

The $B \rightarrow D^* \ell \nu$ semileptonic decay at non-zero recoil from lattice QCD

Alejandro Vaquero

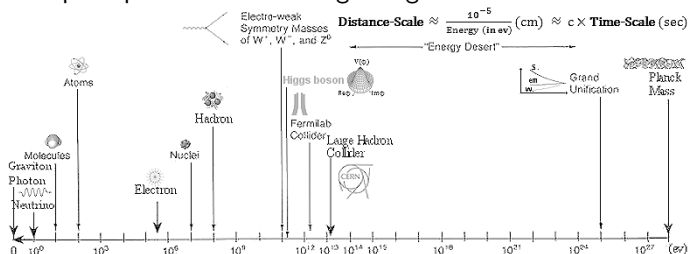
University of Utah

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Carleton DeTar, University of Utah
Aida El-Khadra, University of Illinois and FNAL
Andreas Kronfeld, FNAL
John Laiho, Syracuse University
Ruth Van de Water, FNAL

The Standard Model (SM)

- The Standard Model is (arguably) the most successful theory describing nature we have ever had
- The theory is not completely satisfactory
 - Situation similar to that at the end of the XIX century
- The SM can explain phenomena in a large range of scales

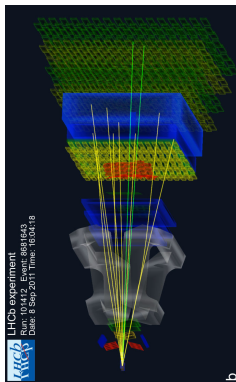


- Yet there is a region where we expect the SM to fail
- The SM is regarded as an effective theory at low energies (low means $E \lesssim v_{EW} \approx 0.1 - 1 \text{ TeV}$)

Where to look for new physics?



Energy frontier



Intensity frontier

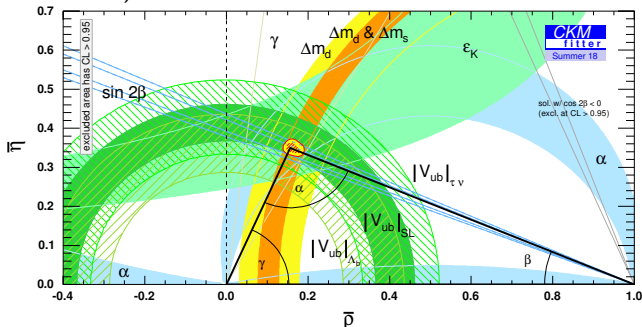


Cosmology frontier

The V_{cb} matrix element: Tensions

$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$	$ V_{cb} \cdot (10^{-3})$	PDG 2016	PDG 2018	PDG 2020
	Exclusive	39.2 ± 0.7	41.9 ± 2.0	39.5 ± 0.9
	Inclusive	42.2 ± 0.8	42.2 ± 0.8	42.2 ± 0.8

- Matrix must be unitary (preserve the norm)
- Current tensions (2020) stand at $\approx 3\sigma$**



The V_{cb} matrix element: Measurement from exclusive processes

$$\underbrace{\frac{d\Gamma}{dw} (\bar{B} \rightarrow D^* \ell \bar{\nu}_\ell)}_{\text{Experiment}} = \underbrace{\frac{G_F^2 m_B^5}{48\pi^2} (w^2 - 1)^{\frac{1}{2}} P(w) |\eta_{ew}|^2}_{\text{Known factors}} \underbrace{|\mathcal{F}(w)|^2}_{\text{Theory}} |V_{cb}|^2$$

- The amplitude \mathcal{F} must be calculated in the theory
 - Extremely difficult task, QCD is non-perturbative
- Can use effective theories (HQET) to say something about \mathcal{F}
 - Separate light (non-perturbative) and heavy degrees of freedom as $m_Q \rightarrow \infty$
 - $\lim_{m_Q \rightarrow \infty} \mathcal{F}(w) = \xi(w)$, which is the Isgur-Wise function
 - **We don't know what $\xi(w)$ looks like, but we know $\xi(1) = 1$**
 - At large (but finite) mass $\mathcal{F}(w)$ receives corrections $O\left(\alpha_s, \frac{\Lambda_{QCD}}{m_Q}\right)$
- Reduction in the phase space $(w^2 - 1)^{\frac{1}{2}}$ limits experimental results at $w \approx 1$
 - Need to extrapolate $|V_{cb}|^2 |\eta_{ew} \mathcal{F}(w)|^2$ to $w = 1$
 - This extrapolation is done using well established parametrizations

The V_{cb} matrix element: The parametrization issue

All the parametrizations perform an expansion in the z parameter

$$z = \frac{\sqrt{w+1} - \sqrt{2N}}{\sqrt{w+1} + \sqrt{2N}}$$

- Boyd-Grinstein-Lebed (BGL)

Phys. Rev. Lett. 74 (1995) 4603-4606

Phys.Rev. D56 (1997) 6895-6911

Nucl.Phys. B461 (1996) 493-511

$$f_X(w) = \frac{1}{B_{f_X}(z)\phi_{f_X}(z)} \sum_{n=0}^{\infty} a_n z^n$$

- B_{f_X} Blaschke factors, includes contributions from the poles
- ϕ_{f_X} is called *outer function* and must be computed for each form factor
- Weak unitarity constraints $\sum_n |a_n|^2 \leq 1$

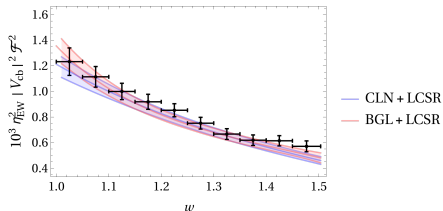
- Caprini-Lellouch-Neubert (CLN)

Nucl. Phys. B530 (1998) 153-181

$$\mathcal{F}(w) \propto 1 - \rho^2 z + cz^2 - dz^3, \quad \text{with } c = f_c(\rho), d = f_d(\rho)$$

- Relies strongly on HQET, spin symmetry and (old) inputs
- Tightly constrains $\mathcal{F}(w)$: four independent parameters, one relevant at $w = 1$

The V_{cb} matrix element: The parametrization issue



From *Phys. Lett. B*769 (2017) 441-445 using Belle data from arXiv:1702.01521 and the Fermilab/MILC'14 value at zero recoil

- CLN seems to underestimate the slope at low recoil
- The BGL value of $|V_{cb}|$ is compatible with the inclusive one

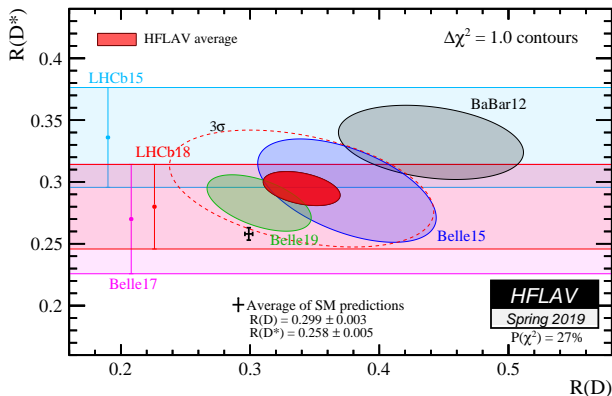
$$|V_{cb}| = 41.7 \pm 2.0 (\times 10^{-3})$$

- Latest Belle dataset and Babar analysis seem to contradict this picture
 - From Babar's paper arXiv:1903.10002 **BGL is compatible with CLN and far from the inclusive value**
 - Belle's paper arXiv:1809.03290v3 finds **similar results in its last revision**
- The discrepancy inclusive-exclusive is not well understood
- Data at $w \gtrsim 1$ is **urgently needed** to settle the issue
- Experimental measurements perform badly at low recoil

We would benefit enormously from a high precision lattice calculation at $w \gtrsim 1$

The V_{cb} matrix element: Tensions in lepton universality

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu_\ell)}$$



- Current $\approx 3\sigma$ tension with the SM

Calculating V_{cb} on the lattice: Formalism

- Form factors

$$\frac{\langle D^*(p_{D^*}, \epsilon^\nu) | \mathcal{V}^\mu | \bar{B}(p_B) \rangle}{2\sqrt{m_B m_{D^*}}} = \frac{1}{2} \epsilon^{\nu*} \epsilon^{\mu\nu}_{\rho\sigma} v_B^\rho v_{D^*}^\sigma \mathbf{h}_V(w)$$

$$\frac{\langle D^*(p_{D^*}, \epsilon^\nu) | \mathcal{A}^\mu | \bar{B}(p_B) \rangle}{2\sqrt{m_B m_{D^*}}} =$$

$$\frac{i}{2} \epsilon^{\nu*} [g^{\mu\nu} (1+w) \mathbf{h}_{A_1}(w) - v_B^\nu (v_B^\mu \mathbf{h}_{A_2}(w) + v_{D^*}^\mu \mathbf{h}_{A_3}(w))]$$

- \mathcal{V} and \mathcal{A} are the vector/axial currents in the continuum
- The h_X enter in the definition of \mathcal{F}
- We can calculate $h_{A_{1,2,3},V}$ directly from the lattice

Calculating V_{cb} on the lattice: Formalism

- Helicity amplitudes

$$H_{\pm} = \sqrt{m_B m_{D^*}}(w+1) \left(\mathbf{h}_{A_1}(w) \mp \sqrt{\frac{w-1}{w+1}} \mathbf{h}_V(w) \right)$$

$$H_0 = \sqrt{m_B m_{D^*}}(w+1)m_B [(w-r)\mathbf{h}_{A_1}(w) - (w-1)(r\mathbf{h}_{A_2}(w) + \mathbf{h}_{A_3}(w))] / \sqrt{q^2}$$

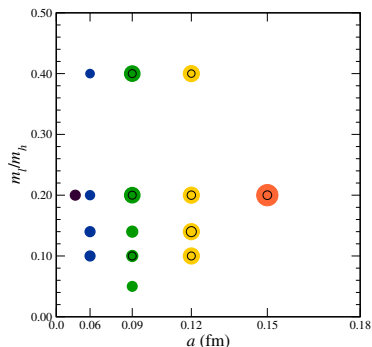
$$H_S = \sqrt{\frac{w^2-1}{r(1+r^2-2wr)}} [(1+w)\mathbf{h}_{A_1}(w) + (wr-1)\mathbf{h}_{A_2}(w) + (r-w)\mathbf{h}_{A_3}(w)]$$

- Form factor in terms of the helicity amplitudes

$$\chi(w) |\mathcal{F}|^2 = \frac{1-2wr+r^2}{12m_B m_{D^*} (1-r)^2} (H_0^2(w) + H_+^2(w) + H_-^2(w))$$

Introduction: Available data and simulations

- Using 15 $N_f = 2 + 1$ MILC ensembles of sea asqtad quarks
- The heavy quarks are treated using the Fermilab action



Analysis: Extracting the form factors

Calculated ratios

$$\frac{\langle D^*(p) | \mathbf{V} | D^*(0) \rangle}{\langle D^*(p) | V_4 | D^*(0) \rangle} \rightarrow x_f, \quad w = \frac{1 + x_f^2}{1 - x_f^2}$$

$$\frac{\langle D^*(p_\perp, \varepsilon_\parallel) | \mathbf{A} | \bar{B}(0) \rangle \langle \bar{B}(0) | \mathbf{A} | D^*(p_\perp, \varepsilon_\parallel) \rangle^*}{\langle D^*(0) | V_4 | D^*(0) \rangle \langle \bar{B}(0) | V_4 | \bar{B}(0) \rangle} \rightarrow R_{A_1}^2, \quad h_{A_1} = (1 - x_f^2) R_{A_1}$$

$$\frac{\langle D^*(p_\perp, \varepsilon_\perp) | \mathbf{V} | \bar{B}(0) \rangle}{\langle D^*(p_\perp, \varepsilon_\parallel) | \mathbf{A} | \bar{B}(0) \rangle} \rightarrow X_V, \quad h_V = \frac{2}{\sqrt{w^2 - 1}} R_{A_1} X_V$$

$$\frac{\langle D^*(p_\parallel, \varepsilon_\parallel) | \mathbf{A} | \bar{B}(0) \rangle}{\langle D^*(p_\perp, \varepsilon_\parallel) | \mathbf{A} | \bar{B}(0) \rangle} \rightarrow R_1, \quad h_{A_3} = \frac{2}{w^2 - 1} R_{A_1} (w - R_1)$$

$$\frac{\langle D^*(p_\perp, \varepsilon_\parallel) | A_4 | \bar{B}(0) \rangle}{\langle D^*(p_\perp, \varepsilon_\parallel) | \mathbf{A} | \bar{B}(0) \rangle} \rightarrow R_0,$$

$$h_{A_2} = \frac{2}{w^2 - 1} R_{A_1} (w R_1 - \sqrt{w^2 - 1} R_0 - 1)$$

* Phys.Rev. D66, 01503 (2002)

Analysis: Workflow

- Fit meson two-point functions to extract E , M and Z
 - Several smearings to fit properly the ground and excited states
 - For the D^* meson, fit a batch of **unpolarized** correlators to calculate the dispersion relation. Use the result to extract priors for the **polarized** fits
 - Two polarized momenta per ensemble $p = (1, 0, 0)$ and $p = (2, 0, 0)$ in lattice units
 - Explicitly fit wrong parity states
- Fit ratios of three-point functions to extract the form factors
 - Use the result of the two-point function fits to remove the prefactors and set priors
 - Smooth out the wrong parity states
- Renormalize the ratios with the matching factors
- Correct for HQ mistuning
- Perform the chiral-continuum extrapolation

Analysis: Systematics in the two-point function fits

- Try $2 + 2$ and $3 + 3$ fits (non-oscillating and oscillating states)
 - Look for agreement in the non-oscillating ground state and ground overlap factors
- Set the **same** t_{Min} **in physical units** for all the ensembles and all the momenta
- Set t_{Max} so the last point of the correlator has an error $\approx 20\% - 30\%$
- Look for a flat distribution of p -values across ensembles and momenta

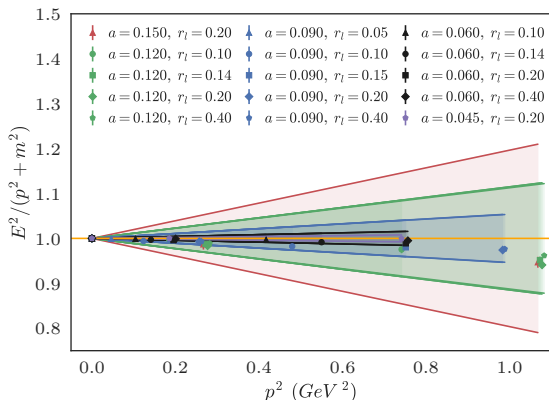
When all conditions all fulfilled, systematic errors coming from the fit procedure should be negligible

Analysis: Systematics in the two-point function fits

- Heavy quark discretization effects break the dispersion relation
- The Fermilab action uses tree-level matching, discretization errors $O(\alpha m)$

$$a^2 E^2(p_\mu) = (am_1)^2 + \frac{m_1}{m_2} (\mathbf{p}a)^2 + \frac{1}{4} \left[\frac{1}{(am_2)^2} - \frac{am_1}{(am_4)^3} \right] (a^2 \mathbf{p}^2)^2 - \frac{am_1 w_4}{3} \sum_{i=1}^3 (ap_i)^4 + O(p_i^6)$$

- Deviations from the continuum expression measure the size of the discretization errors
- As long as the discretization errors are within expected bounds, this is all right



Analysis: Systematics in the three-point function fits

- Use two-point fit results input to remove prefactors and set priors
 - Energy priors are widened to account for different fit ranges
- Set the **same fit ranges in physical units** for all the ensembles and all the momenta
 - Normally on our ratios the D^* meson lives at the source and the B at the sink
 - The double ratio is an exception due to its inherent symmetry, assume D^* at both ends
- Look for a flat distribution of p -values across ensembles and momenta
- The oscillating states are heavily suppressed in our ratios
 - Only the doubly oscillating state is expected to survive
 - This state induces an overall shift in the ratio with sign $(-1)^T$
 - Smooth the doubly oscillating state out

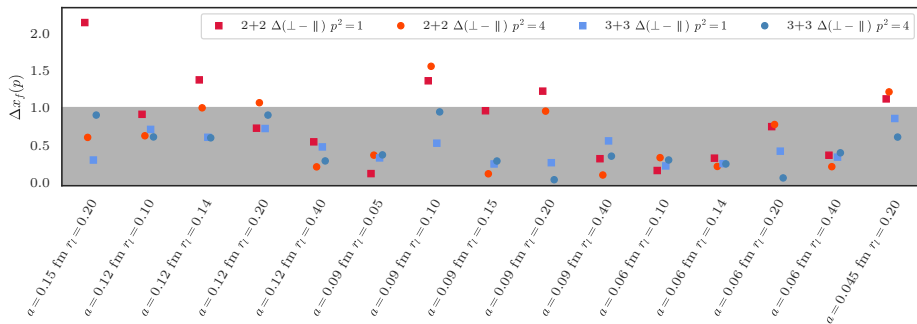
$$\bar{R}(t, T) = \frac{P(t, T)}{2} R(t, T) + \frac{P(t, T + 1)}{4} R(t, T + 1) \\ + \frac{P(t + 1, T + 1)}{4} R(t + 1, T + 1)$$

Analysis: Systematics in the three-point function fits

- Differences in x_f computed using different polarizations inform us about the systematics of the excited states

- The extra excited states are necessary to handle those systematics

$$R(t, T) = R_0 \left(1 + A_0 e^{-E_0 t} + A_1 e^{-E_1 t} + B_0 e^{-M_0(T-t)} + B_1 e^{-M_1(T-t)} + C_0 e^{-(E_0 - M_0)t} \right)$$



Measuring V_{cb} on the lattice: Current renormalization

- In the coefficients of the terms of our effective theory a dependence arises with the scale (i.e. a)
- The renormalization tries to account for the right dependence
- The scheme we employ is called *Mostly non-perturbative renormalization* of results

$$Z_{V^{1,4}, A^{1,4}} = \underbrace{\rho_{V^{1,4}, A^{1,4}}}_{\text{Perturbative factor}} \times \underbrace{\sqrt{Z_{V_{bb}} Z_{V_{cc}}}}_{\text{Non-perturbative piece}}$$

- The (relatively large) non-perturbative piece cancels in our ratios
- The (close to one) perturbative piece (matching factor ρ) is calculated at one-loop level for $w = 1$ and $m_c = 0$
- The errors for $w \neq 1$ and $m_c \neq 0$ are estimated and added to the factor

This analysis is **blinded** and the blinding happens at the level of the matching factors

Analysis: The recoil parameter w

- The recoil parameter is measured dynamically
- In the lab frame (B meson at rest)

$$w^2 = 1 + v_{D^*}^2$$

- Ratio of three point functions

$$X_f(p) = \frac{\langle D^*(p) | \mathbf{V} | D^*(0) \rangle}{\langle D^*(p) | V_4 | D^*(0) \rangle} = \frac{\mathbf{v}_{D^*}}{w + 1}$$

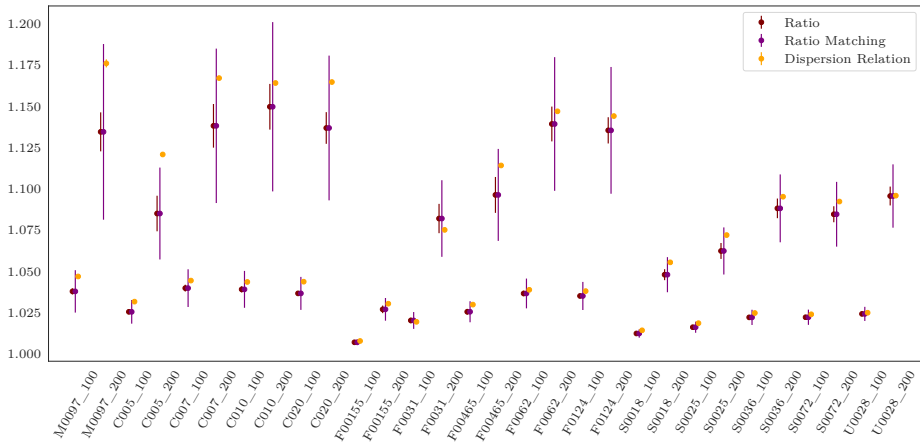
- From here

$$w(p) = \frac{1 + \mathbf{x}_f^2}{1 - \mathbf{x}_f^2}$$

- Alternatively one can use the dispersion relation

Analysis: The recoil parameter

- The recoil parameter suffers heavily from matching errors



Measuring V_{cb} on the lattice: Heavy quark mistuning corrections

- The simulations are run at approximate physical values of m_c, m_b
- After the runs the differences between the calculated and the physical masses is corrected non-perturbatively
 - The Fermilab action uses the kinetic mass m_2 to compute these corrections
 - $m_1 \rightarrow m_2$ as $a \rightarrow 0$

Correction process

- 1 For a particular ensemble correlators are computed at different m_c, m_b
- 2 All the ratios are calculated for the new values of the heavy quark masses, and the form factors are extracted
- 3 The derivative of combinations of the form factors with respect to the heavy quark masses is fitted to a suitable function
- 4 All the form factors are corrected using these results

Shifts are small in most cases, but add a small correlation among all data points

Analysis: Chiral-continuum fits

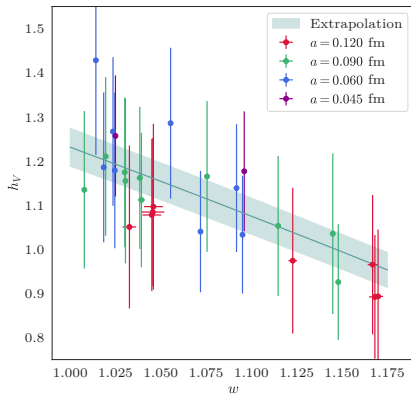
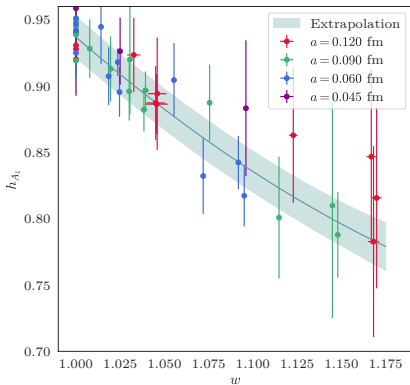
- Our data represents the form factors at non-zero a and unphysical m_π
- Extrapolation to the physical pion mass described by EFTs
 - The EFT describe the a and the m_π dependence
- Functional form explicitly known

$$h_{A_1}(w) = \underbrace{\left[1 + \frac{X_{A_1}(\Lambda_\chi)}{m_c^2} + \frac{g_{D^*D\pi}^2}{48\pi^2 f_\pi^2 r_1^2} \text{logs}_{\text{SU3}}(a, m_l, m_s, \Lambda_{\text{QCD}}) \right]}_{\text{NLO } \chi\text{PT} + \text{HQET}} \times$$
$$\underbrace{\left[\underbrace{\rho^2(w-1) + k(w-1)^2}_{w \text{ dependence}} + \underbrace{c_1 x_l + c_2 x_l^2 + c_{a1} x_{a^2} + c_{a2} x_{a^2}^2 + c_{a,m} x_l x_{a^2}}_{\text{NNLO } \chi\text{PT}} \right]}_{\text{NNLO } \chi\text{PT}} \times$$
$$\underbrace{\left(1 + \beta_{11}^{A_1} \alpha_s a + \beta_{02}^{A_1} a^2 + \beta_{03}^{A_1} a^3 \right)}_{\text{HQ discretization errors}}$$

with

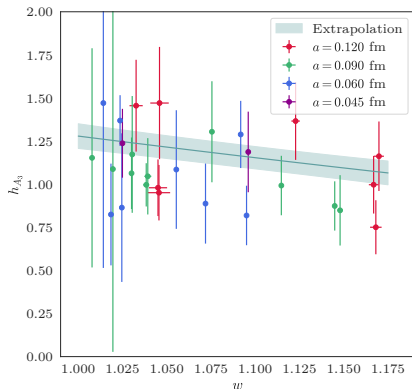
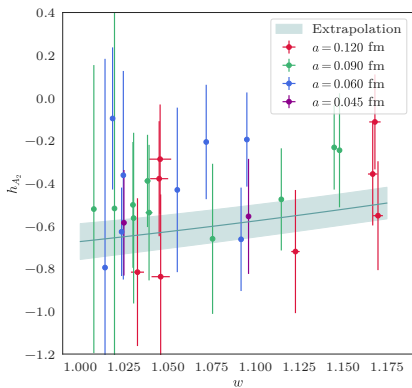
$$x_l = B_0 \frac{m_l}{(2\pi f_\pi)^2}, \quad x_{a^2} = \left(\frac{a}{4\pi f_\pi r_1^2} \right)^2$$

Results: Chiral-continuum fits



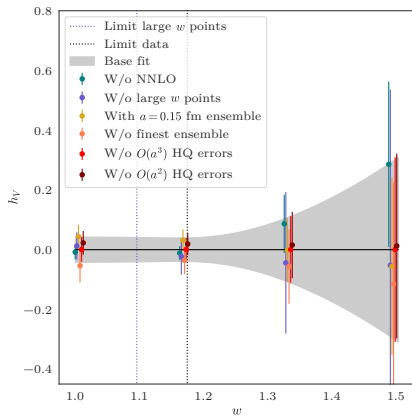
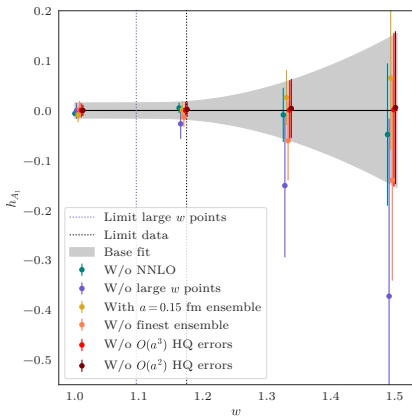
- Preliminary **blinded** results. **Left:** h_{A_1} **Right:** h_V

Results: Chiral-continuum fits



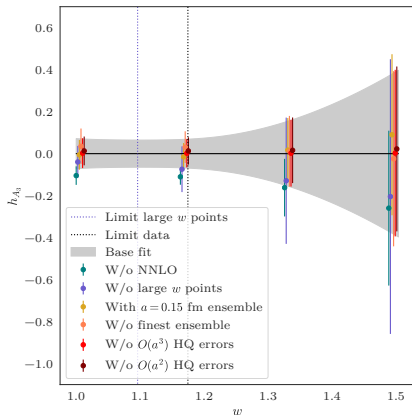
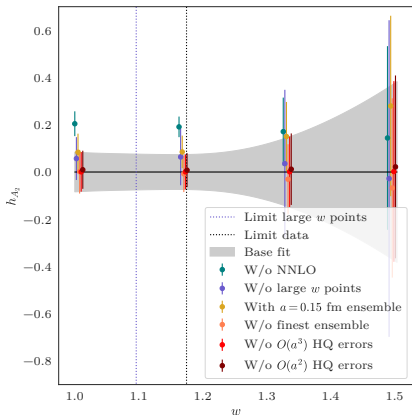
- Preliminary **blinded** results. **Left:** h_{A_2} **Right:** h_{A_3}

Results: Stability of chiral-continuum fits



χ^2/dof	Base 85.2/102	W/o NNLO 132.8/114	W/o large w 62.1/77	W $a = 0.15$ fm 102.8/110
χ^2/dof		W/o $a = 0.045$ fm 76.9/93	W/o HQ $O(a^3)$ 85.2/103	W/o HQ $O(a^2)$ 85.6/106

Results: Stability of chiral-continuum fits



	Base	W/o NNLO	W/o large w	W $a = 0.15$ fm
χ^2/dof	85.2/102	132.8/114	62.1/77	102.8/110
χ^2/dof		W/o $a = 0.045$ fm	W/o HQ $O(a^3)$	W/o HQ $O(a^2)$
		76.9/93	85.2/103	85.6/106

Analysis: Systematic errors

- Error contributions considered:
 - Correlator fits and excited states
 - Use the same fit ranges for all the correlators
 - Make sure the fits are stable under small variations
 - Add extra excited states
 - We assume no extra errors**
 - Lattice scale dependence
 - Redo the chiral-continuum extrapolation with $r_1 \pm \sigma$ and compare
 - The difference is negligible**
 - Heavy quark mistuning
 - The errors are already taken into account in the chiral-continuum extrapolation
 - Try the chiral-continuum extrapolation with and without mistuning corrections to estimate their size
 - Light quark mistuning
 - Try the chiral-continuum extrapolation with $m_{ud} \pm \sigma$ and compare
 - The difference is negligible**
 - Chiral extrapolation and light quark discretization errors
 - The errors are already taken into account in the chiral-continuum extrapolation
 - Try the chiral-continuum extrapolation with and without the NNLO and NNNLO terms to estimate their size

Analysis: Systematic errors

- Error contributions considered:
 - Matching
 - The errors are already taken into account in the chiral-continuum extrapolation
 - Try the chiral-continuum extrapolation with and without the matching errors to estimate their size
 - Heavy quark discretization errors
 - These errors are already taken into account in the chiral-continuum extrapolation via generic terms
 - We employ generic discretization terms $\beta_X \alpha_s^p a^q$, instead of the universal functions
 - Try the chiral-continuum extrapolation with and without the HQ terms to estimate the size of the correction
 - Isospin effects
 - Try the chiral-continuum extrapolation with $m_{ud} = m_{u,d}$ and compare
 - The difference is added as an extra error to the final result
 - Finite volume errors
 - Following Arndt and Lin we estimate the size of the finite volume errors

Phys. Rev. D70, 014503 (2004)

The errors are negligible

Analysis: Preliminary error budget

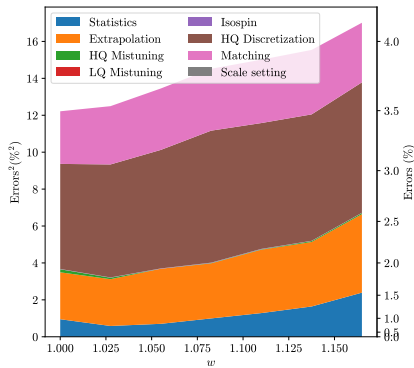
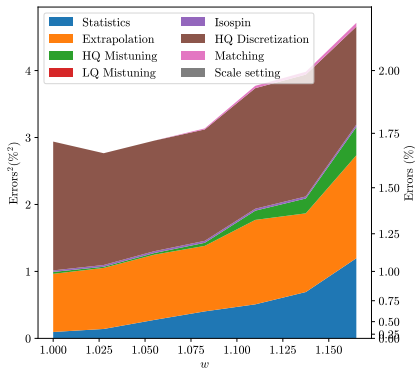
Source	h_V (%)	h_{A_1} (%)	h_{A_2} (%)	h_{A_3} (%)
Statistics + Matching + χ PT + HQ	3.8	1.9	13.2	5.7
(Statistics)	(1.1)	(0.7)	(6.0)	(2.8)
(χPT/cont. extrapolation)	(1.8)	(1.1)	(8.0)	(3.9)
(Matching)	(1.8)	(0.2)	(4.3)	(0.9)
(HQ discretization) *	(2.6)	(1.3)	(7.2)	(2.8)
(HQ mistuning correction)	(0.1)	(0.3)	(1.4)	(0.7)
Isospin effects	0.1	0.2	0.1	0.1
Total error	3.8	1.9	13.2	5.7

Errors at $w = 1.10$

*Preliminary estimate, analysis in progress

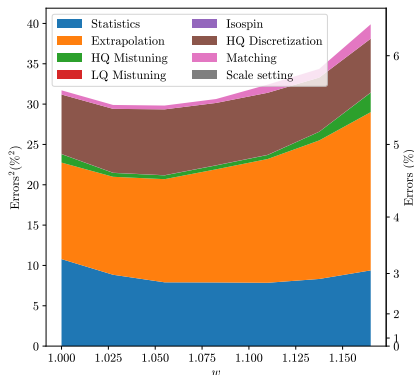
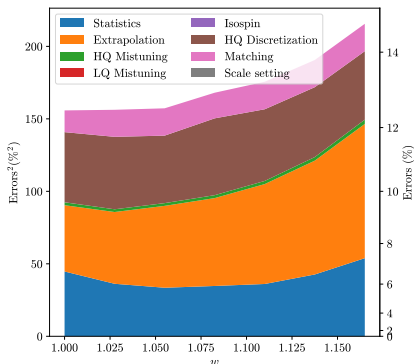
- The inclusion of the discretization errors in the chiral-continuum extrapolation puts in evidence that **the discretization errors are one of the most important contribution to the final error**
- Our discretization errors **are not final** and must be crosschecked carefully
- **Bold** marks errors to be reduced/removed when using HISQ for light quarks
- *Italic* marks errors to be reduced/removed when using HISQ for heavy quarks

Analysis: Preliminary error budget



• Left: h_{A_1} , right: h_V

Analysis: Preliminary error budget



• Left: h_{A_2} , right: h_{A_3}

Analysis: z-Expansion

- The BGL expansion is performed on different (more convenient) form factors

Phys.Lett. **B769**, 441 (2017), Phys.Lett. **B771**, 359 (2017)

$$g = \frac{h_V(w)}{\sqrt{m_B m_{D^*}}} = \frac{1}{\phi_g(z) B_g(z)} \sum_j a_j z^j$$

$$f = \sqrt{m_B m_{D^*}} (1+w) h_{A_1}(w) = \frac{1}{\phi_f(z) B_f(z)} \sum_j b_j z^j$$

$$\mathcal{F}_1 = \sqrt{q^2} H_0 = \frac{1}{\phi_{\mathcal{F}_1}(z) B_{\mathcal{F}_1}(z)} \sum_j c_j z^j$$

$$\mathcal{F}_2 = \frac{\sqrt{q^2}}{m_{D^*} \sqrt{w^2 - 1}} H_S = \frac{1}{\phi_{\mathcal{F}_2}(z) B_{\mathcal{F}_2}(z)} \sum_j d_j z^j$$

- Constraint $\mathcal{F}_1(z=0) = (m_B - m_{D^*}) f(z=0)$
- Constraint $(1+w) m_B^2 (1-r) \mathcal{F}_1(z=z_{\text{Max}}) = (1+r) \mathcal{F}_2(z=z_{\text{Max}})$
- BGL (weak) unitarity constraints

$$\sum_j a_j^2 \leq 1, \quad \sum_j b_j^2 + c_j^2 \leq 1, \quad \sum_j d_j^2 \leq 1$$

Analysis: z expansion fit procedure

- Several different datasets
 - Our lattice data
 - BaBar BGL fit arXiv:1903.10002
 - Belle untagged dataset arXiv:1809.03290
- Several different fits
 - Lattice form factors only
 - Experimental data only (one fit per dataset)
 - Joint fit lattice + experimental data
- Each dataset is given in a different format, and requires a different amount of processing
- Different fitting strategy per dataset

All the experimental and theoretical **correlations are included** in all fits

Constraints

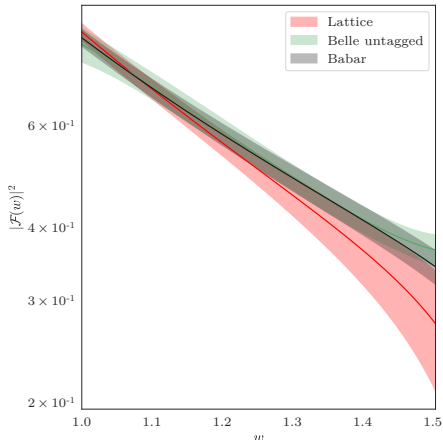
- The constraint at zero recoil is used to remove a coefficient of the BGL expansion
- The constraint at maximum recoil is **not** imposed, but checked for compliance
- The unitarity constraints are **not** imposed, but checked for compliance

How many coefficients in the expansion?

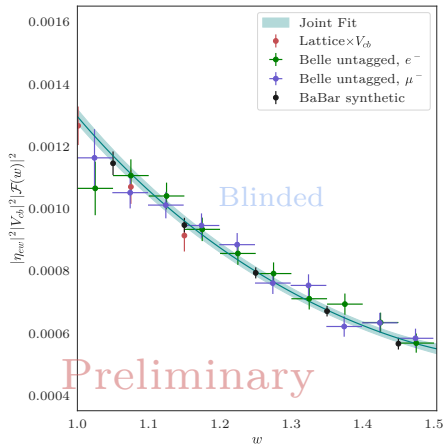
- Add coefficients until
 - We exhaust the degrees of freedom
 - The error is saturated
- In this analysis
 - The lattice only fit uses 3 coefficients per form factor
 - The joint fit uses 4 coefficients for \mathcal{F}_1 and 3 for the other form factors

Results: Pure-lattice prediction and joint fit

Separate fits

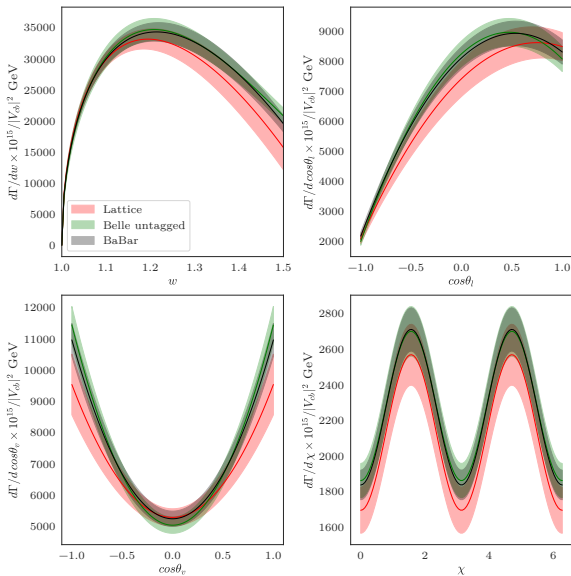


Joint fit

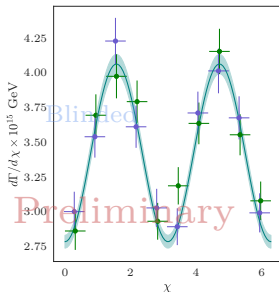
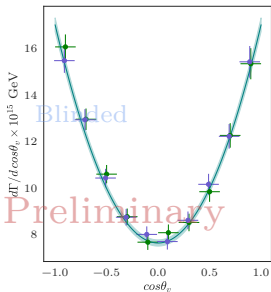
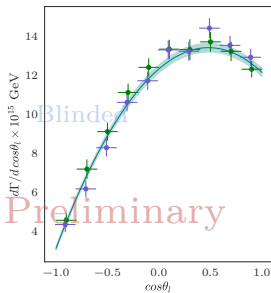
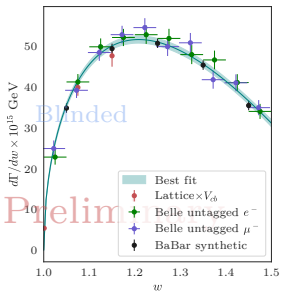


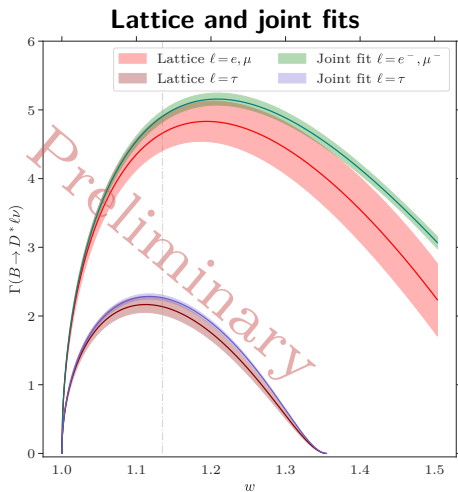
Fit	Lattice	Exp	Lat + Belle	Lat + BaBar	Lat + Exp
p -Value	0.22	0.09	0.07	0.55	0.03

Results: Separate fits, angular bins

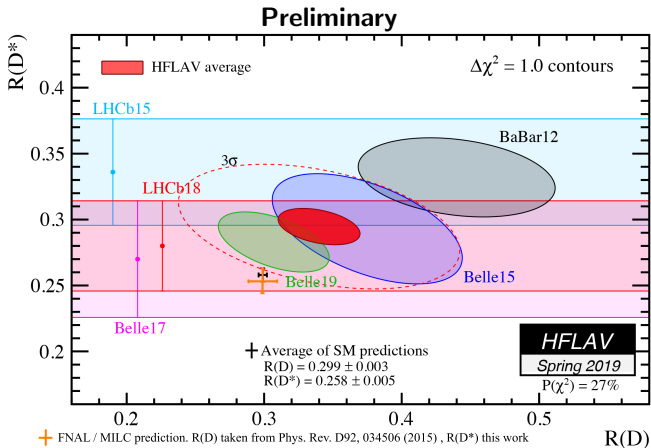


Results: Joint fit, angular bins





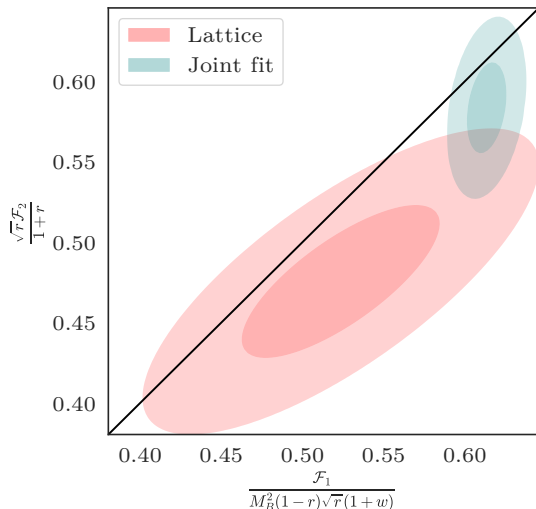
Results: $R(D^*)$



Results: Verification of the constraints

$$A_5(w_{\text{Max}}) = P_1(w_{\text{Max}})$$

$$w = 1.50$$



What to expect

- The preliminary error on V_{cb} from this analysis is of similar size than the error obtained from the $B \rightarrow D\ell\nu$ analysis at non-zero recoil
- The **main new information of this analysis** comes from the behavior at small recoil of the form factors
- Main sources of errors of our form factors are
 - χ PT-continuum extrapolation
 - HQ discretization
 - Matching
- We have a short-term plan to reduce the χ PT-continuum extrapolation errors
- Preliminary results show $R(D^*)$ very close to the **theoretical prediction**
- **Must unblind** to see the impact in the V_{cb} inclusive vs exclusive problem
 - If the blinding factor is small, the tension will persist

Please, do not use our preliminary results in any calculation

Thank you for your attention