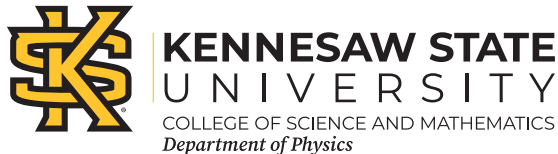


tW and tZ' production at hadron colliders

Nikolaos Kidonakis

- Soft-gluon corrections
- tW production
- tZ' production

with Marco Guzzi (tZ') and Nodoka Yamanaka (tW)



DIS 2021



Soft-gluon corrections

They are important for top-quark processes

They approximate known exact results at NLO and NNLO very well

$$f_1(p_1) + f_2(p_2) \rightarrow t(p_t) + V \quad (V = W \text{ or } Z')$$

define $s = (p_1 + p_2)^2$, $t = (p_1 - p_t)^2$, $u = (p_2 - p_t)^2$ and $s_4 = s + t + u - \sum_i m_i^2$

At partonic threshold $s_4 \rightarrow 0$

Soft corrections $\left[\frac{\ln^k(s_4/m^2)}{s_4} \right]_+$ with $k \leq 2n - 1$ for the order α_s^n corrections

we set $m = m_t$ for tW production and $m = m_{Z'}$ for tZ' production

Resum these soft corrections for the double-differential cross section

At NNLL accuracy we need two-loop soft anomalous dimensions

At N³LL accuracy we need three-loop soft anomalous dimensions

Finite-order expansions \rightarrow no prescription needed

Approximate NNLO (aNNLO) and N³LO (aN³LO) predictions

for cross sections and differential distributions

Soft-gluon Resummation

moments of the partonic cross section with moment variable N :

$$\hat{\sigma}(N) = \int (ds_4/s) e^{-Ns_4/s} \hat{\sigma}(s_4)$$

factorized expression for the cross section

$$\sigma^{f_1 f_2 \rightarrow tV}(N) = \psi_1(N_1, \mu_F) \psi_2(N_2, \mu_F) H^{f_1 f_2 \rightarrow tV}(\alpha_s(\mu_R)) S^{f_1 f_2 \rightarrow tV}\left(\frac{m}{N\mu_F}, \alpha_s(\mu_R)\right)$$

$\psi_1, \psi_2 \rightarrow$ collinear emission from incoming partons

$H^{f_1 f_2 \rightarrow tV}$ is hard function \rightarrow short distance

$S^{f_1 f_2 \rightarrow tV}$ is soft function \rightarrow noncollinear soft gluons

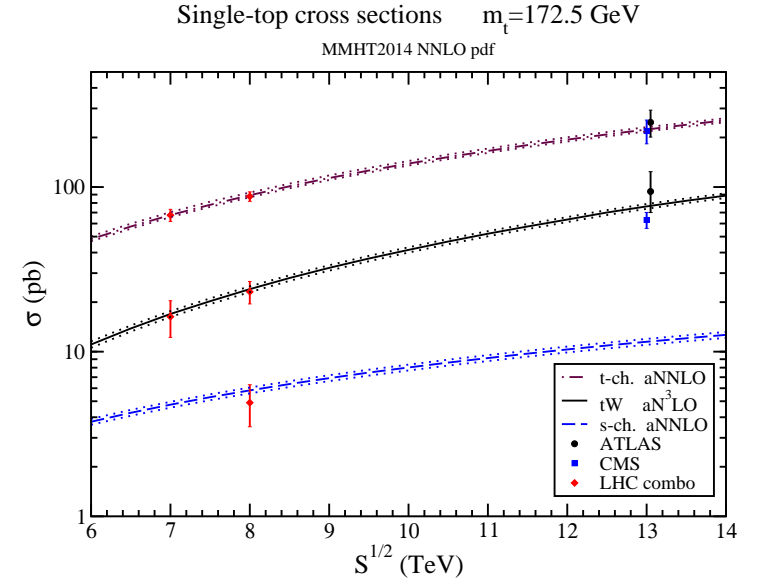
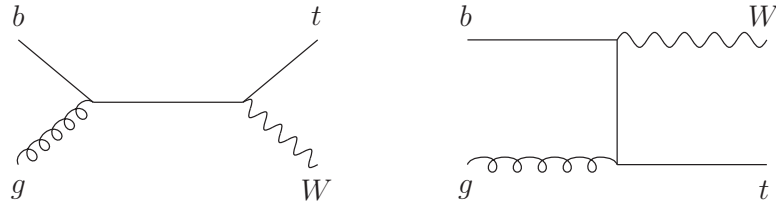
$S^{f_1 f_2 \rightarrow tV}$ satisfies the renormalization group equation

$$\left(\mu_R \frac{\partial}{\partial \mu_R} + \beta(g_s) \frac{\partial}{\partial g_s}\right) S^{f_1 f_2 \rightarrow tV} = -\Gamma_S^\dagger S^{f_1 f_2 \rightarrow tV} - S^{f_1 f_2 \rightarrow tV} \Gamma_S$$

Soft anomalous dimension $\Gamma_S^{f_1 f_2 \rightarrow tV}$ controls the evolution of the soft function which gives the exponentiation of logarithms of N

tW production

leading-order diagrams



At one loop $\Gamma_S^{(1) bg \rightarrow tW} = C_F \left[\ln \left(\frac{m_t^2 - t}{m_t \sqrt{s}} \right) - \frac{1}{2} \right] + \frac{C_A}{2} \ln \left(\frac{u - m_t^2}{t - m_t^2} \right)$

At two loops $\Gamma_S^{(2) bg \rightarrow tW} = K_2 \Gamma_S^{(1) bg \rightarrow tW} + \frac{1}{4} C_F C_A (1 - \zeta_3)$

where $K_2 = C_A \left(\frac{67}{36} - \frac{\zeta_2}{2} \right) - \frac{5}{18} n_f$

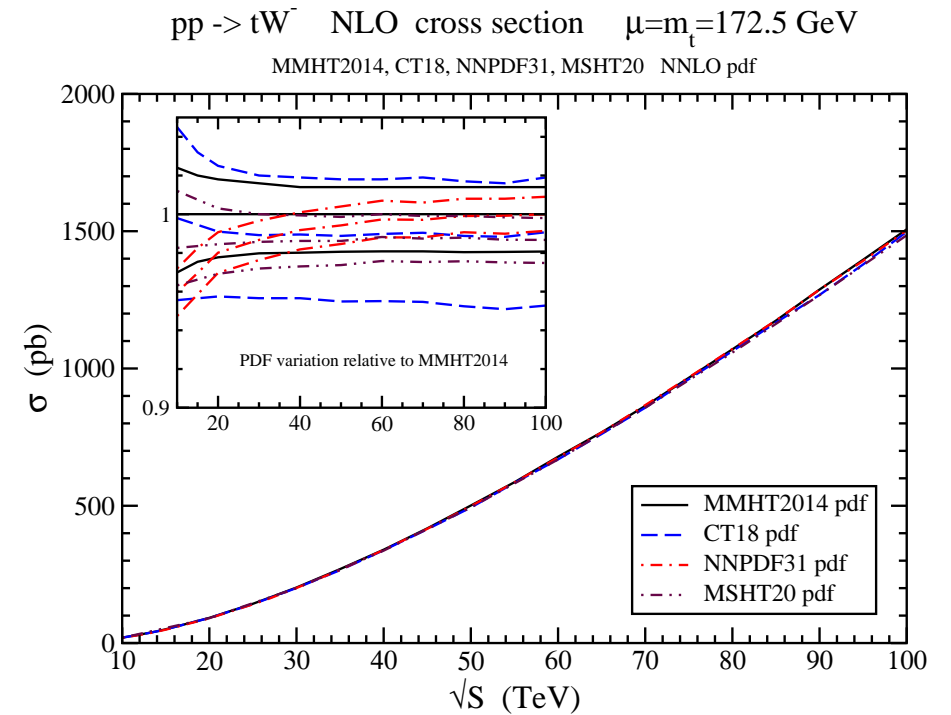
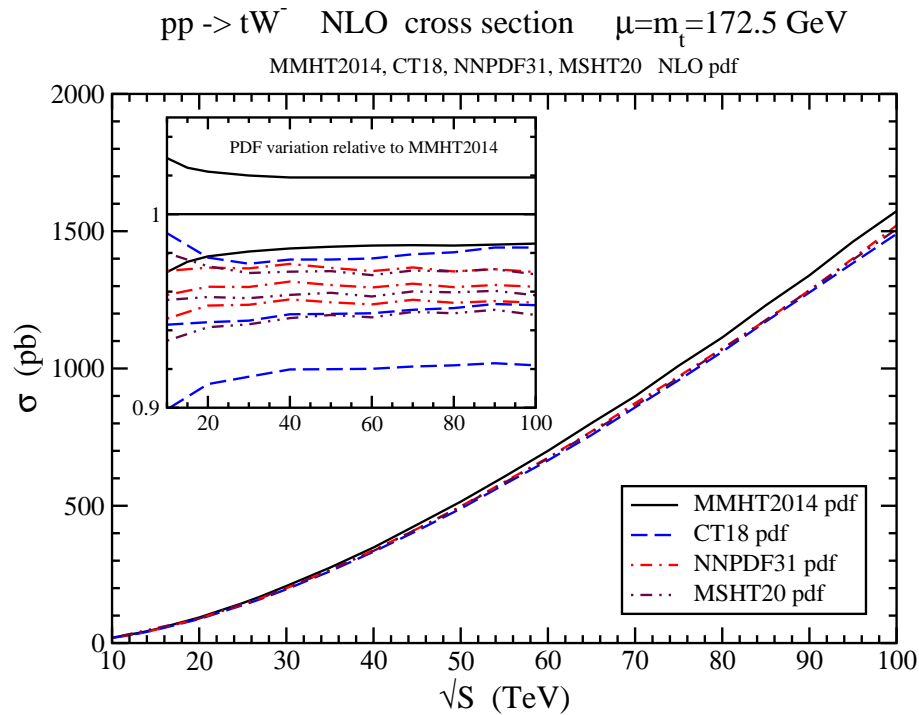
At three loops

$$\Gamma_S^{(3) bg \rightarrow tW} = K_3 \Gamma_S^{(1) bg \rightarrow tW} + \frac{1}{2} K_2 C_F C_A (1 - \zeta_3) + C_F C_A^2 \left[-\frac{1}{4} + \frac{3}{8} \zeta_2 - \frac{\zeta_3}{8} - \frac{3}{8} \zeta_2 \zeta_3 + \frac{9}{16} \zeta_5 \right]$$

(same soft anomalous dimension for tZ' production)

tW production at high-energy colliders

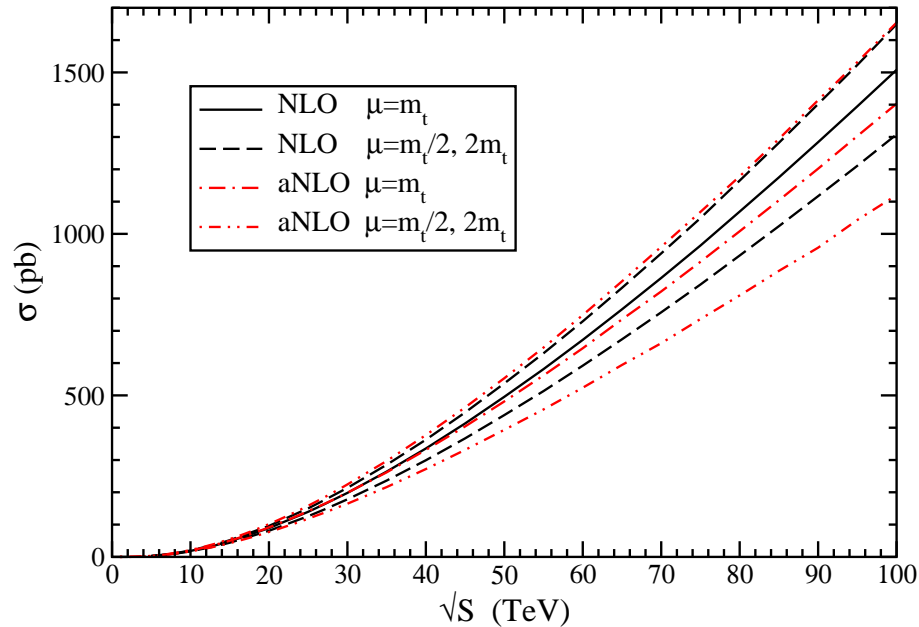
(with Nodoka Yamanaka, arXiv:2102.11300)



smaller pdf-set dependence with NNLO pdf

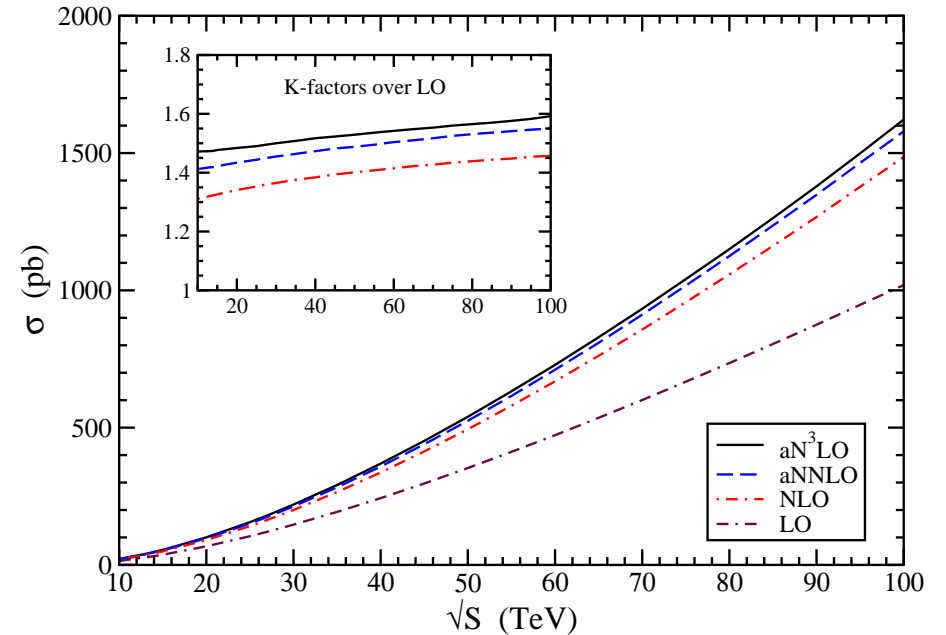
pp \rightarrow tW⁻ NLO and aNLO cross sections $m_t=172.5$ GeV

MSHT20 NLO pdf



pp \rightarrow tW⁻ cross section $\mu=m_t=172.5$ GeV

MSHT20 NNLO pdf



The aNLO cross section is a very good approximation to the complete NLO result for all foreseeable collider energies

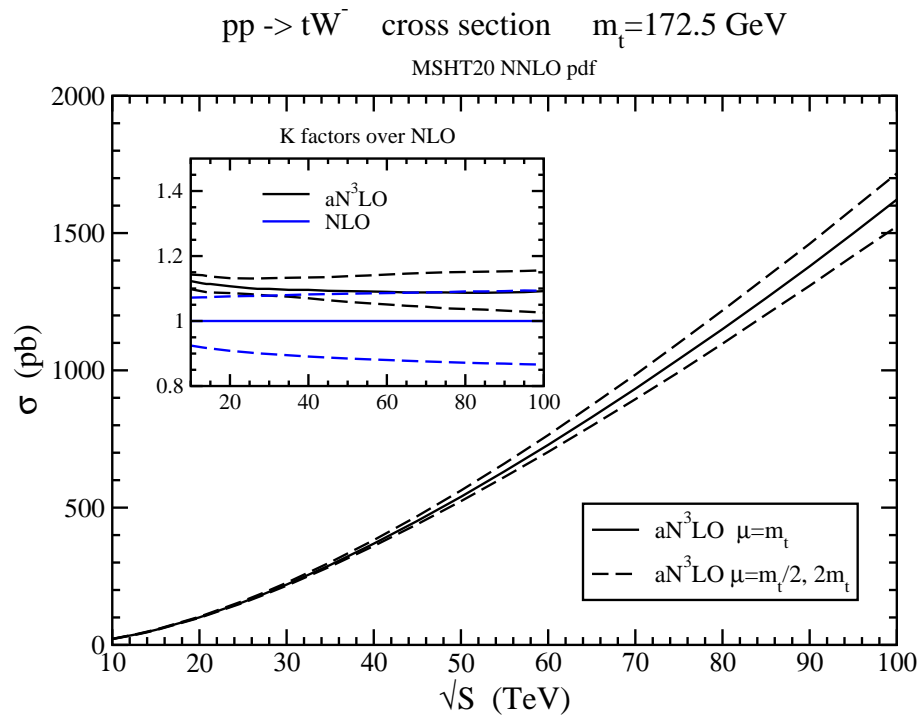
→ the soft-gluon corrections are dominant

The aNNLO and aN³LO corrections (at NNLL) are also significant

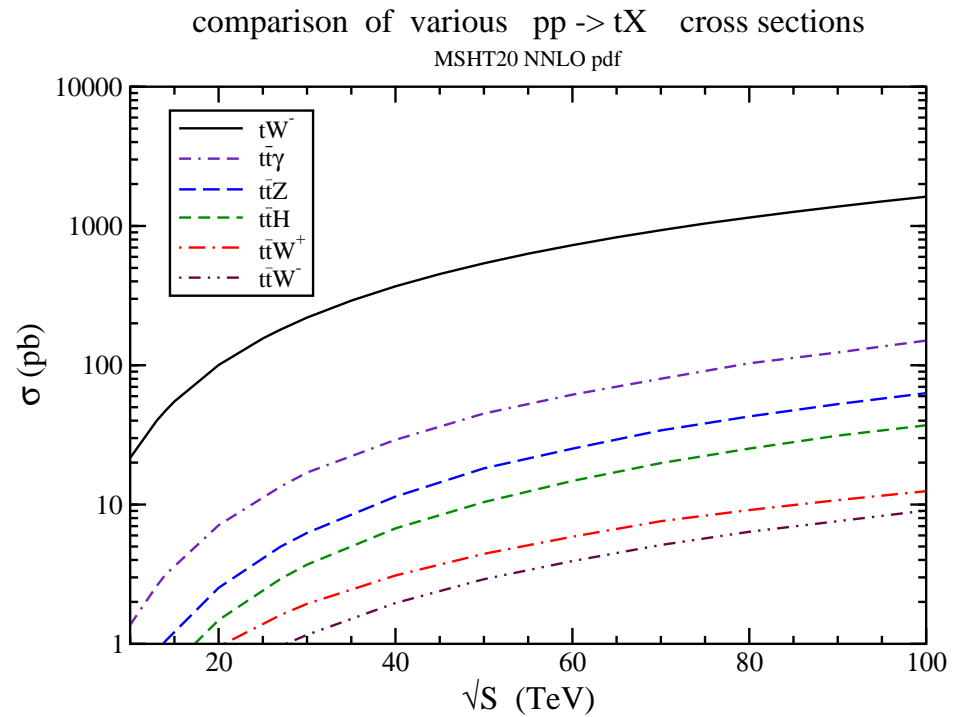
The aN³LO cross section with scale and pdf (MSHT20) uncertainty is

at 13 TeV: $39.9 \pm 0.9^{+1.0}_{-0.7}$ pb

at 14 TeV $47.1^{+1.1+1.1}_{-1.0-0.8}$ pb

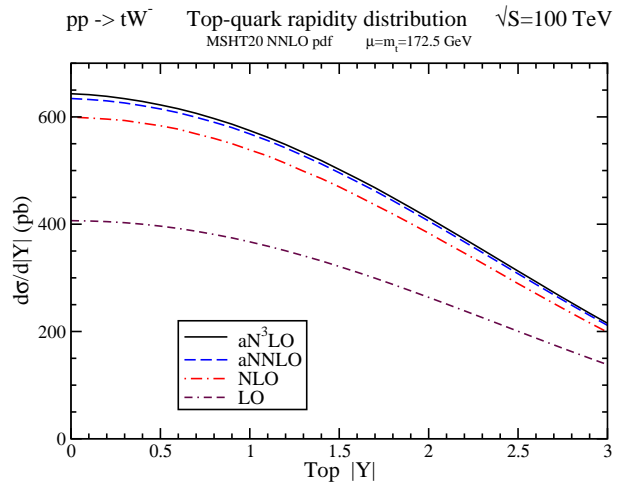
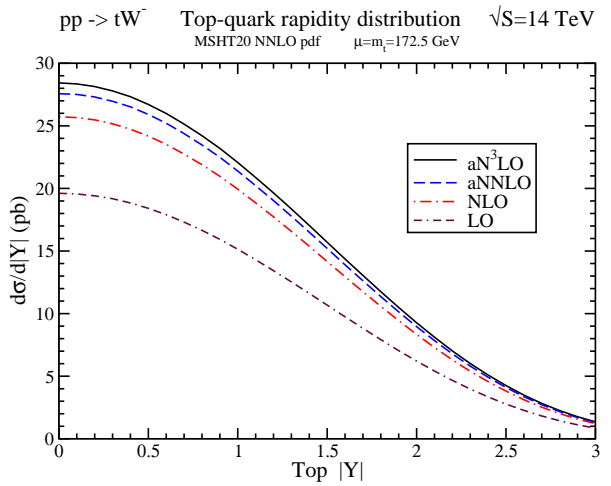
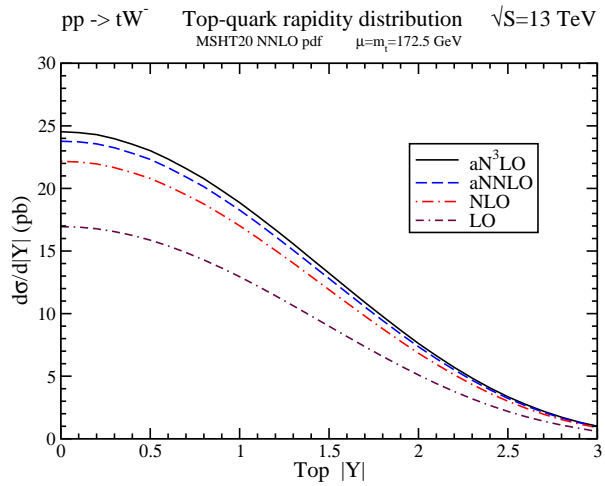
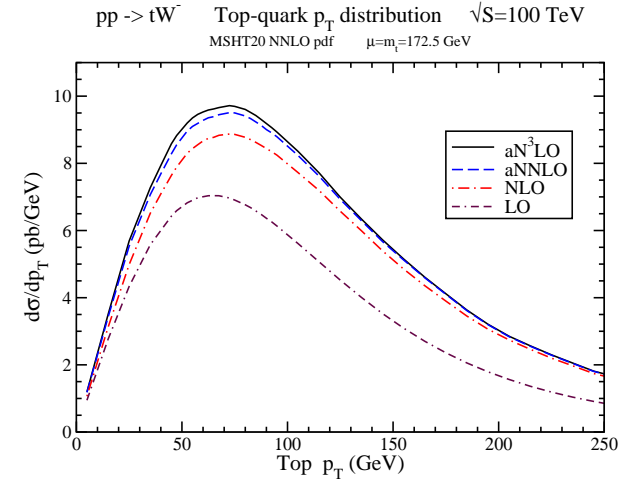
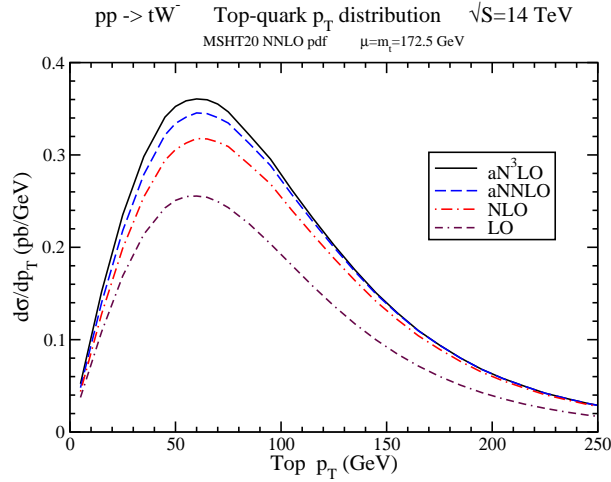
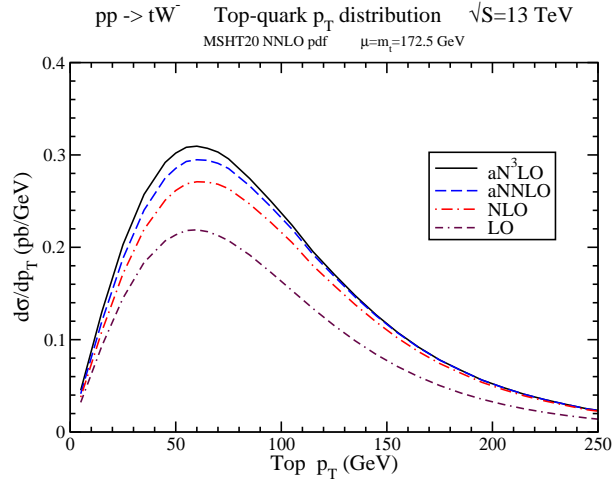


scale dependence at aN³LO
is reduced relative to NLO



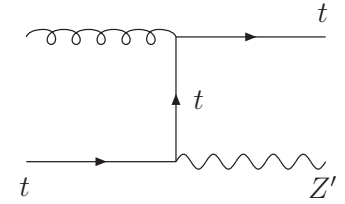
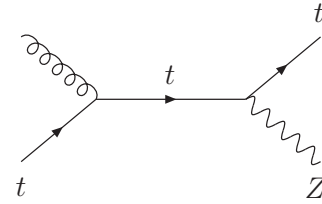
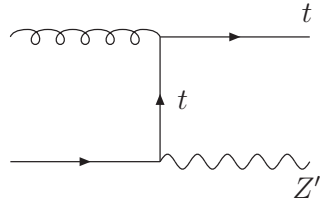
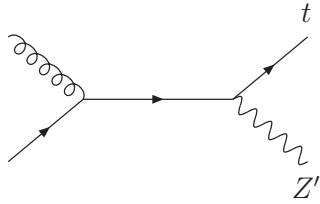
tW production cross sections
are larger than for other top-quark
processes with final-state
electroweak and Higgs bosons

Top quark p_T and rapidity distributions in tW production



tZ' production in various models

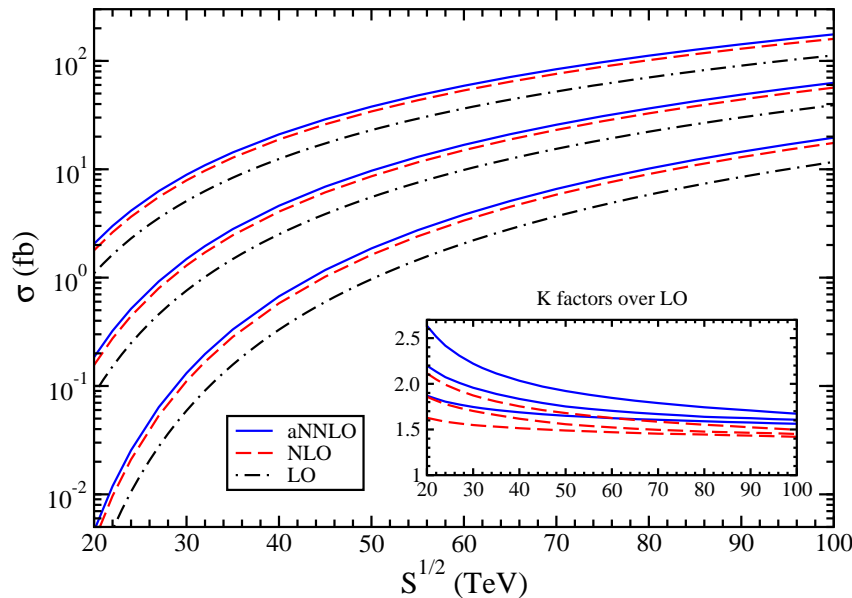
(with Marco Guzzi, Eur. Phys. J. C 80, 467)



via anomalous $t-u-Z'$ or $t-c-Z'$ couplings

$$\mathcal{L}_{FCNC} = (\kappa_{tqZ'}/\Lambda) e \bar{t} \sigma_{\mu\nu} q F_{Z'}^{\mu\nu} + \text{h.c.}$$

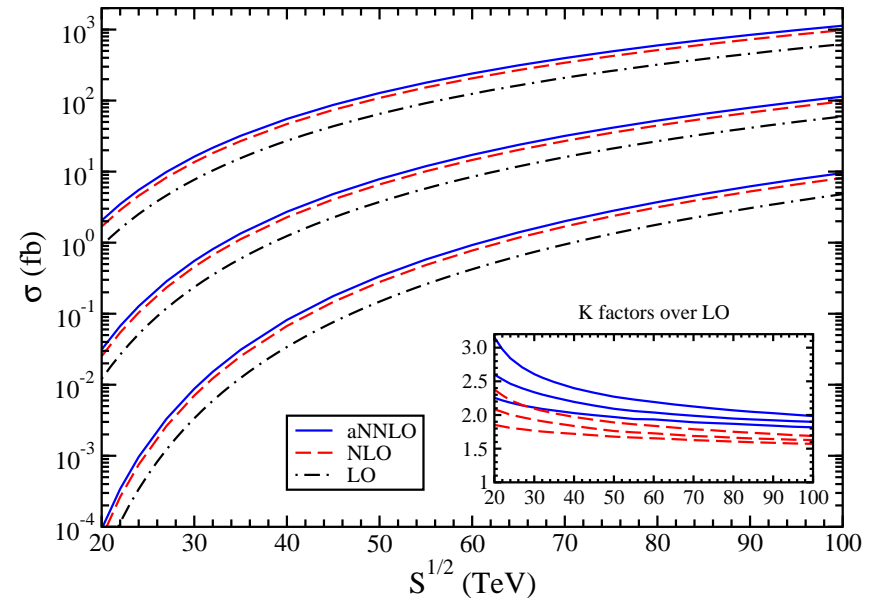
$gu \rightarrow tZ'$ in pp collisions $m_{Z'}=3, 5, 8 \text{ TeV}$ $k_{tuZ'}/\Lambda=0.01/m_t$
 CT14 NNLO pdf $\mu=m_{Z'}$ $m_t=172.5 \text{ GeV}$

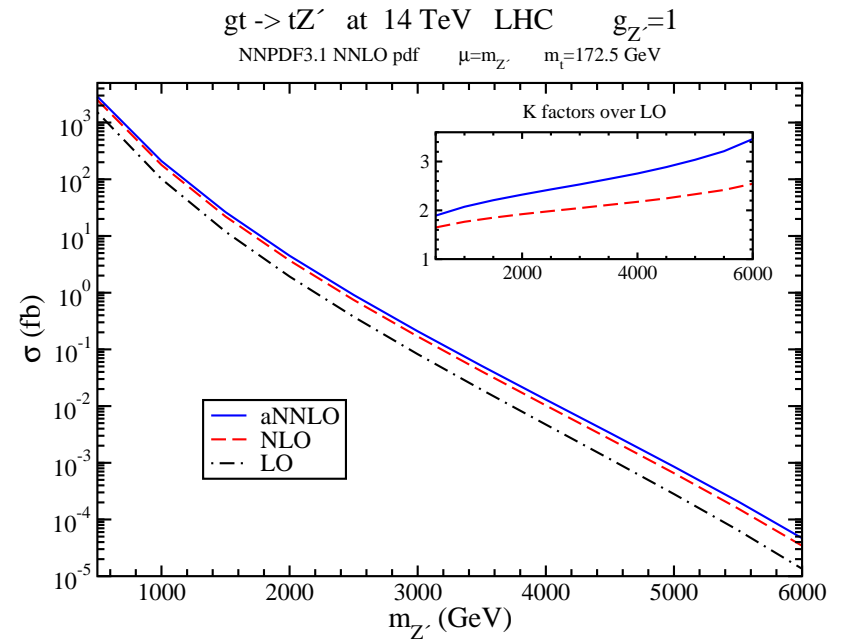
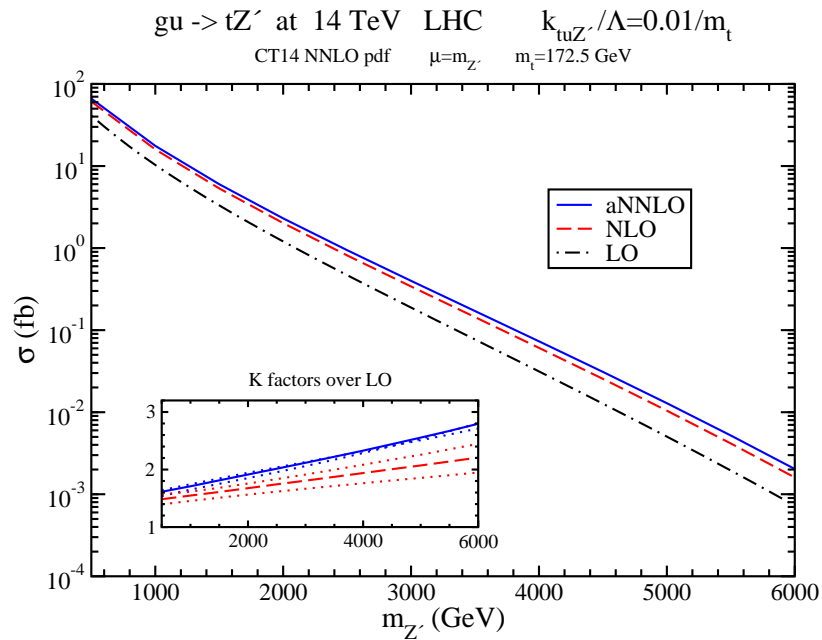
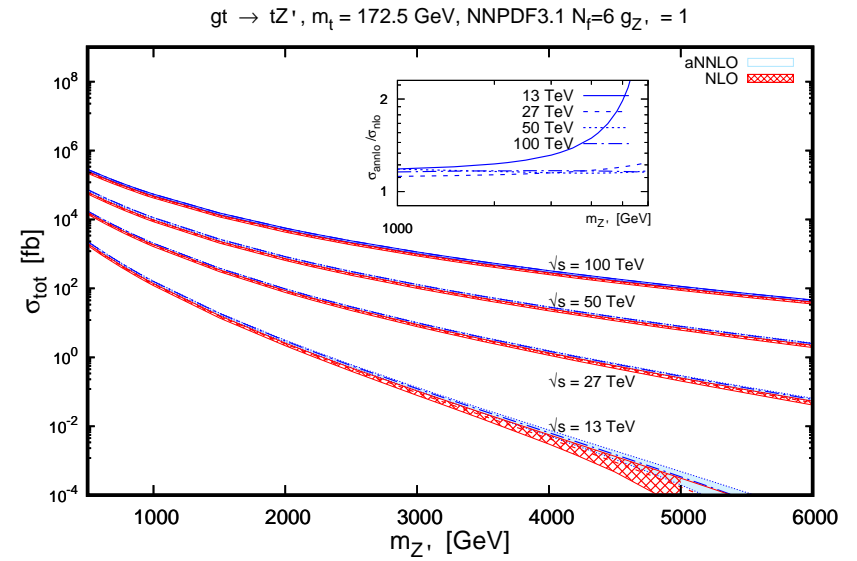
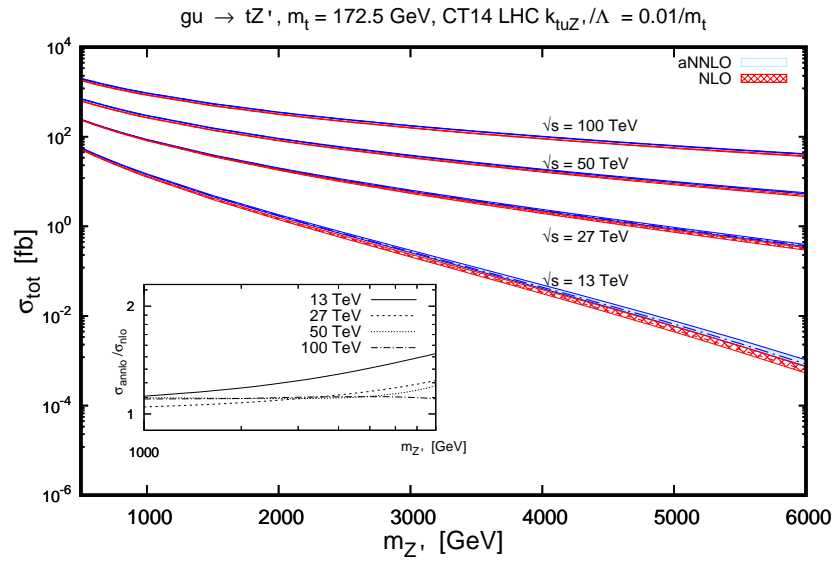


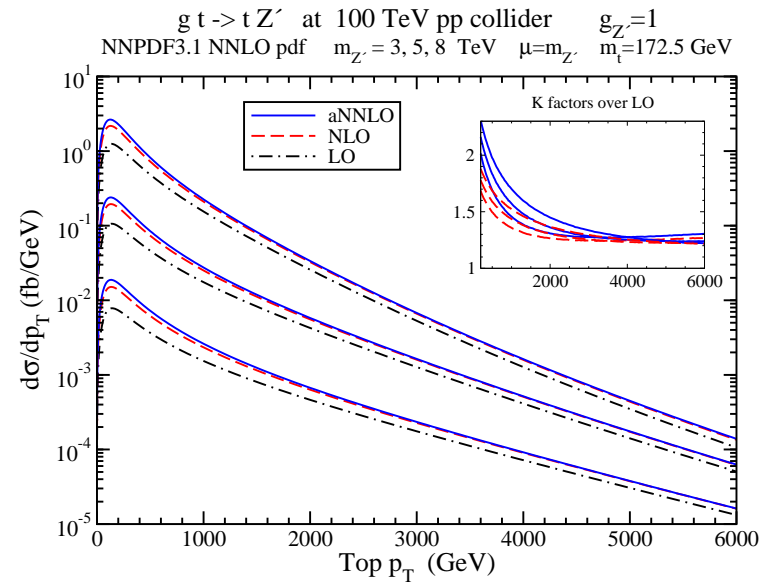
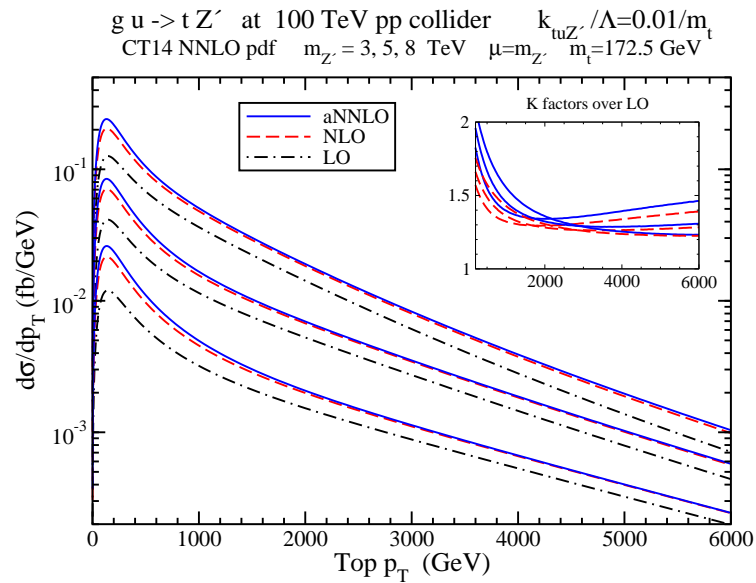
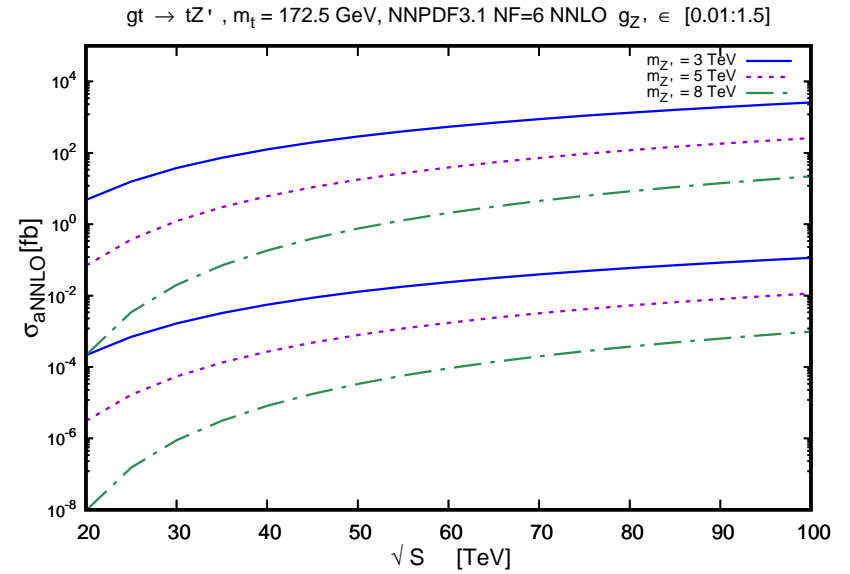
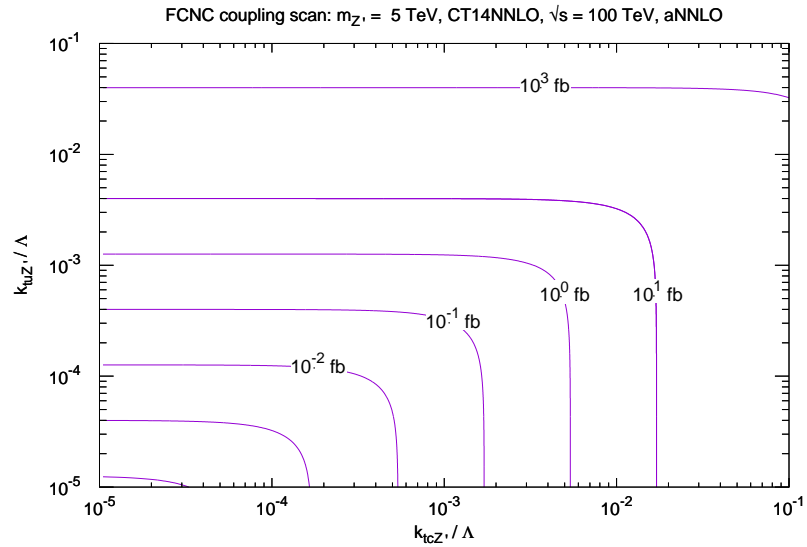
with initial-state top

$$\sum_{i=L,R} z_{t,i} g_{Z'} \bar{t}_i \gamma^\mu t_i Z'_\mu$$

$gt \rightarrow tZ'$ in pp collisions $m_{Z'}=3, 5, 8 \text{ TeV}$ $g_{Z'}=1$
 NNPDF3.1 NNLO pdf $\mu=m_{Z'}$ $m_t=172.5 \text{ GeV}$







Summary

- soft-gluon corrections and resummation
- tW production at aN³LO
- soft-gluon corrections are dominant
- tZ' production in various models
- high-order corrections are very significant