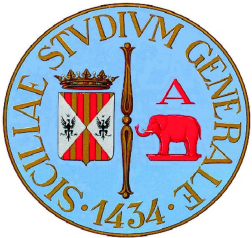


# Open Heavy production & final state interaction(AA,pA)

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Vincenzo Greco - University of Catania/INFN-LNS



An overview of the transport dynamics  
and hadronization in AA (pA,pp)

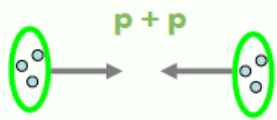
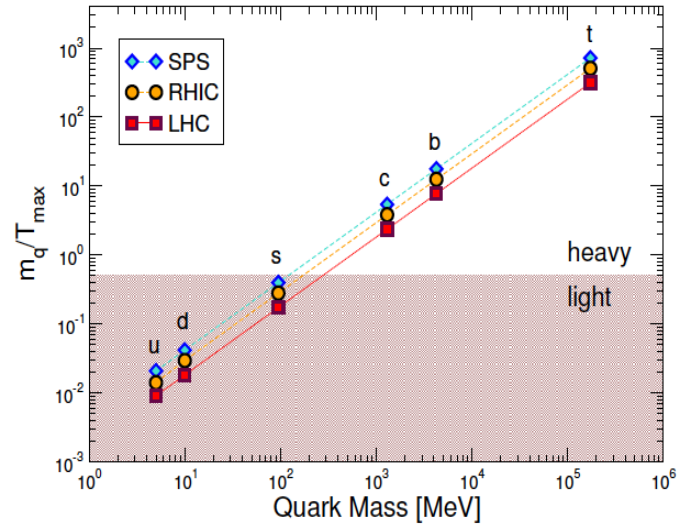
# Basic Scales

## Why Heavy in AA:

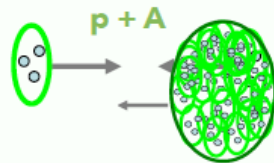
- $m_{c,b} \gg \Lambda_{\text{QCD}}$  pQCD-NNLO initial production
- $m_{c,b} \gg T_{\text{RHIC,LHC}}$  negligible thermal production (not @FCC)

## Specific Features:

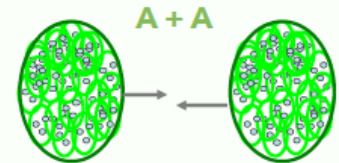
- $\tau_0 < 0.08 \text{ fm}/c \ll \tau_{\text{QGP}}$  witness of all the QGP evolution
- $\tau_{\text{th}} \approx \tau_{\text{QGP}} \gg \tau_{q,g}$  carry more information of their evolution
- $m_{c,b} \gg gT_{\text{RHIC,LHC}}$  soft scatterings  $\rightarrow$  Brownian motion (low p charm)
- Link to IQCD  $F(r,T)$  & space diffusion + NRQCD



Have a baseline/reference system where production is understood



Nuclear/cold effects are under control



Understand the interactions/hadronization in medium



# Link to lattice QCD

## ❖ Extract the Free Energy of QQ

→ HQ Potential  $F=U-TS$

$$q_0^2 \approx \vec{q}^4 / m_Q^2 \ll \vec{q}^2$$

space-like transf. mom. →  $V(r)$

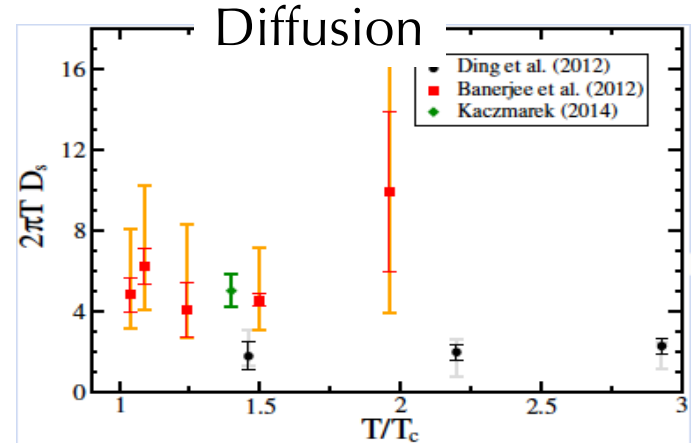
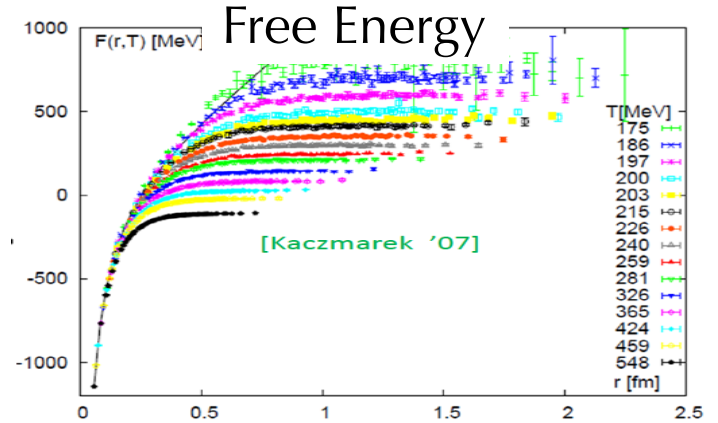
## ❖ Evaluate Diffusion Transp. Coeff.

Extract Spectral function  $\rho_E$  from color-electric correlator with an initial assumption for  $\rho_E$ , then Kubo formula:

$$\kappa/T^3 = \lim_{\omega \rightarrow 0} \frac{2T \rho_E(\omega)}{\omega} \quad D = \frac{2T^2}{\kappa}$$

Approximations/limitations:

*quenched QCD, heavy quark vs. charm quark, continuum extrapolation, ...*



# Outline

---

## ✧ Heavy Flavor dynamical evolution in Hot QCD Matter (AA collisions):

- Collisional Energy loss  $\rightarrow D_s(T)$  transport coefficient [ $p_T < 5$  GeV] [non-perturbative]
- Radiative energy loss and jets [ $p_T > 10$  GeV] [pQCD]
- Parton Energy loss + FF in-medium cold matter: baseline for EIC

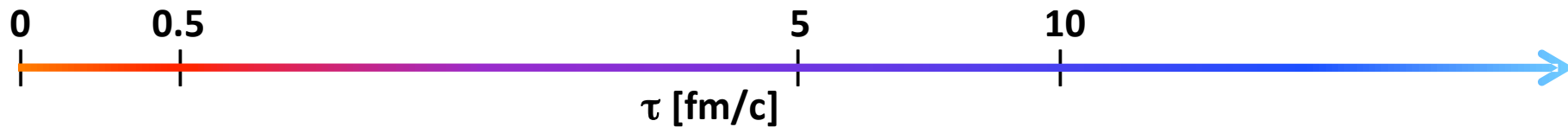
## ✧ Heavy Flavor hadronization:

- $\Lambda_c/D \approx O(1)$  against FF prediction, PYTHIA and  $e^+e^-$ , ep & pp@LHC at forward rapidity
- In-medium hadronization already in pp, pA: **coalescence + fragmentation**, Color Recon
- under current activity@RHIC & LHC (breaking universality of FFs)

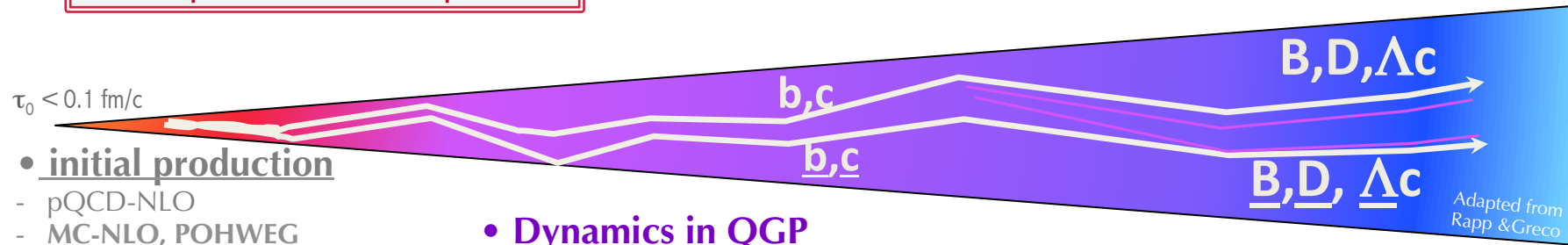
## ✧ Heavy Flavor as a probe of initial stage:

- impact of Glasma dynamics in pA and AA

# Studying the HF in uRHIC



❖ Impact of Glasma phase?!



## • initial production

- pQCD-NLO
- MC-NLO, POWHEG
- CNM effect [pA]

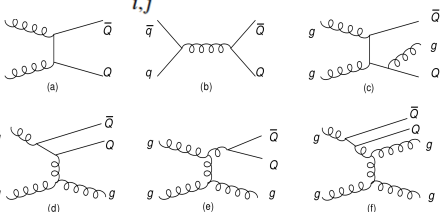
## • Dynamics in QGP

- Thermalization
- Transp. Coeff. of QCD matter  $D_s(T)$
- Radiation & Jet Quenching

## • Hadronization

- coalescence and/or fragm.
- $\Delta c/D$  in pp,pA,AA

$$d\sigma^{Q+X} \simeq \sum_{i,j} f_i^A \otimes f_j^B \otimes d\sigma_{ij \rightarrow Q+X}$$

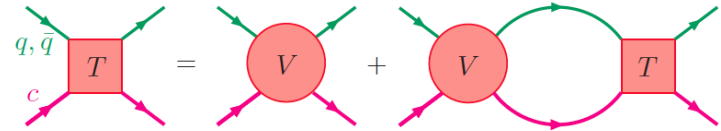
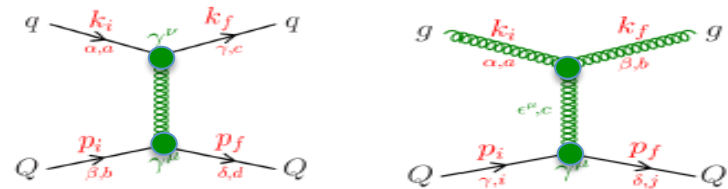


Angular correlations

# How HQ interact with the medium

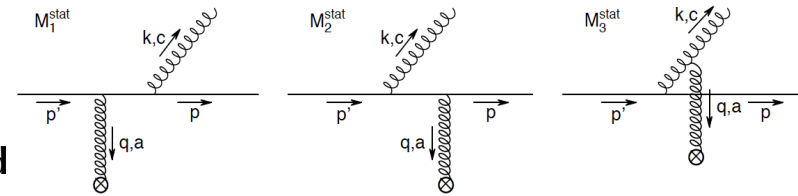
## ❖ Elastic Collisional Energy Loss

- **pQCD inspired+HTL** (*Torino, Nantes,LBL...*)  
LO diagrams, soft scale resummed in HTL  
infrared singularity,  $gT \ll g^2$  ?
- **QuasiParticleModel** (*Catania, Frankfurt-PHSD*)  
LO diagram,  $\alpha_s(T)$  from a fit to IQCD-EoS  
main feature increased strength as  $T \rightarrow T_c$
- **T-matrix** under  $V(r,T)$  deduced from IQCD (*TAMU*)



## ❖ Radiative Energy Loss

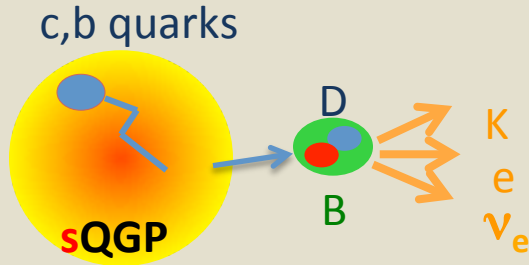
- **pQCD** ( $p_T > 10$  GeV) (*AMY, DGLV, WHDG, HT, SCET ...*)  
collisional & radiative **both light & heavy, but  $v_2$  often missed**



Agreement that:

- $p \approx m_Q$  is dominated by Collisional  $E_{\text{loss}}$
- $p \gg m_Q$  radiative dominated
- what is the crossing is model dependent and exp. data are not able to clarify it even if favors dominance of collisional up to  $p_T \approx 6-8$  GeV for charm

# Standard Dynamics of Heavy Quarks in the QGP



Brownian Motion

Fokker-Planck approach ( $T \ll m_Q$ )  
in Hydro/transport bulk

$$\frac{\partial f_{c,b}}{\partial t} = \gamma \frac{\partial (p f_{c,b})}{\partial p} + D \frac{\partial^2 f_{c,b}}{\partial p^2}$$

$$\langle p \rangle = p_0 e^{-\gamma t}$$

$$\langle \Delta p^2 \rangle = 3D_p / \gamma (1 - e^{-2\gamma t})$$

$$D_p = ET\gamma - \text{Fluct. Diss. Th.}$$

$$D_s = \frac{T}{M\gamma} = \frac{T^2}{D_p} = \frac{T}{M} \tau_{th}$$

A measure of thermalization time

$$\gamma = \int d^3k |M(k, p)|^2 p$$

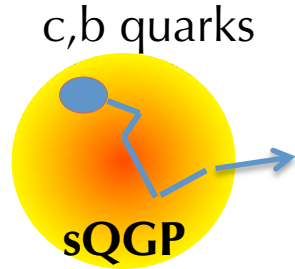
$$D = \frac{1}{2} \int d^3k |M(k, p)|^2 p^2$$

$|M|^2$  scatt. matrix from some theory:  
HTL, pQCD coll., rad., T-matrix  
-  $D_s$  from latticeQCD

- ✧ This is the main set up at east at  $p < 10$  GeV
- ✧ Brownian challenged for charm: Boltzmann dynamics
- ✧ At  $p_T > 10$  GeV radiative Eloss , qhat, ....



# HQ diffusion in the expanding QGP



## Two main approaches:

**1) Langevin approach** ( $T \ll m_q$  soft scattering)

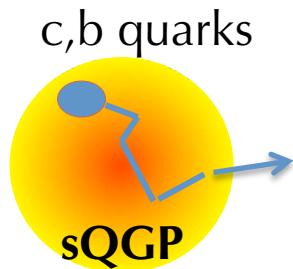
[*TAMU, Duke, Nantes, Torino, Catania, ...*]

**2) Boltzman kinetic transport** (...Kadanoff-Baym-PHSD)

[*Catania, Nantes, Frankfurt, LBL, CCNU, ...*]

background Hydro/transport expanding bulk

# HQ diffusion in the expanding QGP



## Two main approaches:

1) **Langevin approach** ( $T \ll m_q$  soft scattering)

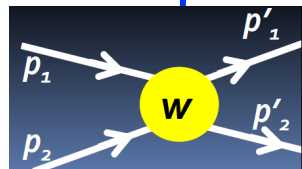
[TAMU, Duke, Nantes, Torino, Catania, ...]

2) **Boltzman kinetic transport** (...Kadanoff-Baym-PHSD)

[Catania, Nantes, Frankfurt, Berkeley LBL, CCNU, ...]

## Boltzmann (BM)

$$\frac{Df_Q(p)}{Dt} = C_{22} = \frac{1}{2E_p} \int \frac{d^3q}{(2\pi)^3 2E_q} \int \frac{d^3p'}{(2\pi)^3 2E_{p'}} \frac{d^3q'}{(2\pi)^3 2E_{q'}} \left[ f'_g(q') f'_Q(p') |M_{gQ \rightarrow gQ}(p'q' \rightarrow pq)|^2 - f_g(q) f_Q(p) |M_{gQ \rightarrow gQ}(pq \rightarrow p'q')|^2 \right] (2\pi)^4 \delta^4(p+q-p'-q')$$



Small  $q^2 \ll M$ ,  $M \ll gT$   
Brownian motion



**Langevin/Fokker Planck (LV)**

Fluct.-Dissip. Th.  
 $D = ET\gamma$

$$\frac{\partial f_Q}{\partial t} = \underbrace{\gamma}_{\text{Drag}} \frac{\partial (p f_Q)}{\partial p} + D \frac{\partial^2 f_Q}{\partial p^2}$$

$\langle p \rangle \approx e^{-\gamma T}$   
Drag

$\langle \Delta p^2 \rangle$   
Diffusion

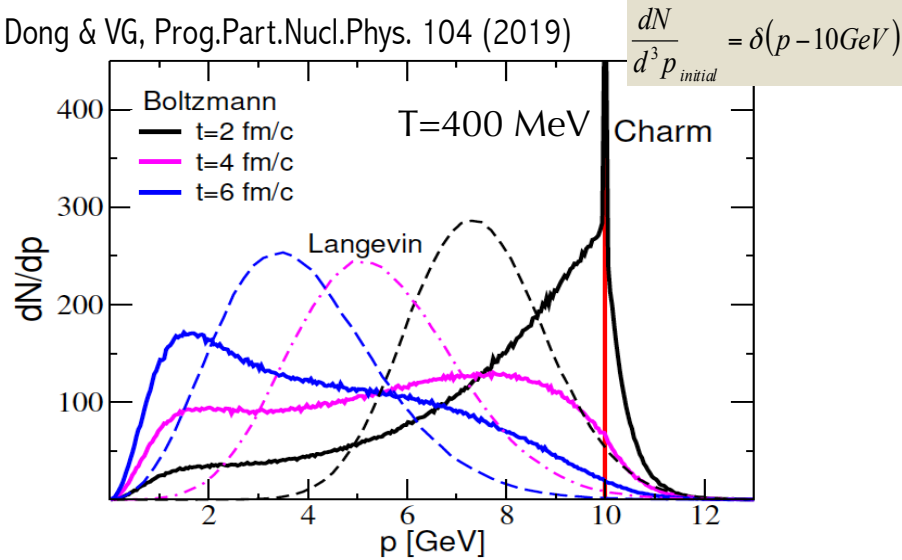
$$\gamma = \int d^3k |M(k, p)|^2 p$$

$$D = \frac{1}{2} \int d^3k |M(k, p)|^2 p^2$$

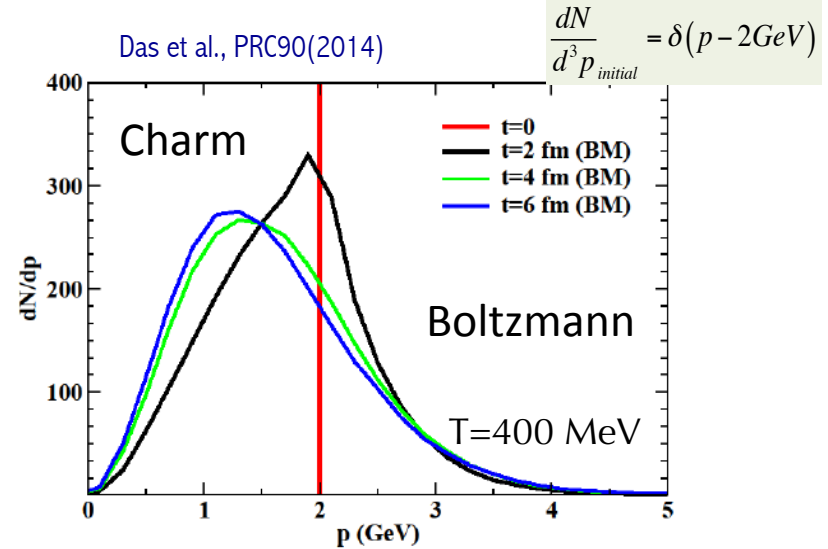
$|M|^2$  scatt. matrix from some theory:  
HTL, pQCD coll., rad., T-matrix..

# Boltzmann vs Langevin: charm in thermal bath

X. Dong & VG, Prog.Part.Nucl.Phys. 104 (2019)



Das et al., PRC90(2014)



✧ Kinematics of collisions (Boltzmann) can throw charm at very low  $p$  soon.

✧ The motion of single HQ does not appear of Brownian type:

$$M_c/T \approx 3 \rightarrow M_c/\langle p_{\text{bulk}} \rangle \approx 1 \quad \& \quad p \gg m_Q$$

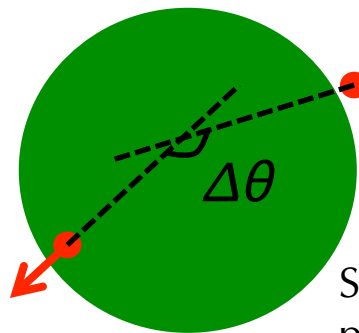
✧ Evolution of  $\langle p \rangle$  is nearly identical in BM & LV

$$\frac{d\sigma}{d\Omega} \propto \frac{1}{(q^2(\theta) + m_D^2)^2}$$

$$m_D = gT = 0.83 \text{ GeV}$$

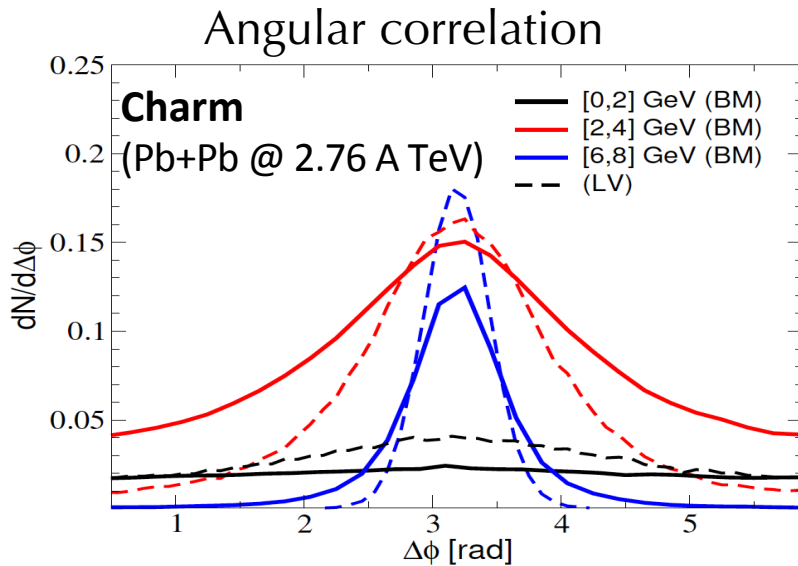
# Boltzmann for angular correlations

BM vs LV would make a difference  
for up coming [D-h] + [D-D]  
triggered angular correlations



Starting from back-to-back  
 $p_T = 10$  GeV as trigger  
only collisional  $E_{\text{loss}}$

$p_T$  [0-2] GeV  
 $p_T$  [2-4] GeV  
 $p_T$  [6-8] GeV



In  $dN/d\Delta\phi_{12}$  sizeable differences  
between BM& LV also for **Bottom**

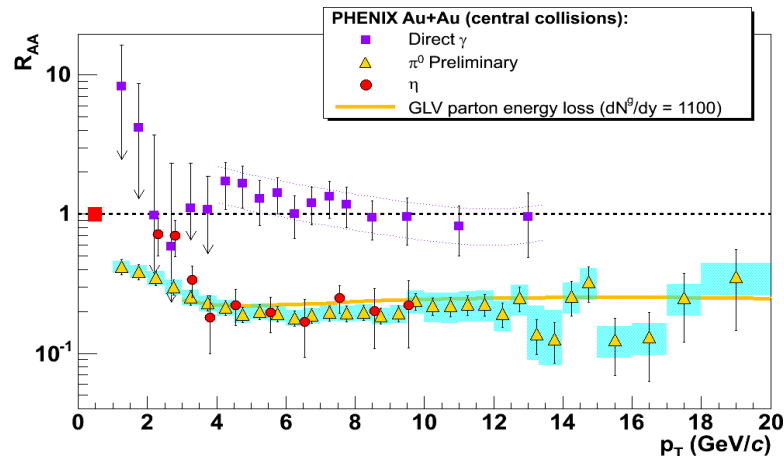
- ❖ Boltzmann especially going to  $dN/d\Delta\phi_{12}$  and high  $p_T$  including both **radiative and collisional** should be more appropriate  
→ SUBATECH, LBL- CCNU,...

# Two Main Observables in HIC

## ❖ Nuclear Modification factor

$$R_{AA}(p_T) = \frac{d^2 N^{AA} / dp_T d\eta}{N_{coll} d^2 N^{NN} / dp_T d\eta}$$

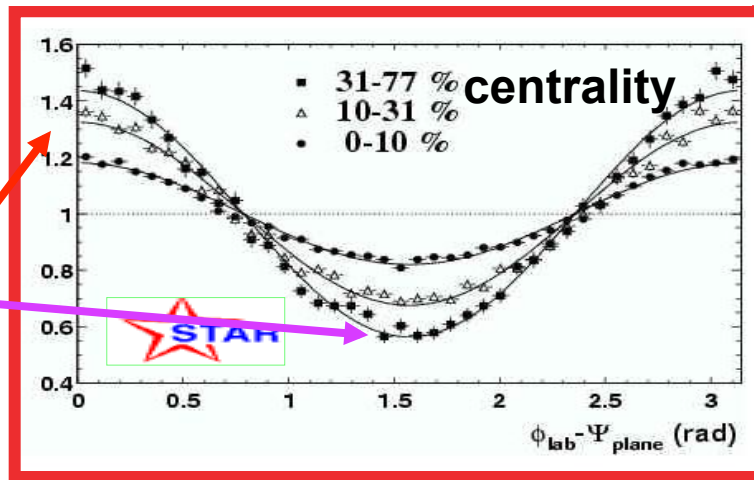
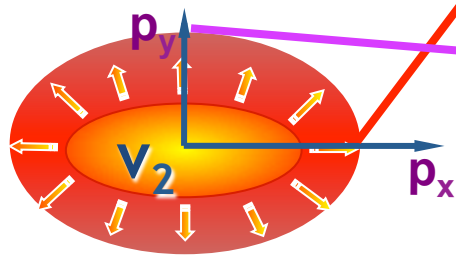
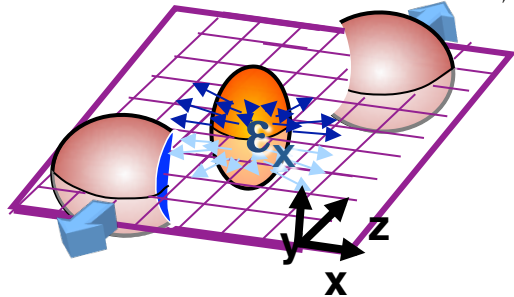
- Modification respect to pp
- Decrease with increasing partonic interaction



## ❖ Anisotropy p-space: Elliptic Flow $v_2$

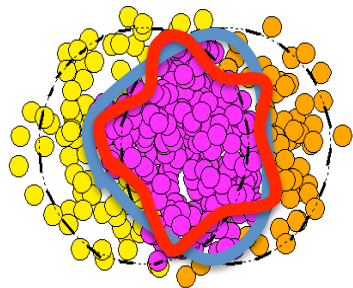
$$\frac{dN}{p_T dp_T d\phi} = \frac{dN}{2\pi p_T dp_T} [1 + 2v_2 \cos(2\phi) + \dots]$$

both at low & high  $p_T$ , but different mechanism



# HF dynamics: e-b-e correlations

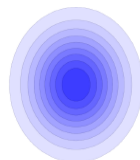
Extending transport approach to event-by-event (space fluctuations in parton distributions):



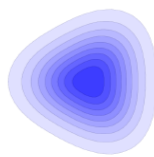
$$\epsilon_n = \frac{\langle r_{\perp}^n \cos[n(\varphi - \Phi_n)] \rangle}{\langle r_{\perp}^n \rangle}$$

$$\Phi_n = \frac{1}{n} \arctan \frac{\langle r_{\perp}^n \sin(n\varphi) \rangle}{\langle r_{\perp}^n \cos(n\varphi) \rangle}$$

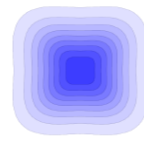
When including fluctuations, all moments appear:



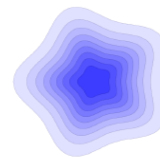
$n = 2$



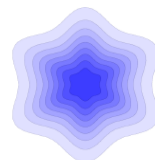
$n = 3$



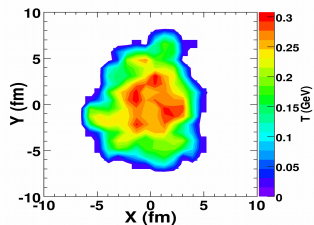
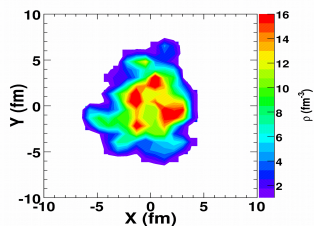
$n = 4$



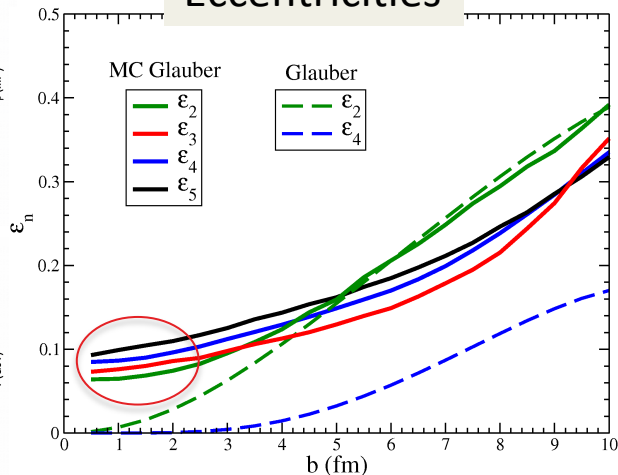
$n = 5$



$n = 6$



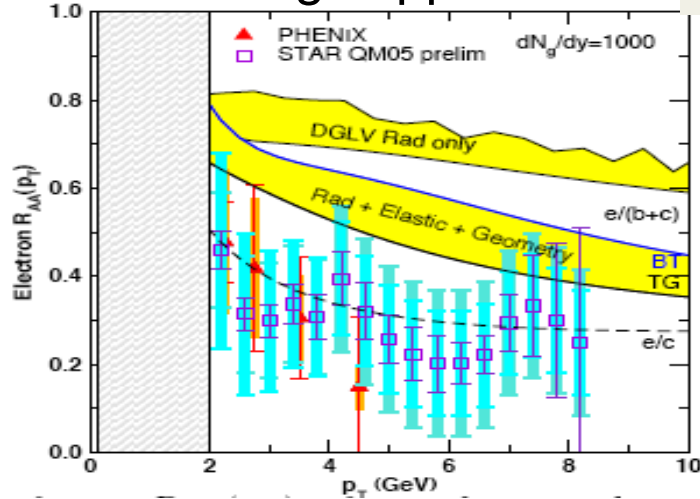
## Eccentricities



- ❖ Higher-order ( $n > 2$ ) anisotropies at EIC ?
- > Spatial fluctuations of parton densities (Sect 3.3. in arXiv:1212.1701 - EIC White Report)
- Key importance for QGP study (IP-Glasma)

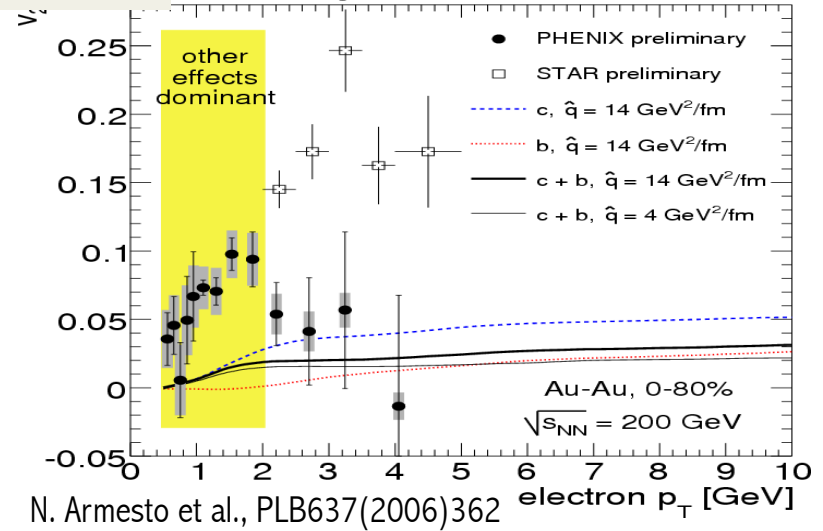
# Surprise at RHIC ( $\approx 15$ years ago)

Strong suppression



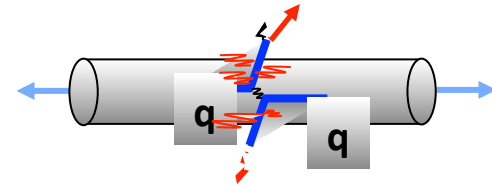
Single e from  
D,B semileptonic decay

Large elliptic Flow



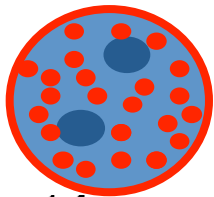
S. Wicks et al. (QM06)

- Radiative energy loss not sufficient ( $p_T < 10$  GeV)
- Charm seems to flow like light quarks



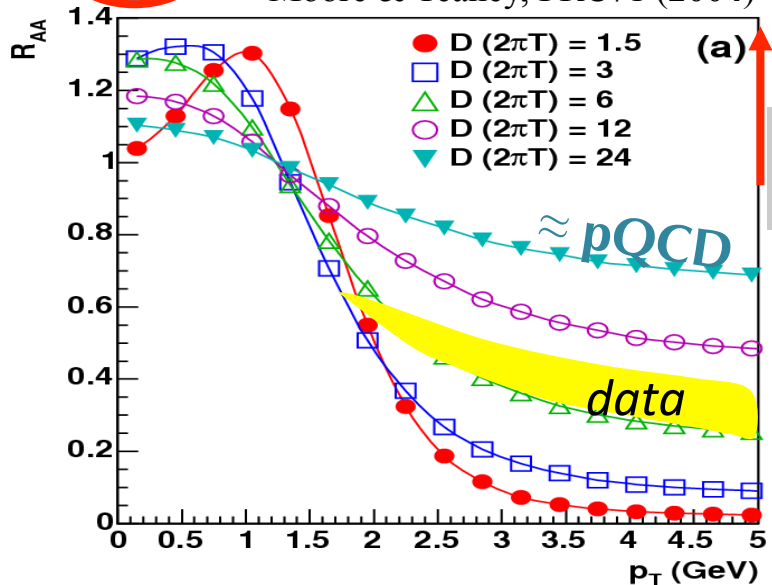
pQCD does not work may be the real cross section is a K factor larger?

# $R_{AA}$ & $v_2$ with upscaled pQCD cross section



Fokker-Plank for charm interaction in a hydro bulk

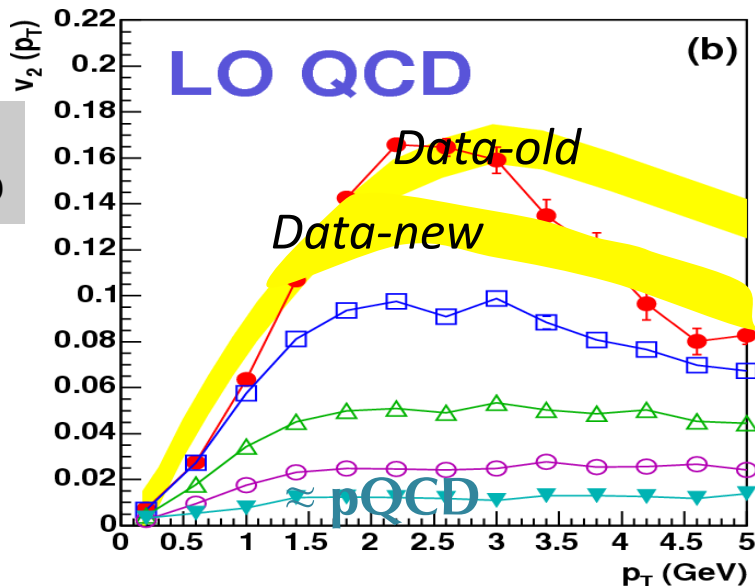
Moore & Teaney, PRC71 (2004)



Diffusion coefficient

$$D_p \propto \int d^3k |M_{g(q)c \rightarrow g(q)c}(k, p)|^2 k^2$$

scattering matrix

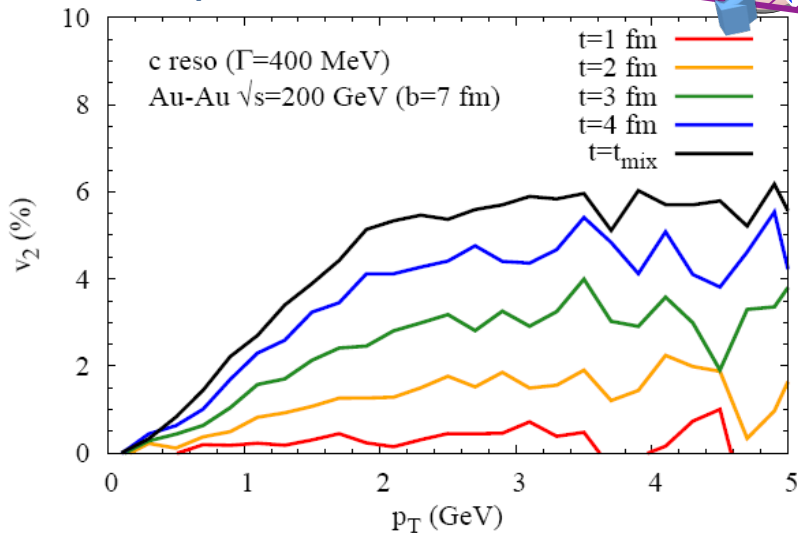
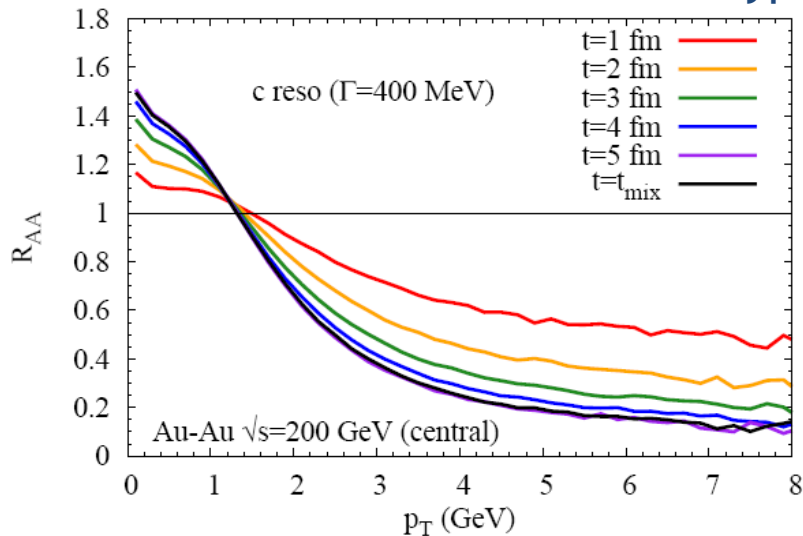
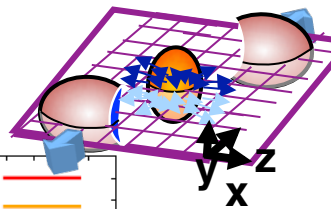


It's not just a matter of pumping up pQCD elastic cross section:  
too low  $R_{AA}$  or too low  $v_2$



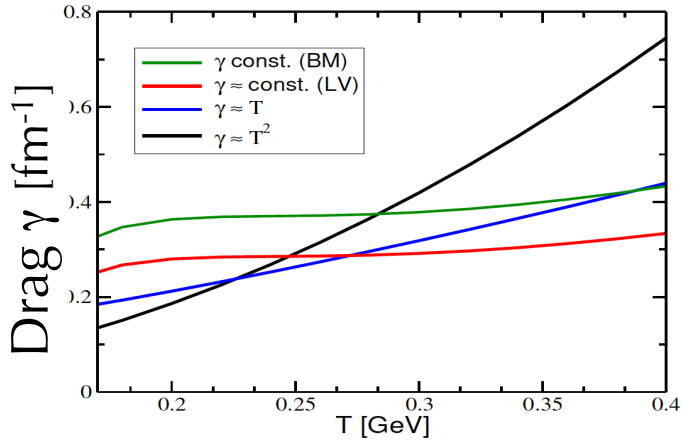
# $R_{AA}$ and $v_2$ correlation: time evolution

$R_{AA}$  can be “generated” faster than  $v_2$   
A typical example



The relation between  $R_{AA}$  and time is not trivial and depend on how one interacts and loose energy with time.

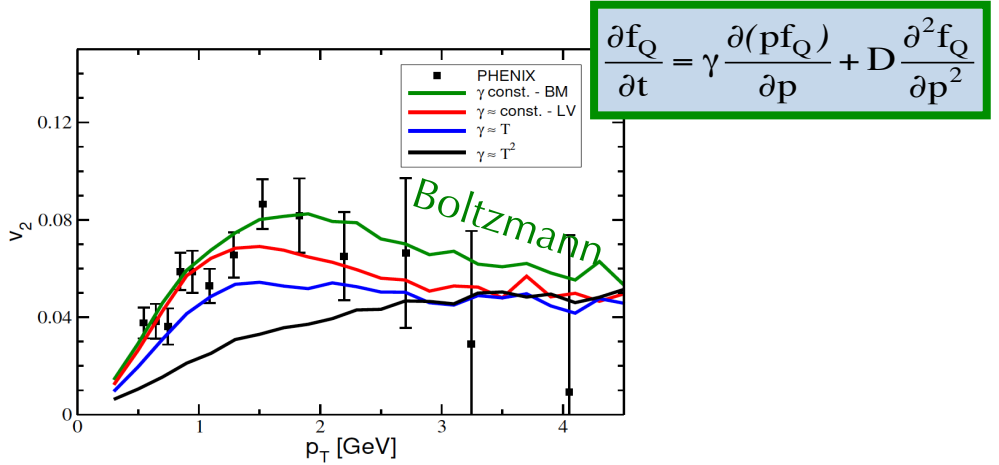
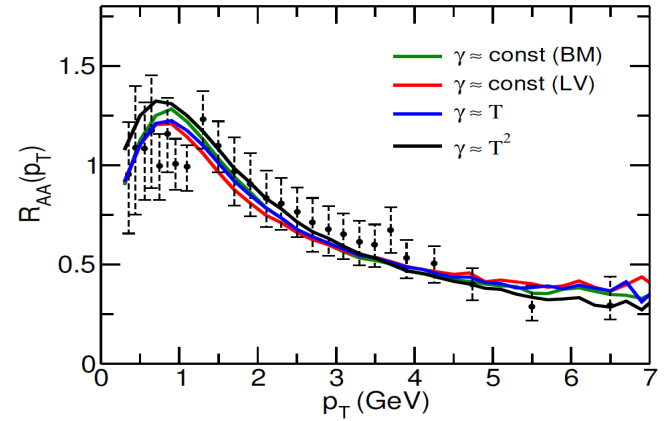
# Impact of T dep. interaction on $R_{AA} - v_2$



## Looking at it beyond the specific modelings

- $\gamma \approx T^2$  [Ads/CFT, pQCD  $\alpha_s = \text{const}$ , Duke]
- $\gamma \approx T$  [pQCD strong  $\alpha_s$  running]
- $\gamma \approx \text{const.}$  [QPM, PHSD,..] [T-matrix] [BT] [MC@HQ]

$\gamma$  rescaled to fit  $R_{AA}(p_T)$ , D from FDT



# Simple QP-Model fitting IQCD

Plumari, Alberico, Greco, Ratti, PRD84 (2011)

$$P(T) = \sum_{i=g,q,\bar{q}} \frac{D_i}{(2\pi)^3} \int_0^\infty d^3k \frac{k^2}{3\omega_i(k)} f_i(k) - B(T),$$

$$\varepsilon(T) = \sum_{i=g,q,\bar{q}} \frac{d_i}{(2\pi)^3} \int_0^\infty d^3k \omega_i(k) f_i(k) + B(T) + \tilde{W}_B(T)$$

Interaction in thermal quasi-particle masses + B(T)

$$\omega_{q,g} = k^2 + m_{q,g}^2(T) \quad m_g^2 = \frac{1}{6} \left( N_c + \frac{1}{2} N_f \right) g^2 T^2 \quad m_q^2 = \frac{N_c^2 - 1}{8N_c} g^2 T^2$$

$g(T)$  from a fit to  $\varepsilon$  from IQCD

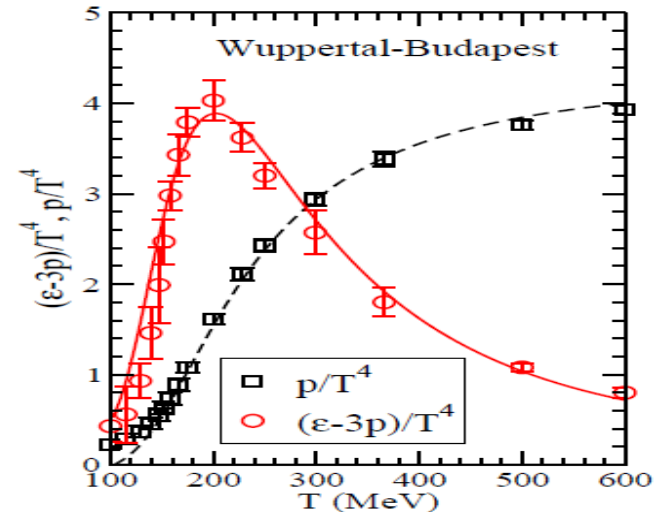
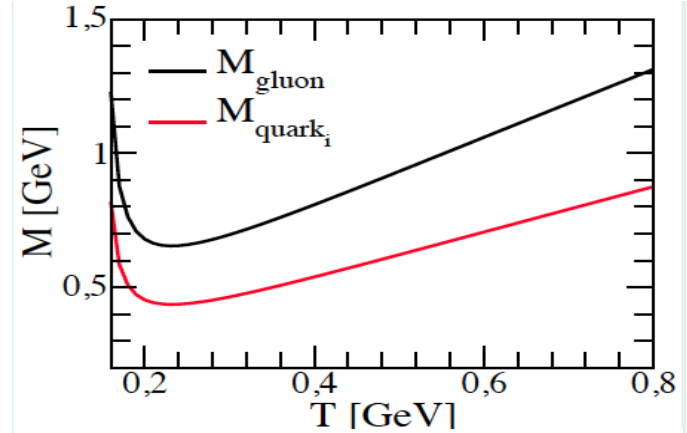
-> good reproduction of  $P$ ,  $e-3P$ ,  $c_s$

$$g_{QP}^2(T) = \frac{48\pi^2}{(11N_c - 2N_f) \ln \left[ \lambda \left( \frac{T}{T_c} - \frac{T_s}{T_c} \right) \right]^2} \quad \lambda = 2.6$$

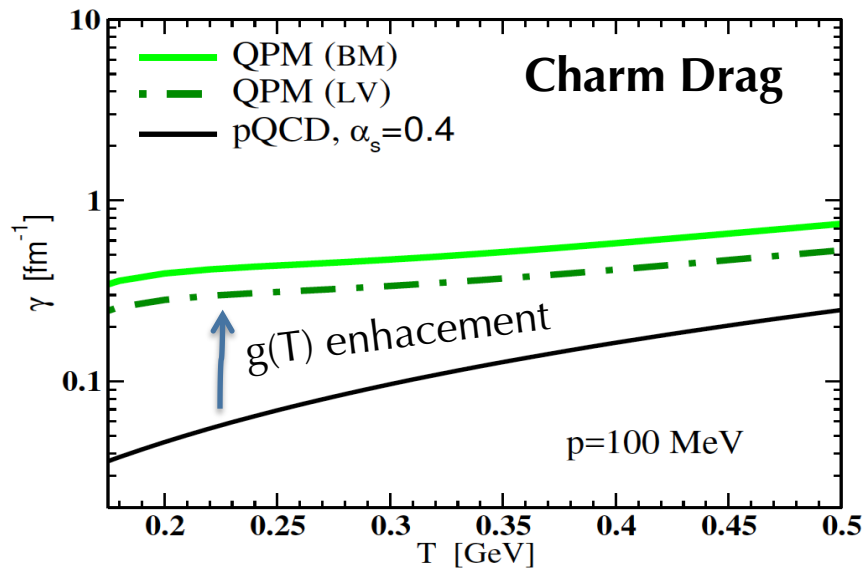
$$T_s = 0.57 T_c$$

**Main features:** as  $T \rightarrow T_c$  enhancement of the coupling  
remnescent of confinement dynamics,

Similarly for T-Matrix with  $V(r,T)$  deduced from lattice QCD



# Drag Transport coefficient in QPM



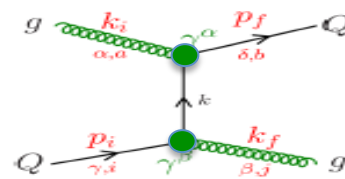
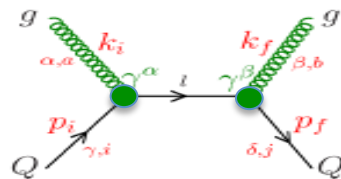
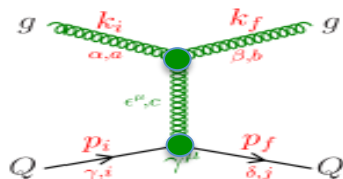
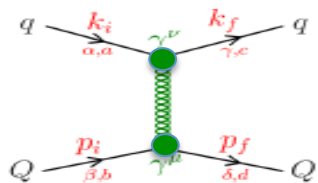
$$f(p,t=0)=\delta(p-p_0)$$

$$\langle p \rangle = p_0 e^{-\gamma t}$$

✧ Drag from QPM quite large than pQCD :  $g(T)$  enhanced as  $T \rightarrow T_c$   
weak dependence on  $T$

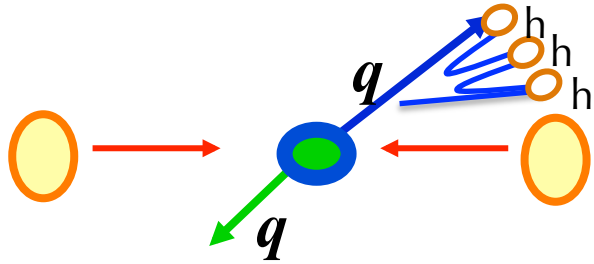
✧ pQCD or AdS/CFT  $\gamma(T) \approx 1/T^2$

$$\gamma_i = \gamma(p^2) p_i = \frac{1}{2E_p} \int \frac{d^3q}{(2\pi)^3 2E_q} \int \frac{d^3q'}{(2\pi)^3 2E_{q'}} \int \frac{d^3p'}{(2\pi)^3 2E_{p'}} \sum |M_{(q,g)+Q \rightarrow (q,g)+Q}|^2 (2\pi)^4 \delta^4(p+q-p'-q') f(q) [(p-p')_i]$$



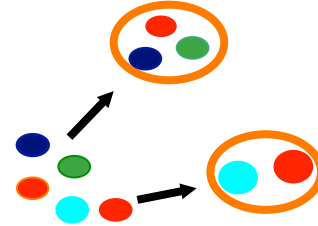
# Fragmentation: $e^+e^-$ , ep, pp

$$f_H(P_H = zp_T) = f_{q,g}(p_T) \otimes D_{q,g \rightarrow H}(z), \quad z < 1$$

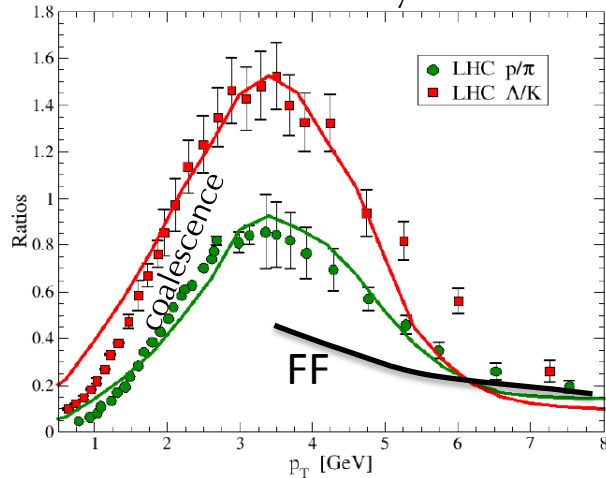


# Quark recombination

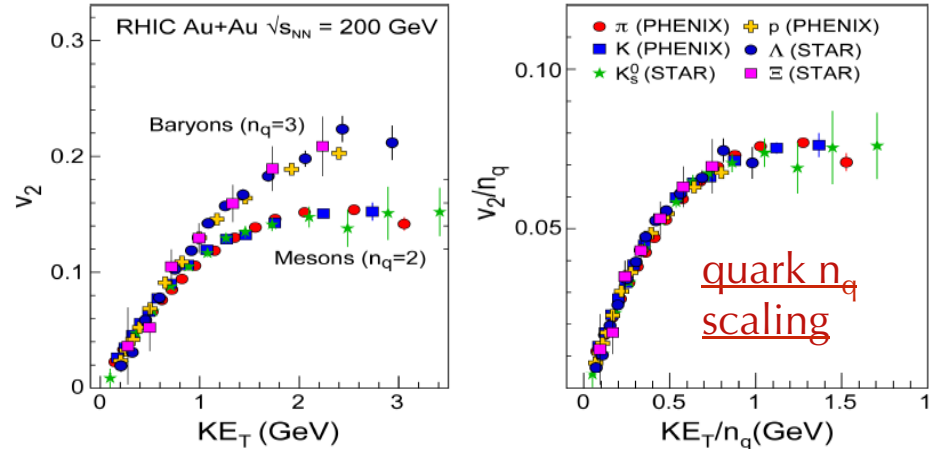
$$f_M(P = p_a + p_b) = \sum_{a,b} f_a(r_a, p_a) \otimes f_b(r_b, p_b) \otimes \Phi_M(r_{ab}, q_{ab})$$



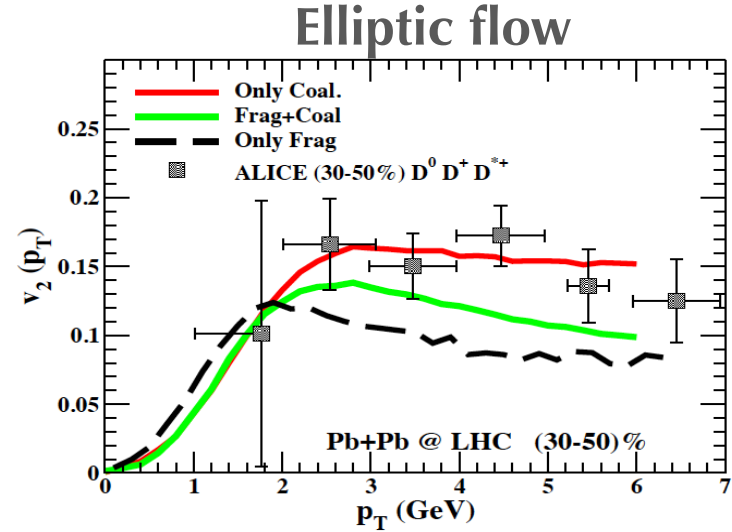
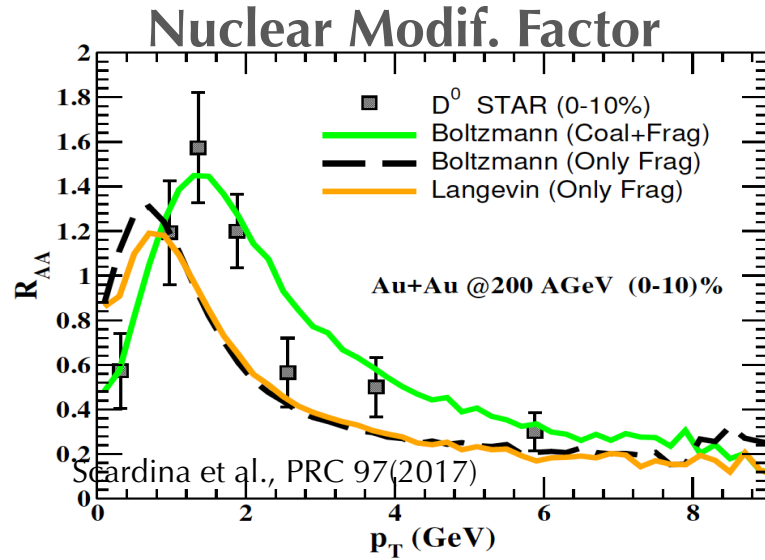
Ratio B/M in Hadr. by Coalescence



B/M Elliptic flow

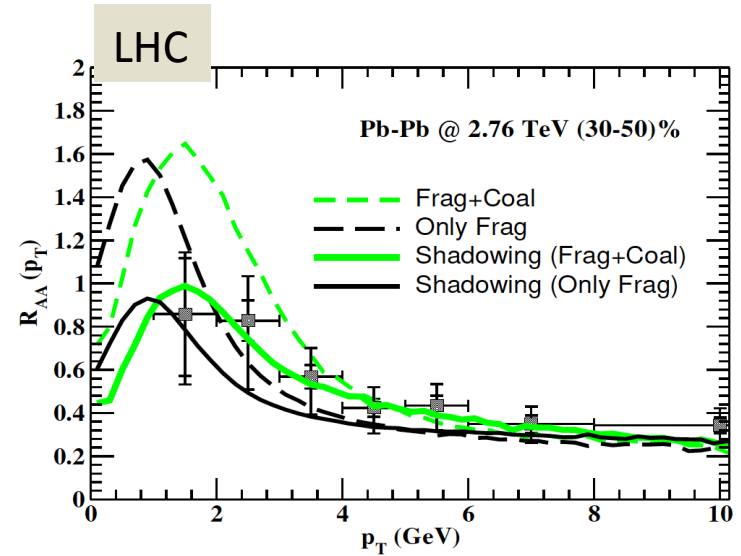
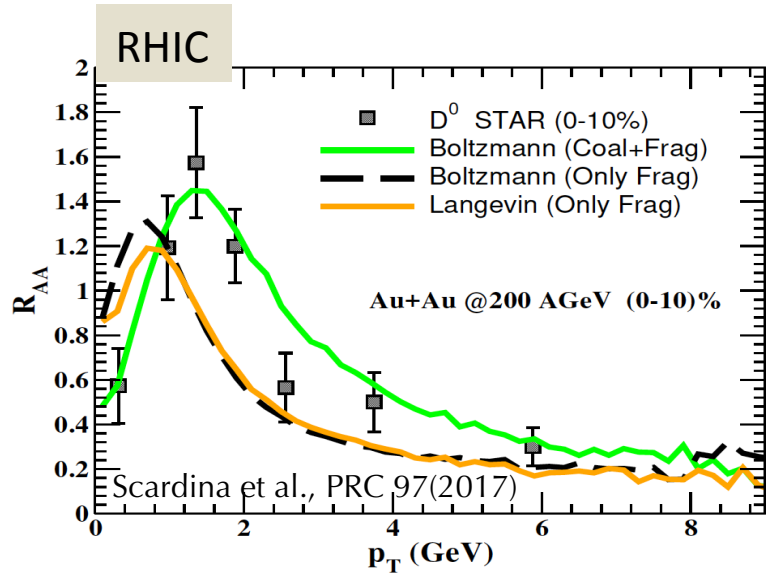


# Some predictions...



✓ Coalescence for  $D$  brings up both  $R_{AA}$  and  $v_2$  toward data

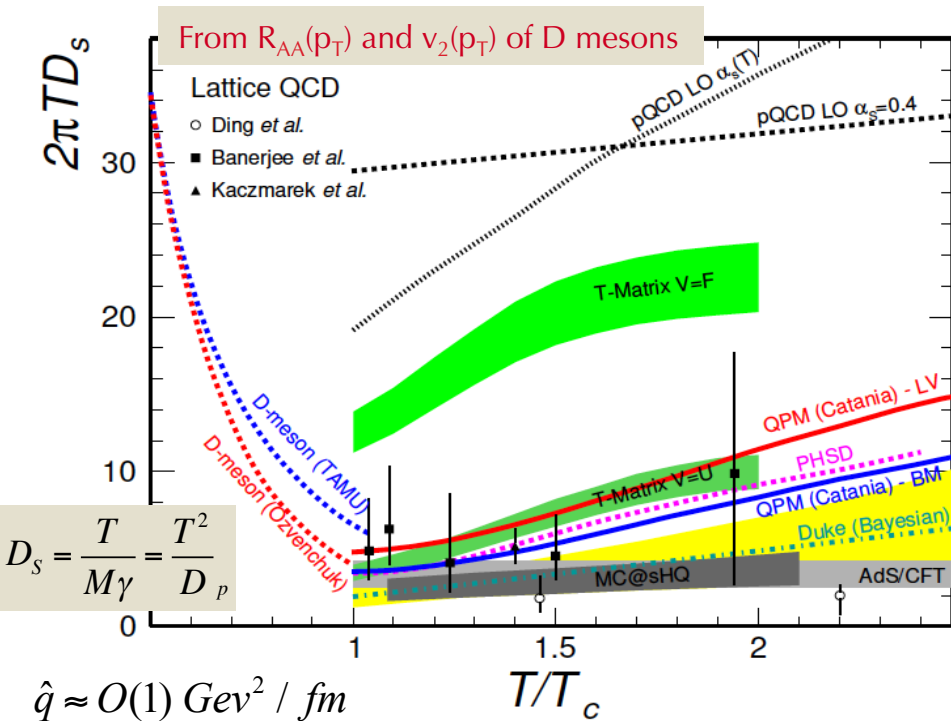
# Some predictions...



- ✓ Coalescence for  $D$  brings up both  $R_{AA}$  and  $v_2$  toward data
- ✓ @LHC shadowing appear necessary [EPS09, Eskola-Salgado JHEP(2009)]
- ✓ EIC on shadowing + new data  $\rightarrow$  much more quantitative statements
- ✓ Hadronic rescattering does not change  $R_{AA}$ , increase by 15%  $v_2$

# What is the underlying $D_s$ ?

X. Dong & VG, Progr. Part. Nucl. Phys.(2019)



$$\tau_{th} = \frac{M}{2\pi T^2} (2\pi T D_s) \cong 1.8 \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

$$\tau_{\text{therm}} \approx \tau_{\text{QGP}} \approx 5 \text{ fm/c}$$

- ❖ Largely non-perturbative  $D_s$  (close AdS/CFT)
- ❖ Agreement with lattice QCD

\*Main Differences in models:

- impact of hadronization
- momentum dependence of diffusion
- inclusion of radiation
- not all models describe data with the same quality

## Future:

- Access low  $p$  & precision data (detector upgrade)
- Better insight into hadronization (...EIC)
- New observables
- Bottom

## Reviews:

- F. Prino and R. Rapp, JPG(2019)
- X. Dong and VG, Progr.Part.Nucl.Phys. (2019)
- Jiaying Zhao *et al.*, arXiv:2005.08277



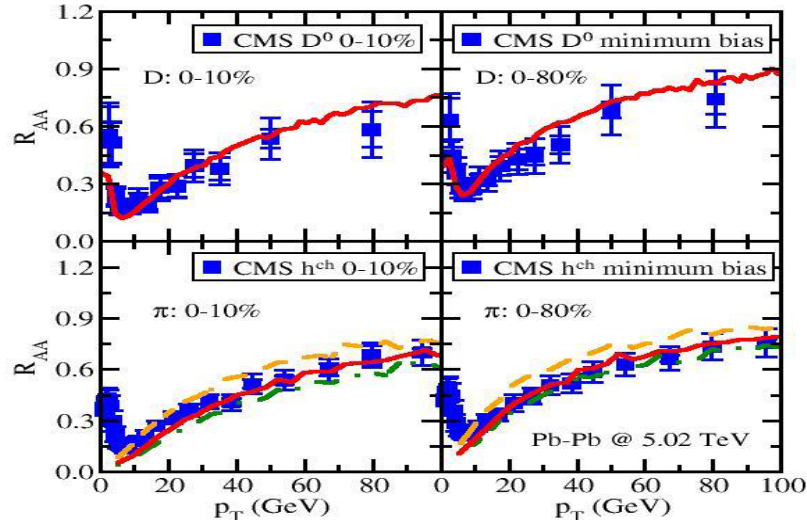
# Linearized Boltzmann: Coll.+Rad.

Linearized Boltzmann Transport : Rad.(pQCD) + Coll.  $E_{\text{loss}}$  (K\*pQCD)  
 Inelastic Scatt. probability based on the average number of medium-induced gluon

Spectrum of medium-induced gluon (Higher-Twist formalism): [ Guo- Wang (2000), Majumder (2012); Zhang, Wang-Wang (2004) ]

$$\frac{dN_g}{dx dk_{\perp}^2 dt} = \frac{2\alpha_s C_A P(x)}{\pi k_{\perp}^4} \hat{q} \left( \frac{k_{\perp}^2}{k_{\perp}^2 + x^2 M^2} \right)^4 \sin^2 \left( \frac{t - t_i}{2\tau_f} \right)$$

Number  $n$  of radiated gluons during  $\Delta t$  – Poisson distribution:  $P(n) = \frac{\langle N_g \rangle^n}{n!} e^{-\langle N_g \rangle}$   $P_{\text{inel}} = 1 - e^{-\langle N_g \rangle}$



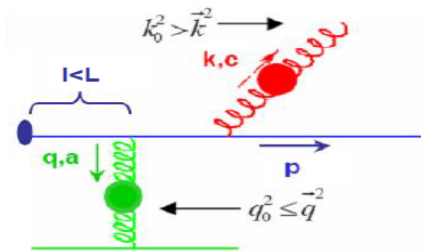
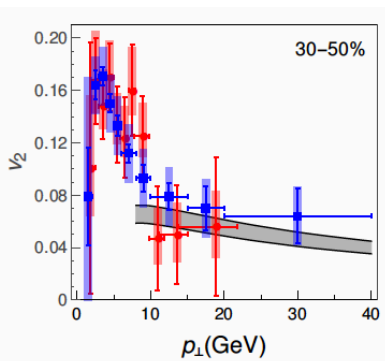
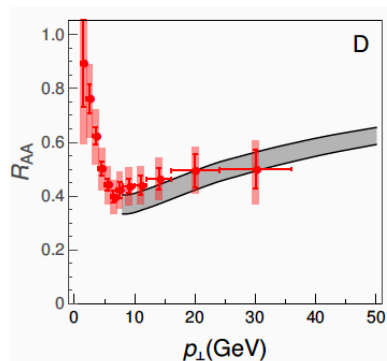
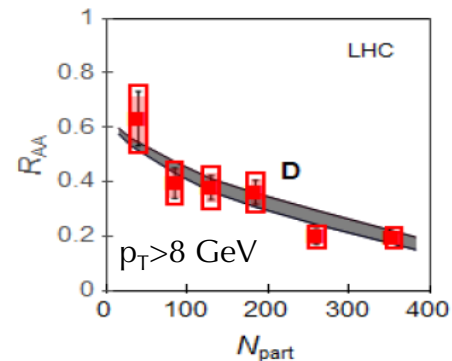
- ✧ Both heavy and light
- ✧ Both radiative and collisional
- ✧ Realistic hydro background

# Radiation: pQCD $E_{\text{loss}}$ extension of DGLV

Continuous improvement on GLV: no static scatterings  $\rightarrow$  collisional+radiative, finite size, magnetic and electric mass,  $\alpha_s$  running ...:

- Collisional non negligible (also at  $p_T > 5-10$  GeV)
- Explain  $R_{AA}(\pi) \approx R_{AA}(D) < R_{AA}(B)$

$$\frac{E_f d^3\sigma}{dp_f^3} = \frac{E_i d^3\sigma(Q)}{dp_i^3} \otimes P(E_i \rightarrow E_f) \otimes D(Q \rightarrow H_Q) \otimes f(H_Q \rightarrow e, J/\psi)$$



HTL Electric & magnetic propagators  
an approach for Hot matter

M. Djordjevic et al., PLB734 (2014)

D. Zigic et al, PLB791(2019)

**Radiative parton Eloss accounts for  $R_{AA}$ ,  $v_2$  of both light and heavy quarks at  $p_T > 8-10$  GeV**

✧ In the past was missing an underlying Hydro background: Under progress (3+1D) calculation  $\rightarrow v_2(p_T)$

# Open HQ in soft-collinear effective theory (SCET)

✧ **Effective theory [power counting in  $p_T/Q$ ]** describing the propagation of HQ in a background QCD medium – SCET<sub>M,G</sub> **beyond parton Eloss**

✧ Role of **mass** understood in vacuum & medium splitting functions that in the limit of soft emission reduce to GLV

Massive splitting function with dead cone

Consistent full NLO calculation

$$\sum_j \hat{\sigma}_i^{(0)} \otimes \mathcal{P}_{i \rightarrow jk}^{\text{med}} \otimes D_j^H \equiv \hat{\sigma}_i^{(0)} \otimes D_i^{H,\text{med}}$$

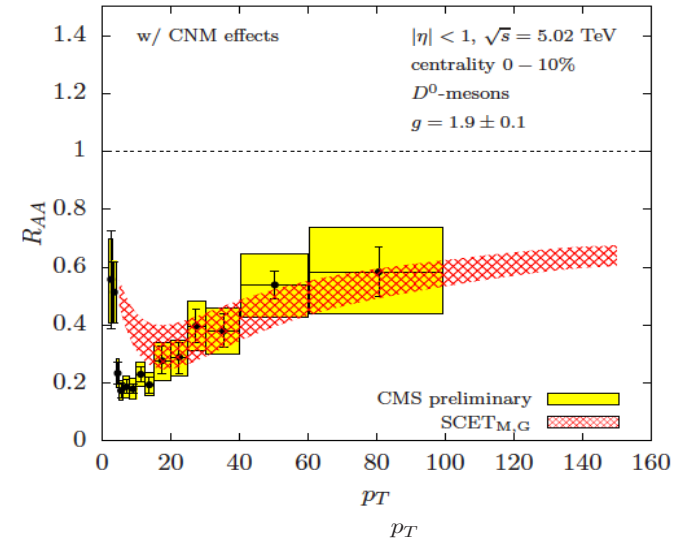
✧ Confirm Radiative process ( $p_T > 20$  GeV)

✧ Approach applies in both cold and hot matter ( $\neq$ DGLV)

➔ **predictions for EIC**

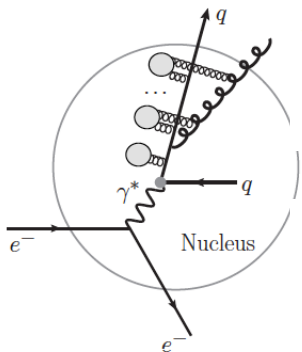
Not applied to study  $v_n$  (to my knowledge)

Z. Kang, F. Ringer, I. Vitev, JHEP 03 (2017)



At lower  $p_T$  including collisional **Dissociation** of D meson ( $\tau_D = \tau_0 * E/m_D$ )

# SCET+DGLAP-FF for EIC

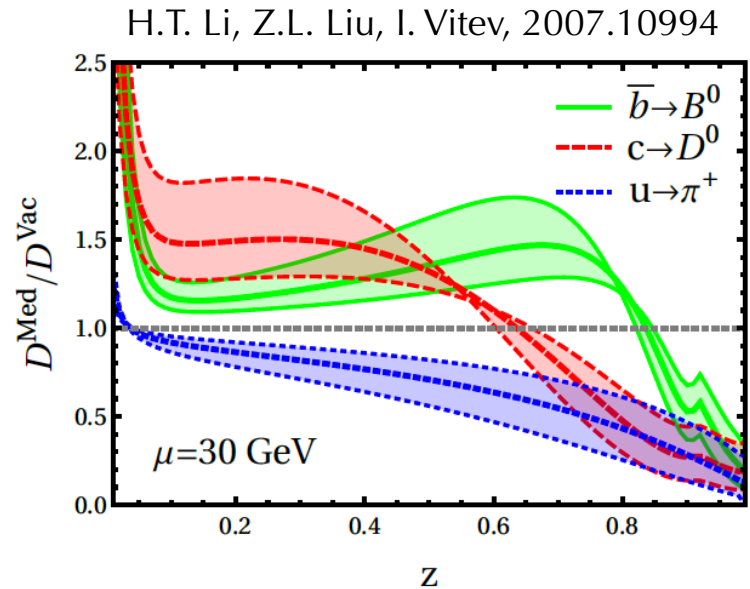
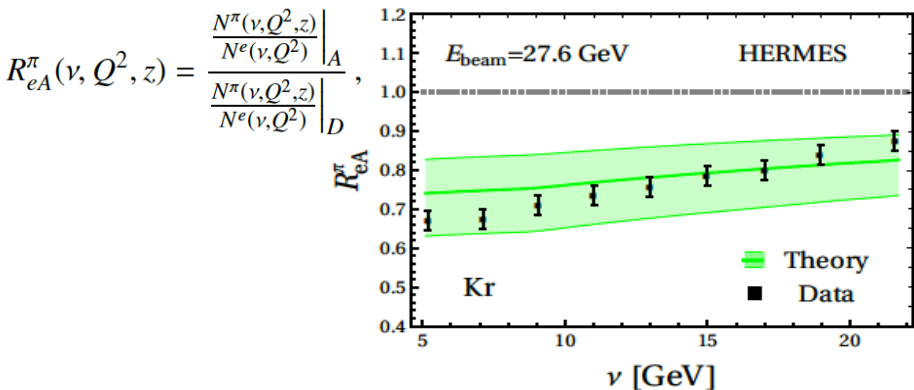


$$E_h \frac{d^3 \sigma^{\ell N \rightarrow hX}}{d^3 P_h} = \frac{1}{S} \sum_{i,f} \int_0^1 \frac{dx}{x} \int_0^1 \frac{dz}{z^2} f^{i/N}(x, \mu) \times D^{h/f}(z, \mu) \left[ \hat{\sigma}^{i \rightarrow f} + f_{\text{ren}}^{\gamma/\ell} \left( \frac{-t}{s+u}, \mu \right) \hat{\sigma}^{\gamma i \rightarrow f} \right]$$

$$\frac{d}{d \ln \mu^2} \bar{D}^{h/i}(x, \mu) = \sum_j \int_x^1 \frac{dz}{z} \bar{D}^{h/j} \left( \frac{x}{z}, \mu \right) \left[ P_{ji}(z, \alpha_s(\mu)) + P_{ji}^{\text{med}}(z, \mu) \right]$$

- SCET: jet – QCD medium interaction as in AA
- Medium induced splitting kernels  $\rightarrow$  FF evolution

New evolution approach with in-medium showers, NLO baseline. Constrained by HERMES.



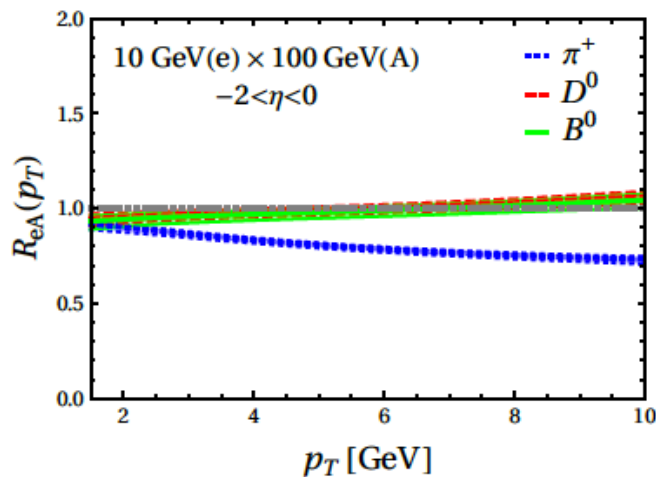
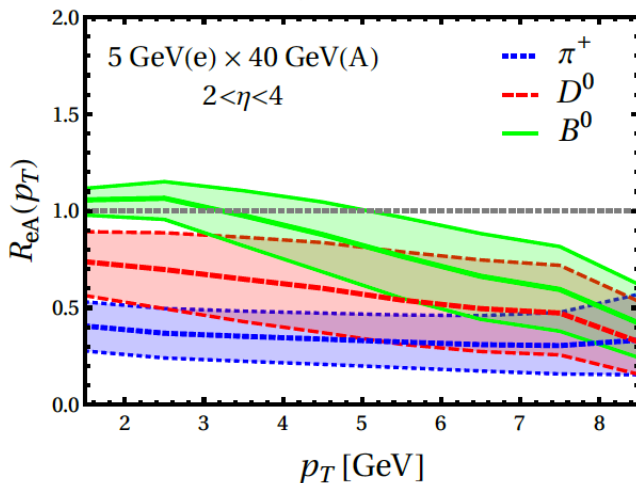
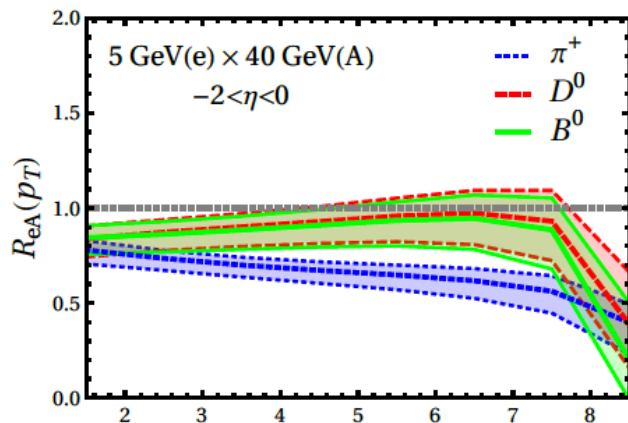
Enhancement at small and moderate values of z. Induced by the hard vacuum fragmentation

# SCET+DGLAP-FF: predictions for EIC

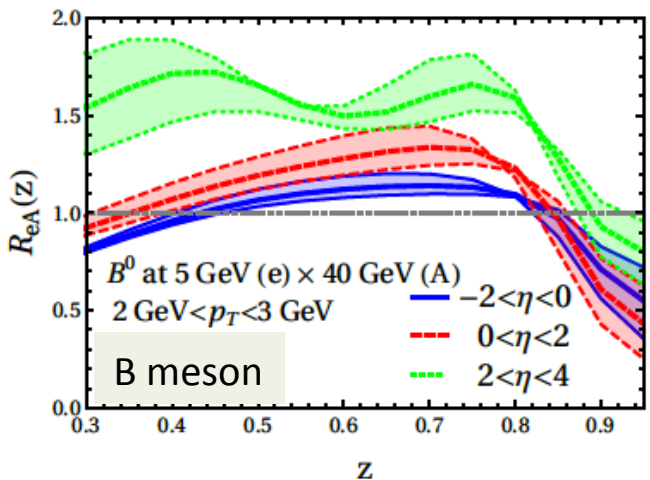
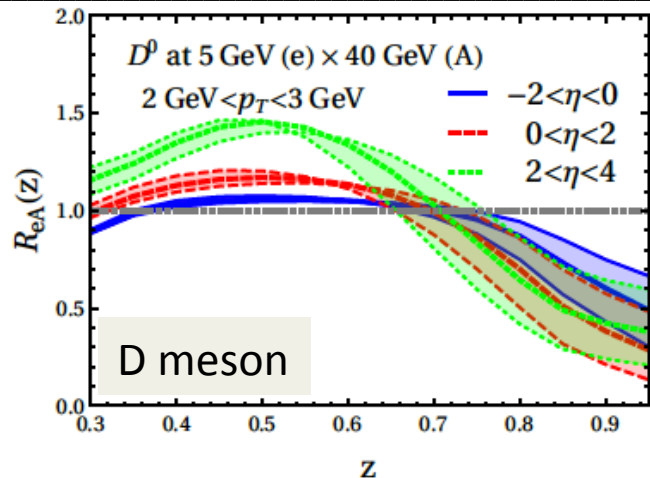
H.T. Li, Z.L. Liu, I. Vitev, 2007.10994

$$R_{eA}^{\pi}(v, Q^2, z) = \frac{N^{\pi}(v, Q^2, z) \Big|_A}{N^e(v, Q^2)} \Big|_A, \quad \frac{N^{\pi}(v, Q^2, z) \Big|_D}{N^e(v, Q^2)} \Big|_D$$

- ✧ First predictions:  
how nuclear effects will change with  $p_T$  and rapidity
- ✧ Effects larger at smaller energy and rapidity gap

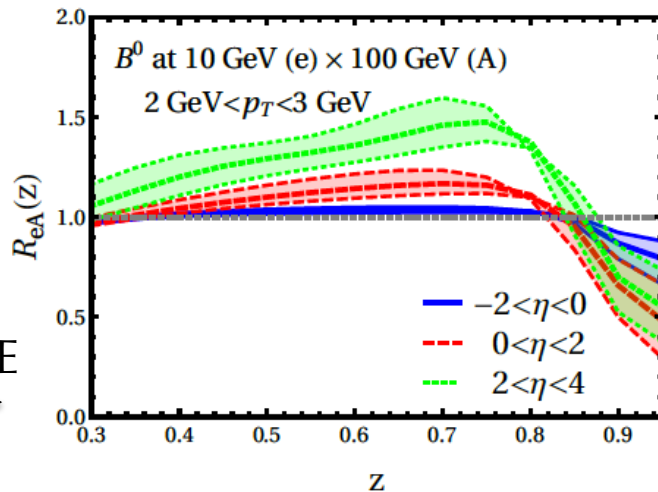


# SCET+DGLAP-FF: prediction for EIC



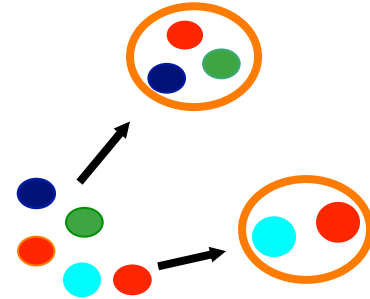
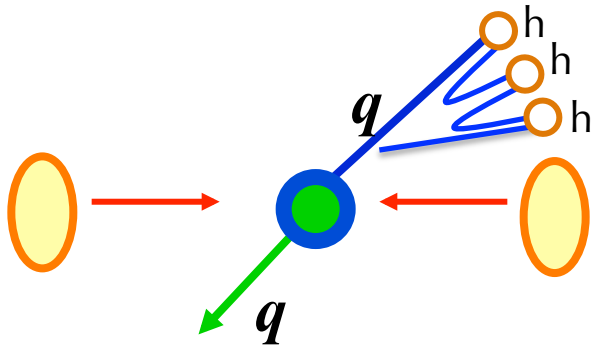
Increasing E  
 $\longrightarrow$

- ✧ For D and B the  $R_{eA}$  vs  $z$  is closely related to Fragmentation Function in-medium modification: more suitable observable for tomography
- ✧ Transition from enhancement to suppression at moderate  $z$  will be an *unambiguous measure of parton shower formation in Nuclei*

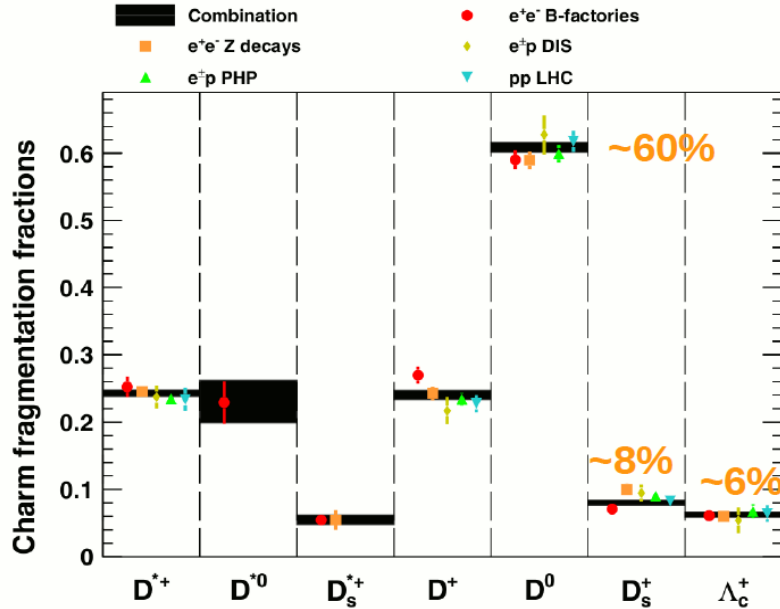


# HADRONIZATION

(AA,pA...pp)



# $\Lambda_c/D$ in elementary collisions



M. Lisovyi, et al. EPJ C76 (2016) no.7, 397

## Fragmentation functions

$$\left(\frac{\Lambda_c}{D^0}\right)_{e^+e^-}^{pp} \approx 0.1$$

## Statistical Hadronization model

$$\left(\frac{\Lambda_c}{D^0}\right)_{e^+e^-}^{pp} \approx 0.25 - 0.30$$

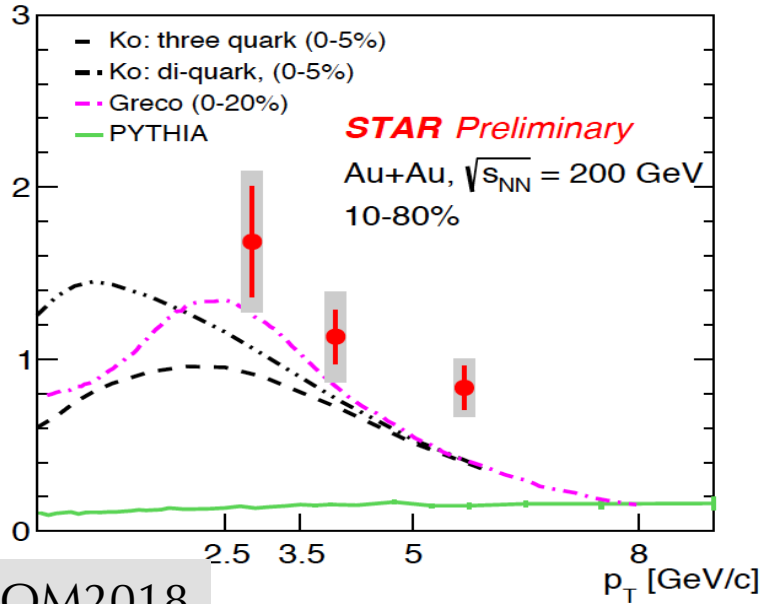
A. Andronic et al. PLB571 (2003)

I. Kuznetsova, J. Rafelski, EPJ C51 (2007)



# $\Lambda_c/D$ in AA and in pp

Quite surprising ...



QM2018

Large  $\Lambda_c/D$  predicted by quark coalescence in the QGP

Y. Oh, C.M. Ko, et al., PRC79 (2009)

S. Plumari, V. Minissale and V.G., Eur. Phys. J. C78(2018)

# Coalescence approach

$$\frac{dN_{Hadron}}{d^2 p_T} = g_H \int \prod_{i=1}^n p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3} f_q(x_i, p_i) f_W(x_1, \dots, x_n; p_1, \dots, p_n) \delta(p_T - \sum_i p_{iT})$$

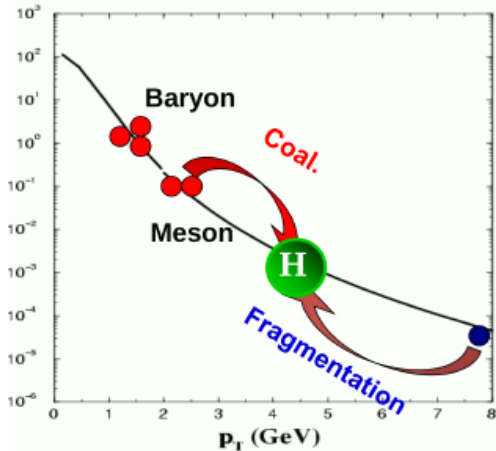
Statistical factor  
colour-spin-isospin

Parton Distribution  
function

Hadron Wigner  
function

distribution function giving  $R_{AA}$  and  $v_2$  for D just discussed

Wigner function with the width fixed by radius from quark model

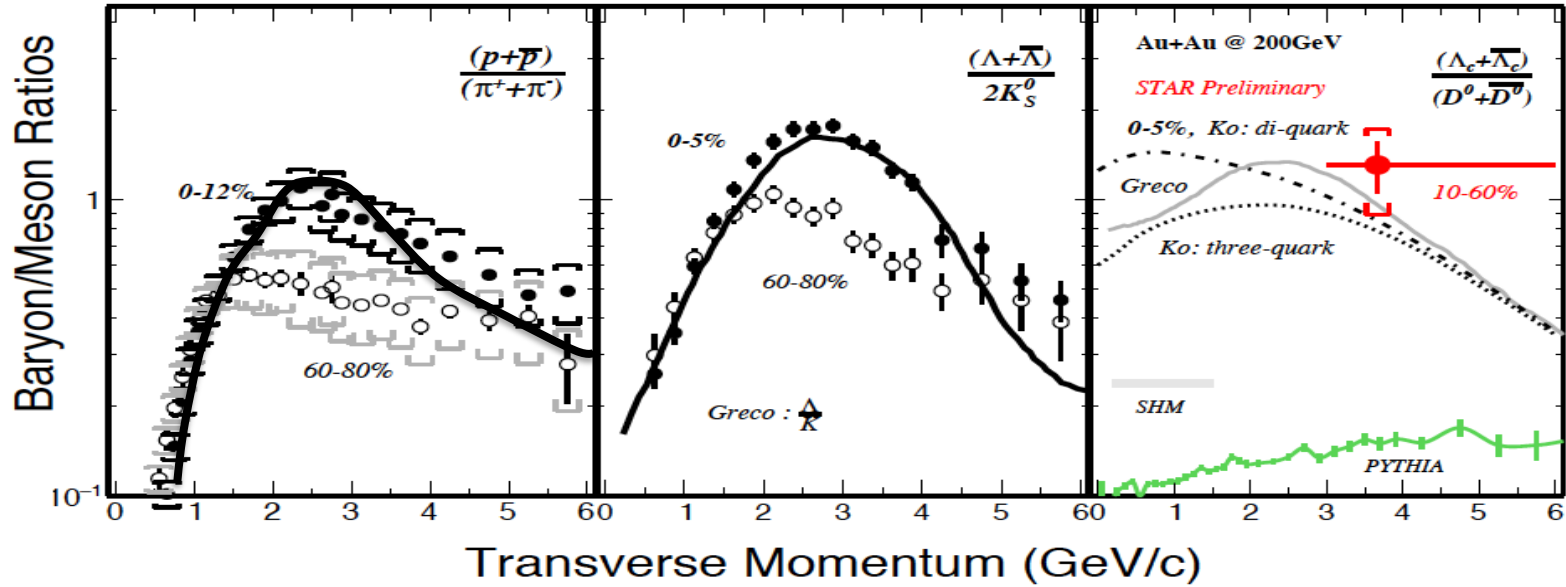


C.-W. Hwang, EPJ C23, 585 (2002).  
C. Albertus et al., NPA 740, 333 (2004), quark model  
 $\langle r^2 \rangle_{D^-} = 0.184 \text{ fm}^2$   $\langle r^2 \rangle_{D_s^-} = 0.124 \text{ fm}^2$   $\langle r^2 \rangle_{\Lambda_c^-} = 0.152 \text{ fm}^2$

Requiring  $P_{\text{coal}}(p \rightarrow 0) = 1$

- ✧ The charm not “coalescing” undergo fragmentation: charm number conserved at each  $p_T$
- ✧ Is the same approach employed to predict  $\rho/\pi$ ,  $\Lambda/K$

# Coalescence in AA for $p/\pi$ $\Lambda/K$ , $\Lambda_c/D$ ?



X. Dong and V. G., Progress in Particle and Nuclear Physics (2018)

Greco-Ko Levai, Phys. Rev. Lett. (2003)

# Studying the HF in uRHIC

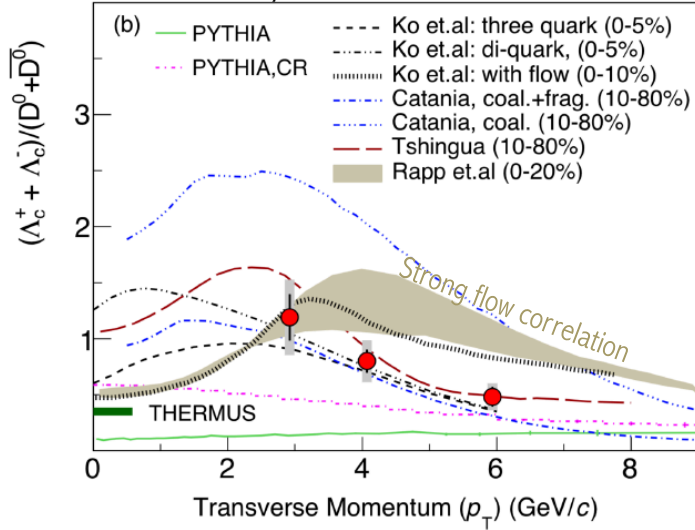
- **Hadronization**  $\Lambda_c/D \approx O(1)$ 
  - coalescence and/or fragm.
  - Large  $\Lambda_c/D$  in pp,pA,AA  $\rightarrow$  affect  $R_{AA}(p_T)$

$\tau_0 < 0.1 \text{ fm}/c$

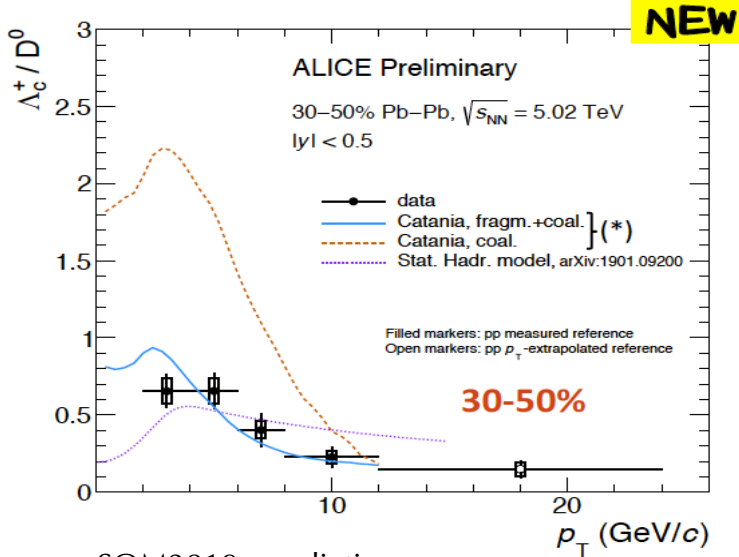
b,  
b,c

Adapted from Rapp & Greco

STAR, Phys.Rev.Lett. 124 (2020)



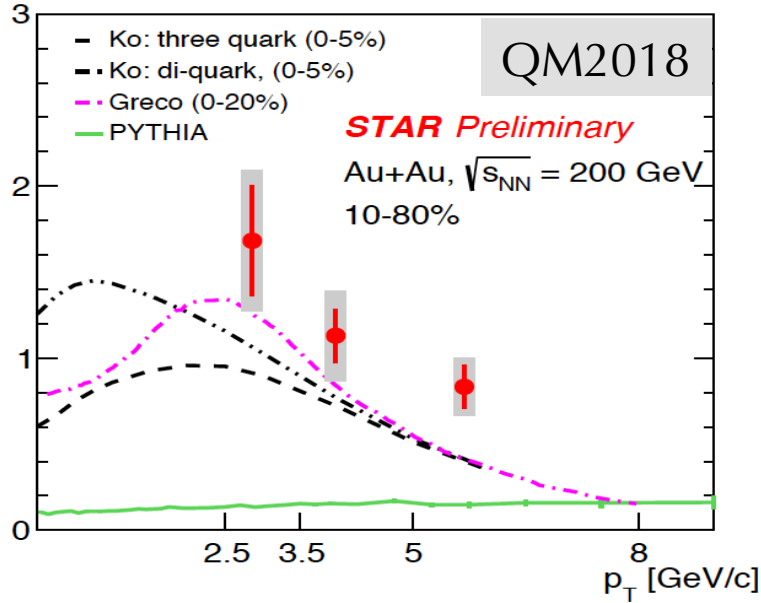
He,Rapp: RQM >> PDG



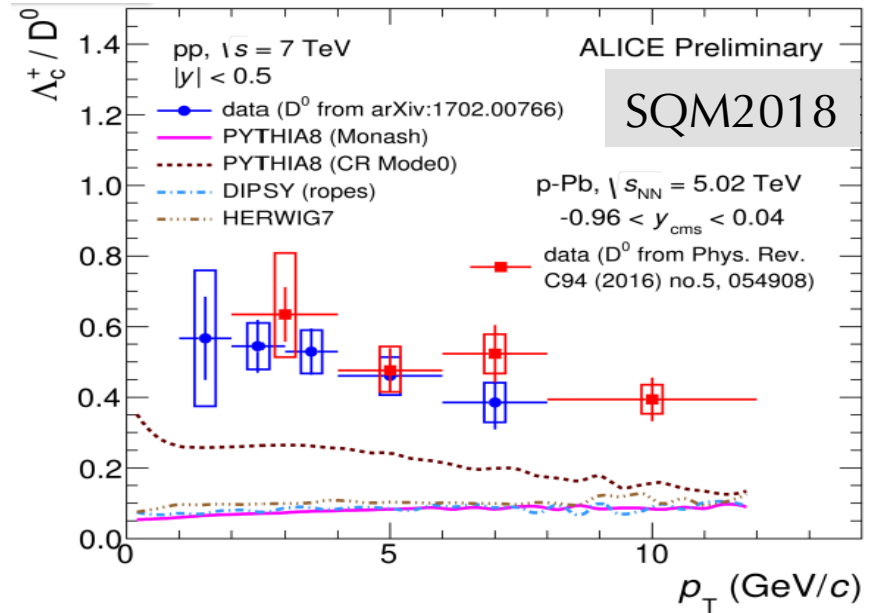
SQM2019, prediction

# $\Lambda_c/D$ in AA and in pA,pp

Quite surprising in AA ...



but even in pp@7TeV & pA@5TeV



Large  $\Lambda_c/D$  predicted by quark coalescence in the QGP

Is there a Hot QCD matter medium also in pA and pp?

Several signatures of flow expansion in high multiplicity pp and pA also for HQ

PRELIMINARY

# Small systems: Coalescence in pp?

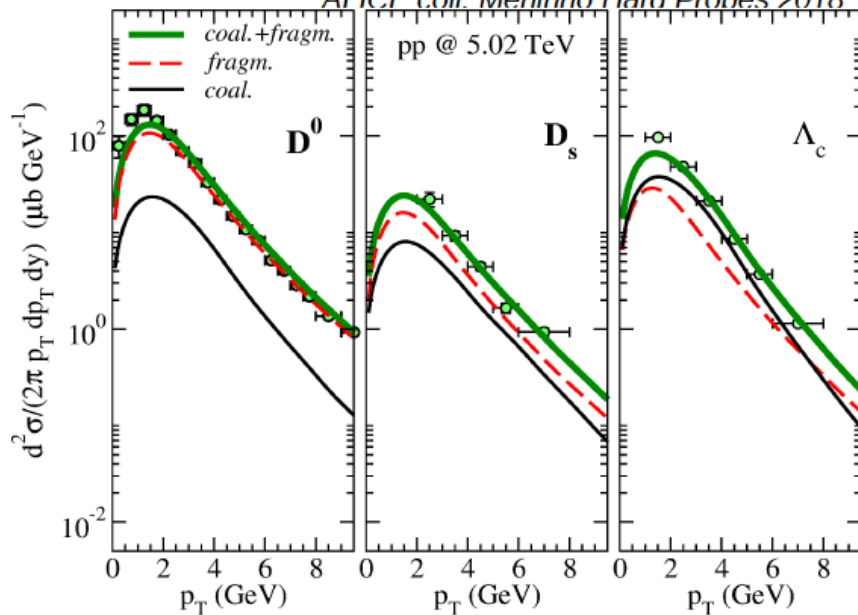
Common consensus of possible presence of QGP in smaller system.

If we assume in  $p+p$  @ 5 TeV a medium similar to the one simulated in hydro:

What if:

- Assuming QGP formation also in pp?
- What coalescence+fragmentation predicts in this case?

Data taken from: ALICE coll. EPJ C79 (2019) no.5, 388  
ALICE coll. Meninno Hard Probes 2018



- ◆ Thermal Distribution ( $p_T < 2$  GeV)

$$\frac{dN_q}{d^2 r_T d^2 p_T} = \frac{g_q \tau m_T}{(2\pi)^3} \exp\left(-\frac{\gamma_T (m_T - p_T \beta_T)}{T}\right)$$

- ◆ Collective flow  $\beta_T = \beta_0 \frac{r}{R}$
  - ◆ Fireball radius+radial flow constraints  $dN_{ch}/dy$  and  $dE_T/dy$
  - ◆ Minijet Distribution ( $p_T > 2$  GeV)
- NO QUENCHING

**p+p @ 5 TeV**

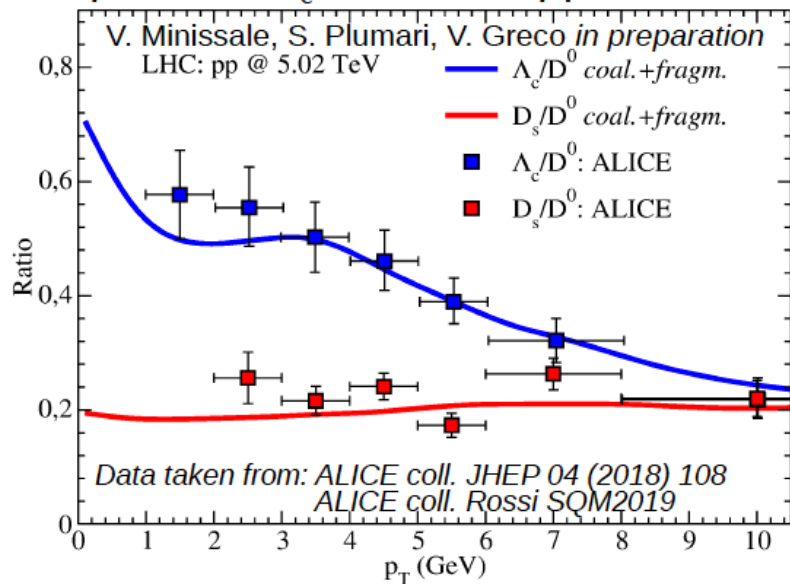
- $t_{pp} = 1.7$  fm/c
- $\beta_0 = 0.4$
- $R = 2.5$  fm
- $V \sim 30$  fm<sup>3</sup>

Hydro simulation

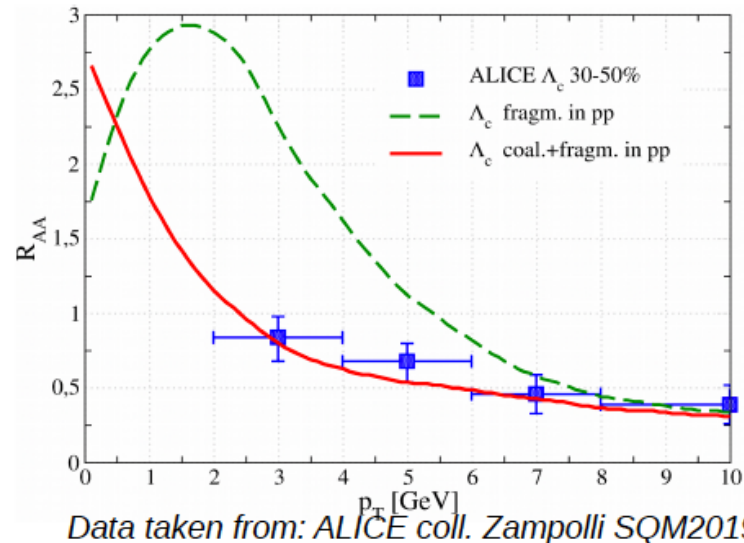
wave function widths  $\sigma_p$  of baryon and mesons kept the same at RHIC and LHC!

# In-medium coalescence in pp

No peak in  $\Lambda_c / D^0$  ratio (pp collision)

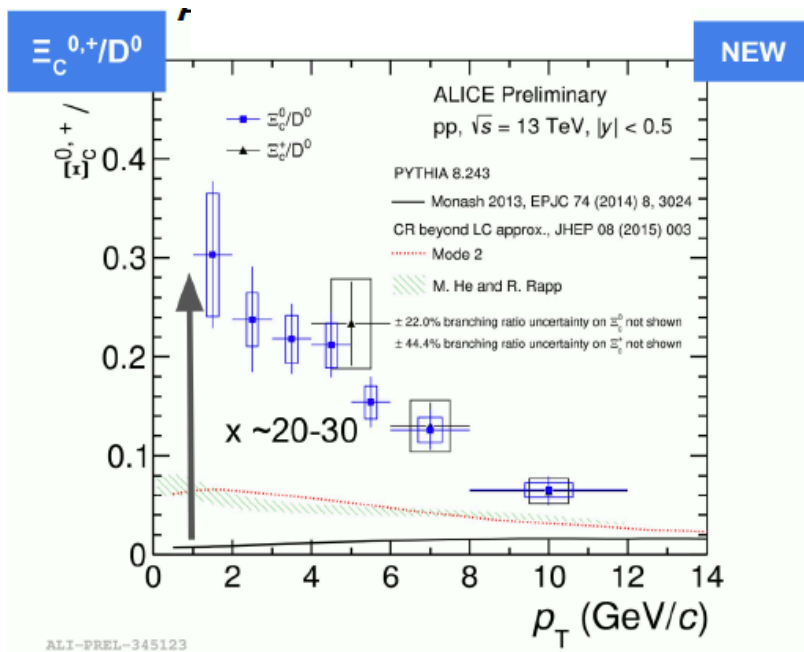


Data seem to favour model where both coalescence and fragmentation are present in pp

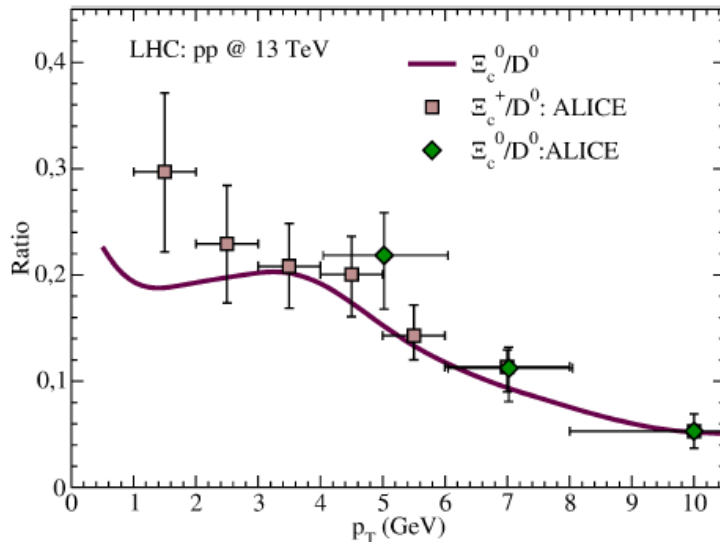


Different hadronization model affects the determination of the HQ transp. Coeff.

# Heavy Baryon hadronization in pp@LHC: internal chemistry



V. Minissale, S. Plumari, V. Greco *in preparation*



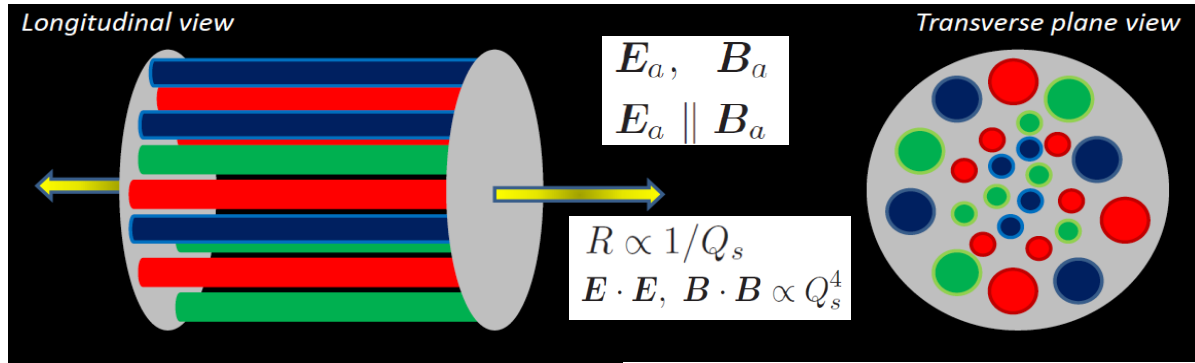
Several ratio of multi charm hadrons where the effect of enhancement are huge  
At high eenergy we will see sign of such an enhancements?

Extension to  $\Omega_{ccc}$  and  $\Xi_{cc}$ ....

**What will be able to see EIC?**



# A first study of HQ in a Glasma



Initialization by MV model, PRD49 (1994)

$$\langle \rho_A^a(x_T) \rho_A^b(y_T) \rangle = (g^2 \mu_A)^2 \delta^{ab} \delta^{(2)}(x_T - y_T),$$

## Solving classical Yang-Mills

$$E^i = \tau \partial_\tau A_i, \quad \partial_\tau E^i = \frac{1}{\tau} D_\eta F_{\eta i} + \tau D_j F_{ji},$$

$$E^\eta = \frac{1}{\tau} \partial_\tau A_\eta, \quad \partial_\tau E^\eta = \frac{1}{\tau} D_j F_{j\eta}.$$

Solved in SU(2)

## Heavy quark in the chromo magnetic field

$$\frac{dx_i}{dt} = \frac{p_i}{E},$$

$$E \frac{dp_i}{dt} = Q_a F_{i\nu}^a p^\nu, \quad E \frac{dQ_a}{dt} = -Q_c \varepsilon^{cba} A_b \cdot p,$$

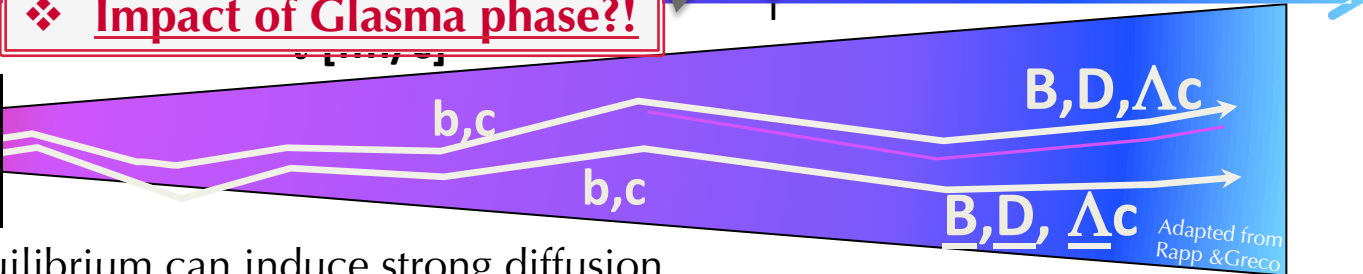
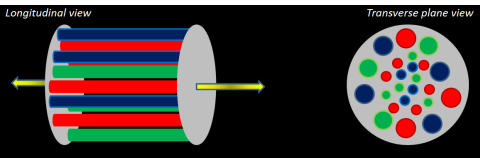
# Studying the HF in uRHIC

0 0.5

**Impact of Initial Stage**

discarded till 2018

❖ **Impact of Glasma phase?!**

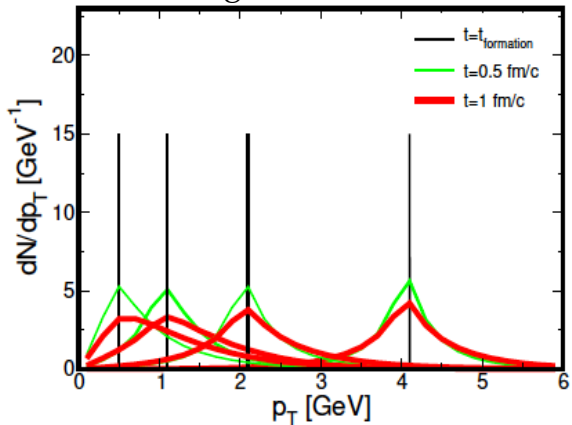


Adapted from Rapp & Greco

Initial Glasma in non-equilibrium can induce strong diffusion

- M.Ruggieri and S.K. Das, PRD98 (2018)

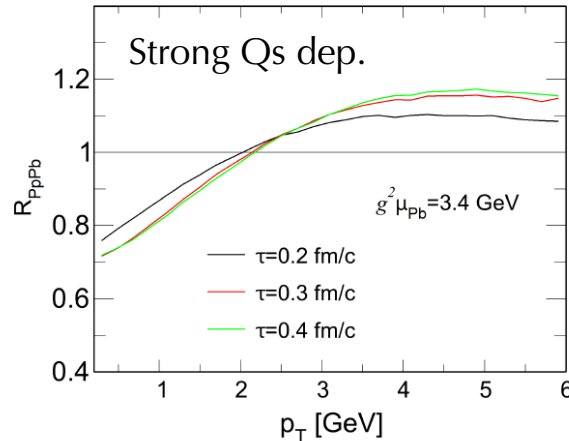
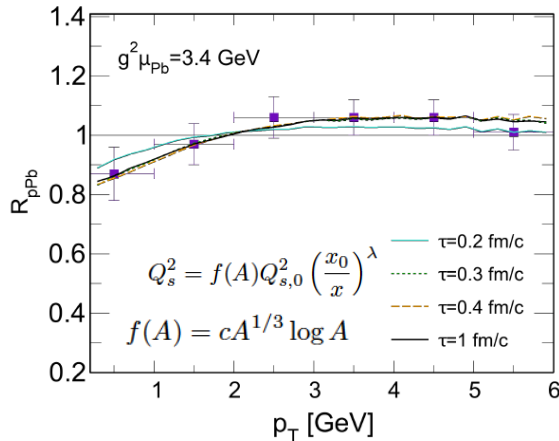
Strong diffusion (box)



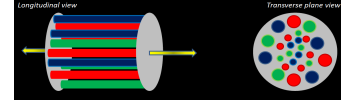
pPb@ 5.02TeV

J.H.Liu et al., PRC 102(2020)

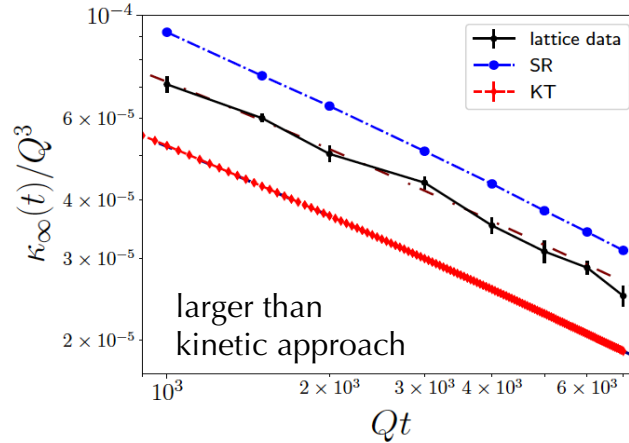
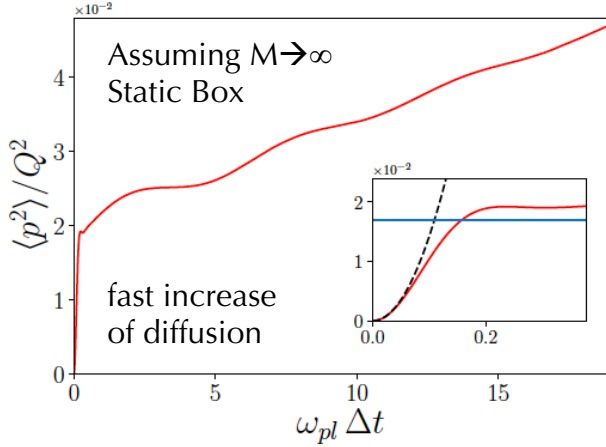
PbPb@5.02ATeV



# Impact of Glasma on HQ



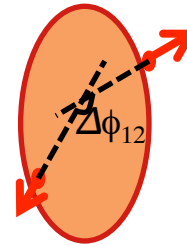
K. Boguslavski, A. Kurkela, T. Lappi and J. Peuron, JHEP09 (2020)077 SU(3)



Correlator method  $\langle \dot{p}_i(t) \dot{p}_i(t') \rangle = \frac{g^2}{2N_c} \langle E_i^a(t) E_i^a(t') \rangle$   $3\kappa(t, \Delta t) \equiv \frac{d}{d\Delta t} \langle p^2(t, \Delta t) \rangle$

## Link pA <-> AA [<-> eA@EIC?]

- > May have key role for D-D angular correlation
- Any effect of glasma dynamics on HF at EIC?
- EIC can determine more precisely the QS scale



Not only suppr./enhanc.  
but also angular diffusion

# Conclusions ? ... Summary

---

## ❖ Standard Open HF physics in uRHICs:

\* from  $R_{AA}, v_2 \rightarrow D_s(T)$  of Hot QCD medium  $\approx$  lattice QCD [non-perturbative dynamics]

\* Dominance of radiative Eloss (jet quenching) at  $p_T > 10$  GeV (SCET, DGLV, ...)

\* Shadowing and Qs Glasma scale need a more precise determination  $\rightarrow$  EIC

\* more precision data +  $p \rightarrow 0$ , additional observables + extension to b quark will allow significant advancements and more direct comparison to IQCD

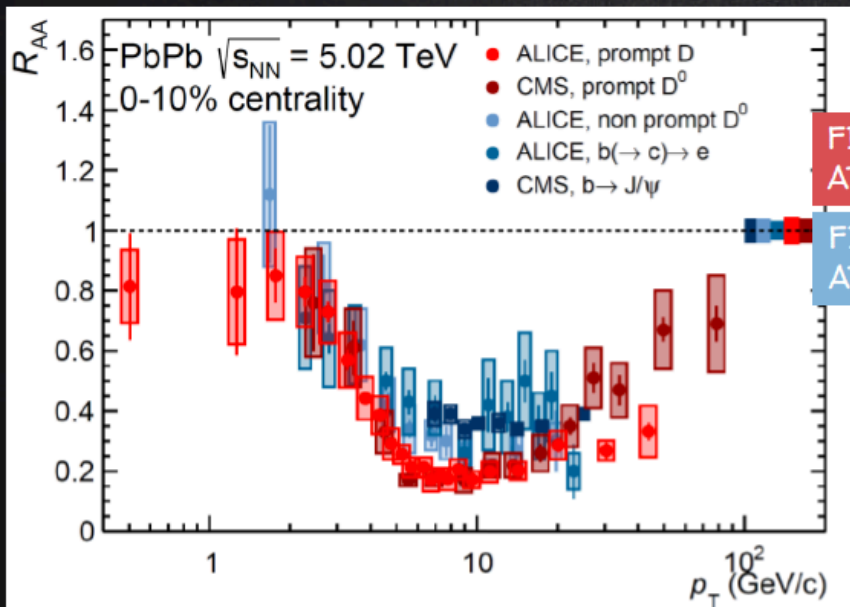
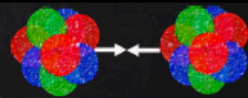
## ❖ SCET prediction for $R_{eA}$ at EIC: specific enhancement at moderate-small $z$

❖ Hadronization and universality of FFs in HQ sector (especially for heavy baryon)... EIC?

❖ HF can play a role in spotting Glasma dynamics, linking pA and eA

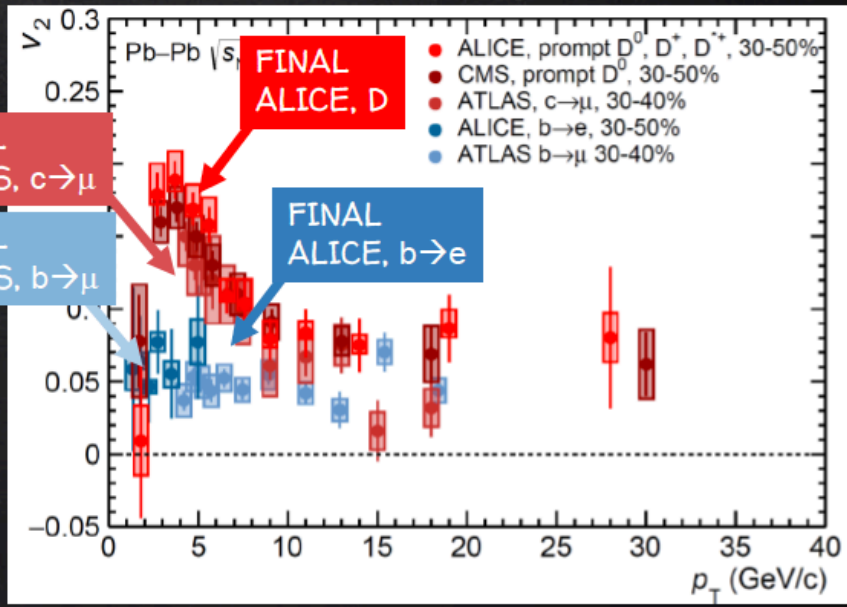
Back-up Slide

# CHARM & BEAUTY



FINAL  
ATLAS, c→μ

FINAL  
ATLAS, b→μ

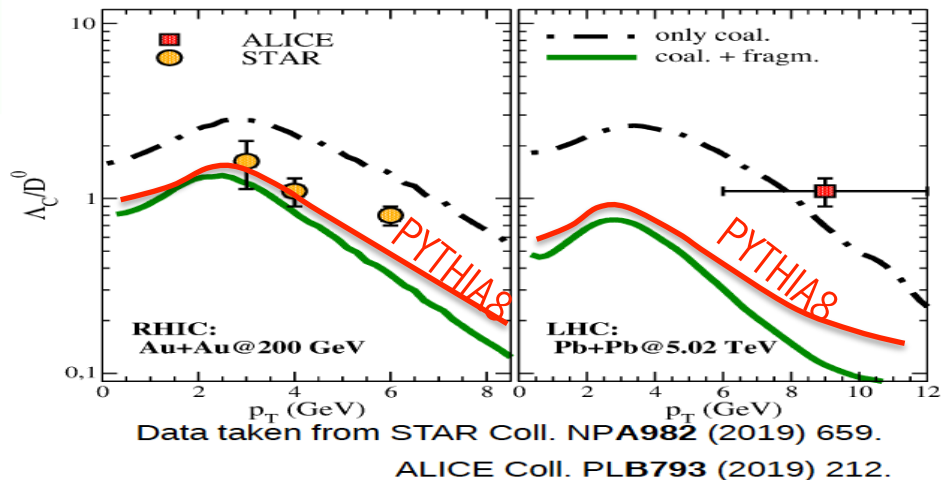


FINAL  
ALICE, D

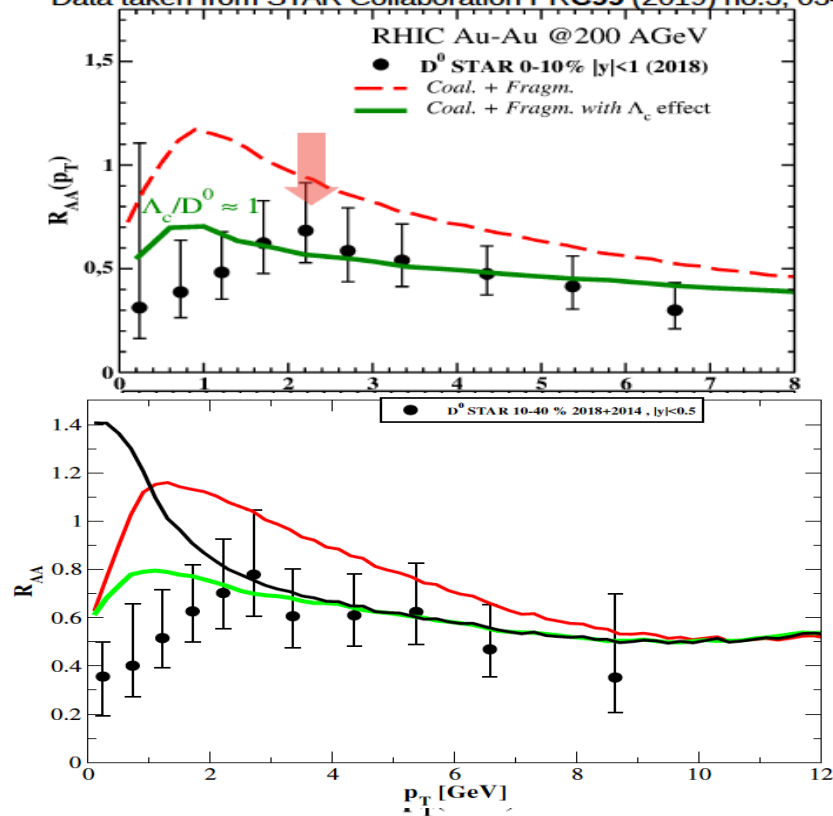
FINAL  
ALICE, b→e

# Impact of large $\Lambda_c$ production on $R_{AA}(p_T)$

With the same coalescence plus fragmentation model we describe the  $\Lambda_c/D^0$  S. Plumari, V. Minissale, S.K. Das, G. Coci, V. Greco, EPJ C78 (2018) no.4, 348



Data taken from STAR Collaboration PRC99 (2019) no.3, 034908



S. Plumari et al., EPJ C (2018)348

✧ This opens a new paradigm in studying HF in the low  $p_T$  region

# RHIC: Baryon/meson

S. Plumari, et al., Eur. Phys. J. C78 no. 4, (2018) 348

## Coalescence

Following: L.W.Chen, C.M. Ko, W. Liu, M. Nielsen, PRC 76, 014906 (2007). K.-J. Sun, L.-W. Chen, PRC 95, 044905 (2017).  
For hypersurface of proper time  $\tau$  and non relativistic limit:

$$\text{for } p_T \ll m \quad \frac{\Lambda_c^+}{D^0} \propto \frac{g_\Lambda}{g_D} \left( \frac{m_T^\Lambda}{m_T^D} \right) e^{-(m^\Lambda - m^D)/T_c} \tau \mu_2$$

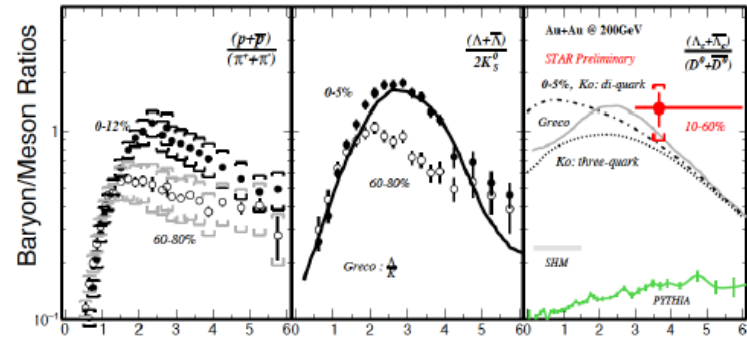
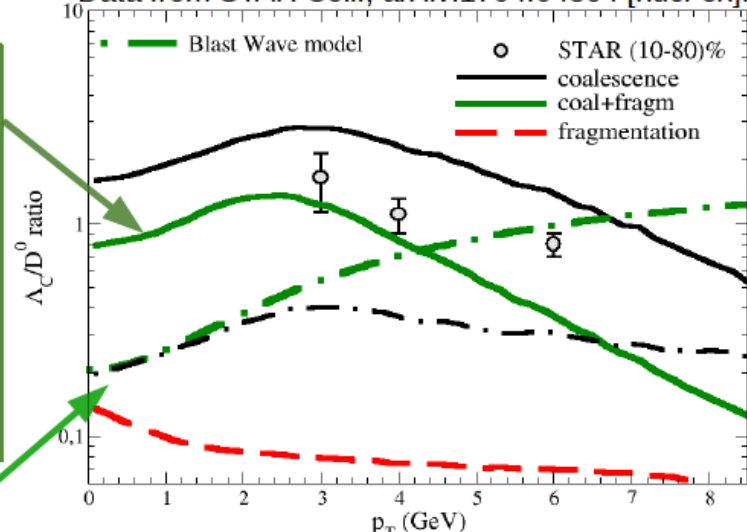
$$\mu_2 = \frac{m_3(m_1 + m_2)}{m_1 + m_2 + m_3} \quad \text{Is the reduced mass of the baryon}$$

## Blast Wave model:

$$\frac{\Lambda_c^+}{D^0} = \frac{g_\Lambda}{g_D} \frac{m_T^\Lambda}{m_T^D} \frac{K_1(m_T^\Lambda/T_c)}{K_1(m_T^D/T_c)}$$

$$\text{for } p_T \ll m \quad \approx \frac{g_\Lambda}{g_D} \left( \frac{m_T^\Lambda}{m_T^D} \right)^{1/2} e^{-(m^\Lambda - m^D)/T_c} \approx 0.17$$

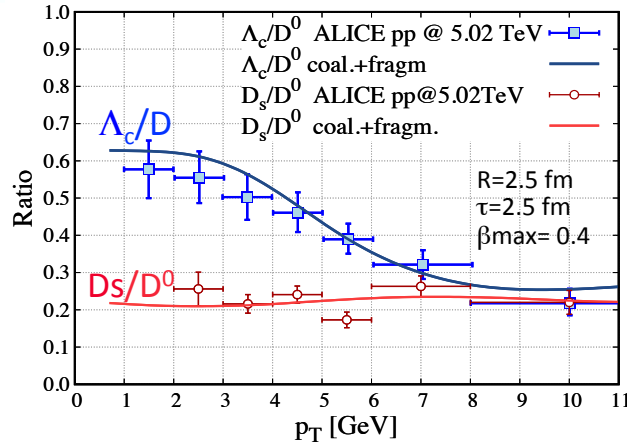
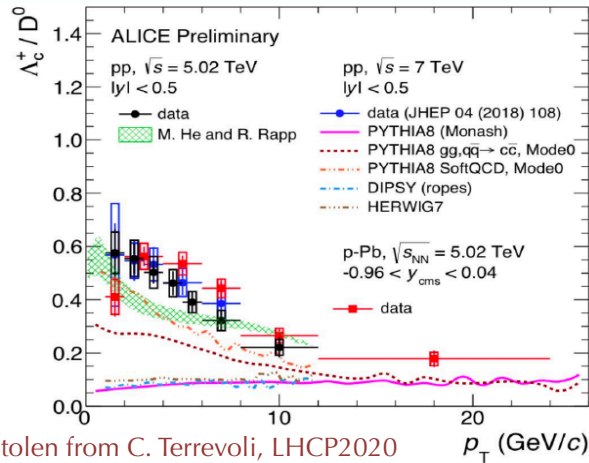
Data from STAR Coll., arXiv:1704.04364 [nucl-ex].



X. Dong and V. Greco., Prog.Part.Nucl. Phys. (2018)



# Heavy Baryon hadronization $\Lambda_c$ in pp



Same Coalescence+fragm as for AA

assuming a pp hydro fireball

M. Habich et al., EPJ. C76 (2016)

naturally explain the ratio in pp:  
- smaller but non-zero radial flow  
Charm baryon from PDG ...

Stolen from C. Terrevoli, LHCP2020

HE-Rapp, RQM  $\gg$  PDG important to assess SHM production  $p \rightarrow 0$

❖ Possibility to have a coherent hadronization scheme from pp to AA

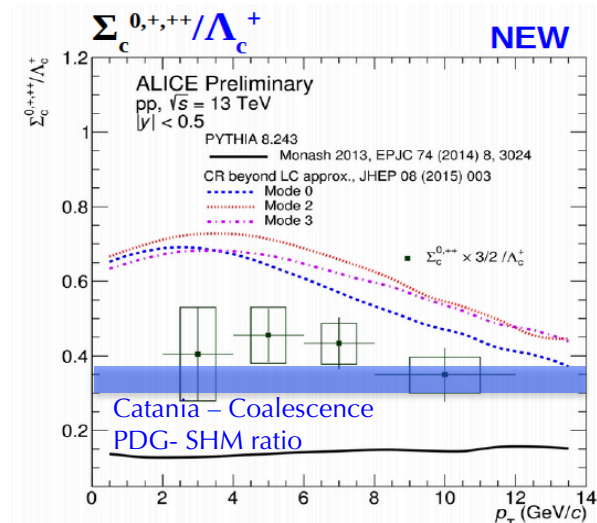
- New CR can also describe it in pp

but there is much more to study:

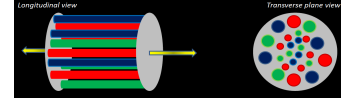
- vs  $dN_{ch}/dh$  with new exp. Data

- vs **internal chemistry**, resonance feeddown

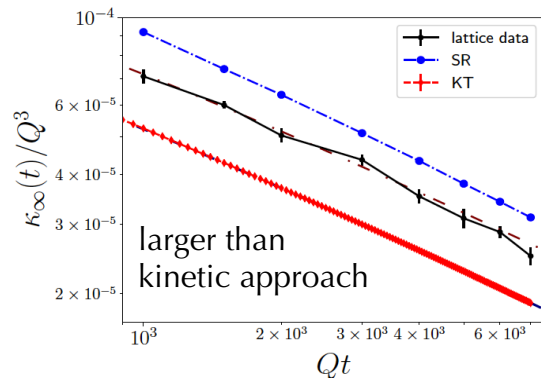
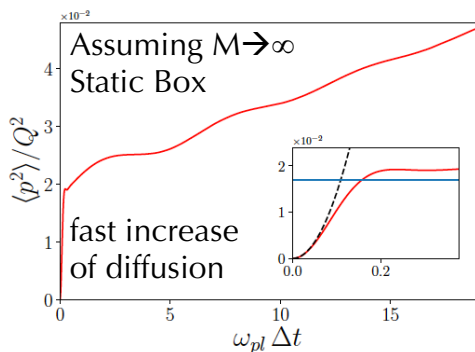
C.Hills, Wed 10.30



# Impact of Glasma on HQ



K. Boguslavski, A. Kurkela, T. Lappi and J. Peuron, arXiv:2005.02418

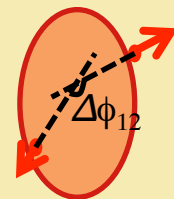


## Correlator method

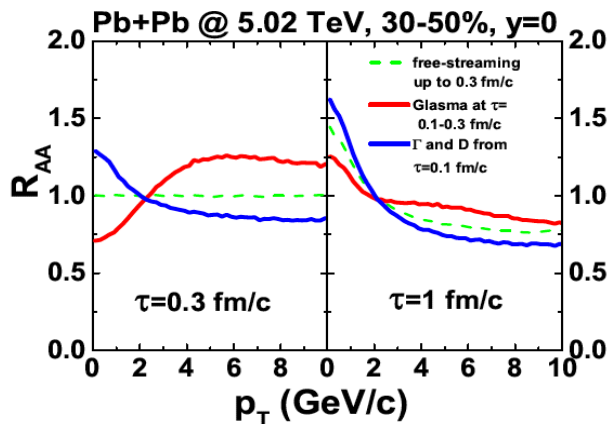
$$\langle \dot{p}_i(t) \dot{p}_i(t') \rangle = \frac{g^2}{2N_c} \langle E_i^a(t) E_i^a(t') \rangle \quad 3\kappa(t, \Delta t) \equiv \frac{d}{d\Delta t} \langle p^2(t, \Delta t) \rangle$$

## Link pA $\leftrightarrow$ AA

Using HQ as a probe of the Glasma  
 $\rightarrow$  May have key role for  
 D-D angular correlation

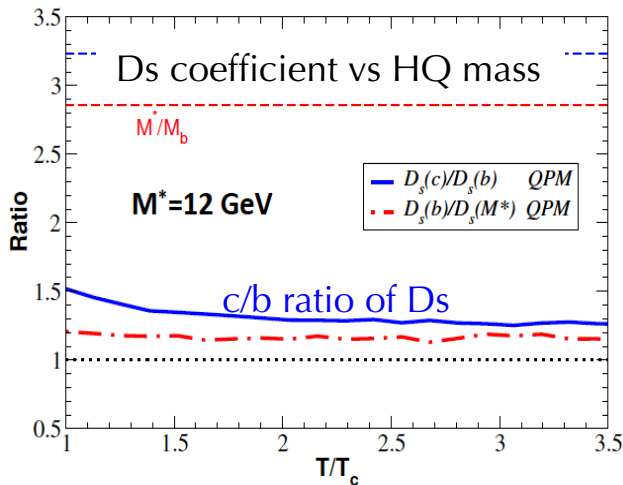


## Impact on AA collisions observables (interacting at $\tau = \tau_{\text{form}}$ )



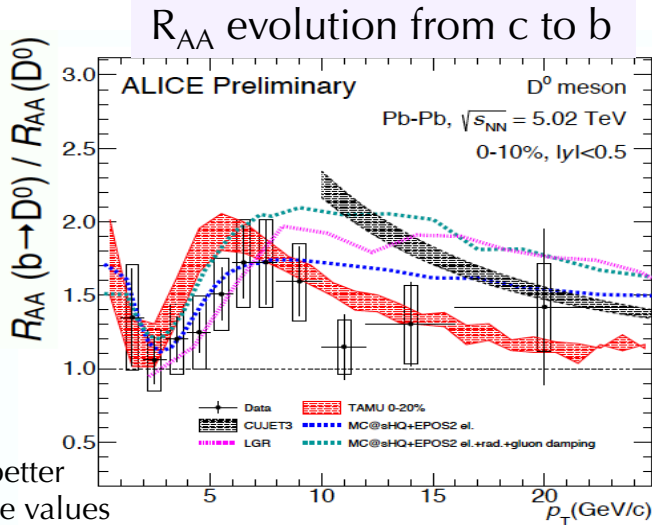
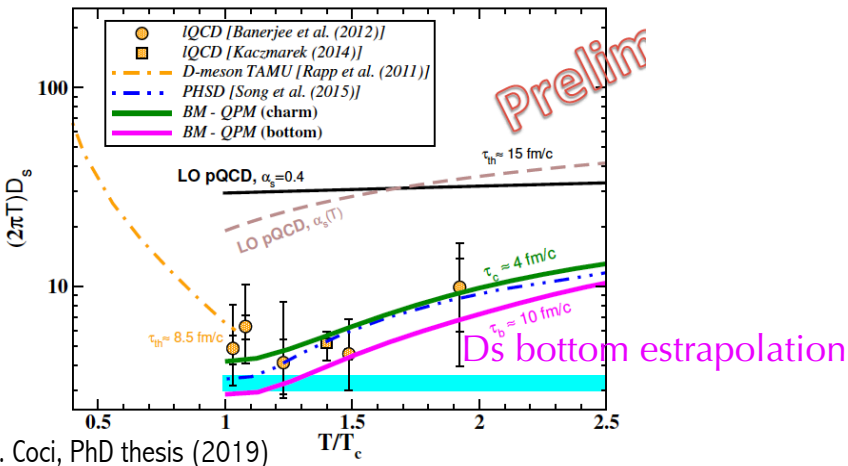
- ❖ Dominance of diffusion-like  $\rightarrow$  enhancement of  $R_{AA}(p_T)$
- ❖ Gain in  $v_2$ : larger interaction in QGP stage to have same  $R_{AA}(p_T)$

# What changes from c to b ? Large mass limit?



Kinetic th. (same interact.):  $\tau_{th}(b)/\tau_{th}(c) \approx \gamma_b/\gamma_c \approx M_b/M_c$  and  $D_s = \frac{T}{M\gamma} = \frac{T}{M} \tau_{th}$   
 $\rightarrow D_s$  ideally M independent ( $M \rightarrow \infty$ )

- ✧  $D_s$  in QPM approach is 30-40% smaller for bottom
- ✧  $M \rightarrow \infty$  limit is not reached for charm
- ✧ Start having similar plots from all the models...



TAMU w/o rad.  $E_{loss}$  - better likely miss the absolute values

# Relativistic Boltzmann at finite $\eta/s$

$$p^\mu \partial_\mu f_q(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_q(x, p) = C[f_q, f_g] \quad \text{Equivalent to}$$

$$p^\mu \partial_\mu f_g(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_g(x, p) = C[f_q, f_g] \quad \text{viscous hydro}$$

free streaming      Interaction  $\varepsilon-3p \neq 0$        $C[f]$  gauged to some  $\eta/s \approx 0.1$

## Heavy Quarks evolution

$$p^\mu \partial_\mu f_Q(x, p) = C[f_q, f_g, f_Q](x, p)$$

$$C[f_Q] = \frac{1}{2E_1} \int \frac{d^3 p_2}{2E_2 (2\pi)^3} \int \frac{d^3 p'_1}{2E'_1 (2\pi)^3}$$

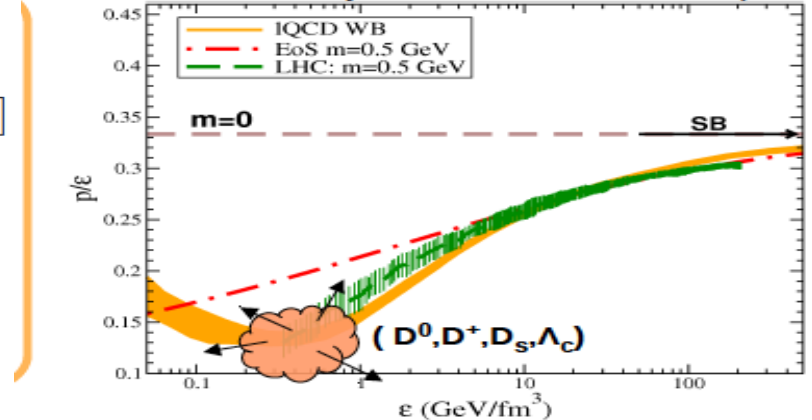
$$\times [f_Q(p'_1) f_{q,g}(p'_2) - f_Q(p_1) f_{q,g}(p_2)]$$

$$\times |\mathcal{M}_{(q,g)+Q}(p_1 p_2 \rightarrow p'_1 p'_2)|^2$$

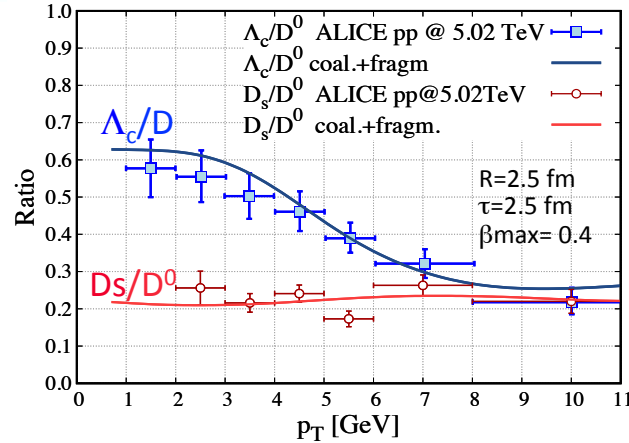
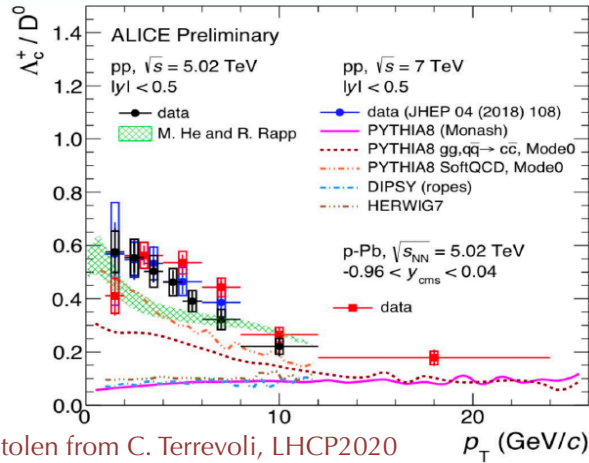
$$\times (2\pi)^4 \delta^4(p_1 + p_2 - p'_1 - p'_2),$$

$\mathcal{M}$  scattering matrix by QPM model  
fit to IQCD thermodynamics

S. Plumari et al., J.Phys.Conf.Ser. 981 012017 (2018).



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assuming a pp hydro fireball

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naturally explain the ratio in pp:  
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Charm baryon from PDG ...

V. Minissaleet al., in preparation

Stolen from C. Terrevoli, LHCP2020

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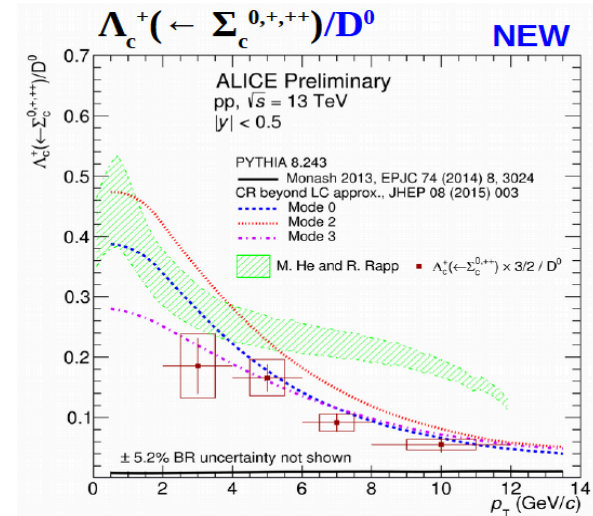
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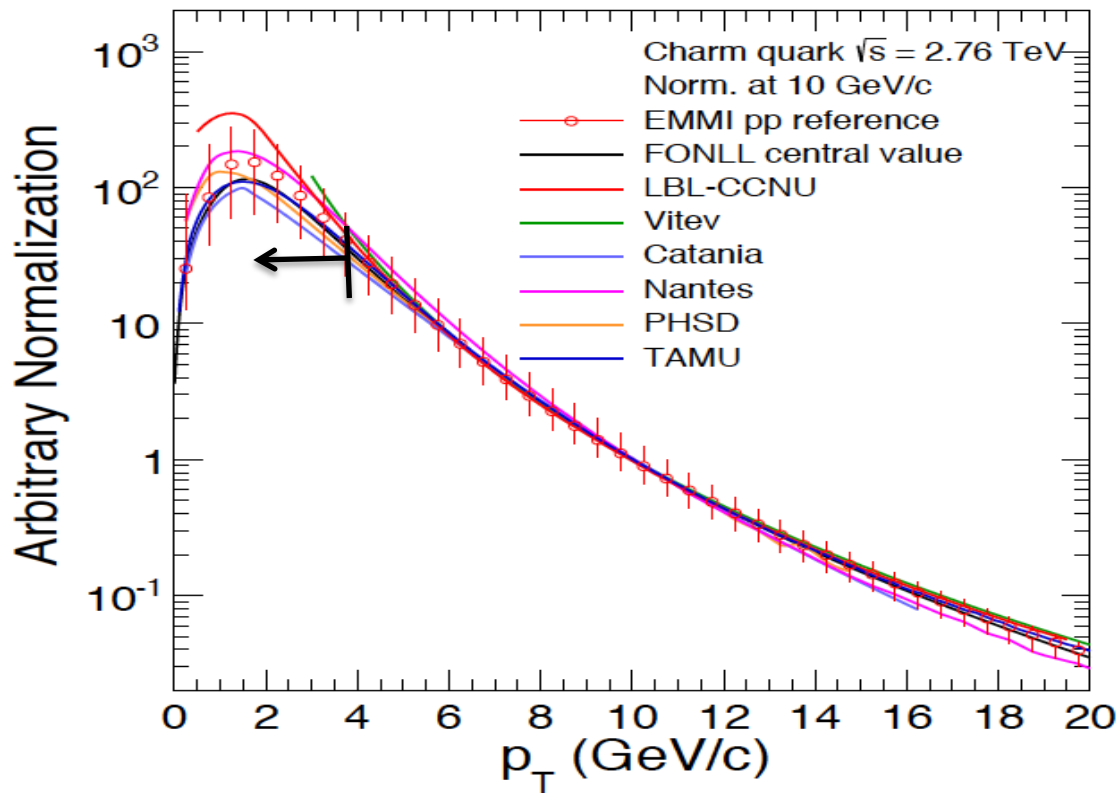
- vs  $dN_{ch}/dh$  with new exp. Data

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C.Hills, Wed 10.30



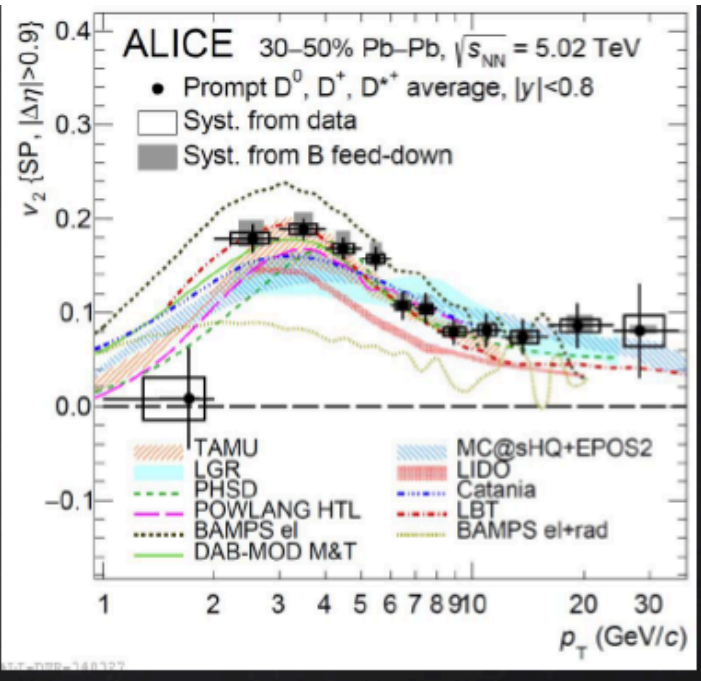
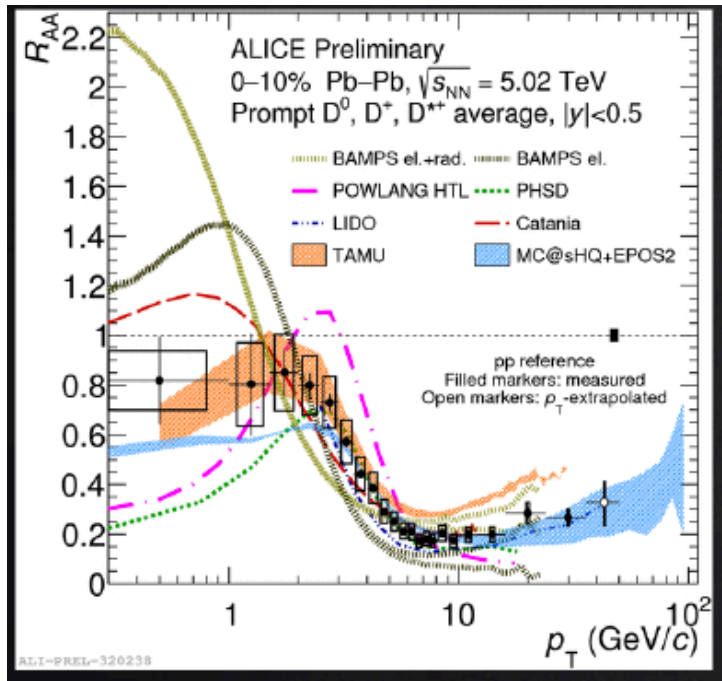
# Initial Charm distribution from various groups

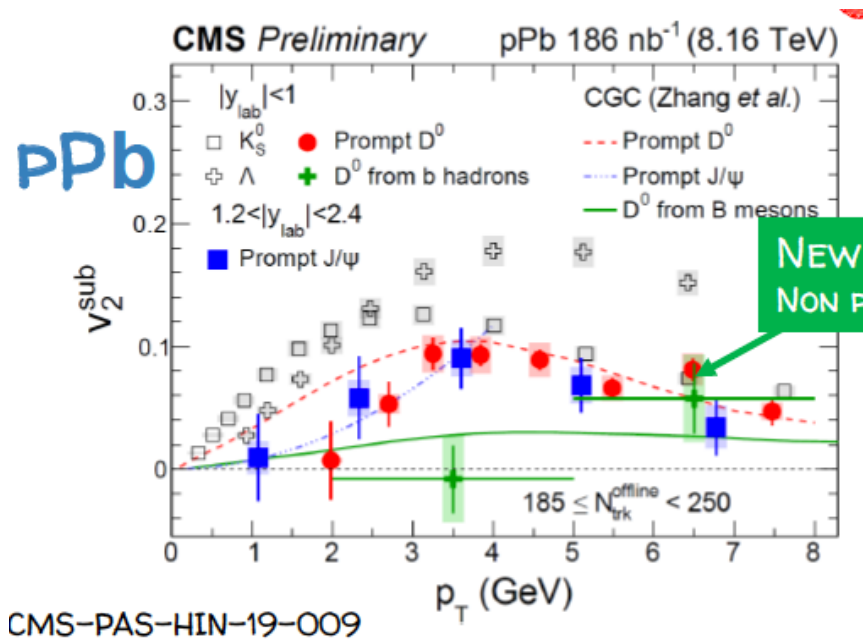
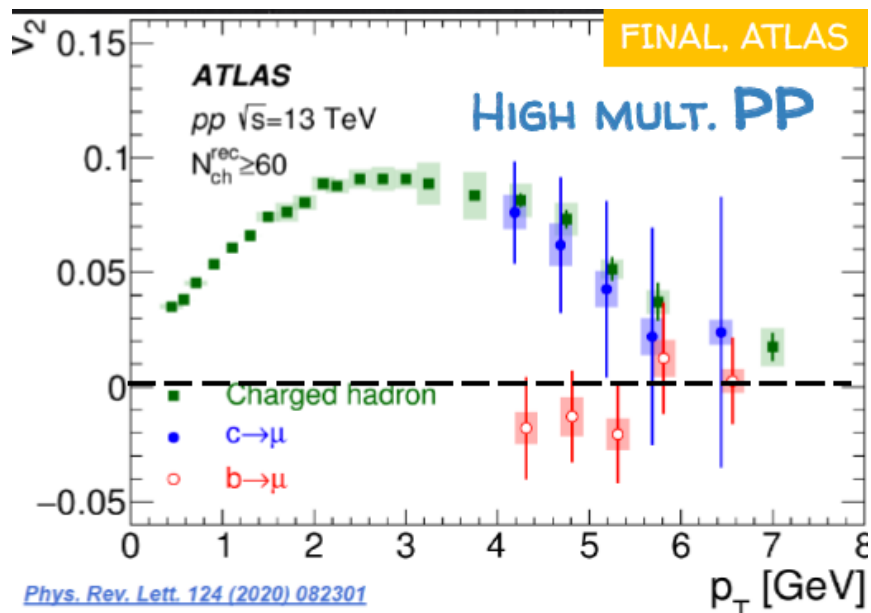


EMMI-RRTF Collab., ArXiv:1803.03824  
NPA979(2018)

Still to our purpose ( $R_{AA}$  at  $p_T < 4-5$  GeV)

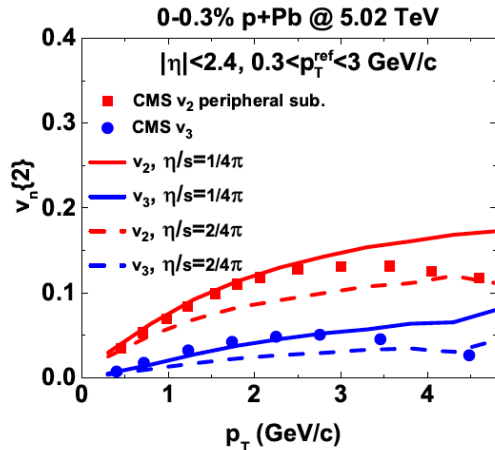
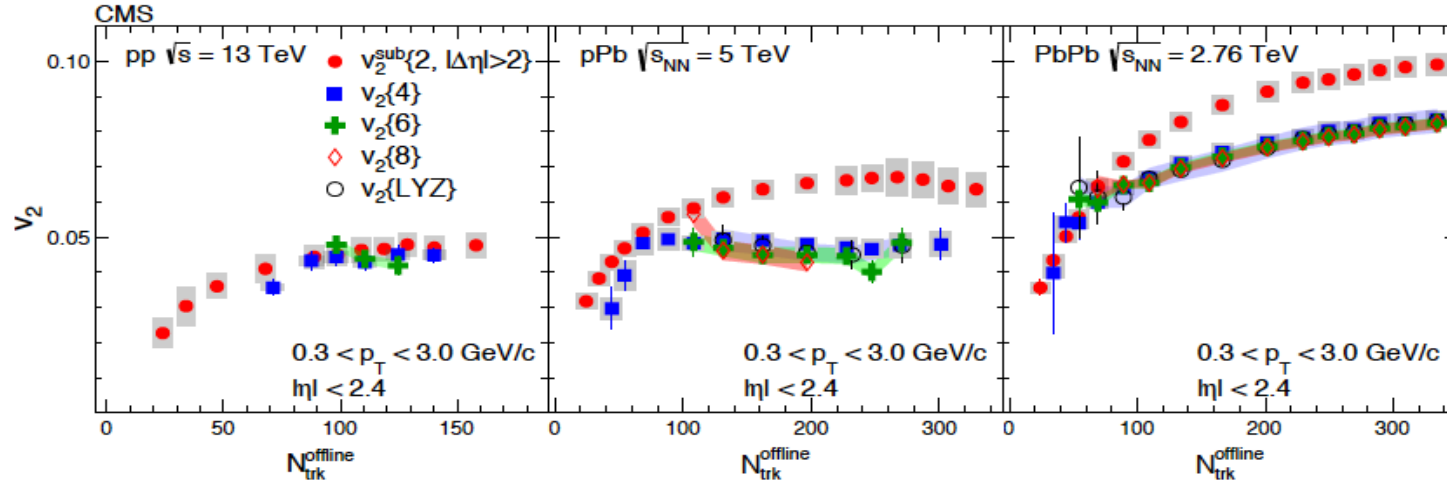
The best would be good precision data at low  $p_T$







# Collective flow in pp, pA and AA



Prediction by a Relativistic Boltzmann approach applied to pA