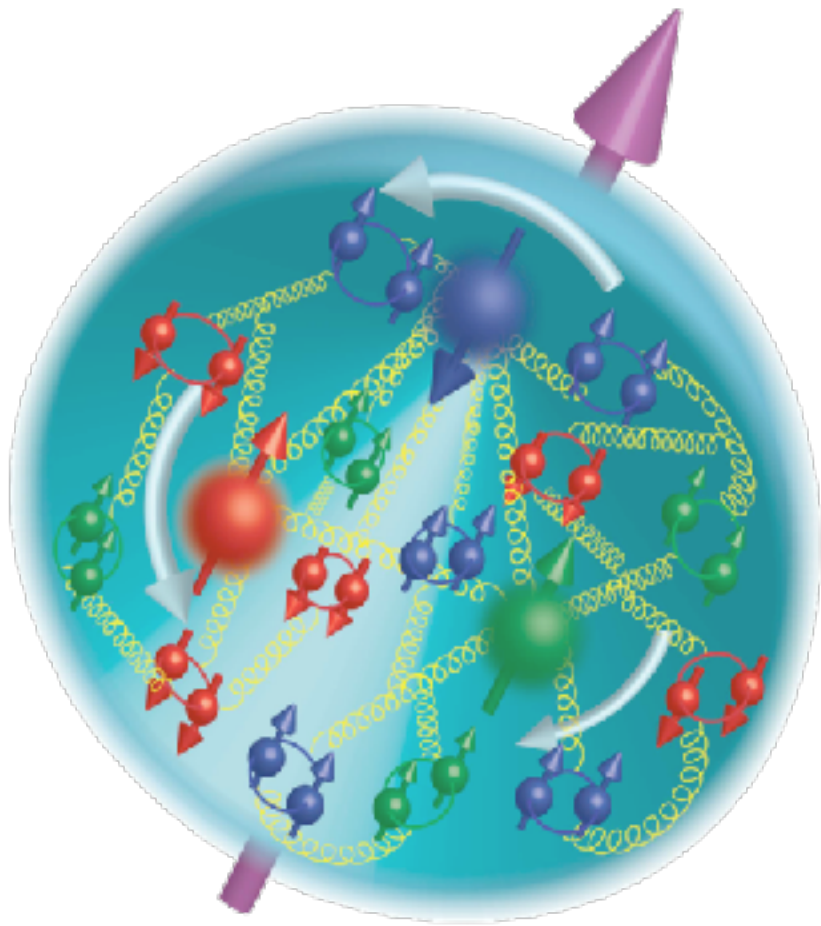


# REGIONS IN SIDIS

Alexei Prokudin



In collaboration with: M. Boglione, M. Diefenthaler, S. Dolan,  
L. Gamberg, S. Gordon, W. Melnitchouk, D. Pitonyak,  
T. Rogers, N. Sato

# SEMI INCLUSIVE DEEP INELASTIC SCATTERING

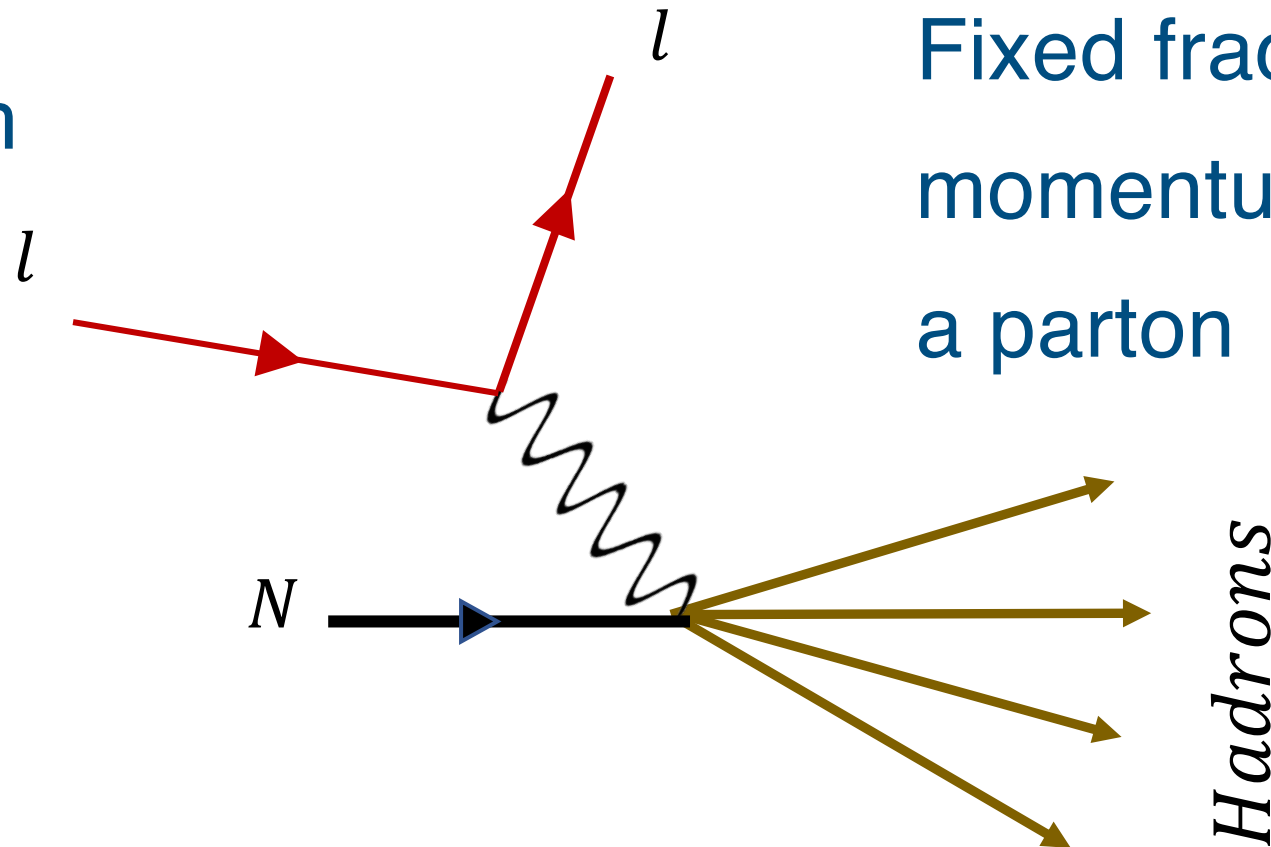
Consider electron - hadron collisions in DIS regime

$$Q^2 \rightarrow \infty$$

Transverse  
resolution  $< 1$  fm

$$x_{Bj} = \frac{Q^2}{2P \cdot q} = \text{const}$$

Fixed fraction of  
momentum carried by  
a parton



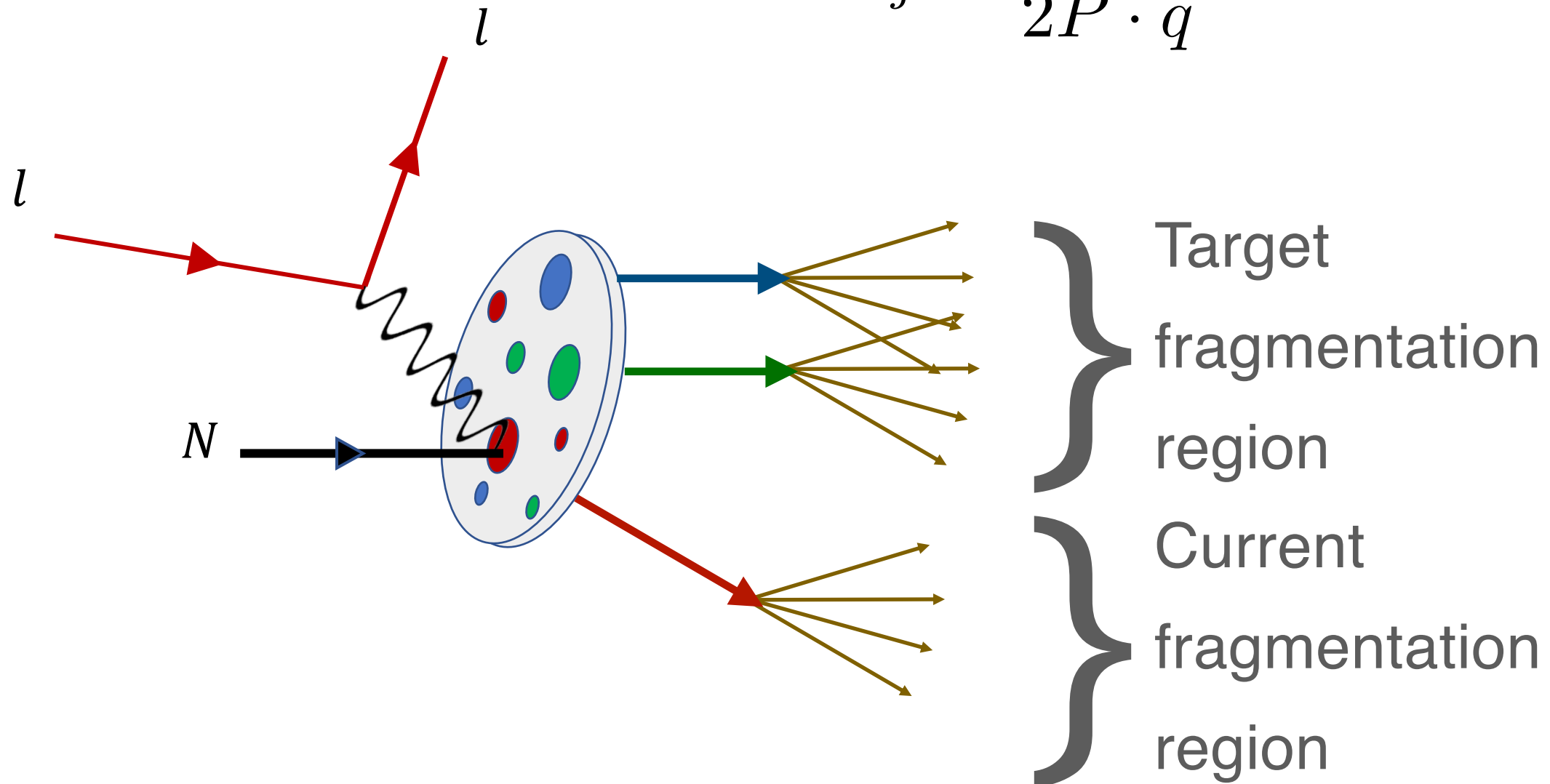
Detect a pion in the final state

# SEMI INCLUSIVE DEEP INELASTIC SCATTERING

.....  
Consider electron - hadron collisions in DIS regime

$$Q^2 \rightarrow \infty$$

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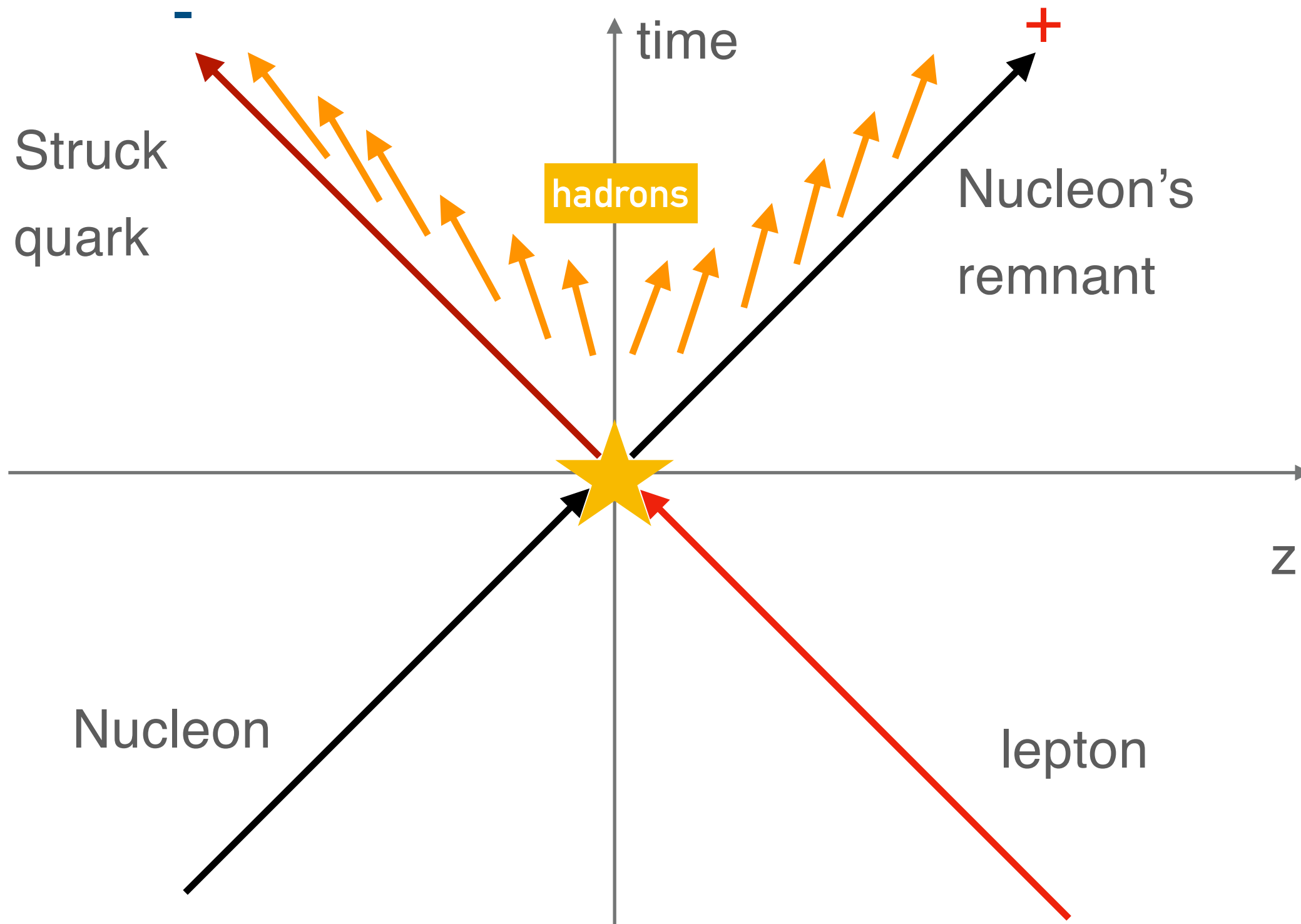


Detect a pion in the final state



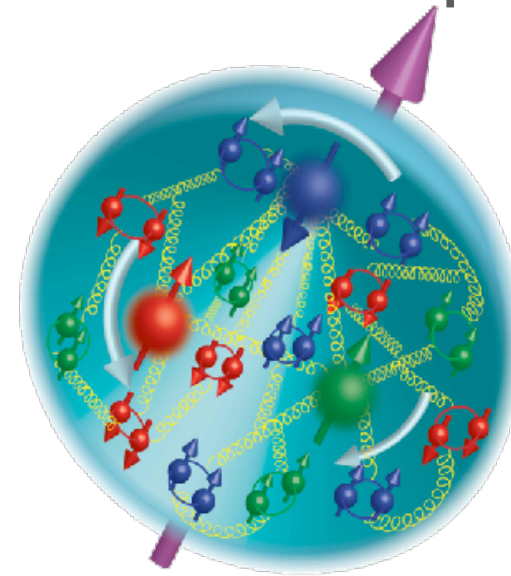
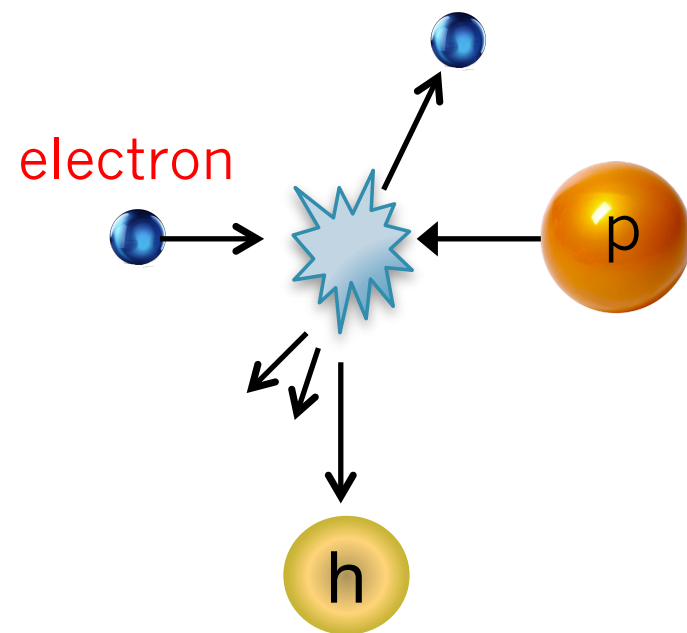
# SPACE-TIME PICTURE OF THE COLLISION

---



# QCD FACTORIZATION IS THE KEY!

We need a probe to “see” quarks and gluons



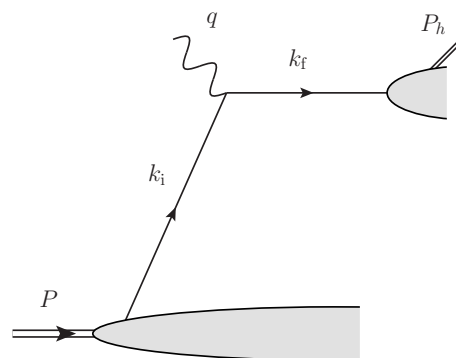
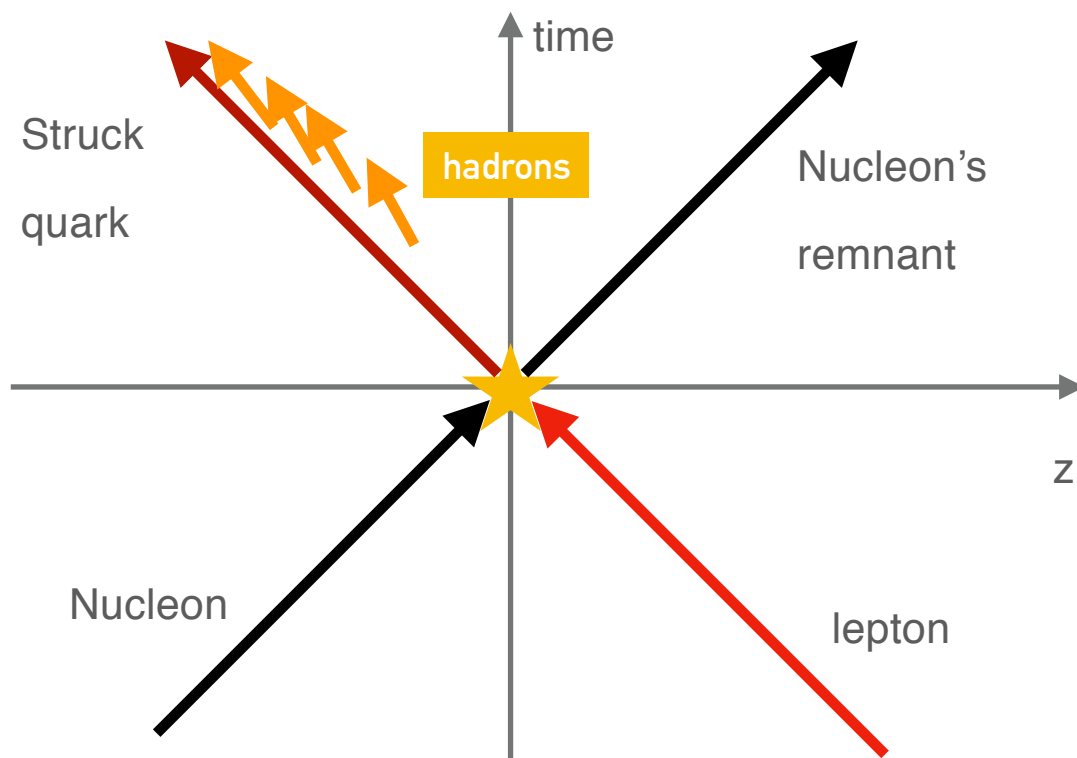
$$\sigma \approx \text{[Diagram of electron-proton interaction]} \otimes \text{[Diagram of proton structure]} + \mathcal{O}\left(\frac{M^2}{Q^2}\right)$$

Factorization      Probe      Structure      Power corrections

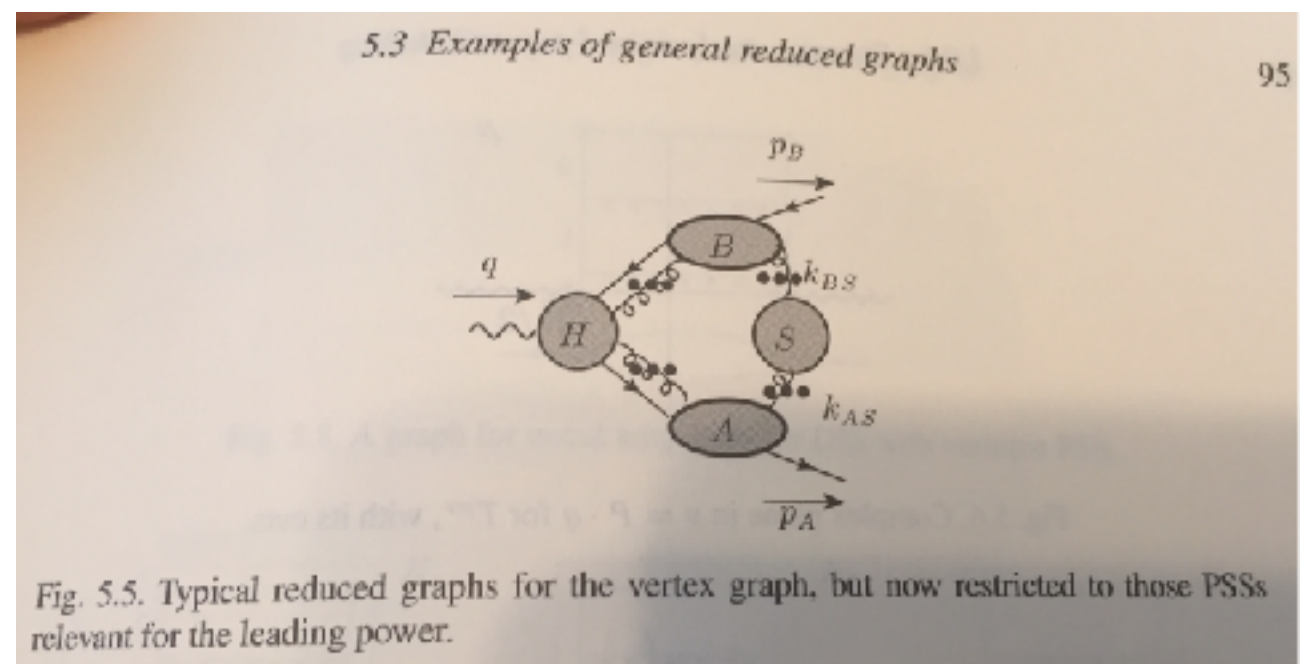
# CURRENT REGION FACTORIZATION

$$\sigma \sim \sigma_0 f_{q/N}(x_{Bj}) \otimes D_{q/h}(z_h)$$

- Libby-Sterman analysis (Collins 2011 Ch.5) suggests that classical trajectories dominate
- Produced hadrons are close in rapidity to the fragmenting quark



Boglione et al, 1611.10329



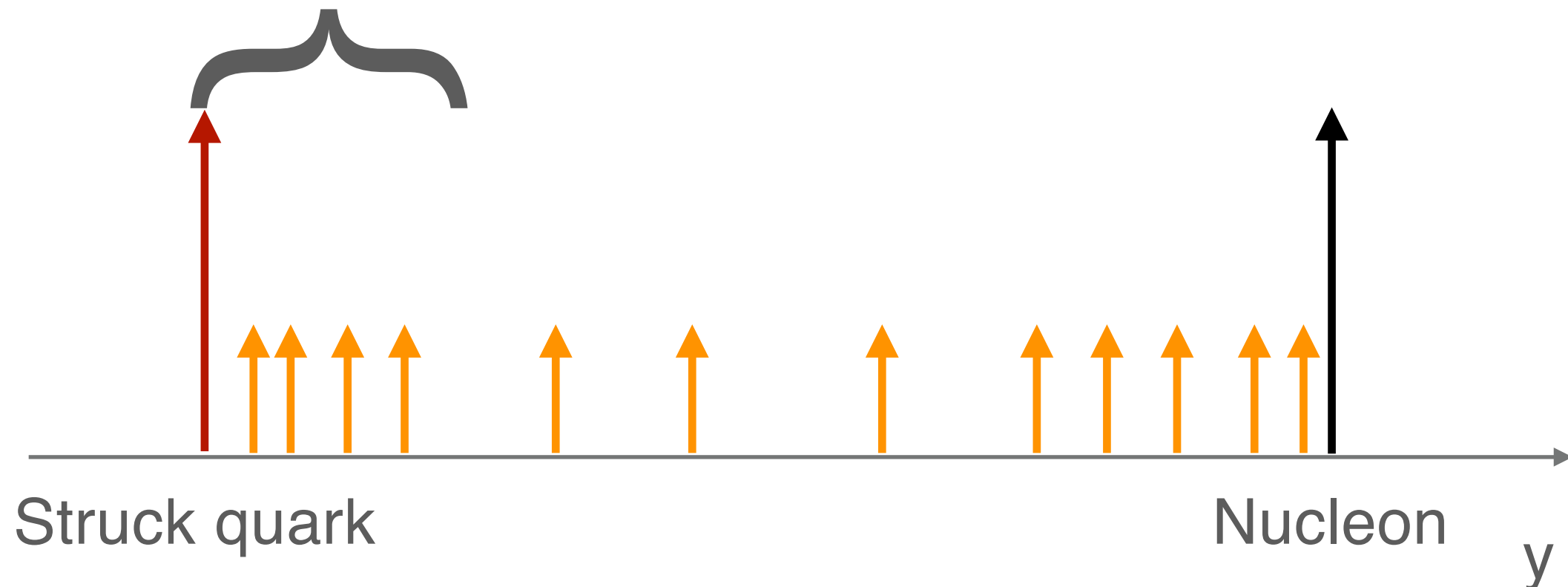
Example of pinch-singular surfaces for e+e-

# CURRENT REGION FACTORIZATION

$$\sigma \sim \sigma_0 f_{q/N}(x_{Bj}) \otimes D_{q/h}(z_h) \quad \text{Rapidity of the hadron is important}$$

$$y = \frac{1}{2} \ln \left| \frac{V^+}{V^-} \right|, \quad V = \left[ \frac{M_T}{\sqrt{2}} e^y, \frac{M_T}{\sqrt{2}} e^{-y}, \mathbf{V}_T \right], \quad M_T = \sqrt{M^2 + \mathbf{V}_T^2}$$

Current fragmentation region



# CURRENT REGION FACTORIZATION

Berger “back of the envelope” criterium is a popular choice

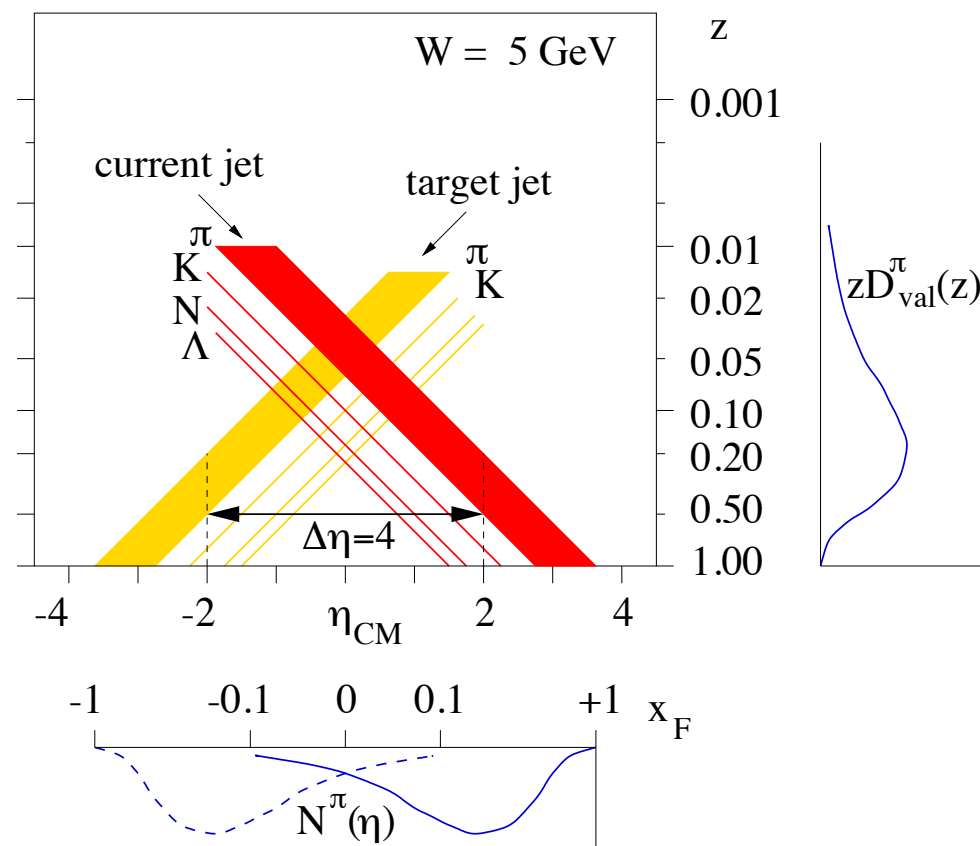
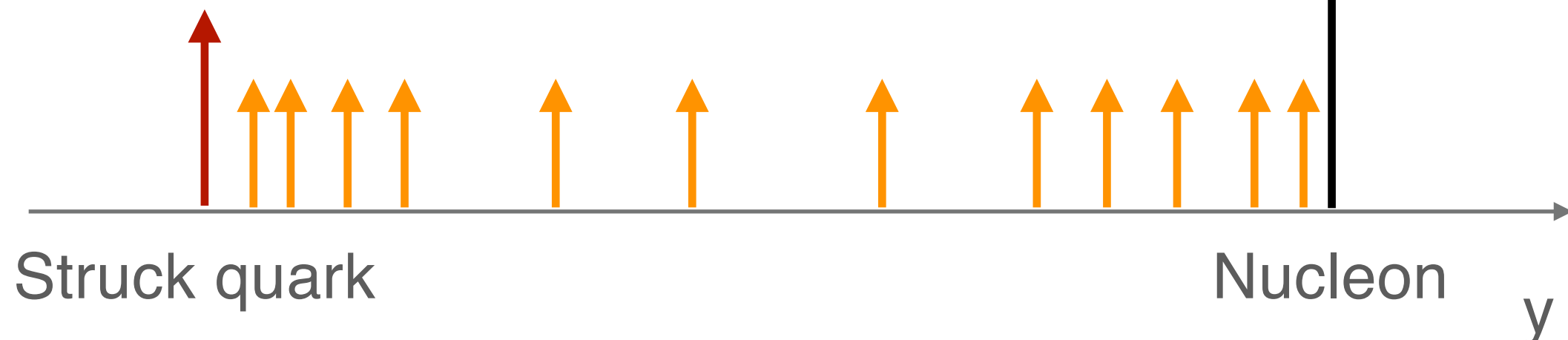


FIGURE 2. Relation between  $z$  - values in fragmentation and CM rapidity for  $W = 5$  GeV.

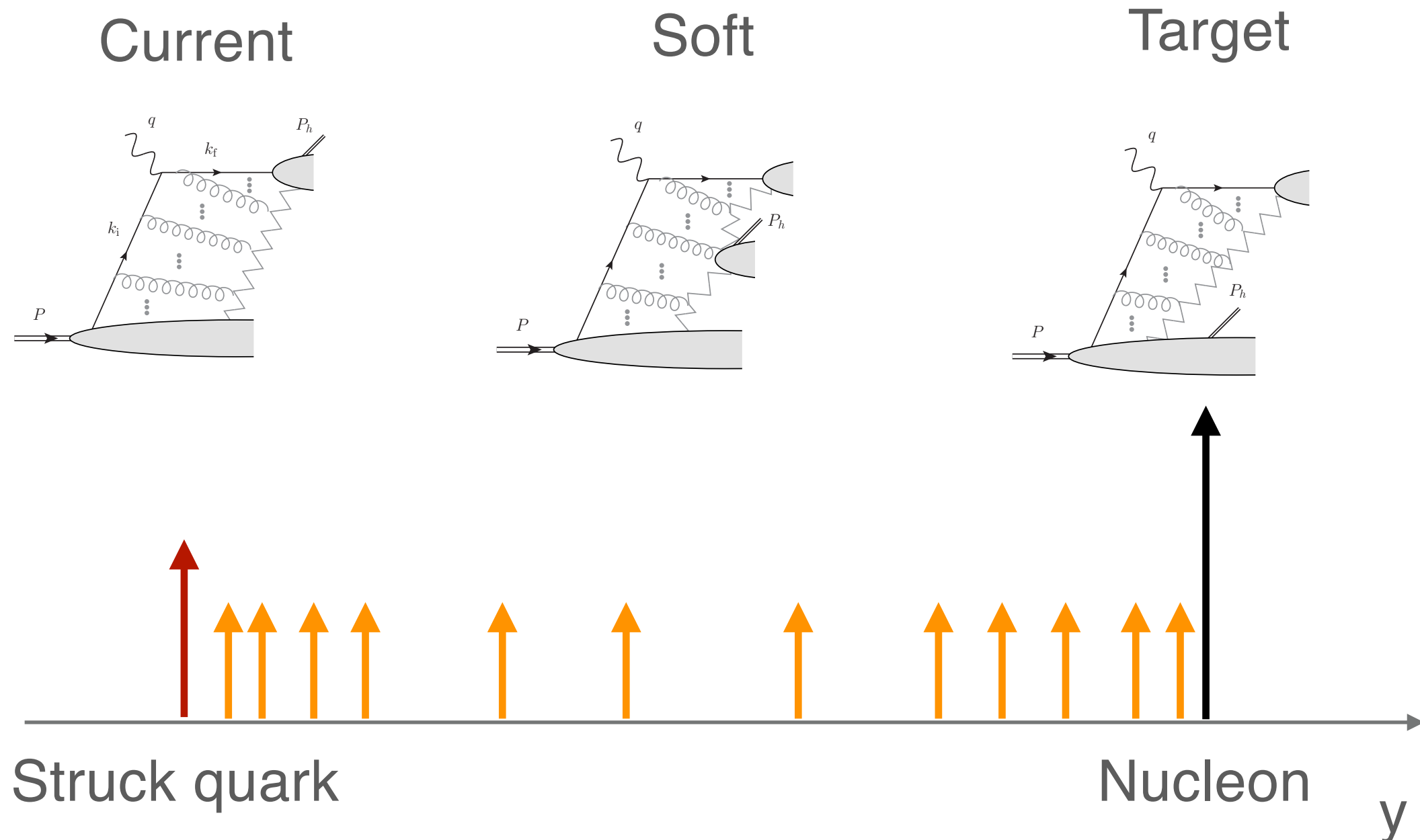


- Berger, '87, Mulders, 001.0199
- Keep rapidity separation
  - Keep  $z_h$  large enough

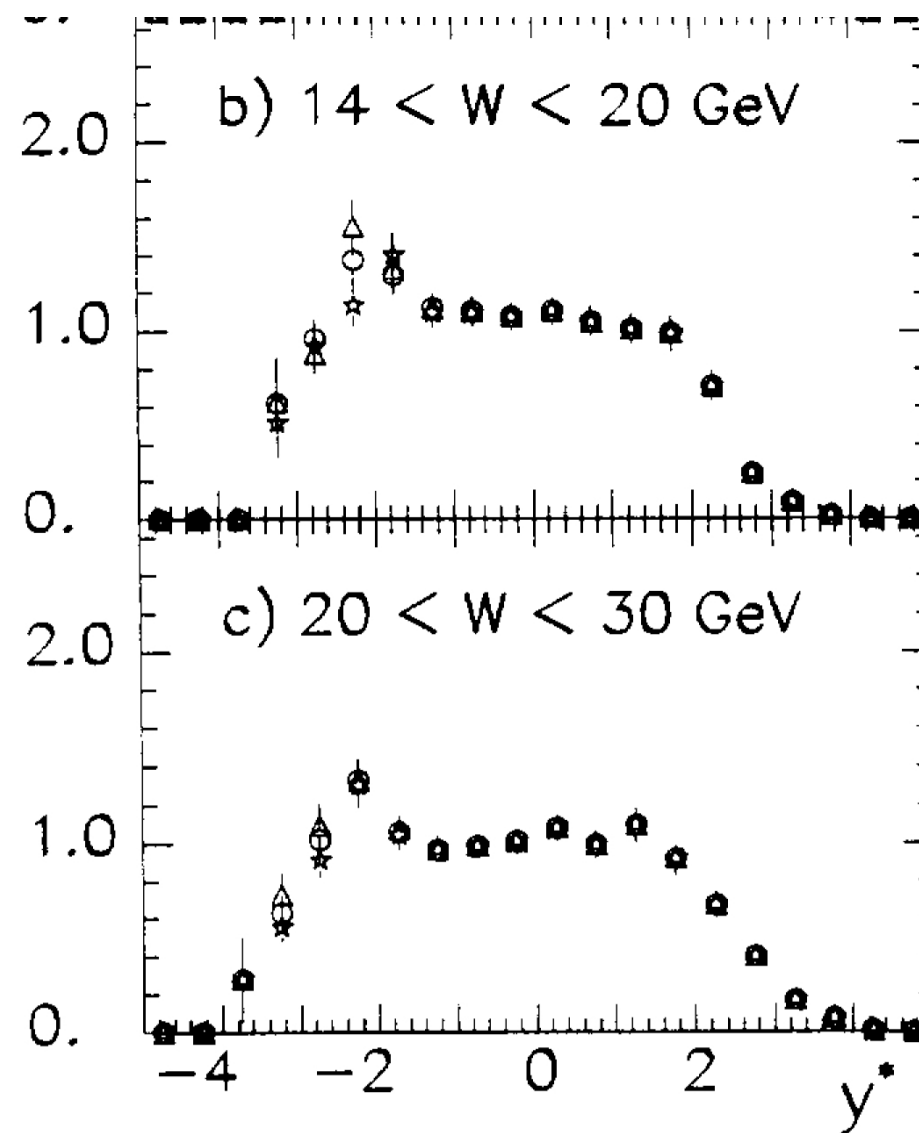
# CURRENT REGION FACTORIZATION

Fresh look:

Define ratios of kinematical variables and identify regions



# CURRENT REGION FACTORIZATION



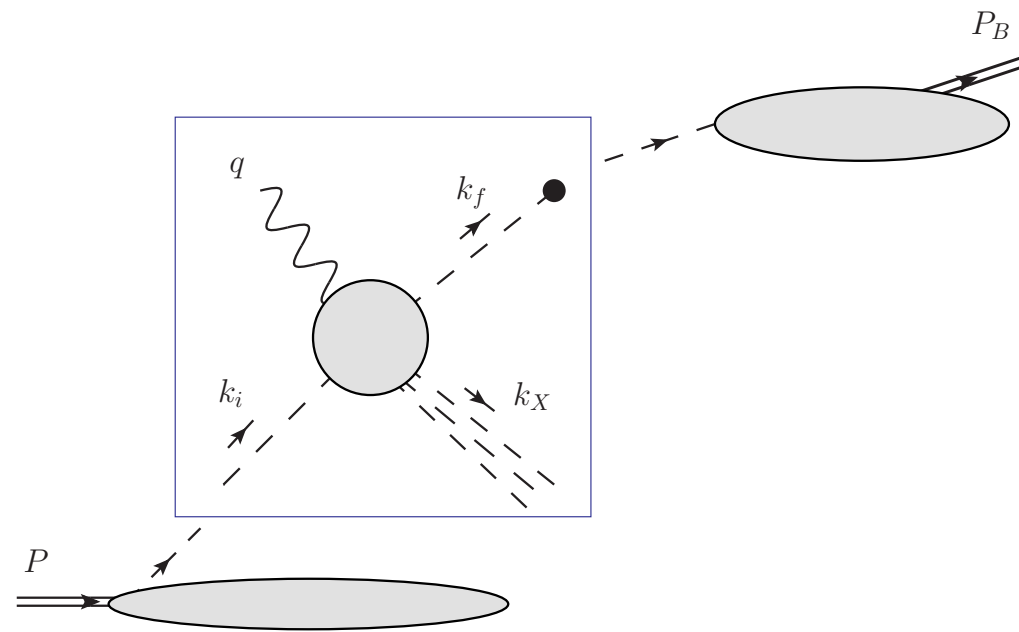
- E665 data rapidity distribution
- From S. Joosten Ph.D. thesis

Figure 8.1: Normalized CM-rapidity distribution of positive hadrons in three bins of  $W$  from  $\mu\text{Xe}$ -scattering at E665. The different markers refer to variants of the PID procedure not relevant to the current discussion. The target jet (negative rapidity) and current jet (positive rapidity) are hard to distinguish from each other due large amount of additional hadrons filling the gap between both jets. The situation becomes slightly better at higher values of  $W$ . See also Fig. 8.2. Figure from [139].

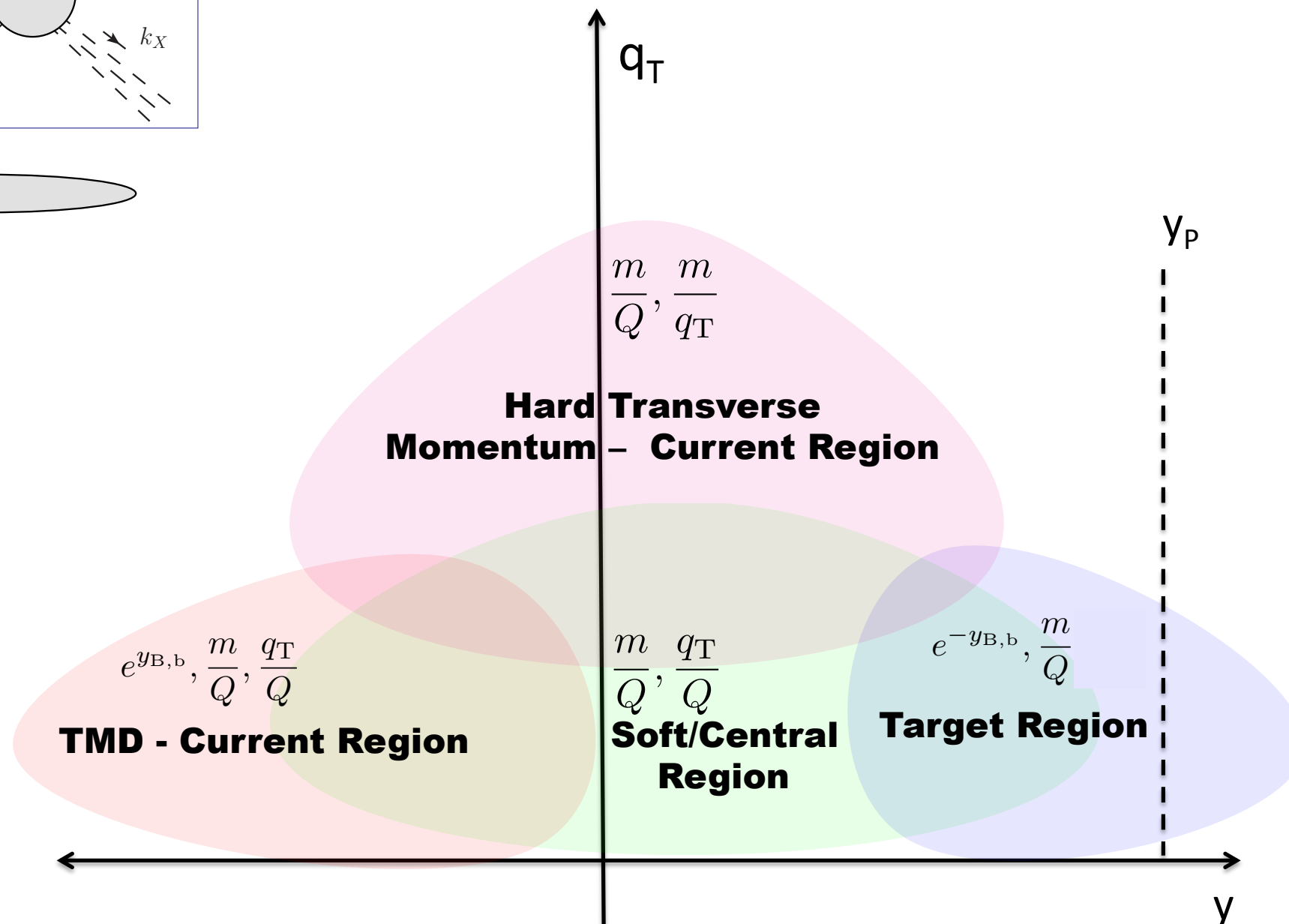
# REGIONS IN SIDIS AND RATIOS

Boglione et al, 1611.10329

Boglione et al, 1904.12882

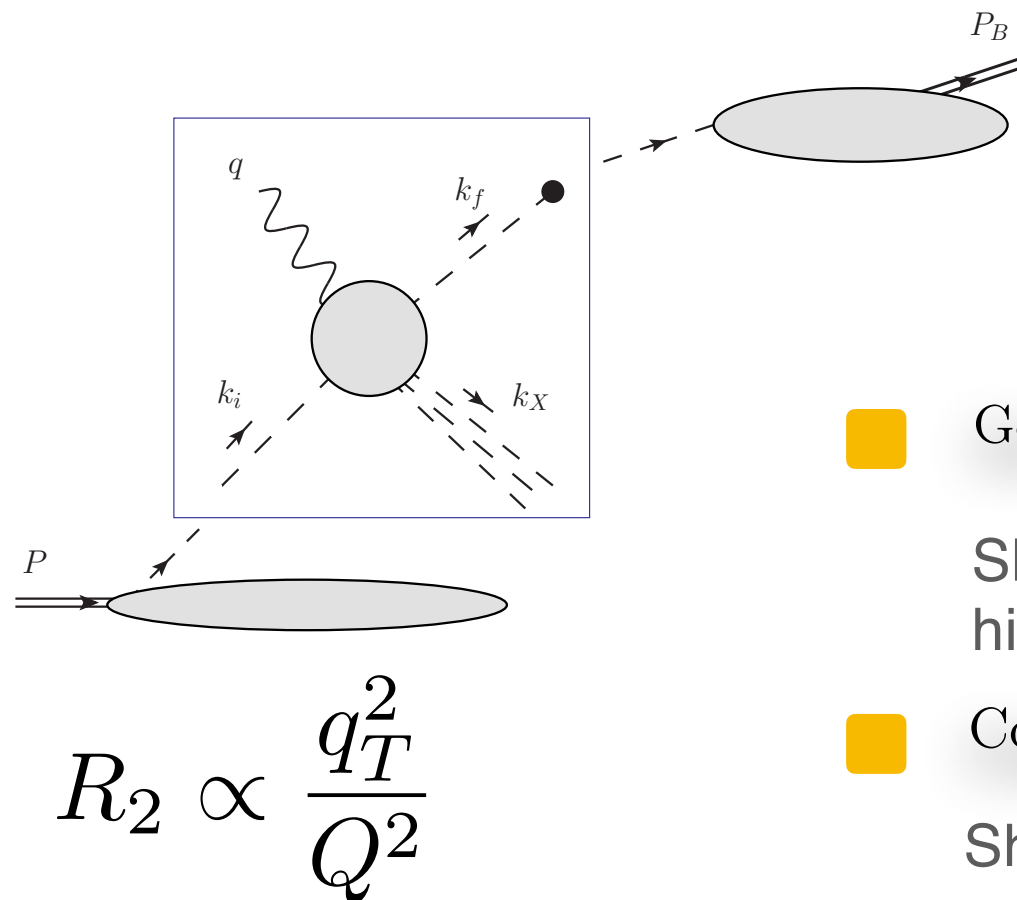


- Define ratios
- Identify regions





# REGIONS IN SIDIS AND RATIOS



- Define ratios
- Identify regions

General Hardness Ratio =  $R_0 \equiv \max \left( \left| \frac{k_i^2}{Q^2} \right|, \left| \frac{k_f^2}{Q^2} \right|, \left| \frac{\delta k_T^2}{Q^2} \right| \right)$ .

Should be small for partonic description to hold,  
high off-shellness = short distance

Collinearity =  $R_1 \equiv \frac{P_B \cdot k_f}{P_B \cdot k_i}$ ,

Should be small for current region, large for target region

Used already in  
phenomenology

Bacchetta et al, 1912.07550

Vladimirov et al, 1912.06532

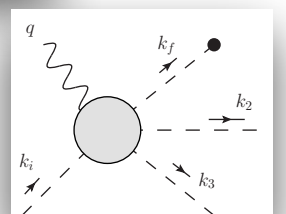
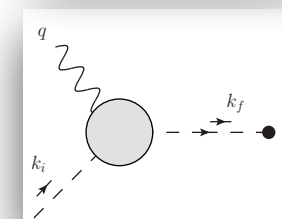
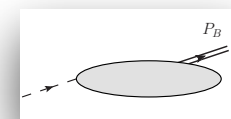
Transverse Hardness Ratio =  $R_2 \equiv \frac{|k^2|}{Q^2}$ .

$k \equiv k_f - q$ .

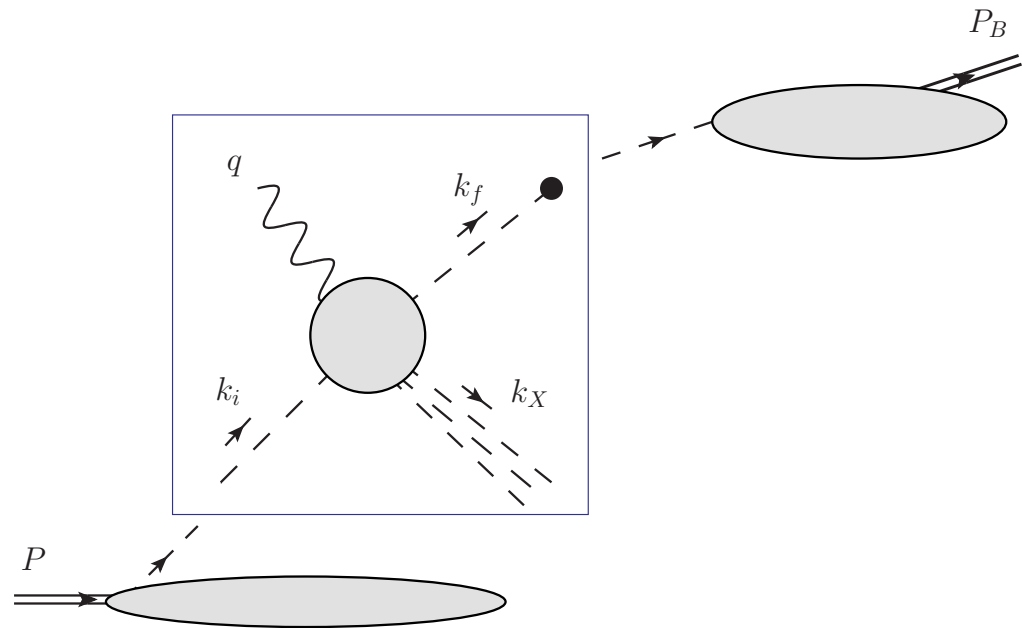
Should be small for  $2 \rightarrow 1$  process

Spectator Virtuality Ratio =  $R_3 \equiv \frac{|k_X^2|}{Q^2}$ .

Small for lowest order QCD to be applicable



# REGIONS IN SIDIS AND RATIOS



- Define ratios
- Identify regions

	$R_0$	$R_1$	$R_2$	$R_3$
TMD Current region	small	small	small	X
Hard region	small	small	large	small (low order pQCD)
	small	small	large	large (high order pQCD)
Target region	small	large	X	X
Soft region	small	large	small	X

**Table 1:** Examples for sizes of ratios corresponding to particular regions of SIDIS. The “X” means “irrelevant or ill-defined.” This ranking should be viewed as schematic since “small” and “large” need to be defined quantitatively and can in general be scale-dependent.

# REGIONS IN SIDIS AND RATIOS

Boglione et al, 1611.10329  
Boglione et al, 1904.12882  
Current study

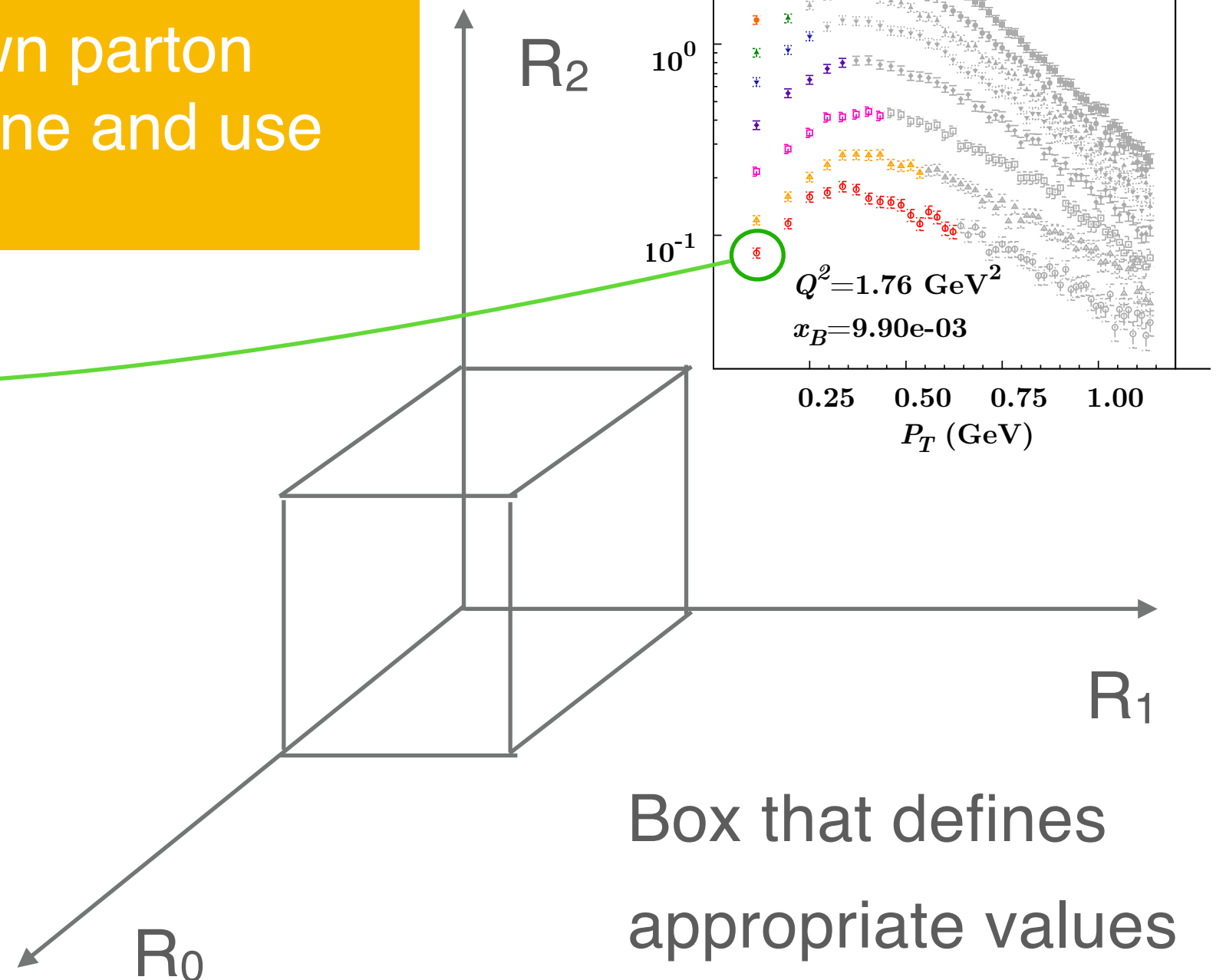
COMPASS

## ➤ Define ratios

Ratios depend on unknown parton momenta. How can we define and use them?

Where does this bin belong?

- Use a Monte Carlo\* with parton momenta
- Sample experimental bins for ratios



\* by saying Monte Carlo we do not intend Pythia!

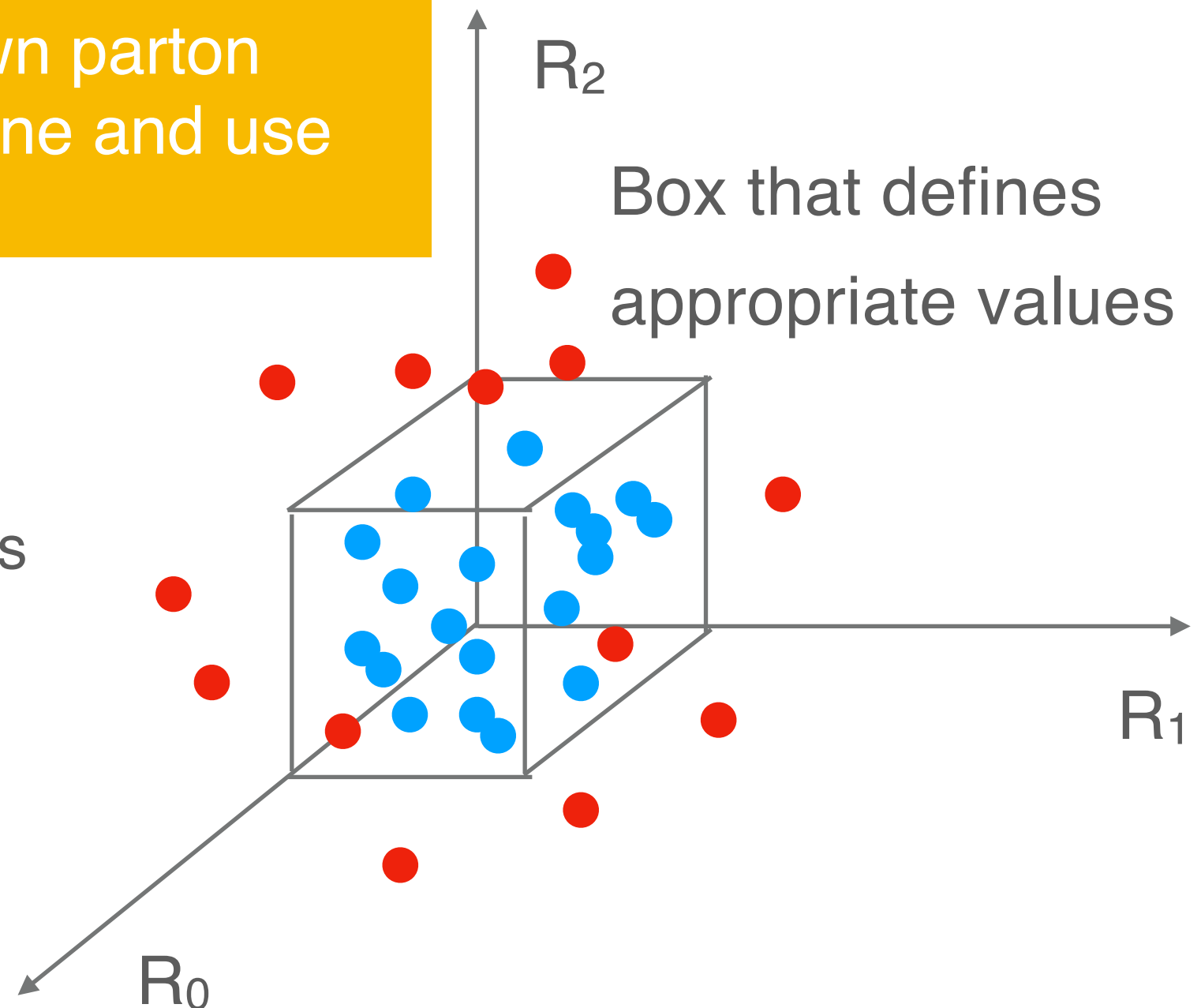
# REGIONS IN SIDIS AND RATIOS

Boglione et al, 1611.10329  
Boglione et al, 1904.12882  
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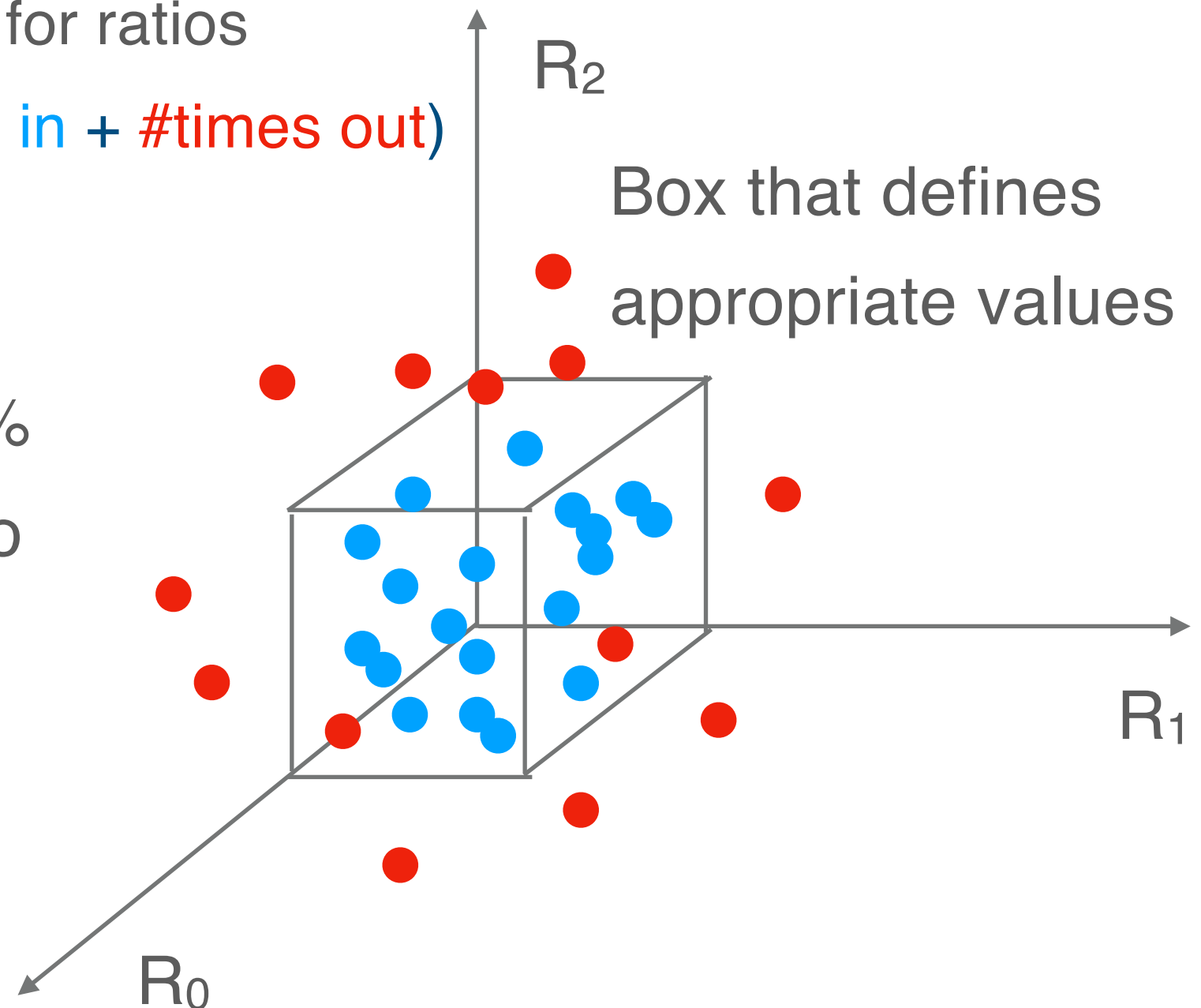
\* by saying Monte Carlo we do not intend Pythia!

# AFFINITY

Boglione et al, 1611.10329  
Boglione et al, 1904.12882  
Current study

- Use a Monte Carlo\* with parton momenta
- Sample experimental bins for ratios
- Affinity =  $\frac{\text{\#times in}}{\text{\#times in} + \text{\#times out}}$

Affinity is from 0% to 100%  
indicates affinity of a bin to  
a particular region



\* by saying Monte Carlo we do not intend Pythia!

# AFFINITY

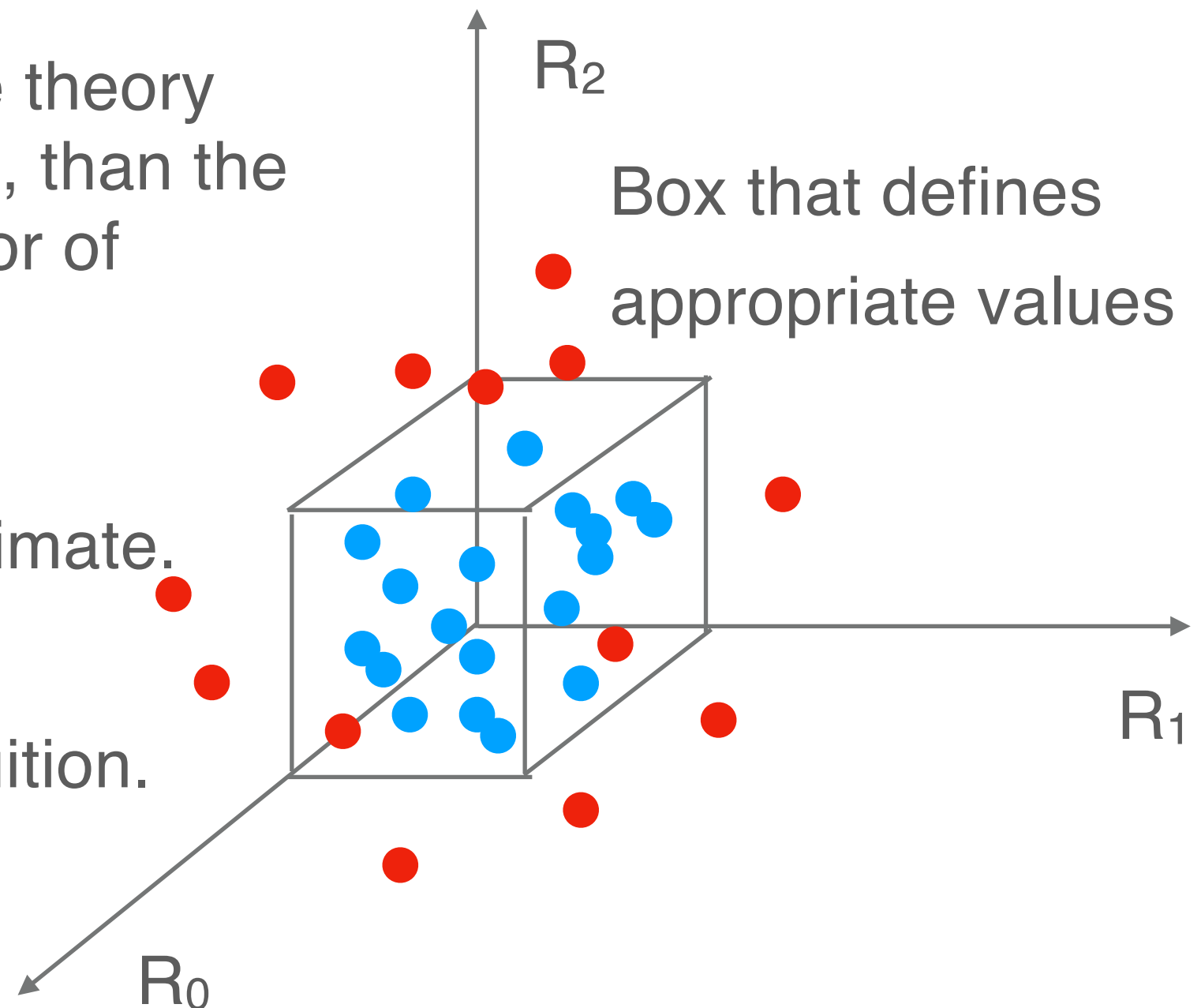
Boglione et al, 1611.10329  
Boglione et al, 1904.12882  
Current study

## ➤ What about size of the box?

If rigorous expansion of the theory in terms of  $R$ s is performed, than the size is  $\sim$  to the relative error of factorization.

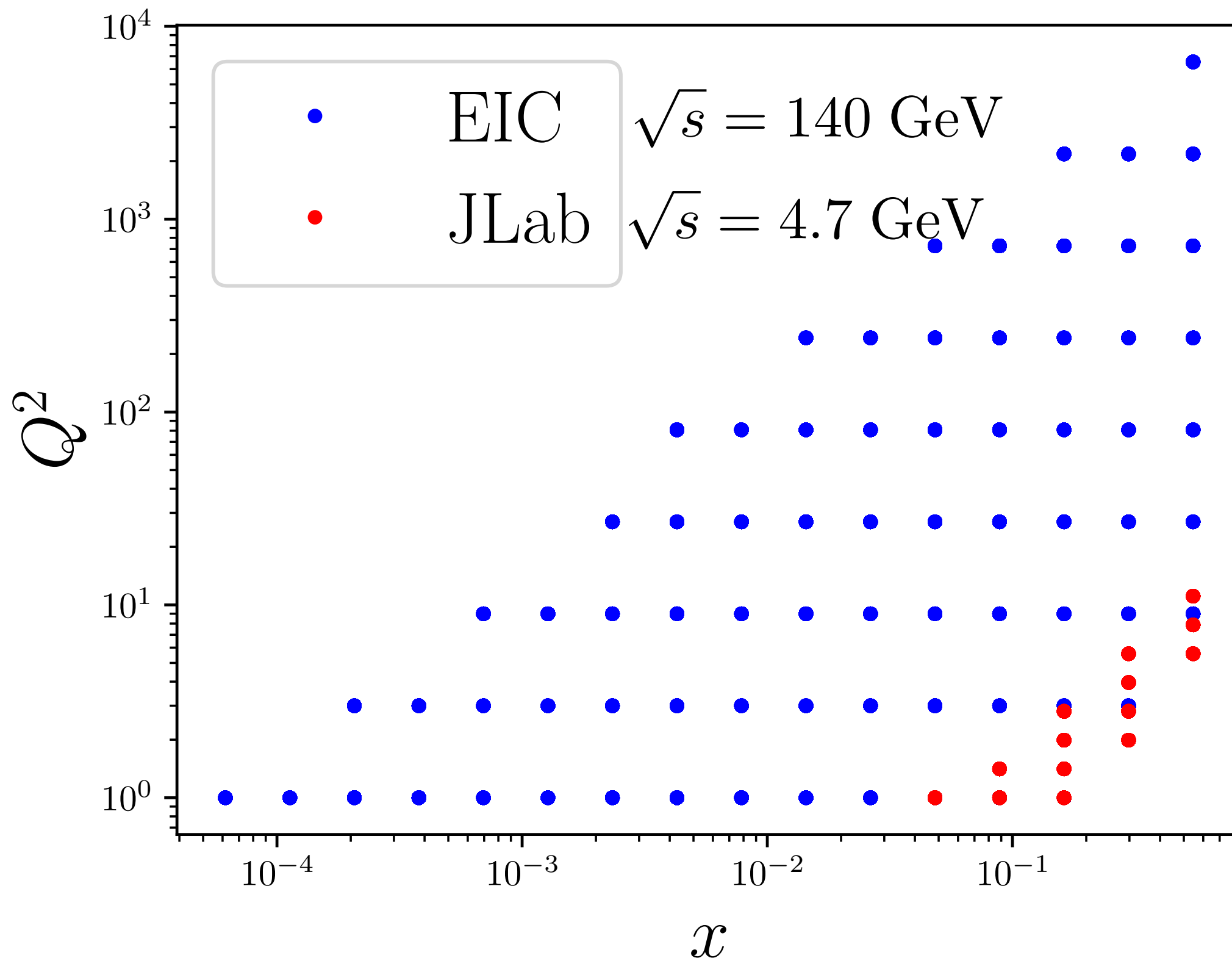
In our case it is only an estimate.

The tool is to guide our intuition.



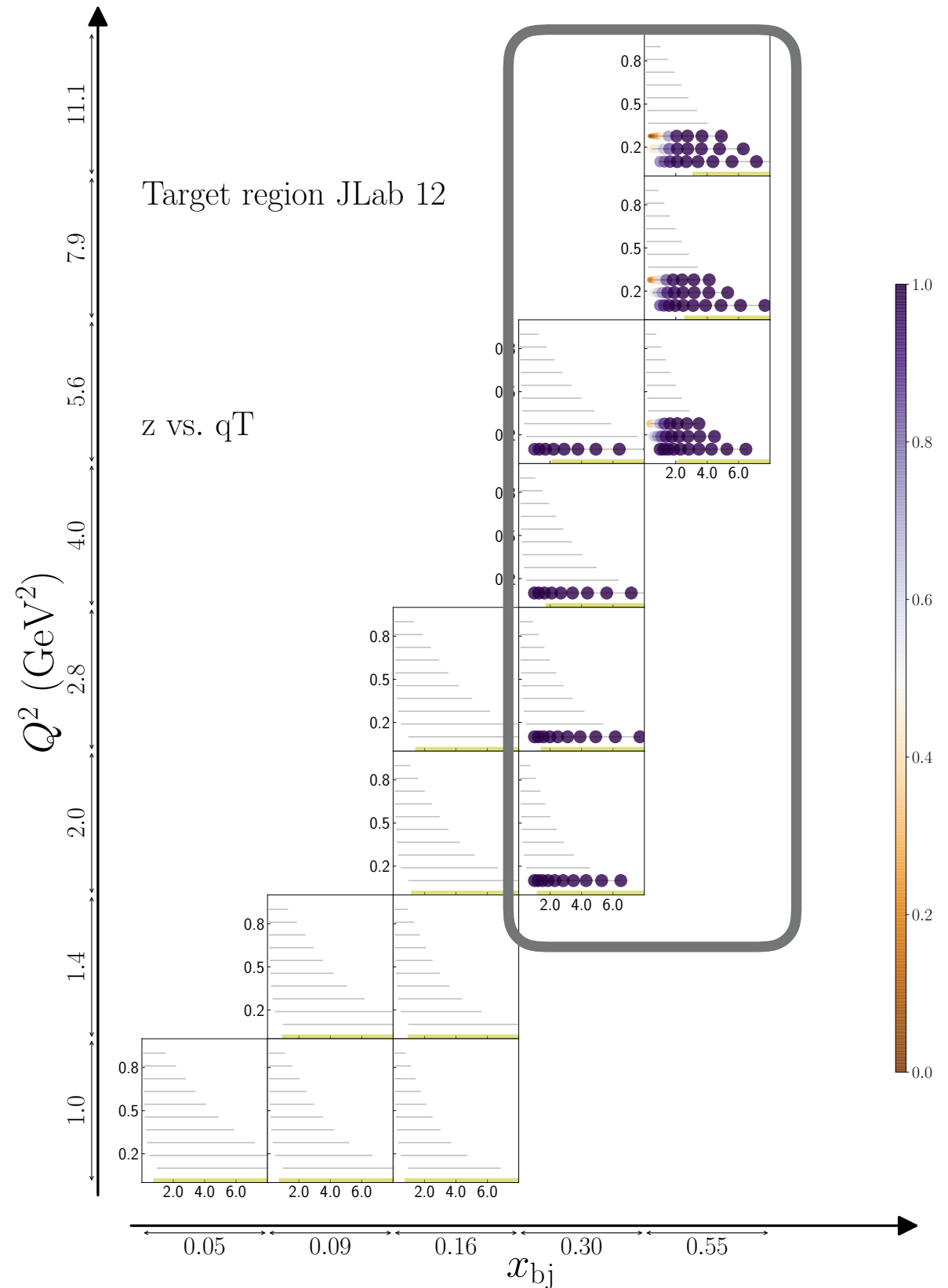
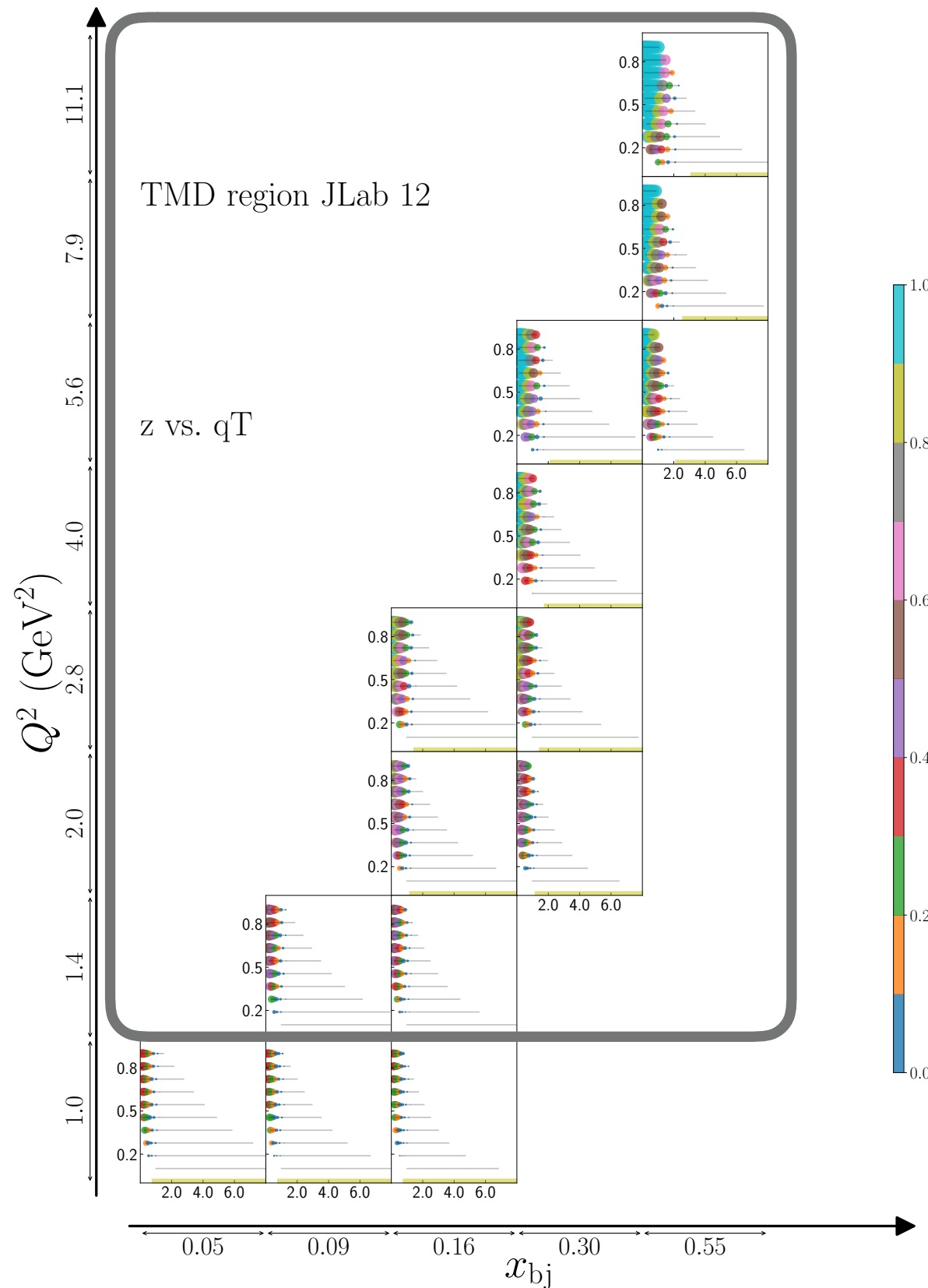
# JEFFERSON LAB 12 AND EIC

Current study



# JEFFERSON LAB 12

Current study



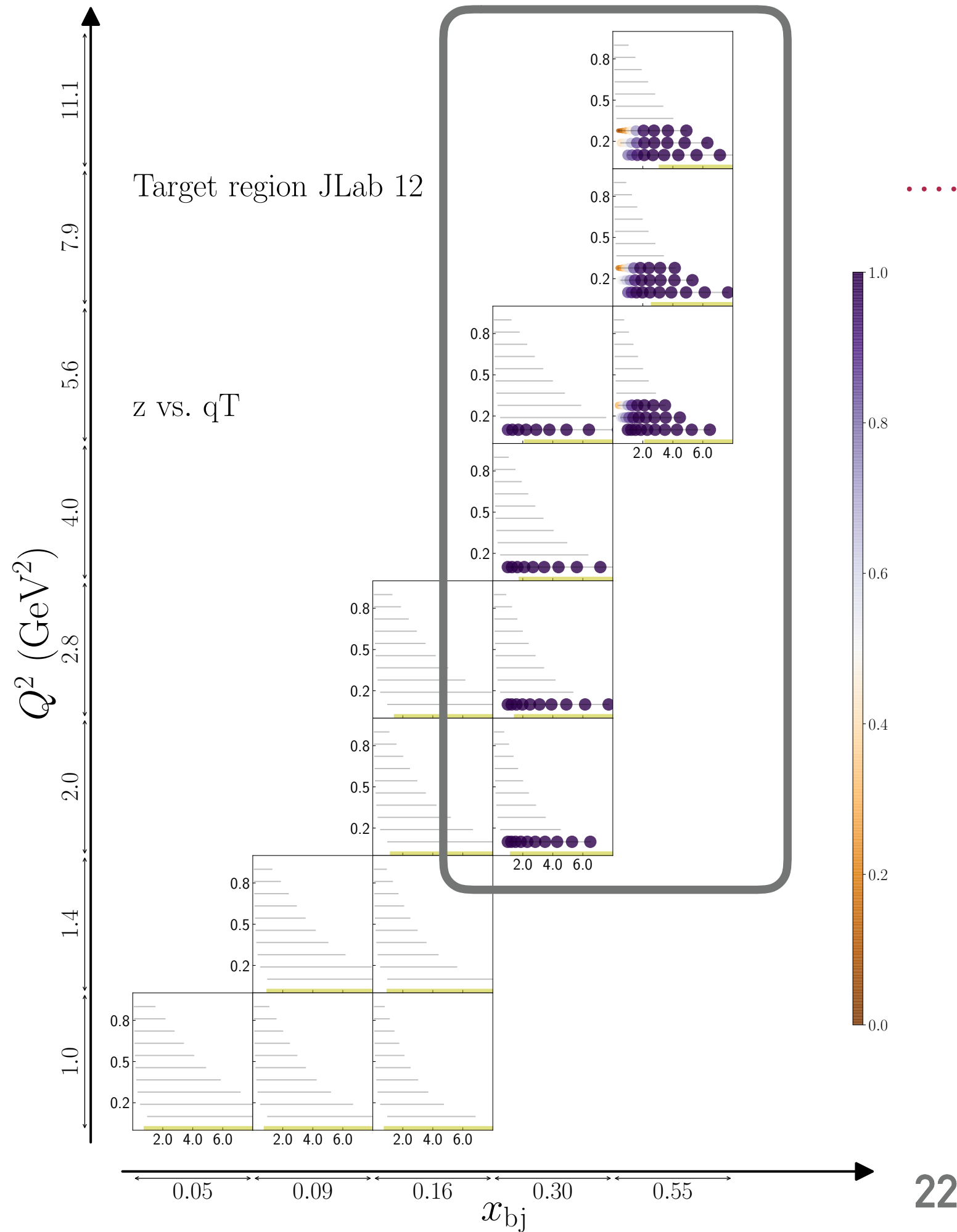


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# JEFFERSON LAB 12

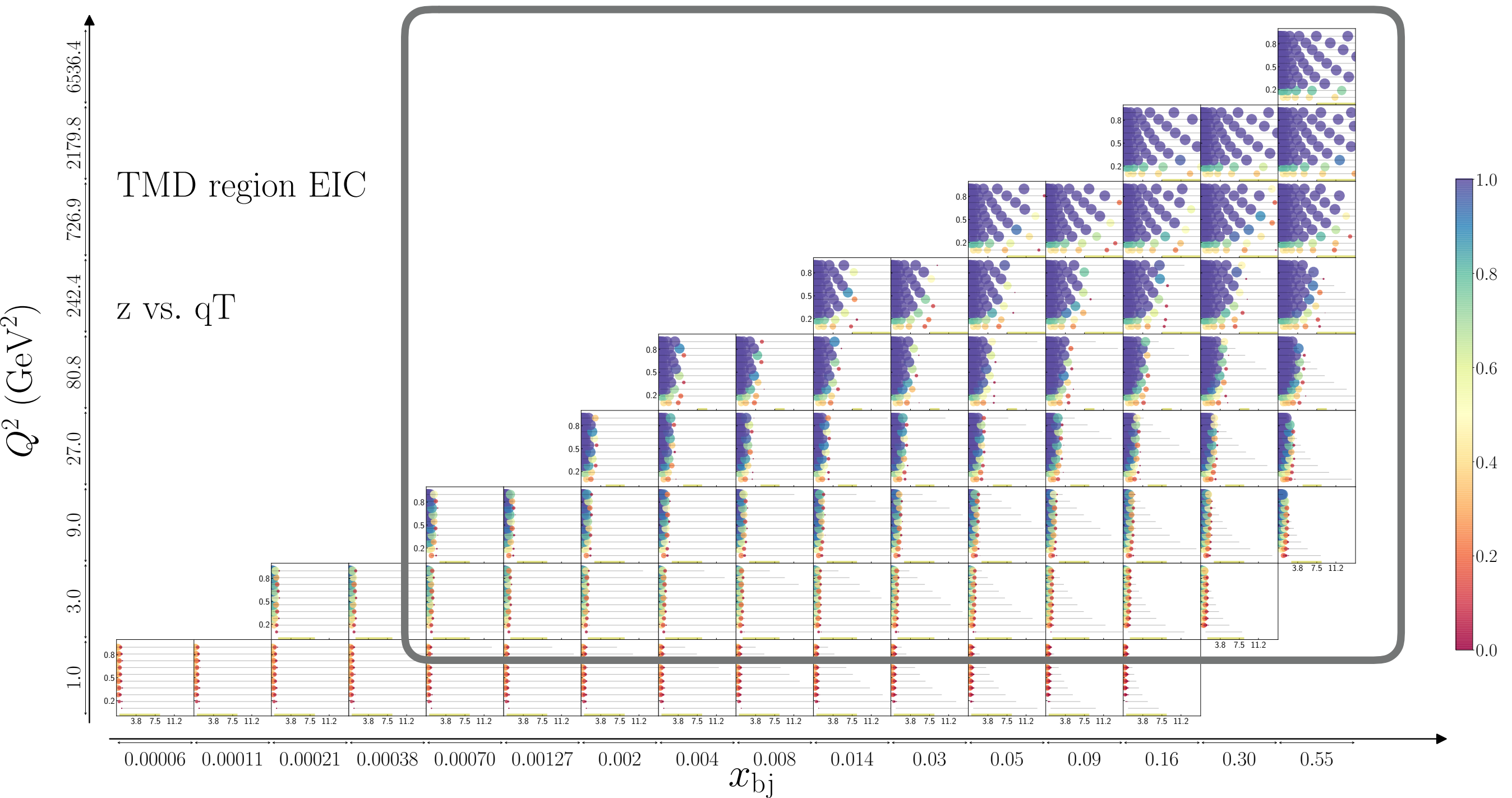
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# EIC: CURRENT REGION

Current study

Relatively large  $x_{Bj}$ ,  $z_h$ ,  $Q$



## Current study

Target region EIC

Z vs. qT

$Q^2$  (GeV<sup>2</sup>)

$x_{bj}$

# THEORETICAL AND PHENOMENOLOGICAL DEVELOPMENT

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- We have studies regions in SIDIS and identified TMD, Target, Soft and Hard regions
- New tool to guide our intuition is provided
- Further phenomenological and theoretical studies to follow