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# Heavy flavor production at hadron colliders

## Simplified ACOT scheme with Massive Phase Space (S-ACOT-MPS)

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In collaboration with  
**John Campbell** (Fermilab) and **Pavel Nadolsky** (SMU),  
SMU-HEP-18-03, 21xx.xxxxx,  
SMU PhD. Thesis [\[link\]](#)

Snowmass2021 LoI: **Constraining heavy flavor PDFs at hadron colliders**

**Authors in alphabetical order:** Marco Guzzi, Timothy Hobbs, Pavel Nadolsky, Laura Reina, Doreen Wackerroth, Keping Xie, C.-P. Yuan

### Thematic Areas:

(EF03) EW Physics: Heavy flavor and top quark physics,  
(EF06) QCD and strong interactions: Hadronic structure and forward QCD

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### Abstract

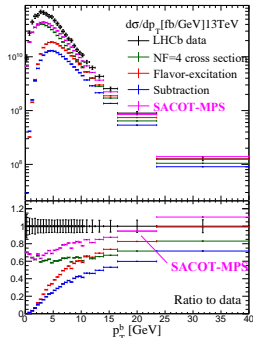
In this letter of interest, we discuss the possibility of constraining heavy-flavor parton distribution functions (PDFs) in the proton using heavy-flavor initiated processes at hadron colliders in global QCD analyses.

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## S-ACOT-MPS

### The Simplified ACOT scheme with Massive Phase Space

- Keping Xie (PITT PACC)
- John Campbell (Fermilab)
- Pavel Nadolsky (SMU)



# HF at hadron colliders

Data:

- heavy-flavor jet production, UA1, DØ, CDF, ATLAS, CMS
- Heavy-flavor hadron ( $D$ ,  $B$ -meson) production, especially LHCb

Theoretical interests:

- pQCD: factorization theorem, scale uncertainty, fragmentation, etc.
- PDF: Forward heavy flavor production probes gluon PDF at small  $x$ .

$$x \sim \frac{m}{\sqrt{s}} e^{-y} \sim 10^{-6}.$$

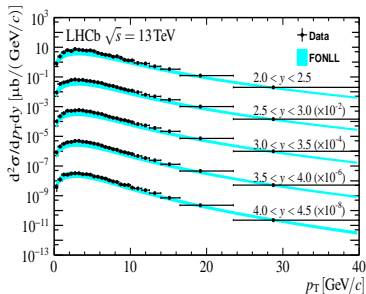
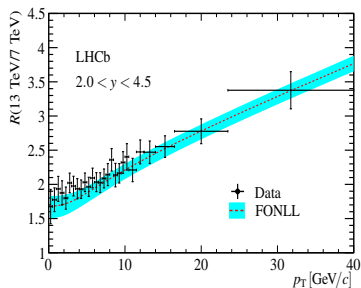


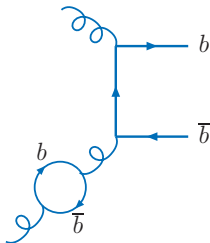
Figure: The  $D^0$  [1510.01707] and  $B^\pm$  [1710.04921] meson production at the LHCb 13 TeV.

## Fixed Flavor Number (FFN) scheme

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For consistency, we should take  $N_f = 3(4)$  for charm(bottom) flavor production, in both  $\alpha_s$  and PDF running.

- The heavy-quark running in the virtual loops is missing.
- No Flavor Excitation contributions as no heavy-flavor PDF.



Inconsistency when using  $N_f = 5$  PDF in MCFM, MadGraph\_aMC@NLO, POWHEG,

- $N_f = 5$  in the  $\alpha_s$  running, e.g. reading directly from LHAPDF;
- No FE contributions, equivalent to  $N_f = 3(4)$  in the PDFs.

We need treat heavy flavor consistently.

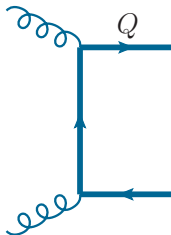
# Theory for heavy-flavor production

Energy scale  $Q$ , such as invariant mass  $M_{QQ}$  or  $p_T$

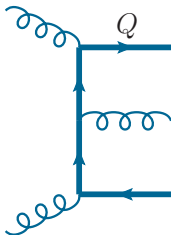
- $Q \lesssim m$  (low energy), Flavor Creation (FC), FFN scheme ( $N_f$ )
- $Q \gg m$  (high energy), Flavor Excitation (FE), Zero-mass (ZM) scheme ( $N_f + 1$ ), resum  $\alpha_s^m \log^n(Q^2/m^2)$  as heavy-flavor PDF
- $Q \sim m$ , **General-mass (GM) variable flavor number (VFN) scheme**  
**matching:** subtracting the double-counted terms (ACOT idea [\[PRD1994\]](#))

$$\text{VFN} = \text{FC} + \text{FE} - \text{SB}$$

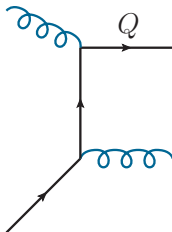
- $Q \lesssim m$ ,  $\text{FE} \simeq \text{SB}$ ,  $\text{VFN} \rightarrow \text{FC}$  FFN scheme
- $Q \gg m$ ,  $\text{FC} \simeq \text{SB}$ ,  $\text{VFN} \rightarrow \text{FE}$  ZM scheme



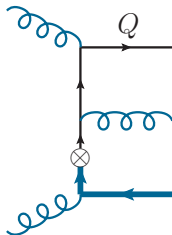
(a) FC LO



(b) FC NLO



(c) FE



(d) SB

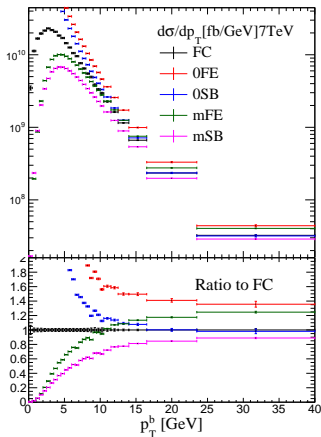
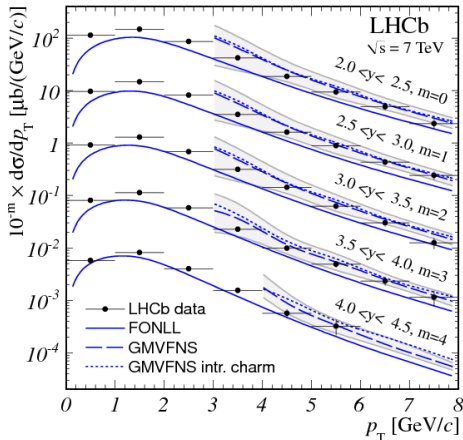
# Comparison among different VFN schemes

FONLL: Tune the matching function  $G(m, p_T)$  [9803400,0102134]

GM-VFNS: Impose a hard cut  $p_T \gtrsim m$  [0410289,11092472]

SACOT-mT: Choose a  $m_T$  dependence  $x_{\min}$  for the FE (SB as well) [1804.03557]

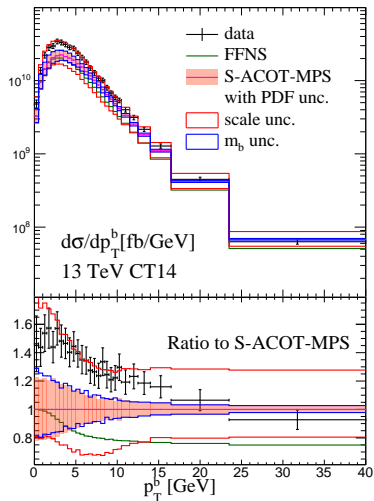
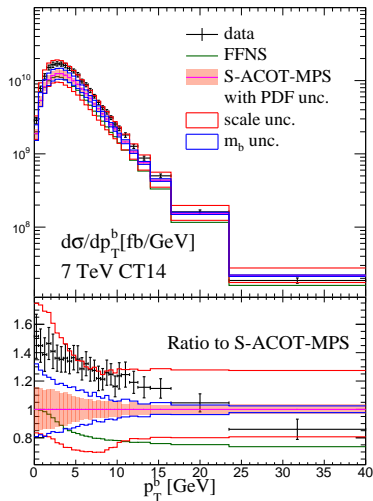
SACOT-MPS: **Massive phase space** tame the matching instability. [KX et al., SMU-HEP-18-03, KX, PhD Thesis], NLO implementation in MCFM in a fully differential way.



# SACOT-MPS vs. LHCb data: the $p_T^b$ distribution

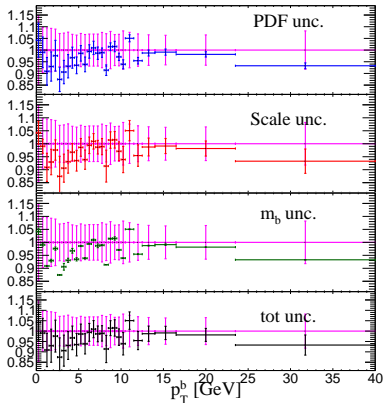
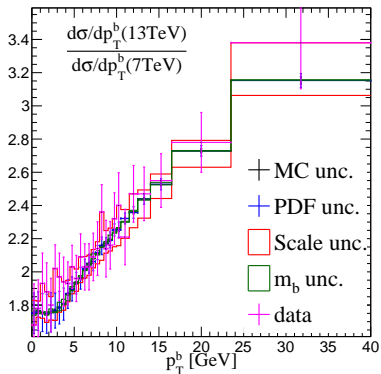
Scale  $(\mu_R, \mu_F) = (1/2, 1, 2)\sqrt{p_{T,b}^2 + m_b^2}$  uncertainty is large:

- $\alpha_s(\mu_R)$  is large and varies drastically around  $\mu_R \sim m_Q$ ,
- Heavy-flavor PDF  $f_Q(x, \mu_F)$  starts to be generated perturbatively at  $\mu_F = m_Q$ .



# The ratio observable $R(13\text{TeV}/7\text{TeV})$

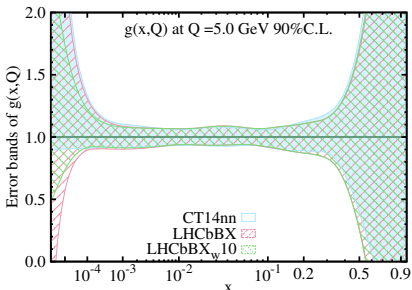
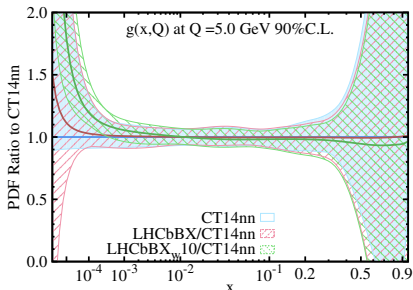
We introduce the ratio observables  $R_{\sqrt{s_1}/\sqrt{s_2}}(X) = \frac{\sigma(X, \sqrt{s_1})}{\sigma(X, \sqrt{s_2})}$  [M. Mangano 1206.3557], of which the theoretical uncertainties cancel, especially the scale uncertainty.





LHCbBX(w10): CT14 PDF updated with weight 1(10) LHCb  $B^\pm$  data.

Caveat: We treat the systematic errors as uncorrelated, since we do not have the full correlated uncertainties.



We observe the impact on gluon PDF, but still mild, because

- CT14 PDF describe the data very well,
- The **experimental uncertainties** are still large.

# Summary

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- We develop **SACOT-MPS** scheme for the heavy flavor production at hadron collider, which gives a good **cancellations** behaviors in both asymptotic limits:
  - $p_T \ll m_Q$ , the SB cancels the FE term, FFN scheme,
  - $p_T \gg m_Q$ , the SB cancels the FC term, ZM scheme.
- The calculation is implemented in MCFM in a **fully differential way**.
- We have obtained the **subtraction**  $\tilde{f}_Q = P_{Q \leftarrow g} \otimes g$  and **residual**  $f_{\text{res}} = f_Q - \tilde{f}_Q$  PDF, available on HEPForge [<https://sacotmps.hepforge.org>]
- The subtraction and residual PDFs can be easily applied to other heavy-flavor process, such as  $H/V + Q$  and extended to NNLO.
- Our calculations agree well with the LHCb  $B^\pm$  measurements.
- With theoretical uncertainties cancel significantly, the ratio observables impact the **gluon and HF** in the **small- $x$**  region. The precise data in next rounds can potentially provide strong constraints.
- Fast computation **grids** are generated, to be implemented in global PDF analysis.