

Jet charge: a flavor prism for spin asymmetries at the EIC

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EIC Yellow Report : Jet and Heavy Flavor Physics WG meeting
August 10, 2020

Based on Kang, Liu, Mantry, Shao, [arXiv:2008.00655](https://arxiv.org/abs/2008.00655)

Jet Physics at the EIC

- Jet physics at the EIC: a fast emerging field of research

The EIC science program with jets

Jets as tools to realize the EIC science goals — Recent publications

- The spin of the proton, PDFs

Hinderer, Schlegel, Vogelsang `15, `17, Abelof, Boughezal, Liu, Petriello `16, Boughezal, Petriello, Xing `18, Aschenauer, Chu, Page `19, Borsa, Florian, Pedron `20, Arratia, Furlotova, Hobbs, Olness, Sekula `20

- 3D nucleon/nucleus tomography

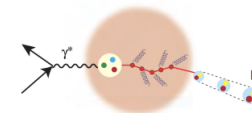
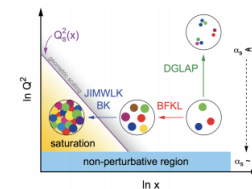
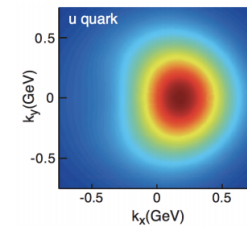
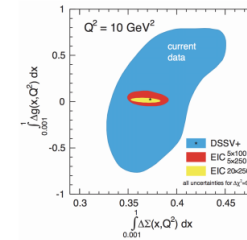
Zheng, Aschenauer, Lee, Xiao, Yin `18, Liu, FR, Vogelsang, Yuan `19, Gutierrez-Reyes, Scimemi, Waalewijn, Zoppi `19, Hatta, Mueller, Ueda, Yuan `19, Arratia, Kang, Prokudin, FR `20

- Saturation, a new form of gluon matter

Hatta, Xiao, Yuan `17, Salazar, Schenke `19, Roy, Venugopalan `19, Kang, Liu `19

- Hadronization and quarks and gluons in the nucleus

Klasen, Kovarik `18, Aschenauer, Lee, Page, FR `19, Qin, Wang, Zhang `19, Arratia, Song, FR, Jacak `19, Li et al. `20



Courtesy of F. Ringer at BNL jet workshop in July

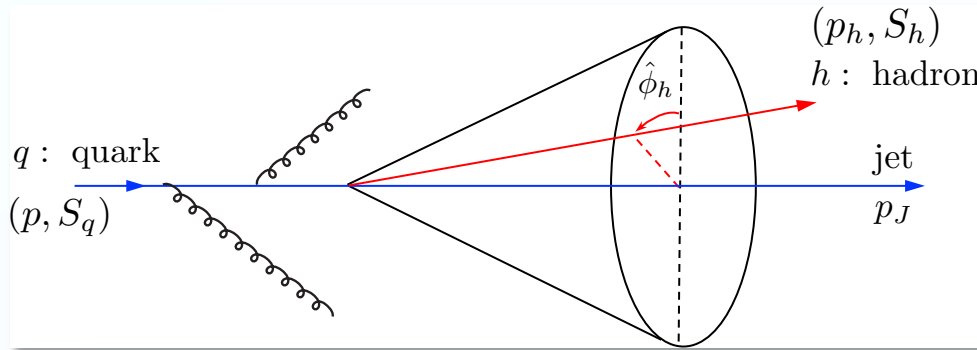
Jets for 3D imaging

- Using jets for 3D imaging of the nucleon
 - seems to become quite feasible
 - seems to attract a lot of interest



Some recent examples

- Jet fragmentation functions



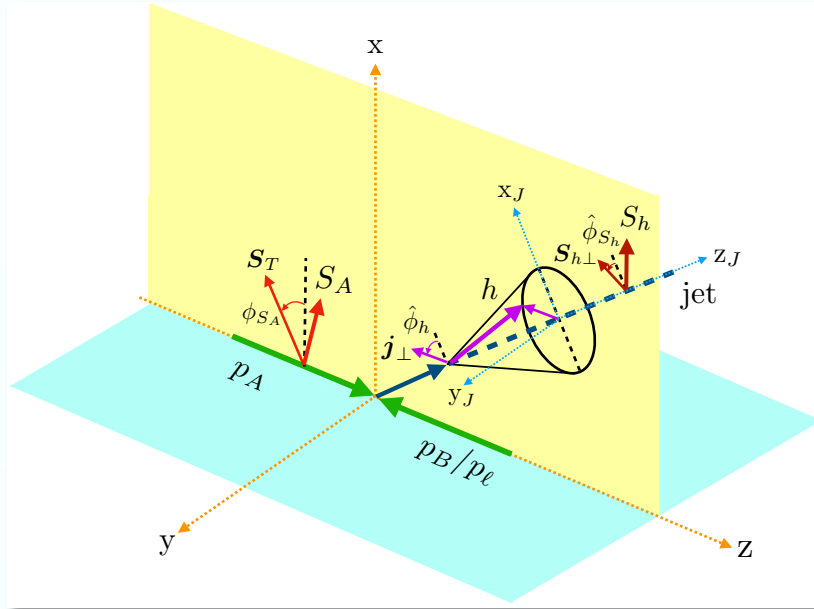
$$z_h = \frac{p_{hT}}{p_{JT}}$$
$$j_T$$

- If one measures only the z_h distribution (integrated over j_T), one probes collinear FFs
 - unpolarized, longitudinally, transversely polarized
- If one measures both z_h and j_T distribution (3D), one probes TMD FFs
 - With all possible polarizations

Azimuthal angular dependence

- All the azimuthal angular dependence for single inclusive jet

Kang, Kyle, Zhao, arXiv:2005.02398



Collins effect

$$\frac{d\sigma^{p(S_A)+p/e \rightarrow (\text{jet } h(S_h))X}}{dp_{JT} d\eta_J dz_h d^2 \mathbf{j}_\perp} = F_{UU,U} + |\mathbf{S}_T| \sin(\phi_{S_A} - \hat{\phi}_h) F_{TU,U}^{\sin(\phi_{S_A} - \hat{\phi}_h)} + \Lambda_h \left[\lambda F_{LU,L} + |\mathbf{S}_T| \cos(\phi_{S_A} - \hat{\phi}_h) F_{TU,L}^{\cos(\phi_{S_A} - \hat{\phi}_h)} \right]$$

$$+ |\mathbf{S}_{h\perp}| \left\{ \sin(\hat{\phi}_h - \hat{\phi}_{S_h}) F_{UU,T}^{\sin(\hat{\phi}_h - \hat{\phi}_{S_h})} + \lambda \cos(\hat{\phi}_h - \hat{\phi}_{S_h}) F_{LU,T}^{\cos(\hat{\phi}_h - \hat{\phi}_{S_h})} \right.$$

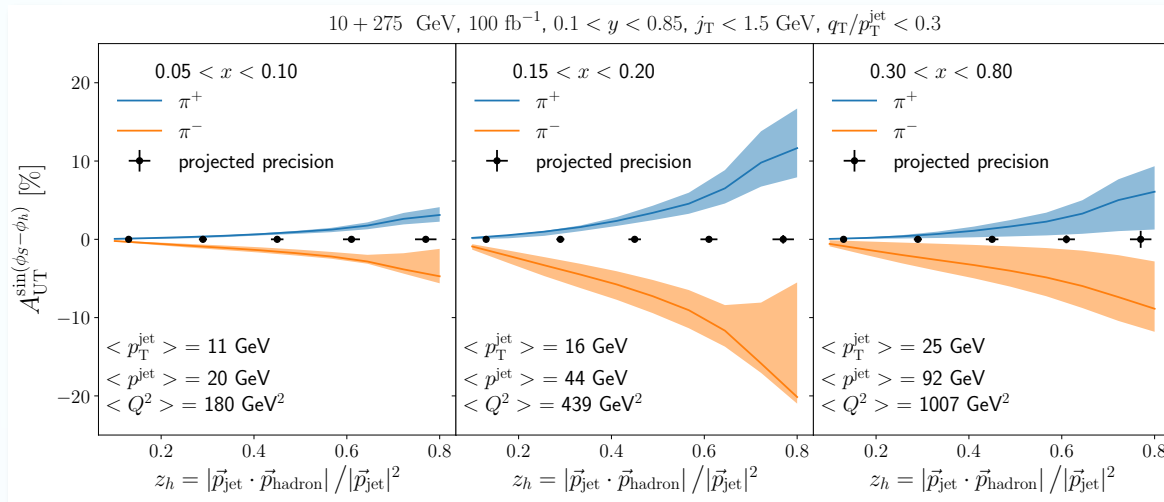
$$\left. + |\mathbf{S}_T| \left(\cos(\phi_{S_A} - \hat{\phi}_{S_h}) F_{TU,T}^{\cos(\phi_{S_A} - \hat{\phi}_{S_h})} + \cos(2\hat{\phi}_h - \hat{\phi}_{S_h} - \phi_{S_A}) F_{TU,T}^{\cos(2\hat{\phi}_h - \hat{\phi}_{S_h} - \phi_{S_A})} \right) \right\}$$

Lambda polarization

Examples

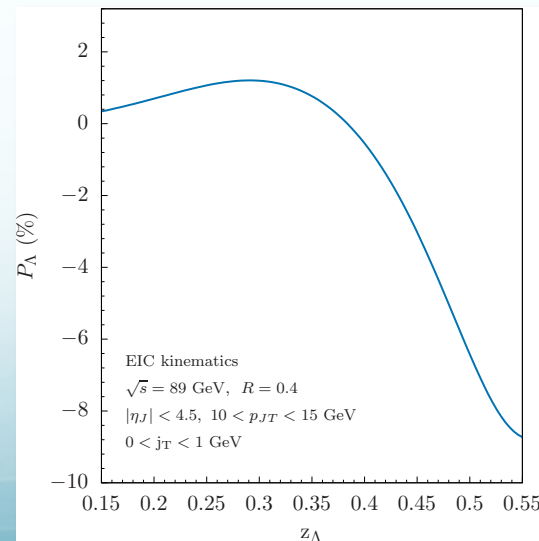
- Collins effect at the EIC

Arratia, Kang, Prokudin, Ringer, arXiv:2007.07281



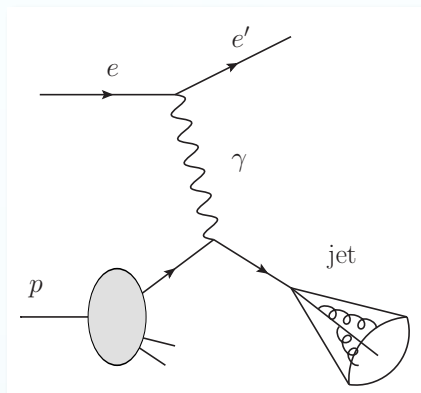
- Lambda polarization at the EIC

Kang, Kyle, Zhao, arXiv:2005.02398

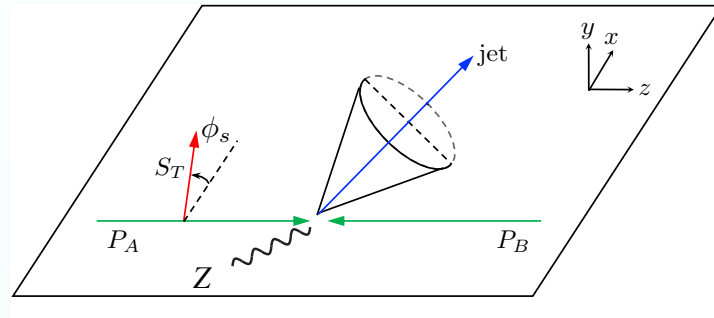


Back-to-back region for TMD PDFs

- One can also study TMD PDFs via back-to-back jet production
 - $e+p \rightarrow e+\text{jet}+X$
 - $p+p \rightarrow (Z, \gamma, \dots)+\text{jet}+X$



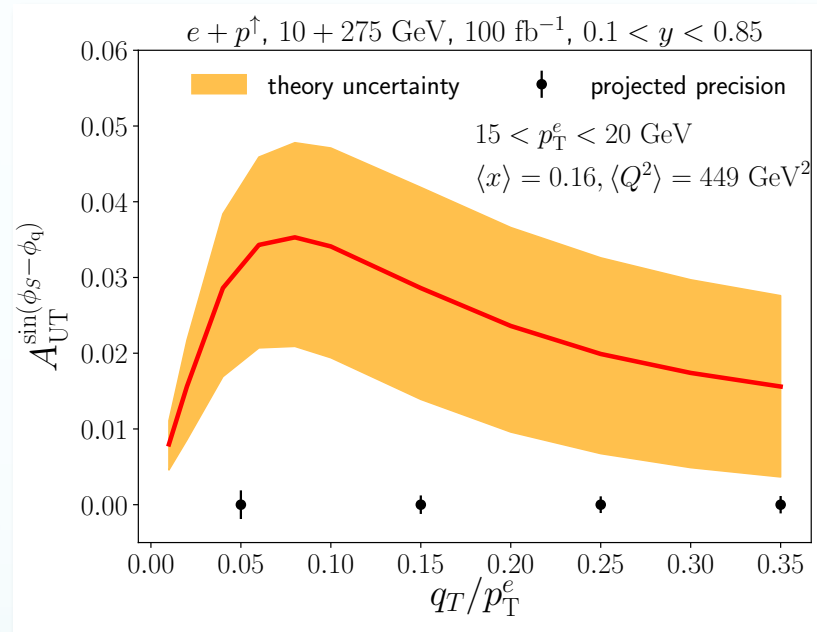
Kang, Lee, Terry, Xing, arXiv:1906.07187
Chien, Shao, Wu, arXiv:1905.01335, ...



Arratia, Kang, Prokudin, Ringer, arXiv:2007.07281
Liu, Ringer, Vogelsang, Yuan, 18, 20, ...

Examples

- Sivers asymmetry at the EIC
 - electron-jet back-to-back production



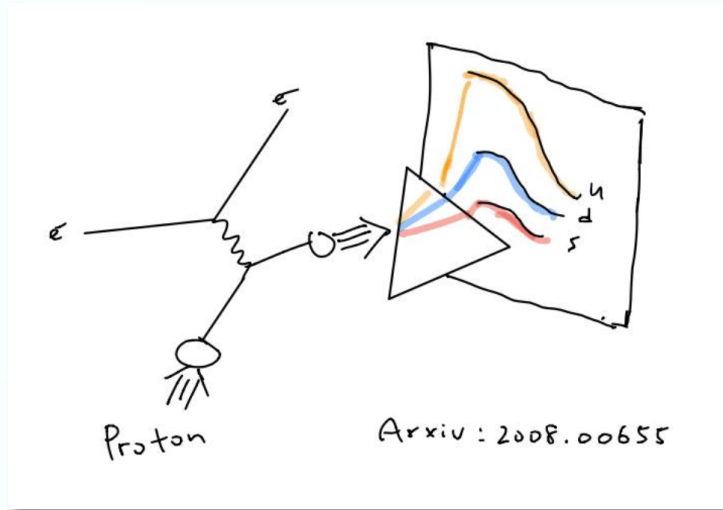
Arratia, Kang, Prokudin, Ringer, arXiv:2007.07281

All seem to be nice

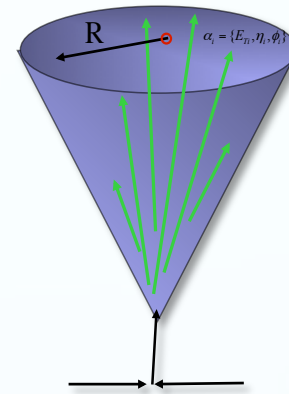
- Perception: all seem to be nice, complimentary to SIDIS measurement
 - It seems that something is missing, or has not been discussed much
 - That is flavor separation, which is important in mapping out the flavor and spin structure of the nucleon – an essential mission of EIC
- Flavor separation in DIS or SIDIS
 - In DIS: using different target – proton, deuteron, He3 (neutron)
 - gives us u and d flavor separation [R. Milner, arXiv:1809.05626](#)
 - In SIDIS: measure different hadrons in the final state (π^+ , π^- , K^+ , K^- , etc)
 - Because FFs are different (π^+ will select u quark, π^- more d quark, Kaons for s quark)
 - Of course it is highly important to know very well FFs for these hadrons, in order to make firm conclusion on the flavor structure of the nucleon
[Sato, Andres, Ethier, Melnitchouk, arXiv:1905.03788](#)
(strange quark)
- How do we perform flavor separation for jet observables?

Jet charge

- Jet charge: a flavor prism



Courtesy of Xiaohui Liu



- Jet charge definition

- One might use subset of hadrons (pions, Kaons) in jet to construct jet charge

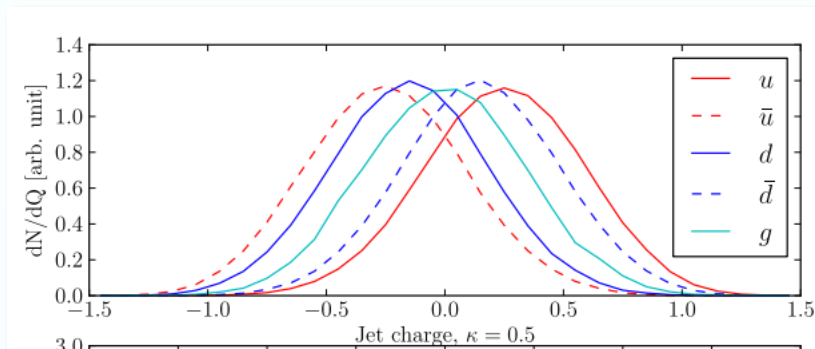
$$Q_\kappa = \sum_h Q_\kappa^h \equiv \sum_{h \in \text{jet}} z_h^\kappa Q_h$$

Charge of the hadron

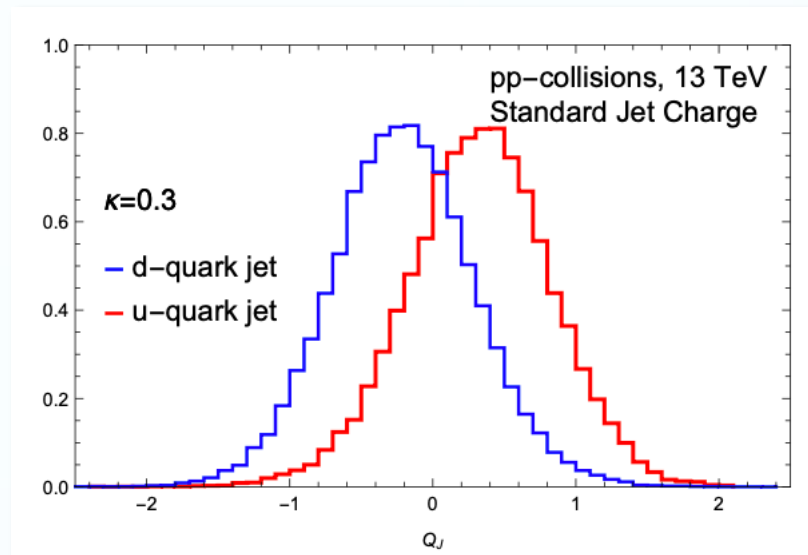
$$z_h = \frac{p_{hT}}{p_{JT}} \quad \kappa = 0.3, 0.4, \dots, 1.0$$

Charge distribution of u and d quark jets

- Jet charge distribution



Krohn, Schwartz, Lin, Waalewijn, arXiv:1209.2421

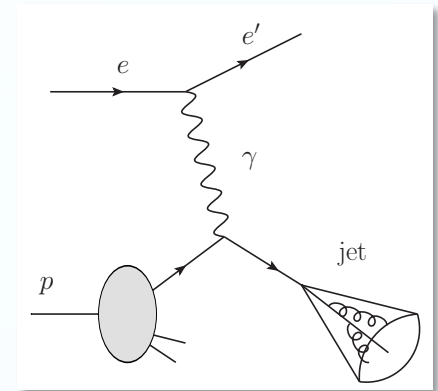


Courtesy of S. Mantry

- If one sums over all particles, u and d jet charges sum over, we have a distribution around $Q_J \sim 0$
 - If one can select the positive jet charge bin, then our result is more sensitive to u quark jet
 - Negative jet charge bin: sensitive to d quark jet

Pick an example

- Pick an example, demonstrate if it works, how it works
 - Sivers asymmetry in electron-jet back-to-back production
- In the back-to-back region
 - Nice thing: $e+q \rightarrow e+q$ dominates at leading power
 - So *jet flavor is the same as the incoming quark flavor*
- Factorization formalism
 - Unpolarized production: for a particular quark scattering (q_T : imbalance)
 - Jet function: describe transition from a parton i into a jet with p_T and R



$$\frac{d\sigma_{UU}^i}{dy_e d^2p_T^e d^2q_T} \propto e_i^2 \int \frac{d^2b_T}{(2\pi)^2} e^{iq_T \cdot b_T} \tilde{f}_i(x, b_T, \mu) S_J(b_T, R, \mu) H(Q, \mu) \mathcal{J}_i(p_T R, \mu)$$

Jet charge function

- Now besides characteristics (p_T , R) of the jet, we also want to measure the jet charge Q_κ
 - Need a new jet function - called it “jet charge function”

$$\frac{d\sigma_{UU}^i(Q_\kappa)}{dy_e d^2p_T^e d^2q_T} \propto e_i^2 \int \frac{d^2b_T}{(2\pi)^2} e^{iq_T \cdot b_T} \tilde{f}_i(x, b_T, \mu) S_J(b_T, R, \mu) H(Q, \mu) \mathcal{G}_i(Q_\kappa, p_T R, \mu)$$

- In comparison with the standard jet production

$$\frac{d\sigma_{UU}^i}{dy_e d^2p_T^e d^2q_T} \propto e_i^2 \int \frac{d^2b_T}{(2\pi)^2} e^{iq_T \cdot b_T} \tilde{f}_i(x, b_T, \mu) S_J(b_T, R, \mu) H(Q, \mu) \mathcal{J}_i(p_T R, \mu)$$

- Obviously if one integrates over the jet charge Q_κ , one would get back to the usual jet function

$$\int dQ_\kappa \mathcal{G}_i(Q_\kappa, p_T R, \mu) = \mathcal{J}_i(p_T R, \mu)$$

- Another NICE thing: due to RG consistency, these two jet functions have the **same QCD evolution**

See also Waalewijn, arXiv:1209.3019

The weighting factor

- The N-th moment of the jet charge in a particular jet charge bin

$$\langle (Q_{\kappa}^i)^N \rangle_{\text{bin}} = \int_{Q_{\kappa}\text{-bin}} dQ_J Q_J^N \frac{\mathcal{G}_i(Q_J, p_T R, \mu)}{\mathcal{J}_i(p_T R, \mu)}$$

$$\sum_{\text{bins}} \langle (Q_{\kappa}^i)^0 \rangle_{\text{bin}} = 1, \quad \sum_{\text{bins}} \langle Q_{\kappa}^i \rangle_{\text{bin}} = \langle Q_{\kappa}^i \rangle$$

- This ratio is RG-invariant, has a small $p_T R$ dependence from NLO as an argument in the coupling constant
- This weighting factor is *non-perturbative but universal*, thus one can determine from other jet production process in p+p, e+e- collisions (recall STAR dijet), it is just a number (like NRQCD matrix elements)
- Then build the cross section in a specific jet charge bin, easily generalize to polarized case (Sivers effect): **same weighting factor**

$$\frac{d\sigma_{UU}(Q_{\kappa, \text{bin}}^N)}{dy_e d^2 p_T^e d^2 q_T} = \sum_{i=u, d, \dots} \langle (Q_{\kappa}^i)^N \rangle_{\text{bin}} \frac{d\sigma_{UU}^i}{dy_e d^2 p_T^e d^2 q_T}$$

$$\frac{d\sigma_{UT}(S_{\perp}, Q_{\kappa, \text{bin}}^N)}{dy_e d^2 p_T^e d^2 q_T} = \sum_{i=u, d, \dots} \langle (Q_{\kappa}^i)^N \rangle_{\text{bin}} \frac{d\sigma_{UT}^i(S_{\perp})}{dy_e d^2 p_T^e d^2 q_T}$$

The weighting factor

- The N-th moment of the jet charge in a particular jet charge bin

$$\langle (Q_{\kappa}^i)^N \rangle_{\text{bin}} = \int_{Q_{\kappa}\text{-bin}} dQ_J Q_J^N \frac{\mathcal{G}_i(Q_J, p_T R, \mu)}{\mathcal{J}_i(p_T R, \mu)}$$

$$\sum_{\text{bins}} \langle (Q_{\kappa}^i)^0 \rangle_{\text{bin}} = 1, \quad \langle (Q_{\kappa}^i)^1 \rangle_{\text{bin}} = \langle Q_{\kappa}^i \rangle$$

- This ratio is RG-invariant, has a small $p_T R$ dependence, and is known to NLO as an argument in the coupling constant
- This weighting factor is *non-perturbative*, thus one can determine from other jet production process in hadron collisions (recall STAR dijet), it is just a number (like NRQCD matrix elements)

- Then build the cross section in a specific jet charge bin, easily generalize to polarized collisions (Sivers effect): **same weighting factor**

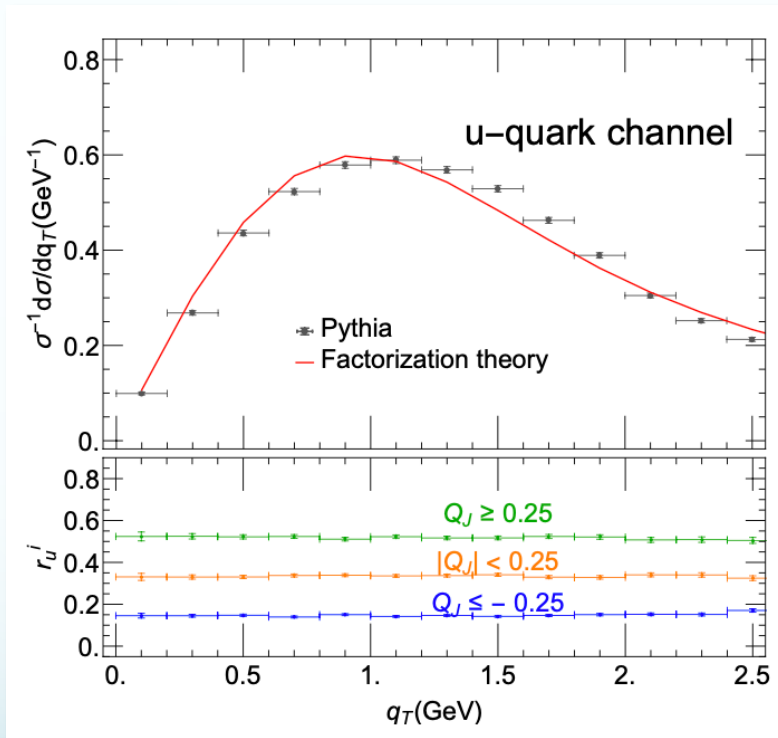
$$\frac{d\sigma_{LHC}^i}{dy_e d^2p_T^e d^2q_T} = \sum_{i=u,d,\dots} \langle (Q_{\kappa}^i)^N \rangle_{\text{bin}} \frac{d\sigma_{UU}^i}{dy_e d^2p_T^e d^2q_T}$$

$$\frac{d\sigma_{UT}(S_{\perp}, Q_{\kappa, \text{bin}}^N)}{dy_e d^2p_T^e d^2q_T} = \sum_{i=u,d,\dots} \langle (Q_{\kappa}^i)^N \rangle_{\text{bin}} \frac{d\sigma_{UT}^i(S_{\perp})}{dy_e d^2p_T^e d^2q_T}$$

Jet charge has been measured extensively at the LHC (charge tracks), **doable at the EIC?!?**

Unpolarized: weighting factors

- Using Pythia for now to determine these non-perturbative weighting factors
 - Pythia works well for this observable: u-quark jet

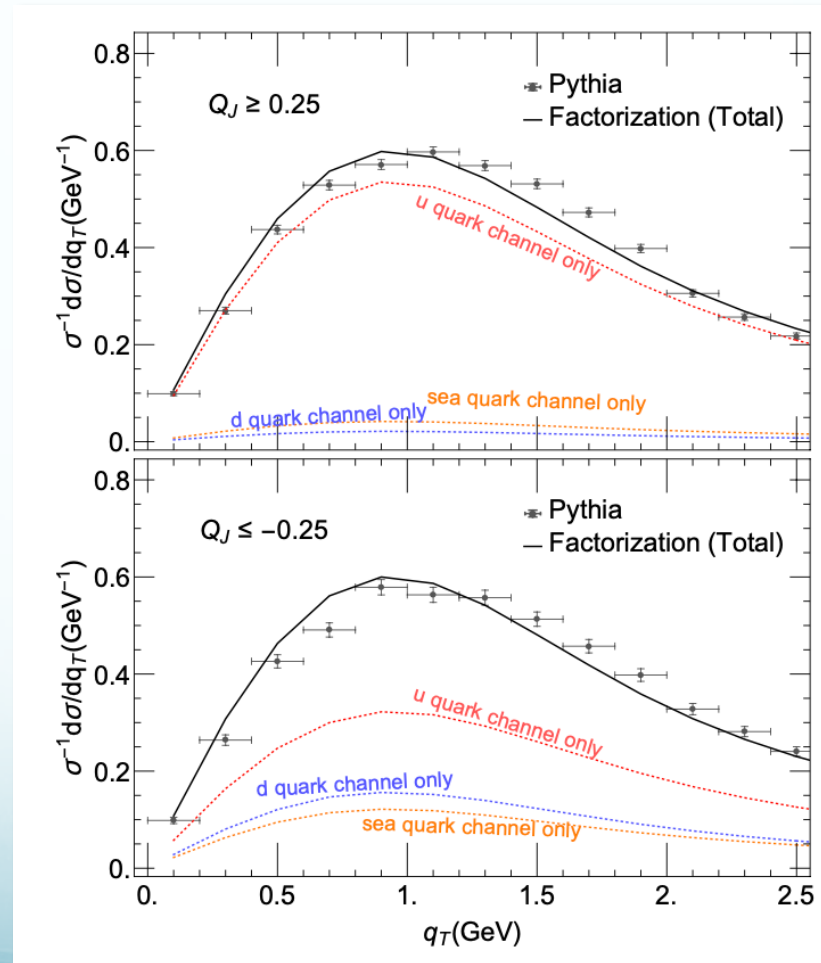


	u	\bar{u}	d	\bar{d}	s	\bar{s}
r_i^+	0.52	0.17	0.15	0.53	0.30	0.34
r_i^-	0.15	0.49	0.52	0.15	0.36	0.32
r_i^0	0.33	0.35	0.33	0.32	0.35	0.34

- Kappa $\sim 0.3 - 0.5$, the energy dependence of these ratios are extremely small ($\sim 5\%$)

Unpolarized: sensitivity

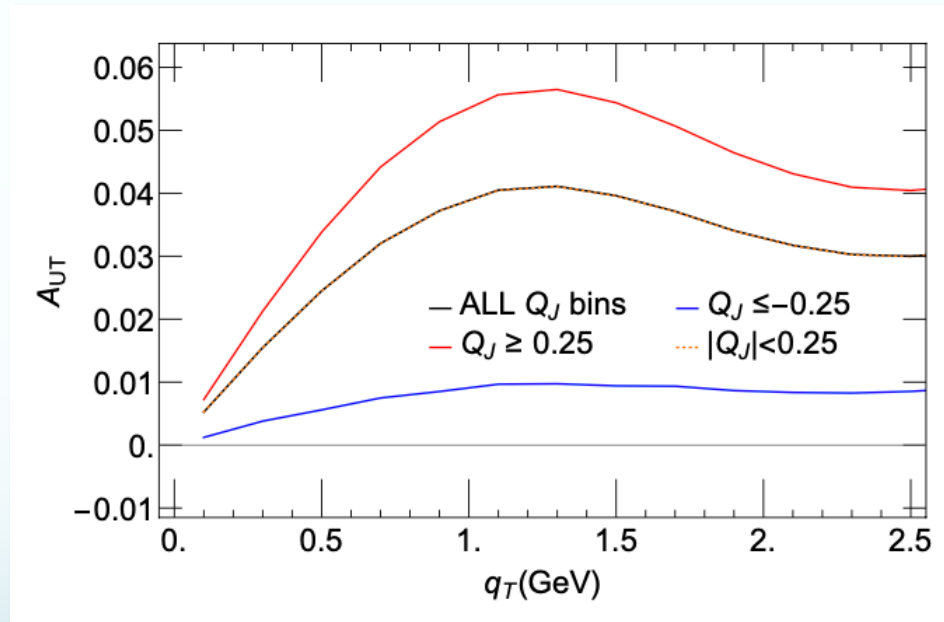
- In general, u quark is more dominant (charge enhancement e_u^2 vs e_d^2)
 - By selecting negative jet charge bin, one can enhance the d quark sensitivity a lot



Sivers asymmetry

- What will experimentalists measure?
 - Sivers asymmetry in different jet charge bins

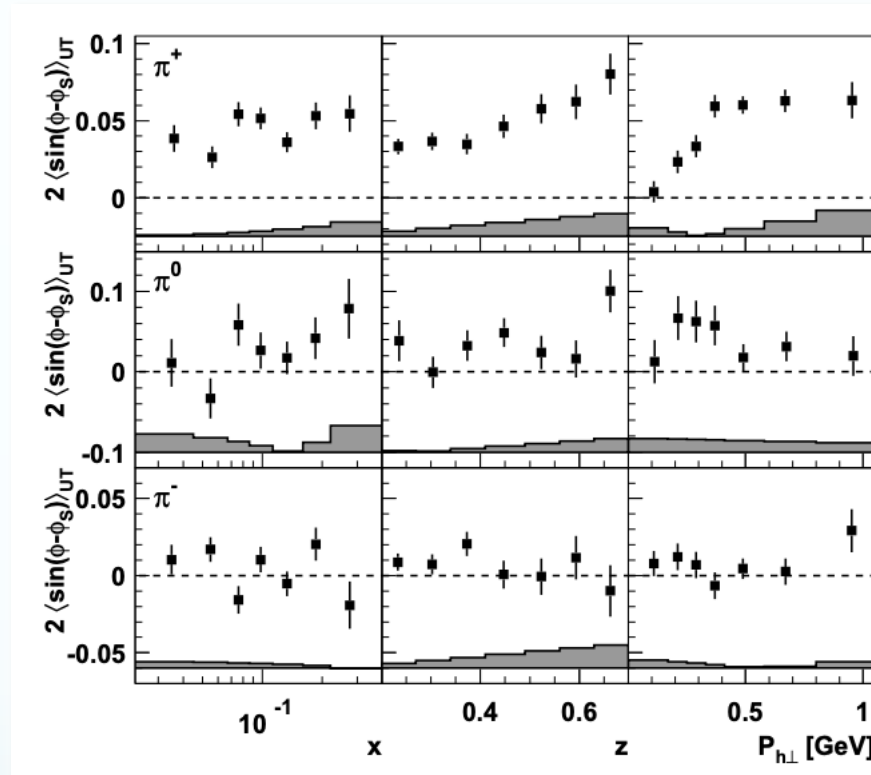
$$A_{UT}(Q_{\kappa,\text{bin}}^N) = \frac{d\sigma(S^\uparrow) - d\sigma(S^\downarrow)}{d\sigma(S^\uparrow) + d\sigma(S^\downarrow)} = \frac{d\sigma_{UT}(Q_{\kappa,\text{bin}}^N)}{d\sigma_{UU}(Q_{\kappa,\text{bin}}^N)}$$



Looks familiar?

- SIDIS Sivers asymmetry of π^+ , π^0 , π^-

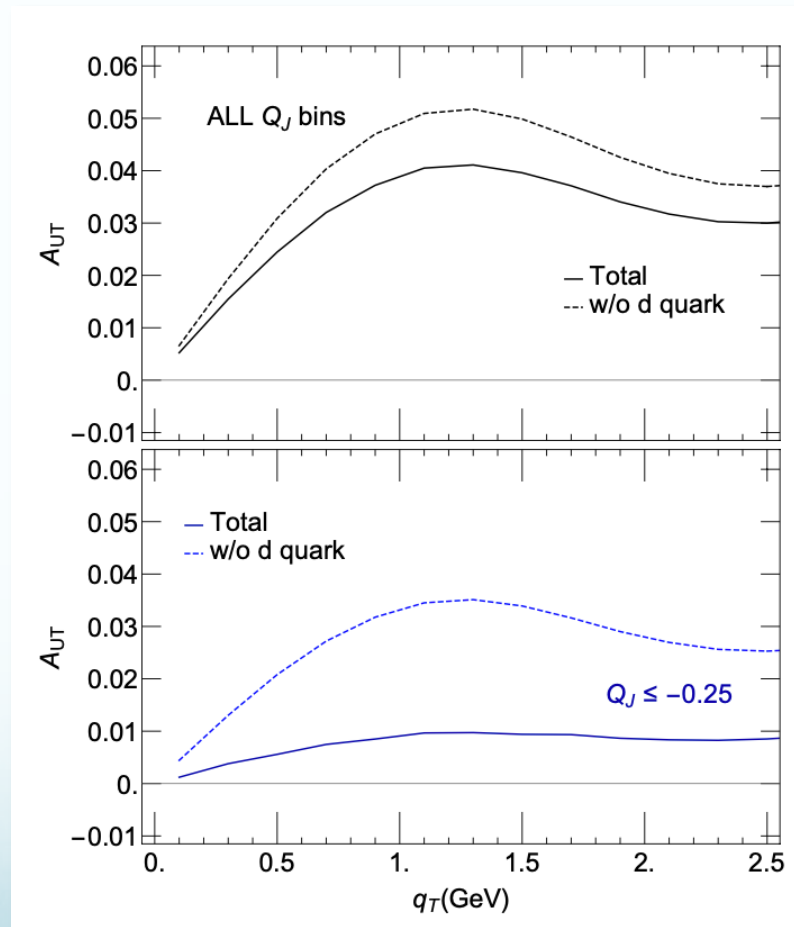
HERMES collaboration, arXiv:0906.3918



- **Fragmentation functions** in SIDIS are replaced by **jet charge weighting factors** in jet production
 - Functions \rightarrow numbers
 - Both universal: can be determined via global analysis

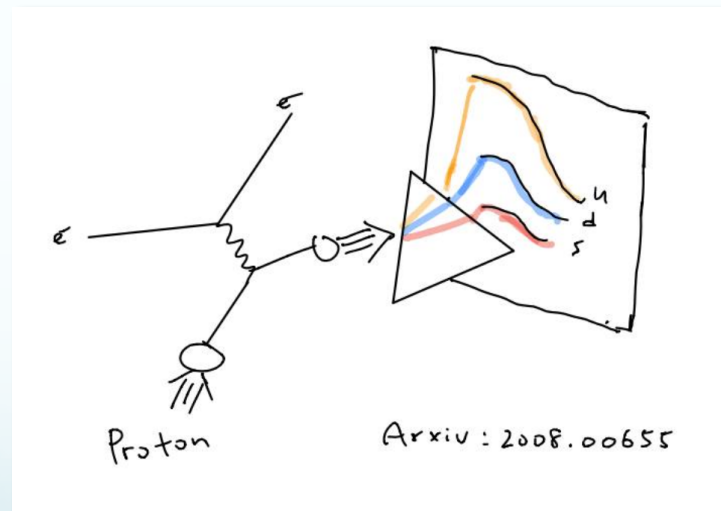
Polarized: sensitivity

- With jet charge bin selection, the sensitivity to d-quark Sivers is significantly enhanced



Summary

- For 3D imaging, jet observables have become quite promising and complementary to the standard SIDIS process
- We demonstrate jet charge can be used for flavor separation in spin asymmetries
 - We demonstrate the effectiveness using Sivers asymmetry, but apparently it should work also for collinear functions, e.g., helicity distributions



Thank you!