

Ideas on probing TMDs and spin entanglement via double Λ polarizations

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BNL

08.06.2020

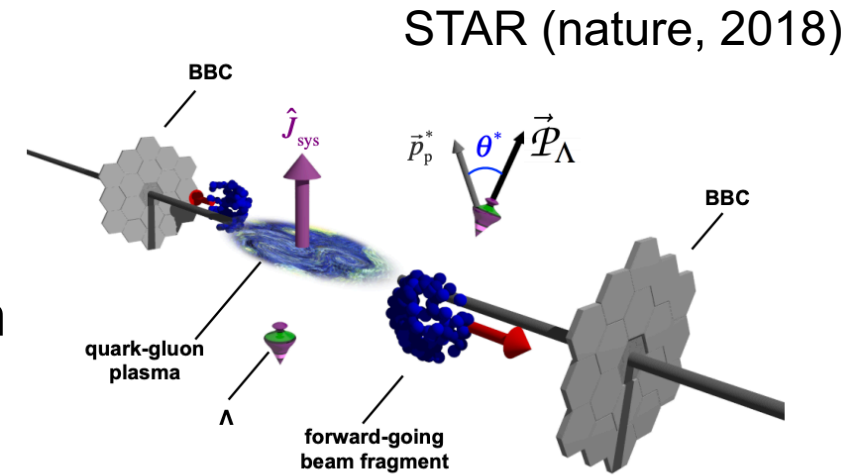
Ideas are inspired from
discussions with Raju, Dima,
Elke, Thomas, et al...

Lambda polarization

- Lambda hyperon - parity-violating nature of its weak decay – results in *angular distribution* of the decay proton preferentially emitting along the lambda direction



- Great tool for studying spin and polarization effects.
 - Lambda polarization was observed in ee. (BELLE)
 - **Lambda polarization was observed in ep unpolarized DIS. (HERMES)**
 - Global Lambda polarization in heavy ion collisions – vorticity (STAR)
 - **Lambda polarization with respect to transversely polarized axis in polarized DIS (COMPASS), Null result**



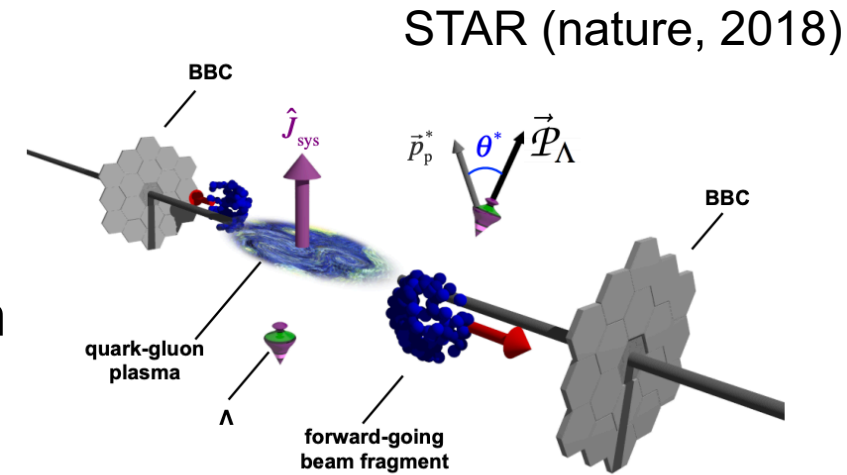
$$\frac{dN}{d \cos \theta} \propto 1 + \alpha P_{\Lambda} \cos \theta$$

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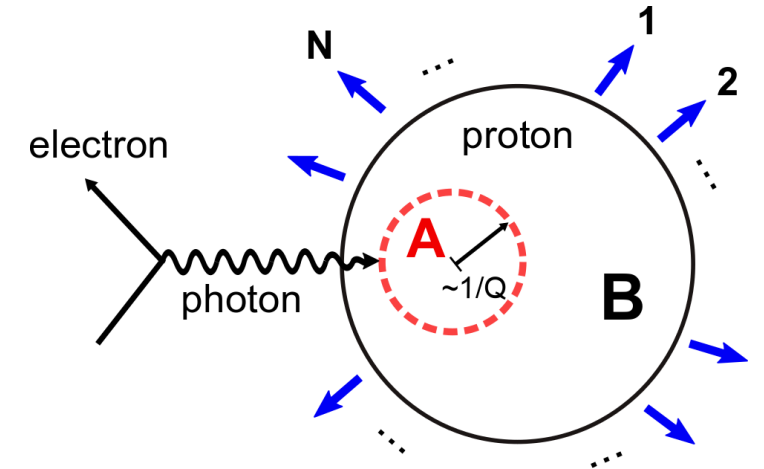


$$\frac{dN}{d \cos \theta} \propto 1 + \alpha P_{\Lambda} \cos \theta$$

These topics are deeply related to TMD physics, e.g., TMD PDFs, TMD FFs, which are in line with the EIC physics.

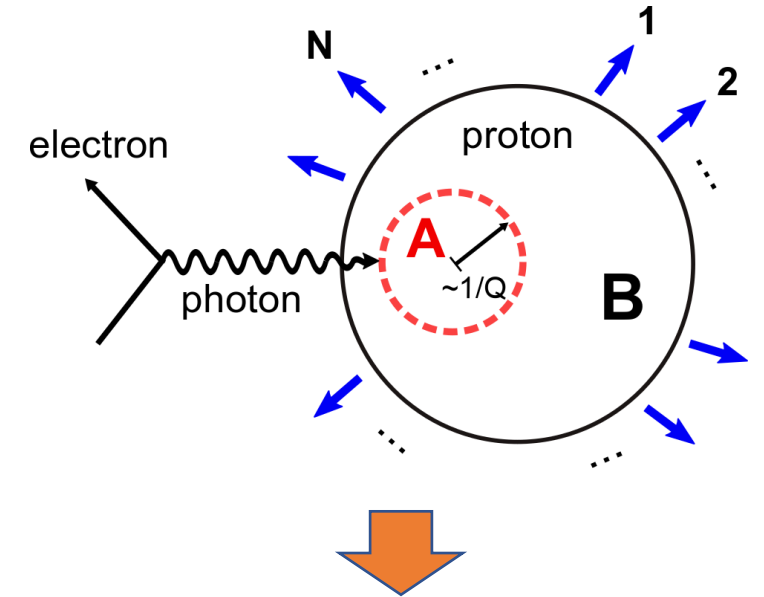
Questions

- Can I use lambda polarization to study entanglement? From two distinct regions that are casually disconnected, e.g., Region A & B. (*Ideas from Dima, Thomas, and our paper*)
- Are quarks/gluons entangled in polarized and/or unpolarized proton?
- What's their dynamical picture from high-x to low-x? Is there a quantum to classical transition? (*saturations? Raju's novel idea for entanglement*)
- What can we learn from their (not) entanglement/correlations? Do these measurements constrain TMDs PDF or FFs? (*questions inspired by Elke's comments*)
- Or turn the question around, can TMDs predict such correlations?



Questions

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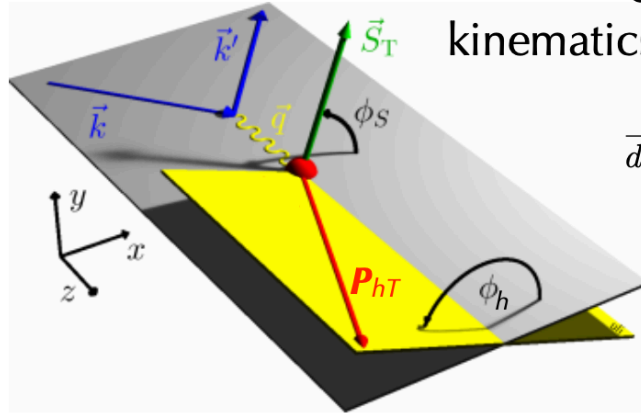
Generally, I would like to build a correlation measurement:

1. Lambda from current region
2. Lambda from target region
3. Their correlation as a function of rapidity gap.

*Correlations can be with respect to each other or a common quantization axis.

Established measurements

– focus on current fragmentations



SIDIS
kinematics & cross section

$$\frac{d\sigma}{dx dy dz d\phi_h dP_{hT}^2} \sim \begin{aligned} & A(y) F_U + B(y) \cos 2\phi_h F_U^{\cos 2\phi_h} \\ & + C(y) F_{LL} + B(y) \sin 2\phi_h F_L^{\sin 2\phi_h} \\ & + A(y) \sin(\phi_h - \phi_S) F_T^{\sin(\phi_h - \phi_S)} \\ & + B(y) \sin(\phi_h + \phi_S) F_T^{\sin(\phi_h + \phi_S)} \\ & + B(y) \sin(3\phi_h - \phi_S) F_T^{\sin(3\phi_h - \phi_S)} \\ & + C(y) \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \end{aligned}$$

- build $\frac{d\sigma^\uparrow(\phi_h, \phi_S) - d\sigma^\downarrow(\phi_h, \phi_S + \pi)}{d\sigma^\uparrow(\phi_h, \phi_S) + d\sigma^\downarrow(\phi_h, \phi_S + \pi)}$ (or similar when electron is polarized)

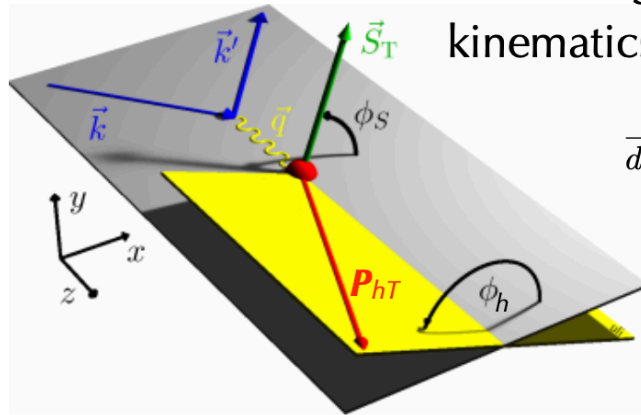
- isolate specific azimuthal component, coefficient $\sim \frac{F_X^{xxx}(x, z, P_{hT}^2; Q^2)}{F_U(x, z, P_{hT}^2; Q^2)}$

Azimuthal Spin Asymmetry $\equiv A_X^{xxx}(x, z, P_{hT}^2; Q^2)$

(Nice summary by Marco Radici's slides,
https://indico.cern.ch/event/797767/contributions/3682622/attachments/1965784/3268756/6_radici.pdf)

Established measurements

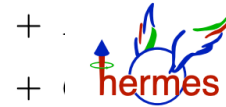
- focus on current fragmentations



SIDIS
kinematics & cross section

$$\frac{d\sigma}{dx dy dz d\phi_h dP_{hT}^2} \sim A(y) F_U + B(y) \cos 2\phi_h F_U^{\cos 2\phi_h} + C(y) F_{LL} + B(y) \sin 2\phi_h F_L^{\sin 2\phi_h} + A(y) \sin(\phi_h - \phi_S) F_{\tau}^{\sin(\phi_h - \phi_S)}$$

+ All 8 asymmetries have been measured (plus more at subleading twist..)



- build $\frac{d\sigma^\uparrow(\phi_h, \phi_S) - d\sigma^\downarrow(\phi_h, \phi_S + \pi)}{d\sigma^\uparrow(\phi_h, \phi_S) + d\sigma^\downarrow(\phi_h, \phi_S + \pi)}$ (or similar w

$A_U^{\cos 2\phi_h}$ on p & D targets [arXiv:1204.4161](https://arxiv.org/abs/1204.4161)
 $A_L^{\sin 2\phi_h}$ on p \rightarrow [hep-ph/0608048](https://arxiv.org/abs/hep-ph/0608048)

$A_U^{\cos 2\phi_h}$ on D targets [arXiv:1401.6284](https://arxiv.org/abs/1401.6284)
 A_{LL} on p \rightarrow [arXiv:1509.03526](https://arxiv.org/abs/1509.03526)

- isolate specific azimuthal component, coefficient

$A_T^{\sin(\phi_h - \phi_S)}$ on p \uparrow [arXiv:0906.3918](https://arxiv.org/abs/0906.3918)
 $A_T^{\sin(\phi_h + \phi_S)}$ on p \uparrow [arXiv:1006.4221](https://arxiv.org/abs/1006.4221)

A_{LL} & $A_L^{\sin 2\phi_h}$ on p \rightarrow [arXiv:1509.03526](https://arxiv.org/abs/1509.03526) on D \rightarrow [arXiv:1609.06062](https://arxiv.org/abs/1609.06062)

$A_T^{\sin(\phi_h - \phi_S)}$ on p \uparrow [arXiv:1205.5122](https://arxiv.org/abs/1205.5122) [arXiv:1609.07374](https://arxiv.org/abs/1609.07374) } [arXiv:1005.5609](https://arxiv.org/abs/1005.5609)
 $A_T^{\sin(\phi_h + \phi_S)}$ on p \uparrow [arXiv:1205.5121](https://arxiv.org/abs/1205.5121) } [arXiv:1408.4405](https://arxiv.org/abs/1408.4405)

$A_T^{\sin(\phi_h \pm \phi_S)}$ on D \uparrow [arXiv:0802.2160](https://arxiv.org/abs/0802.2160)

$A_T^{\sin(\phi_h \pm \phi_S)}$ & $A_{LT}^{\cos(\phi_h - \phi_S)}$ & $A_T^{\sin(3\phi_h - \phi_S)}$ on p \uparrow [arXiv:1512.06590](https://arxiv.org/abs/1512.06590)

Azimuthal Spin Asymmetry

Jefferson Lab

Hall A $A_T^{\sin(\phi_h \pm \phi_S)}$ on $^3\text{He}\uparrow$ with π [arXiv:1106.0363](https://arxiv.org/abs/1106.0363) with K [arXiv:1404.7204](https://arxiv.org/abs/1404.7204)

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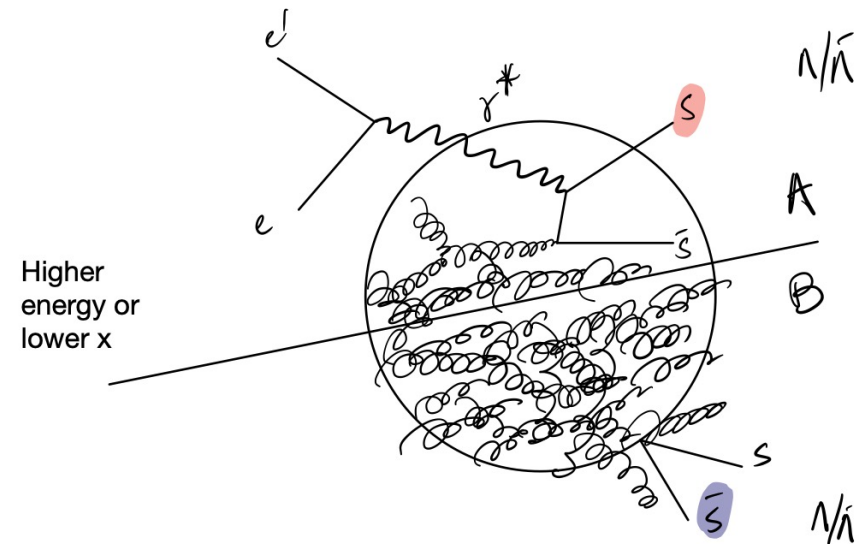
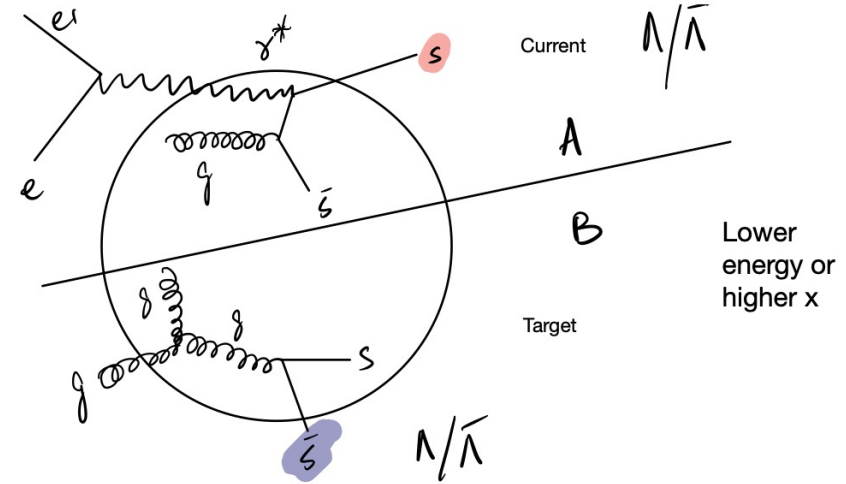
$A_T^{\sin(3\phi_h - \phi_S)}$ on $^3\text{He}\uparrow$ [arXiv:1312.3047](https://arxiv.org/abs/1312.3047)

Hall B A_{LL} & $A_L^{\sin 2\phi_h}$ on p \rightarrow [arXiv:1003.4549](https://arxiv.org/abs/1003.4549)

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Proposing new measurements

- Correlations between two lambdas, can be studied with Same-sign (SS) or Opposite-sign (OS), namely lambda-lambda or lambda-anti-lambda.
- Correlations between current and target regions or large rapidity gap.
- Correlations with respect to each other, or simultaneously with respect to a common axis, e.g., nucleon polarization axis.
- Current vs Target correlations. Entanglement?



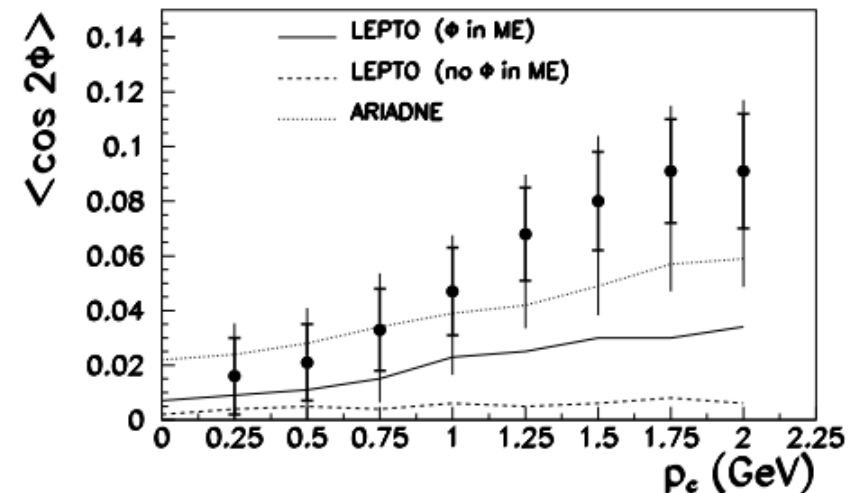
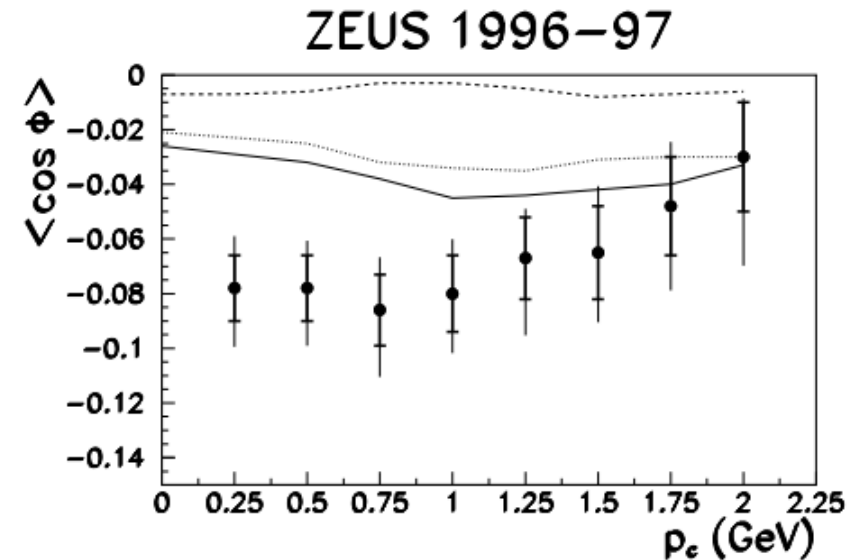
Tool

- Monte Carlo generator, PYTHIA 8, to establish baseline. No spin or nontrivial effect should be expected.
- DIS process at EIC top energy. (18 x 275 GeV² ep)
- $Q^2 > 1$ and $0.05 < y < 0.95$
- Generated 2 billions events with $Q^2 > 1$.
- With EIC detector coverage in mind.

- First to establish the observables and correlators.

HCM – charged pion asymmetry

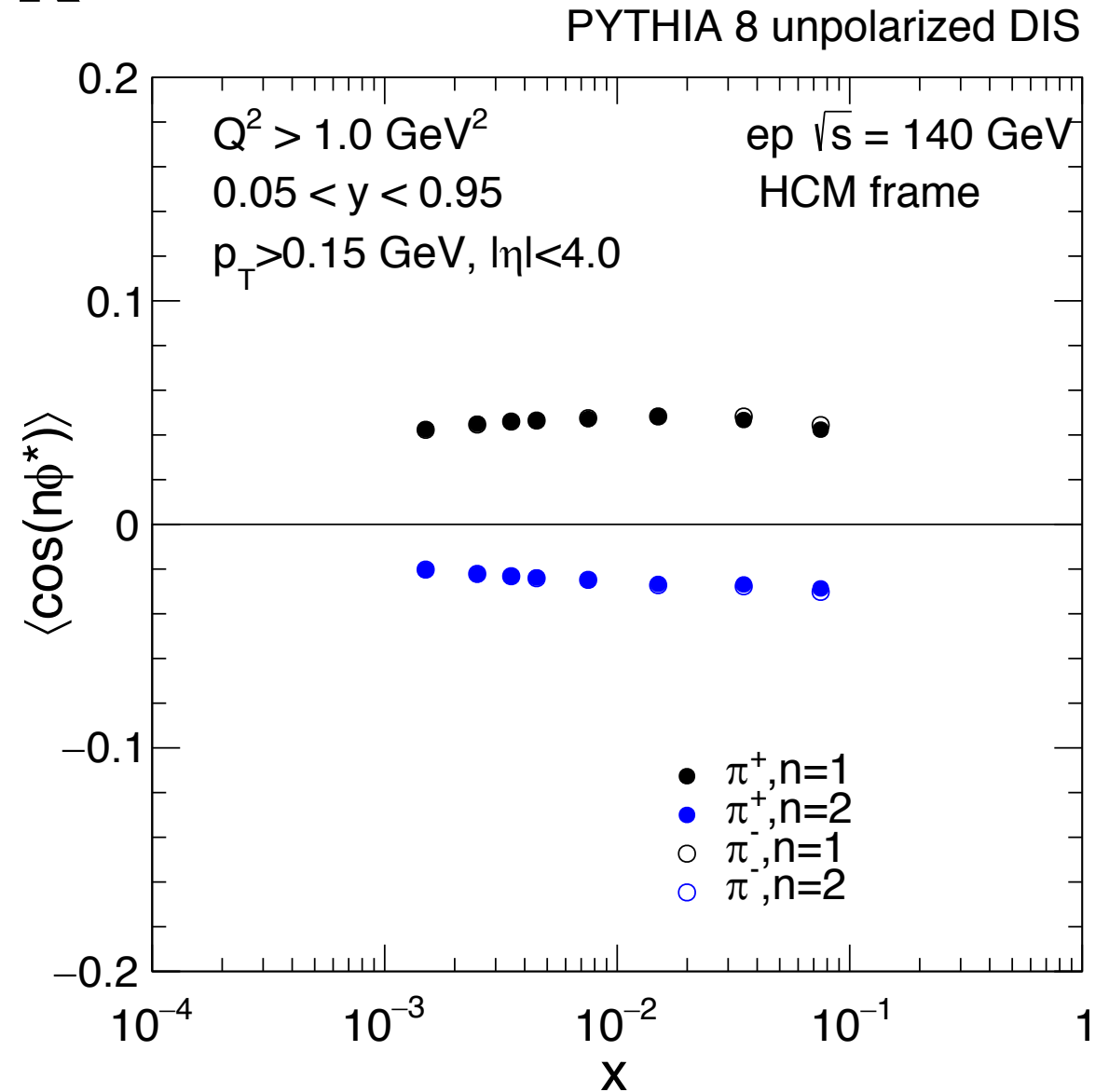
- Boer-Molders distribution uses unpolarized DIS ep and look at $\langle \cos(\phi^*) \rangle$ and $\langle \cos(2\phi^*) \rangle$, have been measured at ZEUS, HERMES, COMPASS.
- MC does have nonzero correlations, seen by ZEUS using Ariadne and LEPTO
- (I don't find much explanations why nonzero in MCs, yet)



<https://arxiv.org/pdf/hep-ex/0003017.pdf>

Pythia 8 – first look

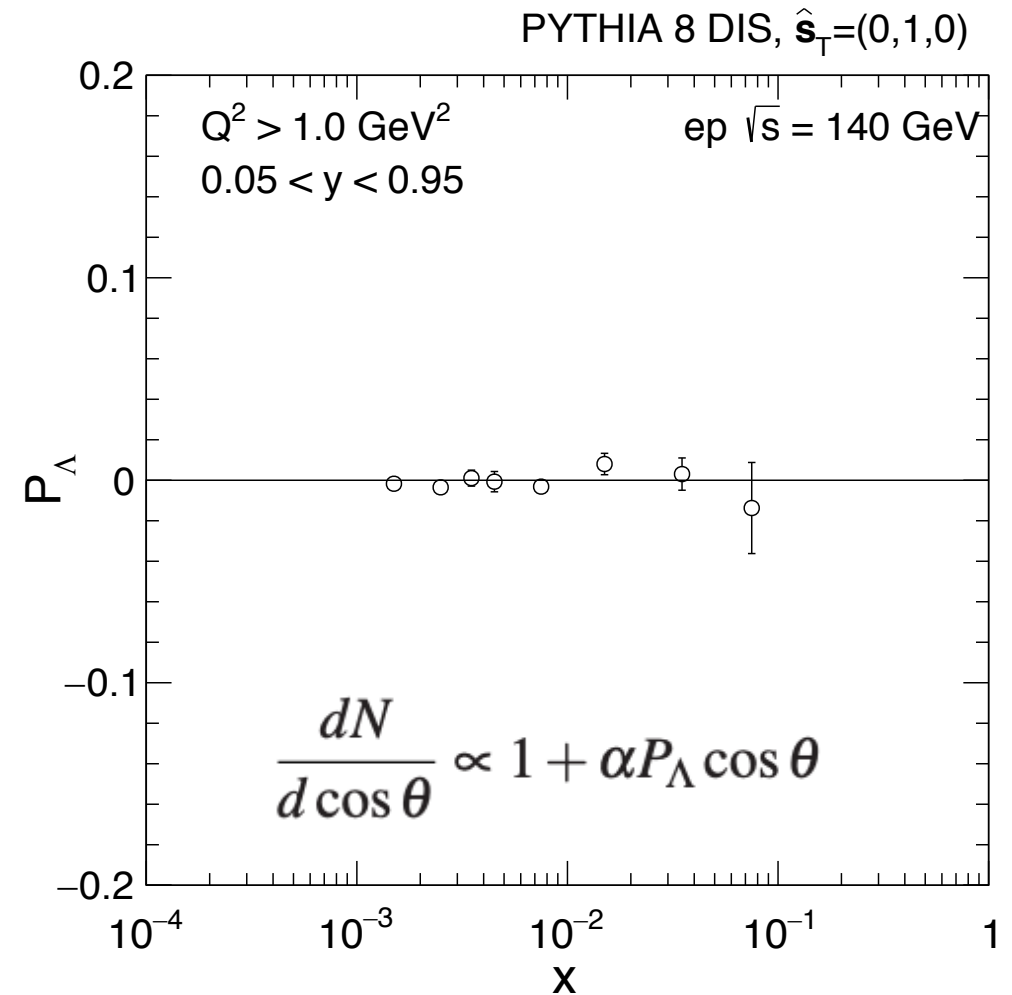
- Used charged pions and both $\cos(\phi^*)$ and $\cos(2\phi^*)$
- Observations are very similar to what ZEUS showed.
- No charge separations are seen. Same for π^+ and π^-
- Good baseline.



Pythia 8

– artificial transversely polarized proton

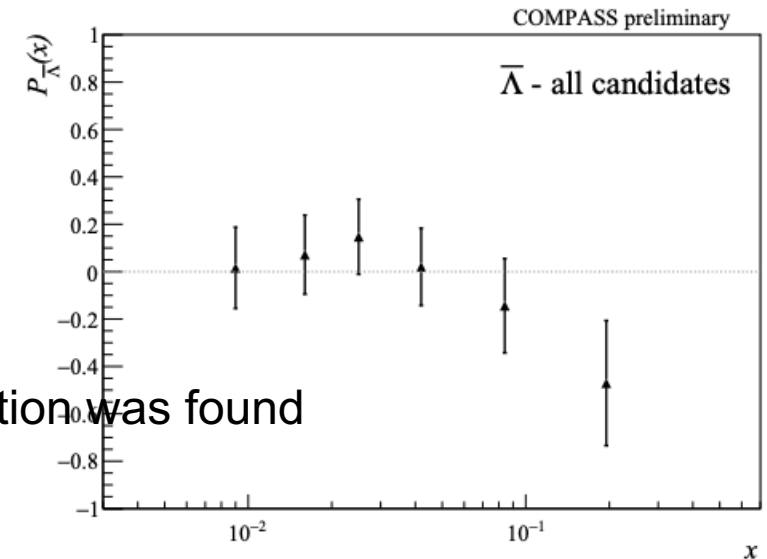
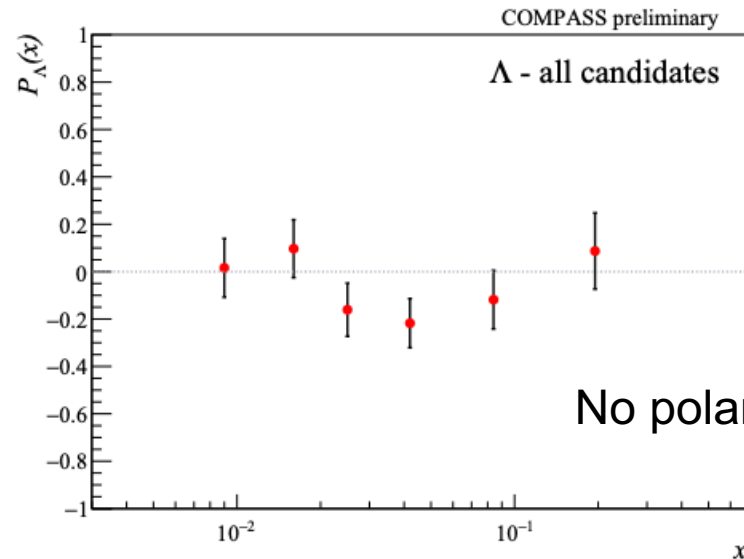
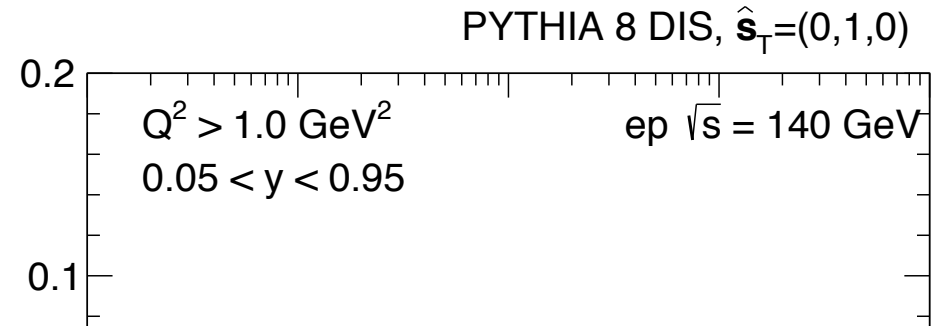
- To establish the observable, I used $(0,1,0)$ as transversely polarized nucleon direction, similar to HERMES or COMPASS. Of course, the underlying physics is still unpolarized DIS.
- Inclusive lambda polarizations, including lambda and lambda-bar.



Pythia 8

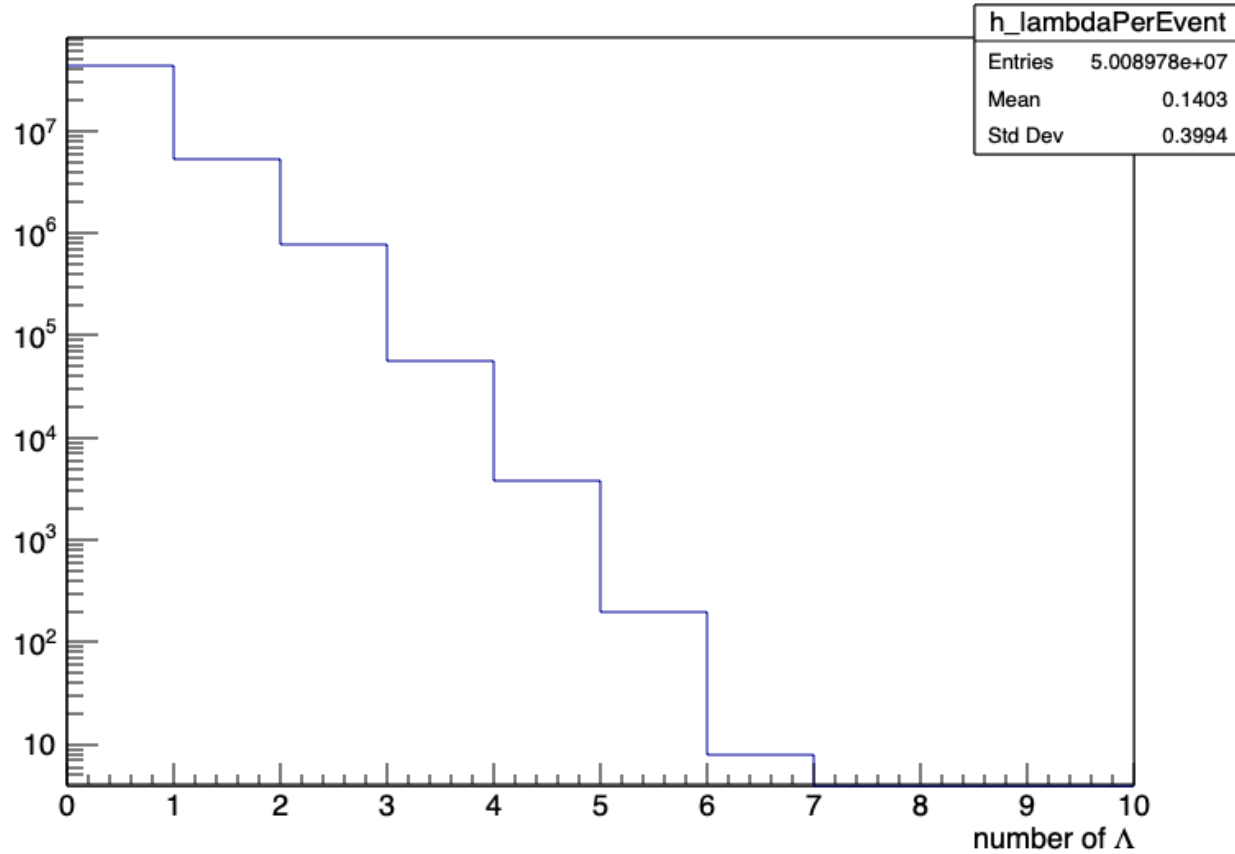
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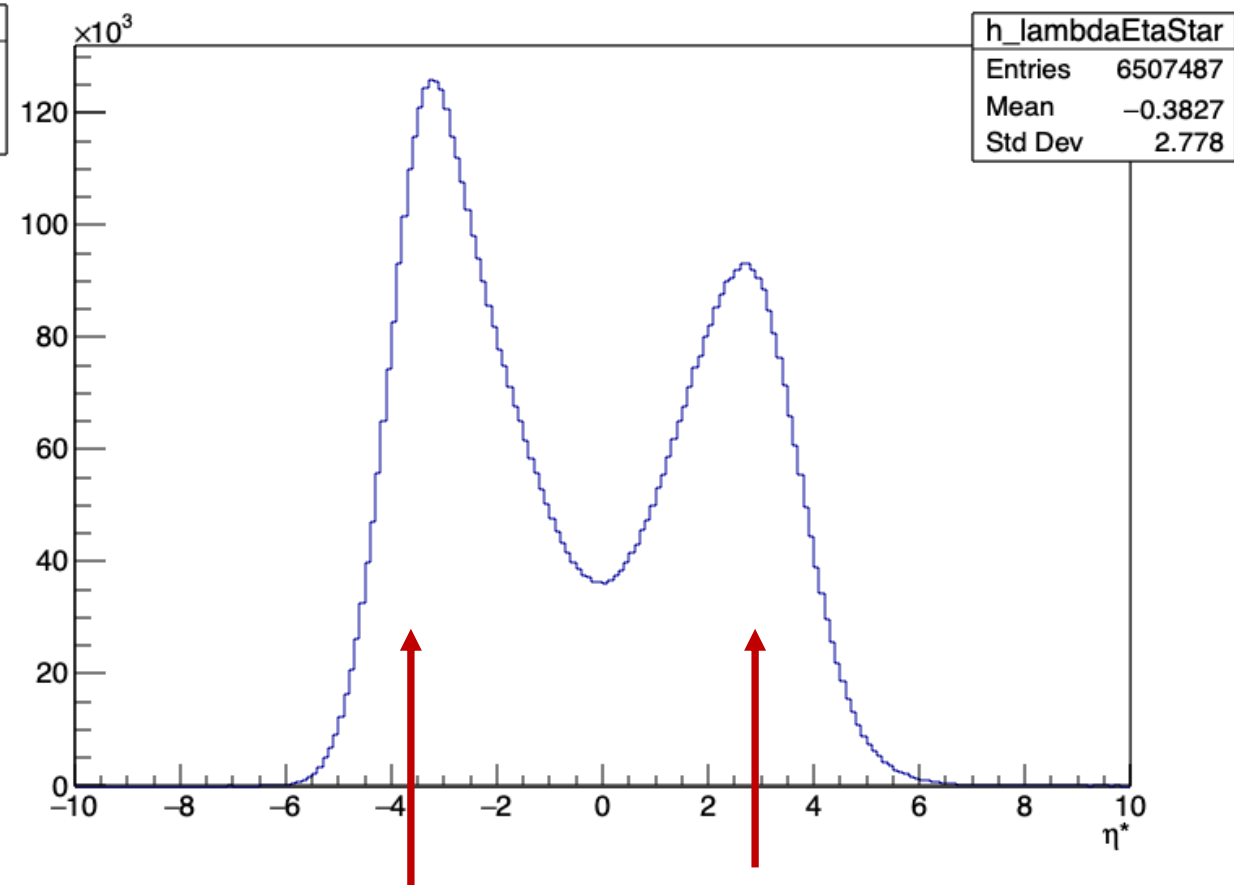
Pythia 8 – double lambdas

2B events of DIS



Number of lambdas per event distribution

HCM frame lambda eta* distribution



Target lambdas

Current lambdas

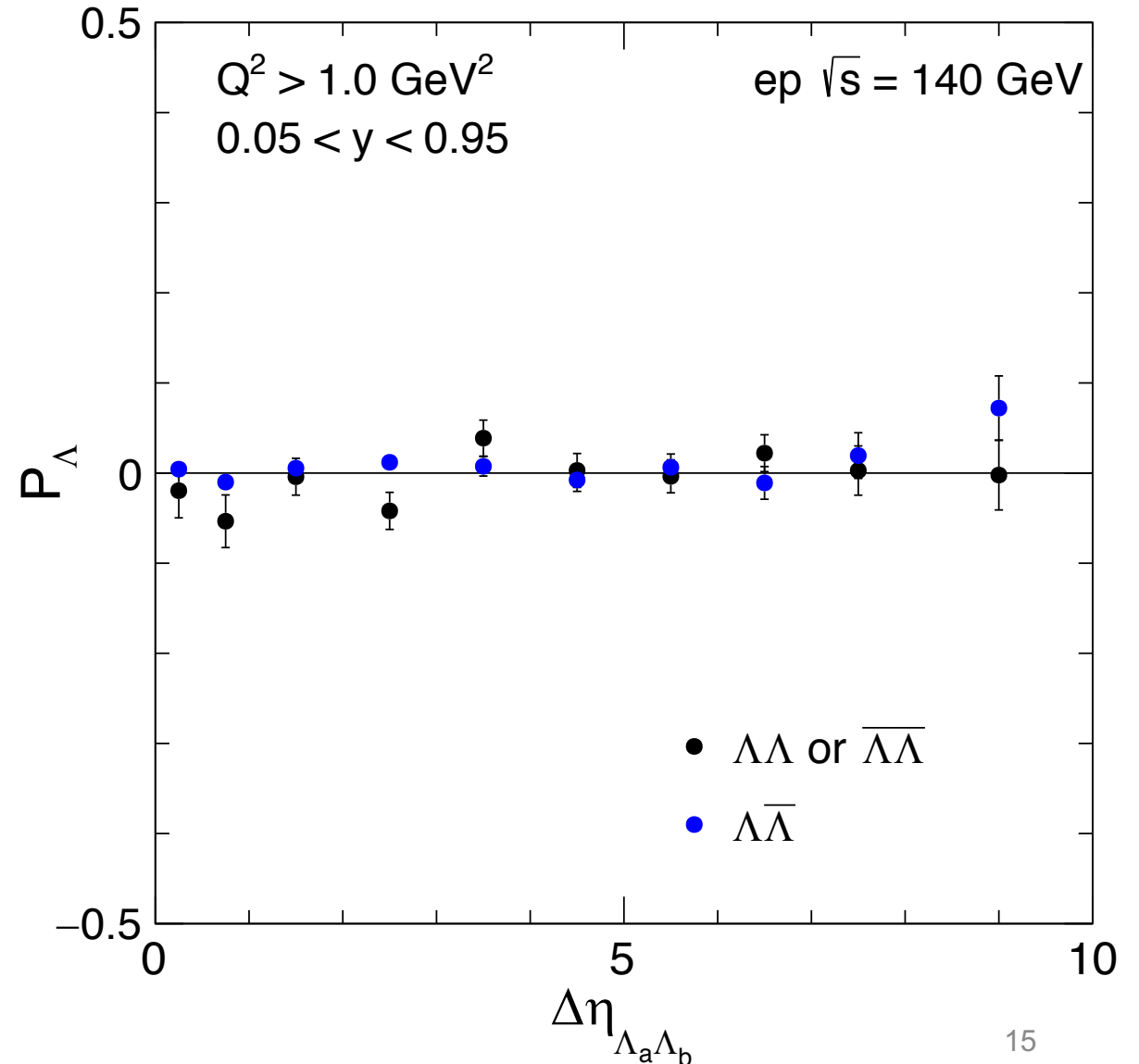
Lambda polarization w.r.t another lambda

- Lambda 1, use its proton daughter in lambda 1's rest frame, with respect to the Lambda 2 momentum direction.

$$\frac{dN}{d \cos \theta} \propto 1 + \alpha P_{\Lambda} \cos \theta$$

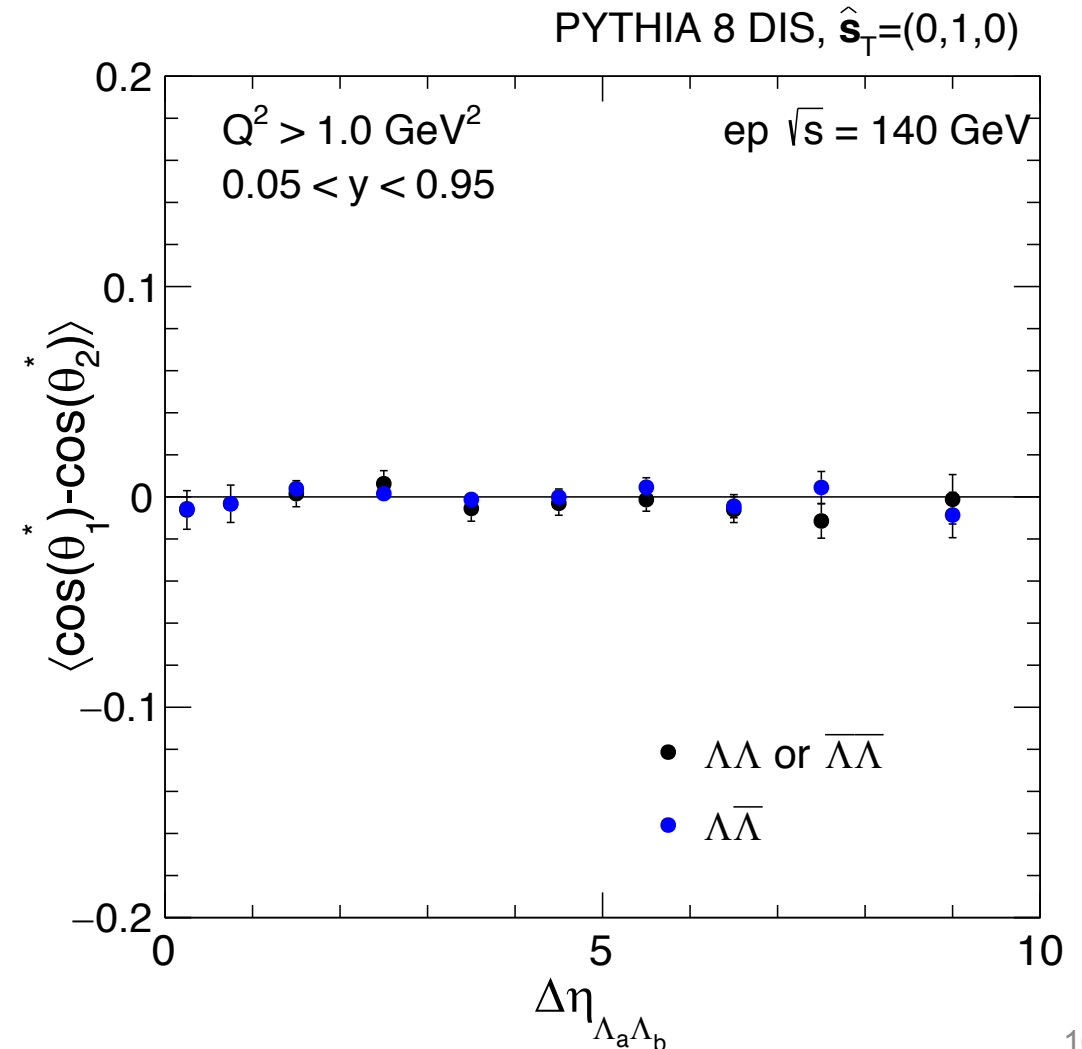
- As a function of two lambdas' rapidity gap
- SS and OS are separated.
- At large rapidity gap, if strange quarks are entangled, will there be correlation? In either polarized or unpolarized target

PYTHIA 8 unpolarized DIS



Double lambda polarization with respect to nucleon spin

- Theta*1 is the lambda 1's proton daughter in lambda 1's rest frame with respect to (0,1,0). Similar for lambda 2.
- Alternative observable can be $\langle \cos(\theta_1^* - \theta_2^*) \rangle$
- Analogy to CME observable for charge separations. Should expect an OS and SS separation?



Summary and next step

- Pythia 8 has been looked at and baselines are established for these new observables.
- MC has no signal, meaning no trivial kinematics or acceptance can give any signal.
- Working on CHSH inequality test (Bell's inequality test) using two lambdas. (some progress has been made but not finish yet)
- Similar (~exact) observables can be built in pp collisions? Test at the LHC and RHIC? STAR forward upgrades with single polarized proton beam?