Neutron stars: from macroscopic collisions to microphysics

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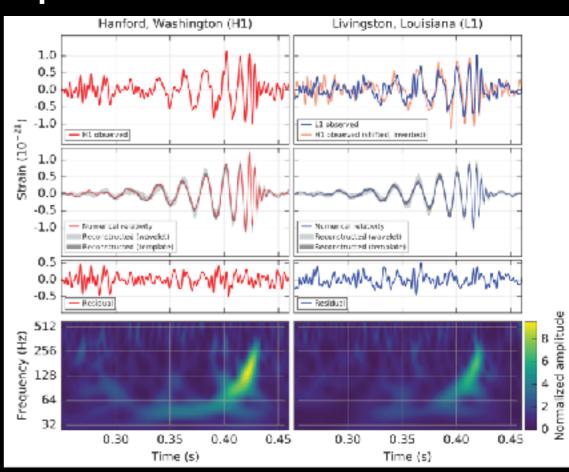


Plan of the talk

- The richness of merging binary neutron stars
- GW spectroscopy: EOS from frequencies
- GW170817: a game changer:
 - * maximum mass
 - * radii and deformabilities
- Signatures of quark-hadron phase transitions

The two-body problem in GR

• For black holes the process is very **simple**:



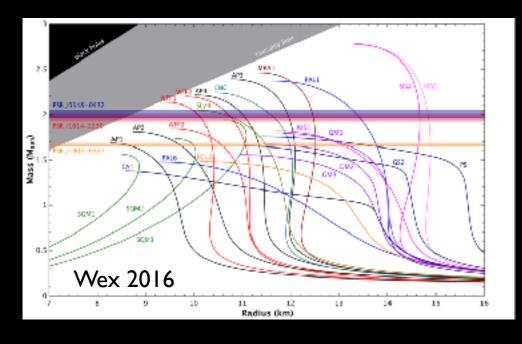
GW150914

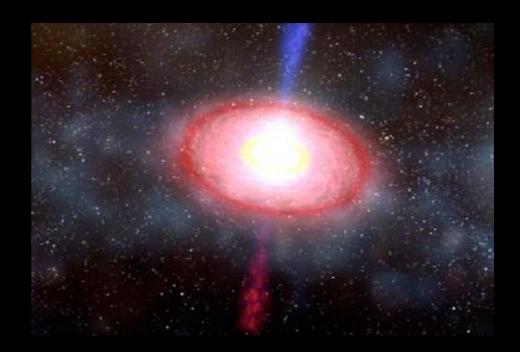
The two-body problem in GR

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• For NSs the question is more **subtle**: the merger leads to an hyper-massive neutron star (HMNS), ie a metastable equilibrium:

• HMNS phase can provide clear information on EOS





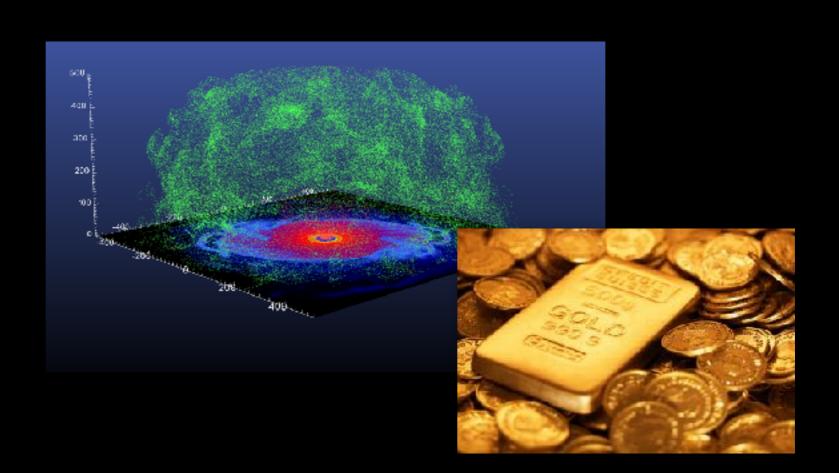
• BH+torus system may tell us on the central engine of GRBs

The two-body problem in GR

• For black holes the process is very simple:

• For NSs the question is more **subtle**: the merger leads to an hyper-massive neutron star (HMNS), ie a metastable equilibrium:

 ejected matter undergoes nucleosynthesis of heavy elements



The equations of numerical relativity

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu} R = 8\pi T_{\mu\nu}, \text{(Einstein equations)}$$

$$\nabla_{\mu}T^{\mu\nu} = 0, \text{ (cons. energy/momentum)}$$

$$\nabla_{\mu}(\rho u^{\mu}) = 0, \text{ (cons. rest mass)}$$

$$p = p(\rho, \epsilon, Y_e, \dots), \text{ (equation of state)}$$

$$\nabla_{\nu}F^{\mu\nu} = I^{\mu}, \qquad \nabla_{\nu}^{*}F^{\mu\nu} = 0, \text{ (Maxwell equations)}$$

$$T_{\mu\nu} = T_{\mu\nu}^{\text{fluid}} + T_{\mu\nu}^{\text{EM}} + \dots \text{ (energy - momentum tensor)}$$

The equations of numerical relativity

All are covariant tensor equations. However: Einstein equations involve smooth fields (metric, extrinsic curvature).

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = 8\pi T_{\mu\nu}$$

Conservation equations discontinuous fields (shocks).

$$\nabla_{\mu}T^{\mu\nu} = 0, \ \nabla_{\mu}(\rho u^{\mu}) = 0$$

Hence, numerical methods are significantly different.

Einstein equations: CCZ4 formulation

$$\begin{split} \partial_t \tilde{\gamma}_{ij} &= -2\alpha \tilde{A}^{\rm TF}_{ij} + 2\tilde{\gamma}_{k(i}\partial_{j)} \, \beta^k - \frac{2}{3}\tilde{\gamma}_{ij}\partial_k \, \beta^k + \beta^k \partial_k \tilde{\gamma}_{ij} \,, \\ \partial_t \tilde{A}_{ij} &= \phi^2 \left[-\nabla_i \nabla_j \alpha + \alpha \left(R_{ij} + \nabla_i Z_j + \nabla_j Z_i - 8\pi S_{ij} \right) \right]^{\rm TF} + \alpha \tilde{A}_{ij} \left(K - 2\Theta \right) \\ &\quad - 2\alpha \tilde{A}_{il} \tilde{A}^l_j + 2\tilde{A}_{k(i}\partial_{j)} \, \beta^k - \frac{2}{3}\tilde{A}_{ij}\partial_k \, \beta^k + \beta^k \partial_k \tilde{A}_{ij} \,, \\ \partial_t \phi &= \frac{1}{3}\alpha \phi K - \frac{1}{3}\phi \partial_k \beta^k + \beta^k \partial_k \phi \,, \\ \partial_t K &= -\nabla^i \nabla_i \alpha + \alpha \left(R + 2\nabla_i Z^i + K^2 - 2\Theta K \right) + \beta^j \partial_j K - 3\alpha \kappa_1 \left(1 + \kappa_2 \right) \Theta + 4\pi \alpha \left(S - 3\tau \right) \,, \\ \partial_t \hat{\Gamma}^i &= 2\alpha \left(\tilde{\Gamma}^i_{jk} \tilde{A}^{jk} - 3\tilde{A}^{ij} \frac{\partial_j \phi}{\phi} - \frac{2}{3} \tilde{\gamma}^{ij} \partial_j K \right) + 2\tilde{\gamma}^{ki} \left(\alpha \partial_k \Theta - \Theta \partial_k \alpha - \frac{2}{3} \alpha K Z_k \right) - 2\tilde{A}^{ij} \partial_j \alpha \\ &\quad + \tilde{\gamma}^{kl} \partial_k \partial_l \beta^i + \frac{1}{3} \tilde{\gamma}^{ik} \partial_k \partial_l \beta^l + \frac{2}{3} \tilde{\Gamma}^i \partial_k \beta^k - \tilde{\Gamma}^k \partial_k \beta^i + 2\kappa_3 \left(\frac{2}{3} \tilde{\gamma}^{ij} Z_j \partial_k \beta^k - \tilde{\gamma}^{jk} Z_j \partial_k \beta^i \right) \\ &\quad + \beta^k \partial_k \hat{\Gamma}^i - 2\alpha \kappa_1 \tilde{\gamma}^{ij} Z_j - 16\pi \alpha \tilde{\gamma}^{ij} S_j \,, \\ \partial_t \Theta &= \frac{1}{2} \alpha \left(R + 2\nabla_i Z^i - \tilde{A}_{ij} \tilde{A}^{ij} + \frac{2}{3} K^2 - 2\Theta K \right) - Z^i \partial_i \alpha + \beta^k \partial_k \Theta - \alpha \kappa_1 \left(2 + \kappa_2 \right) \Theta - 8\pi \alpha \tau \,, \\ \partial_t \alpha &= -2\alpha \left(K - 2\Theta \right) + \beta^k \partial_k \alpha \,, \end{split}$$

 $\partial_t \beta^i = f B^i + \beta^k \partial_k \beta^i,$

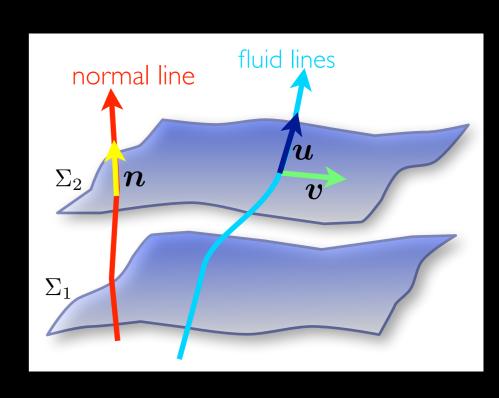
 $\partial_t B^i = \partial_t \hat{\Gamma}^i - \beta^k \partial_k \hat{\Gamma}^i + \beta^k \partial_k B^i - \eta B^i,$

Total system in 1st-order form has 58 variables

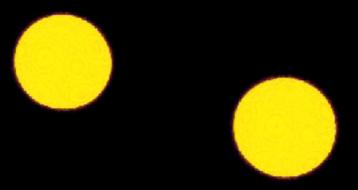
GRHD/GRMHD equations: Valencia formulation

- They express conservation laws with discontinuities.
- Casting them in conservation form guarantees that:
- lead to a well-posed problem.
- solution converges to the correct weak solution of problem.

$$egin{aligned} \partial_t ig(\sqrt{\gamma} \, oldsymbol{U}ig) + \partial_i ig(\sqrt{\gamma} \, oldsymbol{F}^iig) &= oldsymbol{S} \ oldsymbol{U} := egin{pmatrix}
ho W \
ho h W^2 v_j \
ho h W^2 - p \end{pmatrix}, \; oldsymbol{F}^i := egin{pmatrix} lpha v^i D - eta^i D \ lpha S^i_j - eta^i S_j \ lpha S^i - eta^i E \end{pmatrix} \end{aligned}$$



A prototypical simulation with possibly the best code looks like this...



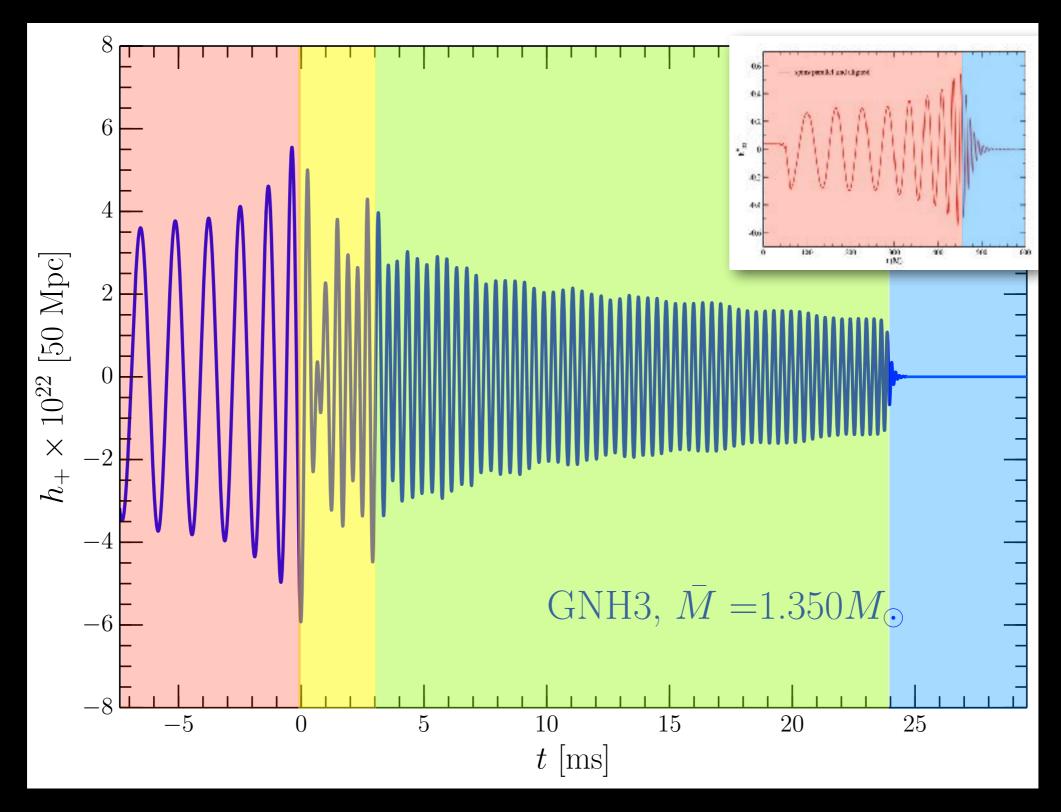
$$M = 2 \times 1.35 M_{\odot}$$
LS220 EOS

Qualitatively, this is what normally happens:

Quantitatively, differences are produced by:

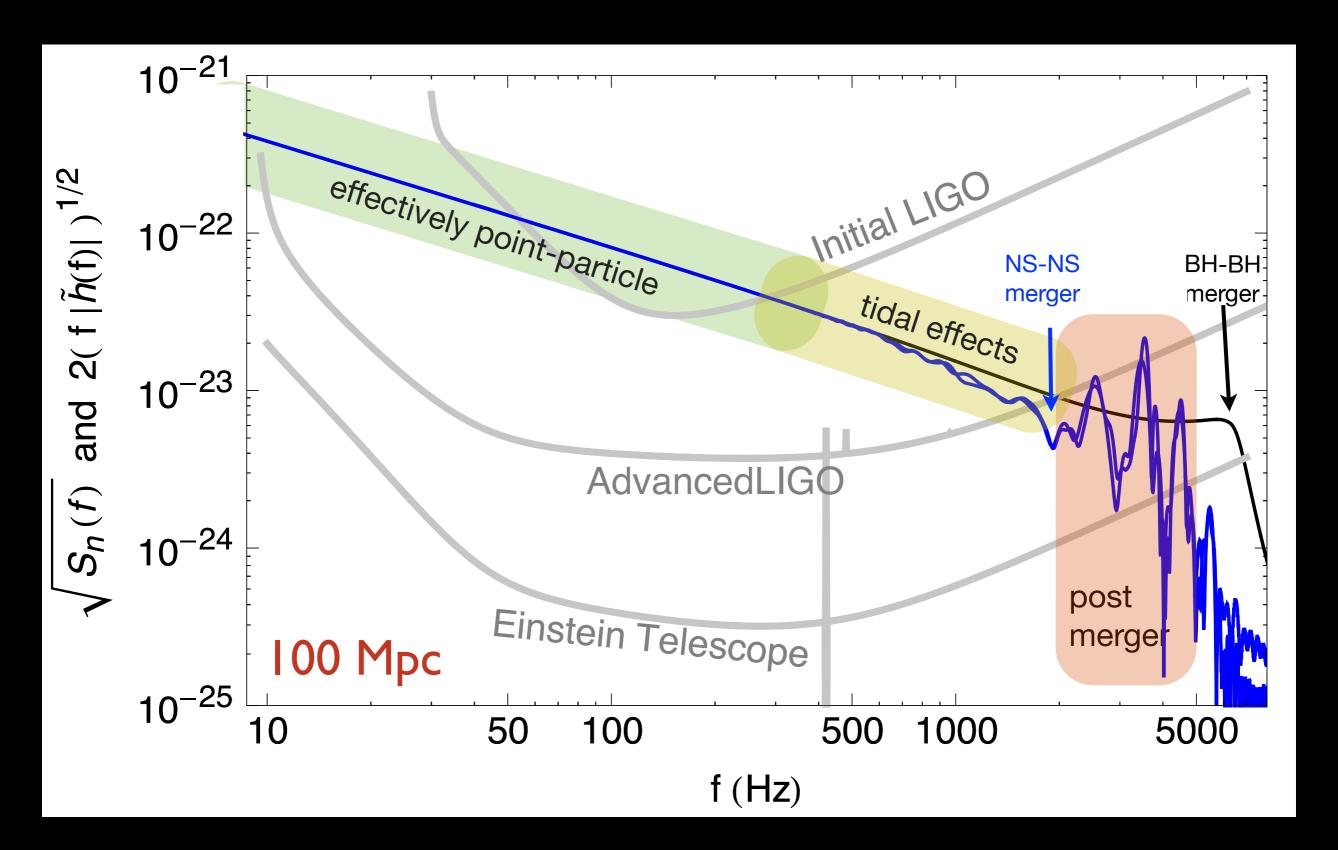
- total mass (prompt vs delayed collapse)
- mass asymmetries (HMNS and torus)
- soft/stiff EOS (inspiral and post-merger, PT)
- magnetic fields (equil. and EM emission)
- radiative losses (equil. and nucleosynthesis)

Anatomy of the GW signal



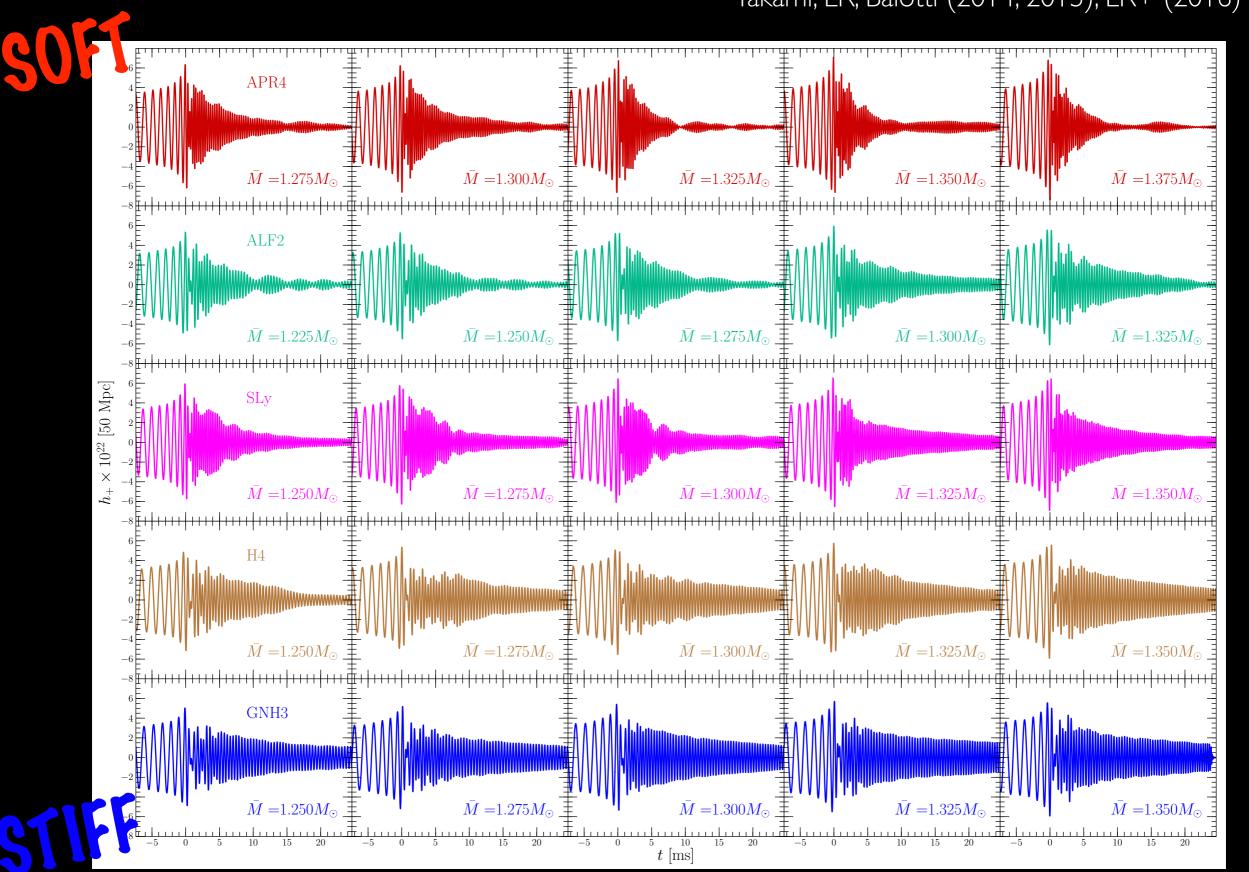
Postmerger signal: peculiar of binary NSs

In frequency space



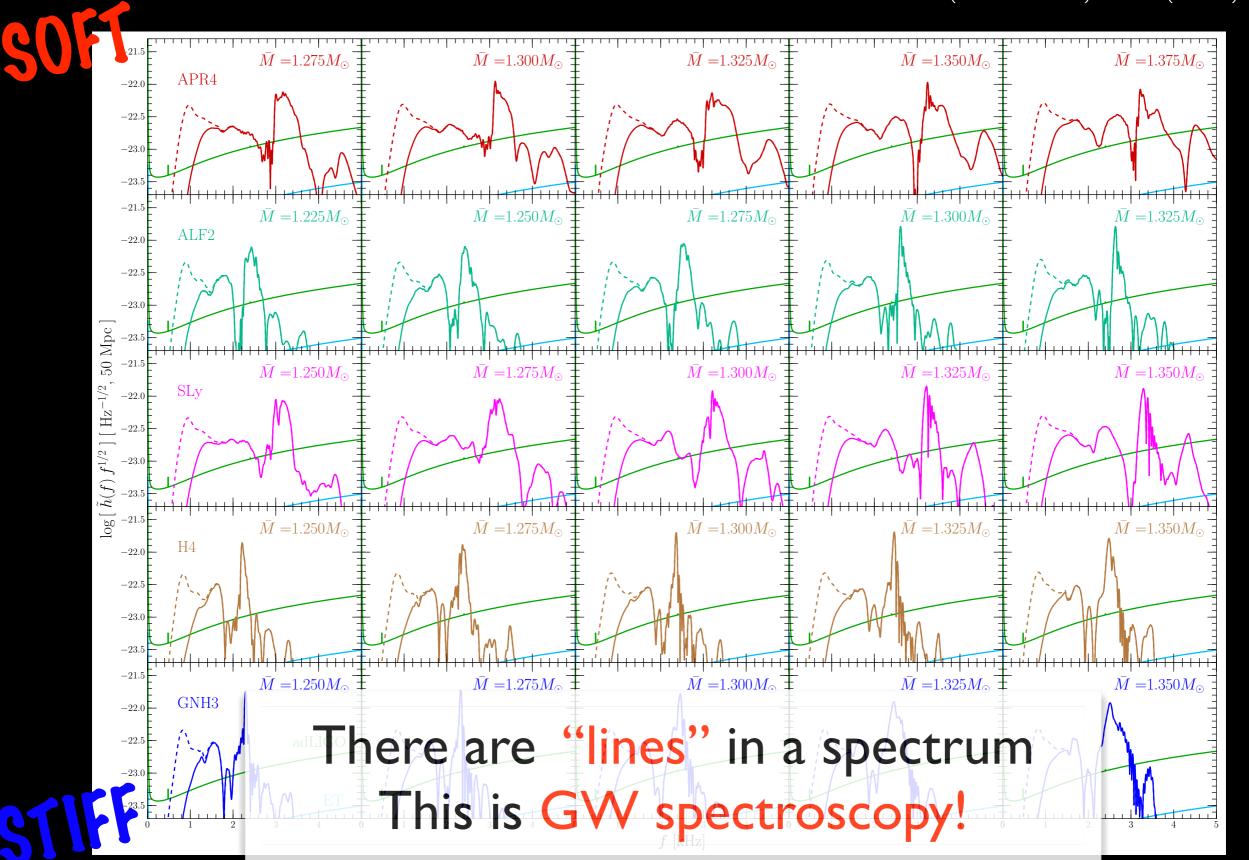
What we can do nowadays

Takami, LR, Baiotti (2014, 2015), LR+ (2016)



Extracting information from the EOS

Takami, LR, Baiotti (2014, 2015), LR+ (2016)



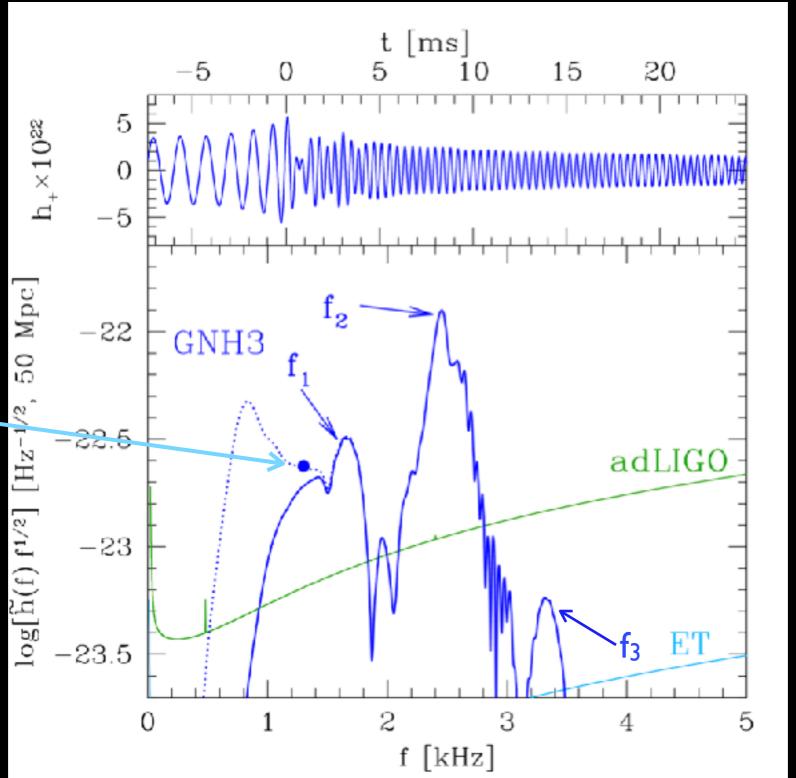
A spectroscopic approach to the EOS

Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, Clark+ 2016, LR+2016, de Pietri+ 2016, Feo+

2017, Bose+ 2017.

merger

frequency

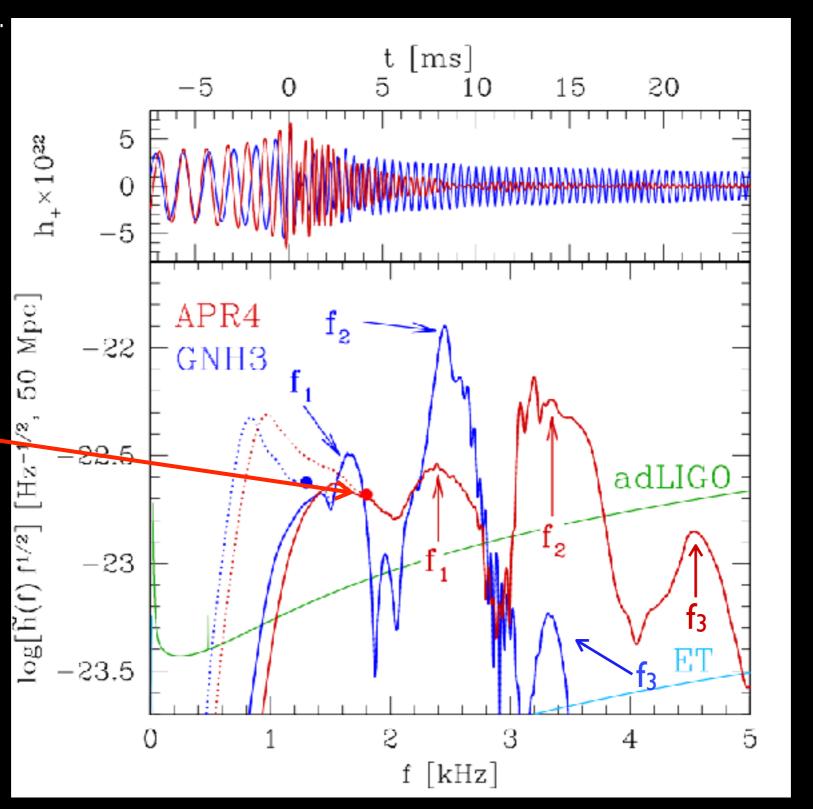


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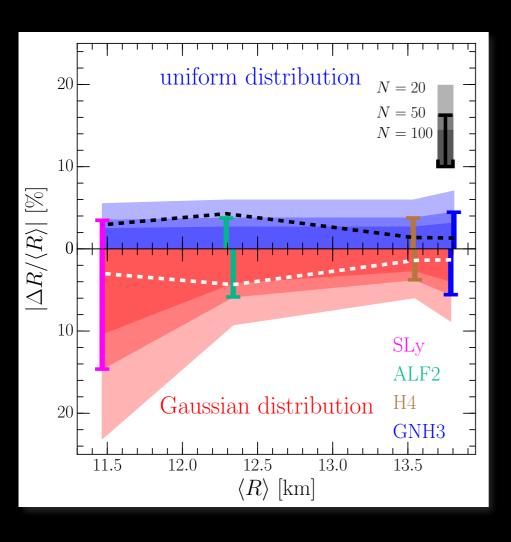
2017, Bose + 2017.

merger frequency



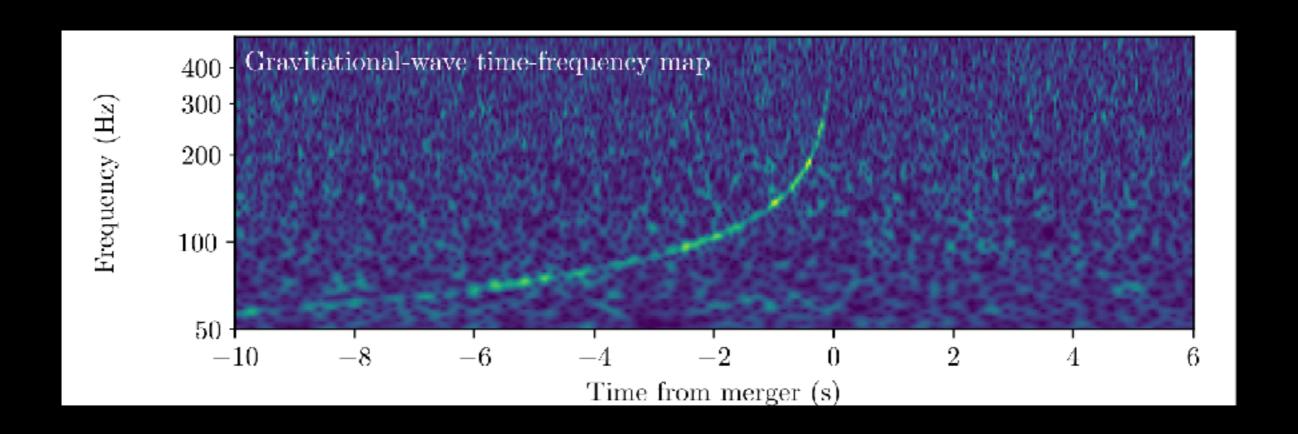
A spectroscopic approach to the EOS

- Universal behaviour and analytic modelling of postmerger relates position of these peaks with the EOS.
- Question: how well can we constrain the EOS (radius) given N detections?



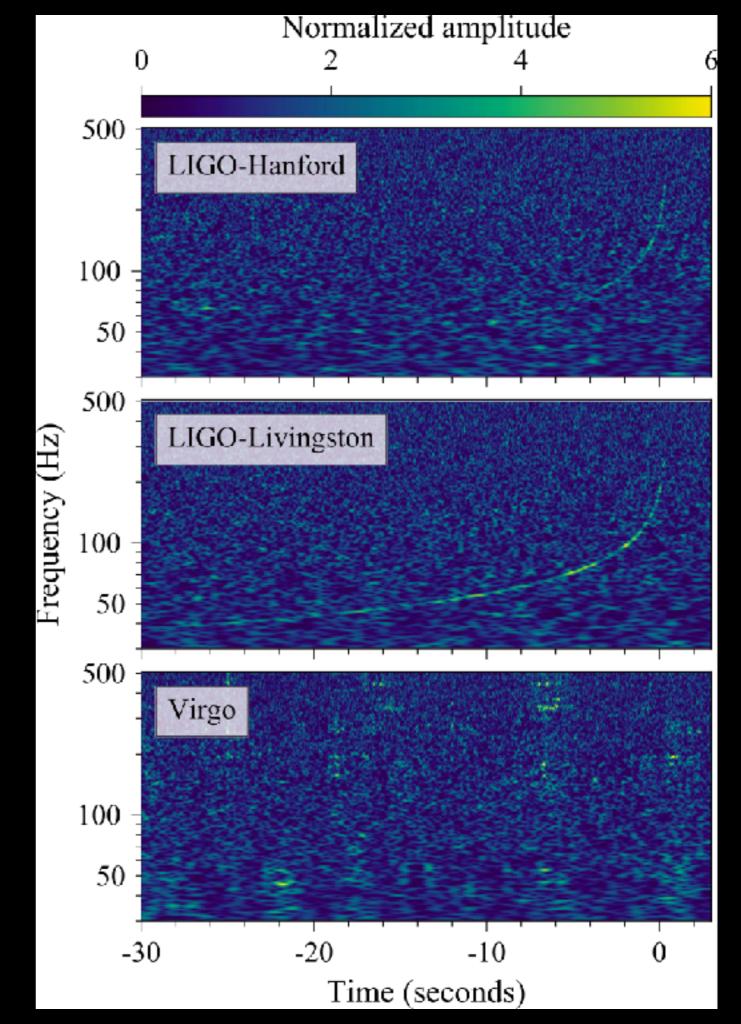
- discriminating stiff/soft EOSs possible
 even with moderate N~10
- •stiff EOSs: $|\Delta R/\langle R \rangle| < 10\%$ for N~20
- •soft EOSs: $|\Delta R/\langle R \rangle| \sim 10\%$ for N~50
- •golden binary: SNR ~ 6 at 30 Mpc $|\Delta R/\langle R\rangle| \simeq 2\% \ \ {\rm at\ 90\%\ confidence}$

GW170817: a game changer



GWI708I7: the first binary neutron-star system

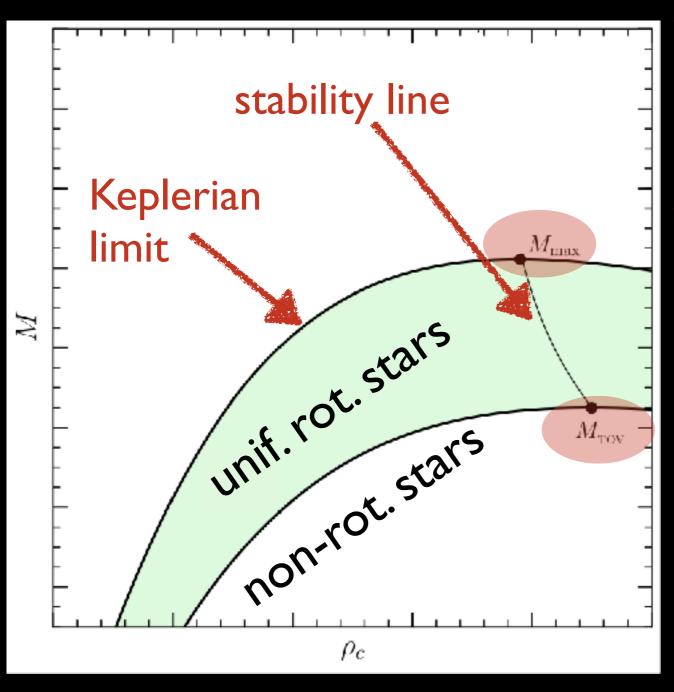
- * Unfortunately only the inspiral signal was detected.
- * Fortunately this was sufficient to set a number of constraints on max. mass, tidal deformability, radii, etc.



Limits on the maximum mass

• The remnant of GW170817 was a hypermassive star, i.e. a differentially rotating object with initial **gravitational** mass:

$$M_1 + M_2 = 2.74^{+0.04}_{-0.01} M_{\odot}$$



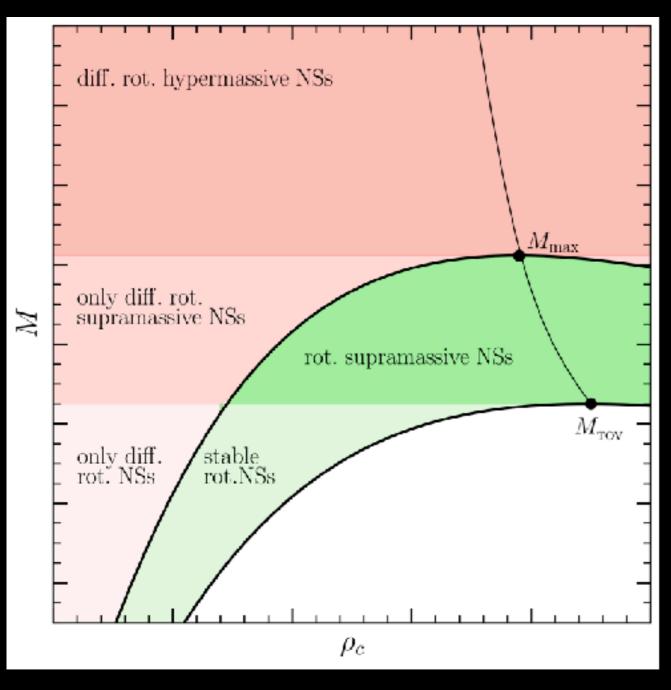
- Sequences of equilibrium models of **nonrotating** stars will have a maximum mass: $M_{\scriptscriptstyle \rm TOV}$
- This is true also for **uniformly** rotating stars at mass shedding limit: $M_{\rm max}$
- $M_{
 m max}$ simple and quasiuniversal function of $M_{
 m TOV}$ (Breu & LR 2016)

$$M_{\text{max}} = 1.20^{+0.02}_{-0.05} \, M_{\odot}$$

Limits on the maximum mass

• The remnant of GW170817 was a hypermassive star, i.e. a differentially rotating object with initial gravitational mass:

$$M_1 + M_2 = 2.74^{+0.04}_{-0.01} M_{\odot}$$



- Green region is for uniformly rotating equilibrium models.
- •Salmon region is for differentially rotating equilibrium models.
- Supramassive stars have:

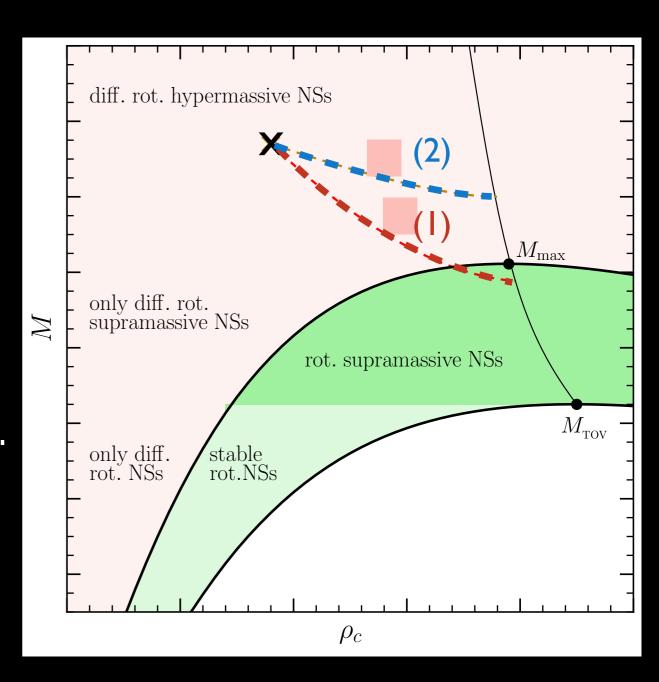
$$M > M_{\rm TOV}$$

• Hypermassive stars have:

$$M > M_{\rm max}$$

Limits on the maximum mass

- •GW170817 produced object "X"; GRB implies a BH has been formed: "X" followed two possible tracks: fast (2) and slow (1)
- •It rapidly produced a BH when still differentially rotating (2)
- It lost differential rotation leading to a uniformly rotating core (1).
- (1) is much more likely because of large ejected mass (long lived).
- Final mass is near $M_{
 m max}$ and we know this is universal!



let's recap...

Consider evolution track (1)

- •Use measured gravitational mass of GW170817
- Remove rest-mass deduced from kilonova emission (need conversion baryon/gravitational)
- Use universal relations, account for errors to obtain

$$2.01^{+0.04}_{-0.04} \le 1$$

$$2.01^{+0.04}_{-0.04} \le M_{\text{TOV}}/M_{\odot} \le 2.16^{+0.17}_{-0.15}$$

Tension on the maximum mass

Nathanail, Most, LR (2021)

• The recent detection of GWI908I4 has created a significant tension on the maximum mass

$$M_1=22.2-24.3\,M_{\odot}$$

$$M_2=2.50-2.67\,M_{\odot} \qquad {
m smallest~BH~or~heaviest~NS!}$$

- If secondary in GW190814 was a NS, all previous results on the maximum mass are incorrect.
- No EM counterpart was observed with GW190814 and no estimates possible for ejected matter or timescale for survival.
- How do we solve this tension?

Tension on the maximum mass

• We can nevertheless explore impact of larger maximum mass, i.e., what changes in the previous picture if

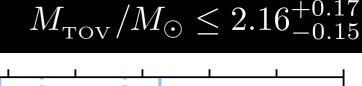
$$M_{\rm TOV}/M_{\odot} \gtrsim 2.5$$
?

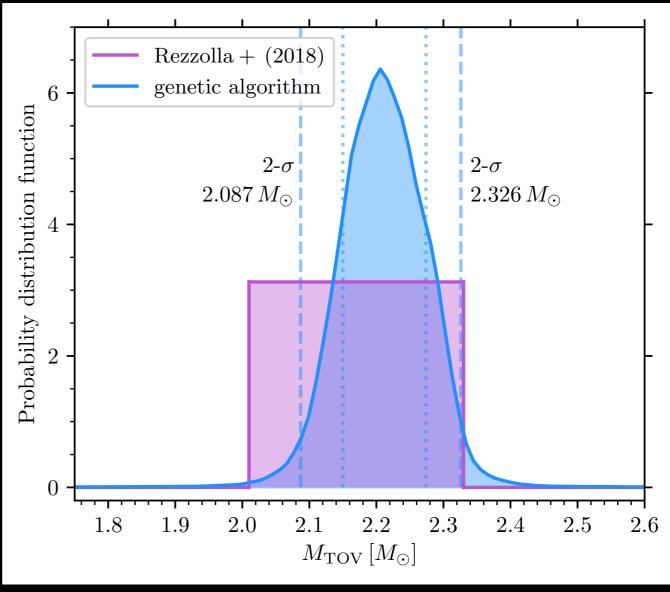
- •In essence, this is a multi-dimensional parametric problem satisfying conservation of rest-mass and gravitational mass.
- Observations provide limits on gravitational and ejected mass.
- Numerical relativity simulations provide limits on emitted GWs
- •All the rest is contained in 10 parameters that need to be varied within suitable ranges.

Genetic algorithm

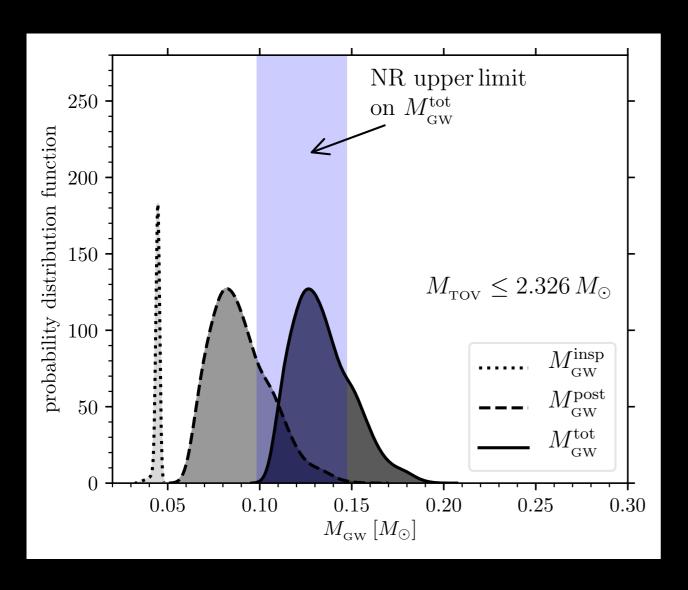
- A genetic algorithm is used to sample through the parameter space of the 10 free parameters.
- The algorithm reflects genetic adaptation: given a mutation (i.e. change of parameters) it will be adopted if it provides a better fit to data.
- Consider first previous estimate:

$$M_{\rm TOV}/M_{\odot} \lesssim 2.3$$

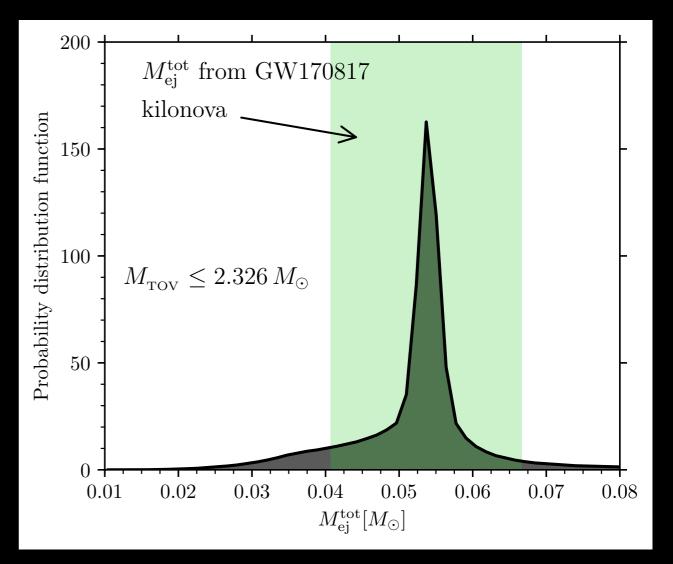




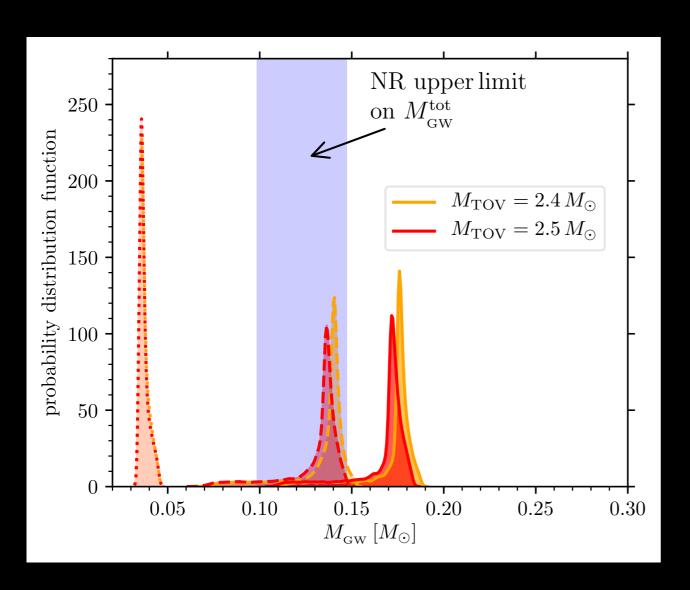
First hypothesis: $M_{\scriptscriptstyle { m TOV}}/M_{\odot} \lesssim 2.3$



 Total mass ejected is in perfect agreement with predictions from kilonova signal • Total mass emitted in GWs is in perfect **agreement** with predictions from numerical relativity

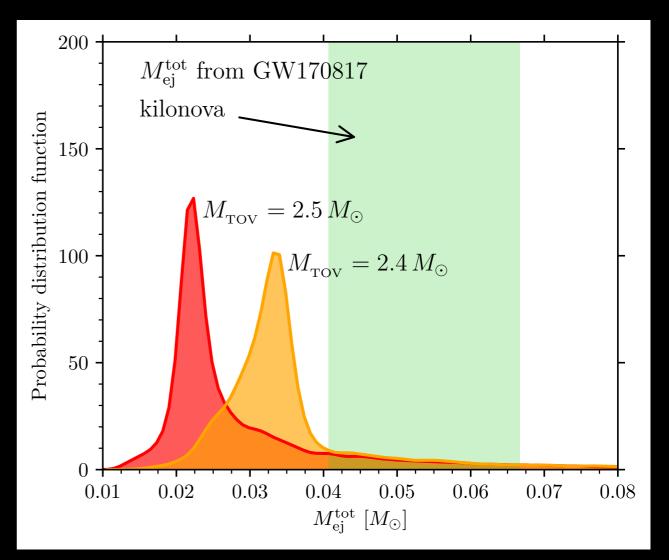


Second hypothesis: $M_{\rm TOV}/M_{\odot}\gtrsim 2.5$



• Total mass ejected is in perfect much smaller than observed from kilonova signal.

- Total mass emitted in GWs is much larger than predicted from simulations;
- Mismatch becomes worse with larger masses



Tension on the maximum mass

Nathanail, Most, LR (2020)

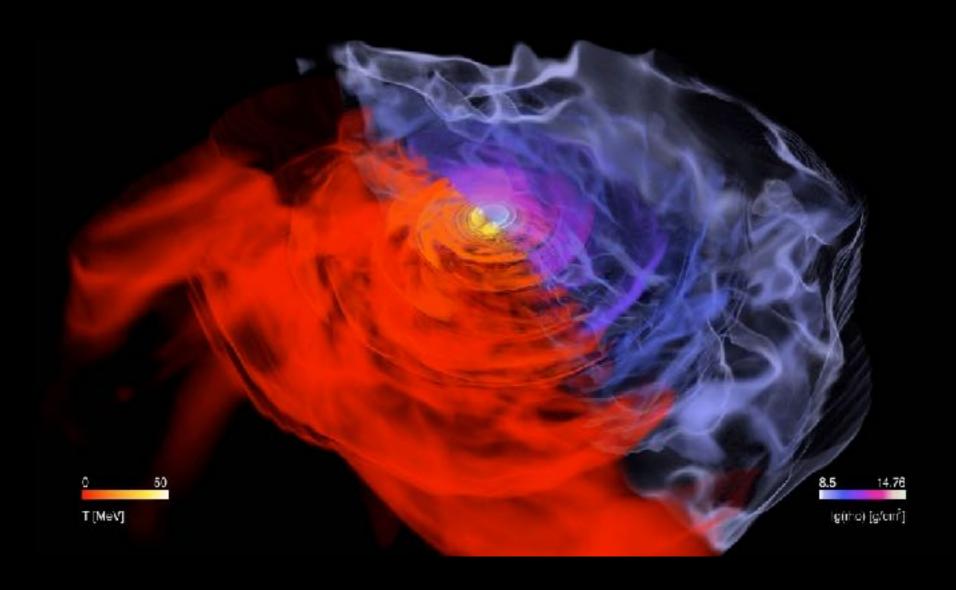
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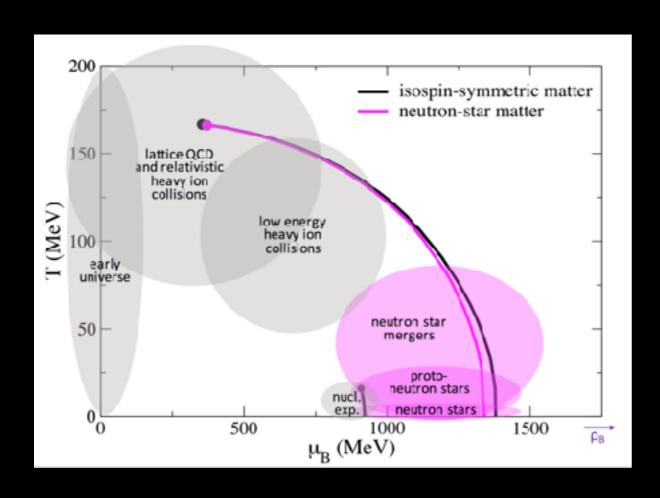
- If secondary in GW190814 was a NS, all previous considerations are incorrect.
- No EM counterpart was observed with GW190814 and no estimates possible on ejected matter or timescale for survival.
- How do we solve this tension?
- Solution: secondary in GW190814 was a BH at merger but could have been a NS before

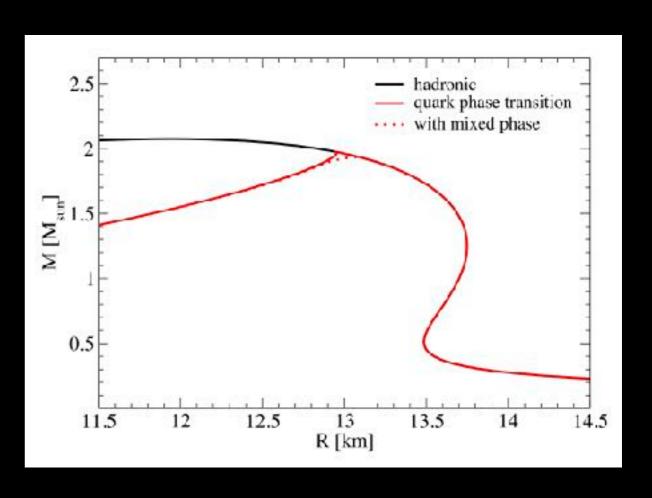
Phase transitions and their signatures



Most, Papenfort, Dexheimer, Hanauske, Schramm, Stoecker, LR (2019) Weih, Hanauske, LR (2020)

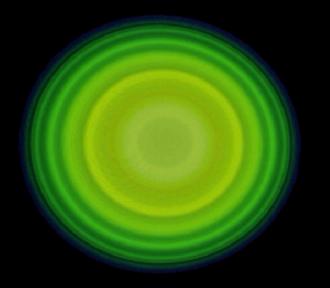
- Isolated neutron stars probe a small fraction of phase diagram.
- Neutron-star binary mergers reach temperatures up to 80 MeV and probe regions complementary to experiments.

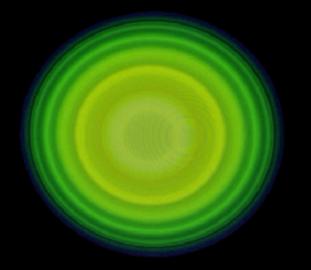


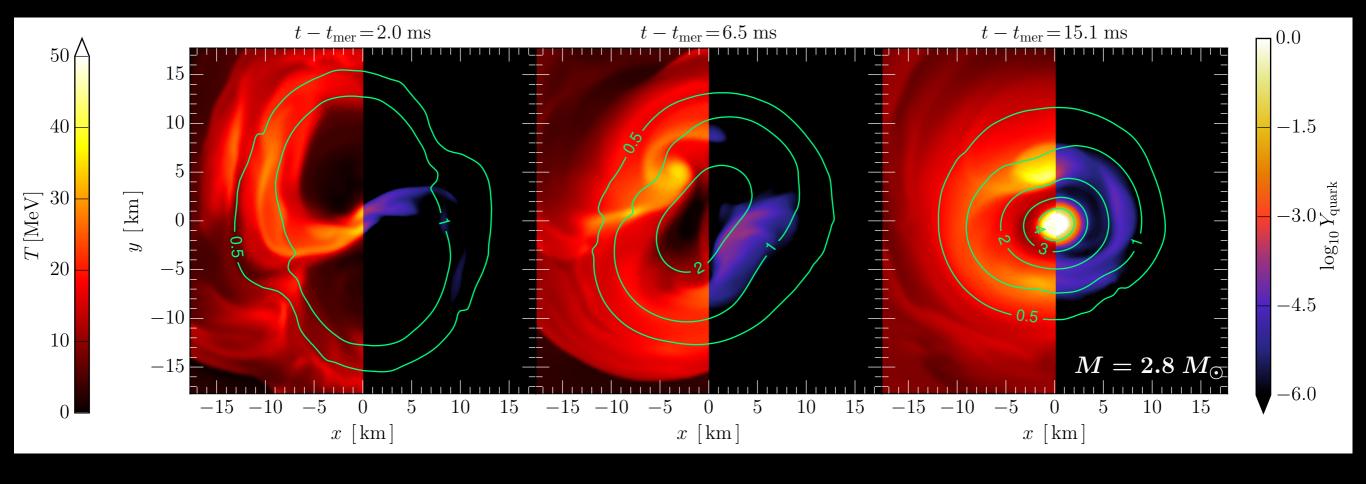


- Considered EOS based on Chiral Mean Field (CMF) model, based on a nonlinear SU(3) sigma model.
- Appearance of quarks can be introduced naturally.

Animations: Weih, Most, LR



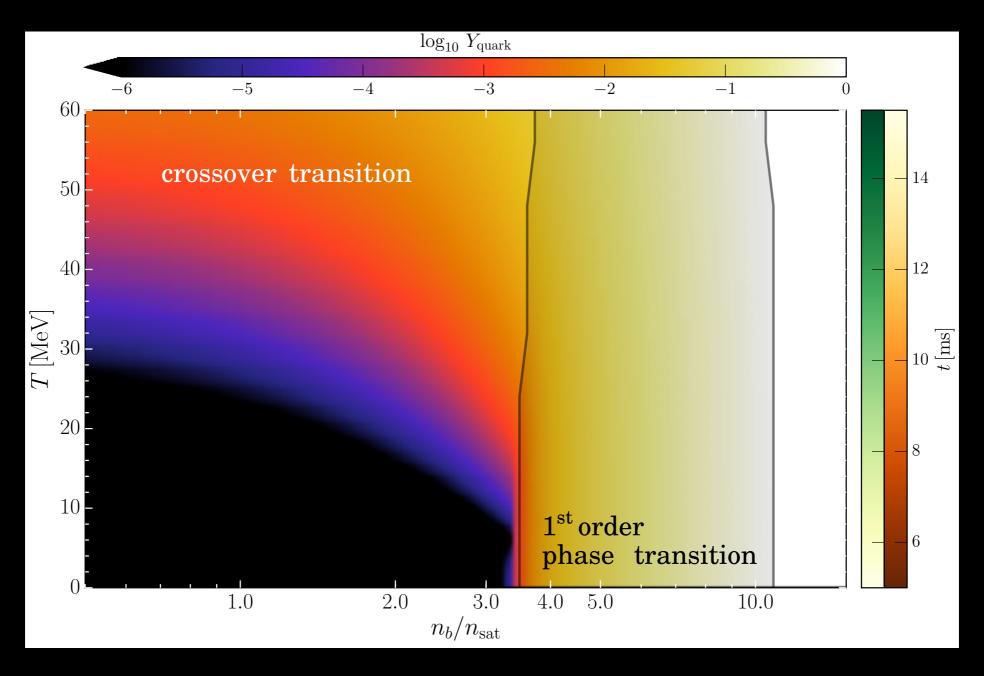




Quarks appear at sufficiently large temperatures and densities.

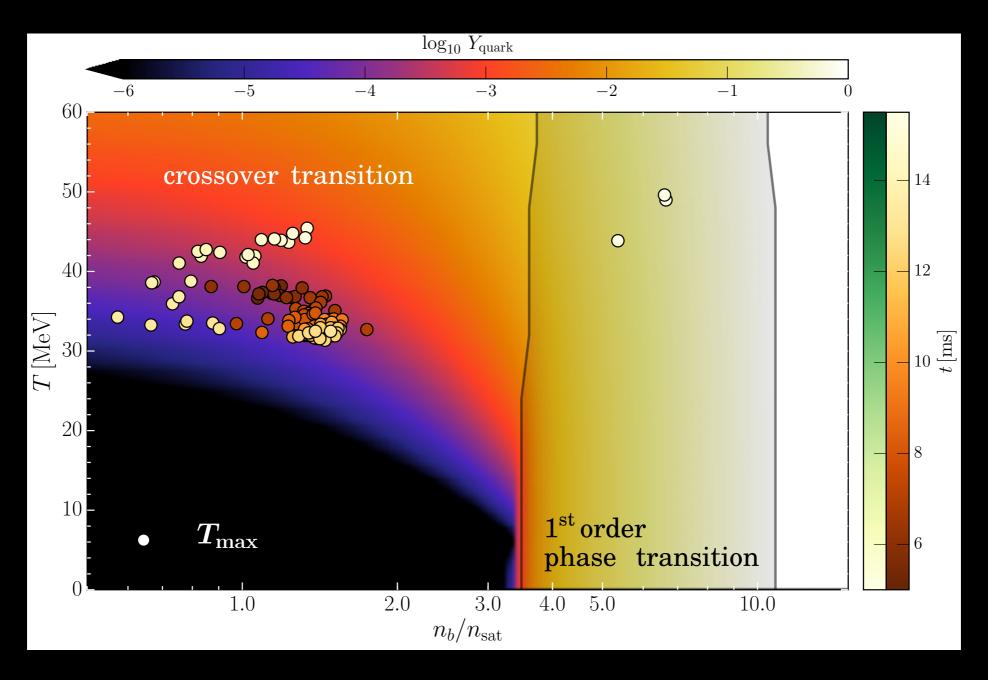
When this happens the EOS is considerably softened and a BH produced.

Comparing with the phase diagram



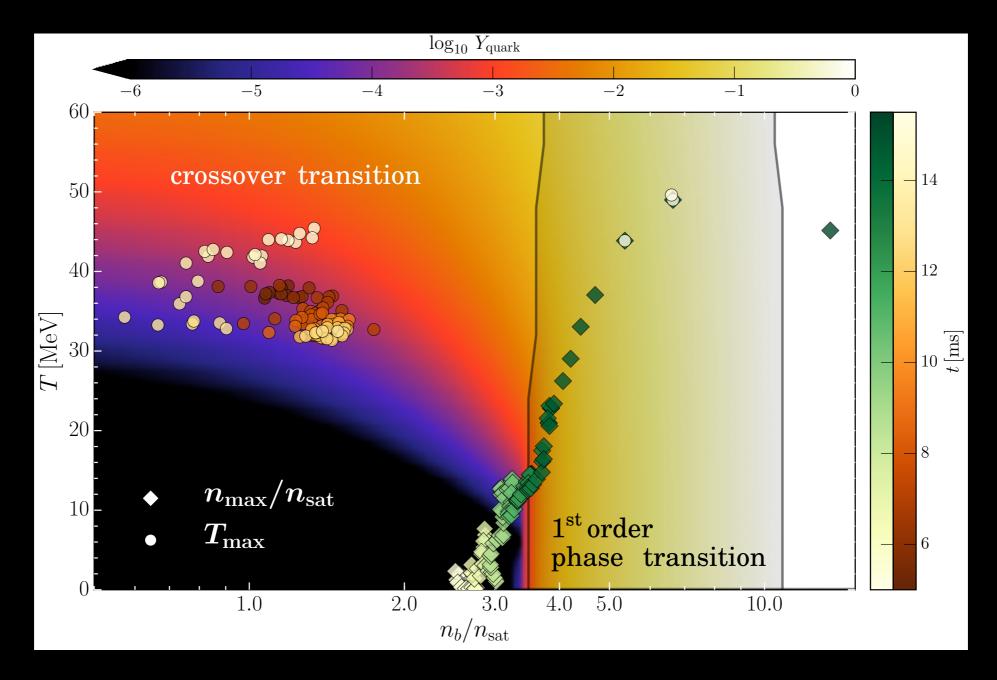
Phase diagram with quark fraction

Comparing with the phase diagram



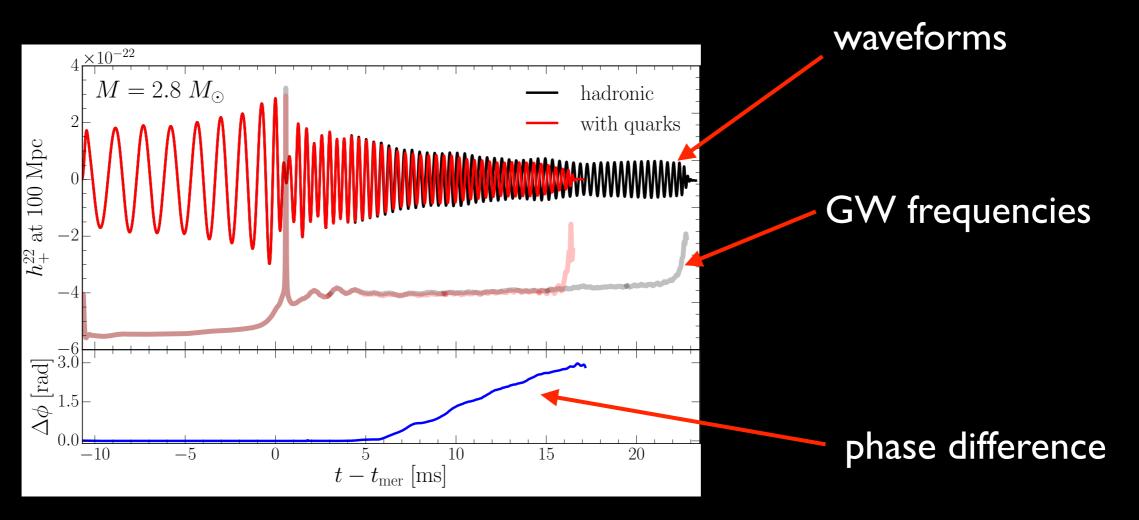
- Phase diagram with quark fraction
- Circles show the position in the diagram of the maximum temperature as a function of time

Comparing with the phase diagram



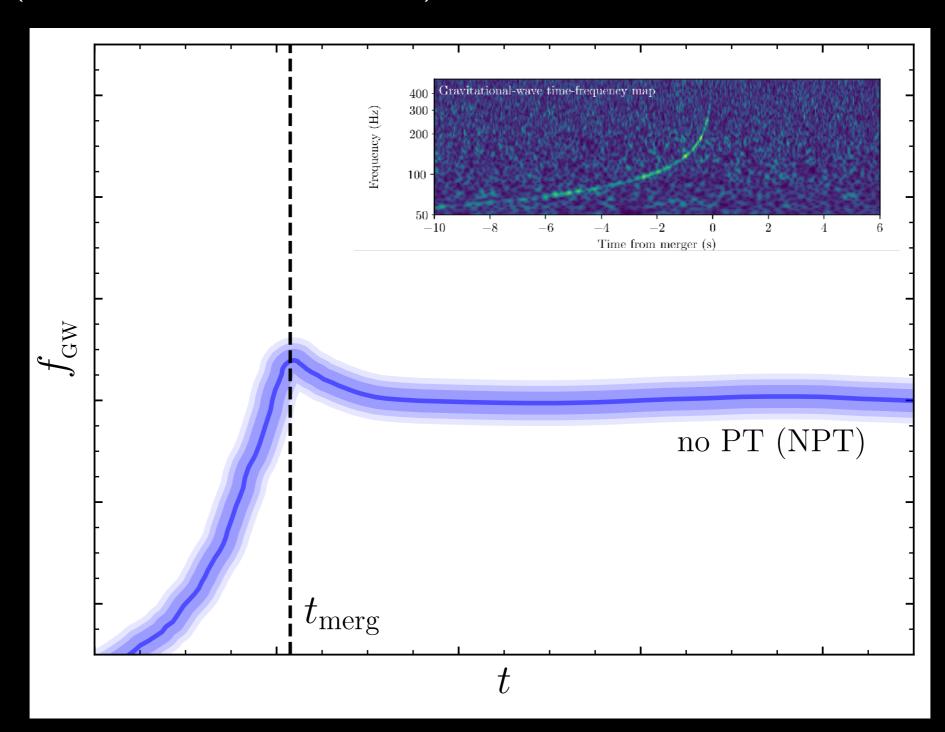
- Reported are the evolution of the max. temperature and density.
- Quarks appear already early on, but only in small fractions.
- Once sufficient density is reached, a full phase transition takes place.

Gravitational-wave emission

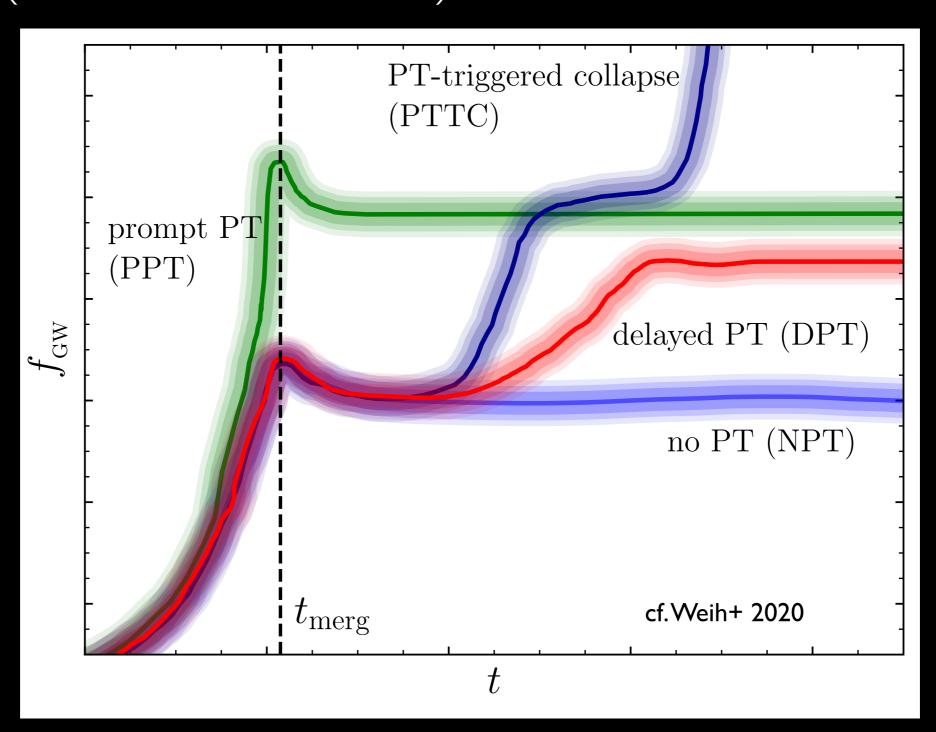


- After ~ 5 ms, quark fraction is large enough to change quadrupole moment and yield differences in the waveforms.
- Sudden softening of the phase transition leads to collapse and large difference in phase evolution.
 - Observing mismatch between **inspiral** (fully hadronic) and **post-merger** (phase transition): clear **signature** of a PT

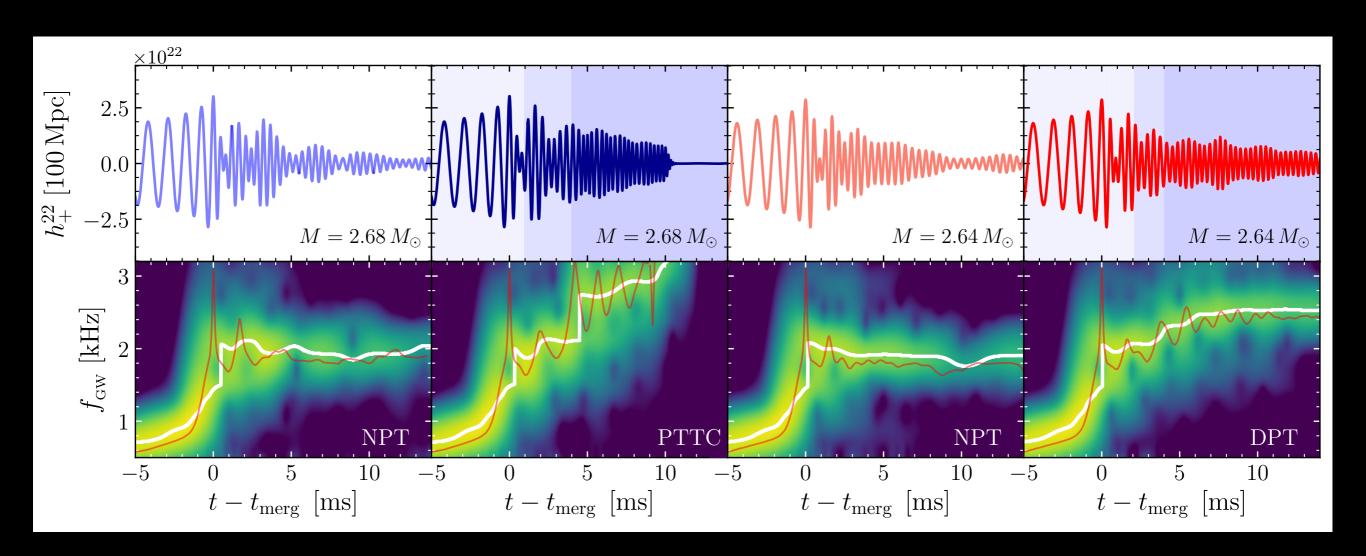
We have recently added another possible scenario for a post-merger **PT**, which completes the picture of possible scenarios (Weih, Hanauske, LR 2020).



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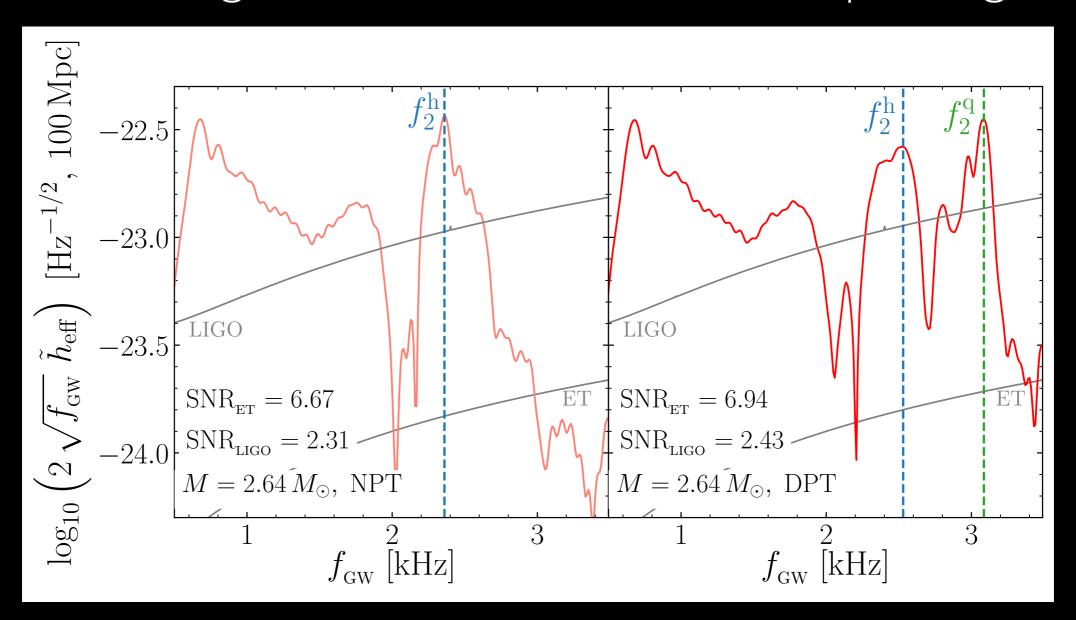


Different signatures are also quite transparent when shown in terms of the gravitational waves and their spectrograms.



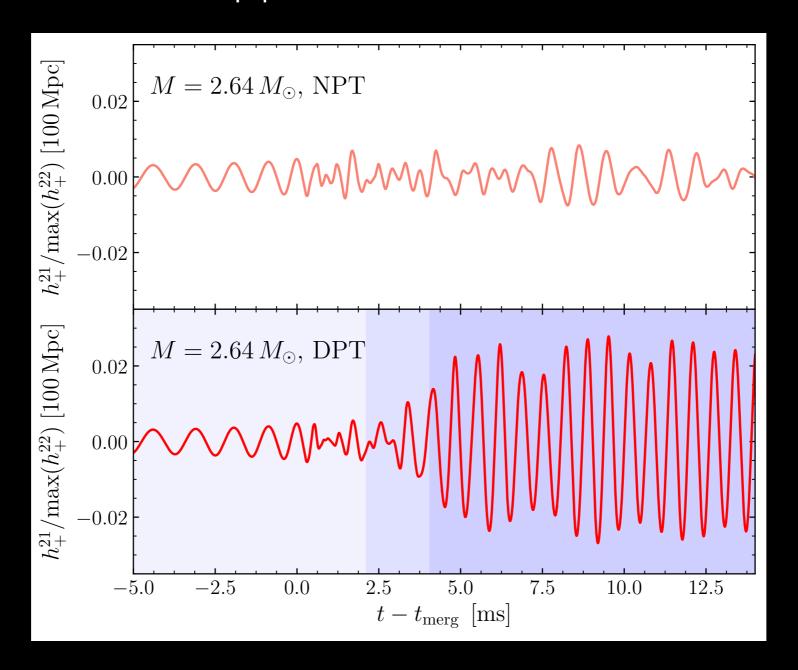
Importance of DPT is that it leads to two different "stable" f_2 frequencies that are easily distinguishable in the PSD

Different signatures are also quite transparent when shown in terms of the gravitational waves and their spectrograms.



Importance of DPT is that it leads to two different "stable" f_2 frequencies that are easily distinguishable in the PSD

Another signatures is appearance of an $\ell=2, m=1$ mode



The mode is triggered by the PT and the non-axisymmetric deformations it produces.

Conclusions

- *Spectra of post-merger shows peaks, some "quasi-universal".
- *When used together with tens of observations, they will set tight constraints on EOS: radius known with ~ km precision.
- *Threshold mass has universal behaviour with spin and mass ratio
- *GW170817 has already provided new limits on

$$2.01^{+0.04}_{-0.04} \le M_{\rm TOV}/M_{\odot} \le 2.16^{+0.17}_{-0.15}$$
 maximum mass

$$12.00 < R_{1.4}/{
m km} < 13.45$$
 $\tilde{\Lambda}_{1.4} > 375$ radius, tidal deformability

$$M_{\rm th}/M_{\rm TOV} \approx 1.41~R_{\rm TOV} \geq 9.74^{+0.14}_{-0.04}\,{\rm km}$$
 threshold mass

*A phase transition after a BNS merger leaves GW signatures and opens a gate to access quark matter beyond accelerators

Conclusions

Much of the research presented is is part of **ELEMENTS**, an Hessian Research Cluster with Frankfurt Darmstadt and Giessen

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