from the above formulas that smearing increases the denominators, therefore ϵ_n is quenched, in agreement with intuition. At the same time we observe that the principal axes angles Ψ_n are not altered by smearing.

The reduction of the contribution of a single source placed at ρ_i for first few eccentricities, quantified with $\rho_i^2/D_i^{(n)}$, is shown in Fig. 7. We note that, as expected, the effect increases with n and with the value of the smearing parameter σ .

Taking for definiteness the ellipticity ($n = 2$) and collecting the contributions from all sources, we find the smearing reduction factor $\langle r^2 \rangle / (\langle r^2 \rangle + \sigma^2)$, which becomes increasingly important with decreasing mean squared radius, $\langle r^2 \rangle$, of the fireball.

Smearing is incorporated in GLISSANDO 3 in the evaluation of eccentricities

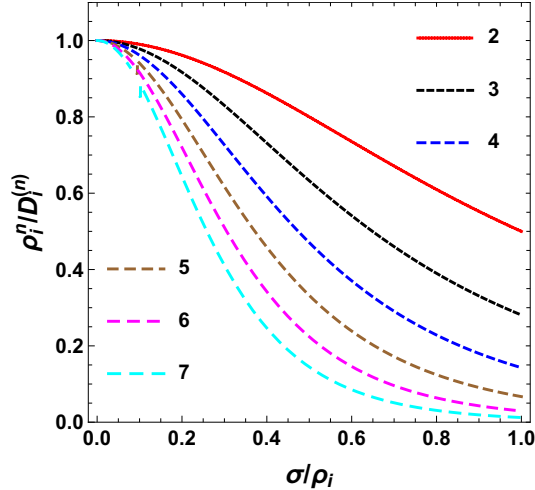


Fig. 7. The reduction of the contribution to eccentricities ϵ_n from a source placed at ρ_i , plotted versus σ/ρ_i for $n = 2, 3, \dots, 7$.

and the mean squared radius of the fireball. The amount of smearing is controlled with the parameter $DS = \sigma/2$, whereby it has the interpretation of the Gaussian width in one dimension.

2.5 Rapidity modeling

The modeling in rapidity, present to some extent in ver. 2 of the code, has been removed. This is because, unlike the modeling in the transverse plane where the Glauber approach became one of the standards, the longitudinal modeling has much more freedom and is under development. If the user wishes to model the rapidity dependence of the fireball, she/he may use the transverse distributions (generated event-by-event and written to an output file) in an external application.

3 Installation and running

The user must first install the CERN ROOT package [102]. After downloading and unpacking GLISSANDO 3, the command

```
make
```

should be run, which creates the executable binary `glissando3`.

To optionally recreate the `doxygen` manual (provided as `/doc/latex/refman.pdf` with the distribution), the `doxygen` [92] package should be installed and the

following commands executed:

```
make cleandoc
make doc
```

With the code installed, the user may look at an instructive presentation of the main features of the present version by executing the shell script

```
./demo_ver_3.sh
```

To see the created pdf files `evince` should be installed prior to the run. To use another pdf viewer, the line `VIEW=evince` should be edited in the `*.sh` files. The features of ver. 2, retained in the present release, may be explored by executing

```
./demo_ver_2.sh
```

For collisions of two nuclei, the standard running command has the syntax

```
./glissando3 [input_file] [output_file]
```

where the nuclei can be any, including the proton and the deuteron. When the input or output arguments are absent, the defaults are

```
input.dat - default input
glissando.root - default output
```

The input parameters with their defaults are collected in Appendix A.

3.1 Makefile

The `Makefile` contains commands for compilation and linking. It can be used for profiling the code by modifying the preprocessor options. Most importantly, the user should decide if she/he uses the wounded nucleon or the wounded parton version of the model. In the nucleon case the standard preprocessor options should read

```
PREPROCESS := -D_partons=0 -D_nnwp=2
             -D_bindep=1 -D_files=0 -D_profile=0 -D_weight=0 -D_evout=0
             -D_clusters=0 -D_uncluster=0 -D_pardis=0 -D_rdsconv=1
```

whereas for the wounded parton model

```
PREPROCESS := -D_partons=1 -D_nnwp=1
             -D_bindep=1 -D_files=0 -D_profile=0 -D_weight=0 -D_evout=0
             -D_clusters=0 -D_uncluster=0 -D_pardis=0 -D_rdsconv=1
```

The meaning of all preprocessor parameters is as follows:

```
_nnwp_0 - hard-sphere NN wounding profile, =1 - Gaussian, =2 - gamma
_bindep_1 - binary and wounding depend on each other, =0 - do not
_files_1 - read the nuclear distributions from external files,
          =0 - generate randomly
_profile_1 - generate the nucleon profile and NN correlation data, =0 - do not
_weight_1 - generate data for the NN collision profiles
           and for the weight (RDS) distributions, 0 - do not
_evout_0 - do not generate the text event data, =1 - short, =2 -long
_clusters_1 - generate clusters in light nuclei, =0 do not
_uncluster_1 - smoothe out the alpha clusters in nucleus A,
              =2 - in nucleus B,
              =3 in both nuclei,
              =0 - do not smoothe
_partons_1 - wounded parton model, =0 - wounded nucleon model
_pardis_0 - exponential parton distribution in nucleus, =1 - Gaussian
_rdsconv_2 - convention for RDS: 1 -  $Nw/2$ , 2 -  $Nw$ 
```

The user may modify the Makefile file to suit his needs, or, alternatively, run `make` for example as follows:

```
make 'PREPROCESS = -D_partons_1 -D_nnwp_1 -D_evout_1 '
```

to produce the binary code for the wounded parton model with the Gaussian wounding profile and with generation of some results to an external ASCII file.

Another functionality is the storage of the current version of the package,

```
make package
```

as well as the cleaning options:

```
make clean
make cleandoc
make cleanoutput
```

3.2 *Input*

The input file is a standard ASCII file. Every line contains the name of the parameter separated with space from the assigned value. The sequence of the lines with parameters is flexible. When a parameter is missing in the input file, or a line containing it is commented out with `#`, the default value is used. See Appendix A for details concerning the input parameters.

3.3 Output

A typical output from a run of `GLISSANDO 3` to the console is shown in Table 2.

The results of the simulation are stored in the `ROOT` output file or, optionally, also in text files when the preprocessor parameter `_evout_=1` or `2` is used.

To see the physical results, the user should enter the `ROOT` environment

```
root
```

and execute one of the supplied scripts `*.C`

```
.x macro/demo_3/<script name>.C(<optional parameters>)
```

or directly examine the output `ROOT` file, e.g. with a

```
TBrowser a
```

command (executed within `ROOT` environment). An alternative method of executing the `ROOT` scripts is provided in the example shell `demo_ver_3.sh`. Proceeding this way does not require a greater familiarity with `ROOT`.

The preprocessor option `_evout_` controls the possible event-by-event output to an additional external ASCII file with the name of the `ROOT` output file appended with `.points`. If `_evout_=2`, then the file stores the transverse positions event-by-event. Its content consists of the blocks

```
RDS   NwAB   specA   atan2(ycmA,xcmA)   specB   atan2(ycmB,xcmB)
```

followed with `NwAB` lines of the format

```
x   y   z   c   w
```

The second part of the block is

```
Nbin
```

followed with `Nbin` lines of the format

```
x   y   z   c   w
```

Above we use the notation `RDS` for the relative deposited strength in the event (defined below), `NwAB` for the number of wounded objects (nucleons or partons), `specA` for the number of spectators from nucleus A and `atan2(ycmA,xcmA)` for the azimuthal angle of their center of mass relative to the x axis, and `specB` and `atan2(ycmB,xcmB)` for analogous quantities for nucleus B, and `Nbin` for

the number of binary collisions. Next, x and y are the transverse coordinates of the sources in fm, z is the longitudinal coordinate, $|c|$ indicates how many times a wounded nucleon collided, with positive (negative) c corresponding to nucleus A (B), while $c=0$ indicates the binary collisions. The last entry is the weight w of the given source (by *source* we customarily mean a wounded nucleon or a binary collision). The number of blocks is equals to the number of events.

If `_evout_=1`, then a simplified output is generated, with the format

```
NwA  NwB  Nbin  RDS
```

where `NwA` and `NwB` are the numbers of wounded objects in nuclei A and B, respectively. The number of output lines equals to the number of events.

The *relative deposited strength* (term introduced in [1]) is equal to

$$\text{RDS} = \frac{1 - \alpha}{2} \text{NwAB} + \alpha \text{Nbin}, \quad (22)$$

in accordance to the Glauber model with the binary collision admixture [29, 30]. Correspondingly, the weight of a given source is $(1 - \alpha)/2$ for the wounded objects and α for the binary collisions.

3.4 Reading external nuclear distributions

The user may provide external files with nuclear distributions. We have used two sets of such files. The first one comes from Alvioli et al. [86] for the case of ^{16}O , ^{40}Ca , and ^{208}Pb . They can be obtained from <http://sites.psu.edu/color/>. The user must create from the downloaded files a single file, for instance running

```
cat ca40-1.dat ca40-2.dat ca40-3.dat [more files] > ca40.dat
```

The resulting file `o16.dat` should be placed in the relative subdirectory `nucl`.

The files have the format

```
x  y  z  k
```

where x , y , and z denote the Cartesian coordinates of the centers on nucleons in fm, while $k = 0$ for neutrons and $k = 1$ for protons. Groups of `A` lines, where `A` is the mass number of the nucleus, correspond to a single nuclear configuration.

The second case concerns ^3He or ^3H distributions, which are taken from the Green's function Monte Carlo simulations [103] as provided in [7]. For the user's convenience the files `he3_plaintext.dat` and `h3_plaintext.dat` are also provided at the GLISSANDO web site. The format of these files is

```
x1  y1  z1  x2  y2  z2  x3  y3  z3  foo  foo  foo  foo
```

where (x_i, y_i, z_i) are the Cartesian coordinates of the i th nucleon in a given configuration.

Similarly, the configurations of ^{12}C or ^{16}O from [103] as provided in [7] may be used. They are provided at the GLISSANDO web site as `carbon_plaintext.dat` and `oxygen_plaintext.dat`.

To use the nuclear configurations from external files, the code must be compiled with

```
make 'PREPROCESS = -D_files_=1'
```

and executed as

```
./glissando3 [input_file] [output_file] [nucleus_A_file] [nucleus_B_file]
```

When the syntax

```
./glissando3 [input_file] [output_file] [nucleus_A_file]
```

is used, then the distribution of the nucleons in nucleus A is read from an external file, whereas for nucleus B the positions of nucleons are generated randomly. This syntax must also be used for the collisions of nucleus A with the proton or the deuteron.

3.5 *Fixing centrality cuts*

We explain how to impose centrality cuts on GLISSANDO 3 simulations and how to properly choose the range for the impact parameter b (a too large range slows down the simulations). The supplied shell script `centrality.sh` implements the following procedure. First, a minimum-bias simulation must be run, with no (or broad-range) values for the `W0`, `W1`, `RDS0`, and `RDS1` parameters, as well as `BMIN=0` and `BMAX` set to a larger value than the sum of the radii of the two colliding nuclei. We typically use `BMAX` as about twice this sum to account for the tails in the Woods-Saxon distributions. Note, however, that large values for `BMAX` lead to a larger Monte Carlo rejection rate, slowing down the simulation. Next, the `macro/demo_3/cent.C` script should be executed in root. The values of `W0`, `W1`, or `RDS0`, `RDS1` corresponding to the desired centrality

classes can be read off from the generated file `output/centrality.dat`. Next, the input file must be modified with the proper values for `W0`, `W1` supplied (if centrality is determined by the multiplicity of the wounded objects), or `RDS0`, `RDS1` (if centrality is given by the relative deposited strength RDS), and the code must be rerun (with low statistics). Running `/macro/demo_3/b_dist.C` and looking at the plot `b_dist.pdf` allows us to determine the optimum values for `BMIN=0` and `BMAX`. We thus should update these parameters in the input file and rerun simulations with full statistics.

The above steps can be simply traced by executing `centrality.sh`.

4 Structure of the code

The structure of the code is provided in the supplied reference manual created with `doxygen`.

5 Summary

We have presented `GLISSANDO 3`, with hopes it will continue to be a useful and versatile tool for the heavy-ion community. The authors most welcome suggestions and questions from the users.

We would like to thank dr Maksym Deliyergiyev for his help to make our scripts compatible with `ROOT6`.

This research was carried out in laboratories created under the project "Development of research base of specialized laboratories of public universities in Swietokrzyskie region" no POIG 02.2.00-26-023/08 dated May 19, 2009.

A Input and output

The input parameters are collected in Table A.1. The hash sign `#` at the beginning of the line in the input file comments it out, in which case a default value of the parameter as set in the code (file `functions.h`) is used.

Table A.1: Parameters in the input file.

name	default	description
ECM	-1	center of mass energy of the colliding system [GeV]
NUMA	208	mass number of nucleus A
NUMB	208	mass number of nucleus B
EVENTS	10000	number of generated events
BMIN	0.	minimum impact parameter [fm]
BMAX	25.	maximum impact parameter [fm]
W0	2	minimum allowed number of wounded nucleons
W1	100000	maximum allowed number of wounded nucleons
RDS0	0	minimum allowed RDS
RDS1	100000	maximum allowed RDS
MODEL	0	0 - constant superimposed weight, 1 - Poisson, 2 - Gamma, 3 - Negative Binomial
Uw	1.	Poisson, Gamma, or Negative Binomial mean value for wounded objects
Ubin	1.	Poisson, Gamma, or Negative Binomial mean value for binary collisions
Vw	2.	Gamma or Negative Binomial variance for wounded objects
Vbin	2.	Gamma or Negative Binomial variance for binary collisions
NCS	3	number of partons in the nucleon
NBIN	40	number of bins for histograms in ρ , x , or y
RWSA	-1	Woods-Saxon radius for the distribution of centers, nucleus A [fm]
AWSA	0.459	Woods-Saxon width, nucleus A [fm]
BETA2A	-1	deformation parameter β_2 , nucleus A
BETA4A	-1	deformation parameter β_4 , nucleus A
ROTA.THETA	-1	rotation parameter (angle θ), -1 - random rotation, nucleus A
ROTA.PHI	-1	rotation parameter (angle ϕ), -1 - random rotation, nucleus A
RWSB	-1	Woods-Saxon radius for the distribution of centers, nucleus B [fm]
AWSB	0.459	Woods-Saxon width, nucleus B [fm]
BETA2B	-1	deformation parameter β_2 , nucleus B
BETA4B	-1	deformation parameter β_4 , nucleus B
ROTB.THETA	-1	rotation parameter (angle θ), -1 - random rotation, nucleus B
ROTB.PHI	-1	rotation parameter (angle ϕ), -1 - random rotation, nucleus B
SNN	-1	NN (parton-parton) "wounding" cross section [mb]
SBIN	-1	NN (parton-parton) binary cross section [mb]
ALPHA	0.12	mixed model parameter, 0 - wounded, 1 - binary, 0.12 - LHC@2.76 TeV/nucleon
CD	0.9	closest allowed distance between centers of nucleons [fm]
ISEED	0	seed for the random number generator, if 0 a random seed is generated

Continued on Next Page...

Table A.1 – Continued

name	default	description
BTOT		range parameter for histograms [fm], default= $\max(\text{RWSA}, \text{RWSB}) + \text{AWSA} + \text{AWSB}$
SHIFT	1	1 - shift the coordinates of the fireball to the c.m. in the fixed-axes case, 0 - do not shift
DW	0.	dispersion of the location of the source for wounded objects [fm]
DBIN	0.	dispersion of the location of the source for binary collisions [fm]
WFA	0	the w parameter of the Fermi distribution, nucleus <i>A</i>
WFB	0	the w parameter of the Fermi distribution, nucleus <i>B</i>
FBIN	72	number of bins for histograms in the azimuthal angle
DOBIN	0	1 - compute the binary collisions also for the case ALPHA=0, 0 - do not
GA	1.0	central value of the Gaussian wounding profile
PP	-1	power of the transverse radius in the Fourier moments
RO	0	rank of the rotation axes (0 - rotation rank = rank of the Fourier moment)
RCHA	5.66	harmonic oscillator shell model density mean squared charge radii of nucleus <i>A</i> (^{12}C -nucleus)
RCHB	5.66	harmonic oscillator shell model density mean squared charge radii of nucleus <i>B</i> (^{12}C -nucleus)
RCHP	0.7714	harmonic oscillator shell model density mean squared charge radii of proton
OMEGA	-1	relative variance of cross-section fluctuations for the Gamma wounding profile
GAMA	-1	central value of the Gamma wounding profile
SCALEA	1.	scale parameter for the size of the nucleus (cluster version) [fm]
SIGMAA	1.	standard deviation of x, y, z coordinates of nucleons in the alpha cluster [fm]
SIGMABISA	1.	standard deviation of x, y, z coordinates of nucleons in the ^3He cluster or nucleon no. 9 [fm]
SCALEB	1.	scale parameter for the size of the nucleus (cluster version) [fm]
SIGMAB	1.	standard deviation of x, y, z coordinates of nucleons in the alpha cluster [fm]
SIGMABISB	1.	standard deviation of x, y, z coordinates of nucleons in the ^3He cluster or nucleon no. 9 [fm]
QSCALE	-1	scale parameter in the parton distribution function [fm]
DS	-1	source smearing parameter

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Table 2

A typical output to the console from GLISSANDO3.

user@host: ~/GL3\$./glissando3

Start: Mon Nov 12 15:36:16 2018

```
-----
*****
GLISSANDO 3 ver. 3.3
ver. 3: http://arxiv.org.abs/1901.04484
ver. 2: Computer Physics Communications 185 (2014) 1759, arXiv:1310.5475
ver. 1: Computer Physics Communications 180 (2009) 69, arXiv:0710.5731
*****
Simulation of nuclear collisions in Glauber models
-----
parameters reset from default in input/input.dat:
EVENTS 2000
NUMA 208
NUMB 208
ECM 2760

generates ROOT output file output/glissando.root

number of events: 2000

208+208 @ sqrt(s_NN)=2760GeV

Woods-Saxon: RA=6.40677fm, aA=0.459fm, dA=0.9fm
Woods-Saxon: RB=6.40677fm, aB=0.459fm, dB=0.9fm

NUCLEON MODEL
mixed model: sig_w=61.9917mb, sig_bin=61.9917mb, alpha=0.12
RDS distribution scale with u=1 (wounded) and u=1 (binary)
gamma wounding profile, G=0.972569, omega=0.586854
source smearing width: 0.4 fm
acceptance window: b_min=0fm, b_max=25fm, Nw_min=2, Nw_max=100000

event: 2000      (100%)

Some quantities for the specified acceptance window
(+/- gives the e-by-e standard deviation):
A+B cross section = 7226.7mb (makes sense for min. bias)
efficiency (accepted/all) = 36.8053%
N_w = 113.994+/-114.84
RDS: 93.5426+/-107.285

Finish: Mon Nov 12 15:37:04 2018
(0h:0m:48s)
*****
```