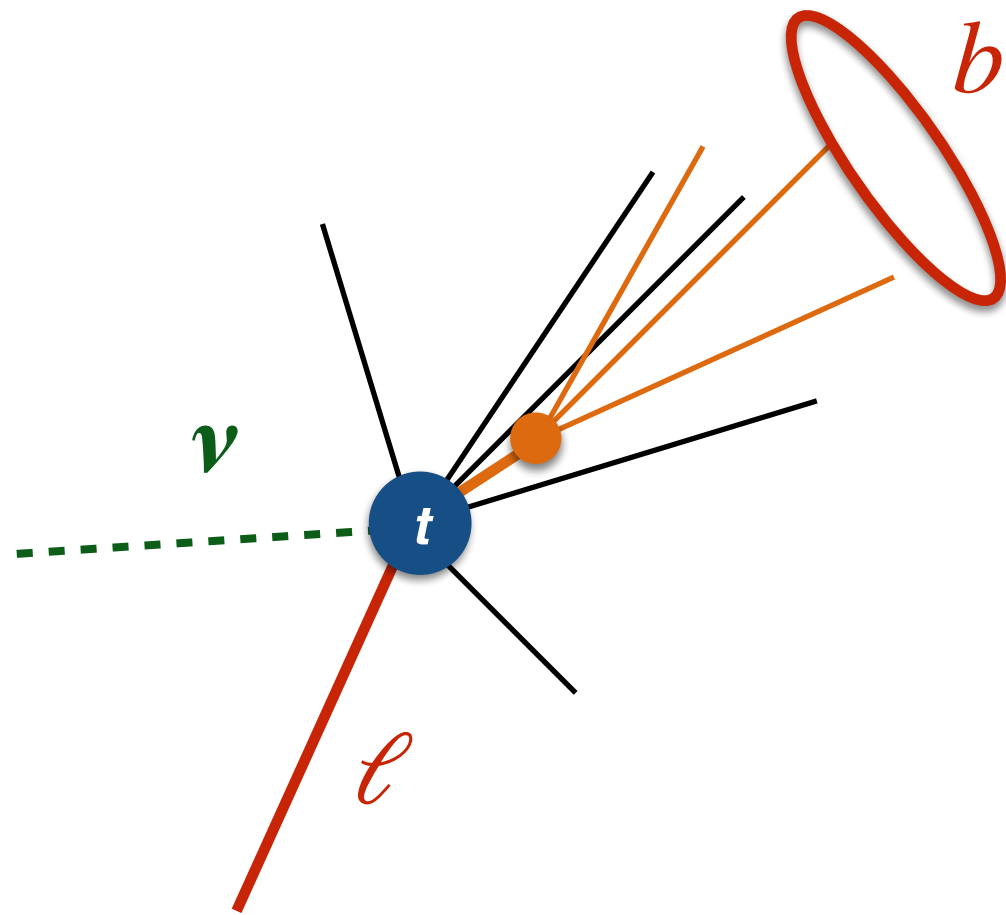


measuring b -fragmentation in $t\bar{t}$ events with ATLAS



Chris Pollard
on b -half of the ATLAS collaboration

DIS
2021 04 14

<https://cds.cern.ch/record/2730444>

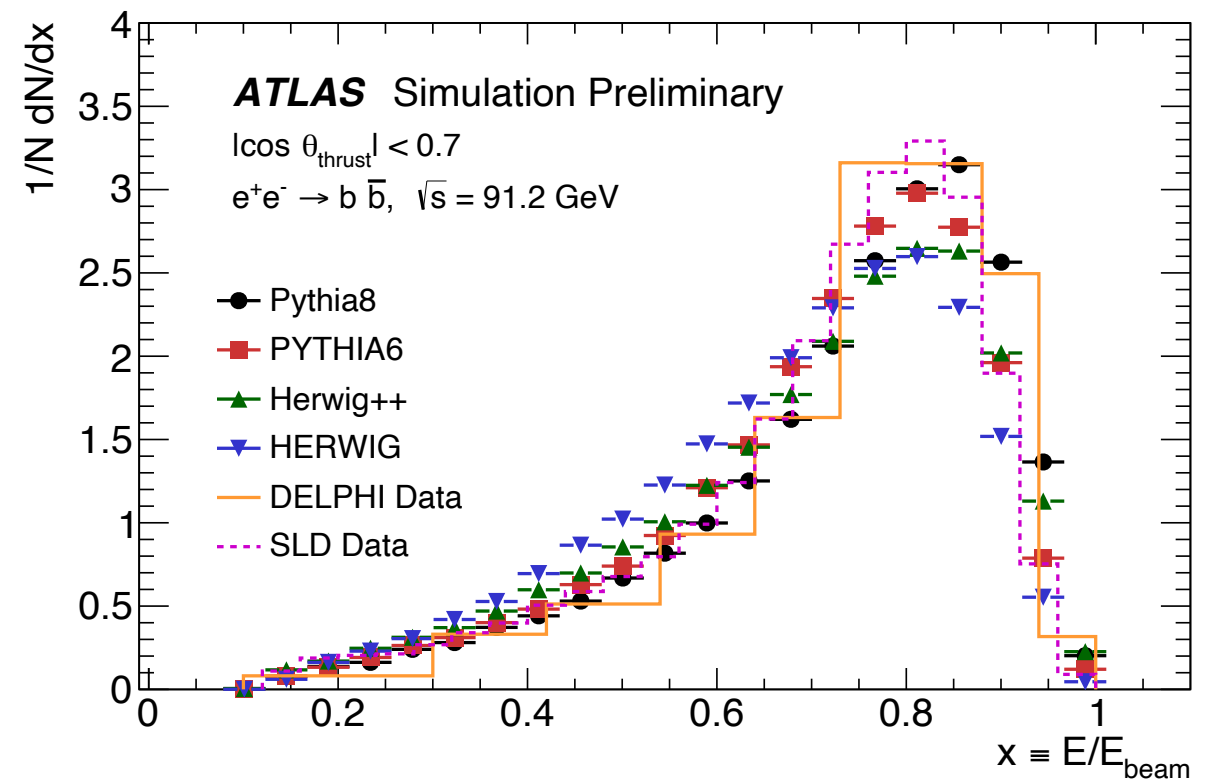
ATLAS-CONF-2020-050



motivation I

the fragmentation of b -quarks into hadrons is of interest for many reasons.

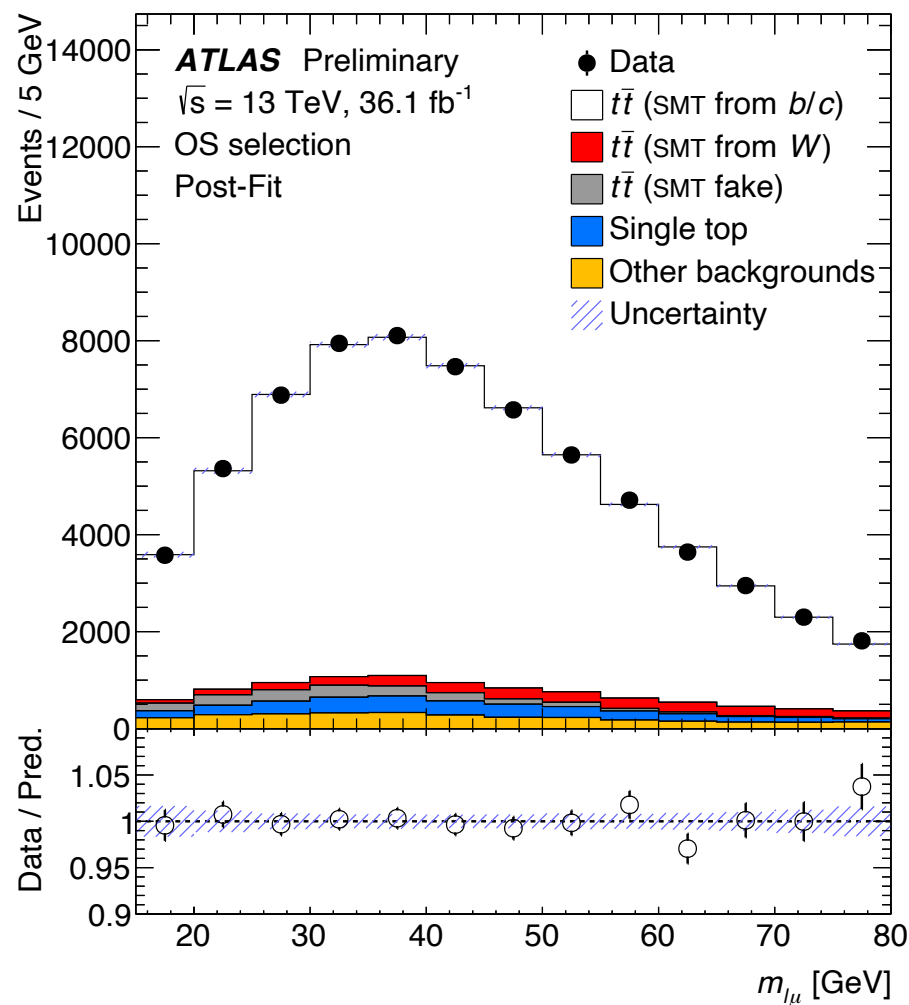
- b -hadrons leave a striking experimental signature and...
- a unique correspondence to the originating b -quarks
 - ergo a precise probe of QCD
- b -fragmentation currently tuned to e^+e^- data ...
- then extrapolated to the LHC environment
 - to what degree is this correct?



ATLAS-PHYS-PUB-2014-008

some tension between $e^+e^- \rightarrow b\bar{b}$ measurements of b -fragmentation
parton-shower generators are also not in good agreement

motivation II

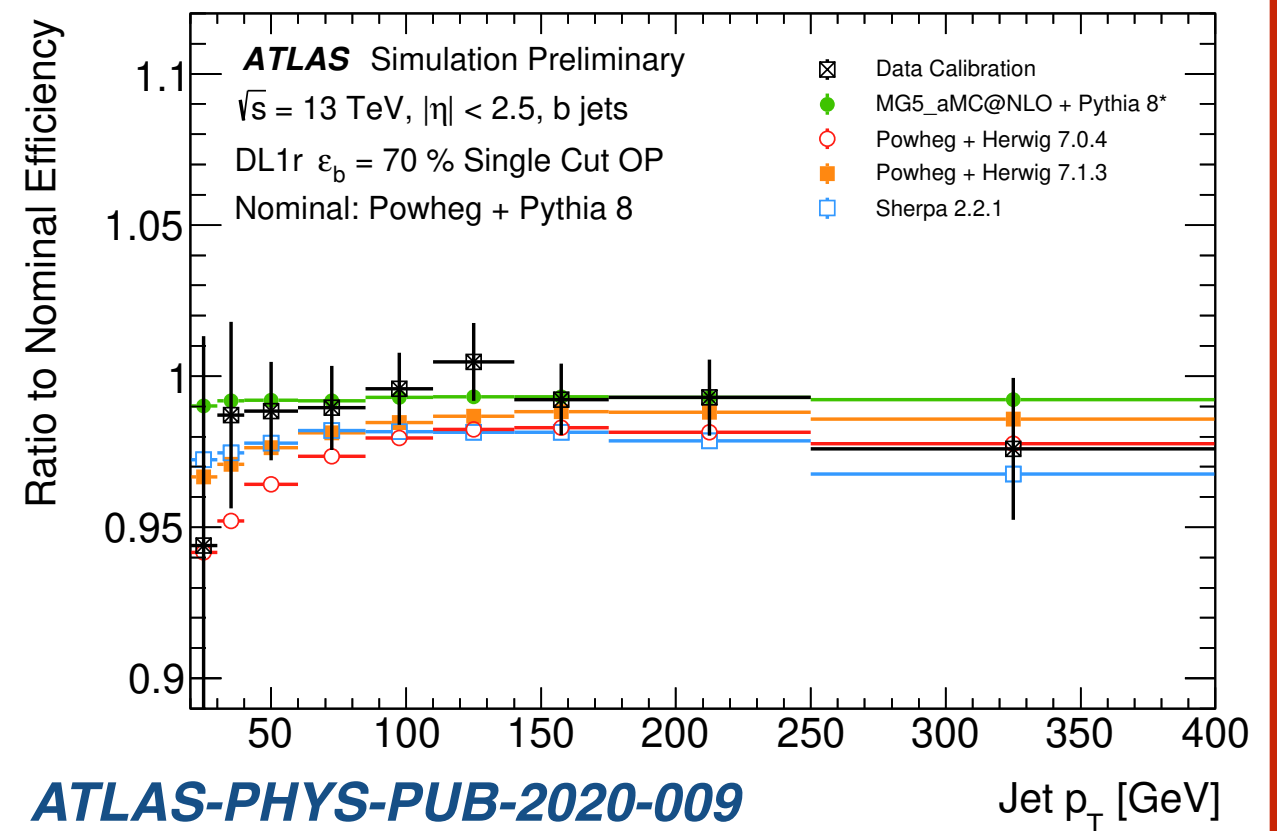


ATLAS-CONF-2019-046

$b \rightarrow \mu$ momentum transfer key for new top mass measurements, which rely on precise $b \rightarrow B$ prediction

critical for delivering the best LHC physics results with b -jets.

b -jet reconstruction and identification are very sensitive to b -fragmentation.



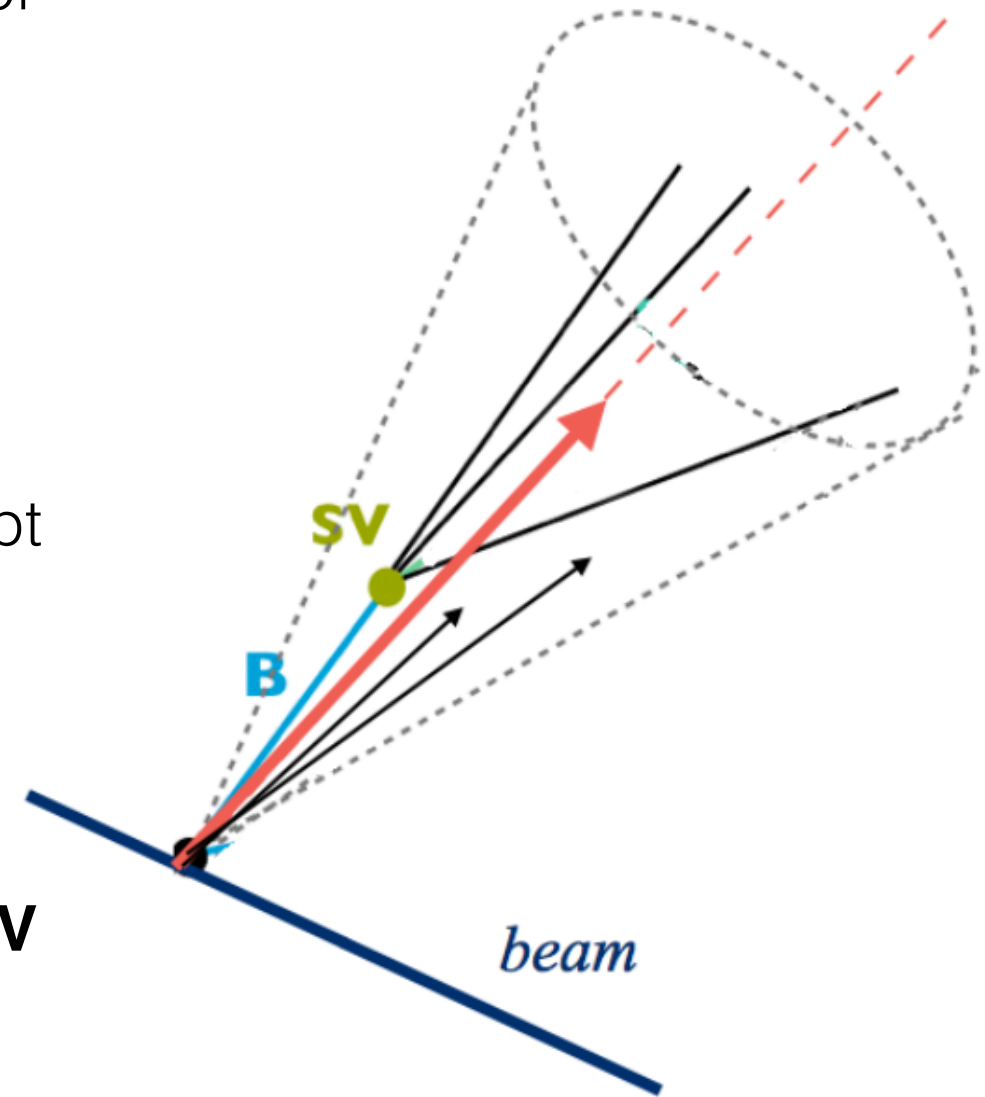
ATLAS-PHYS-PUB-2020-009

analysis strategy

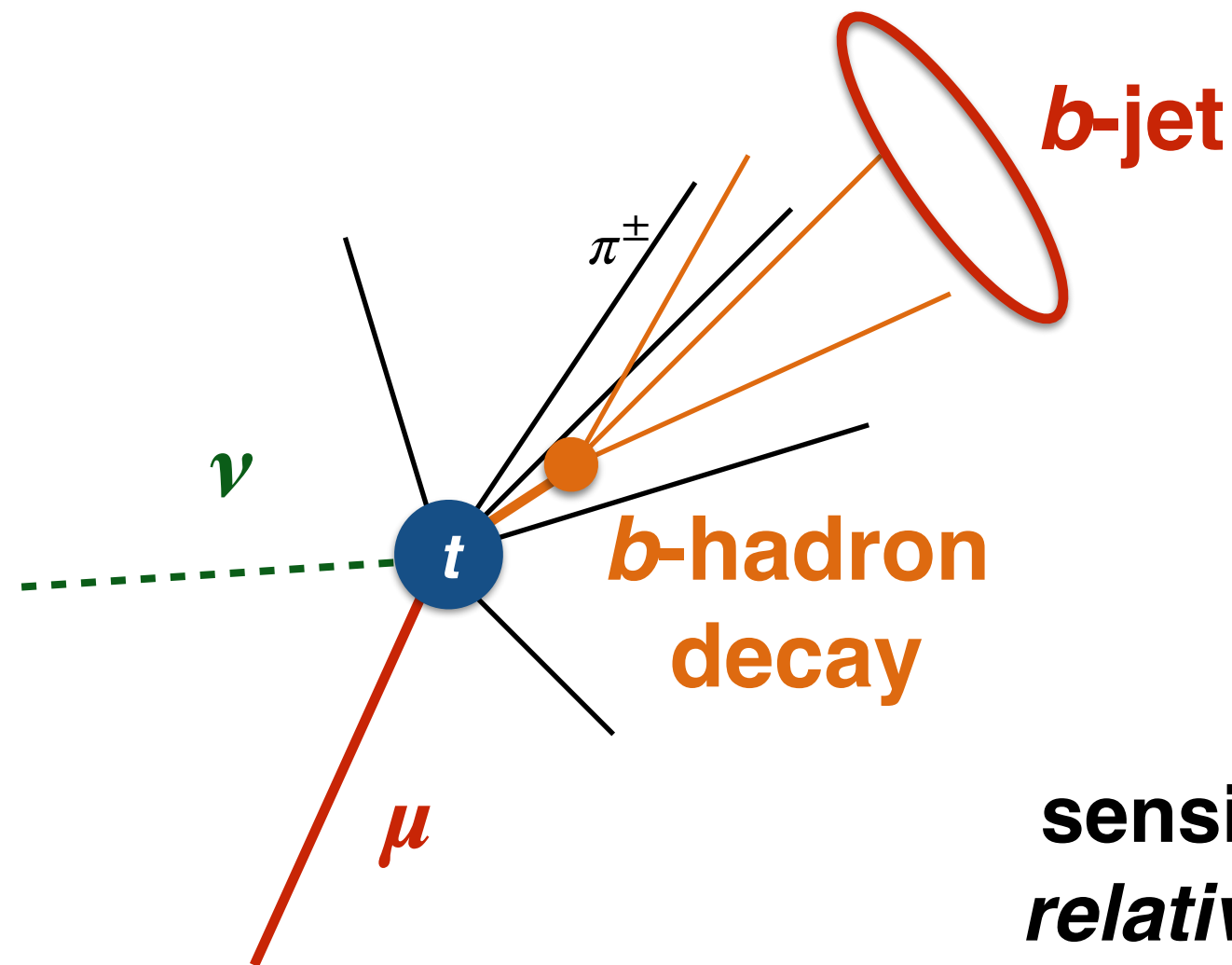
1. obtain sample of b -jets from $t\bar{t} \rightarrow e\mu\nu\nu bb$ events
2. identify b -hadron candidates using ATLAS single secondary vertex finder (SSVF)
3. measure properties of the b -hadron sensitive to the modeling of b -quark fragmentation, unfolded to particle level

fiducial definition

- $t\bar{t}$ events (single top is treated as background for ease of interpretation)
- $1\ \mu, 1\ e$
- exactly 2 b -jets with $|\eta| < 2.1, p_T > 30\ \text{GeV}, \Delta R(\text{jet}, \text{jet}) > 0.5$
 - jet of stable particles, excluding neutrinos and prompt leptons
 - 1 weakly-decaying b -hadron ($p_T > 5\ \text{GeV}$) with $\Delta R(\text{jet}, \text{hadron}) < 0.3$
- **sum over stable charged particles with $p_T > 500\ \text{MeV}$**
 - b -hadron decay products make up $\vec{p}_b^{\text{ch}}$
 - particles ghost-associated to jet make up $\vec{p}_{\text{jet}}^{\text{ch}}$



observables I



$$z_{L,b}^{\text{ch}} = \frac{\vec{p}_b^{\text{ch}} \cdot \vec{p}_{\text{jet}}^{\text{ch}}}{|p_{\text{jet}}^{\text{ch}}|^2},$$

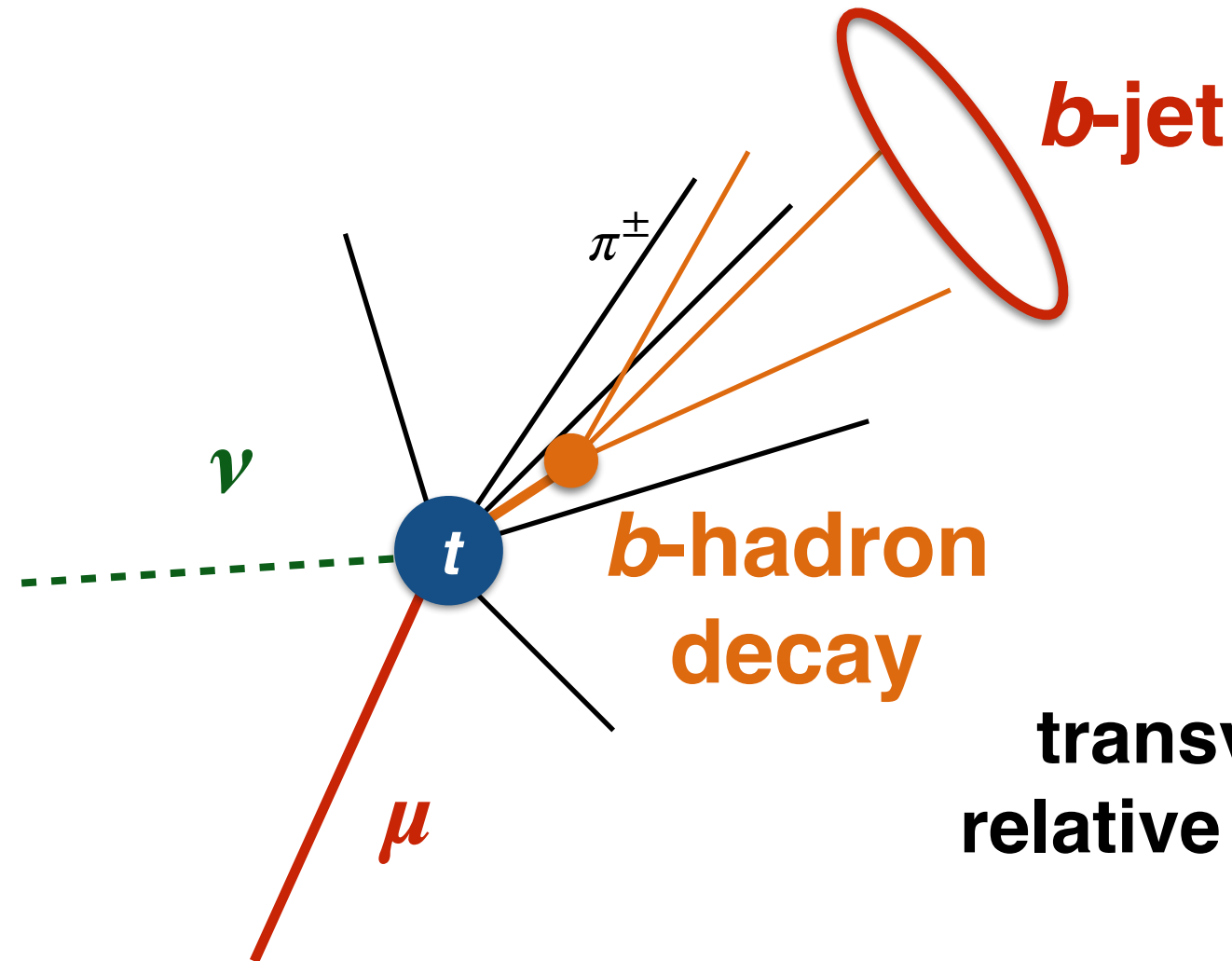
$$z_{T,b}^{\text{ch}} = \frac{p_{T,b}^{\text{ch}}}{p_{T,\text{jet}}^{\text{ch}}},$$

sensitive to momentum of b -hadron
relative to the local hadronic activity,

*e.g. the b -hadron momentum compared to
the b -quark momentum*

and related model parameters: r_B , α_S^{FSR}

observables II



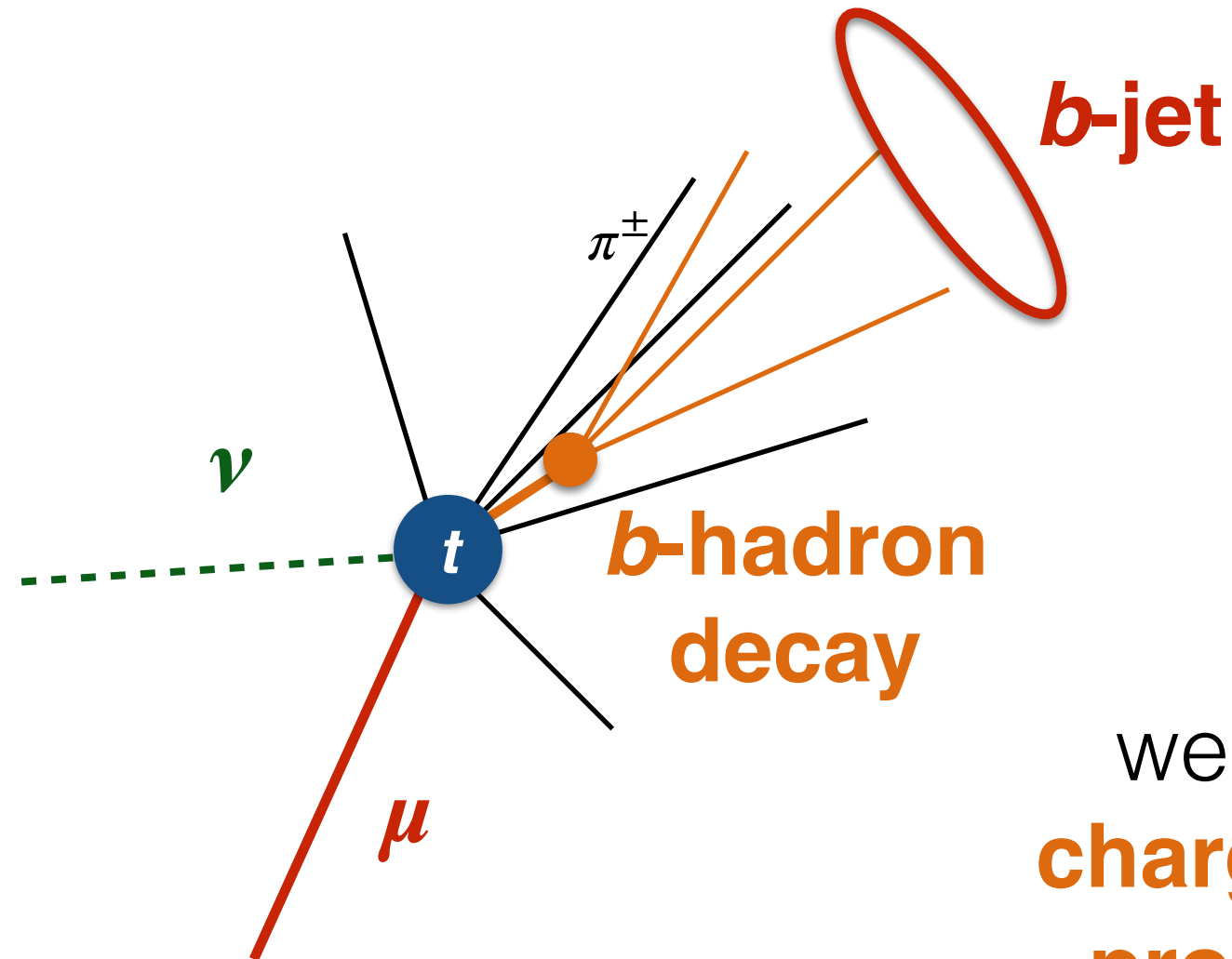
$$\rho = \frac{2p_{T,b}^{\text{ch}}}{p_T^e + p_T^\mu}$$

transverse momentum of b -hadron
relative to the average pt of the leptons
in the event

sensitive to choice of e.g. $\alpha_s(FSR)$ but **not** $\alpha_s(ISR)$

sensitivity also to wide-angle radiation
in top-quark decays

observables III



we also unfold the **number of charged, stable b -hadron decay products with $p_T > 500$ MeV.**

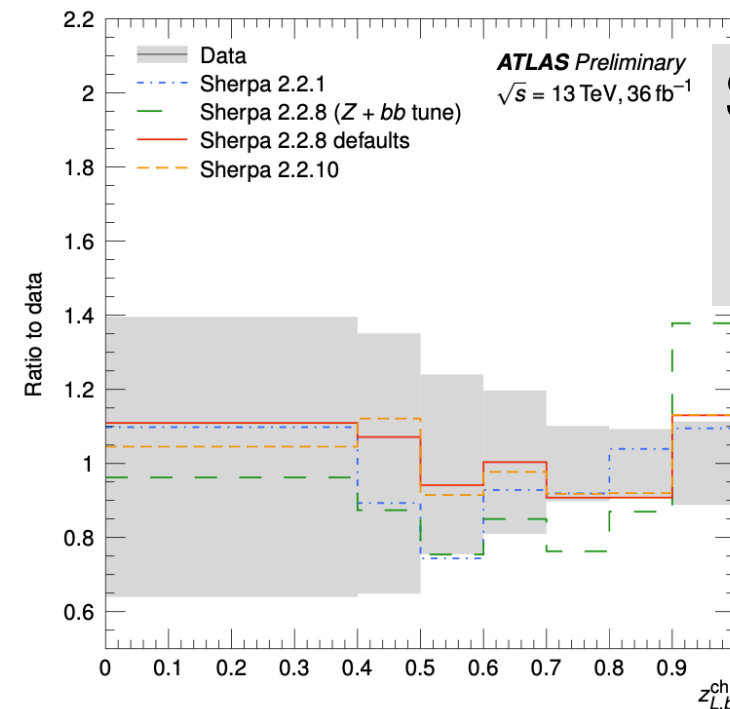
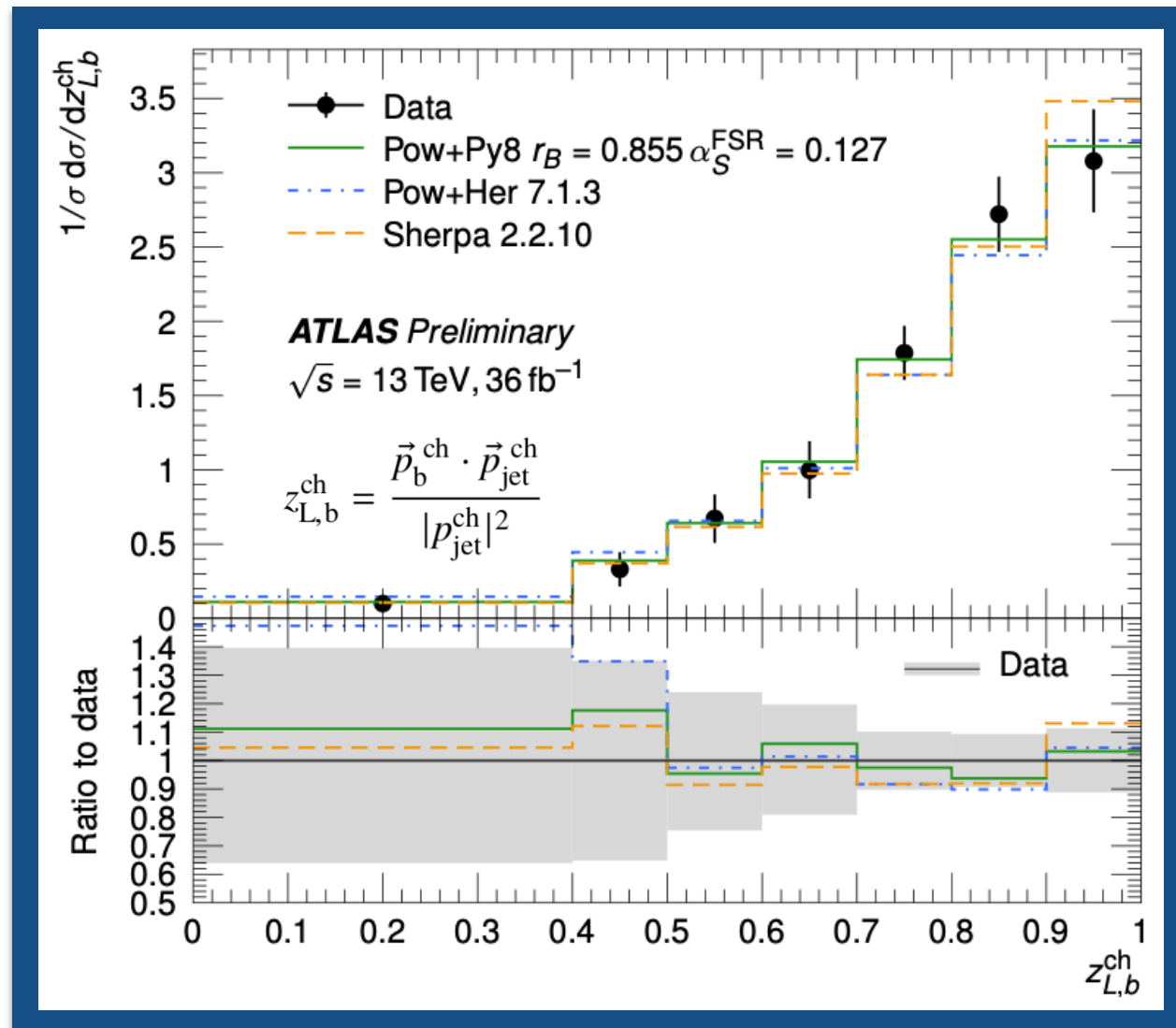
sensitive to the of b -hadron species production rates

systematic uncertainties

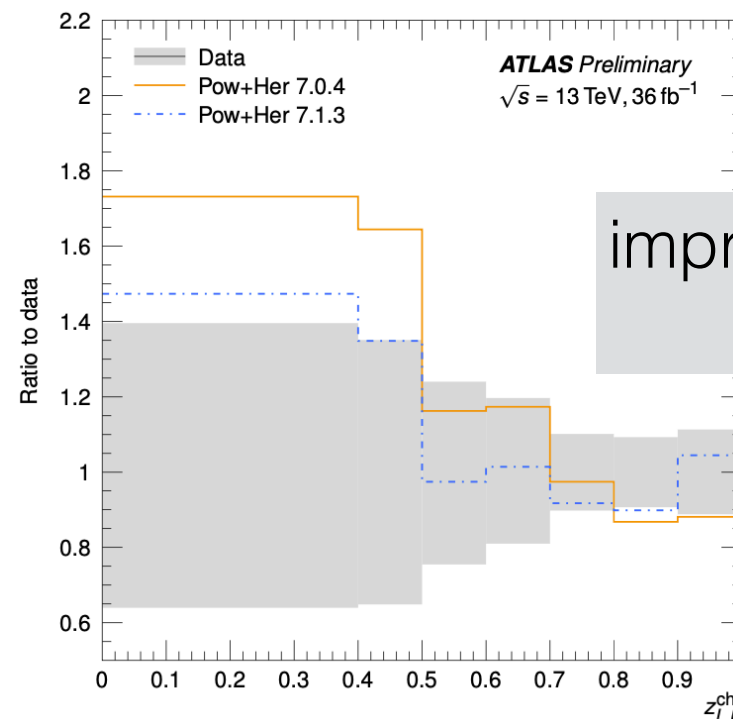
the dominant uncertainties in the unfolding model come from

- tracking efficiency and impact-parameter resolutions
- $t\bar{t}$ modeling:
 - Pythia vs Herwig
 - α_S^{FSR} tune variations
 - B production fractions
 - b -jet p_T mismodeling
- pileup modelling

fiducial data/MC comparisons I



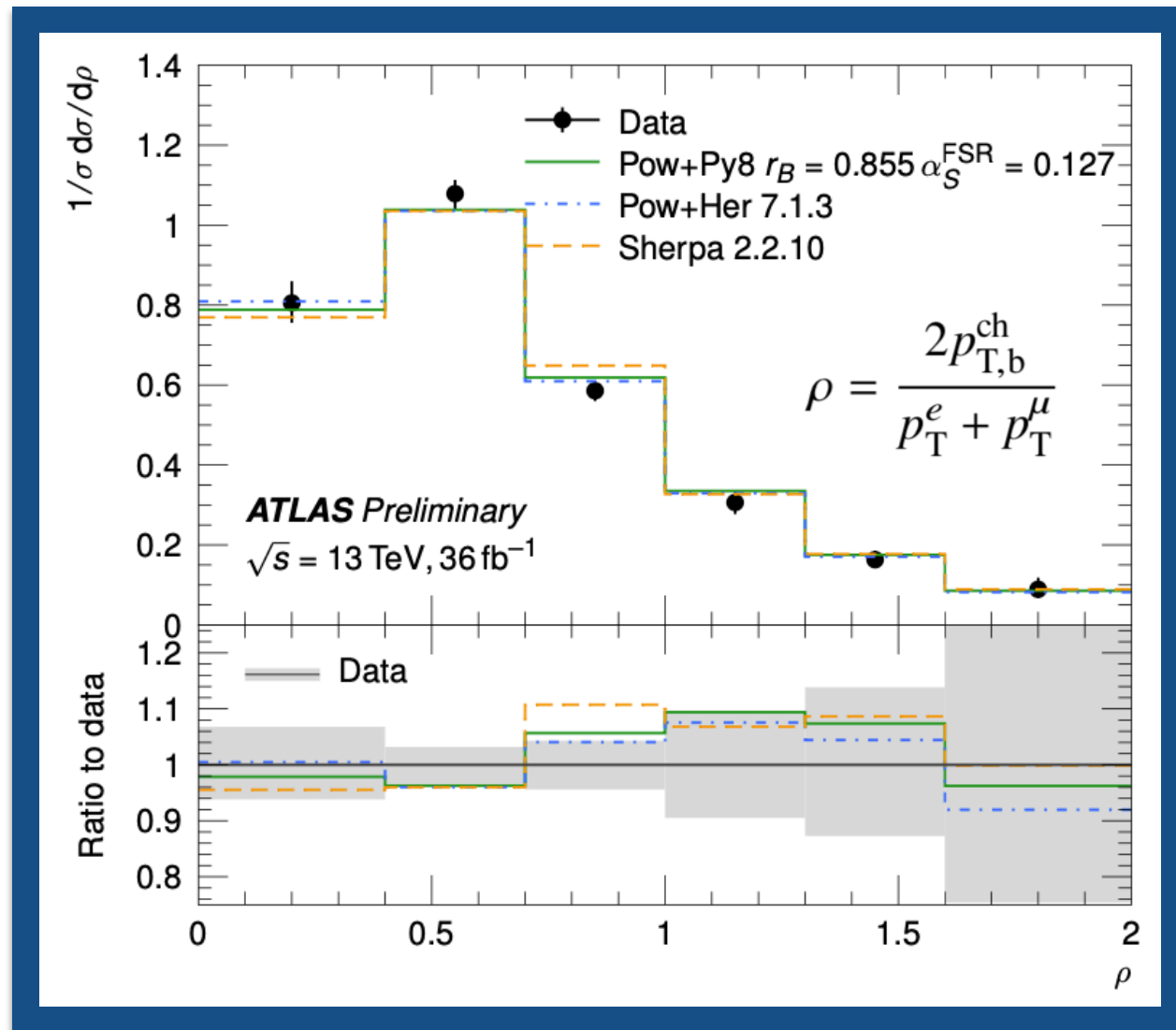
Sherpa: 2.2.10 with default tune looks good.



improvements in newer versions of H7

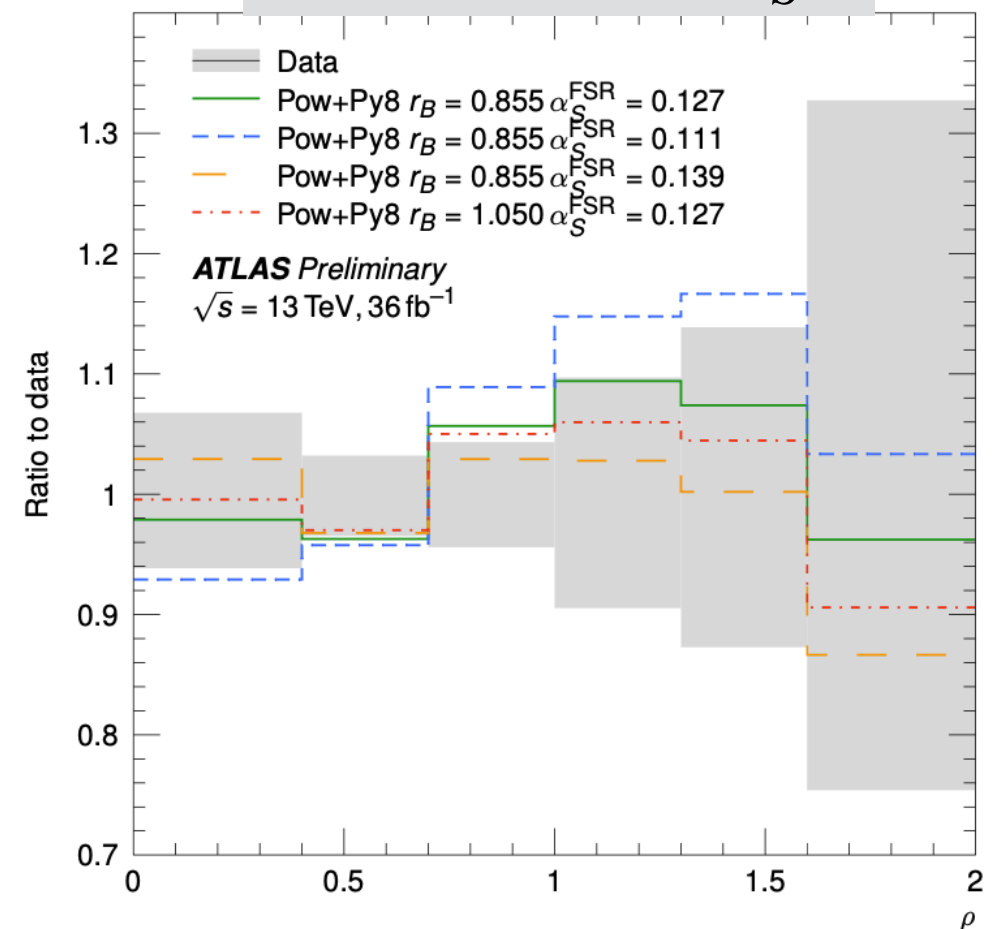
recent generator tunes
 to $e^+e^- \rightarrow Z \rightarrow bb$
 do a reasonable job.

fiducial data/MC comparisons II



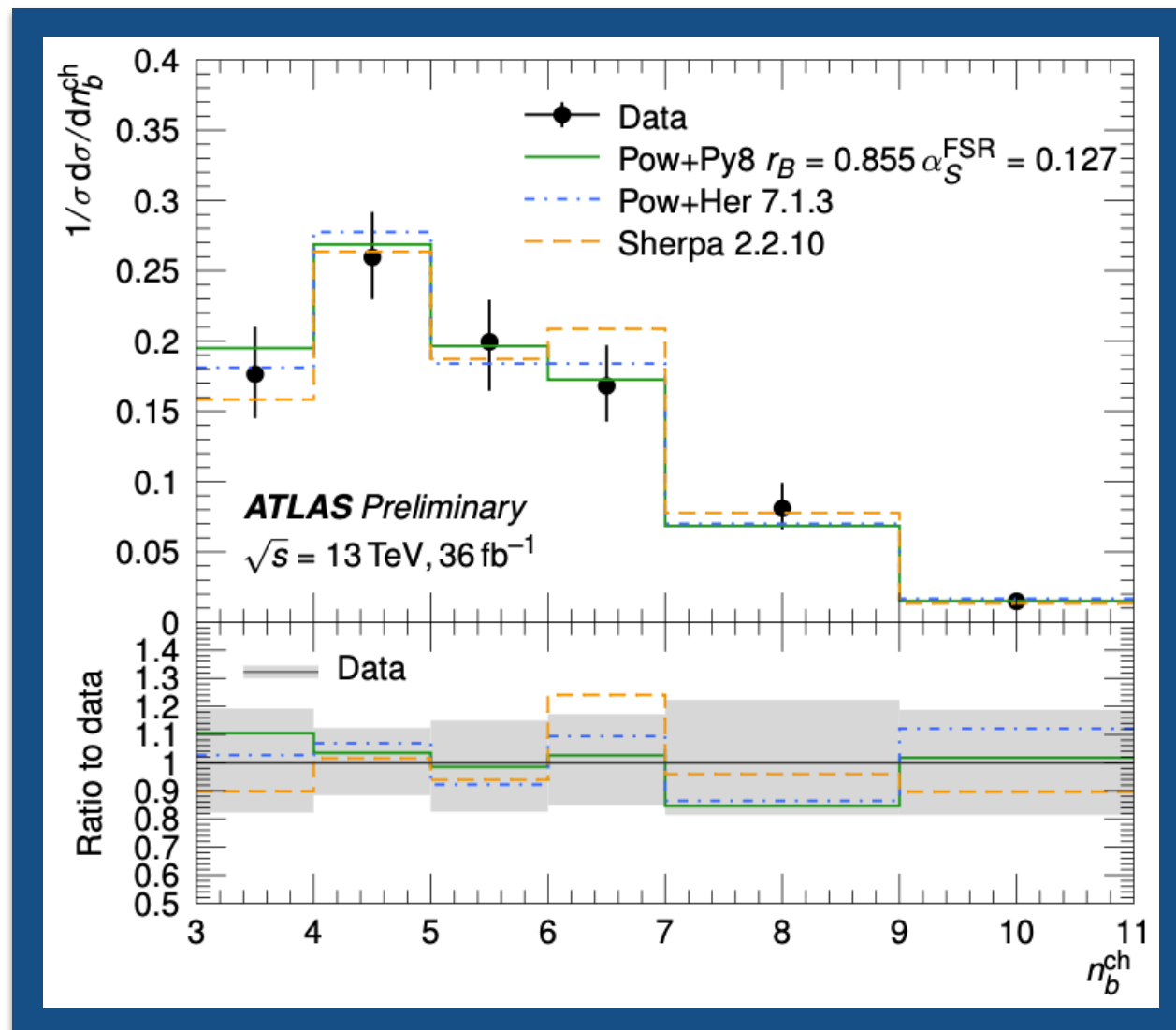
large impact from
A14 α_S^{FSR} variations

no sensitivity to α_S^{ISR}

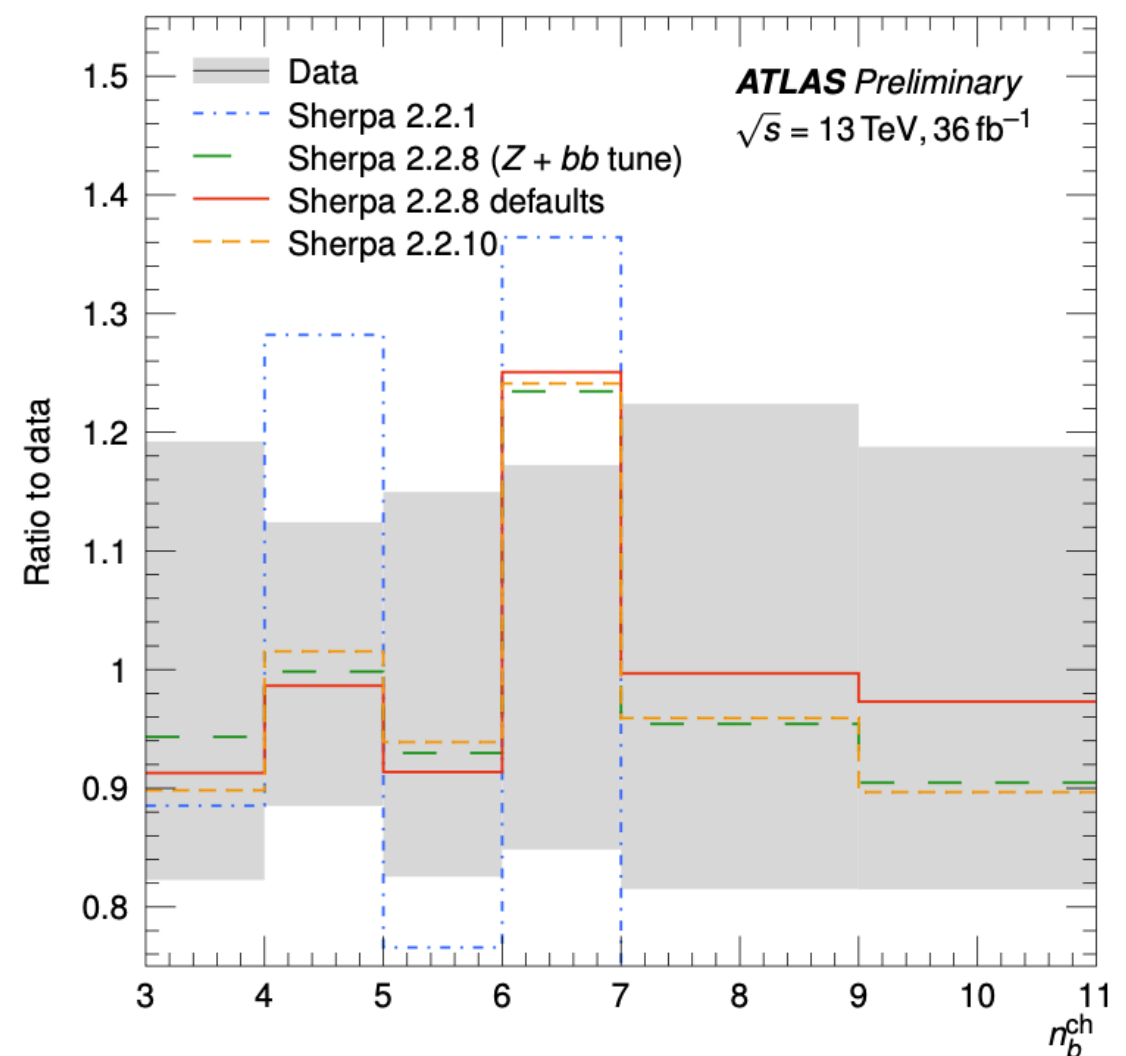


$\sim 1\sigma$ tensions
with recent generators
→ further investigation.

fiducial data/MC comparisons II



poor choice of heavy baryon enhancement
 in ATLAS's Sherpa 2.2.1 setup
 has now been fixed.

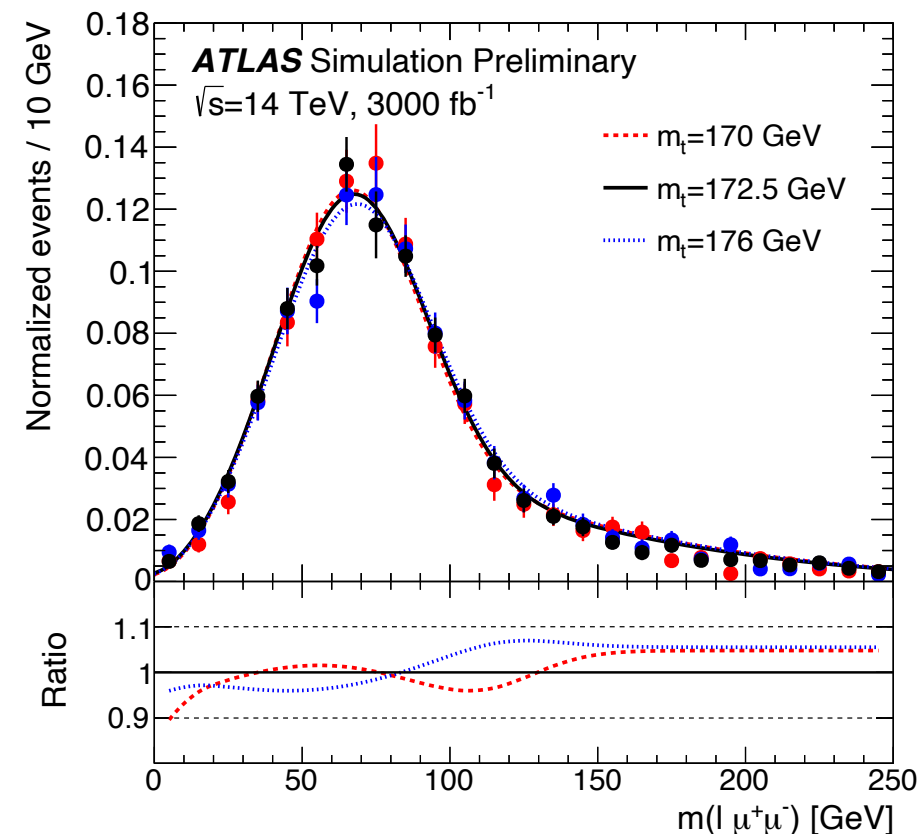
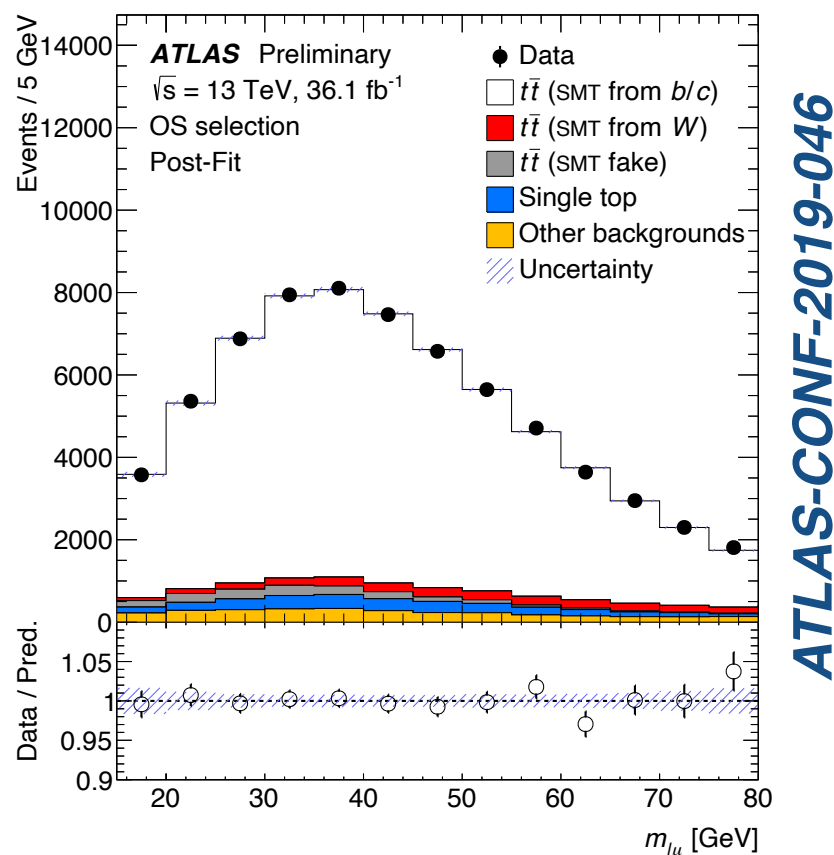


Py8/Her7 + EvtGen and
 Sherpa 2.2.10 all
 perform admirably.

impact: top mass

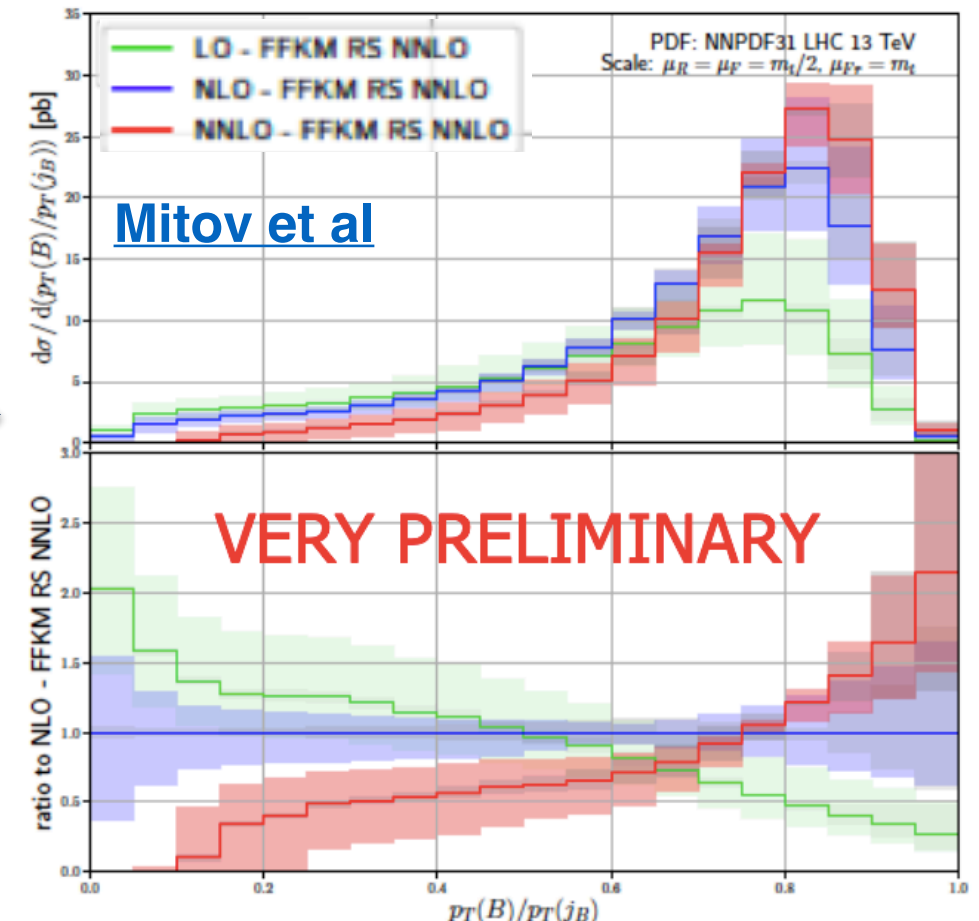
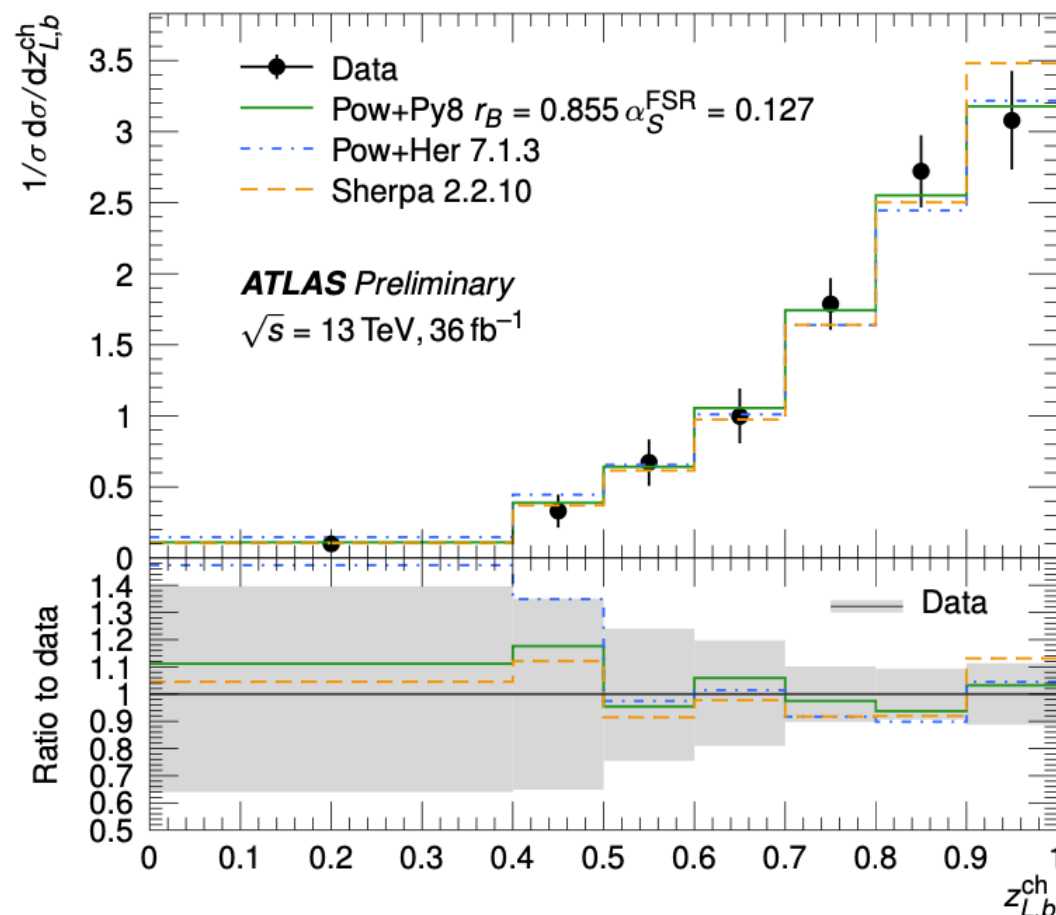
at our current precision, **generators well-tuned to $e^+e^- \rightarrow bb$ data yield good predictions in $t\bar{t}$ events and top-quark decays.**

- we now have unfolded data to guide our choice of related uncertainties.
- precise b -fragmentation $\rightarrow$ smaller uncertainties on the b -quark to b -jet transfer
- a better understanding of $t \rightarrow b^{\text{quark}} \rightarrow b^{\text{hadron}}$ crucial for fully-leptonic template mass extractions ($m_{\ell\mu}$ or $m_{\ell,J/\psi}$)
- joint fragmentation+mass measurements in leptonic modes **should be investigated**



status of ~analytic calculations

- Mitov et al. showed the first quasi-analytic calculations of similar distributions at TOP2020.
- will be very interesting to compare to unfolded data
- challenges for comparison:
 - calculations are for production of exclusive B-hadron species
 - jets are defined at parton-level in calculation
 - ATLAS measurement is to stable, charged particles



summary and outlook

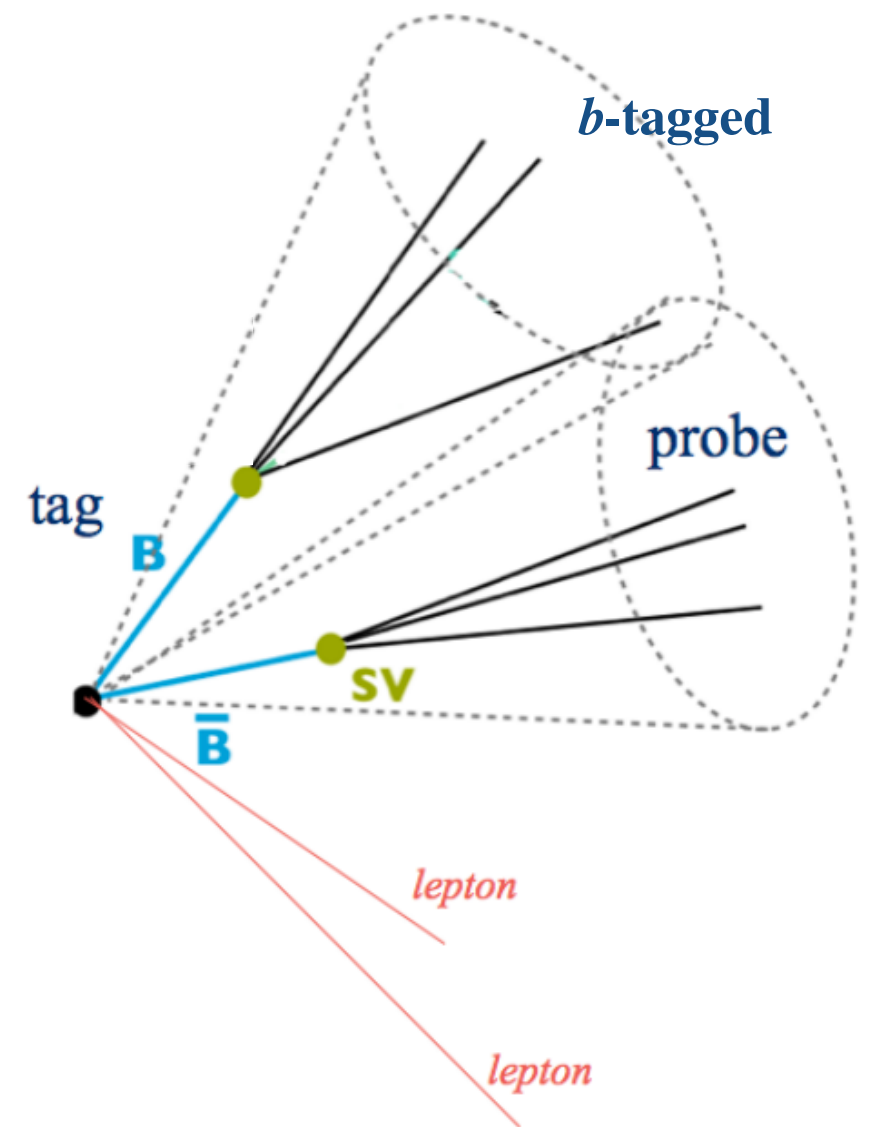
- several differential observables sensitive to b -quark fragmentation have been measured in $t\bar{t} \rightarrow e\mu b\bar{b}$ events with the 2015+2016 ATLAS data
- comparisons to modern MC generator predictions are made
- we will provide Rivet routine + HEPData entries for the unfolded data.
- many improvements possible: more precise measurements may be necessary for best “direct” top-quark mass extraction
- first ~analytic calculations of b -quark fragmentation in top-quark decays are on the horizon for comparison!

bonus

overview: detector-level event selection

obtain sample of b -jets from $t\bar{t} \rightarrow e\mu\nu\nu bb$ events

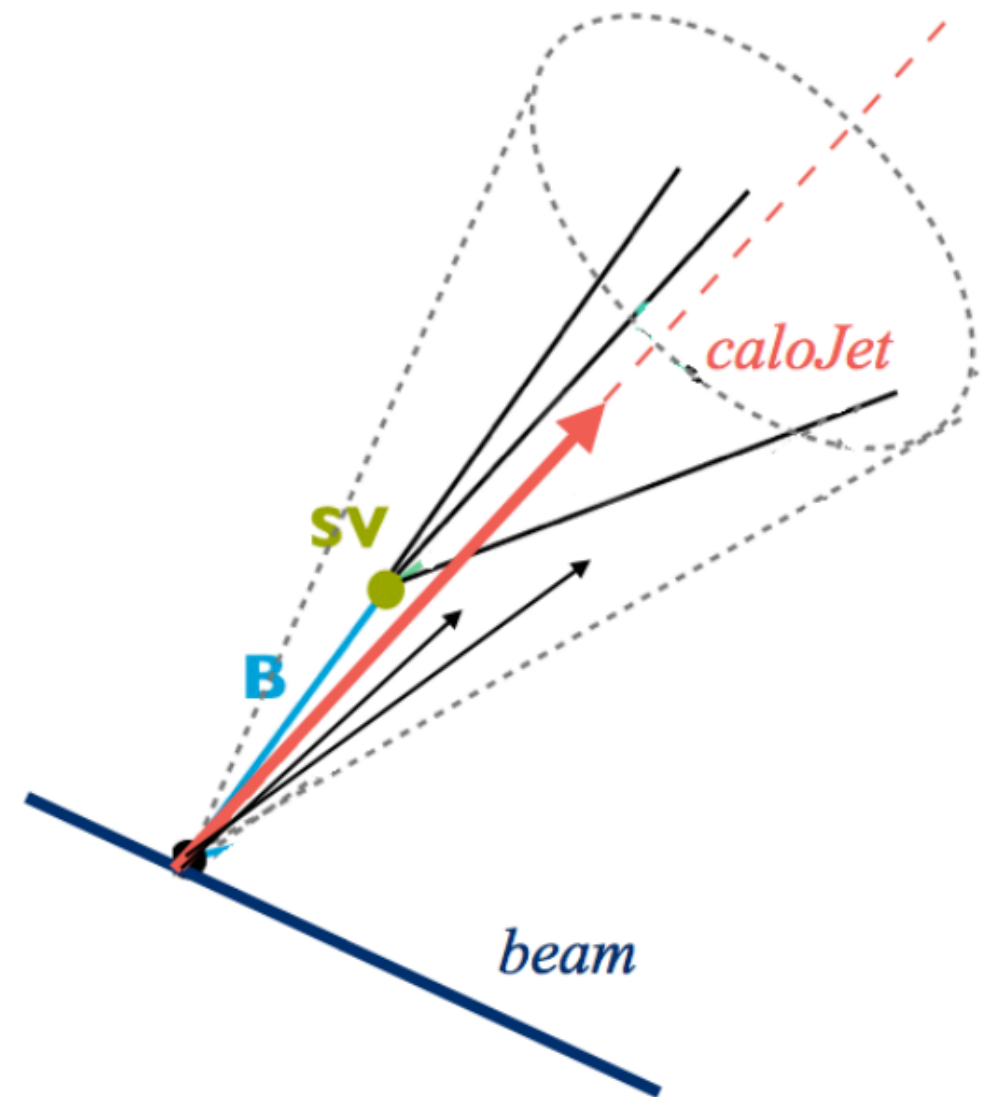
- require $=1$ e and $=1$ μ with opposite charge
- $=2$ anti- k_t $R = 0.4$ calorimeter jets
 - $|\eta| < 2.5, p_T > 30$ GeV
 - at least **one jet must be b -tagged** (“the tag”)
 - we measure the other jet (“the probe”)
 - if both jets are b -tagged, **both jets are measured**



b-hadron reconstruction

identify *b*-hadron candidates using the ATLAS single secondary vertex finder (SSVF)

- we require a reconstructed SSVF vertex with ≥ 3 tracks for “probe” jets
 - **95+% *b*-jet purity after this cut**
- the SSVF vertex **only has tracking information**
- track constituents of the SV make up the *b*-hadron candidate.
- tracks ghost-associated to the jet make up the jet charged component.



detector-level yields: predicted and observed

	events with $e\mu jj$ (≥ 1 b -tag)	probe-jets
process	predicted yields	
fiducial $t\bar{t}$	—	44000 $\pm$ 12000
non-fiducial $t\bar{t}$	—	6700 $\pm$ 1900
total $t\bar{t}$	76000 $\pm$ 18000	51000 $\pm$ 12000
single top	4400 $\pm$ 1500	1580 $\pm$ 600
Z+jets	125 $\pm$ 45	13.0 $\pm$ 5.1
diboson	90 $\pm$ 34	9.7 $\pm$ 3.9
total non- $t\bar{t}$	4600 $\pm$ 1600	1600 $\pm$ 600
b -jets	—	52200 $\pm$ 12000
c -jets	—	180 $\pm$ 60
other jets	—	250 $\pm$ 70
total prediction	81000 $\pm$ 18000	53000 $\pm$ 12000
	observed yields	
data	88511	57476

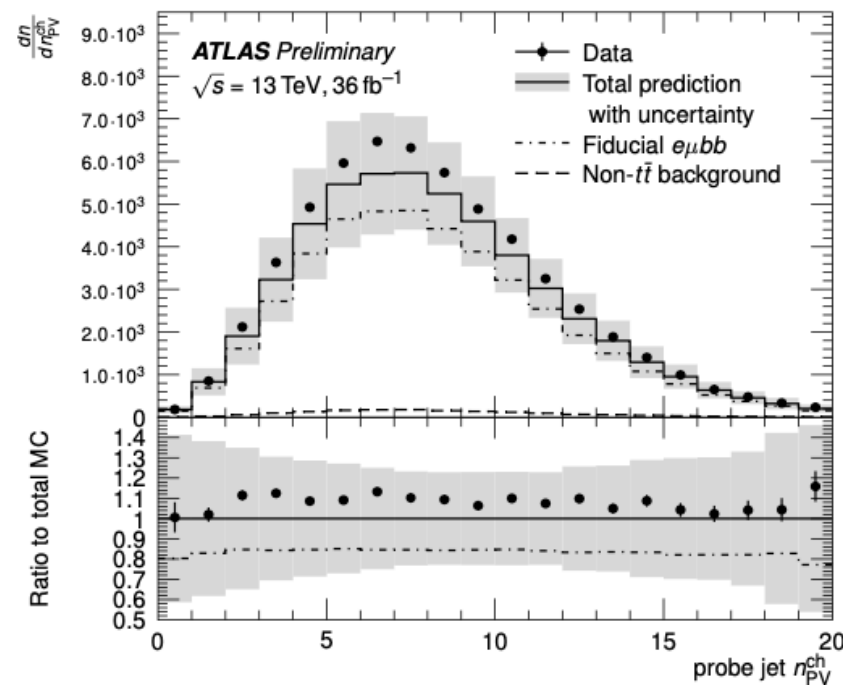
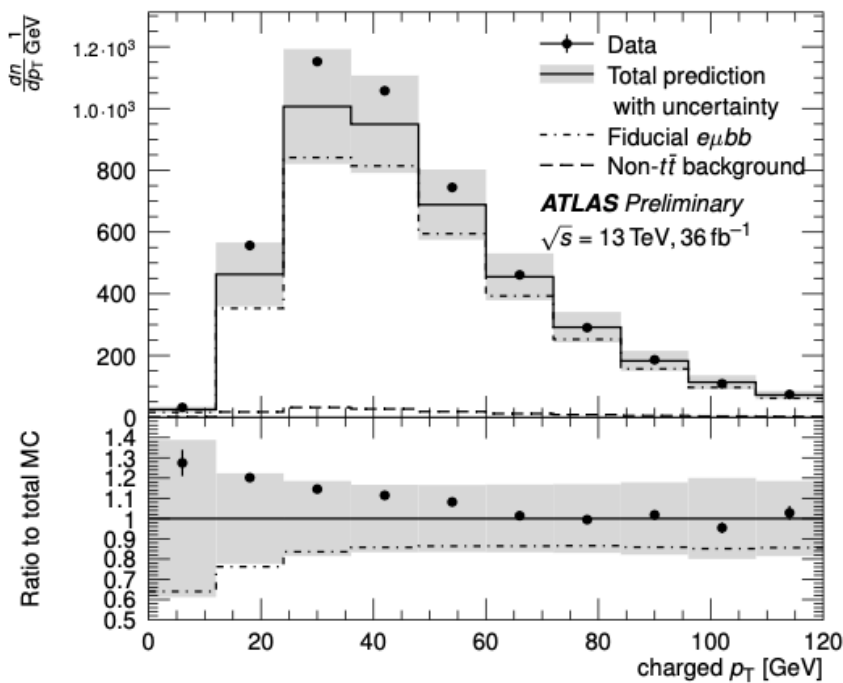
$t\bar{t}$ dominant

high expected
 b -jet purity

7.5% data / MC
discrepancy

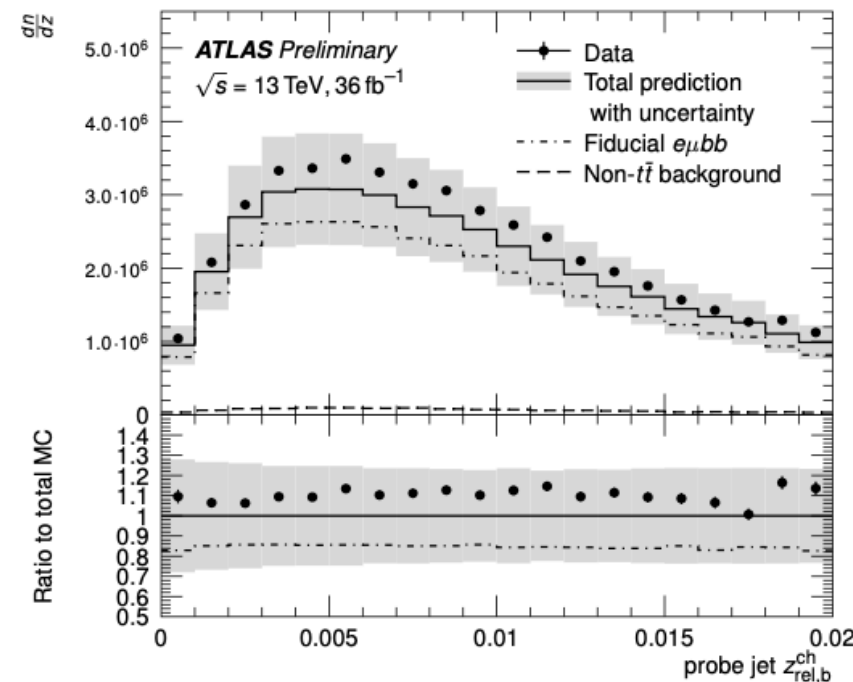
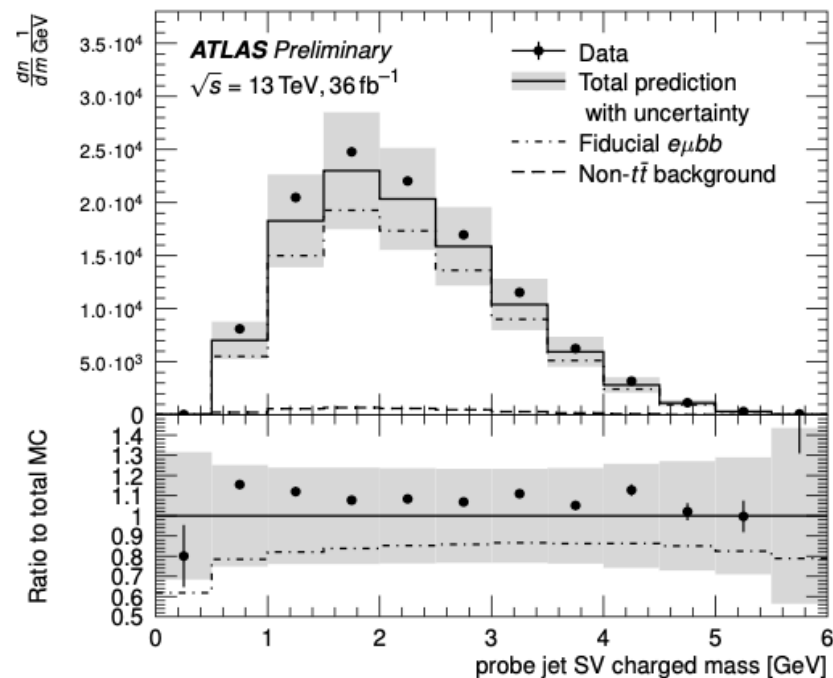
Table 1: Summary of expected and observed event and probe-jet yields.

detector-level control plots



charged component of jet p_T
has similar slope to jet p_T
(data vs MC taken as uncertainty)

other relevant PV and SV
quantities are well-modeled



SV mass and relative momentum
transverse to jet axis,

$$z_{\text{rel},b}^{\text{ch}} = (\vec{p}_b^{\text{ch}} \times \vec{p}_{\text{jet}}^{\text{ch}}) / |\vec{p}_{\text{jet}}^{\text{ch}}|^2$$

are also shown.

unfolding (FBU)

- **based on the "Fully Bayesian Unfolding" technique (arxiv: 1201.4612)**
- we use the following likelihood to unfold the detector effects:

$$\mathcal{L}(d|\sigma, \Lambda) = \prod_{i \in \text{recobins}} \text{Pois}(d_i|x_i(\sigma, \Lambda))$$

$$x_i(\sigma, \Lambda) = L(\Lambda) \times (b_i(\Lambda) + M_{ij}(\Lambda) \sigma_j)$$

- where $\vec{x}$ is the total number of predicted events in detector-level bins, L is the luminosity, $\vec{b}$ are predicted background events, M_{ij} is probability that a particle-level jet in bin i is reconstructed in detector-level bin j , and Λ are the systematic nuisance parameters.
- **we marginalize over nuisance parameters through MCMC sampling to build the marginal posteriors on $\vec{\sigma}$, the parameters-of-interest.**

unfolding procedure: background and response matrices

- to calculate the background predictions and response matrices at a given point in parameter space, we take linear combinations of the background predictions for nominal and the 1-sigma variation corresponding to a systematic uncertainty:

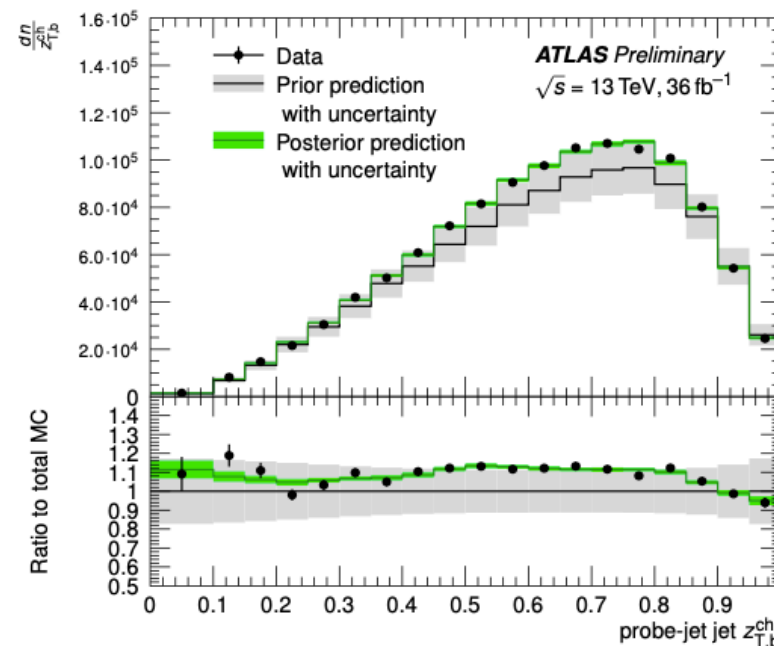
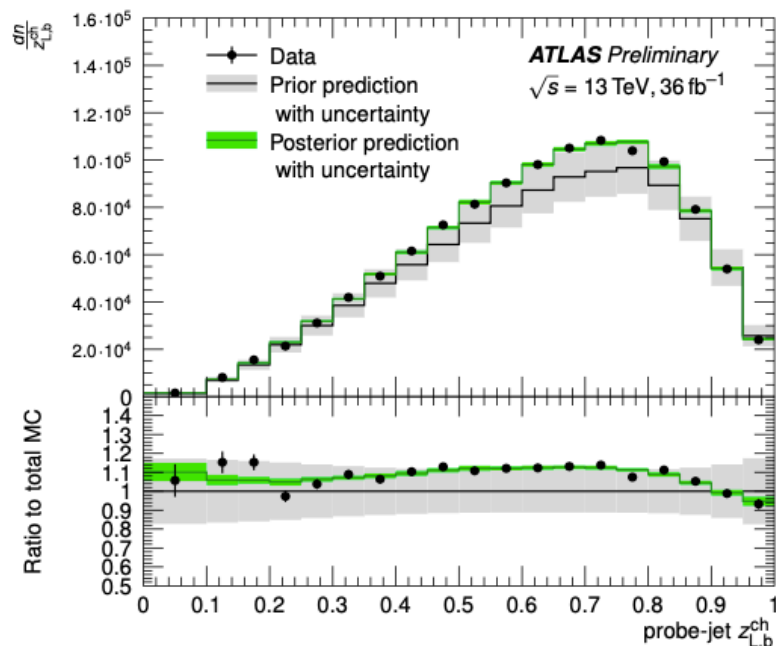
$$M_{ij}^{p \rightarrow d}(\vec{p}) = M_{ij,0}^{p \rightarrow d} + \sum_{k \in \text{systematics}} p_k * (M_{ij,k}^{p \rightarrow d} - M_{ij,0}^{p \rightarrow d})$$

$$b_i(\vec{p}) = b_{i,0} + \sum_{k \in \text{systematics}} p_k * (b_{i,k} - b_{i,0})$$

where the $\vec{p}$ are the nuisance parameters at a particular point in parameter space.

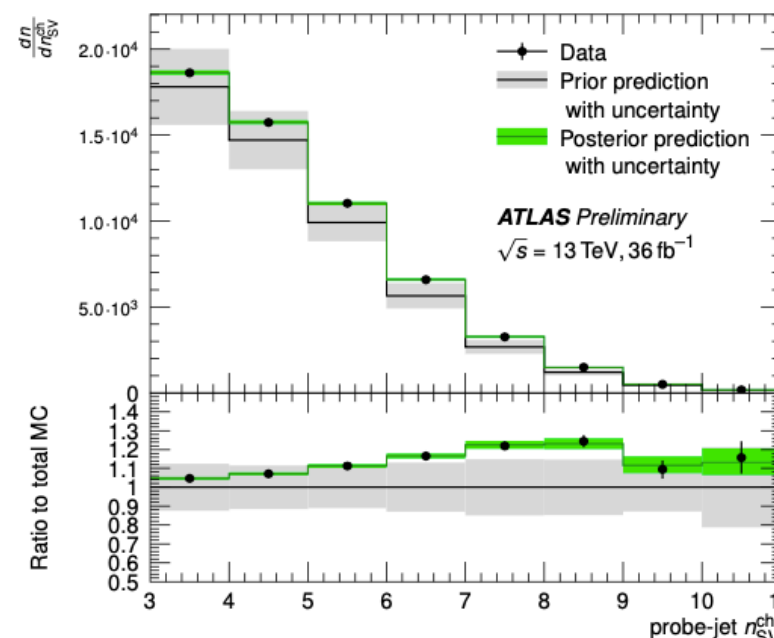
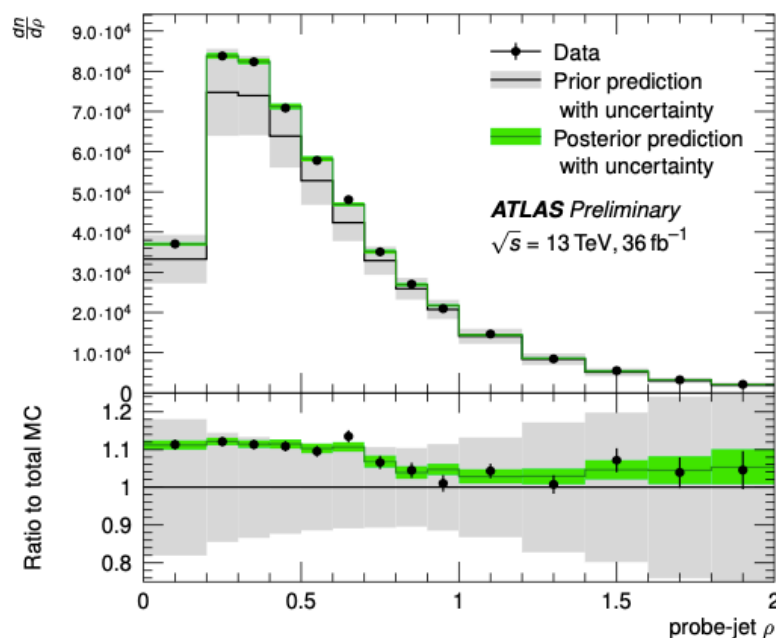
- in this way we can coherently and smoothly vary the response matrices and background predictions corresponding to systematic variations.
- we're wandering around the space of possible response matrices and background predictions available given our understanding of the predictions.

detector-level data/MC comparison before/after unfolding



detector-level observables
before (prior) and
after (posterior) unfolding

**unfolding model is capable
of describing observed data**



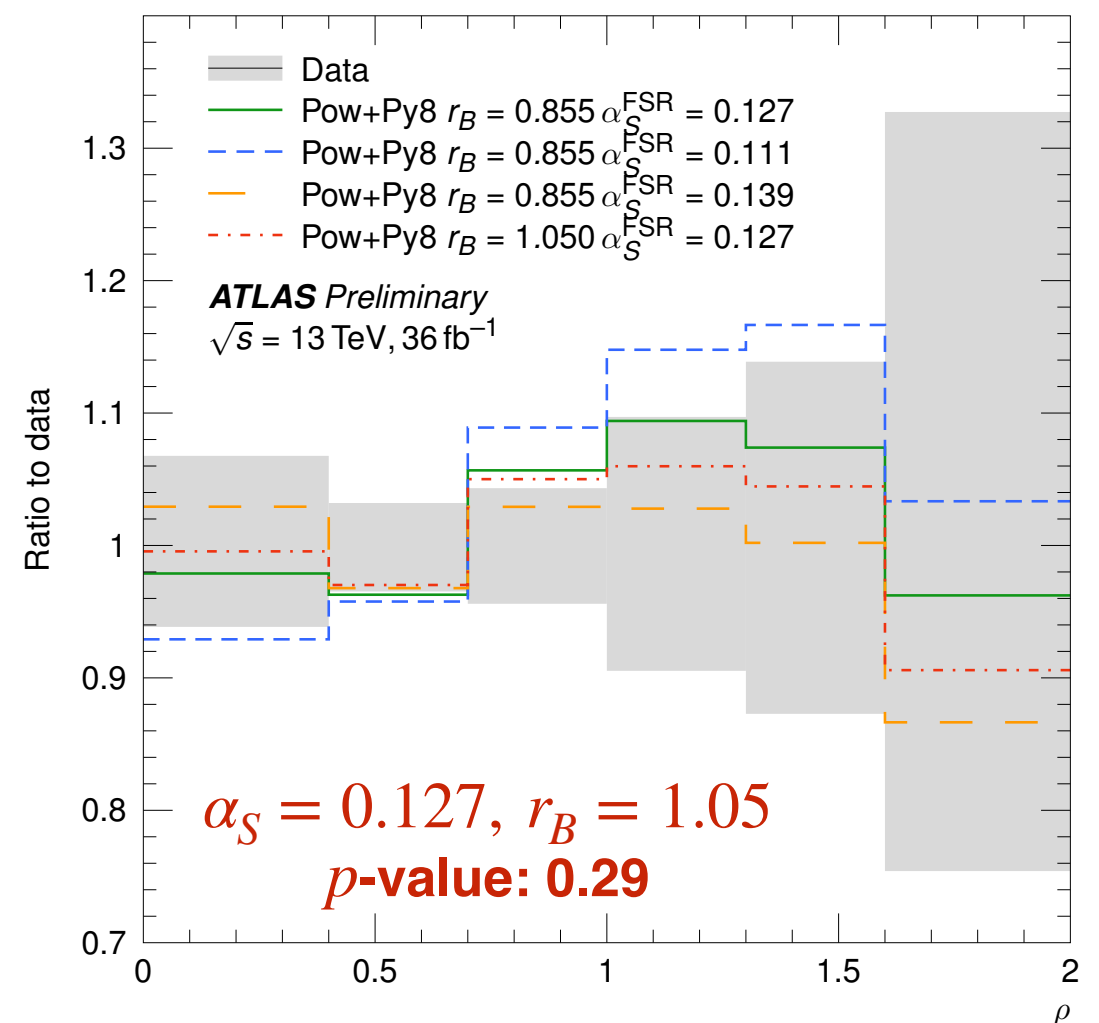
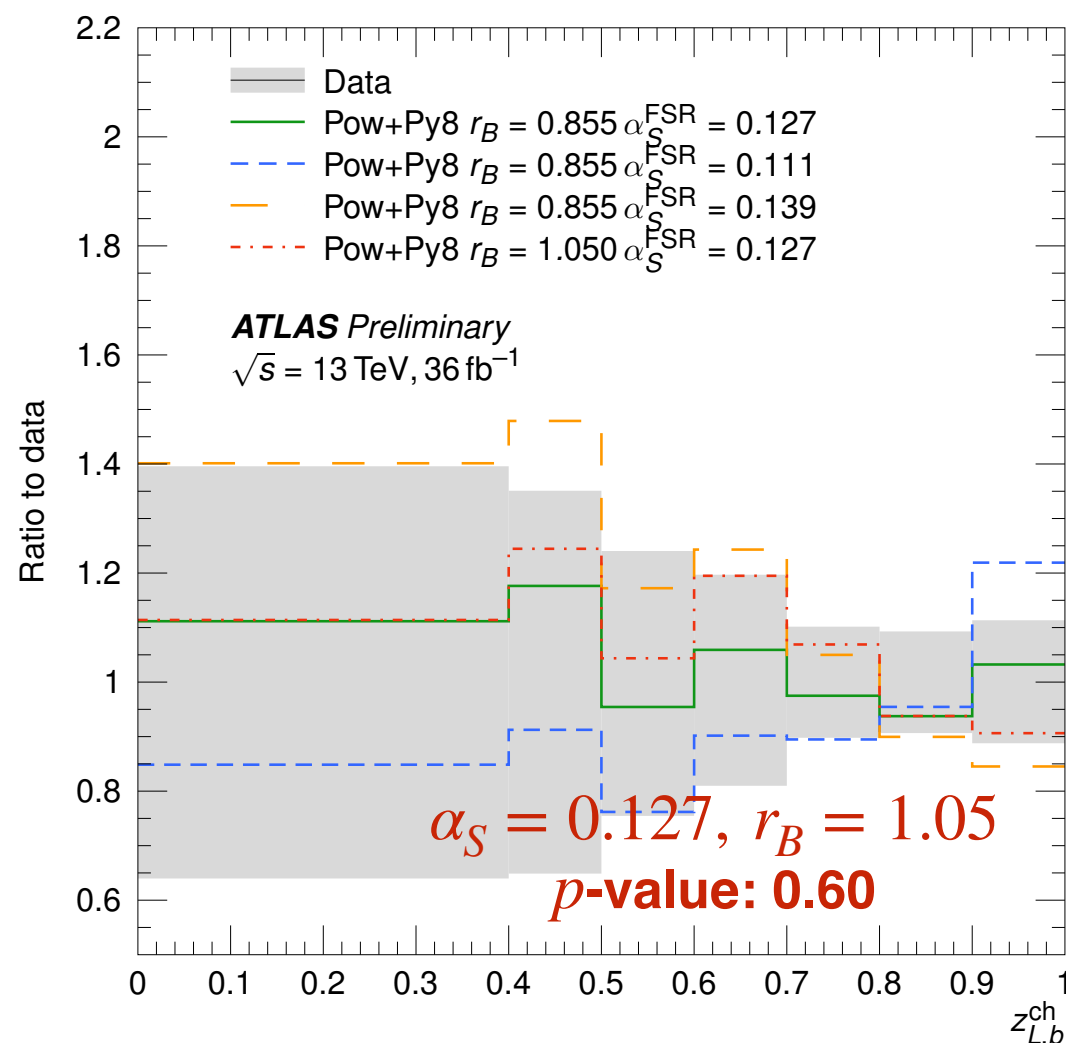
parameter anti-correlations cause
reduction in total uncertainty

posterior uncertainty closely follows
data stat uncertainty

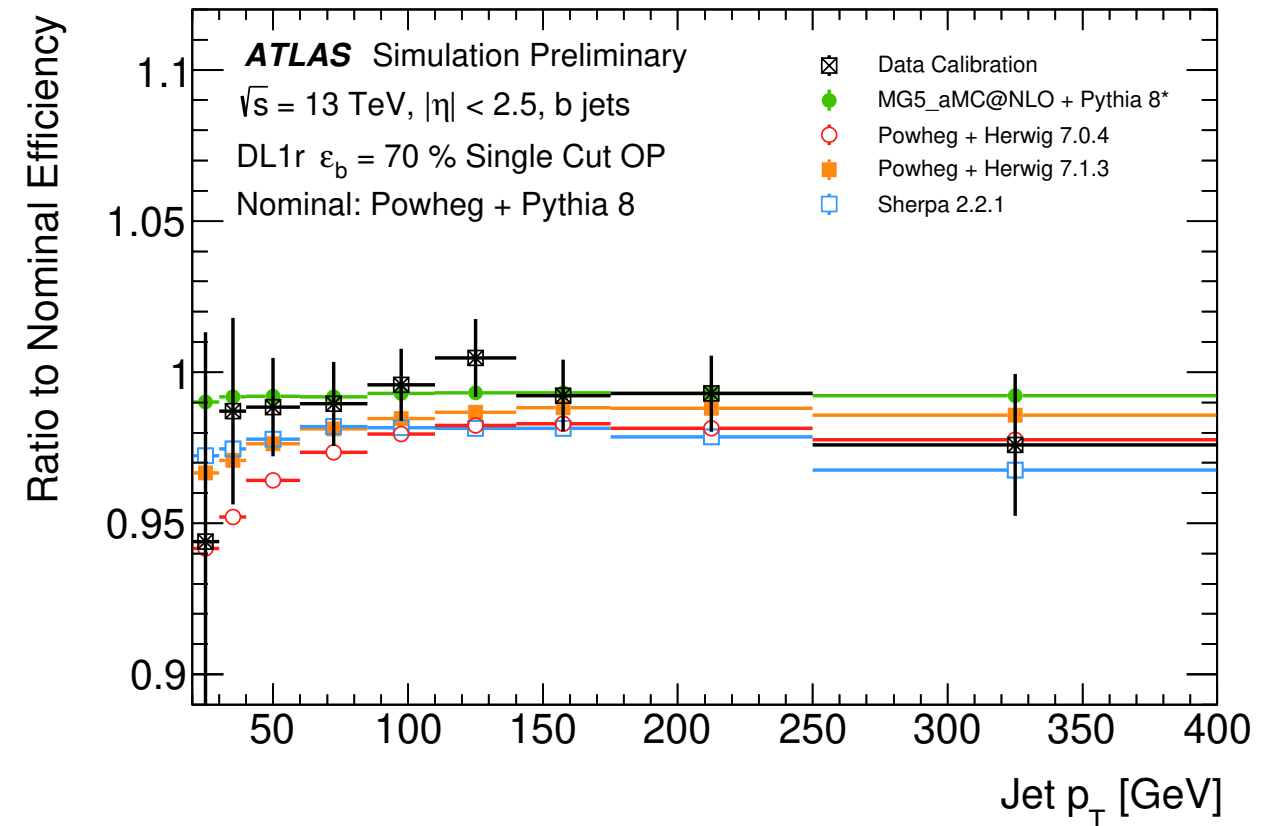
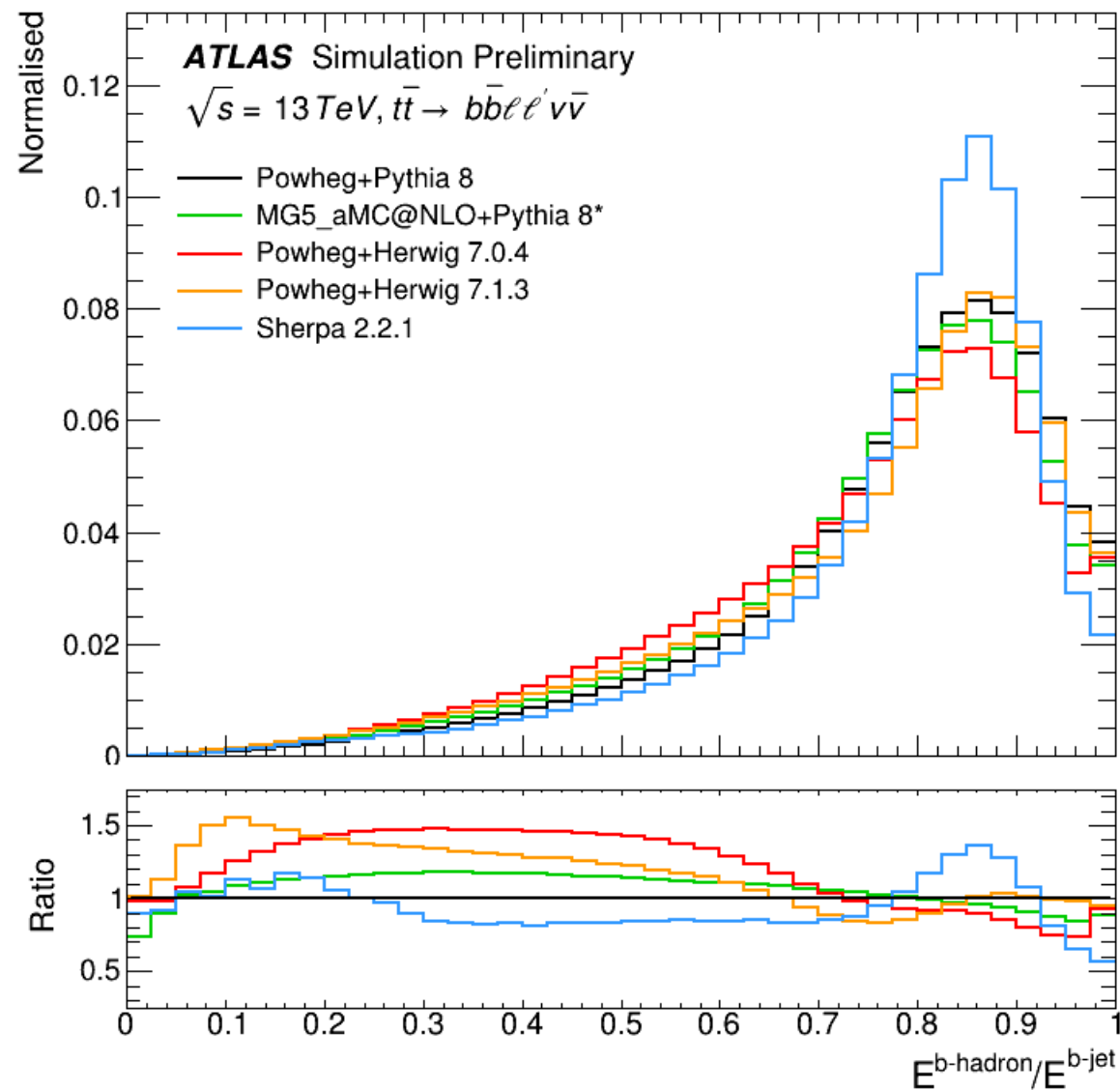
impact: top mass

ATLAS retuned the Lund-Bowler r_B parameter to LEP data with the A14 α_S

- used in preliminary mass measurement ATLAS-CONF-2020-046
- this combination of $\alpha_S = 0.127$, $r_B = 1.05$ agrees with observed data to current precision. **(dash-dotted red curve)**

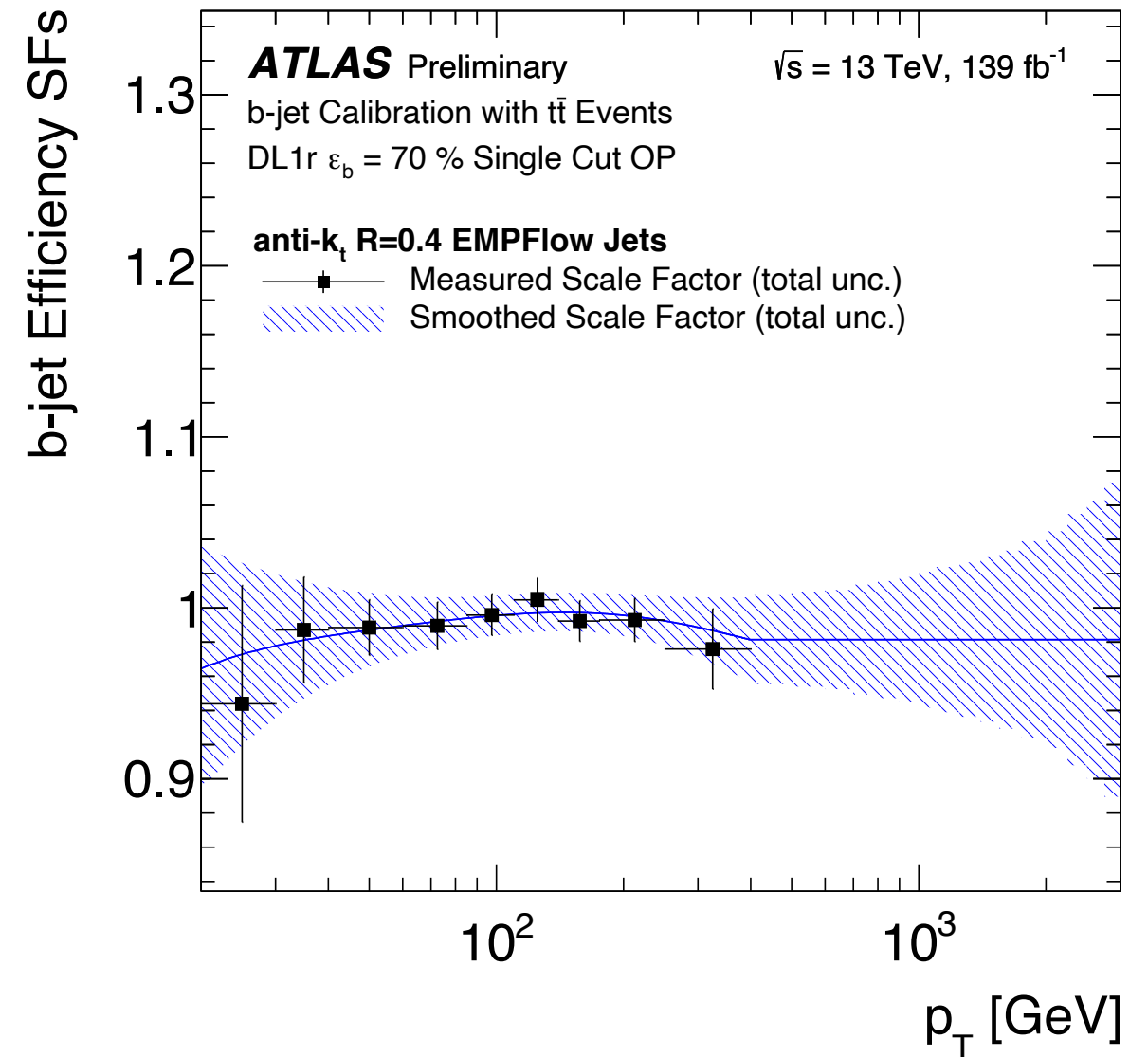
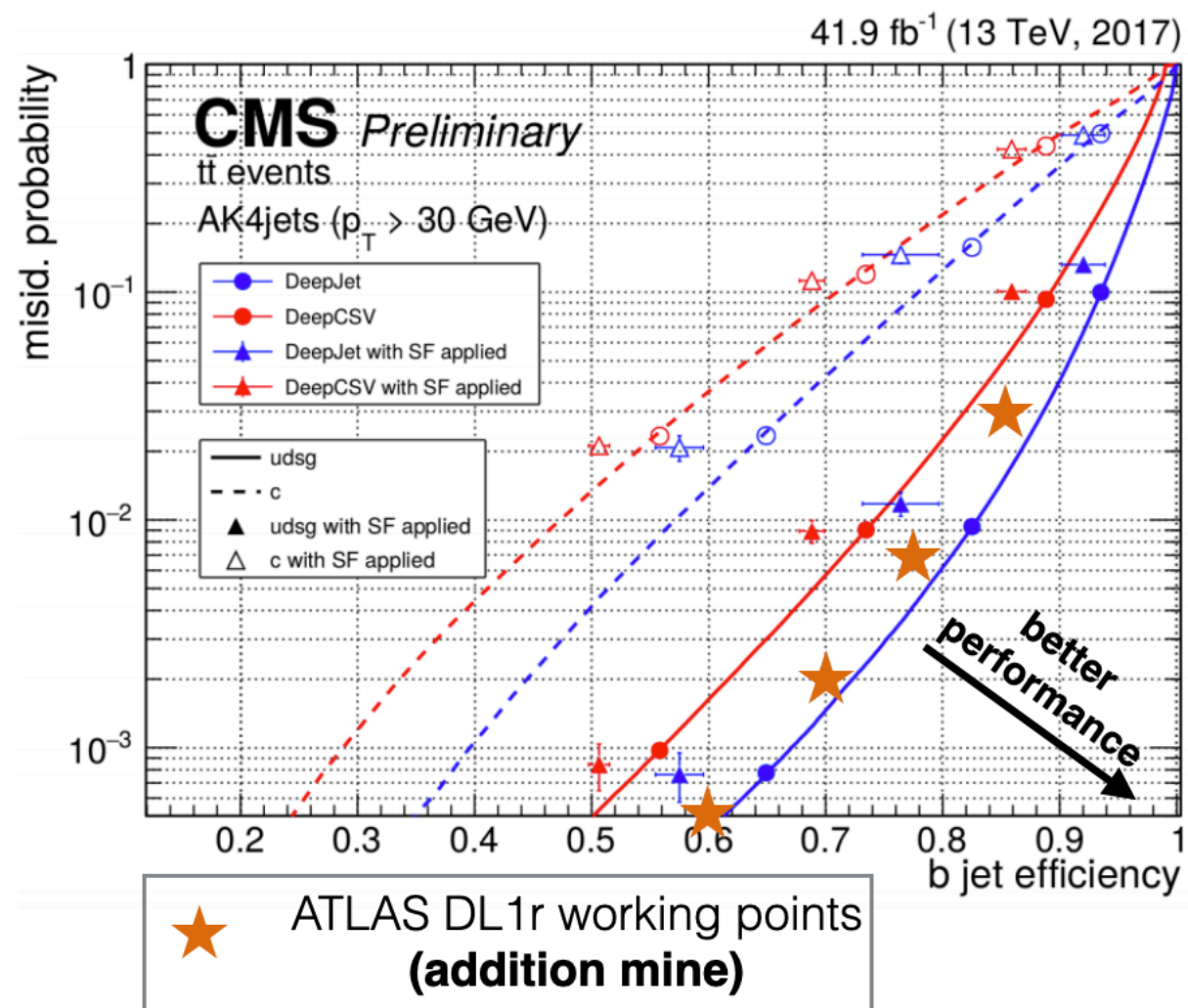


impact on b -tagging

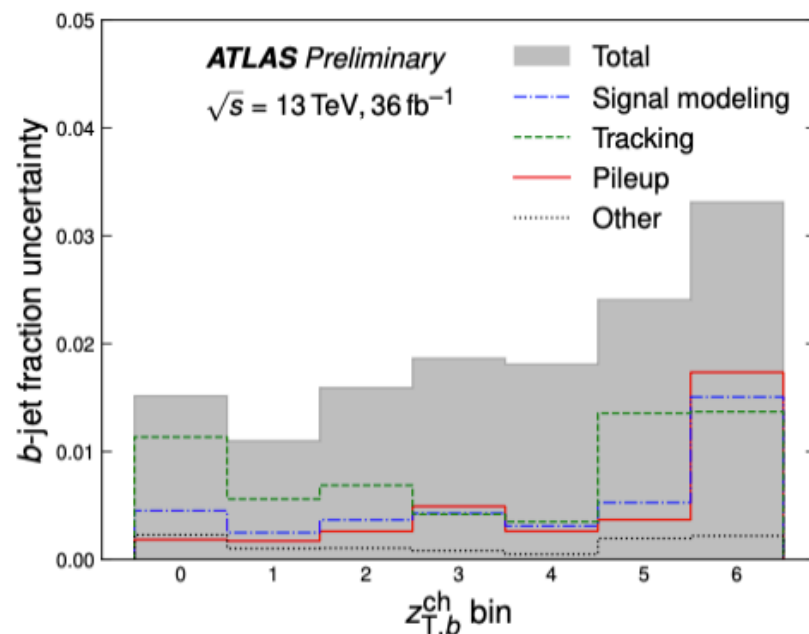


ATLAS-PHYS-PUB-2020-009

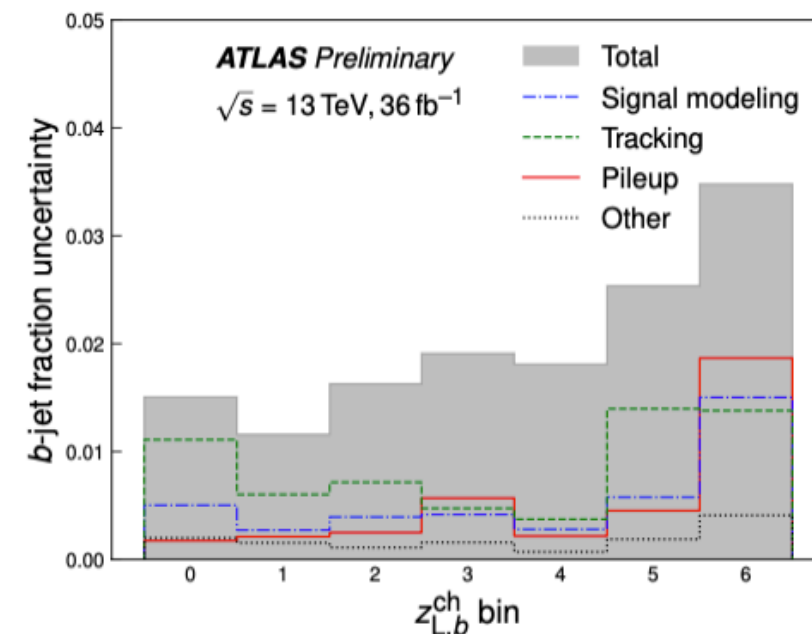
b -tagging SFs



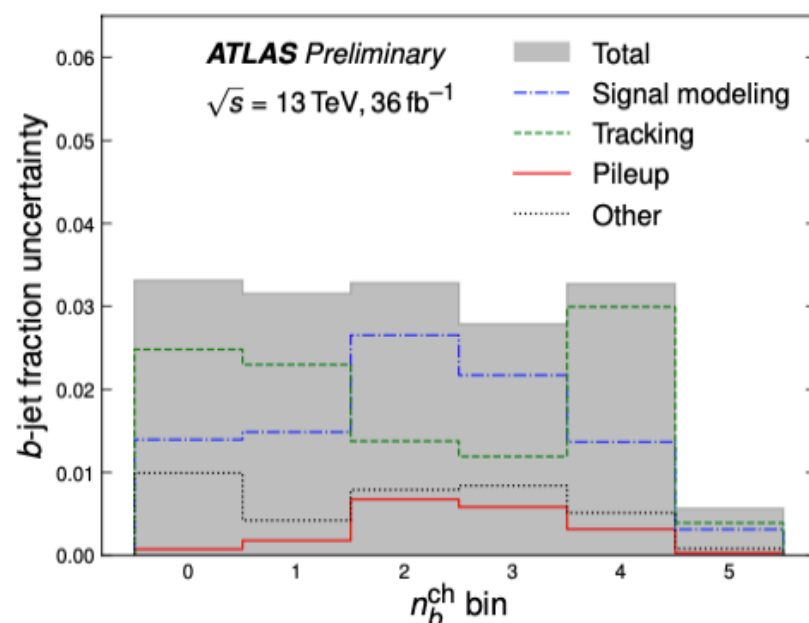
uncertainty breakdowns



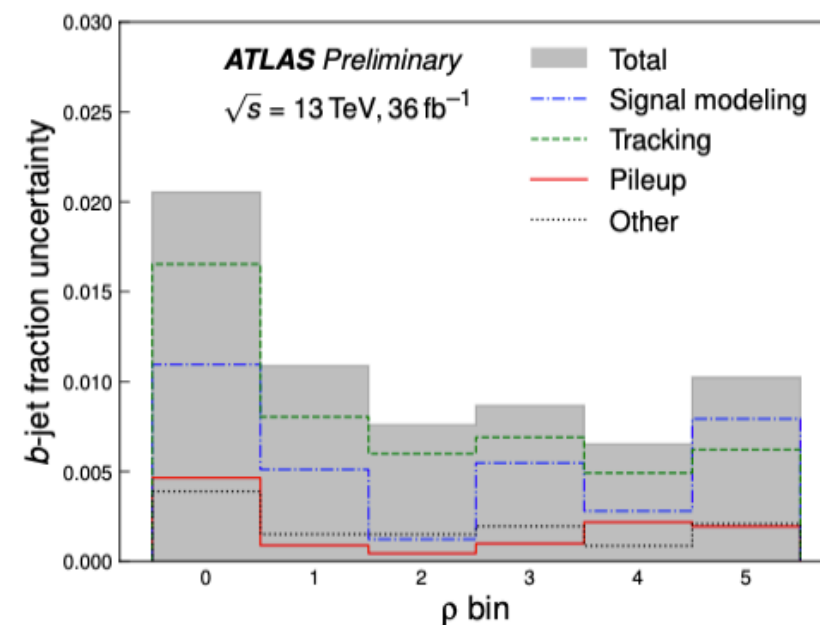
(a) $z_{T,b}^{\text{ch}}$



(b) $z_{L,b}^{\text{ch}}$



(c) n_b^{ch}



(d) ρ

p -values

generator configuration	$z_{T,b}^{\text{ch}}$	$z_{L,b}^{\text{ch}}$	n_b^{ch}	ρ
POWHEG+PYTHIA8 A14 $r_B = 0.855$ $\alpha_S^{\text{FSR}} = 0.127$	0.50	0.98	0.94	0.20
POWHEG+PYTHIA8 A14 $r_B = 0.855$ $\alpha_S^{\text{FSR}} = 0.139$	0.13	0.37	0.95	0.31
POWHEG+PYTHIA8 A14 $r_B = 0.855$ $\alpha_S^{\text{FSR}} = 0.111$	0.16	0.62	0.95	0.07
POWHEG+PYTHIA8 A14 $r_B = 1.050$ $\alpha_S^{\text{FSR}} = 0.127$	0.18	0.60	0.94	0.29
POWHEG+HERWIG7.0.4	0.22	0.50	0.95	0.12
POWHEG+HERWIG7.1.3	0.42	0.84	0.92	0.18
SHERPA2.2.1	0.14	0.45	0.01	0.52
SHERPA2.2.8 ($Z + bb$ tune)	0.004	0.02	0.45	0.24
SHERPA2.2.8	0.32	0.79	0.49	0.11
SHERPA2.2.10	0.27	0.84	0.32	0.08

Table 3: Summary of p -values for various MC generator configurations based on the observed data distributions