



*DIS 2021*

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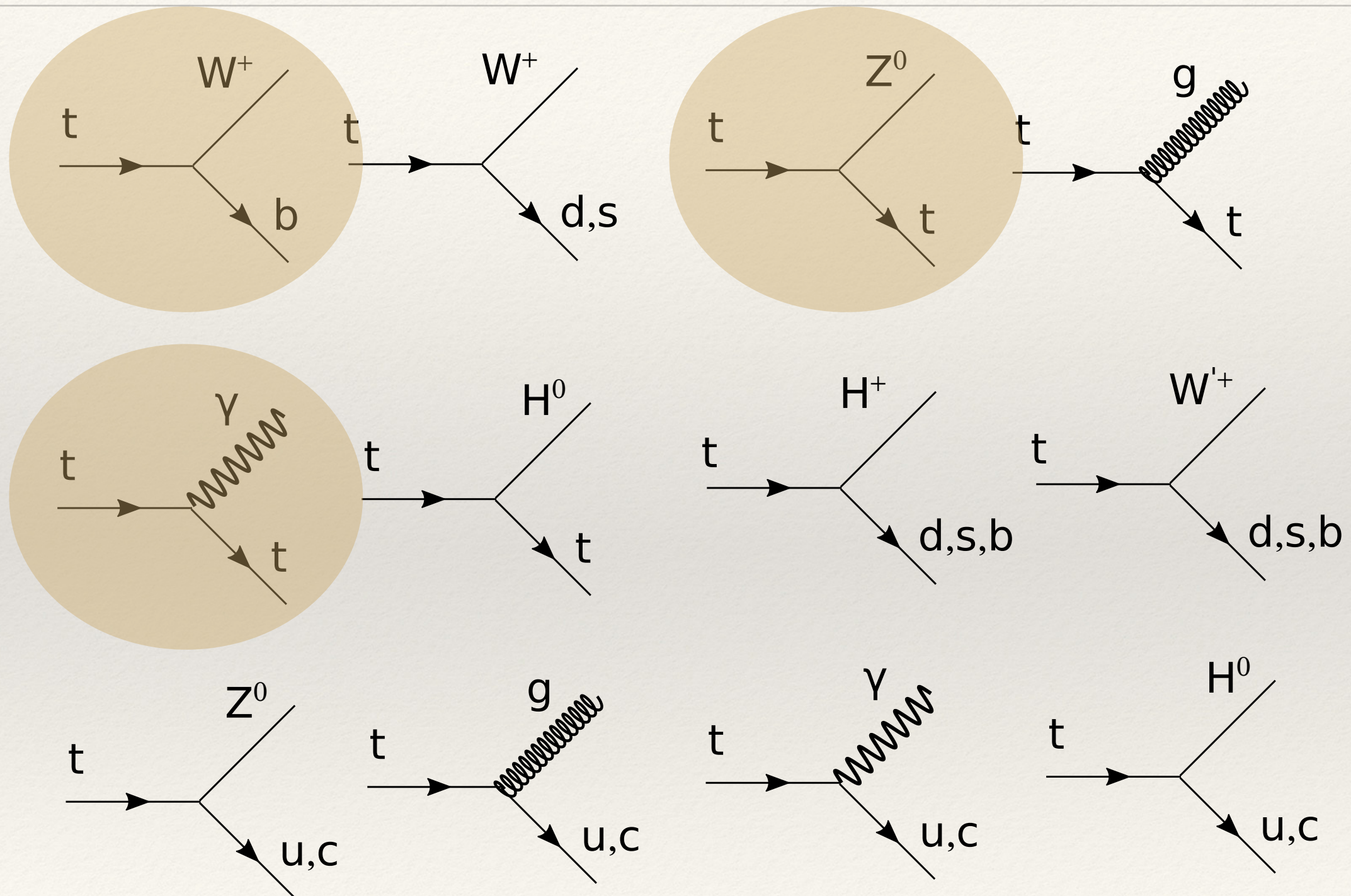
# Measurements of the top quark electro-weak couplings with the ATLAS experiment at the LHC

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Catalogue of standard & exotic processes involving the top quark. Top physics program is concerned with all of these. This talk puts the spotlight on EW vertices.



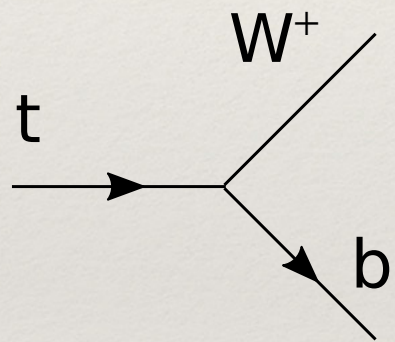


# EFT, anomalous couplings & the Wtb vertex

The effect of BSM physics at a high mass scale  $\Lambda$  is parameterized using higher dimensional operators

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum c_i \mathcal{O}_i + \dots$$

After EW symmetry breaking, for 3rd generation



$$\mathcal{O}_{\phi q}^{3(ij)} = \left( \phi^\dagger \overleftrightarrow{D}_\mu^I \phi \right) (\bar{q}_i \gamma^\mu \tau^I q_j)$$

$$\mathcal{O}_{\phi ud}^{(ij)} = \left( \tilde{\phi}^\dagger D^\mu \phi \right) (\bar{u}_i \gamma^\mu \tau^I d_j)$$

$$\mathcal{O}_{uW}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} \tau^I u_j) \tilde{\phi} W_{\mu\nu}^I$$

$$\mathcal{O}_{dW}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} \tau^I d_j) \phi W_{\mu\nu}^I$$

$$\mathcal{O}_{\phi q}^3 \rightarrow -\frac{gv^2}{\sqrt{2}} \bar{b}_L \gamma^\mu t_L W_\mu^-$$

$$\mathcal{O}_{\phi tb} = \left[ \frac{gv^2}{2\sqrt{2}} \bar{b}_R \gamma^\mu t_R W_\mu^- \right]^\dagger$$

$$\mathcal{O}_{tW} = 2v \bar{b}_L i \sigma^{\mu\nu} q_\nu t_R W_\mu^-$$

$$\mathcal{O}_{bW} = [2v \bar{b}_R i \sigma^{\mu\nu} q_\nu t_L W_\mu^-]^\dagger$$

Anomalous couplings:

$$\mathcal{L}_{Wtb} = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i \sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + H.c.$$

$$V_L = V_{tb} + \frac{v^2}{\Lambda^2} c_{\phi q}^{(3)}$$

$$V_R = \frac{1}{2} \frac{v^2}{\Lambda^2} c_{\phi tb}^*$$

$$g_L = -\sqrt{2} \frac{v^2}{\Lambda^2} c_{bW}^*$$

$$g_R = -\sqrt{2} \frac{v^2}{\Lambda^2} c_{tW}$$



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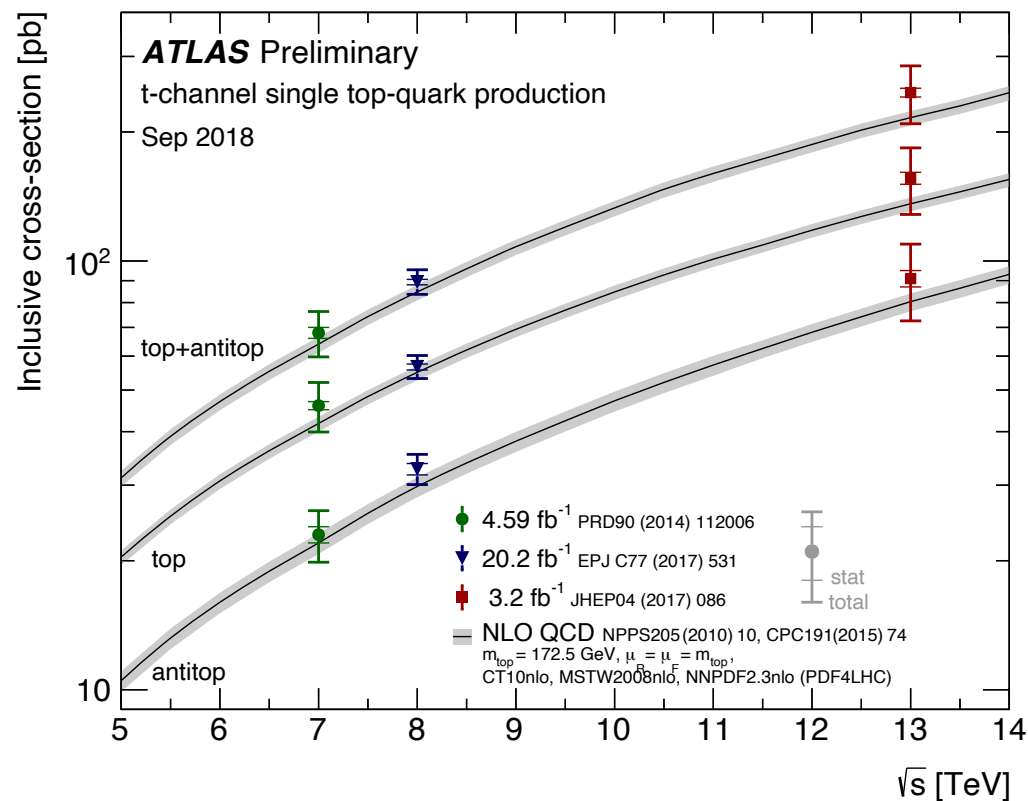
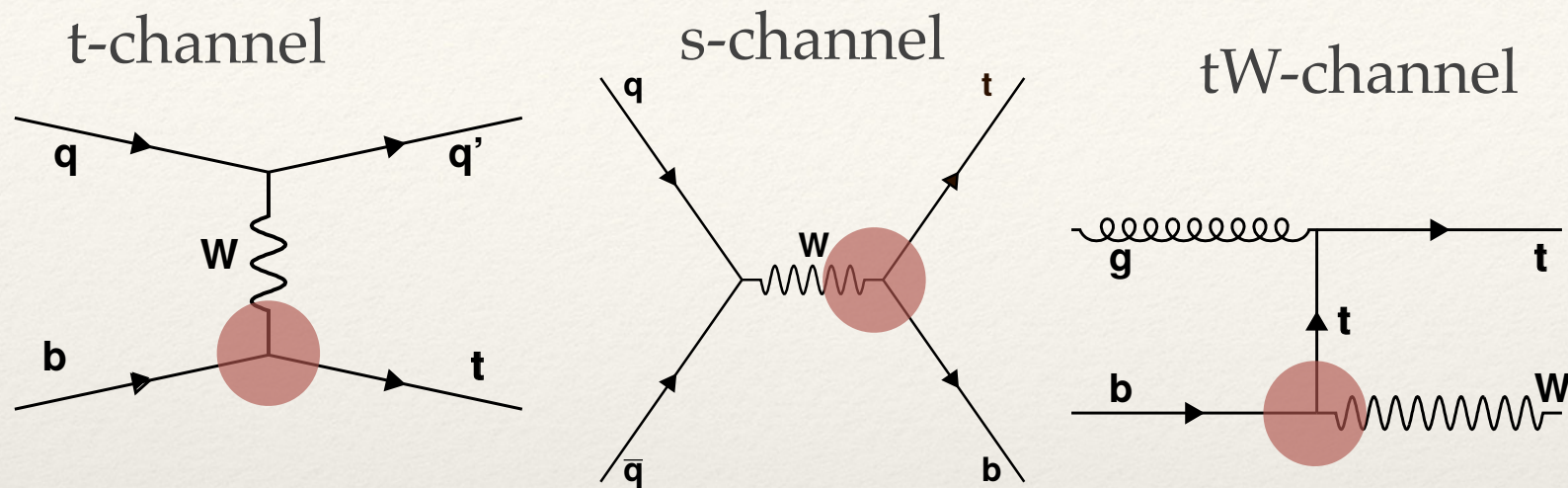
# There are three ATLAS measurements that contribute to constraints on the couplings:

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- ❖ The single-top production cross-section.
  - ❖ PRD 90 (2014) 11206 (7 TeV)
  - ❖ EPJC 77 (2017) 531 (8 TeV)
  - ❖ JHEP 04 (2017) 086 (13 TeV)
- ❖ Measurement of W-boson helicity fractions in  $t\bar{t}$  events.
  - ❖ EPJC 77 2017 264 (8 TeV)
  - ❖ JHEP 08 (2020) 051 (8 TeV, ATLAS/CMS combination)
- ❖ Measurement of angular distributions in the decay of single top quarks.
  - ❖ JHEP 12 (2017) 017 (8 TeV)



# Electroweak production (single top)

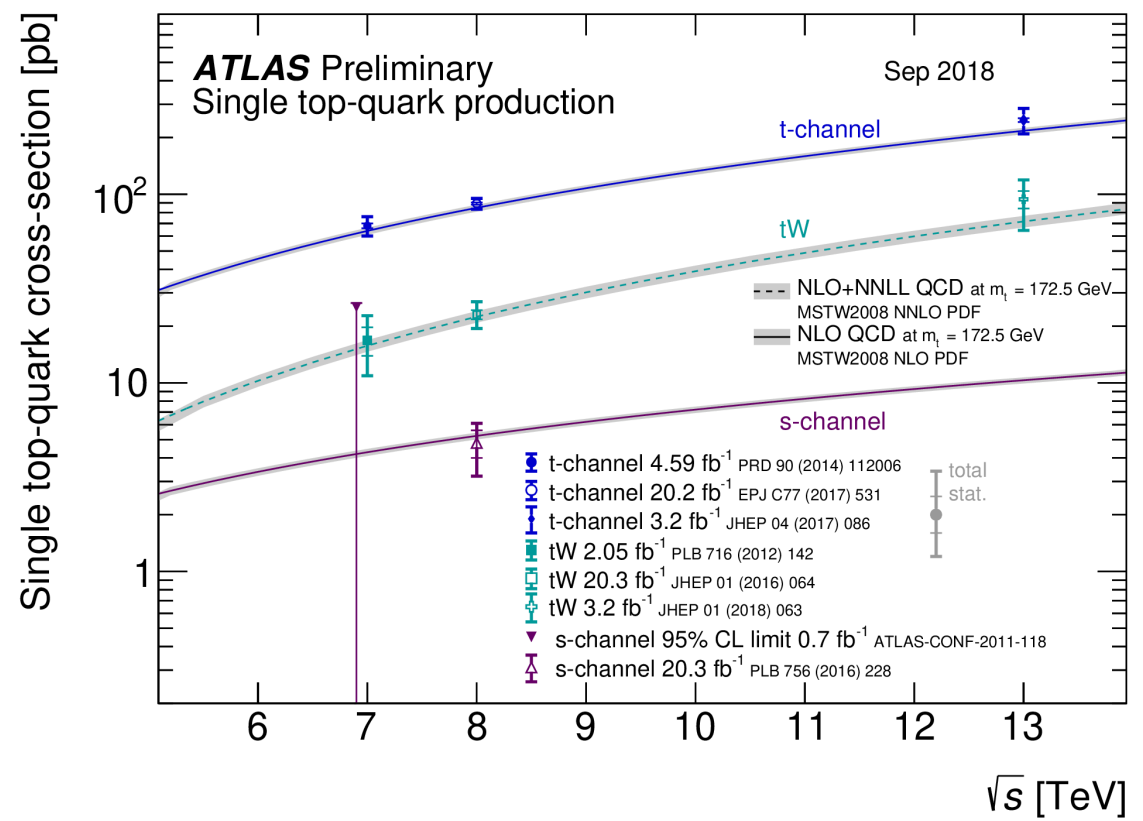


Cross-sections have a quadratic dependence on EFT coefficients.

Due to the prevalence of up-type valence quarks, the single-top cross section is larger than the single-antitop cross section.



# Single top cross section measurements in ATLAS

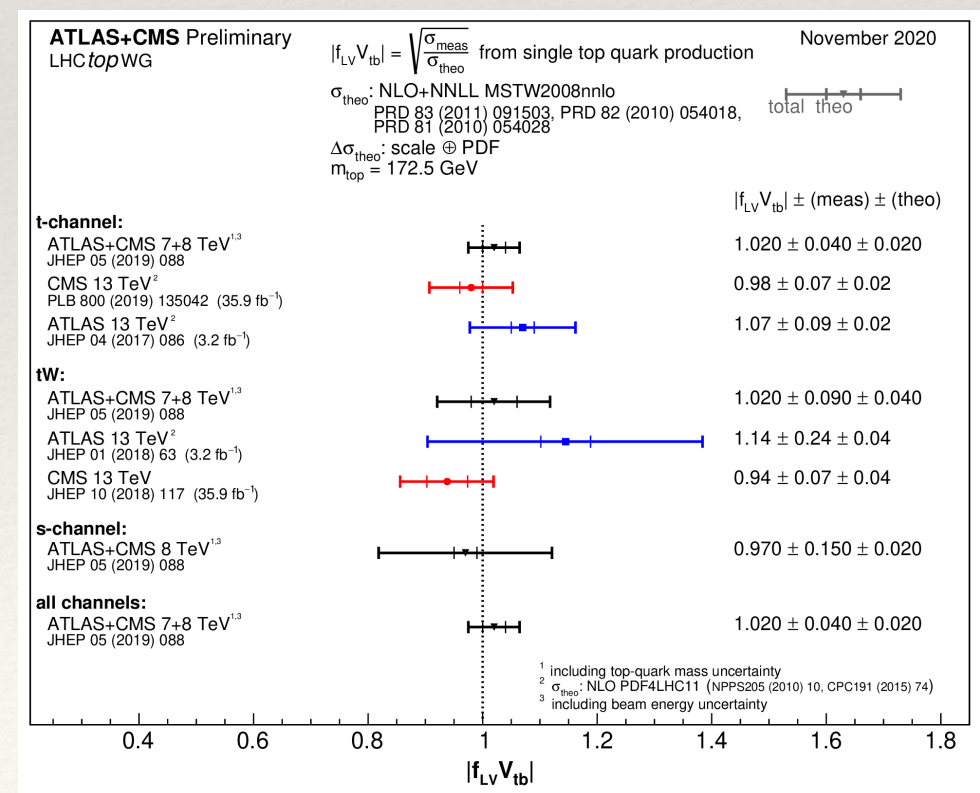


Cross section measurements are interpreted in terms of  $f_{LV}V_{tb}$ .

$f_{LV}$  is an overall form factor incorporating the effects of all BSM physics.

The most precise measurements are obtained at  $\sqrt{s} = 8$  TeV.

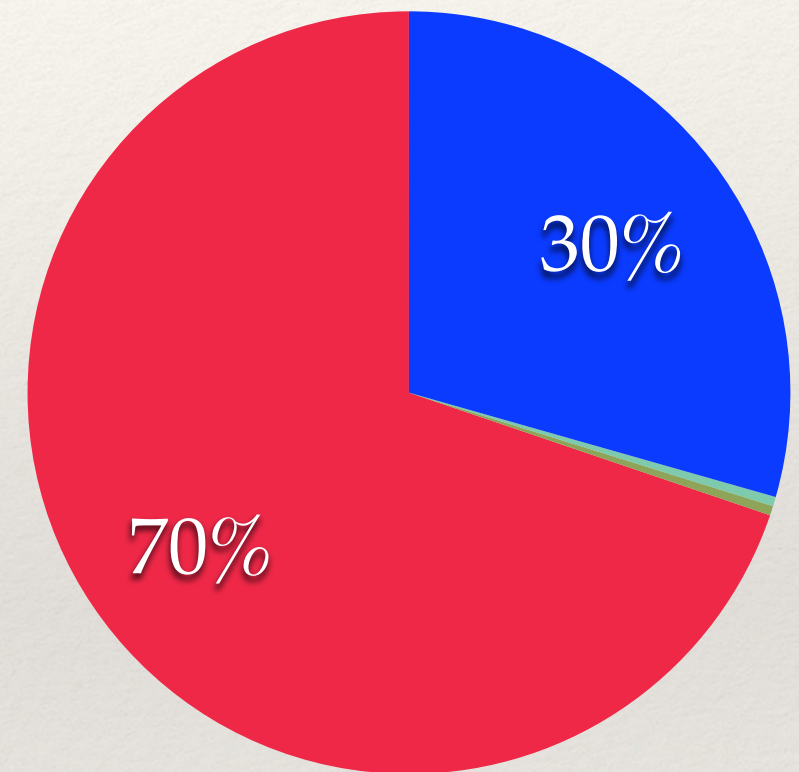
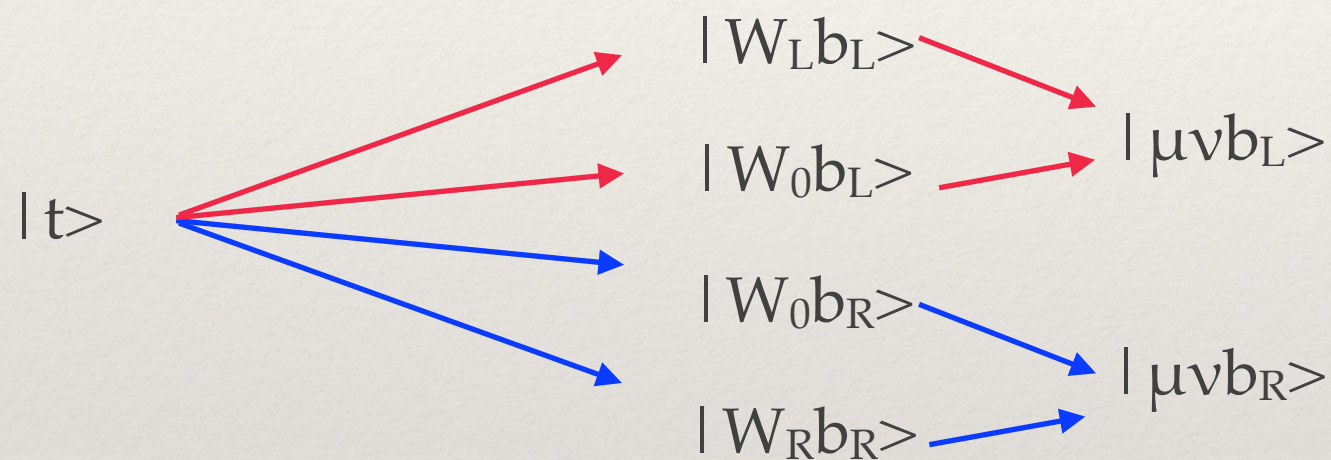
More precision is required at  $\sqrt{s} = 13$  TeV, where current measurements are based on only 3.2 fb<sup>-1</sup> of the available 139 fb<sup>-1</sup> (work in progress).





# The $Wtb$ vertex from top quark decay

Four transition amplitudes are involved in the decay of the top quark.  
Interference occurs between pairs of transitions.



In principle it is possible to measure:

- four amplitudes
- ~~two~~ one phases (only one because amplitudes to right handed  $b$ 's are tiny.)

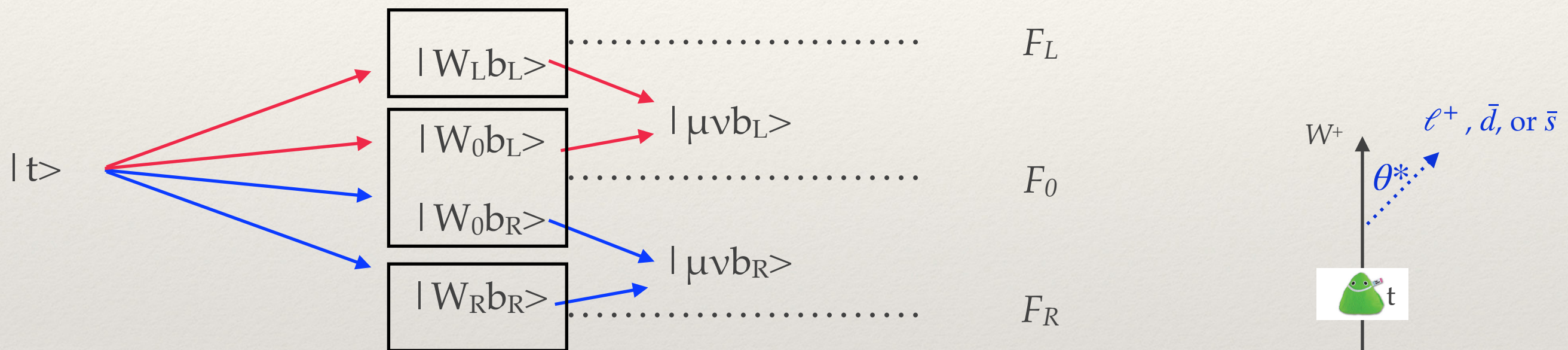
and then to relate these to the  $V_L$ ,  $V_R$ ,  $g_L$ , and  $g_R$

alternately, to  $c_{\phi q}^{(3)}$ ,  $c_{\phi tb}$ ,  $c_{bW}$ , and  $c_{tW}$



# EPJC 77 (2017) 264: W-boson helicity fractions in top quark decay

Main innovation: use of both the leptonic and hadronic side in the lepton+jets channel.



The determination of helicity fractions in **top** decay uses the helicity angle  $\theta^*$ : the angle between the **antifermion** from the  $W^+$  in the  $W^+$  rest frame, and the  $W^+$  in the **top** rest frame.

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta^*} = \frac{3}{4} (1 - \cos^2\theta^*) F_0 + \frac{3}{8} (1 - \cos\theta^*)^2 F_L + \frac{3}{8} (1 + \cos\theta^*)^2 F_R$$

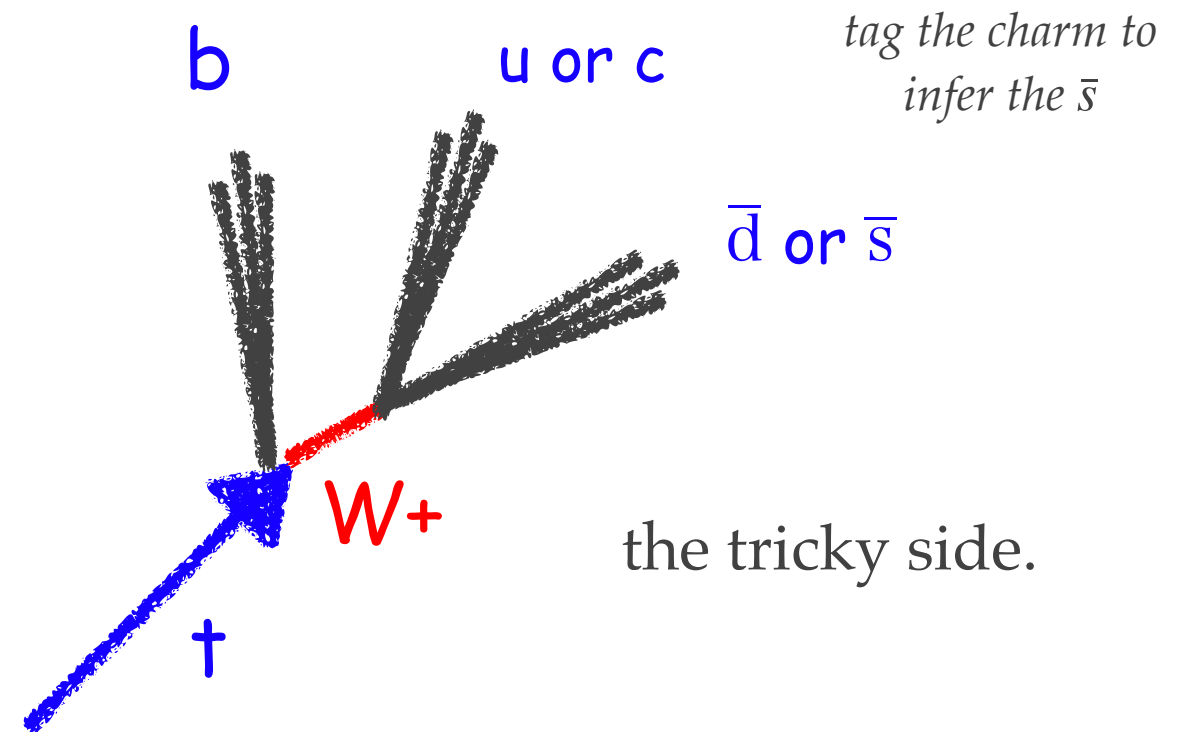
Since  $F_0 + F_L + F_R = 1$ , there only two of three quantities are independently constrained in a fit to the helicity angle  $\theta^*$



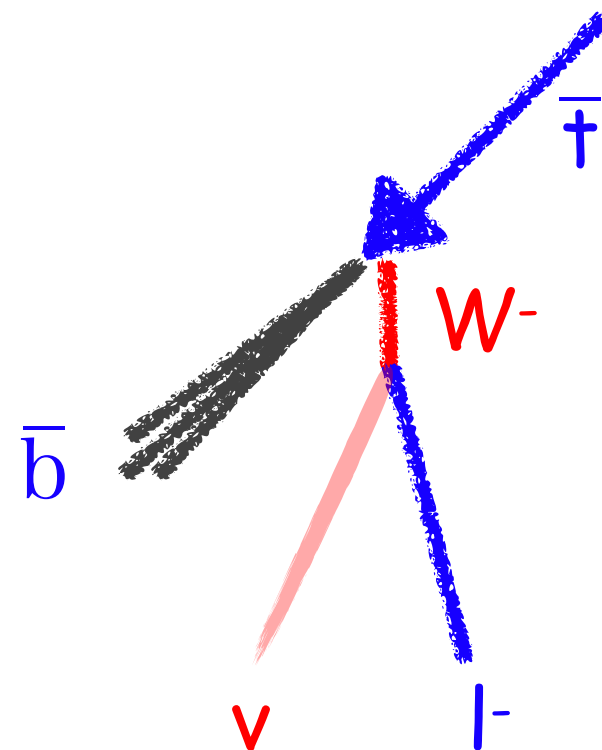
# The analysis EPJC 77 (2017) 264 is carried out in $t\bar{t}$ events

The lepton+jets channel is used.

The determination of helicity fractions in **top** decay uses the helicity angle  $\theta^*$ : the angle between the **antifermion** from the  $W^+$  in the  $W^+$  rest frame, and the  $W^+$  in the **top** rest frame.



the easy side.



The determination of helicity fractions in **antitop** decay uses the helicity angle  $\theta^*$ : the angle between the **fermion** from the  $W^-$  in the  $W^-$  rest frame, and the  $W^-$  in the **antitop** rest frame.

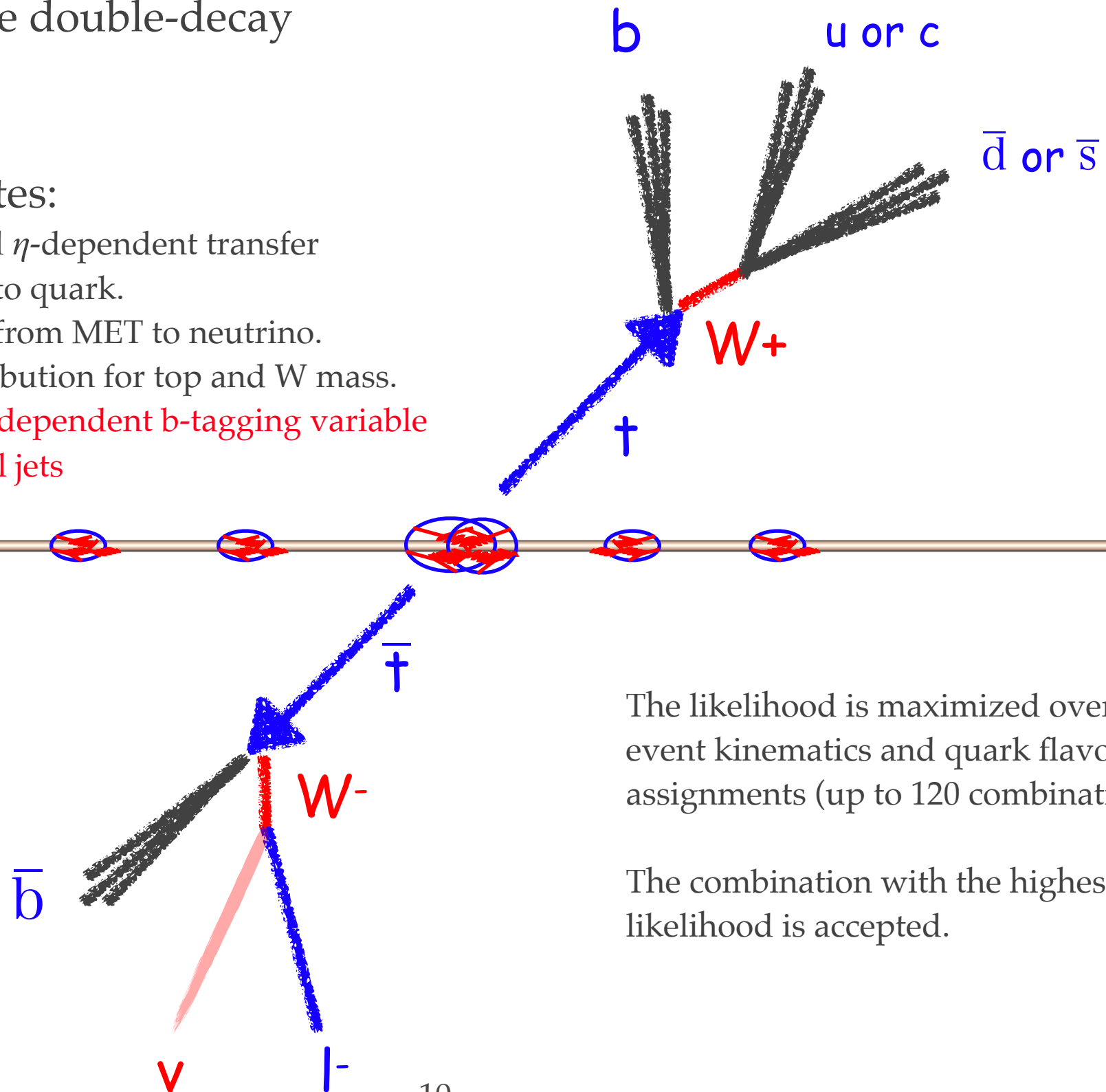


# Event reconstruction, more precisely:

Kinematic fitter (KL Fitter) is used to infer the kinematics of the double-decay process.

The fitter incorporates:

- \* flavor-specific and  $\eta$ -dependent transfer functions from jet to quark.
- \* transfer functions from MET to neutrino.
- \* Breit-Wigner distribution for top and W mass.
- \* Flavor-specific,  $p_T$  dependent b-tagging variable probabilities on all jets



The likelihood is maximized over both event kinematics and quark flavor assignments (up to 120 combinations).

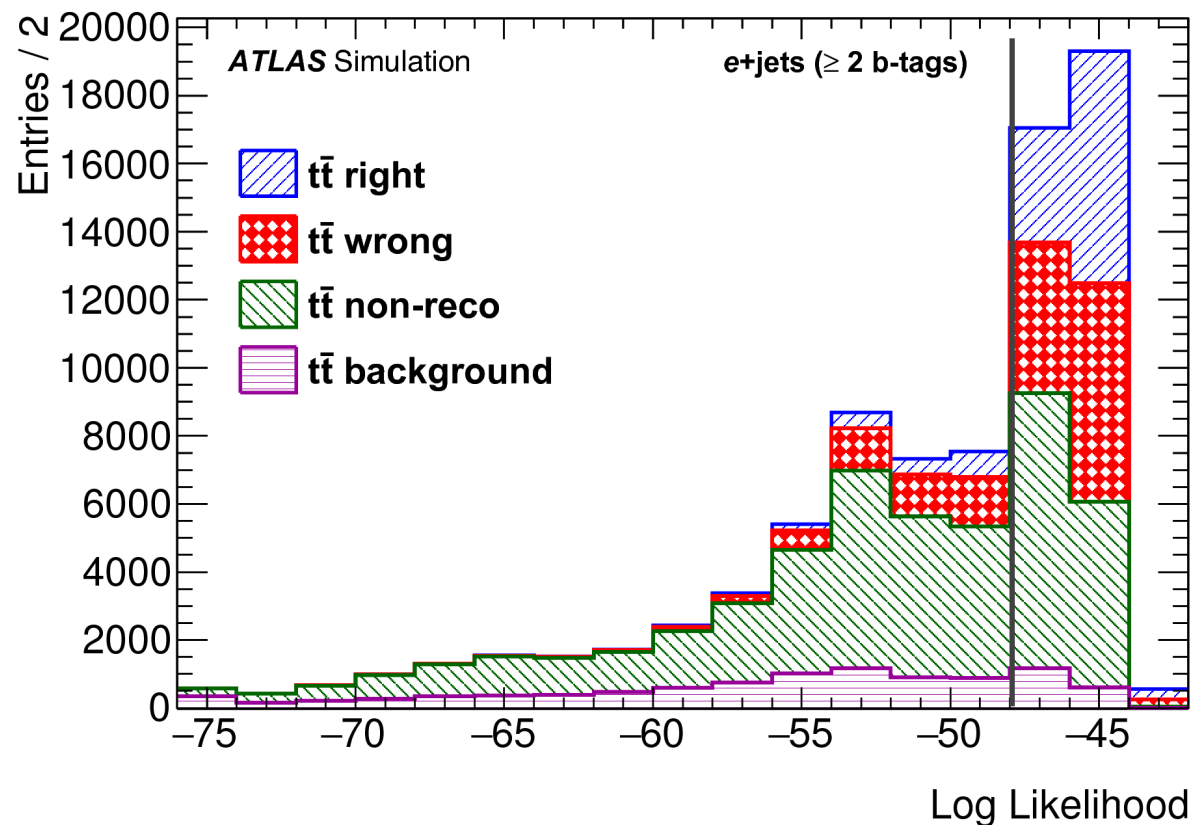
The combination with the highest likelihood is accepted.



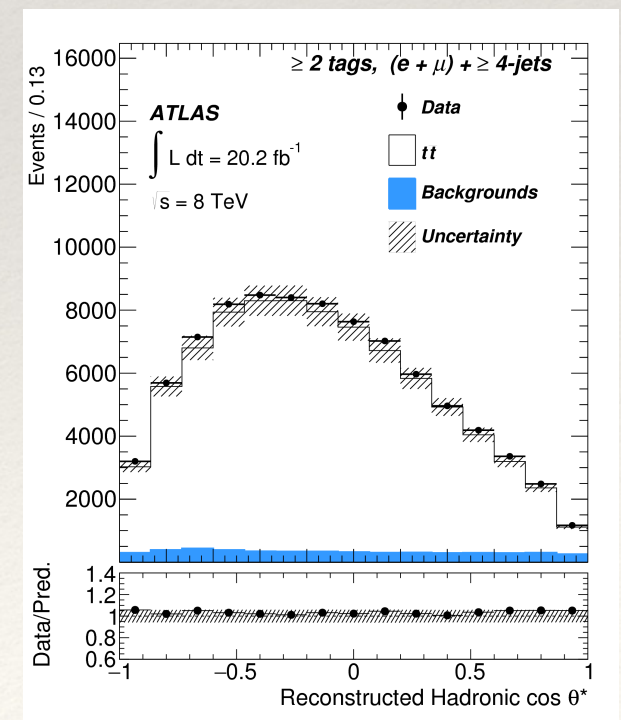
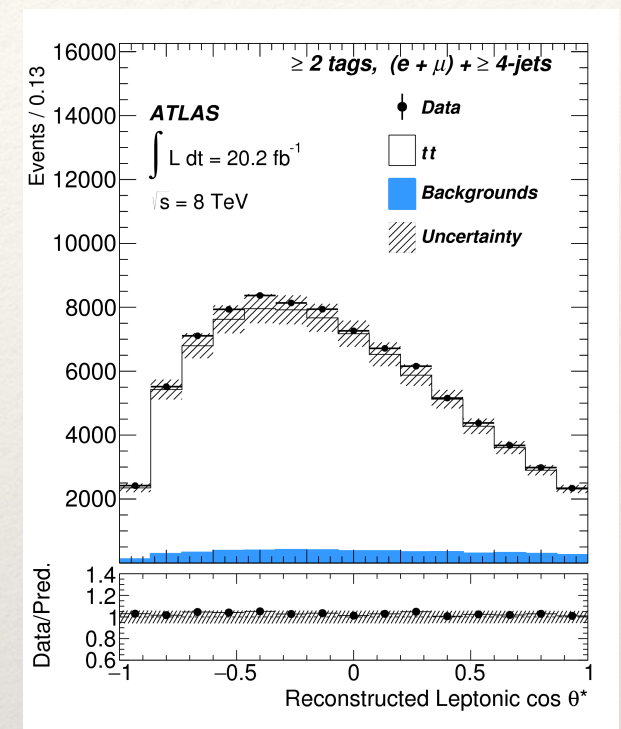
# Event reconstruction

Log likelihood after minimization over kinematic parameters and jet assignment combinations.

cut →



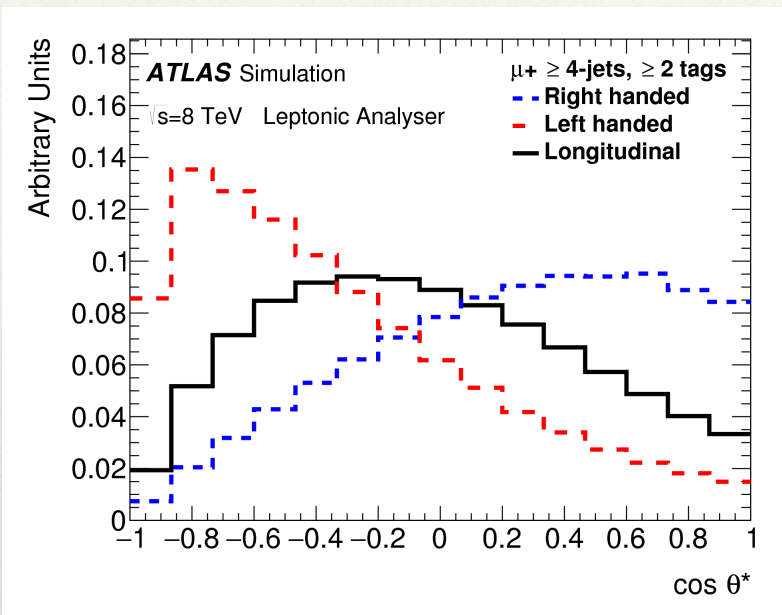
In 60% of  $t\bar{t}$  lepton+jet events, the assignment of down-type quark is correct.



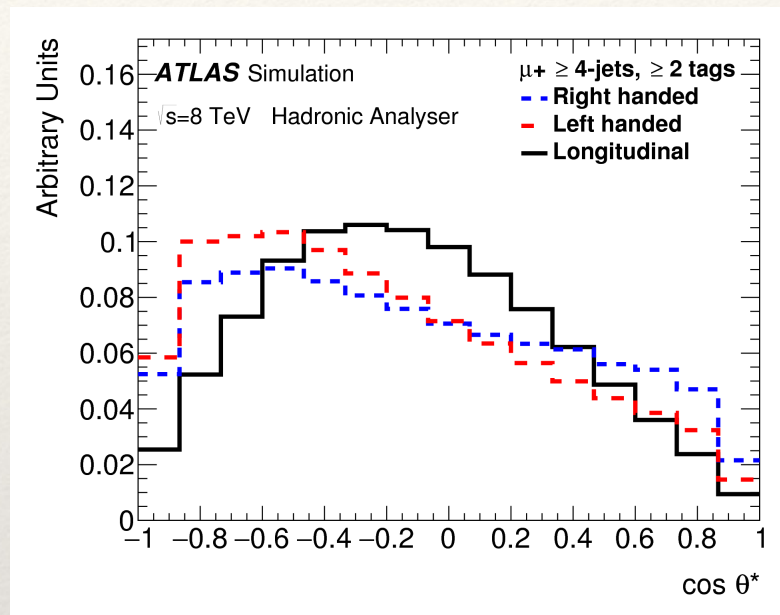


# Template-fits are performed simultaneously in

the leptonic channel

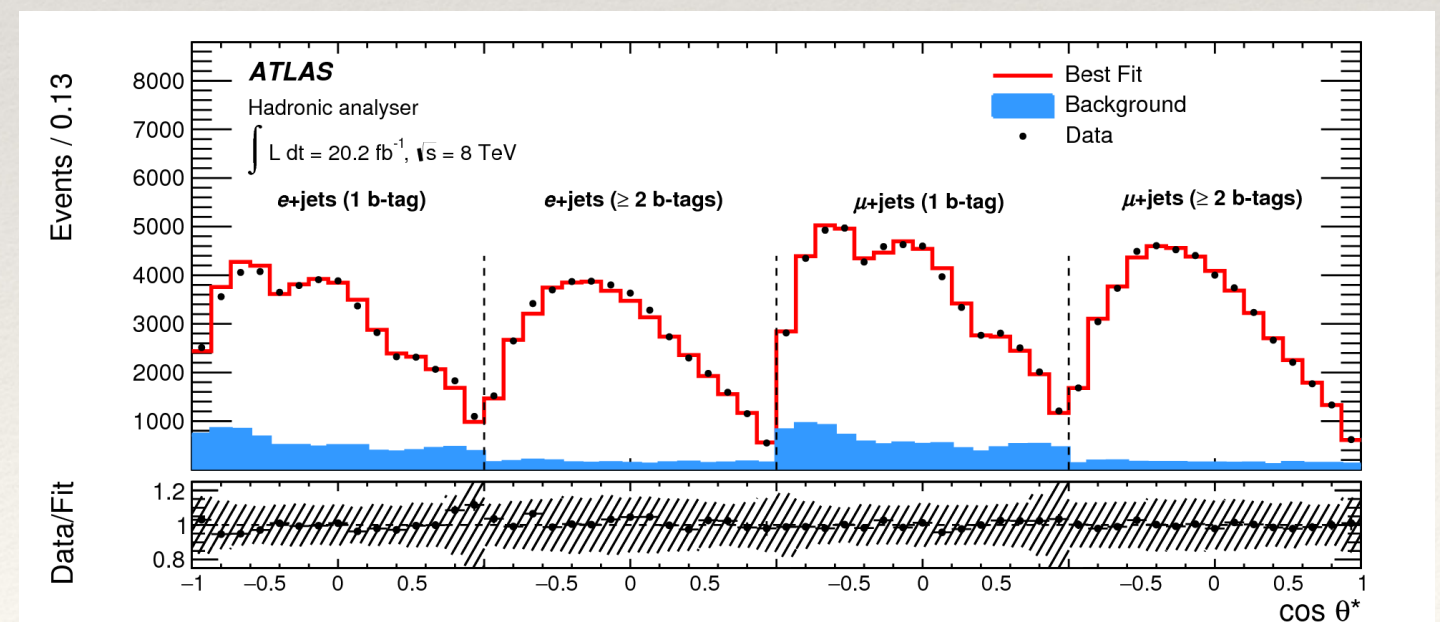
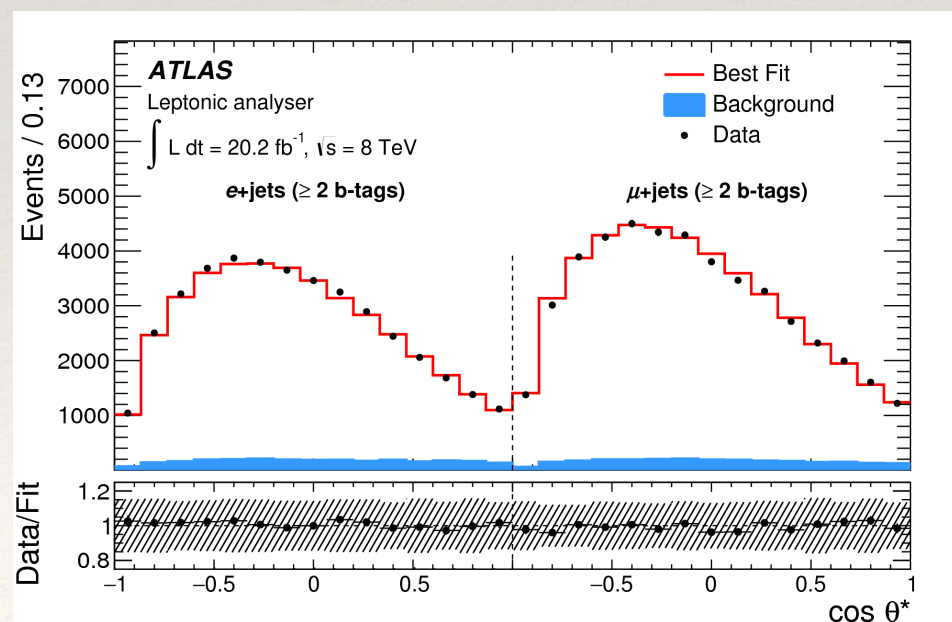


the hadronic channel



Templates for the signal are derived from NLO  $t\bar{t}$  signal MC reweighted at the generator level to distributions from the relevant W boson polarization.

Then the data is fit to templates for the signal and all background sources.



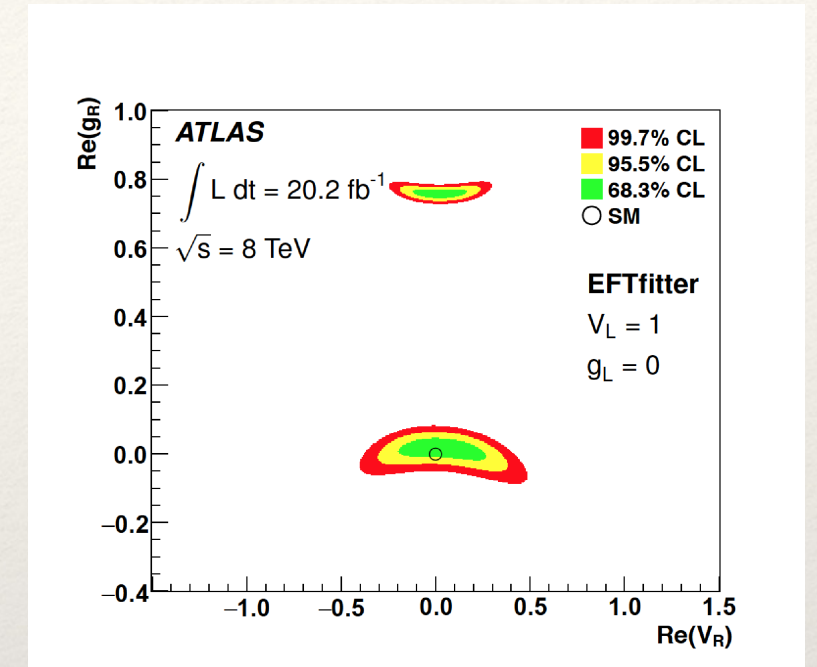
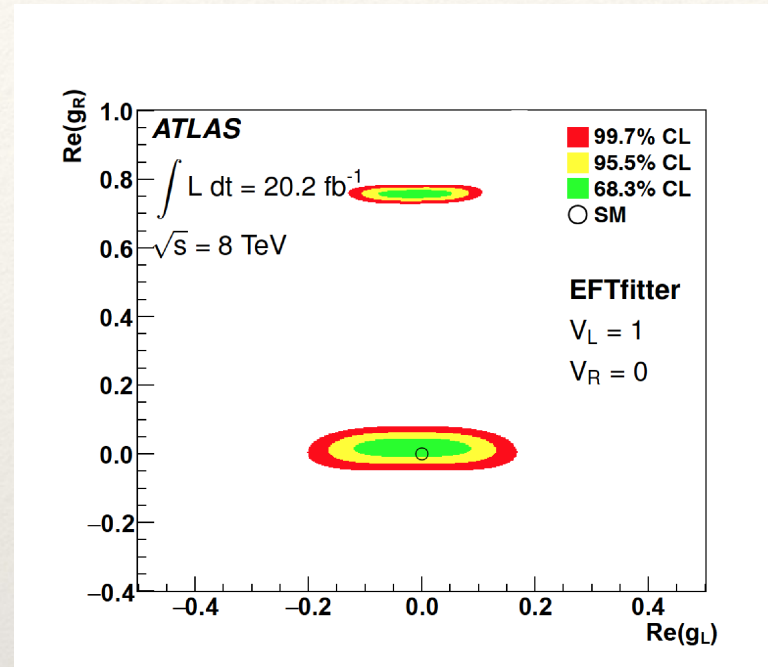


# Results

$$F_0 = 0.709 \pm 0.012 \text{ (stat)} \pm 0.015 \text{ (syst)}$$

$$F_R = -0.008 \pm 0.006 \text{ (stat)} \pm 0.012 \text{ (syst)}$$

$$F_L = 0.299 \pm 0.008 \text{ (stat)} \pm 0.013 \text{ (syst)}$$



## Assumptions:

- All anomalous couplings are real.
- Unconsidered couplings are fixed to their SM values.

The measurements are consistent with the Standard Model; however

- there is an ambiguity, as shown in the plots.
- there is essentially no constraint on the couplings if the above assumptions are not imposed.

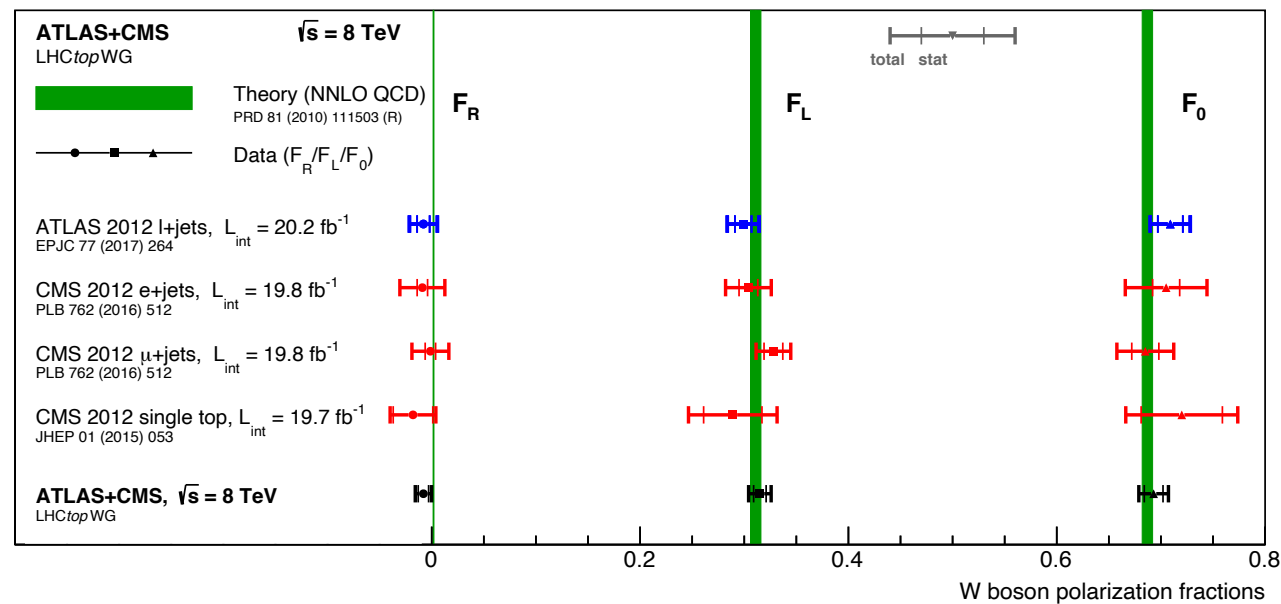
$$F_0 = \frac{|V_L - x_w g_R|^2 + |V_R - x_w g_L|^2}{|V_L - x_w g_R|^2 + |V_R - x_w g_L|^2 + 2|x_w V_L - g_R|^2 + 2|x_w V_R - g_L|^2}$$

$$F_L = \frac{2|x_w V_L - g_R|^2}{|V_L - x_w g_R|^2 + |V_R - x_w g_L|^2 + 2|x_w V_L - g_R|^2 + 2|x_w V_R - g_L|^2}$$

$$F_R = \frac{2|x_w V_R - g_L|^2}{|V_L - x_w g_R|^2 + |V_R - x_w g_L|^2 + 2|x_w V_L - g_R|^2 + 2|x_w V_R - g_L|^2}$$



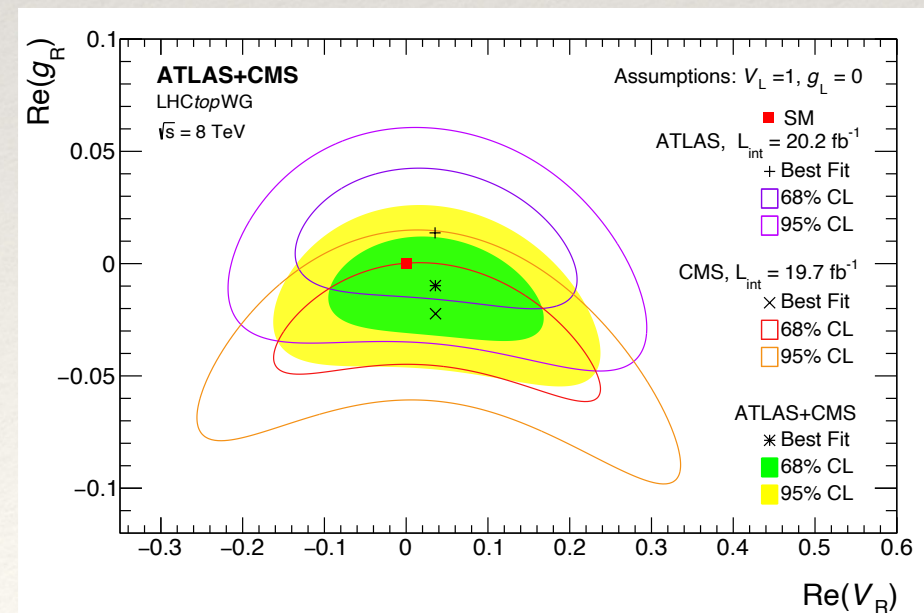
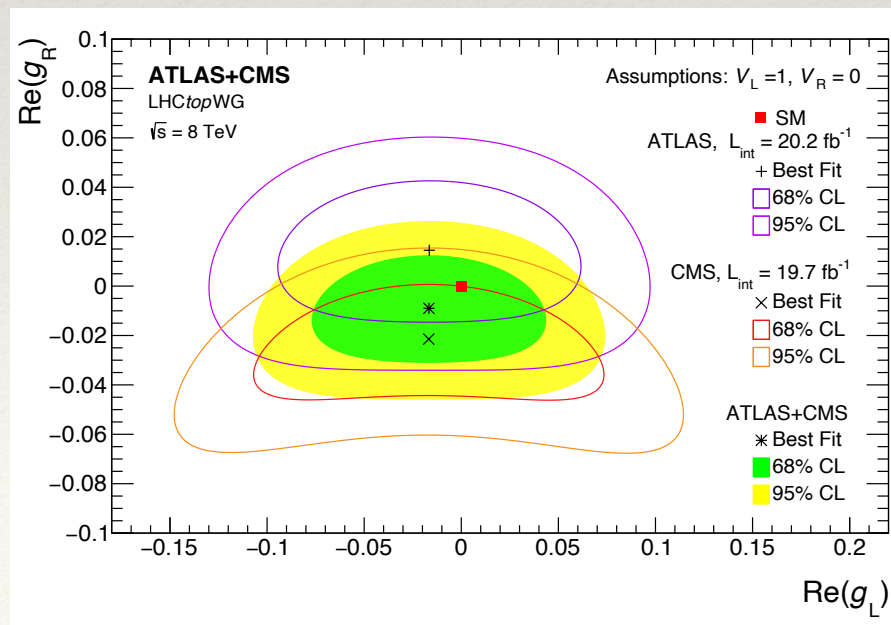
# ATLAS-CMS combination



Results are very precise and agree with the standard model.

Production of right-handed  $W$ 's too small to be observed.

In the ATLAS-CMS combination, the ambiguity is resolved using the cross section measurements.





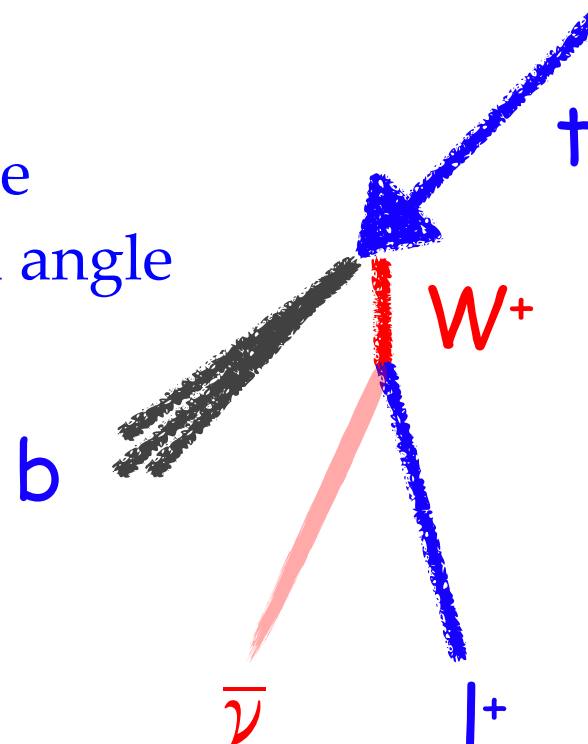
# Angular analysis in single top t-channel

❖ JHEP 12 (2017) 017 (8 TeV)

In single top  $t$ -channel events, the top quark is almost fully polarized along the direction of the spectator quark.

Because of that circumstance, it is germane to consider not one but three angles.:

$\theta$ :  $t$  decay polar angle  
 $\theta^*$ :  $W$  decay polar angle  
 $\phi^*$ :  $W$  decay azimuthal angle



$\bar{q}$

The  $A$ 's are the amplitudes we previously encountered.

- \*  $P$  is the polarization  $\Rightarrow$
- \* The triple differential cross section yields new information only in situations where  $P \neq 0$

Triple differential decay rate

$$\begin{aligned} \frac{1}{N} \frac{d^3 N}{d \cos \theta d \Omega^*} = \frac{1}{8\pi} & \left\{ \frac{3}{4} |A_{1,\frac{1}{2}}|^2 (1 + P \cos \theta) (1 + \cos \theta^*)^2 \right. \\ & + \frac{3}{4} |A_{-1,-\frac{1}{2}}|^2 (1 - P \cos \theta) (1 - \cos \theta^*)^2 \\ & + \frac{3}{2} \left( |A_{0,\frac{1}{2}}|^2 (1 - P \cos \theta) + |A_{0,-\frac{1}{2}}|^2 (1 + P \cos \theta) \right) \sin^2 \theta^* \\ & - \frac{3\sqrt{2}}{2} P \sin \theta \sin \theta^* (1 + \cos \theta^*) \operatorname{Re} \left[ e^{i\phi^*} A_{1,\frac{1}{2}} A_{0,\frac{1}{2}}^* \right] \\ & \left. - \frac{3\sqrt{2}}{2} P \sin \theta \sin \theta^* (1 - \cos \theta^*) \operatorname{Re} \left[ e^{-i\phi^*} A_{-1,-\frac{1}{2}} A_{0,-\frac{1}{2}}^* \right] \right\} \end{aligned}$$



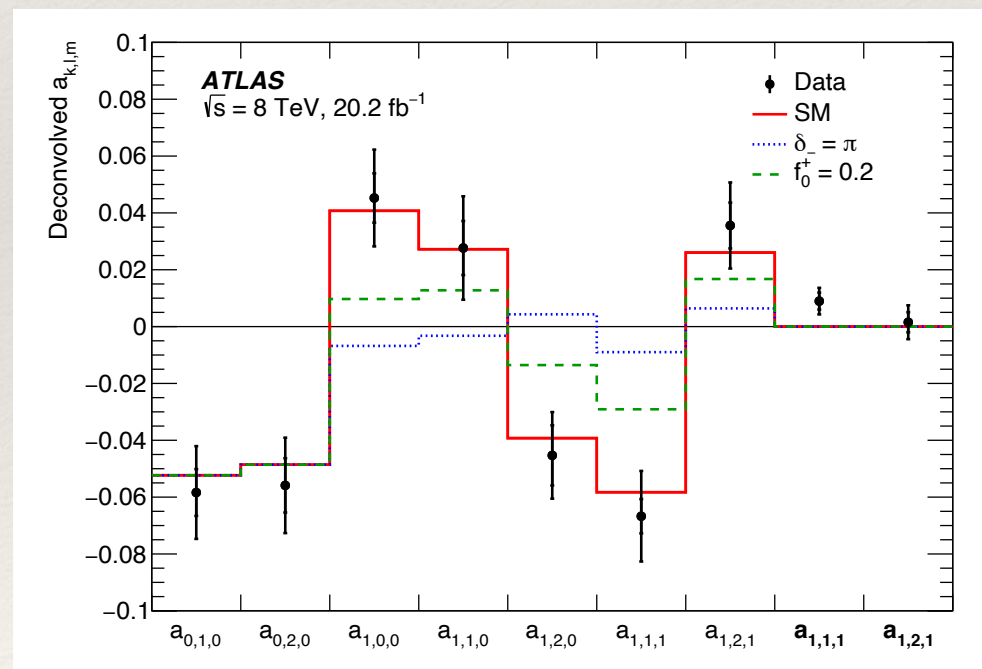
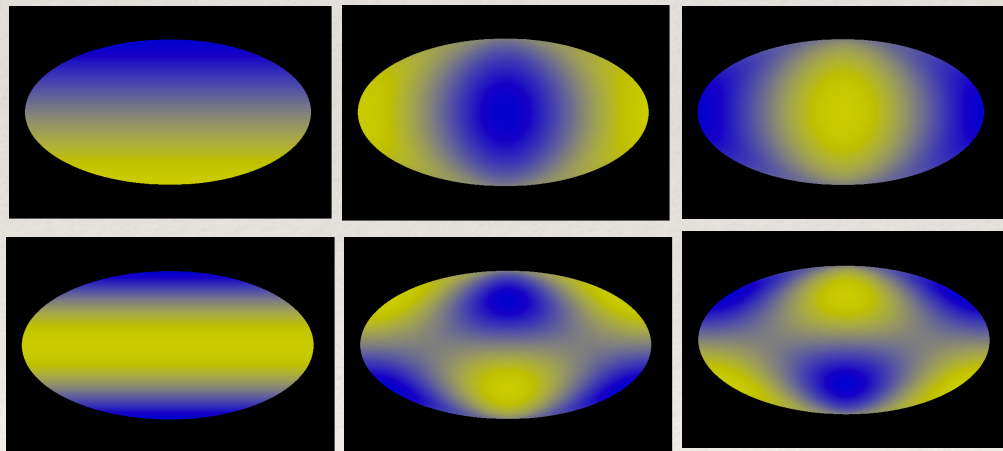
# Series of analyses from ATLAS

Double [JHEP 04 (2016) 023] and triple [JHEP 12 (2017) 017] differential decay rates.

Triple differential cross section:

$$\begin{aligned}\rho(\theta, \theta^*, \phi^*) &\equiv \frac{1}{\Gamma} \frac{d\Gamma}{d\Omega_3} \\ &= a_{k,l}^m M_{k,l}^m(\theta, \theta^*, \phi^*)\end{aligned}$$

$$\begin{aligned}M_{k,l}^m(\theta_1, \theta_2, \phi) &= \sqrt{2\pi} Y_k^m(\theta_1, 0) Y_l^m(\theta_2, \phi) \\ &= \sqrt{2\pi} Y_k^m(\theta_1, \phi) Y_l^m(\theta_2, 0)\end{aligned}$$



[JHEP 12 (2017) 017]

Decompose the differential decay rate into orthogonal functions and perform Fourier analysis.

Use Fourier techniques to deconvolve the detector.



# Helicity fractions & phases with *no assumptions on other parameters*

$f_0^+$ : the fraction of  $b$ 's which are right-handed in events with longitudinal  $W$ 's

$$f_0^+ < 0.041 \text{ (68\% CL)}$$

$$f_0^+ < 0.085 \text{ (95\% CL) } \textit{unique measurement}$$

$f_1^+$ : the fraction of  $b$ 's which are right-handed in events with transverse  $W$ 's.

$$f_1^+ < 0.053 \text{ (68\% CL)}$$

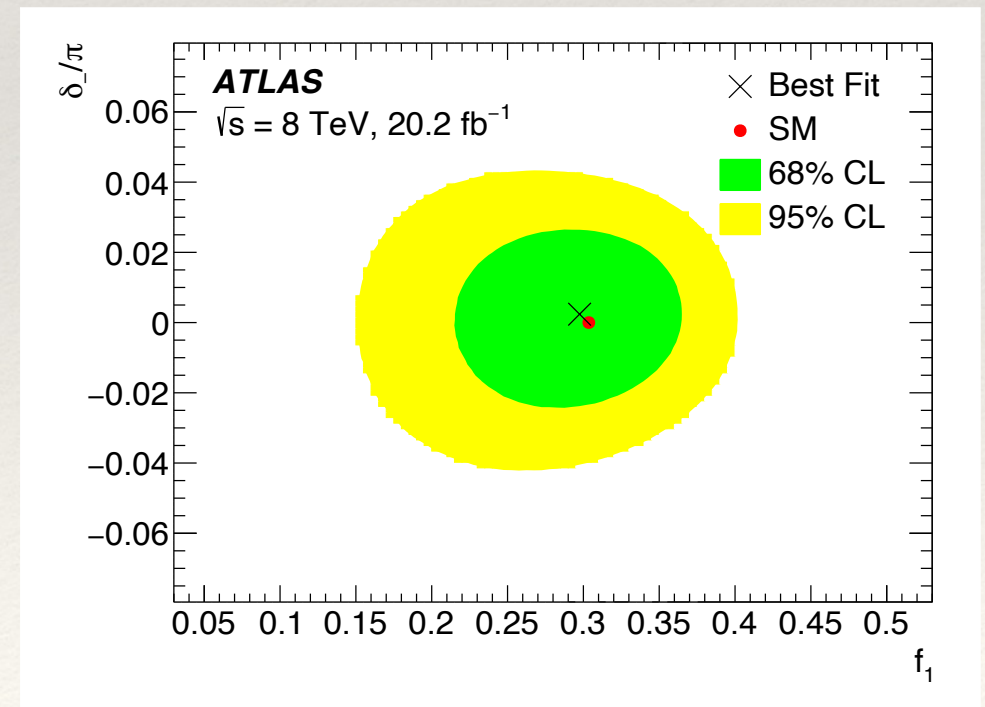
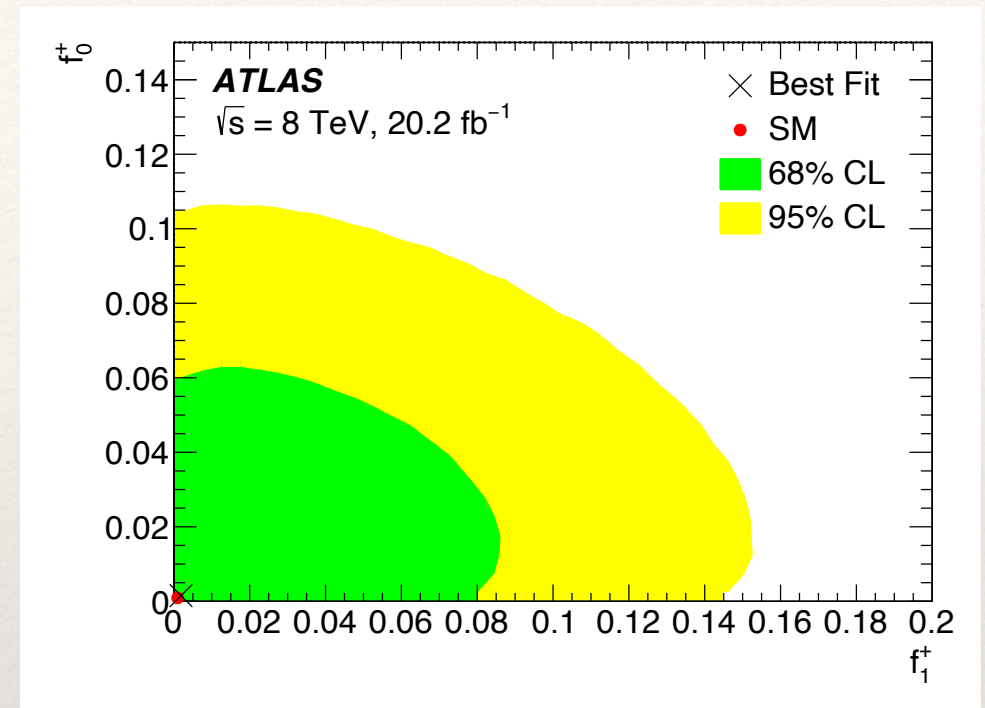
$$f_1^+ < 0.120 \text{ (95\% CL)}$$

$f_1=1-F_L$ : Also measured in  $W$  boson polarization analyses.

$\delta_-$ : If nonzero, could signify CP violation in top quark decay.

$$f_1 = 0.296^{+0.020}_{-0.023} \text{ (stat.) } ^{+0.043}_{-0.046} \text{ (syst.) } = 0.296^{+0.048}_{-0.051},$$

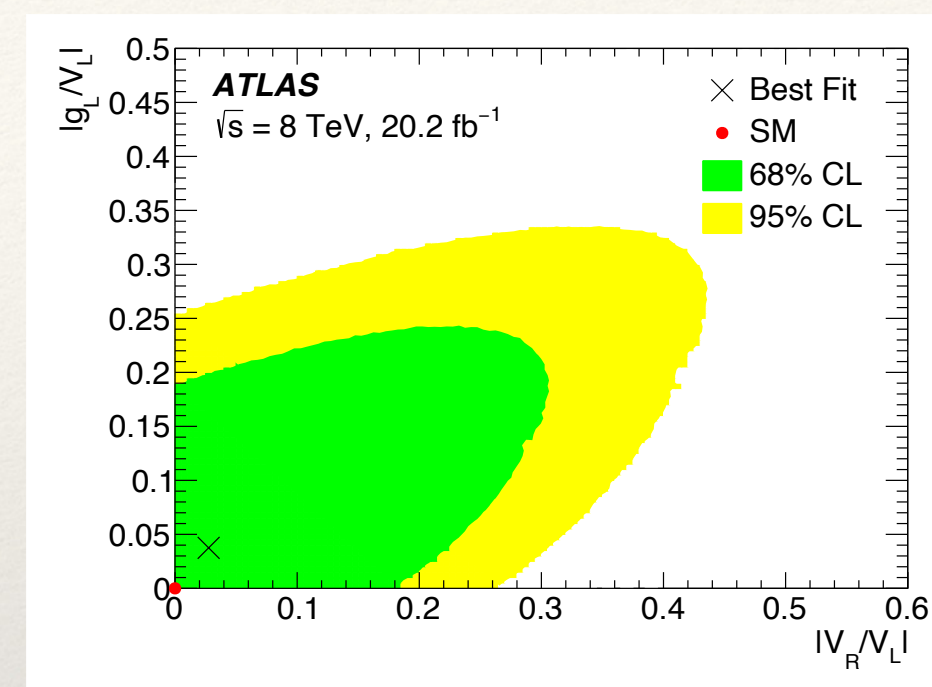
$$\delta_- = 0.002\pi^{+0.013\pi}_{-0.014\pi} \text{ (stat.) } ^{+0.010\pi}_{-0.011\pi} \text{ (syst.) } = 0.002\pi^{+0.016\pi}_{-0.017\pi}.$$



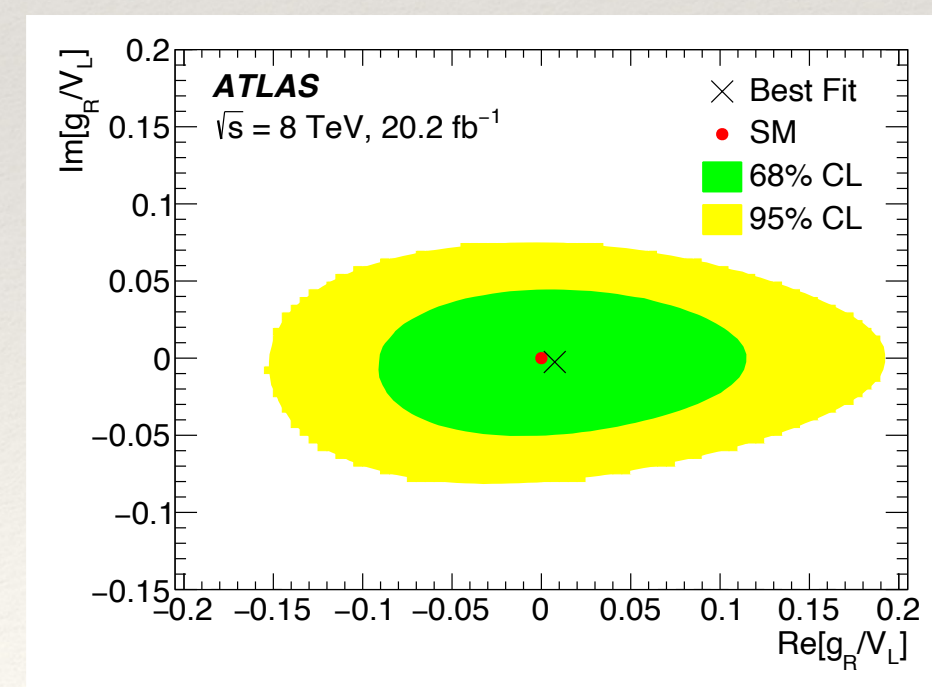


# Anomalous couplings with *no assumptions on other parameters*.

- $|V_R/V_L| < 0.23$  (68% CL)
- $|V_R/V_L| < 0.37$  (95% CL)
- $|g_L/V_L| < 0.19$  (68% CL)
- $|g_L/V_L| < 0.29$  (95% CL)
- Tighter limits exist from  $b \rightarrow s\gamma$  and from W helicity fractions in  $t\bar{t}$  events, but with assumptions on other parameters.

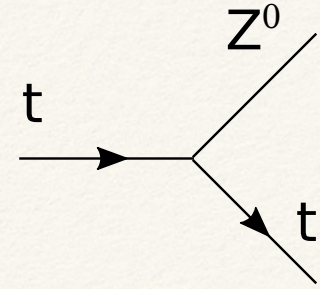


$$\text{Re}\left[\frac{g_R}{V_L}\right] \in [-0.12, 0.17] \quad \text{and} \quad \text{Im}\left[\frac{g_R}{V_L}\right] \in [-0.07, 0.06].$$





# The $Ztt$ vertex

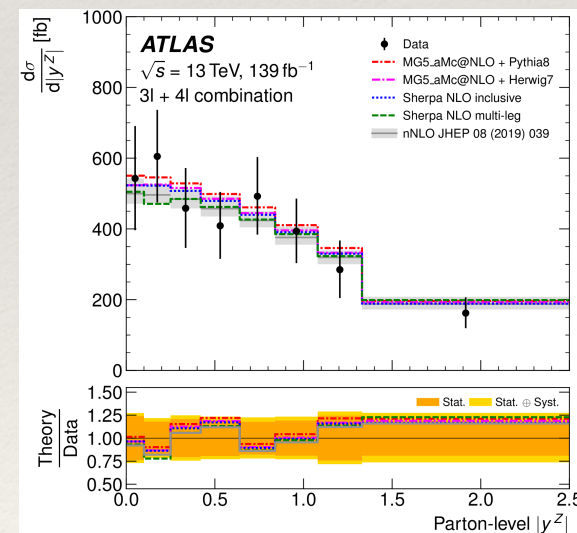
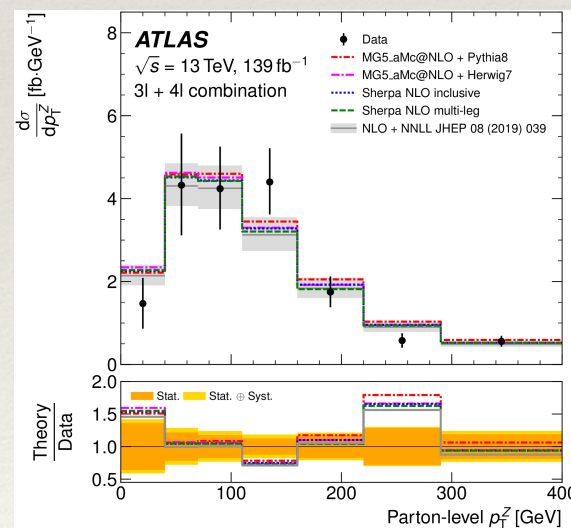
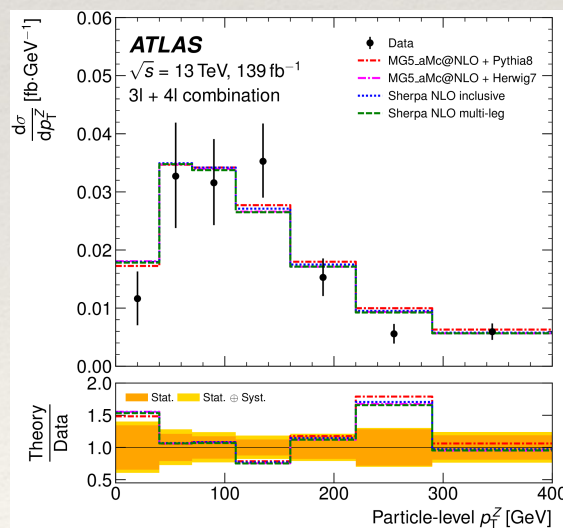
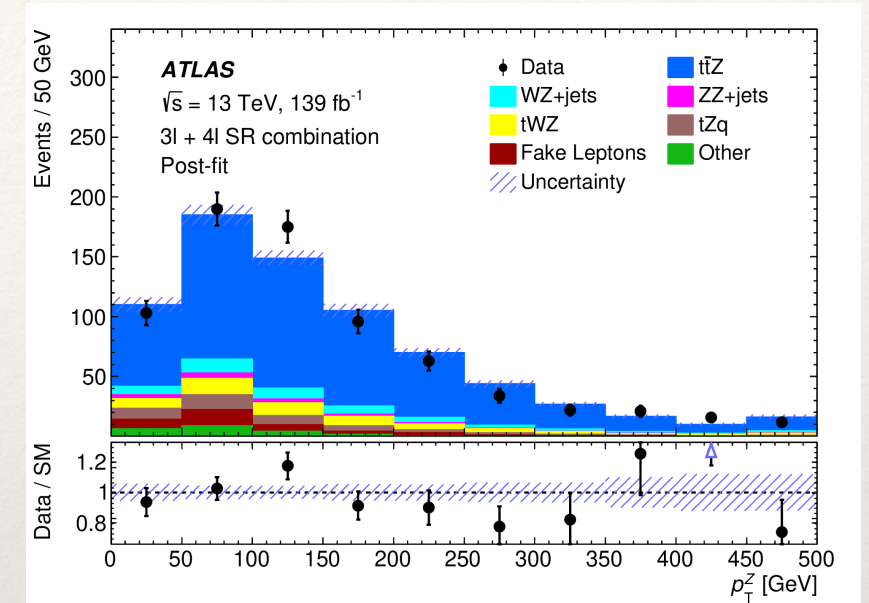


$$\mathcal{L}_{Ztt} = e\bar{t} \left[ \gamma^\mu (C_{1,V} + \gamma^5 C_{1,A}) + \frac{i\sigma^{\mu\nu} p_\nu}{M_Z} (C_{2,V} + i\gamma^5 C_{2,A}) \right] t Z_\mu$$

The vertex is probed in  $t\bar{t}Z$  production in an updated ATLAS measurement of **total** and **differential** cross sections using full Run II data sample.

arXiv: 2103.12603.

3-and 4- lepton final states are considered; distributions unfolded to particle and parton level:

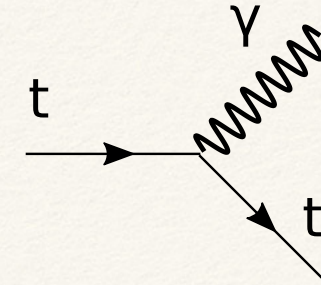


**Inclusive cross section:**

$$\sigma_{t\bar{t}Z} = 0.99 \pm 0.05 \text{ (stat.)} \pm 0.08 \text{ (syst.) pb}$$



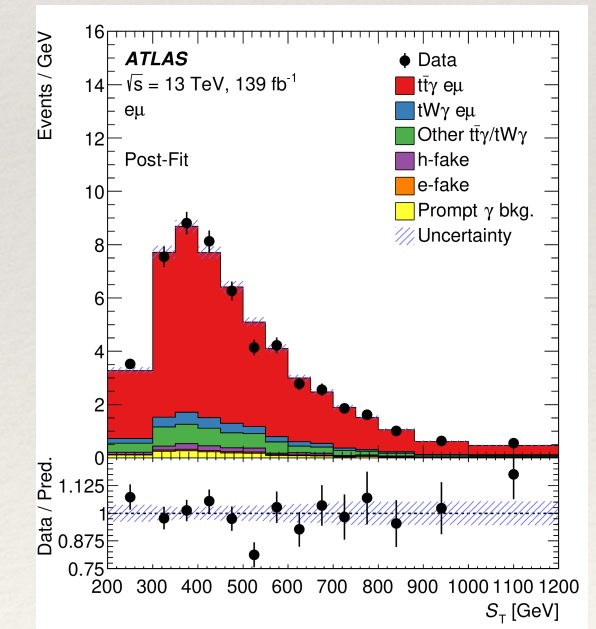
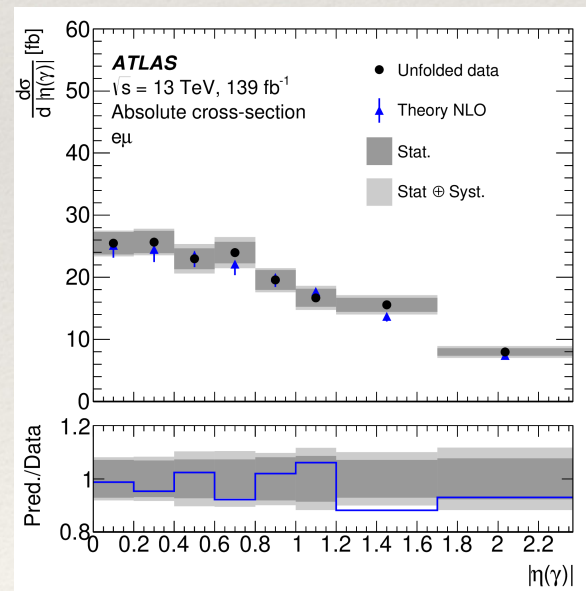
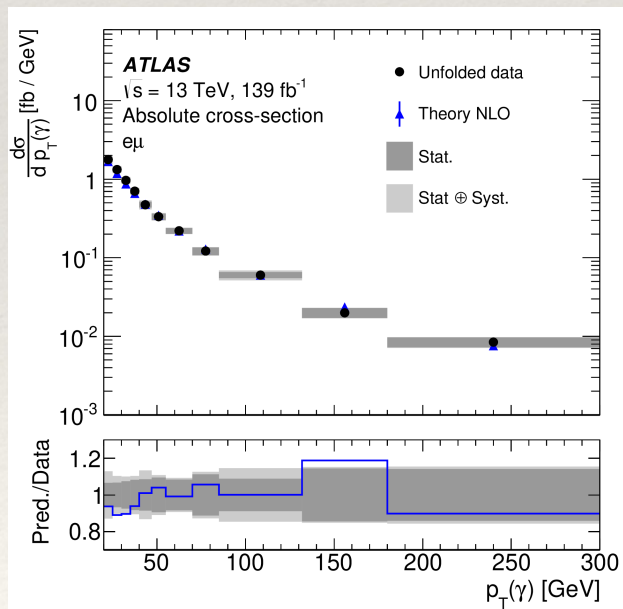
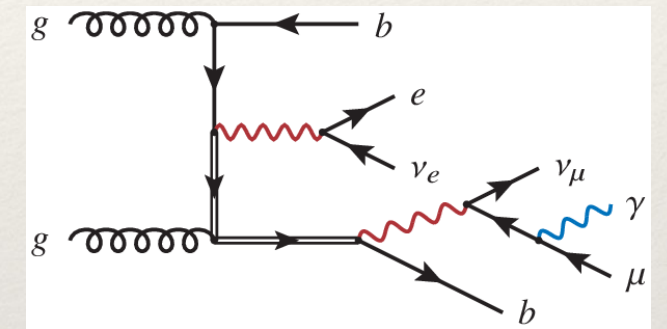
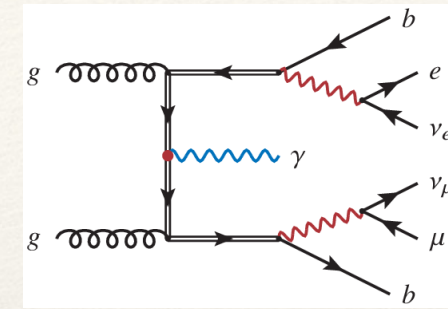
# The $\gamma tt$ vertex



$$\mathcal{L}_{\gamma tt} = -eQ_t \bar{t} \gamma^\mu t A_\mu - e \bar{t} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (d_V^\gamma + i d_A^\gamma \gamma_5) t A_\mu$$

The vertex is probed in  $t\bar{t}\gamma/tW\gamma$  production in an updated ATLAS measurement of **total** and **differential** cross sections using full Run II data sample. JHEP 09 (2020) 049

Signature: one electron, one oppositely charged muon, 2 b-jets, 1 photon.



**Inclusive fiducial cross section:**  $\sigma = 39.6 \pm 0.8 \text{ (stat)}_{-2.2}^{+2.6} \text{ (syst) pb}$



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# Conclusions

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- ❖ We have reviewed three analysis related to the Wtb vertex: Single top cross sections, W Boson polarization in top quark decay, and angular analysis in single top t-channel events.
- ❖  $f_1 = 1 - F_L$ ,  $f_0^+$ ,  $f_1^+$ ,  $\delta_-$  from **single top angular distributions** and  $|f_{LV}V_{tb}|$  from **cross section measurements** represent **5 independent observables quantities**.
- ❖ Helicity fraction measurements provide the best precision on two parameters,  $F_L$  and  $F_0$  (independent of each other, but dependent on those previously mentioned).
- ❖ The Wtb vertex is described by:
  - ❖ 4 couplings strengths + 3 relative phases = **7 parameters**.
- ❖ An ideal way to use all this information would be to combine it, but correlations in systematic uncertainties make this challenging.
- ❖ Future measurements are being designed with combination in mind.
- ❖ Total and differential cross sections in  $t\bar{t}\gamma$  and  $t\bar{t}Z$  productions measured in full Run II dataset, presaging rich opportunities to fully investigate the  $Ztt$  and  $\gamma tt$  vertices.



# Furthermore: ATLAS results on other top couplings?

