

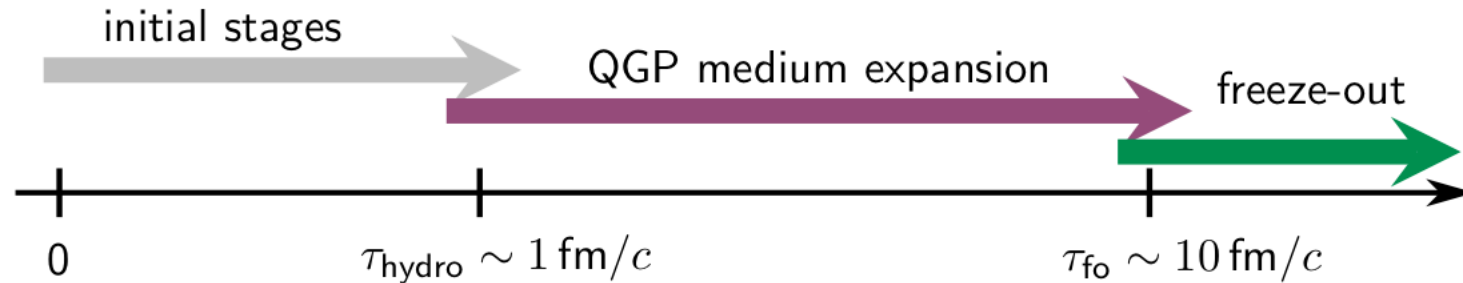


Challenges and opportunities in flow studies

Jiangyong Jia

- Introduction
- Challenges
- Opportunities

Dynamics and properties of QGP



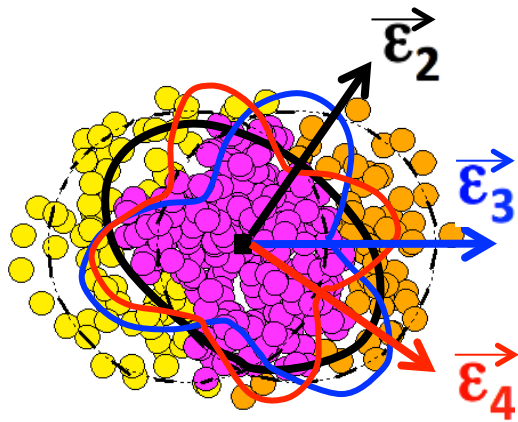
Challenge: simultaneous determination of two unknowns

Dynamics \longleftrightarrow Properties

- Properties drives the dynamics of the medium
- Extraction of properties require good knowledge of dynamics

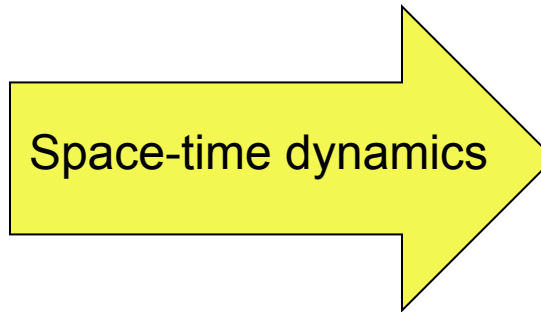
Connecting the initial state and final state

Initial state

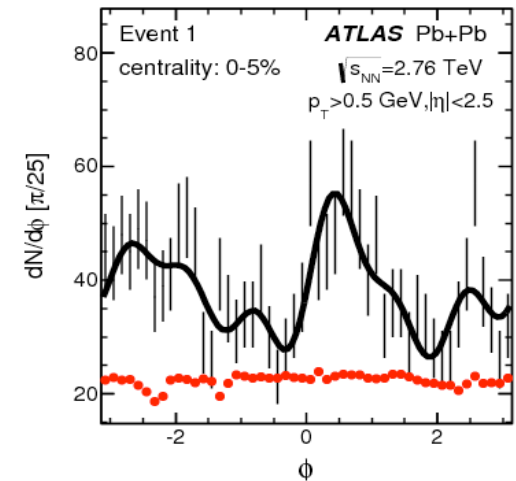


$$\vec{\epsilon}_n \equiv \epsilon_n e^{in\Phi_n^*} \equiv -\frac{\langle r^n e^{in\phi} \rangle}{\langle r^n \rangle}$$

Hydro-response



Particle flow

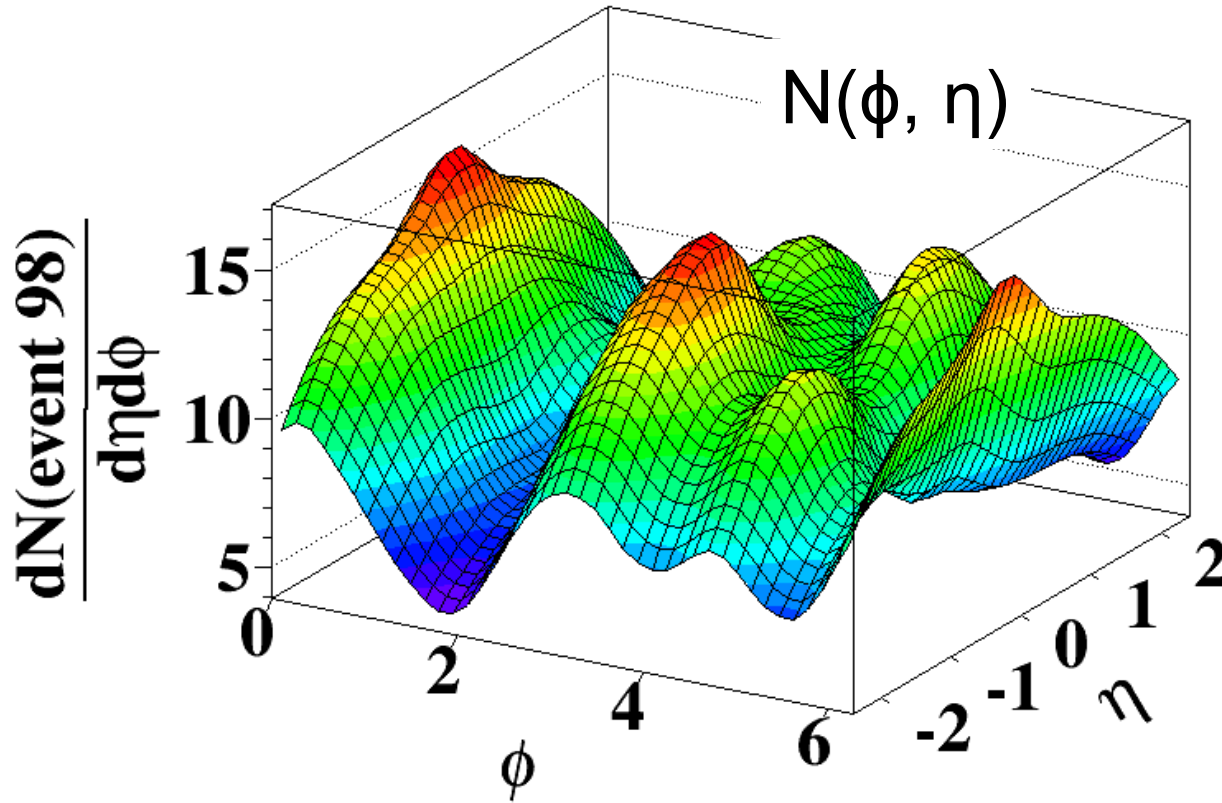


$$\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n \cos n(\phi - \Phi_n)$$

Perturbing the system with different initial state fluctuations

Richness of flow fluctuations

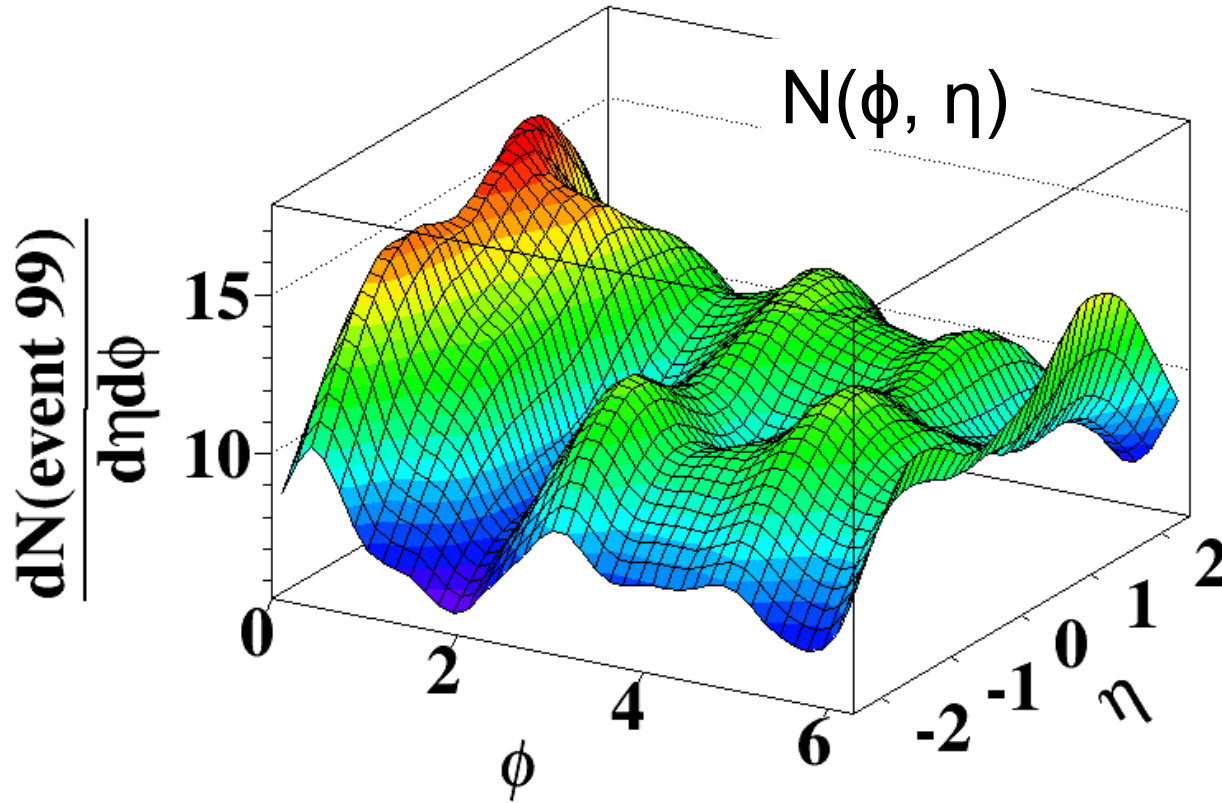
Curtsey of L.Pang and X.N Wang, EbyE 3D hydro+AMPT condition



Fluctuation from event to event

Richness of flow fluctuations

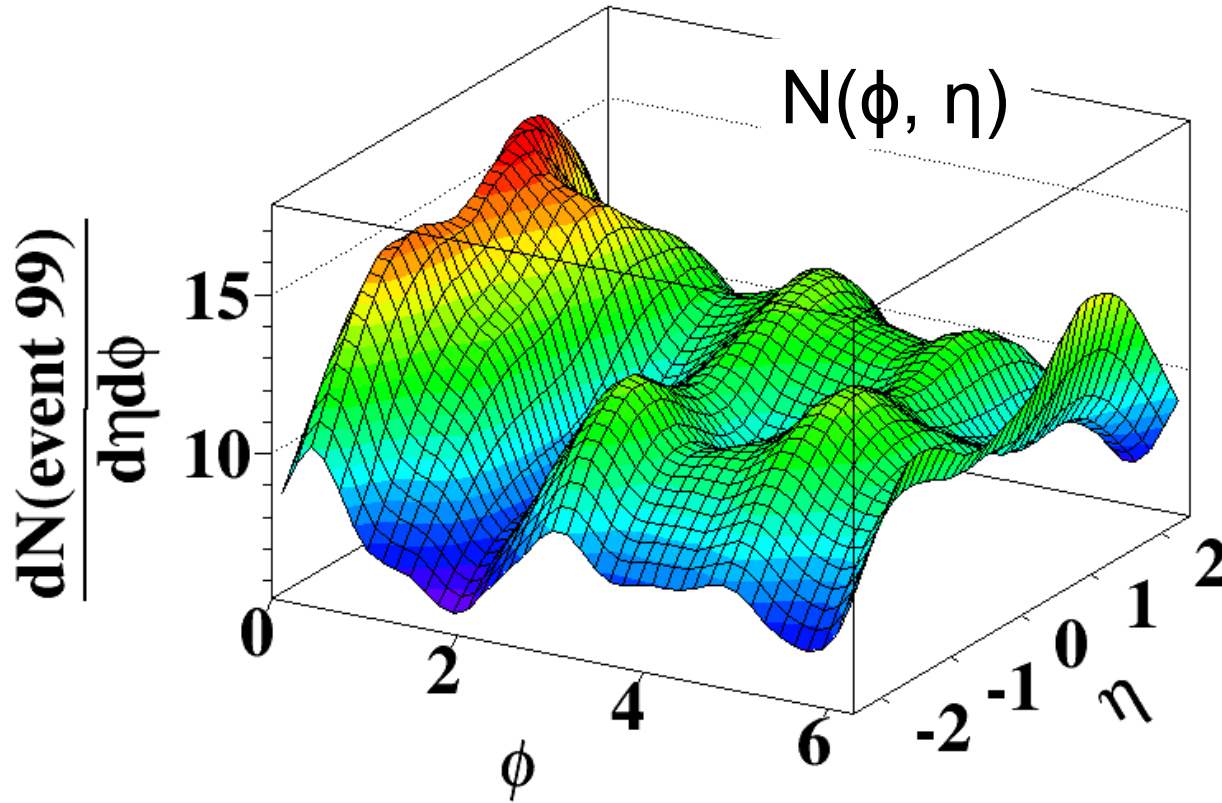
Curtsey of L.Pang and X.N Wang, EbyE 3D hydro+AMPT condition



Fluctuation from event to event

Richness of flow fluctuations

Curtsey of L.Pang and X.N Wang, EbyE 3D hydro+AMPT condition



Fluctuation within a single event

$$\frac{dN}{d\phi} \propto 1 + 2 \sum_n v_n(p_T, \eta, \dots) \cos n(\phi - \Phi_n(p_T, \eta, \dots))$$

Flow observables

Single particle distribution

Flow vector: $V_n = v_n e^{in\Phi_n}$

$$\begin{aligned} \frac{dN}{d\phi d\eta dp_T} &= N(p_T, \eta) \left[1 + 2 \sum_n v_n(p_T, \eta) \cos n(\phi - \Phi_n(p_T, \eta)) \right] \\ &= N(p_T, \eta) \left[\sum_{n=-\infty}^{\infty} V_n(p_T, \eta) e^{in\phi} \right] \\ &\quad \begin{array}{l} \text{Radial flow} \nearrow \text{=} V_0(p_T, \eta) \\ \text{Anisotropic flow} \nwarrow \end{array} \end{aligned}$$

Two-particle correlation function

$$\left\langle \frac{dN_1}{d\phi d\eta dp_T} \frac{dN_2}{d\phi d\eta dp_T} \right\rangle \Rightarrow \langle V_n(p_{T1}, \eta_1) V_n^*(p_{T2}, \eta_2) \rangle \quad v_n \text{ from 2PC}$$

Multi-particle correlation function

$$\begin{aligned} \left\langle \frac{dN_1}{d\phi d\eta dp_T} \cdots \frac{dN_m}{d\phi d\eta dp_T} \right\rangle &\Rightarrow \langle V_{n_1} V_{n_2} \cdots V_{n_m} \rangle \quad n_1 + n_2 + \dots + n_m = 0 \\ &\quad \downarrow \\ &\langle v_{n_1} v_{n_2} \cdots v_{n_m} \cos(n_1 \Phi_{n_1} + n_2 \Phi_{n_2} + \dots + n_m \Phi_{n_m}) \rangle \end{aligned}$$

Flow observables

Single particle distribution

Flow vector: $V_n = v_n e^{in\Phi_n}$

$$\frac{dN}{d\phi d\eta dp_T} = N(p_T, \eta) \left[1 + 2 \sum_n v_n(p_T, \eta) \cos n(\phi - \Phi_n(p_T, \eta)) \right]$$

$$= N(p_T, \eta) \left[\sum_{n=-\infty}^{\infty} V_n(p_T, \eta) e^{in\phi} \right]$$

Radial flow \nearrow $V_0(p_T, \eta)$ \nwarrow Anisotropic flow

Two-particle correlation function

$$\left\langle \frac{dN_1}{d\phi d\eta dp_T} \frac{dN_2}{d\phi d\eta dp_T} \right\rangle \Rightarrow \langle V_n(p_{T1}, \eta_1) V_n^*(p_{T2}, \eta_2) \rangle \quad v_n \text{ from 2PC}$$

Multi-particle correlation function

$$\left\langle \frac{dN_1}{d\phi d\eta dp_T} \cdots \frac{dN_m}{d\phi d\eta dp_T} \right\rangle \Rightarrow \langle V_{n_1} V_{n_2} \cdots V_{n_m} \rangle \quad n_1 + n_2 + \cdots + n_m = 0$$

$$p(v_n, v_m, \dots, \Phi_n, \Phi_m, \dots) = \frac{1}{N_{\text{evts}}} \frac{dN_{\text{evts}}}{dv_n dv_m \cdots d\Phi_n d\Phi_m \cdots}$$

Examples

- Single-flow cumulants

$$c_n\{2\} = \langle v_n^2 \rangle \quad n=1-7$$

$$c_n\{4\} = \langle v_n^4 \rangle - 2 \langle v_n^2 \rangle^2$$

$$c_n\{6\} = \langle v_n^6 \rangle - 9 \langle v_n^4 \rangle \langle v_n^2 \rangle + 12 \langle v_n^2 \rangle^3$$

$$\dots$$
- Symmetric cumulants

$$sc_{n,m}\{4\} = \langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle \quad (n,m)=(2,3), (2,4)\dots$$
- Asymmetric cumulants (Event plane correlator)

$$\langle v_2^2 v_4 \cos 4(\Psi_2 - \Psi_4) \rangle$$

$$\langle v_2^3 v_3^2 \cos 6(\Psi_2 - \Psi_3) \rangle$$

$$\langle v_2 v_3 v_5 \cos(2\Psi_2 + 3\Psi_3 - 5\Psi_5) \rangle$$

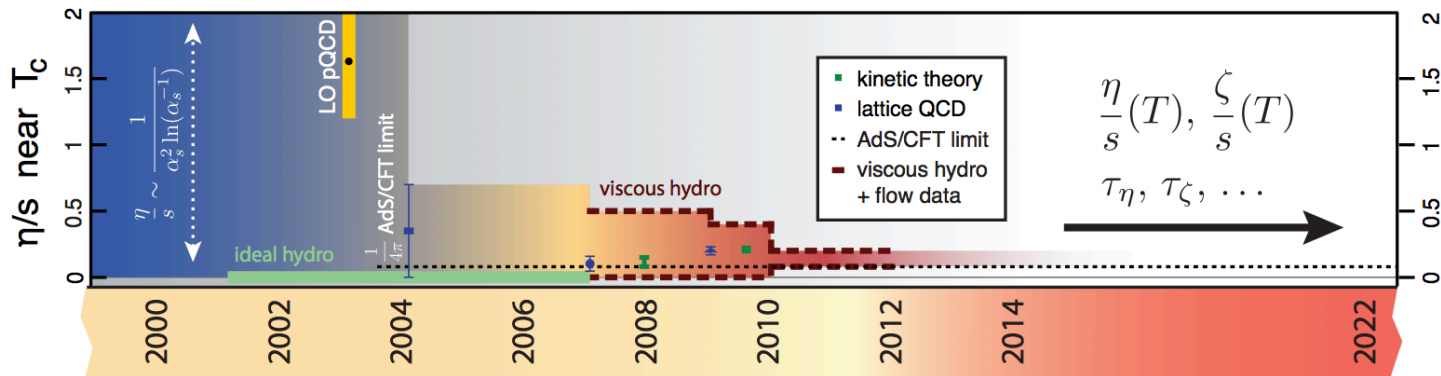
$$\dots$$
- v_n-v_0 correlator

$$\langle v_n^2 N \rangle, \langle v_n^2 \delta p_T \rangle \dots$$

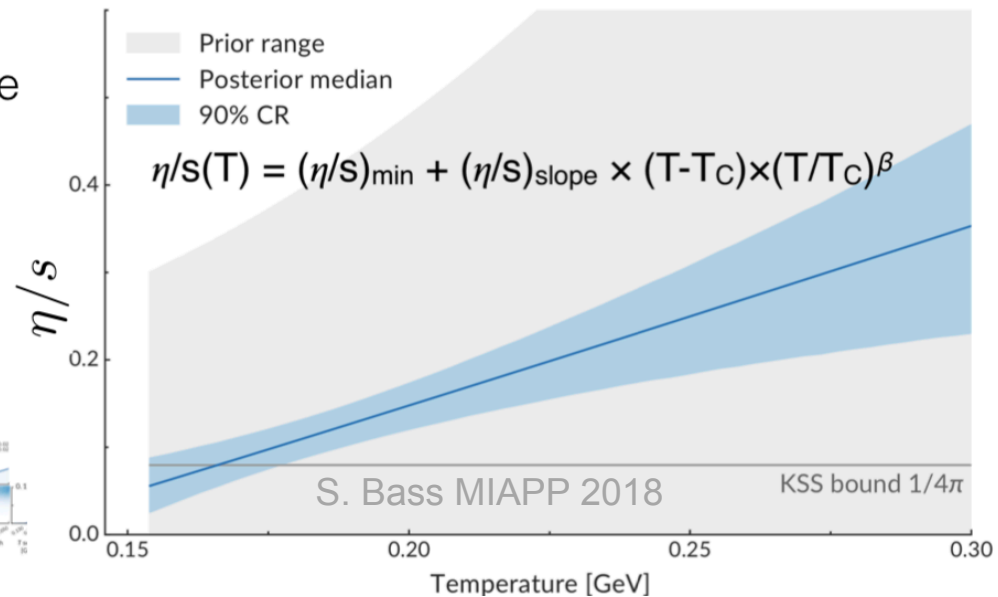
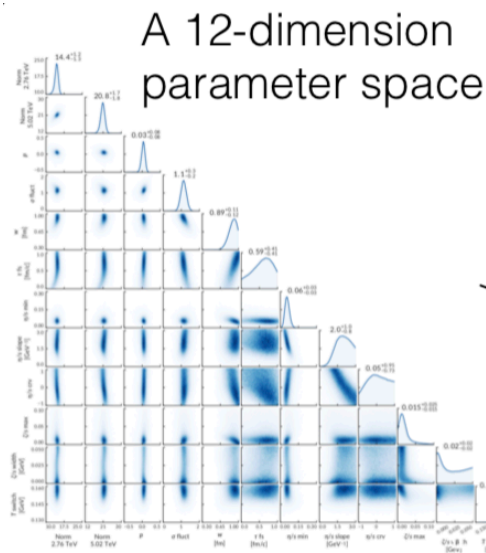
$$\langle \delta p_T \delta p_T \rangle, \langle \delta p_T \delta p_T \delta p_T \rangle \dots$$

Success of hydrodynamics

- Data-model comparison improves precision of transport parameters

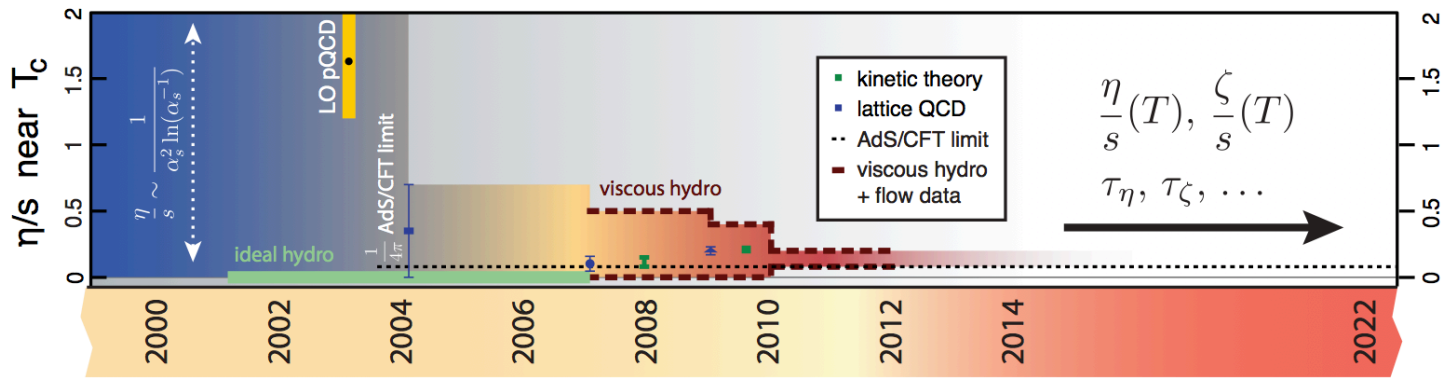


- Multi-parameter adaptive fitting optimizes constraining power.
 - Differential information in the parameter space ...within a given model



Success of hydrodynamics

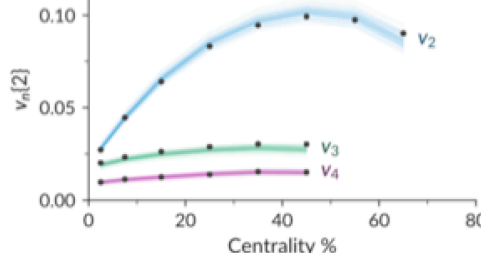
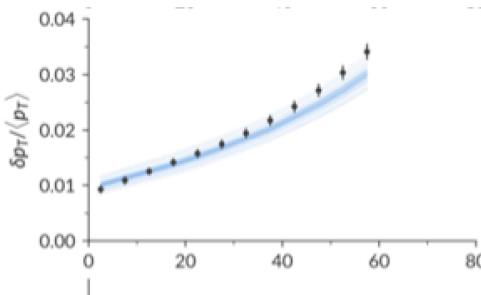
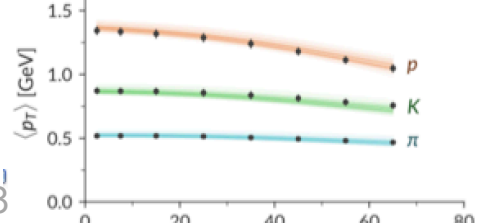
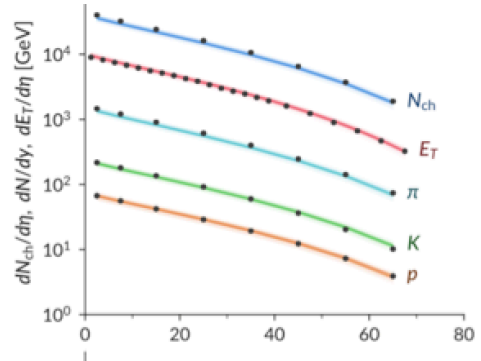
- Data-model comparison improves precision of transport parameters



- Multi-parameter adaptive fitting optimizes constraining power.
 - Differential information in the parameter space ...within a given model

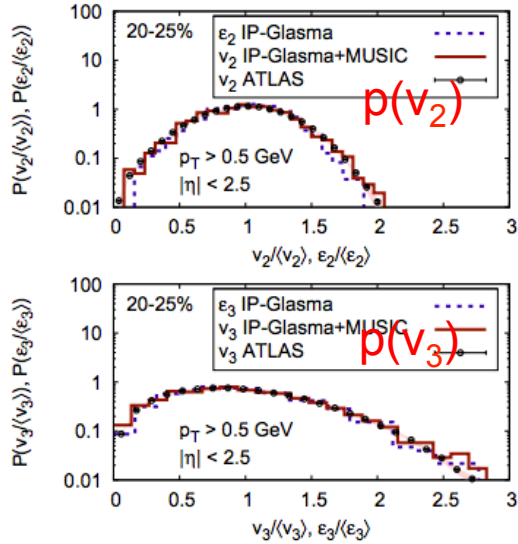
Only utilize limited set of observables:
 dN/dp_T , $\langle p_T \rangle$, $\langle \delta p_T \delta p_T \rangle$, $\langle v_n^2 \rangle$

Limited by model uncertainties!
 Initial state, QGP dynamics, freezeout/hadronic

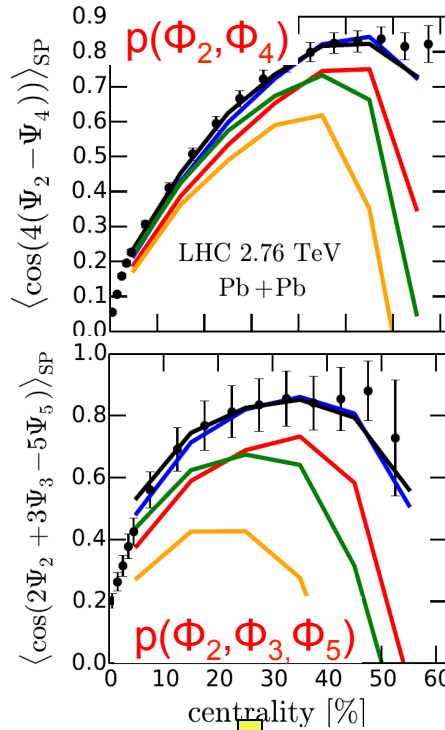


Power of flow fluctuations

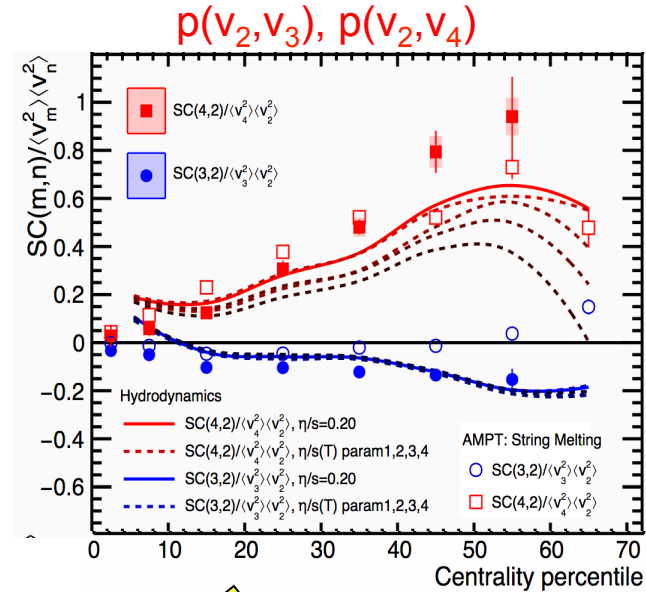
Gale, Jeon, Schenke, Tribedy, Venugopalan 1209.6330



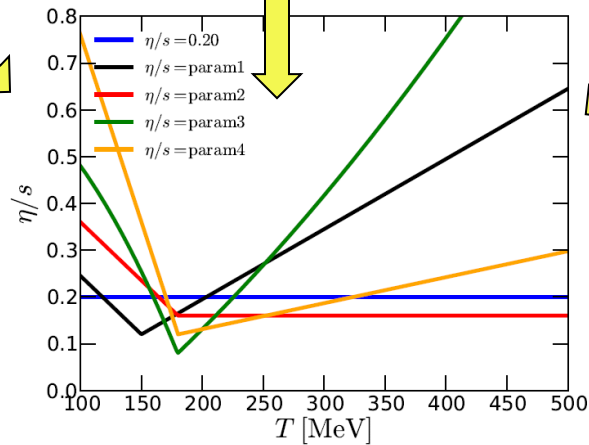
Niemi, Eskola, Paatelainen 1505.02677



ALICE 1604.07663



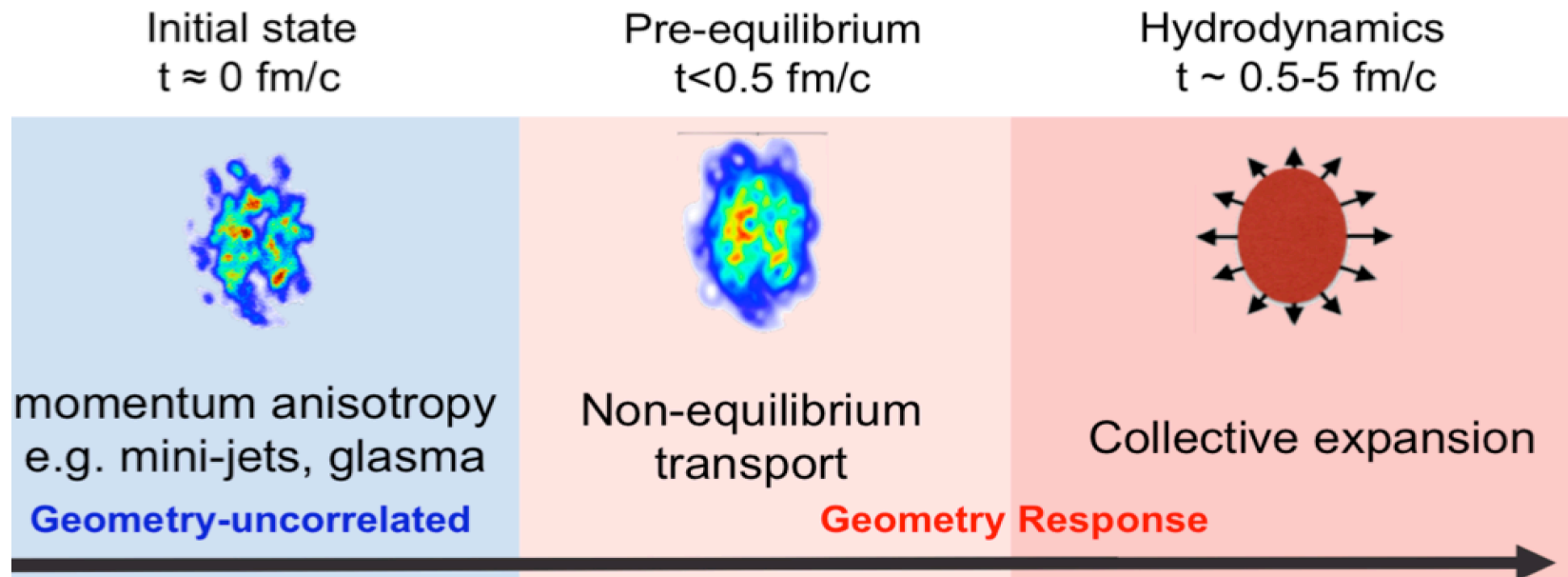
Probe the hydrodynamic response: $(\epsilon_n, \Phi_n^*) \rightarrow (v_n, \Phi_n)$



Sensitive to detail of transport coeffs: $\eta/s(T)$

Potential to further reduce model uncertainties

Challenge for understanding



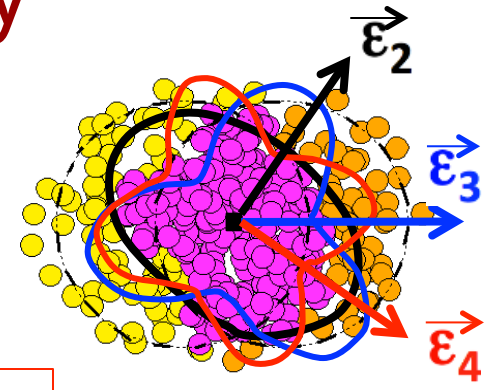
Contributions from different stages are difficult to disentangle

- Initial geometry and Initial momentum anisotropy
- pre-equilibrium dynamics and entropy production
- $\eta/s(T)$, $\zeta/s(T)$, EOS, non-equilibrium dynamics
- Phase transition and hadronization
- Hadronic transport and Freezeout

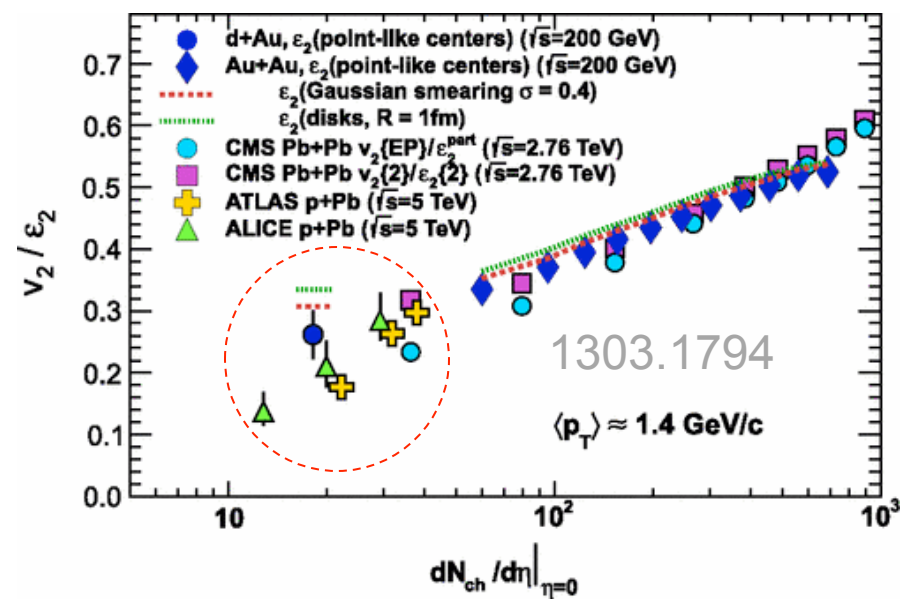
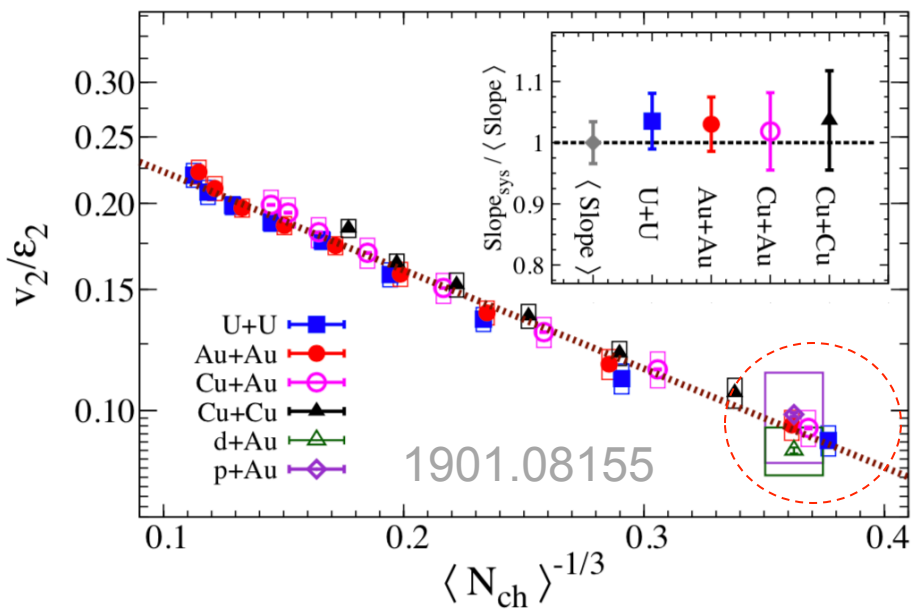
Hard to experimentally vary one ingredient at a time

Initial state geometry

- By far the dominating source of fluctuations that we use to define the hydro response.



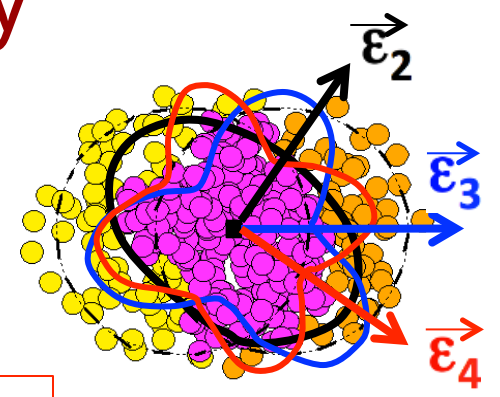
- Linear response works well on average $v_n \propto \epsilon_n$



Consists with geometry-driven hydrodynamic response

Initial state geometry

- By far the dominating source of fluctuations that we use to define the hydro response.



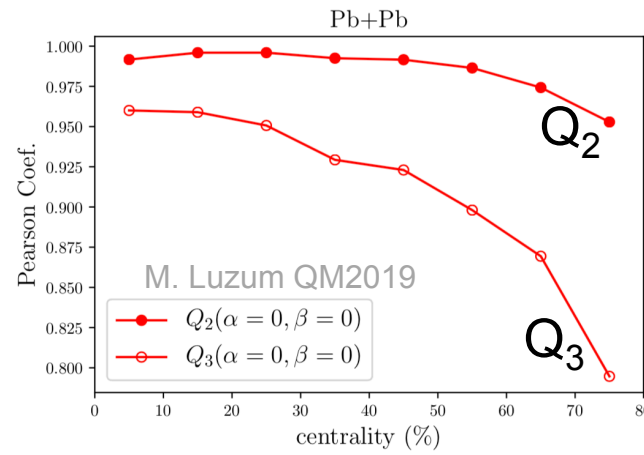
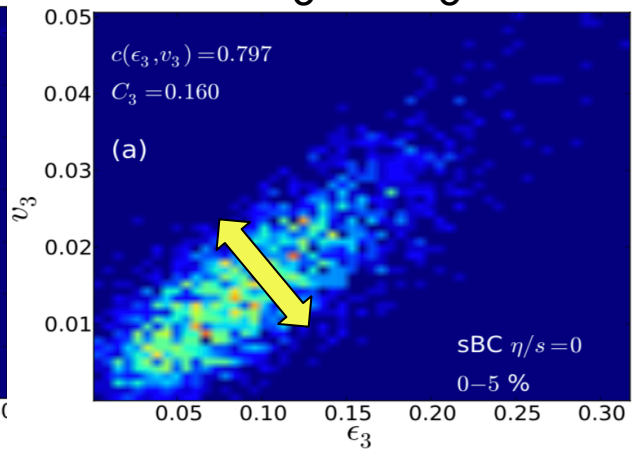
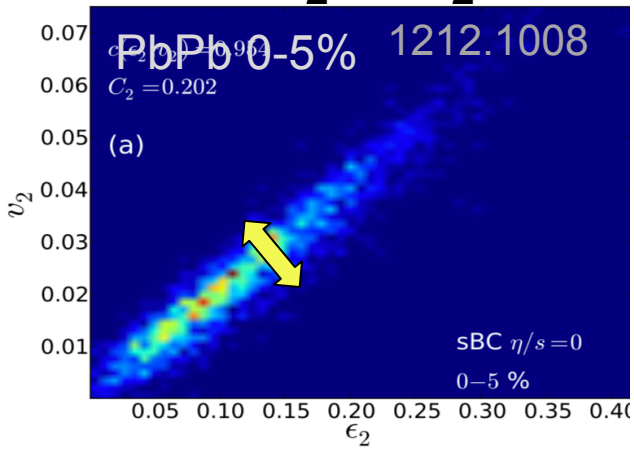
- Linear response works well on average $v_n \propto \epsilon_n$

But significant EbyE spread remains

$$Q_n = \frac{\langle v_n \epsilon_n \cos(n[\psi_n - \phi_n]) \rangle}{\sqrt{\langle |\epsilon_n|^2 \rangle \langle |v_n|^2 \rangle}} \sim 1$$

V_2 VS ϵ_2

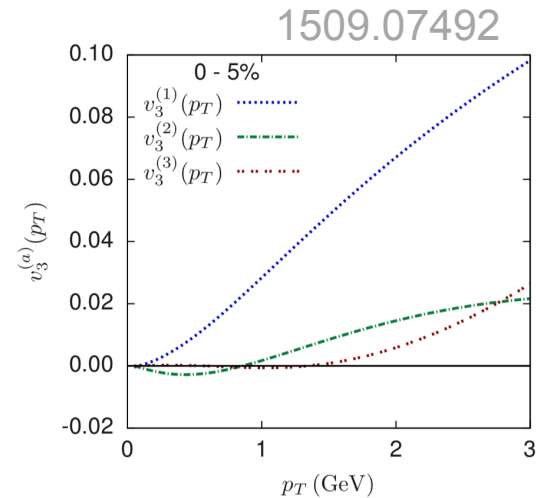
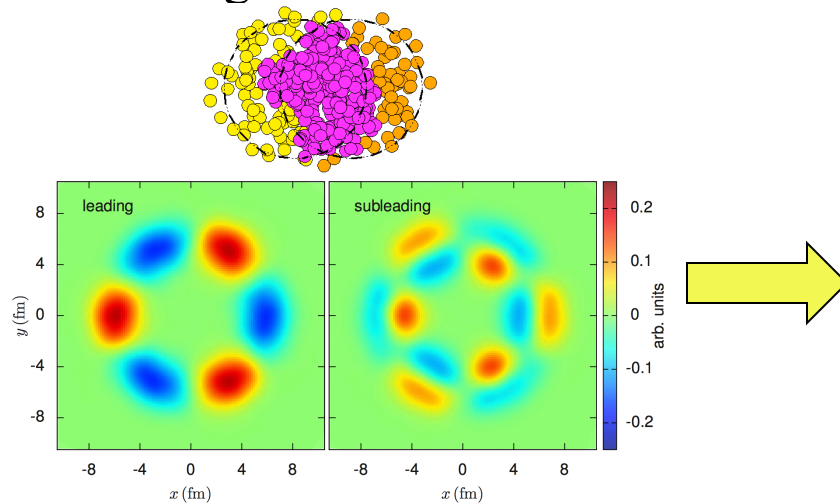
V_3 VS ϵ_3



What is the origin of these spreads?

Dissecting the hydro response

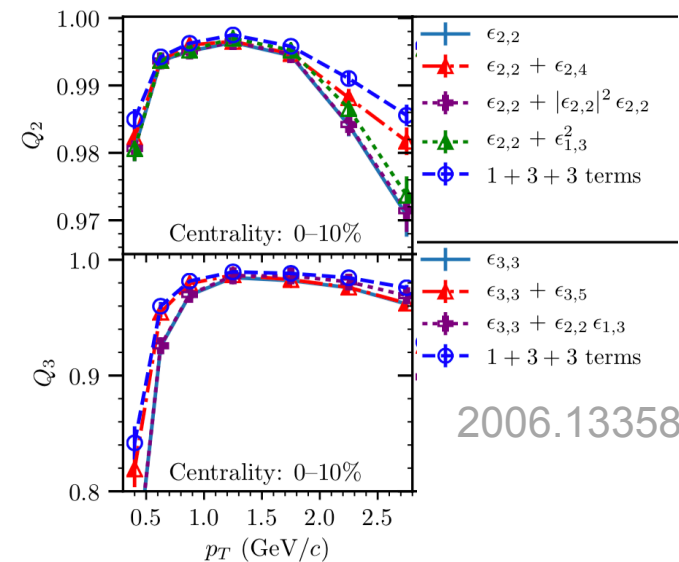
- Leading ϵ_n does not capture everything about initial state
 - Subleading eccentricities from radial excitations



- Re-sum subleading ϵ_n and mode-mixing terms improves agreement

$$V_n(p_T) \approx \sum_{p=1}^{p_{\max}} \sum_{\{n', m'\}}^{\sum n'_i = n} \kappa_{\{n', m'\}}^{(n)}(p_T) \prod_{i=1}^p \epsilon_{n'_i, m'_i} + \mathcal{O}(\epsilon_{n, m_{\max}}) + \mathcal{O}(\epsilon^{p_{\max}+1})$$

How to characterize and understand the residual differences?



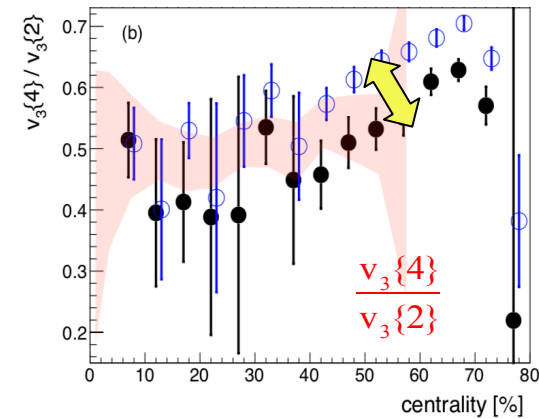
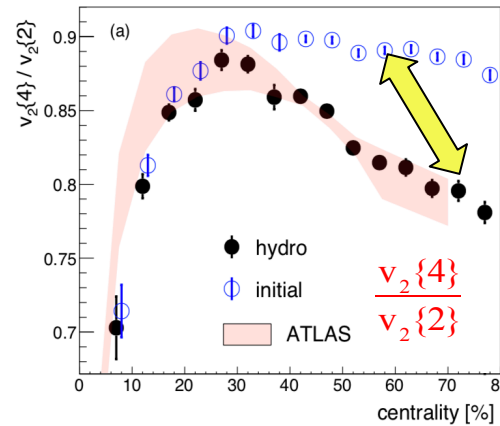
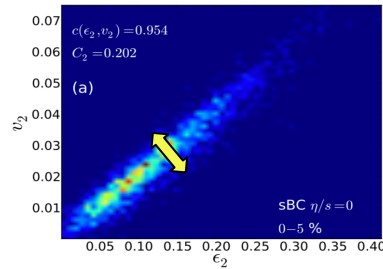
Understand the difference via flow fluctuations 17

Often assumes:

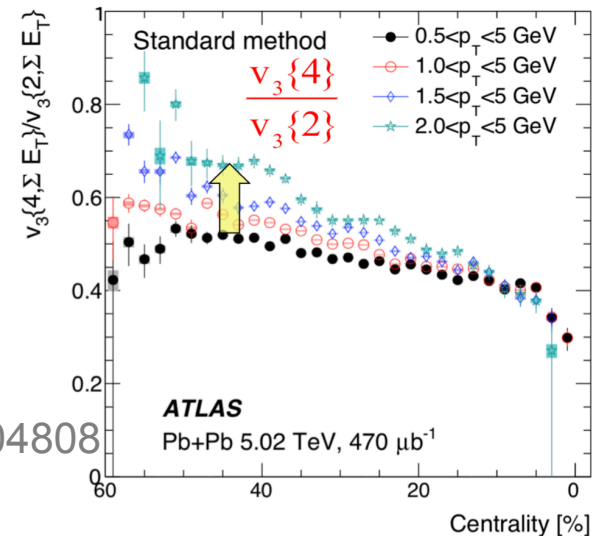
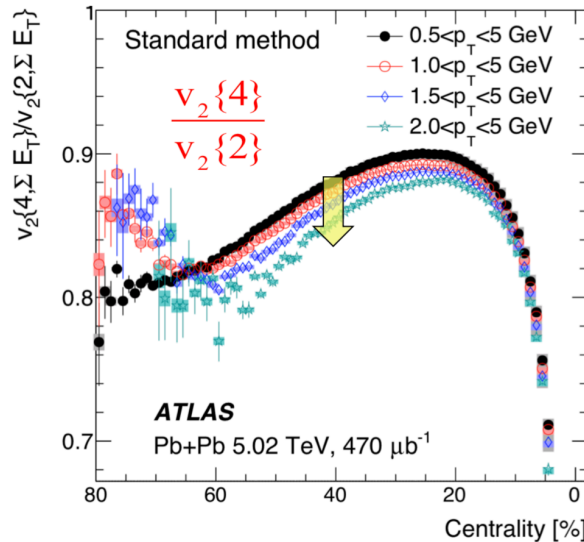
L. Yan, J. Ollitrault arXiv:1312.6555

Giacalone, JNH, Ollitrault Phys.Rev. C95 (2017) no.5, 054910

$$V_n \propto \mathcal{E}_n \quad \rightarrow \quad \frac{v_n\{4\}}{v_n\{2\}} = \frac{\mathcal{E}_n\{4\}}{\mathcal{E}_n\{2\}} \quad \times$$



Also not supported by data:

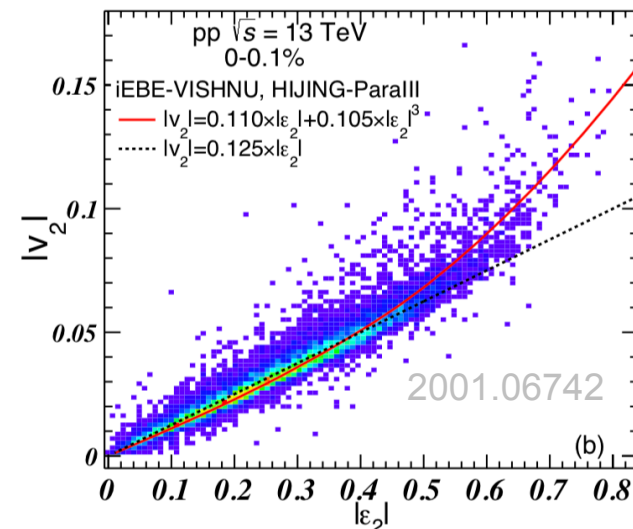
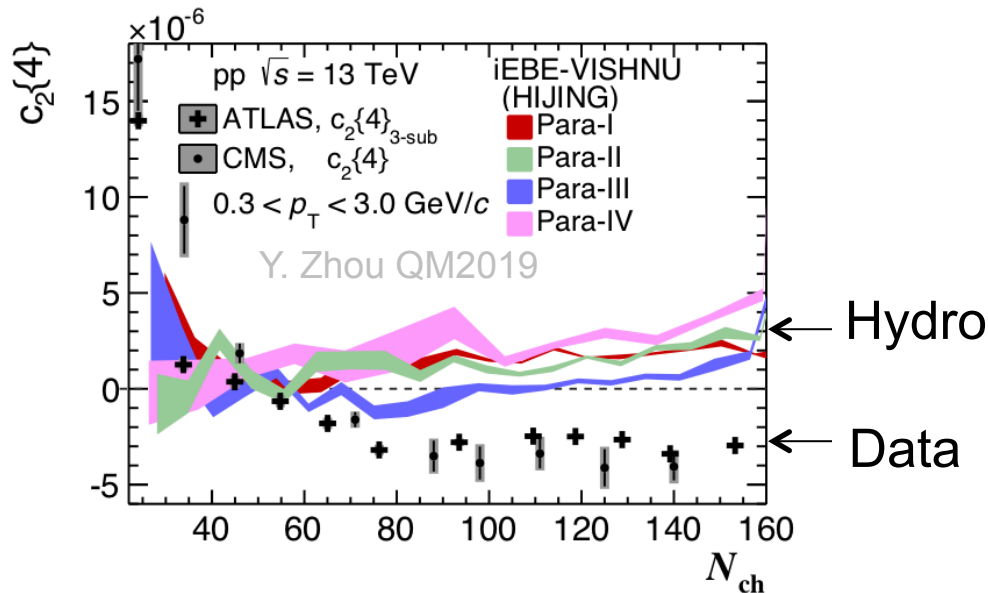


1904.04808

Role of initial-flow or final-state fluctuations?

Flow fluctuation in pp collisions

- Hydro calculation yields positive $c_2\{4\}$, opposite to data.



Significant cubic response,
 responsible for $+c_2\{4\}$

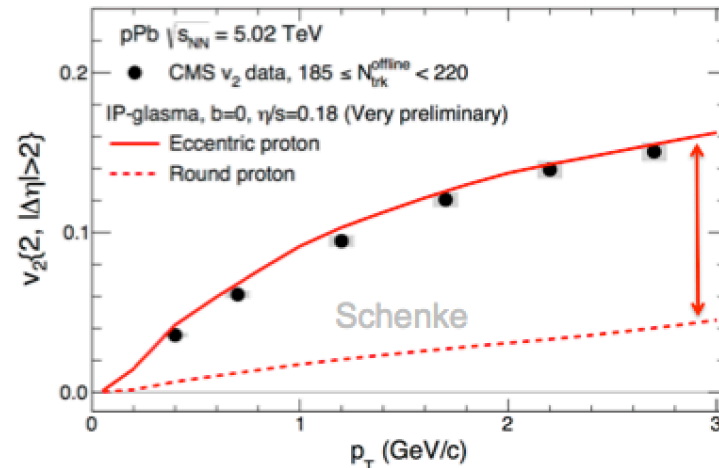
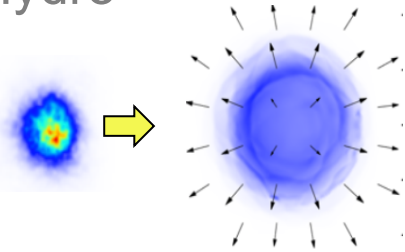
- Additional source of non-Gaussian fluctuations $\frac{v_n\{4\}}{v_n\{2\}} \neq \frac{\epsilon_n\{4\}}{\epsilon_n\{2\}}$

What is missing in this hydro simulation?

Role of initial-flow in pA collisions

Hydrodynamics with subnucleonic fluctuations describe the data

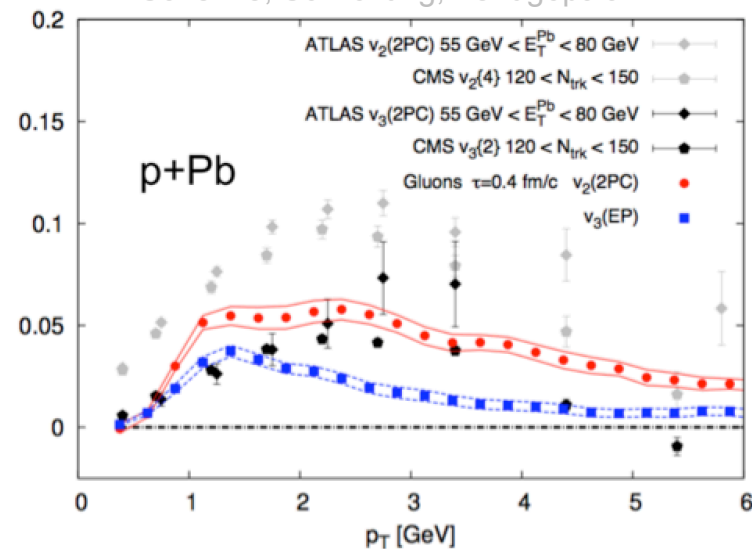
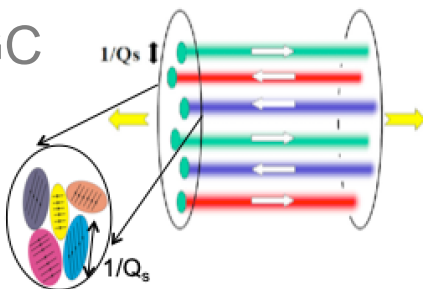
Hydro



Initial momentum anisotropy contribution alone could be large

Schenke, Schlichting, Venugopalan

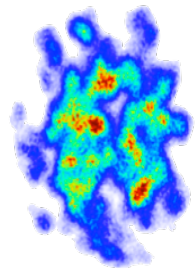
CGC



Role of initial-flow in pA collisions

Initial-state $T^{\mu\nu}(x,y)$ tensor contains large momentum T^{0i} and stress T_{ij}

→ source for initial flow



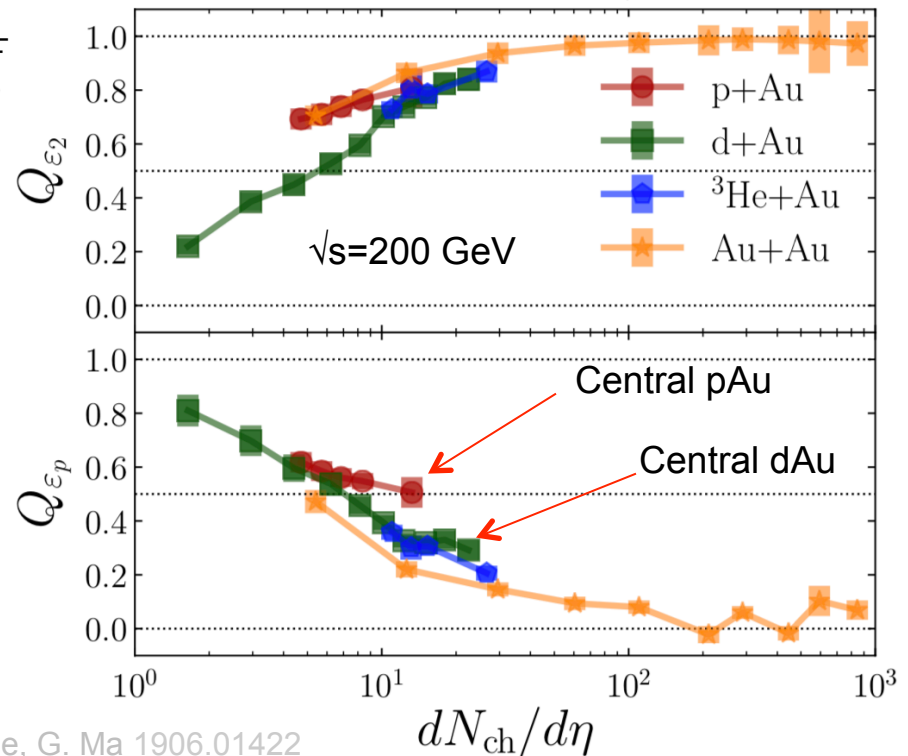
$$Q_{\varepsilon_2} = \frac{\text{Re}\langle \vec{\mathcal{E}}_2 \cdot \vec{V}_2^* \rangle}{\sqrt{\langle |\vec{\mathcal{E}}_2|^2 \rangle \langle |\vec{V}_2|^2 \rangle}}$$

$T^{00}(x,y)$
+

other $T^{\mu\nu}(x,y)$

$$Q_{\varepsilon_p} = \frac{\text{Re}\langle \vec{\mathcal{E}}_p \cdot \vec{V}_2^* \rangle}{\sqrt{\langle |\vec{\mathcal{E}}_p|^2 \rangle \langle |\vec{V}_2|^2 \rangle}}$$

B. Schenke, C. Shen, P. Tribedy, 1908.06212



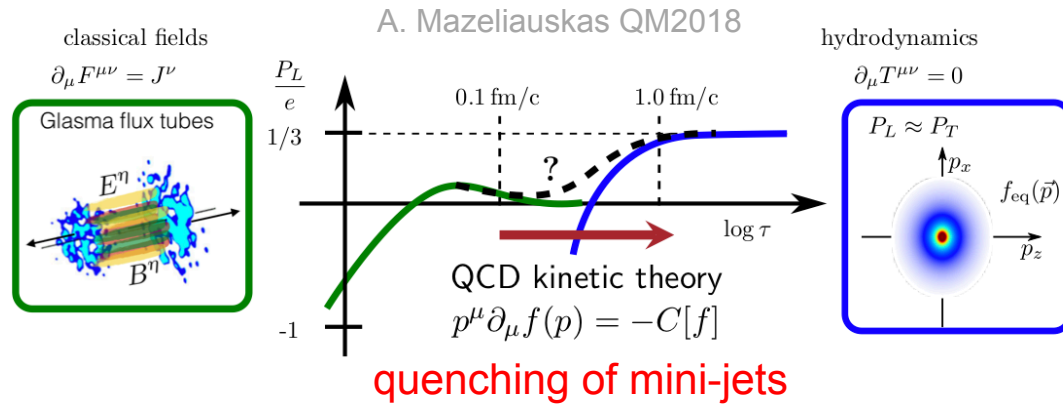
Similar earlier study in J.Jia, M. Nie, G. Ma 1906.01422

Geometry component of the $T^{\mu\nu}$ dominates at large N_{ch} .
Momentum component of the $T^{\mu\nu}$ dominates at low N_{ch}

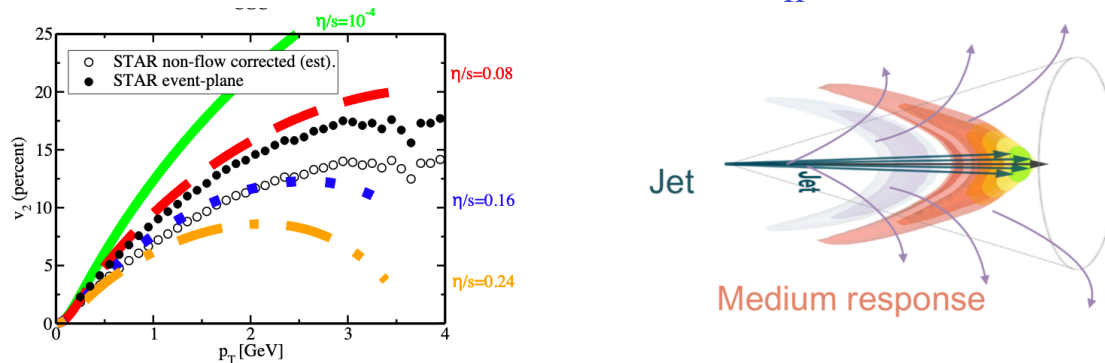
Any direct experimental evidences for this ??

Pre-equilibrium dynamics in large system ²¹

- Initial-flow is natural e.g. in bottom up thermalization 1506.06647 1605.04287
 - Interactions damp momentum-anisotropy, drive QGP towards local equilibrium
 - Necessary for rapid entropy production.



- Non-equilibrium effects important for v_n and spectra at $p_T > 2-3 \text{ GeV}/c$



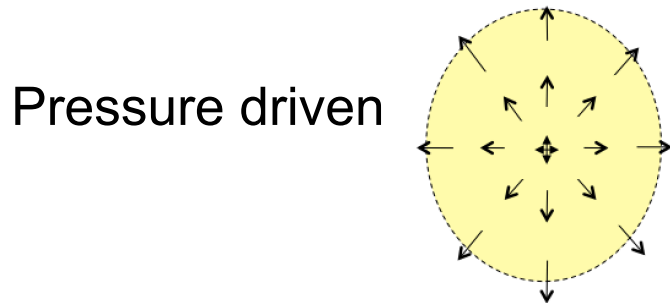
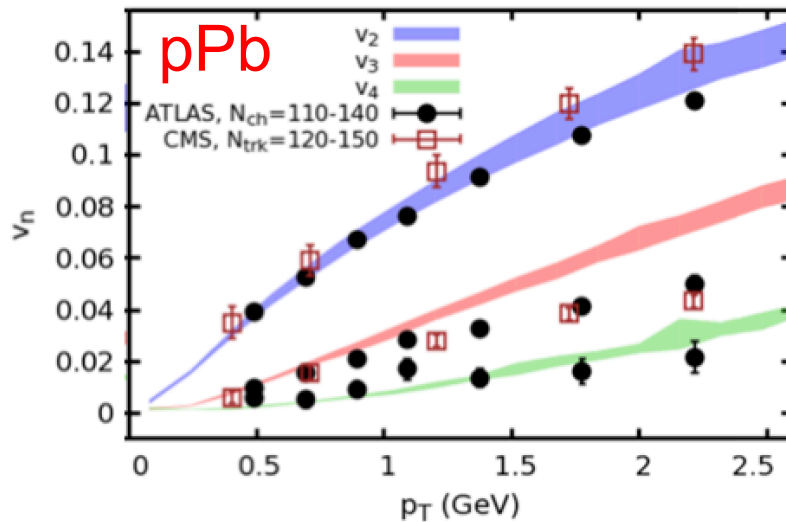
How to identify and quantify non-equilibrium effects and understand their role for bulk physics?

Hydro vs. non-equilibrium transport

- Non-equilibrium effects are naturally included in transport approach

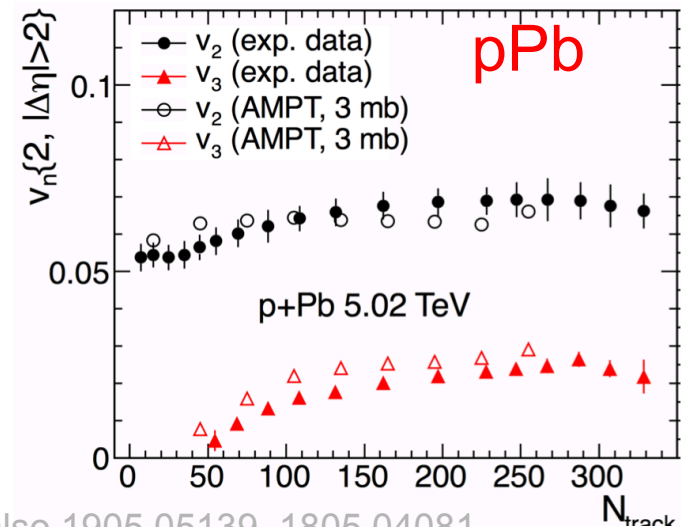
P. Romatschke, R. Weller 1701.07145

Hydrodynamics /, 0-5%

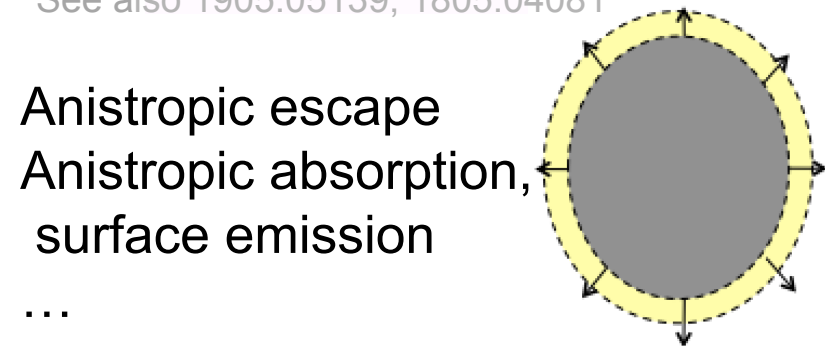


L.He, T.Edmonds, Z.Lin, F.Liu, D. Molnar and F. Wang 1502.05572, G. Ma and A Bzdak 1406.2804

AMPT transport



See also 1905.05139, 1805.04081



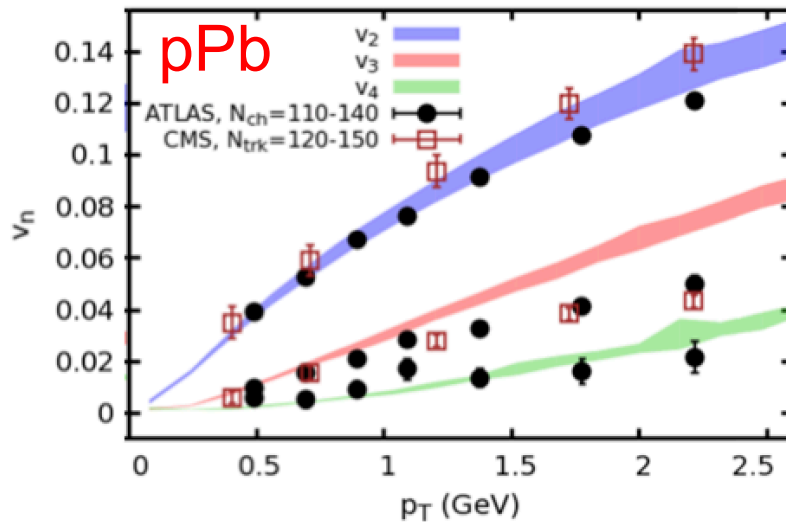
Both reflects final-state geometry response: $v_n = k_n \epsilon_n$
but different space-time dynamics

Hydro vs. non-equilibrium transport

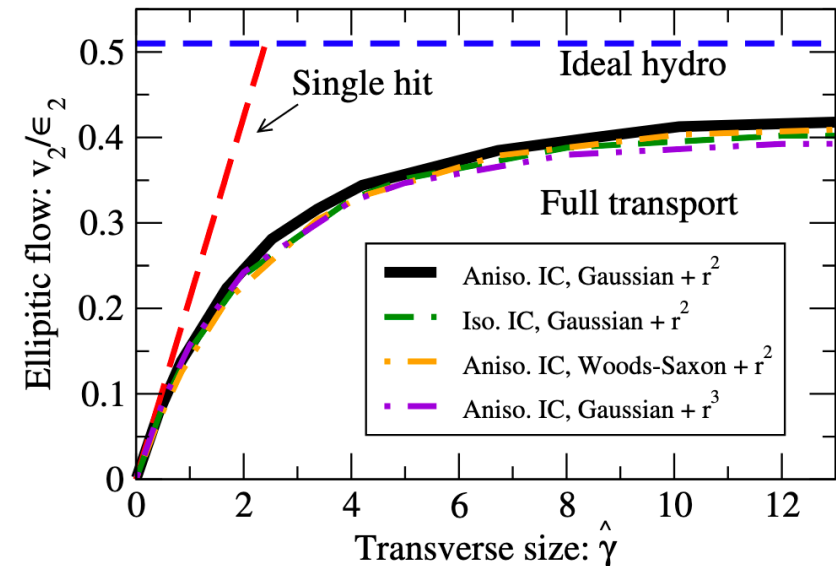
- Non-equilibrium effects are naturally included in transport approach

P. Romatschke, R. Weller 1701.07145

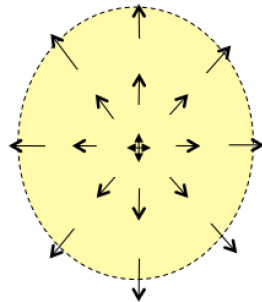
Hydrodynamics \sqrt{s} , 0-5%



A Kurkela, U. Wiedemann, B.Wu 1905.05139, 1805.04081

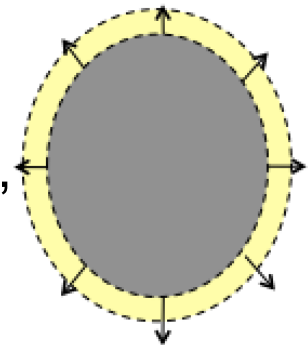


Pressure driven



Anisotropic escape
Anisotropic absorption,
surface emission

...



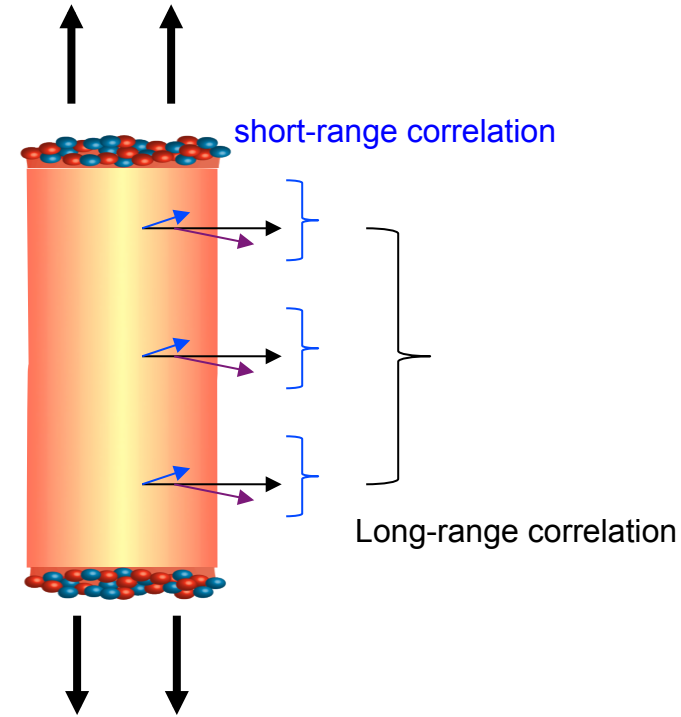
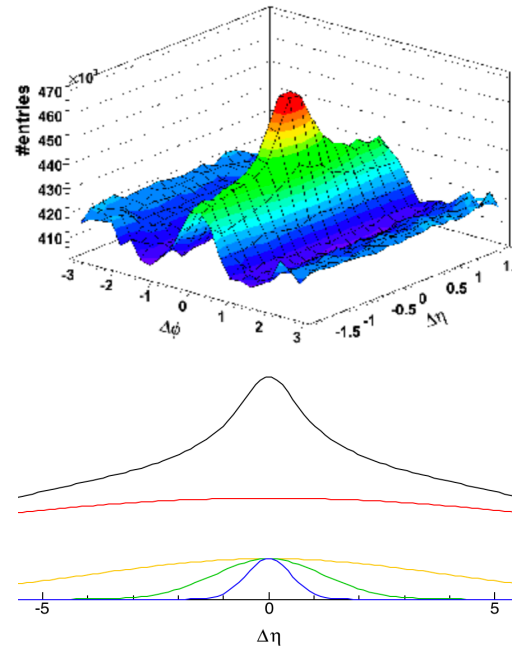
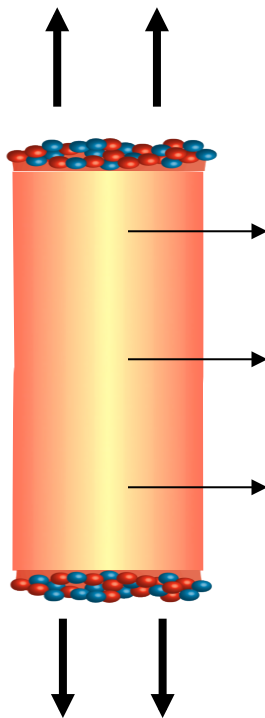
Expect response coefficients k_n is smaller in transport $v_n = k_n \epsilon_n$

$$\partial_\mu T^{\mu\nu} = 0$$

$$p^\mu \partial_\mu f(p) = -C[f]$$

Flow from hydro is a
single body distribution

Flow from transport is
n-body distribution



Focus on short-range correlations!

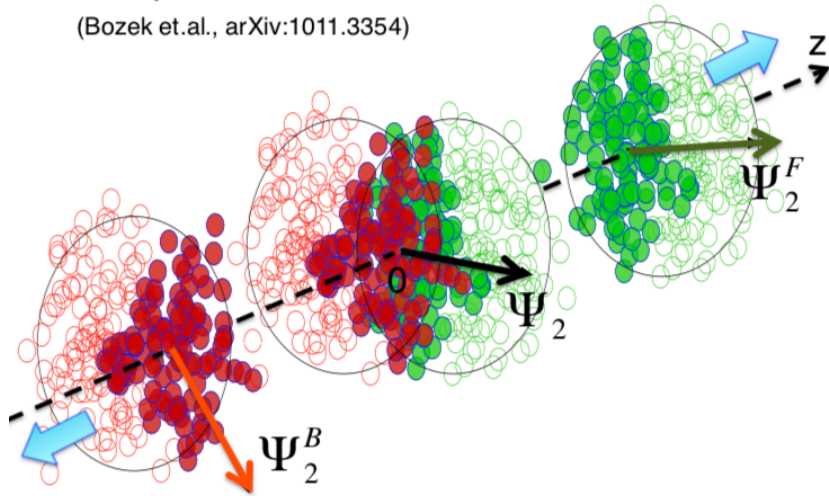
Long-range reflects geometry response, $v_n \propto \epsilon_n$, hard to distinguish
Short-range sensitive to the transport physics.

Break the boost-invariance

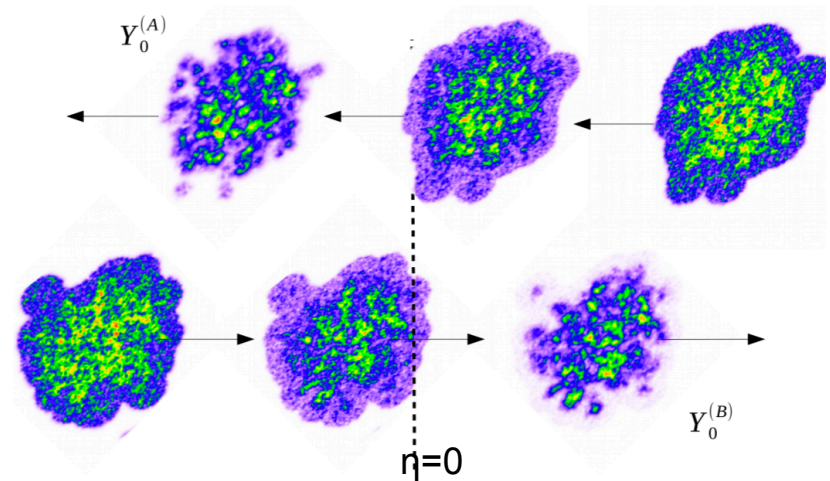
- The initial condition changes with rapidity

Torqued QGP fireball

(Bozek et.al., arXiv:1011.3354)



small-x evolution (JIMWLK)



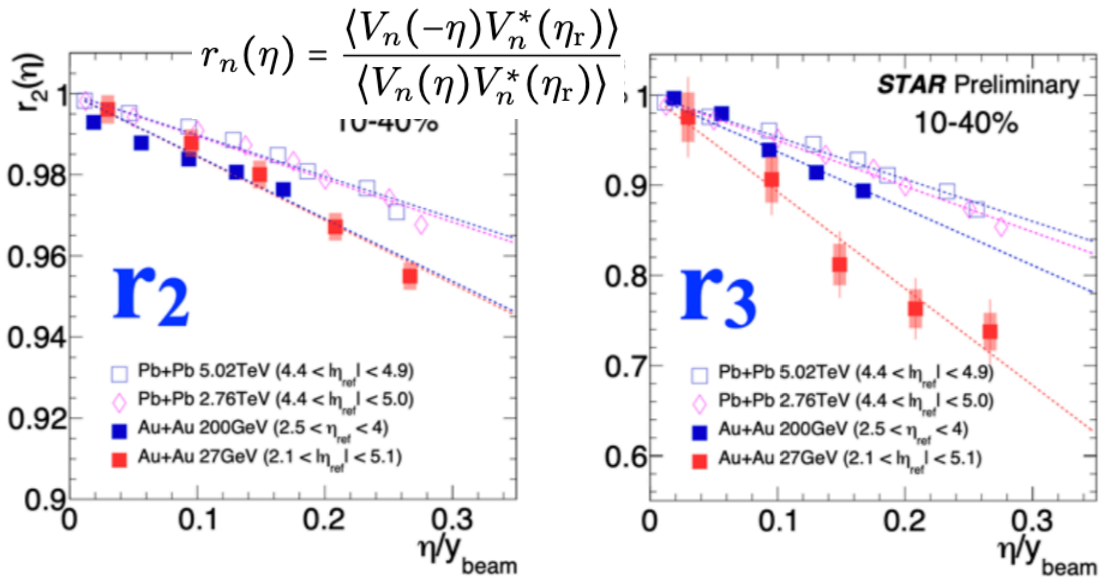
$$\langle \vec{\varepsilon}_n(\boldsymbol{\eta}_1^s) \vec{\varepsilon}_n^*(\boldsymbol{\eta}_2^s) \rangle \Rightarrow \langle \vec{V}_n(\boldsymbol{\eta}_1) \vec{V}_n^*(\boldsymbol{\eta}_2) \rangle$$

Flow decorrelation

$$\langle \varepsilon_0(\boldsymbol{\eta}_1^s) \varepsilon_0(\boldsymbol{\eta}_2^s) \rangle \Rightarrow \langle N(\boldsymbol{\eta}_1) N(\boldsymbol{\eta}_2) \rangle$$

Multiplicity/centrality decorrelation

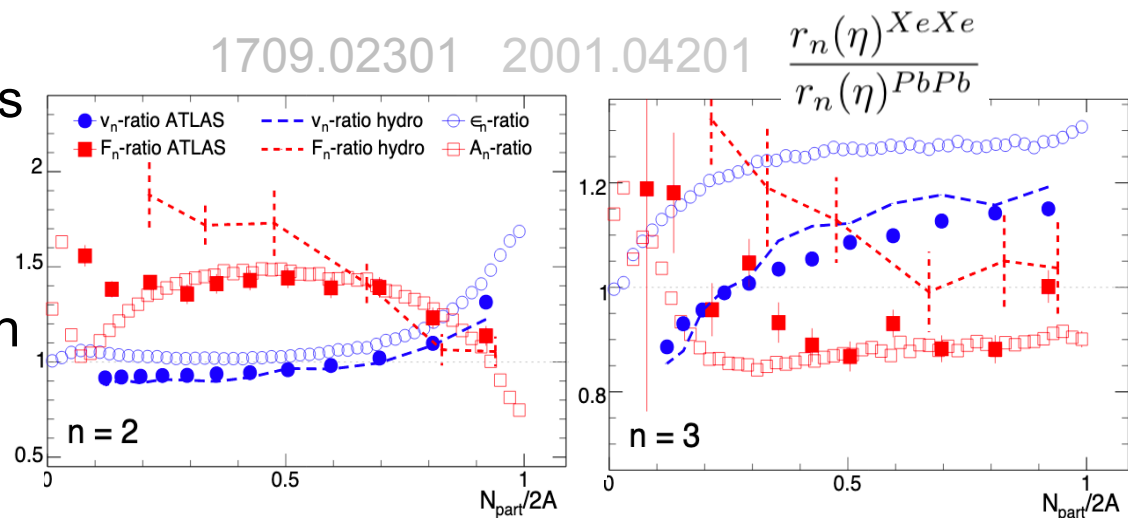
Longitudinal flow decorrelations



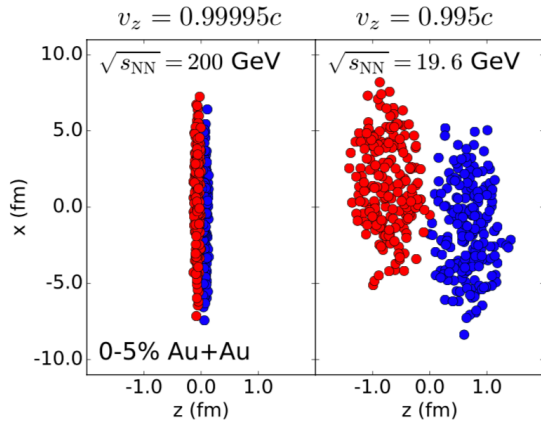
- strong \sqrt{s} dependence
 - sensitive to η/s , thermal fluctuation and stopping
 - systematics not described by models
- 2003.13496

- system-size dependence scales with $N_{part}/2A$, reflects overall shape not the size
- sensitive to nuclear deformation
- systematics not fully described by models

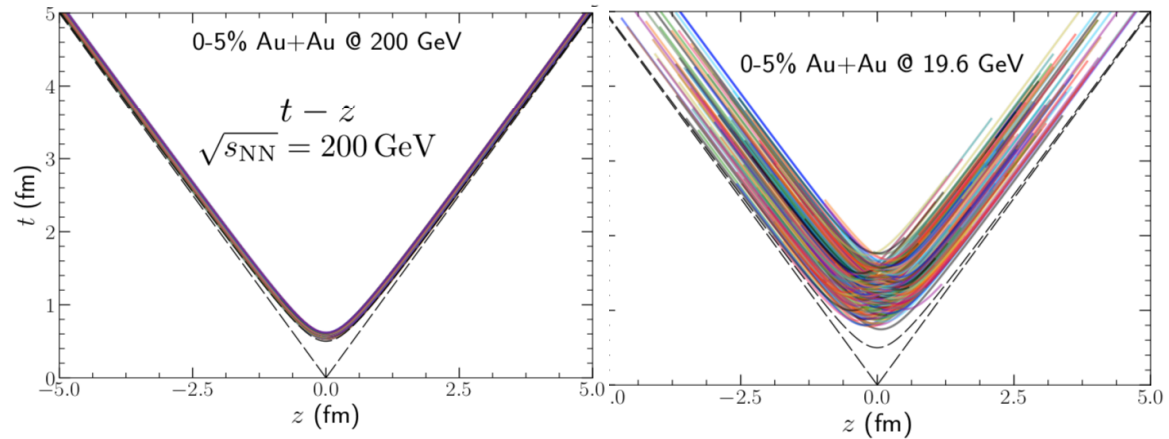
See 2003.04340



Beam-energy scan and longitudinal dynamics²⁷



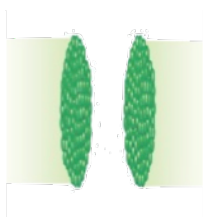
Nuclear overlap time becomes large at lower energies



Nucleons are decelerated with energy deposited over a larger space-time volume

Different stages no longer separated

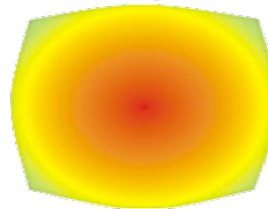
initial state



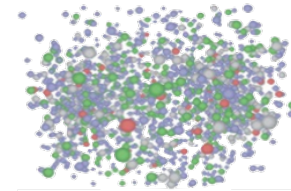
pre-equilibrium



QGP & expansion

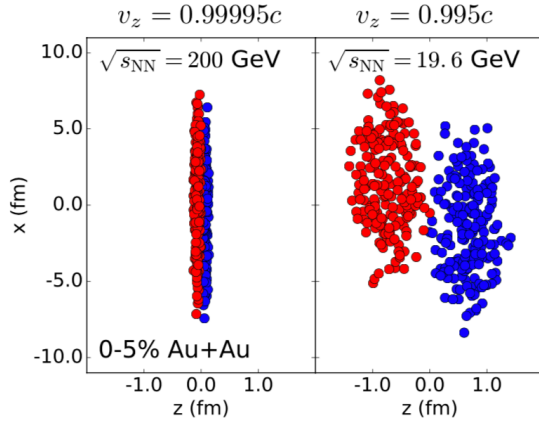


Phase transition & freeze-out

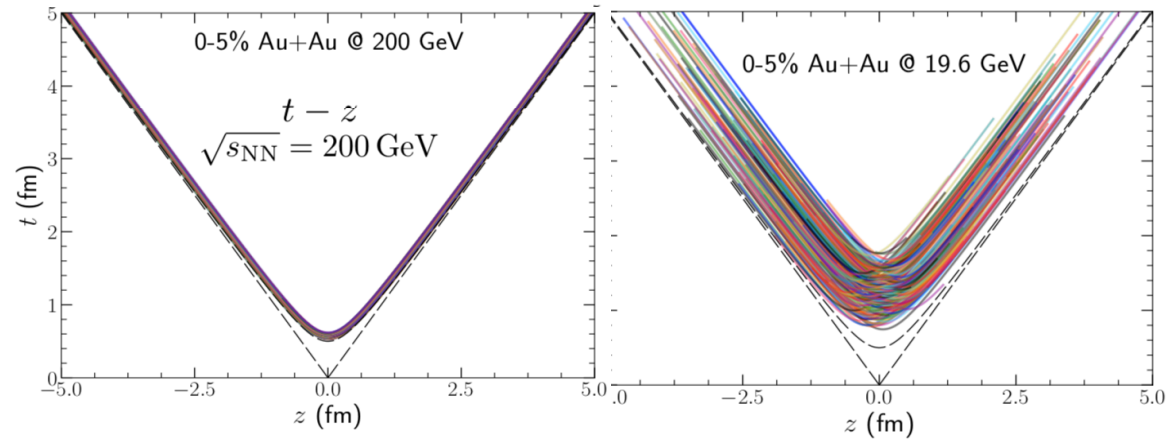


τ

Beam-energy scan and longitudinal dynamics²⁸



Nuclear overlap time becomes large at lower energies



Nucleons are decelerated with energy deposited over a larger space-time volume

Longitudinal dynamics as important as transverse dynamics

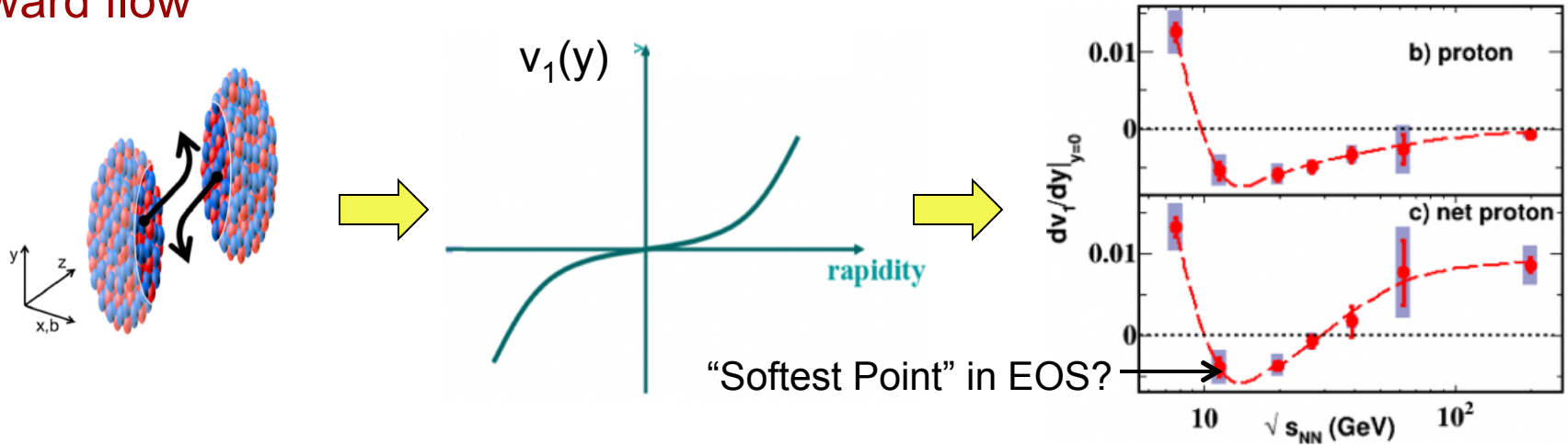
- Overlap between longitudinal stopping and transverse expansion
- Collective flow no-longer reflects only eccentricity.
- Nuclear stopping, baryon transport and importance of global vorticity
- EOS and transport properties are different
- Hadronic phase are more important

Description requires full 3+1D hydrodynamics or transport

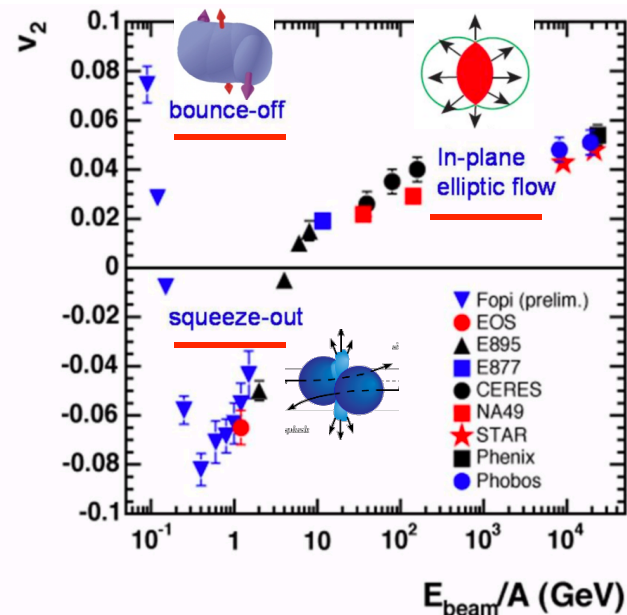
Collective flow at low \sqrt{s}

Interplay between nuclear stopping and final-state collective motion

Sideward flow

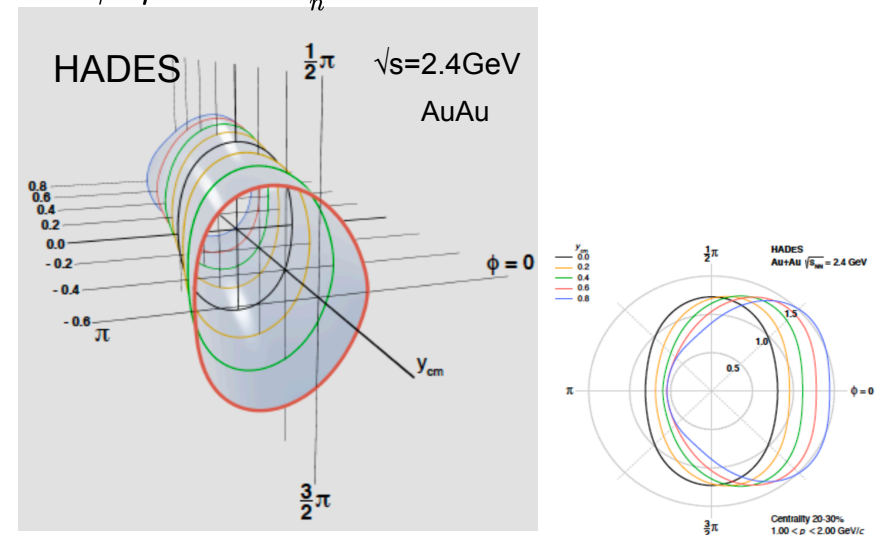


Elliptic flow



Higher-order flow harmonics

$$\frac{dN}{d\phi d\eta} \propto 1 + 2 \sum_n v_n(\eta) \cos n(\phi - \Psi_{RP})$$

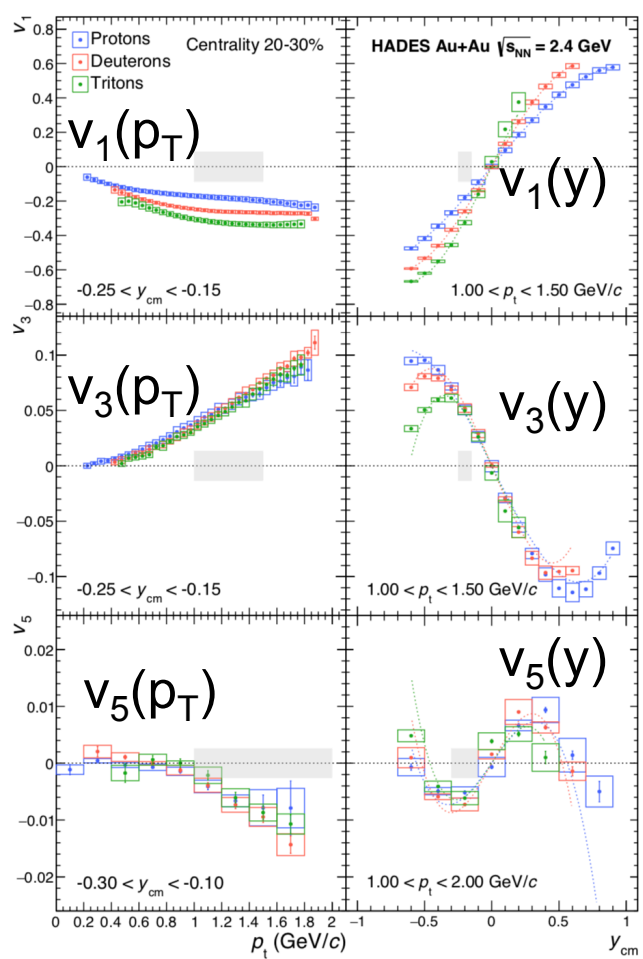


Flow results at HADES $\sqrt{s}=2.4$ GeV

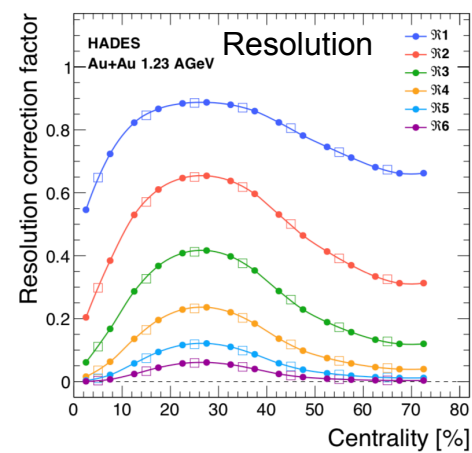
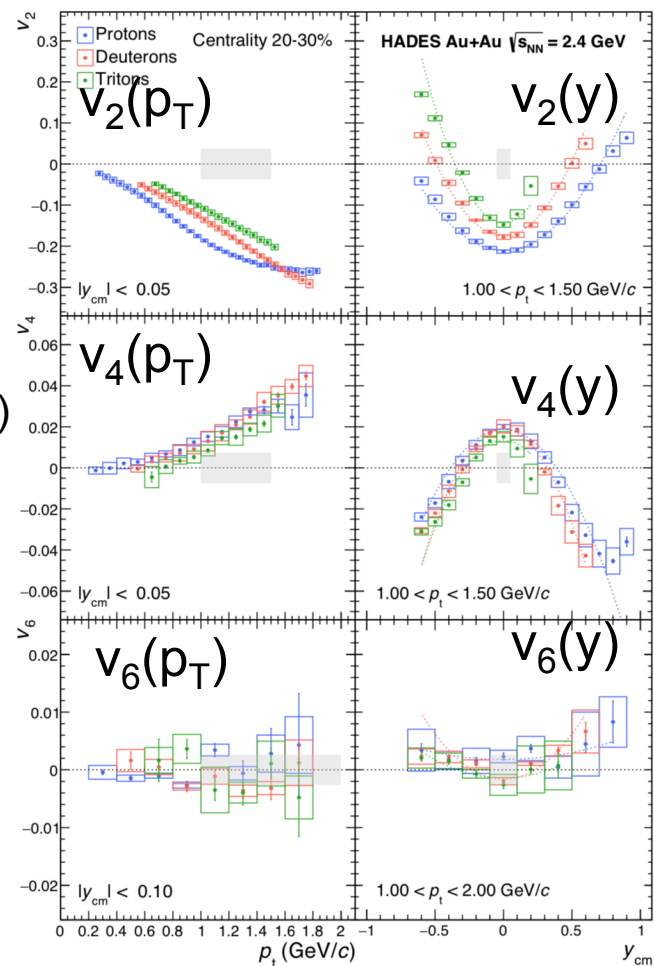
2005.12217

all light nuclei. Theory calculations within a hydrodynamic framework adapted to the description of baryon dominated matter are needed to investigate the question whether this kind of matter really exhibits a hydrodynamical behavior, at least in the last stages of the collision prior to freeze-out. The high precision information on higher order flow coefficients is a major step forward in constraining the EOS.

Challenge to theory



- Complex interplay between longitudinal and transverse dynamics.
- Measured in $\Psi_1 \rightarrow$ Large mode-coupling terms between different harmonics
- Interesting to measure $v_n(\Psi_n)$ as well as EbyE fluctuations.



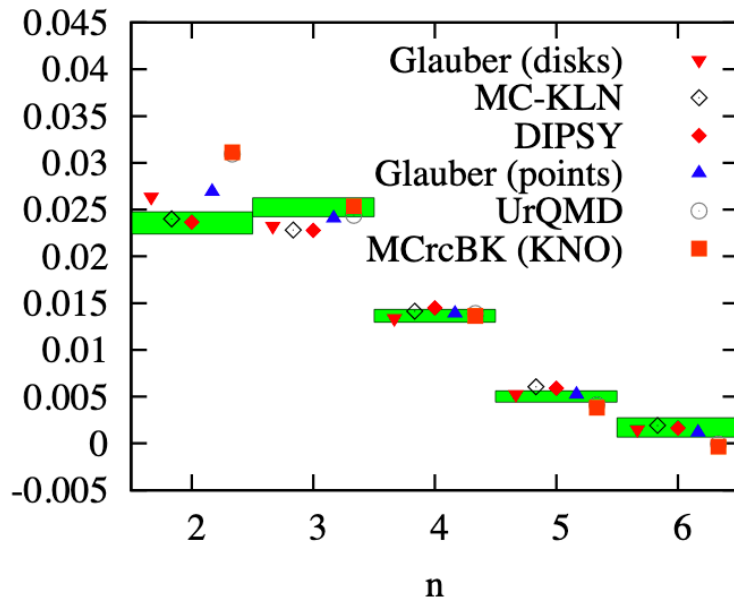
Look into the future

- Top \sqrt{s} : aim for precision in both dynamics and properties.
 - Easier with larger multiplicity and \sim boost invariance
- BES \sqrt{s} : more reliable modeling of the 3D dynamics
 - Identify observables with direct physics intuition
 - More measurements on flow fluctuations
- Improve understanding in
 - Initial state geometry
 - Early time dynamics
 - Final state dynamics and properties
- New directions
 - Collision System scan
 - Rapidity scan

Flow in Ultra-central collisions

$$v_2 \approx v_3 > v_4 > v_5$$

$$\epsilon_2 \approx \epsilon_3 \approx \epsilon_4 \approx \epsilon_5$$



Volume fluctuation?

Goes opposite direction
See 1904.04808

Bulk/shear viscosity and EOS

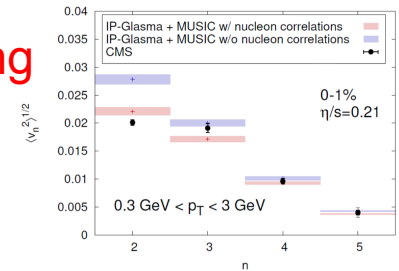
1408.0024, 1502.04636, 1711.05207

May improve v_2 v_3 ordering
but not sufficient

Nucleon-nucleon correlation

1406.7792

Improves v_2 v_3 ordering
but not sufficient



Octupole deformation

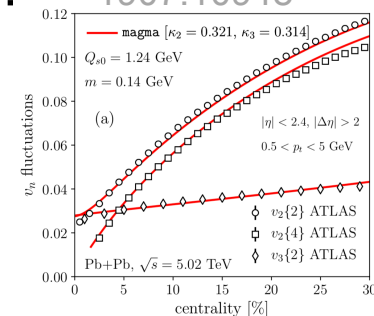
2007.00780

Improves v_2 v_3 ordering but worsening
description of $v_3\{4\}/v_3\{2\}$

Subnucleon fluctuations?

1907.10948

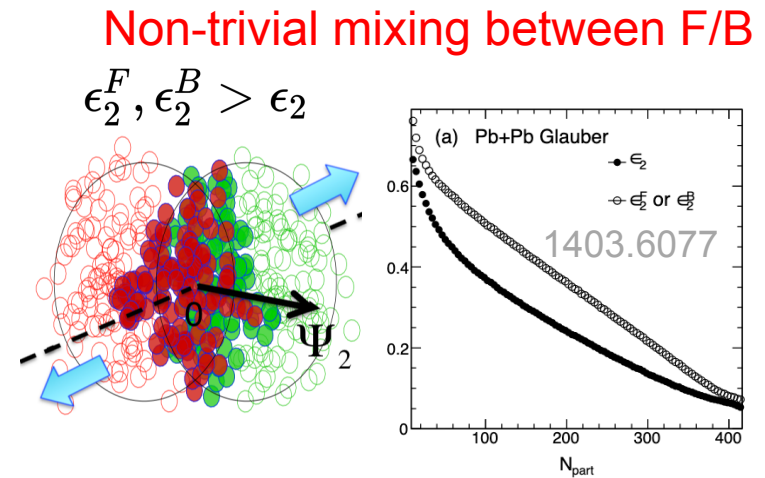
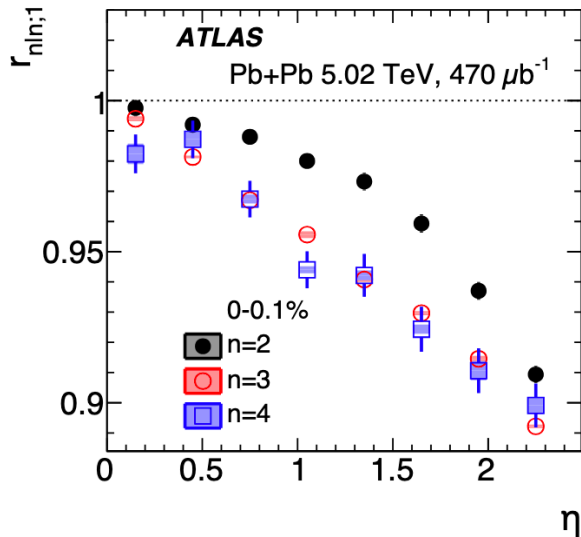
Produce v_2 v_3 ordering
via fitting k_n in $v_n = k_n \epsilon_n$
but $k_2 \approx k_3$?



Flow in Ultra-central collisions

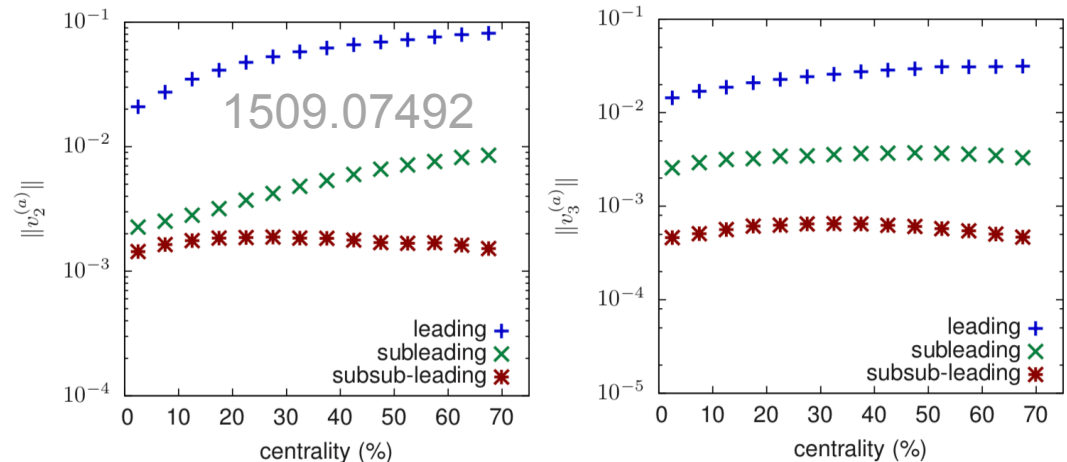
My bet: it is due to longitudinal dynamics

Large and non-linear decorrelation not yet reproduced by models



Analyze subleading flow including longitudinal fluctuations?

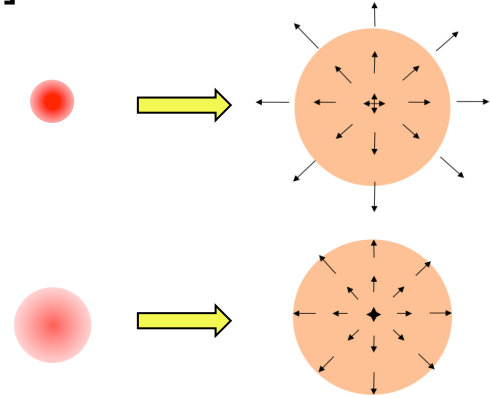
Likely some unknown
3D initial state effects
amplified in UCC.



only transverse dynamics included so far

New handle on the initial state: v_n - p_T correlation

$[p_T]$ anti-correlates with size

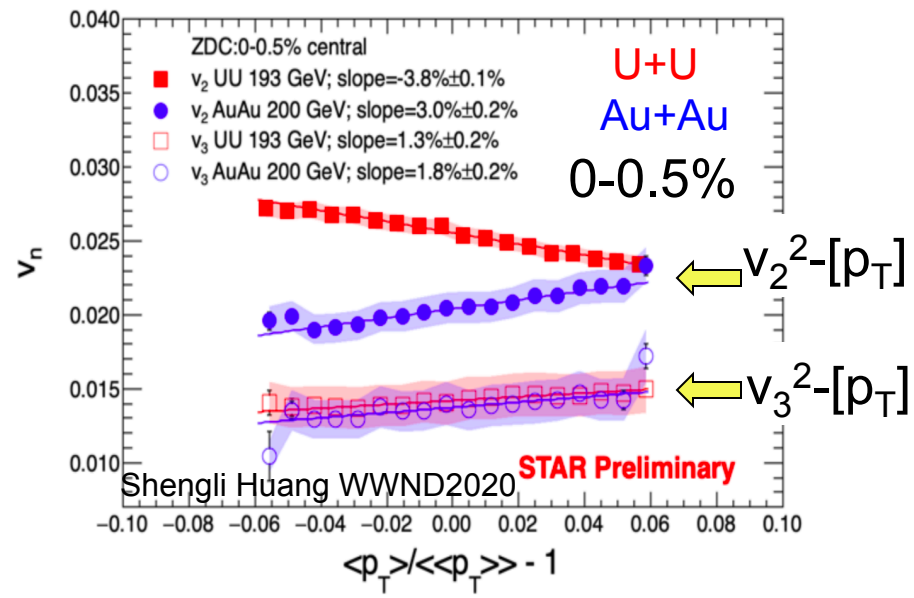
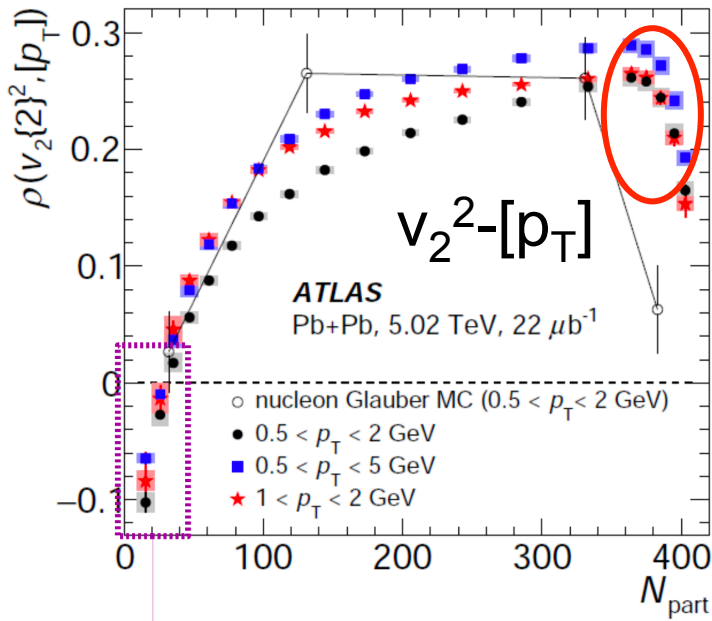


Fluctuation of radial size correlates with radial flow and harmonic flow

→ Strong v_n - p_T correlation, unique probe of the radial structures

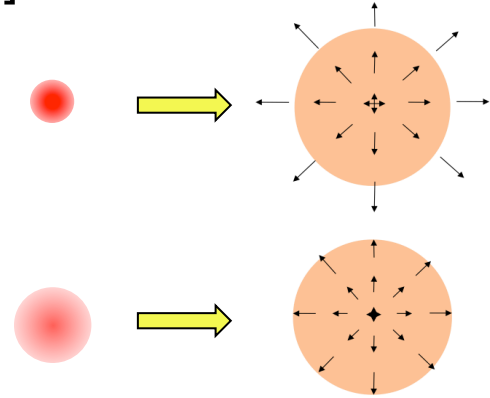
sensitive to shape-size correlation

sensitive to nuclear deformation



New handle on the initial state: v_n - p_T correlation

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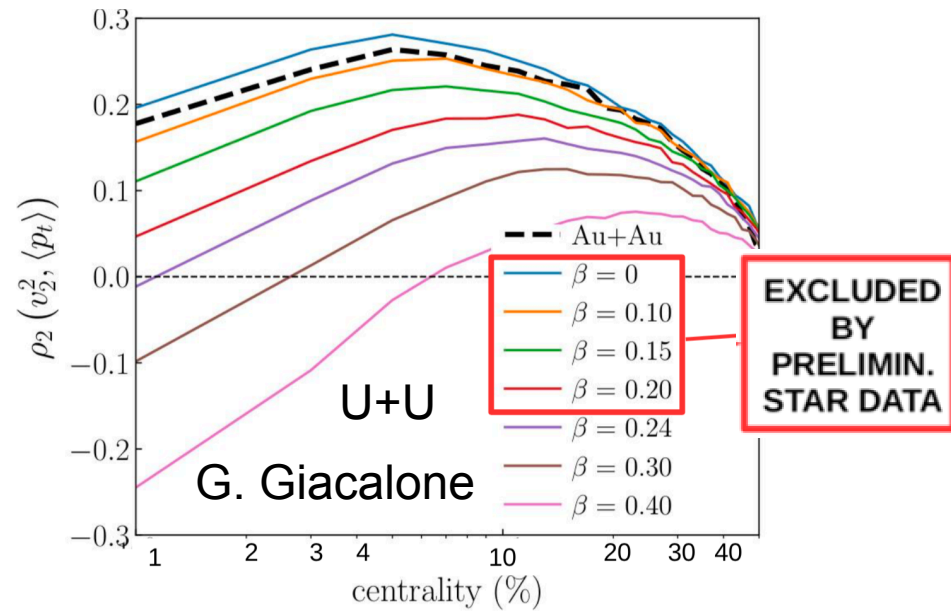
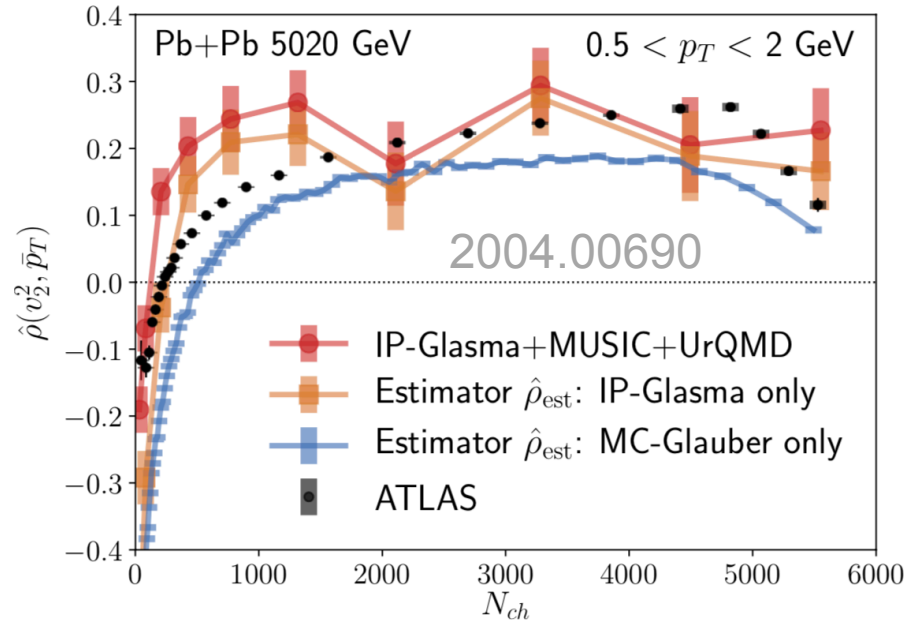


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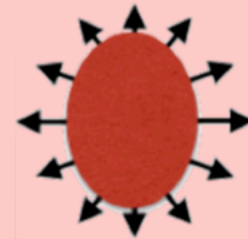
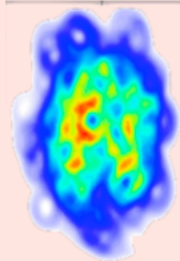
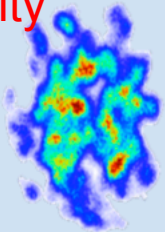
Disentangle early-time dynamics

Initial state
 $t \approx 0$ fm/c

Pre-equilibrium
 $t < 0.5$ fm/c

Hydrodynamics
 $t \sim 0.5-5$ fm/c

eccentricity



momentum anisotropy
e.g. mini-jets, glasma

Non-equilibrium
transport

Collective expansion

Geometry-uncorrelated

Geometry Response

Nucleon & subnucleon

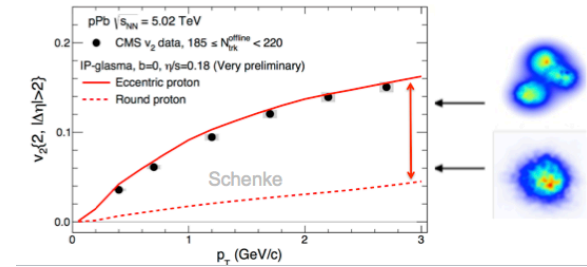
AuAu/PbPb

pp/pA/dA/HeA
???

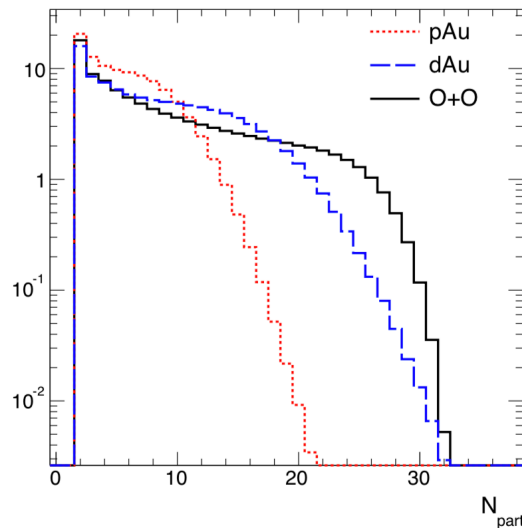
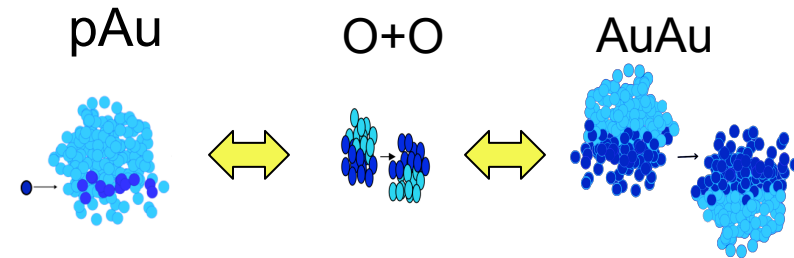
Extend lever-arm with symmetric small A+A collisions
to disentangle different contributions

Why small A+A?

Subnucleon DOF is important for pAu ridge:



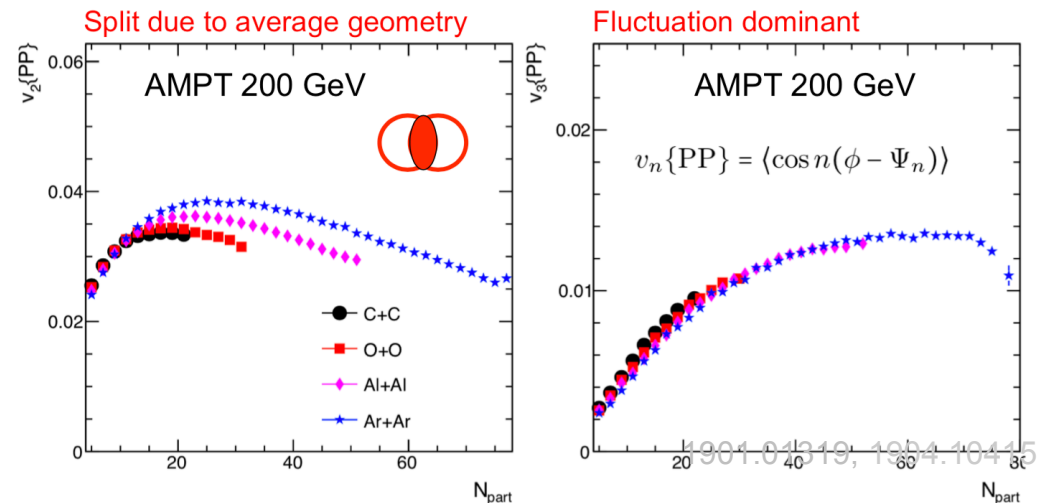
Nucleon & subnucleon DOF comparable in small A+A \rightarrow Bridging pAu and AuAu



O+O a reasonable choice in terms of N_{part} coverage

	pAu	dAu	$^{16}\text{O}+^{16}\text{O}$
$\langle N_{part} \rangle$	5.8	8.8	9.5

Disentangle nucleon geometry vs fluctuations

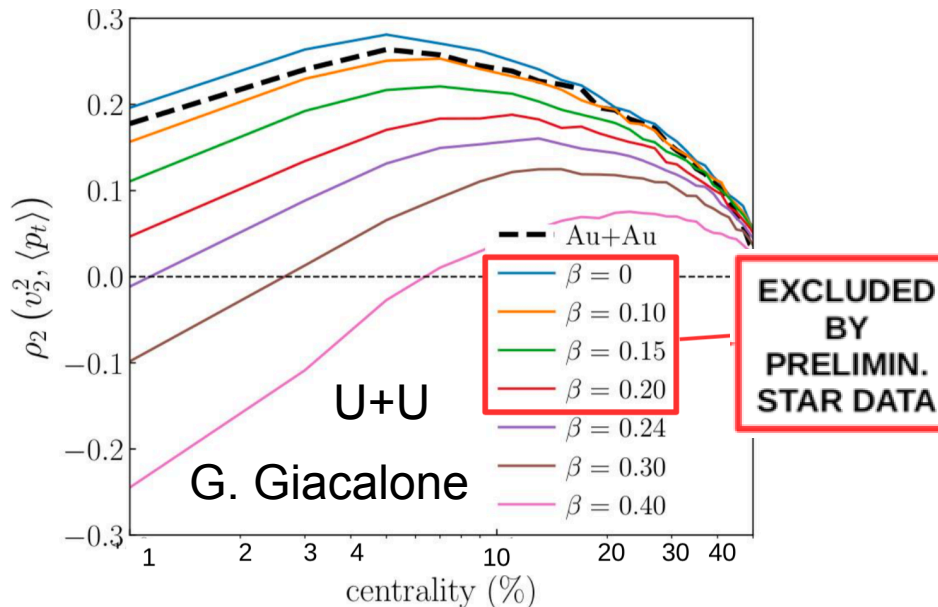


- STAR is pushing for a short O+O run in 2021
- Synergy with planned LHC O+O run in 2023: **identical Glauber geometry, but different subnucleonic fluct. (Q_s)**.

Collision System Scan

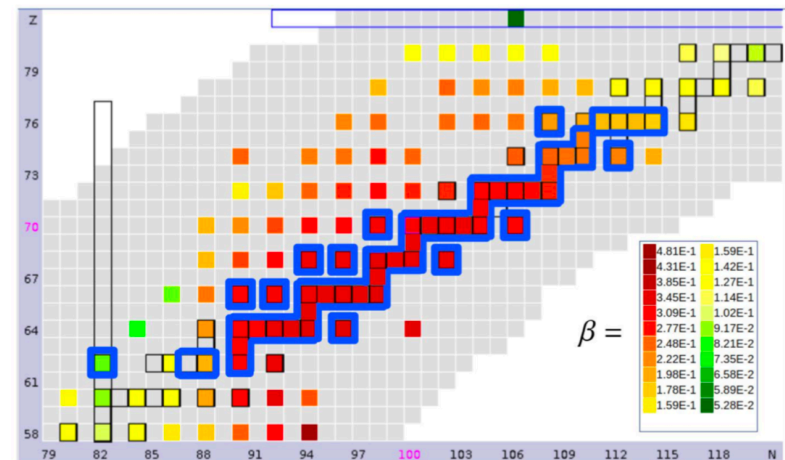
- Beam Energy Scan program has been vastly successful
 - Explore QCD Phase diagram
 - Bridge between high T and high μ_B frontiers
- An extensive system-size scan could be equally fruitful
 - Detailed exploration of the initial state via hydrodynamics $v_n = k_n \epsilon_n$
 - New tool for nuclear structure physics via $v_n - v_n$, $v_n - p_T$, $p_T - p_T$ correlations

Nuclear deformation



Region $144 < A < 190$ populated by large well-deformed nuclei.
Systematic study of nuclear deformation at RHIC.
Simple proposal.

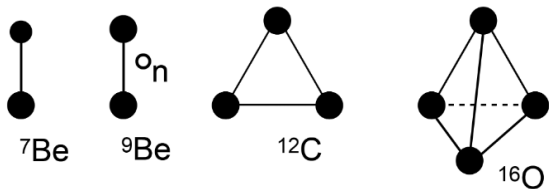
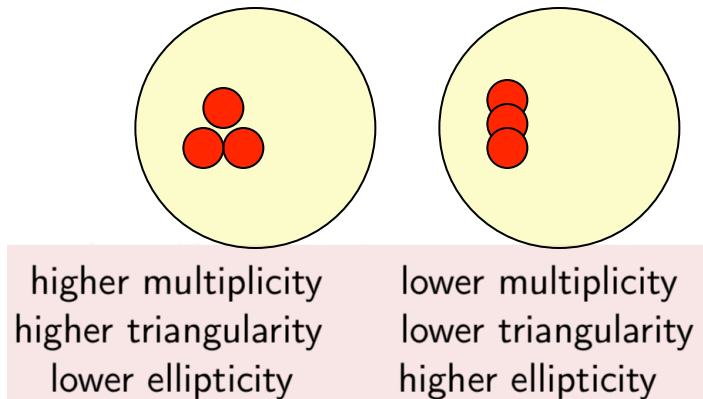
<https://www.nndc.bnl.gov/nudat2/>



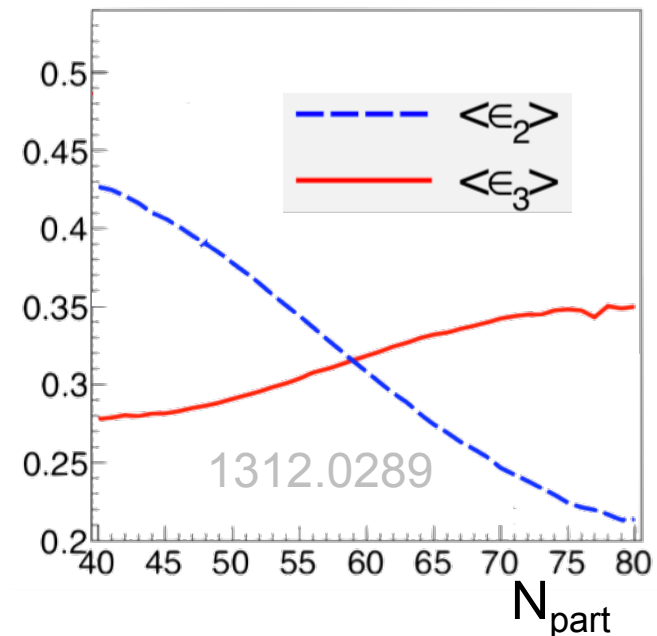
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Alpha-clustering Analyzing ^{12}C structure via collisions with a “disk” of Au:



1711.00438



Explore Be/C/O+Au collisions

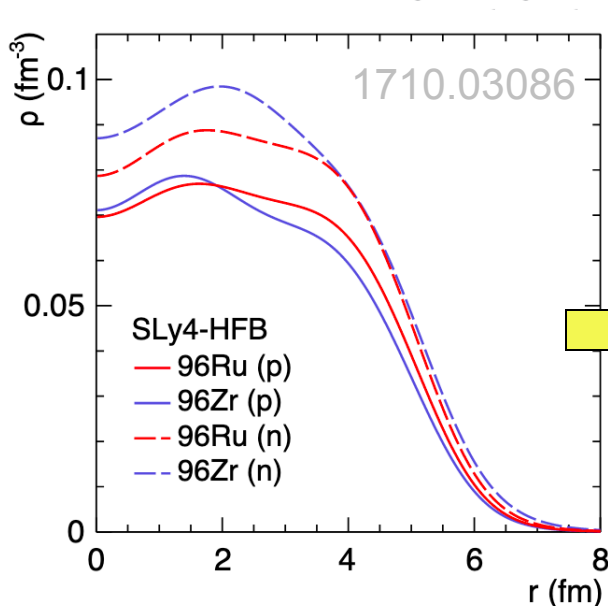
Collision System Scan

Scan doable during sPHENIX era 2023-2027!

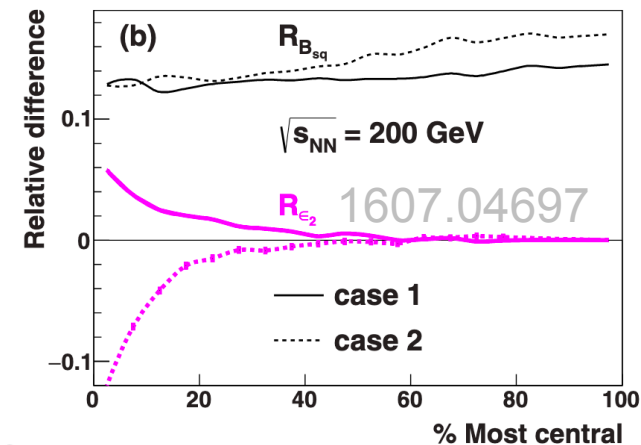
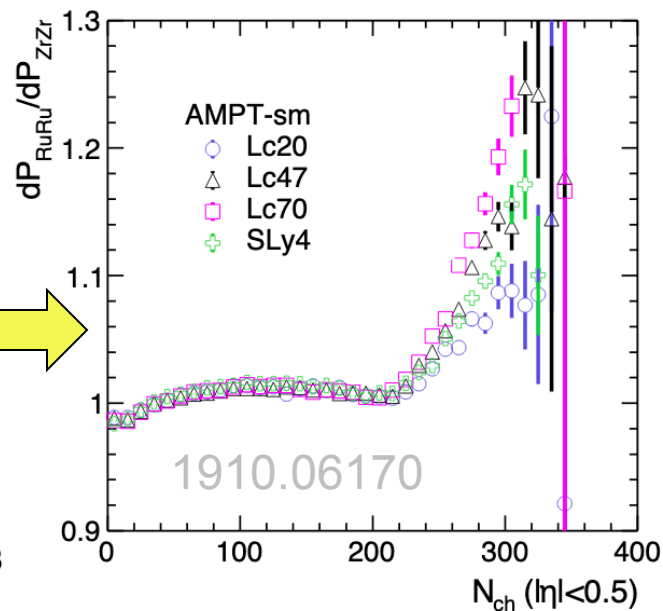
- Beam Energy Scan program has been vastly successful
 - Explore QCD Phase diagram
 - Bridge between high T and high μ_B frontiers
- An extensive system-size scan could be equally fruitful
 - Detailed exploration of the initial state via hydrodynamics $v_2 = \kappa_2 \varepsilon_2$
 - New tool for nuclear structure physics via $V_n - V_n$, $V_n - p_T$, $p_T - p_T$ correlations

Neutron skin

$^{96}_{44}\text{Ru} + ^{96}_{44}\text{Ru}$ $^{96}_{40}\text{Zr} + ^{96}_{40}\text{Zr}$

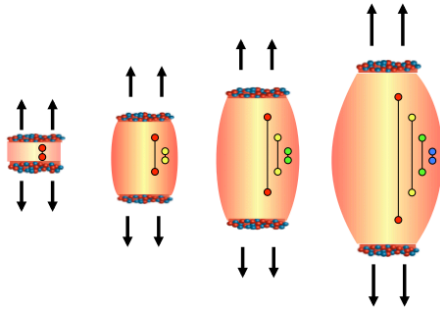


Isobar-run demonstrates RHIC ability for controlled study of nuclei geometry

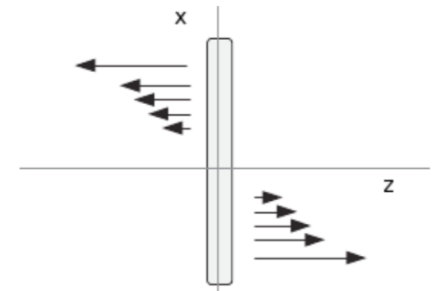


New frontier: Rapidity correlations

Many sources of fluctuations, generated at different time, and has different longitudinal/transverse dynamics

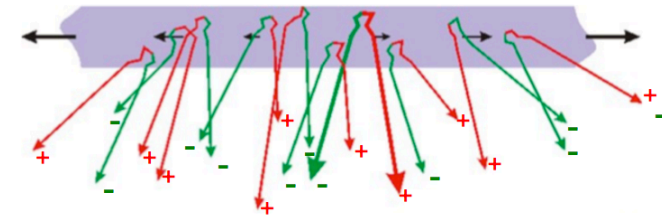


Longitudinal flow

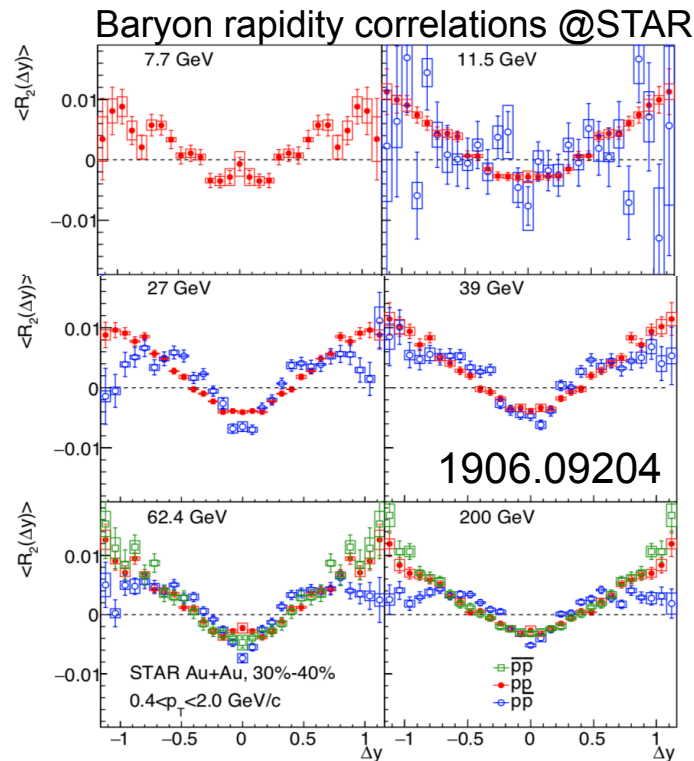
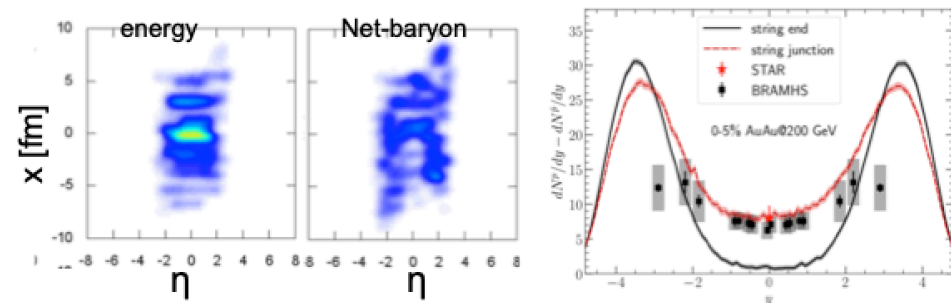


Charge transport

Balance function

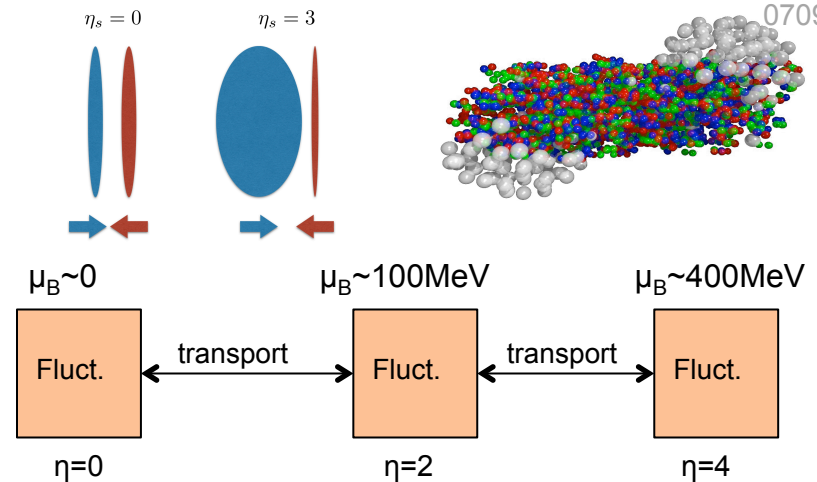
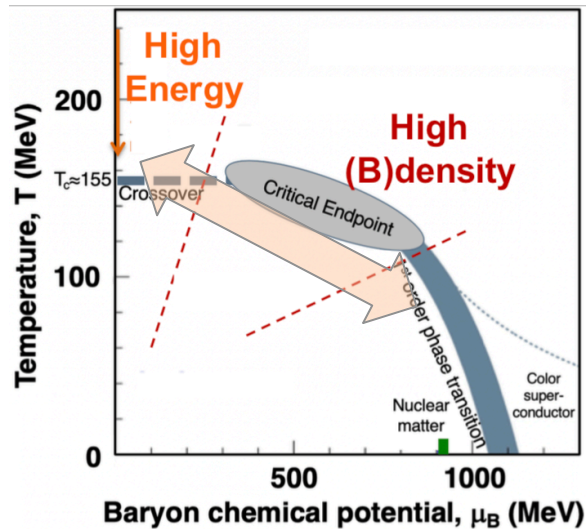


Net-baryon transport

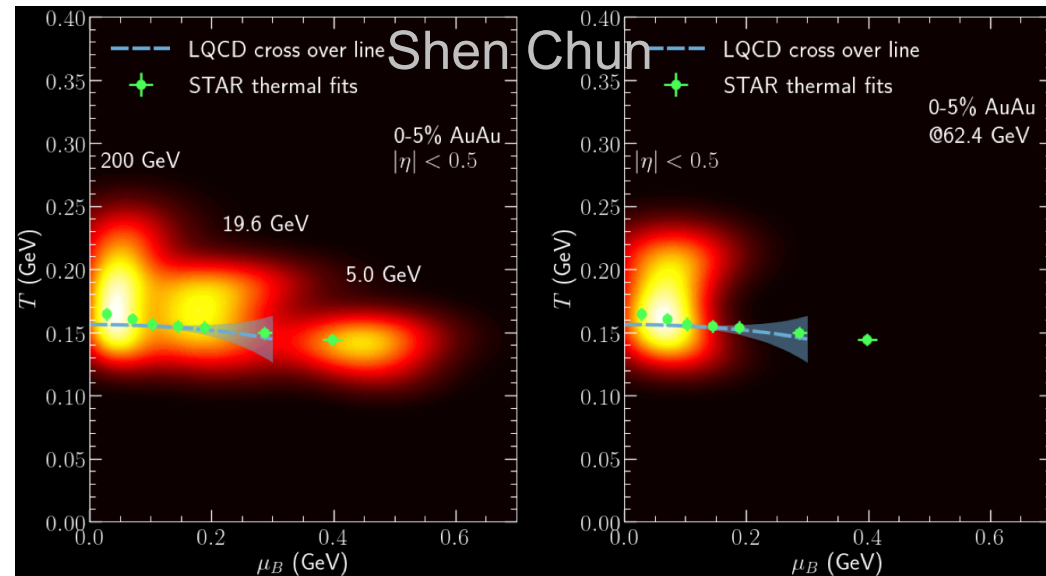


Rapidity Scan

- Rapidity scan at fixed \sqrt{s} \leftrightarrow Beam-Energy scan within same event
 - Similar properties but very different dynamics
 - More information, especially flow fluctuations \rightarrow more constrain on 3D hydrodynamics

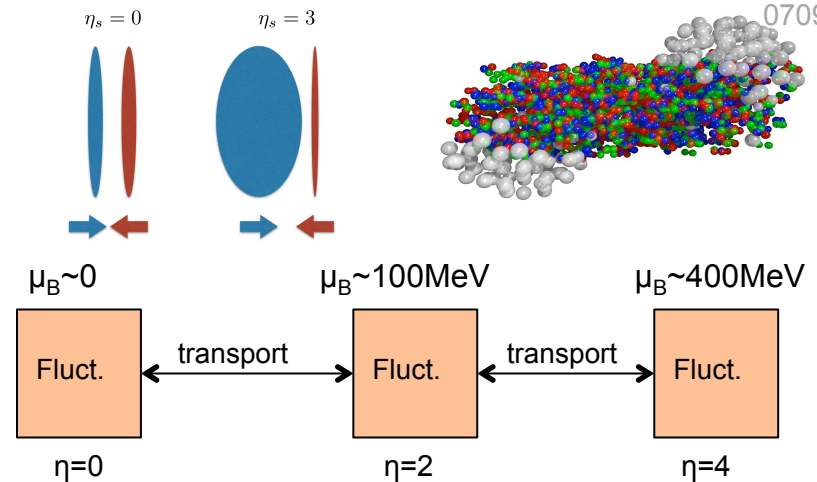
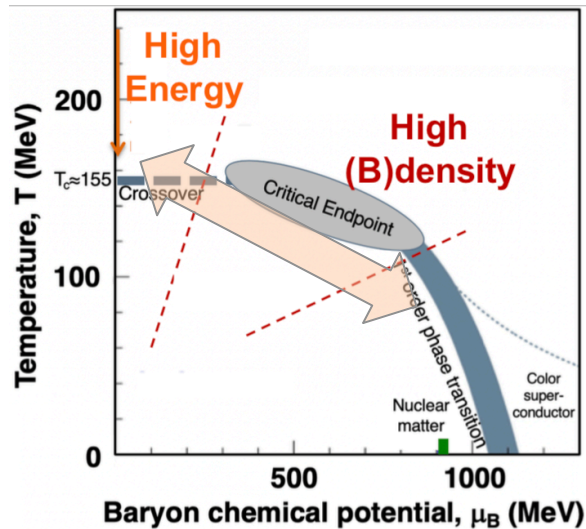


New handle on phase diagram, dynamics and properties

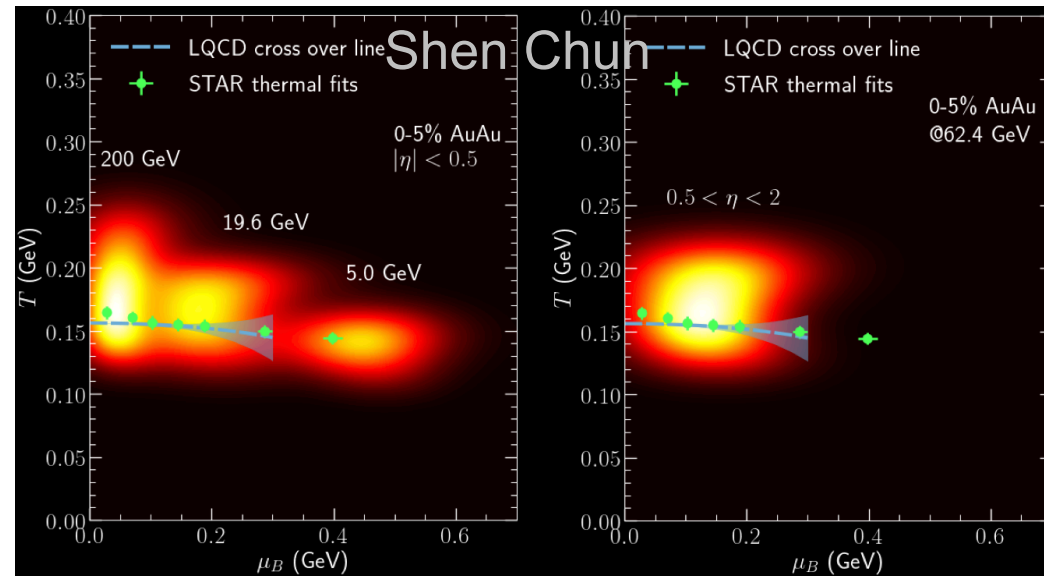


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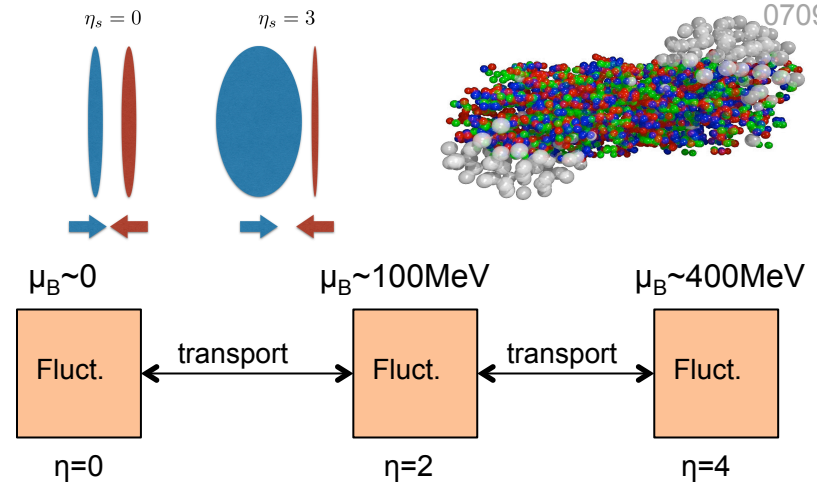
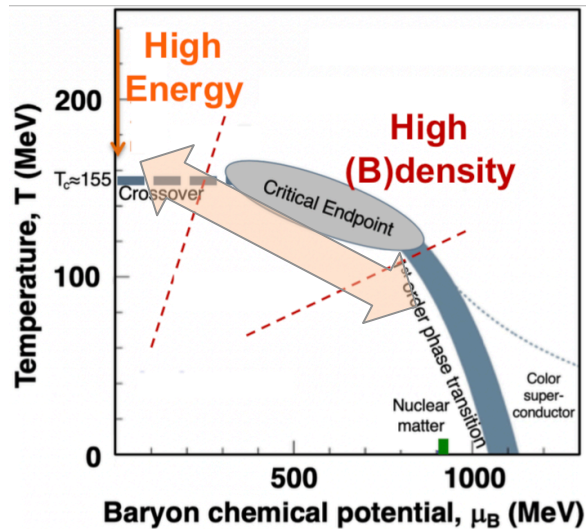


New handle on
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dynamics and
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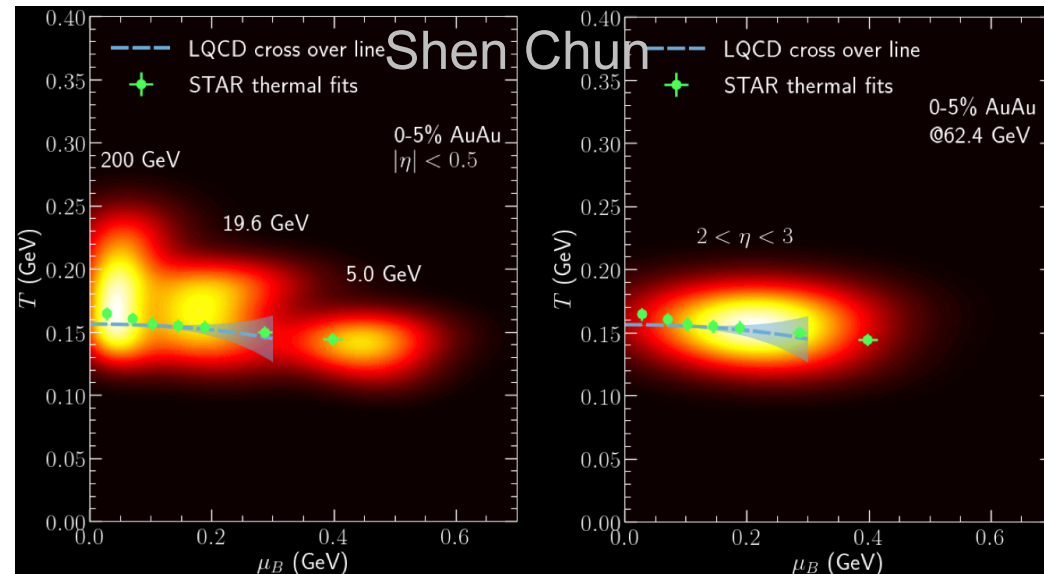


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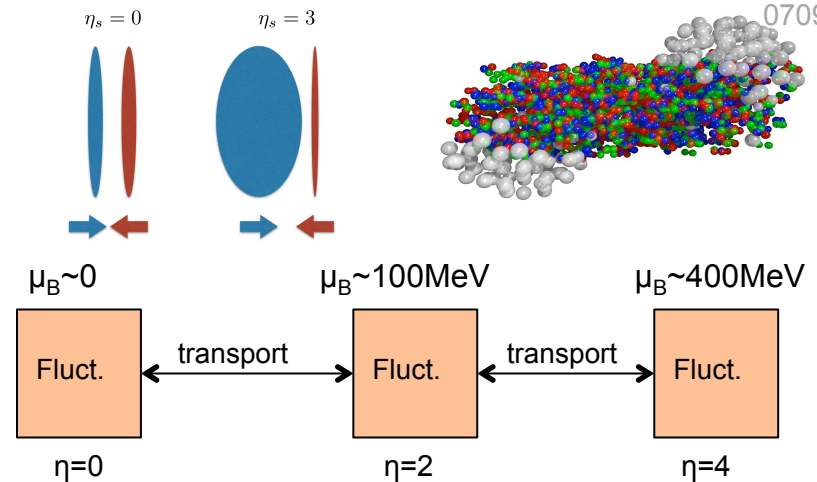
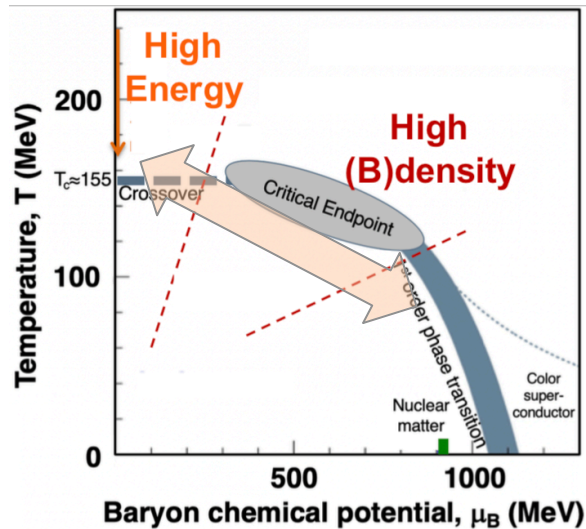


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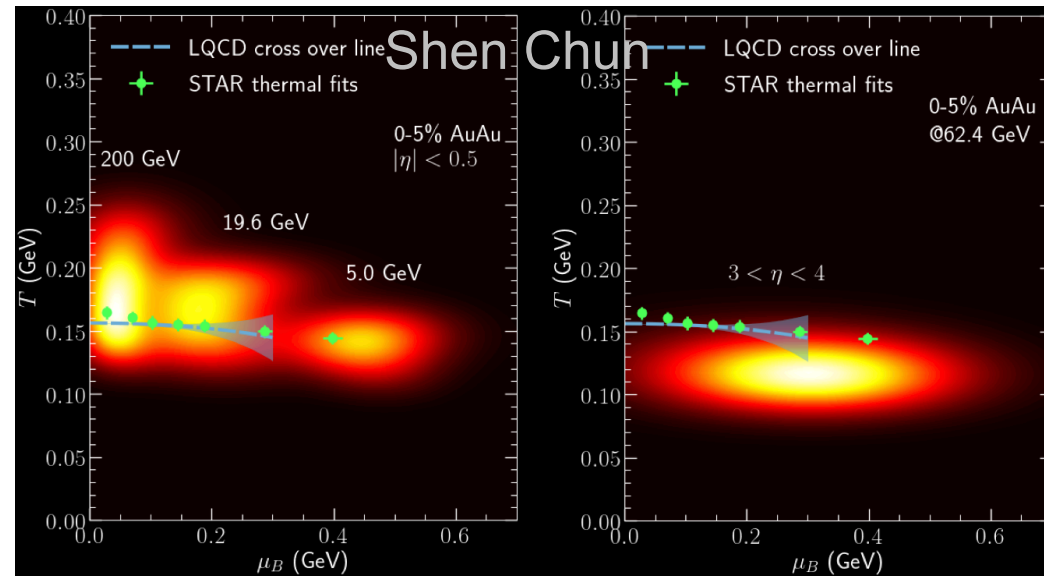


Rapidity Scan

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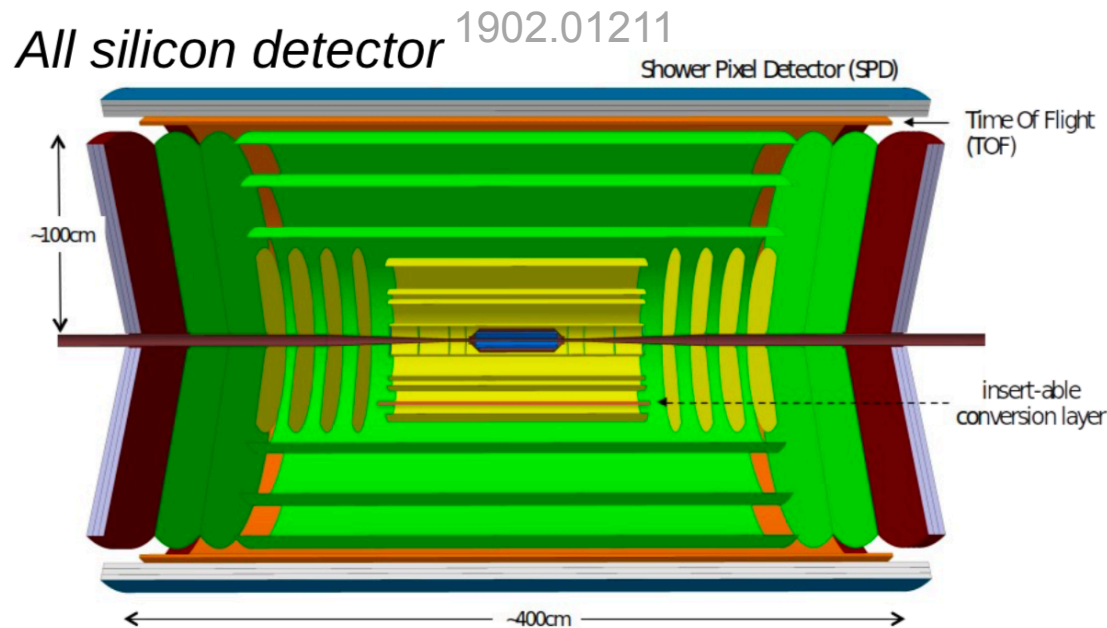


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Rapidity Scan

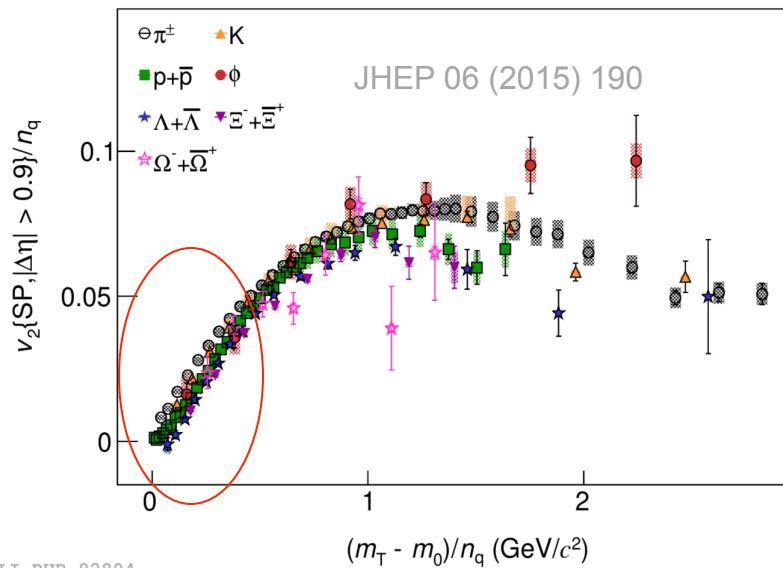
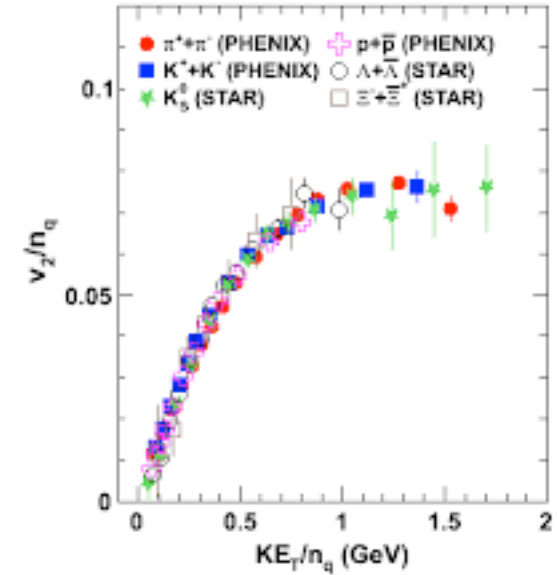
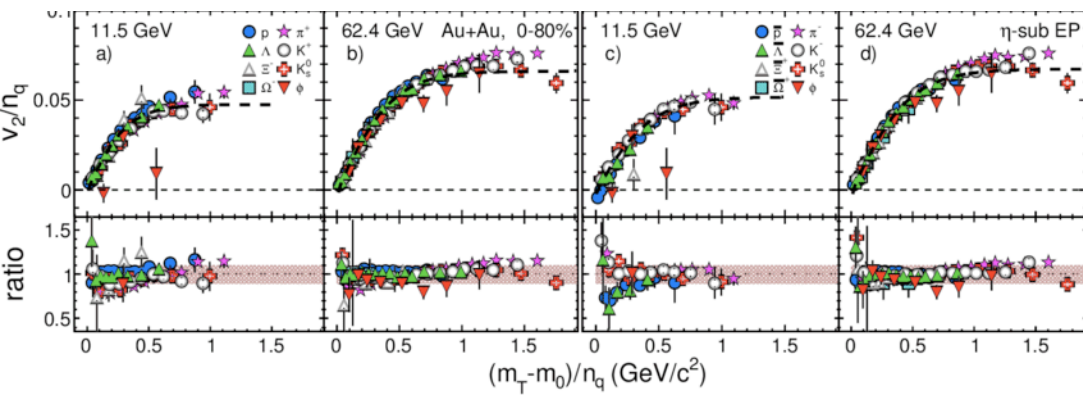
- A possibility with future detector upgrades
 - STAR forward upgrade $2.5 < \eta < 4$ with p_T and maybe some PID information
 - ATLAS/CMS forward upgrades with some PID capability
 - New hermetic HI detector with PID and $|\eta| < 4$
- LHC @ lower \sqrt{s} and explore the rapidity correlations?



Summary

- Collective flow & hydrodynamics are most important tools to gain understanding on the dynamics and properties of HI
- Key challenge: how to disentangle different stages.
 - Initial geometry, initial flow and non-equilibrium dynamics
 - Longitudinal dynamics is crucial for BES
 - Comment: precision at high \sqrt{s} as baseline for modeling the more complex physics at low \sqrt{s} .
- Future opportunities
 - Need new approaches and observables to pinpoint initial state
 - Collision system scan to understand initial geometry and initial flow
small A+A, deformation, alpha cluster
 - Rapidity scan as another handle on Phase diagram and longitudinal dynamics.

NCQ scaling

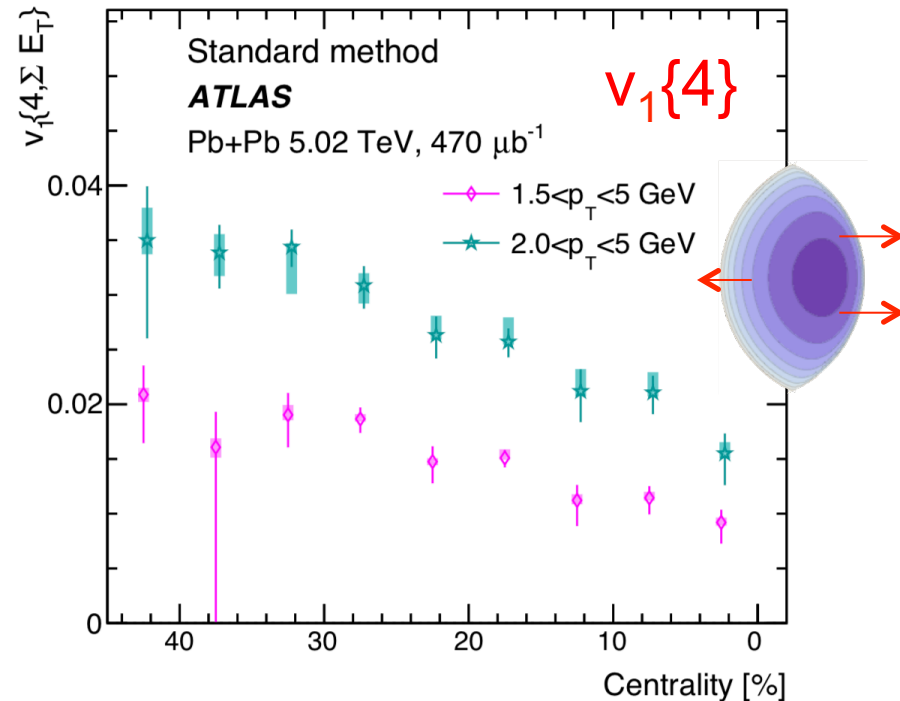
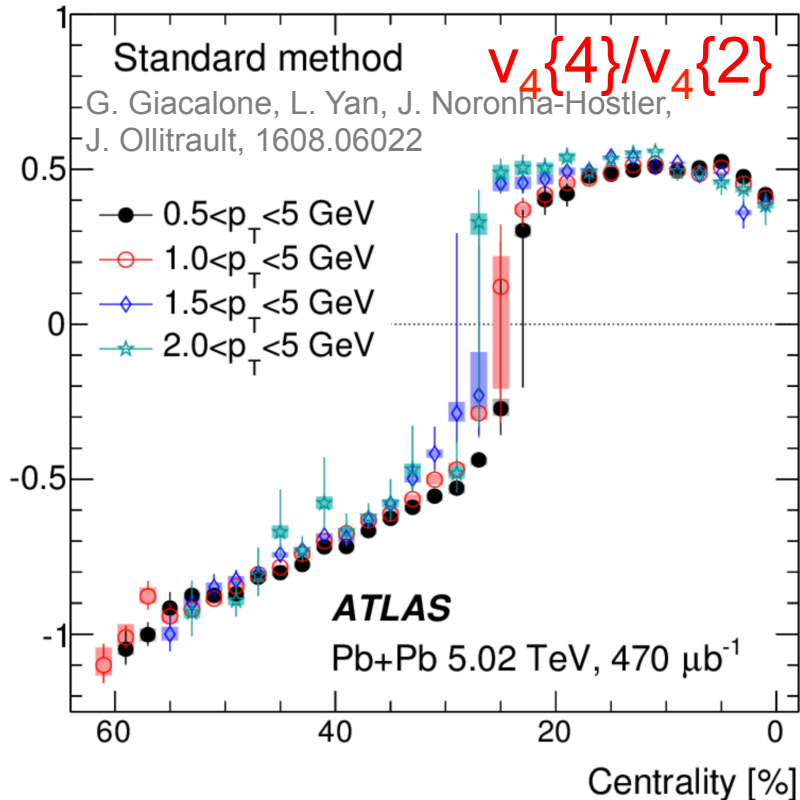


Higher-order flow fluctuations

$$(v_n\{4\})^4 \equiv 2\langle v_n^2 \rangle^2 - \langle v_n^4 \rangle$$

Peculiar sign change in v_4 fluctuations
 → Not explained by non-linear effects

Significant dipolar flow fluctuations



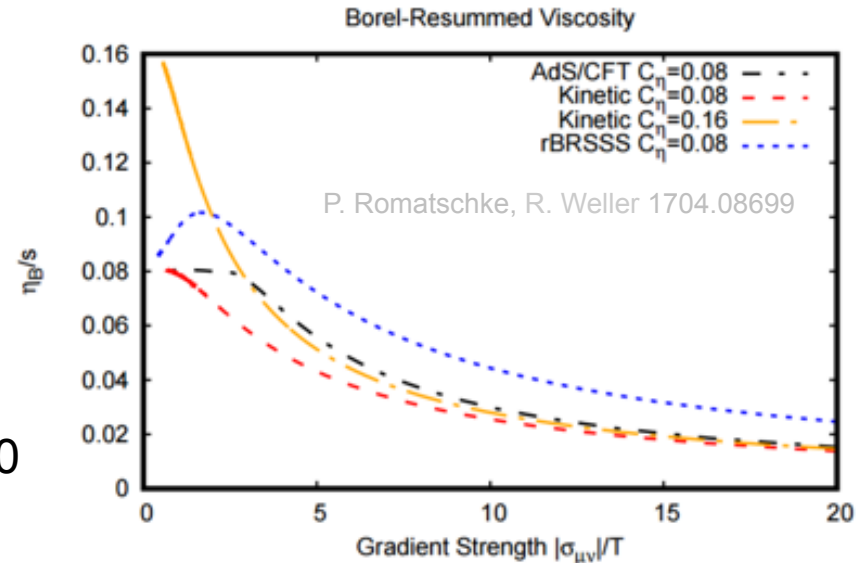
Unreasonable success of hydro?

- In far from equilibrium region, hydro still fit the data, but gives wrong viscosity

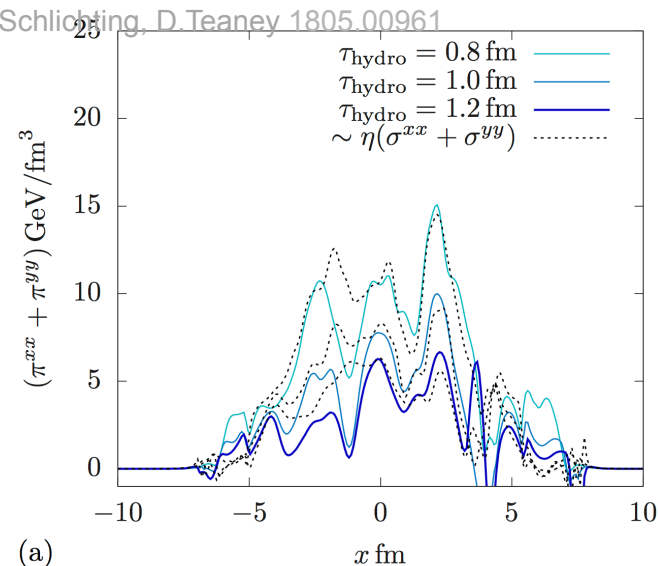
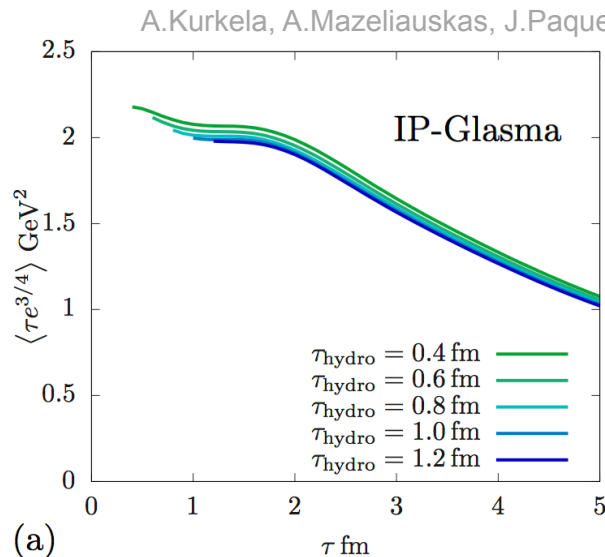
$$T_{\text{hydro}}^{\mu\nu} = (\epsilon + P_B)u^\mu u^\nu + P_B g^{\mu\nu} - \eta_B \sigma^{\mu\nu}$$

Small gradients $\eta_B \sim \eta$ Large gradients $\eta_B \rightarrow 0$

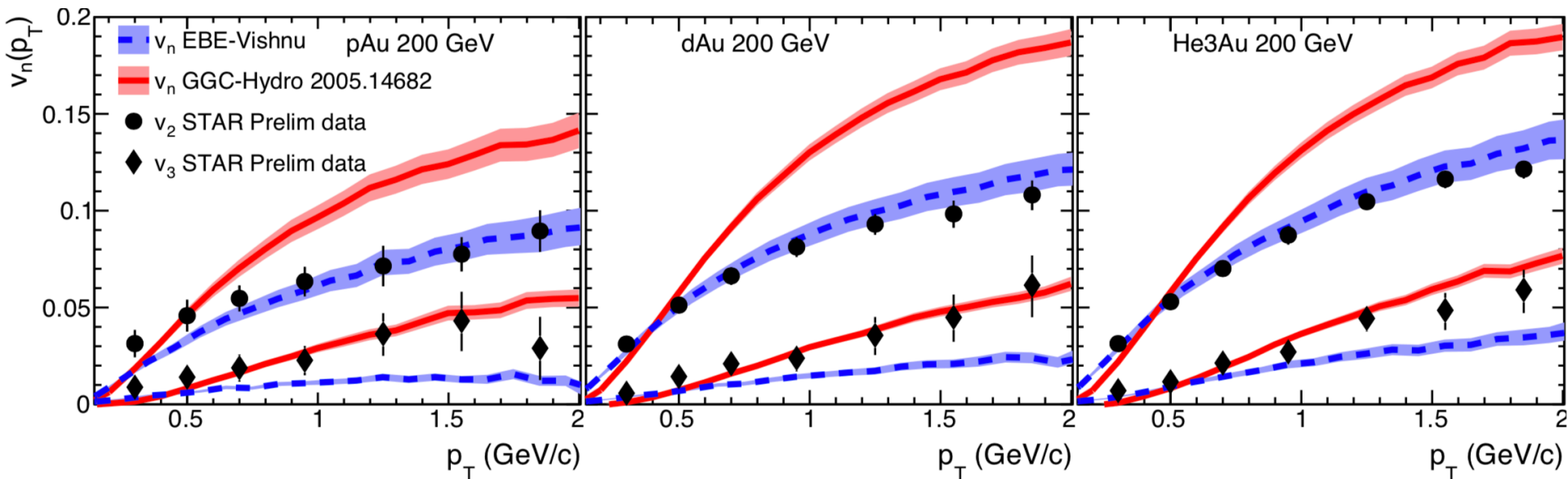
Also A.Kurkela, U.Wiedemann, B. Wu 1805.04081



- Different models for early-time dynamics have similar average hydro-field, but different differential distri., e.g shear tensor $\pi^{\mu\nu}(\mathbf{x})$.



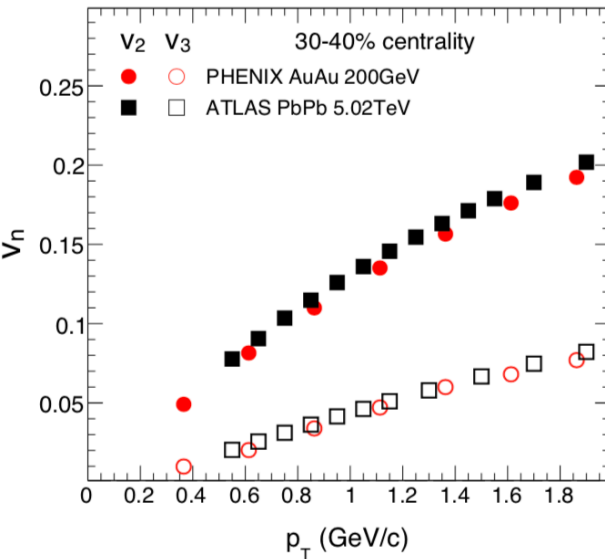
Small system



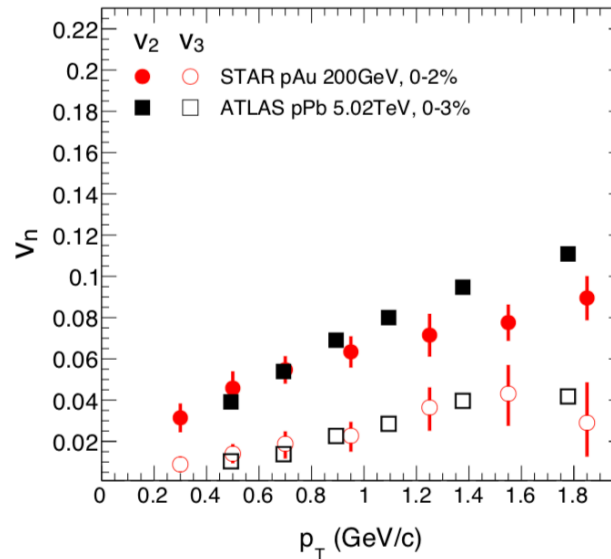
- Current models can't simultaneously describe v_2 and v_3
 - iEBE-Vishnu underestimate v_3
 - CGC-Hydro over-estimate v_2 (driven mainly by initial flow).

Compare RHIC and LHC

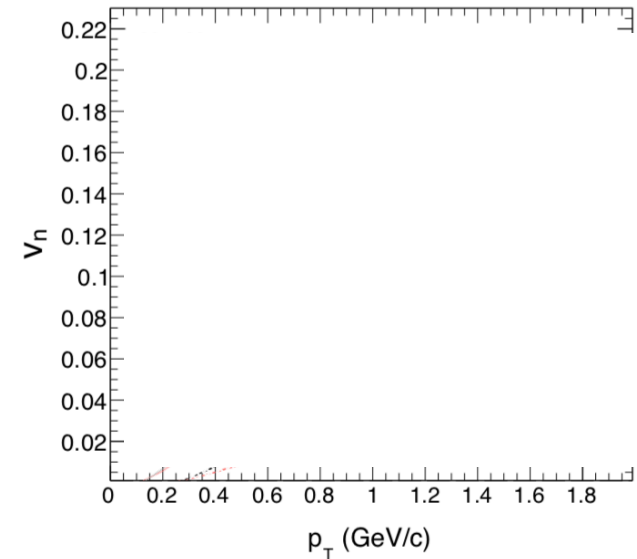
AuAu vs PbPb



pAu vs pPb



OO@RHIC vs OO@LHC?



No difference between PbPb@LHC and AuAu@RHIC

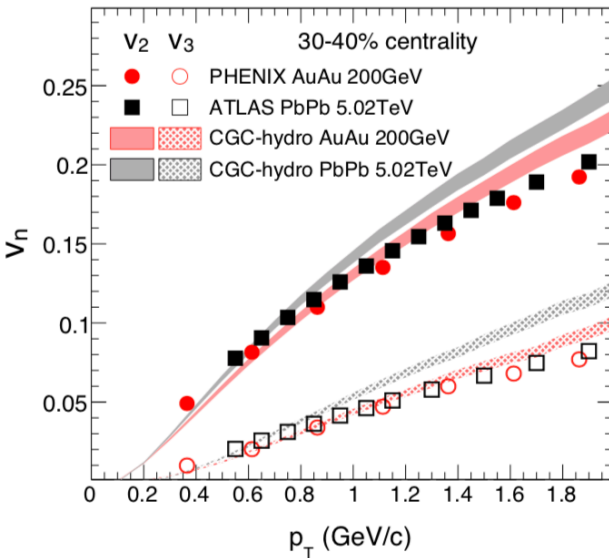
No difference between pPb@LHC and pAu@RHIC

Will OO@LHC and OO@RHIC show consistent trend?

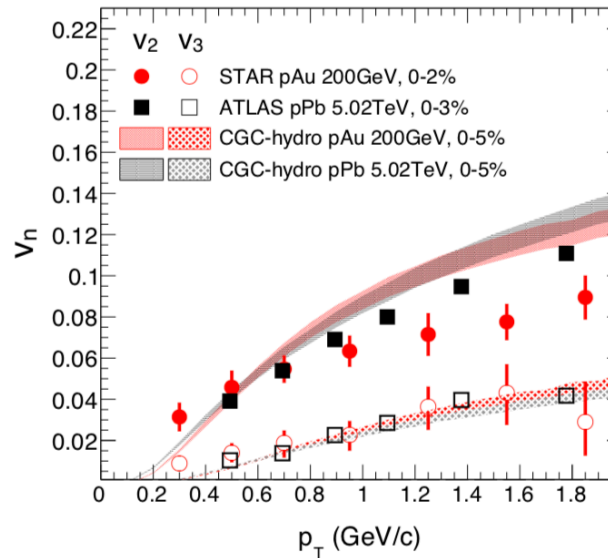
Agreement between two energies does not mean same viscous effects

Compare RHIC and LHC

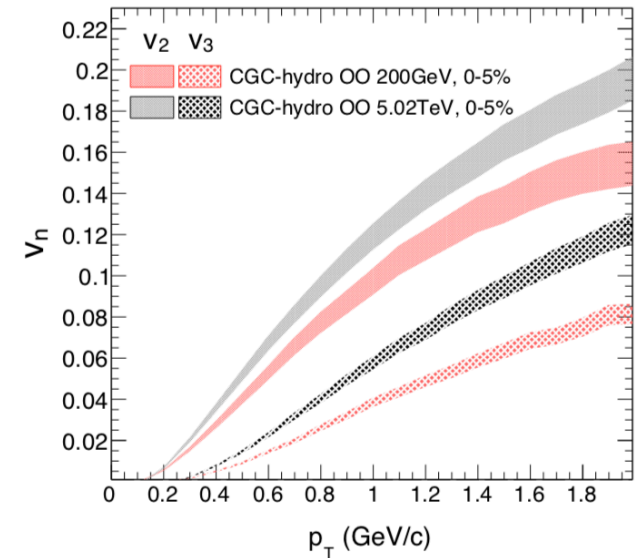
AuAu vs PbPb



pAu vs pPb



OO@RHIC vs OO@LHC?



No difference between PbPb@LHC and AuAu@RHIC

No difference between pPb@LHC and pAu@RHIC

Will OO@LHC and OO@RHIC show consistent trend?

What about model prediction?

- predict 30% difference for OO
- predict no difference for pA
- predict small difference for AA

The O+O comparison provides strong constraints on these models