

Review of the light nuclei production in both theoretical and experimental side

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Lawrence Berkeley National Laboratory
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RHIC BES seminar



Subject of this talk: Light nuclei and anti-nuclei

Anti-



Deuteron (d)



Deuteron (\bar{d})



Tritium (t)



Tritium (\bar{t})



Helium-3 (${}^3\text{He}$)



Helium-3 (${}^3\bar{\text{He}}$)



Hypertriton (${}^3_{\Lambda}\text{H}$)



Hypertriton (${}^3_{\Lambda}\bar{\text{H}}$)

Main question: Nuclei (or pp , or $p\bar{p}$, or e^+e^-) collide at high energy. How many light (anti-)nuclei of each sort will be born in collision and where do they fly?

Anti-helium by Alpha-Magnetic Spectrometer



- Few events (compatible with) ${}^3\overline{\text{He}}$, ${}^4\overline{\text{He}}$
Caveats: hard measurement, 1 event/year, not published
- Where do they come from?
Antimatter clouds? Dark matter annihilations? pp collisions?

Is anti-helium at AMS compatible with $pp \rightarrow \overline{\text{He}}$?

- K. Blum, K. C. Y. Ng, R. Sato and M. Takimoto,
"Cosmic rays, antihelium, and an old navy spotlight," , PRD 96, no. 10, 103021 (2017)

Conclusion: $\overline{\text{He}}$ production compatible with pp

- V. Poulin, P. Salati, I. Cholis, M. Kamionkowski and J. Silk,
"Where do the AMS-02 antihelium events come from?" , PRD 99, no. 2, 023016 (2019)

Conclusion: pp cannot produce that much $\overline{\text{He}}$
advocate presence of anti-clouds in our Galaxy

- M. Kachelriess, S. Ostapchenko and J. Tjemsland
"Revisiting cosmic ray antinuclei fluxes with a new coalescence model" , arXiv:2002.10481 [hep-ph]

Conclusion: $\overline{\text{He}}$ production compatible with pp

Different coalescence models, tuned to (subsets of) data from

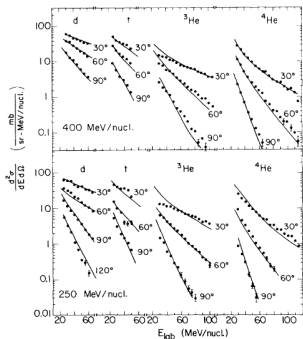
- $e^+e^- \rightarrow \overline{\text{He}}$ at Z resonance [ALEPH, OPAL]
- $pp \rightarrow \overline{\text{He}}$ at 53 GeV [CERN ISR], at 0.9, 2.76, 7 TeV [ALICE]

Naive coalescence framework

- Nuclei are formed at late stages of collision
- Nucleons bind into nuclei if they are close in phase space

$$E_A \frac{dN_A}{d^3P_A} = B_A \left(E_p \frac{dN_p}{d^3P_p} \right)^Z \left(E_n \frac{dN_n}{d^3P_n} \right)^N \Bigg|_{P_p=P_n=P_A/A}$$

B_A : B_2 for deuteron, B_3 for tritium, ${}^3\text{He}$, B_4 for ${}^4\text{He}$



p_0 “coalescence momentum”

$$B_A = \frac{1}{Z!(A-Z)!} \left(\frac{4}{3} \pi p_0^3 \right)^{A-1}$$

Gutbrod et al, PRL 37 (1976) 667-670

Described $A = 2, 3, 4$ spectra in

$\text{Ne} + \text{U}$ at 250, 400 A MeV

But: different p_0 for each A

Note large sensitivity to p_0

Not state-of-the art approach for B_A

The role of wavefunction and source size

Overlap of nucleus wavefunction and source size matters

Sato, Yazaki, Phys. Lett. 98B (1981) 153-157

For deuteron:

$$\frac{4}{3}\pi p_0^3 \Rightarrow 2^3 \frac{3}{4} (2\pi)^3 \int d^3\vec{r} |\Psi_d(\vec{r})|^2 S_2(\vec{r})$$
$$S_2(\vec{r}) = \int d\vec{r}' S_p(\vec{r} - \vec{r}') S_n(\vec{r}')$$

$S_{p,n}$ – normalized spatial distributions of p,n; “source functions”

$\Psi_d(\vec{r})$ – deuteron wavefunction

Relation to femtosopic (HBT) correlations

Scheibl, Heinz, Phys.Rev. C59 (1999) 1585-1602

Blum, Takimoto, PRC 99, no.4, 044913 (2019)

$$C_2(p, q) = \int d^3\vec{r} \Psi_{pp}(q, \vec{r}r) S_2(\vec{r})$$
$$\Psi_{pp}(q, \vec{r}) \sim (e^{iqr} \pm e^{-iqr})$$

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Analytical coalescence

- Source is homogeneous on the scale of wavefunction size
- Gaussian source
- $q^2 \ll m^2$
- A-particle correlation function = \prod (2-particle correlations)
Scheibl, Heinz, Phys.Rev. C59 (1999) 1585-1602
Blum, Takimoto, PRC 99, no.4, 044913 (2019), m vs m_T discrepancy

$$\frac{B_A}{m^{2(A-1)}} \approx \frac{2J_A+1}{2^{A-1}\sqrt{A}} \left(\frac{\pi^{3/2}}{m^3(R_\perp^2(p_T)+d_A^2/4)^2(R_\parallel^2(p_T)+d_A^2/4)} \right)^{A-1}$$

Simplified qualitative expectations:

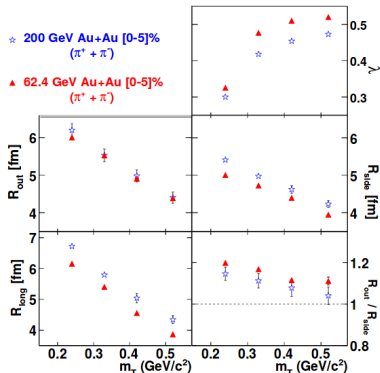
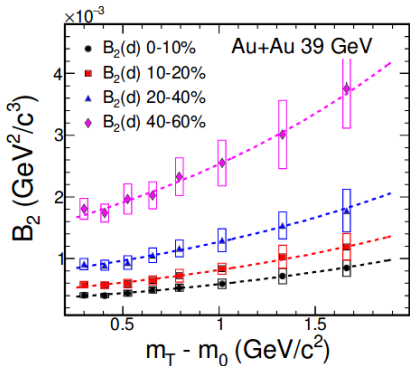
- $B_A \sim V_{HBT}^{-(A-1)}$
- $B_2 \sim 1/V_{HBT}$, $B_3 \sim 1/V_{HBT}^2$
- $B_A(p_T) \approx \text{const}$ in pp
- larger charged multiplicity, smaller B_A

Are these expectations fulfilled?

Dependencies of B_2 : transverse momentum

STAR, PRC 99 (2019) 6, 064905

PRC 80 (2009) 024905

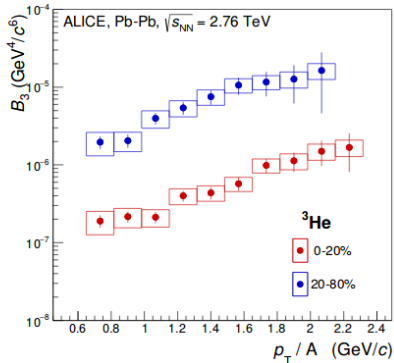
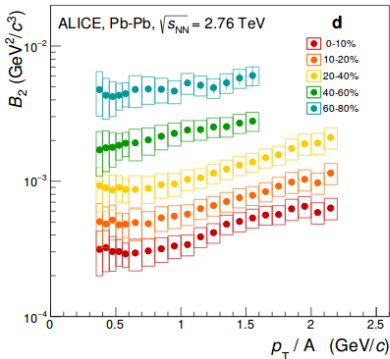


compatible with coalescence expectation

$$V_{HBT}(m_T) \downarrow, B_2(m_T) \uparrow$$

Dependencies of B_2 : transverse momentum

ALICE, PRC93 (2016) no.2, 024917

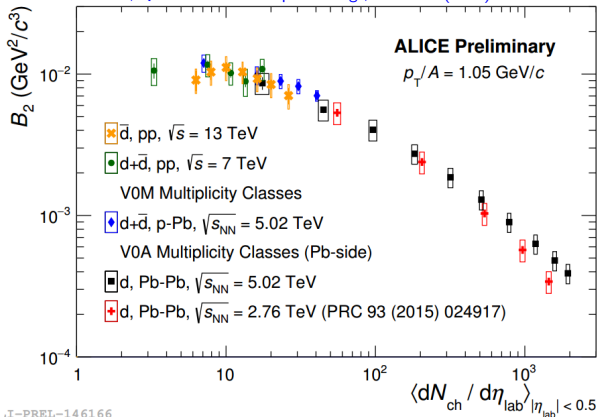


compatible with coalescence expectation

$$V_{HBT}(m_T) \downarrow, B_2(m_T) \uparrow$$

Dependencies of B_2 : system size

M. Puccio, Quark Matter 2018 proceedings, NPA 982 (2019) 447-450



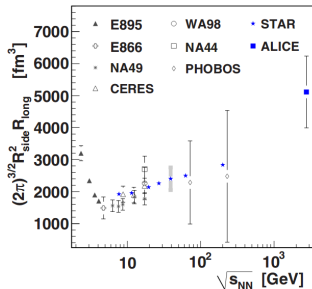
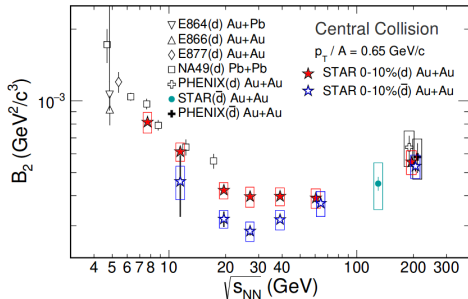
compatible with coalescence expectation

$$V \uparrow, B_2 \downarrow$$

Dependencies of B_2 : collision energy

STAR, PRC 92 (2015) no.1, 014904

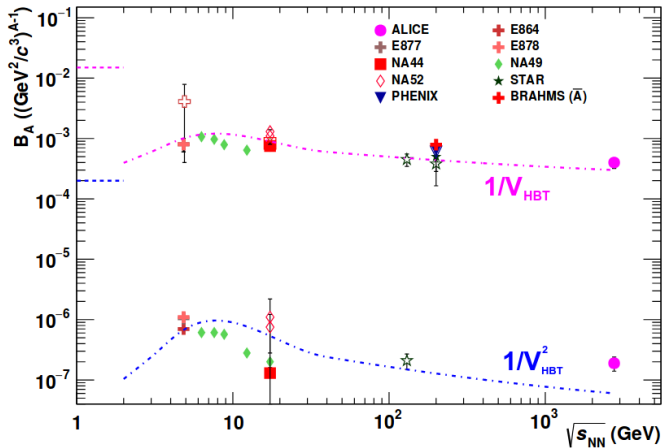
STAR, PRC 99 (2019) 6, 064905



Not really compatible with $B_A \sim V_{HBT}^{-(A-1)}$ qualitatively!

Dependencies of B_2 : collision energy

Braun-Munzinger, Dönigus Nucl. Phys. A 987 (2019) 144-201

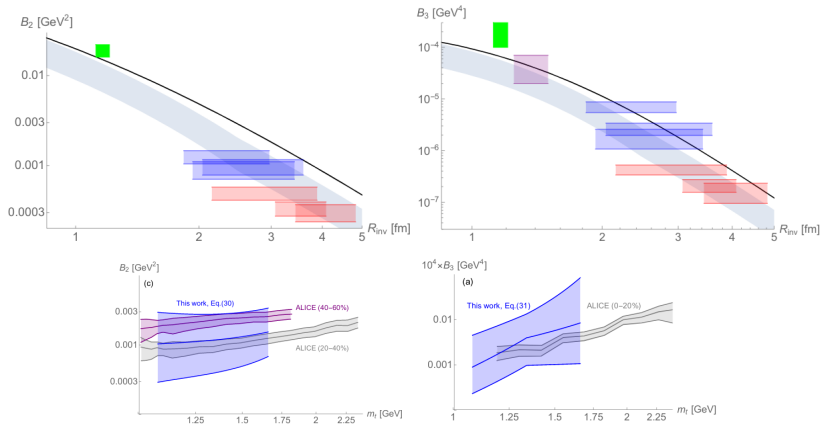


But the order of magnitude is still right

More quantitative comparison

Blum, Takimoto, PRC 99, no.4, 044913 (2019)

Bellini, Blum, Kalweit, Puccio, 2007.01750 [nucl-th]



Need HBT-measurement, further comparison for NA49, STAR data

Challenge: simple phenomenological formula to fit

$$B_A(\sqrt{s}, dN_{ch}/d\eta, p_T, y)$$

Testing coalescence with hypertriton

${}^3_{\Lambda}\text{H}$ is d bound to Λ by 130 keV, size ~ 10 fm

Large wavefunction compared to system size \Rightarrow suppression

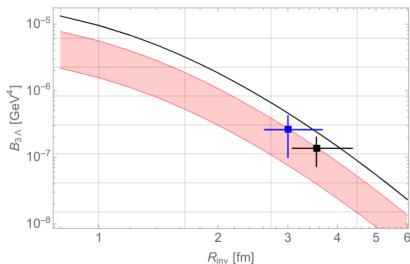
- Coalescence model is far below the data

[Bellini, Kalweit, Phys. Rev. C99 \(2019\) no.5, 054905](#)

- Coalescence model is compatible with the data

[Zhang, Ko, PLB 780, 191-195 \(2018\)](#); [Bellini, Blum, Kalweit, Puccio, 2007.01750 \[nucl-th\]](#)

More careful consideration of ${}^3_{\Lambda}\text{H}$ wavefunction



Research in progress, waiting for more ALICE, and for STAR measurements

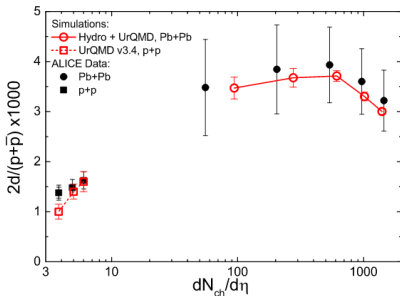
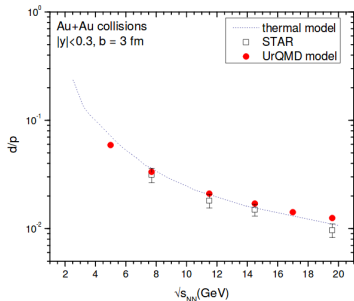
Need ${}^3_{\Lambda}\text{H}$ and HBT measurements

Realistic source function: [hydro +] transport + coalescence

Recipe to make a deuteron:

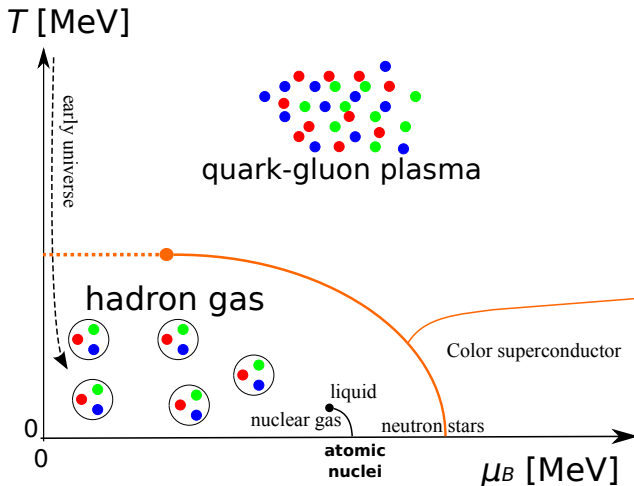
1. Take nucleon pair at $t =$ maximum of last interaction times
2. Boost to their rest frame
3. Bind $|\Delta p| < 0.28$ GeV and $|\Delta x| < 3.5$ fm
4. Take isospin factor into account

UrQMD — Sombun et al, PRC 99 (2019) no. 1, 014901



Good description from low to high energies with 2 parameters

Light nuclei and critical fluctuations



Generic critical point feature: **spatial** fluctuations increase

Nucleon density fluctuations in coordinate space

Kaijia Sun et al., Phys. Lett. B 774, 103 (2017)

Kaijia Sun et al., Phys. Lett. B 781 (2018) 499-504

Proton and neutron density:

$$\rho_n(x) = \langle \rho_n \rangle + \delta \rho_n(x)$$

$$\rho_p(x) = \langle \rho_p \rangle + \delta \rho_p(x)$$

Correlations and fluctuations:

$$C_{np} \equiv \langle \delta \rho_n(x) \delta \rho_p(x) \rangle / (\langle \rho_n \rangle \langle \rho_p \rangle)$$

$$\Delta \rho_n \equiv \langle \delta \rho_n(x)^2 \rangle / \langle \rho_n \rangle^2$$

From a simple coalescence model

$$N_d \approx \frac{3}{2^{1/2}} \left(\frac{2\pi}{mT} \right)^{3/2} \int d^3x \rho_p(x) \rho_n(x) \sim \langle \rho_n \rangle N_p (1 + C_{np})$$

$$N_t \approx \frac{3^{1/2}}{4} \left(\frac{2\pi}{mT} \right)^3 \int d^3x \rho_p(x) \rho_n^2(x) \sim \langle \rho_n \rangle^2 N_p (1 + 2C_{np} + \Delta \rho_n)$$

$$\frac{N_t N_p}{N_d^2} = \frac{1}{2\sqrt{3}} \frac{1 + 2C_{np} + \Delta \rho_n}{(1 + C_{np})^2}$$

Thermal ratio

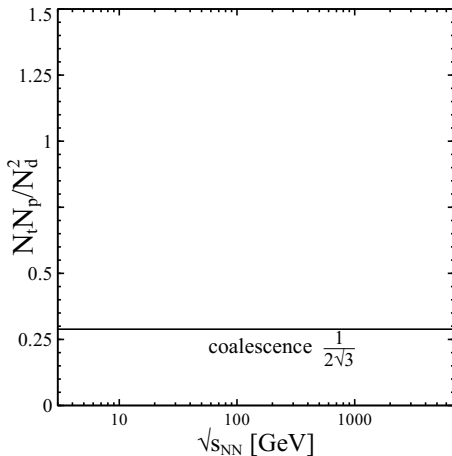
$$\frac{g_t g_p}{g_d^2} \left(\frac{3m \cdot m}{(2m)^2} \right)^{3/2} = \frac{1}{2\sqrt{3}} \approx 0.29$$

Fluctuations and correlations

Light nuclei are sensitive to spatial density fluctuations

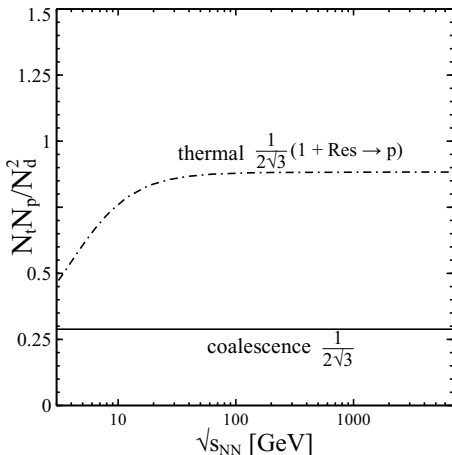
Comparing the p - d - t ratio to NA49, STAR, and ALICE data

Data: NA49 [Anticic:2010mp,Blume:2007kw,Anticic:2016ckv], STAR [Adam:2019wnb,Zhang:2019wun], ALICE [Adam:2015vda]; model JAM + coalescence [Liu:2019nii]



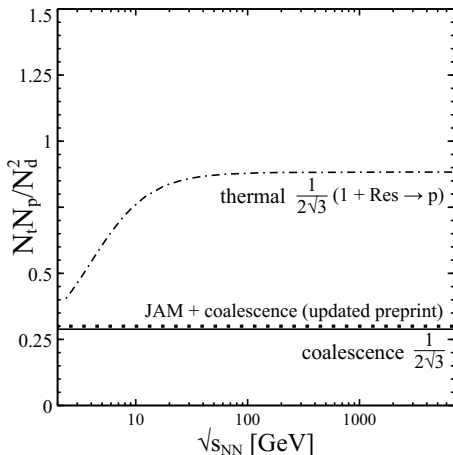
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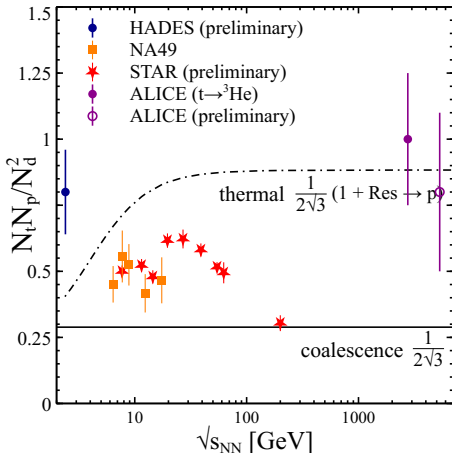
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Are the bumps related to fluctuations?

Critical point and ${}^4\text{He}$ excited states

- Deeply attractive nucleon-nucleon potential V around the critical point

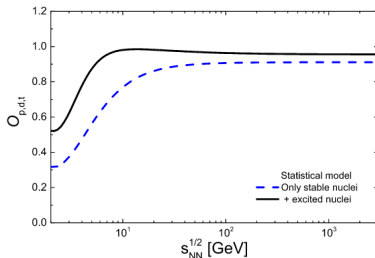
$$N_t N_p / N_d^2 \approx 0.29 \langle e^{-V/T} \rangle$$

$$N_\alpha N_t N_p^2 / N_{3\text{He}} N_d^3 \approx 0.42 \langle e^{-3V/T} \rangle: \text{ more sensitive}$$

[Shuryak, Torres-Rincon, PRC 101, no.3, 034914 \(2020\)](#)

- Decay of many ${}^4\text{He}$ excited states, thermal model, no V

[Vovchenko, Dönigus, Kardan, Lorenz, Stoecker, arXiv:2004.04411 \[nucl-th\]](#)



$$O_{p,d,t} \equiv N_p N_t / N_d^2$$

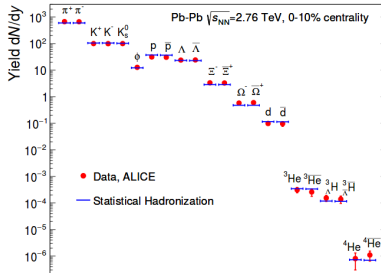
Thermal model and “snowballs in hell”

- Nuclei formed early — at hadronic freeze-out

$$N_A \approx g_A V (\pi T m_A / 2)^{3/2} e^{(A\mu_B - m_A)/T}$$

- ALICE fit of yields, Pb+Pb, $\sqrt{s_{NN}} = 2.76$ TeV: $T = 155$ MeV
- Nuclei momentum spectra: $T_{kin} \simeq 110$ MeV
- How can they survive from chemical to kinetic freeze-out?
- Binding energies per particle: d , ${}^3\text{He}$, ${}^3\text{H}$, ${}^4\text{He}$ – \simeq few MeV

Snowballs in hell.



Andronic, Braun-Munzinger, Redlich, Stachel, Nature 561 (2018) no.7723, 321-3305

Light nuclei: rapid chemical freeze-out at 155 MeV, like hadrons?

Relation of thermal + blast wave to coalescence model

Blast-wave model:

- Cooper-Frye formula on hypersurface Σ , $B \ll m$
- If boost-invariant hypersurface \Rightarrow Siemens-Rasmussen formula
- $\mu_{p,n}$ before resonance decays
normalization to thermal model yields
light nuclei formed at chemical freeze-out

$$E_d \frac{dN_d}{d^3p_d} = \int_{\Sigma} p_d^\mu d\sigma_\mu e^{(\mu_p - \frac{p_d^\nu}{2} u_\nu)/T} e^{(\mu_n - \frac{p_d^\nu}{2} u_\nu)/T}$$

Coalescence model:

$$E_d \frac{dN_d}{d^3p_d} = \int_{\Sigma} p_d^\mu d\sigma_\mu e^{(\mu_p - \frac{p_d^\nu}{2} u_\nu)/T} e^{(\mu_n - \frac{p_d^\nu}{2} u_\nu)/T} C_d(r_d, p_d)$$
$$C_d(r_d, p_d) = \int \frac{d^3q d^3r}{(2\pi^3)} \mathcal{D}(q, r) \frac{f(r_d + r/2, p_d/2 + q/2) f(r_d - r/2, p_d/2 - q/2)}{f^2(r_d, p_d/2)}$$

- $\mathcal{D}(q, r)$ – Wigner transform of deuteron wavefunction
- $C_d(r_d, p_d)$ – measures fireball inhomogeneity over wavefunction size
 $C_d(r_d, p_d) = 1$ for large homogeneous fireball
- $\mu_{p,n}$ after resonance decays
light nuclei formed at kinetic freeze-out

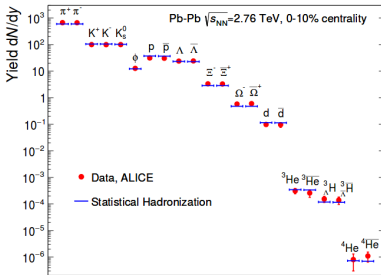
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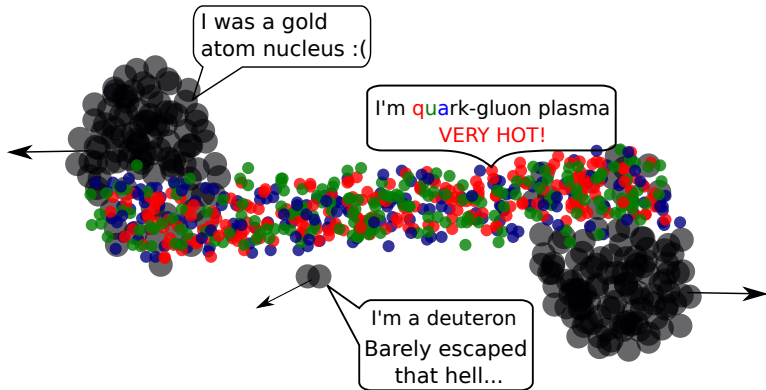
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"Snowballs in hell"

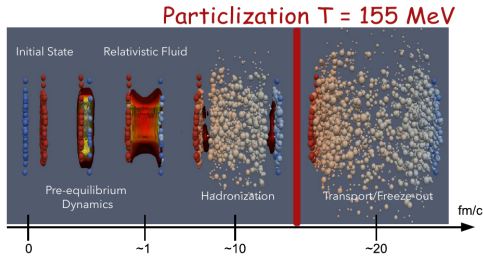


How deuteron survived: Oliinychenko et. al, Phys.Rev.C 99 (2019) 4, 044907

Purely dynamical model

DO, Pang, Elfner, Koch, PRC99 (2019) no.4, 044907

DO, Pang, Elfner, Koch, MDPI Proc. 10 (2019) no.1, 6

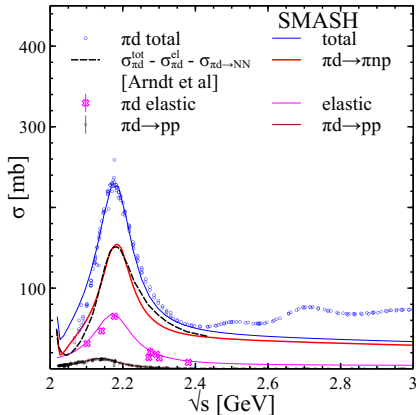


- CLVisc hydro [L. G. Pang, H. Petersen and X. N. Wang, arXiv:1802.04449 \[nucl-th\]](#)
- SMASH hadronic afterburner [J. Weil et al., PRC 94, no. 5, 054905 \(2016\)](#)
- Treat deuteron as a single particle
 - implement deuteron + X cross-sections explicitly

Light nuclei production by pion catalysis

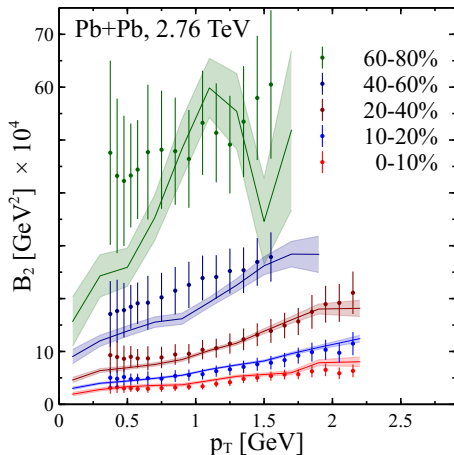
- $\pi d \leftrightarrow \pi np, Nd \leftrightarrow Nnp$
- all are tested to obey detailed balance within 1% precision
- large disintegration cross sections \rightarrow large reverse rates

DO, Pang, Elfner, Koch, PRC99 (2019) no.4, 044907



$B_2(p_T)$ and v_2 for different centralities

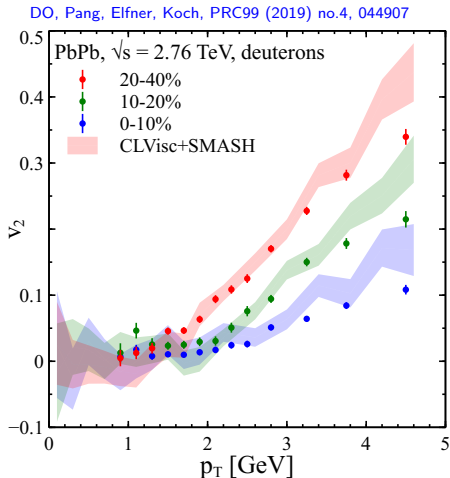
DO, Pang, Elfner, Koch, PRC99 (2019) no.4, 044907



$$B_2(p_T) = \frac{\frac{1}{2\pi} \frac{d^3 N_d}{p_T dp_T dy} \Big|_{p_T^d = 2p_T^p}}{\left(\frac{1}{2\pi} \frac{d^3 N_p}{p_T dp_T dy} \right)^2}$$

No free parameters. Works well for all centralities.

$B_2(p_T)$ and v_2 for different centralities

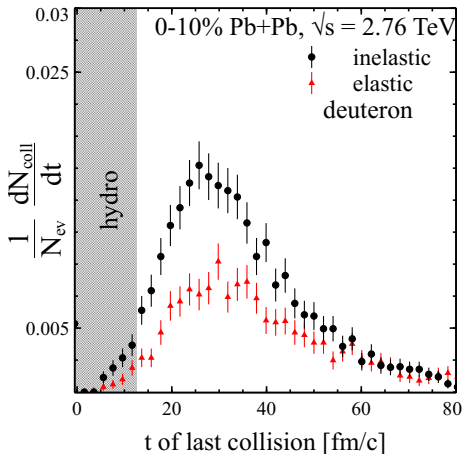


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Does deuteron freeze out at 155 MeV?

Only less than 1% of final deuterons originate from hydrodynamics

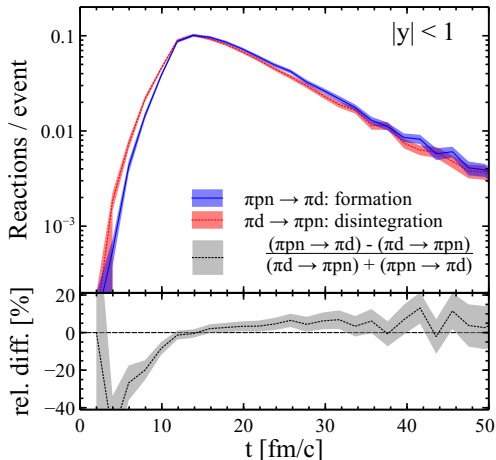


Deuteron freezes out at late time

Its chemical and kinetic freeze-outs roughly coincide

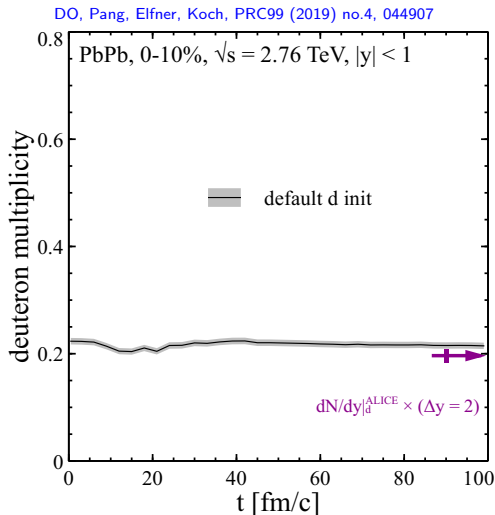
Is $\pi d \leftrightarrow \pi np$ reaction equilibrated

DO, Pang, Elfner, Koch, PRC99 (2019) no.4, 044907



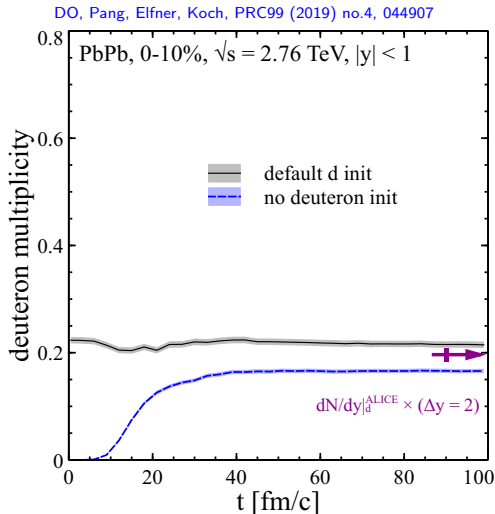
After about 12-15 fm/c within 5% $\pi d \leftrightarrow \pi np$ is equilibrated

Deuteron yield



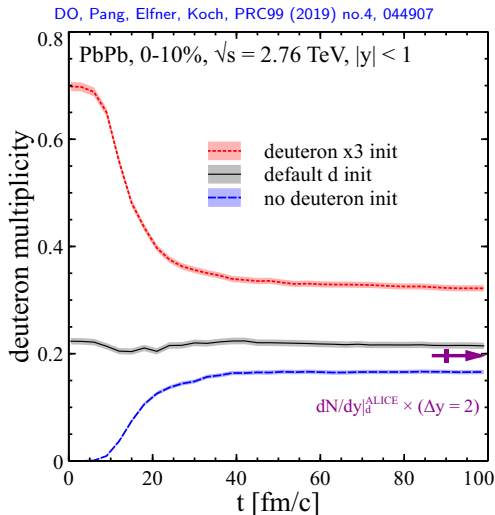
The yield is almost constant. Why? Does afterburner really play any role?

Deuteron yield



No deuterons at particlization: also possible. Here **all** deuterons are from afterburner.

Deuteron yield



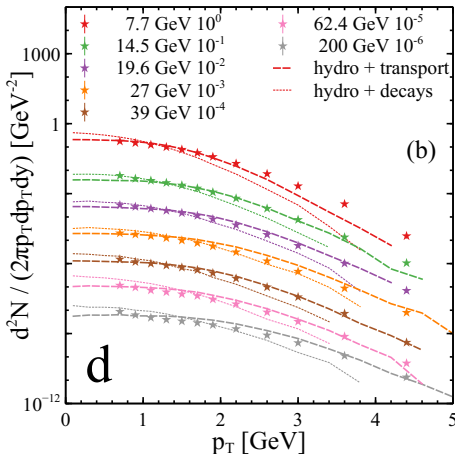
No deuterons at particlization: also possible. Here **all** deuterons are from afterburner.

Why thermal model describes light nuclei yields at LHC

- Stable hadron yields (π , K , N , Λ , ...) comprising resonances are fixed at chemical freeze-out
- Nuclei are kept in partial (relative) equilibrium by huge cross-sections of $A + h \leftrightarrow A \times N + h$ until kinetic freeze-out
 - Therefore nuclei yields stay constant from hadron chemical freeze-out to kinetic
 - This picture works for all measured nuclei at LHC
[Xu, Rapp, Eur. Phys. J. A55 \(2019\) no.5, 68](#)
[Vovchenko et al, arXiv:1903.10024](#)
 - It works even if no nuclei are produced at chemical freeze-out
[DO, Pang, Elfner, Koch, Phys.Rev. C99 \(2019\) no.4, 044907](#)
[DO, Pang, Elfner, Koch, MDPI Proc. 10 \(2019\) no.1, 6](#)

Exactly the same mechanism, lower energies

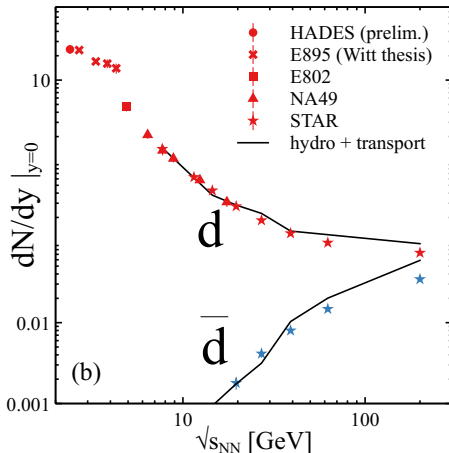
Data: Alt:2006dk, Anticic:2010mp, Adams:2003xp, Adamczyk:2017iwn, Abelev:2009bw, Adcox:2003nr, Klay:2001tf, Ahle:1999in



Same mechanism still works for deuteron down to 7.7 GeV!

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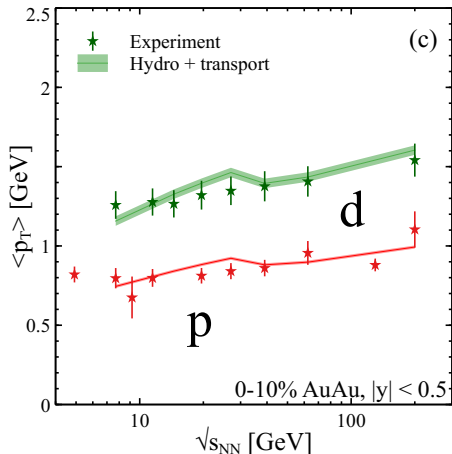
Data: Alt:2006dk, Anticic:2010mp, Adams:2003xp, Adamczyk:2017iwn, Abelev:2009bw, Adcox:2003nr, Klay:2001tf, Ahle:1999in



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- Potential benefits
 - Background for antimatter in space from pp, pA, AA.
May lead to discovery of antimatter clouds in the Universe
 - Possible detection of critical point from density fluctuations
 $\implies \frac{N_t N_p}{N_d^2}$, other ratios

Conclusions

Need better understanding of light nuclei production

- Potential benefits
 - Background for antimatter in space from pp, pA, AA.
May lead to discovery of antimatter clouds in the Universe
 - Possible detection of critical point from density fluctuations
 $\implies \frac{N_t N_p}{N_d^2}$, other ratios
- Challenges
 - Need model for light nuclei yields in e^+e^- , pp, p \bar{p} , AA as a function of \sqrt{s} , $dN_{ch}/d\eta$, p_T , y
 - Need to improve models, both dynamical and analytical
 - Need models including critical point
 - Does wavefunction size matter?
Still an open question: small systems, ${}^3_\Lambda\text{H}$
 - Need hadronic exclusive cross-sections:
 $d + \pi$, $d + p$, $t + \pi$, $t + p$, etc, to be measured or analytically computed

Thank you!

Most important deuteron production/disintegration reactions

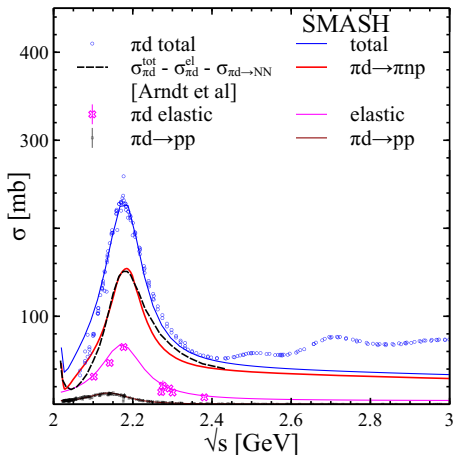
Largest $d + X$ disintegration rate \rightarrow largest reverse production rate

Most important = largest $\sigma_{d+X}^{\text{inel}} n_X$

X	$\sigma_{d+X}^{\text{inel}}$ [mb] ($\sqrt{s} - \sqrt{s_{thr}} = [0.05, 0.25]$ GeV)	$\frac{dN^X}{dy} _{y=0}$
π^\pm	80 - 160	732
K^+	< 40	109
K^-	< 80	109
p	50 - 100	33
\bar{p}	80 - 200	33
γ	< 0.1	comparable to π ?

$\pi + d$ are the most important because of pion abundance

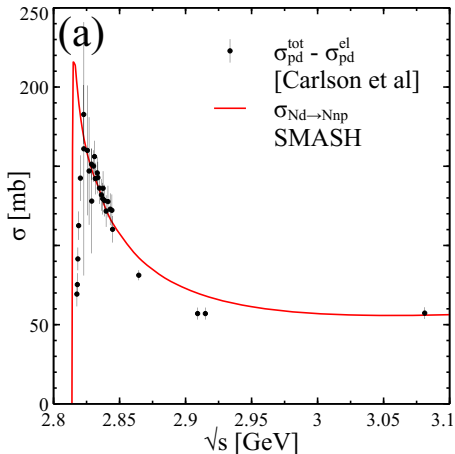
Reactions of deuteron with pions



$\pi d \leftrightarrow \pi np$ is the most important at LHC energies

$\sigma_{\pi d}^{\text{inel}} > \sigma_{\pi d}^{\text{el}}$, not like for hadrons

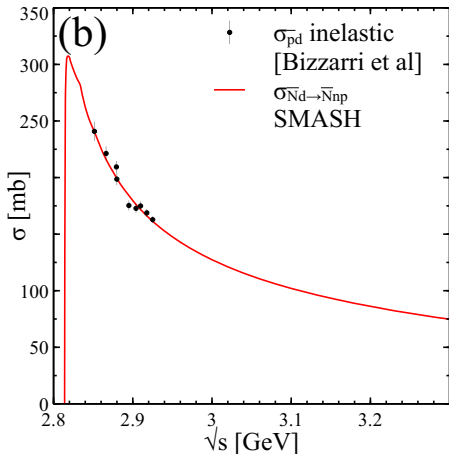
Reactions of deuteron with (anti-)nucleons



$Nd \leftrightarrow Nnp, \bar{N}d \leftrightarrow \bar{N}np$: large cross-sections

but not important at LHC energies, because N and \bar{N} are sparse

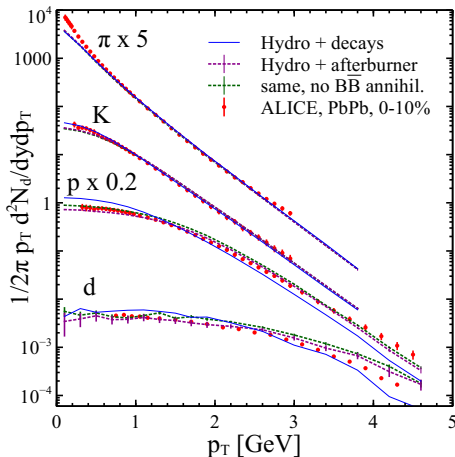
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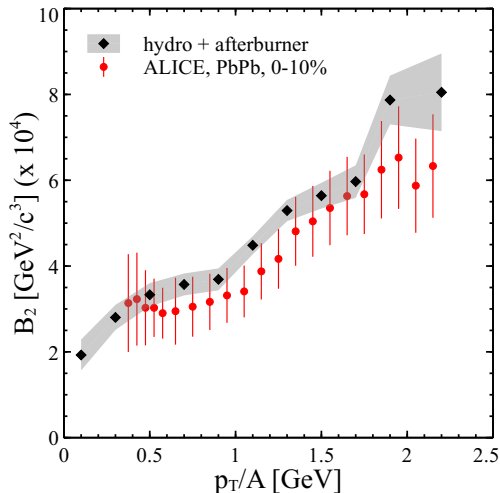
Transverse momentum spectra



Pion and kaon spectra not affected by afterburner
Proton spectra: pion wind effect and $B\bar{B}$ annihilations ($\sim 10\%$)

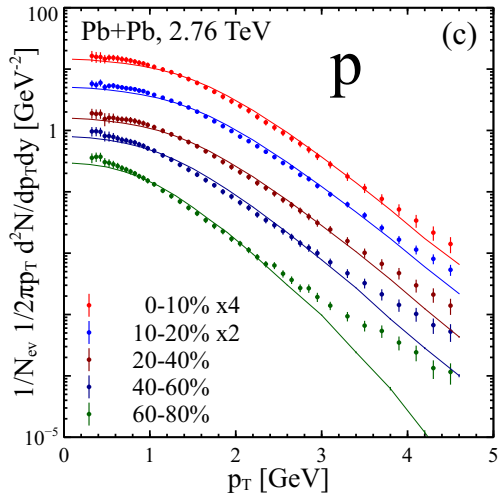
Obtaining $B_2(p_T)$ coalescence parameter

$$B_2(p_T) = \frac{\overline{\frac{1}{2\pi} \frac{d^2 N_p}{p_T dp_T dy}} \Big|_{p_T^d = 2p_T^p}}{\left(\frac{1}{2\pi} \frac{d^2 N_p}{p_T dp_T dy} \right)^2}$$

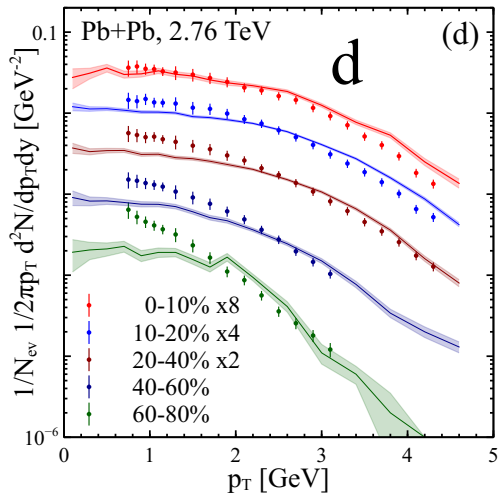


Reproducing B_2 without any free parameters

p_T -spectra for different centralities



p_T -spectra for different centralities



Toy model of deuteron production: no annihilations

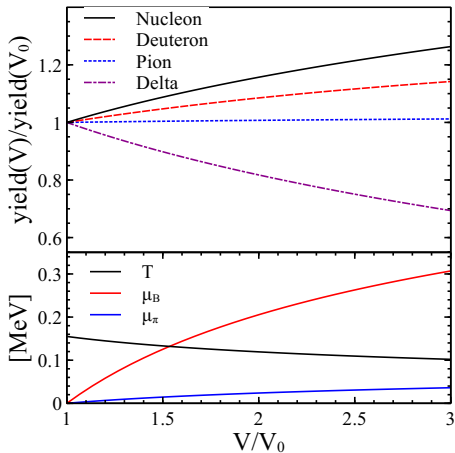
- only π , N , Δ , and d
- isoentropic expansion
- pion number conservation
- baryon (not net!) number conservation

$$(s_\pi(T, \mu_\pi) + s_N(T, \mu_B) + s_\Delta(T, \mu_B + \mu_\pi) + s_d(T, 2\mu_B))V = \text{const}$$

$$(\rho_\Delta(T, \mu_B + \mu_\pi) + \rho_\pi(T, \mu_\pi))V = \text{const}$$

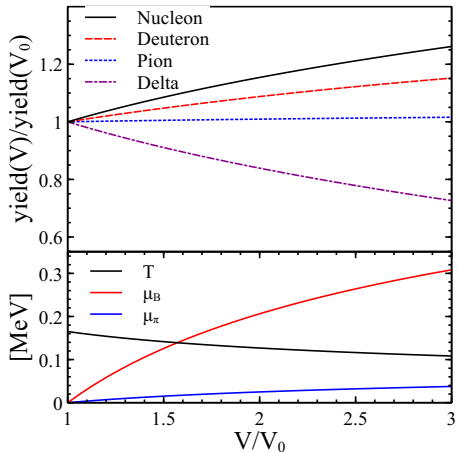
$$(\rho_N(T, \mu_B) + \rho_\Delta(T, \mu_B + \mu_\pi) + 2\rho_d(T, 2\mu_B))V = \text{const}$$

Toy model of deuteron production: results



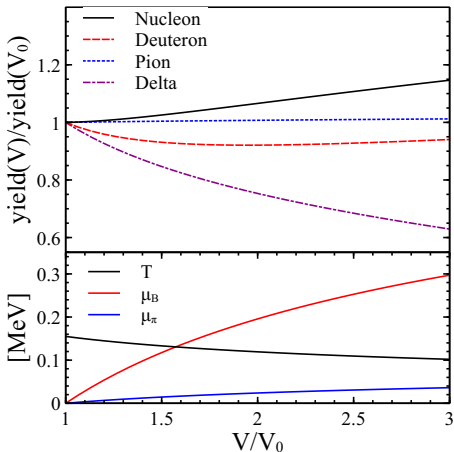
No annihilation: deuteron yield grows, like in simulation.

Toy model of deuteron production: results



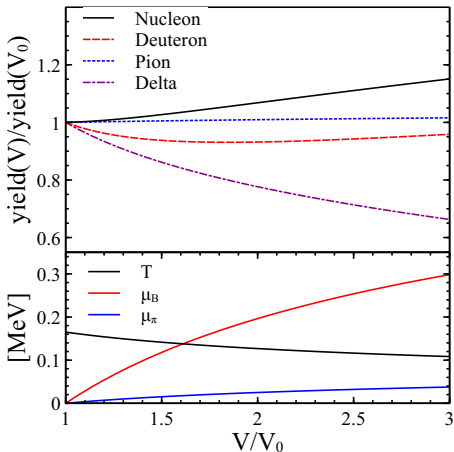
$T_{\text{particlization}} = 165$ MeV. Relative yields are similar, like in simulation.

Toy model of deuteron production: results



Annihilation out of equilibrium: $\mu_B = \mu_B \frac{V/V_0}{a+V/V_0}$, $a = 0.1$
 $T_{\text{particization}} = 155 \text{ MeV}$.

Toy model of deuteron production: results



Annihilation out of equilibrium: $\mu_B = \mu_B \frac{V/V_0}{a+V/V_0}$, $a = 0.1$
 $T_{\text{particlization}} = 165$ MeV. Qualitatively similar to our simulation.