

# Jet Substructure at EIC

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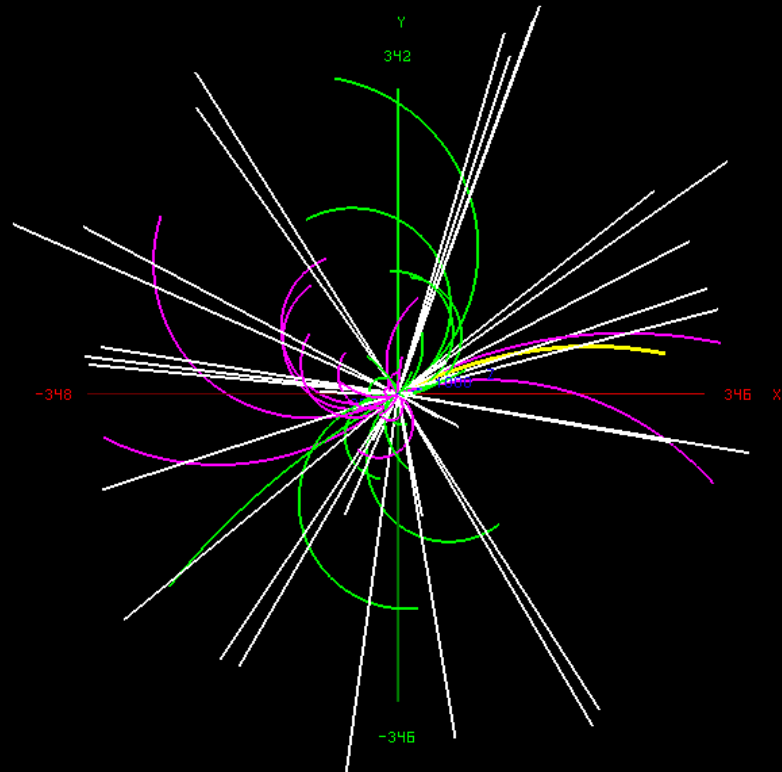
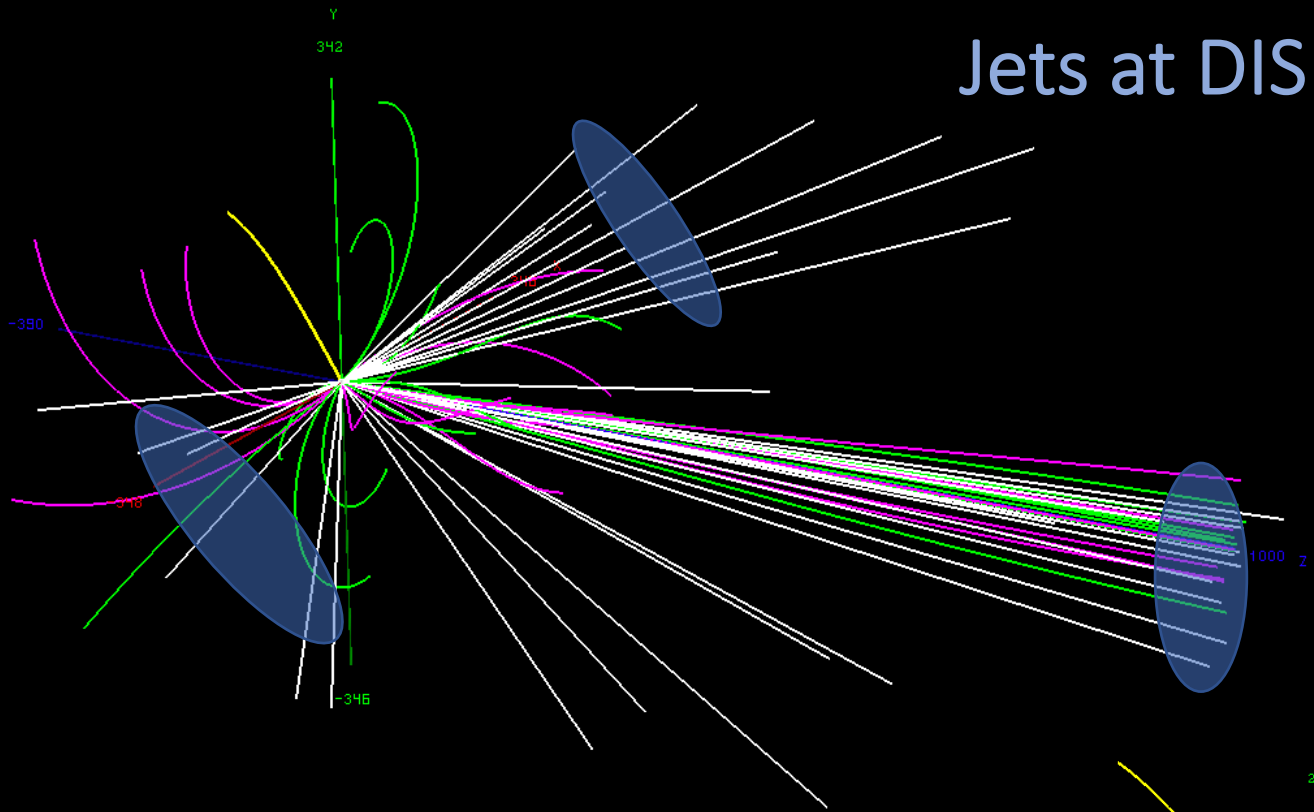
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# Introduction

- Jets and their structure
  - Correlations in momentum, charge and flavor : leading and next to leading particles in a jet
  - access to the dynamics of fragmentation and color entanglement in QCD
- Observable
  - Charge asymmetry
  - Connection to dihedron fragmentation function
- Pythia event studies
  - Acceptance of Jet and constituent particles
  - Charge asymmetry and in combination of various particle species
  - At various center of mass energies at EIC
- Summary and Outlook

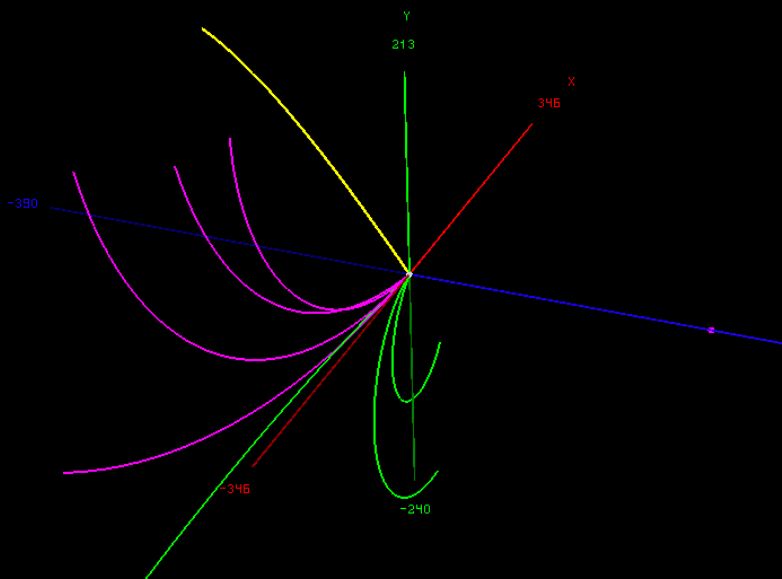
# Jets at DIS



Leading momentum particles in the jet –  $K, \bar{p}$

Particles in Jet :

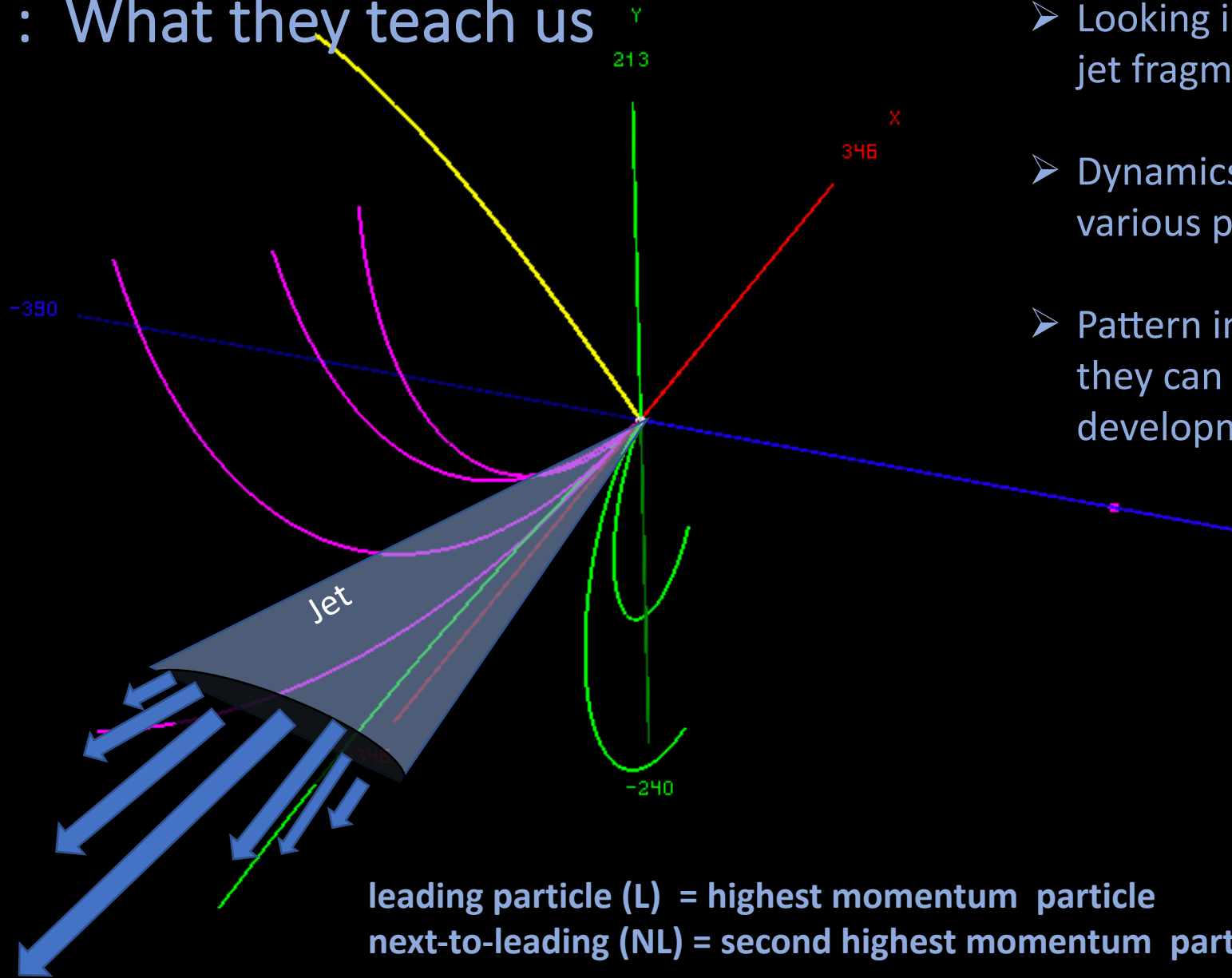
Px	Py	Pz	PID
-7.64	-4.41	-4.21	321
-2.06	-1.89	-1.40	-2212
-1.44	-0.87	-0.69	-211
-1.07	-0.08	0.04	2212
-0.58	-0.45	-0.53	-211
-0.70	-0.39	-0.39	-211
-0.65	-0.52	-0.04	211



Scattered-electron  
 +ve particles  
 -ve particles  
 Neutral particles

Charged Jet – anti-kt R = 0.7 ( $p_{T,jet} > 8\text{GeV}$ )

# Jets : What they teach us



- Looking in the nonperturbative aspect of jet fragmentation
- Dynamics that led to fragmentation of various particle species in certain ways
- Pattern in charge and flavor separation : they can inform in future theoretical development

leading particle (L) = highest momentum particle  
next-to-leading (NL) = second highest momentum particle

# Momentum-charge correlations

□ Leading particle (L) and next-to-leading (NL) are both pions generated in two pictures

i) “**random**” picture : L is fixed and NL is random and both L and NL pions are charged

$$N_{C\bar{C}}^{\text{random}} = N_{CC}^{\text{random}} = \frac{N^{\text{random}}}{2}$$

$C\bar{C}$  indicates opposite charges  
 $CC$  same charge

ii) “**alternating**” picture : perturbative shower gives  $q_L$  followed by  $\bar{q}'_{NL}$ , which form pions by sharing a soft pair:

$$q_L + \bar{q}_{NL} \rightarrow q_L + (\bar{q}_s + q_s) + \bar{q}'_{NL} \rightarrow \pi(q_L, \bar{q}_s) + \pi(q_s, \bar{q}'_{NL})$$

$$N_{C\bar{C}}^{\text{alternating}} = N_{CC}^{\text{alternating}} \quad \text{and} \quad N_{CC}^{\text{alternating}} = 0$$

□ **The observable :**

$$r_{\text{asy}} \equiv \frac{N_{CC} - N_{C\bar{C}}}{N_{CC} + N_{C\bar{C}}} = \frac{1 - a}{2} - \left( \frac{1 - a}{2} + a \right) = -a$$

- ✓ provided every event results from one of these two processes, with no interference
- ✓ percentage of “alternating” =  $a$ ; and percentage of random events =  $1-a$

➤  $r_{\text{asy}}$  is a measurement of the fraction of hadronizations that are “string-like”, alternating between quark and antiquark (classical picture)

# Measurements of $r_{\text{asy}}$ and expressing in terms of di-hadron fragmentation functions

- **Measurements of  $r_{\text{asy}}$  :**
  - differentially in fractions  $z_L$  and  $z_{NL}$  in a jet,
  - “transverse” kinematic variables:
    - ✓ relative transverse momentum
    - ✓ pair invariant mass
    - ✓ pair formation time
    - ✓ including polarization where applicable

## □ $r_{\text{asy}}$ and its connection with generalized di-hadron fragmentation functions

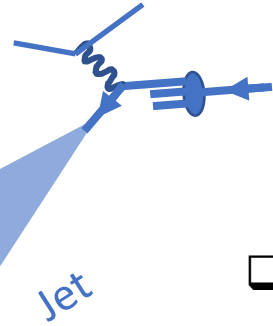
generalized di-hadron fragmentation functions for any hadrons  $h_1, h_2$  :  $D_{h_L, h_{NL}}^>(z_L z_{NL})$

$$N_{h_L, h_{NL}}^> = \int_0^1 dz_L \int^{\min(z_L, 1-z_L)} dz_{NL} D_{h_1, h_2}^>(z_L, z_{NL}, Q)$$

When  $z_L$  and  $z_{NL}$  are large enough, this is the usual di-hadron distribution  $D^>(x_1, x_2, Q) = D(x_1, x_2, Q)$  when  $x_2 > 1 - x_1 - x_2$

$$r_S = \frac{\sum_{h_1, h_2 \in S} Q_{h_1} Q_{h_2} N_{h_1, h_2}^>}{\sum_{h_1, h_2 \in S} |Q_{h_1} Q_{h_2}| N_{h_1, h_2}^>}$$

18x275 GeV



$$r_{\text{asy}} \equiv \frac{N_{CC} - N_{C\bar{C}}}{N_{CC} + N_{C\bar{C}}}$$

□ Construct  $r_{\text{asy}}$  with particle compositions with various parameters

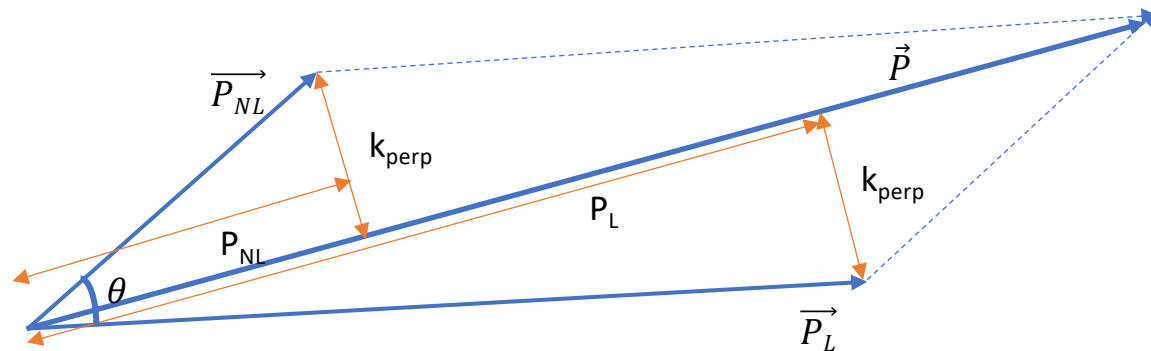
- ✓ Leading particle ( $\pi$ ) and next leading particles ( $\pi/K/p$ )
- ✓ Leading particle ( $K$ ) and next leading particles ( $K/\pi/p$ )
- ✓ Leading particle ( $p$ ) and next leading particles ( $p/\pi/K$ )

□ Looking via

- ✓ Momentum-next lead particle/momentum of leading particle
- ✓ Faction of jet momentum carried by leading particle
- ✓ Angle between the leading and next to leading particles ( $\Delta\theta$ )
- ✓ relative transverse momentum ( $k_{\text{perp}}$ )
- ✓ pair invariant mass
- ✓ Formation time :  $[2z(1-z) P] / k_{\text{perp}}^2$

PYTHIA-6 : 1M events :  
 $Q_2 > 65 \text{ GeV}$

Jet Reconstruction :  
 anti-kt  $R = 0.7$   
 Jet  $pt > 8 \text{ GeV}$   
 pt-tracks  $> 0.2 \text{ GeV}$   
 track  $|\eta| < 3.5$   
 Jet  $|\eta| < 2.8$



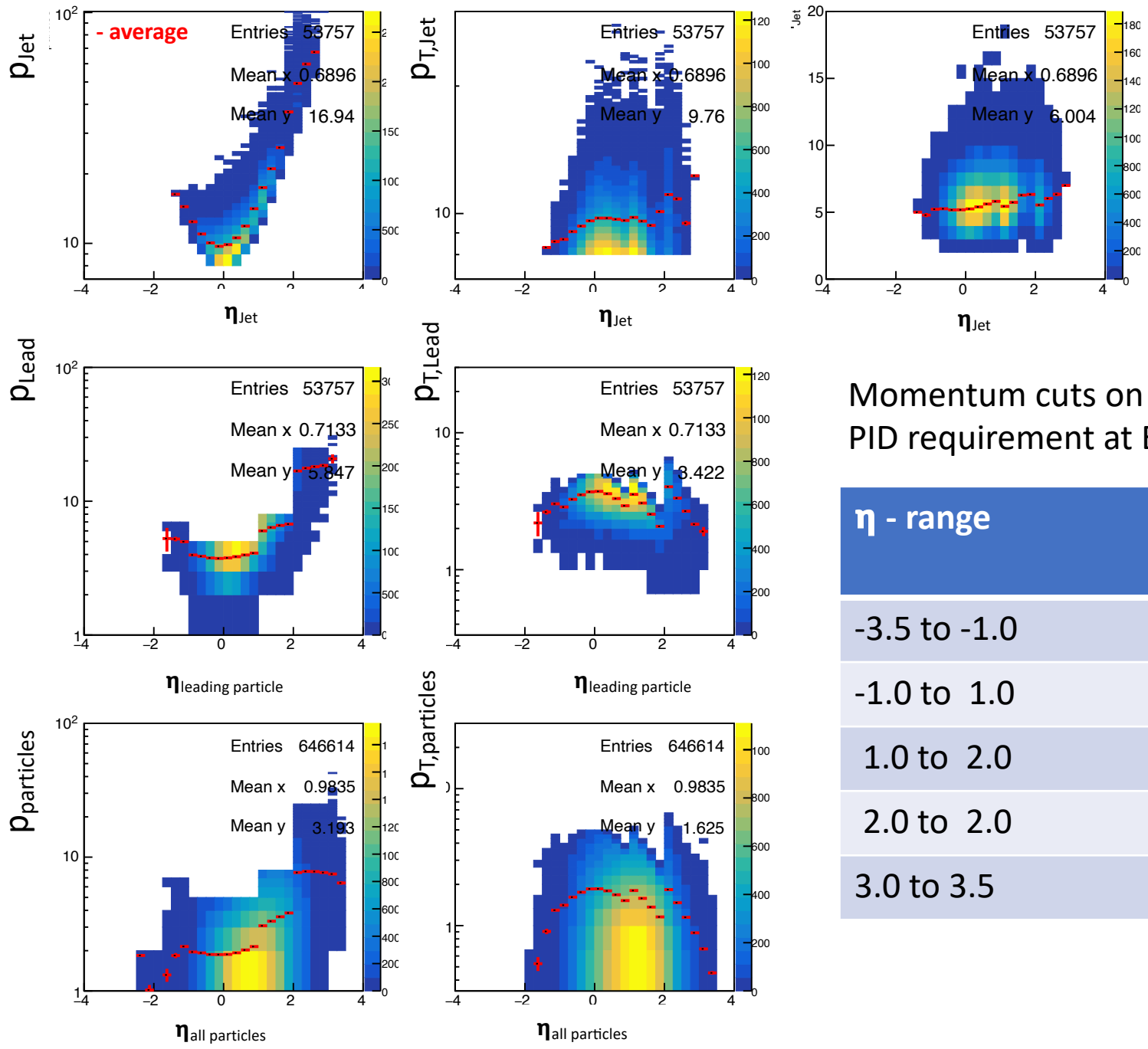
$$z = P_{NL} / (P_{NL} + P_L)$$

$$P_L = (1-z)P$$

$$P_{NL} = zP$$

# Acceptance

18x275 GeV

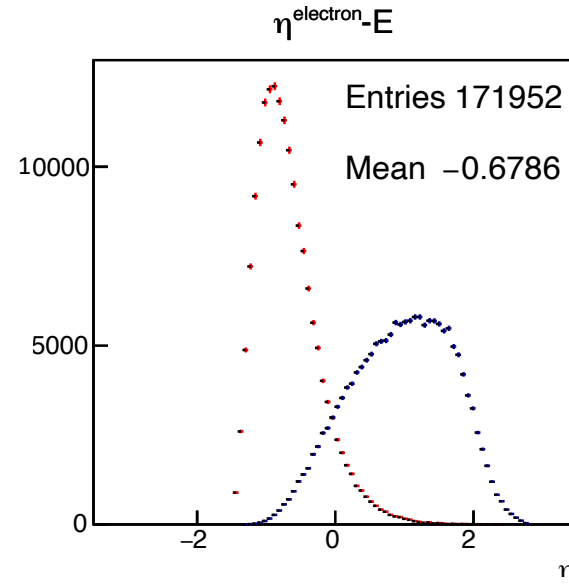
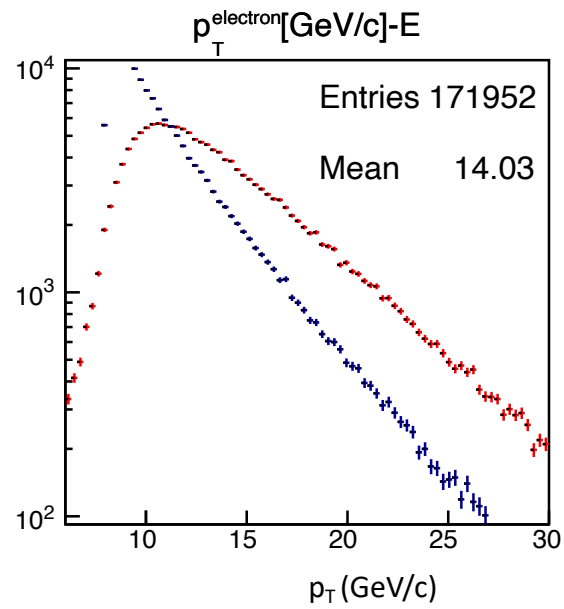


Momentum cuts on tracks for approximate PID requirement at EIC at different  $\eta$  regions

$\eta$ - range	Momentum cut (GeV/c <sup>2</sup> )
-3.5 to -1.0	7
-1.0 to 1.0	5
1.0 to 2.0	8
2.0 to 2.0	25
3.0 to 3.5	45

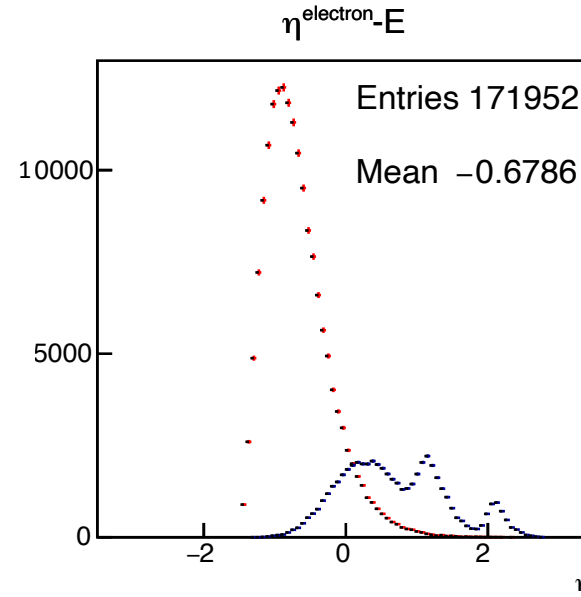
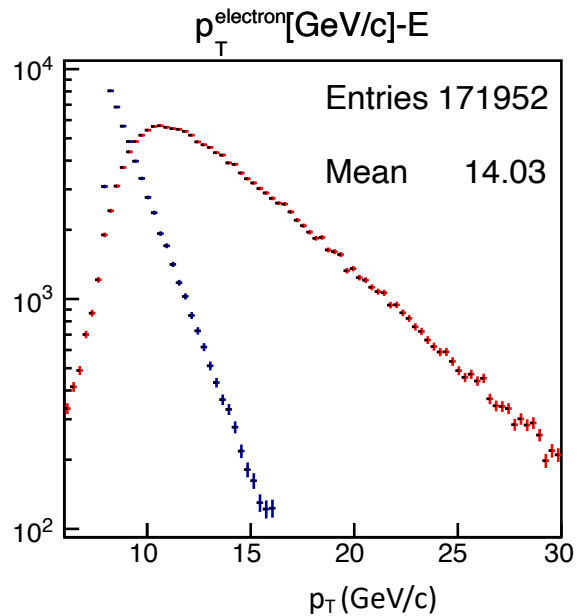


# The effect of momentum cuts in traverse momentum and acceptance of jets



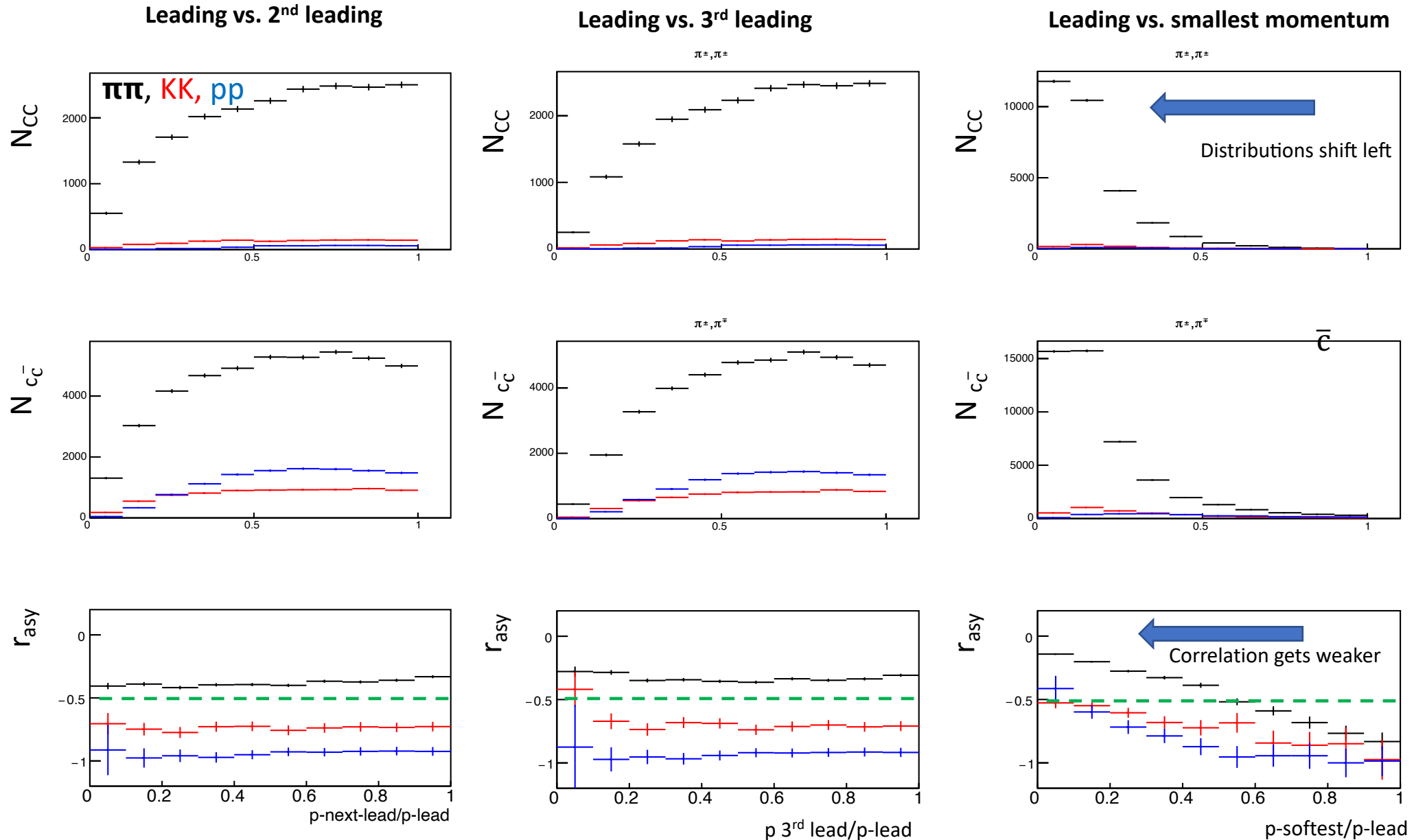
RED-electron  
BLUE-JET

NO  
momentum  
cuts



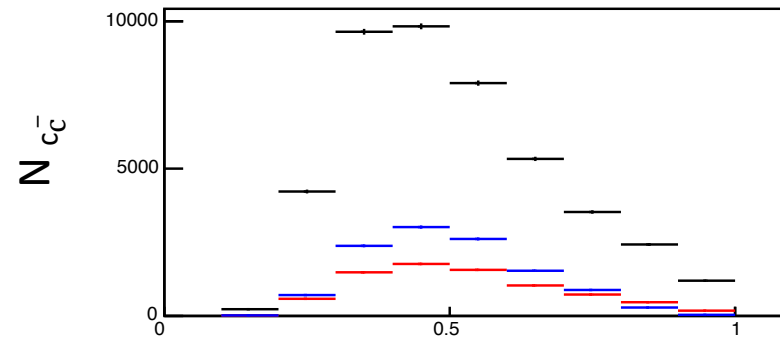
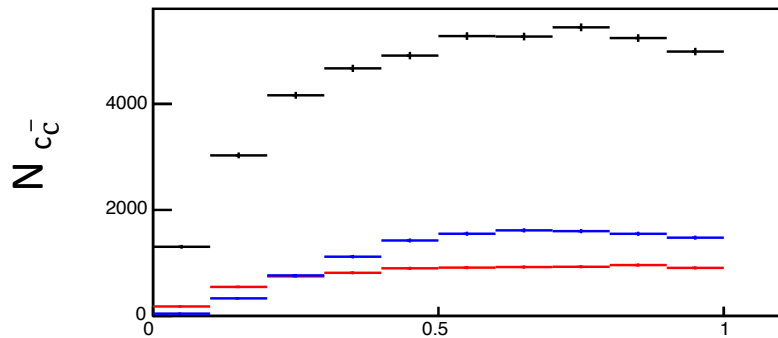
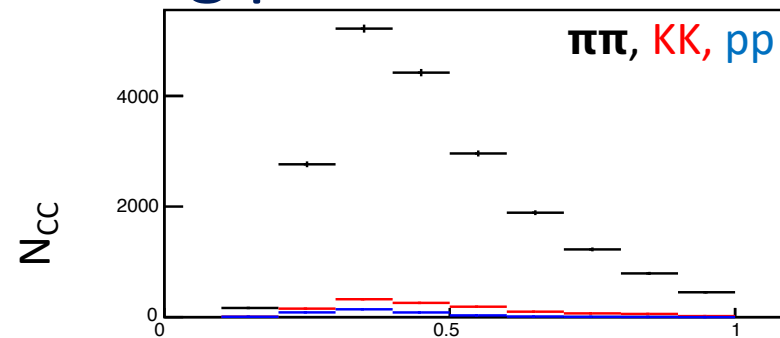
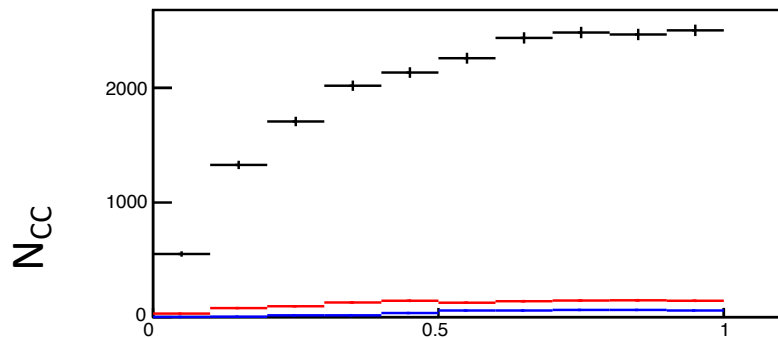
After  
momentum  
cuts

# Correlation with different particles

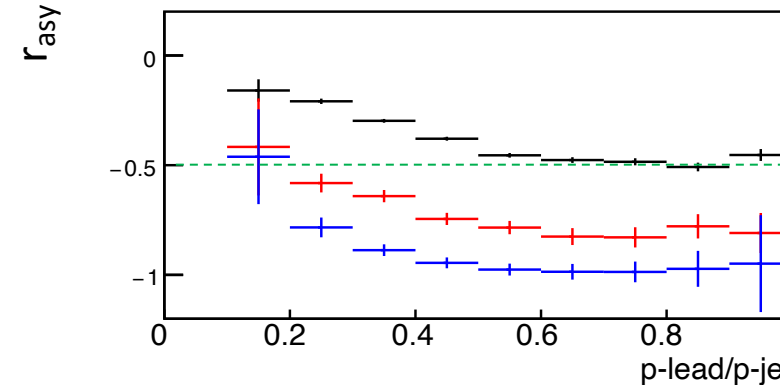
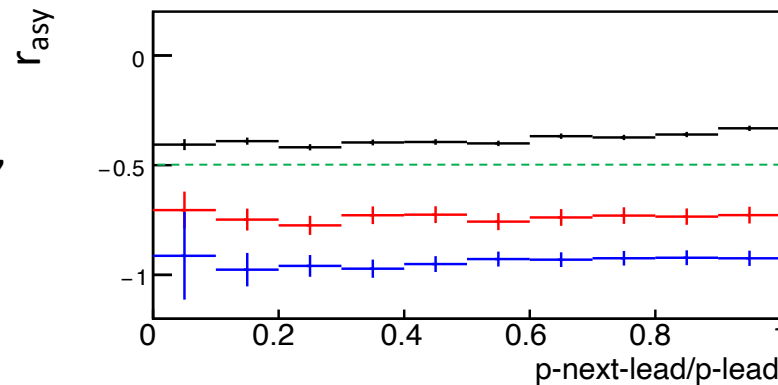


# Correlation with two leading particles

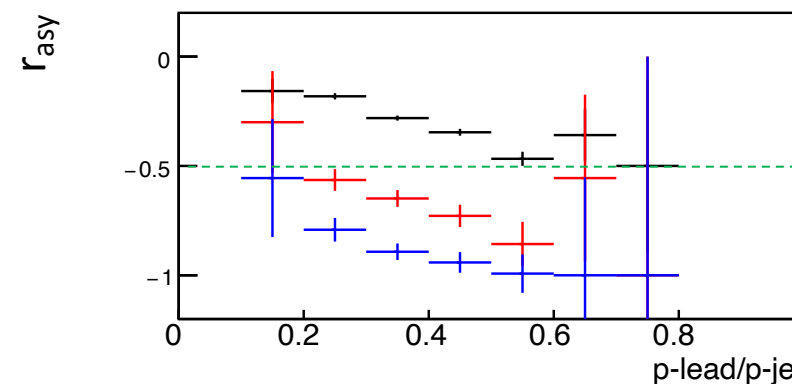
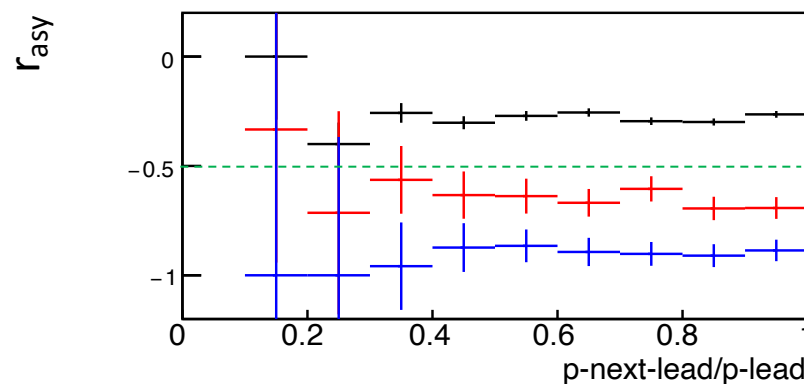
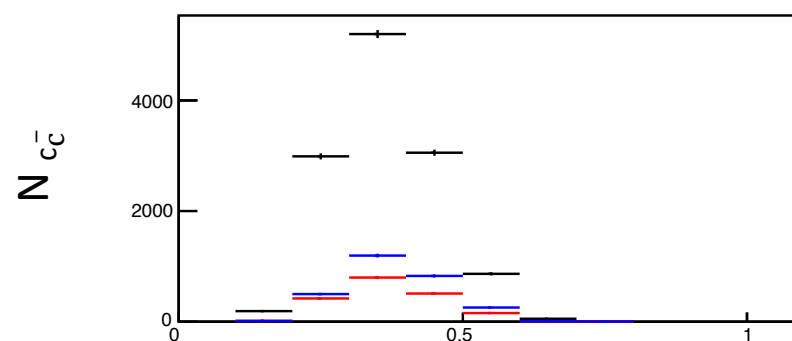
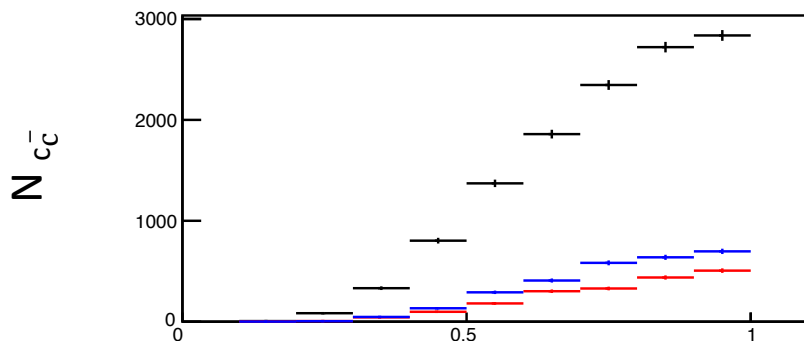
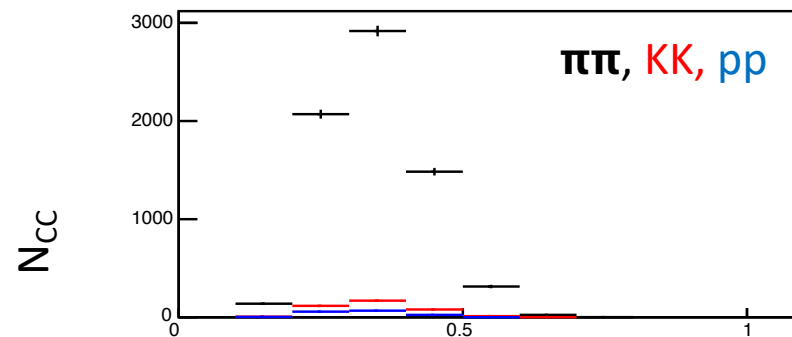
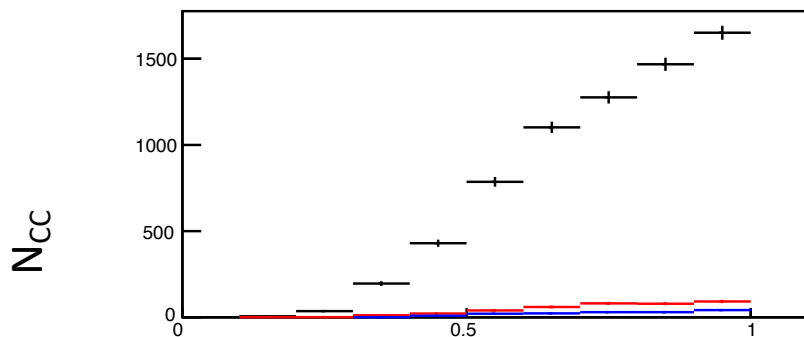
NO  
momentum  
cuts



- The strength of correlations are different for pions, kaons and proton



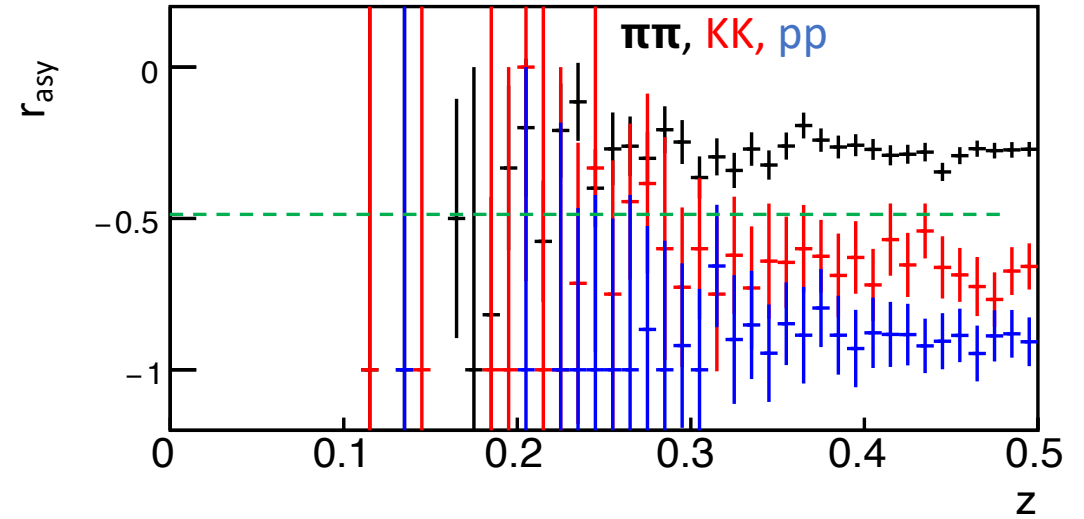
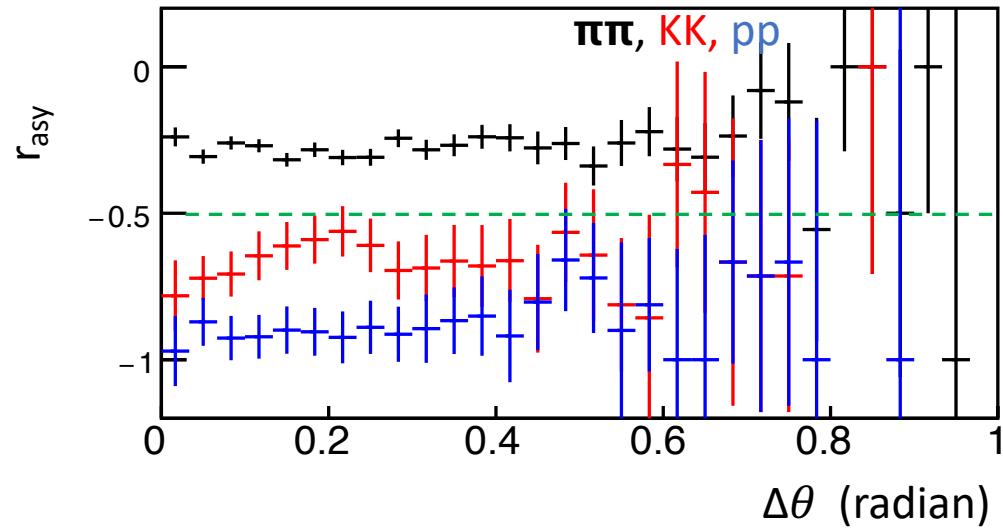
**After  
momentum  
cuts**



- The strength of correlations are different decrease as an acceptance effect

- Acceptance changes in certain regions due to momentum cuts

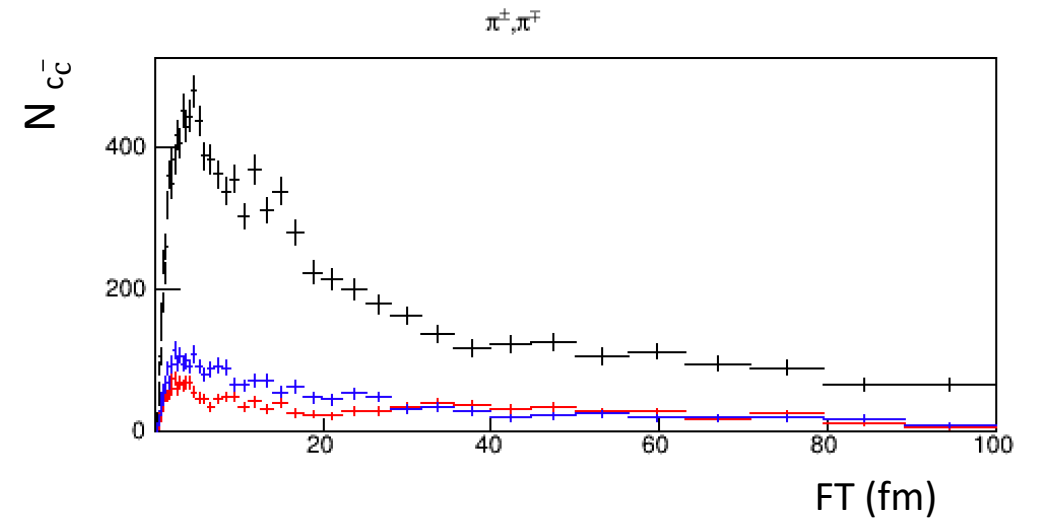
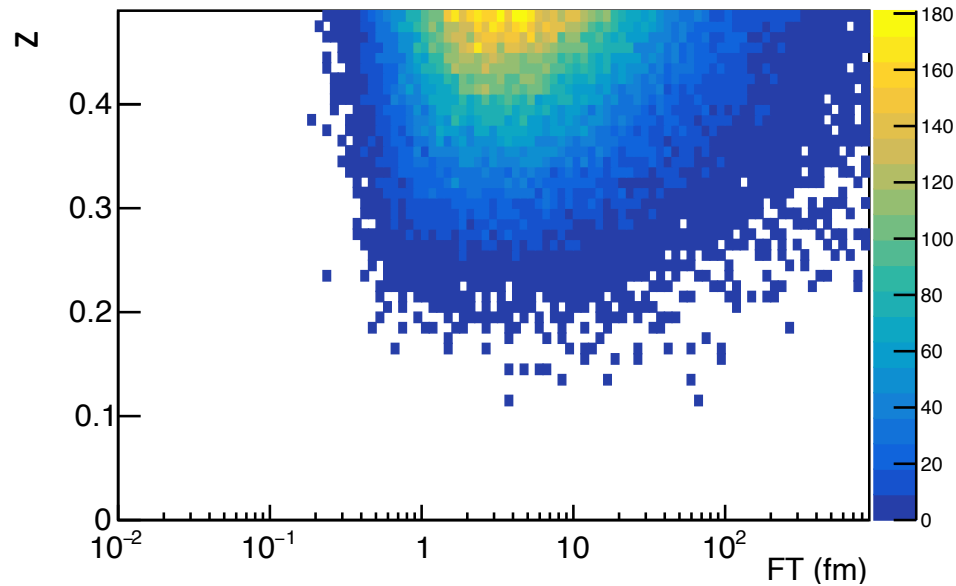
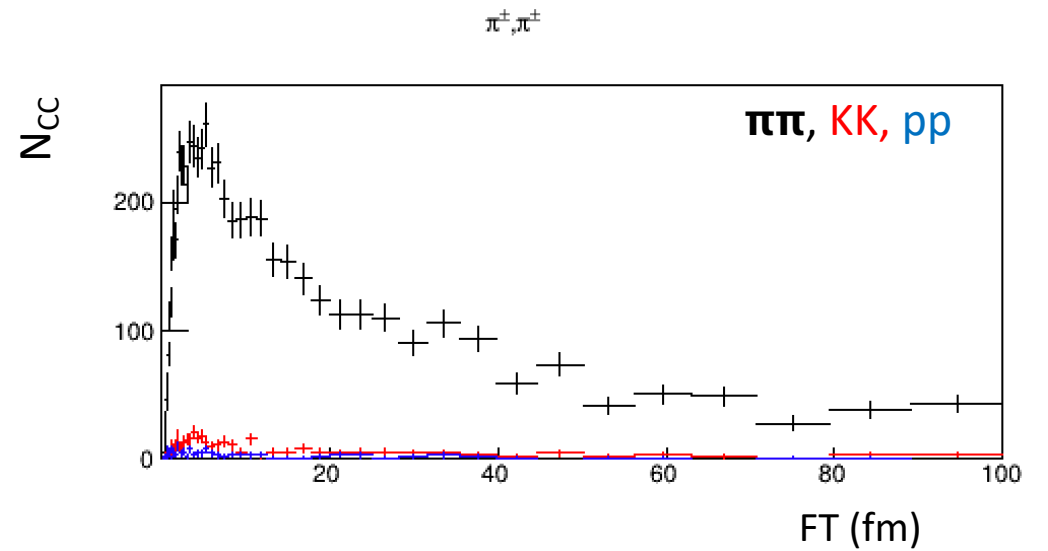
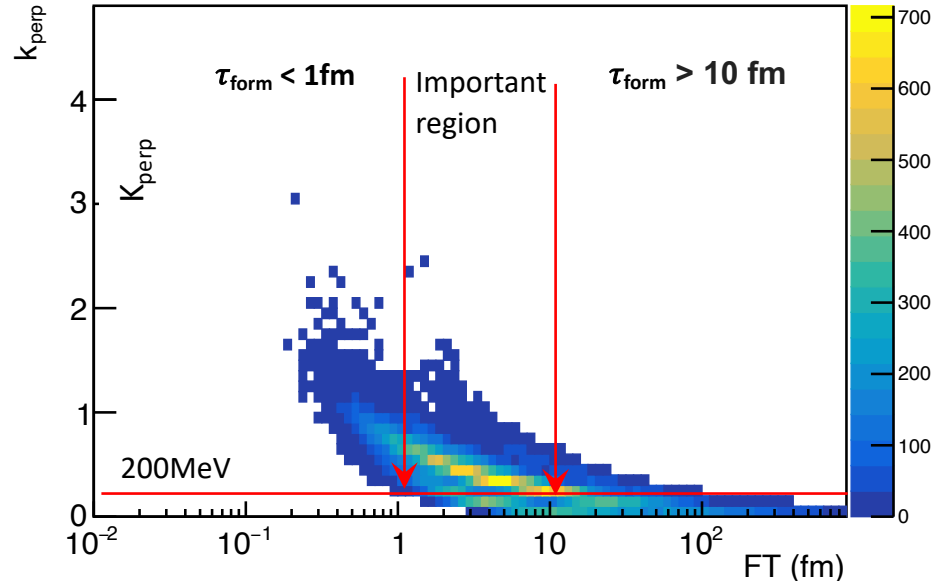
# Dependence on $\Delta\theta$ and $z$



- $r_{asy}$  values remain almost flat opening angle and  $z$  with some little variations

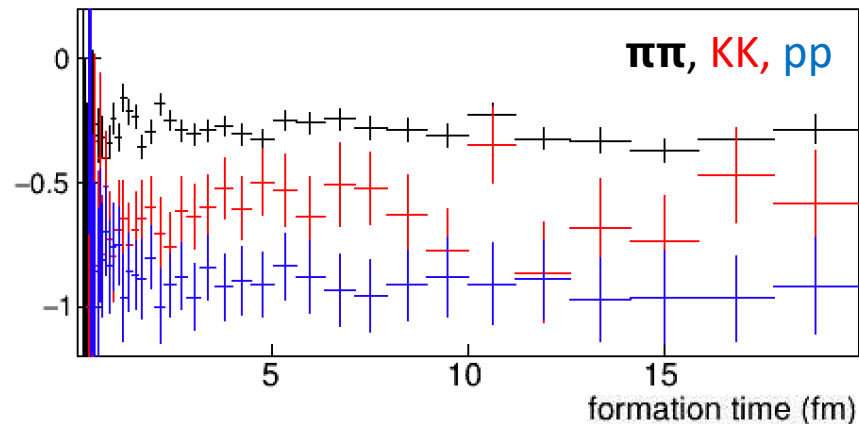
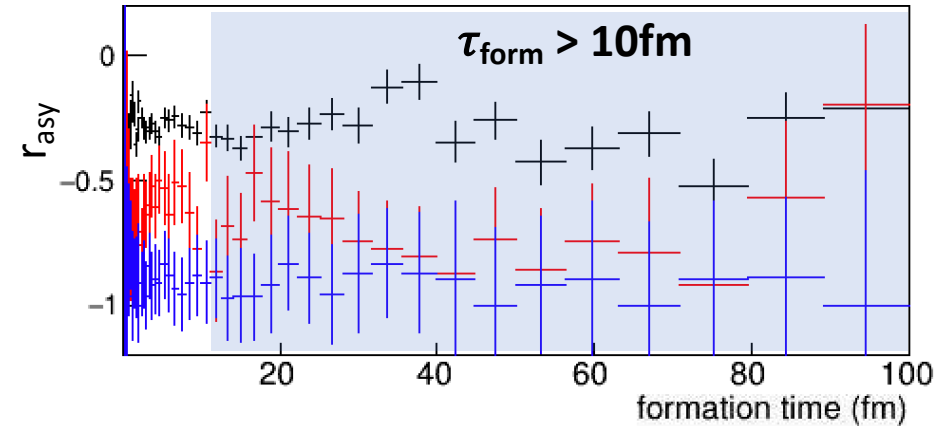
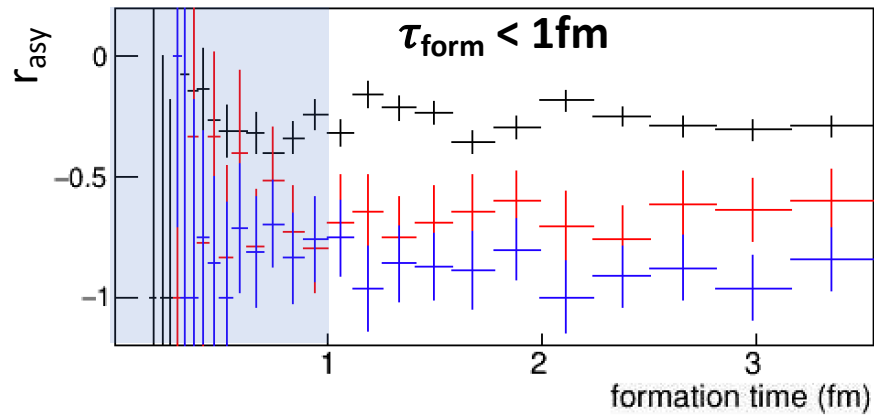
# Formation time

Formation time,  $\tau_{\text{form}} = [2z(1-z) P] / k_{\text{perp}}^2$



# Formation time

$$\text{Formation time, } \tau_{\text{form}} = [2z(1-z) P] / k_{\text{perp}}^2$$

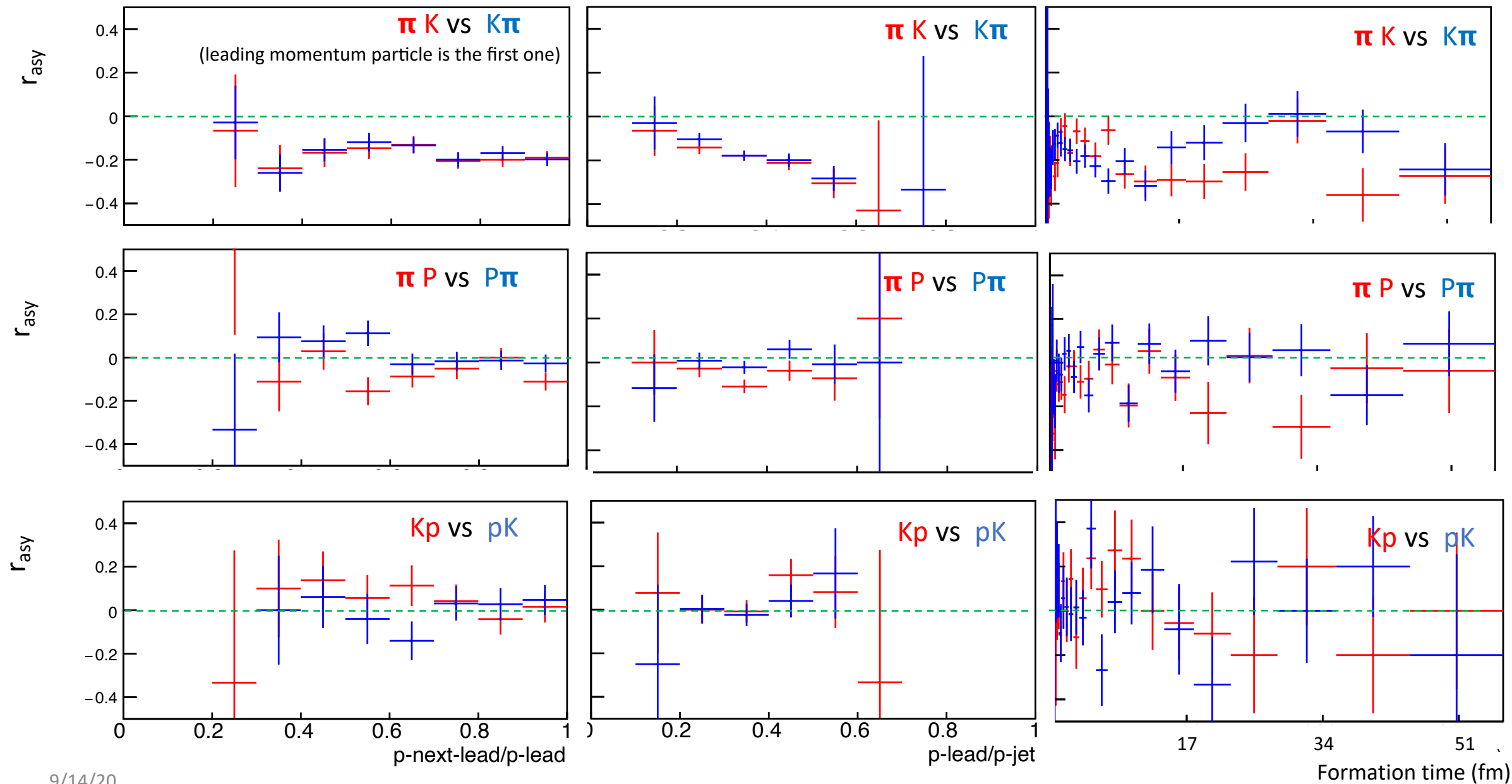


$\tau_{\text{form}} < 1\text{fm}$  : L and NL particles seem to separate after a very short time, which might decorrelate their hadronization.

$\tau_{\text{form}} > 10\text{fm}$  ( $k_{\text{perp}} < 200\text{ MeV}$ ) : nonperturbative transverse momenta in the jet, and we don't think that going to longer  $\tau_{\text{form}}$  or smaller  $k_{\text{perp}}$  leads to new dynamics

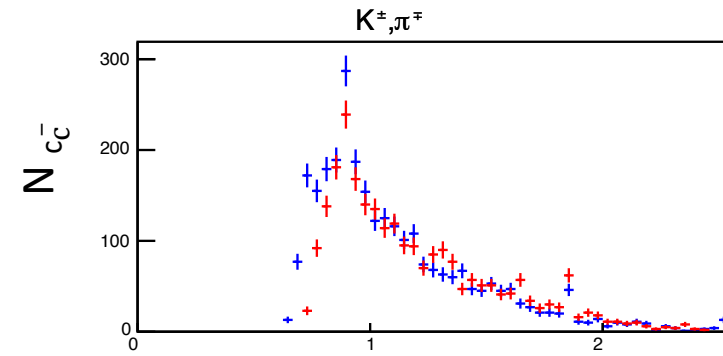
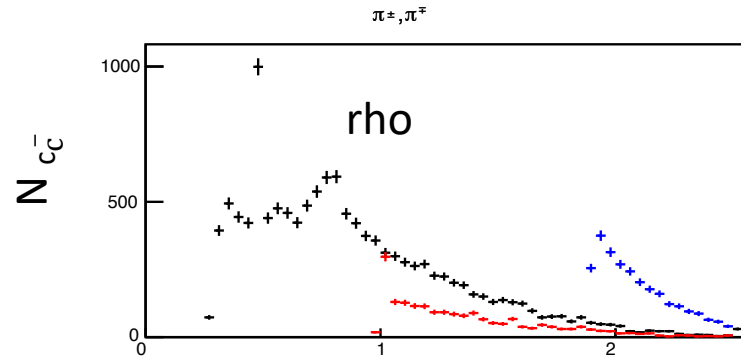
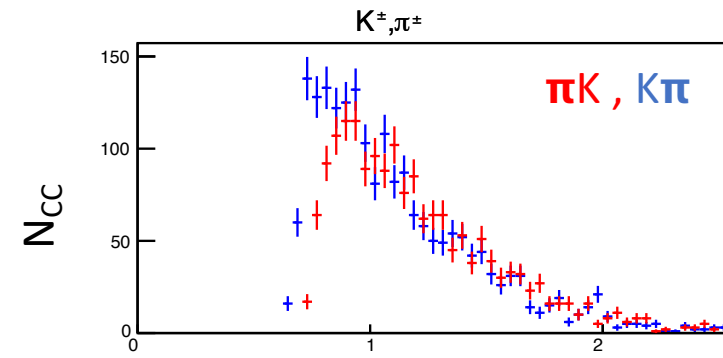
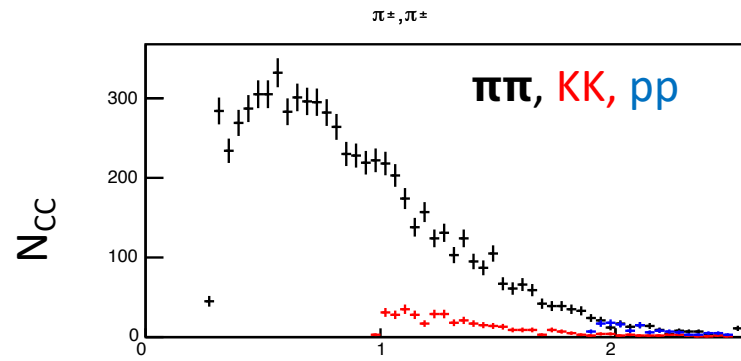
Important region to study in data  $\tau_{\text{form}} =$  "a few fermi" and "a few dozen fermi",  $k_{\text{perp}} =$  "a few GeV" to "several hundred MeV"

# Combination of different leading particles

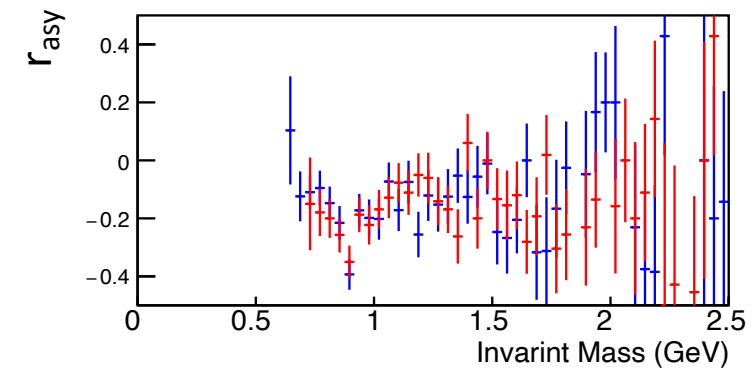
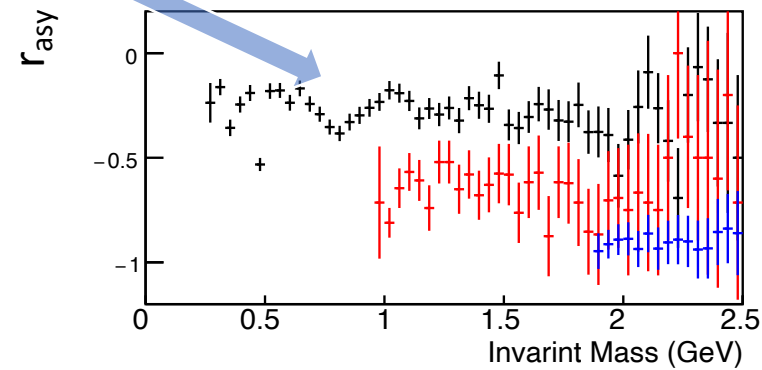




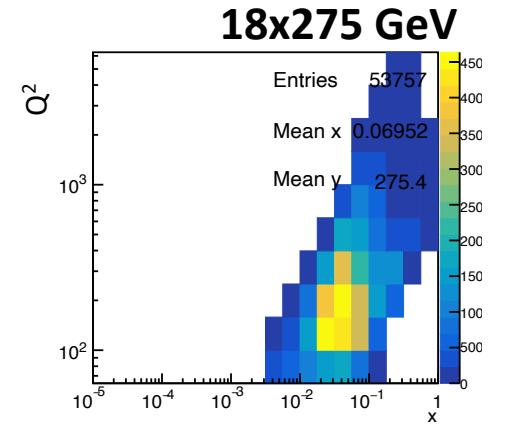
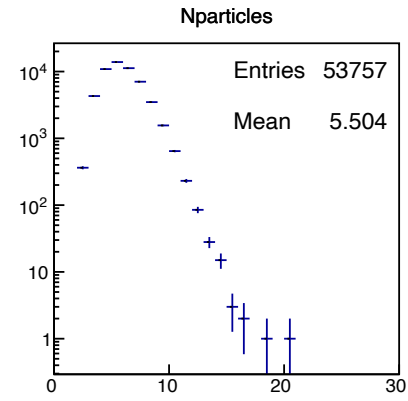
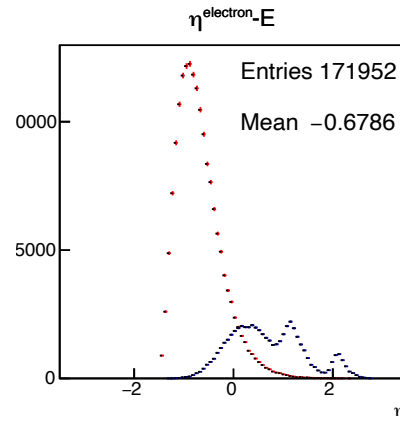
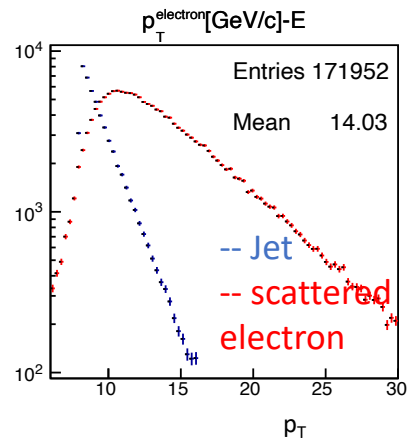
# Invariant mass



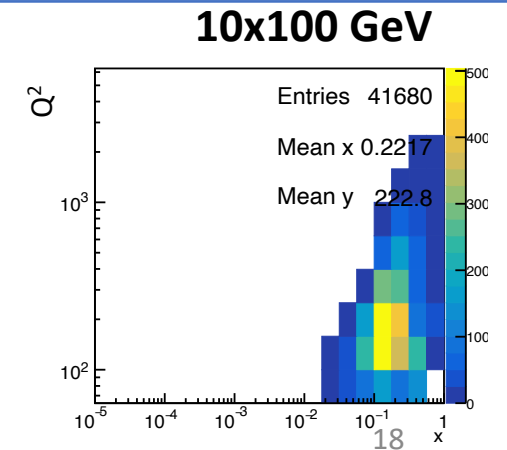
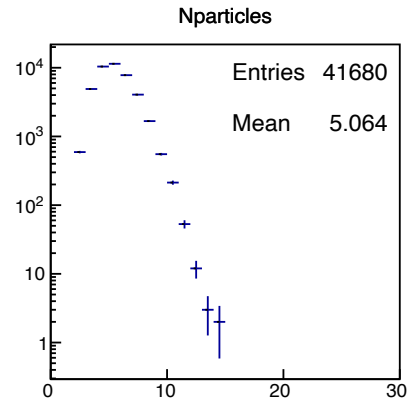
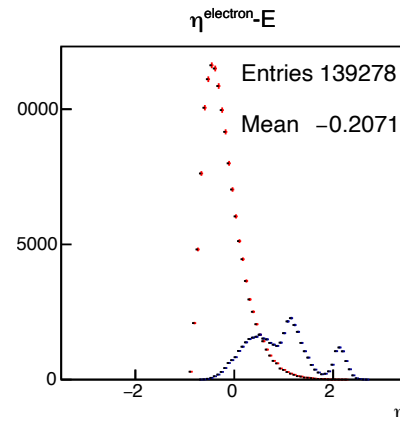
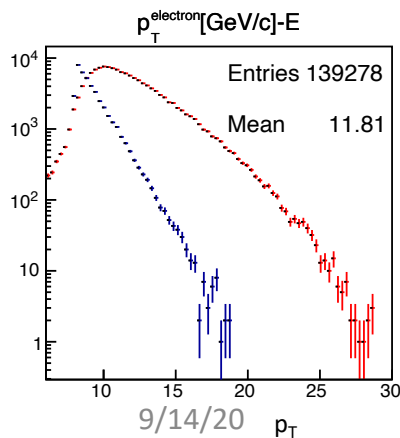
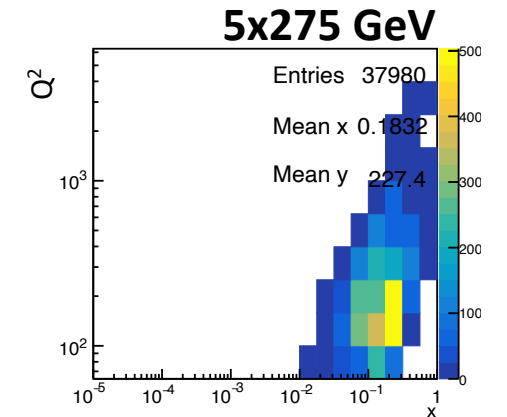
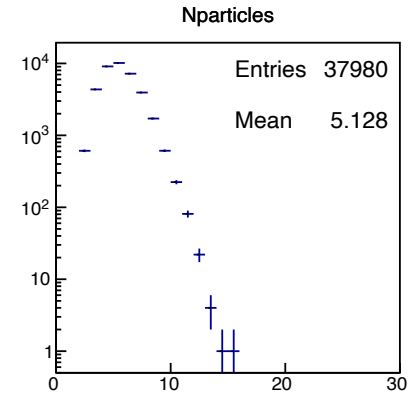
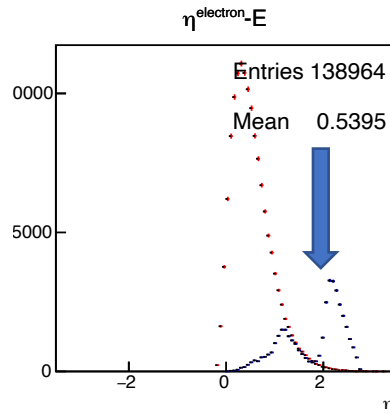
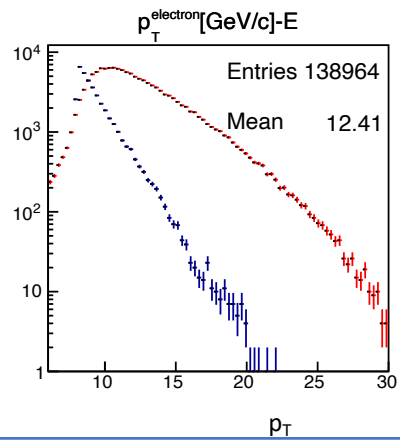
Resonance  
decorrelate the  
asymmetry



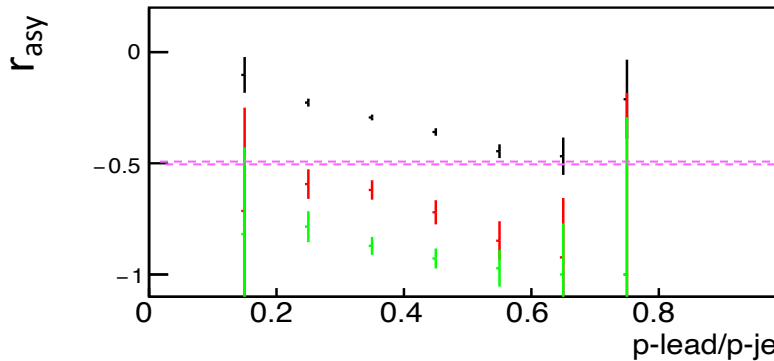
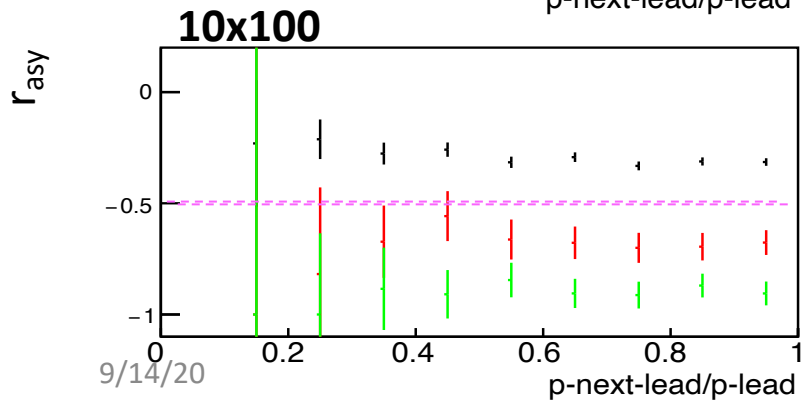
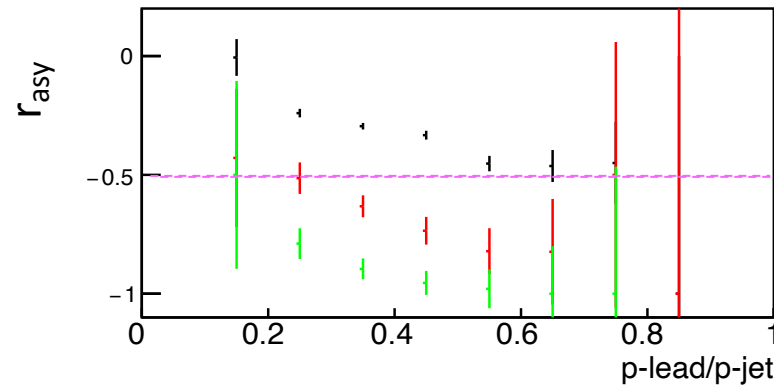
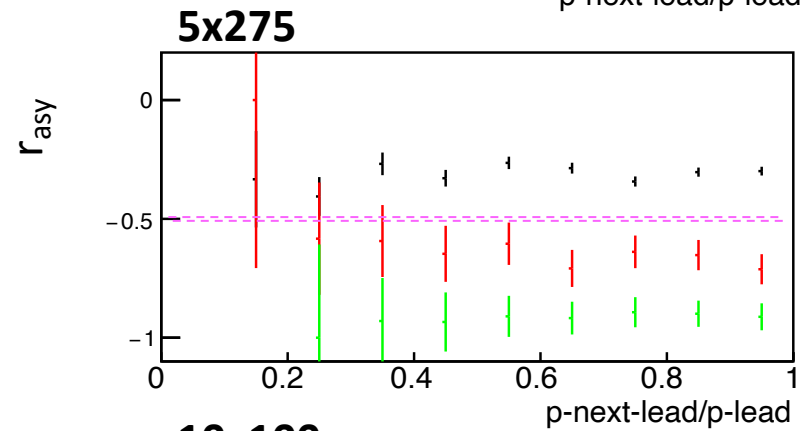
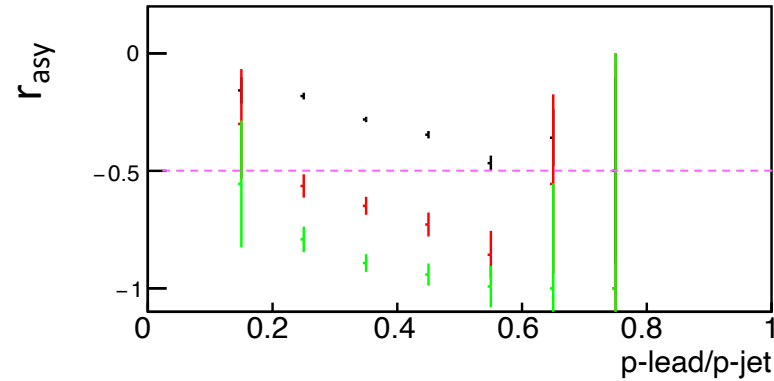
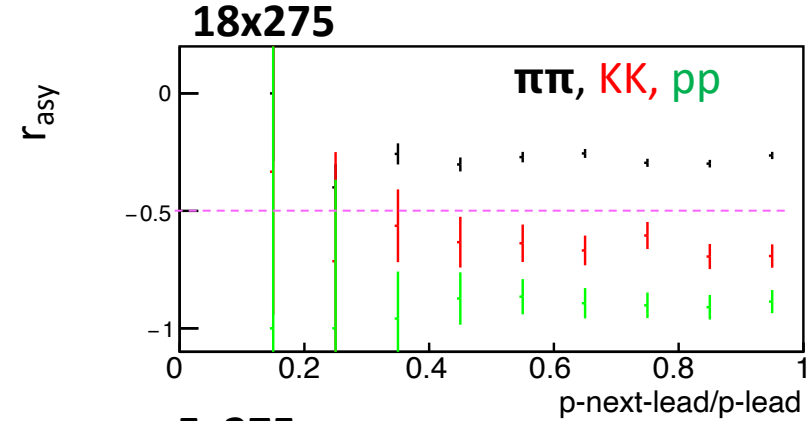
# Acceptance at various collision energies



Most asymmetric – acceptance shift to Forward rapidity : 5x275 GeV



# At different collision energies



- At various center of mass energies  $r_{asy}$  looks similar

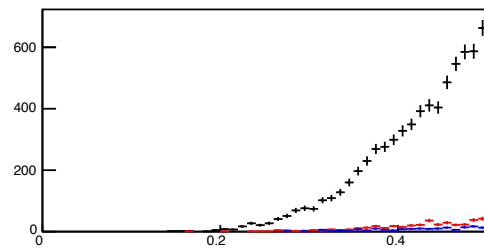
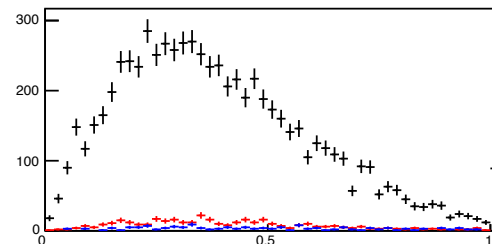
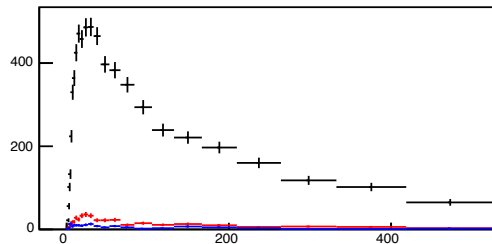
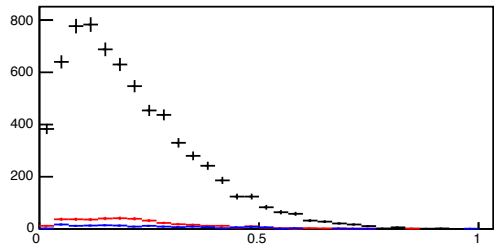
# Summary

- Correlations in momentum, charge and flavor of leading particles in jet carry information of non perturbative aspect of jet fragmentation
- At EIC this can be measured with high momentum PID capabilities
- The embedded correlations in PYTHIA is studied at different set of collision energies for pions, kaons and protons
- We plan to study :
  - ✓ Bringing neutral particle in the correlations
  - ✓ other fragmentation models using HERWIG
  - ✓ Inclusion of jet charge in our study
- We would like to include the studies in Yellow Report activities

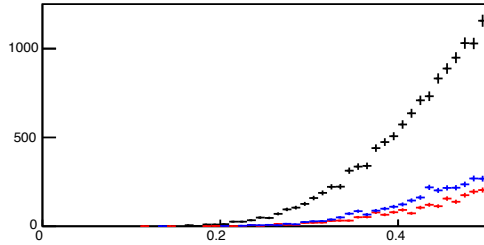
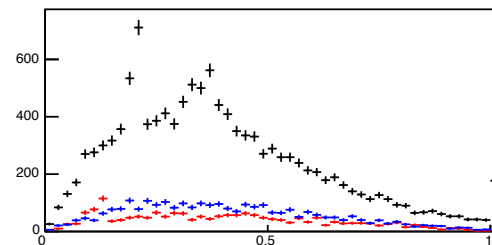
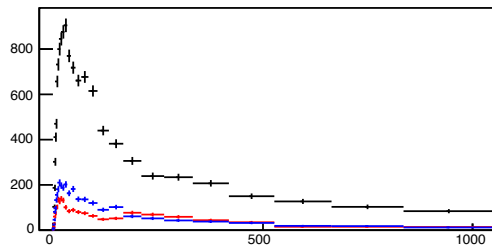
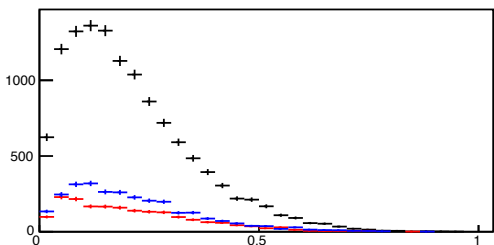
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# $\pi\pi, KK, pp$ (18x275 GeV)

# of ++ or --



# of +- or -+



Opening angle (radian)

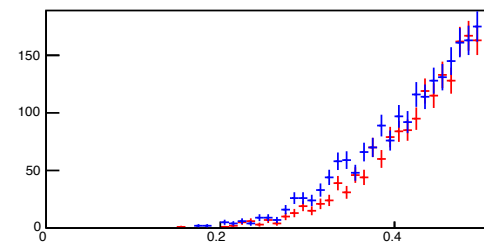
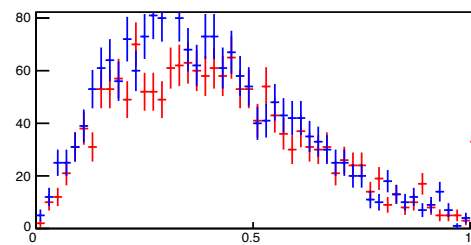
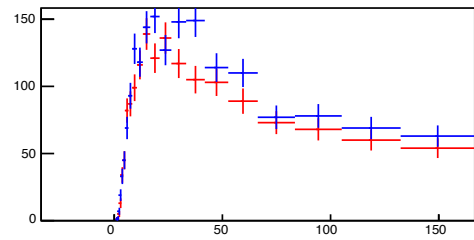
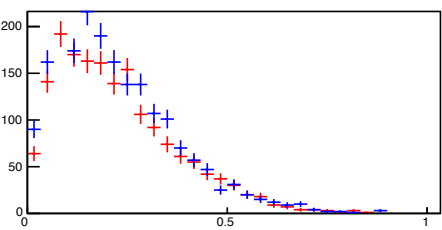
$\tau_{\text{form}}$  (fm)

$K_{\text{perp}}$  (GeV)

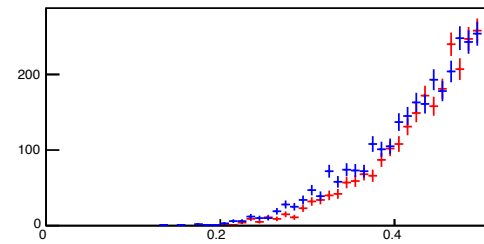
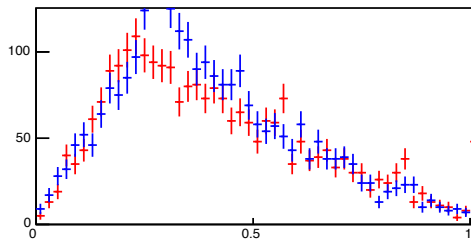
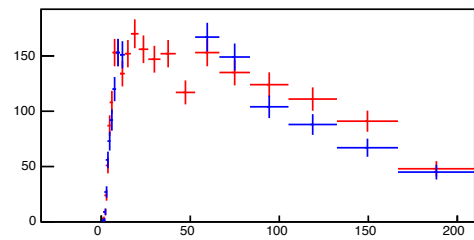
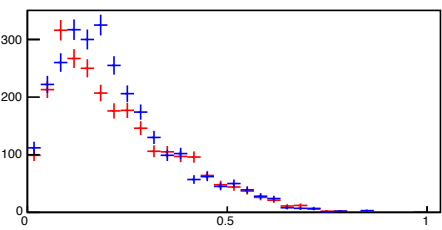
$z$

# $\pi K$ vs $K\pi$

# of ++ or --



# of +- or -+



Opening angle (radian)

$\tau_{\text{form}}$  (fm)

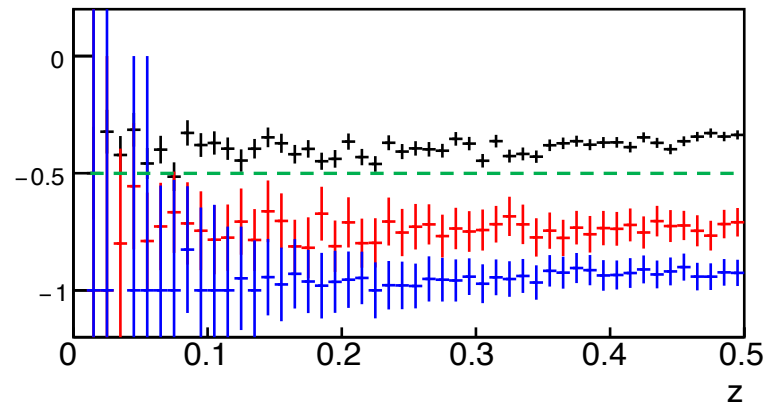
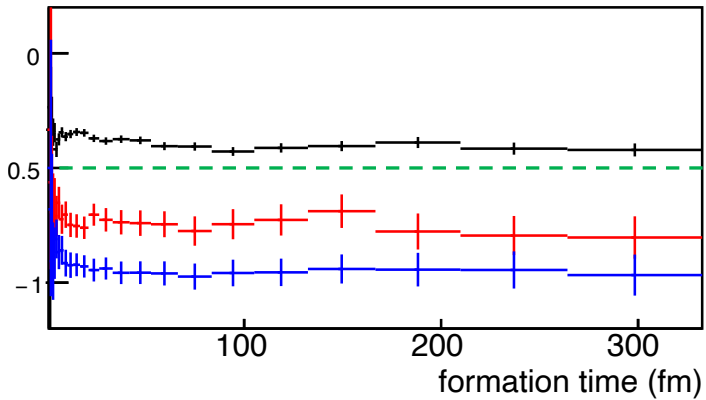
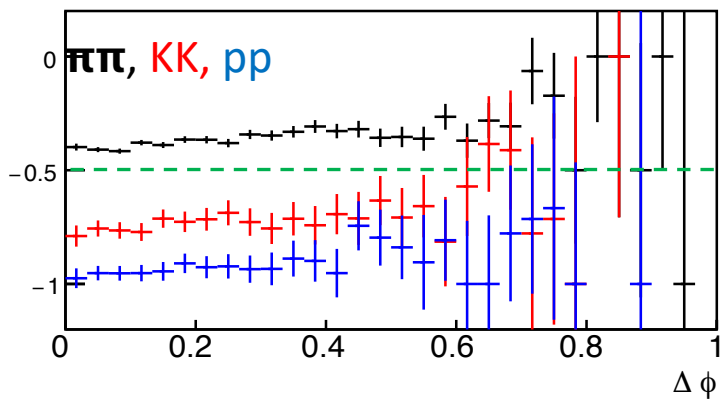
$K_{\text{perp}}$  (GeV)

$z$

9/14/20

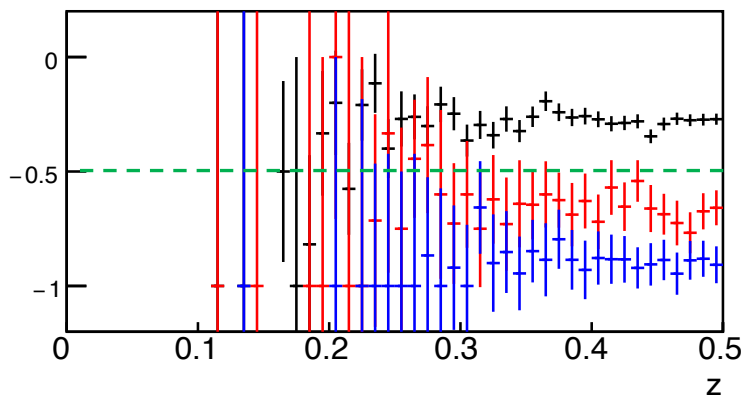
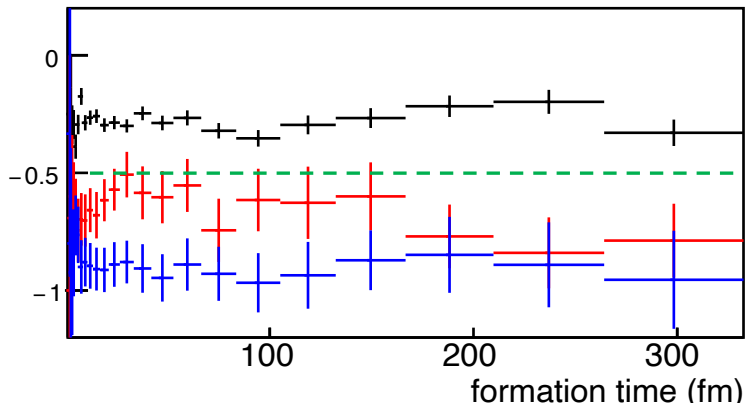
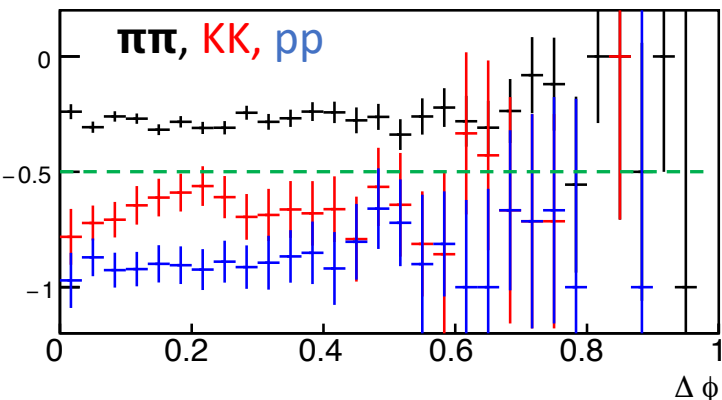
$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$

### NO momentum cuts



$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$

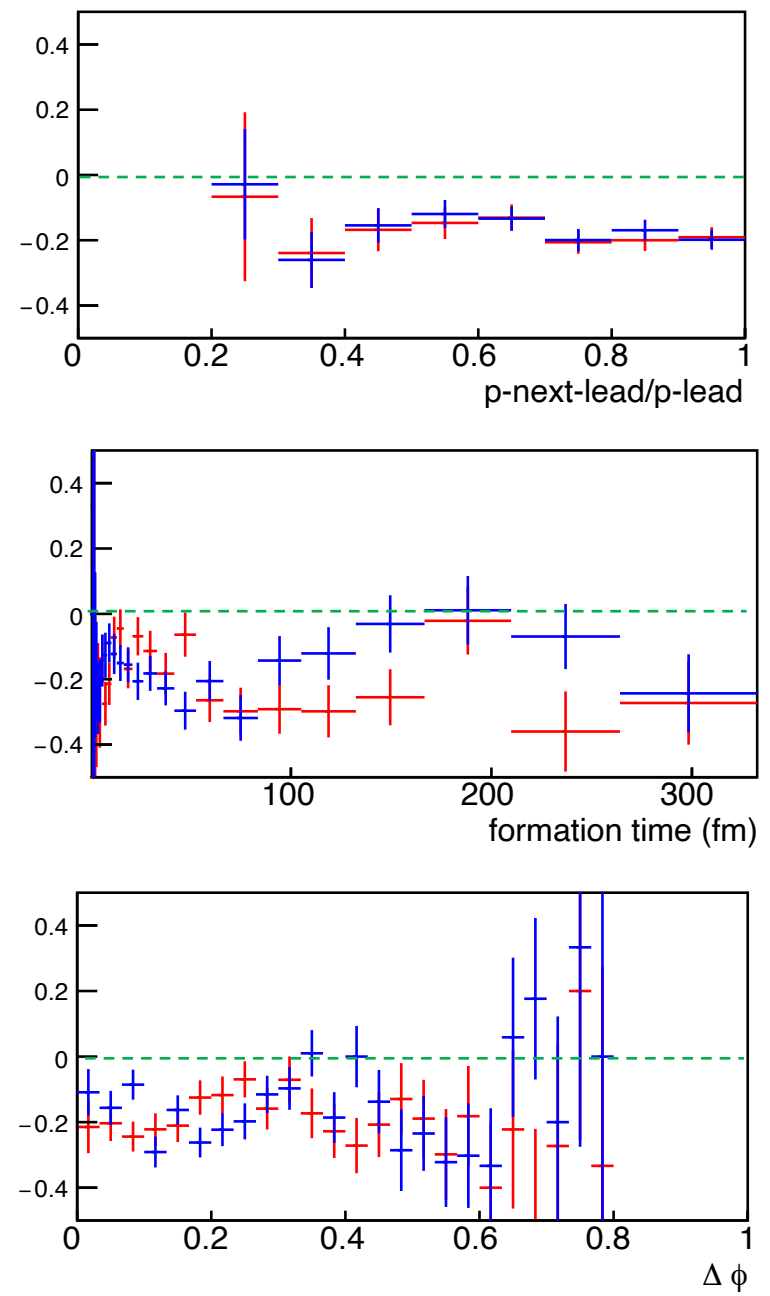
### After momentum cuts



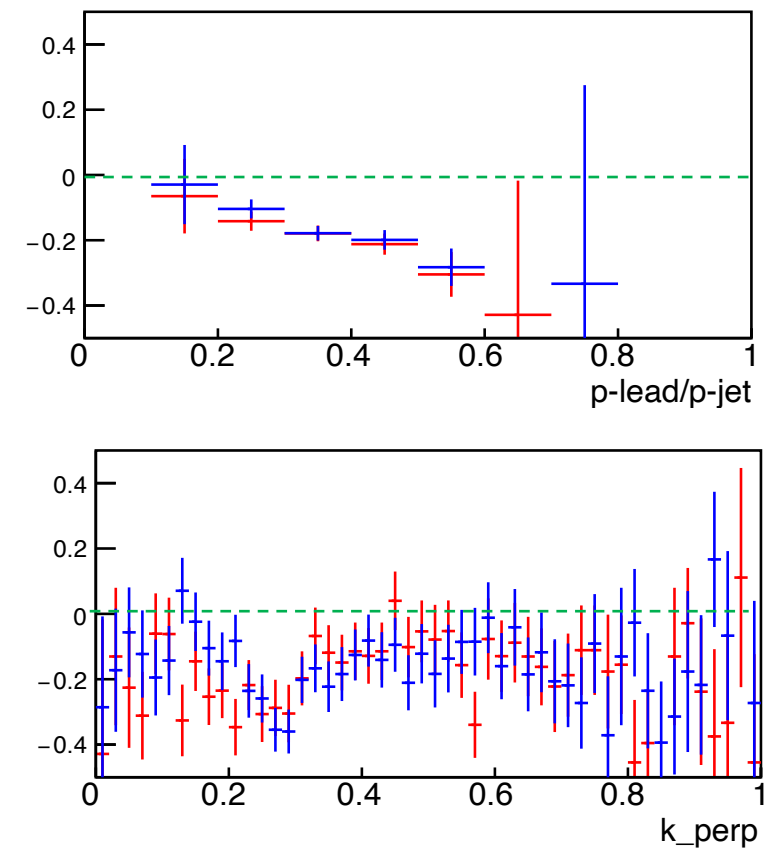
# $\pi K$ vs $K\pi$ - with p cut

(leading momentum particle is the first one)

$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$



$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$

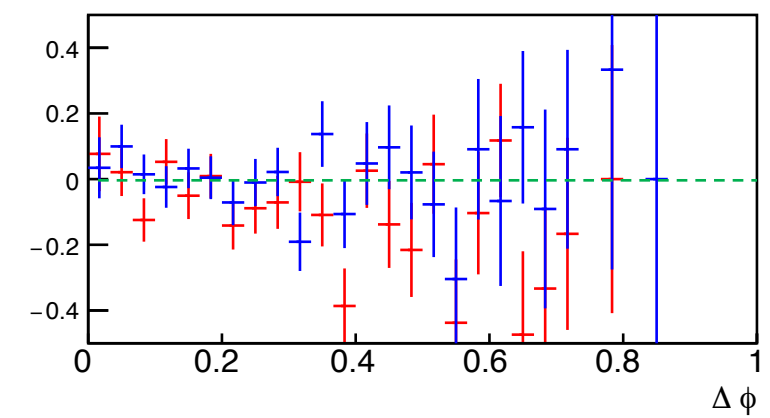
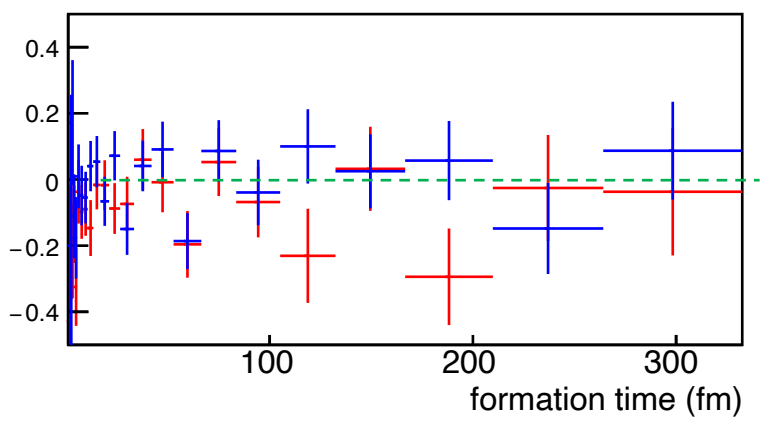
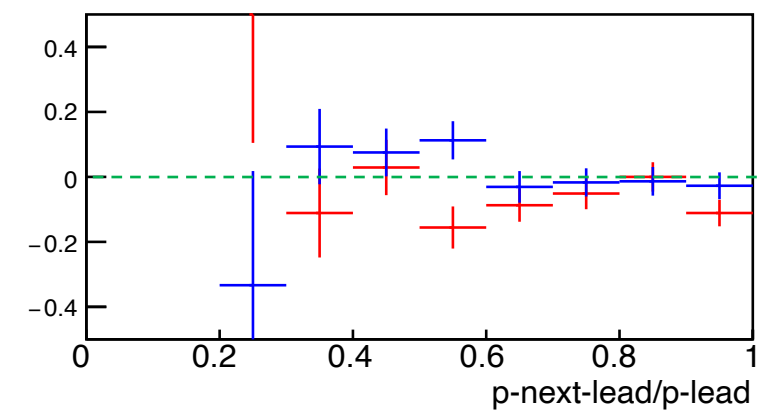




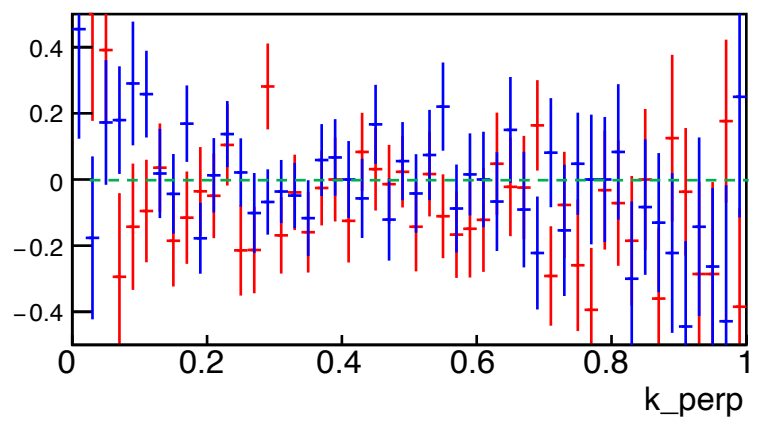
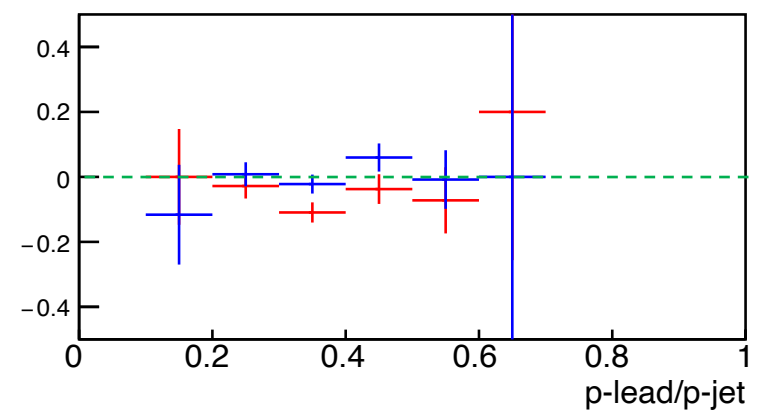
# $\pi P$ vs $P\pi$ - with p cut

(leading momentum particle is the first one)

$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$



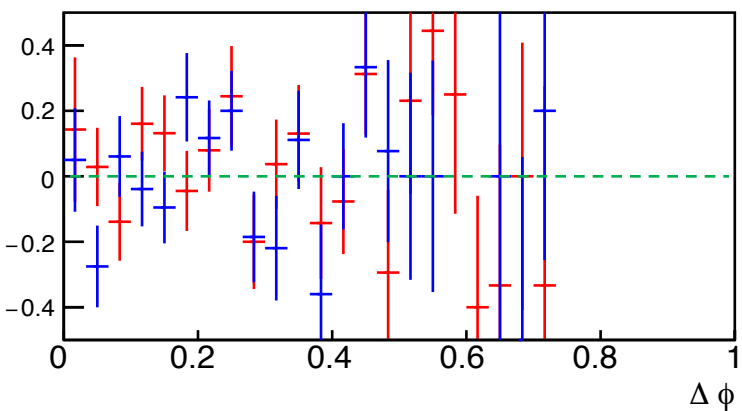
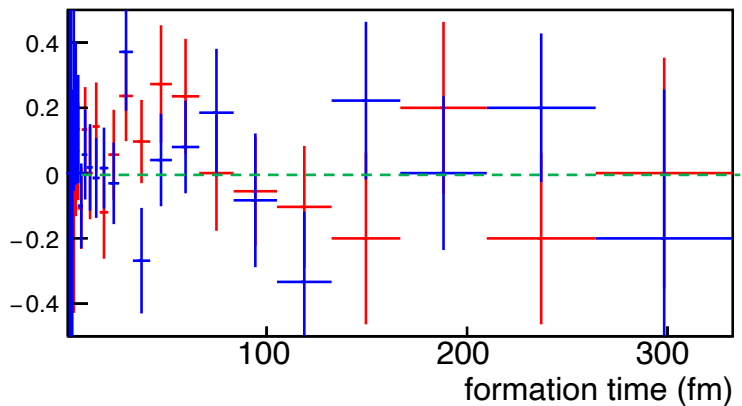
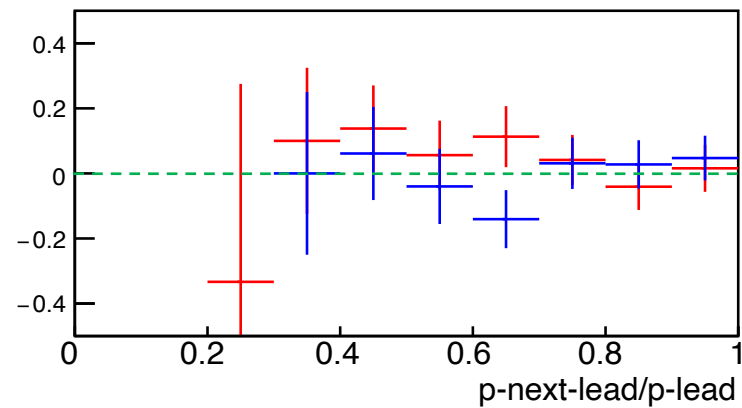
$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$



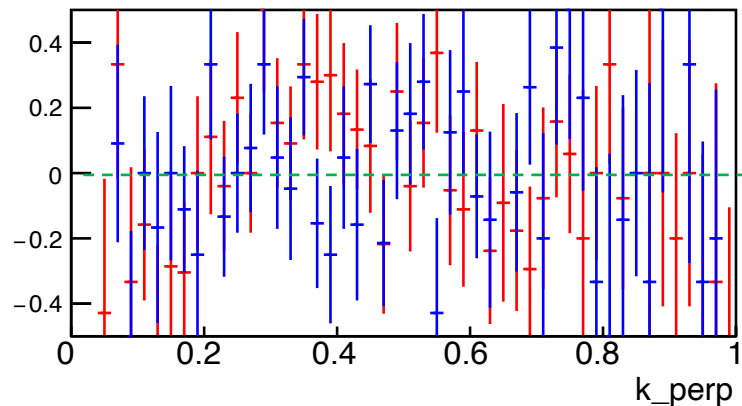
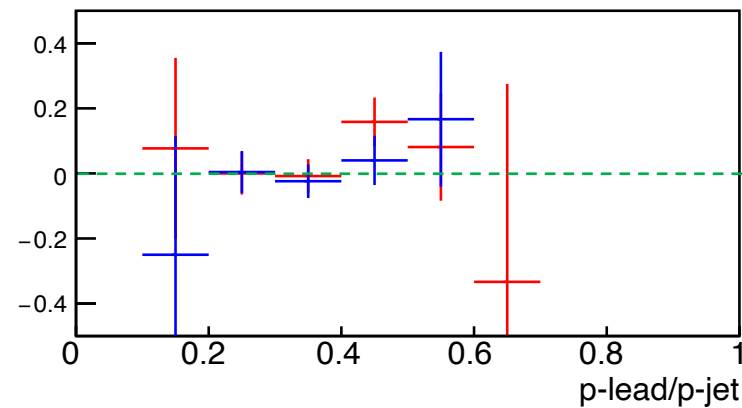
# Kp vs pK - with p cut

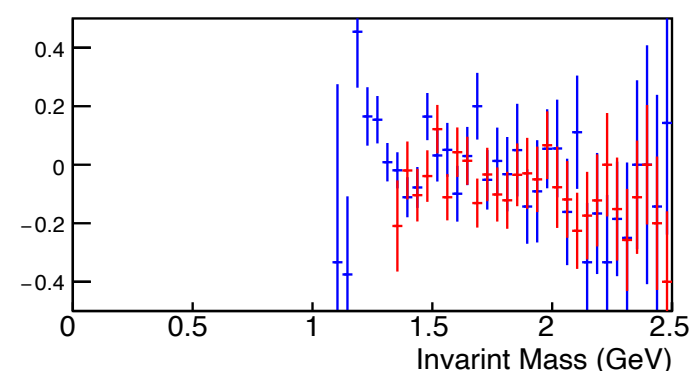
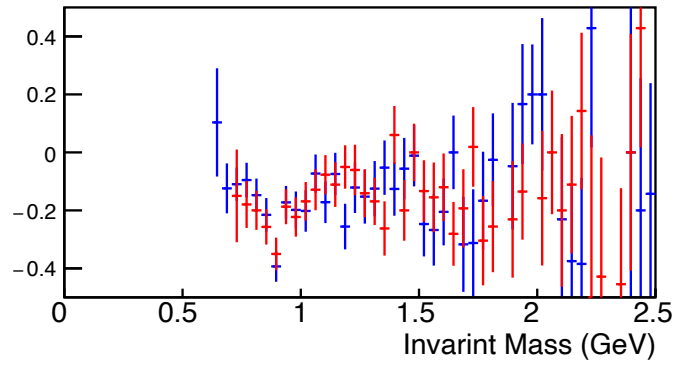
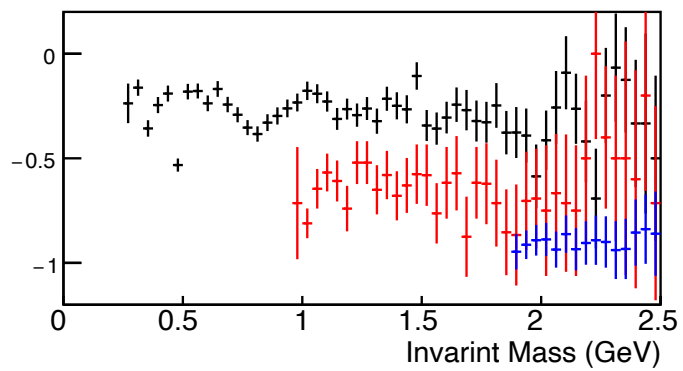
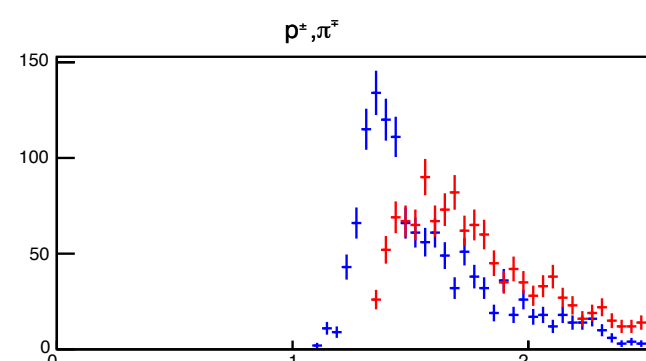
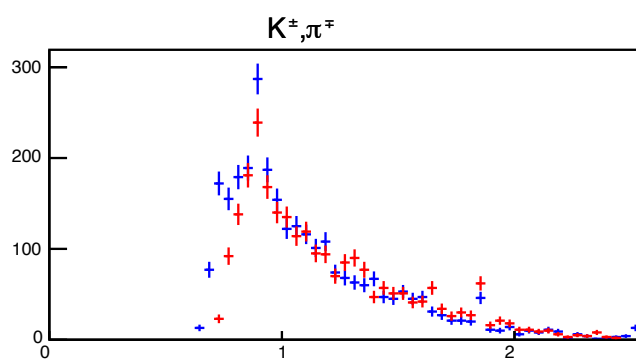
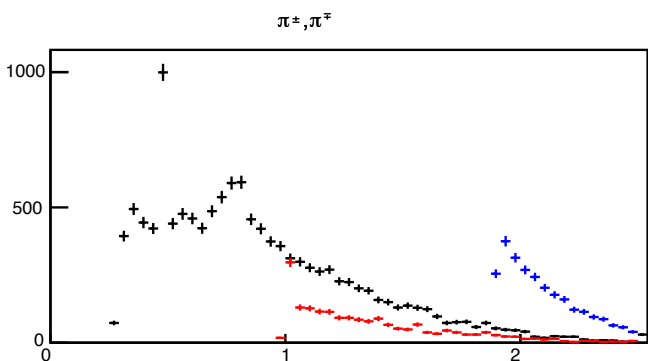
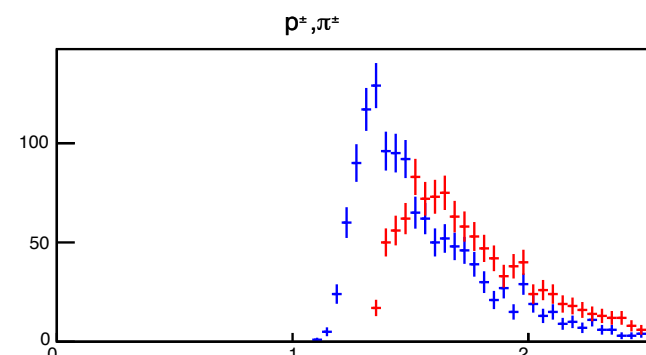
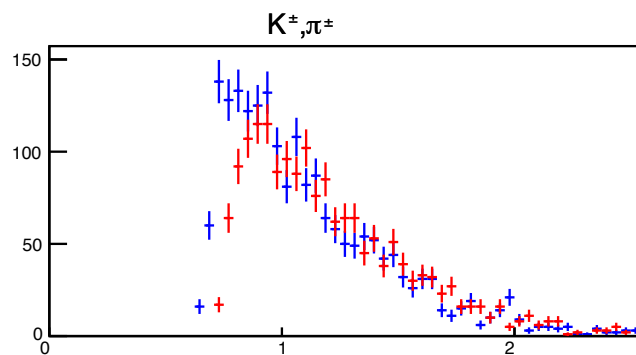
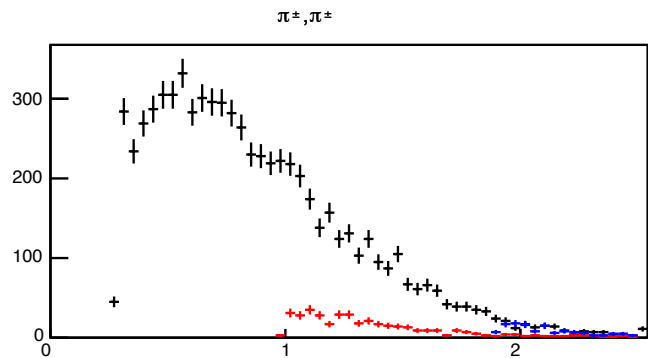
(leading momentum particle is the first one)

$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$



$$r = \frac{(\# \text{ of } ++ \text{ or } --) - (\# \text{ of } \pm \text{ or } \mp)}{\text{total pairs}}$$





$$Q^2 = 65 \text{ GeV}^2$$

$$\text{Maximum Cross section} = 2.2 \times 10^4 \text{ mb}$$

$$2.2 \times 10^{-4} \text{ mb}$$

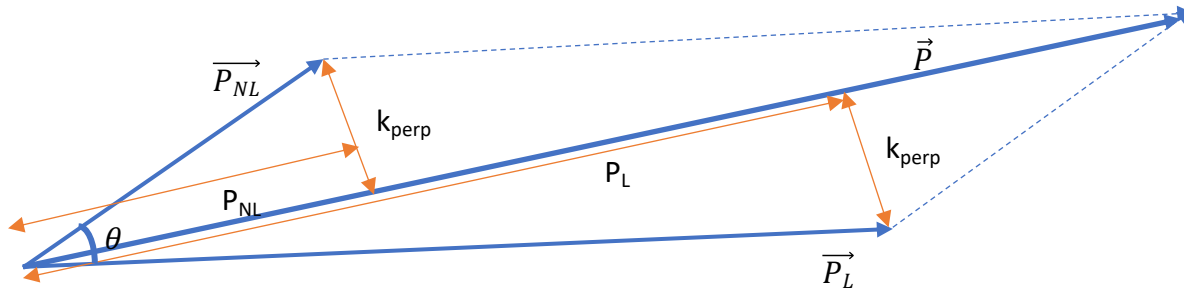
$$2.2 \times 10^8 \text{ fb}$$

$$\text{Integrated luminosity} = 10 \text{ fb}^{-1}$$

$$= 2.2 \times 10^9 \text{ events}$$

$$= 2200 \text{ M events}$$

# Formation time



$$z = P_{NL} / (P_{NL} + P_L)$$

$$P_L = (1-z)P$$

$$P_{NL} = zP$$

$$\text{formation time} = [2z(1-z) P] / k_{\text{perp}}^2$$

What is the interpretation of tau\_form?

It's the inverse of the "energy deficit" in the lab frame if we imagine that two massless particles with 3-momenta  $\vec{P}_L$  and  $\vec{P}_{NL}$  emerged from the decay of an off-shell massless particle with total momentum  $\vec{P}$ .

Long formation times should correspond to particles that "stayed together" for a long time before separating.

